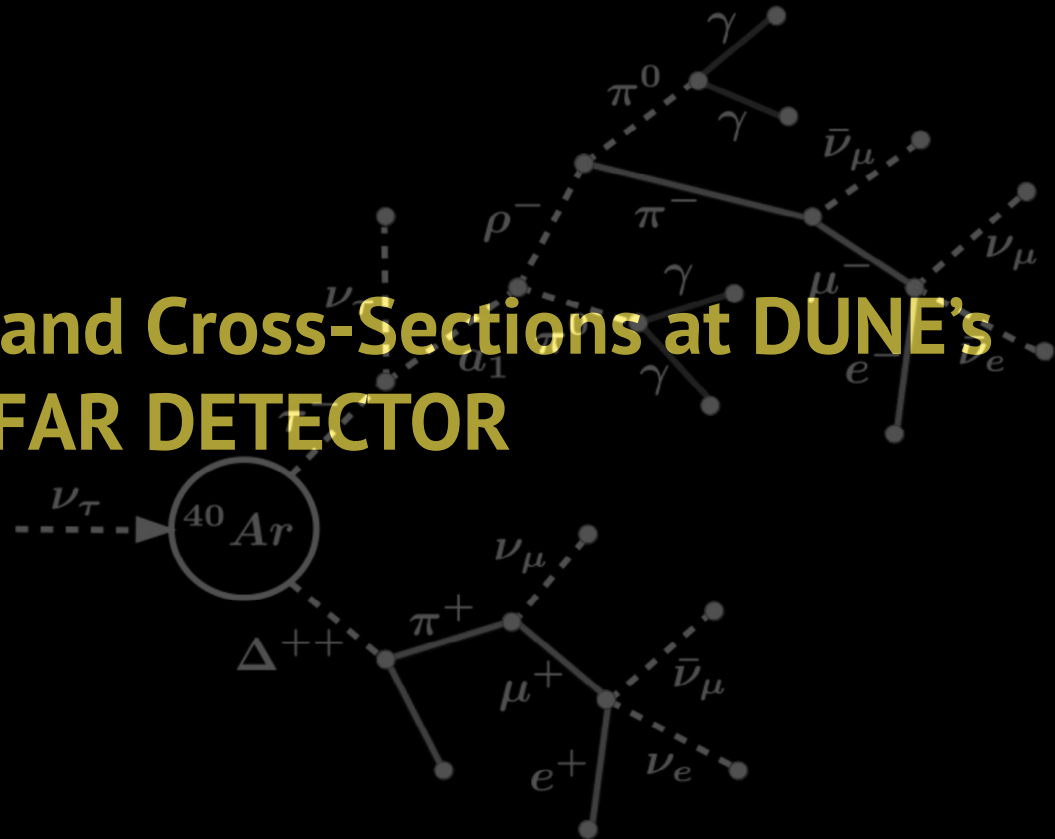


APS April Meeting 2022
Neutrino Cross Sections

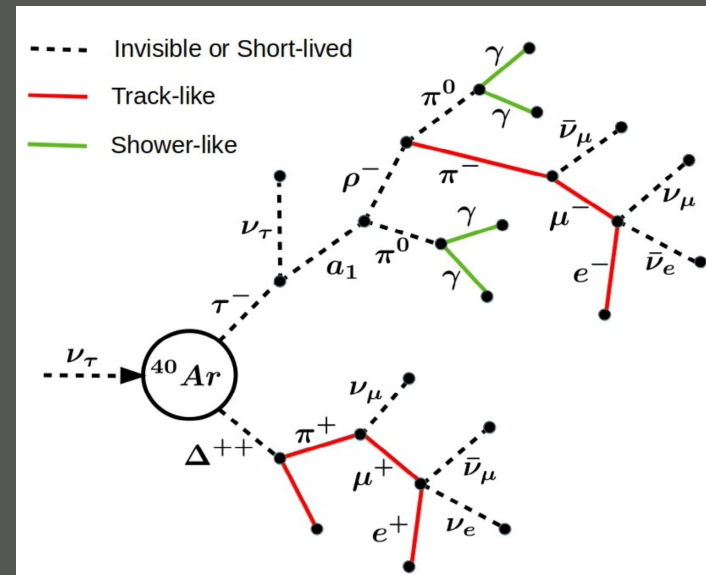
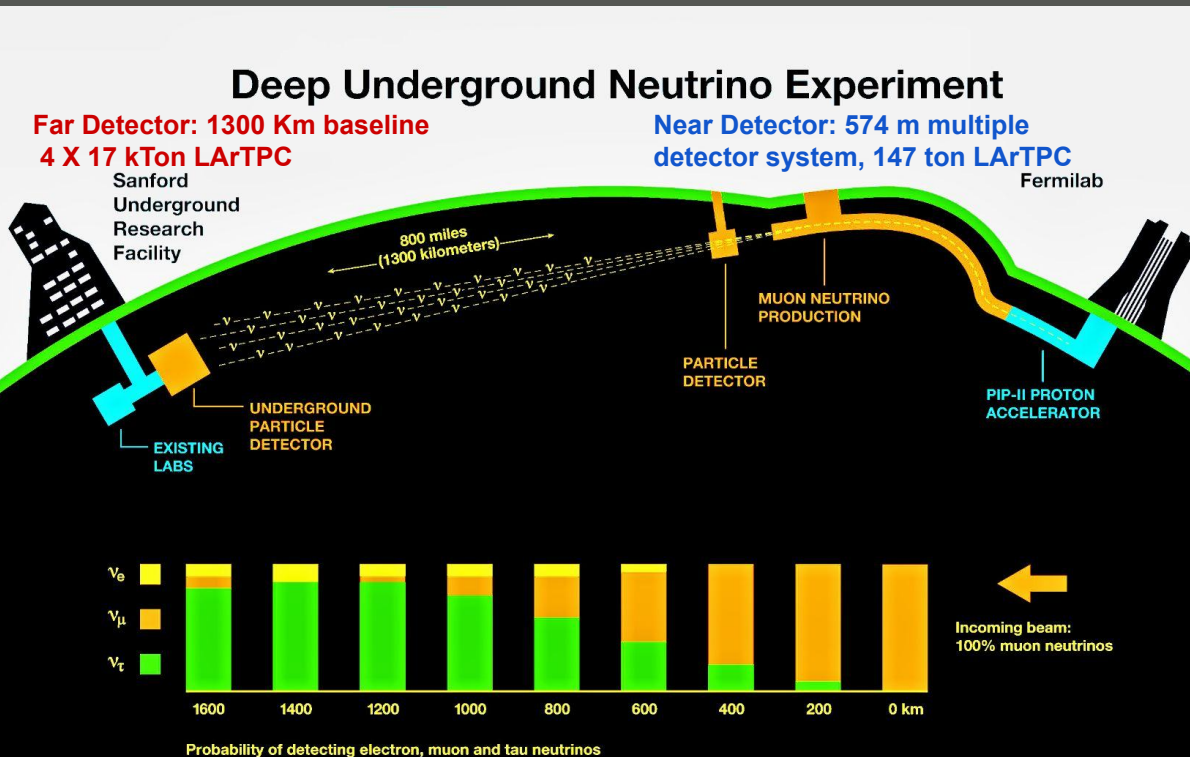
Tau Neutrinos and Cross-Sections at DUNE's FAR DETECTOR



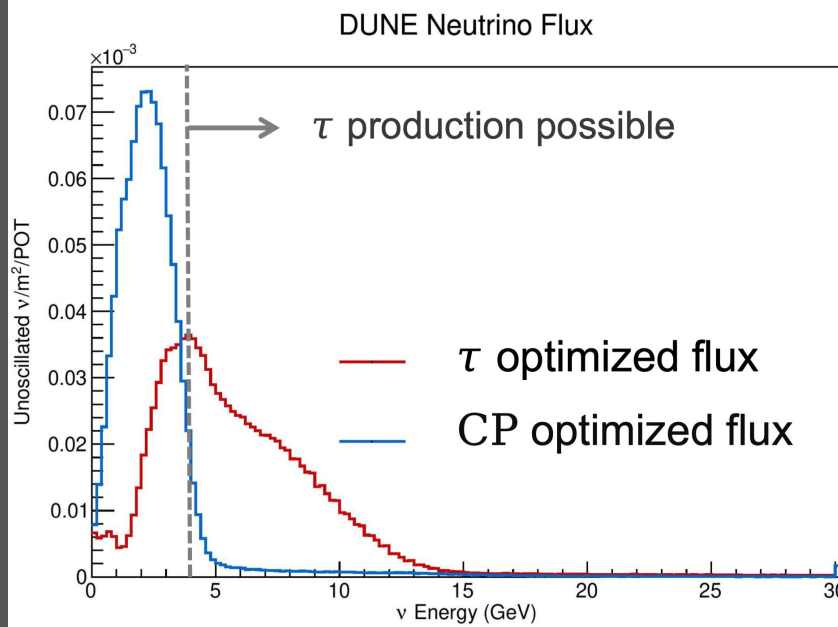
Barbara Yaeggy
(04/09/2022)

NuTau at DUNE

- While **DUNE is optimized to measure ν_e appearance in a ν_μ beam** the broadband beam and long baseline lead to significant ν_τ appearance above the kinematic threshold to produce a τ -lepton.
- Due to this, **DUNE is the only upcoming neutrino experiment** expected to be able to **collect** a sample of oscillated ν_τ - CC beam events.
- DUNE will be capable to distinguish between electrons, photons, muons, and pions with high efficiency at the typical energies of beam produced ν_τ - CC beam interactions.



DUNE will be able to constrain the three flavor paradigm!



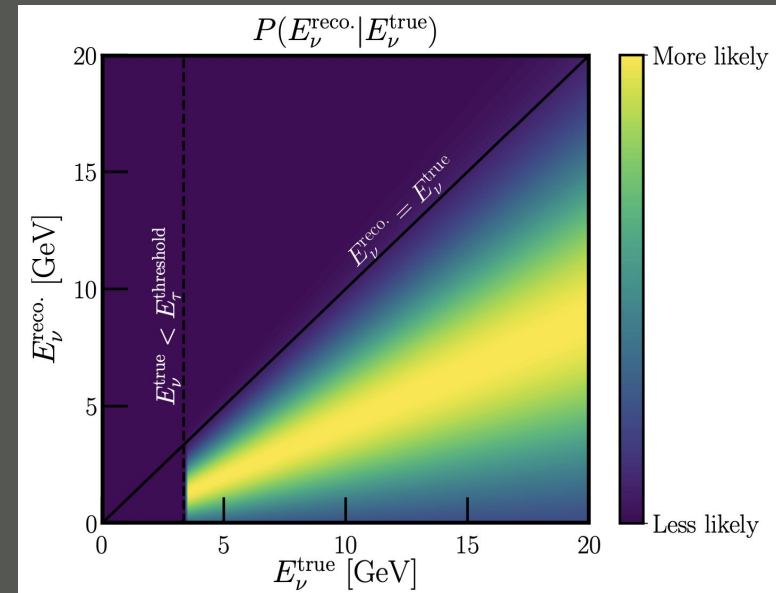
- Optimized for the CP sensitivity phase measurement
- Low energy
- Default starting configuration
- **Tau-optimized beam:** modified to produce a higher energy spectrum by modifying the relative position of the target and horns, and using NuMI style parabolic horns

Expected counts/year:

- $\sim 30 \nu_\tau$ in CP-optimized neutrino mode
- $\sim 130 \nu_\tau$ in CP-optimized neutrino mode
- $\sim 800 \nu_\tau$ in Tau-optimized neutrino mode

DUNE has studied using **kinematic cuts** (first proposed in J. Conrad, et al, PRD 82, 093012 (2010))

- Select ν_τ with hadronically decaying tau lepton
- Assume near perfect e/γ and μ/π discrimination
- Simple kinematic cuts on $\pi^{+/-}$ yield good ν_τ -CC/NC discrimination



Migration matrix for hadronically decaying τ leptons produced via ν_τ charged-current interactions. [PhysRevD.100.016004](https://arxiv.org/abs/1908.01604)

Due to the large mass of the τ^\pm relative to the e^\pm and μ^\pm , the threshold for this process to occur is 3.5 GeV.

In the few GeV region [1-10] GeV there are contributions from several kinds of lepton-nucleon interaction processes as defined by W and Q^2 .

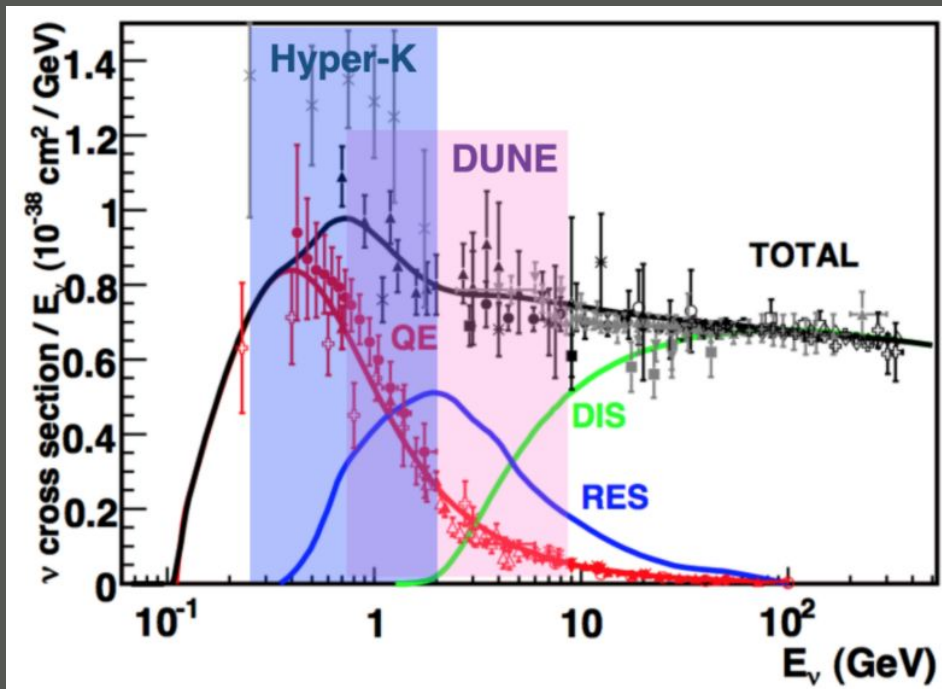
Quasi-elastic (QE): $W < 1.07$ GeV

Resonance $\Delta(1232)$: $1.1 < W < 1.4$ GeV

Higher mass resonances: $1.4 < W < 1.8$ GeV

Inelastic continuum: $W > 1.8$ GeV, at low Q^2 (Shallow Inelastic) and at high Q^2 (DIS)

At low Q^2 (< 1 GeV) there are large non-perturbative contributions to the inelastic cross section: target mass corrections, dynamic higher twist effects, higher order QCD terms, and nuclear effects in nuclear targets.



- To avoid double counting, the evaluation of the inelastic piece is done over a restricted phase space.
- Generally, a limit on the hadronic final state invariant mass W is applied, such as $W > W_{\min}$.
- This W_{\min} is used to separate the exclusive and inclusive calculations.

DIS CC- ν_τ Cross-section

$$\frac{d^2\sigma_A}{dx dy} = \frac{G_F^2 M_N E_\nu}{\pi(1 + \frac{Q^2}{M_W^2})^2} \left\{ \left[y^2 x + \frac{m_l^2 y}{2E_\nu M_N} \right] F_{1A}(x, Q^2) + \left[\left(1 - \frac{m_l^2}{4E_\nu^2}\right) - \left(1 + \frac{M_N x}{2E_\nu}\right) y \right] F_{2A}(x, Q^2) \right. \\ \left. \pm \left[xy \left(1 - \frac{y}{2}\right) - \frac{m_l^2 y}{4E_\nu M_N} \right] F_{3A}(x, Q^2) + \frac{m_l^2 (m_l^2 + Q^2)}{4E_\nu^2 M_N^2 x} F_{4A}(x, Q^2) - \frac{m_l^2}{E_\nu M_N} F_{5A}(x, Q^2) \right\}$$

The scaling variables $x (= \frac{Q^2}{2p \cdot q})$ and $y (= \frac{\nu}{E_\nu} = \frac{q_0}{E_\nu})$ lie in the range:

$$\frac{m_l^2}{2M_N(E_\nu - m_l)} \leq x \leq 1 \quad \text{and} \quad a - b \leq y \leq a + b,$$

where

$$a = \frac{1 - m_l^2 \left(\frac{1}{2M_N E_\nu x} + \frac{1}{2E_\nu^2} \right)}{2 \left(1 + \frac{M_N x}{2E_\nu} \right)} \quad \text{and} \quad b = \frac{\sqrt{\left(1 - \frac{m_l^2}{2M_N E_\nu x} \right)^2 - \frac{m_l^2}{E_\nu^2}}}{2 \left(1 + \frac{M_N x}{2E_\nu} \right)}.$$

Albright, Jarlskog '75 Paschos, Yu '98 Kretzer, Reno '02

F_4 and F_5 are ignored in the muon neutrino interactions because of a suppression factor depending on the square of the m_l divided by the nucleon mass times neutrino energy, $m_l^2 / (M_N E_\nu)$.

At leading order, in the limit of massless quarks and target hadrons:

- **Albright-Jarlskog relations:**

$$F_4 = 0 \quad \text{and} \quad F_2 = 2xF_5$$

Which are a generalization **Callan-Gross relation:**

$$F_2(x, Q^2) = 2xF_1(x, Q^2)$$

$\nu\tau$ (CC) interactions give access to cross section physics not accessible otherwise!

A look to the CC ν_τ and ν_μ Cross Section M. H. Reno - PhysRevD.74.033001

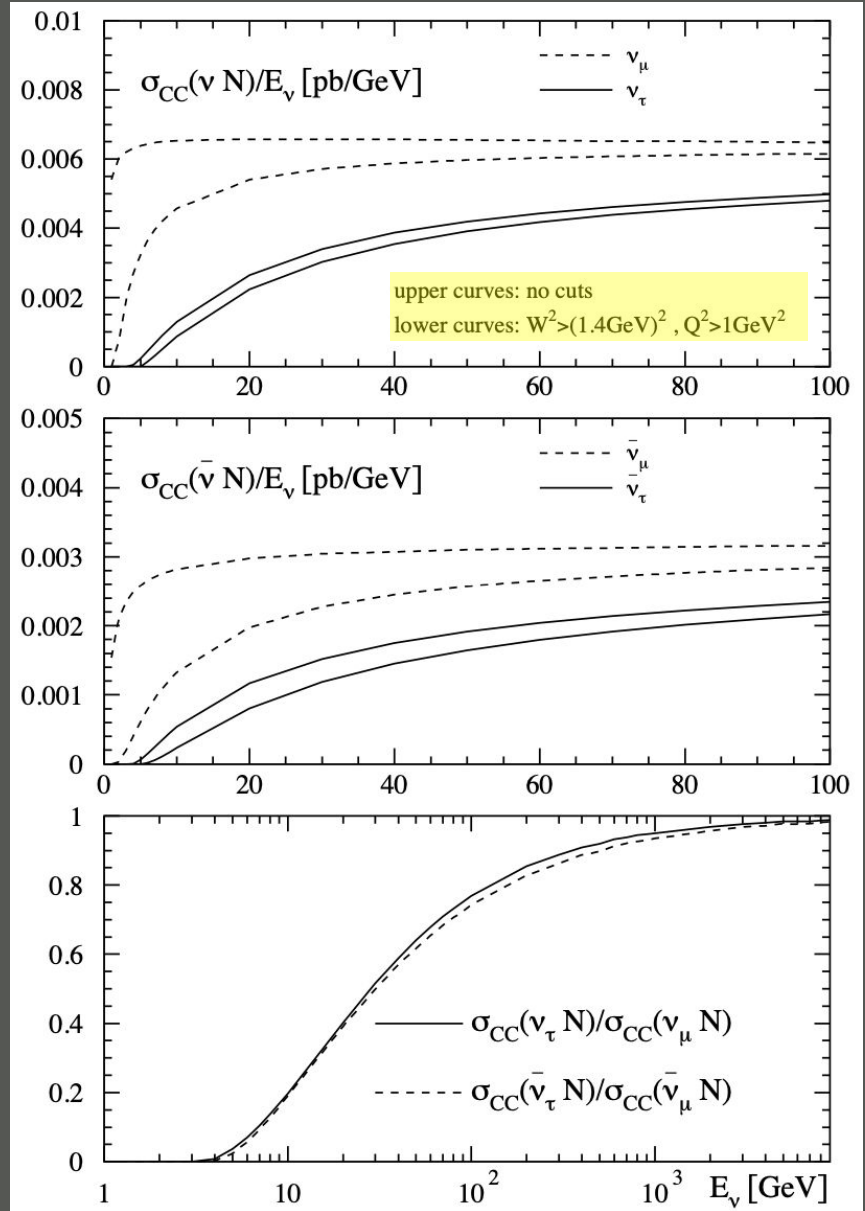
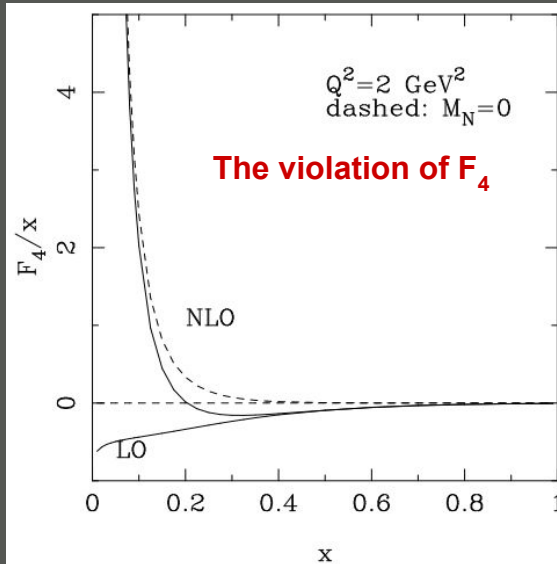
The effect of these imposed cuts is much less pronounced for ν_τ DIS where m_τ acts as a physical cut-off of non-DIS interaction.

See how slowly $\sigma_{CC}(\nu_\tau)$ approaches to $\sigma_{CC}(\nu_\mu)$ from below at very HE indicating a persistent τ threshold effect.

About half of the reduction at high energies is actually of dynamic origin, to be attributed to a negative contribution of F5

$$-\frac{m_\tau^2}{E_\nu M_N} F_5^{W^\pm}$$

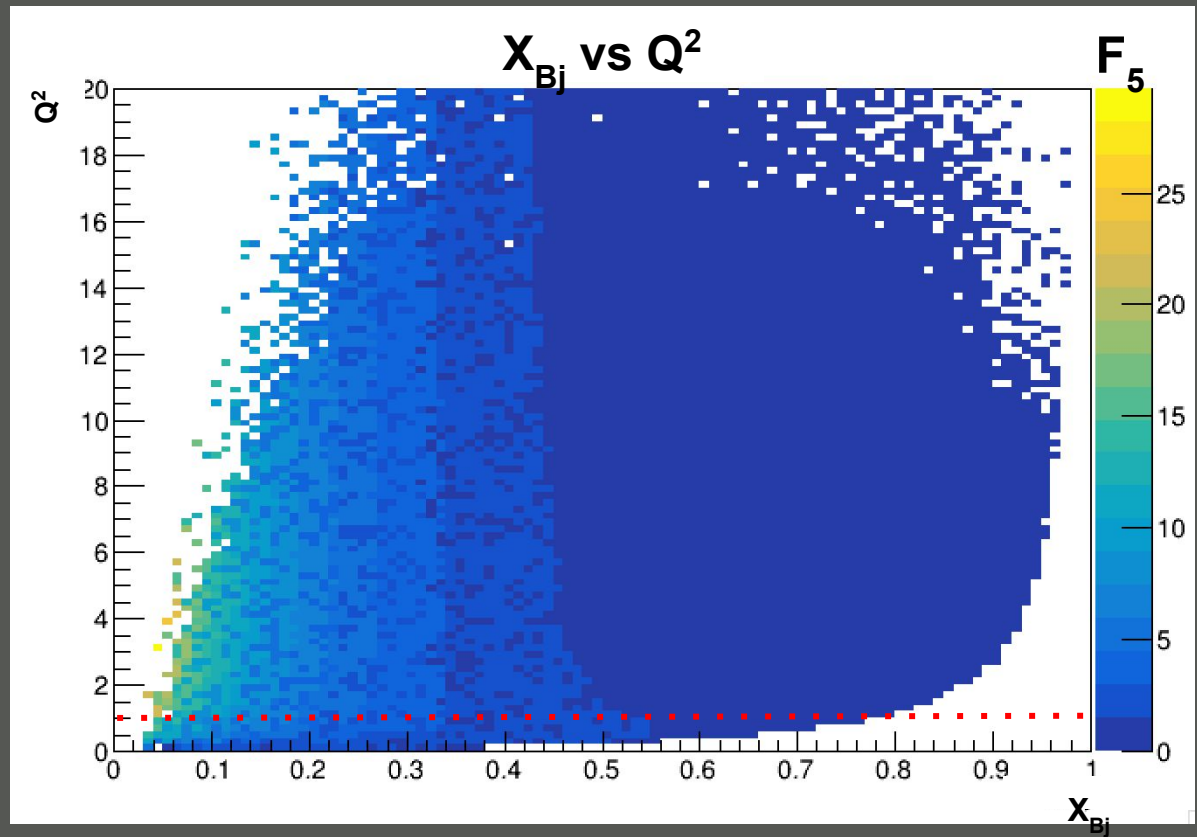
Suppressed around 1 TeV and is compensated to some extent by the low-x rise of $F_5 \sim q(x)$



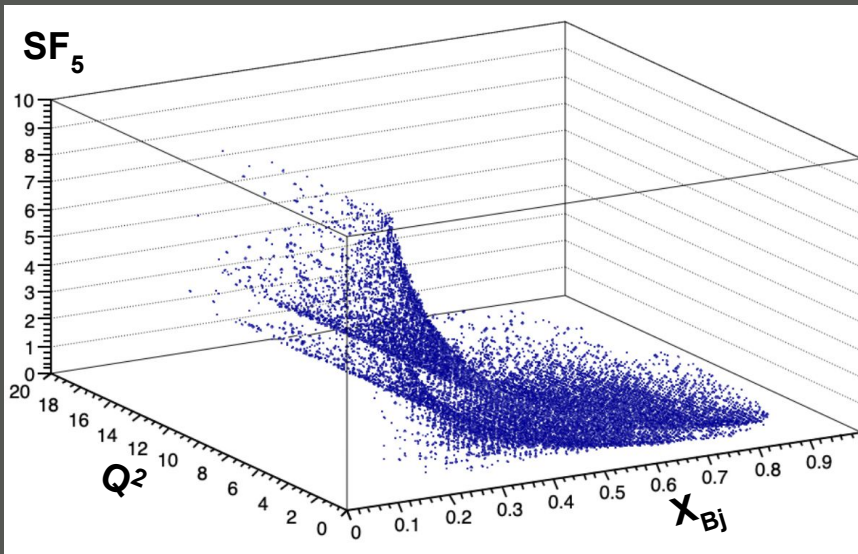
Exploring The Nature of F_5

Nature of $F_5(x, Q^2)$

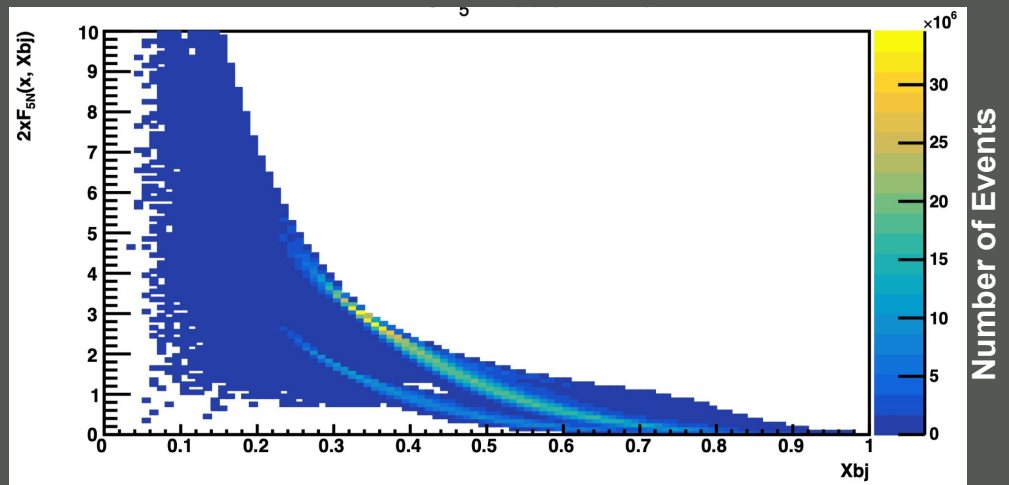
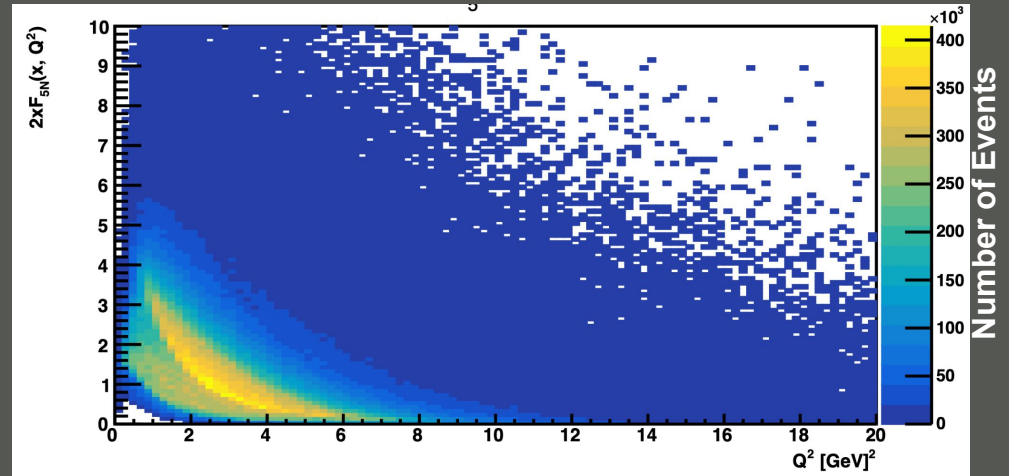
- This is F_5 in terms of x and Q^2 , its effect is in all $[x, Q^2]$ phase space.
- At lower X_{Bj} , F_5 values are high.
- Below $Q^2=1$, non-perturbative
- Above $Q^2=1$, perturbative



$$\frac{d^2\sigma^{\nu(\bar{\nu})}}{dxdy} = \frac{G_F^2 M E_\nu}{\pi(1 + Q^2/M_W^2)^2} \left((y^2x + \frac{m_\tau^2 y}{2E_\nu M}) F_1 + \left[(1 - \frac{m_\tau^2}{4E_\nu^2}) - (1 + \frac{Mx}{2E_\nu}) \right] F_2 \right. \\ \left. \pm \left[xy(1 - \frac{y}{2}) - \frac{m_\tau^2 y}{4E_\nu M} \right] F_3 + \frac{m_\tau^2 (m_\tau^2 + Q^2)}{4E_\nu^2 M^2 x} F_4 - \frac{m_\tau^2}{E_\nu M} F_5 \right),$$

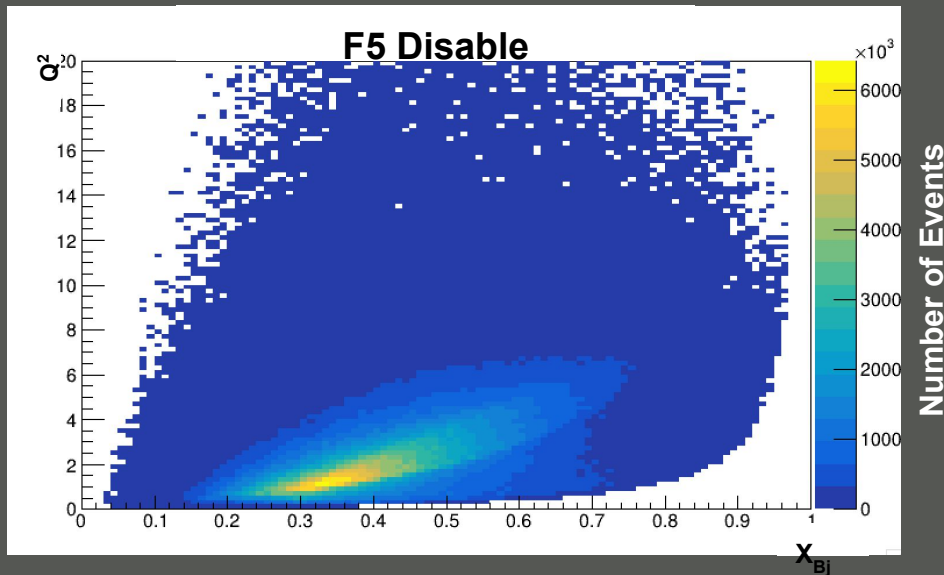
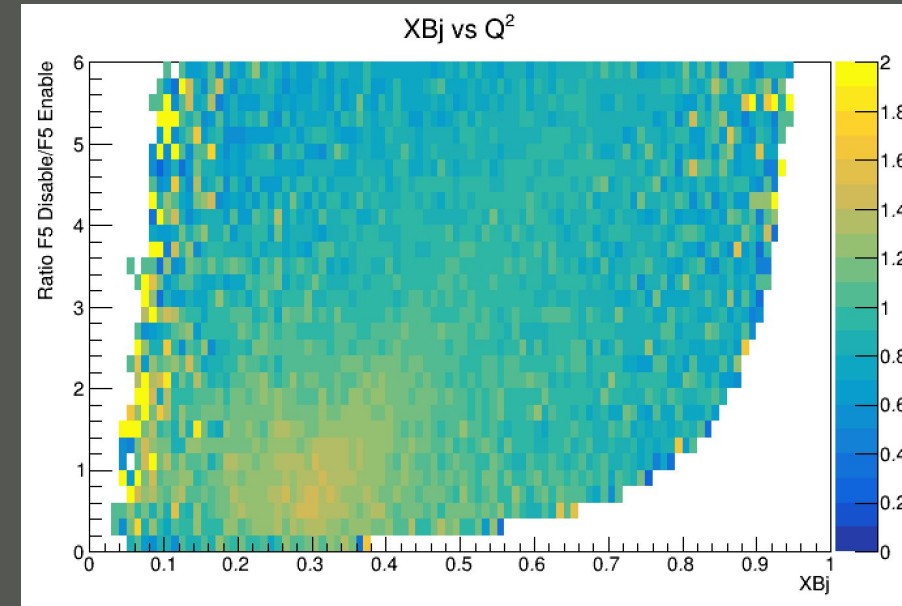
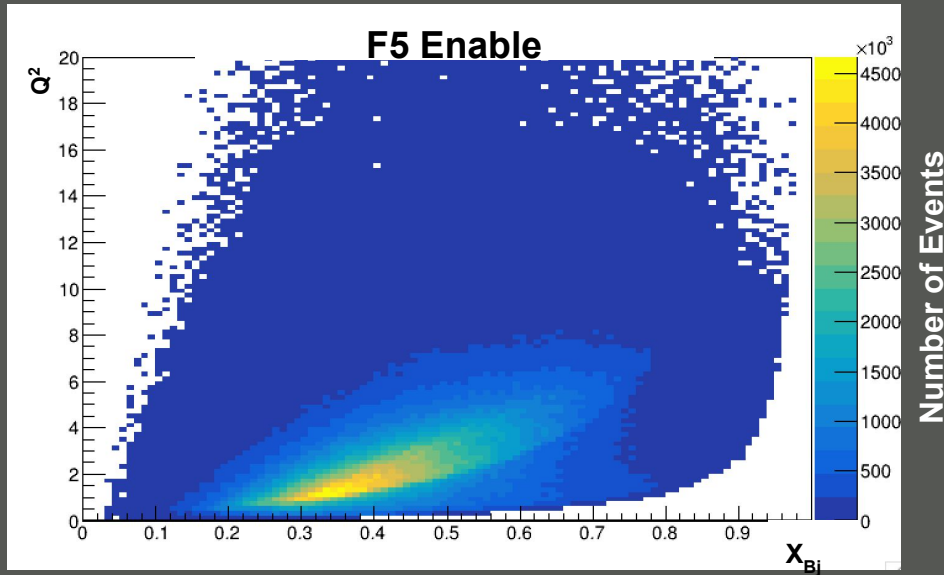


- This is F₅ in terms of x and Q², its effect is in all [x, Q²] phase space.



Effect of F_5 in the total number of events.

In Xsec and Events the F_5 value covers all the phase space

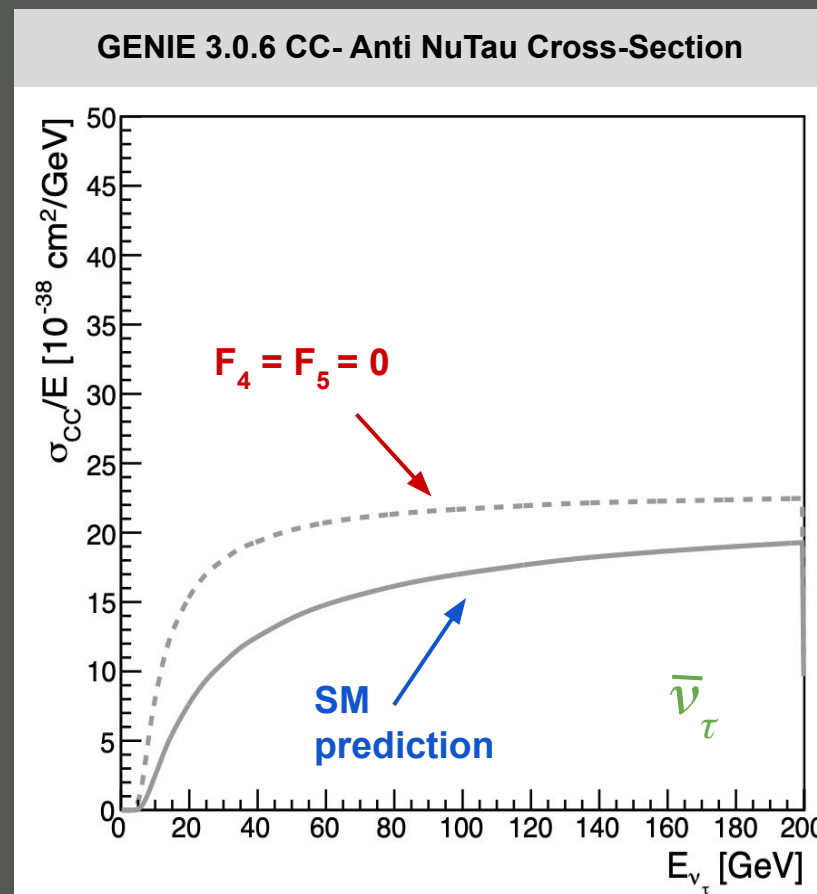
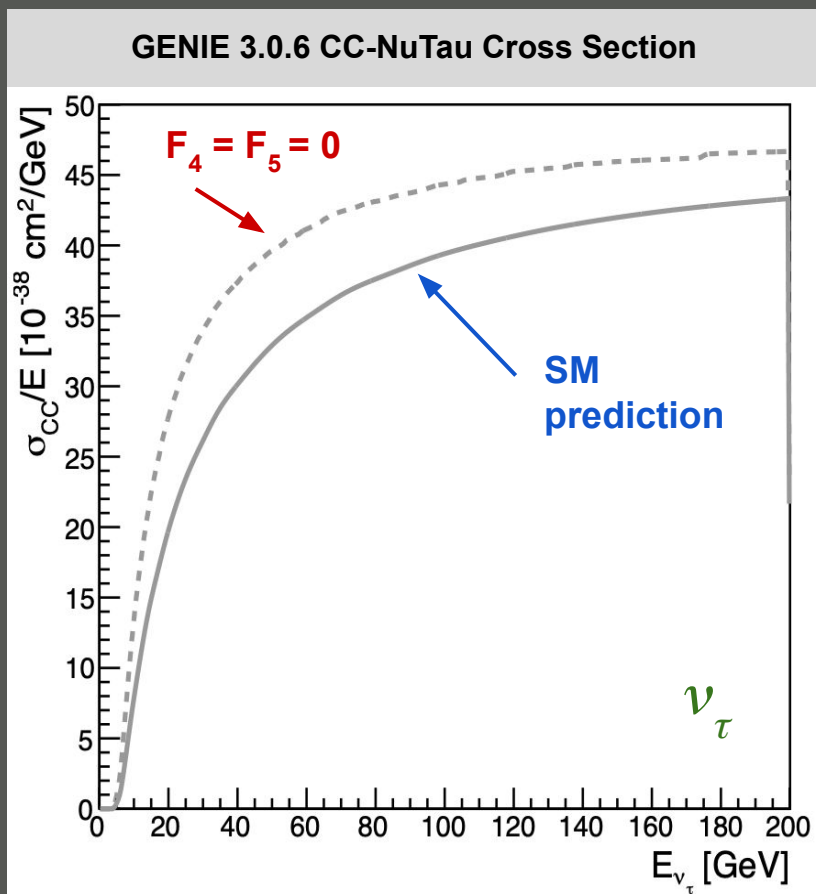


Ratio of F5 Disable / F5 Enable

The ratio is greater than 1:

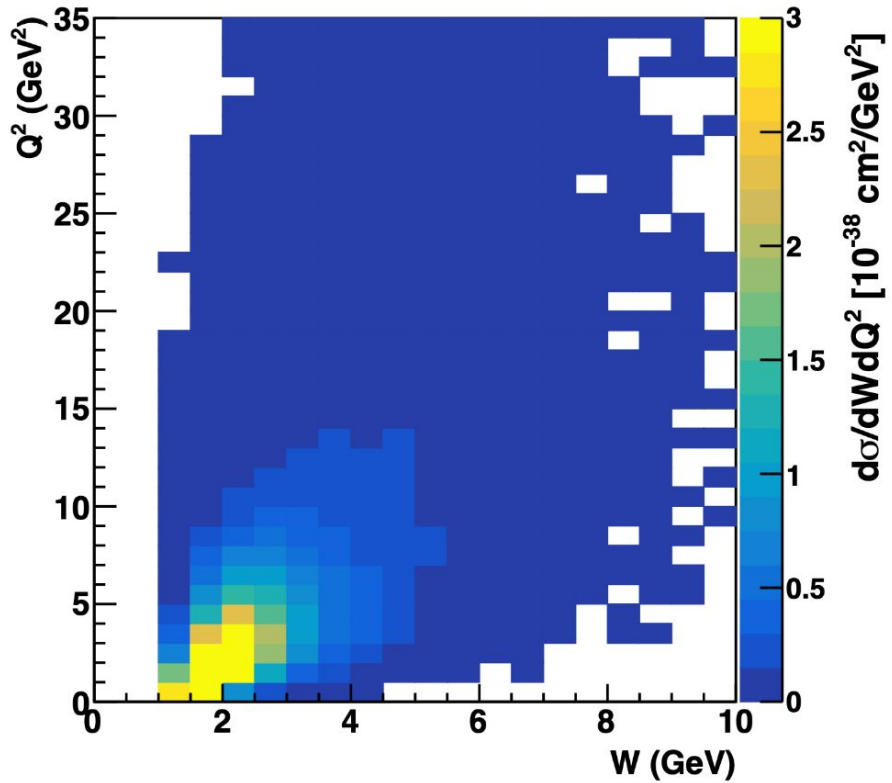
- Which is expected since F_5 is a subtracted component of the total XSec.
- Also, it means that there is a chance to disentangle an overall normalization change from a scaling of F_5

Notice the difference between the cross-sections in the $F_4 = F_5 = 0$ hypothesis and the SM prediction **is larger for lower neutrino energies.**

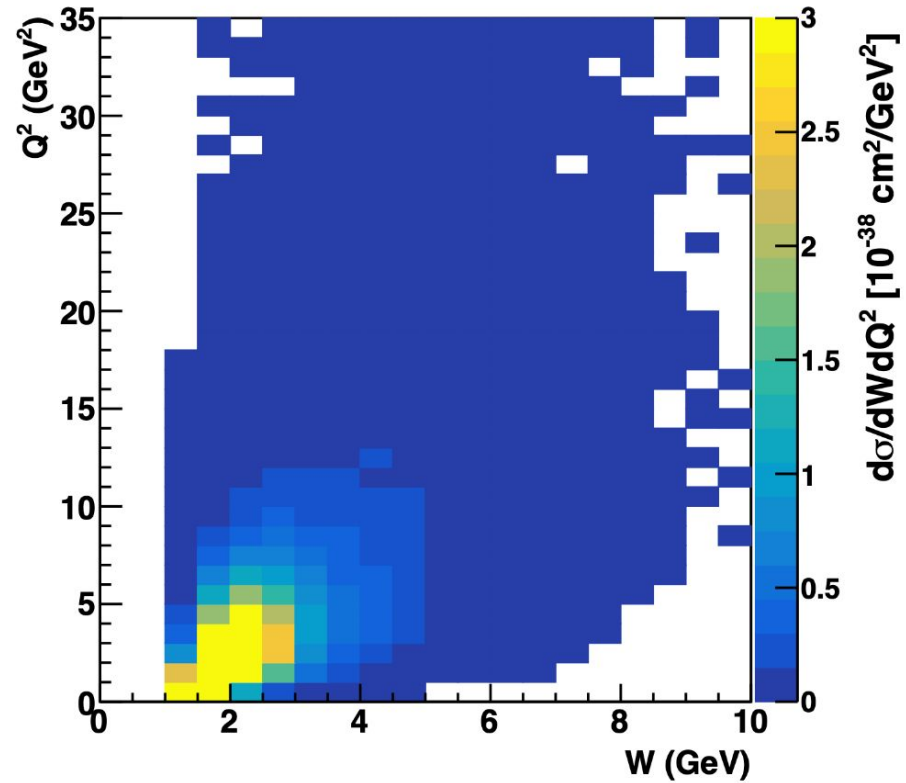


SF₅ Disable

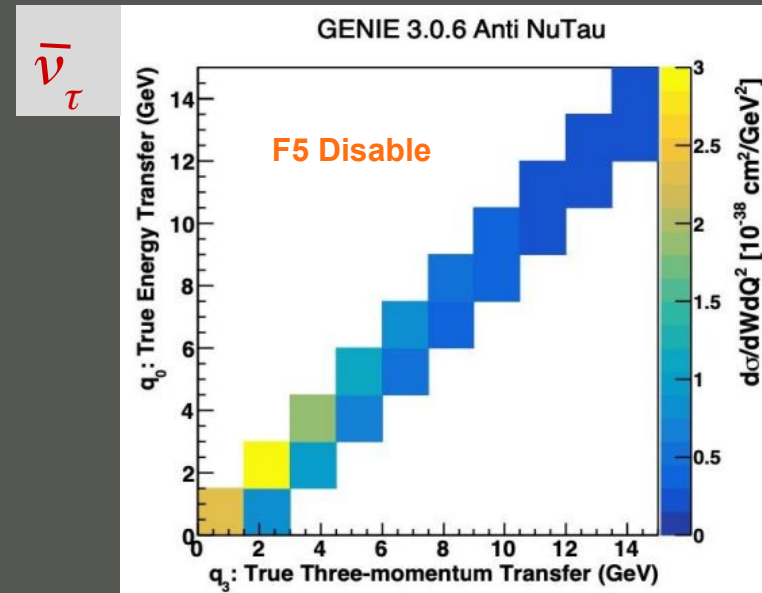
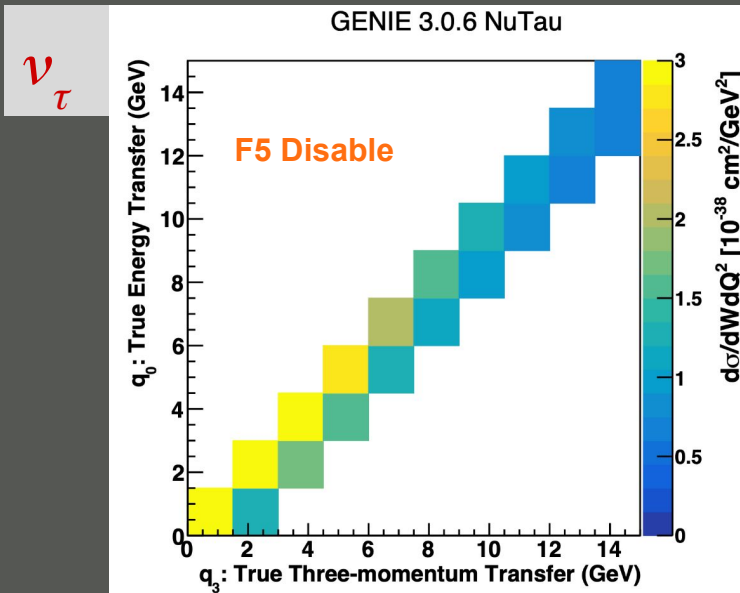
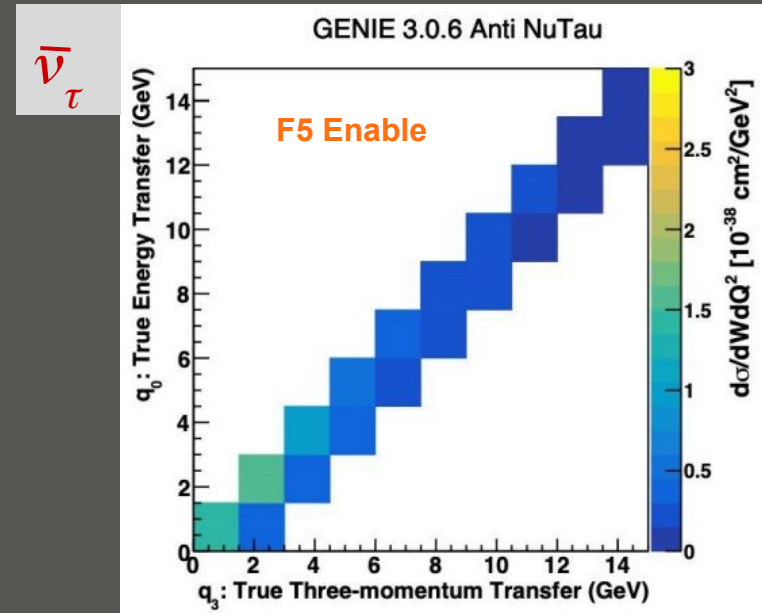
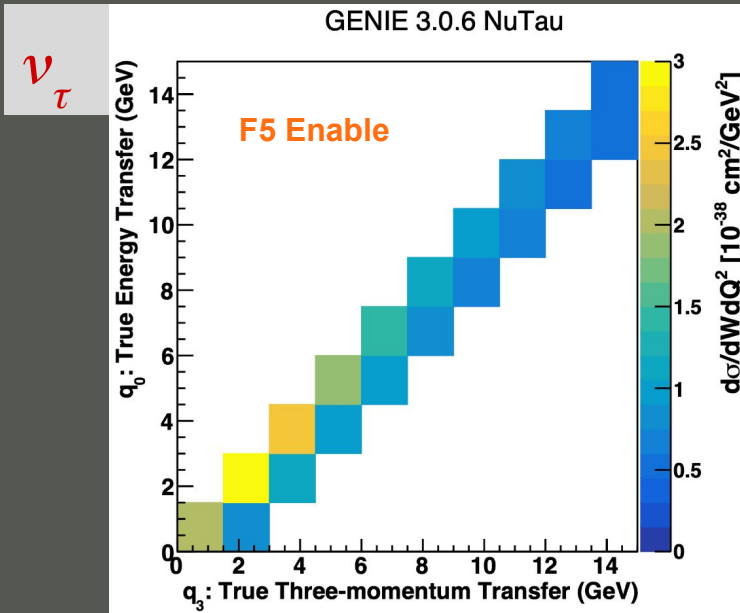
GENIE 3.0.6 NuTau

SF₅ Enable

GENIE 3.0.6 NuTau



CC - ν_τ TRUTH Level studies show that indeed, when DIS cuts are applied and $F_5 = 0$ we can extract new information from the lepton cross section.



Comments

The new features which appear in the case of the V_τ -A interaction as compared to the v_e -A and V_μ -nucleon interactions and contribute to modify the cross sections are:

- Kinematical changes in Q^2 and E_ℓ due to the presence of m_τ
- The contributions due to the additional nucleon structure functions $F_{4N}(X, Q^2)$ and $F_{5N}(X, Q^2)$ in the presence of $m_\tau \neq 0$.
- Modifications in cross-sections due to the effect of polarization state of the τ leptons produced in the final state.

Some of the above effects are modified in the nuclear medium \rightarrow we need reliable nuclear model to describe DIS of leptons from nuclear targets.

- The produced τ -leptons in the final state may get polarized in the nuclear medium affecting the cross-section from nuclear targets. The polarization will also affect the topologies and characteristics of its decay products.
- The shadowing and anti-shadowing effects in the respective kinematics regions of the Bjorken variable x .

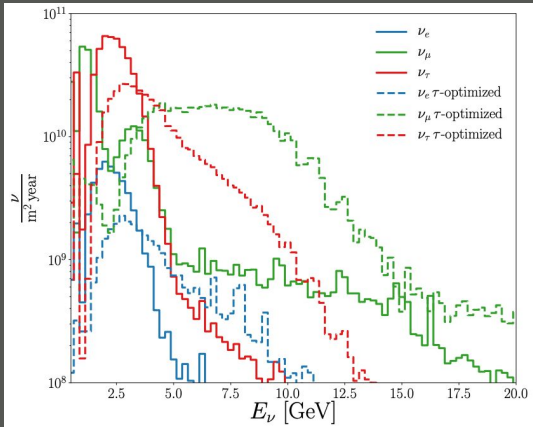
Thank you!



Milky Way and Volcan de Fuego , Guatemala

BACKUP

A key element in the study of tau neutrino physics is the decay modes of the tau lepton



Tau decay length $\sim 87 \mu\text{m}$
Ar nuclear radius, $\sim 3.4 \text{ fm}$

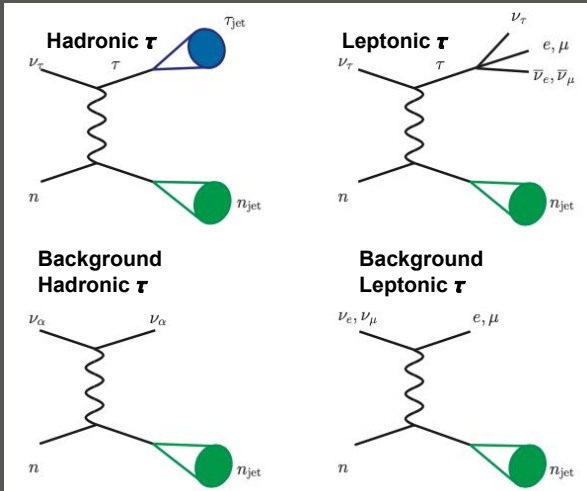
Tau decay products aren't subject to the Ar nuclear potential

Tau lifetime $(2.903 \pm 0.005) \times 10^{-13} \text{ s}$

Tau doesn't lead to observables displaced vertices

Decay mode	Branching ratio
Leptonic	
$e^- \bar{\nu}_e \nu_\tau$	17.8%
$\mu^- \bar{\nu}_\mu \nu_\tau$	17.4%
Hadronic	
$\pi^- \pi^0 \nu_\tau$	25.5%
$\pi^- \nu_\tau$	10.8%
$\pi^- \pi^0 \pi^0 \nu_\tau$	9.3%
$\pi^- \pi^- \pi^+ \nu_\tau$	9.0%
$\pi^- \pi^- \pi^+ \pi^0 \nu_\tau$	4.5%
other	5.7%

Neutrino fluxes at the DUNE far detector. [arXiv:2007.00015](https://arxiv.org/abs/2007.00015)



DUNE granularity is limited by wire spacing of a few millimeters

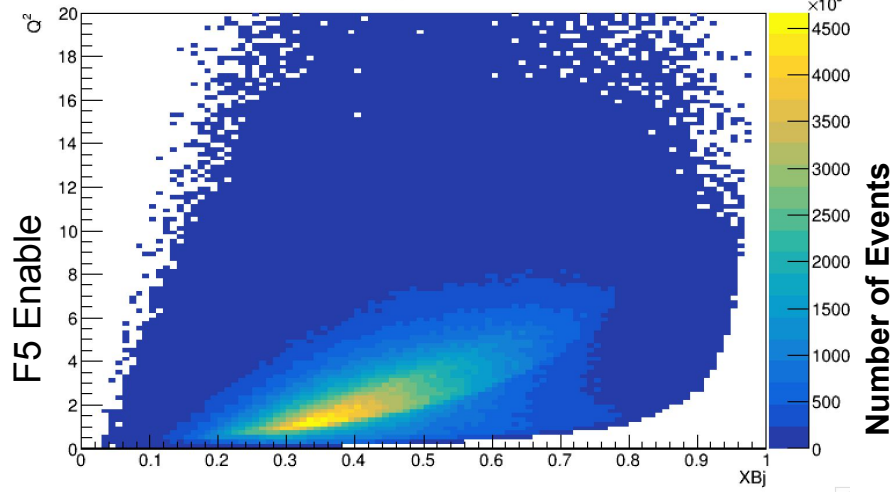
Dominant decay modes of τ -Kaonic decays and others go into the "other" category. [arXiv:2007.00015](https://arxiv.org/abs/2007.00015)

Observation of Tau tracks is unlikely

Background for τ_μ signal mainly comes from CC- ν_μ being ν_μ flux very large.

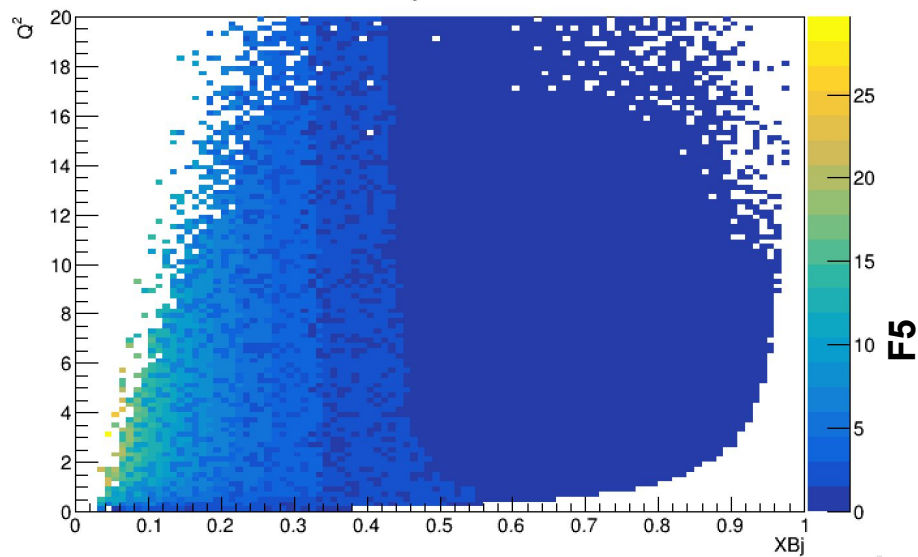
Background for τ_e signal are CC- ν_e events, being ν_e flux a small fraction of the total neutrino flux.

X_{Bj} vs Q^2

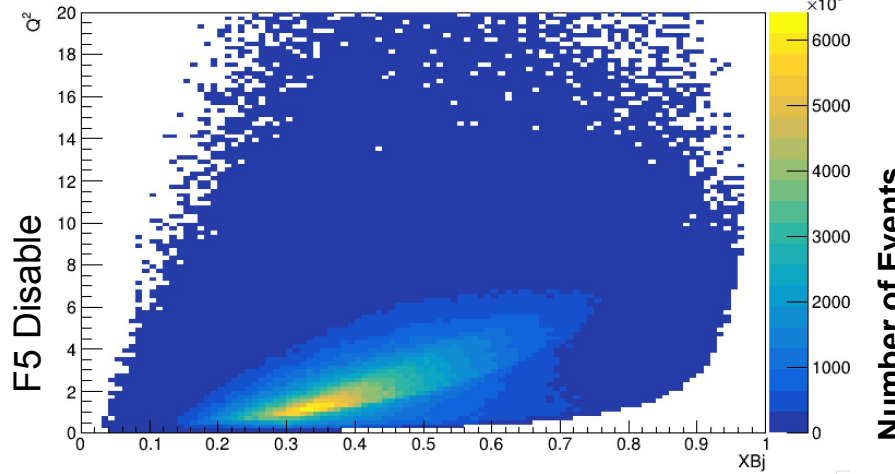


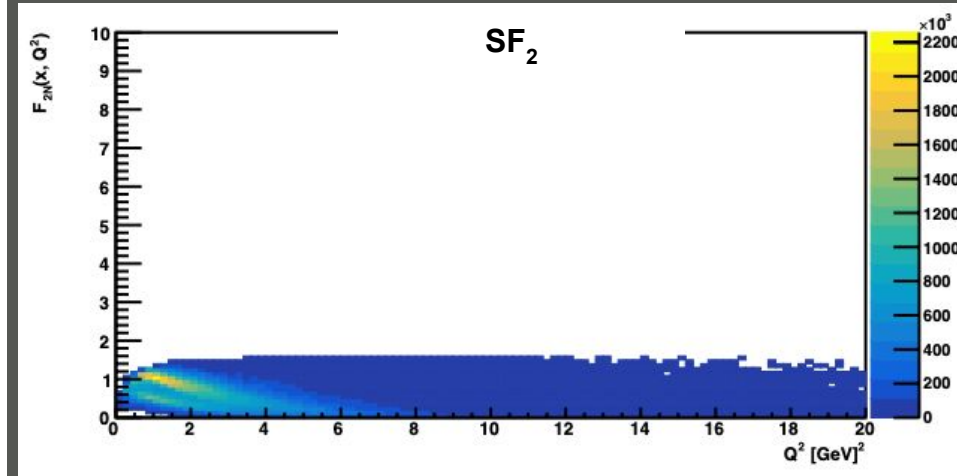
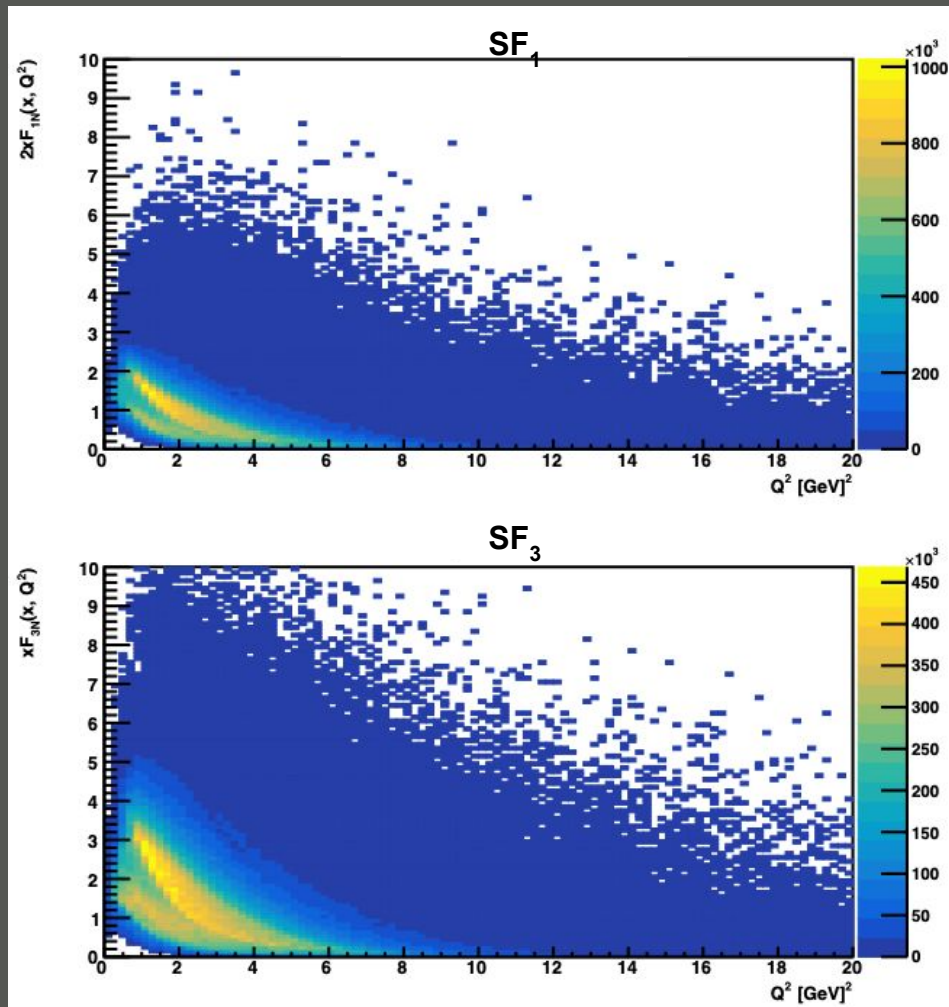
- In Xsec and Events the F5 value covers all the phase space

X_{Bj} vs Q^2

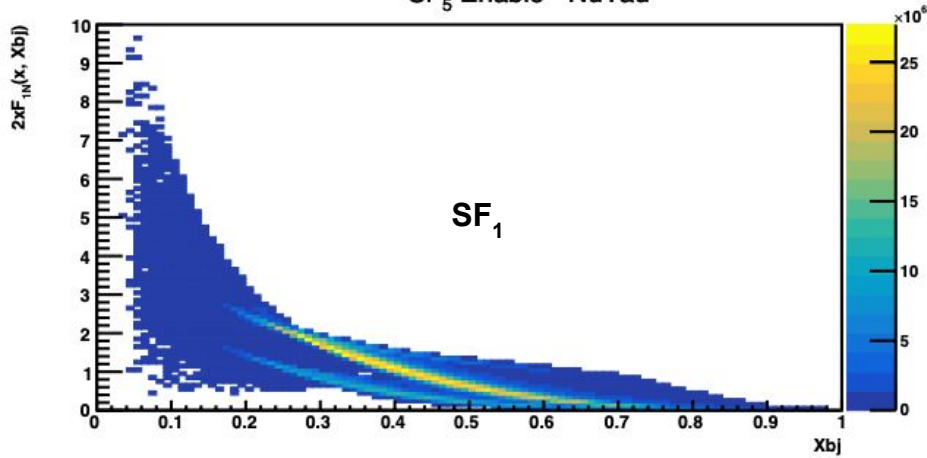


X_{Bj} vs Q^2

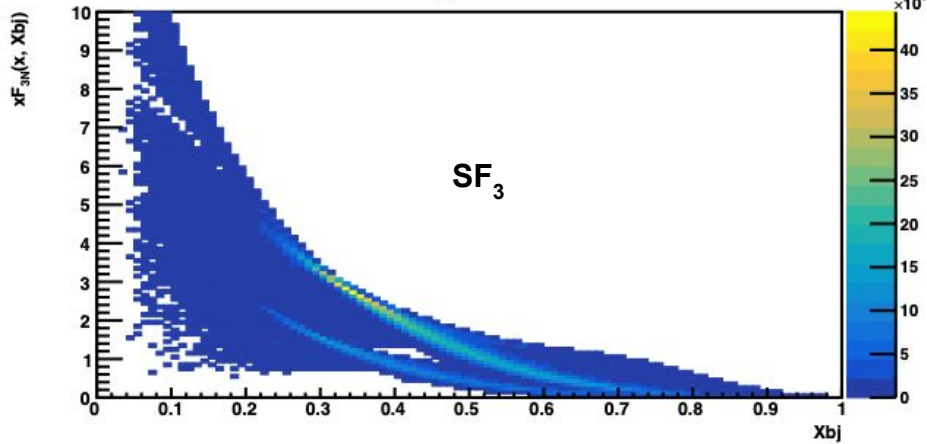




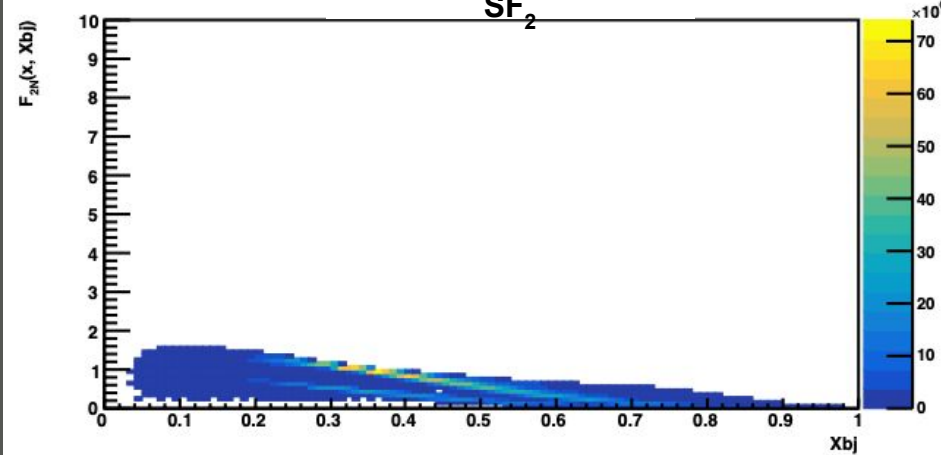
SF₅ Enable - NuTau



SF₅ Enable - NuTau



SF₂



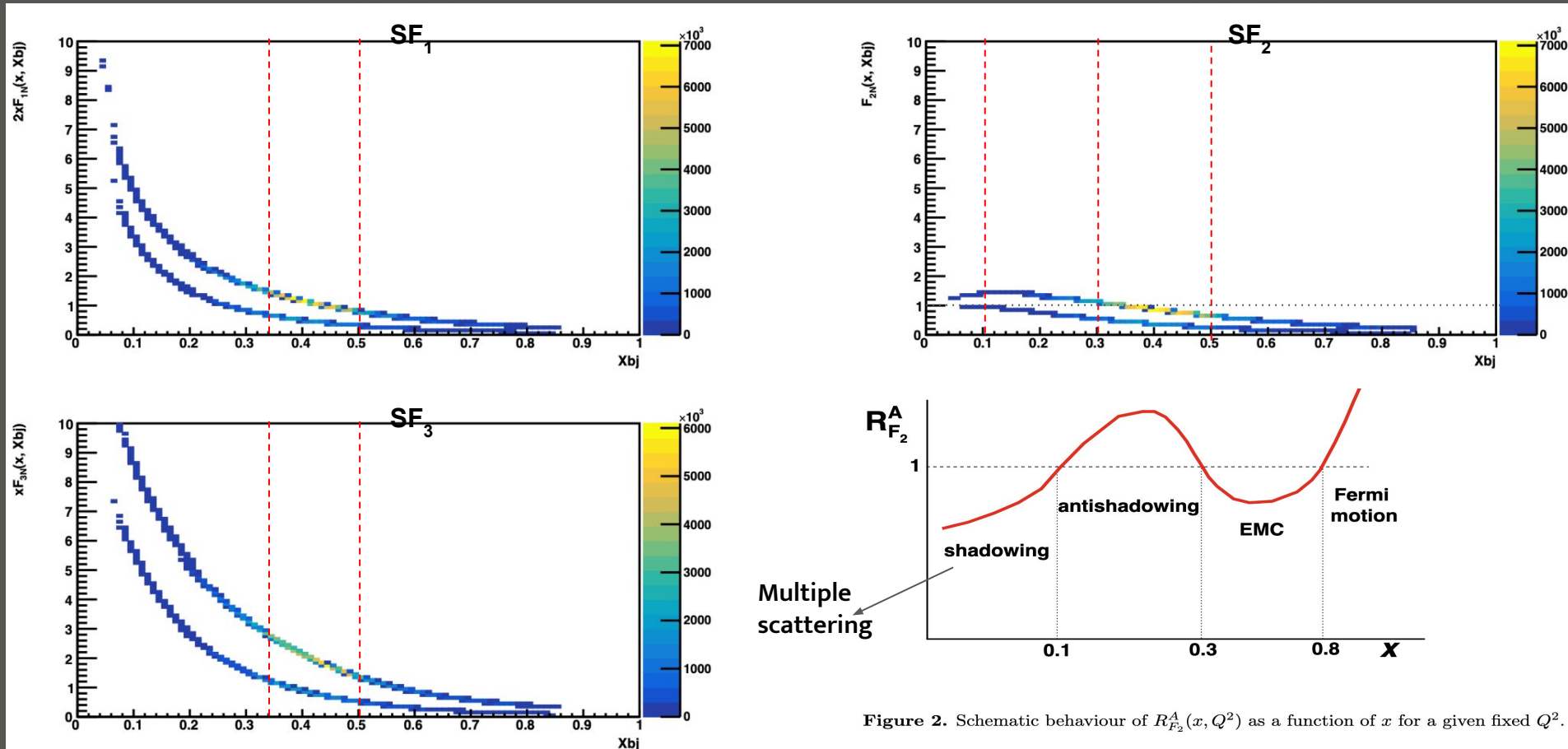
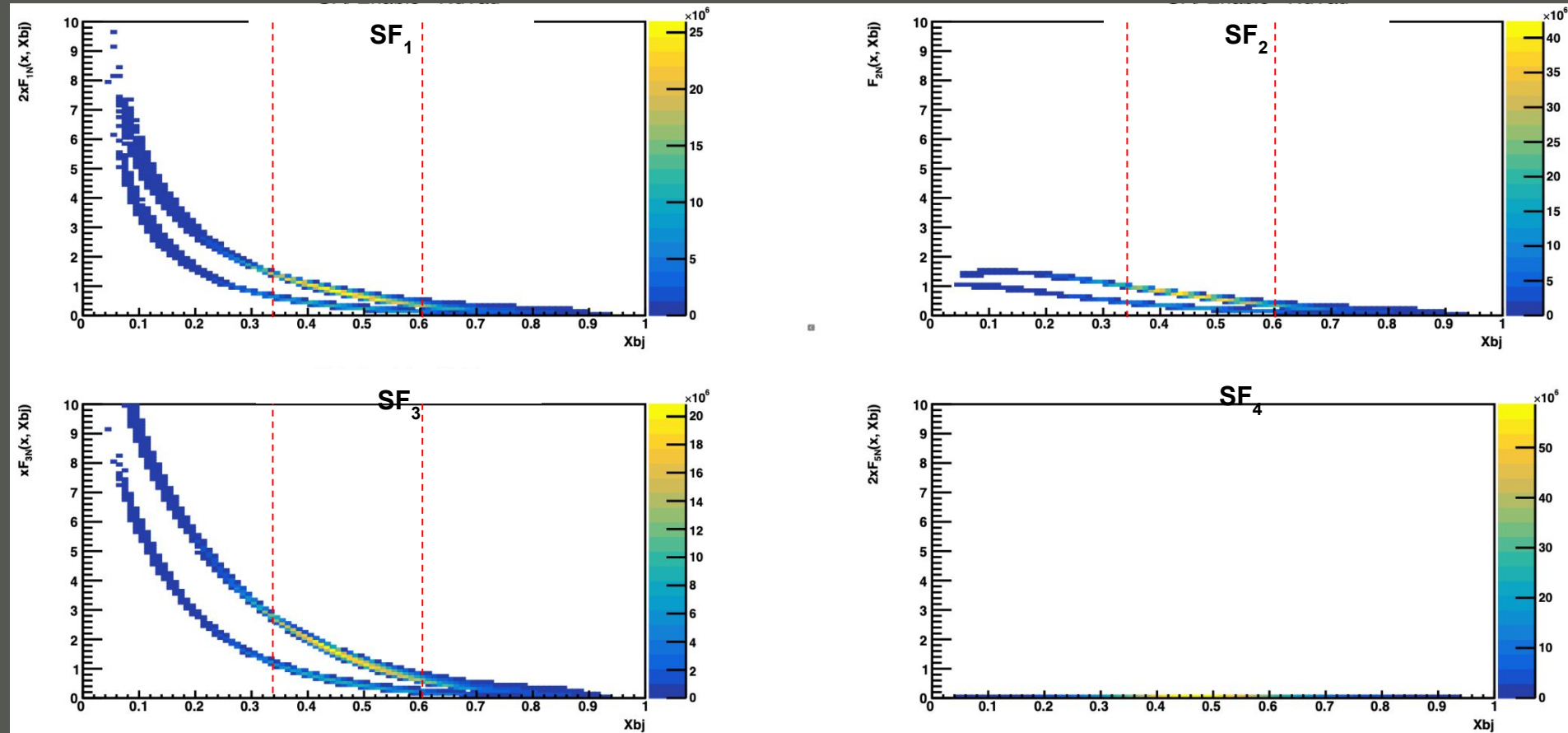
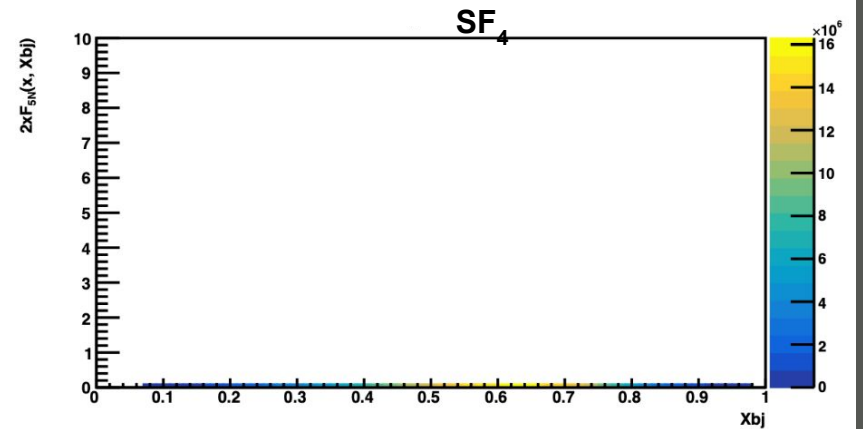
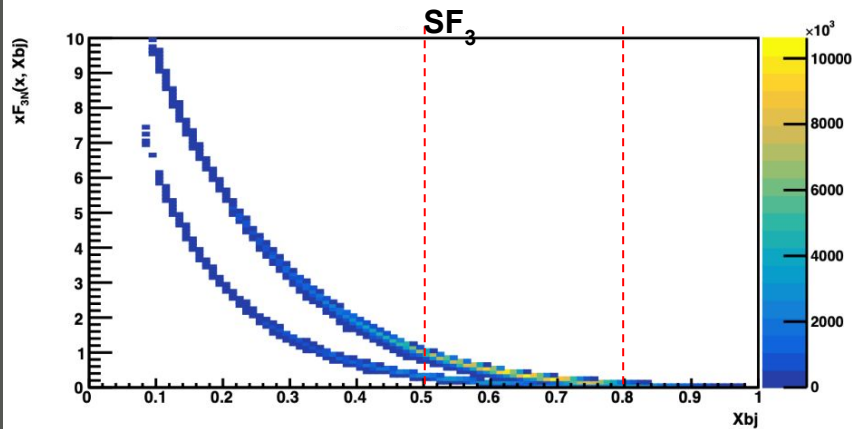
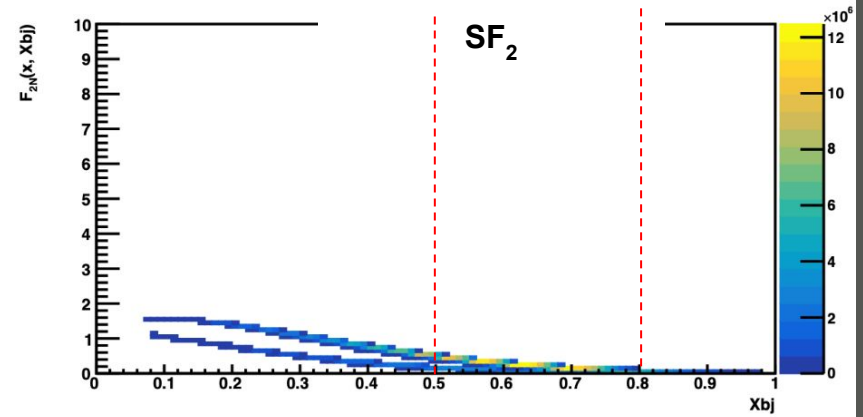
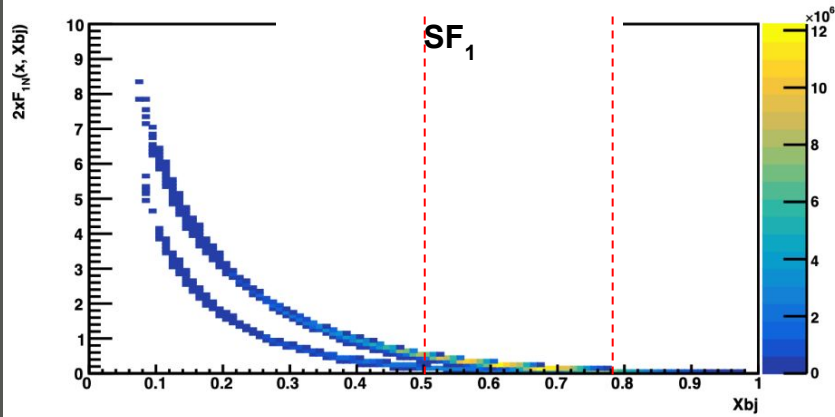
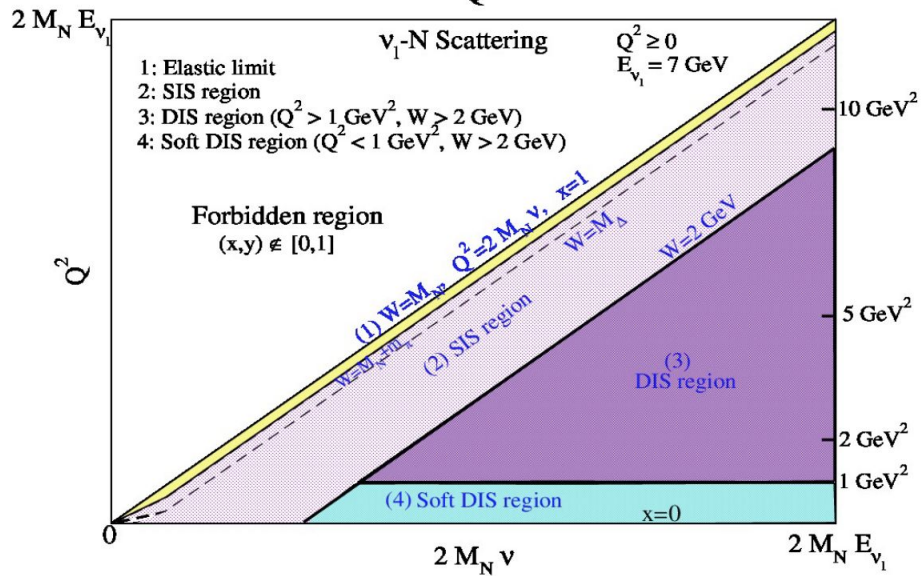
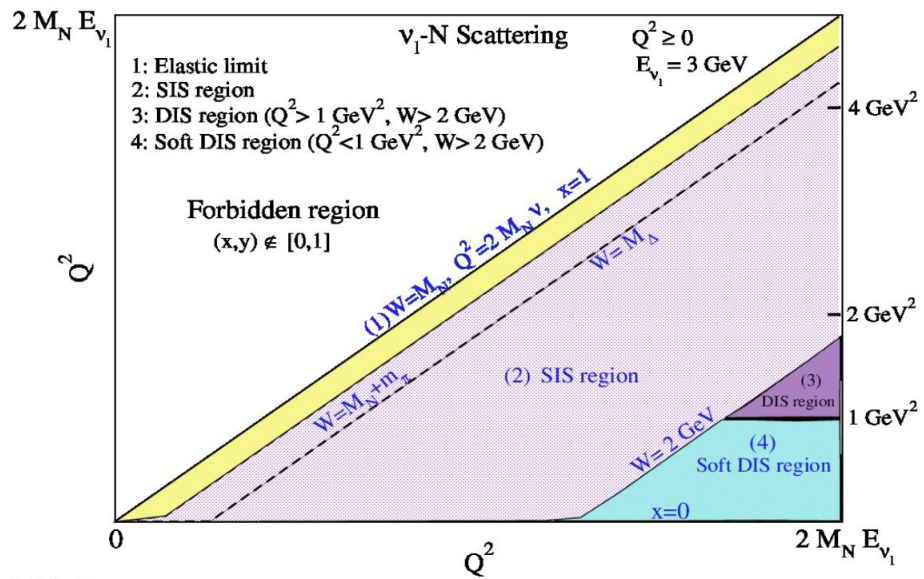


Figure 2. Schematic behaviour of $R_{F_2}^A(x, Q^2)$ as a function of x for a given fixed Q^2 .

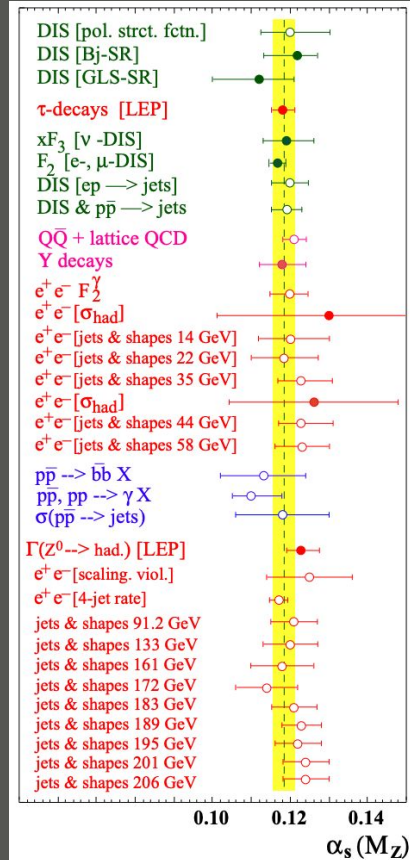
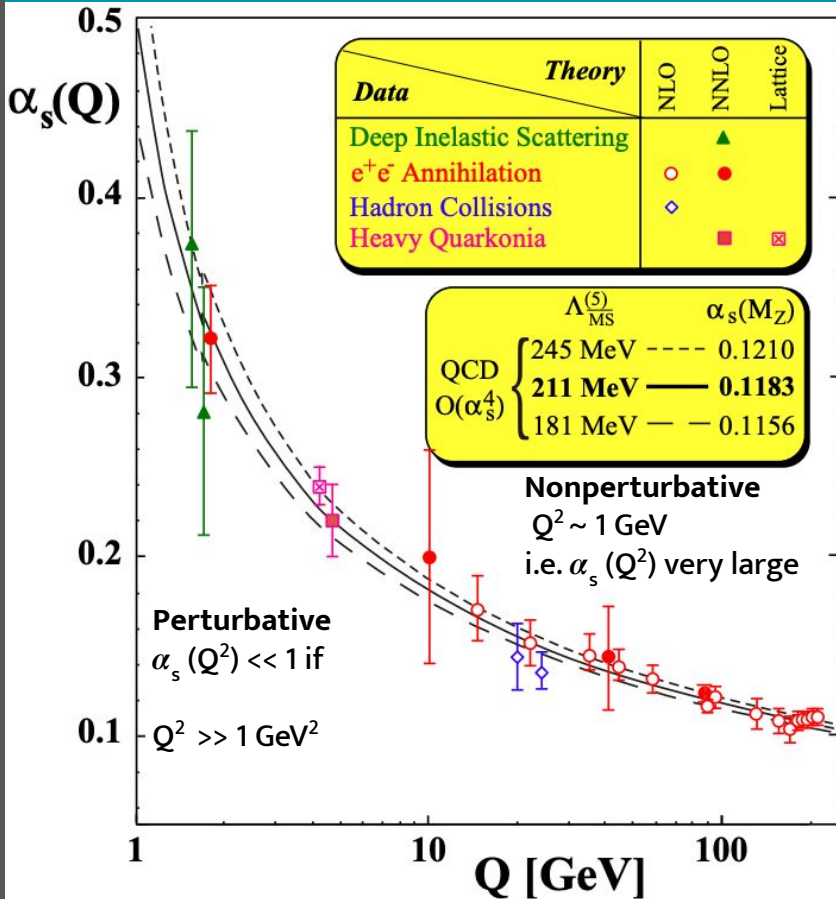






Asymptotic freedom makes it possible to calculate the small distance interaction for quarks and gluons, assuming that they are free particles.

The production of any particle can be determined by the cross section!



Bodek-Yang model aims for describing DIS cross section in all Q^2 regions
[arXiv:hep-ex/0308007](https://arxiv.org/abs/hep-ex/0308007)

DIS experiments extract information from the lepton scattering cross sections to measure **Structure Functions** of the target, which are directly related to the nonperturbative Parton Distribution Functions, PDFs.

Albright and Jarlskog, in Nucl. Phys. B 84, 467 (1975), pointed out that there are two additional **structure functions, F_4 and F_5** that contribute to the ν_τ XSec.

α_s 2002 by Siegfried Bethke (MPI of Physics, Munich, Germany)
[arXiv:hep-ex/0211012](https://arxiv.org/abs/hep-ex/0211012)