

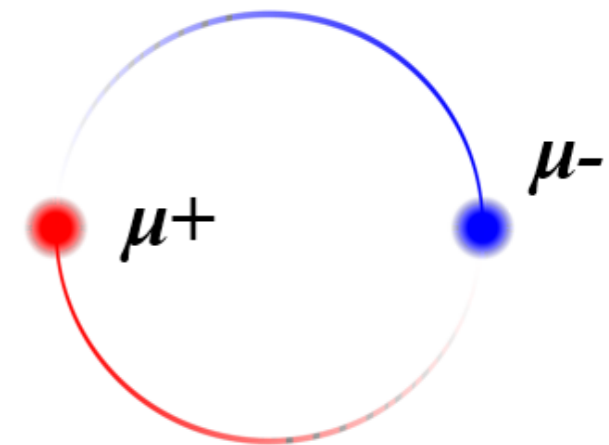


DIMUS: Di-Muonium Spectroscopy Collider

Patrick Fox (with Sergo Jindariani and Vladimir Shiltsev)

Muon Properties and Related Topics III, Snowmass

February 4, 2022



Bound States of QED

- Hydrogen atom $(p^+ e^-)$
- Positronium $(e^+ e^-)$
- Muonium $(\mu^\pm e^\mp)$
- “True” Muonium/Dimuonium $(\mu^+ \mu^-)$
- More exotic di-leptonic resonances $(\tau^\pm \ell^\mp), (\tau^+ \tau^-)$
- “Molecular systems” $(e^+ e^-)(e^+ e^-)$
- Other atoms $(\pi^\pm \mu^\mp)$

Bohr atom $E_n = -\frac{\alpha^2 \mu}{2n^2}$ $r_n = \frac{n^2}{\alpha \mu}$

Higher order corrections (fine and hyper-fine) e.g. relativistic, spin-orbit, Lamb shift, spin-spin, lift degeneracy

True muonium

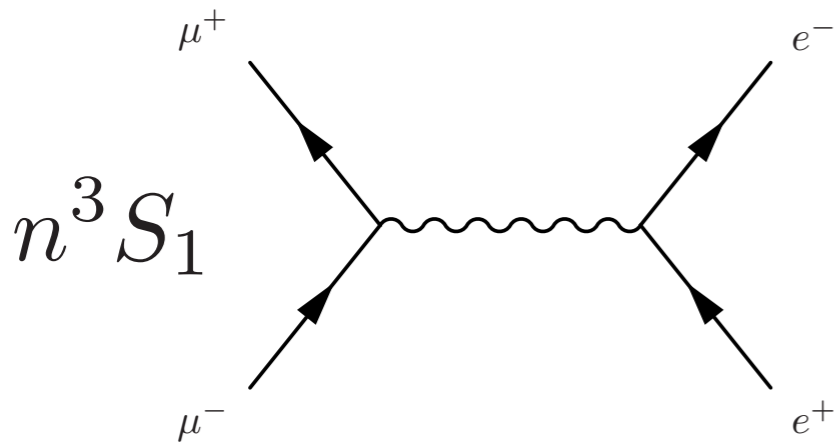
Rescale positronium. Mass is $2m_\mu - E_1$

$$E_1(H) = -13.6 \text{ eV} \quad E_1(e^+e^-) = -6.8 \text{ eV} \quad \underline{E_1(\mu^+\mu^-) = -1407 \text{ eV}}$$

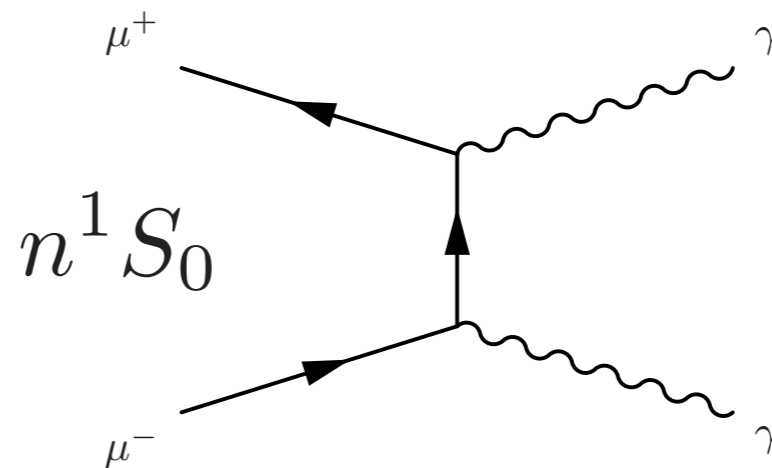
$$r_1(H) = a_0 = 53000 \text{ fm} \quad r_1(e^+e^-) = 2a_0 \quad \underline{r_1(\mu^+\mu^-) = 530 \text{ fm}}$$

Unlike positronium there are fermionic decays (for S levels)

$$\Gamma \propto |\psi(0)|^2$$



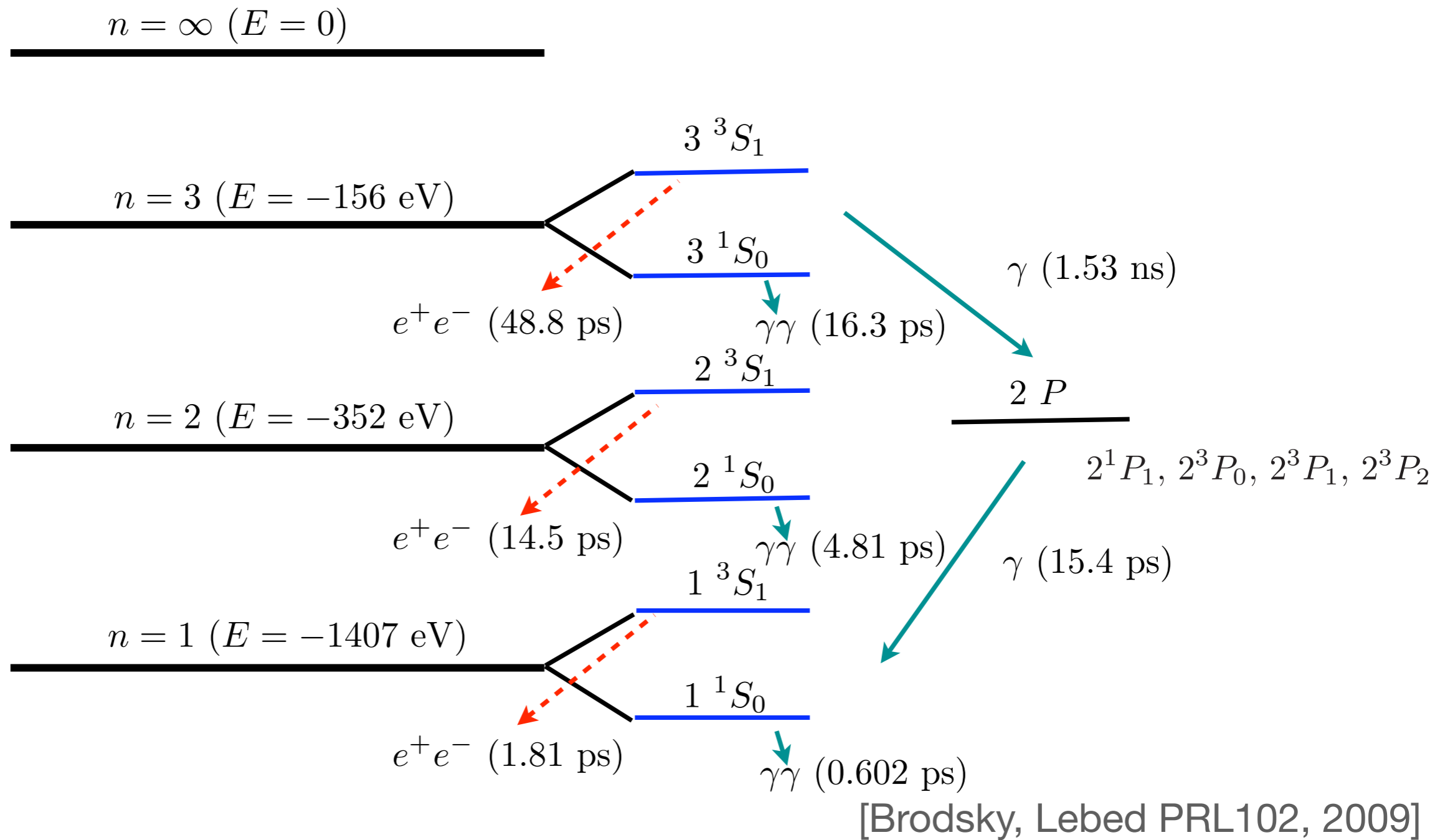
$$\tau = \frac{6n^3}{\alpha^5 m_\mu}$$



$$\tau = \frac{2n^3}{\alpha^5 m_\mu}$$

$$n^{2s+1}l_J$$

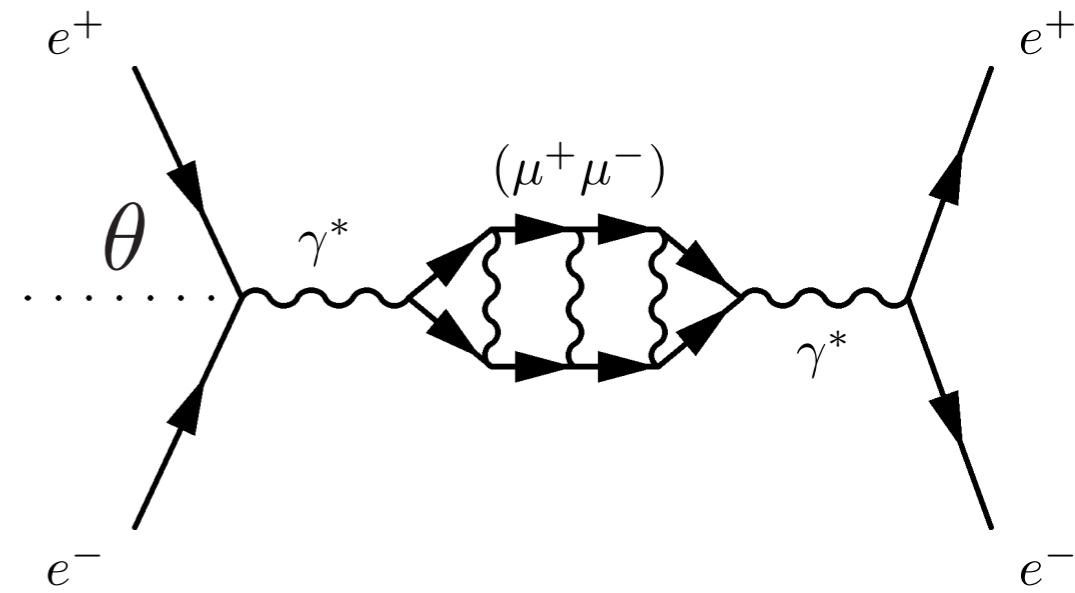
Muonium decays



Decays/transitions short compared to muon lifetime (~ 2 microsec)

Muonium Production

Fool's Intersection Storage Ring



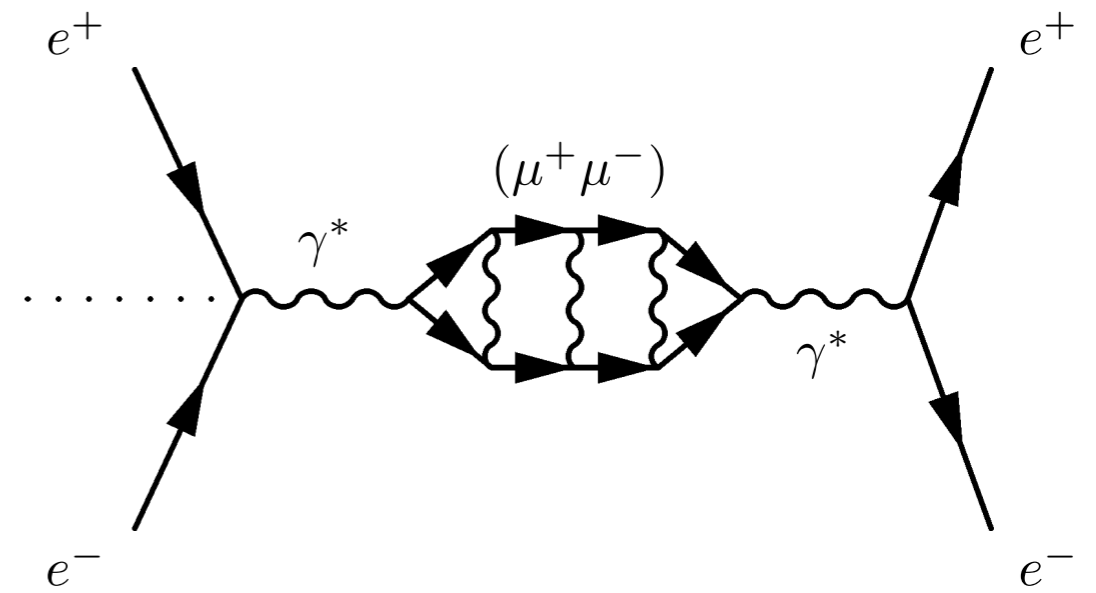
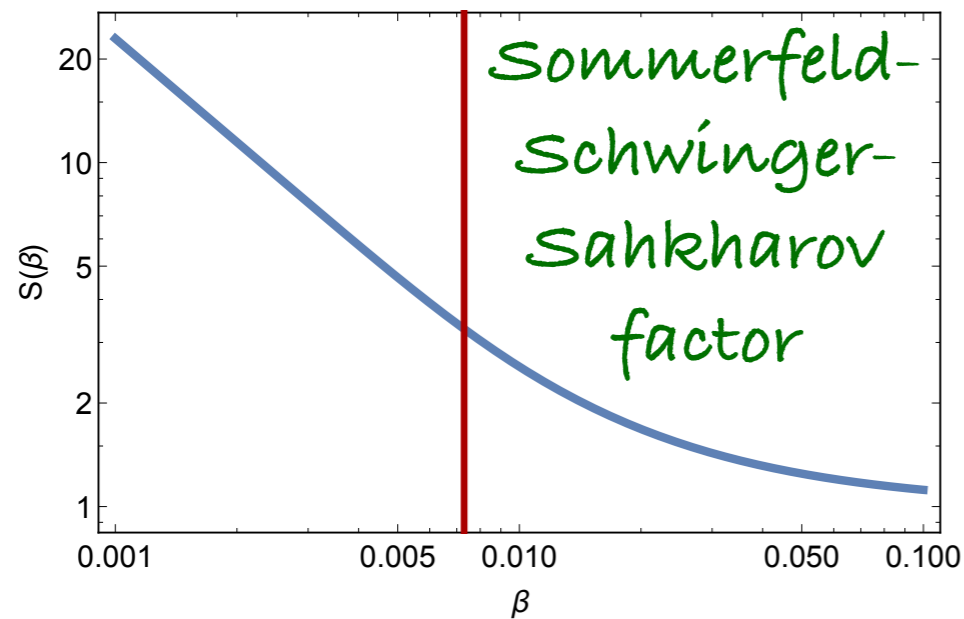
Alternative schemes included production in meson decays (eg LHCb), or radiative production (TM+gamma)

- Produces n^3S_1 states with relative rate n^{-3}
- For symmetric beam energies $p_z = \frac{2m_\mu}{\tan \theta}$ and boost $\gamma = \frac{1}{\tan \theta}$

Boost is critical for separating signal from background (Bhabha)

$$c\tau(^3S_1) \approx 0.5 \text{ mm}$$

Muonium Production

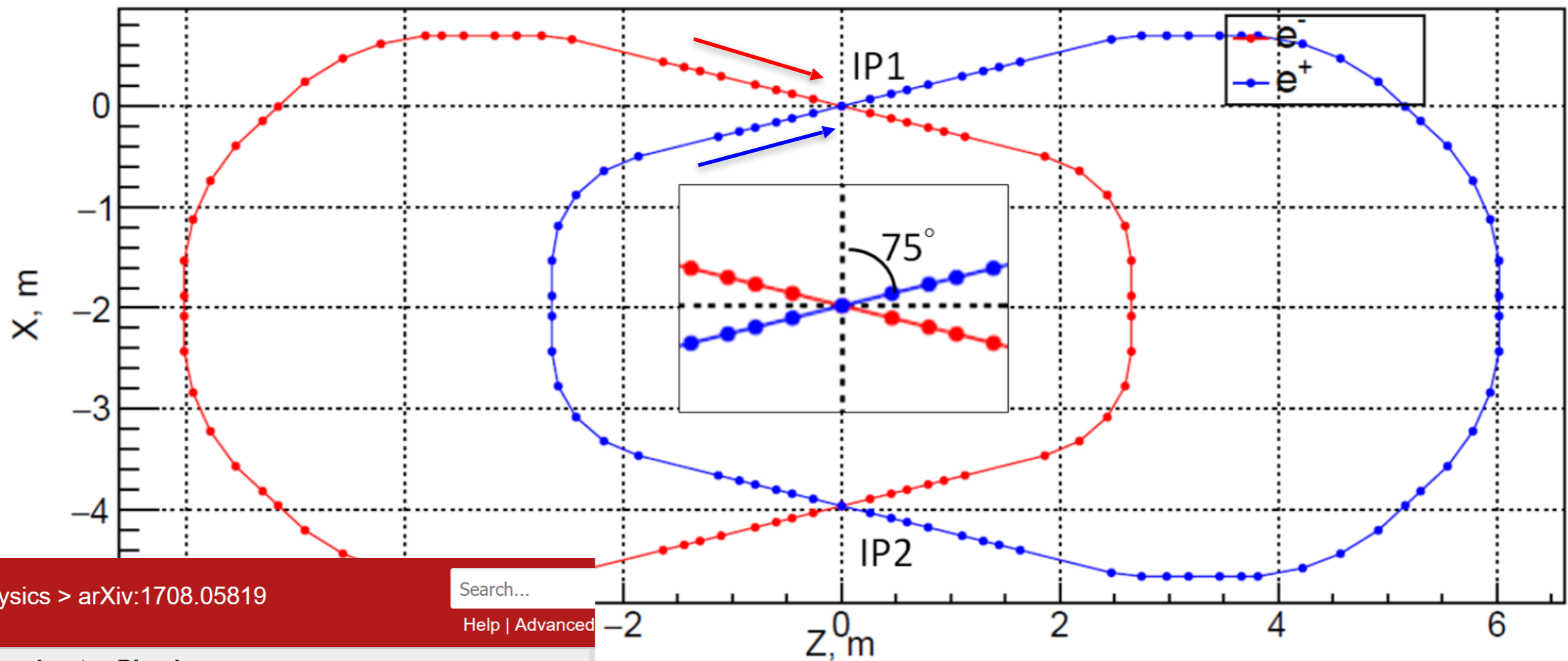


$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) \Big|_{\beta \approx 0} = \frac{2\pi\alpha^2\beta}{s} \left(1 - \frac{\beta^2}{3}\right) S(\beta)$$

$$\sigma_{b.s} = \left(\frac{\pi^2\alpha^3}{2m_\mu^2}\right) \left(\frac{\alpha^2 m_\mu}{4\Delta E_e}\right) \sim \left(\frac{1\text{MeV}}{\Delta E_e}\right) 10^{-34} \text{cm}^2$$

$$\frac{\sigma_{b.s}}{\sigma_{Bhabha}} \sim \left(\frac{3\pi\alpha}{2}\right) \left(\frac{\alpha^2 m_\mu}{4\Delta E_e}\right) \sim \left(\frac{1\text{MeV}}{\Delta E_e}\right) 10^{-4}$$

Novosibirsk “Mu-Mu-Tron” Design



arXiv.org > physics > arXiv:1708.05819

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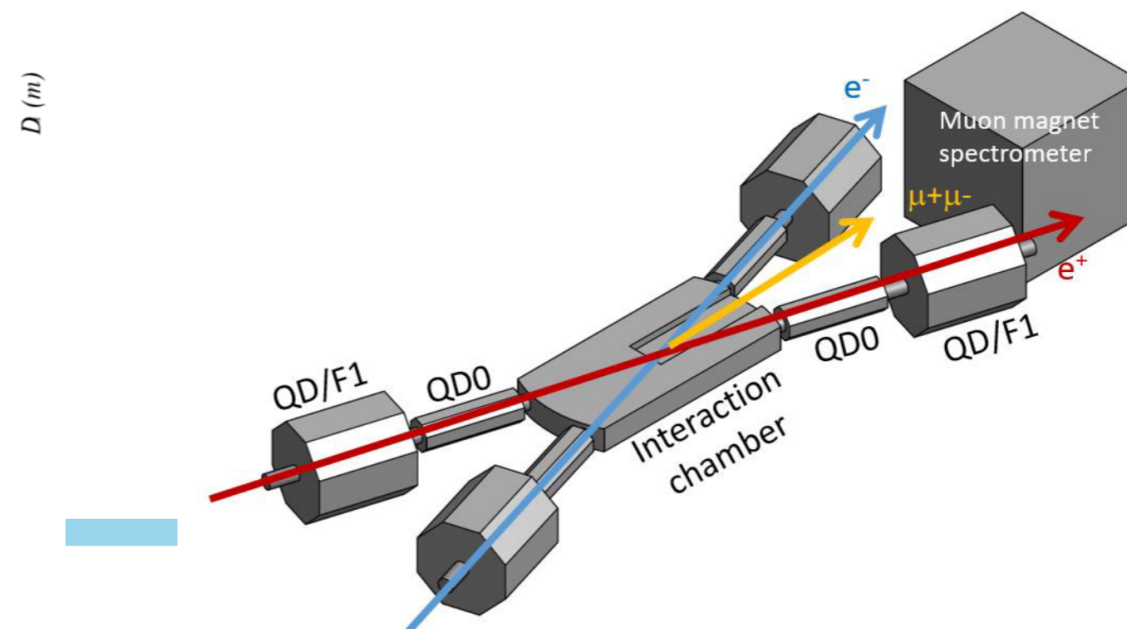
Physics > Accelerator Physics

[Submitted on 19 Aug 2017]

Low-energy electron-positron collider to search and study $(\mu^+\mu^-)$ bound state

A. Bogomyagkov, V. Druzhinin, E. Levichev, A. Milstein, S. Sinyatkin

We discuss a low energy e^+e^- collider for production of the not yet observed $(\mu^+\mu^-)$ bound system (dimuonium). Collider with large crossing angle for e^+e^- beams intersection produces dimuonium with non-zero momentum, therefore, its decay point is shifted from the beam collision area providing effective suppression of the elastic e^+e^- scattering background. The experimental constraints define subsequent collider specifications. We show preliminary layout of the accelerator and obtained main parameters. High luminosity in chosen beam energy range allows to study π^\pm and η -mesons.



Fermilab

- Public Areas
- not to scale



NORTH



Kirk Road

NML



Power Line Rd

Town Road

Wilson St.

Site 70

Wilson St

Road B

Site 37

Site 39

Site 65

Meson Area

Neutrino Area

Site 67

Proton Area

Site 50

Master Substation

Buffalo Farm

Technical Division

Road D

Bike Path

Fermilab Village

Lederman Science Center

Main Entrance

Feynman Computing Center

Pine St.

Bike Path
NuMI/Minos
MiniBoone

Antiproton Source

Wilson Hall & Ramsey Auditorium
(Public Welcome)

CDF

C-Zero

Site 55

Dog Training Area

Batavia Rd

Bike Path

Lake Law
Nature Area

A.E. Sea

East Gate
to:
Rt-59

Main Injector

Tevatron

D-Zero

Site 56

Site 3

Kautz Rd.
Substation

Site 12

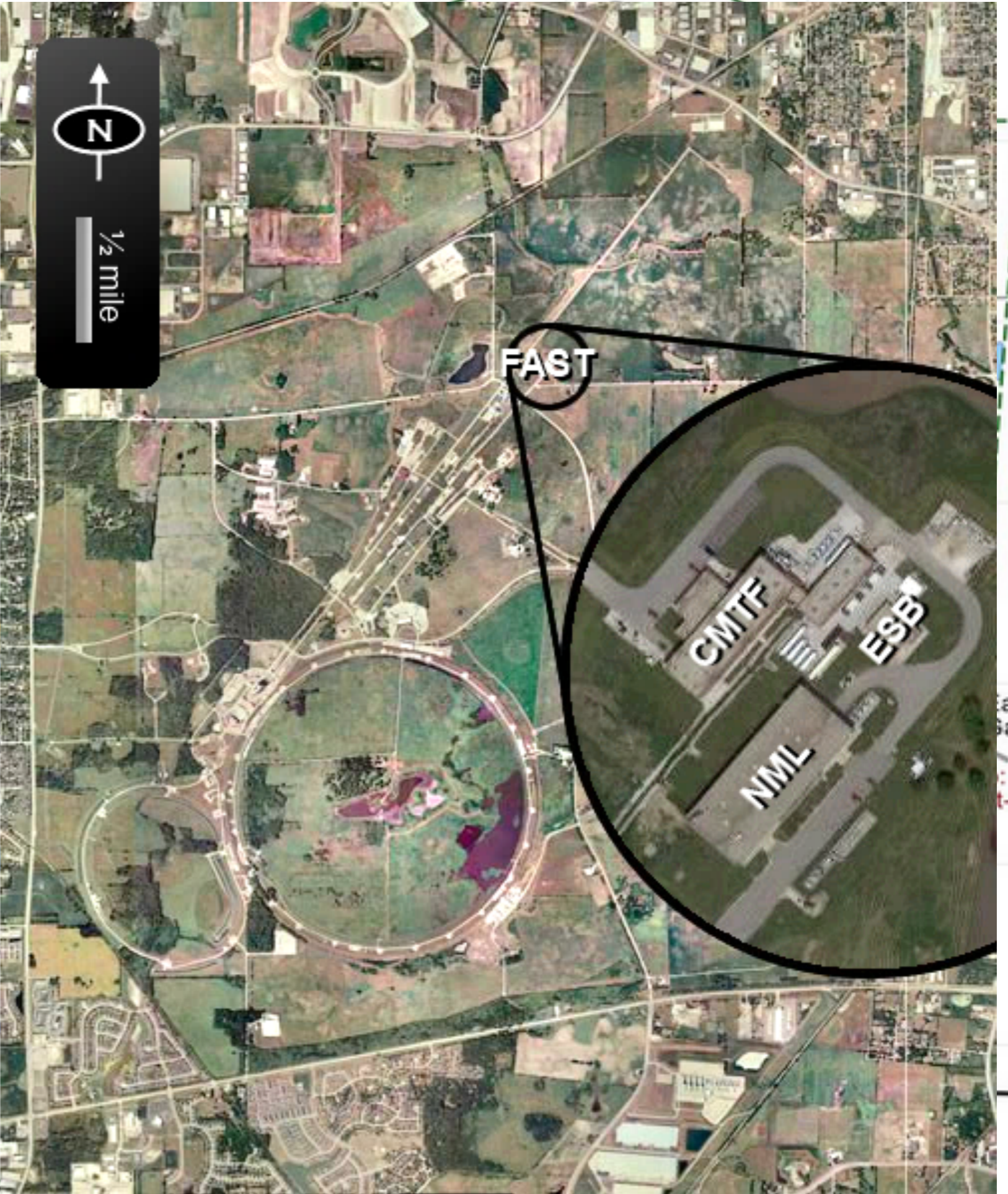
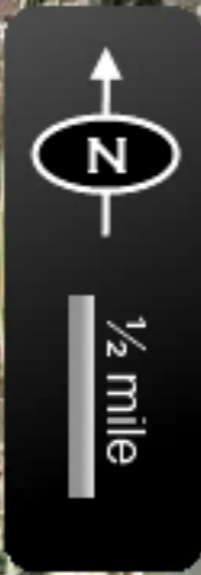
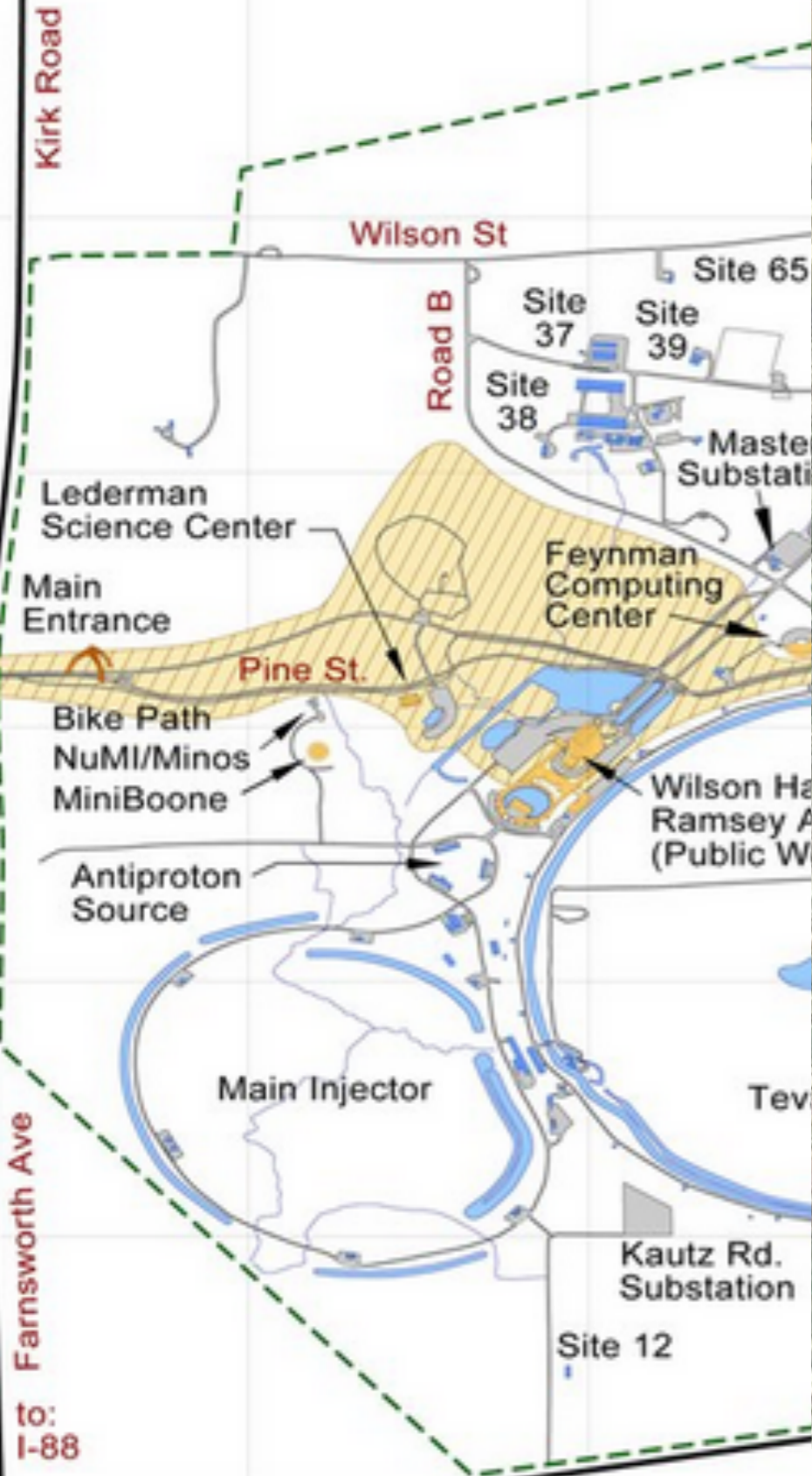
Butterfield Road

Farnsworth Ave

to:
I-88

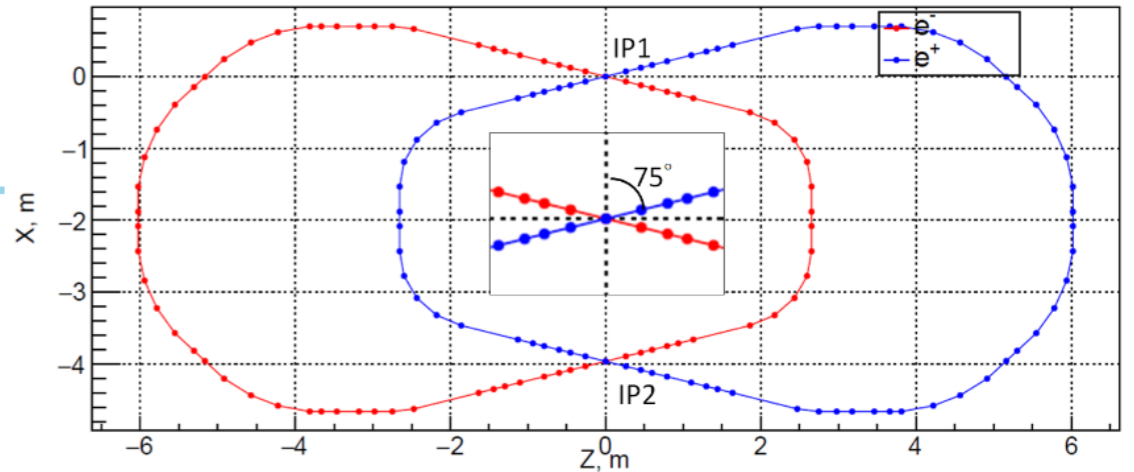
Fermilab

- Public Areas
- not to scale

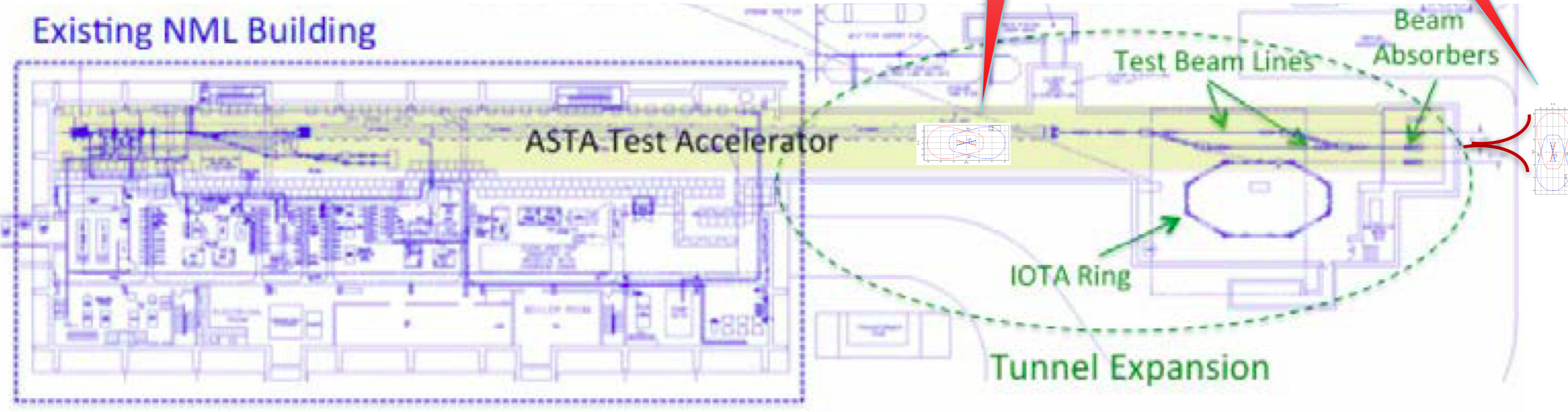


East Gate
I-59

Placement of the DIMUS Collider

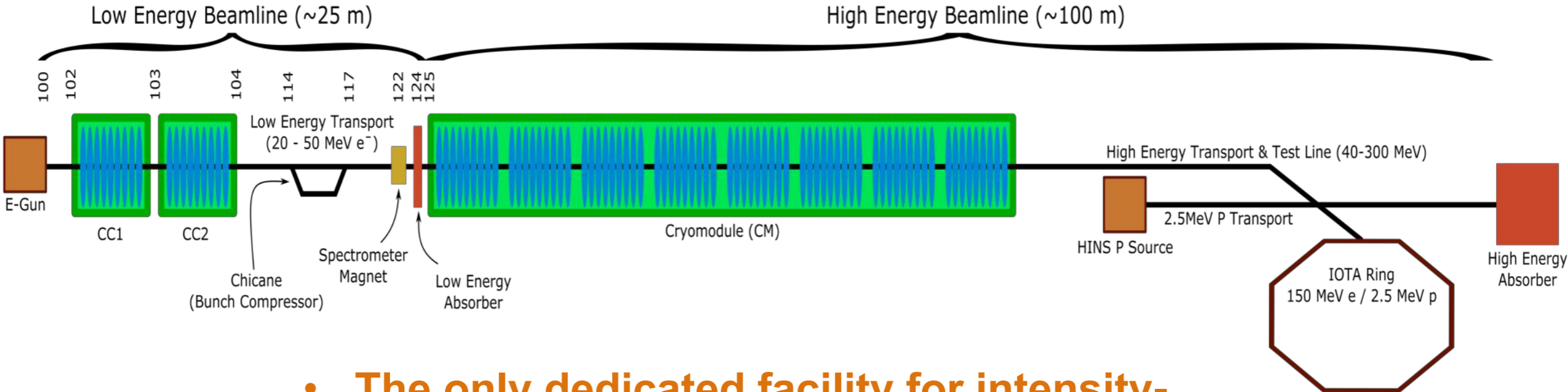


~12m x 6m



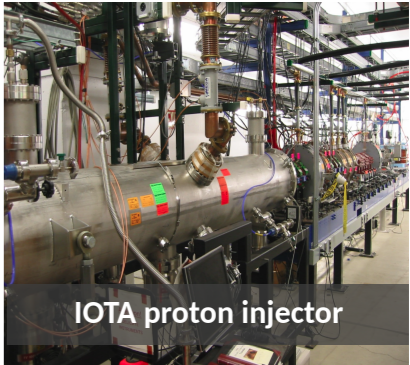
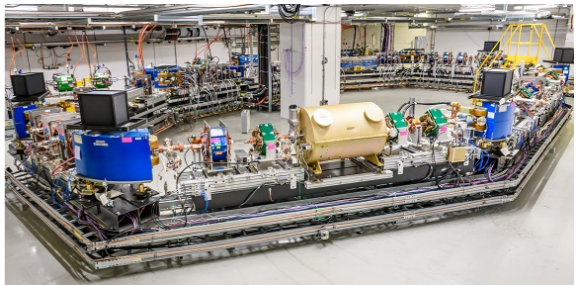
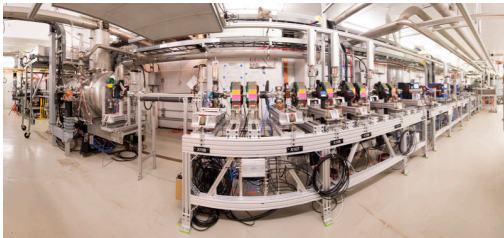
IOTA/FAST Facility for Accelerator and Beam Physics R&D

- IOTA/FAST: 5 MeV e⁻, 50 MeV e⁻, 100-300 MeV e⁻, ring and 2.5 MeV p⁺**



- The only dedicated facility for intensity-frontier accelerator R&D; ranked as top facility (“Tier 1”) for acc. & beam physics thrust by recent GARD review (Jul 2018)**

- ~30 Collaborating institutions
- Nat. Lab Partnerships: ANL, BNL, LANL, LBNL, ORNL, SLAC, TJNAF
- Many opportunities for R&D with cross-office benefit in DOE/SC



IOTA proton injector

DiMuonSpectroscopy (DiMuS) at NML : Opportunities

- **Excellent source of high energy electrons:**
 - eg 3000 bunches x 5 Hz x $2e10$ = $3e14$ e-/s
 - at 1% conversion → $3e12$ e+/s
- **DIMUS will probably need much less**
 - eg 200 bunches x 1 Hz x $2e10$ = $4e12$ e-/s
 - at 1% conversion → $4e10$ e+/s
- **Efficient linac – now upto 300 MeV**
 - DIMUS will need extra ~ 108 MeV → total of 408 MeV
- **Infrastructure and expertise:**
 - wide & (important) long tunnel, cryo, power, HCW, etc
 - knowledgeable people

To Covert NML into Collider Facility One Needs:

- Collider e^+e^- Rings (2 x 408 MeV)
- Second CM, so the final energy 408 MeV
- Positrons:
 - Conversion/collection system
 - Acceleration
 - Storage ring accumulator
- Fast injection kickers

The Second CryoModule

- *will be good for 250-320 MeV*
- *DIMUS might need only 208 MeV*

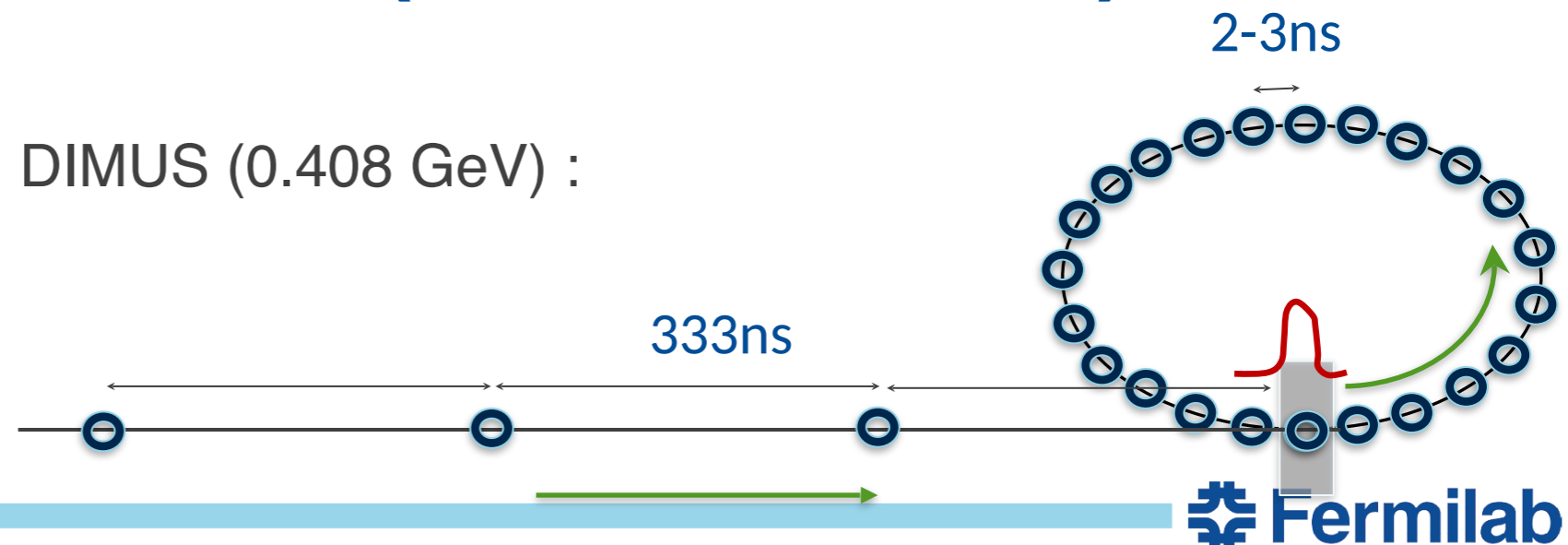


Positron Production - Several Options Exist

- **Need (at least) two linacs:**
 - Accelerate electrons (50... 300 MeV)
 - Convert them on tungsten target
 - Accelerate positrons which then go to a damping ring

Will require fast kickers (similar to ILC)

- DIMUS (0.408 GeV) :



DiMuS at NML : Summary

- They can be created in e^+e^- collision with large longitudinal momentum (as they quickly decay)
 - e.g. 408 MeV/beam at 75°
- **FAST/NML is perfectly suitable for DIMUS:**
 - SRF accelerators, plenty of e^- , wide/long tunnels
 - potential for $O(1e32)$ luminosity and $\sim 0.5M$ dimuons per year
- **Requires:**
 - second SRF CM, positron production and accumulation system, collider rings, detector(s)

After production

If muonium transits material it can be destroyed

$$\sigma_{dissoc.} \approx 13Z^2 \text{ barn}$$

If muonium exposed to intense laser it can be put into P-state

If transits regions with strong B-field, level mixing can also populate other states

Spectroscopy: measure Lamb shift, hyperfine etc
Decay lifetimes and branching ratios

New Physics

Ongoing anomalies in muon sector: $g-2$, muonic Hydrogen, R_K
New physics coupled to muons?

Great probe of short distances, no nuclear effects to contend with

New forces can change size of muonium, altering production/
decay

$$(\mu^+ \mu^-) \rightarrow V_{NP}^* \rightarrow e^+ e^-$$

and provide new **decay** channels

$$(\mu^+ \mu^-) \rightarrow \gamma X \qquad (\mu^+ \mu^-) \rightarrow XX$$

$$X \rightarrow SM \ SM$$

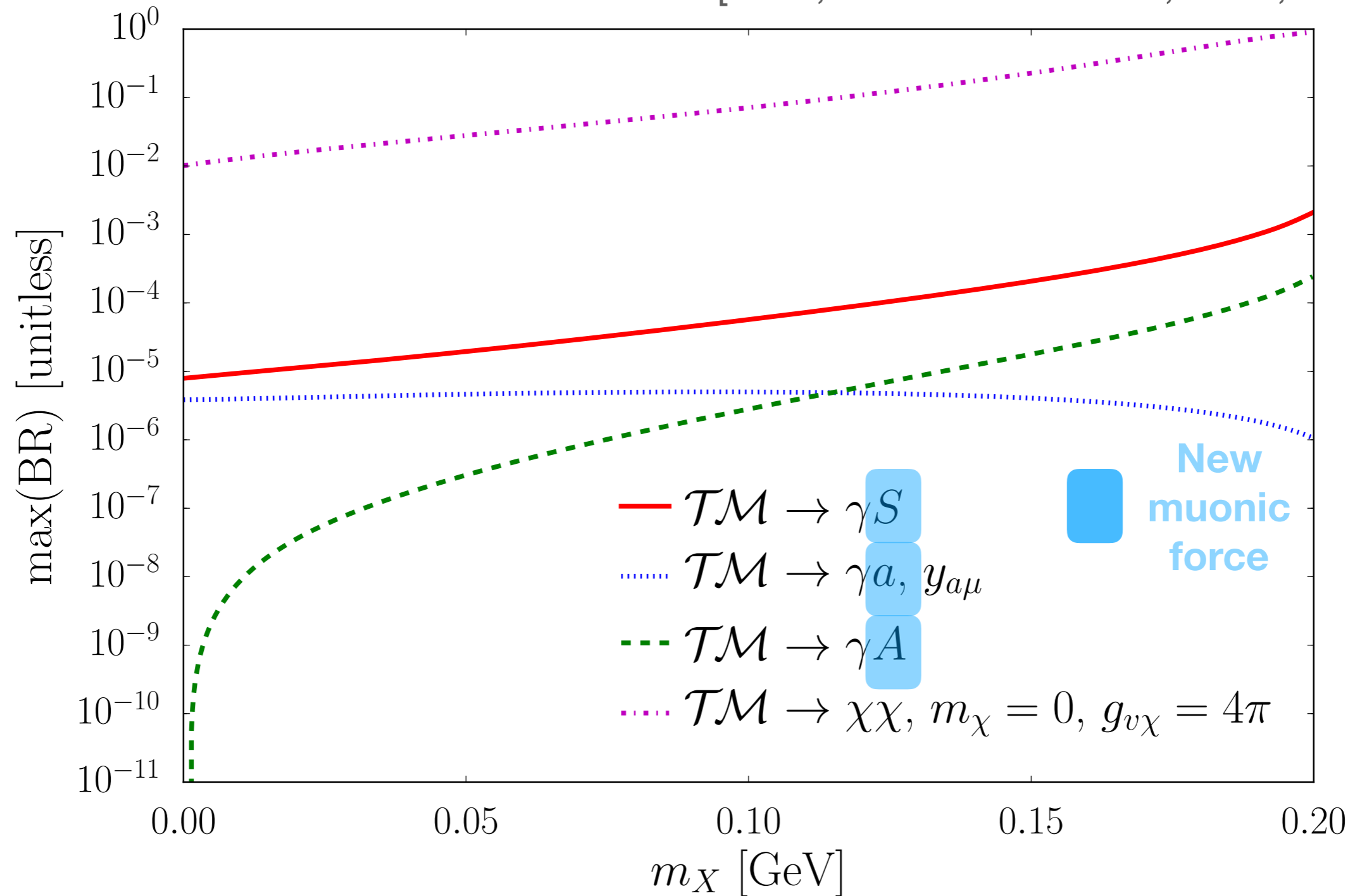
or change energy levels (**spectroscopy**)

2S-2P transition

Strong constraints from other measurements

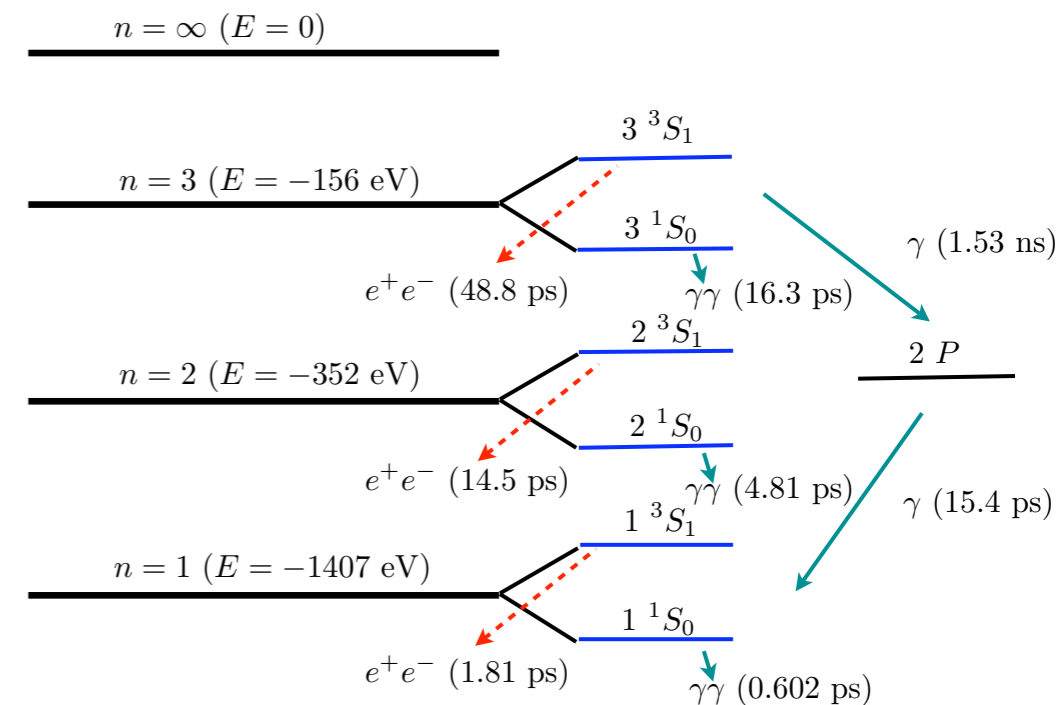
New Decay Modes

[Vidal, Ilten et al PRD100, 2019; 1904.08458]



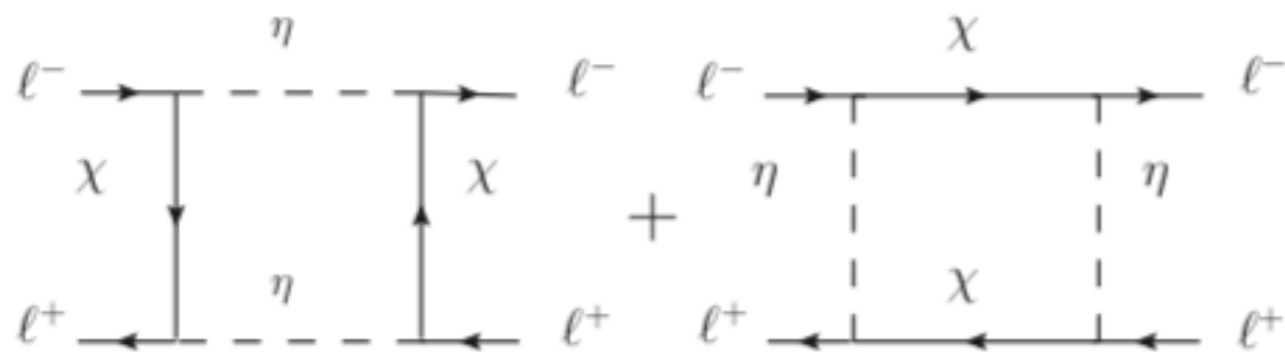
Spectroscopy [Ji,Lamm; 1712.03429]

| Transition | E_{theory} [MHz] |
|-------------------|----------------------------------|
| $1^3S_1 - 1^1S_0$ | $42329355(51)_{\text{had}}(700)$ |
| $2^3S_1 - 1^3S_1$ | $2.550014(16) \times 10^{11}$ |
| $2^3P_0 - 2^3S_1$ | $1.002(3) \times 10^7$ |
| $2^3P_1 - 2^3S_1$ | $1.115(3) \times 10^7$ |
| $2^3P_2 - 2^3S_1$ | $1.206(3) \times 10^7$ |
| $2^1P_1 - 2^3S_1$ | $1.153(3) \times 10^7$ |

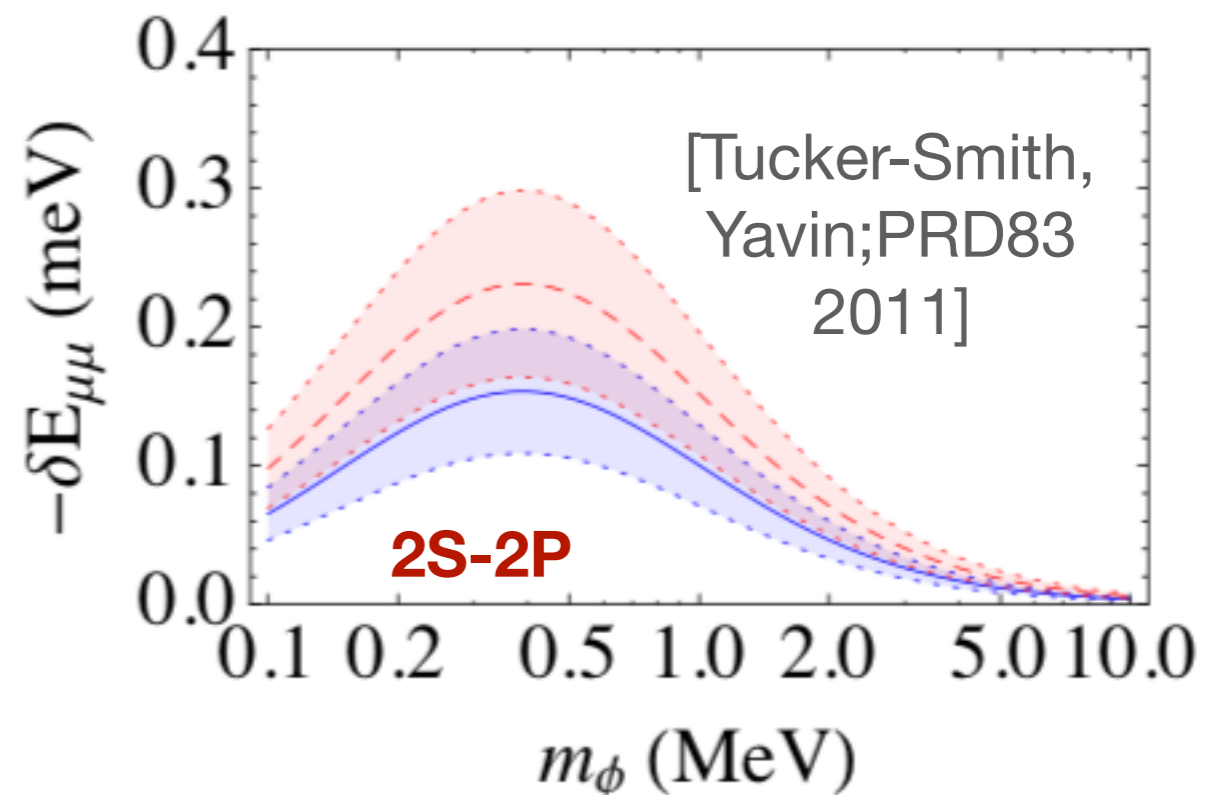


Muonic forces/contact interactions can alter energy levels: Lamb shift, hyperfine, 2P-2S, 2S-1S, etc

QED prediction known to $\mathcal{O}(m_\mu \alpha^5)$ BSM ~ 100 MHz



$$\Delta E_{\text{hfs}}^{\mu^+\mu^-} = -1.47 \text{ MHz} \times y^4 \left(\frac{100 \text{ GeV}}{m_\chi} \right)^2,$$



Detection

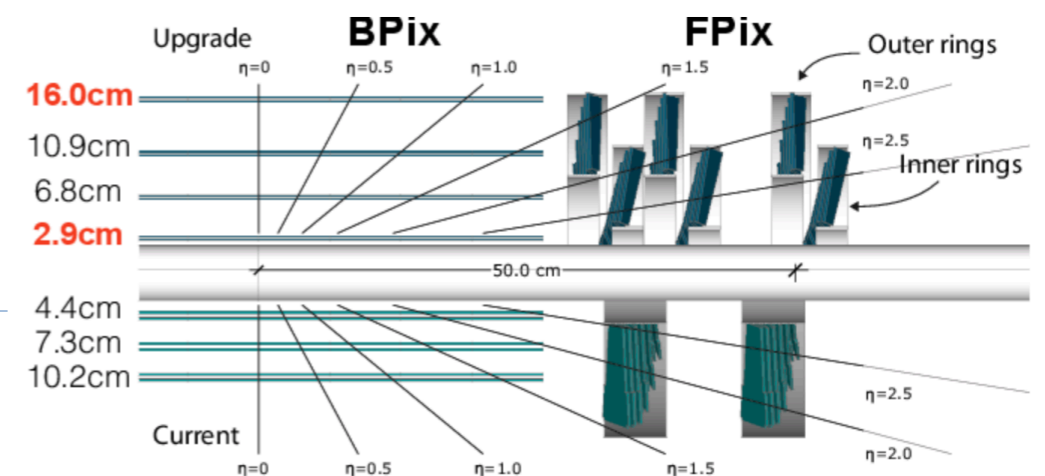
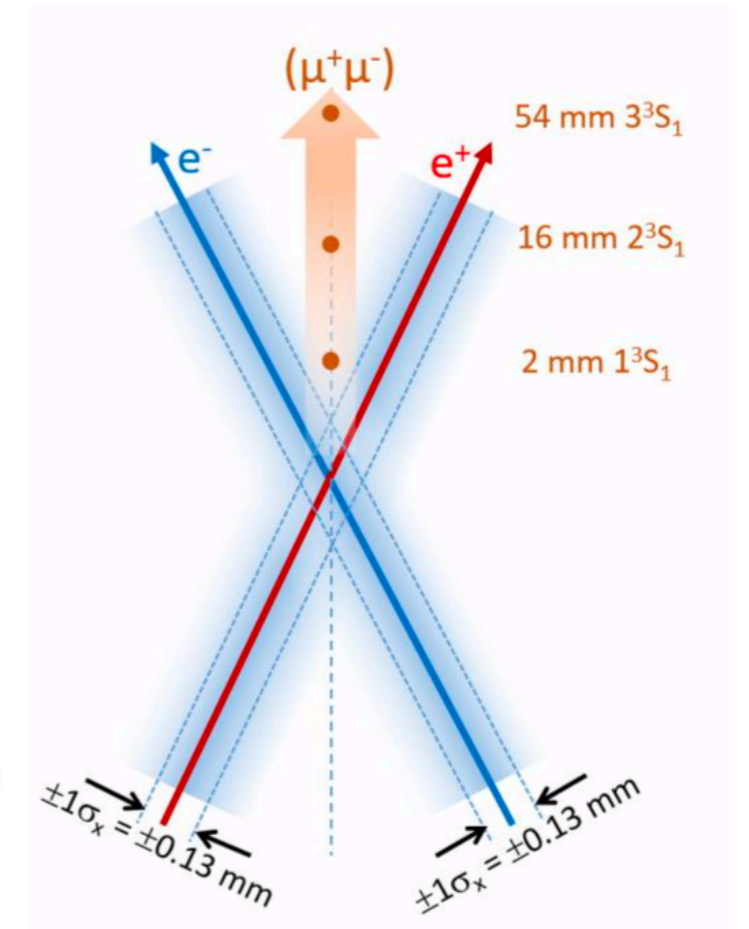
- ◆ **Detector requirements can depend on the physics goals**
- ◆ Can we observe True Muonium (TM) ?
- ◆ Can we perform spectroscopy analysis of TM ?
- ◆ Are there exotic decays of TM we should look for?
- ◆ Can we do other physics with this setup?

The Challenge:

- $e^+e^- \rightarrow \text{TM} \rightarrow e^+e^-$
- The primary background is Bhabha events
- For $\Delta(E_e) \sim 10$ keV, the signal x-section is ~ 5 nb
- Bhabha $\sim 22,000$ nb \rightarrow **S/B $\sim 1/4,000$**

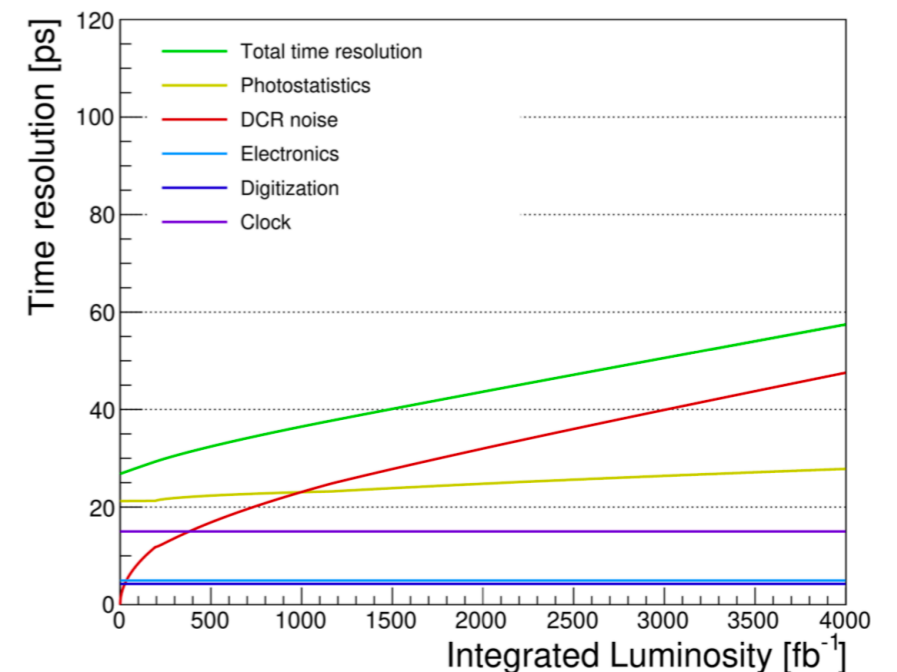
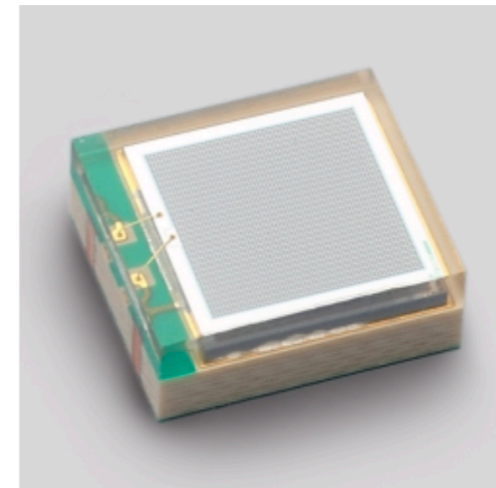
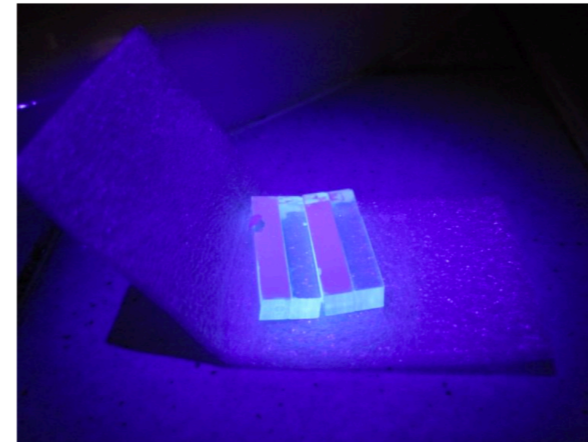
Tracker Considerations

- ◆ For Dimuonium: $\beta \gamma c \tau = 2 \text{ mm}$
- ◆ Interaction region spread ~ 300
 - Detector resolution can be small (< 100 microns)
 - Total vertex resolution < 400 microns
- ◆ Requiring $z > 2 \text{ mm}$ would suppress Bhabba events
 - Prompt background free after the cut
- ◆ Extract 1S/2S/3S fractions from the vertex position
- ◆ Need a vertex detector:
 - Pixelated silicon
 - ★ – CMS Phase-0 had 100-150 micron pitch pixels and allowed z resolution of < 100 microns in r - z and < 30 microns transverse plane. Good enough!
 - Drift chamber? Straw tracker?

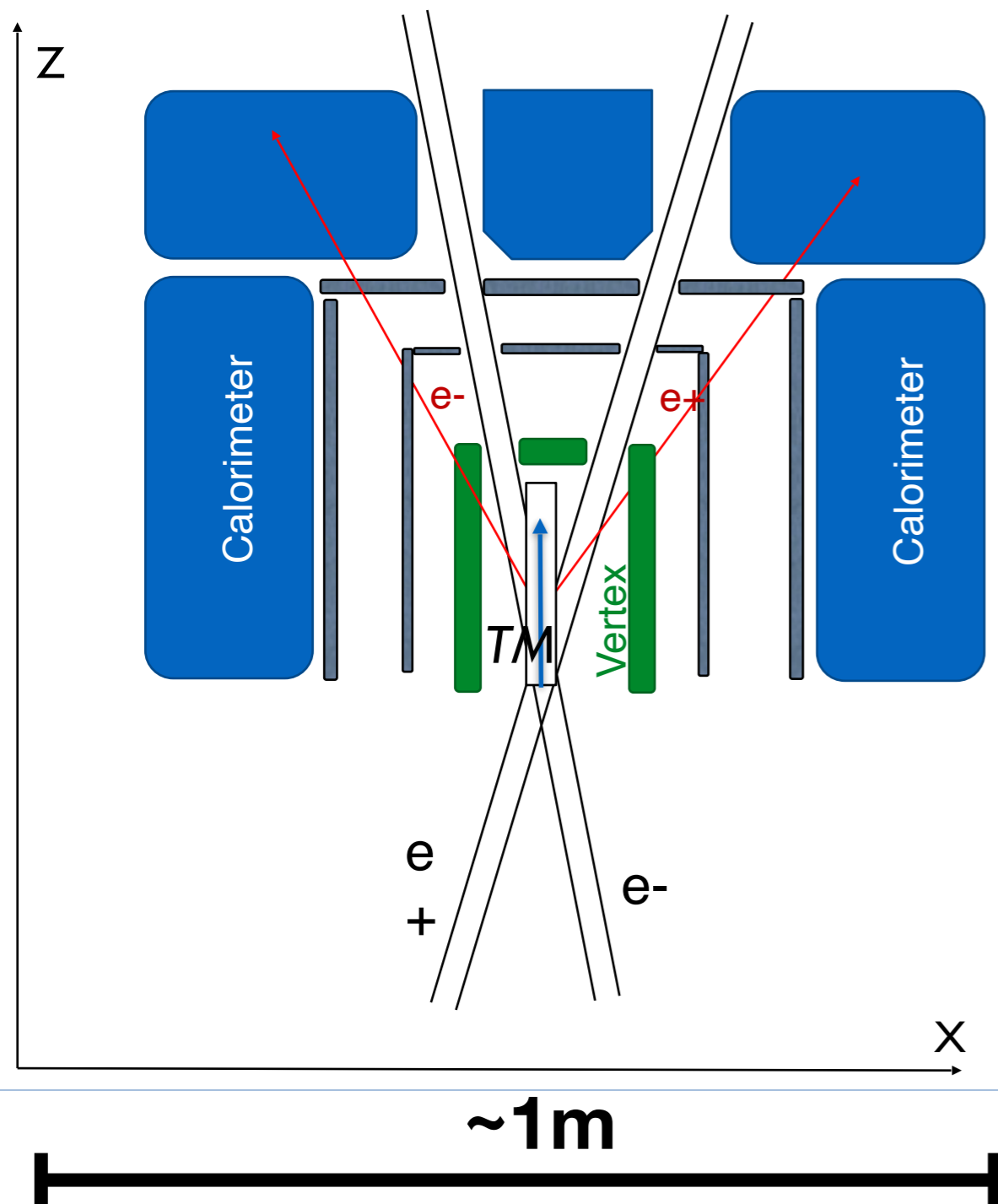


Calorimeter Considerations

- ◆ Electron/positron energy ~ 100 MeV
- ◆ Only few particles in the event – do not need fine segmentation, but do need good resolution and good coverage/acceptance
- ◆ A decently large crystal would contain the electron/positron and the right choice of crystal would give a lot of light
 - LYSO crystal read out by SiPM
 - PbWO₄ cheaper but probably not bright enough
 - Plastic is not going to work
- ◆ Precision timing desirable for further BG suppression and spectroscopy measurements?



Detector Sketch



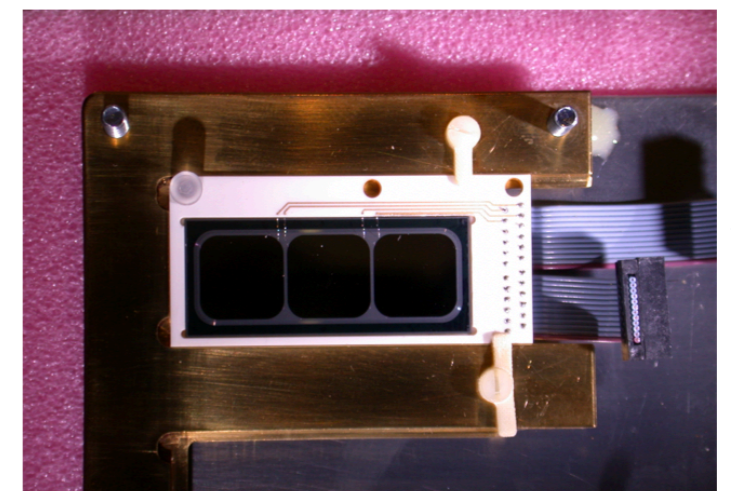
- ◆ Vertex: Pixelated silicon vertex detector
- ◆ LYSO calorimeter with excellent timing and energy resolution
- ◆ Directionality: Additional 2-3 tracking layers between the vertex detector and the calorimeter. Gas based (GEM) or silicon strips
- ◆ No magnetic field necessary
- ◆ Can probably achieve 50+% acceptance per track, 25% total.
- ◆ **100k-0.5M signal events per year**
- ◆ Integrated radiation dose small
- ◆ Devil is in the details...

X-ray Photon Detection

- ◆ Transition between the TM states happens with the emission of photons in the 100 eV – 10 KeV range.
- ◆ Can you infer this from the energy resolution of the electron/positron?
 - $\Delta E/E \sim 10 \text{ keV} / 100 \text{ MeV} < 10^{-4}$, **very hard** even at the higher end of the spectrum
- ◆ Direct detection of KeV photons
 - Examples DEAR, SIDDHARTA experiments at DAFNE (kaon spectroscopy, ~6 KeV x-ray photons)
 - SDD a possibility. Beam backgrounds?
- ◆ What about Laser spectroscopy?

| Detector | Si(Li) | CCD | SDD |
|-------------------------|--------|------|------|
| Area [mm ²] | 200 | 724 | 100 |
| Thickness [mm] | 5 | 0.03 | 0.30 |
| ΔE (FWHM) [eV] | 410 | 170 | 185 |
| Δt (FWHM) [ns] | 290 | - | 430 |

200 SDDs with 1cm² per SDD



Conclusions

- Dimuonium is a bound state of QED, never seen before!
- Provides a precision laboratory to test QED and muons
- Existing anomalies: $g-2$, proton radius, R_D , R_K
- FISR produces relativistic dimuonium in $3S1$ states
- Proposal for DIMUS at NML/FAST, modest upgrades (eg 2nd cryo-module, fast kicker, positrons)
- Detection of TM in e^+e^- final state needs vertex detector, high resolution, good timing calorimeter
- Opportunity for detailed study of its properties — production rate, decays, transitions. Constraints on new physics.

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Thank you!

| | | |
|-------------------------------|---------------------|-------------------------------|
| Beam energy | 408 | MeV |
| C.m.e. \sqrt{s} | 211 | MeV |
| C.m.e. spread | 0.4 | MeV |
| Crossing angle | 75 | deg. |
| Circumference | 23 | m |
| Beta-functions at IP (y, x) | 20/0.2 | cm |
| Bunch length | 1.2 | cm |
| Bunch spacing | 1.9 | ns |
| Beam sizes at IP (y, x) | 0.7/130 | μm |
| Number of bunches | 40 | |
| Number of e^+/e^- per bunch | $4 \cdot 10^{10}$ | |
| Beam lifetime | ≥ 30 | sec |
| Max e^+ production rate | $4 \cdot 10^{10}$ | e^+/s |
| Peak luminosity | $1.6 \cdot 10^{32}$ | $\text{cm}^{-2}\text{s}^{-1}$ |

TABLE I. Main parameters of the DIMUS collider at Fermilab's NML/FAST.