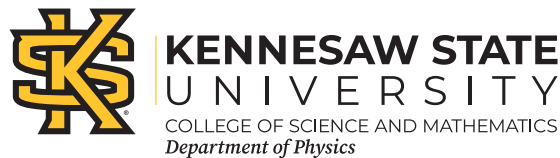


# Higher-order corrections for $t\bar{t}$ production at high energies

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- Soft-gluon corrections
- Top-antitop pair production
- $aN^3LO$  cross sections



Snowmass 2021  
Energy Frontier Workshop



## Soft-gluon corrections

partonic processes at LO:  $q\bar{q} \rightarrow t\bar{t}$  and  $gg \rightarrow t\bar{t}$

in 1PI kinematics  $f_1(p_1) + f_2(p_2) \rightarrow t(p_t) + X$

we define  $s = (p_1 + p_2)^2$ ,  $t = (p_1 - p_t)^2$ ,  $u = (p_2 - p_t)^2$  and  $s_4 = s + t + u - 2m_t^2$

At partonic threshold  $s_4 \rightarrow 0$

Soft corrections  $\left[ \frac{\ln^k(s_4/m_t^2)}{s_4} \right]_+$  with  $k \leq 2n - 1$  for the order  $\alpha_s^n$  corrections

Factorization and Resummation of these soft-gluon corrections

Soft anomalous dimension  $\Gamma_S^{f_1 f_2 \rightarrow t X}$  controls the evolution of the soft function

At NNLL accuracy we need two-loop results

only partial three-loop results are known

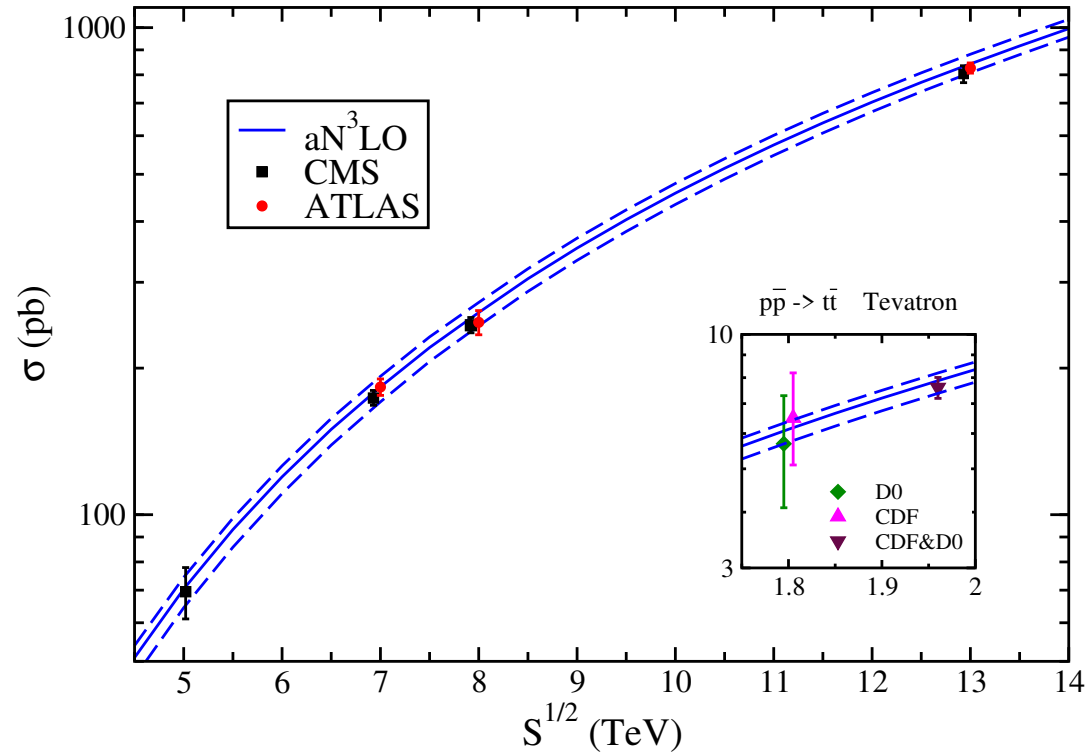
Finite-order expansions  $\rightarrow$  no prescription needed

Approximate N<sup>3</sup>LO (aN<sup>3</sup>LO) predictions for total cross sections  
and for (single and double) differential distributions

# Top-antitop pair production

$pp \rightarrow t\bar{t}$  at LHC energies  $aN^3LO$   $m_t=172.5$  GeV

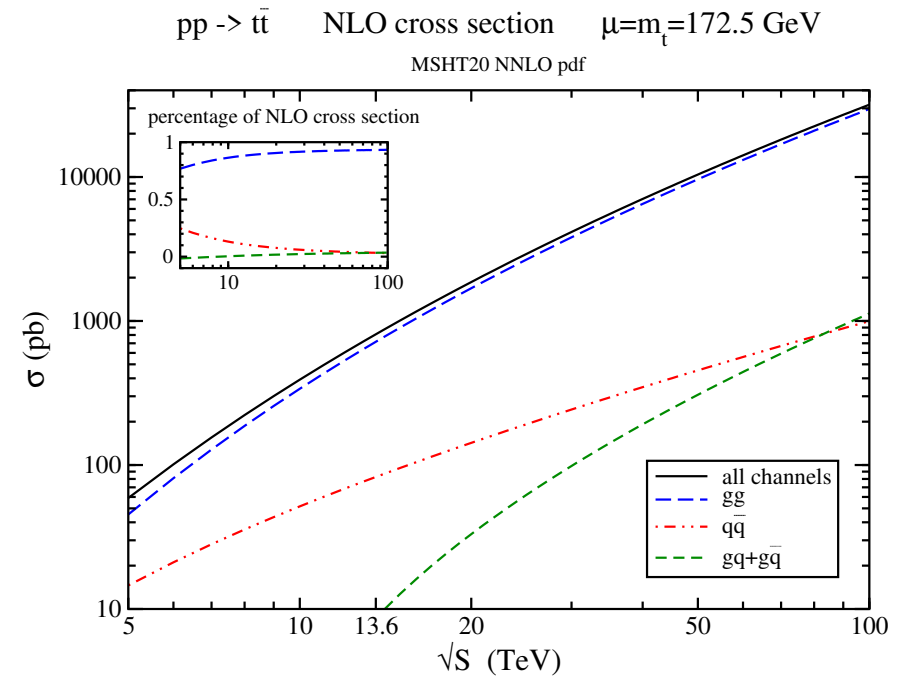
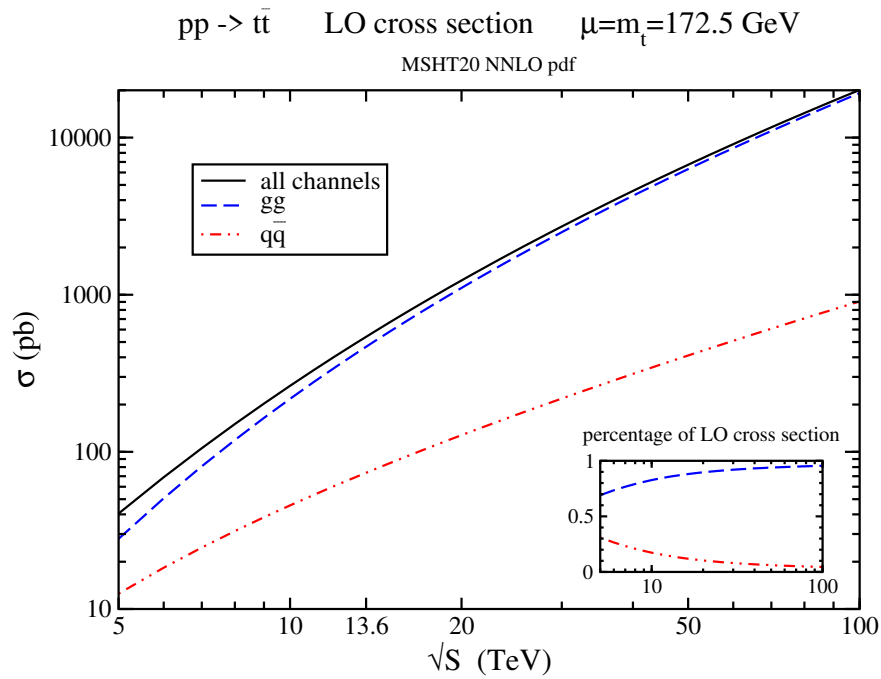
MMHT2014 NNLO pdf



soft-gluon corrections are dominant in total & differential cross sections

excellent agreement with collider data

# $t\bar{t}$ production at high energies



the  $gg \rightarrow t\bar{t}$  channel is increasingly dominant at higher energies

## $t\bar{t}$ production cross sections

$t\bar{t}$ cross sections at LHC energies					
$\sigma$ in pb	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
<b>LO</b>	<b>106</b>	<b>150</b>	<b>488</b>	<b>540</b>	<b>576</b>
<b>NLO</b>	<b>155</b>	<b>222</b>	<b>730</b>	<b>809</b>	<b>864</b>
<b>NNLO</b>	<b>174</b>	<b>249</b>	<b>814</b>	<b>902</b>	<b>963</b>
<b>aN<sup>3</sup>LO</b>	<b>181</b>	<b>258</b>	<b>839</b>	<b>928</b>	<b>990</b>

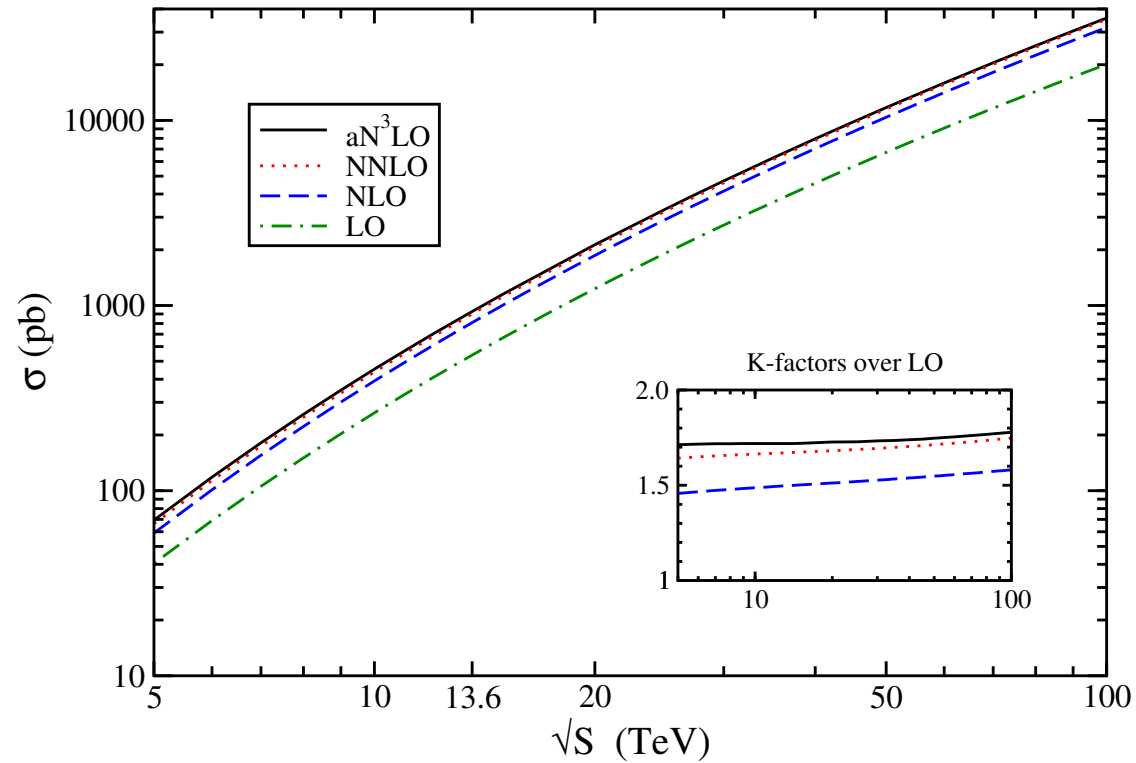
$\text{aN}^3\text{LO} = \text{NNLO} + \text{soft-gluon N}^3\text{LO corrections}$

$t\bar{t}$ cross sections in high-energy $pp$ collisions			
$\sigma$ in pb	27 TeV	50 TeV	100 TeV
<b>LO</b>	<b><math>2.23 \times 10^3</math></b>	<b><math>6.72 \times 10^3</math></b>	<b><math>20.1 \times 10^3</math></b>
<b>NLO</b>	<b><math>3.39 \times 10^3</math></b>	<b><math>10.4 \times 10^3</math></b>	<b><math>31.8 \times 10^3</math></b>
<b>NNLO</b>	<b><math>3.77 \times 10^3</math></b>	<b><math>11.5 \times 10^3</math></b>	<b><math>35.1 \times 10^3</math></b>
<b>aN<sup>3</sup>LO</b>	<b><math>3.86 \times 10^3</math></b>	<b><math>11.7 \times 10^3</math></b>	<b><math>35.8 \times 10^3</math></b>

# aN<sup>3</sup>LO $t\bar{t}$ cross sections

pp →  $t\bar{t}$  cross sections  $\mu=m_t=172.5$  GeV

MSHT20 NNLO pdf



aN<sup>3</sup>LO cross section at 13 TeV →  $839^{+23+17}_{-18-11}$  pb

at 13.6 TeV →  $928^{+25+18}_{-20-12}$  pb

at 14 TeV →  $990^{+27+19}_{-22-13}$  pb

## *K*-factors at LHC and higher energies

<i>K</i> -factors for $t\bar{t}$ production at LHC energies					
<i>K</i> -factor	7 TeV	8 TeV	13 TeV	13.6 TeV	14 TeV
NLO/LO	1.47	1.48	1.50	1.50	1.50
NNLO/LO	1.65	1.66	1.67	1.67	1.67
aN <sup>3</sup> LO/LO	1.72	1.72	1.72	1.72	1.72
aNLO/NLO	1.01	1.00	0.99	0.99	0.99
aNNLO/NNLO	1.01	1.01	1.00	1.00	1.00

aNLO = LO + soft-gluon NLO corrections

aNNLO = NLO + soft-gluon NNLO corrections

<i>K</i> -factors for $t\bar{t}$ production in $pp$ collisions			
<i>K</i> -factor	27 TeV	50 TeV	100 TeV
NLO/LO	1.52	1.55	1.58
NNLO/LO	1.69	1.71	1.75
aN <sup>3</sup> LO/LO	1.73	1.75	1.78
aNLO/NLO	0.97	0.95	0.92
aNNLO/NNLO	1.00	0.99	0.98

## Summary

- top-antitop pair production in high-energy  $pp$  collisions
- quality of soft-gluon approximation at LHC energies is excellent and it remains very good even at much higher energies
- soft-gluon corrections are dominant and they are significant through  $aN^3LO$