

Overview of **cLFV** in the muon sector

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@Snowbird

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Flavour and CP violation: SM

Flavour in the **Standard Model**: interactions (and transitions) between **fermion families**

Gauge interactions are **flavour universal**

Yukawas Y_{ij}^u , Y_{ij}^d and Y_{ij}^ℓ encode all **flavour dynamics**

(Masses, mixings and **CP violation**)

$$\begin{aligned}\mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i\bar{\psi} \not{D} \psi + h.c. \\ & + \bar{\chi}_i Y_{ij} \chi_j \phi + h.c. \\ & + |D_\mu \phi|^2 - V(\phi)\end{aligned}$$

SM quark sector:

6 massive states

flavour violated in charged current interactions $V_{CKM}^{ij} W^\pm \bar{q}_i q_j$

total **baryon number** is conserved in **SM** interactions

CP violation: δ_{CKM} and θ_{QCD}

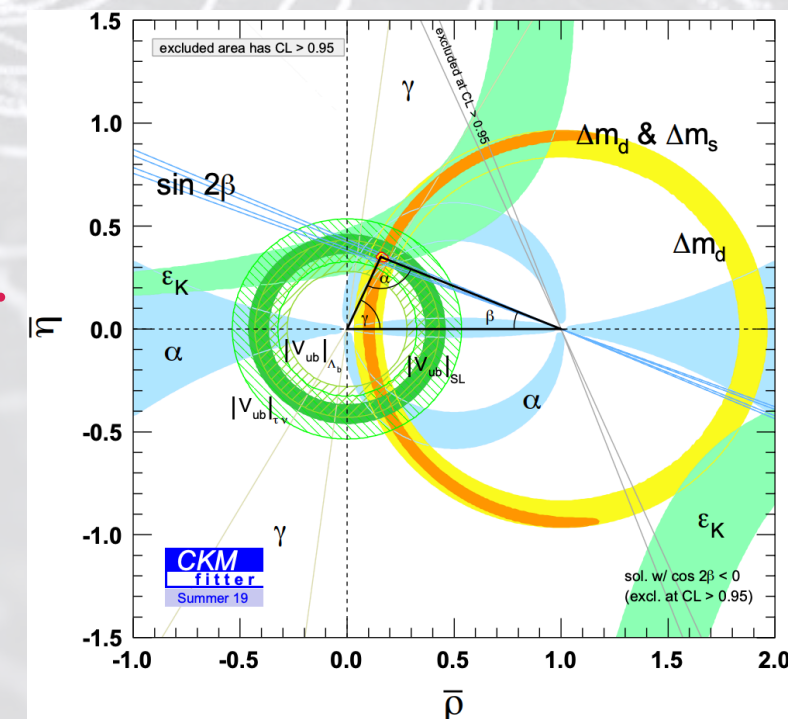
(not enough to explain BAU from baryogenesis)

CKM paradigm extensively probed:

Meson oscillations & decays, β decays, **CP violation...**

SM lepton sector: neutrinos are strictly massless

- Conservation of (total) **lepton number** and **lepton flavour**
- **Lepton flavour universality** only broken by Yukawas
- No intrinsic **CPV sources** — (tiny) lepton **EDMs** @ 4-loop



Lepton flavour and CP violation beyond SM

Strong arguments in **f(l)avour** of New Physics!

Observations **unaccounted** for in SM: **ν -oscillations**, **Dark matter**,

baryon asymmetry of the Universe

(also some theoretical caveats...)

How to unveil the NP model at work?

⇒ Test SM **symmetries** with flavour observables:

(c)LFV, **lepton flavour universality violation**, ...

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ν -oscillations 1st laboratory *evidence* of New Physics!

- ▶ New mechanism of mass generation? Majorana fields?
- ▶ New sources of **CP violation**?

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► New sources of **CP violation?**

Currently many tensions with SM related to **charged leptons**

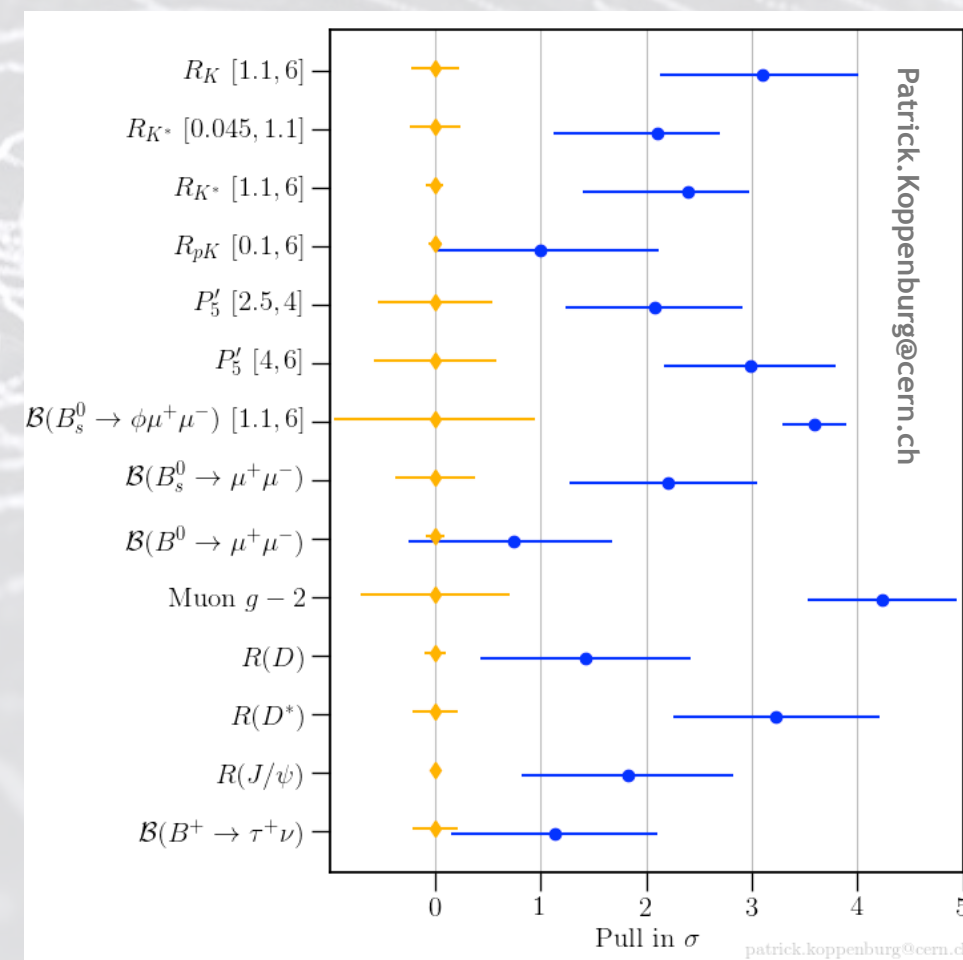
► $(g - 2)_{\mu,e}$, **B-meson anomalies**, ...

Muons are uniquely versatile and sensitive probes of NP!

► Abundantly available, many different observables

► Unprecedented **future experimental prospects**

(See talks by Angela Papa & Kevin Lynch, and maaaaany WG4 contributions)



Lepton flavour probes of New Physics

Neutrinos oscillate \Rightarrow **neutral lepton flavour violated**, neutrinos are massive,
new sources of **CPV?**

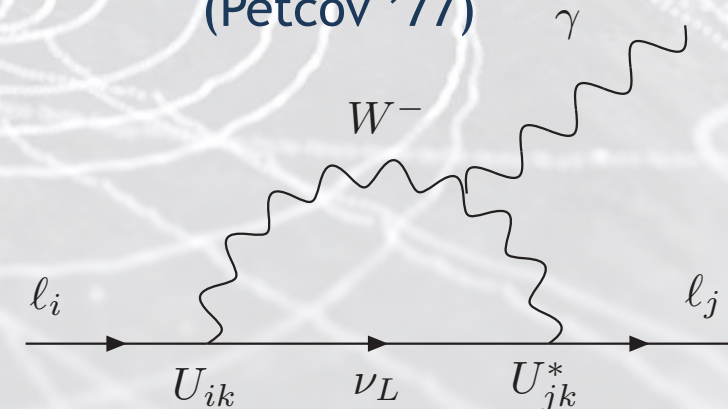
Extend SM to accommodate $\nu_\alpha \leftrightarrow \nu_\beta$: ad-hoc 3 $\nu_R \Rightarrow$ Dirac masses, “ SM_{m_ν} ”, U_{PMNS}

In SM_{m_ν} : **flavour-universal** lepton couplings, lepton number conserved

cLFV possible ... but not observable! $BR(\mu \rightarrow e\gamma) \propto \left| \sum U_{\mu i}^* U_{ei} m_{\nu_i}^2 / m_W^2 \right| \simeq 10^{-54}$
(Petcov '77)

EDMs still tiny... (2-loop from δ_{CP} , $|d_\ell| \sim 10^{-35} ecm$)

\Rightarrow any **cLFV signal** would imply **non-minimal New Physics!**
(Not necessarily related to m_ν generation)



Lepton flavours offer a plethora of observables and probes of New Physics

\Rightarrow **Negative search results**: allow to place **tight bounds** on New Physics

- ▶ **Muons: a gateway for New Physics**
- ▶ **(Dis)entangling cLFV sources**
- ▶ **The probing power of Muons**
- ▶ **Conclusions**

Muons: a gateway for New Physics



Muons: a long history

Muon (aka mu-meson or mesotron) discovered in **cosmic rays** in 1937

Early searches and limits on $\mu(e^*) \rightarrow e\gamma$ decay (Hincks, Pontecorvo 1947)
 \Rightarrow hypothesis of ν_μ , second **lepton family**

Since then: μ one of the **best understood** SM particles:

Mass $m_\mu = 105.6583755 \pm 0.0000023$ MeV, **Lifetime** $\tau_\mu = 2.1969811 \pm 0.0000022$ μ s

Magnetic moment: $(g - 2)/2 = (11659206.1 \pm 4.1) \times 10^{-10}$ (BNL + FNAL)

Electric dipole moment: $|d_\mu| \lesssim 1.8 \times 10^{-19}$ ecm (BNL) For future prospects see WG4 talks

Michel decay: $\text{BR}(\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu) \approx 100\%$ (determination of G_F)

Rare SM decays: $\text{BR}(\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu \gamma) = (6.0 \pm 0.5) \times 10^{-8}$

$\text{BR}(\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu e^+ e^-) = (3.4 \pm 0.4) \times 10^{-5}$

Bound states: Muonium ($\mu^+ e^-$) \leadsto QED and gravity tests

Muonic atoms: search for P violation

Anomalous magnetic moments

Magnetic moment: particle's tendency to align with a **magnetic field**

$$\vec{\mu}_\ell = g_\ell \frac{e}{2m_\ell} \vec{s} \quad g_\ell \sim \text{gyromagnetic ratio (Landé factor)}$$

Dirac's prediction: $g_e = 2$

SM electromagnetic current:

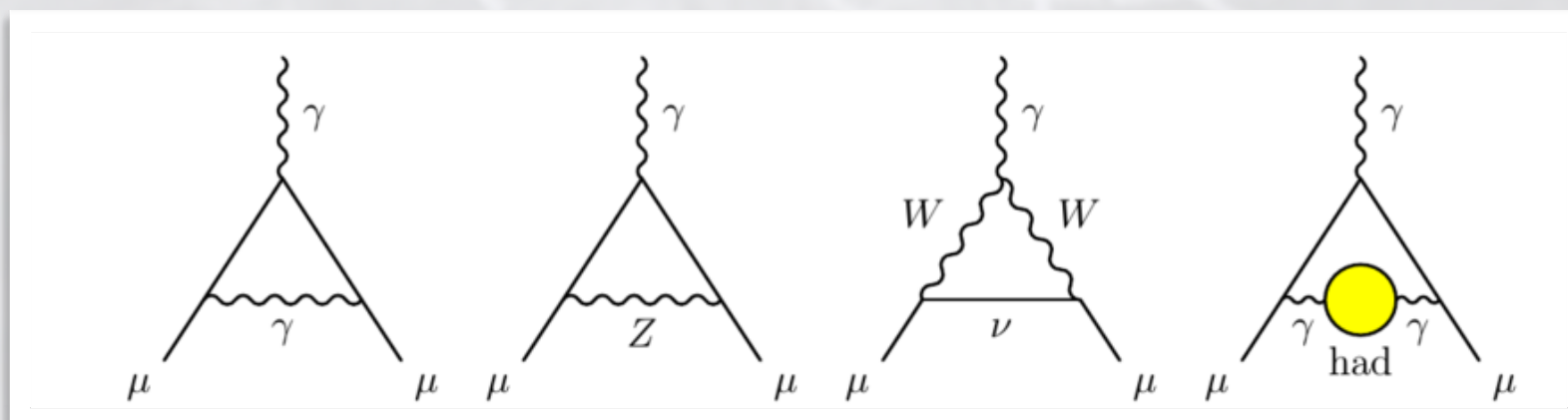
$$\mathcal{J}_\mu = \bar{\ell}(p') \left[\gamma_\mu F_1(q^2) + \frac{i\sigma_{\mu\nu}q^\nu}{2m_\ell} F_2(q^2) + \gamma_5 \frac{i\sigma_{\mu\nu}q^\nu}{2m_\ell} F_3(q^2) + \gamma_5 (q^2 \gamma_\mu - \not{q} q_\mu) F_4(q^2) \right] \ell(p)$$

@ tree-level: $F_1(0) = 1$; $F_{2,3,4}(0) = 0 \Rightarrow g_\ell = 2 (F_1(0) + F_2(0)) = 2$

@ higher orders: quantum corrections to $F_2(0) \Rightarrow$ **anomalous magnetic moment**

$$\Delta a_\ell = \frac{g_\ell - 2}{2} = F_2(0)$$

Higher-order (SM) corrections from QED, EW (W^\pm , Z and Higgs) and QCD



Muon anomalous magnetic moment circa 2022

► Anomalous magnetic moment of the muon: from theory to experiment and back

$$a_\mu^{\text{SM}} = \frac{1}{2} (g_\mu - 2) = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{had}} \quad \text{in conflict with BNL \& FNAL? Or not?}$$

see WG4 talks for future exp prospects

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = ?$$

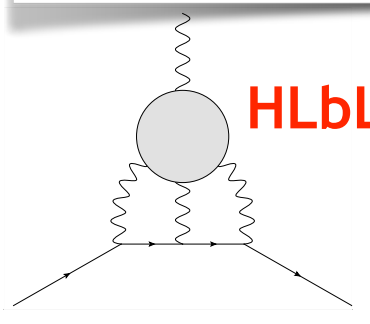
Full QED $\mathcal{O}(\alpha^5)$ - 12672 diagrams!

EW completed at 2-loop (3-loop negligible)

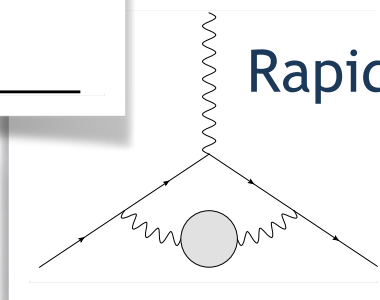
	$10^{11} \cdot a_\mu$	$10^{11} \cdot \Delta a_\mu$
QED total	116 584 718.931	0.104
EW	153.6	1.0
HVP	6 845	40
HLbL	92	18
SM total	116 591 810	43

Hadronic: smaller than QED, but dominate theoretical uncertainties!

HVP - evaluated from *dispersion relations* & *data-driven* input from $e^+e^- \rightarrow \text{hadrons}$
(a_μ "White paper" HVP result)



HLbL - recent progress, from hadronic models to dispersive framework, 1st LQCD results!



Rapid LQCD progress!

$$\text{BMW 2021: } 10^{11} \cdot a_\mu^{\text{LQCD}} = 7\,075(55)$$

$\Rightarrow 2.1\sigma$ tension!

2022: confirmation by Mainz & ETMC

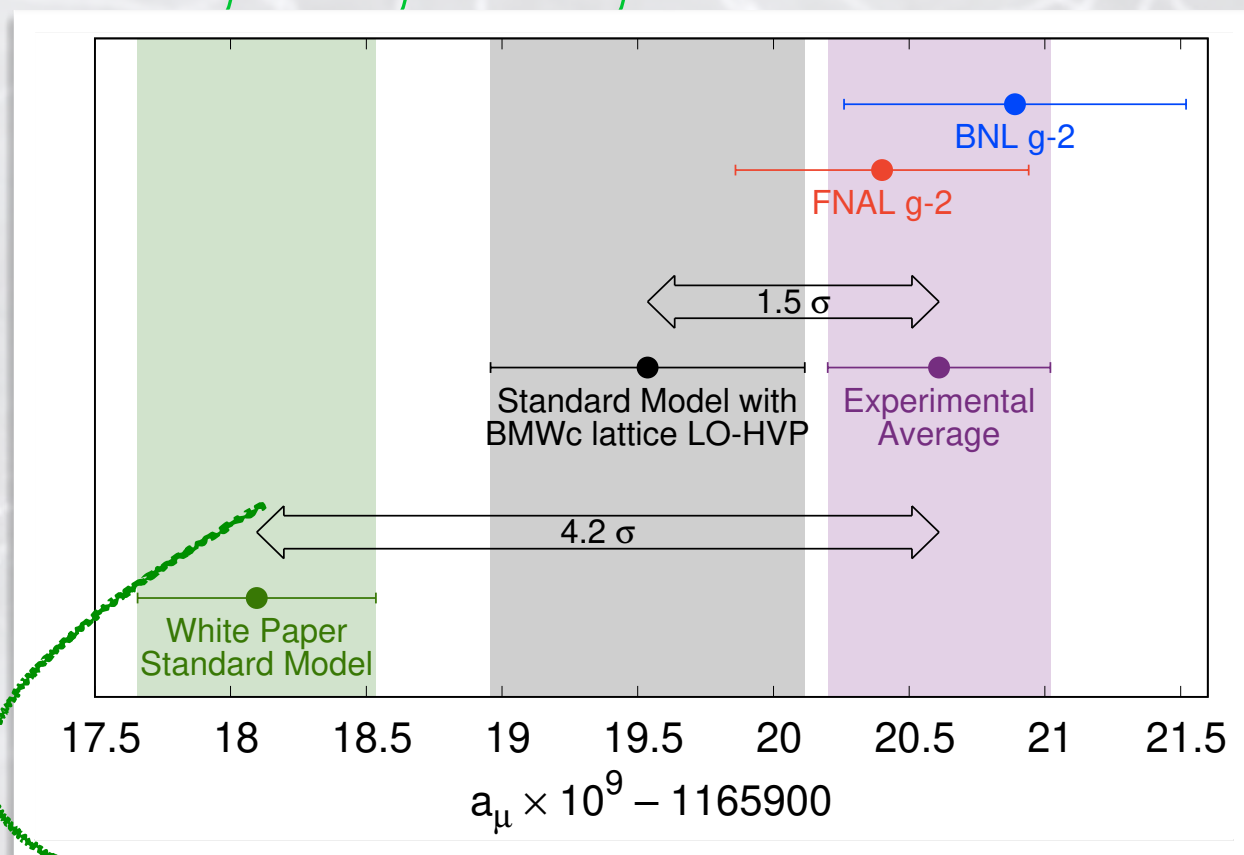
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Recent LQCD results seem to *confirm* BMWc
Mainz [2206.06582], ETMC [2206.15084]

⇒ **New tensions** with $e^+e^- \rightarrow$ hadrons scattering

New Physics needed elsewhere?

see e.g. Darmé et al. [2112.09139], Di Luzio et al. [2112.08312]

MUonE experiment to conclusively measure **HVP!**

see talks by Javad Komijani and Lorenzo Capriotti

New Physics needed for $g - 2$? or not?

$$\mathcal{H}_{\text{eff}}^{\text{NP}} \sim \frac{C_{a_\mu}^6}{\Lambda_{\text{NP}}^2} \left(\bar{\Psi}_\mu \sigma_{\alpha\beta} \Psi_\mu \right) F^{\alpha\beta} H$$

If $\Delta a_\mu \sim \mathcal{O}(\text{few } \sigma) \approx 2 \times a_\mu^{\text{SM}}$, weak

$$\Rightarrow \Delta a_\mu \approx \frac{C_{a_\mu}^6}{\Lambda_{\text{NP}}^2} (m_\mu v)$$

Loop-induced, chirality-flipping,

Typically $\Lambda_{\text{NP}} \sim \text{few} \times 100 \text{ GeV}$

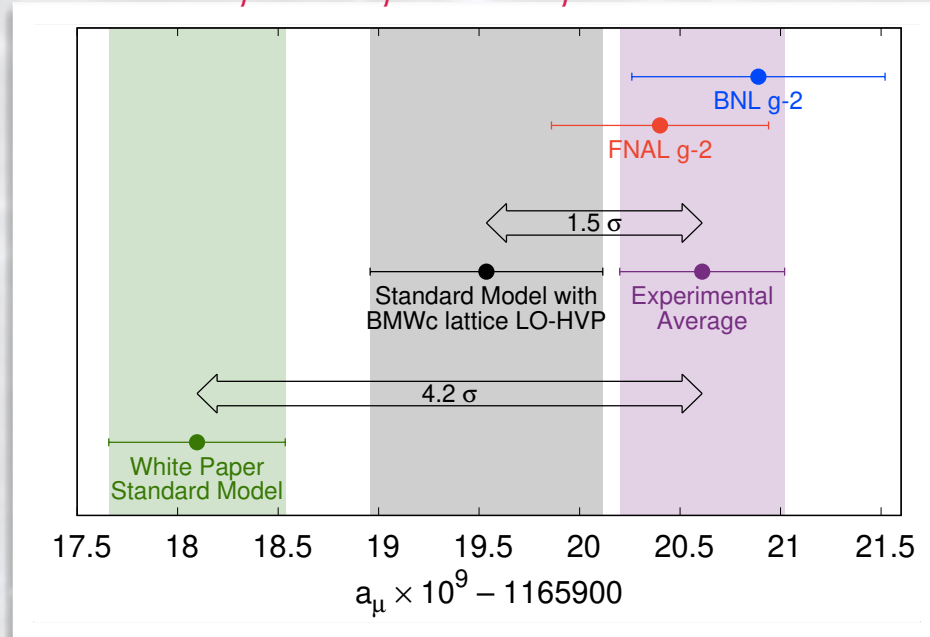
⇒ Huge impact for flavour pheno!

For recent “model survey” see e.g. Athron et al. [2104.03691]

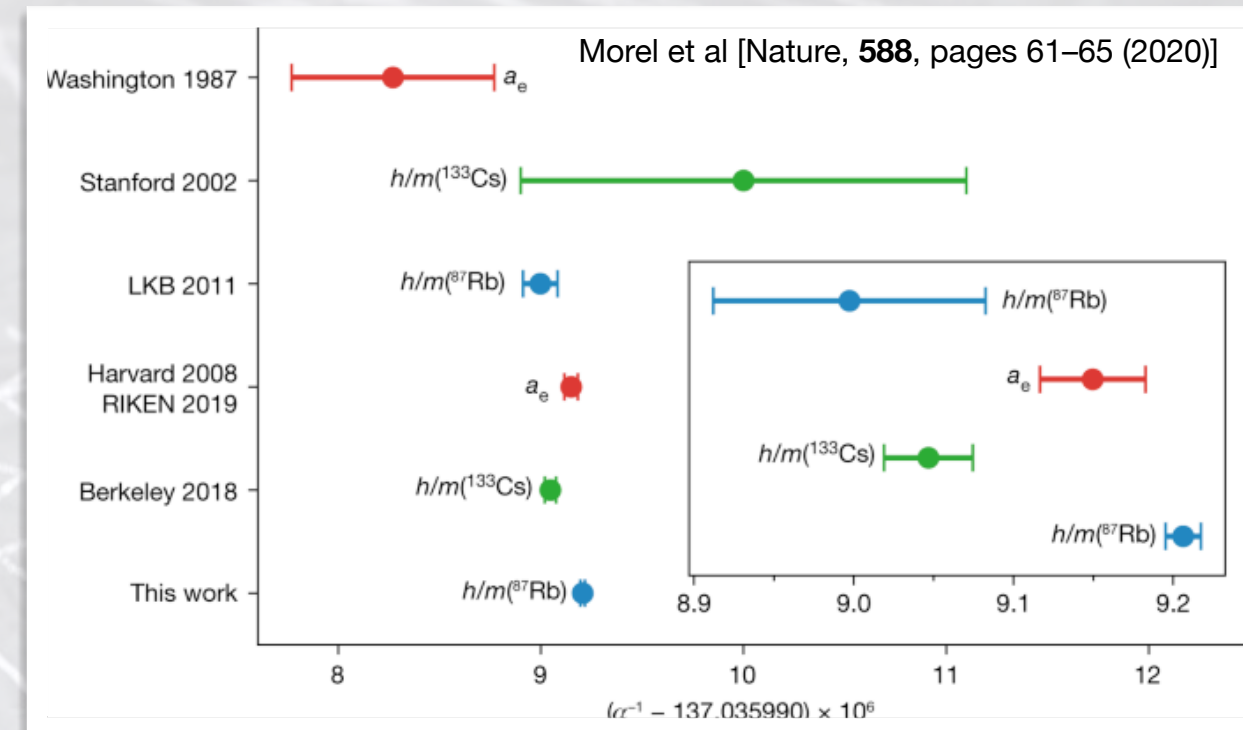
Anomalous magnetic moments: muon and electrons

Anomalous magnetic moment of the muon

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = ?$$



New Physics: badly needed? or not?



Recent experimental progress on α_e & a_e :

$$(2018) \Delta a_e^{\text{Cs}} = -0.88(36) \times 10^{-12} \sim -2.3\sigma$$

$$(2020) \Delta a_e^{\text{Rb}} = +0.48(30) \times 10^{-12} \sim +1.7\sigma$$

Lepton universality (MFV) suggests:

$$\Delta a_e / \Delta a_\mu \simeq m_e^2 / m_\mu^2 = +2.4 \times 10^{-5}$$

But $\Delta a_e^{\text{Cs}} / \Delta a_\mu = -3.3 \times 10^{-4} !$

\Rightarrow Hint of **violation** of lepton universality?

Explaining both Δa_e^{Cs} & Δa_μ in simple **BSM** is very hard...

... but possible! e.g. scalar leptoquarks, axions, light Z' , etc.

Difference of **5.4 σ** in determination of α_e ???

Lepton flavour universality

Accidental “symmetry” in the SM: couplings of electroweak gauge bosons are “blind” to **lepton flavour**
 \Rightarrow **Lepton Flavour Universality (LFU)**

Violation of **LFU** also signals the presence of **NP!**

Construct observables sensitive to **LFUV**:

\Rightarrow Compare **flavour-dependent** rates of charged and neutral current transitions

e.g. ratios of **EW gauge boson decays**:

$$R_Z^{\alpha\beta}, R_W^{\alpha\beta} = \frac{\Gamma(Z \rightarrow \ell_\alpha^+ \ell_\alpha^-)}{\Gamma(Z \rightarrow \ell_\beta^+ \ell_\beta^-)}, \frac{\Gamma(W \rightarrow \ell_\alpha \nu)}{\Gamma(W \rightarrow \ell_\beta \nu)}, \text{ in SM: } R_Z^{\alpha\beta}, R_W^{\alpha\beta} \simeq 1$$

$$R_Z^{\mu e} = 1.0001 \pm 0.0024 \text{ (LEP)}$$

$$R_W^{\mu e} = 0.996 \pm 0.008 \text{ (ATLAS)}$$

$$R_Z^{\tau\mu} = 1.0010 \pm 0.0026 \text{ (LEP)}$$

$$R_W^{\tau\mu} = 1.070 \pm 0.026 \text{ (LEP)}$$

$$R_Z^{\tau e} = 1.0020 \pm 0.0032 \text{ (LEP)}$$

$$R_W^{\tau e} = 1.063 \pm 0.027 \text{ (LEP)}$$

$$R_W^{\tau e} = 0.992 \pm 0.013 \text{ (ATLAS)}$$

\Rightarrow Place **strong bounds** on **New Physics**: e.g. neutrino mass models modifying W -vertex ...

Lepton flavour universality: leptonic meson decays

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Construct observables sensitive to **LFUV**:

Kaon sector: $R_K^\ell = \frac{\Gamma(K \rightarrow e\nu)}{\Gamma(K \rightarrow \mu\nu)} \propto \frac{m_e^2}{m_\mu^2}$

$$R_K^{\text{SM}} = (2.477 \pm 0.001) \times 10^{-5} \quad [\text{Cirigliano et al. '07}]$$

$$R_K^{\text{exp}} = (2.488 \pm 0.009) \times 10^{-5} \quad [\text{NA62}]$$

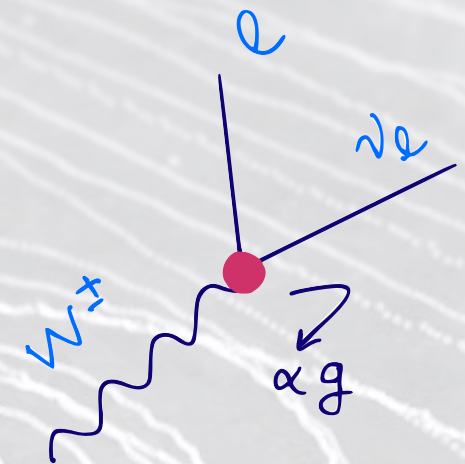
Pion sector: $R_{e/\mu}^\pi = \frac{\Gamma(\pi \rightarrow e\nu(\gamma))}{\Gamma(\pi \rightarrow \mu\nu(\gamma))}$

$$R_\pi^{\text{SM}} = (1.2354 \pm 0.0002) \times 10^{-4}$$

$$R_\pi^{\text{exp}} = (1.2327 \pm 0.0023) \times 10^{-4} \quad [\text{PiENU}]$$

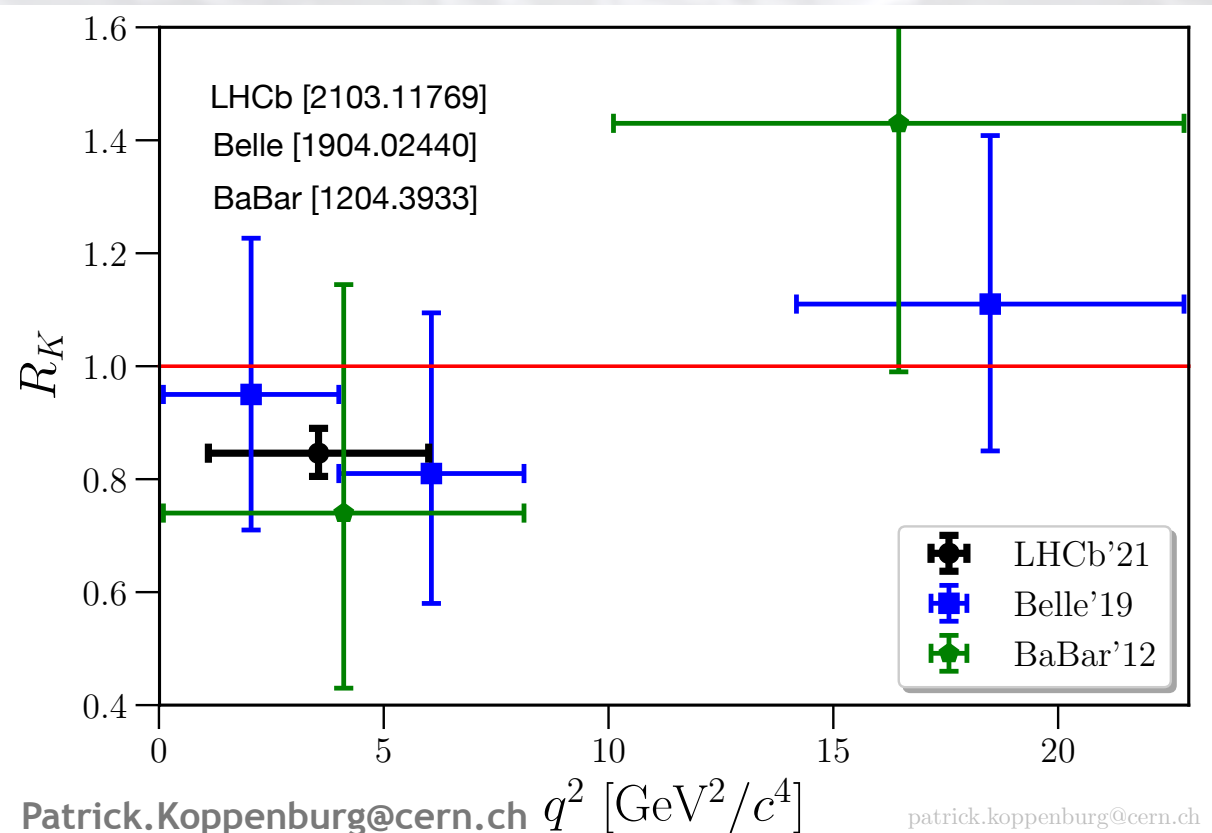
\Rightarrow **New Physics** contributions can be
 at most $\mathcal{O}(10^{-3})!!!$

(Similar observables for τ decays...)



Lepton flavour universality: semi-leptonic meson decays

Violation of **LFU** signals the presence of **NP**!



Theoretically clean: **hadronic uncertainties**
(mostly) cancel in ratios

$$\text{SM: } R_K = R_{K^*} \simeq 1$$

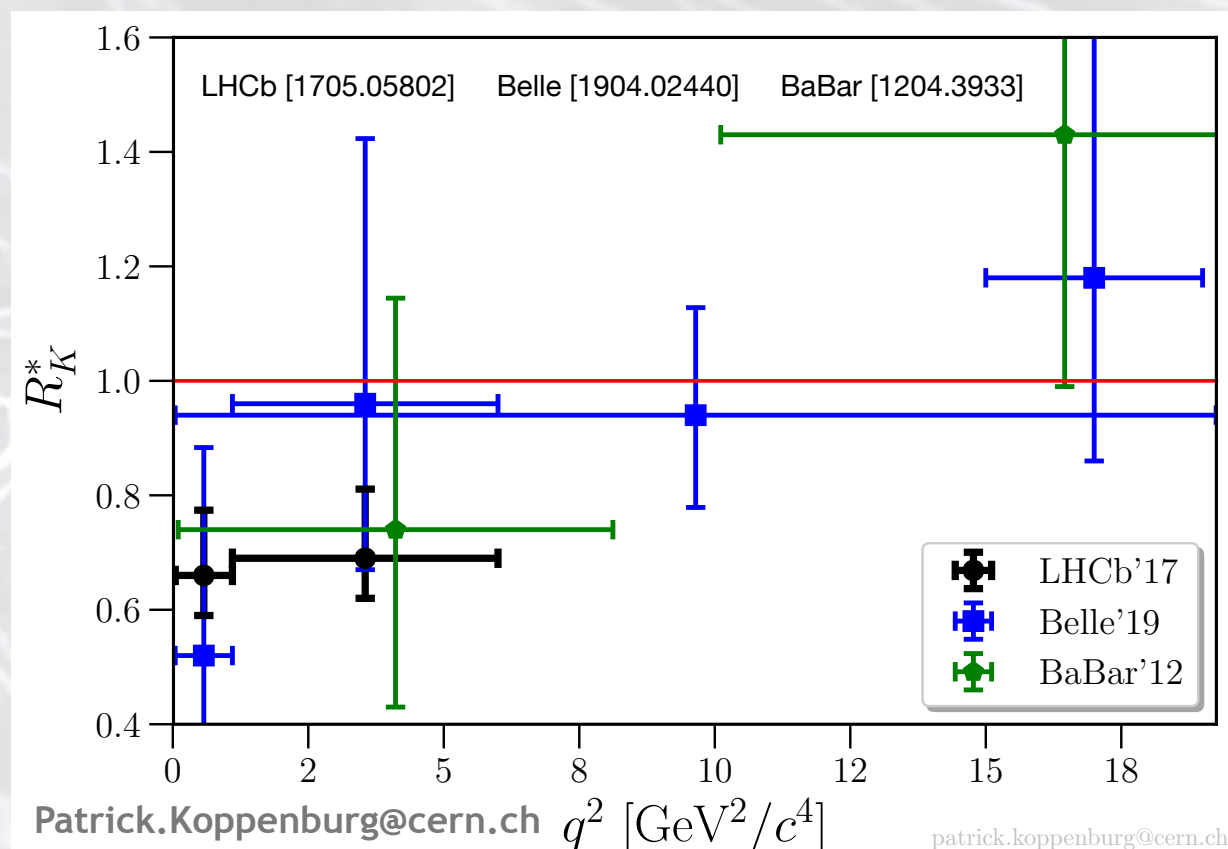
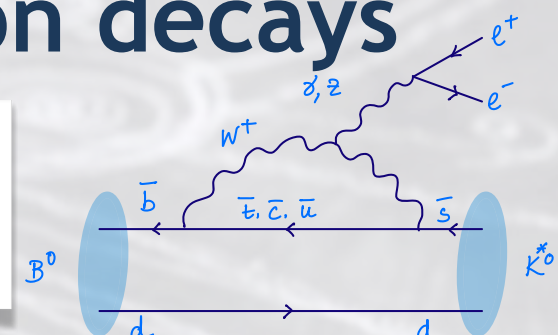
$$\text{Exp: } R_K^{[1.1,6]} = 0.846^{+0.044}_{-0.041} \text{ [LHCb]}$$

\Rightarrow **2 – 3 σ smaller than SM!** Hint on **LFUV** New Physics coupled to **muons**?

(Many other observables in $b \rightarrow s\ell\ell$ also in tension with SM)

See ATLAS, Belle II and LHCb talks in WG4!

$$R_{K^{(*)}} = \frac{\text{BR}(B \rightarrow K^{(*)}\mu\mu)}{\text{BR}(B \rightarrow K^{(*)}ee)}$$



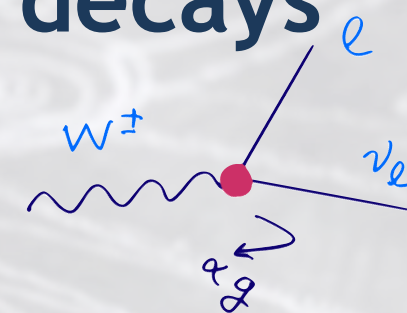
$$\text{Exp: } R_{K^*}^{[1.1,6]} = 0.69^{+0.11}_{-0.07} \pm 0.05 \text{ [LHCb]}$$

Lepton flavour universality: semi-leptonic meson decays

Violation of **LFU** signals the presence of **NP**!

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(mostly) cancel in ratios

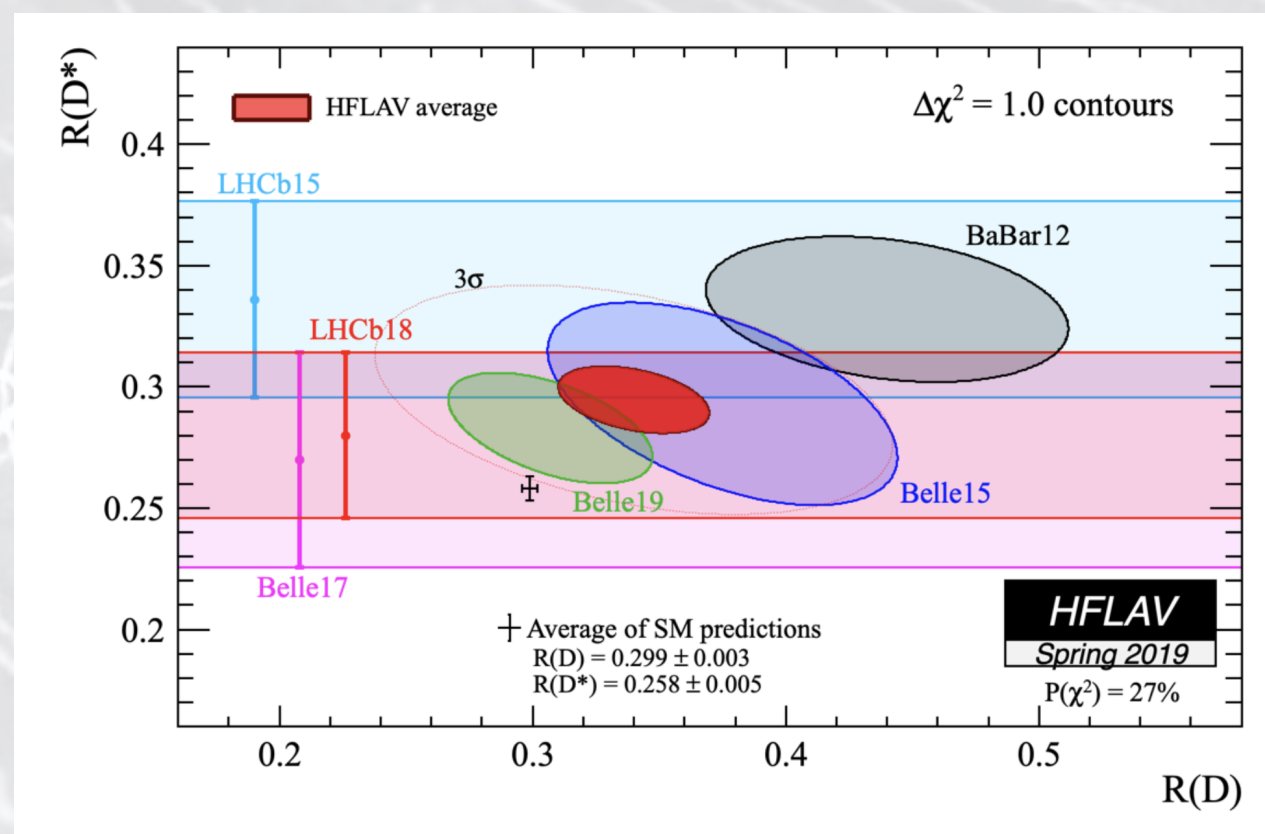
$$R_{D^{(*)}} = \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)}$$



SM: $R_D \simeq 0.299 \pm 0.003$, $R_{D^*} \simeq 0.258 \pm 0.005$

Exp: $R_D = 0.340 \pm 0.027 \pm 0.013$

$R_{D^*} = 0.295 \pm 0.011 \pm 0.008$



⇒ combined: $\sim 3\sigma$ larger than SM!

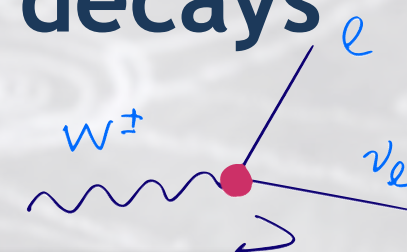
Hint on **LFUV** New Physics coupled to **tau leptons**?

See ATLAS, Belle II and LHCb talks in WG4!

Lepton flavour universality: semi-leptonic meson decays

Violation of **LFU** also signals the presence of **NP**!

$$R_{D^{(*)}} = \frac{\text{BR}(B \rightarrow D^{(*)}\tau\nu)}{\text{BR}(B \rightarrow D^{(*)}\ell\nu)}$$



S. Glashow '14: “[...] any departure from **lepton universality** is necessarily associated with the **violation of lepton flavour conservation**. No known symmetry principle can protect the one in the absence of the other”

[1411.0565]



R(D)

⇒ combined: $\sim 3\sigma$ larger than SM!

Hint on **LFUV** New Physics coupled to **tau leptons**?

See ATLAS, Belle II and LHCb talks in WG4!

cLFV decays

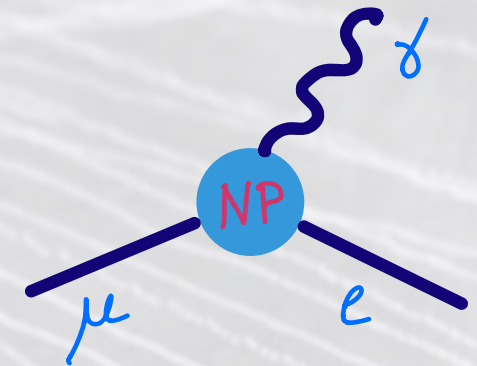
Any **cLFV** signal necessarily implies the presence of **New Physics**!

cLFV decay $\mu^+ \rightarrow e^+ \gamma$:

Clean event signature: **back-to-back** $e^+ \gamma$, with $E_\gamma = E_{e^+} \simeq m_\mu/2$

Current bound: $\text{BR}(\mu \rightarrow e \gamma) \lesssim 4.2 \times 10^{-13}$ (MEG)

Future **prospects**: $\text{BR}(\mu \rightarrow e \gamma) \lesssim 6 \times 10^{-14}$ (MEG II) (see also WG4 talk by Dylan Palo)

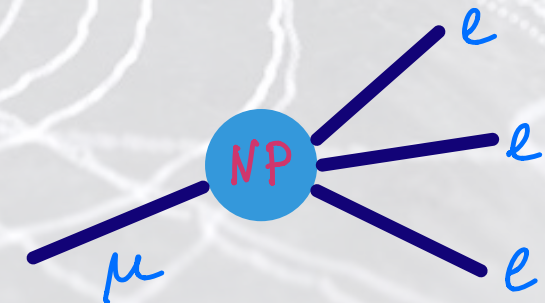


cLFV decay $\mu^+ \rightarrow e^+ e^- e^+$:

Event signature: **3 electrons in coincidence**, with $\sum p_e = (m_\mu, \vec{0})^T$

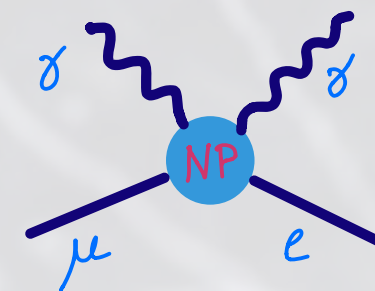
Current bound: $\text{BR}(\mu \rightarrow eee) \lesssim 1 \times 10^{-12}$ (Sindrum)

Future **prospects**: $\text{BR}(\mu \rightarrow eee) \lesssim 10^{-15(16)}$ (Mu3e) (see also WG4 talk by Ann-Kathrin Perrevoort)



More cLFV decays:

$\mu^+ \rightarrow e^+ \gamma \gamma$, $\mu^+ \rightarrow e^+ X (\rightarrow \gamma \gamma, e^+ e^-)$, $\mu \rightarrow e a$ (ALPs), ...



Muonic bound states & muonic atoms

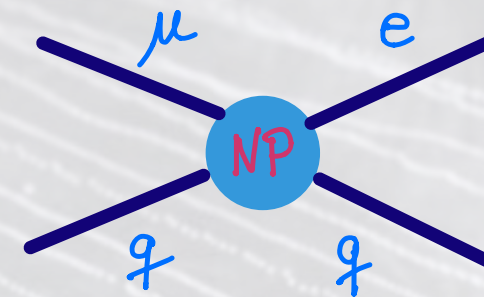
Any **cLFV** signal necessarily implies the presence of **New Physics**!

► **cLFV $\mu^- \rightarrow e^-$ conversion**: $\mu^- + (A, Z) \rightarrow e^- + (A, Z)^{(*)}$ (coherent conversion dominant)

Event signature: single mono-energetic e^- , with $E_e \simeq \mathcal{O}(100 \text{ MeV})$

Current bound: $\text{CR}(\mu \rightarrow e, \text{Au}) \lesssim 7 \times 10^{-13}$ (Sindrum II)

Future **prospects**: $\text{CR}(\mu \rightarrow e, \text{Al}) \lesssim \mathcal{O}(10^{-17} - 10^{-18})$ (Mu2e, COMET)
See many talks in WG4! (also DeeMe)



► **Coulomb enhanced $\mu^- e^- \rightarrow e^- e^-$ decay**: $\Gamma \propto \sigma_{\mu e \rightarrow ee} v_{\text{rel}} [(Z-1)\alpha_e m_e]^3$

Clean event signature: back-to-back e^- pair, with $E_e \simeq m_\mu/2$ Koike et al. [1003.1578]

Experimental status: **NEW observable!** (to be studied at COMET phase I ?)

Large Z enhancement, very complementary to $\mu \rightarrow eee$ & $\mu \rightarrow e\gamma$ Uesaka et al. [1508.05747]

► **cLFV & LNV $\mu^- - e^+$ conversion**: $\mu^- + (A, Z) \rightarrow e^+ + (A, Z-2)^*$

Complicated event signature, NMEs poorly known... **but: strong correlation with $0\nu 2\beta$!**

► **Muonium**: $\text{Mu}(\mu^+ e^-) \rightarrow \overline{\text{Mu}}(\mu^- e^+)$ **oscillation**, $\text{Mu}(\mu^+ e^-) \rightarrow e^+ e^-$ **decay**

$P(\text{Mu} \rightarrow \overline{\text{Mu}}) \lesssim 8 \times 10^{-11}$ (Willmann et al. '99)

cLFV observables across all sectors and energies

Any **cLFV** signal necessarily implies the presence of **New Physics**!

- ▶ **“Purely” leptonic cLFV observables:** $\ell_\beta \rightarrow \ell_\alpha \gamma, \ell_\beta \rightarrow \ell_\alpha \ell_\gamma \ell_{\gamma'}$
Most stringent exp. bounds: $\text{BR}(\mu \rightarrow e \gamma) \lesssim 4.2 \times 10^{-13}, \text{BR}(\mu \rightarrow eee) \lesssim 10^{-12}$
- ▶ **Muonic atoms:** many “nuclear-assisted” cLFV observables
e.g. neutrinoless $\mu - e$ conversion ($\mu^- N \rightarrow e^- N$): $\text{CR}(\mu - e, \text{Au}) \lesssim 7 \times 10^{-13}$
- ▶ **Semi-leptonic cLFV τ decays:** $\tau \rightarrow P \ell', \tau \rightarrow V \ell'; \text{BR}(\tau \rightarrow \phi \mu) \lesssim 8.4 \times 10^{-8}$
- ▶ **(Semi-) leptonic cLFV meson decays:** $M \rightarrow \ell_\alpha^\pm \ell_\beta^\mp, M \rightarrow M' \ell_\alpha^\pm \ell_\beta^\mp;$
 $\text{BR}(K_L \rightarrow \mu^\pm e^\mp) \lesssim 4.7 \times 10^{-12}, \text{BR}(B_{(s)} \rightarrow \ell_\alpha^\pm \ell_\beta^\mp) \lesssim \mathcal{O}(10^{-5})$
- ▶ **cLFV @ higher energies:** $Z \rightarrow \ell_\alpha^\pm \ell_\beta^\mp, H \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$, high- p_T di-lepton tails $pp \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$,
 $\text{BR}(Z \rightarrow \ell_\alpha^\pm \ell_\beta^\mp) \lesssim \mathcal{O}(10^{-6})$

cLFV observables across all sectors and energies

Any cLFV sign

► “Purely

Mo

► Muonic

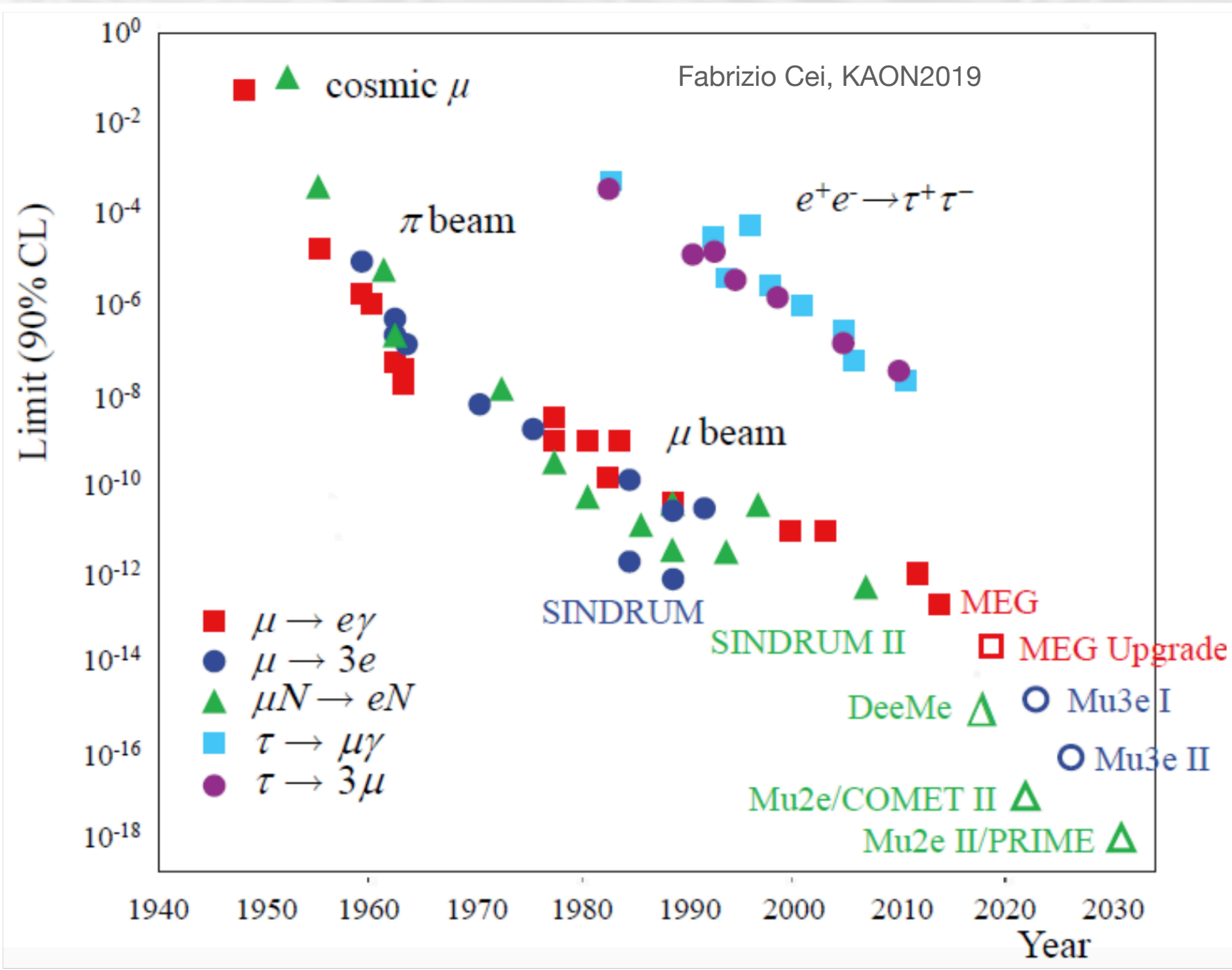
e.g. ne

► Semi-le

► (Semi-)

► cLFV @

BR



$e) \lesssim 10^{-12}$

10^{-13}

10^{-8}

$p \rightarrow \ell_\alpha^\pm \ell_\beta^\mp$

(Dis)entangling cLFV sources

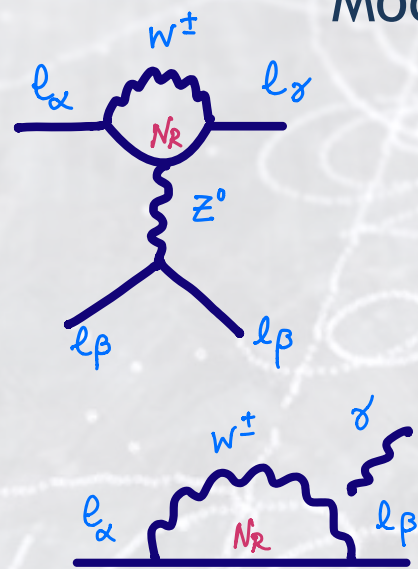
cLFV signals – correlations matter

Synergy of **cLFV observables** very important: probe different **operators/topologies**

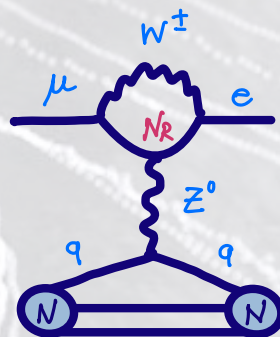
$\text{BR}(\mu \rightarrow e\gamma)$, $\text{BR}(\mu \rightarrow eee)$, $\text{CR}(\mu - e, N)$ correlated by **common topologies**:

γ **dipoles & anapoles**, **Z penguins**, tree-level contributions,... \Rightarrow 4-fermion operators

Model-dependent: certain **topologies** dominate, **tree-level cont. might be present**



Model	$\mu \rightarrow eee$	$\mu N \rightarrow eN$	$\frac{\text{BR}(\mu \rightarrow eee)}{\text{BR}(\mu \rightarrow e\gamma)}$	$\frac{\text{CR}(\mu N \rightarrow eN)}{\text{BR}(\mu \rightarrow e\gamma)}$
MSSM	Loop	Loop	$\approx 6 \times 10^{-3}$	$10^{-3} - 10^{-2}$
Type-I seesaw	Loop*	Loop*	$3 \times 10^{-3} - 0.3$	$0.1 - 10$
Type-II seesaw	Tree	Loop	$(0.1 - 3) \times 10^3$	$\mathcal{O}(10^{-2})$
Type-III seesaw	Tree	Tree	$\approx 10^3$	$\mathcal{O}(10^3)$
LFV Higgs	Loop [†]	Loop* [†]	$\approx 10^{-2}$	$\mathcal{O}(0.1)$
Composite Higgs	Loop*	Loop*	$0.05 - 0.5$	$2 - 20$



Calibbi et al. [1709.00294]

\Rightarrow study **correlations/ratios** of **cLFV observables**, might find **peculiar cLFV patterns**

\Rightarrow provide complementary information to direct searches

In **EFT**: RGE leads to **operator mixing**, need to consider as many **observables** as possible

$$\text{to constrain } \mathcal{L}^{\text{eff}} = \mathcal{L}^{\text{SM}} + \frac{\mathcal{O}^5 \mathcal{O}^5}{\Lambda_{\text{LNV}}^5} (m_\nu) + \frac{\mathcal{O}^6 \mathcal{O}^6}{\Lambda_{\text{CLFV}}^2} (\ell_i \leftrightarrow \ell_j) + \dots + \frac{\mathcal{O}^9 \mathcal{O}^9}{\Lambda_{\text{LNV}}^5} (0\nu 2\beta) + \dots$$

See S. Davidson NuFact 2021

Neutrino **mass** generation

Mechanisms of m_ν generation: account for **oscillation data**

and ideally address **SM issues** – BAU (leptogenesis), DM candidates, ...

Many well motivated possibilities, featuring distinct NP states (singlets, triplets)

Realised at **very different scales** $\Lambda_{EW} \rightsquigarrow \Lambda_{GUT}$

⇒ Expect very different **phenomenological impact**

See also talk by
Julian Heeck tomorrow

Compare “vanilla” type I seesaw vs. **low-scale seesaw**:

High scale: $\mathcal{O}(10^{10-15} \text{ GeV})$

Theoretically “natural” $Y^\nu \sim 1$

“Vanilla” leptogenesis

Decoupled new states

Low scale: $\mathcal{O}(\text{MeV} - \text{TeV})$

Finetuning of Y^ν (or approximate LN conservation)

Leptogenesis possible (resonant, ...)

New states **within experimental reach!**

Collider, high-intensities (“leptonic observables”)

⇒ **low-scale seesaws** (and variants): non-decoupled states, **modified lepton currents!**

⇒ rich phenomenology at colliders, high intensities and **low energies**

(Also expect tight constraints)

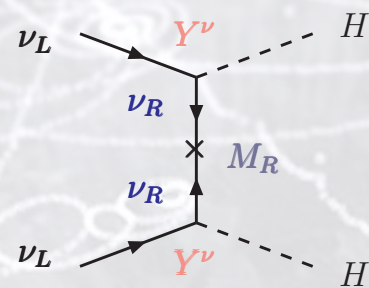
testability!!

Disentangle seesaw mass models – more correlations

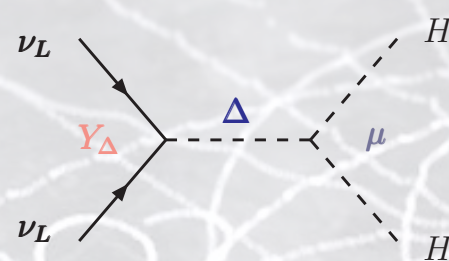
- **Models of m_ν** (and leptonic LFV) predict/accommodate **extensive ranges for cLFV...**

In the absence of direct NP discovery - **correlations** might allow to disentangle models and provide important **complementary information** to direct searches!

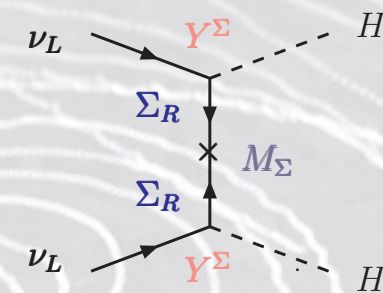
- **Seesaw realisations:** distinctive signatures for numerous **cLFV observables**
ratios of **observables** to **identify seesaw mediators** & constrain their masses!



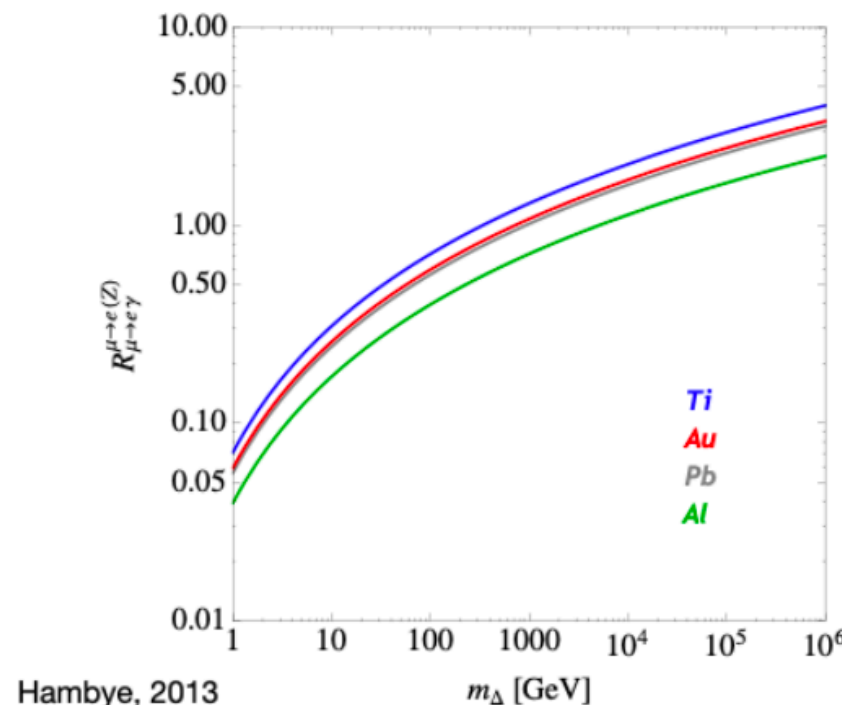
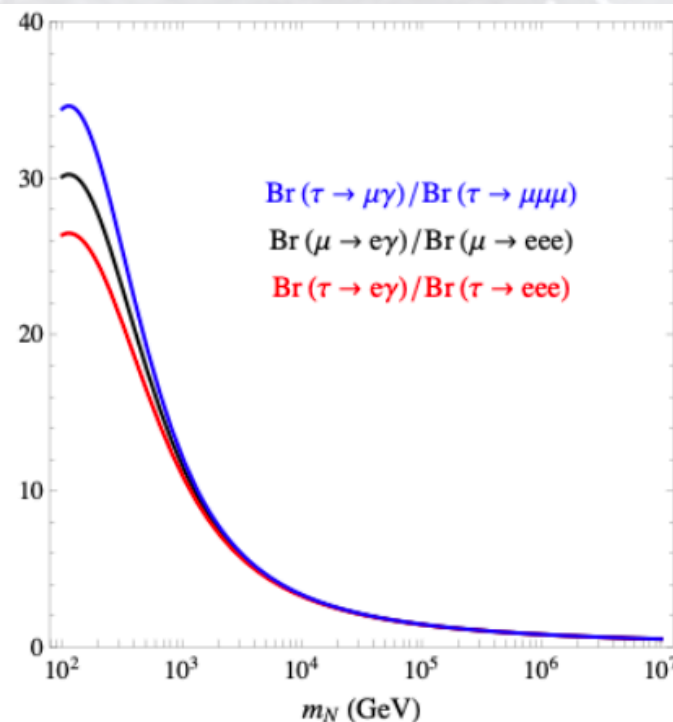
Type I (fermion singlet)



Type II (scalar triplet)



Type III (fermion triplet)



$$\frac{\text{BR}(\mu \rightarrow e\gamma)}{\text{BR}(\mu \rightarrow 3e)} = 1.3 \times 10^{-3}$$

$$\frac{\text{BR}(\tau \rightarrow \mu\gamma)}{\text{BR}(\tau \rightarrow 3\mu)} = 1.3 \times 10^{-3}$$

$$\frac{\text{BR}(\mu \rightarrow e\gamma)}{\text{CR}(e-\mu, \text{Ti})} = 3.1 \times 10^{-4}$$

A “3+2” neutrino toy model

Simplified “toy models” for phenomenological analyses: SM + ν_s

► Ad-hoc (low-energy) constructions: SM extended via n_s **Majorana massive** states

No assumption on mechanism of mass generation

Well-defined interactions in physical basis

Phenomenological low-energy limit of complete constructions (type I seesaw, ISS, ...)

Hypotheses: **3 active neutrinos** + **2 sterile states**

interaction basis \leftrightarrow physical basis

Left-handed lepton mixing \tilde{U}_{PMNS}

3×3 sub-block, **non-unitary!**

Active-sterile mixing $U_{\alpha i}$

3×5 rectangular matrix

$$n_L = (\nu_{Le}, \nu_{L\mu}, \nu_{L\tau}, \nu_s^c, \nu_{s'}^c)^T$$

$$|n_L\rangle = \mathcal{U}_{5 \times 5} |\nu_i\rangle$$

$$\mathcal{U}_{5 \times 5} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} & U_{e5} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} & U_{\mu5} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} & U_{\tau5} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} & U_{s5} \\ U_{s'1} & U_{s'2} & U_{s'3} & U_{s'4} & U_{s'5} \end{pmatrix}$$

$$\mathcal{U} = R_{45} R_{35} R_{25} R_{15} R_{34} R_{24} R_{14} R_{23} R_{13} R_{12} \times \text{diag}(1, e^{i\varphi_2}, e^{i\varphi_3}, e^{i\varphi_4}, e^{i\varphi_5})$$

Would-be **PMNS** no longer unitary, leptonic **W** and **Z** vertices modified

► **Physical parameters:** 5 masses [3 light (mostly active) & 2 heavier (mostly sterile) states]

10 mixing angles, **10 CPV phases** (6 **Dirac** δ_{ij} , 4 **Majorana** φ_i)

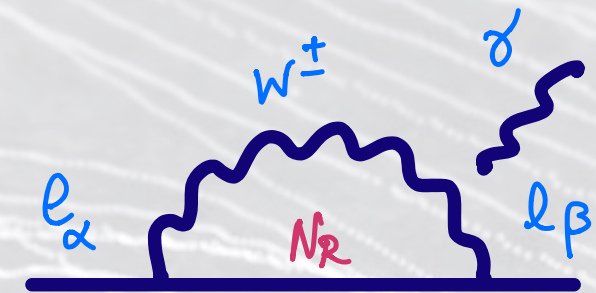
The impact of **CP violating** phases

cLFV processes mediated by HNL at loop-level

Consider "**3+2**" **toy model** (addition of **2 heavy sterile** states; leptonic mixing $\mathcal{U}_{5 \times 5}$, **CPV** phases)

► **Radiative decays:** $\text{BR}(\mu \rightarrow e\gamma) \propto |G_\gamma^{\mu e}|^2$

$$G_\gamma^{\mu e} = \sum_{i=4,5} \mathcal{U}_{ei} \mathcal{U}_{\mu i}^* G_\gamma \left(\frac{m_{N_i}^2}{m_W^2} \right)$$



Assume (for *simplicity & illustrative purposes*): $m_4 \approx m_5$ and $\sin \theta_{\alpha 4} \approx \sin \theta_{\alpha 5} \ll 1$

$$|G_\gamma^{\mu e}|^2 \approx 4 \sin^2 \theta_{e4} \sin^2 \theta_{\mu 4} \cos^2 \left(\frac{\delta_{14} + \delta_{25} - \delta_{15} - \delta_{24}}{2} \right) G_\gamma \left(\frac{m_{N_i}^2}{m_W^2} \right)$$

⇒ **Radiative decays:** rate depends **only on Dirac phases**; full cancellation for $\Sigma \delta = \pi$

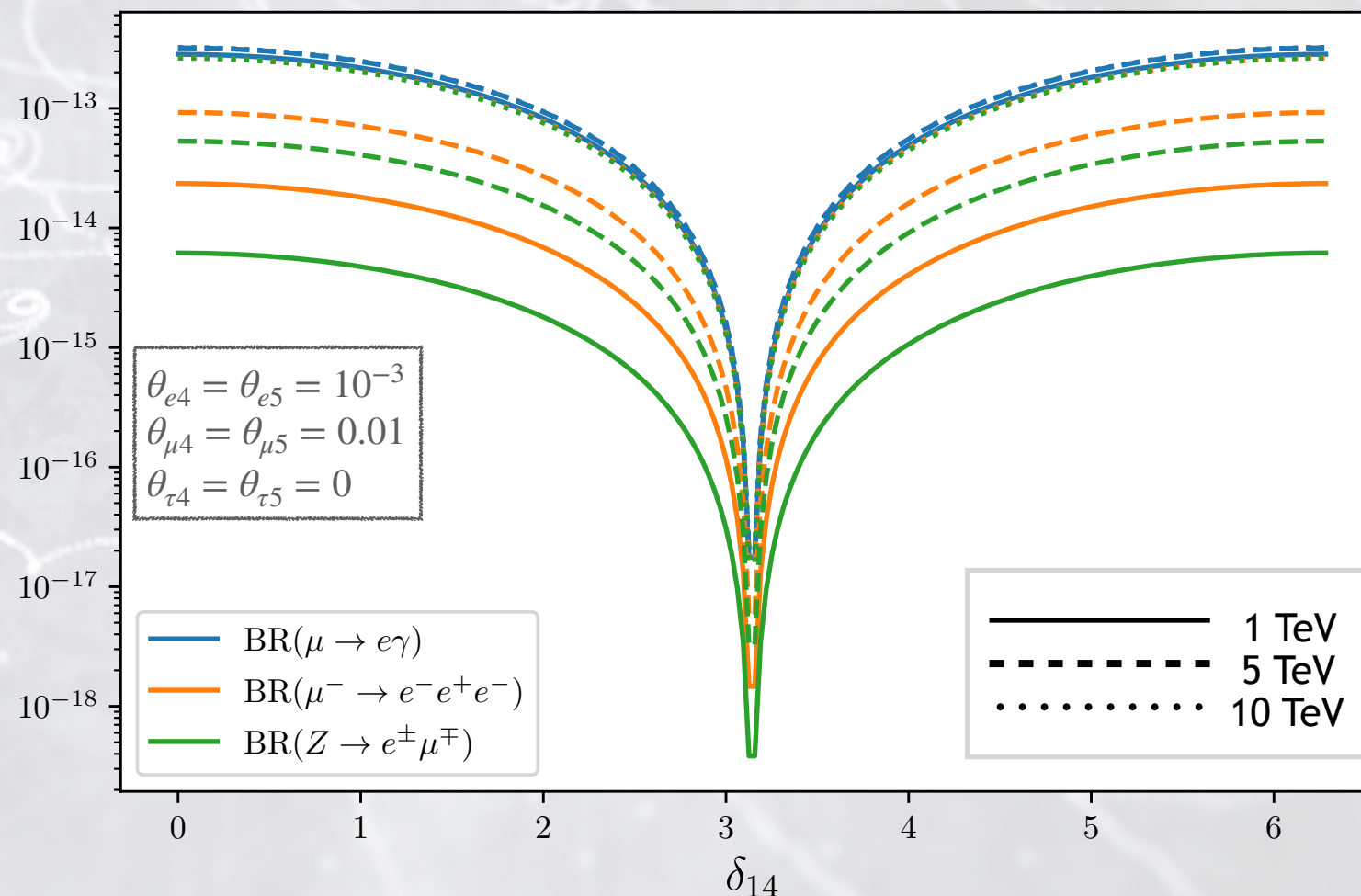
(Other form factors - more involved expressions, depend also on **Majorana phases** $\varphi_{4,5}$)

The impact of CP violating phases: Dirac

cLFV processes mediated by HNL at loop-level

Consider "3+2" toy model (addition of 2 heavy sterile states; leptonic mixing $\mathcal{U}_{5 \times 5}$, CPV phases)

Abada, JK, Teixeira [2107.06313]



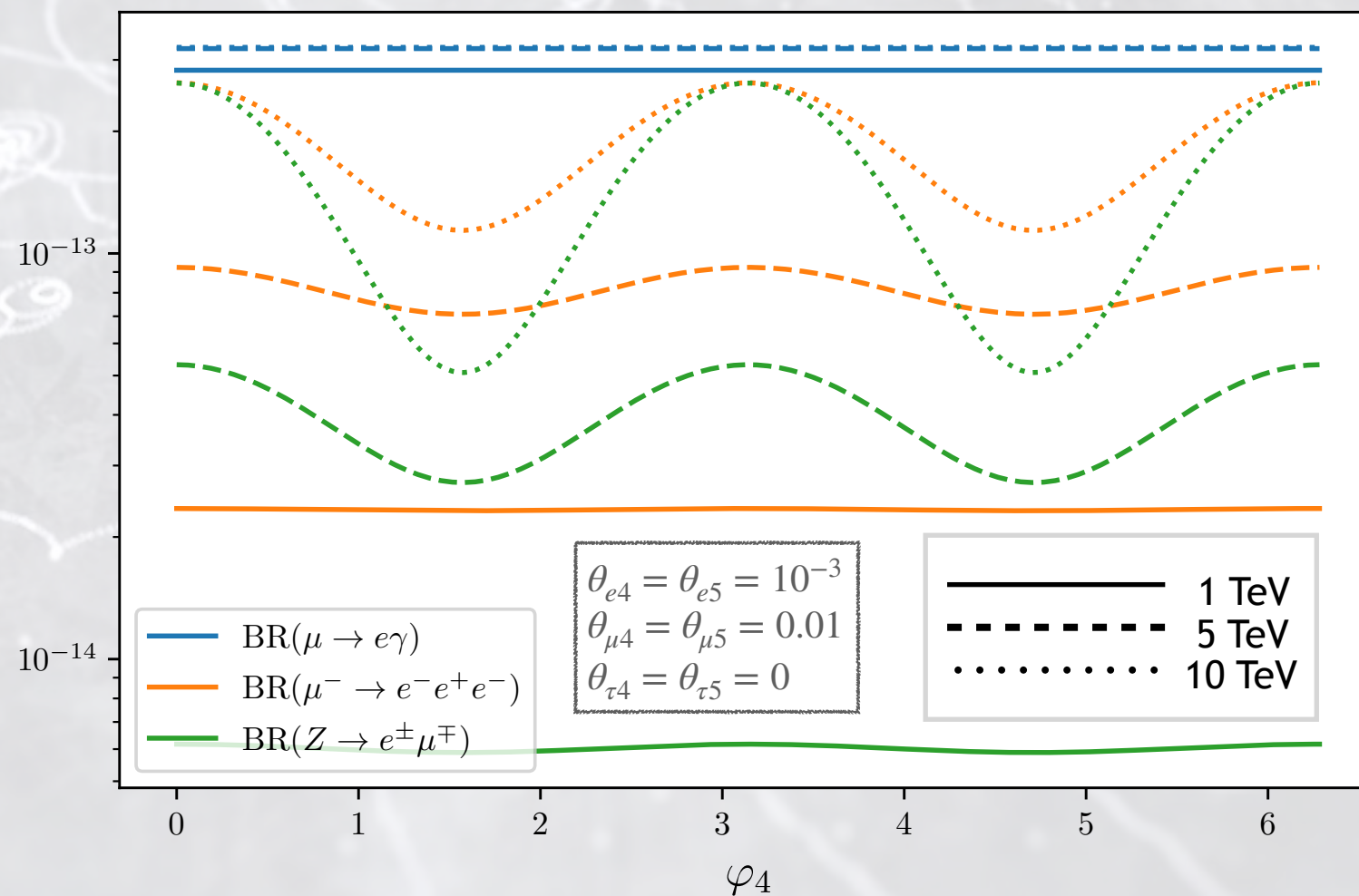
⇒ Full cancellation of the rates for $\delta_{14} = \pi$, similar results for other (Dirac) phases

The impact of CP violating phases: Majorana

cLFV processes mediated by HNL at loop-level

Consider "3+2" toy model (addition of 2 heavy sterile states; leptonic mixing $\mathcal{U}_{5 \times 5}$, CPV phases)

Abada, JK, Teixeira [2107.06313]



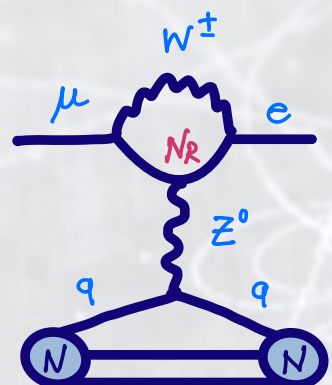
⇒ Milder dependence, γ -penguin independent of Majorana phases

The impact of CP violating phases – no more correlations

cLFV signatures: ratios of **observables** to identify mediators & constrain their masses!

But - **CP violating phases do matter!** And impact naïve expectations...

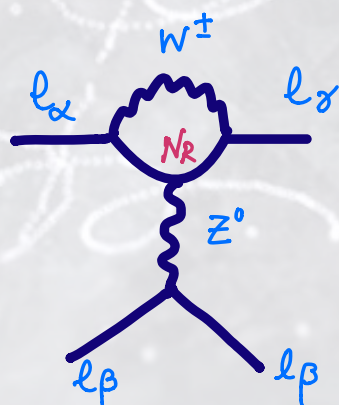
Consider "3+2" toy model (addition of 2 heavy sterile states; leptonic mixing $\mathcal{U}_{5 \times 5}$, **CPV** phases)



Observables dominated by **common topology: Z-penguins**

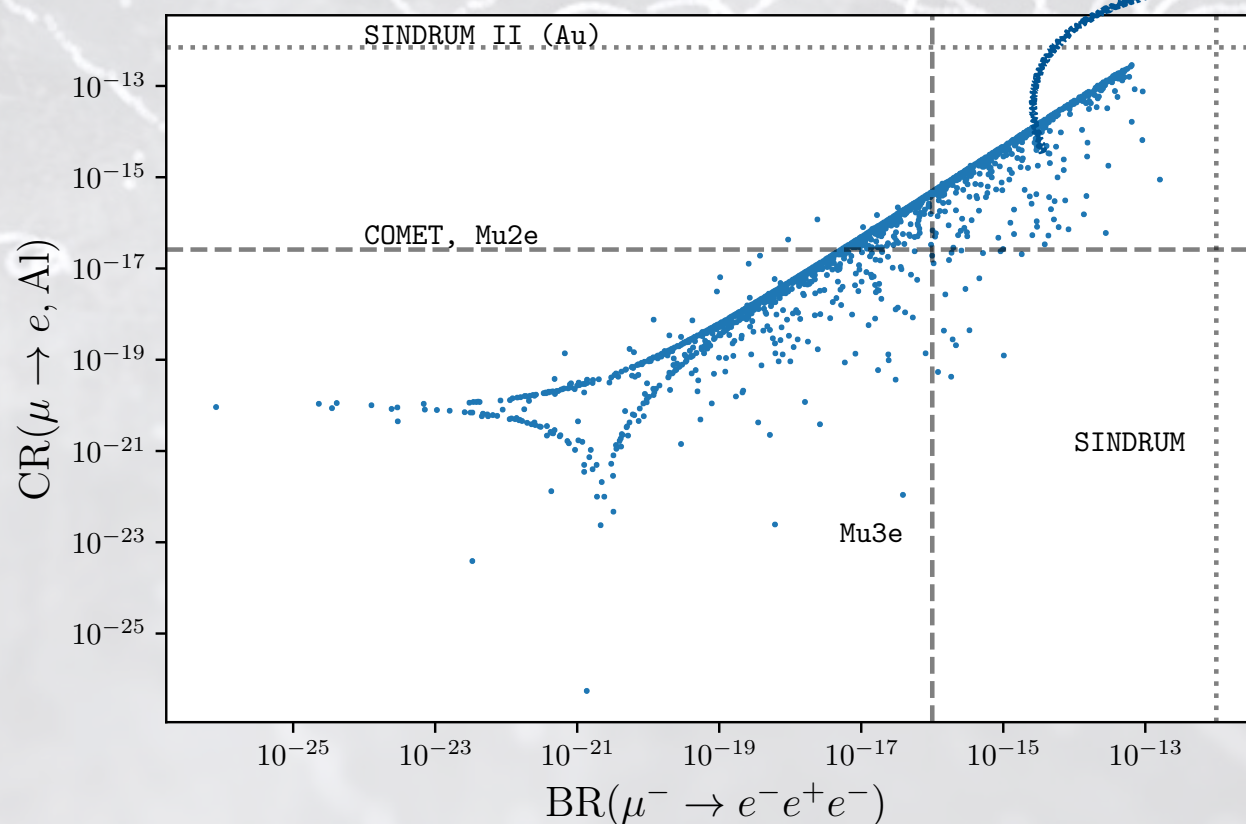
$\mu - e$ conversion in nuclei

3-body muon decays ($\mu \rightarrow 3e$)



$m_4 = m_5 = 1 \text{ TeV}$

• CP conserving



Strong correlation
(CP conserving)

Observation of $\mu \rightarrow 3e$
 \Rightarrow observation of
 $\mu - e$ conversion

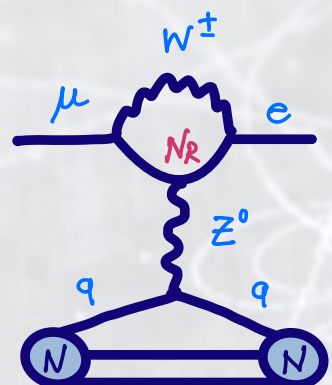
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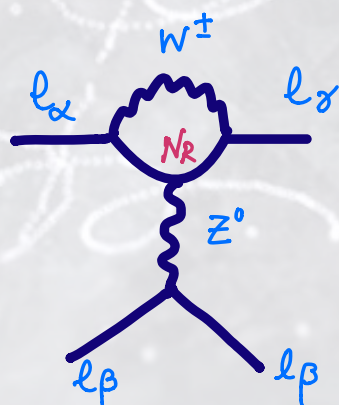
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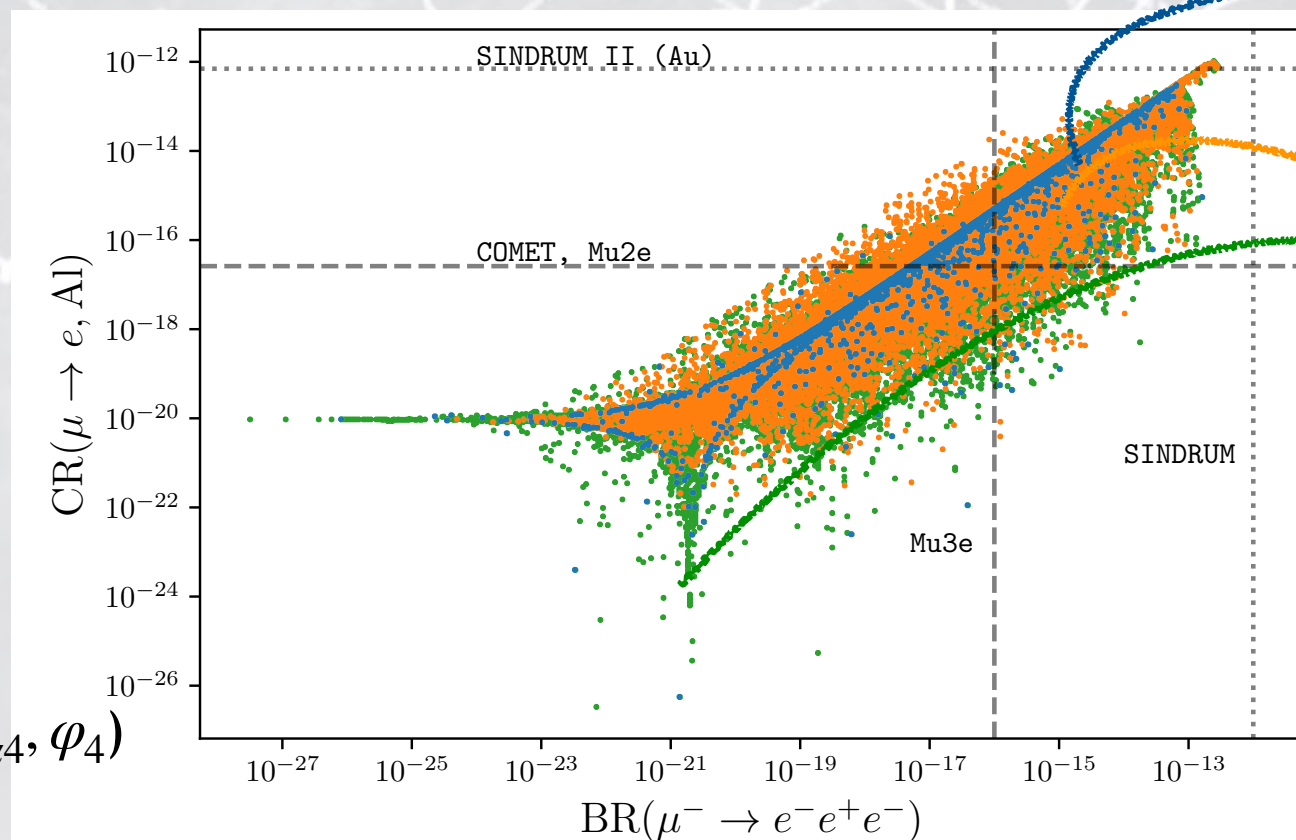
$\mu - e$ conversion in nuclei

3-body muon decays ($\mu \rightarrow 3e$)



$m_4 = m_5 = 1 \text{ TeV}$

- CP conserving
- CPV phases (random $\delta_{\alpha 4}, \varphi_4$)
- CPV phases (grid $n\pi/4$)



Abada, JK, Teixeira [2107.06313]

Strong correlation
(CP conserving)

Loss of correlation!
(CP violating)

Observation of $\mu \rightarrow 3e$
↯ observation of $\mu - e$ conversion

The impact of CP violating phases – no more correlations

cLFV signatures: ratios of **observables** to identify mediators & constrain their masses!

But - **CP violating phases do matter!** And impact naïve expectations...

Some *illustrative* benchmark points - **CP conserving** (P_i) and **CPV variants** (P'_i)

	$\text{BR}(\mu \rightarrow e\gamma)$	$\text{BR}(\mu \rightarrow 3e)$	$\text{CR}(\mu - e, \text{Al})$	$\text{BR}(\tau \rightarrow 3\mu)$	$\text{BR}(Z \rightarrow \mu\tau)$
P_1	3×10^{-16} ○	1×10^{-15} ✓	9×10^{-15} ✓	2×10^{-13} ○	3×10^{-12} ○
P'_1	1×10^{-13} ✓	2×10^{-14} ✓	1×10^{-16} ✓	1×10^{-10} ✓	2×10^{-9} ✓
P_2	2×10^{-23} ○	2×10^{-20} ○	2×10^{-19} ○	1×10^{-10} ✓	3×10^{-9} ✓
P'_2	6×10^{-14} ✓	4×10^{-14} ✓	9×10^{-14} ✓	8×10^{-11} ✓	1×10^{-9} ✓
P_3	2×10^{-11} ✗	3×10^{-10} ✗	3×10^{-9} ✗	2×10^{-8} ✓	8×10^{-7} ✓
P'_3	8×10^{-15} ○	1×10^{-14} ✓	6×10^{-14} ✓	2×10^{-9} ✓	1×10^{-8} ✓

Abada, JK, Teixeira [2107.06313]

P_3 : only **cLFV τ decays** in allowed region; **cLFV μ transitions** already experimentally disfavoured
Regime of large mixing angles excluded?

P'_3 : *all* considered **cLFV transitions** currently allowed, $\mu \rightarrow e\gamma$ beyond sensitivity!

(Non)-observation of **cLFV observable(s)** \Rightarrow *not* necessarily **disfavour** HNL extension!

CP-asymmetries

Correlations broken, large mixing angles still possible, how do we “tag” the presence of **CPV**?

Benchmark points (with different mixing)

P_1 (CP-conserving), P_2 (CP-violating)

lead to identical **cLFV** predictions!

Observable	$\mu \rightarrow eee$	$\mu - e$ (Al)	$\tau \rightarrow \mu\mu\mu$	$Z \rightarrow \mu\tau$
$P_{1,2}$ prediction	2×10^{-15}	5×10^{-14}	1×10^{-10}	2×10^{-10}

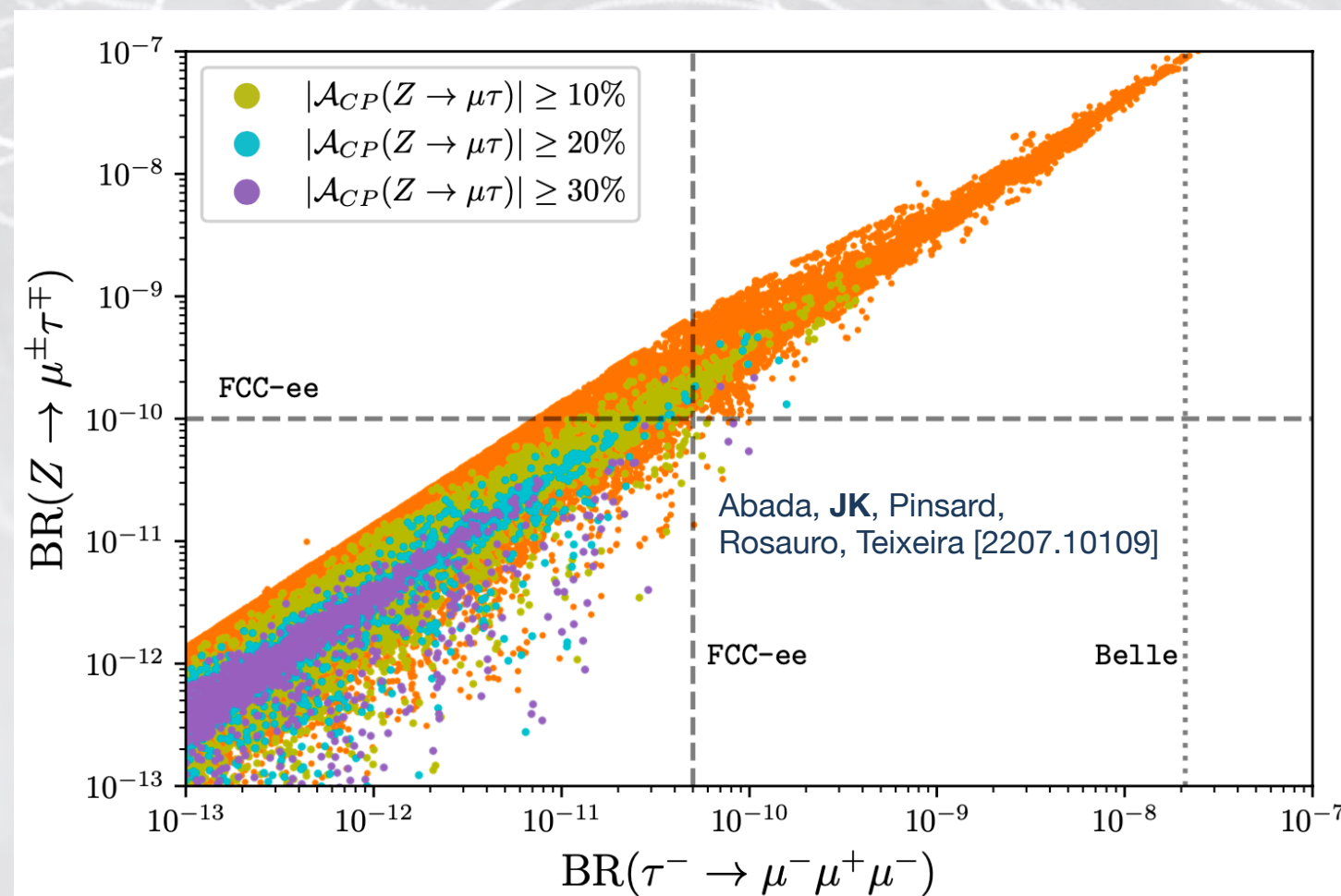
Abada, **JK**, Pinsard,
Rosauro, Teixeira [2207.10109]

Consider **CP**-asymmetries: $\mathcal{A}_{CP}(Z \rightarrow \ell_\alpha \ell_\beta) = \frac{\Gamma(Z \rightarrow \ell_\alpha^+ \ell_\beta^-) - \Gamma(Z \rightarrow \ell_\alpha^- \ell_\beta^+)}{\Gamma(Z \rightarrow \ell_\alpha^+ \ell_\beta^-) + \Gamma(Z \rightarrow \ell_\alpha^- \ell_\beta^+)}$

$\Rightarrow P_2$: $\mathcal{A}_{CP}(Z \rightarrow \mu\tau) \simeq 30\%$!

Measuring **CP**-asymmetries, i.e. searching for $Z \rightarrow \ell_\alpha^+ \ell_\beta^-$ and $Z \rightarrow \ell_\alpha^- \ell_\beta^+$ independently might allow to constrain **CPV** phases and can help to identify the **source of cLFV**!

CP (T)-asymmetries have also been considered in angular distributions of $\mu \rightarrow eee$
(see Bolton & Petcov [2204.03468])



CP-asymmetries

Correlations broken, large mixing angles still possible, how do we “tag” the presence of CPV?

Benchmark points (with different mixing)

P_1 (CP-conserving), P_2 (CP-violating)

lead to identical cLFV predictions!

Observable	$\mu \rightarrow eee$	$\mu - e$ (Al)	$\tau \rightarrow \mu\mu\mu$	$Z \rightarrow \mu\tau$
$P_{1,2}$ prediction	2×10^{-15}	5×10^{-14}	1×10^{-10}	2×10^{-10}

Consider CP-asymmetries: $\mathcal{A}_{CP}(Z \rightarrow \ell^+ \ell^-)$

$\Rightarrow P_2$:

"You cannot spell **flaVour** without **CP Violation**"
Phases do really matter!

Measuring CP-asymmetries

for $Z \rightarrow \ell_\alpha^+ \ell_\beta^-$ and $Z \rightarrow \ell_\alpha^- \ell_\beta^+$ independently

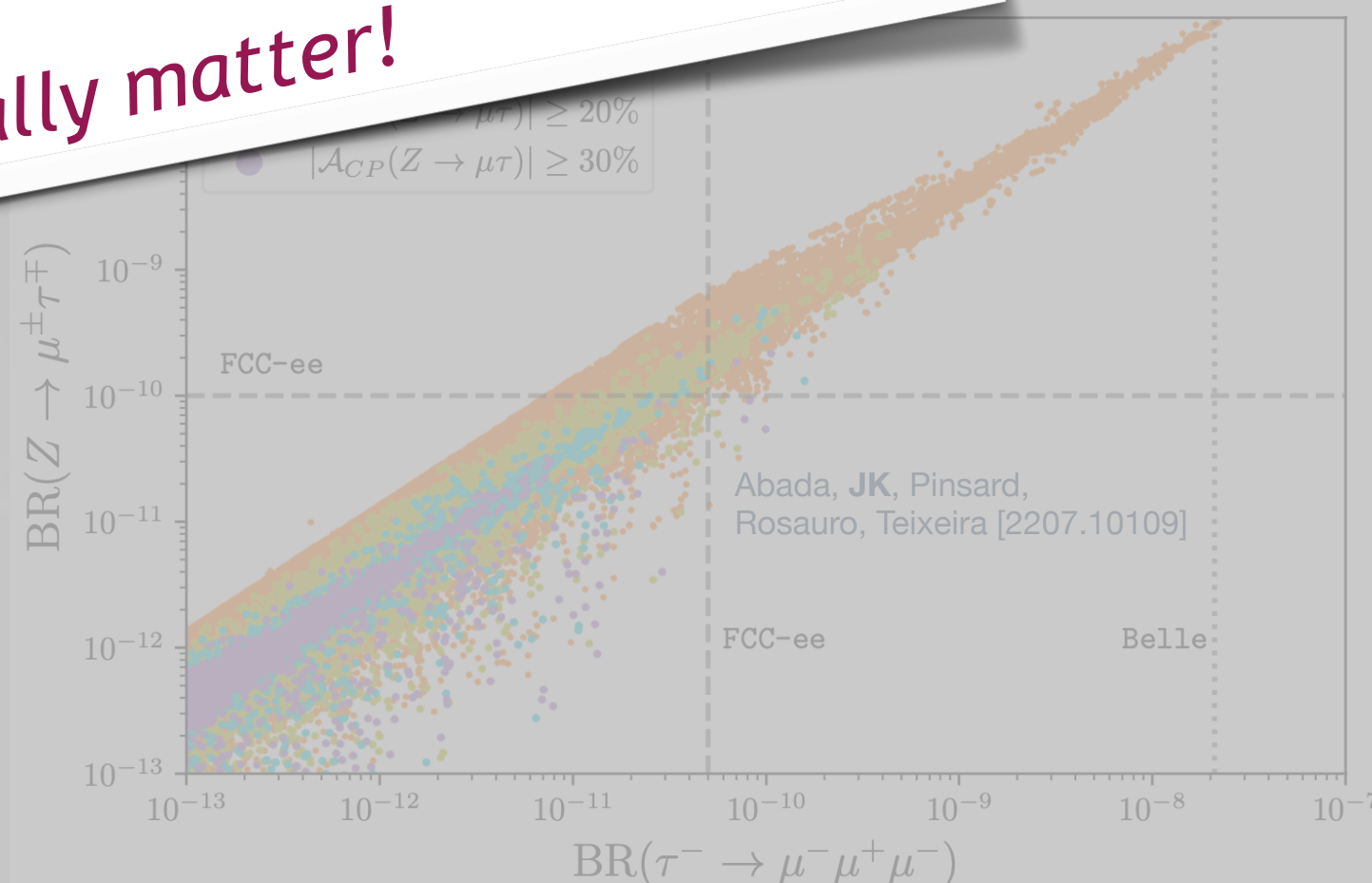
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CP (T)-asymmetries also been considered in

angular distribution of $\mu \rightarrow eee$

(see Bolton & Petcov [2204.03468])



The probing power of muons

The probing power of flavour violation

Paving the way to the SM: from prediction of **charm** to the existence of **3 families!**

⇒ **Indirect probes** of much higher scales: e.g. **top mass** in $K^0 - \bar{K}^0$ oscillations

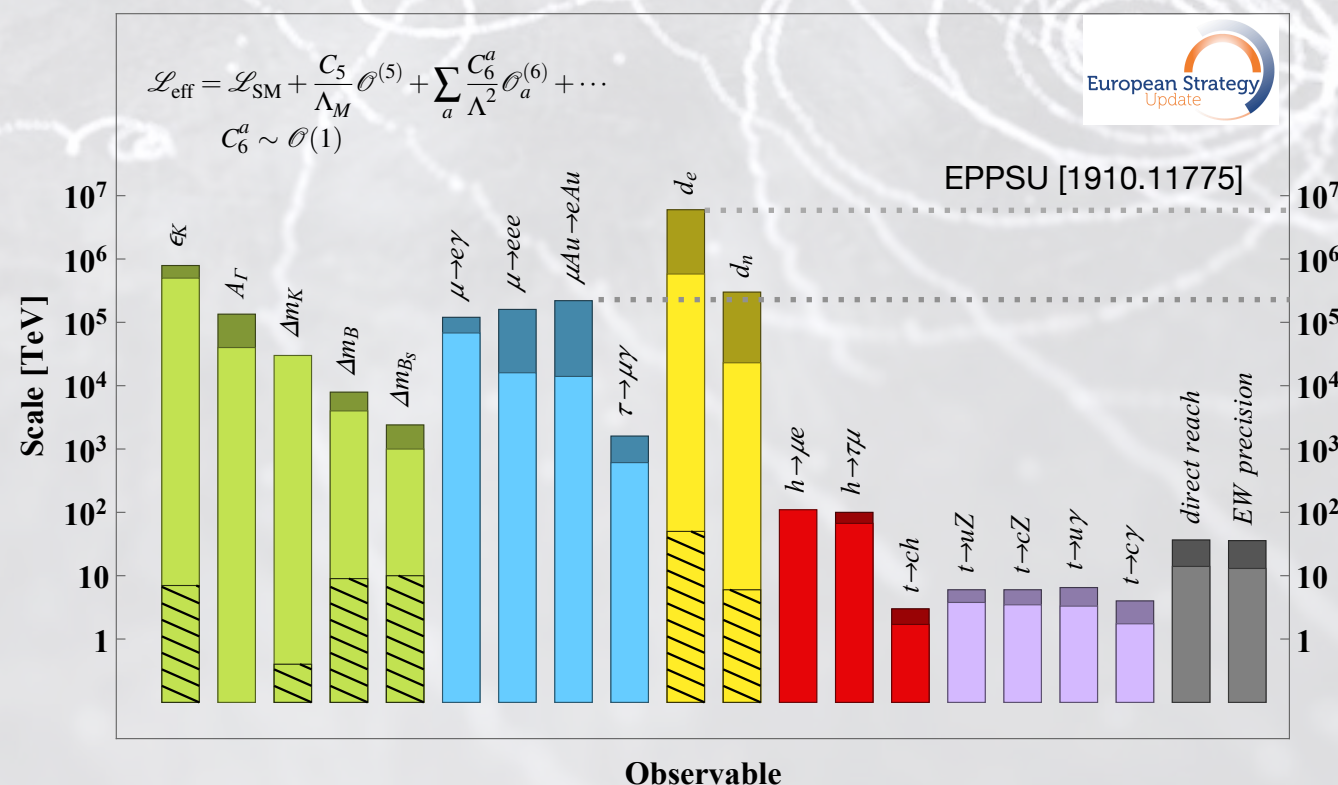
SM interpreted as a **low-energy limit** of a (complete, yet unknown) **NP model**

⇒ Study various classes of well-motivated models

⇒ Model-independent, **effective approach (EFT)**

$$\mathcal{L}^{\text{eff}} = \mathcal{L}^{\text{SM}} + \sum_{n \geq 5} \frac{1}{\Lambda^{n-4}} \mathcal{C}^n(g, Y, \dots) \mathcal{O}^n(\ell, q, H, \gamma, \dots)$$

Cast **current data** in terms of \mathcal{C}_{ij}^6 and Λ_{NP} : $\mathcal{C}_{ij}^6 \approx 1 \Rightarrow$ bounds on Λ_{NP}

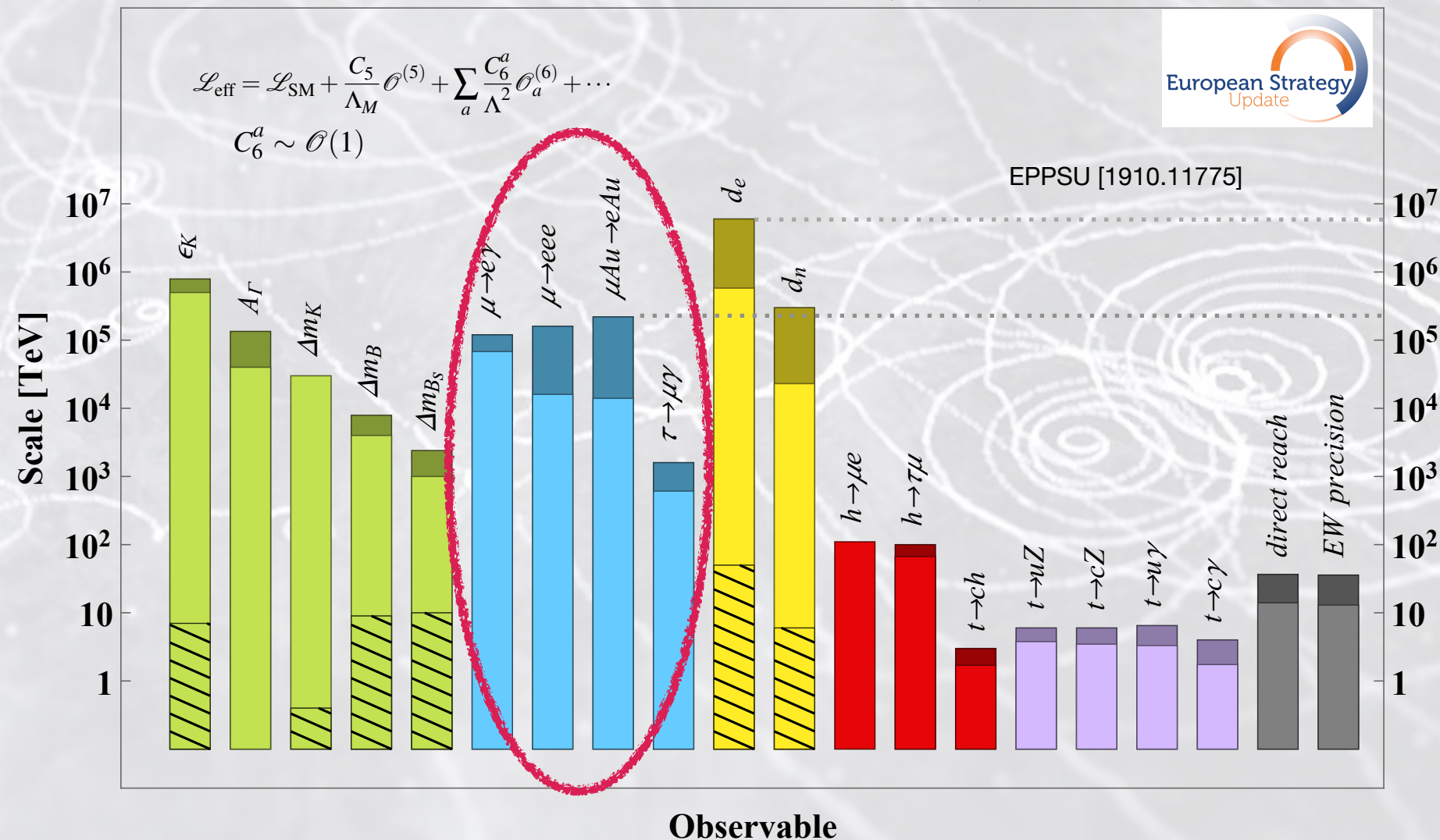


The probing power of flavour violation

SM interpreted as a **low-energy limit** of a (complete, yet unknown) **NP model**

⇒ Study various classes of well-motivated models

⇒ Model-independent, **effective approach (EFT)**



Probe scales **much higher** than direct collider reach!

⇒ possibly **indirect NP signals** long before (direct) discovery LHC...

Low-scale type I seesaw

Extend SM with 3 “heavy” RH **Majorana neutrinos**: $\text{MeV} \lesssim m_{N_i} \lesssim 1 - 100 \text{ TeV}$

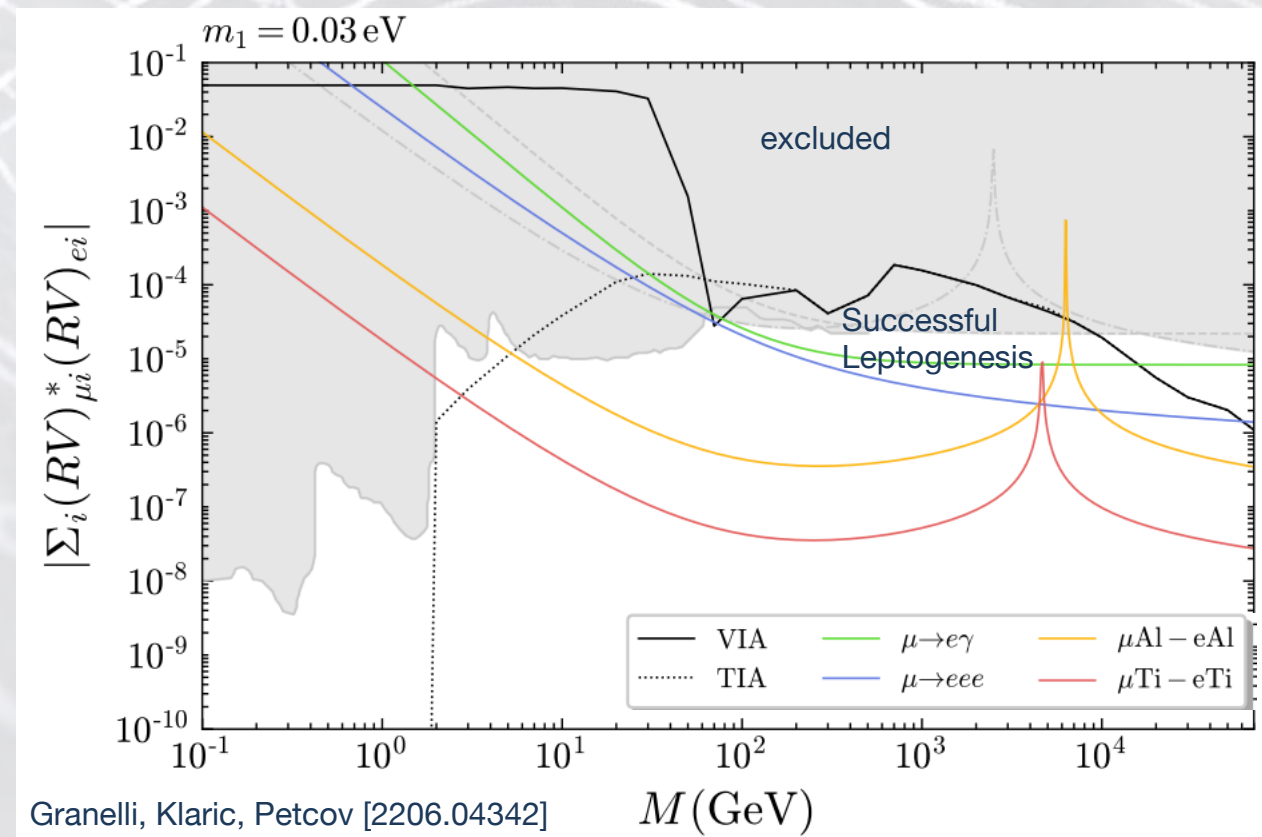
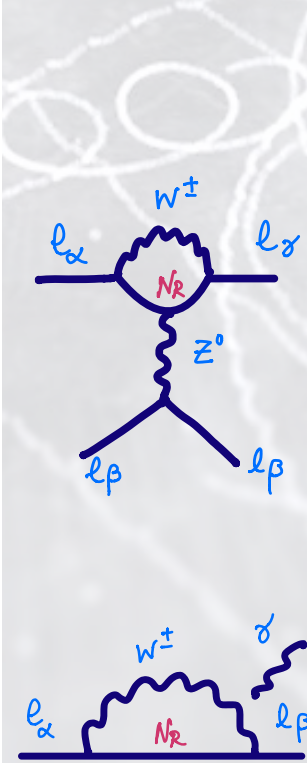
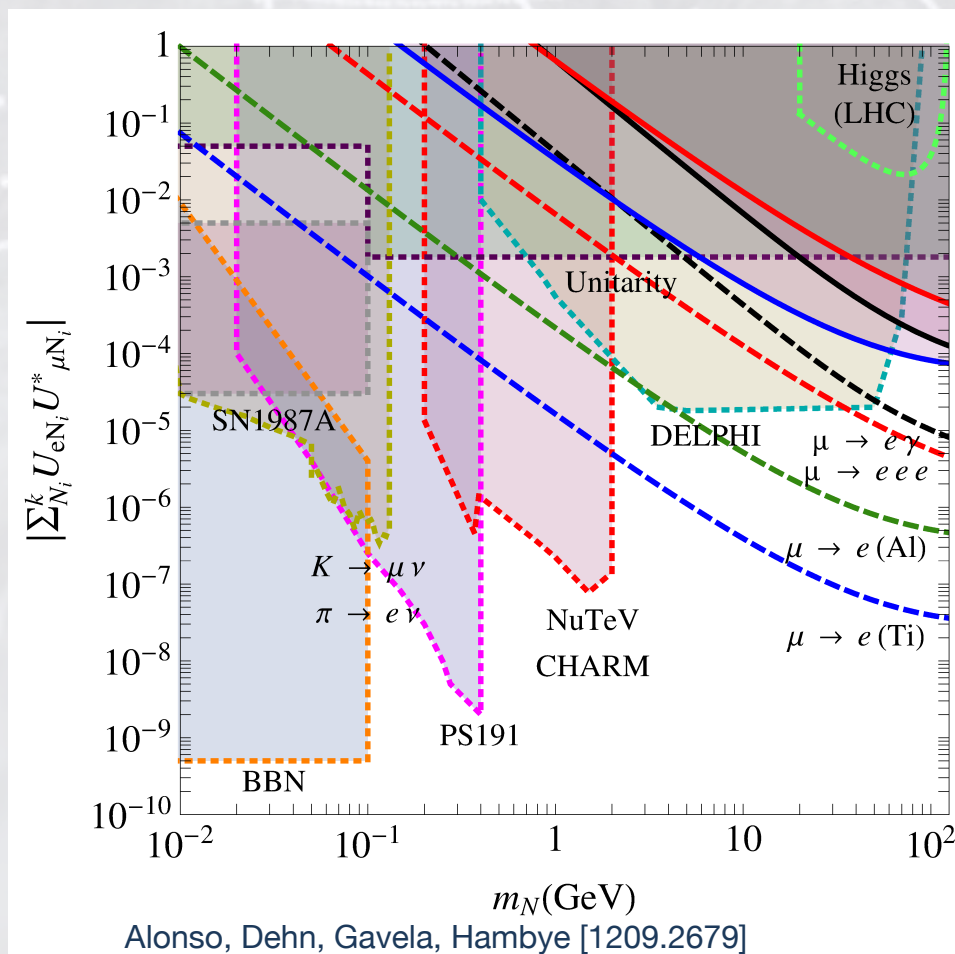
Spectrum & mixings:

$$m_\nu \simeq -v^2 Y_\nu^T M_N^{-1} Y_\nu, \quad \mathcal{U}^T \mathcal{M}_\nu^{6 \times 6} \mathcal{U} = \text{diag}(m_i)$$

$$\mathcal{U} = \begin{pmatrix} U_{\nu\nu} & U_{\nu N} \\ U_{N\nu} & U_{NN} \end{pmatrix}, \quad U_{\nu\nu} \simeq (1 - \eta) U_{\text{PMNS}}$$

Heavy states do not decouple \Rightarrow neutral and charged leptonic currents **modified**

Rich phenomenology at high intensities and at colliders



Scotogenic models – connection to dark matter

► **Scotogenic models**: a link between **neutrino mass** generation and **dark matter**!

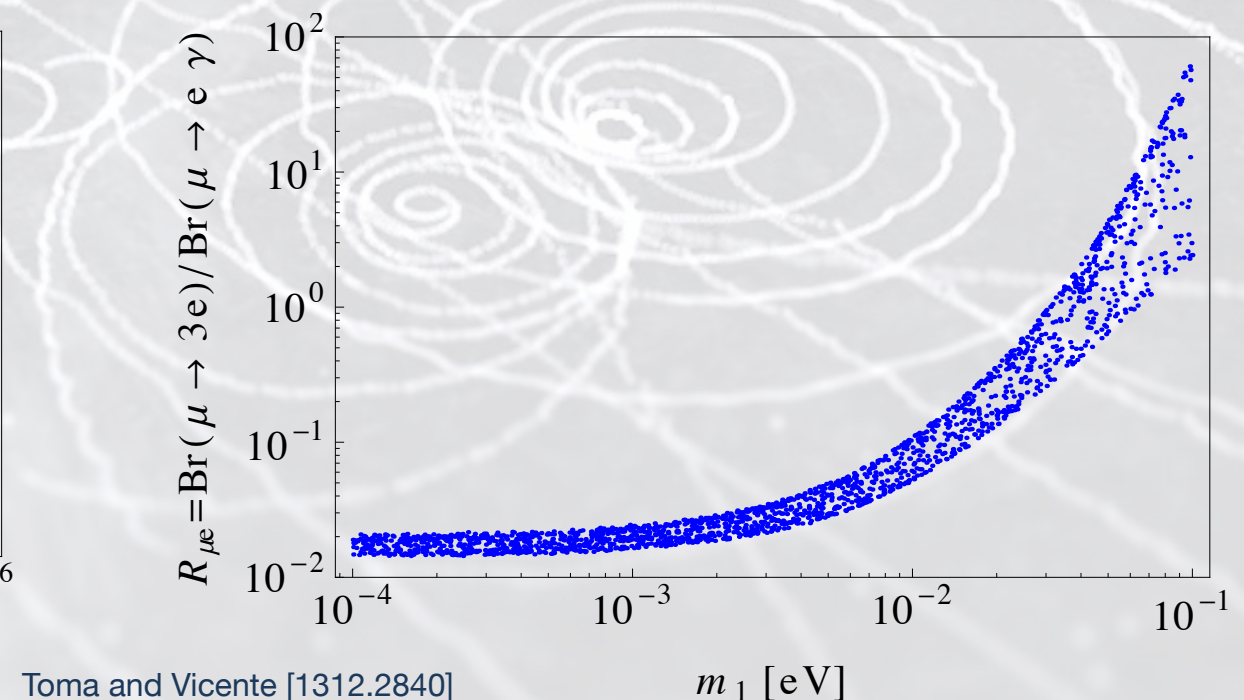
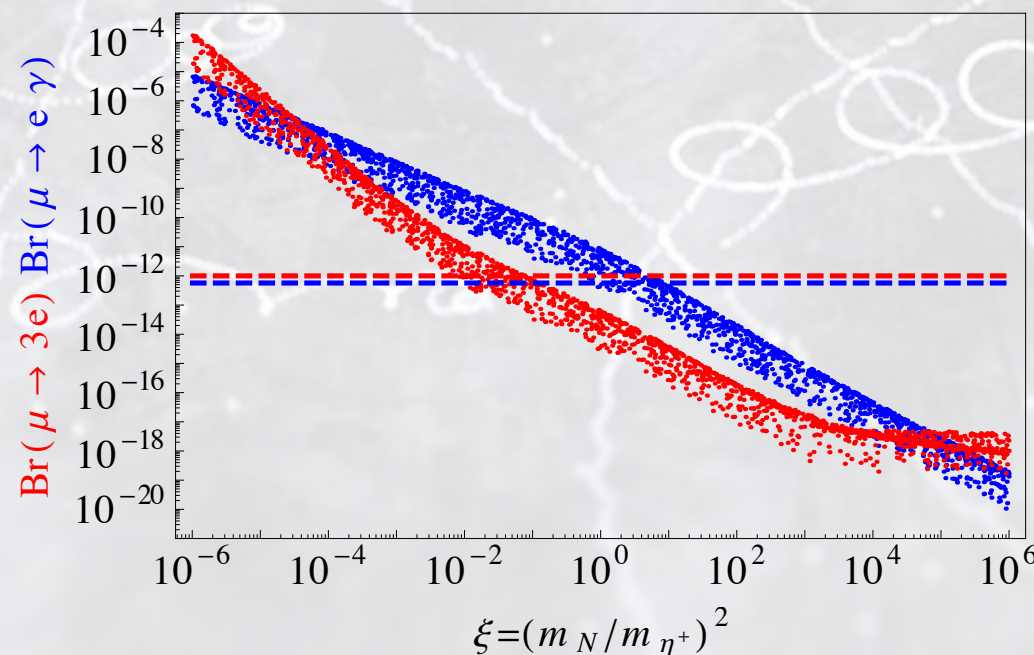
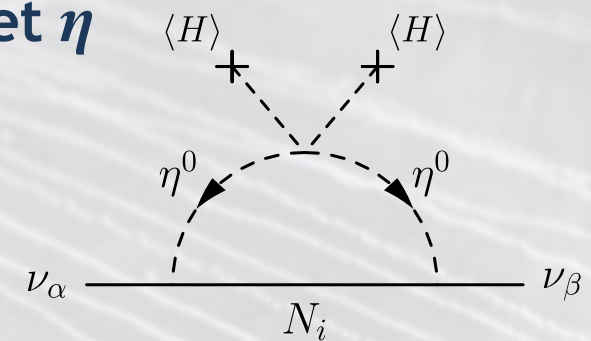
minimal realisations: extend SM by (inert) scalar doublet η
and RH neutrinos N_R

Additional Z_2 symmetry: **neutrino masses @ 1-loop**

dark matter candidate (η or N_R)

[Review on phenomenology of generalised scotogenic models: Hagedorn et al, 1804.04117]

► **cLFV observables**: hints on the **nature of the DM candidate** and absolute **ν mass scale**



Toma and Vicente [1312.2840]

Current (muon) **cLFV bounds** favour $m_N \geq m_\eta$; $\eta \rightsquigarrow$ **DM candidate**!

Determination of $R_{\mu e} = \text{BR}(\mu \rightarrow 3e) / \text{BR}(\mu \rightarrow e\gamma) \Rightarrow$ hints on lightest neutrino mass m_{ν_1}

Leptoquarks – flavour anomalies and muon cLFV

- Minimal SM extension via **single vector LQ** (V_1^μ)

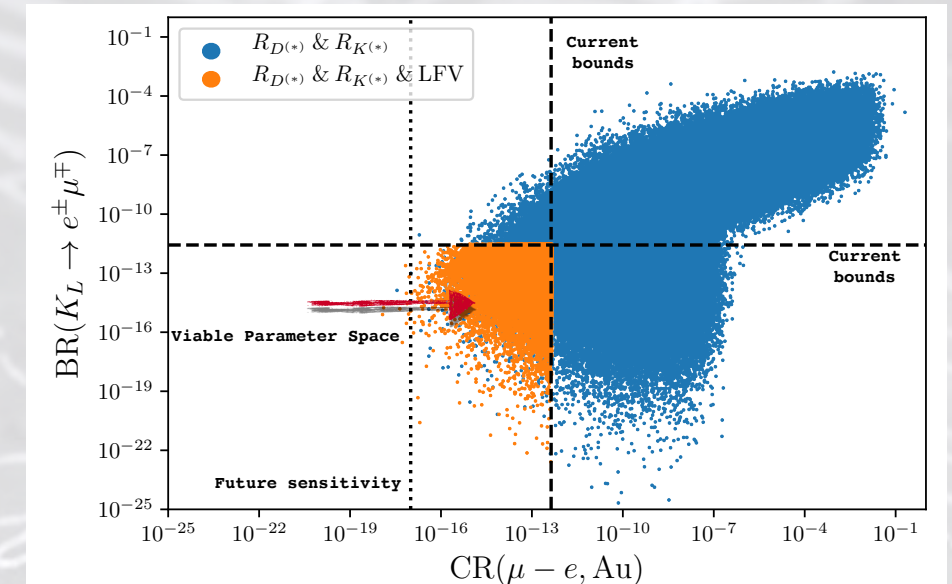
explain both $R_{K^{(*)}}$ and $R_{D^{(*)}}$ at tree-level

Strongly constraining observables:

$K_L \rightarrow e\mu$ and $\mu - e$ conversion in nuclei

⇒ **viable regimes** within sensitivity of Mu2e and COMET

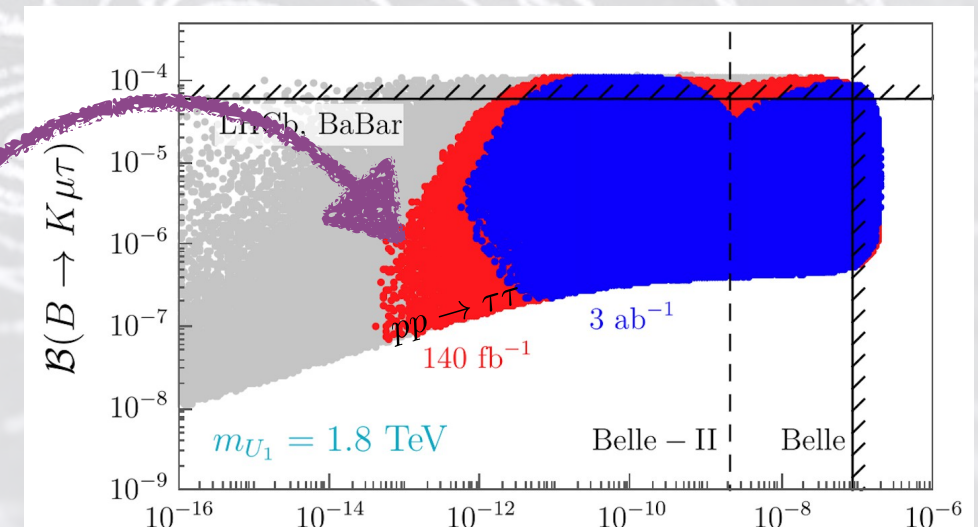
(“Natural” Pati-Salam scales pushed to $\gtrsim 100$ TeV)



Hati, JK, Orloff, Teixeira [1907.05511]

- Flavour + **high p_T** di-lepton tails:

predict **lower bounds** on $B \rightarrow K\mu\tau$ & $\tau \rightarrow \phi\mu$
(close to current limit)



Angelescu et al [2103.12504] $B(\tau \rightarrow \mu\phi)$

- Minimal SM extensions via 1 or 2 **scalar LQs**:

explain both Δa_μ & Δa_e , $\mu \rightarrow e\gamma$ crucial

to identify viable scenarios!!!

Doršner et al. [2006.11624]

Muon cLFV without cLFV @ muon colliders

Light(ish) Z' with only off-diagonal lepton couplings to accommodate Δa_μ

$\mu \rightarrow e\gamma$ and $\text{Mu} - \overline{\text{Mu}}$ conversion

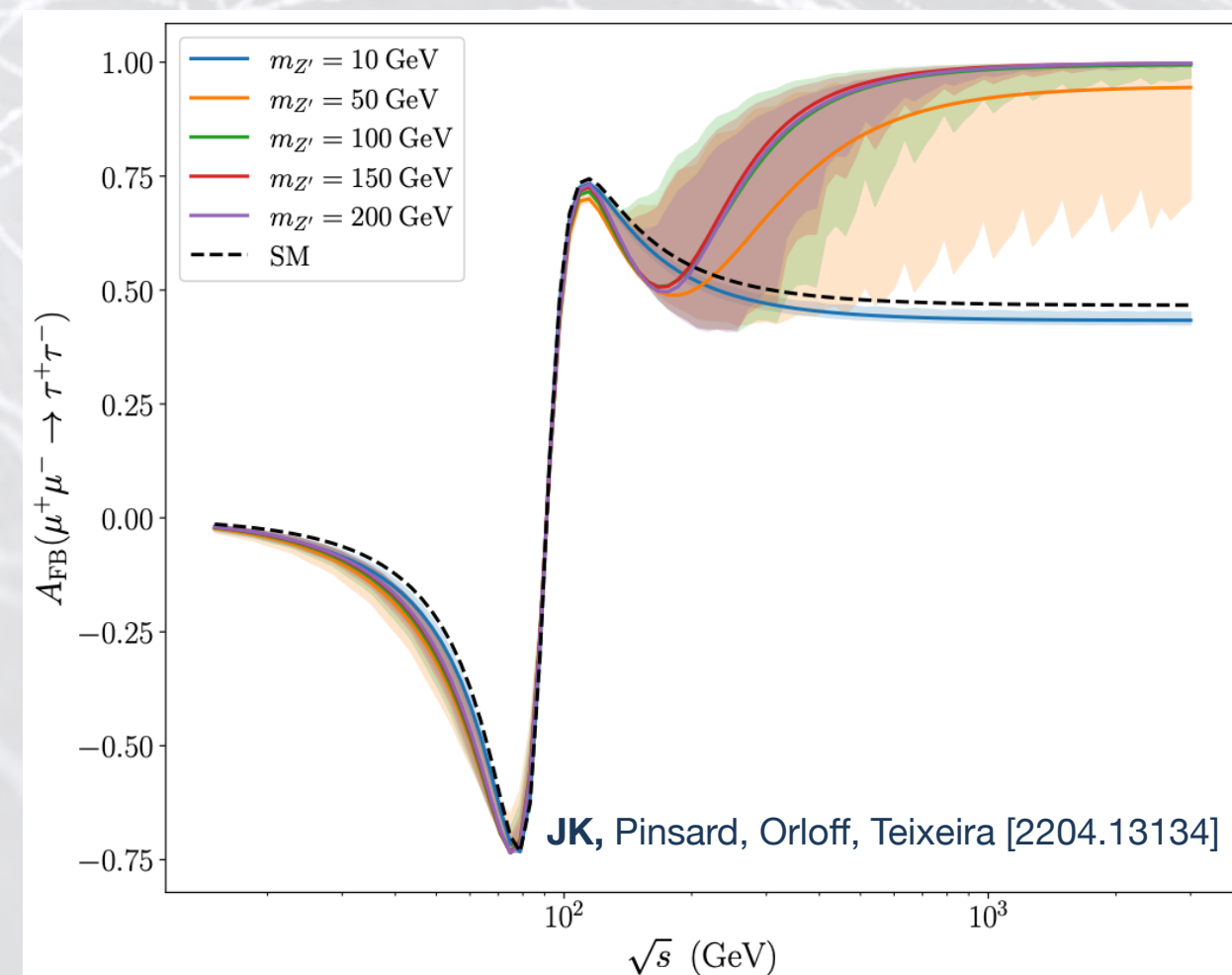
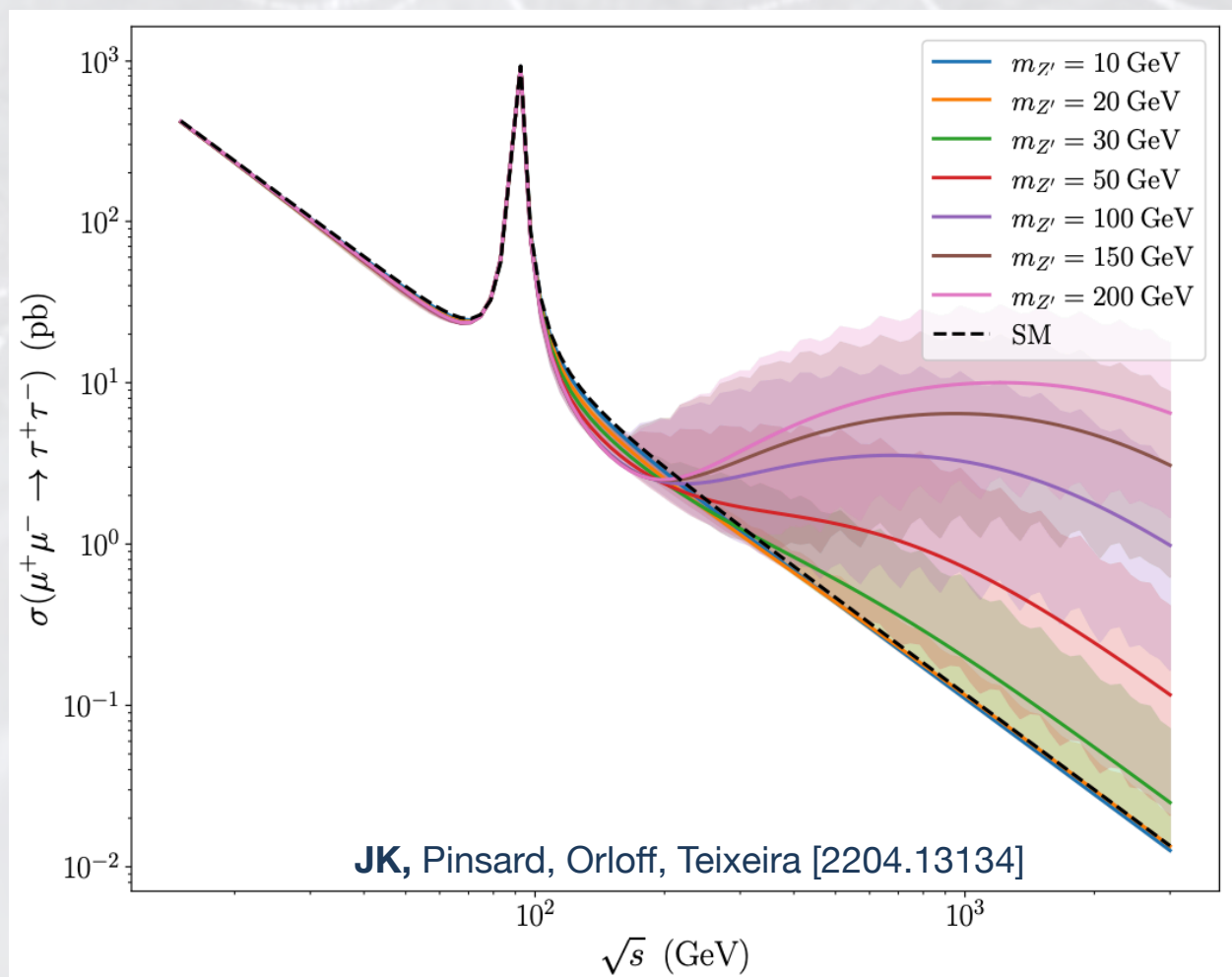
strongly constrain $e\mu$ & $e\tau$ couplings

$\mu\tau$ couplings can be sizeable $\mathcal{O}(10^{-3} - 10^{-2})$

\Rightarrow new t -channel in $\mu^+\mu^- \rightarrow \tau^+\tau^-$ scattering

Interference with huge impact on σ and A_{FB} !

“Indirect” muon cLFV



Concluding remarks

Muons rock!



Concluding remarks

Muons rock!

Currently intriguing hints of **New Physics** related to muon-flavoured observables

- ▶ $(g - 2)_\mu$ (and $(g - 2)_e$???) puzzles, rapid EXP and TH progress
- ▶ **B-meson decay anomalies** (& $(g - 2)_{\mu,e}$) might signify the breakdown of **lepton universality!**
- ▶ **LFUV** necessarily implies **cLFV!** \Rightarrow if confirmed, we should expect signals



Concluding remarks

Muons rock!

Currently intriguing hints of **New Physics** related to muon-flavoured observables

- ▶ $(g - 2)_\mu$ (and $(g - 2)_e$???) puzzles, rapid EXP and TH progress
- ▶ **B-meson decay anomalies** (& $(g - 2)_{\mu,e}$) might signify the breakdown of **lepton universality!**
- ▶ **LFUV** necessarily implies **cLFV!** \Rightarrow if confirmed, we can be cautiously optimistic

Muon (cLFV) observables crucial to probe countless models,
many of them related to mechanisms of m_ν **generation...**

But: need to consider correlations and effects of **CPV**
to disentangle sources of **cLFV**

Very exciting **future** ahead, leave no **flavoured** stone unturned :)

