

# Neutrino Mass Models and Nonstandard Interactions

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# Products Developed with NTN Support

- ▶ Our group at OSU was supported by NTN jointly with Washington University group of Bhupal Dev in the first two years of NTN
- ▶ Funding helped travel exchange between OSU, WashU, and Fermilab

## Main Products:

1. K. S. Babu, P. S. B. Dev, S. Jana and A. Thapa, “Non-Standard Interactions in Radiative Neutrino Mass Models,” JHEP **03**, 006 (2020).
2. K. S. Babu, P. S. Dev, S. Jana and Y. Sui, “Zee-Burst: A New Probe of Neutrino Nonstandard Interactions at IceCube,” Phys. Rev. Lett. **124**, no.4, 041805 (2020).
3. K. S. Babu, G. Chauhan and P. S. Bhupal Dev, “Neutrino nonstandard interactions via light scalars in the Earth, Sun, supernovae, and the early Universe,” Phys. Rev. D **101**, no.9, 095029 (2020).
4. K. S. Babu, D. Gonçalves, S. Jana and P. A. N. Machado, “Neutrino Non-Standard Interactions: Complementarity Between LHC and Oscillation Experiments,” Phys. Lett. B **815**, 136131 (2021).
5. K. S. Babu, P. S. B. Dev, S. Jana and A. Thapa, “Unified framework for  $B$ -anomalies, muon  $g-2$  and neutrino masses,” JHEP **03**, 179 (2021).
6. K. S. Babu, S. Jana, M. Lindner and V. P. K, “Muon  $g-2$  anomaly and neutrino magnetic moments,” JHEP **10**, 240 (2021).
7. P. S. Bhupal Dev, K. S. Babu, P. B. Denton, P. A. N. Machado *et al.* “Neutrino Non-Standard Interactions: A Status Report,” SciPost Phys. Proc.2, 001 (2019).

# Students Involved in NTN Projects



Anil Thapa (OSU)  
Currently at UVA



Sudip Jana (OSU)  
Currently at MPI, Heidelberg



Vishnu P.K (OSU)  
Graduating next year



Garv Chauhan (WashU)  
Currently at UC Louvain, Belgium



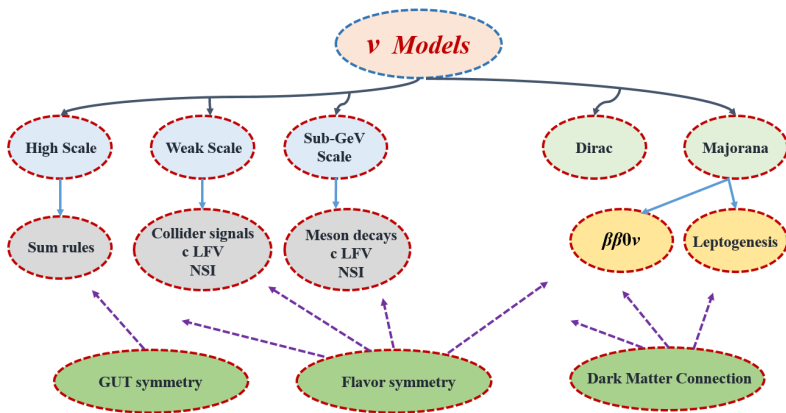
Yicong Sui (WashU)  
Currently in private sector

# Current knowledge of 3-neutrino oscillations

		Normal Ordering (best fit)		Inverted Ordering ( $\Delta\chi^2 = 7.1$ )	
		bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^\circ$	$33.44^{+0.77}_{-0.74}$	$31.27 \rightarrow 35.86$	$33.45^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.573^{+0.016}_{-0.020}$	$0.415 \rightarrow 0.616$	$0.575^{+0.016}_{-0.019}$	$0.419 \rightarrow 0.617$
	$\theta_{23}/^\circ$	$49.2^{+0.9}_{-1.2}$	$40.1 \rightarrow 51.7$	$49.3^{+0.9}_{-1.1}$	$40.3 \rightarrow 51.8$
	$\sin^2 \theta_{13}$	$0.02219^{+0.00062}_{-0.00063}$	$0.02032 \rightarrow 0.02410$	$0.02238^{+0.00063}_{-0.00062}$	$0.02052 \rightarrow 0.02428$
	$\theta_{13}/^\circ$	$8.57^{+0.12}_{-0.12}$	$8.20 \rightarrow 8.93$	$8.60^{+0.12}_{-0.12}$	$8.24 \rightarrow 8.96$
	$\delta_{\text{CP}}/^\circ$	$197^{+27}_{-24}$	$120 \rightarrow 369$	$282^{+26}_{-30}$	$193 \rightarrow 352$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.517^{+0.026}_{-0.028}$	$+2.435 \rightarrow +2.598$	$-2.498^{+0.028}_{-0.028}$	$-2.581 \rightarrow -2.414$

Esteban, Gonzalez-Garcia, Maltoni, Schwetz, Zhou (2020)

# Roadmap for Neutrino Models



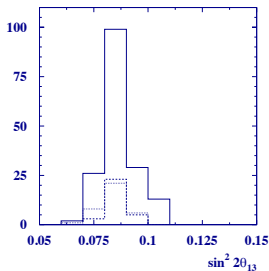
# Fit to all fermion masses and mixings

Observables (masses in GeV)	SUSY			non-SUSY		
	Input	Best Fit	Pull	Input	Best Fit	Pull
$m_u/10^{-3}$	0.502±0.155	0.515	0.08	0.442±0.149	0.462	0.13
$m_c$	0.245±0.007	0.246	0.14	0.238±0.007	0.239	0.18
$m_t$	90.28±0.89	90.26	-0.02	74.51±0.65	74.47	-0.05
$m_b/10^{-3}$	0.839±0.17	0.400	-2.61	1.14±0.22	0.542	-2.62
$m_s/10^{-3}$	16.62±0.90	16.53	-0.09	21.58±1.14	22.57	0.86
$m_b$	0.938±0.009	0.933	-0.55	0.994±0.009	0.995	0.19
$m_e/10^{-3}$	0.3440±0.0034	0.344	0.08	0.4707±0.0047	0.470	-0.03
$m_\mu/10^{-3}$	72.625±0.726	72.58	-0.05	99.365±0.993	99.12	-0.24
$m_\tau$	1.2403±0.0124	1.247	0.57	1.6892±0.0168	1.688	-0.05
$ V_{us} /10^{-2}$	22.54±0.07	22.54	0.02	22.54±0.06	22.54	0.06
$ V_{cb} /10^{-2}$	3.93±0.06	3.908	-0.42	4.856±0.06	4.863	0.13
$ V_{ub} /10^{-2}$	0.341±0.012	0.341	0.003	0.420±0.013	0.421	0.10
$\delta_{CKM}^\circ$	69.21±3.09	69.32	0.03	69.15±3.09	70.24	0.35
$\Delta m_{21}^2/10^{-5}(eV^2)$	8.982±0.25	8.972	-0.04	12.65±0.35	12.65	-0.01
$\Delta m_{31}^2/10^{-3}(eV^2)$	3.05±0.04	3.056	0.02	4.307±0.059	4.307	0.006
$\sin^2 \theta_{12}$	0.318±0.016	0.314	-0.19	0.318±0.016	0.316	-0.07
$\sin^2 \theta_{23}$	0.563±0.019	0.563	0.031	0.563±0.019	0.563	0.01
$\sin^2 \theta_{13}$	0.0221±0.0006	0.0221	-0.003	0.0221±0.0006	0.0220	-0.16
$\delta_{CP}^\circ$	224.1±33.3	240.1	0.48	224.1±33.3	225.1	0.03
$\chi^2$	-	-	7.98	-	-	7.96

Babu, Saad (2021)

# Minimal Yukawa sector of $SO(10)$

- ▶ 12 parameters plus 7 phases to fit  $13 + 5 = 18$  observed quantities
- ▶ This setup fits all observables quite well
- ▶ Large neutrino mixings coexist with small quark mixings
- ▶  $\theta_{13}$  prediction turned out to be correct



Babu, Mohapatra (1993); Bajc, Senjanovic, Vissani (2001); (2003); Fukuyama, Okada (2002); Goh, Mohapatra, Ng (2003); Bajc, Melfo, Senjanovic, Vissani (2004); Bertolini, Malinsky, Schwetz (2006); Babu, Macesanu (2005); Dutta, Mimura, Mohapatra (2007); Aulakh et al (2004); Bajc, Dorsner, Nemevsek (2009); Joshipura, Patel (2011); Dueck, Rodejohann (2013); Ohlsson, Penrow (2019); Babu, Bajc, Saad (2018); Babu, Saad (2021)

# Yukawa Sector of Minimal $SO(10)$

$$16 \times 16 = 10_s + 120_a + 126_s$$

- ▶ At least two Higgs fields needed for family mixing
- ▶ Symmetric  $10_H$  and  $\overline{126}$  is the minimal model

$$W_{SO(10)} = 16^T (Y_{10} 10_H + Y_{126} \overline{126}_H) 16 .$$

$$M_U = v_u^{10} Y_{10} + v_u^{126} Y_{126}$$

$$M_D = v_d^{10} Y_{10} + v_d^{126} Y_{126}$$

$$M_E = v_d^{10} Y_{10} - 3v_d^{126} Y_{126}$$

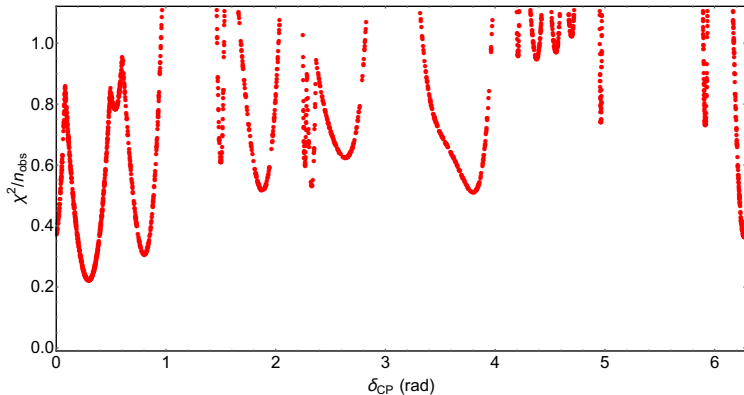
$$M_{\nu_D} = v_u^{10} Y_{10} - 3v_u^{126} Y_{126}$$

$$M_R = Y_{126} V_R$$



# Dirac CP phase

Multiple  $\chi^2$  minima make  $\delta_{CP}$  prediction difficult



Babu, Bajc, Saad (2018)

# Proton decay predictions

- ▶ Proton decay branching ratios determined by neutrino oscillation fits
- ▶ Mediated by superheavy gauge bosons
- ▶ Lifetime has large uncertainties,  $\tau_p \approx (10^{32} - 10^{36})$  yrs.

## Prediction of branching ratios

$$\Gamma(p \rightarrow \pi^0 e^+) \rightarrow 47\%$$

$$\Gamma(p \rightarrow \pi^0 \mu^+) \rightarrow 1\%$$

$$\Gamma(p \rightarrow \eta^0 e^+) \rightarrow 0.20\%$$

$$\Gamma(p \rightarrow \eta^0 \mu^+) \rightarrow 0.00\%$$

$$\Gamma(p \rightarrow K^0 e^+) \rightarrow 0.16\%$$

$$\Gamma(p \rightarrow K^0 \mu^+) \rightarrow 3.62\%$$

$$\Gamma(p \rightarrow \pi^+ \bar{\nu}) \rightarrow 48\%$$

$$\Gamma(p \rightarrow K^+ \bar{\nu}) \rightarrow 0.22\%$$

Nemesvek, Bajc, Dorsner (2009)

Babu, Khan (2015)

# Radiative neutrino mass generation

- ▶ An alternative to seesaw is radiative neutrino mass generation, where neutrino mass is absent at tree level, but arises via quantum loop corrections
- ▶ The smallness of neutrino mass is explained by loop and chiral suppressions
- ▶ Loop diagrams may arise at 1-loop, 2-loop or 3-loop levels
- ▶ New physics scale typically near TeV and thus accessible to LHC
- ▶ Further tests in observable LFV processes and as nonstandard neutrino interaction (NSI) in oscillations

# Effective $\Delta L = 2$ Operators

$$\begin{aligned}
 \mathcal{O}_1 &= L^i L^j H^k H^l \epsilon_{ik} \epsilon_{jl} \\
 \mathcal{O}_2 &= L^i L^j L^k e^c H^l \epsilon_{ij} \epsilon_{kl} \\
 \mathcal{O}_3 &= \{ L^i L^j Q^k d^c H^l \epsilon_{ij} \epsilon_{kl}, \quad L^i L^j Q^k d^c H^l \epsilon_{ik} \epsilon_{jl} \} \\
 \mathcal{O}_4 &= \{ L^i L^j \bar{Q}_i \bar{u}^c H^k \epsilon_{jk}, \quad L^i L^j \bar{Q}_k \bar{u}^c H^k \epsilon_{ij} \} \\
 \mathcal{O}_5 &= L^i L^j Q^k d^c H^l H^m \bar{H}_i \epsilon_{jl} \epsilon_{km} \\
 \mathcal{O}_6 &= L^i L^j \bar{Q}_k \bar{u}^c H^l H^k \bar{H}_i \epsilon_{jl} \\
 \mathcal{O}_7 &= L^i Q^j \bar{e}^c \bar{Q}_k H^k H^l H^m \epsilon_{il} \epsilon_{jm} \\
 \mathcal{O}_8 &= L^i \bar{e}^c \bar{u}^c d^c H^j \epsilon_{ij} \\
 \mathcal{O}_9 &= L^i L^j L^k e^c L^l e^c \epsilon_{ij} \epsilon_{kl} \\
 \mathcal{O}'_1 &= L^i L^j H^k H^l \epsilon_{ik} \epsilon_{jl} H^{*m} H_m
 \end{aligned}$$

Babu & Leung (2001)

de Gouvea & Jenkins (2008)

Angel & Volkas (2012)

Cai, Herrero-Garcia, Schmidt, Vicente, Volkas (2017)

Lehman (2014) – all  $d = 7$  operators

Li, Ren, Xiao, Yu, Zheng (2020); Liao, Ma (2020) – all  $d = 9$  operators

# Operator $\mathcal{O}_2$ and the Zee model

- Introduce a singly charged scalar and a second Higgs doublet to standard model:

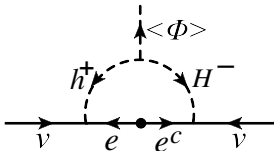
$$\mathcal{L} = f_{ij} L_i^a L_j^b h^+ \epsilon_{ab} + \mu H^a \Phi^b h^- \epsilon_{ab} + \text{h.c.}$$

$\Downarrow$

$$\mathcal{O}_2 = L^i L^j L^k e^c H^l \epsilon_{ij} \epsilon_{kl}$$

Zee (1980)

- Neutrino mass arises at one-loop.



- A minimal version of this model in which only one Higgs doublet couples to a given fermion sector with a  $Z_2$  symmetry yields: Wolfenstein (1980)

$$m_\nu = \begin{pmatrix} 0 & m_{e\mu} & m_{e\tau} \\ m_{e\mu} & 0 & m_{\mu\tau} \\ m_{e\tau} & m_{\mu\tau} & 0 \end{pmatrix}, \quad m_{ij} \simeq \frac{f_{ij}}{16\pi^2} \frac{(m_i^2 - m_j^2)}{\Lambda}$$

It requires  $\theta_{12} \simeq \pi/4 \rightarrow$  ruled out by solar + KamLAND data.

Koide (2001); Frampton *et al.* (2002); He (2004)

# Neutrino oscillations in the Zee model

- ▶ Neutrino oscillation data can be fit to the Zee model consistently without the  $Z_2$  symmetry
- ▶ Some benchmark points for Yukawa couplings of second doublet:

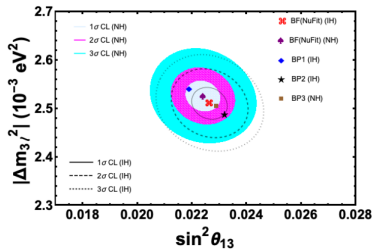
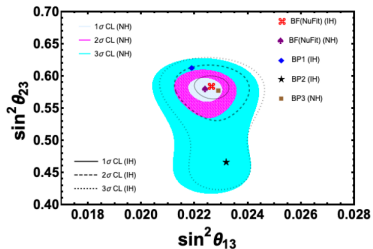
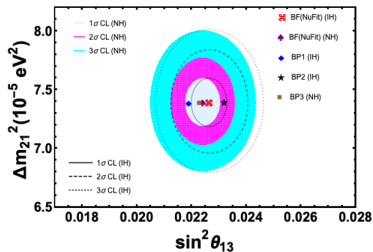
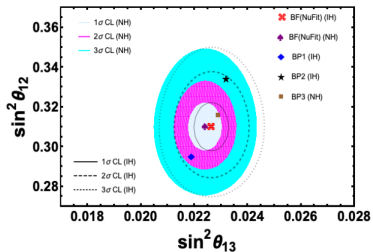
$$\text{BP I: } Y = \begin{pmatrix} Y_{ee} & 0 & Y_{e\tau} \\ 0 & Y_{\mu\mu} & Y_{\mu\tau} \\ 0 & Y_{\tau\mu} & Y_{\tau\tau} \end{pmatrix}$$

$$\text{BP II: } Y = \begin{pmatrix} 0 & Y_{e\mu} & Y_{e\tau} \\ Y_{\mu e} & 0 & Y_{\mu\tau} \\ 0 & Y_{\tau\mu} & Y_{\tau\tau} \end{pmatrix}$$

$$\text{BP III: } Y = \begin{pmatrix} Y_{ee} & 0 & Y_{e\tau} \\ 0 & Y_{\mu\mu} & Y_{\mu\tau} \\ Y_{\tau e} & 0 & Y_{\tau\tau} \end{pmatrix}$$

Babu, Dev, Jana, Thapa (2019)

# Neutrino fit in the Zee model



Babu, Dev, Jana, Thapa (2019)

# Neutrino Non-Standard Interactions (NSI)

- ▶ Neutrino oscillation picture would change if there are non-standard interactions
- ▶ Modification of matter effects most important
- ▶ EFT for neutrino NSI:

$$\mathcal{L}_{\text{NSI}}^{\text{NC}} = -2\sqrt{2}G_F \sum_{f, X, \alpha, \beta} \varepsilon_{\alpha\beta}^{fX} (\bar{\nu}_\alpha \gamma^\mu P_L \nu_\beta) (\bar{f} \gamma_\mu P_X f) ,$$

$$\mathcal{L}_{\text{NSI}}^{\text{CC}} = -2\sqrt{2}G_F \sum_{f, f', X, \alpha, \beta} \varepsilon_{\alpha\beta}^{ff'X} (\bar{\nu}_\alpha \gamma^\mu P_L \ell_\beta) (\bar{f}' \gamma_\mu P_X f)$$

Wolfenstein (1978)

- ▶ Effective Hamiltonian for neutrino propagation in matter is now:

$$H = \frac{1}{2E} U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger + \sqrt{2}G_F N_e(x) \begin{pmatrix} 1 + \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}$$

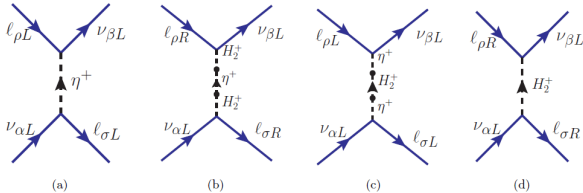
- ▶  $\varepsilon_{\alpha\beta}$  measure of NSI normalized to weak interaction strength

See next talk by Bhupal Dev



# Neutrino NSI in the Zee model

- The two charged scalars of the Zee model mediate NSI



- The NSI parameters are given by:

$$\varepsilon_{\alpha\beta} = \frac{1}{4\sqrt{2}G_F} Y_{\alpha e} Y_{\beta e}^* \left( \frac{\sin^2 \varphi}{m_{h^+}^2} + \frac{\cos^2 \varphi}{m_{H^+}^2} \right)$$

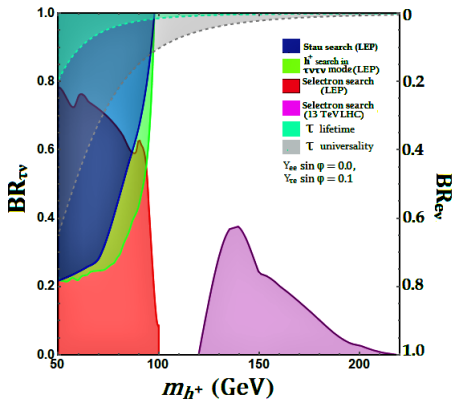
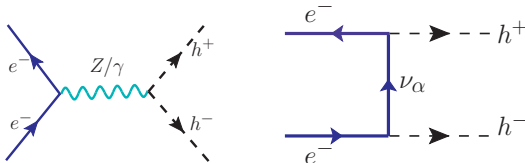
- Constrained by LHC and LEP direct limits; cLFV; precision electroweak tests; neutrino oscillation data; and theory

Babu, Dev, Jana, Thapa (2019)

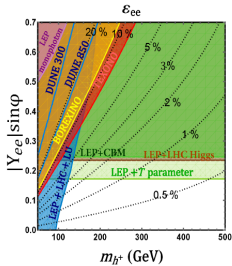
# Constraints on Zee model parameters

- ▶ Electroweak  $T$  parameter sets limits on mixing  $\sin \varphi$
- ▶  $\mu \rightarrow e + \gamma$  type processes limit products of couplings
- ▶  $\mu \rightarrow 3e$  type processes lead to further constraints
- ▶  $\tau$  lifetime and universality constraints
- ▶ Lepton universality in  $W^\pm$  decays
- ▶ Theoretical constraint from avoiding charge breaking minima
- ▶ LEP direct search limits on charged scalars
- ▶ Constraints from LHC searches
- ▶ Higgs precision physics limits

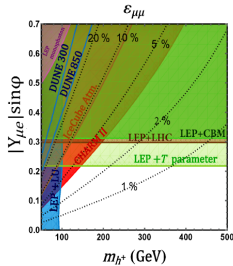
# LEP and LHC constraints on Charged Scalar



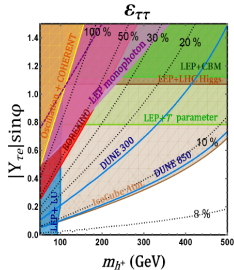
# Diagonal NSI in Zee model



(a)



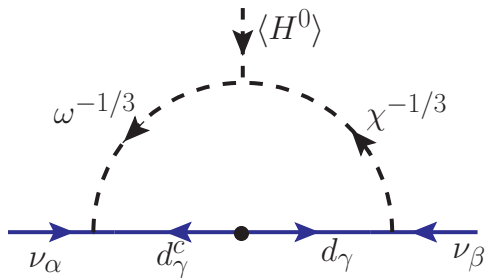
(b)



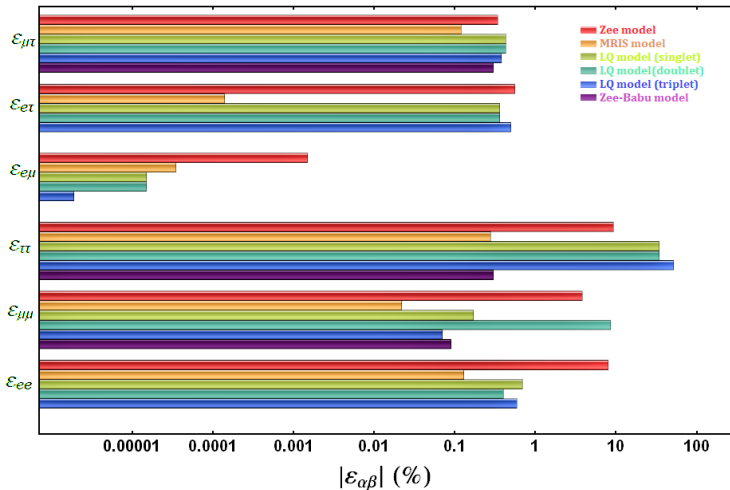
Babu, Dev, Jana, Thapa (2019)

# Leptoquark models of radiative neutrino mass

- ▶ Charged lepton in Zee diagram may be replaced by quarks
- ▶ Charged scalars will then be replaced by Leptoquark scalars
- ▶ Several such models exist in literature
- ▶ More interest in context of  $B$  meson decay anomalies



# Summary of NSI in radiative models

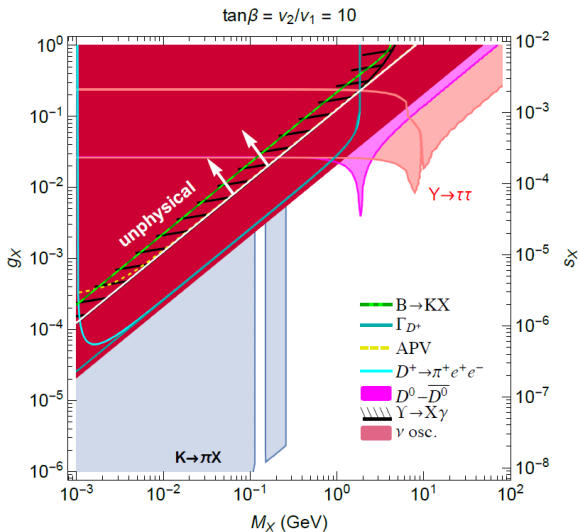


Babu, Dev, Jana, Thapa (2019)

# Neutrino Mass Models with Light Mediators

- ▶ If the mediator generating  $(\bar{\nu}_\alpha \gamma_\mu \nu_\beta)(\bar{f} \gamma^\mu f)$  interactions is light, the severe charged lepton flavor violation constraints may be evaded
- ▶ Gauging  $(B - L)$  for the third family is an explicit example of this  
Babu, Friedland, Machado, Mocioiu (2017)
- ▶ The model has  $\nu_R$  fields, a second Higgs doublet  $\phi_2$  and a singlet  $s$ , both with  $(B - L)$  charge of  $1/3$
- ▶  $\phi_2$  generates quark mixings; charged leptons remain unmixed  $\Rightarrow$  No flavor violation in charged leptons
- ▶ If mass of the new gauge boson  $X$  is of order 100 MeV, with the gauge coupling  $g_X \sim 10^{-3}$  all constraints are satisfied
- ▶ This explicit model generates  $\epsilon_{\tau\tau} \sim 0.5$
- ▶  $\nu_3^c$  is light and may serve as the sterile neutrino relevant for short baseline anomalies  
Babu, Friedland, Mocioiu, Machado (to appear)

# $(B - L)_3$ Model Constraints



Babu, Friedland, Machado, Mocioiu (2017)



# Other Models with large NSI

- ▶ Several models have been proposed to generate observable NSI
- ▶ Main challenge is to control charged lepton flavor violation and universality constraints
- ▶ Some models use cancellations among  $d = 6$  and  $d = 8$  operators  
Gavela, Hernandez, Ota, Winter (2009)
- ▶ Light mediators help with satisfying such constraints Farzan, Shoemaker (2016); Farzan (2016); Denton, Farzan, Shoemaker (2018)
- ▶ Collider signals of these models have been studied, especailly for monojet signals Friedland, Graesser, Shoemaker (2012); Elahi, Martin (2019); Babu, Goncalves, Jana, Machado (2021)

# Naturally Light Dirac Neutrinos from Left-Right Symmetry

- ▶ In a “universal seesaw” version of left-right symmetry, neutrinos are naturally Dirac particles
- ▶ These models provide understanding of Parity violation; some understanding of smallness of Yukawa couplings; requires right-handed neutrinos to exist; can provide a solution to the strong CP problem via Parity

Davidson, Wali (1987); Babu, He (1989); Babu, Mohapatra (1990); Craig, Garcia Garcia, Koszegi, McCune (2020)

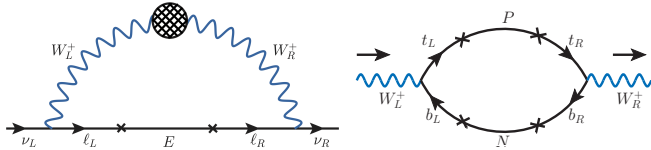
- ▶ Higgs sector is very simple; new vector-like singlet fermions ( $U, D, E$ ) generate charged fermion masses via a seesaw:

$$M_F = \begin{pmatrix} 0 & Y_{\kappa_L} \\ Y_{\kappa_R}^\dagger & M \end{pmatrix} \Rightarrow m_f = \frac{Y^2 \kappa_L \kappa_R}{M}$$

- ▶ There is no seesaw for neutrinos, since there is no corresponding singlet fermion
- ▶ Dirac neutrino masses arise via two-loop diagrams

# Two-loop Dirac Neutrino Masses

- $W_L^+ - W_R^+$  mixing is absent at tree-level in model



- Oscillation data fits well within the model Babu, He, Su, Thapa (2022)

Oscillation parameters	$3\sigma$ range NuFit5.1	Model prediction			
		BP I (NH)	BP II (NH)	BP III (IH)	BP IV (IH)
$\Delta m_{21}^2 (10^{-5} \text{ eV}^2)$	6.82 - 8.04	7.42	7.32	7.35	7.30
$\Delta m_{23}^2 (10^{-3} \text{ eV}^2) (\text{IH})$	2.410 - 2.574	-	-	2.48	2.52
$\Delta m_{31}^2 (10^{-3} \text{ eV}^2) (\text{NH})$	2.43 - 2.593	2.49	2.46	-	-
$\sin^2 \theta_{12}$	0.269 - 0.343	0.324	0.315	0.303	0.321
$\sin^2 \theta_{23} (\text{IH})$	0.410 - 0.613	-	-	0.542	0.475
$\sin^2 \theta_{23} (\text{NH})$	0.408 - 0.603	0.491	0.452	-	-
$\sin^2 \theta_{13} (\text{IH})$	0.02055 - 0.02457	-	-	0.0230	0.0234
$\sin^2 \theta_{13} (\text{NH})$	0.02060 - 0.02435	0.0234	0.0223	-	-
$\delta_{\text{CP}} (\text{IH})$	192 - 361	-	-	$271^\circ$	$296^\circ$
$\delta_{\text{CP}} (\text{NH})$	105 - 405	$199^\circ$	$200^\circ$	-	-
$m_{\text{light}} (10^{-3}) \text{ eV}$		0.66	0.17	0.078	4.95
$M_{E1}/M_{WR}$		917	321.3	639	3595
$M_{E2}/M_{WR}$		0.650	19.3	1.54	5.03
$M_{E3}/M_{WR}$		0.019	1.26	0.054	2.94

# Tests with $N_{\text{eff}}$ in Cosmology

- Dirac neutrino models of this type will modify  $N_{\text{eff}}$  by about 0.14

$$\Delta N_{\text{eff}} \simeq 0.027 \left( \frac{106.75}{g_*(T_{\text{dec}})} \right)^{4/3} g_{\text{eff}}$$

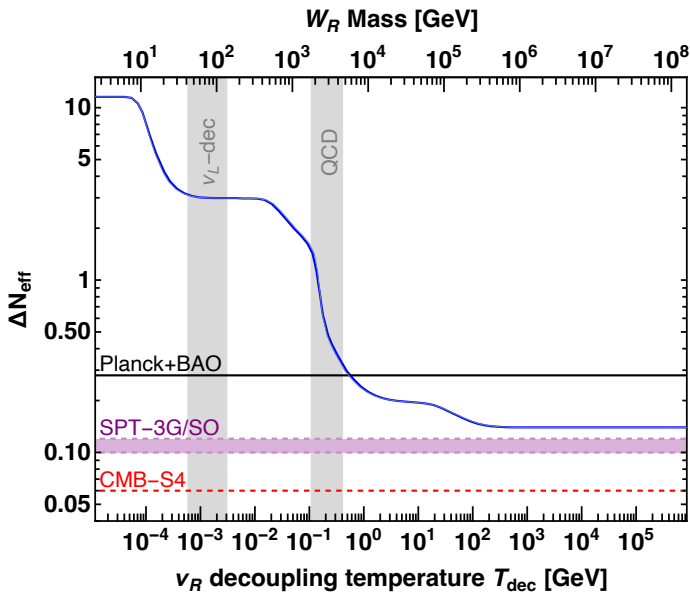
$$g_{\text{eff}} = (7/8) \times (2) \times (3) = 21/4$$

- Can be tested in CMB measurements:  $N_{\text{eff}} = 2.99 \pm 0.17$  (Planck+BAO)

$$G_F^2 \left( \frac{M_{W_L}}{M_{W_R}} \right)^4 T_{\text{dec}}^5 \approx \sqrt{g^*(T_{\text{dec}})} \frac{T_{\text{dec}}^2}{M_{\text{Pl}}}$$

$$T_{\text{dec}} \simeq 400 \text{ MeV} \left( \frac{g_*(T_{\text{dec}})}{70} \right)^{1/6} \left( \frac{M_{W_R}}{5 \text{ TeV}} \right)^{4/3}$$

- Present data sets a lower limit of 7 TeV on  $W_R$  mass



# Conclusions

- ▶ The scale of neutrino mass generation can be of order GUT scale, weak scale, or sub-GeV scale
- ▶ Grand Unification provides powerful tools to interconnect neutrino sector with quark sector
- ▶ Various  $d = 7$  and  $d = 9$  lepton number violating EFT operators can lead to interesting neutrino mass models.
- ▶ These models may be realized near the TeV scale, with potential signals for NSI, cFLV and direct detection at colliders
- ▶ Neutrino may very well be Dirac particles; interesting models of Dirac neutrino exist.  $\Delta N_{\text{eff}}$  in cosmology could test this scenario

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