
ν_e Cross Sections and ν STORM

M. Day - K. McFarland: Phys.Rev. D86 (2012) 053003

M.Day: <https://www.jlab.org/indico/contributionDisplay.py?contribId=231&confId=0>

S. Zeller: <https://indico.fnal.gov/conferenceDisplay.py?confId=5824>

NuInt12 – Rio de Janeiro, Brazil

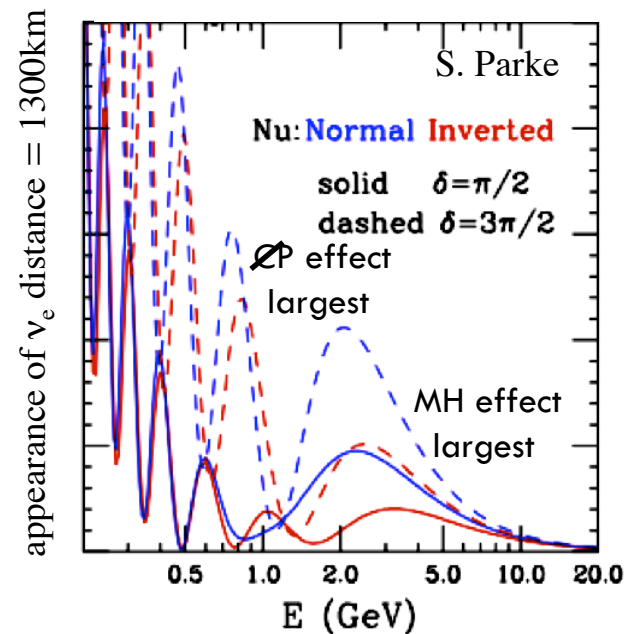
October 2012

Jorge G. Morfin

Fermilab

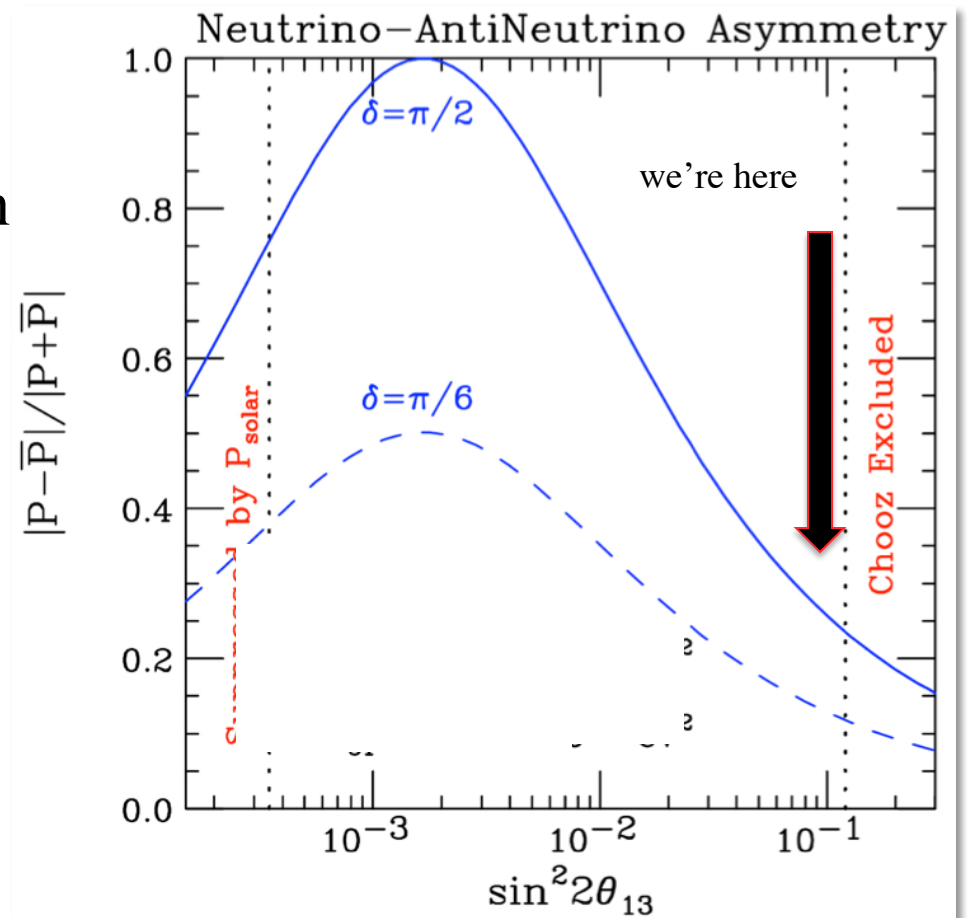
Why are ν_e Cross Sections Important?

- ◆ ν_e A – scattering results are interesting on their own.
- ◆ Recent determination of large θ_{13} has opened up possibilities of
 - ▼ Determining ν mass ordering.
 - ▼ Searching for CP-violation in the ν sector.
- ◆ To be sensitive to these effects, current/near-future long-baseline experiments will be looking for ν_μ to ν_e and $\bar{\nu}_\mu$ to $\bar{\nu}_e$ oscillations over a range of energies.
- ◆ These will no longer be only “counting” experiments but rather will depend on observing distortions in the far detectors neutrino energy spectrum in **both neutrino and anti-neutrino samples**.



Why are ν_e and $\bar{\nu}_e$ Cross Sections Important?

- ◆ Large θ_{13} means we could have reasonable statistics.
- ◆ However, as the now-well-known plot at right suggests, the asymmetry between ν and $\bar{\nu}$ will be small and the goal of constraining the range of δ will demand minimal systematic errors.
- ◆ One of these systematics will be our knowledge of ν_e and $\bar{\nu}_e$ cross sections in the relevant energy range.



(not including matter effects & backgrounds)
(S. Parke)
 3

What do we observe in our detectors?

-
- ◆ The events we observe in our detectors are convolutions of:

$$Y(E) \propto \phi(E) \otimes \sigma(E) \otimes \text{Nuc}(E' \geq E)$$

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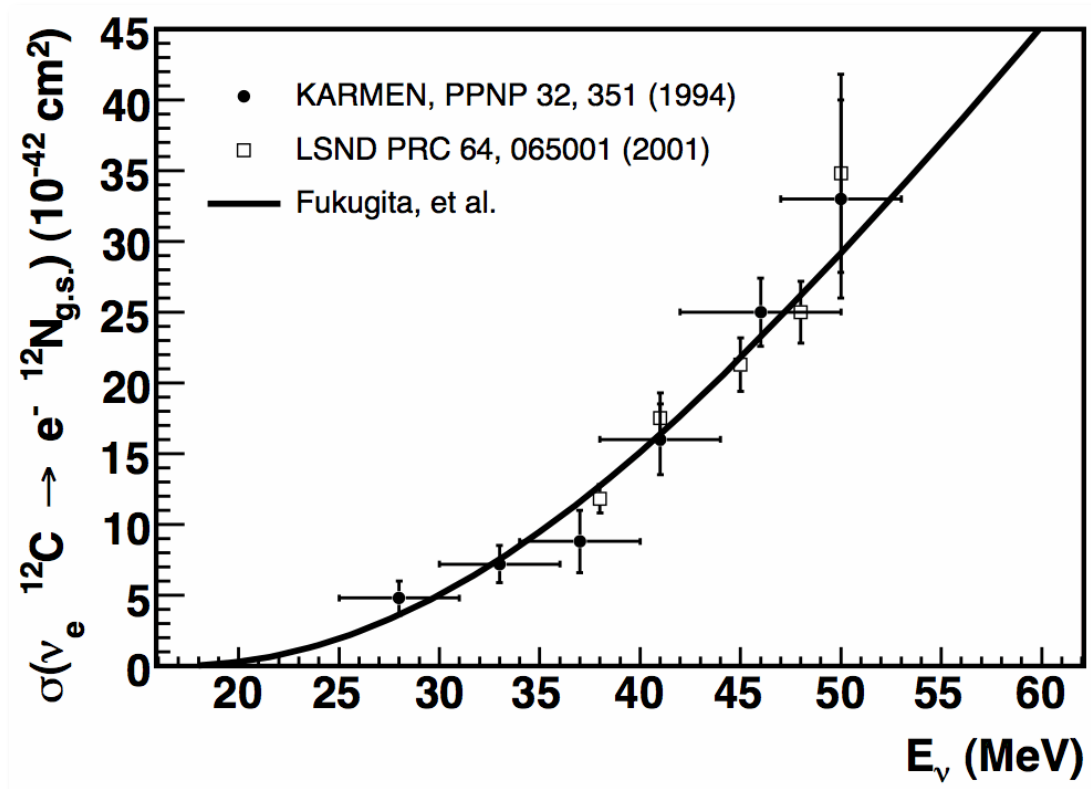
$$Y(E) \propto \phi(E) \otimes \sigma(E) \otimes \text{Nuc}(E' \geq E) \leftarrow \text{effective } \sigma^A(E)$$

- ◆ When the last two terms are for ν_μ then we have experiments currently measuring these cross sections on relevant nuclear targets but with limited knowledge of the incoming flux for absolute cross sections.
- ◆ When the last two terms are for ν_e then we have **no** higher energy experimental measurements of these cross sections. We infer them from $\sigma_{\nu_\mu}(E)$ results. The validity of this inference directly impacts the uncertainty of the measurements.
- ◆ What do we know about $\sigma_{\nu_e}(E)$? **Mostly very low energy results.**
 - ▼ Reactor neutrinos studying Inverse Beta Decay
 - ▼ Solar neutrino off deuterium (SNO)
 - ▼ Stopping π/μ decay neutrinos off higher A targets
 - ▼ See Formaggio and Zeller **Rev. Mod. Phys.** **84**, 1307–1341 (2012).

Example of Existing Data: Carbon



- ◆ One of few measurements of spectral shape of σ reflects the upper limit of most existing measurements, $E \leq 50$ MeV.

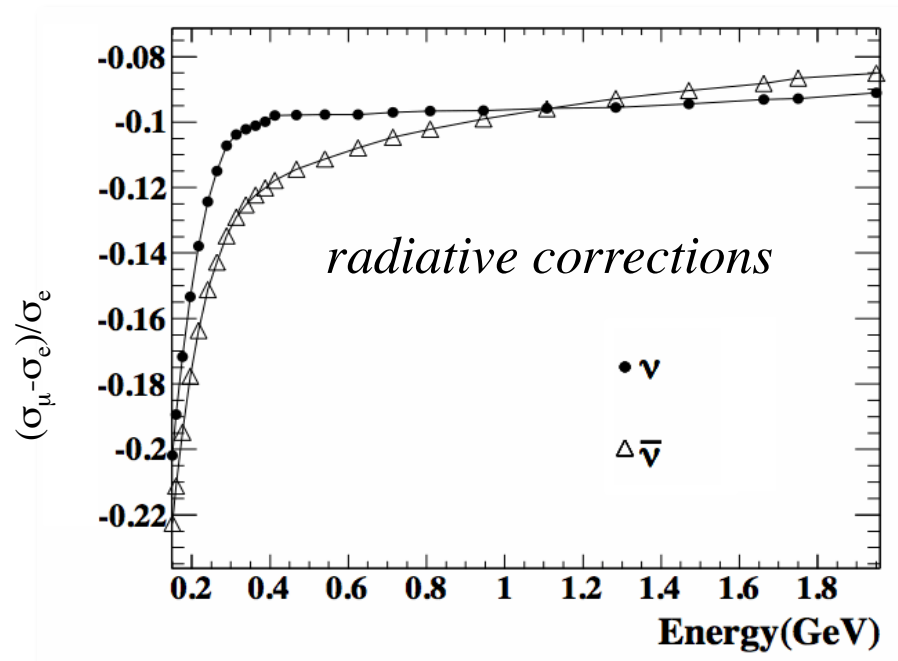
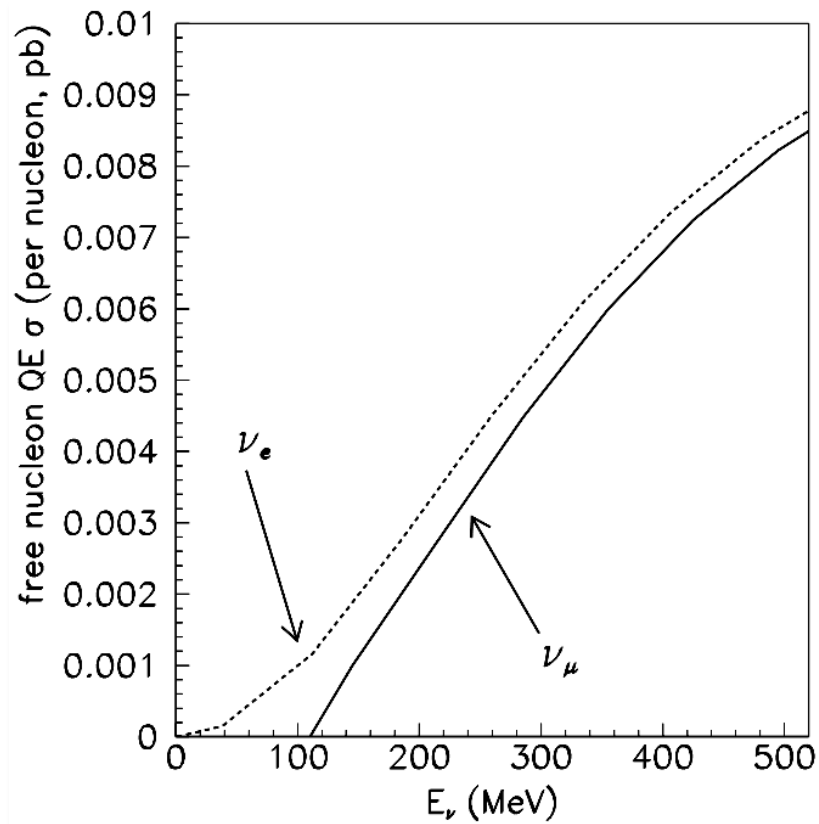


(Formaggio & Zeller, Rev. Mod. Phys. 2012)

What are the Differences $\sigma_{\nu\mu}(E)$ and $\sigma_{\nu e}(E)$? Quasi-elastic Scattering

Day-McFarland study: Phys.Rev. D86 (2012) 053003

- ◆ QE scattering dominates at low energies (2^{nd} oscillation maxima)
- ◆ Sources of possible differences and uncertainties - obvious:
 - ▼ Kinematic limits from μ / e mass difference.
 - ▼ Radiative Corrections. This may be an overestimate. Need full calculation.

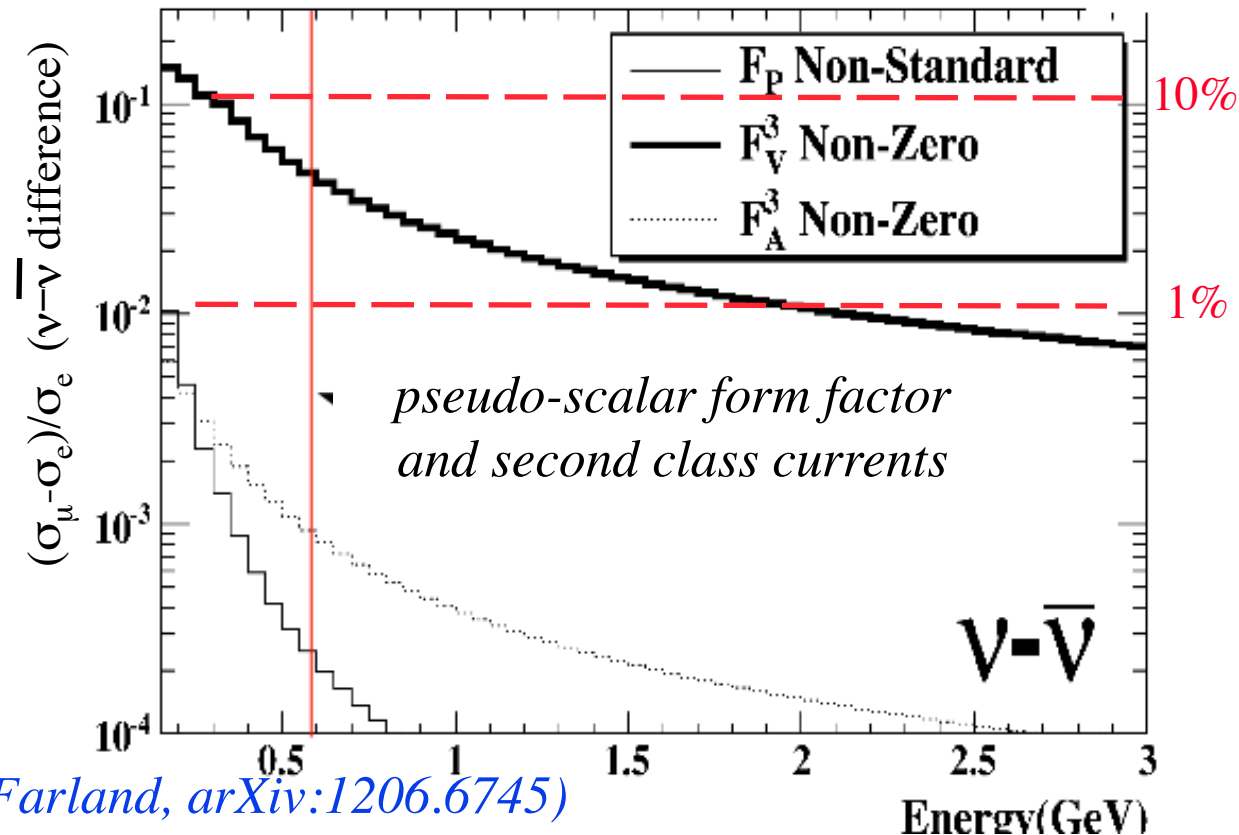


(M. Day, K. McFarland, arXiv:1206.6745)

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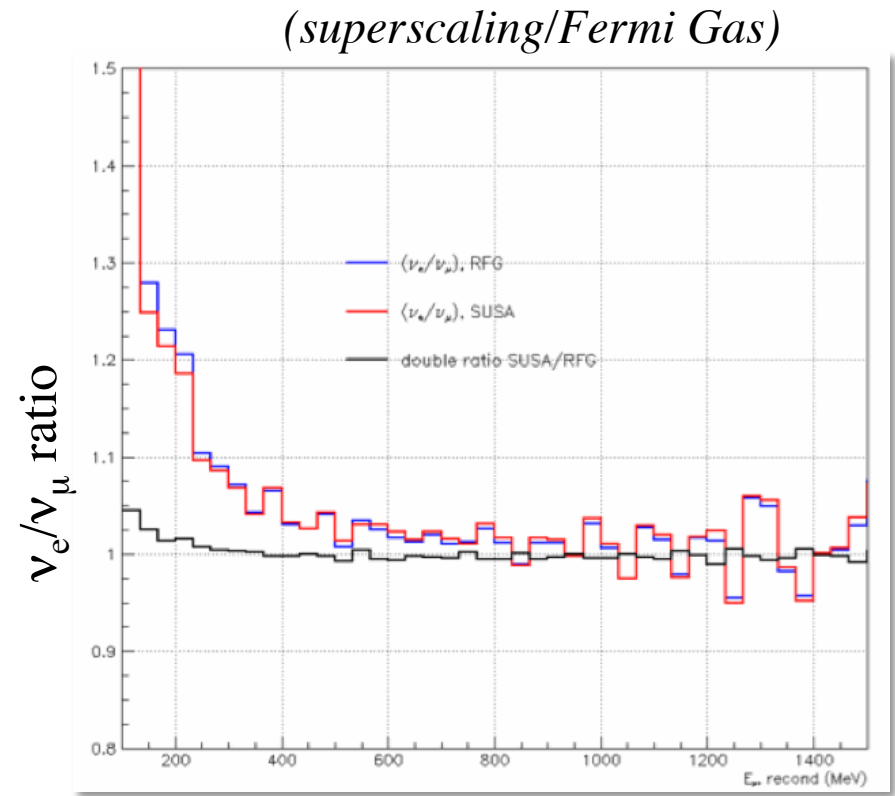
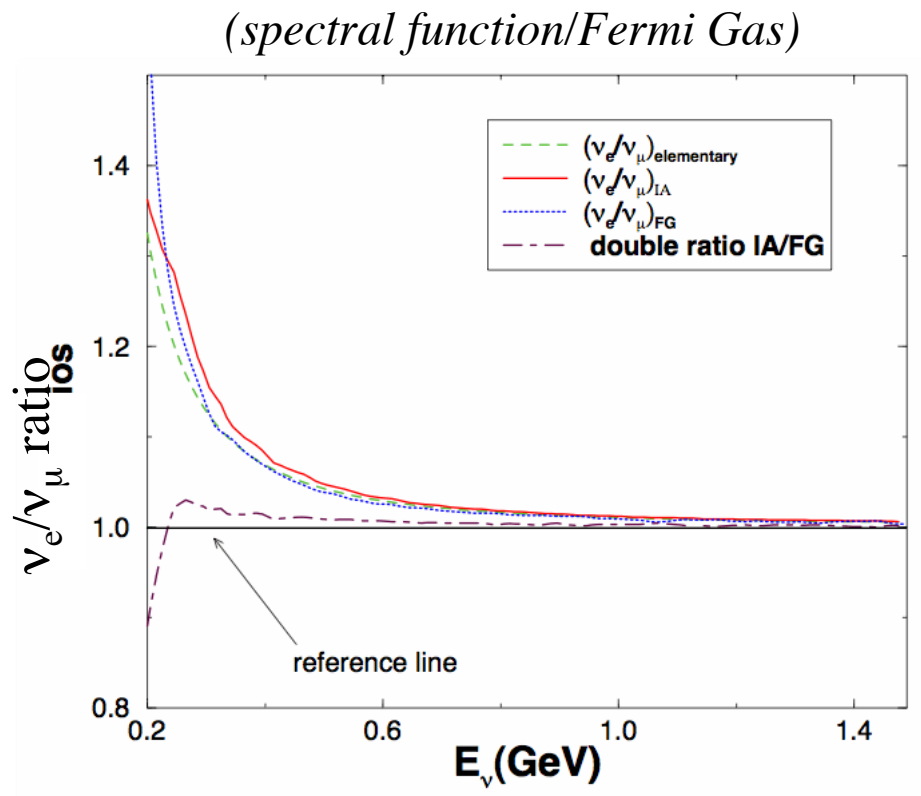
- ◆ Sources of possible differences: form factor uncertainties entering through lepton mass alterations - much more subtle:
 - ▼ Form factor contributions – both Axial and Pseudoscalar
 - ▼ Second class current contributions to vector and axial-vector form factors
- ◆ Possible contribution to CP uncertainties: effect on the FF could be different for ν and $\bar{\nu}$



(M. Day, K. McFarland, arXiv:1206.6745)

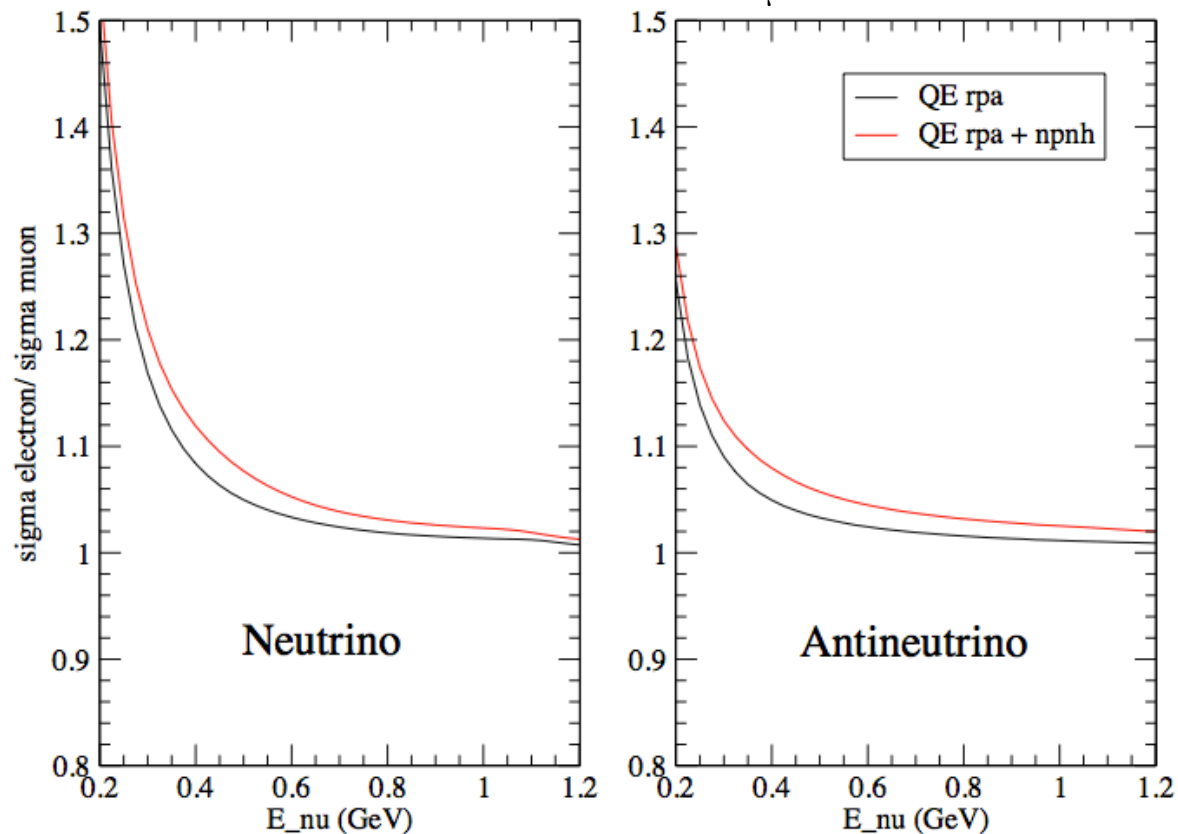
What are the Differences? Mainly QE Scattering Due to Nuclear Effects

- ◆ For standard models, $\leq 5\%$ differences on ν_e/ν_μ ratio $E < 200$ MeV



What are the Differences? Mainly QE Scattering Meson-exchange Current Contributions – Marco Martini via S. Zeller

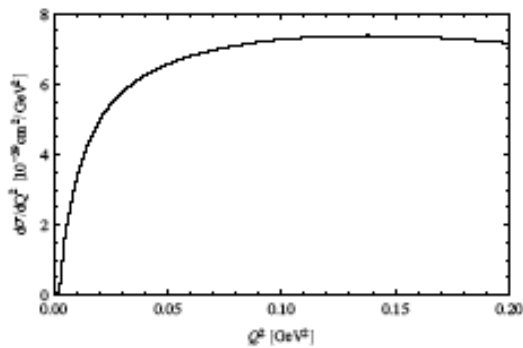
- ◆ Hadronic part (nuclear response functions) is the same for ν_e or ν_μ cross section.
- ◆ However, the lepton tensor changes \rightarrow the relative weight of the nuclear responses in the several channels may change.
- ◆ The double ratio suggests the effect on the ν_e/ν_μ cross section ratio is $\leq 5\%$ (S. Zeller)



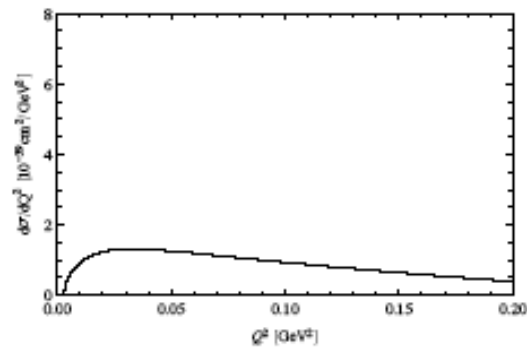
What are the Differences? Δ Production

Paschos – Schalla: arXiv:1209.4219

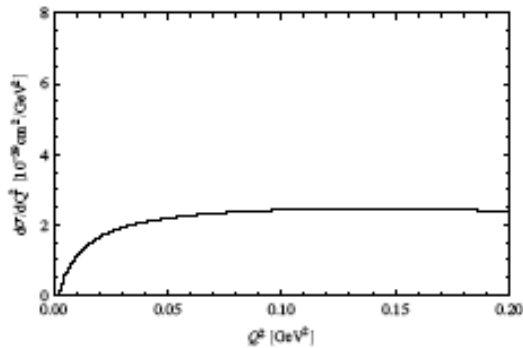
- ◆ Manny and his student have investigated ν_μ and $\bar{\nu}_\mu$ differences in Δ production in the low- Q ($Q^2 \approx m_\pi^2$) region where PCAC dominates the axial contribution.
- ◆ At $E = 1-2$ GeV, V part and V/A interference same size \rightarrow cancel for $\bar{\nu}$
- ◆ Use the Adler-Nussinov-Paschos model for nuclear corrections.



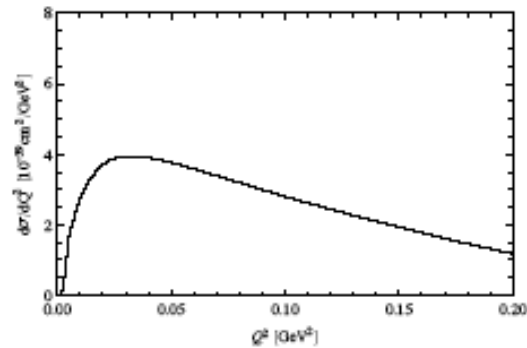
(a) $\nu_\mu p \rightarrow \mu^- X^{++}$



(b) $\bar{\nu}_\mu p \rightarrow \mu^+ X^0$



(c) $\nu_\mu n \rightarrow \mu^- X^+$

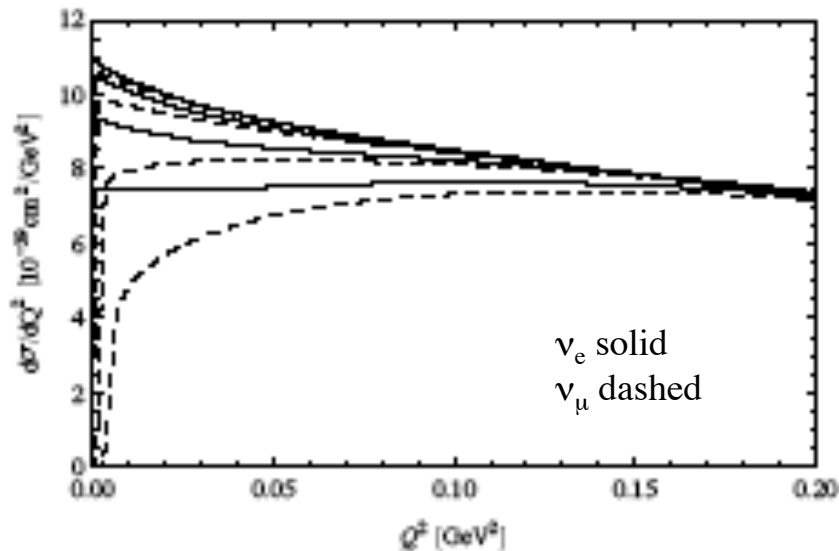


(d) $\bar{\nu}_\mu n \rightarrow \mu^+ X^-$

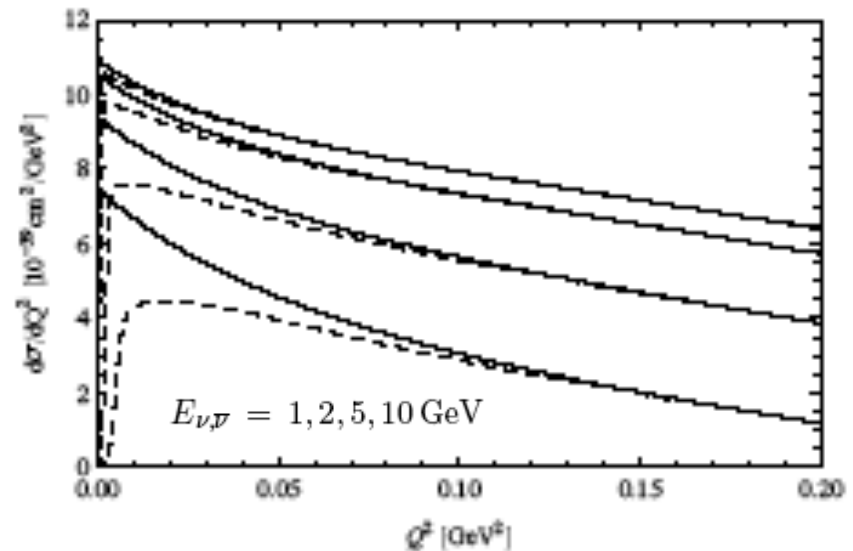
What are the Differences? Δ Production

Paschos – Schalla: arXiv:1209.4219

- ◆ Paschos-Schalla predicts the following differences in cross sections where only the lepton mass term contributions are shown and any differences in form factors are not yet included.



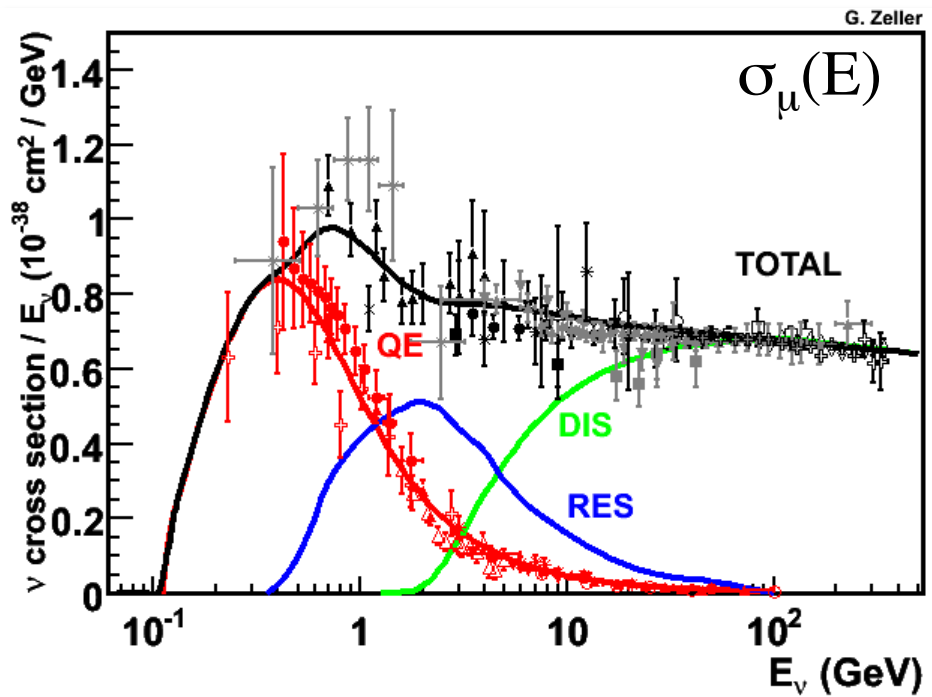
(a) $\nu_{\ell} p \rightarrow \ell^{-} \Delta^{++}$



(b) $\bar{\nu}_{\ell} n \rightarrow \ell^{+} \Delta^{-}$

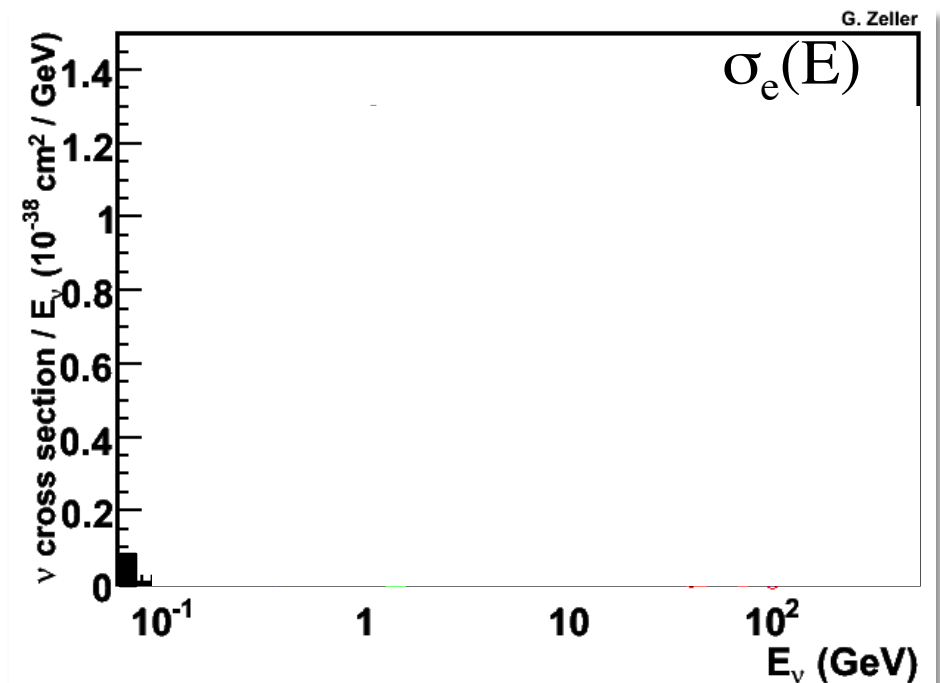
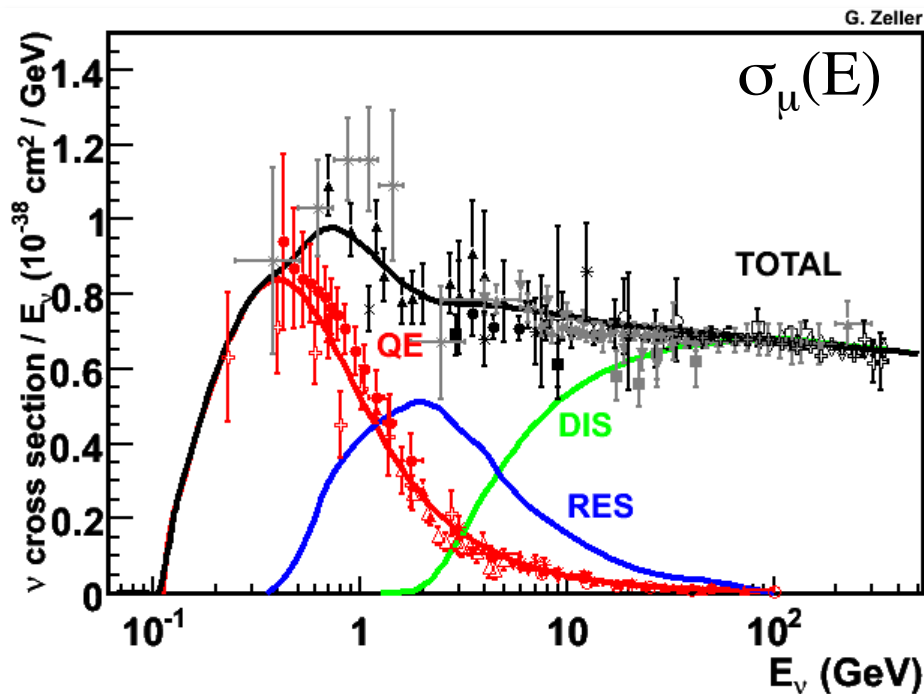
Can we Actually MEASURE these Differences in the 0.5 – 6 GeV region

- ◆ Need to measure the $\sigma_e(E)$ of multiple channels to predict spectrum at the far detector.
 - ▼ Want an intense source of ν_e events.
 - ▼ Would like to know the flux of ν_e (and ν_μ , by the way) to order 1%.



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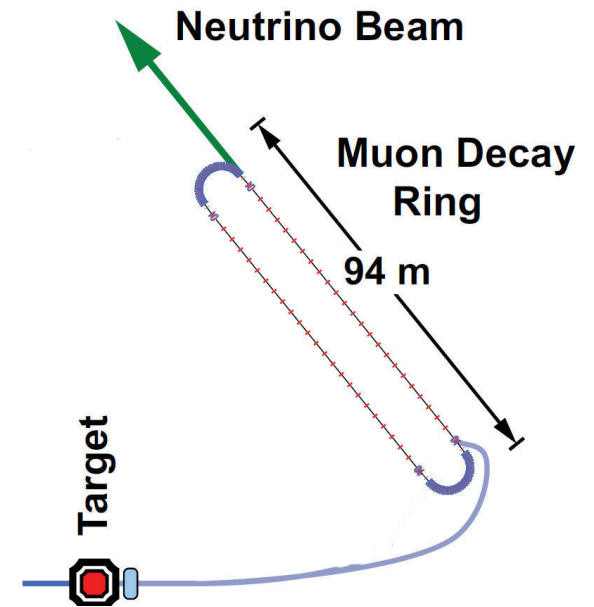
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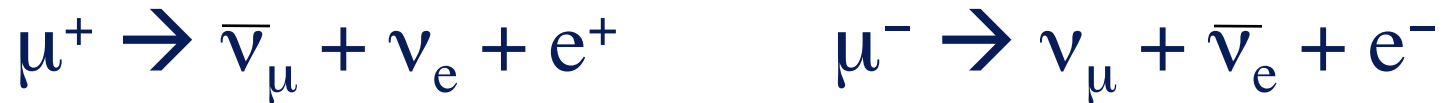
Enter - ν STORM

Neutrinos from Stored Muons – Alan Bross Presentation on Friday

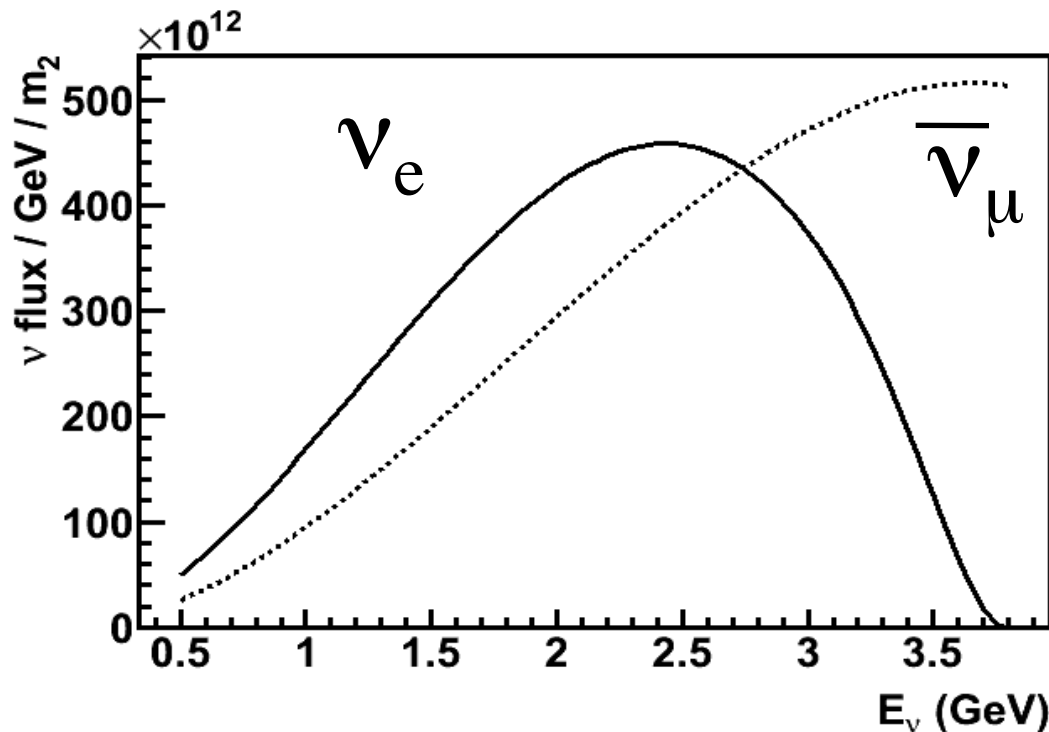
- ◆ High-Precision ν interaction physics program.
 - ▼ ν_e and $\bar{\nu}_e$ cross-section measurements.
- ◆ Address the large Δm^2 oscillation regime, make a major contribution to the study of sterile neutrinos.
 - ▼ Either allow for precision study (in many channels), if they exist in this regime.
 - ▼ Or greatly expand the dis-allowed region.
- ◆ Provide a technology test demonstration (μ decay ring) and μ beam diagnostics test bed.
- ◆ Provide a precisely understood ν beam for detector studies.
- ◆ **Change the conception of the neutrino factory.**



The ν STORM Neutrino Beam



- ◆ The ν STORM beam will provide a very well-known ($\delta \phi(E) \approx 1\%$) beam of ν and $\bar{\nu}$.
- ◆ A high-intensity source of ν_e events for experiments.



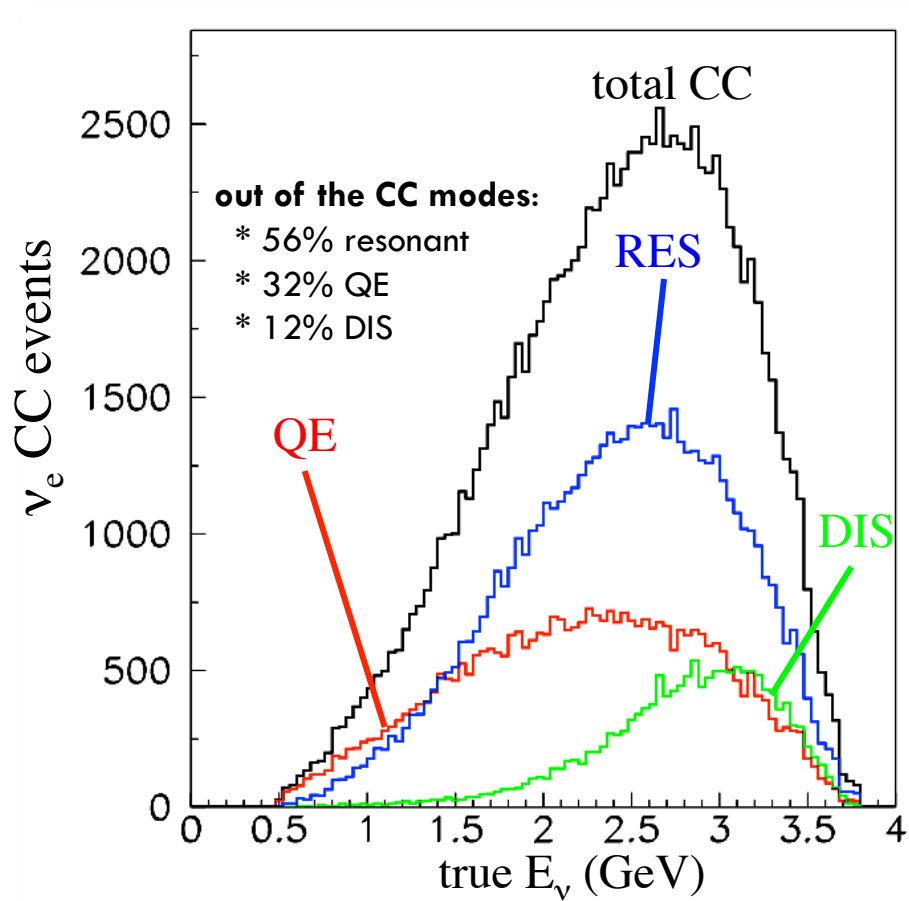
3.8 GeV μ^+ stored, 150m straight, flux at 100m
(thanks to Sam Zeller and Chris Tunnell!)

μ^+		μ^-	
Channel	N_{evts}	Channel	N_{evts}
$\bar{\nu}_\mu$ NC	844,793	$\bar{\nu}_e$ NC	709,576
ν_e NC	1,387,698	ν_μ NC	1,584,003
$\bar{\nu}_\mu$ CC	2,145,632	$\bar{\nu}_e$ CC	1,784,099
ν_e CC	3,960,421	ν_μ CC	4,626,480

event rates per 1E21 POT -
 100 tons at 50m

ν_e Event Fractions in ν STORM

- ◆ ν_e produced by 3.8 GeV μ^+ beam.

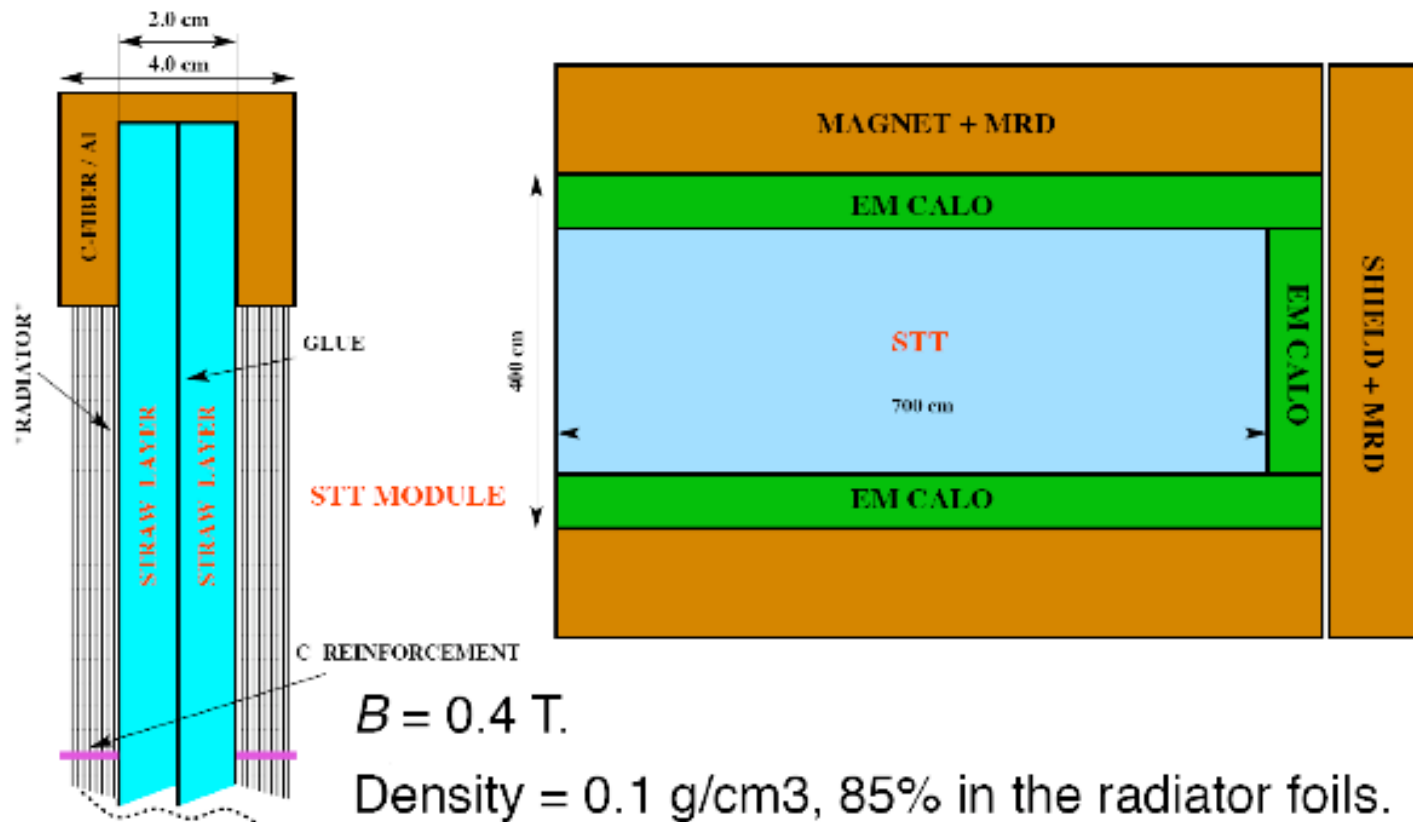


- ◆ For $\bar{\nu}_e$ sample, 52% resonant, 40% QE, 8% DIS)

ν STORM Near Detector

High Resolution Straw-tube Magnetized Detector

- ◆ HighRes – Mishra/Petti



Transition Radiation \Rightarrow Electron ID \Rightarrow γ (w. Kinematics)
dE/dx \Rightarrow Proton, π , K ID
Magnet/Muon Detector \Rightarrow μ

High Resolution Near Detector

- ◆ NOMAD-like resolution in HiRes detector allows to:
 - ▼ Measure absolute flux using ν - e elastic scattering –
 - ▼ Measure quasi-elastic scattering
 - ▼ NC vs CC events (NOMAD with 90% purity)
 - ▼ Coherent π^0
 - ▼ Comparison $\sin^2 \theta_W$ from DIS and $\nu e \rightarrow \nu e$
 - ▼ 77 different physics topics!

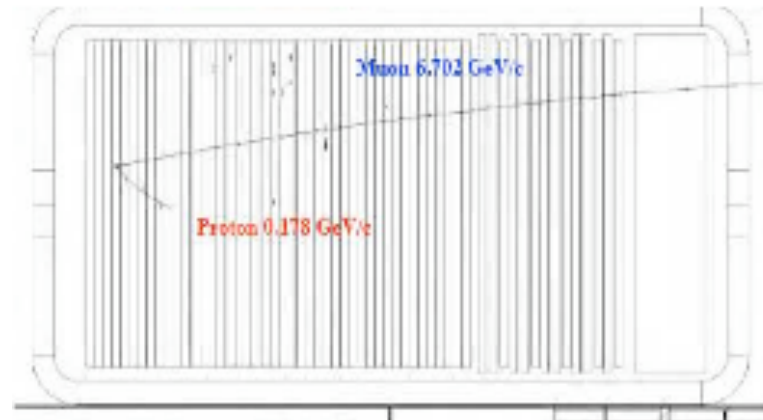
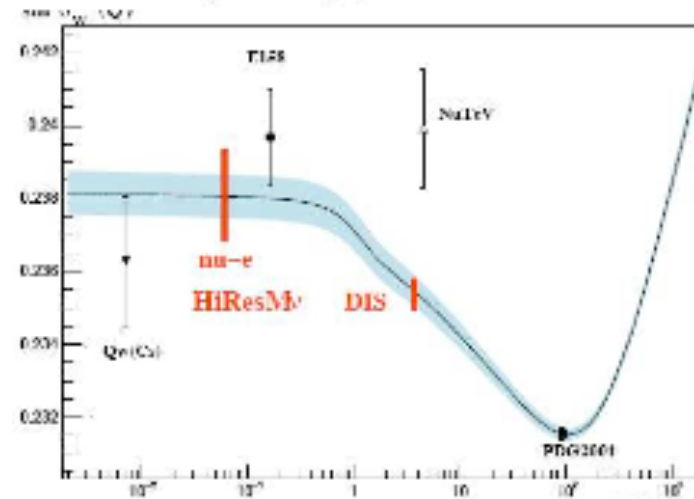


Figure 14: A ν_{μ} -QE candidate in NOMAD

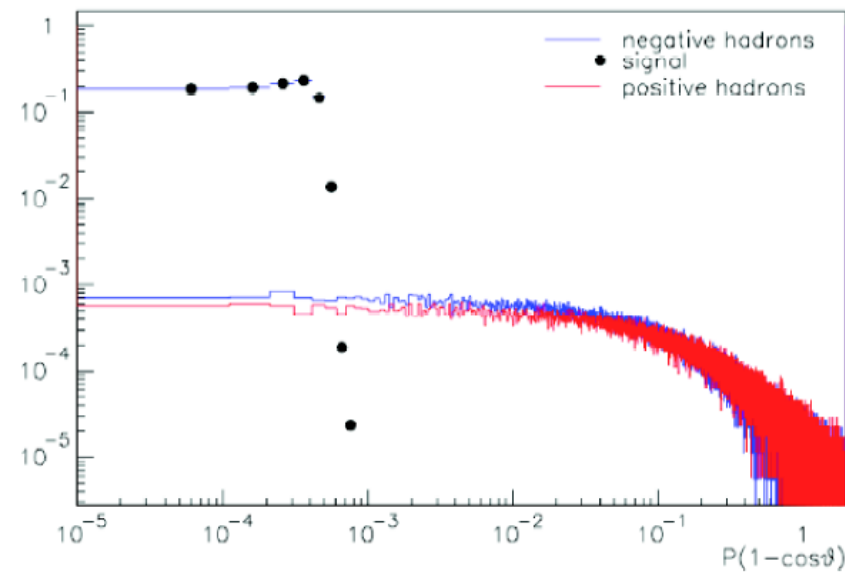
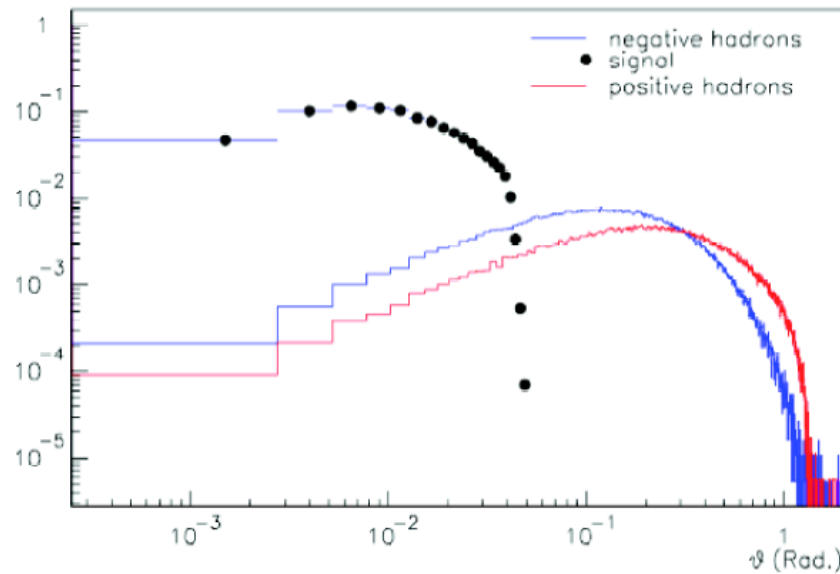


ν - e NC elastic scattering

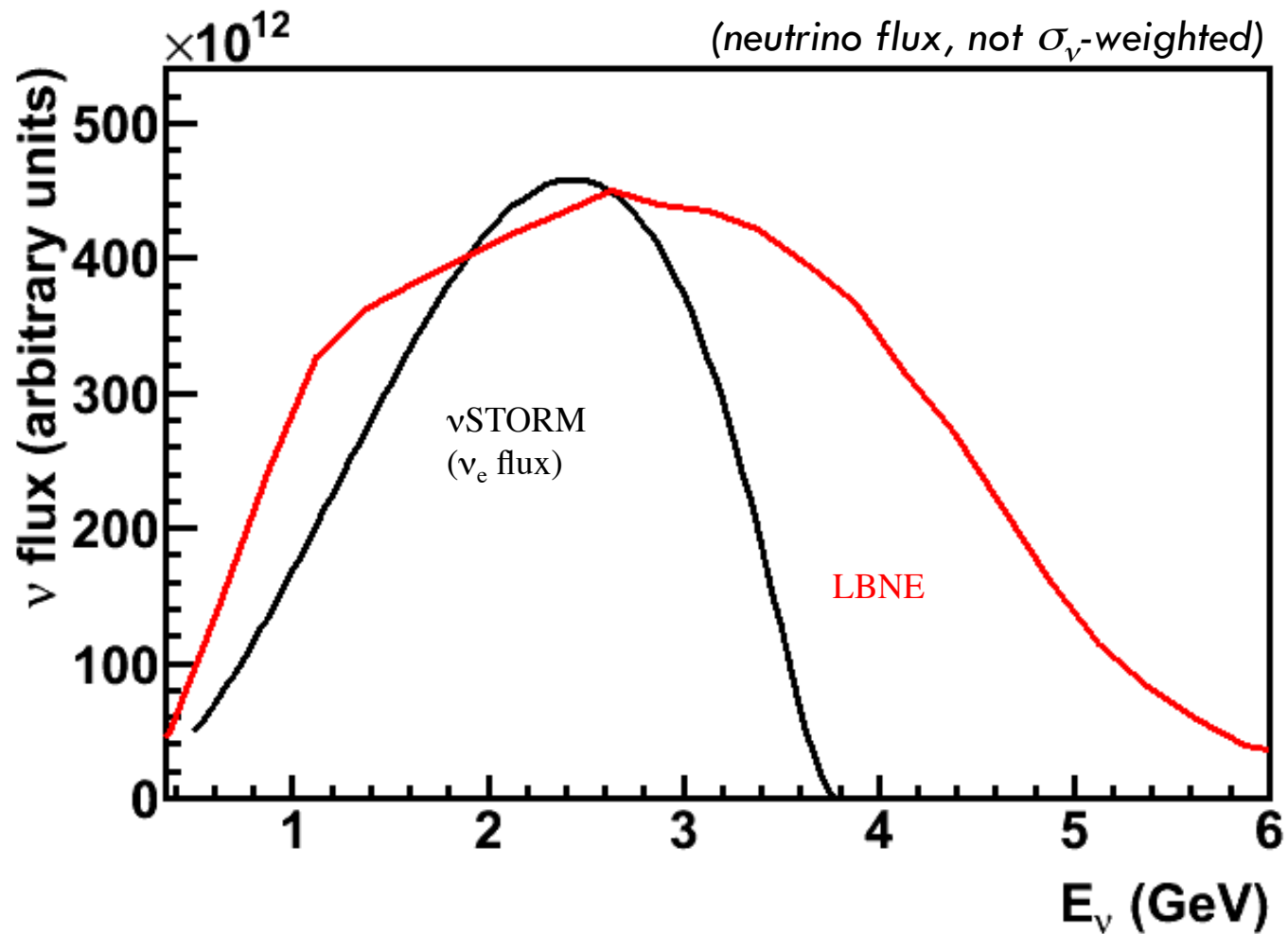
Mishra

$$\sigma(\nu_l e \rightarrow \nu_l e) = \frac{G_\mu^2 m_e E_\nu}{2\pi} \left[1 - 4 \sin^2 \theta_W + \frac{16}{3} \sin^4 \theta_W \right] \sim 10^{-42} (E_\nu / \text{GeV})^2 \text{ cm}^2$$

$$\sigma(\bar{\nu}_l e \rightarrow \bar{\nu}_l e) = \frac{G_\mu^2 m_e E_\nu}{2\pi} \left[\frac{1}{3} - \frac{4}{3} \sin^2 \theta_W + \frac{16}{3} \sin^4 \theta_W \right]$$



Practicality of ν STORM Neutrino Spectrum



Conclusions

- ◆ An important systematic error in measurement of CP-violations could be our knowledge of ν_e cross sections.
 - ▼ Simply assuming we can infer ν_e cross sections from ν_μ cross sections is unjustified.
 - ▼ Simply correcting cross section for the difference in lepton mass is not necessarily sufficient.
- ◆ There is then a need to actually measure ν_e cross sections to minimize the systematic error from this source.
- ◆ ν STORM, based on the decay of a circulating beam of muons, could provide an intense beam of well-know flux (order 1%) of ν_e (and $\bar{\nu}_\mu$) for ν_e and $\bar{\nu}_\mu$ cross section measurements in a single experiment.
- ◆ Stay-tuned for the presentation of Alan Bross on Friday afternoon for details of the ν STORM facility and agenda.

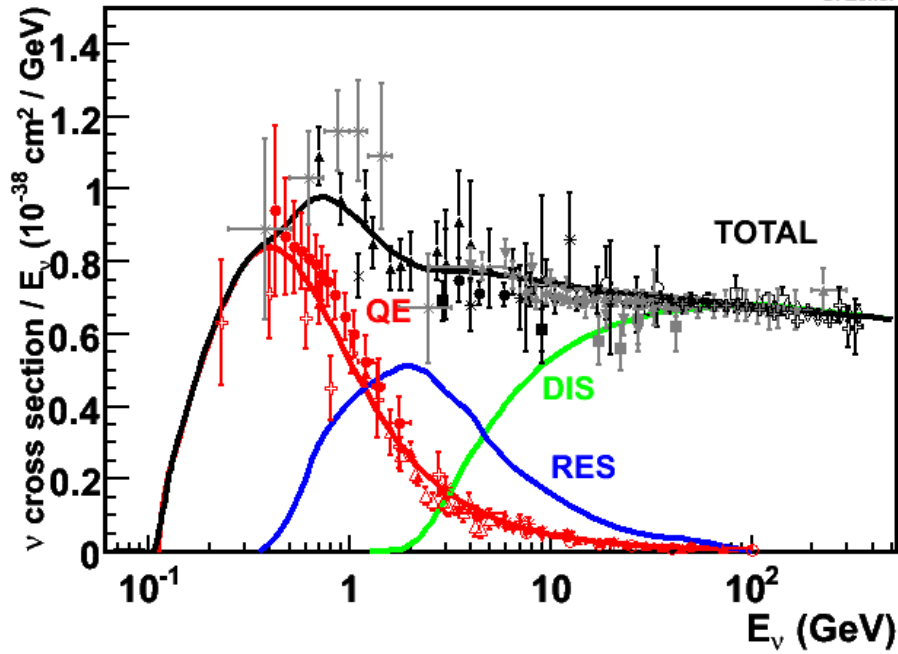
Extra Details

Current Knowledge

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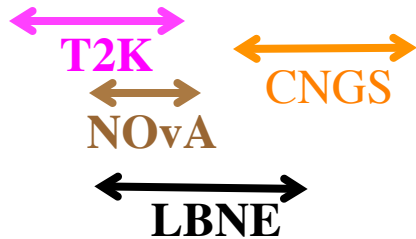
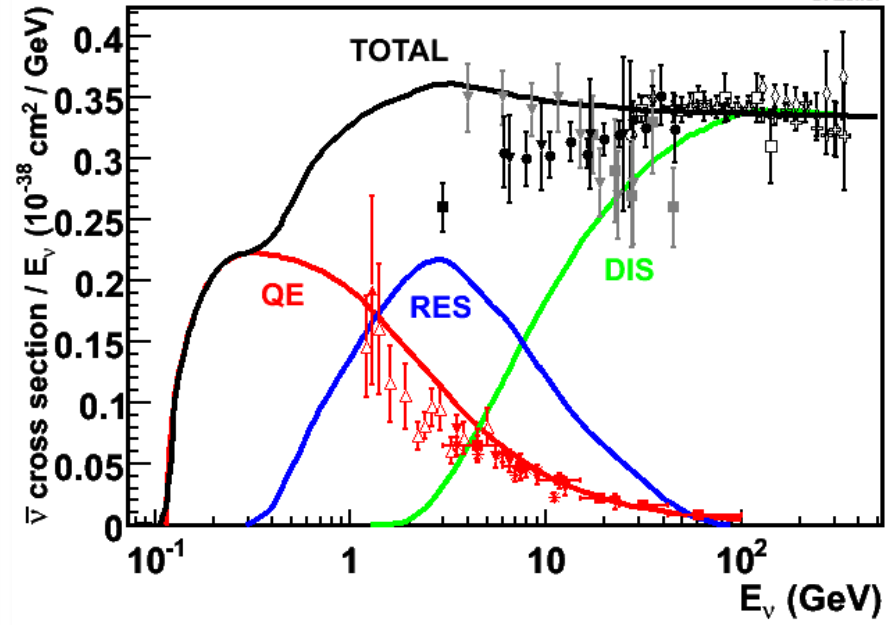
neutrino

G. Zeller



antineutrino

G. Zeller



ν_e Event Fractions in ν STORM

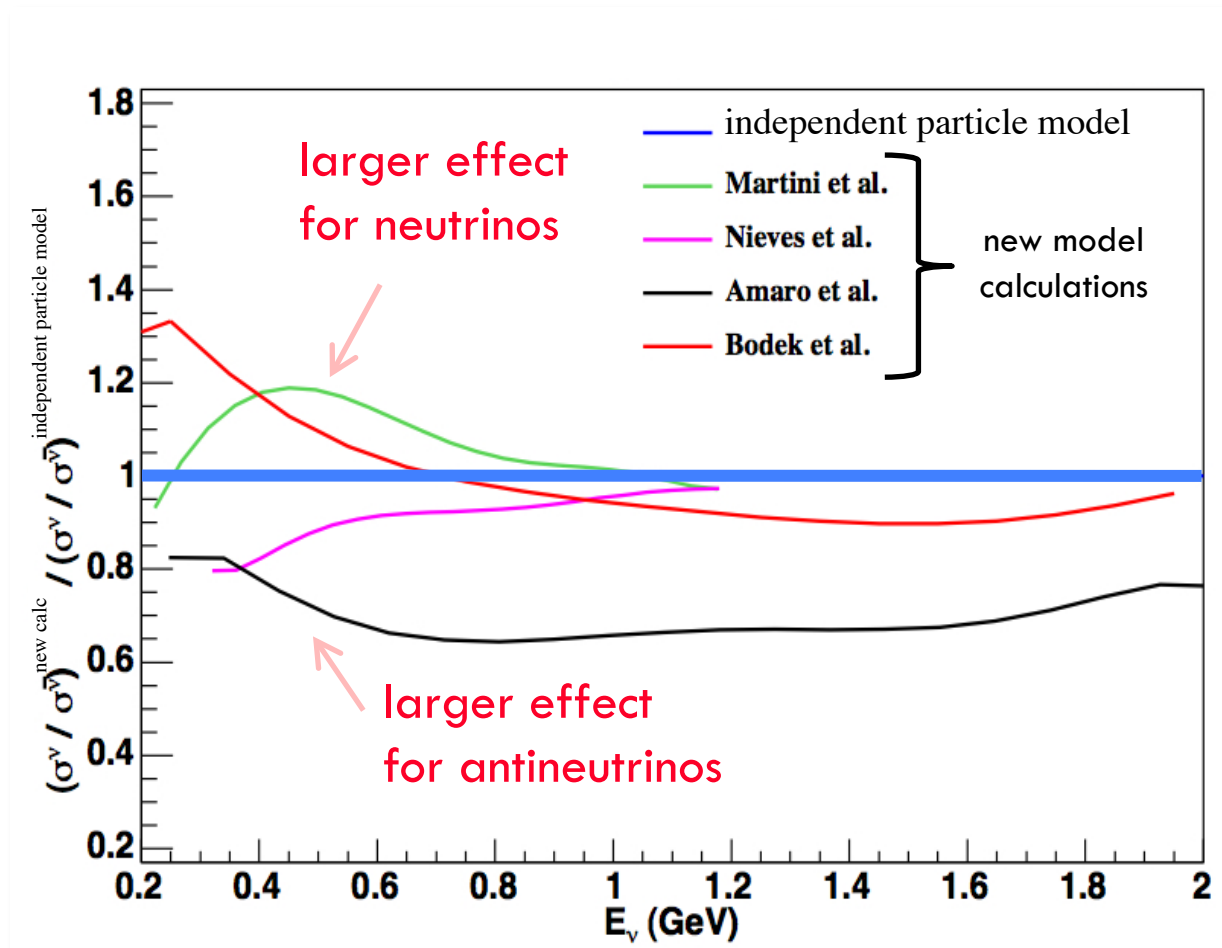
sources of ν_e events produced by ν STORM 3.8 GeV μ^+ beam

production mode	# fraction of total (%)
QE ($\nu_e n \rightarrow e^- p$)	23.3
NC elastic ($\nu_e N \rightarrow \nu_e N$)	10.0
CC resonant π^+ ($\nu_e N \rightarrow e^- N \pi^+$)	25.5
CC resonant π^0 ($\nu_e n \rightarrow e^- p \pi^0$)	5.6
NC resonant π^0 ($\nu_e N \rightarrow \nu_e N \pi^0$)	6.4
NC resonant π^\pm ($\nu_e N \rightarrow \nu_e N \pi^\pm$)	4.5
CC DIS ($\nu_e N \rightarrow e^- X, W > 2$)	8.3
NC DIS ($\nu_e N \rightarrow e^- X, W > 2$)	2.7
other CC	9.9
other NC	3.8
total CC	72.7
total NC	27.3

Table 1: NUANCE-predicted ν_e event rate fractions for a 3.8 GeV μ^+ beam, 100m from the source. Processes are defined at the initial neutrino interaction vertex and do not include final state effects. These estimates have been integrated over the ν STORM flux spectrum and do not include detector efficiency or acceptance corrections.

$\nu_\mu/\bar{\nu}_\mu$ QE Ratio

- current models give different predictions for $\nu_\mu/\bar{\nu}_\mu$ QE scattering



Full Cross Section Expression

$$\frac{d\sigma}{dQ^2}(\nu n \rightarrow l^- p) = \left[A(Q^2) \mp B(Q^2) \frac{s-u}{M^2} + C(Q^2) \frac{(s-u)^2}{M^4} \right]$$

$$\times \frac{M^2 G_F^2 \cos^2 \theta_c}{8\pi E_\nu^2} \left[|F_A|^2 - \left(4 - \frac{Q^2}{M^2}\right) |F_V^1|^2 + \frac{Q^2}{M^2} \xi |F_V^2|^2 \left(1 - \frac{Q^2}{4M^2}\right) + \frac{4Q^2 \text{Re} F_V^{1*} \xi F_V^2}{M^2} \right.$$

$$\left. - \frac{Q^2}{M^2} \left(4 + \frac{Q^2}{M^2}\right) |F_A^3|^2 - \frac{m^2}{M^2} \left(|F_V^1 + \xi F_V^2|^2 + |F_A + 2F_P|^2 - \left(4 + \frac{Q^2}{M^2}\right) (|F_V^3|^2 + |F_P|^2) \right) \right]$$

$$B(Q^2) = \frac{Q^2}{M^2} \text{Re} F_A^* (F_V^1 + \xi F_V^2) - \frac{m^2}{M^2} \text{Re} \left[\left(F_V^1 - \frac{Q^2}{4M^2} \xi F_V^2 \right)^* F_V^3 - \left(F_A - \frac{Q^2 F_P}{2M^2} \right)^* F_A^3 \right]$$

$$C(Q^2) = \frac{1}{4} \left(|F_A|^2 + |F_V^1|^2 + \frac{Q^2}{M^2} \left| \frac{\xi F_V^2}{2} \right|^2 + \frac{Q^2}{M^2} |F_A^3|^2 \right)$$

- ◆ F_P , F_A^3 and F_V^3 terms are less well studied