

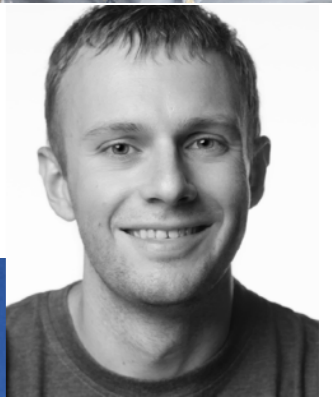
New Constraints on New Explanations of the MiniBooNE anomaly

Based on: 1812.08768, 2105.06470,
2109.03831, 2205.12273, 2206.07100

Austin Schneider



Starring:



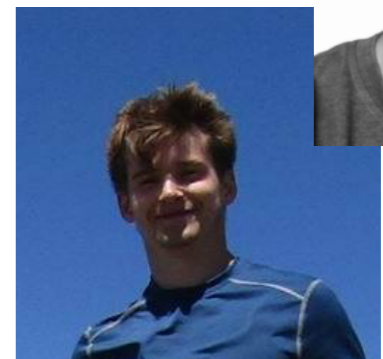
Stephano
Vergani



Matheus Hostert



Nicolo Foppiani



Nicholas Kamp

Neutrino Theory Network Workshop
Illinois, June 22, 2022

Carlos Argüelles



HARVARD
UNIVERSITY



Alfred P. Sloan
FOUNDATION

Outline

- Why go beyond vanilla sterile neutrinos?
- The garden of forking paths
- Focusing on two explanations:
 - Only Di-electron
 - Single photon + oscillations
- Future

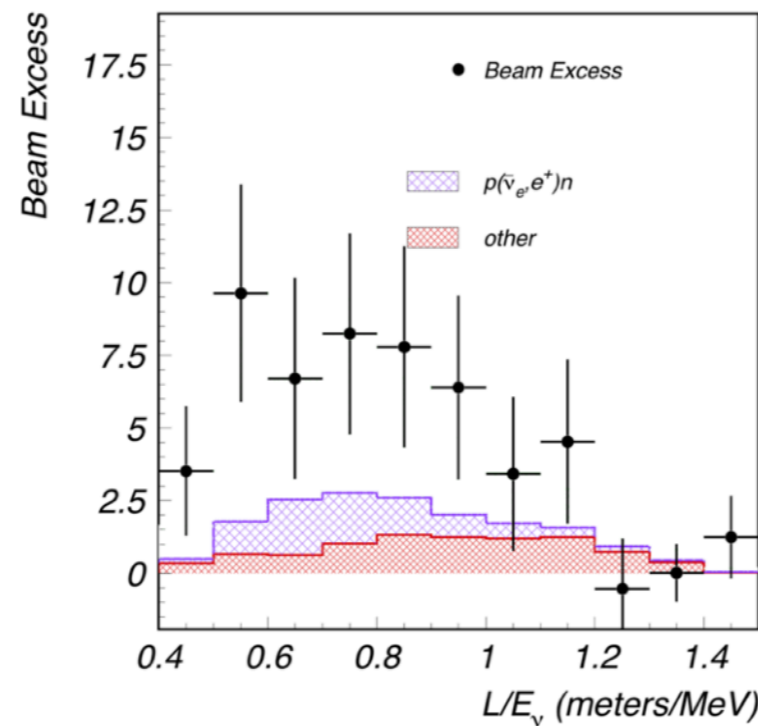
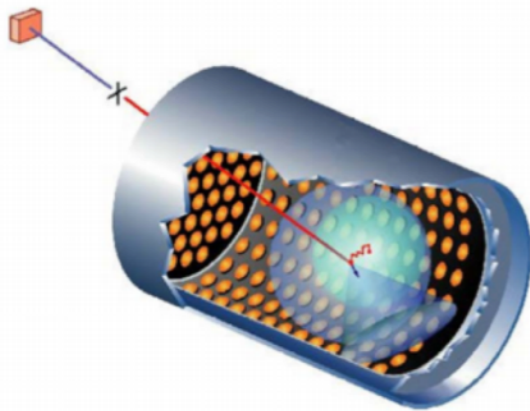
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The pieces that do not fit: short-baseline anomalies

LSND

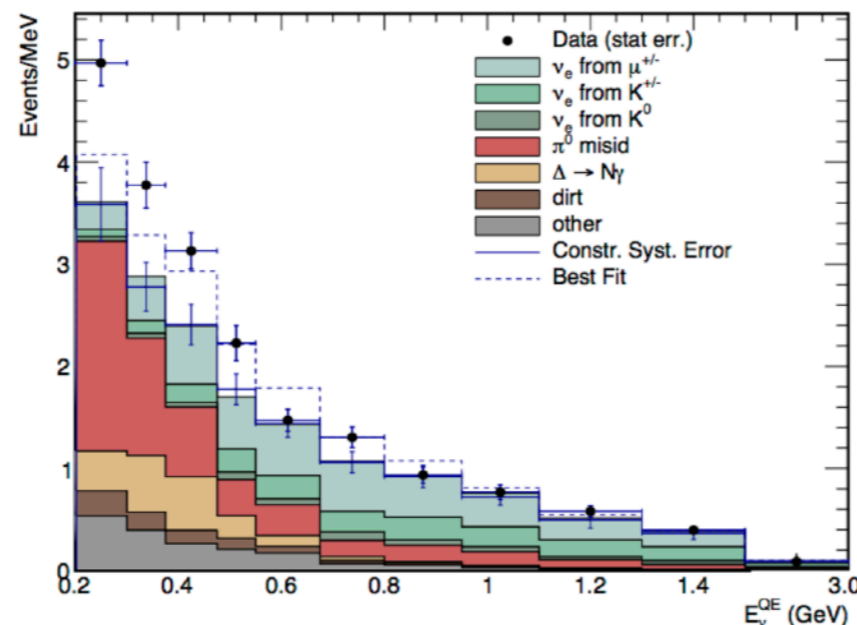
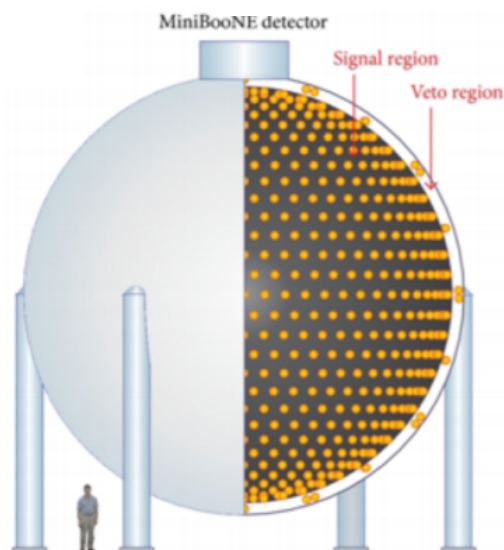
(3.8 σ !)



These experiments observe ν_e appearance at $L/E \sim 1$ km/GeV!

MiniBooNE

(4.8 σ !)



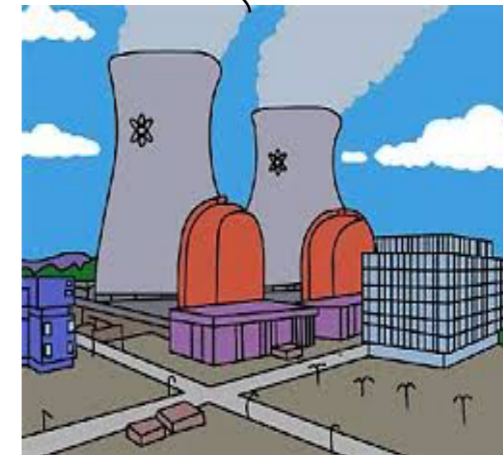
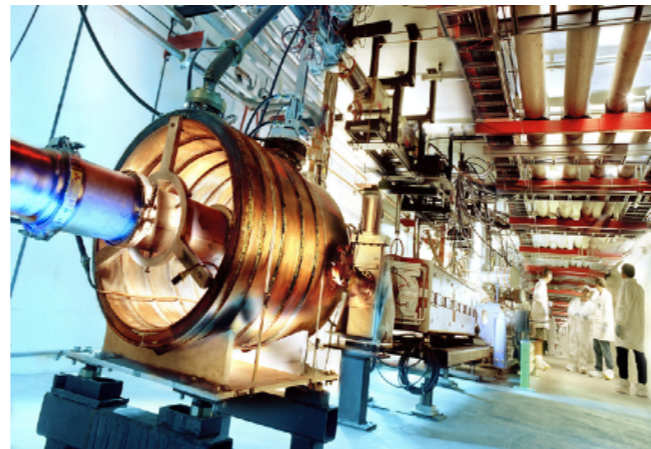
This points to
 $\Delta m^2 \sim 1 \text{ eV}^2$

These are not alone, other interesting observations

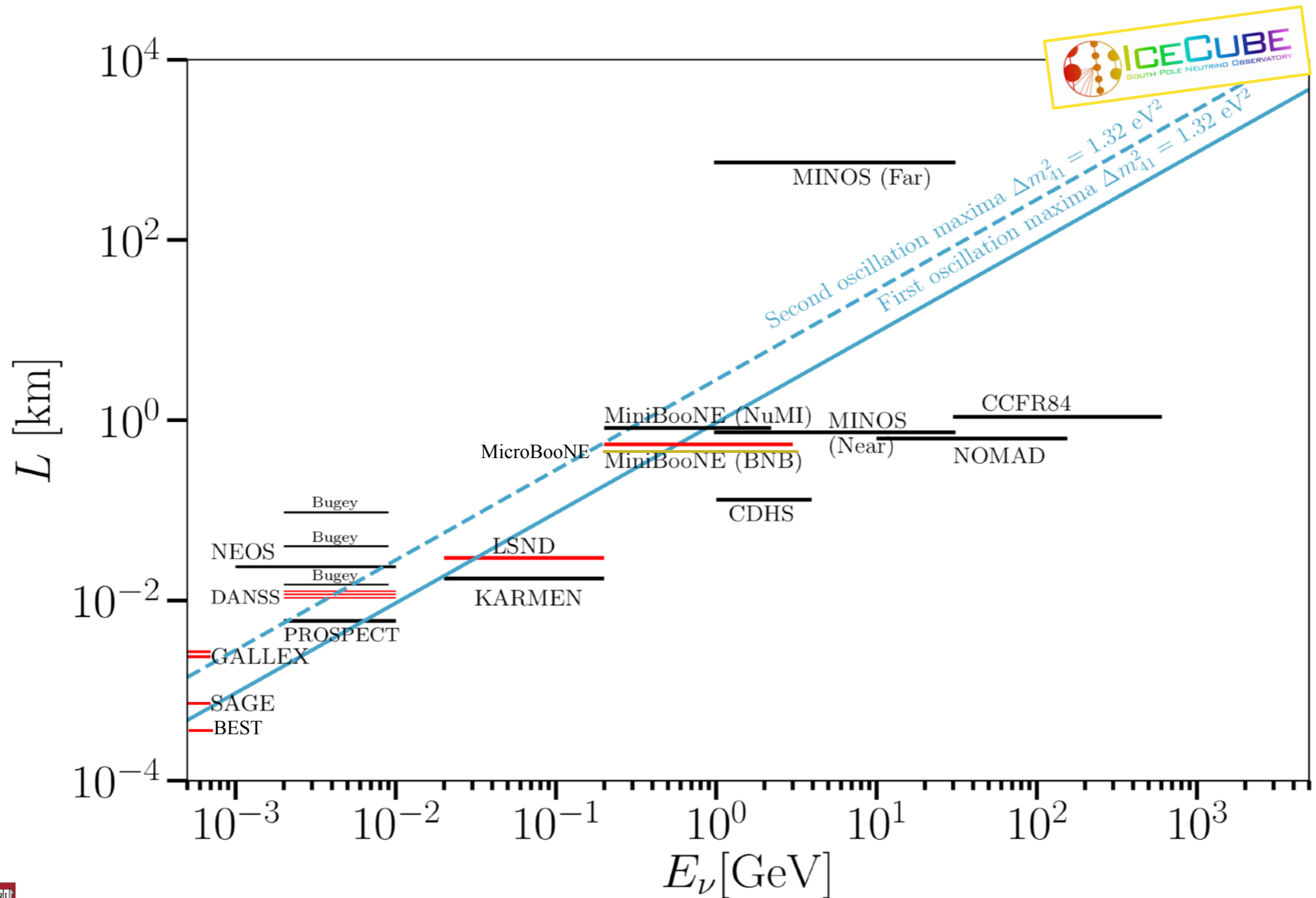
	$\nu_\mu \rightarrow \nu_e$	$\nu_\mu \rightarrow \nu_\mu$	$\nu_e \rightarrow \nu_e$
Neutrino	MiniBooNE (BNB) *	SciBooNE/MiniBooNE CCFR CDHS MINOS IceCube	KARMEN/LSND Cross Section
	MiniBooNE(NuMI) NOMAD		Gallium *
	MicroBooNE (BNB) (*?)		BEST *
Antineutrino	LSND *	SciBooNE/MiniBooNE CCFR MINOS IceCube (*?)	Bugey Daya Bay NEOS PROSPECT DANSS STEREO Neutrino-4 *
	KARMEN		
	MiniBooNE (BNB) *		

* $\Rightarrow >2\sigma$ "signal"

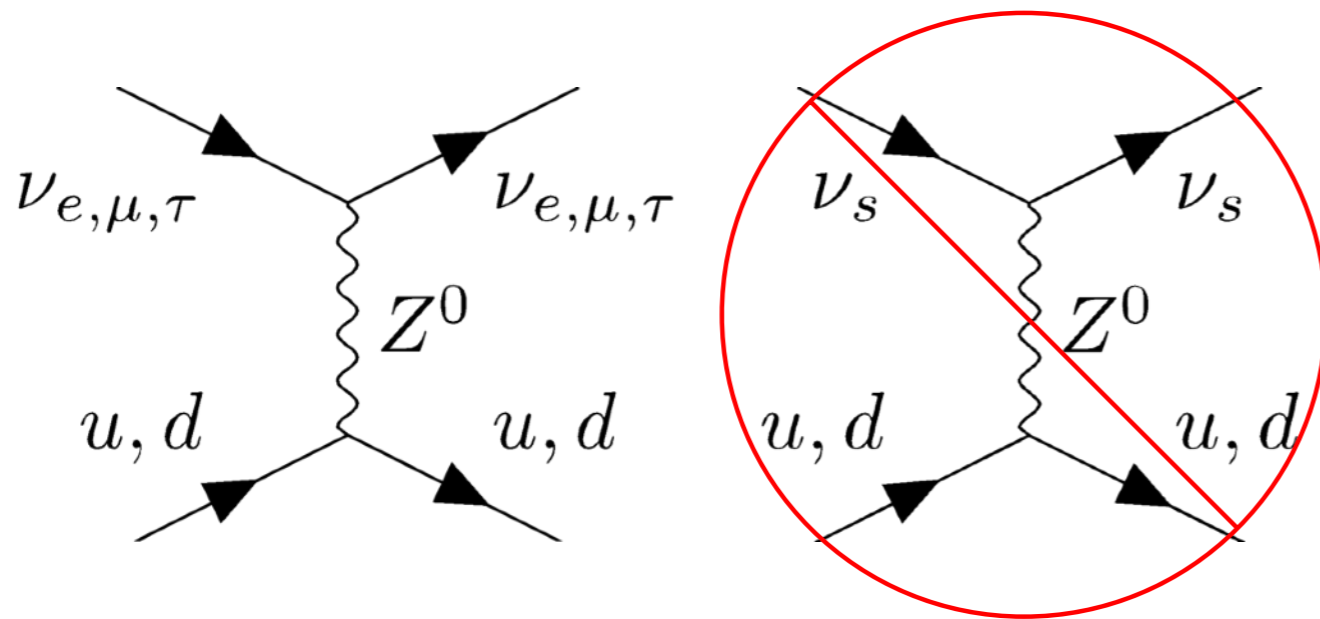
* \Rightarrow unclear "signal"



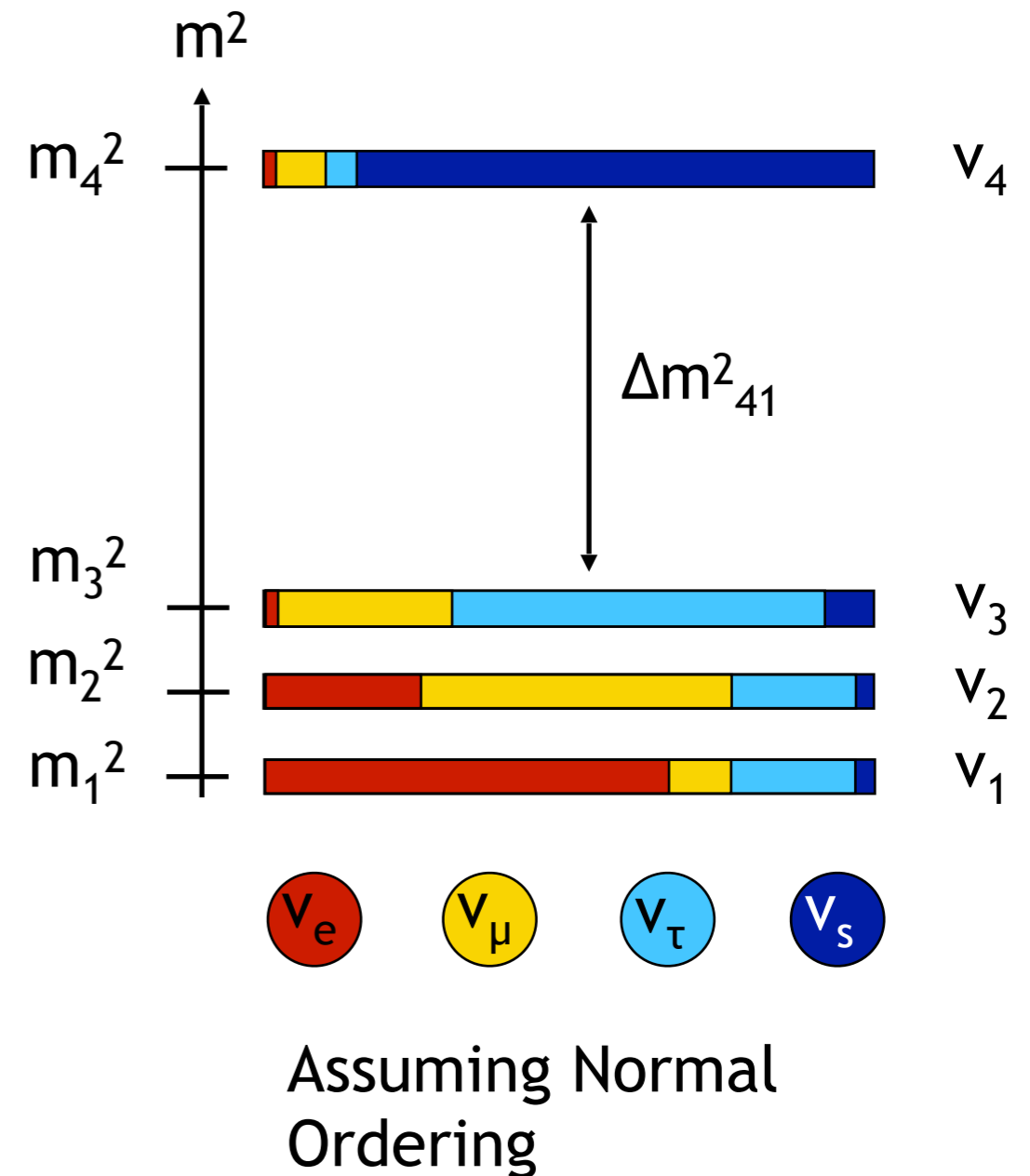
The anomalies lie ~ in a line



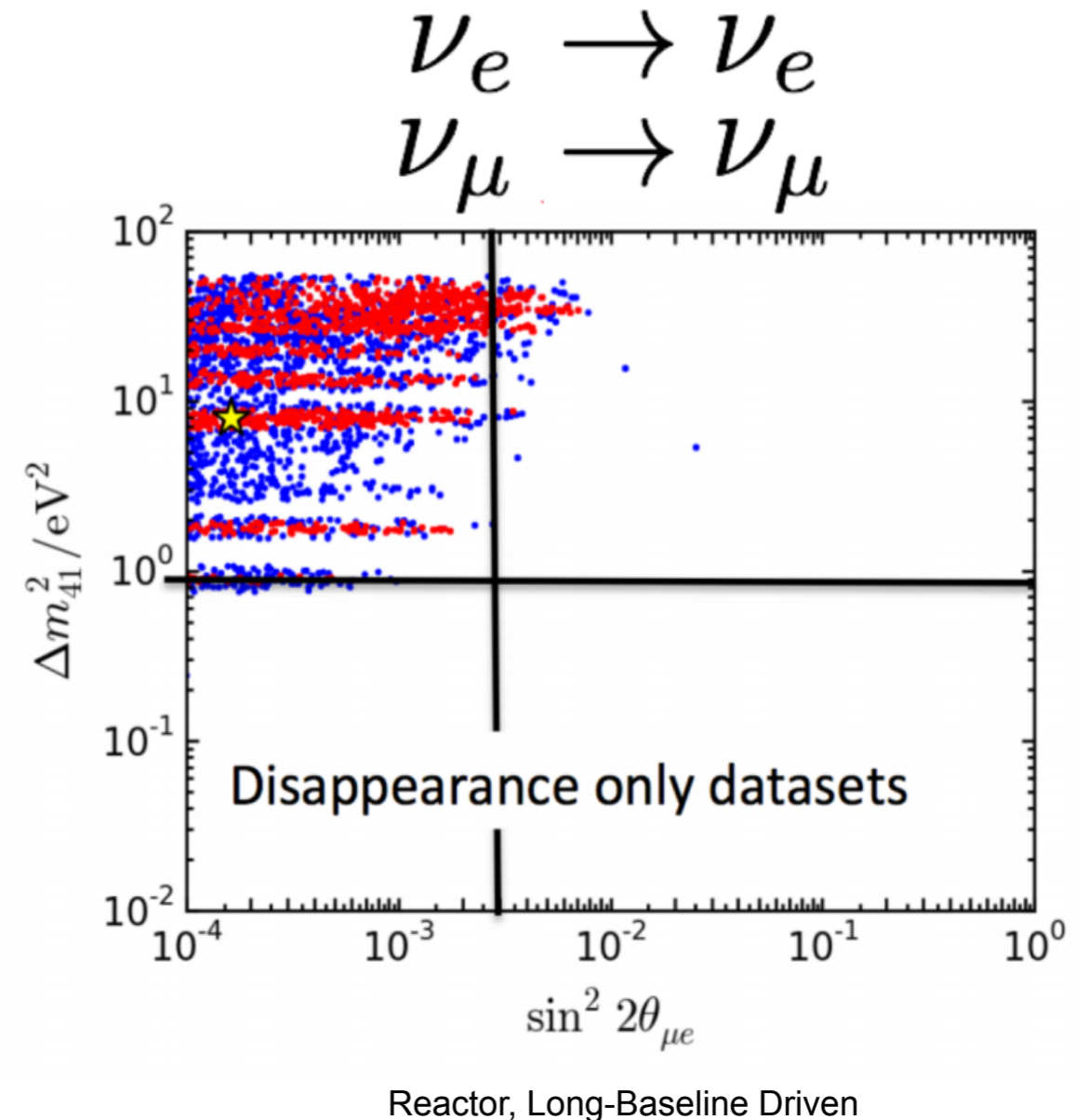
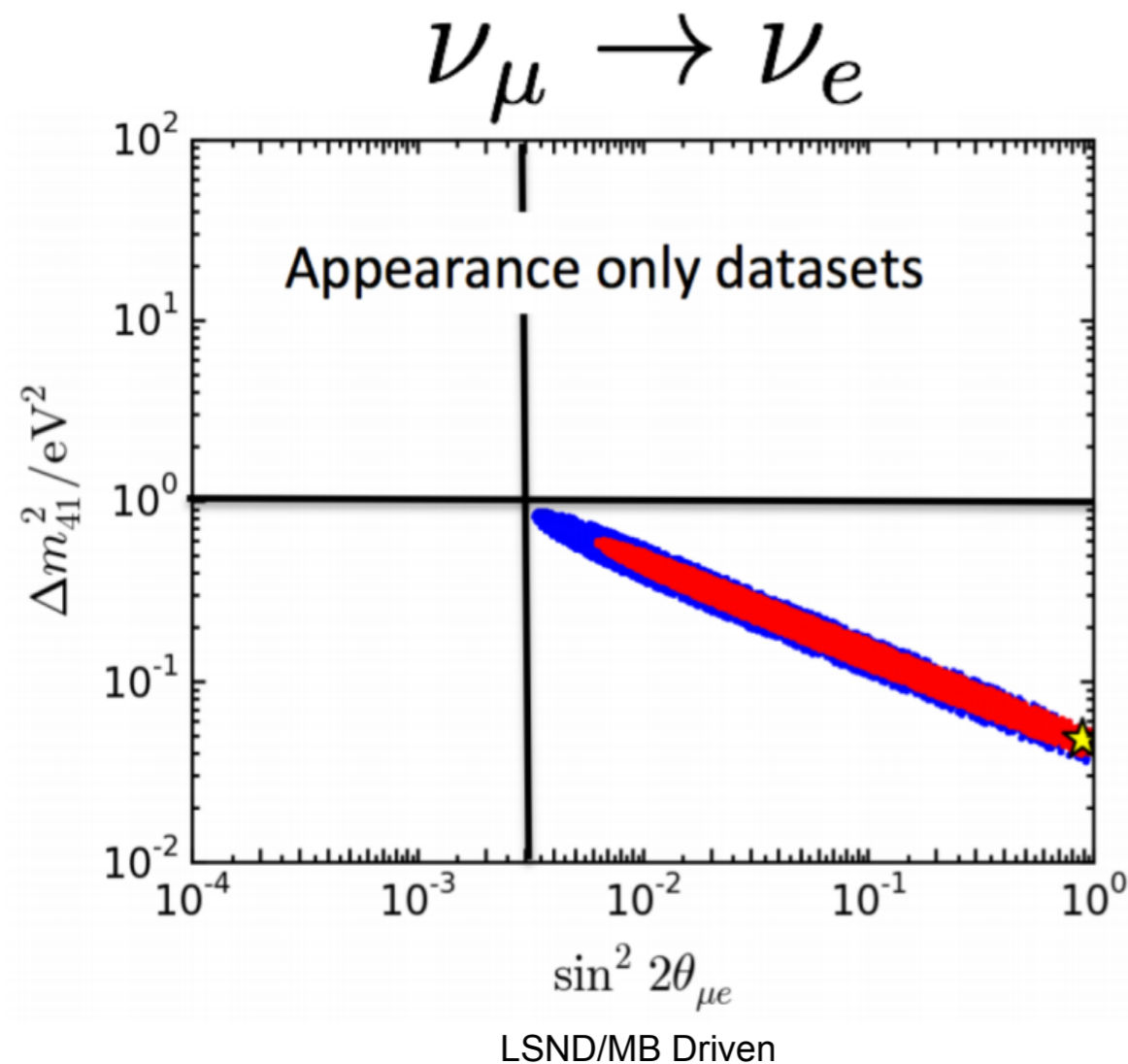
Introducing a sterile neutrino



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4 \end{pmatrix}$$

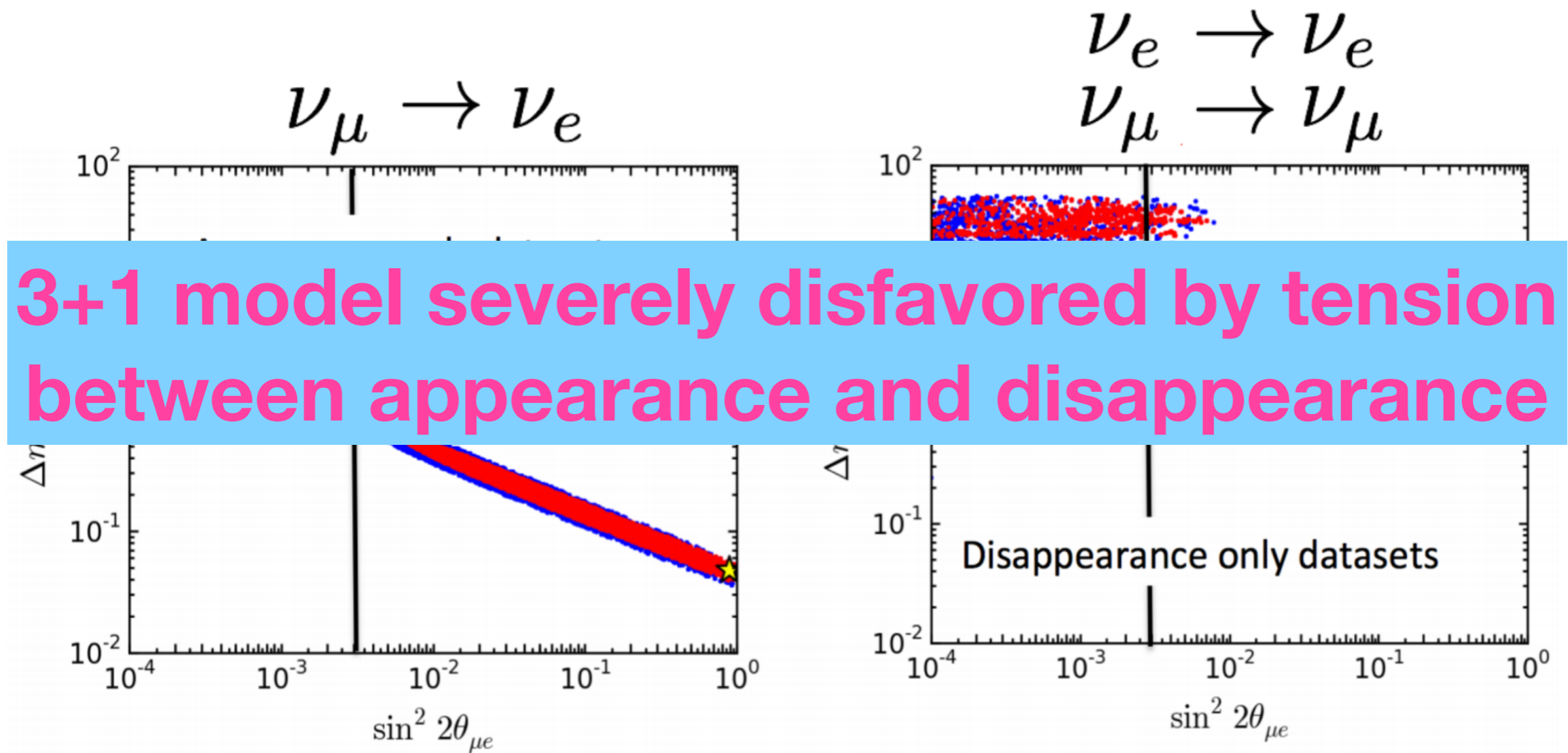


Appearance and disappearance “preference regions” don’t overlap!



From Collin et al. 1602.00671, similar conclusions from other groups see Gariazzo et al. 1703.00860, and Dentler et al JHEP 1808 (2018). See Diaz et al. arXiv:1906.00045 for more discussion.

Appearance and disappearance “preference regions” don’t overlap!



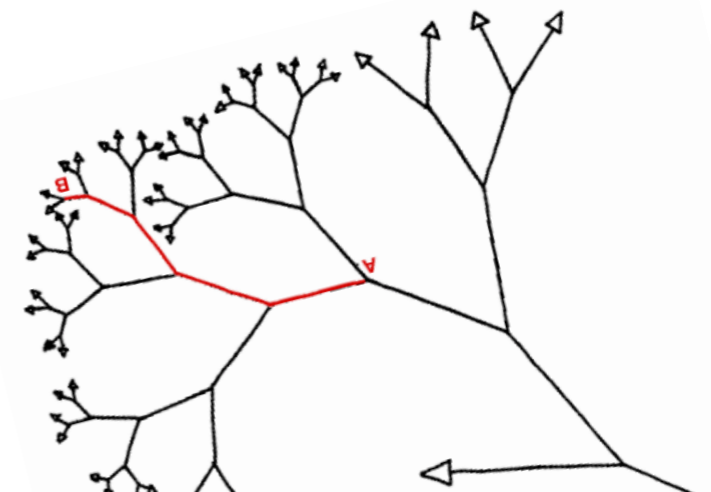
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From here: The Garden of Forking Paths*

- Do we understand all SM background/process well enough?
- Do we understand how neutrino oscillations work?
- Are all the anomalies (MB, LSND, reactors) related? Or only some of them?
- Since null results are not scrutinized as carefully as anomalous ones
- Why is there a very significant signal for ν_e disappearance in sources, but not in reactors?
- How do we interpret MicroBooNE data? Electron-neutrino disappearance? Nothing?
- Is IceCube seeing hints of the missing muon-neutrino disappearance?
- If the anomalies are confirmed as new physics, in what theories are they embedded?



*Garden of Forking Paths is spy/mystery short story by Jorge Luis Borges

Stepping back: What do we know?

- LSND saw an excess of electron-antineutrino events.
- MiniBooNE saw an excess of electron-like events in neutrino and antineutrino modes.
- MicroBooNE saw no single photons; electron results need further discussion.
- Reactor experiments using ratios see hints of oscillations at large mass-square-differences.
- Source experiments see very significant deficit.
- Muon-neutrino disappearance has resulted in weak signals at large mass-square-differences.
- Anomalous observations are on a line on L/E.
- Standard cosmological scenarios disfavor an additional neutrino. Though tensions in the Hubble parameter indicate that something is missing.

Indications of
new neutrino
oscillations

Indications of
additional new
physics

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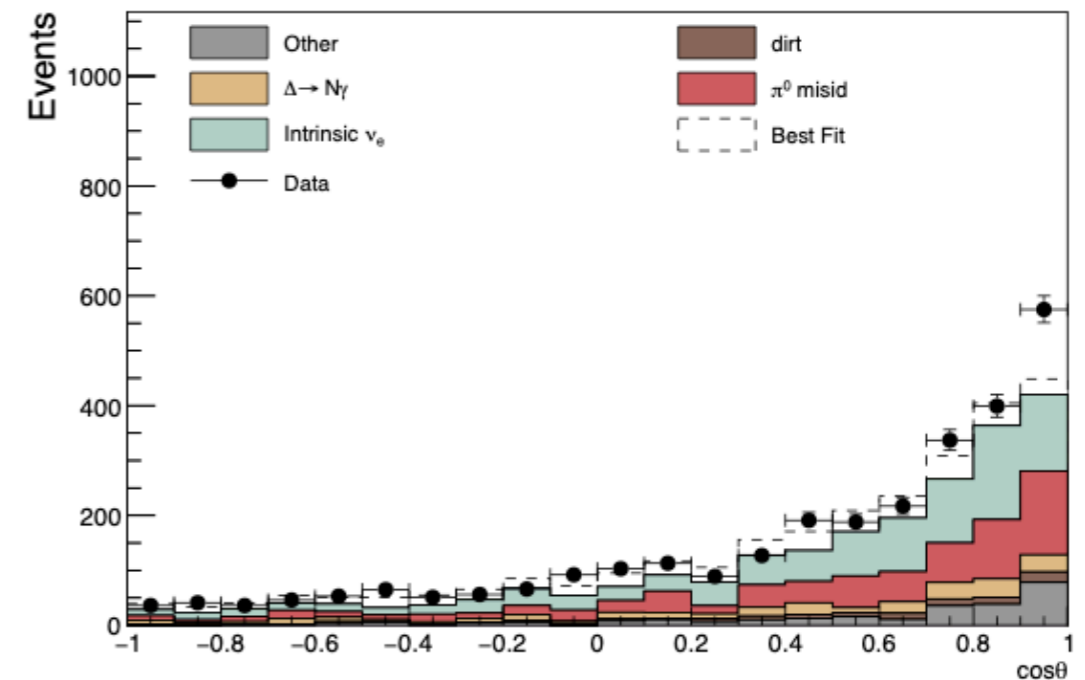
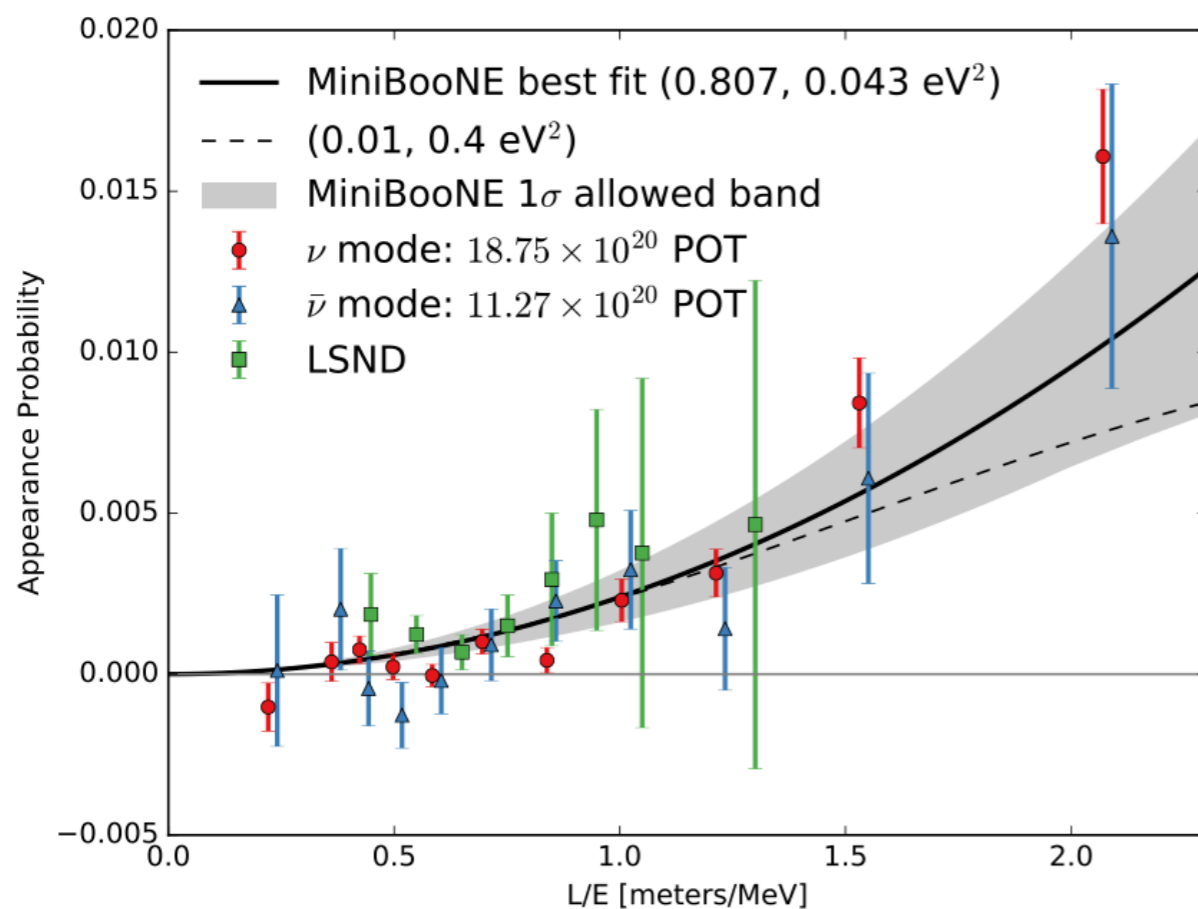
Many elements suggest
something like 3+1, but
something else is hinted by
observations and tensions in
the data sets.

Outline

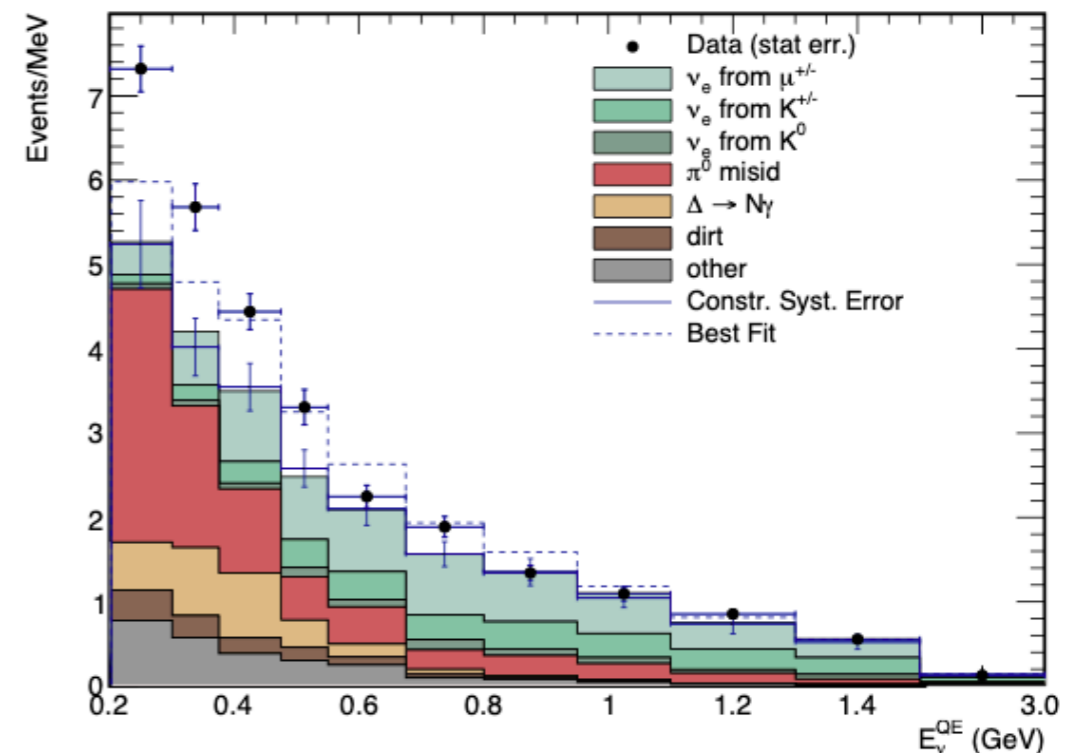
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Switching gears: Changing how we look at things

This is useful if we are after an oscillation explanation



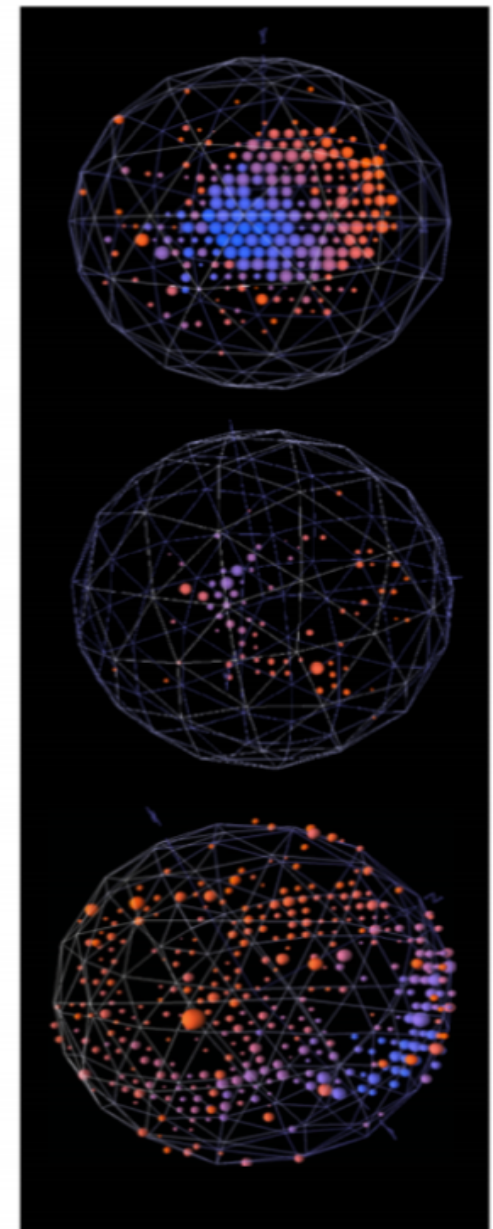
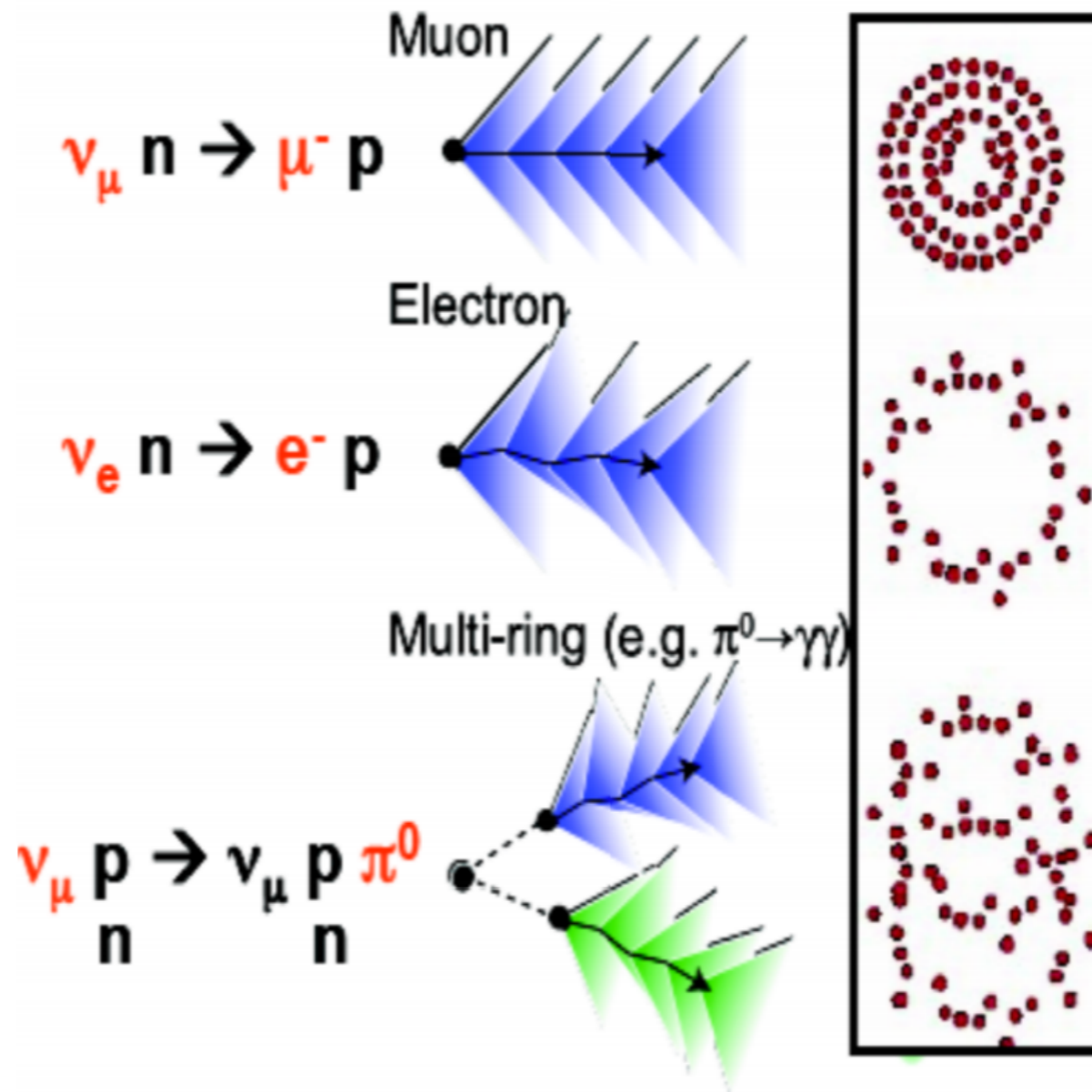
In other cases we need to fit these two!



MiniBooNE event identification

Three typical event signatures:

- Muon-neutrino CCQE produces sharp photon ring on PMTS,
- Electron-neutrino CCQE events produces fuzzy ring,
- Muon-neutrino NC can produce π_0 : two gammas -> two fuzzy rings.



Cannot distinguish between
electrons and photons!

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Dark Neutrino

E. Bertuzzo et al., PhysRevLett.121.241801

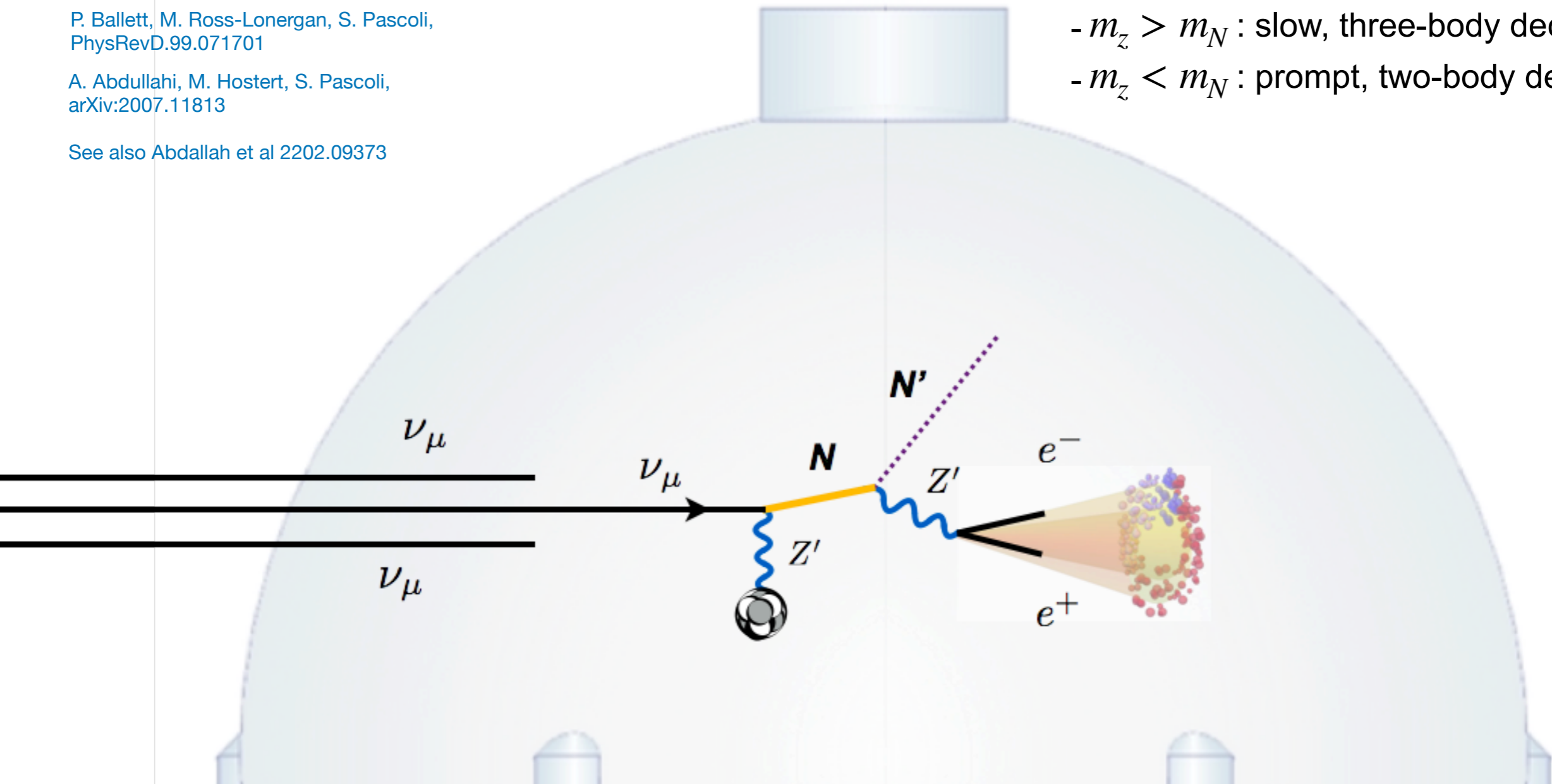
P. Ballett, M. Ross-Lonergan, S. Pascoli,
PhysRevD.99.071701

A. Abdullahi, M. Hostert, S. Pascoli,
arXiv:2007.11813

See also Abdallah et al 2202.09373

Two phenomenologically distinct scenarios:

- $m_z > m_N$: slow, three-body decays.
- $m_z < m_N$: prompt, two-body decays.

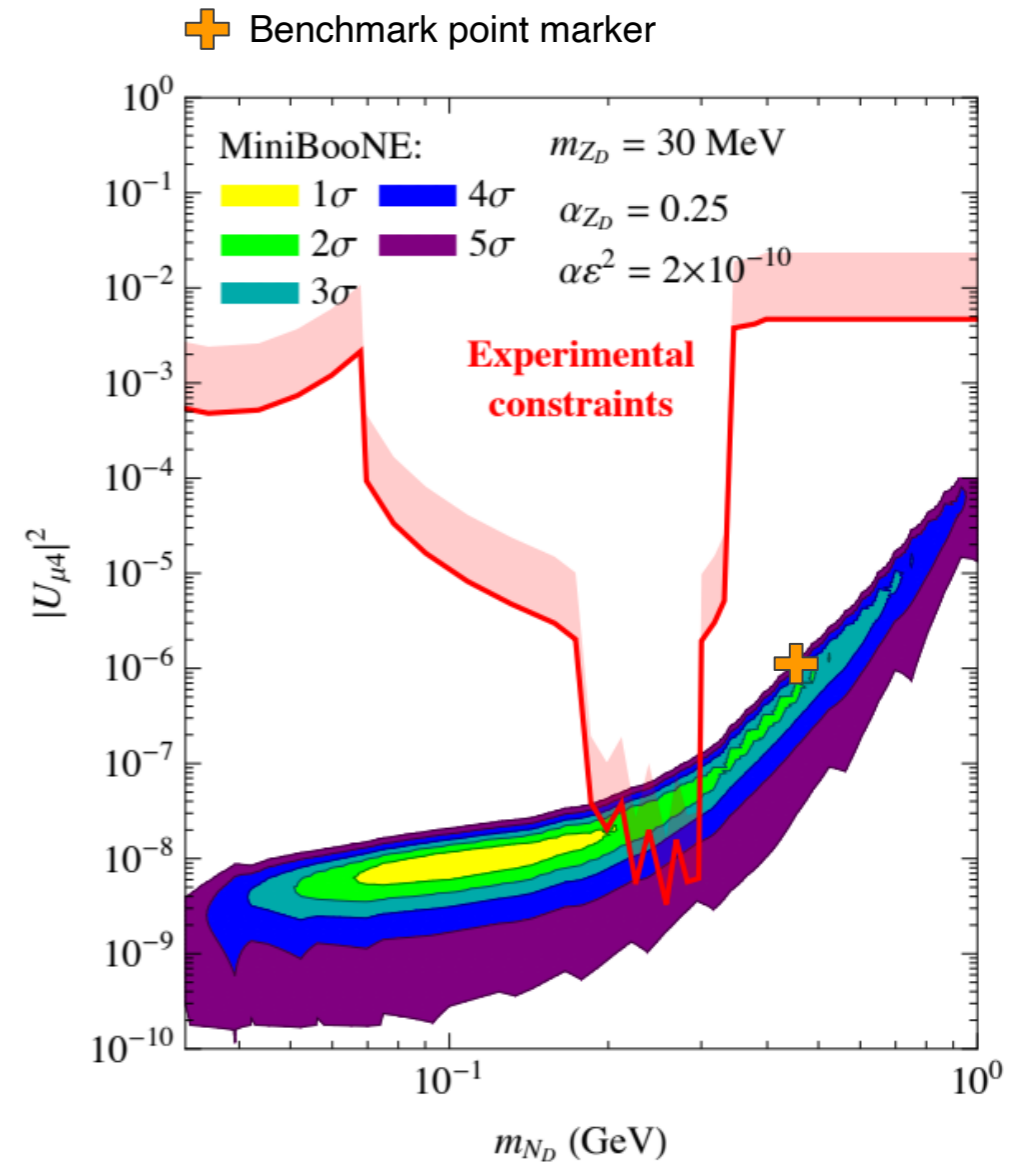
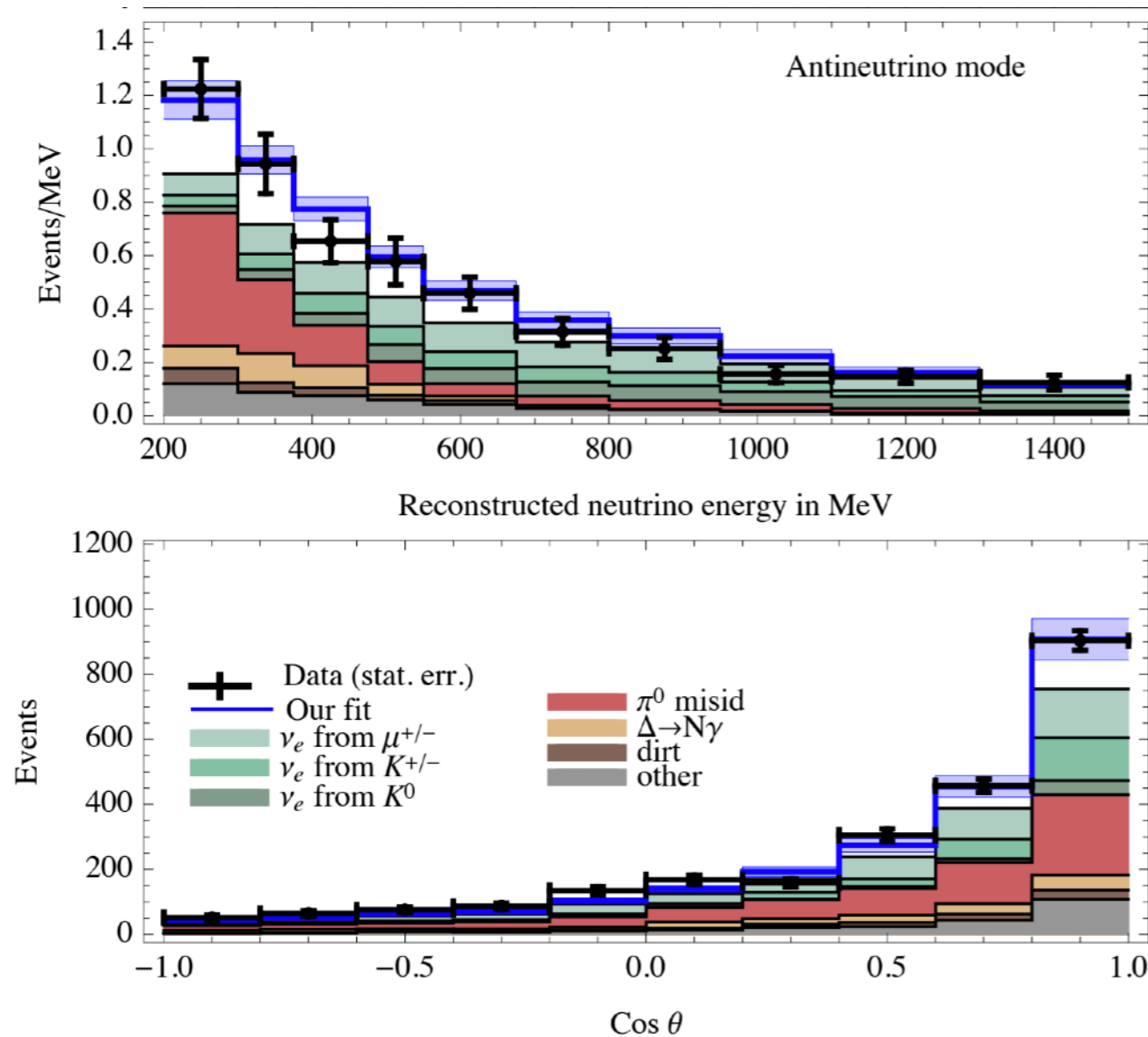


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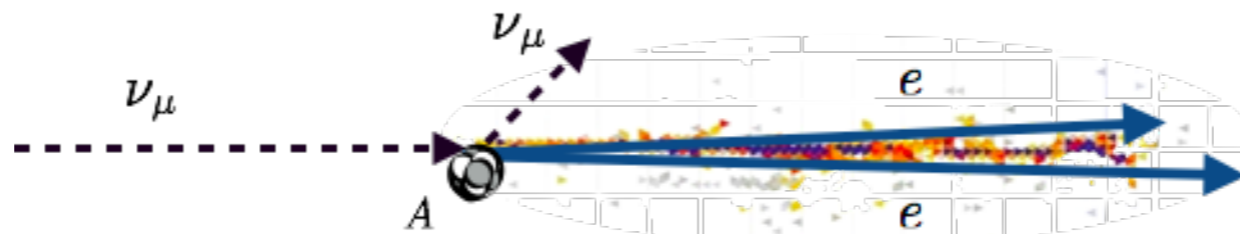
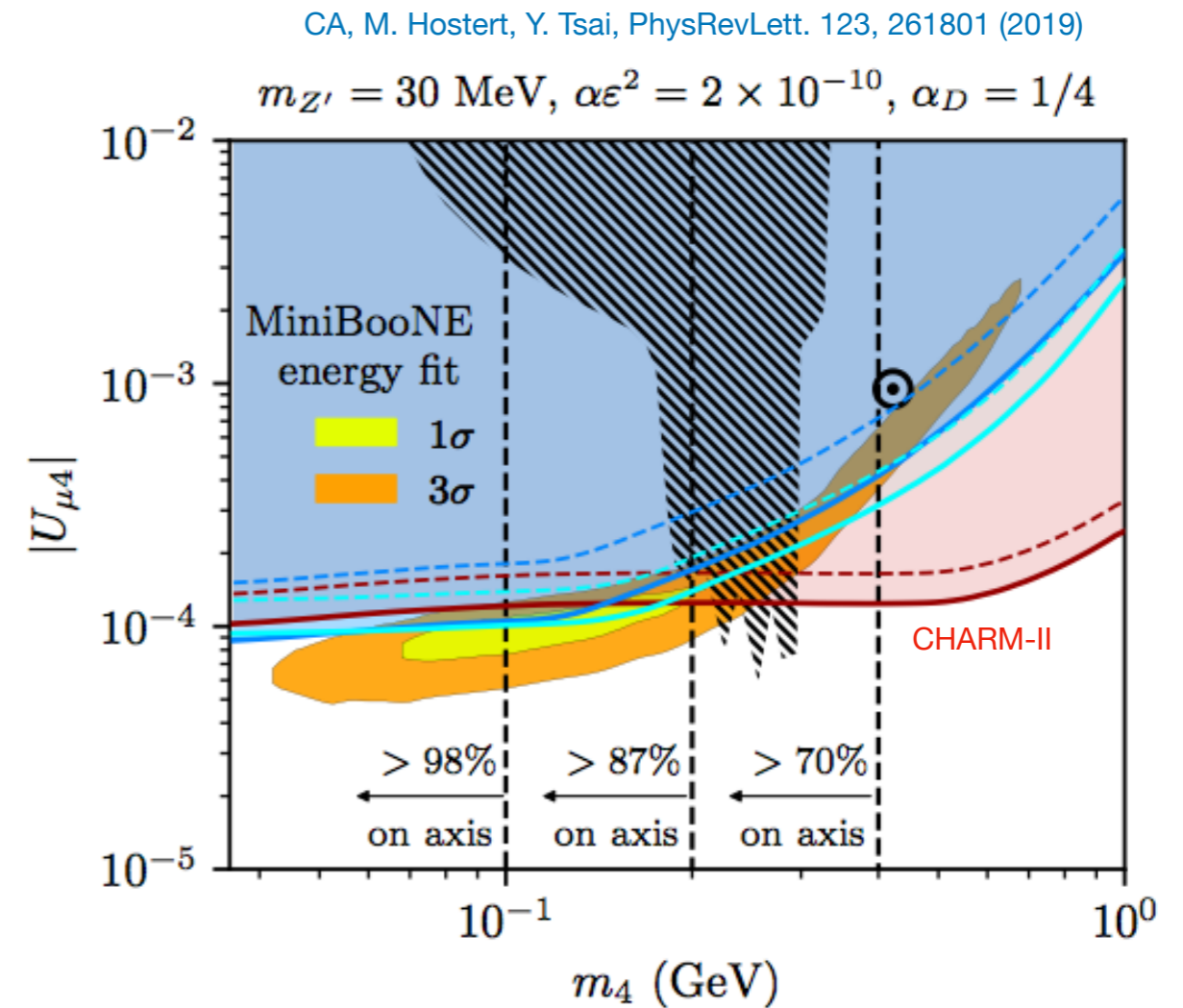
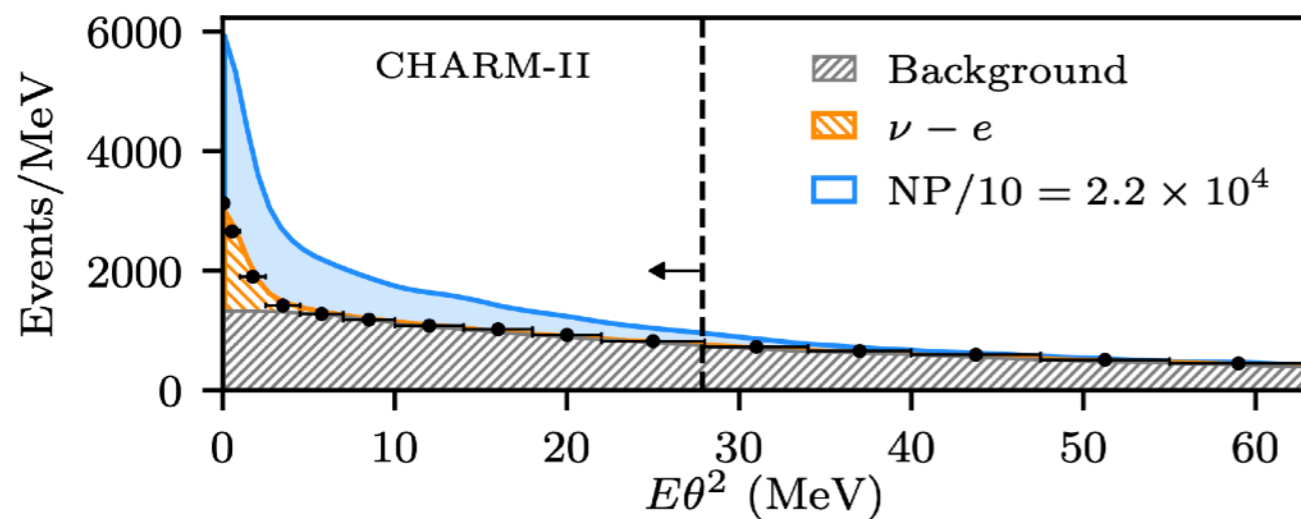
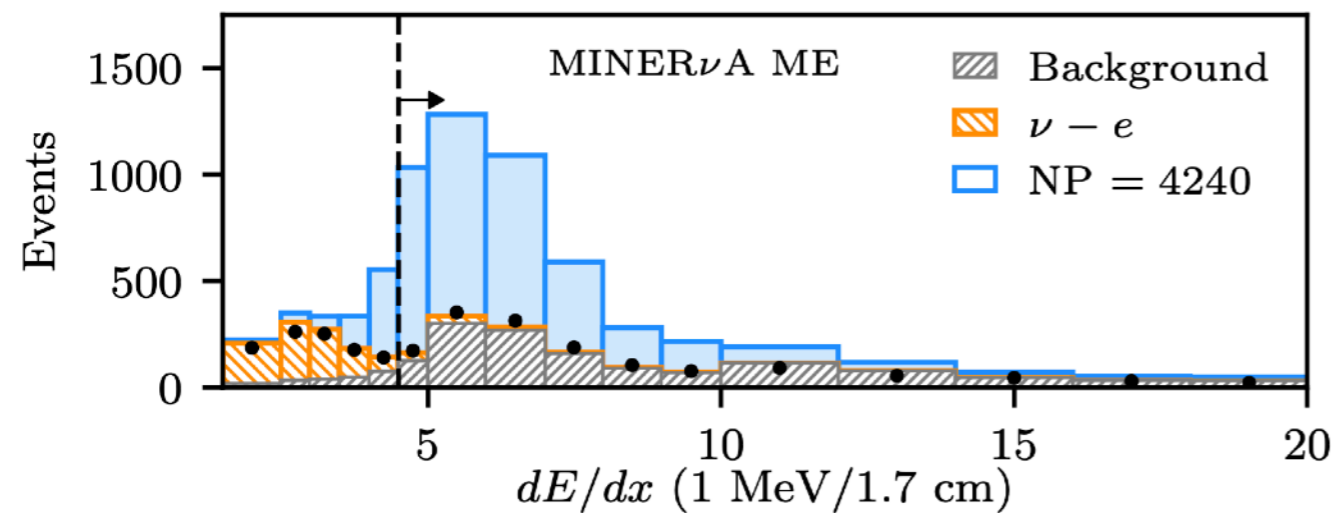
P. Ballett, M. Ross-Lonergan, S. Pascoli,
PhysRevD.99.071701



Good fit to the energy and angular distribution.

Dark Neutrino

This model can be constraint by Minerva electron-neutrino scattering data sets.



In tension with measurements of electron-neutrino scattering

Dark Neutrino

Sometime before the pandemic in a conference in the midwest ...



But
Carlos, you are fixing
some parameters ... how
about a full parameter
scan?

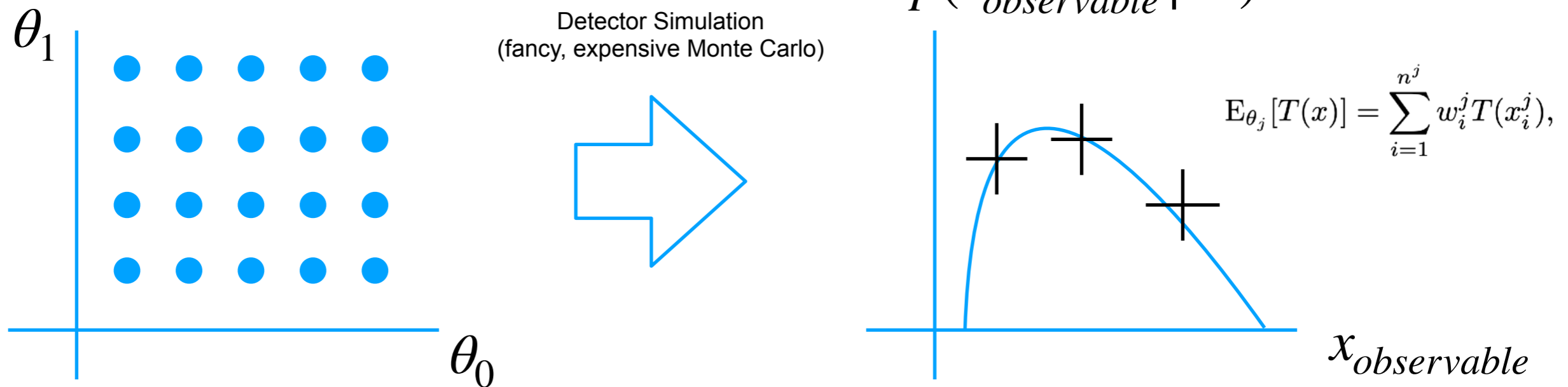
Good
point ... so many
parameters Let me think
about it ... ill be back ...



Benchmark	(A) Light Z'	(B) Heavy Z'
m_N	100 MeV	100 MeV
$m_{Z'}$	30 MeV	1.25 GeV
$ V_{\mu N} ^2$	8×10^{-9}	2.2×10^{-7}
α_D	1/4	0.4
ϵ	1.7×10^{-4}	2×10^{-2}
$ V_N ^2$	$ V_{\mu N} ^2$	1

Addressing the High-Dimensionality Problem: Exploring New Parameter Space!

What do we normally do:

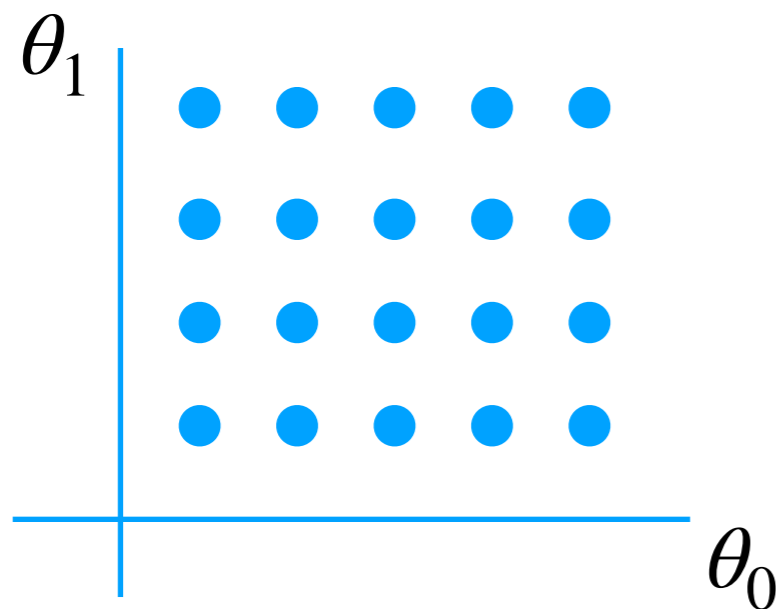


From this we can construct our test-statistic distribution (likelihood, χ^2 , etc.) and obtain the test-statistic for each point on our parameter space grid.

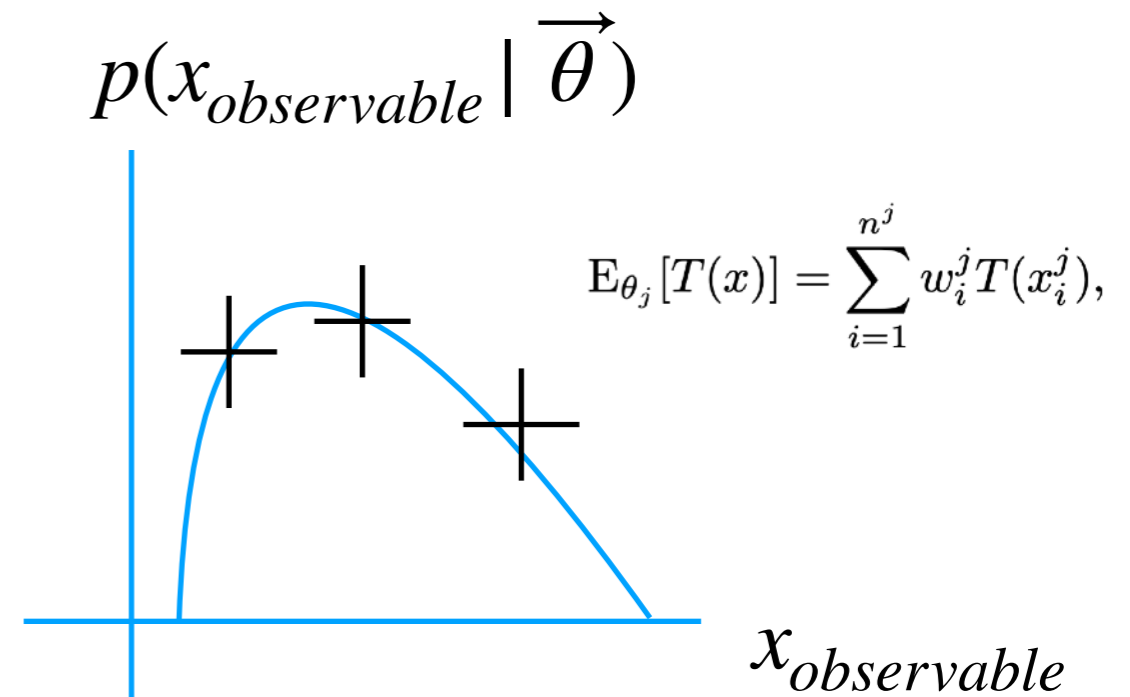
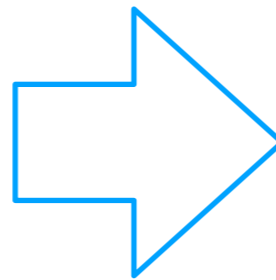
Then we interpolate the test statistic on the grid and voila: we get our constraint plot.

Addressing the High-Dimensionality Problem: exploring new parameter space!

What do we normally do:



Detector Simulation
(fancy, expensive Monte Carlo)



From the Idea: why don't we treat the physics parameters space variables like we do with the true kinematic distributions?

Then obtain the plot.

Addressing the High-Dimensionality Problem: exploring new parameter space!

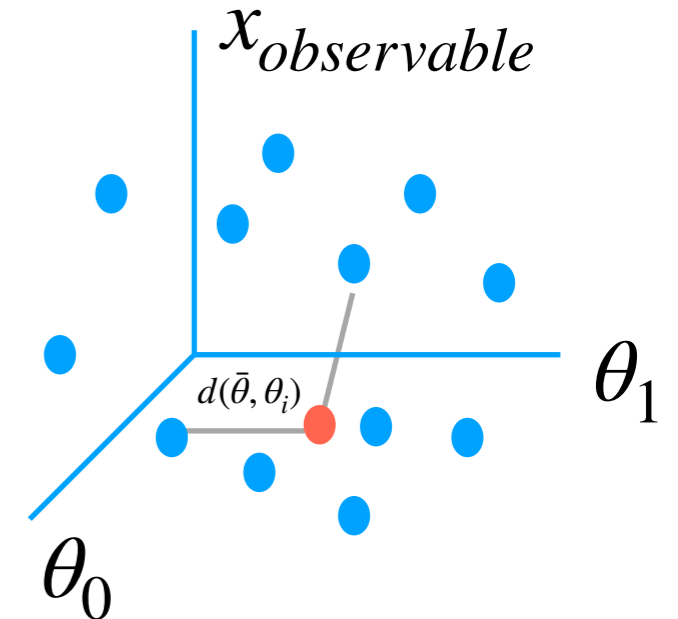
Instead of computing the test statistic on the sample this:

$$\mathbb{E}_{\theta_j}[T(x)] = \sum_{i=1}^{n^j} w_i^j \overset{\text{Test-statistic}}{\downarrow} T(x_i^j),$$

$$p(x, \theta) = \dot{p}(x|\theta)\mathcal{N}(\theta)q(\theta)$$

Promote $\vec{\theta}$ to a random variable and sample from that distribution too. In this case each Monte Carlo event has a different underlying physics parameter point.

$$\begin{aligned}\mathbb{E}_{\bar{\theta}}[T(x)] &= \sum_i^n w_i T(x_i) \frac{w(\bar{\theta}, \theta_i)}{q(\theta_i)} \\ &= \sum_i w_i T(x_i) \frac{K(d(\bar{\theta}, \theta_i), \delta)}{q(\theta_i)}\end{aligned}$$

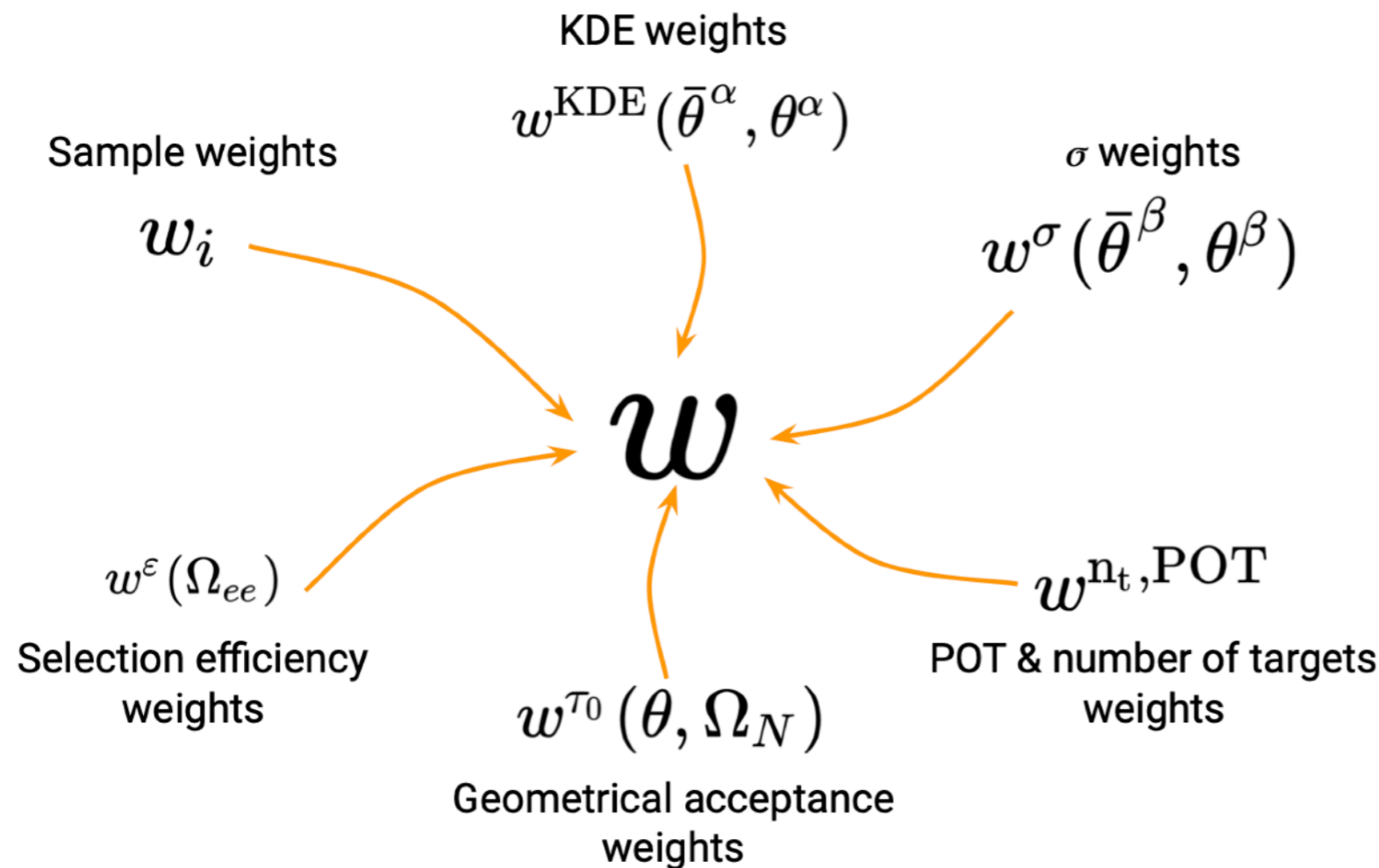


We can generate the points on the parameter space and the observable kinematic distributions efficiently by formulating this problem as a importance sampling problem. Namely computing this integral:

$$\int d\theta^\alpha q(\theta^\alpha) \int d\Omega_N \frac{d\sigma}{d\Omega_N}(\Omega_N|\theta) \int d\Omega_{ee} \frac{1}{\Gamma(\theta)} \frac{d\Gamma}{d\Omega_{ee}}(\Omega_{ee}|\Omega_N)$$

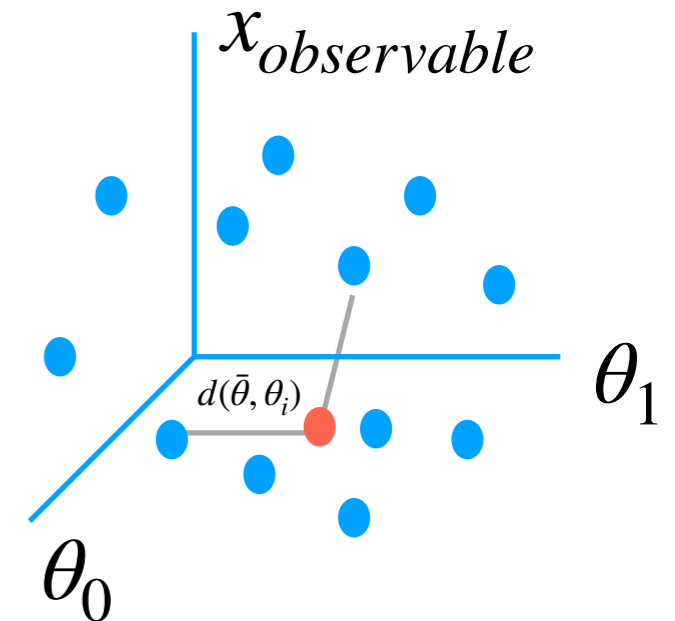
See arXiv:2205.12273 for details

Addressing the High-Dimensionality Problem: exploring new parameter space!



$$\mu(\theta) \simeq \sum_i^n w_i w_i^{\text{KDE}}(\bar{\theta}^\alpha, \theta_i^\alpha) w_i^\sigma(\bar{\theta}^\beta, \theta_i^\beta) w_i^\varepsilon(\Omega_{ee,i}) w_i^{\tau_0}(\theta_i, \Omega_{N,i}) w_i^{\text{n}_t, \text{POT}}$$

$$p(x, \theta) = \hat{p}(x|\theta) \mathcal{N}(\theta) q(\theta)$$

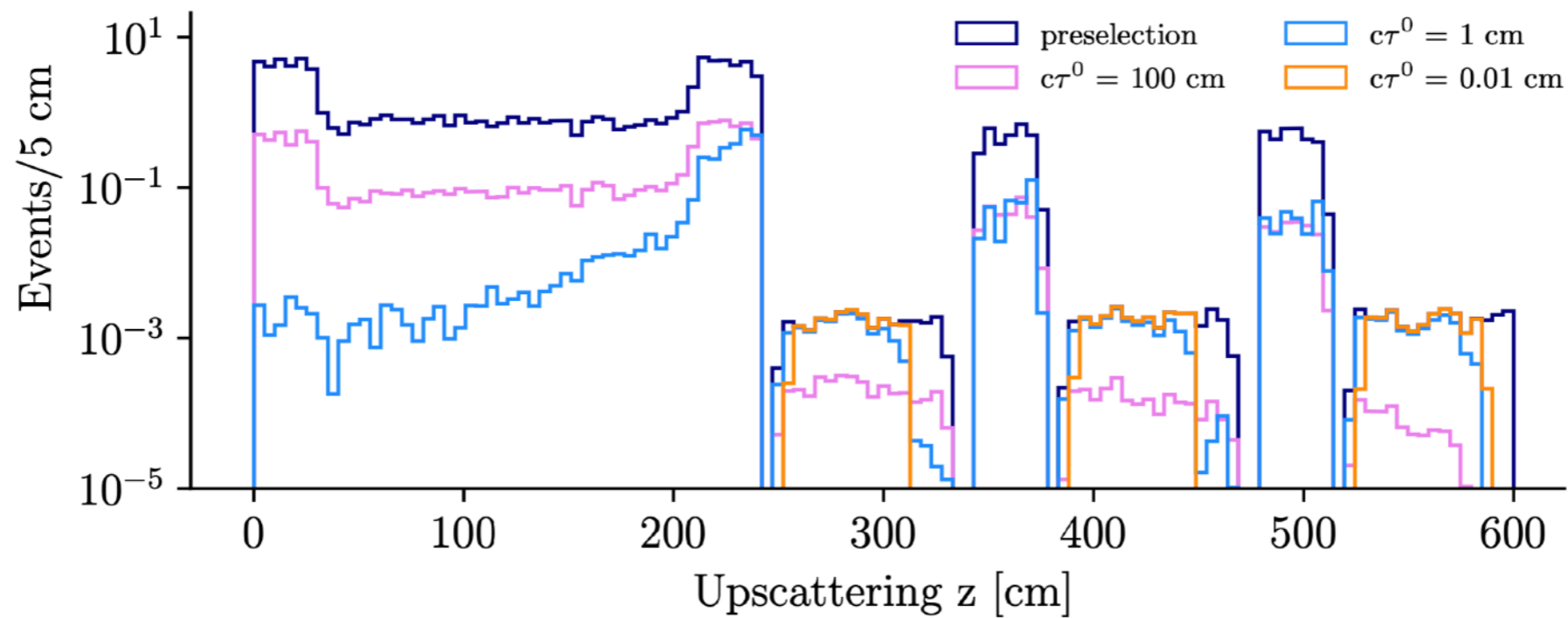
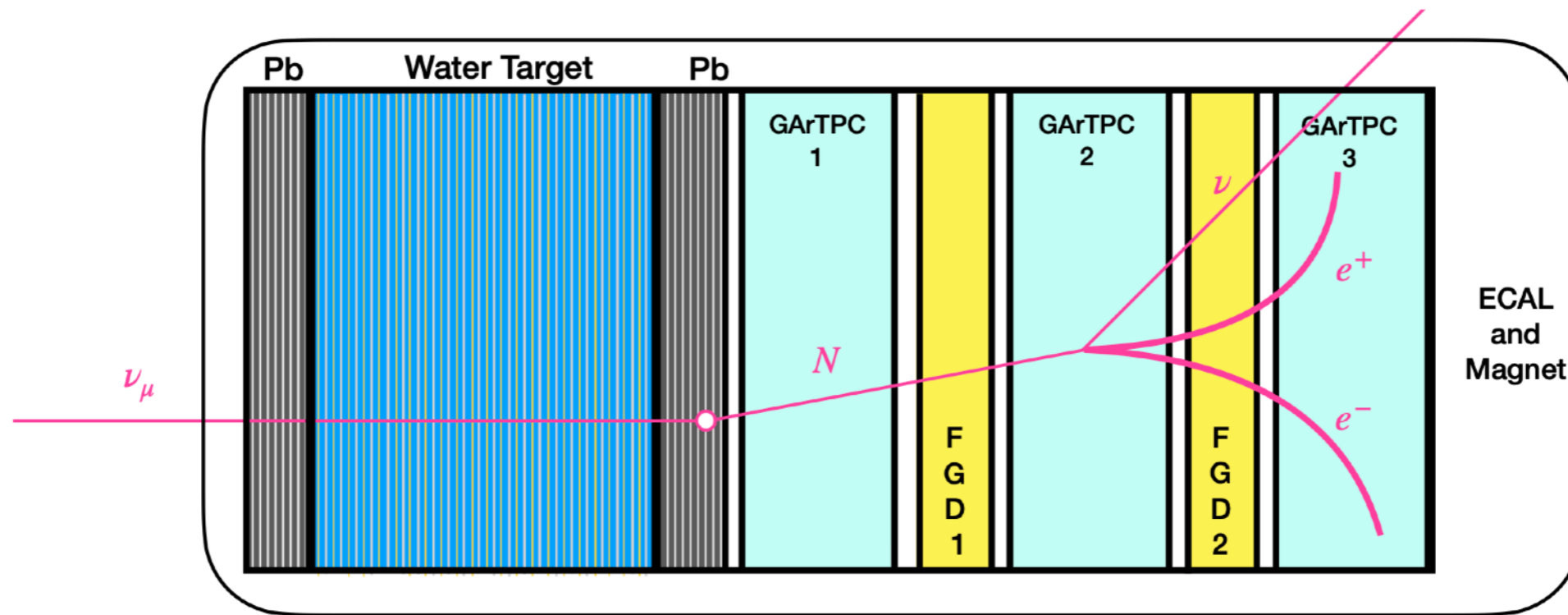


The trade off is that now you have to take into account the error on the prediction.

But that can be handled by either using the *Effective Likelihood* (1901.04645) in the poisson regime or adding an error to your χ^2 in the gaussian regime.

Dark Neutrino at T2K ND280

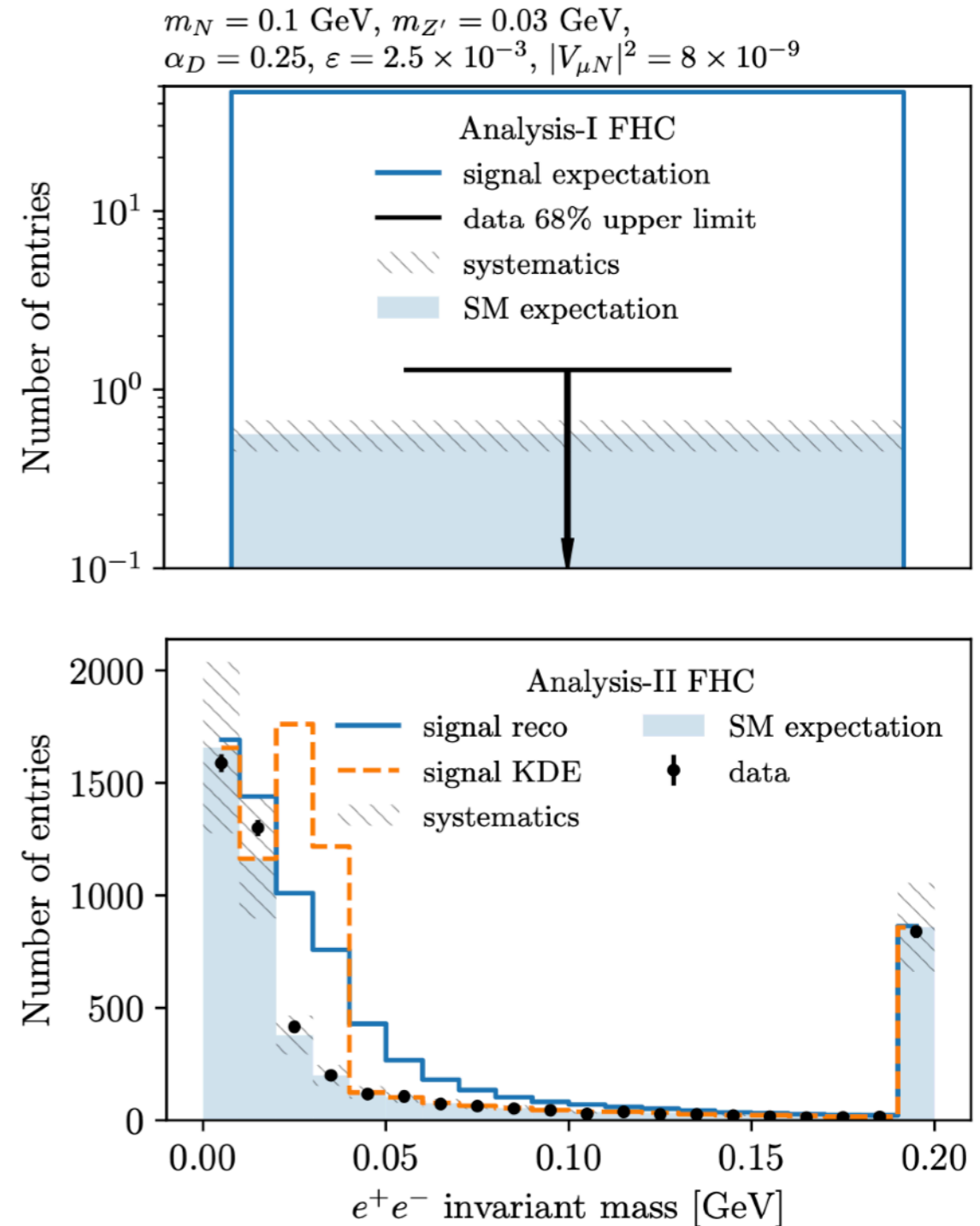
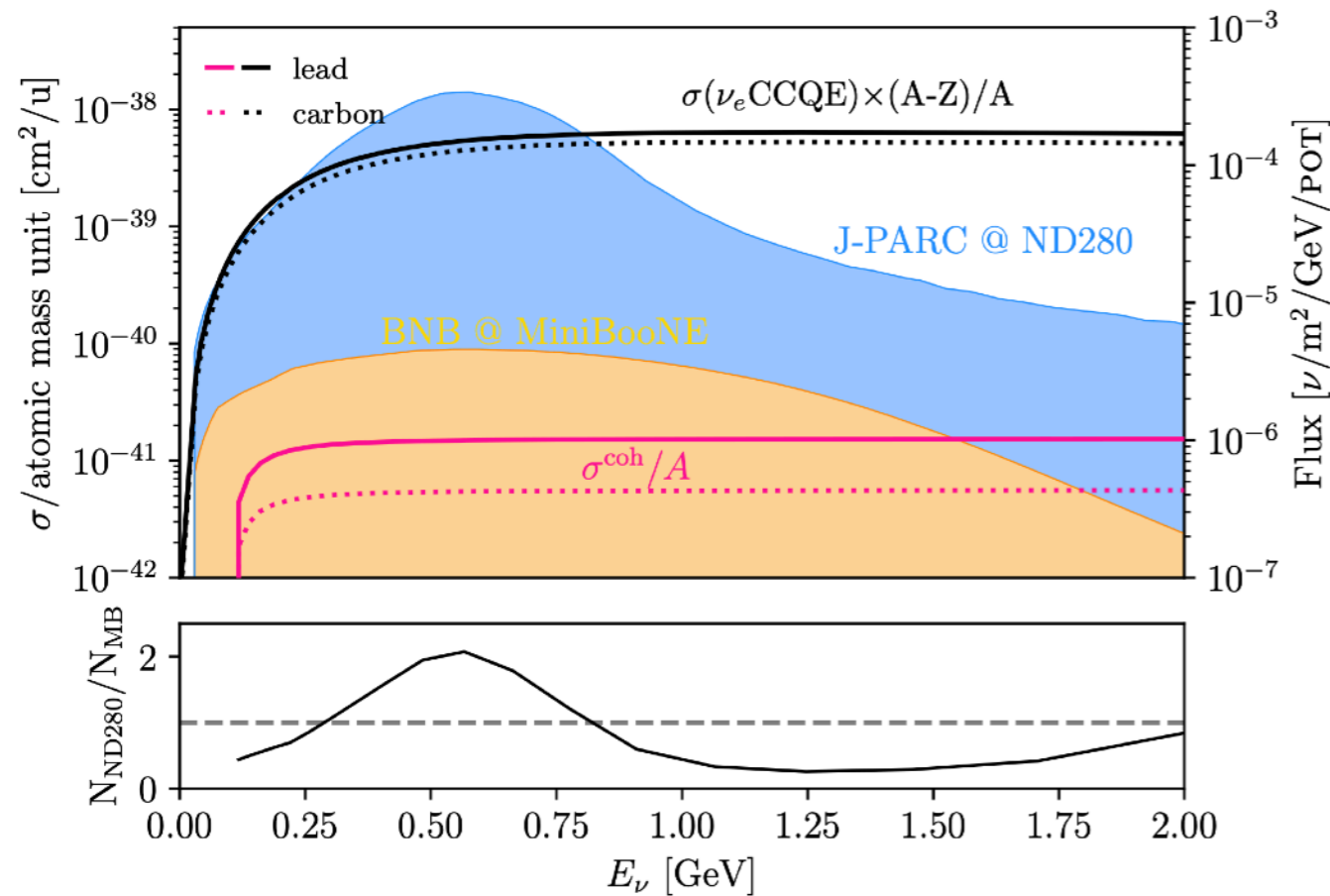
CA, Foppiani, Hostert 2205.12273



Dark Neutrino at T2K ND280

CA, Foppiani, Hostert 2205.12273

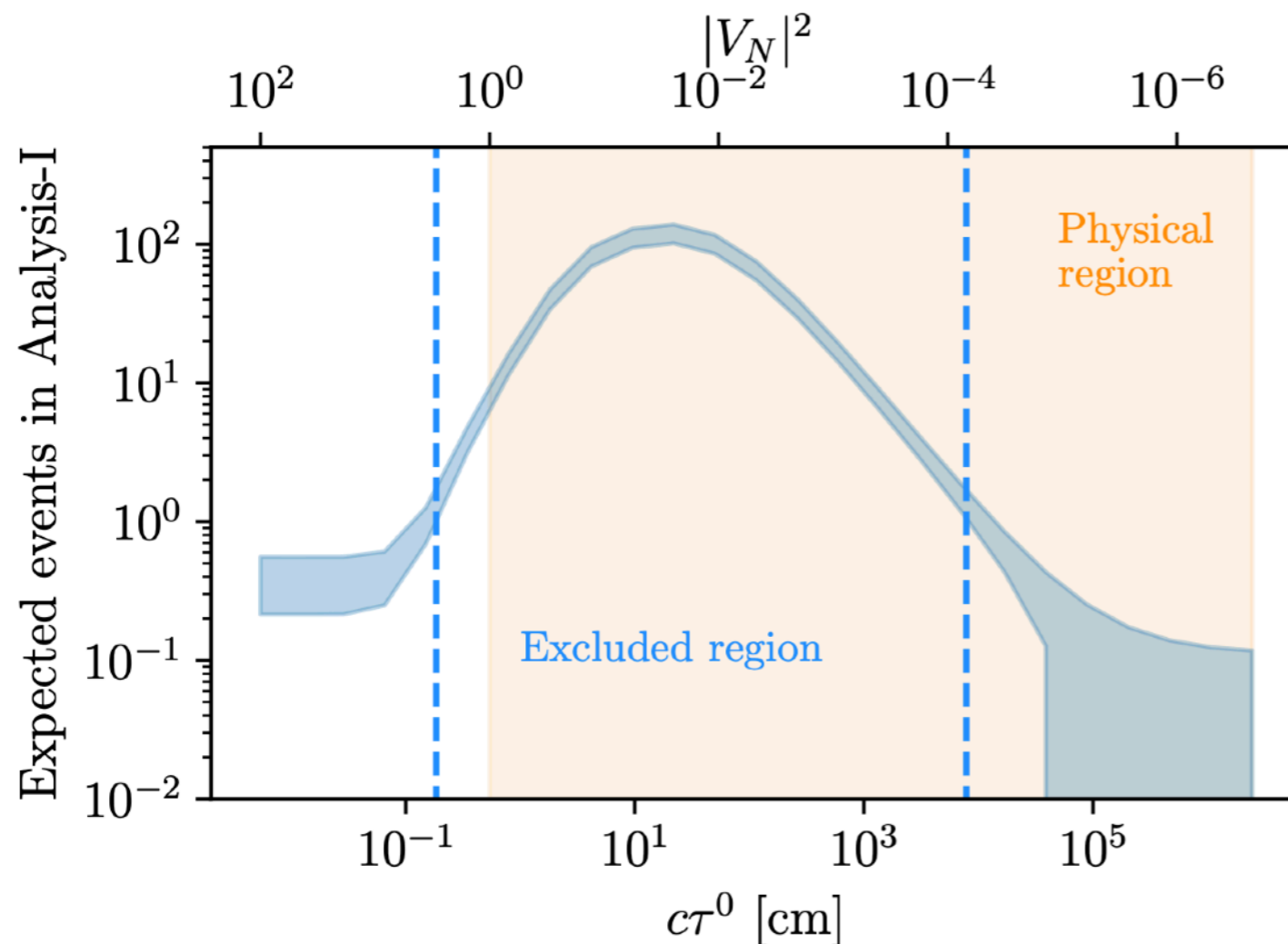
T2K ND280 detector is smaller, but flux at T2K
Is much more intense than at MB. Rates event out.



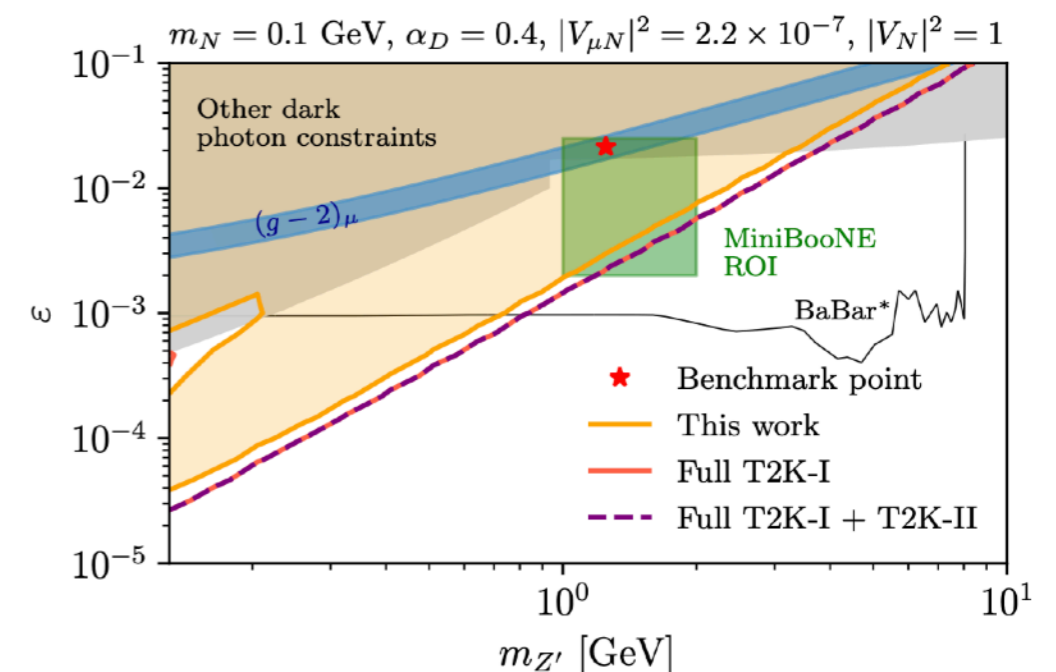
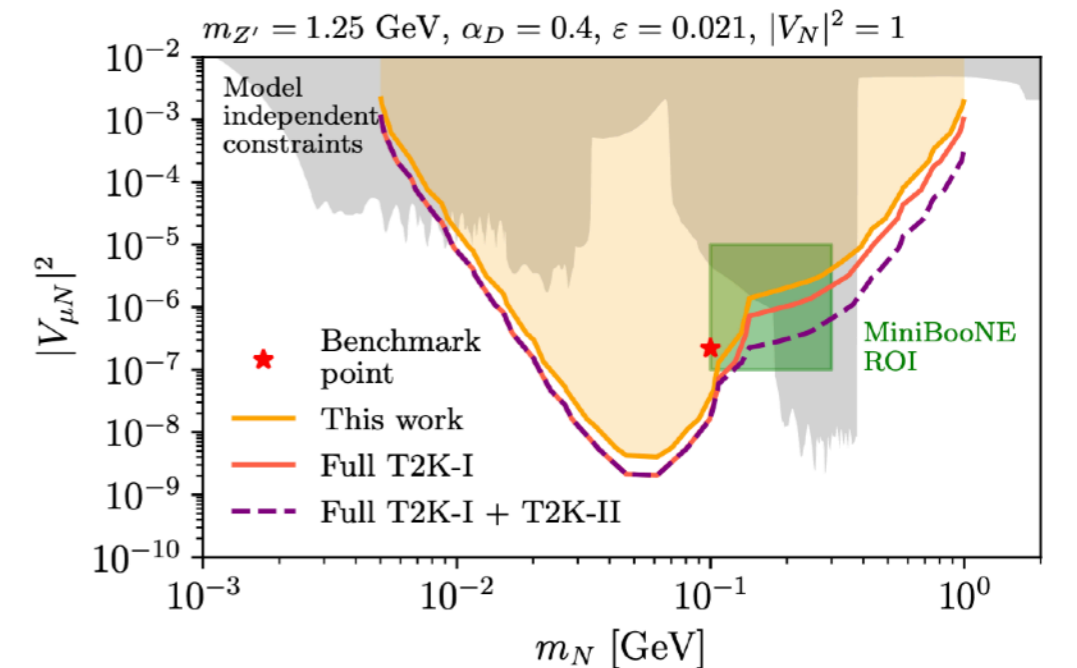
Dark Neutrino at T2K ND280

Constraints from T2K are powerful when the mediator is heavier, in the light case dominated by Minerva bounds.

CA, Foppiani, Hostert 2205.12273



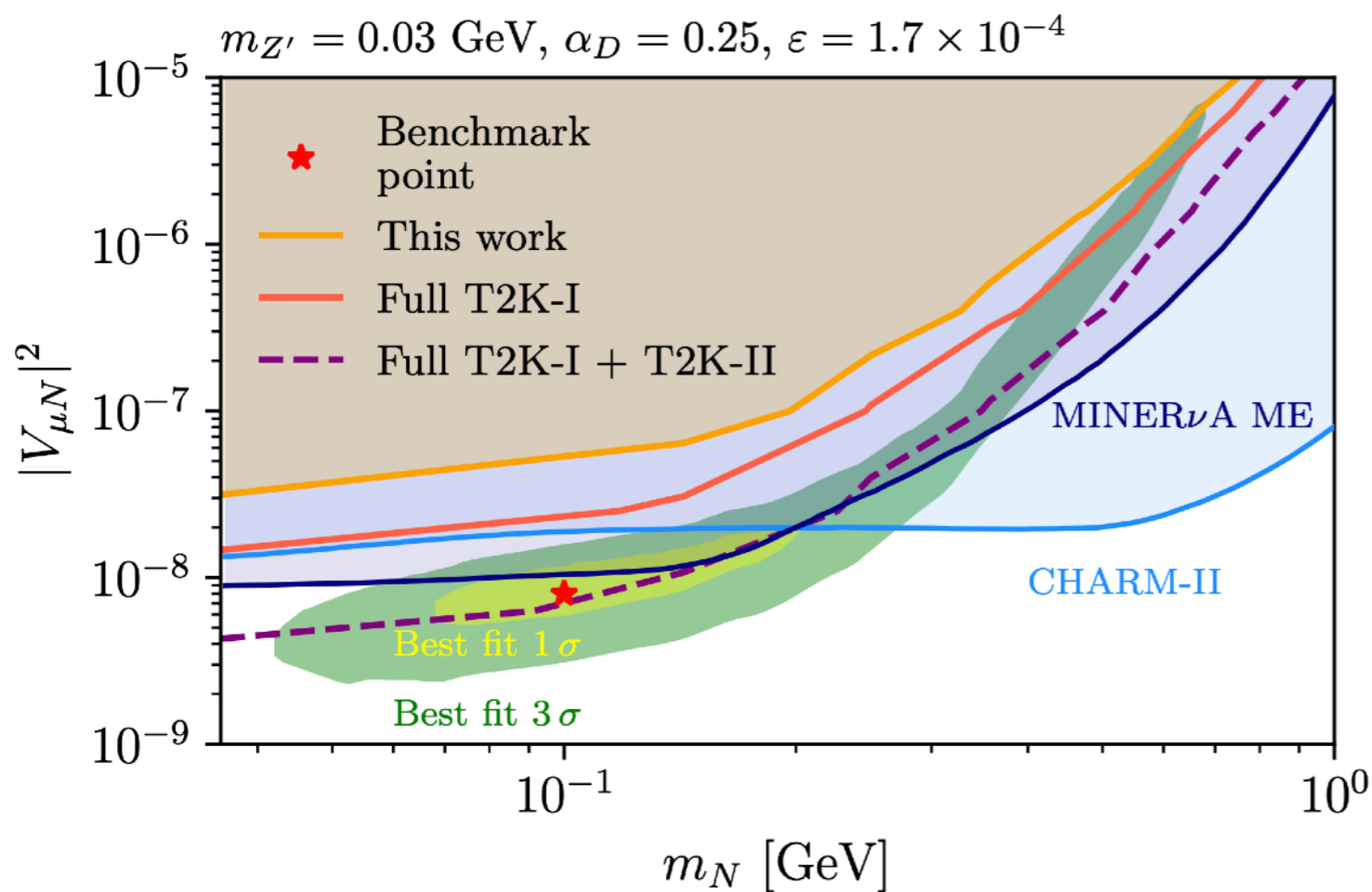
Dedicated T2K analysis should significantly improve these constraints.



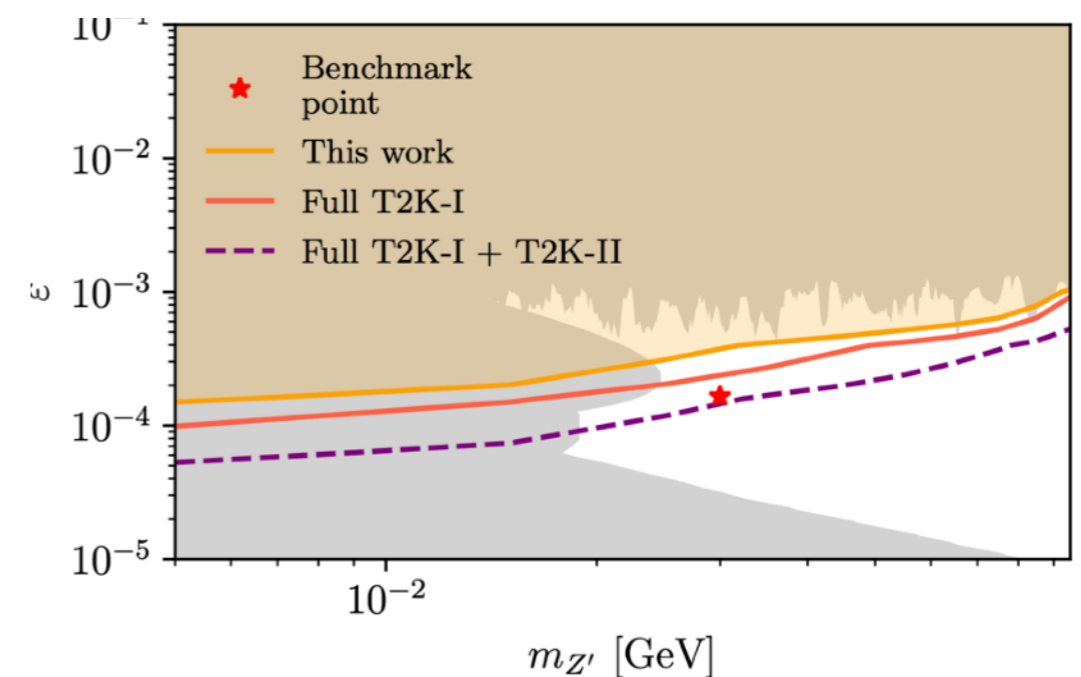
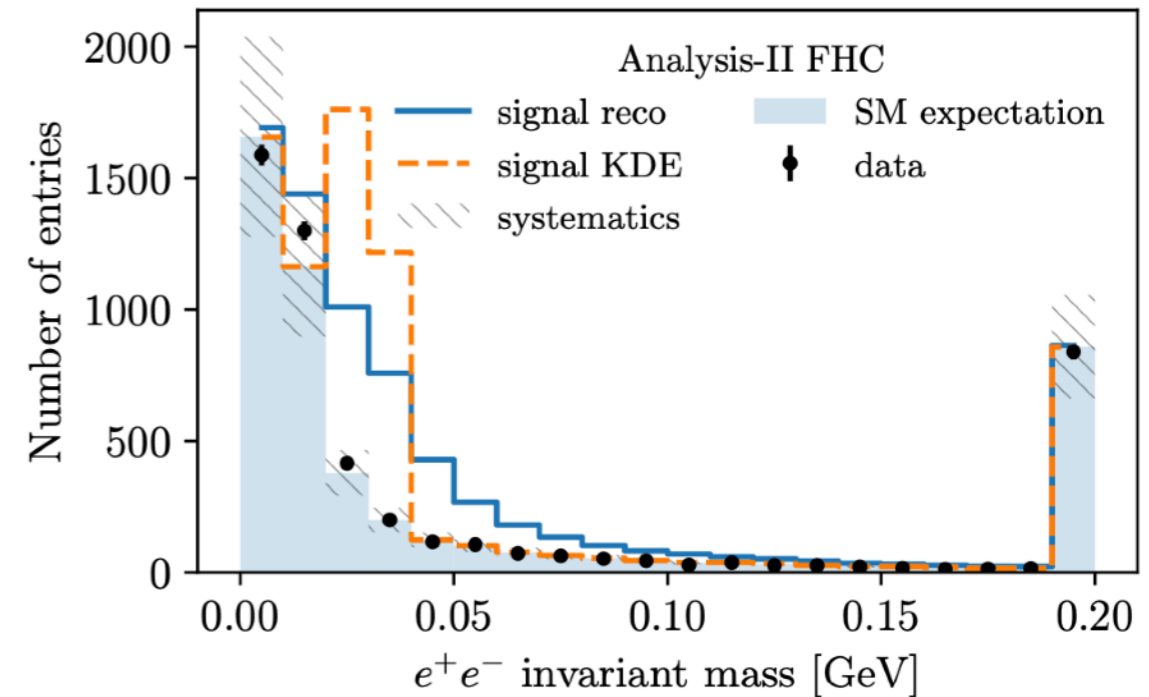
Dark Neutrino at T2K ND280

T2K light case constraints are dominated by quasi-elastic scattering photon side band. However, light case dominated by Minerva bounds.

CA, Foppiani, Hostert 2205.12273



Dedicated T2K analysis should significantly improve these constraints.

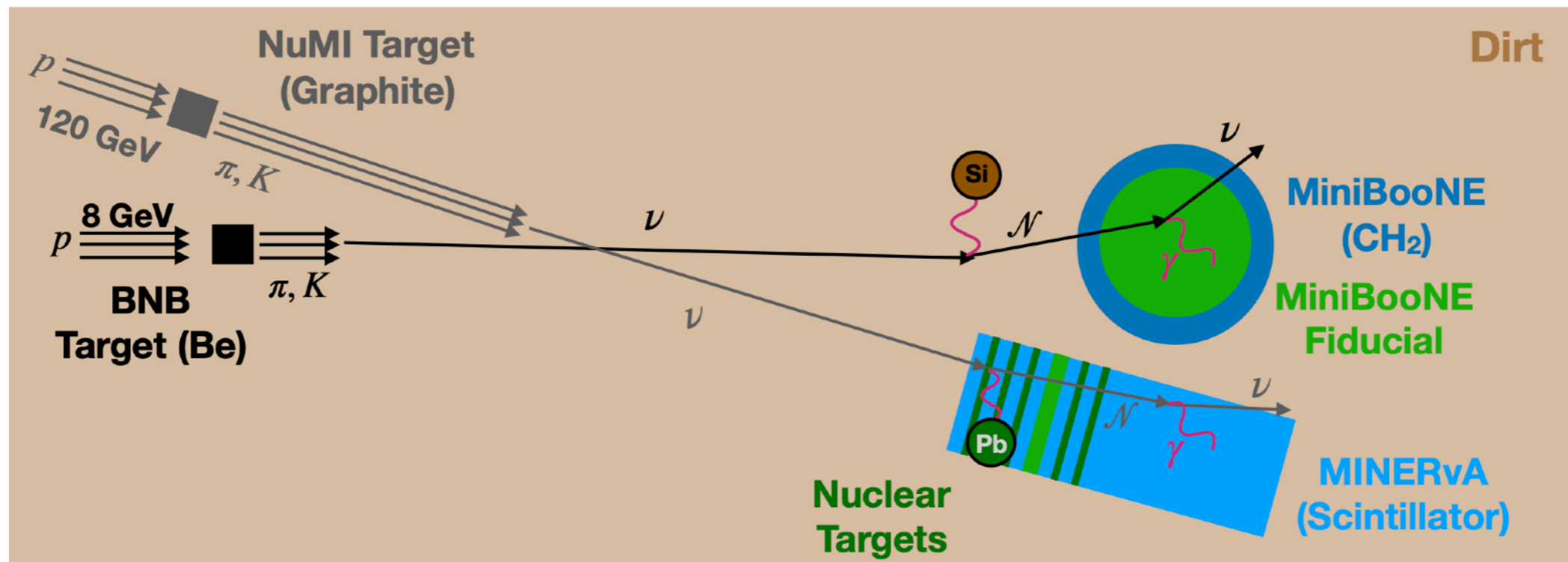


Outline

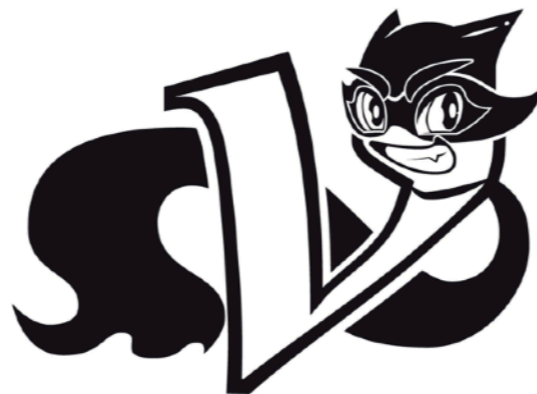
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Neutrissimo Scenario

This scenario is predicated under the idea that there are oscillations, but *something else is going on ...*



Neutrissimo: HNL with Transition Magnetic Moment

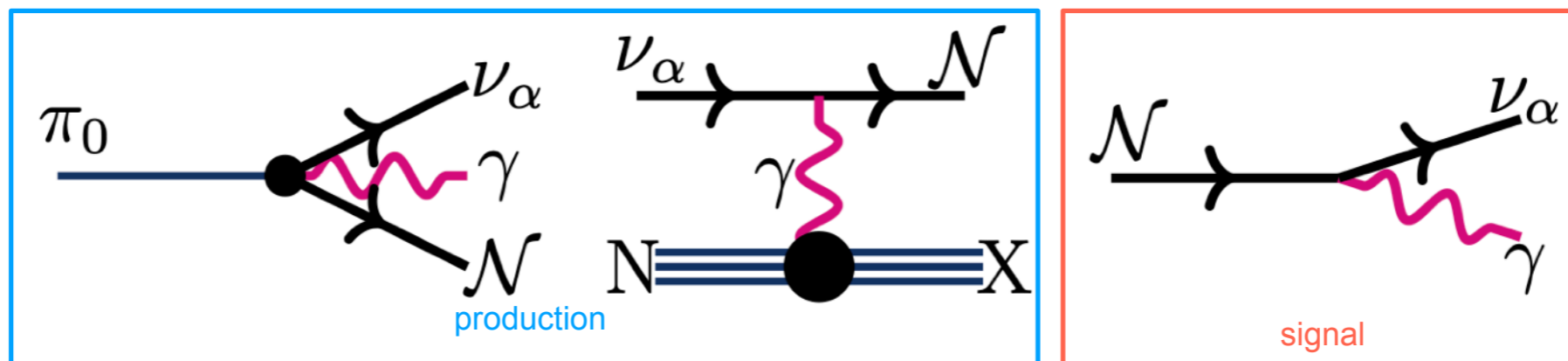


Light sterile neutrino explains:

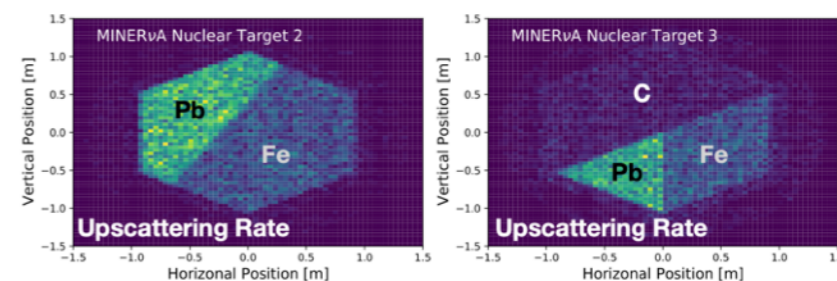
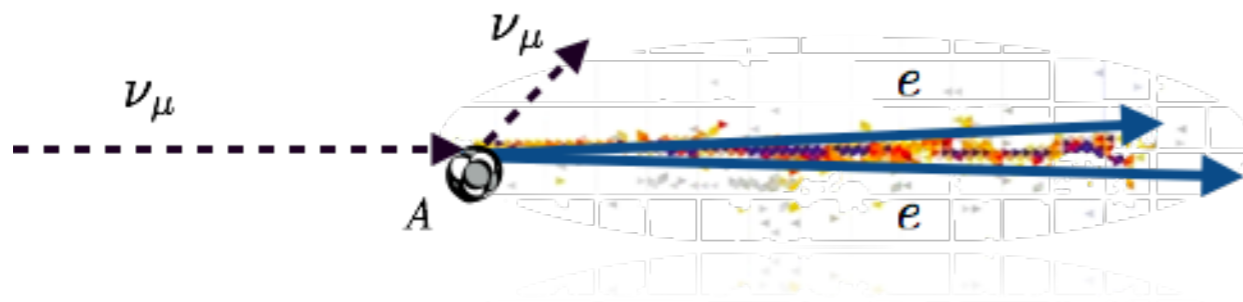
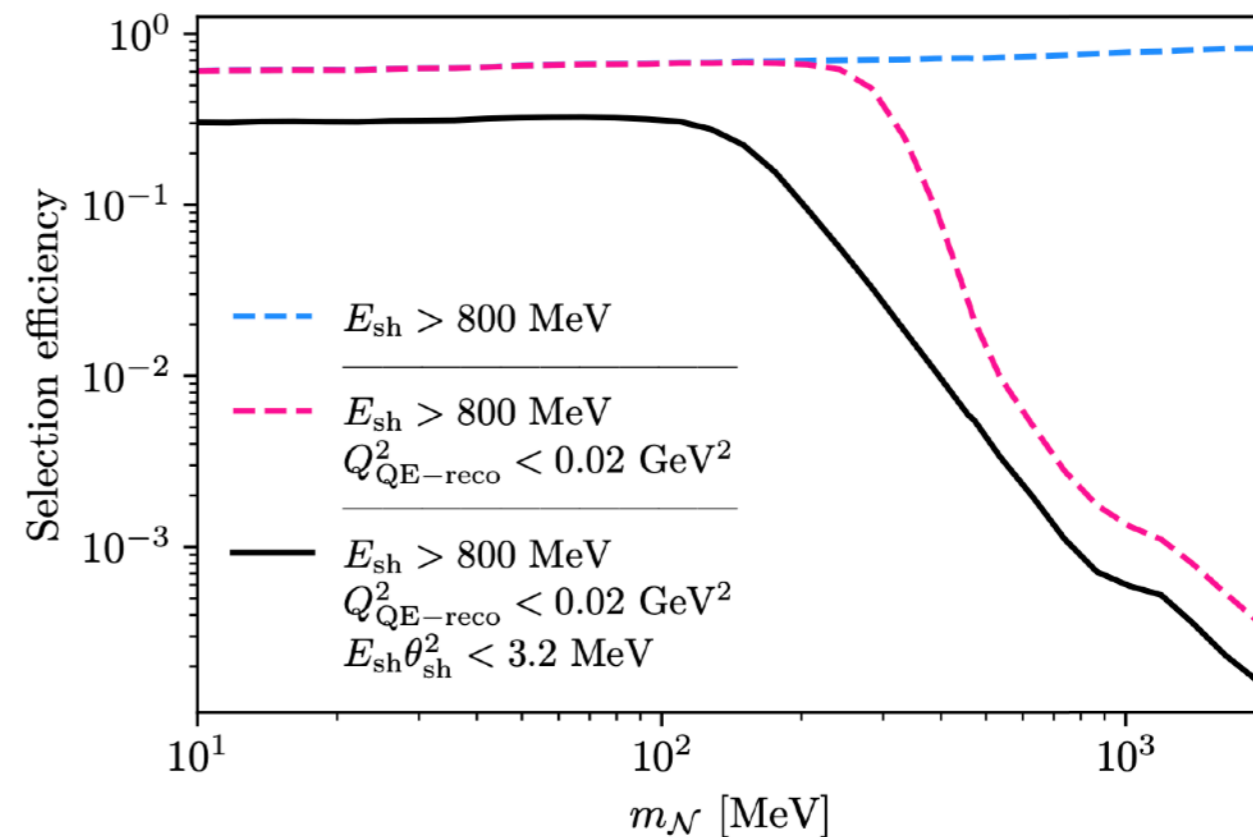
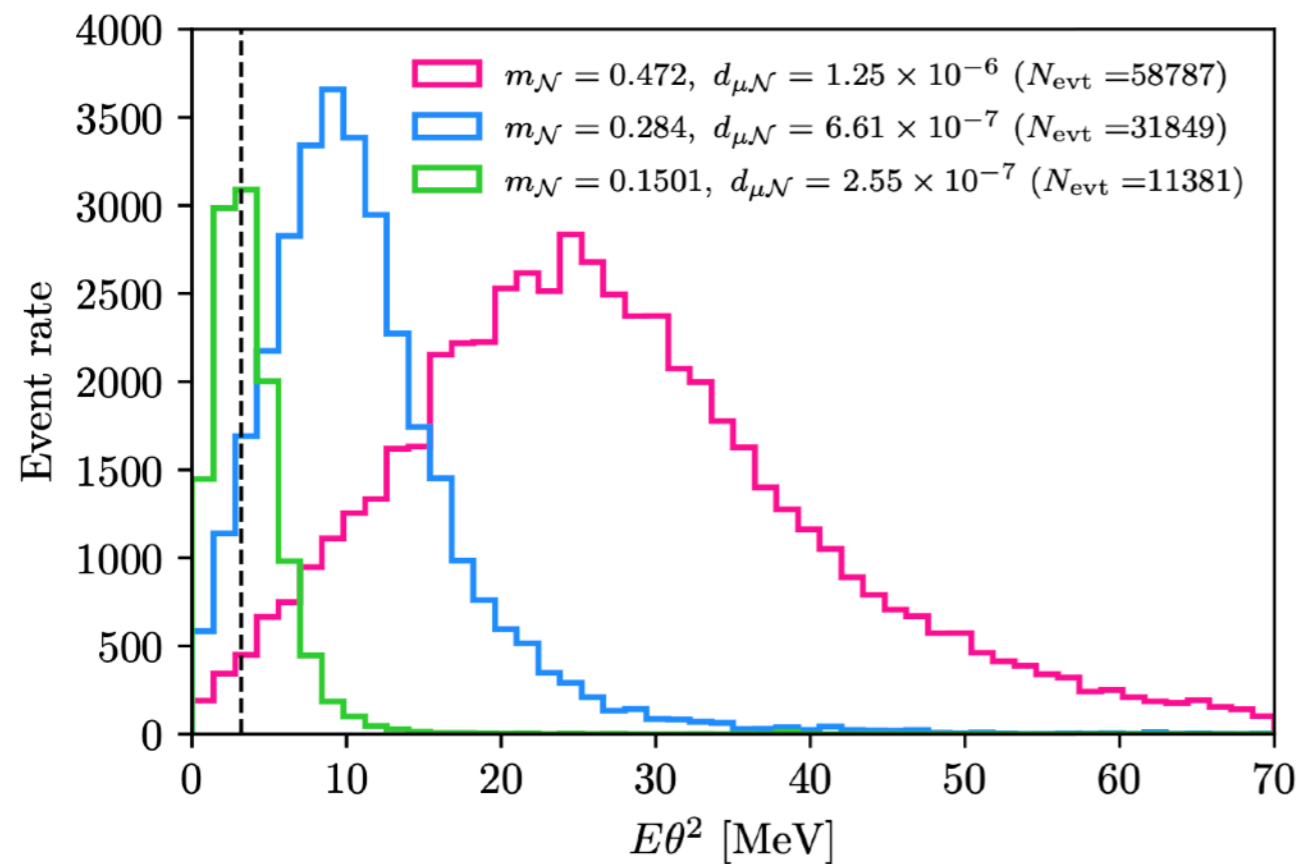
- Reactors
- LSND
- Part of MiniBooNE

See arXiv: 2105.06470, 2206.07100

Neutrissimo Scenario

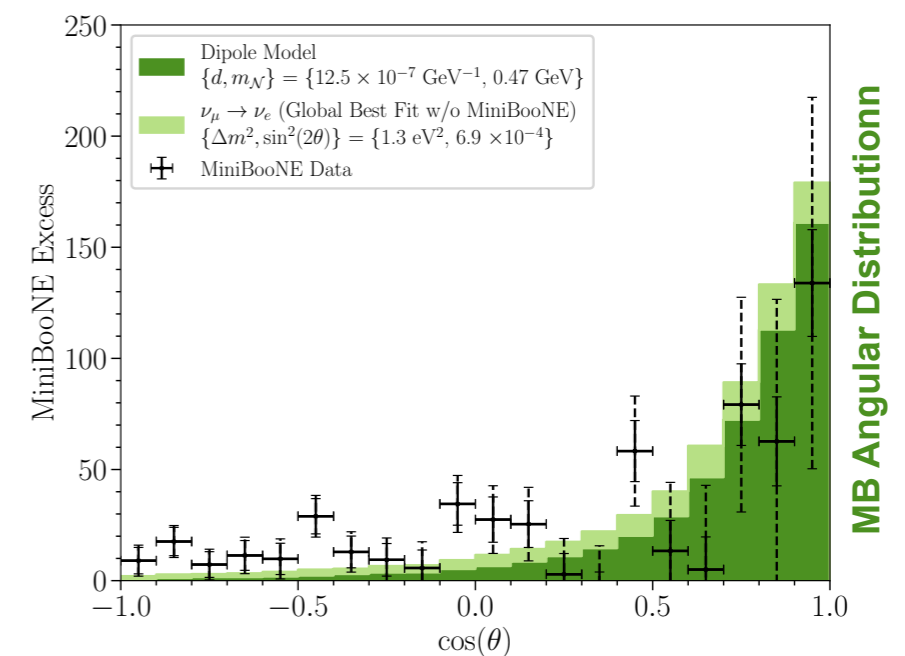
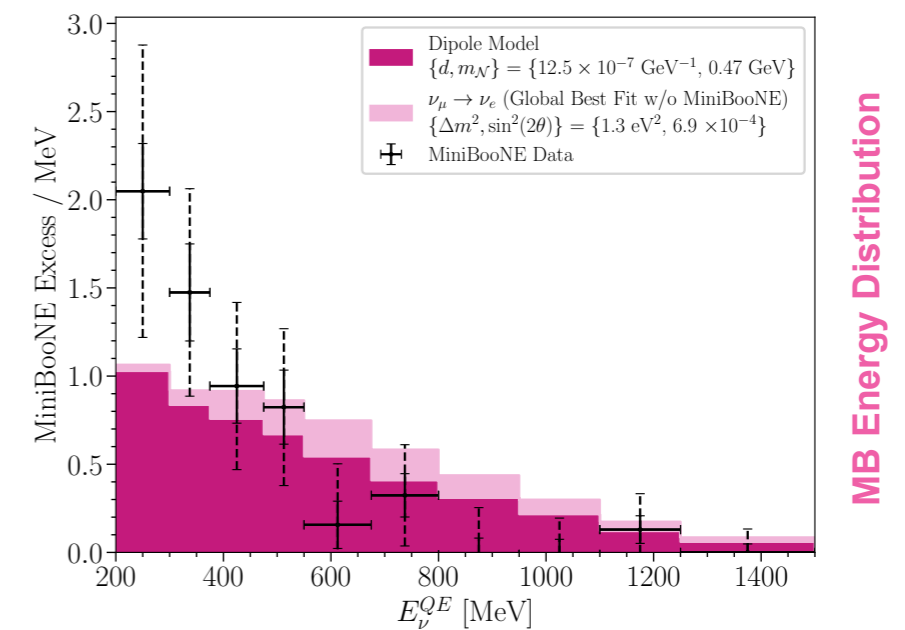
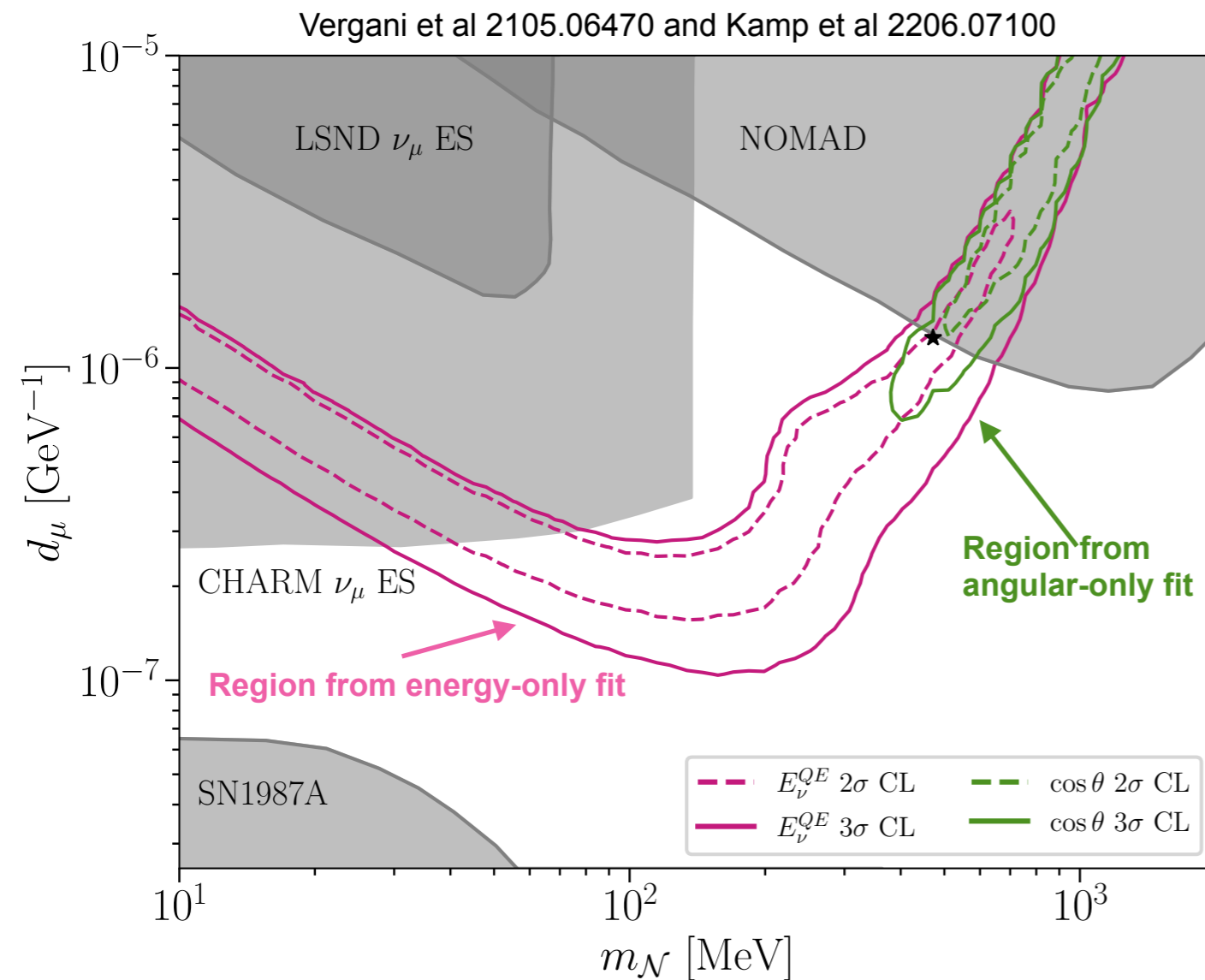
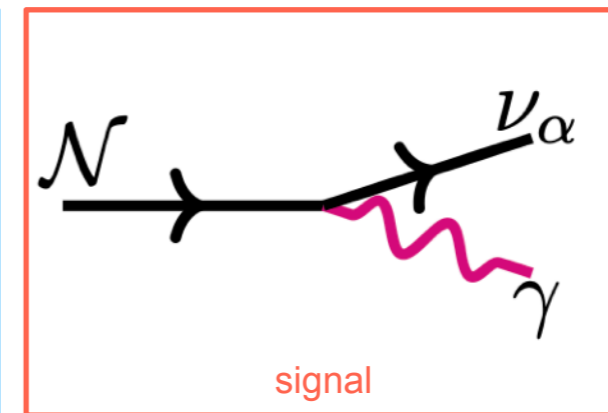
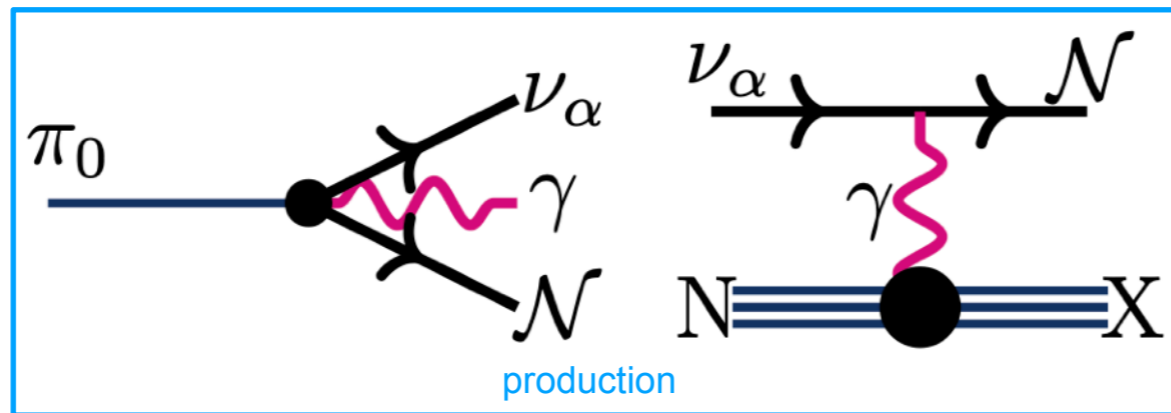


Minerva NUMI electron-neutrino scattering data selection efficiency.



See arXiv: 2105.06470, 2206.07100

Neutrissimo Dominated



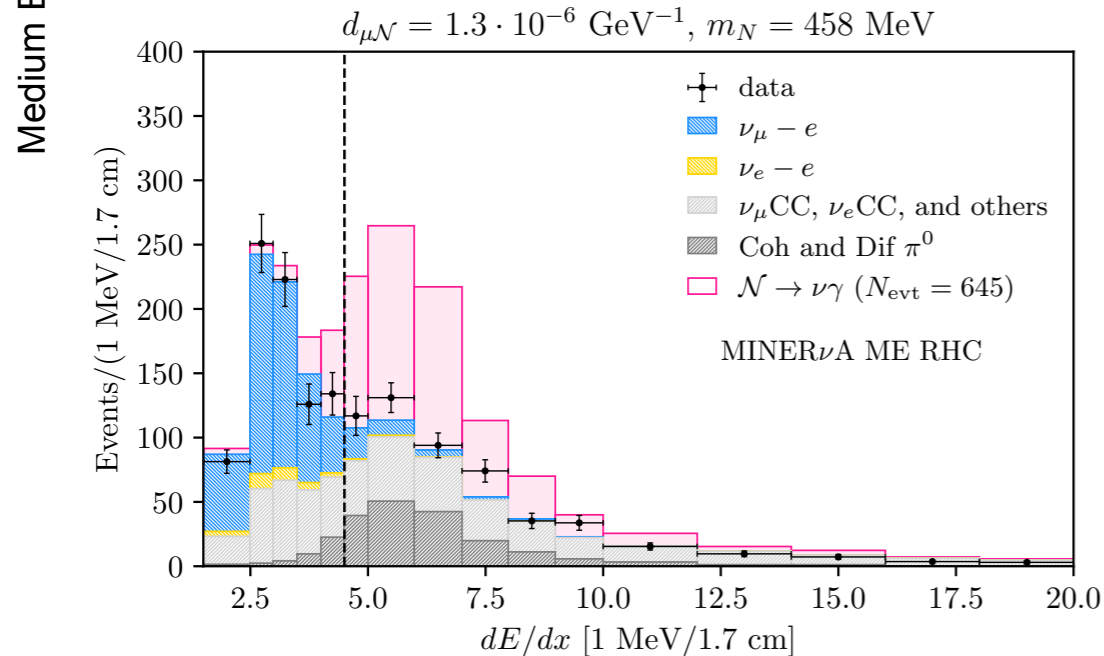
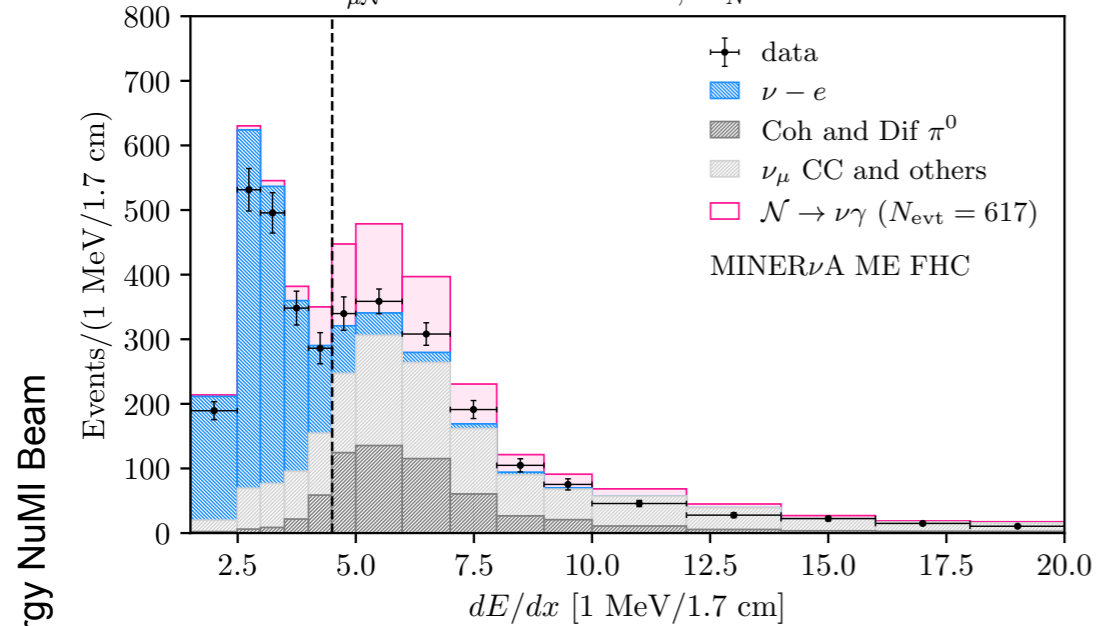
See also Magill et al 1803.03262, and Brdar et al 2007.15563.

Neutrissimo Dominated

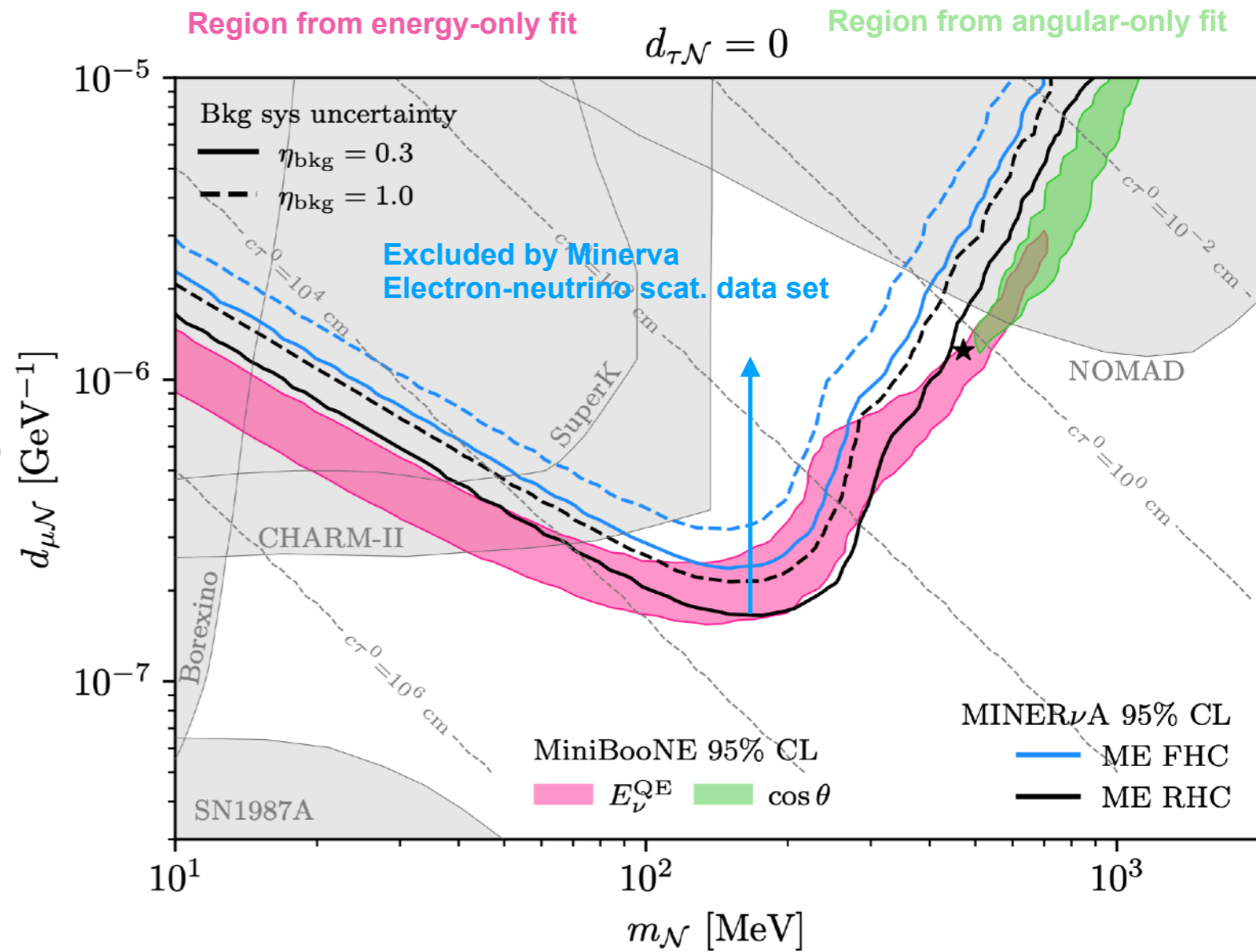
This model can be constraint by Minerva neutrino-electron scattering data sets.

Neutrino mode

$$d_{\mu\mathcal{N}} = 1.3 \cdot 10^{-6} \text{ GeV}^{-1}, m_{\mathcal{N}} = 458 \text{ MeV}$$

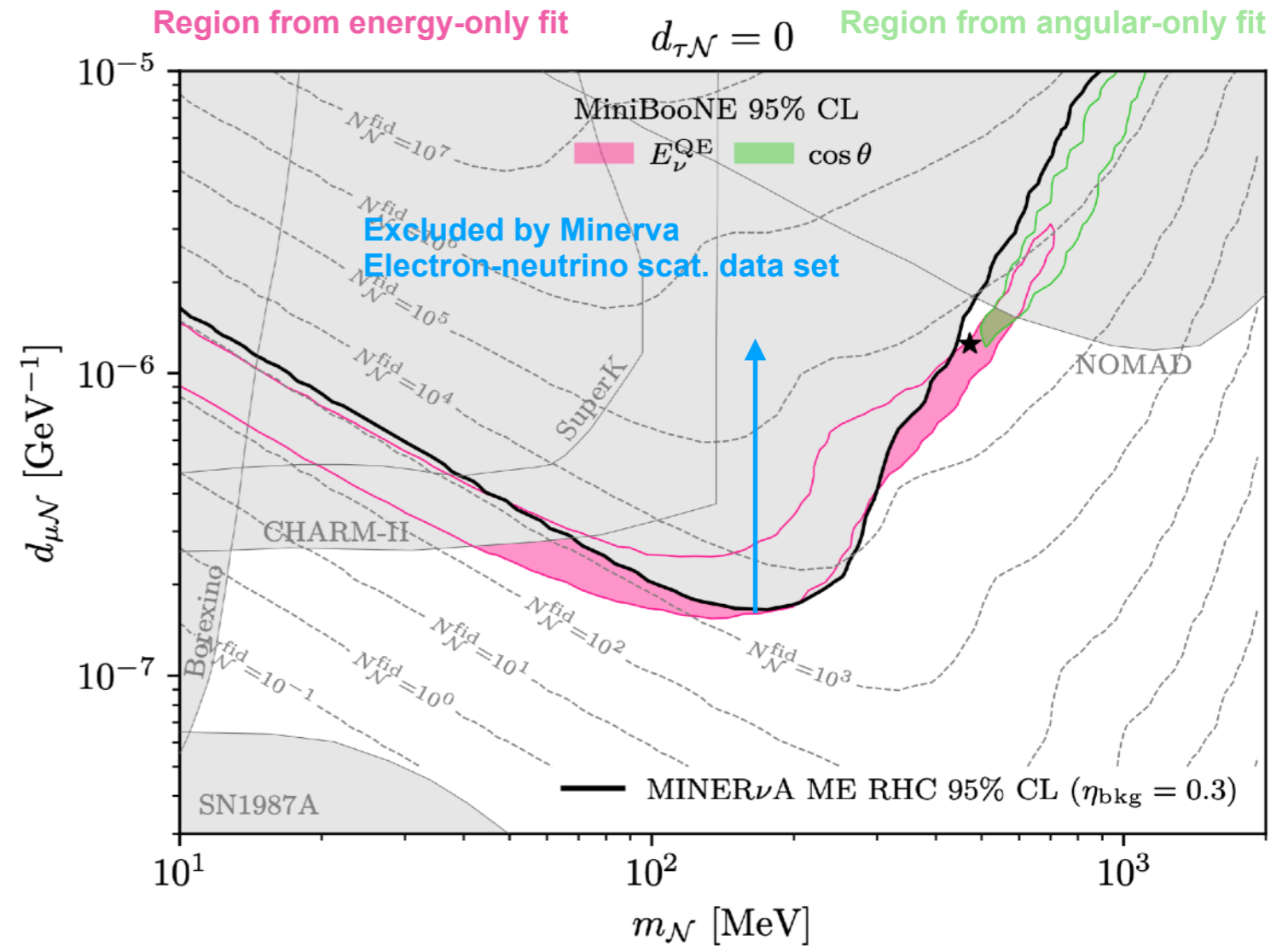
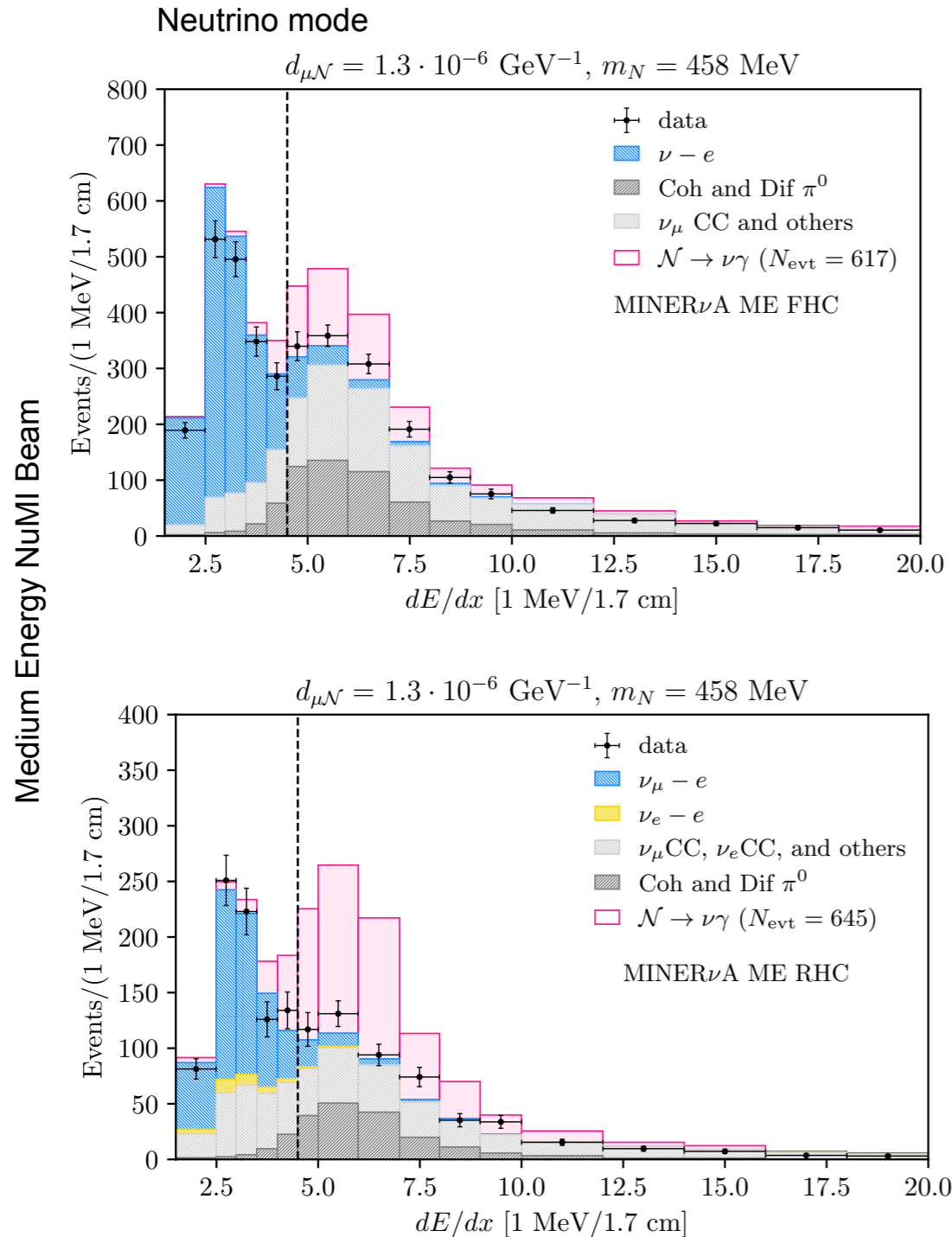


Antineutrino mode



Neutrissimo Dominated

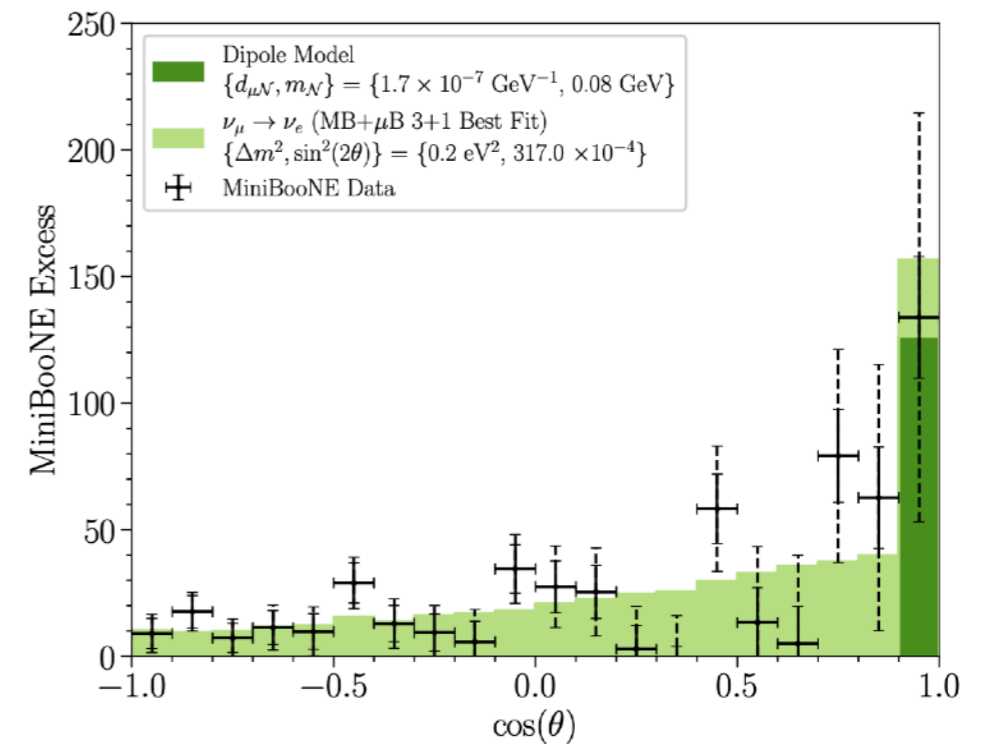
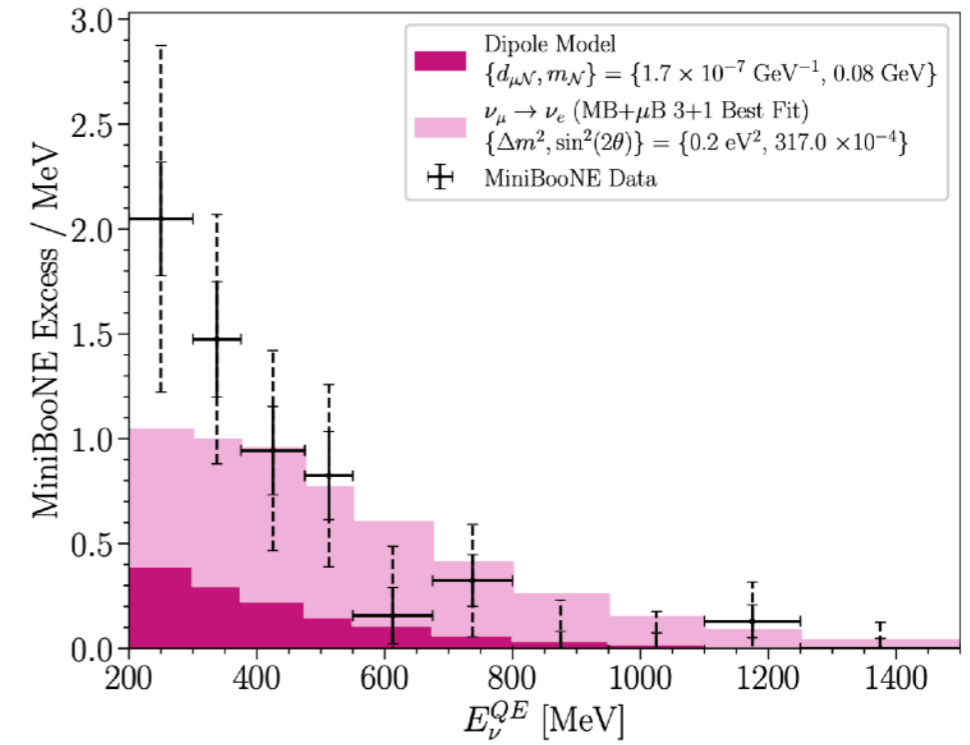
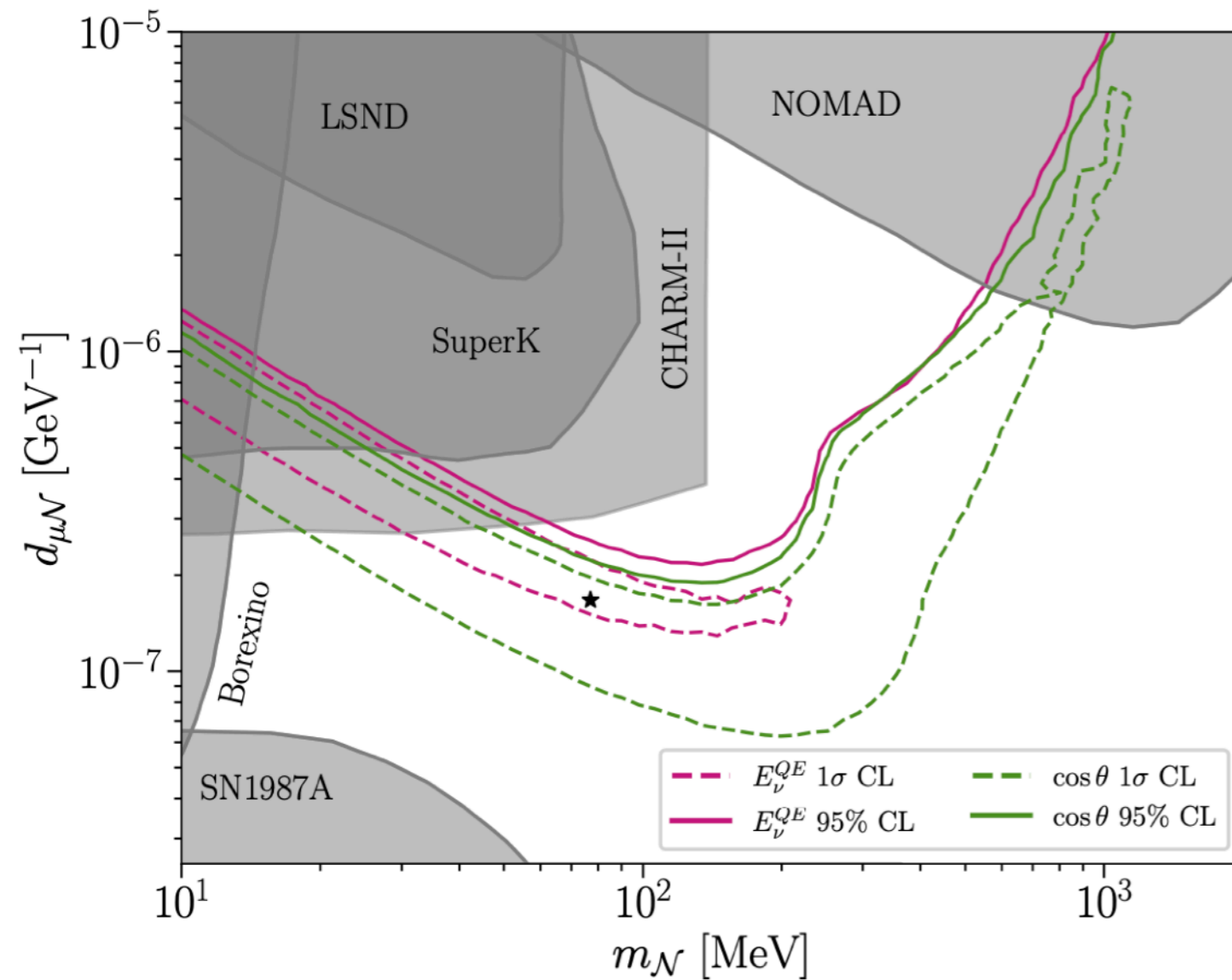
This model can be constraint by Minerva neutrino-electron scattering data sets.



A dedicated Minerva analysis should be sensitive to the entire MiniBooNE a preferred region.

Oscillation Dominated

Subleading Neutrissimo contribution avoids current constraints



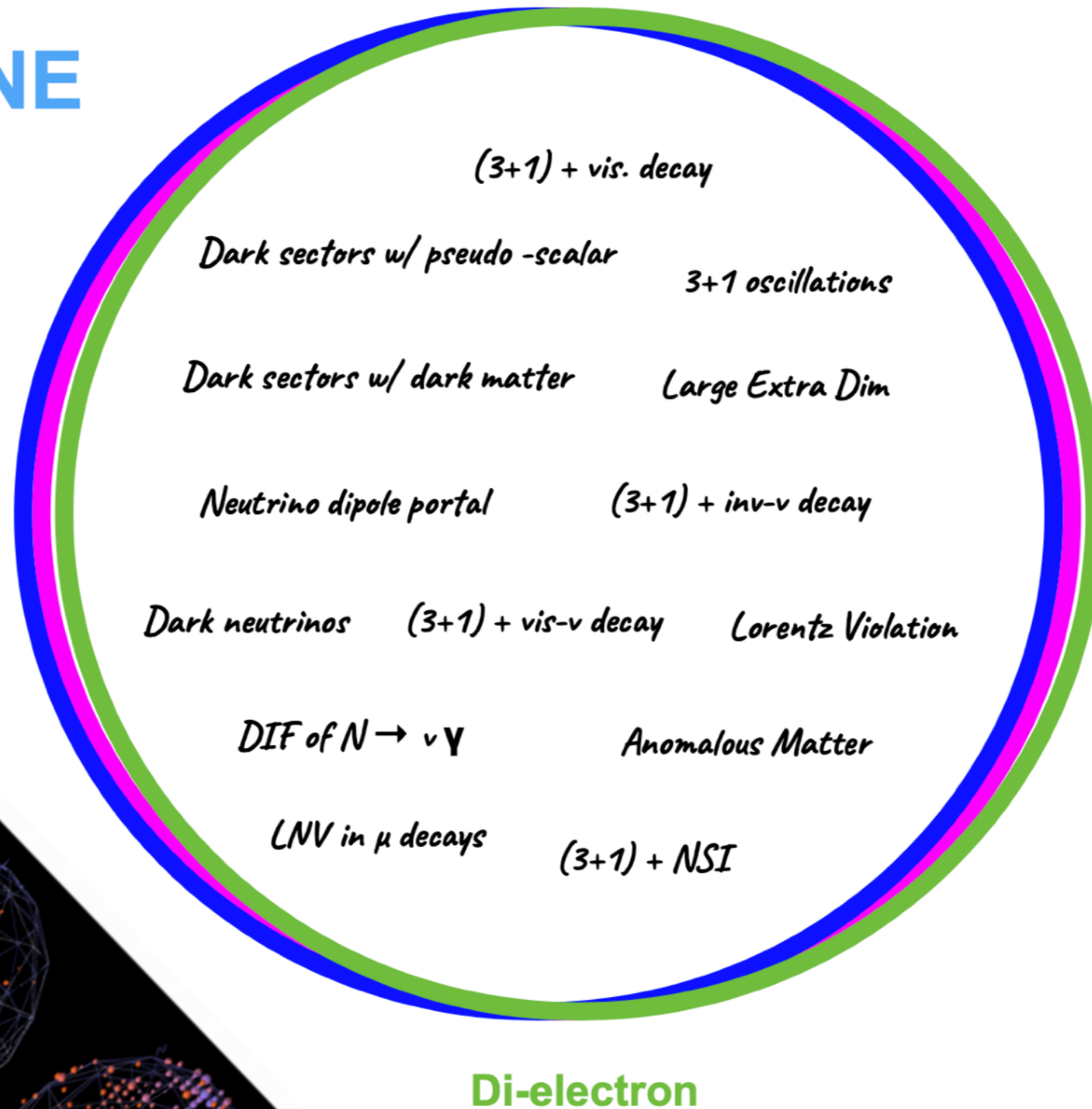
Outline

- Why go beyond vanilla sterile neutrinos?
- The garden of forking paths
- Non-vanilla sterile neutrinos
- Other explanations of MiniBooNE:
 - Single electron
 - Single photon
 - Di-electron
- Future

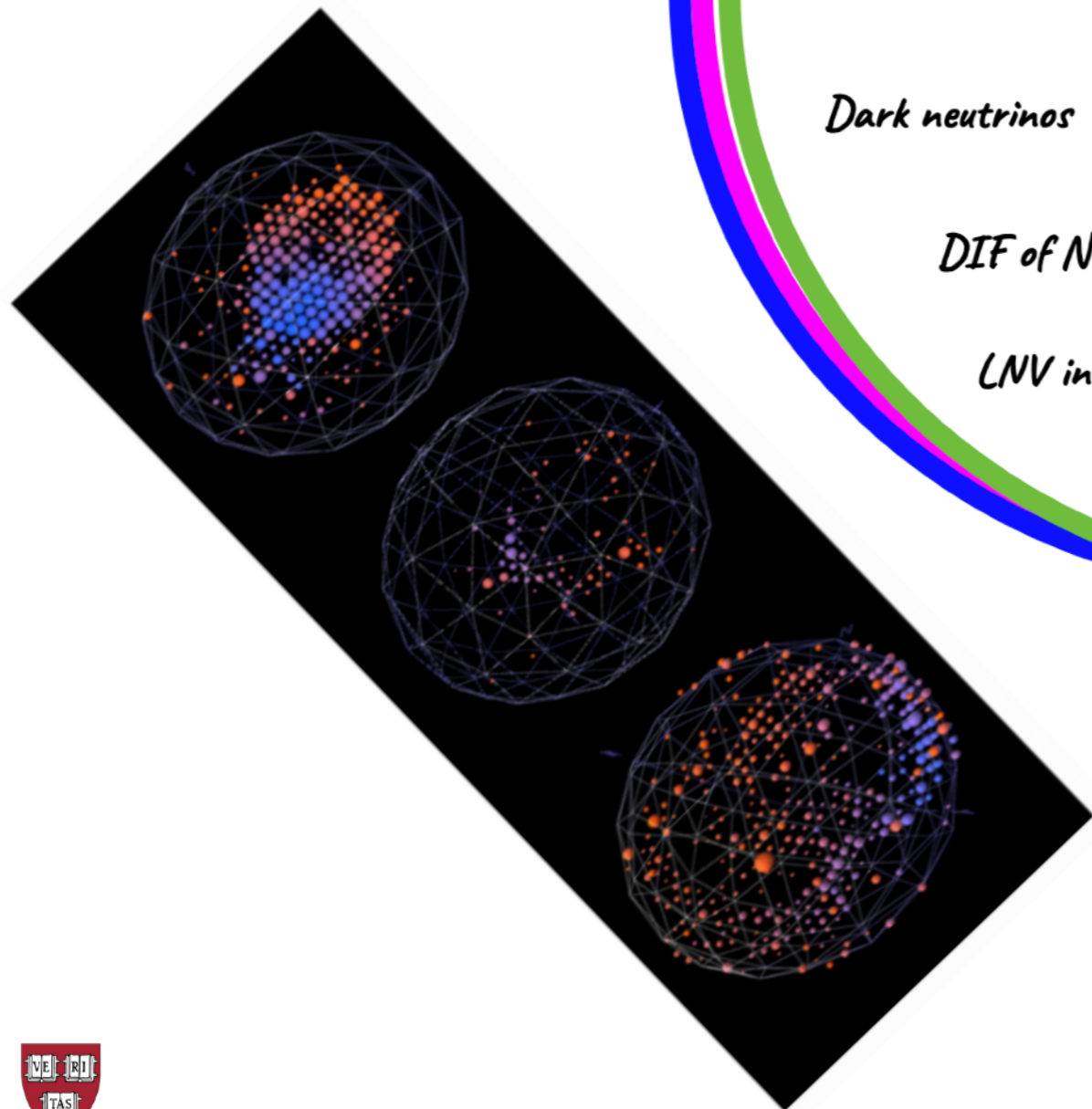
The MiniBooNE Lens

Single photon

Single electron



Di-electron

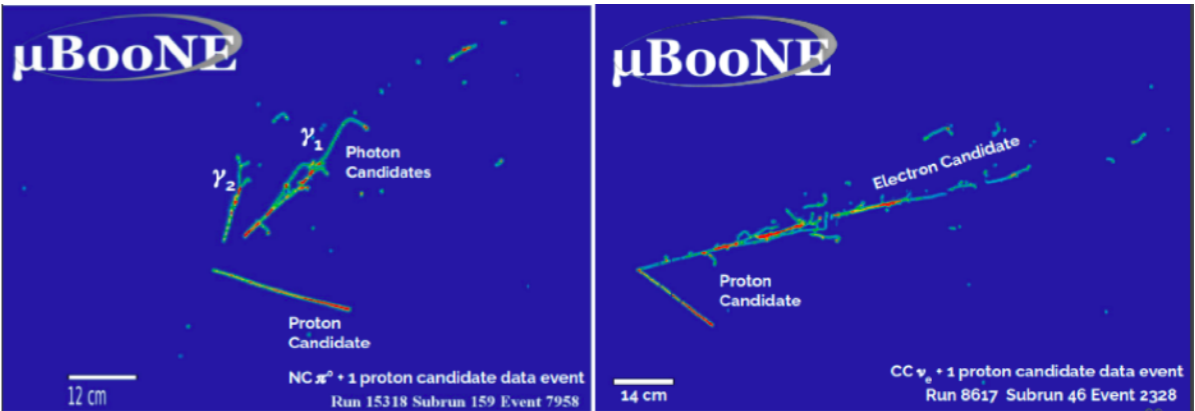
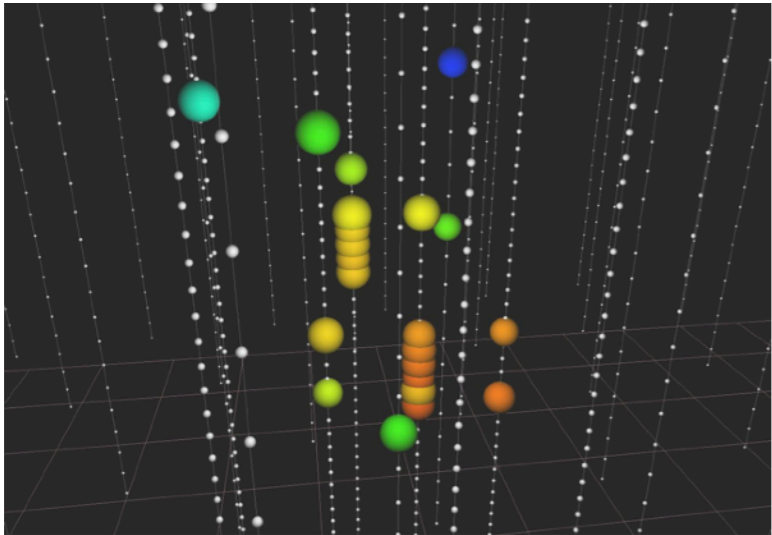
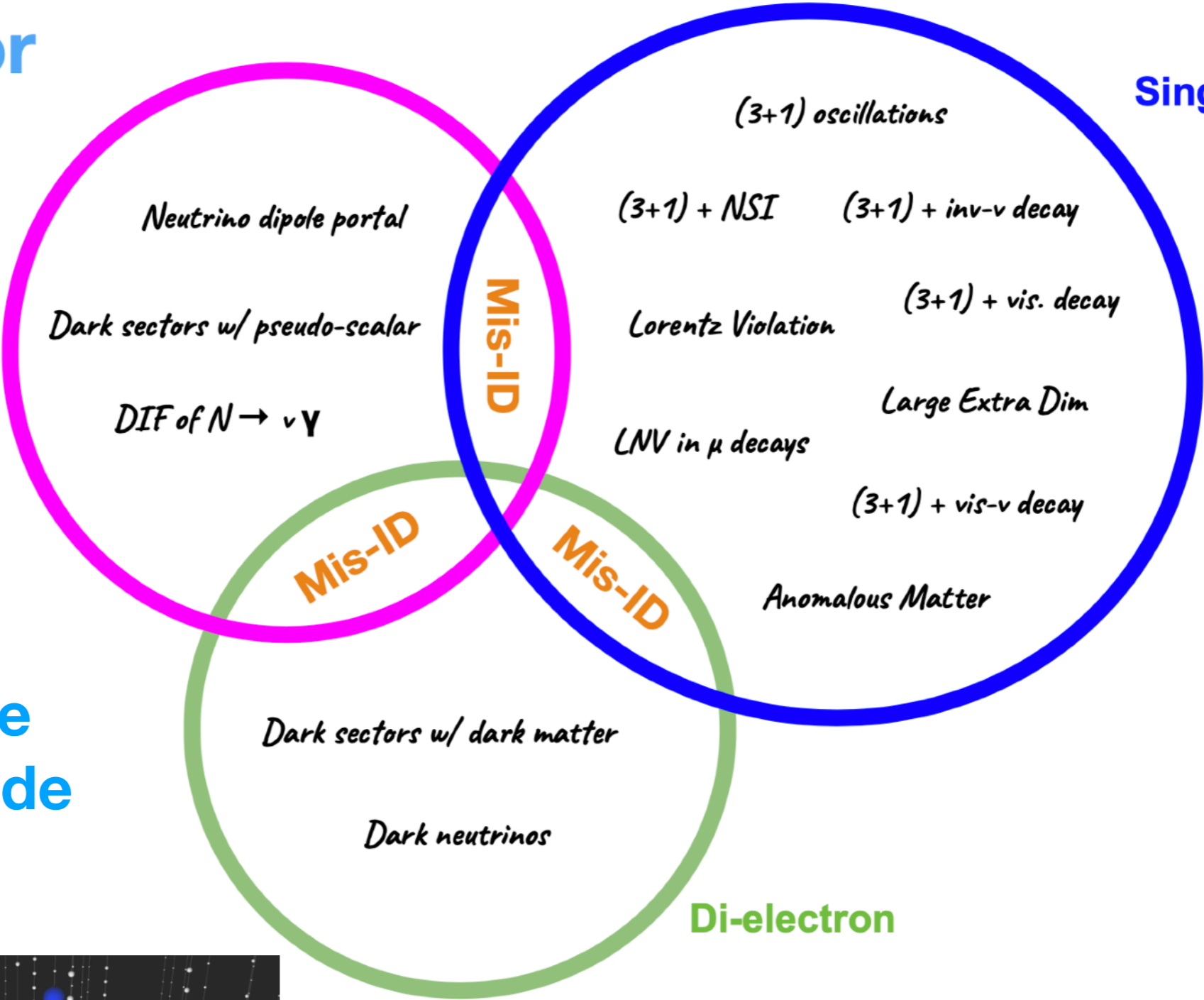


SBN Tricolor Lens

Single photon

Single electron

Also IceCube
Double cascade
search



Take home message

- ❖ The short-baseline anomalies are an unresolved puzzle in neutrino physics
- ❖ Minerva and T2K offer already important constraints on new models. Gas Argon TPC of T2K specially useful.
- ❖ Upcoming results from MicroBooNE, ICARUS, and others will help constraint these models.
- ❖ Current constraints only by phenomenologist. Need experiments to do these analyses!
- ❖ We need a combination of benchmark points of new models and full scans.



May your physics be
BSM!

New Explanations: Not yet dead!



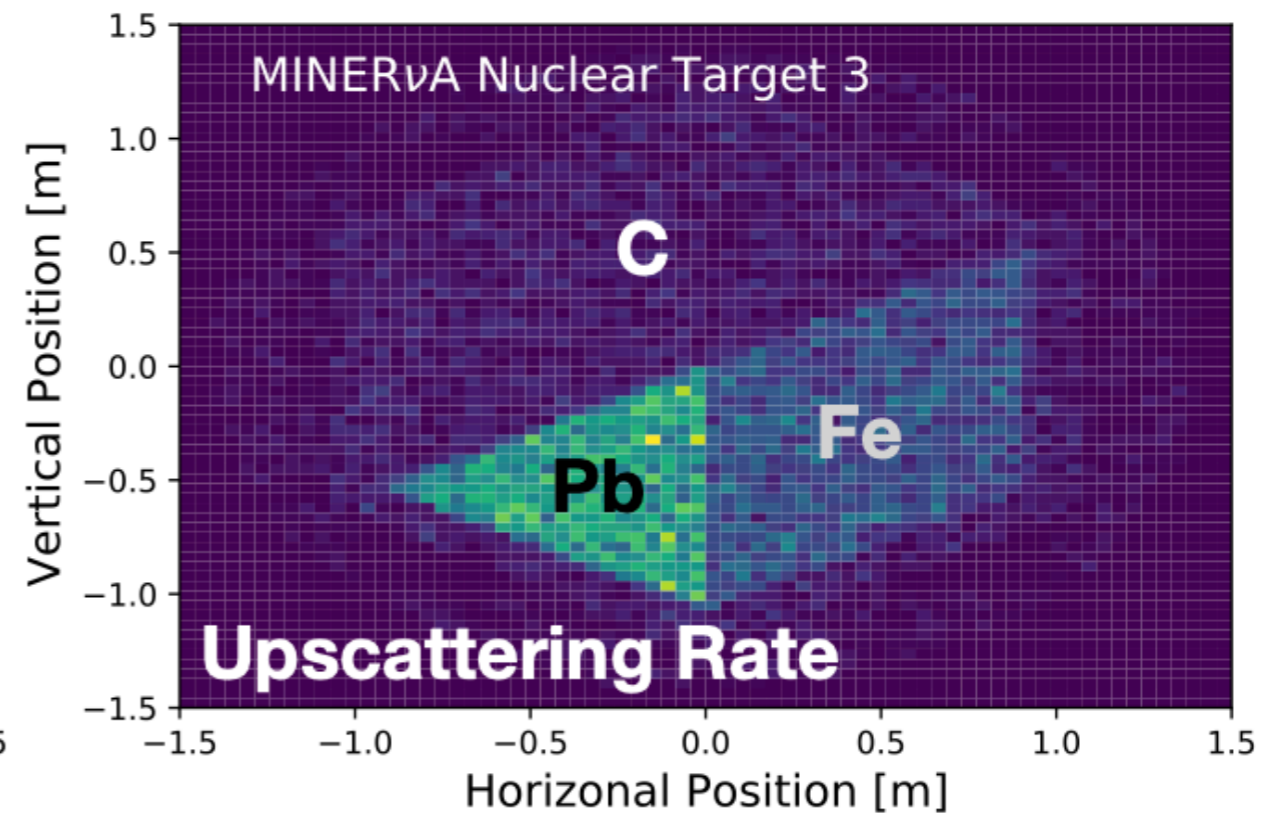
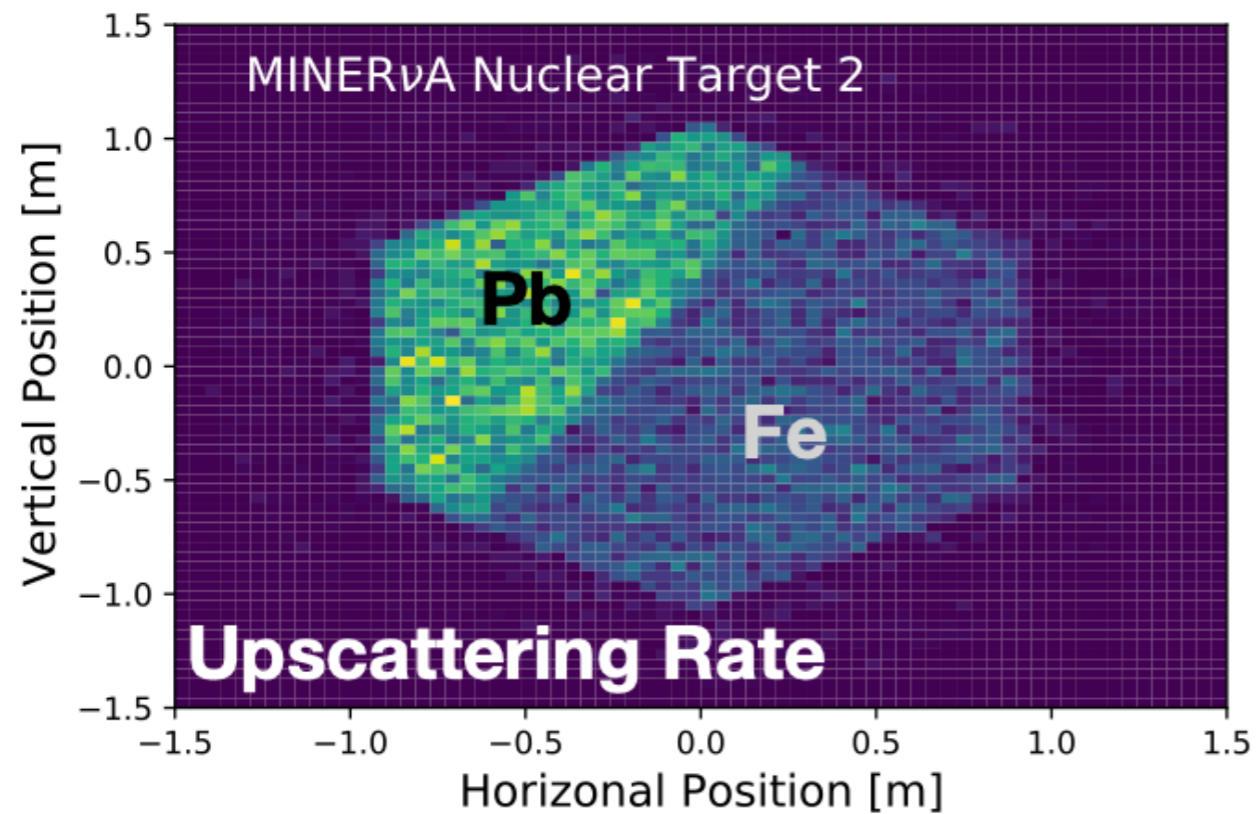
<https://www.youtube.com/watch?v=uBxMPqxJGqI>

Thank you!

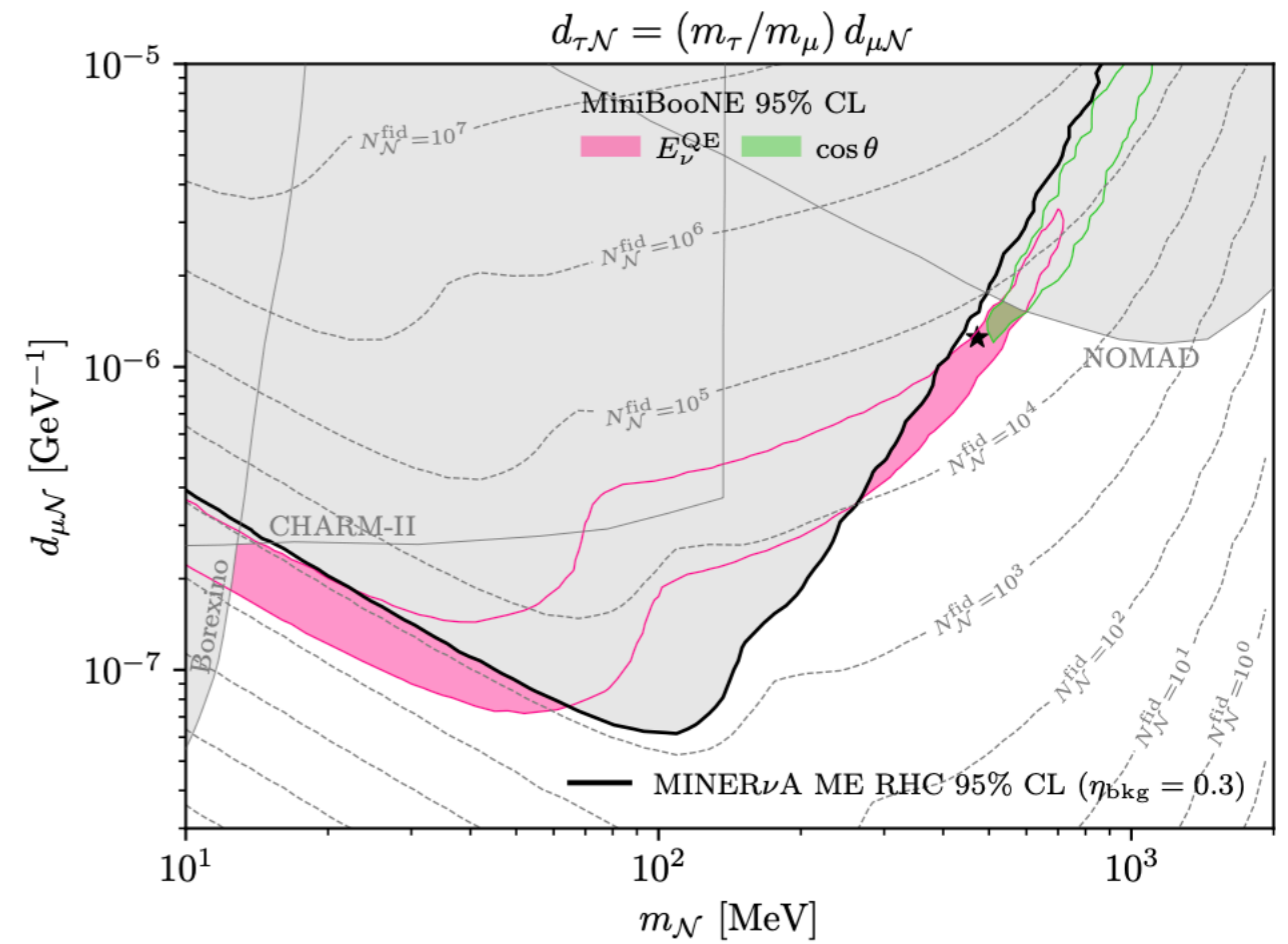
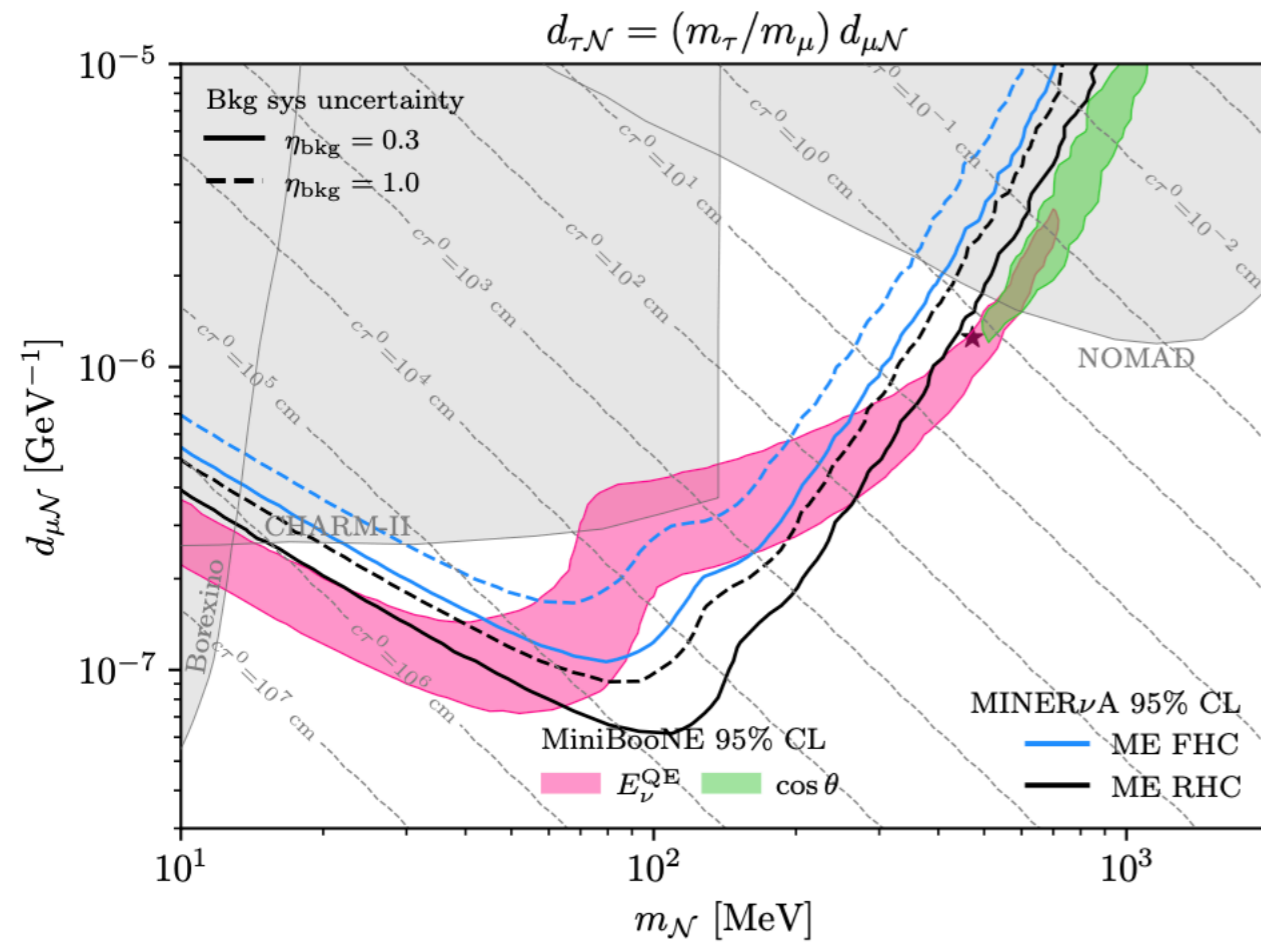


Bonus slides

Minerva Neutrissimo Production

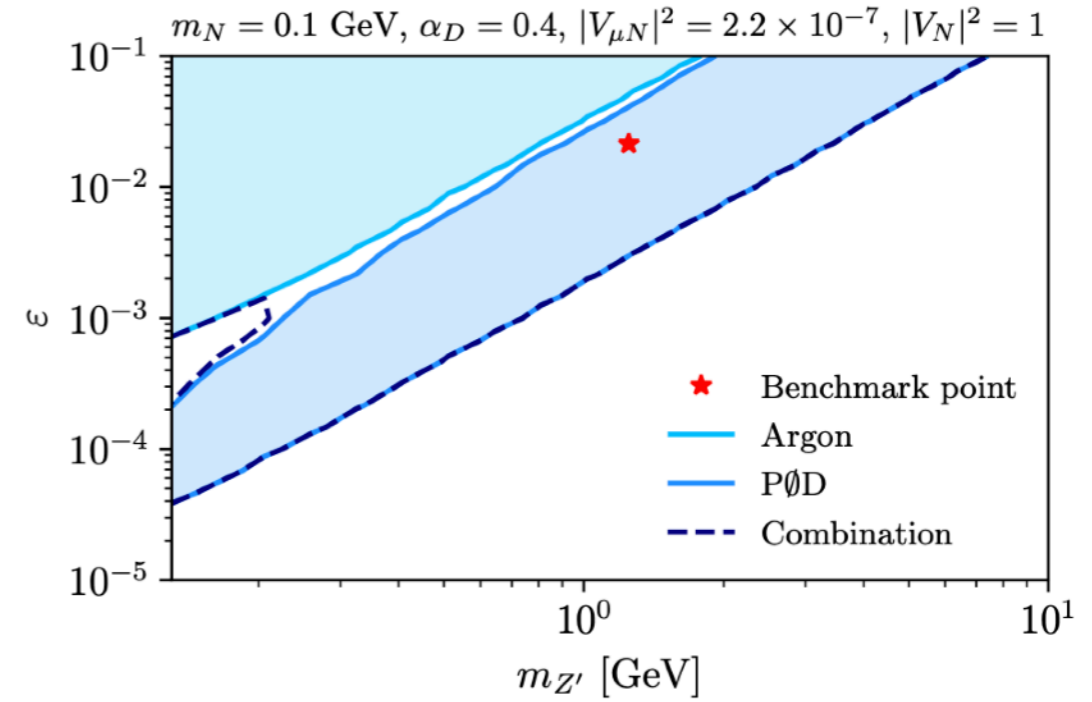
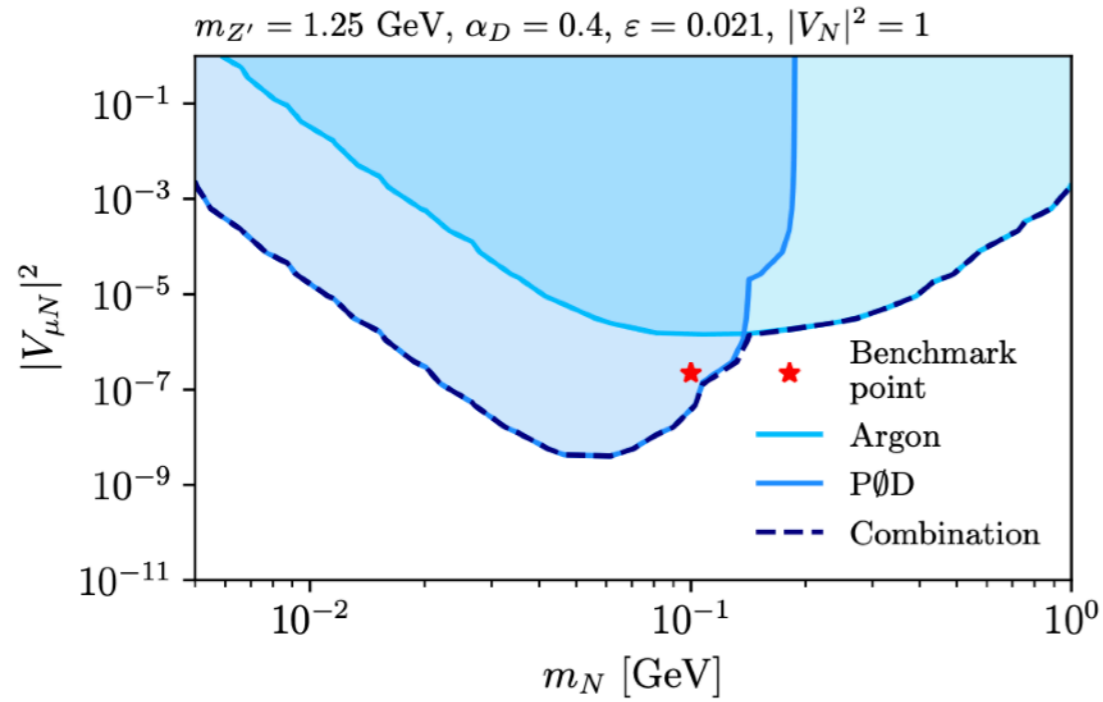


Neutrissimo with Tau Mixing

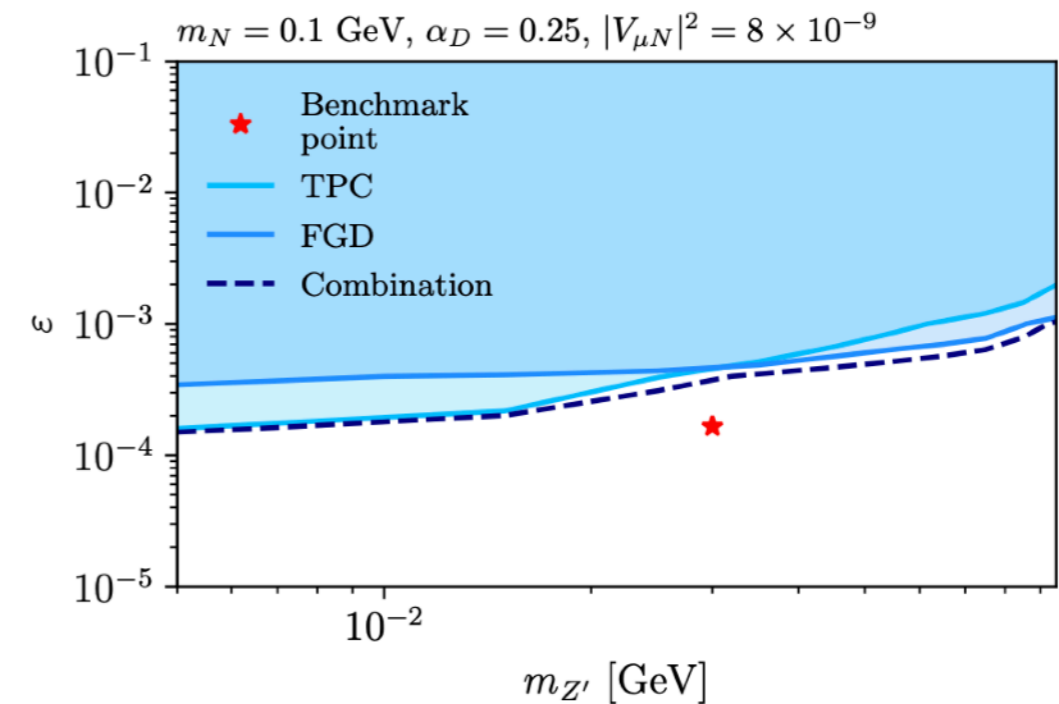
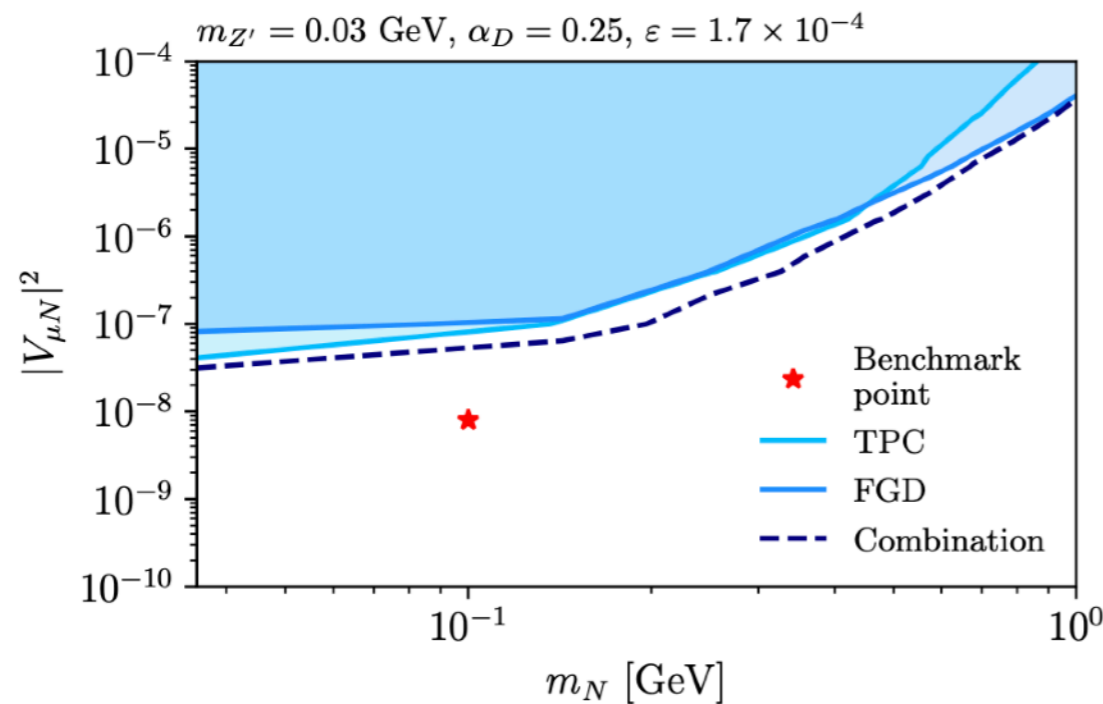


Dark Neutrino Production Regions

Heavy mediator scenario



Light mediator scenario

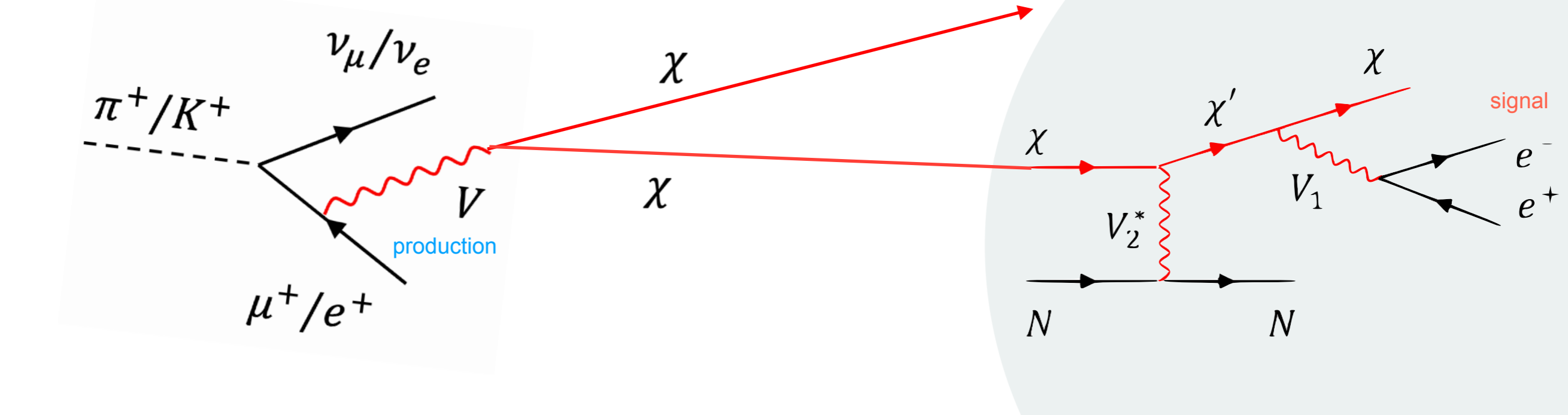


Dark Photon With Upscattering

B. Dutta et al. 2110.11944

Booster Beam

MiniBooNE detector

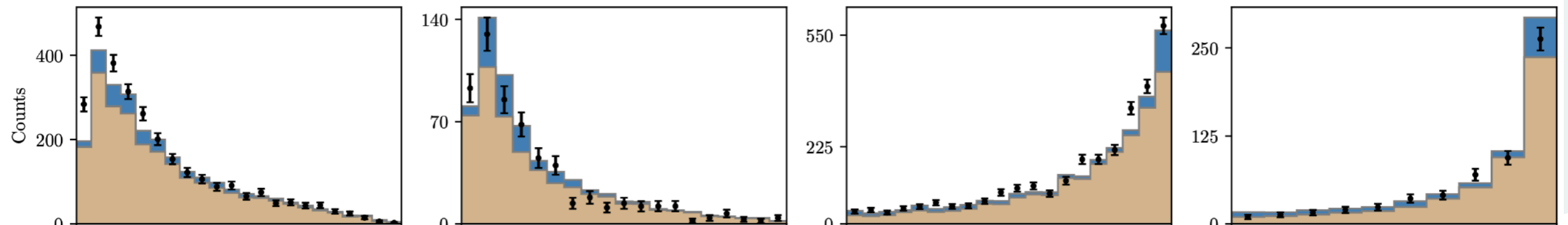


ν -mode

$\bar{\nu}$ -mode

ν -mode

$\bar{\nu}$ -mode



Energy distribution

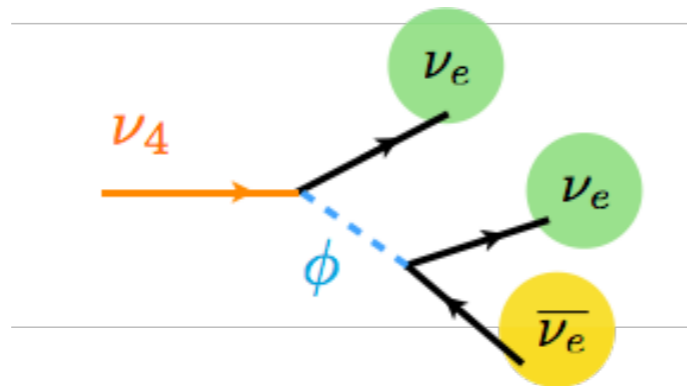
Angular distribution

χ Upscattering
 MiniBooNE Background

Vector-portal dark matter			
Scenario	$(m_{V_1}, m_{V_2}, m_\chi, m_{\chi'})$	$\epsilon_1 \epsilon_2 g_2'^2 / (4\pi)$	χ^2/dof
Single	(17, -, 8, 40)	3.6×10^{-9}	2.5
Double	(17, 200, 8, 50)	1.3×10^{-7}	2.2

Visible Neutrino Decay in Beam

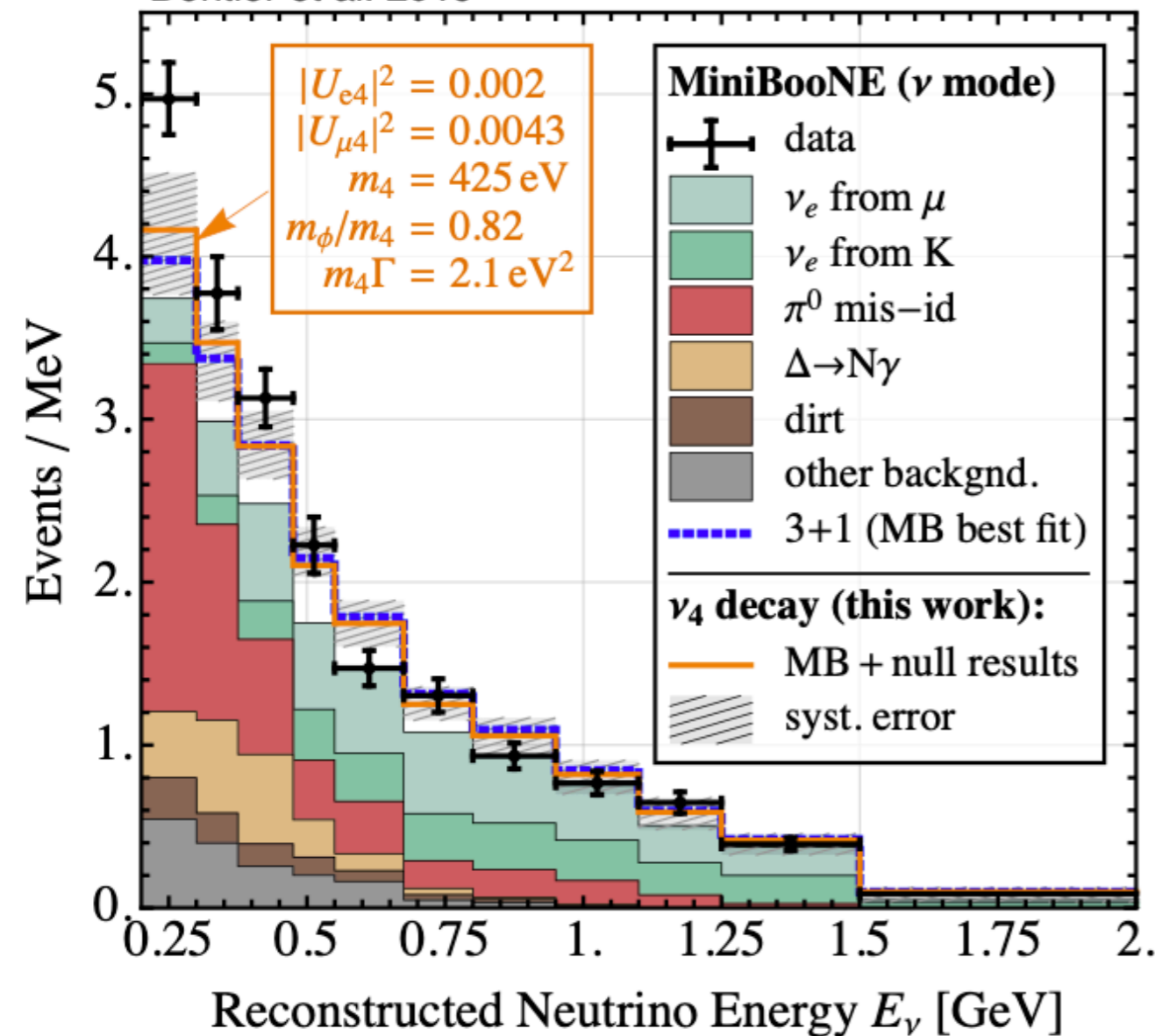
Dentler et al 1911.01427
Gouvea et al 1911.01447



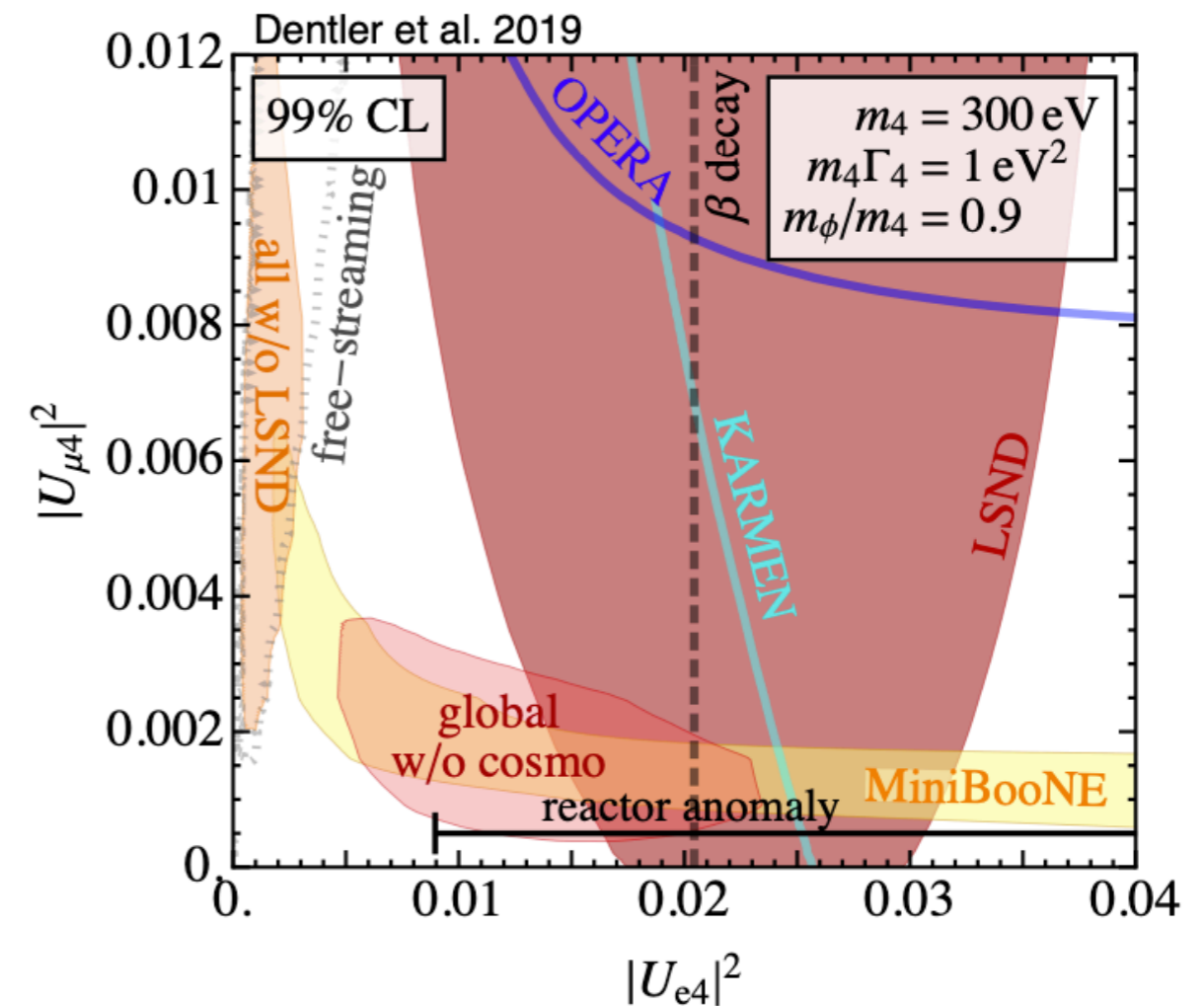
Heavy neutrino component in the neutrino beam decays into lighter less energetic neutrinos.

These neutrinos interact in the detector and produce the excess.

Dentler et al. 2019



$$\mathcal{L} \supset -g \bar{\nu}_s \nu_s \phi - \sum_{a=e,\mu,\tau,s} m_{\alpha\beta} \bar{\nu}_\alpha \nu_\beta$$

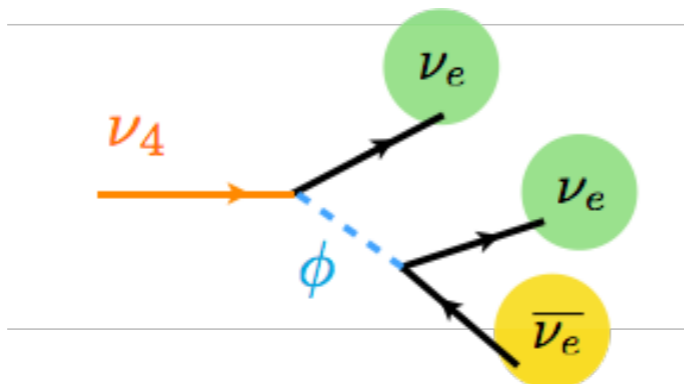


See also Fisher et al 1911.01447

Carlos Argüelles (Neutrino 2022)

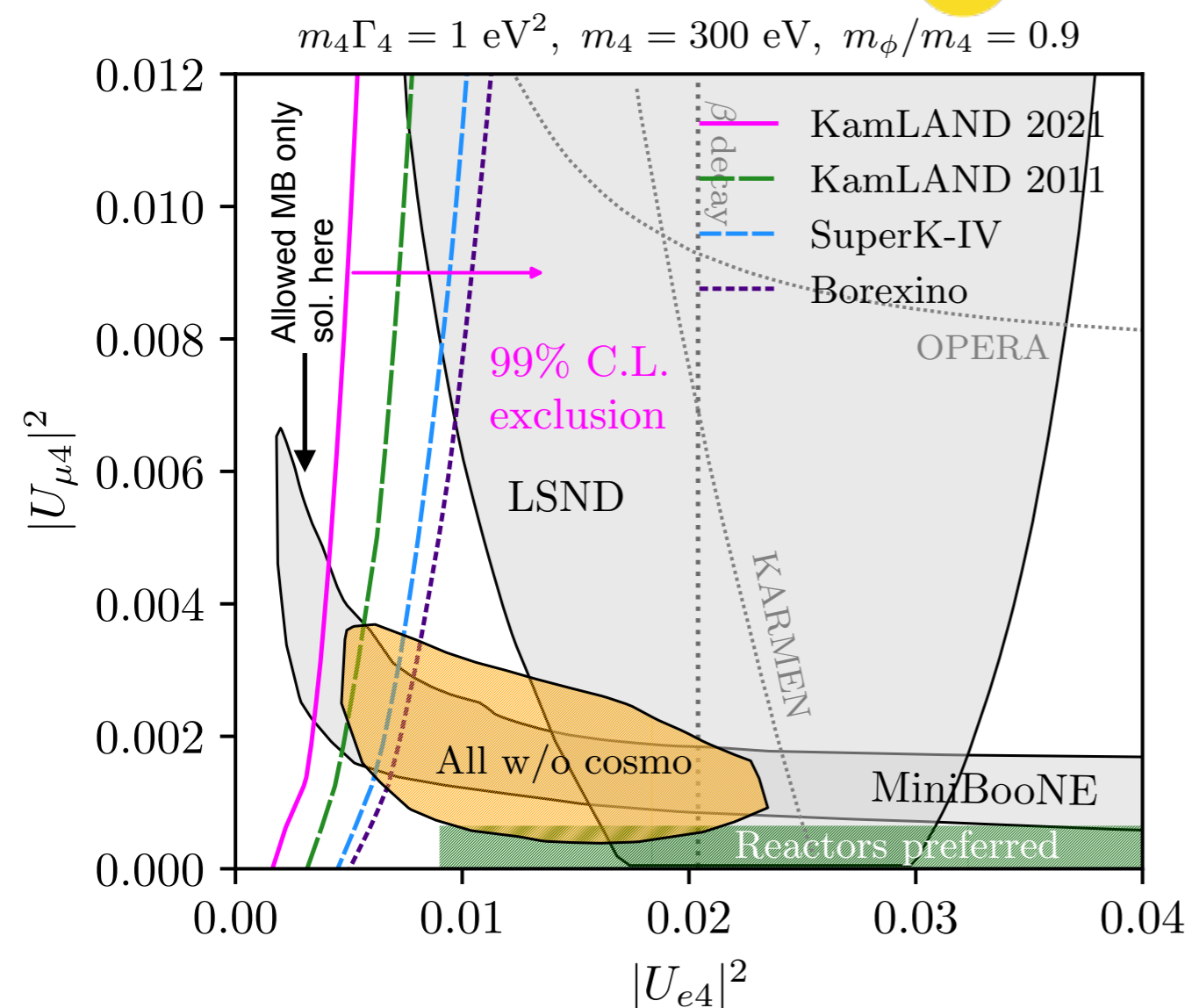
Visible Neutrino Decay in Beam

Dentler et al 1911.01427
Gouvea et al 1911.01447

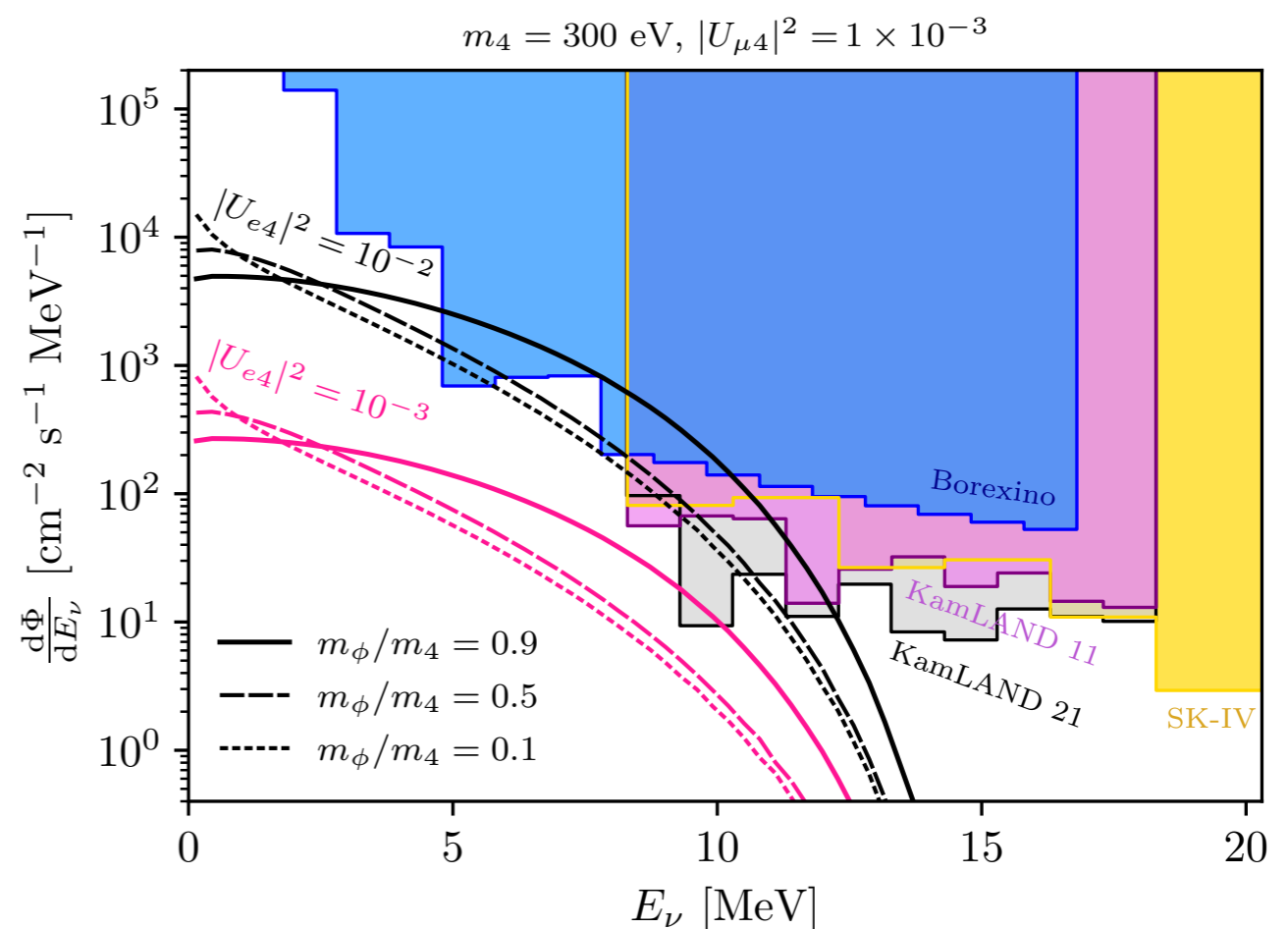


Constrains from antineutrinos from the Sun do not allow this to be a global solution of the anomalies.

MiniBooNE alone can be explained.



M. Hostert & M. Pospelov 2008.11851

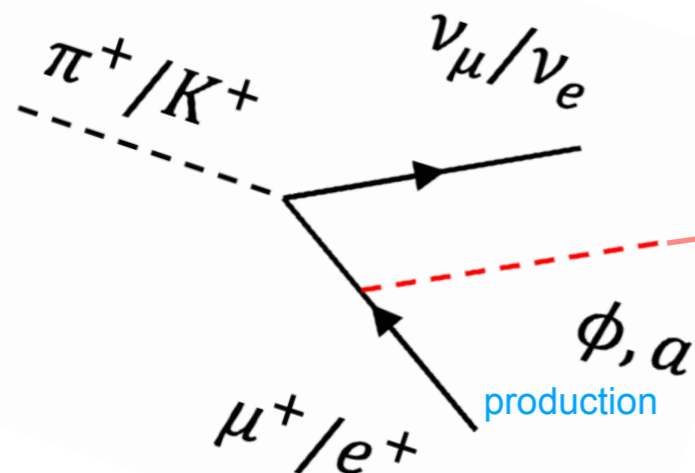


Visible decay predicts emission of antineutrinos from the Sun!

Idea 5: Scalar With “Primakoff” Upscattering

B. Dutta et al. 2110.11944
See also Abdallah et al 2202.09373

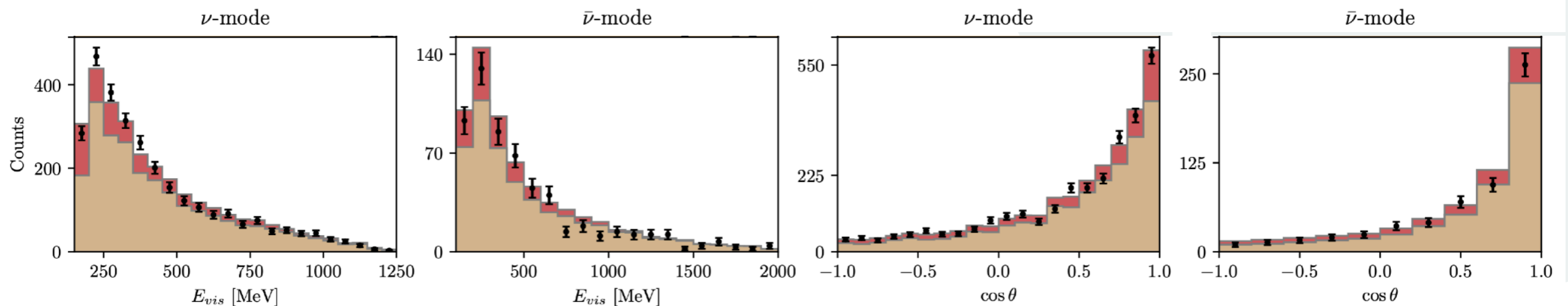
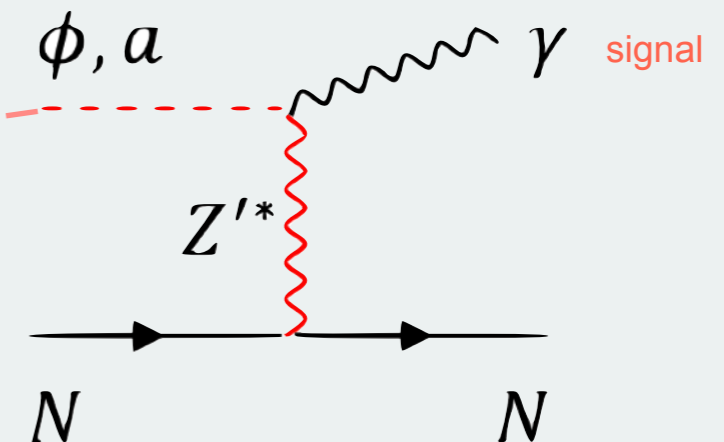
Booster Beam



$$\mathcal{L}_S \supset g_\mu \phi \bar{\mu} \mu + g_n Z'_\alpha \bar{u} \gamma^\alpha u + \frac{\lambda}{4} \phi F'_{\mu\nu} F^{\mu\nu} + \text{h.c.},$$

$$\mathcal{L}_P \supset i g_\mu a \bar{\mu} \gamma^5 \mu + g_n Z'_\alpha \bar{u} \gamma^\alpha u + \frac{\lambda}{4} a F'_{\mu\nu} \tilde{F}^{\mu\nu} + \text{h.c.}$$

MiniBooNE detector



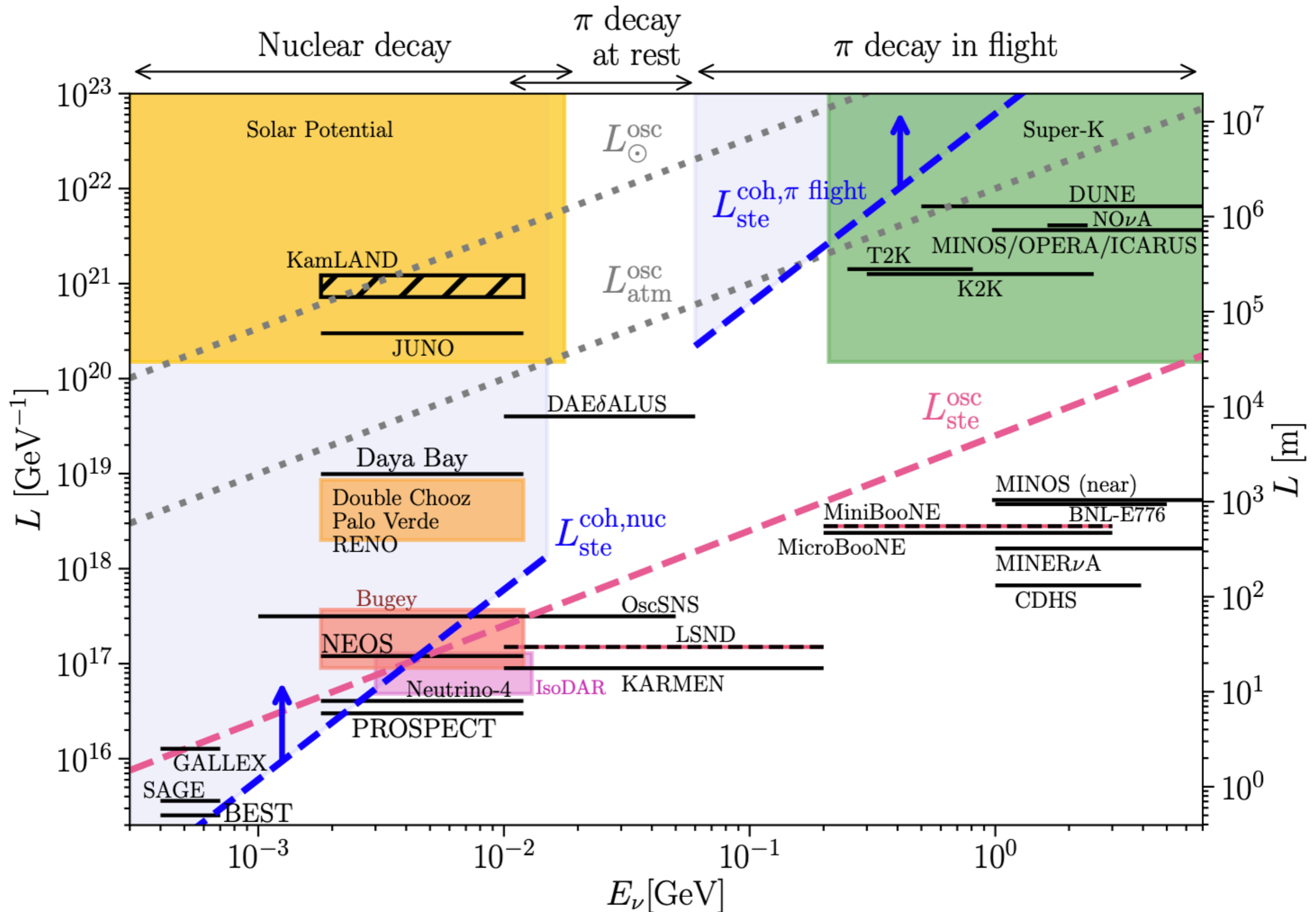
Energy distribution

Angular distribution

■ ϕ/a Dark Primakoff
■ MiniBooNE Background

Long-lived (pseudo)scalar			
Scenario	$(m_{Z'}, m_{\phi/a})$	$(g_\mu g_n \lambda) [\text{MeV}^{-1}]$	χ^2/dof
Scalar	(49, 1)	2.2×10^{-8}	1.6
Pseudoscalar	(85, 1)	5.9×10^{-7}	1.6

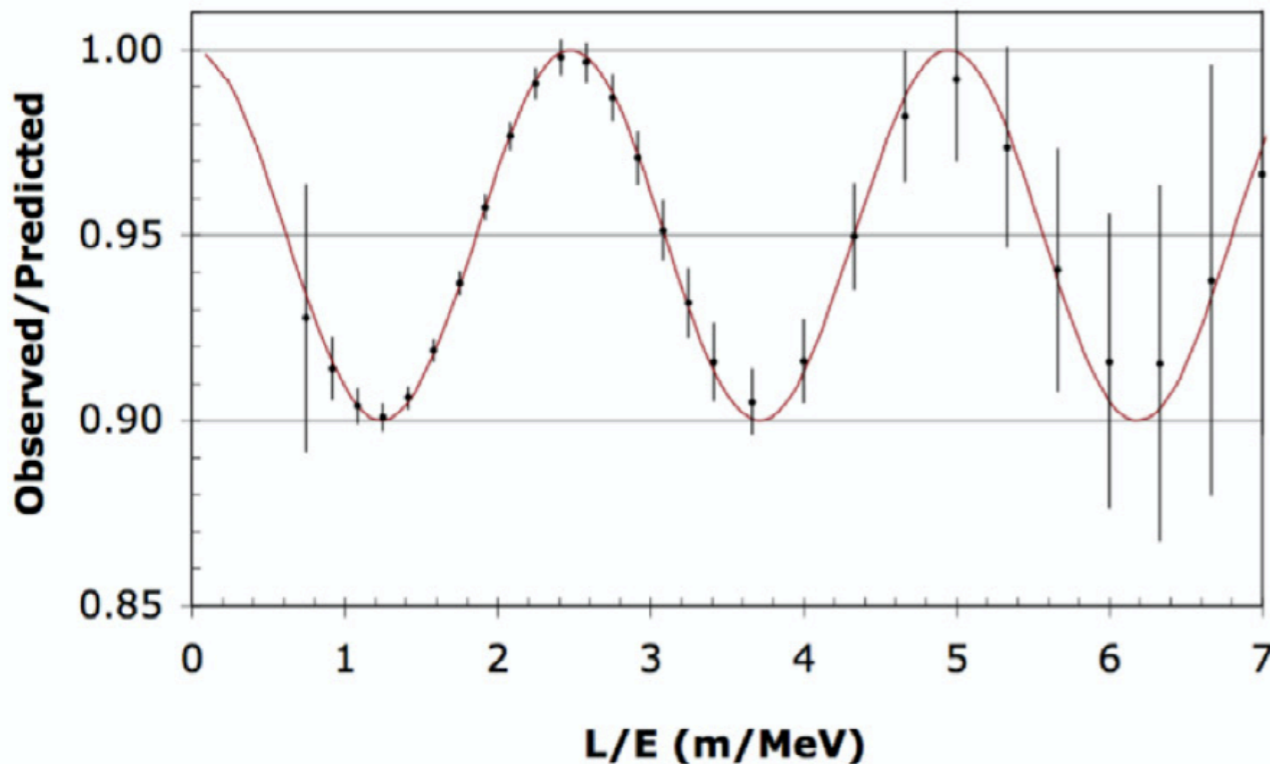
Where does it matter?



IsoDAR@Yemilab

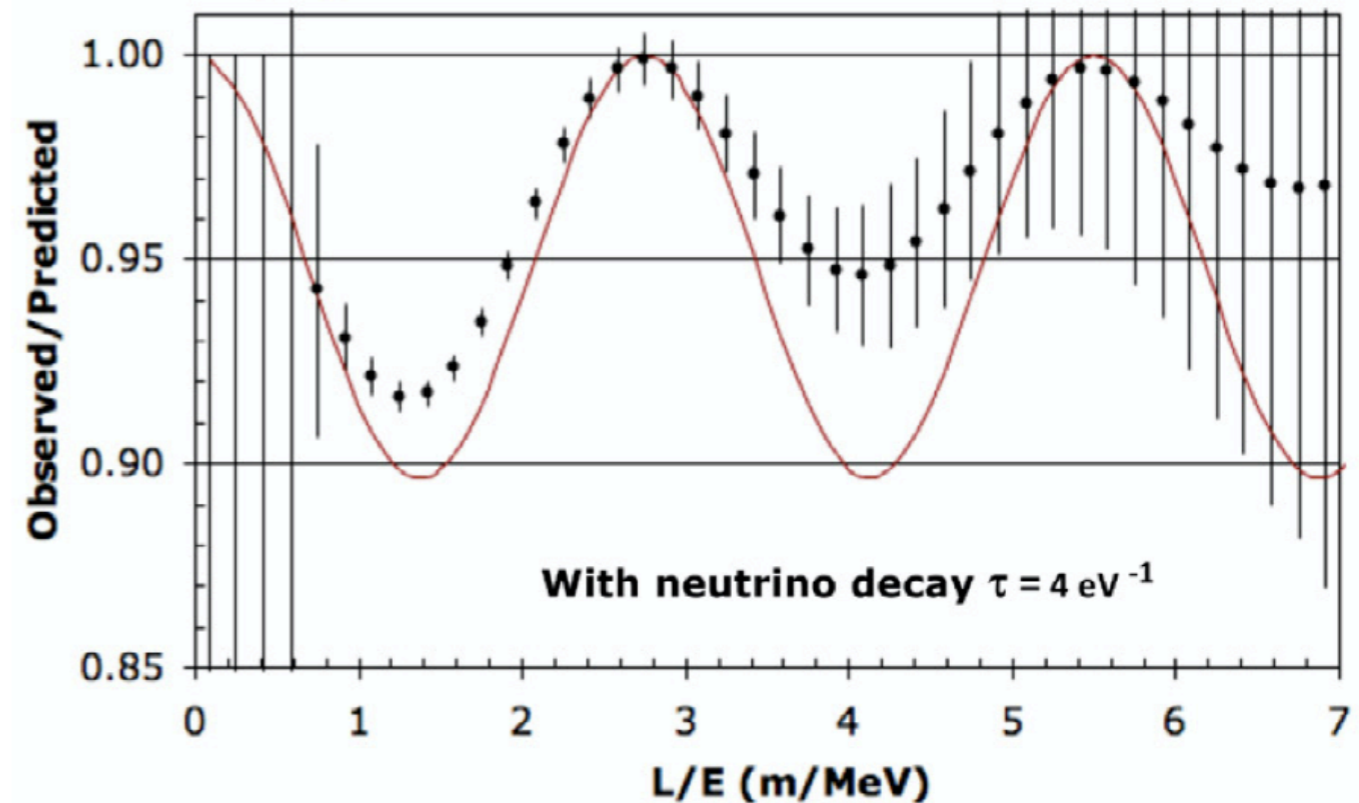
No decay

(3+1) Model with $\Delta m^2 = 1.0 \text{ eV}^2$ and $\sin^2 2\theta = 0.1$



With decay

(3+1) Model with $\Delta m^2 = 0.9 \text{ eV}^2$ and $\sin^2 2\theta = 0.1035$



IsoDAR with O(1M) events

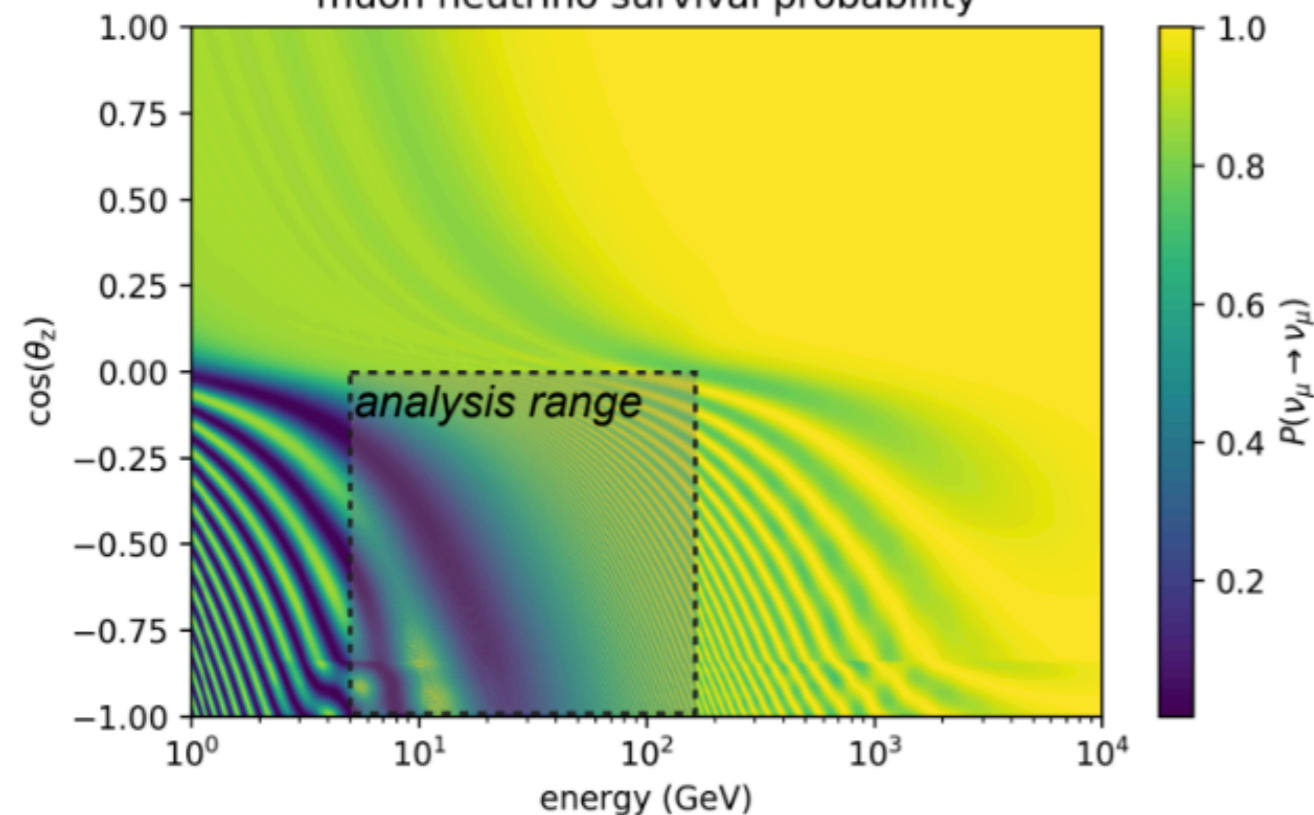
IsoDAR@Yemilab will conclusively rule out the 3+1 model, but also due to its ability to trace the oscillation wave see variants on this model such as 3+1+Decay

IceCube@Antartica

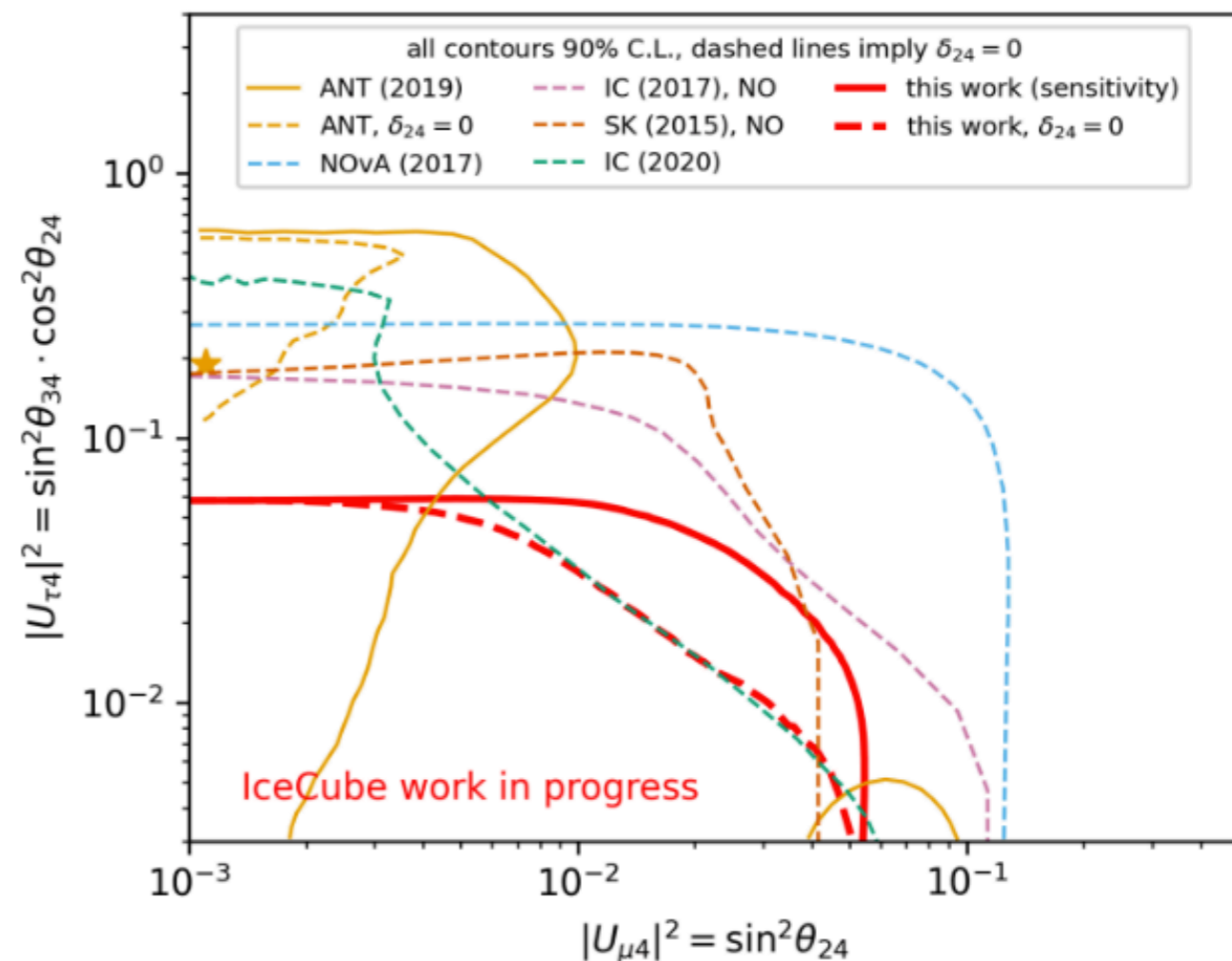
Talk by A. Trettin@PANIC2021

“Low” energies: 5 - 150 GeV

muon neutrino survival probability



- > very fast, unresolvable oscillations + distortion
- > IceCube: World-leading limits on $|U_{\tau 4}|^2$ and $|U_{\mu 4}|^2$!



Projected sensitivity of sterile search with 8 years of DeepCore data

IceCube will continue improving muon neutrino disappearance searches.
“Low energy” sample (<100 GeV) still not studied.

Menu of other explanations

New signatures

Gninenko 1107.0279

Magill et al 1803.03262

Heavy neutrino $O(\text{MeV})$, magnetic moment, decay

Bertuzzo et al 1807.09877, Ballett et al 1808.02916,
CA, Hostert, Tsai et al 1812.08768

Heavy neutrino $O(1-100\text{MeV})$, light Z' , decay

Heavy Neutrino Decay

Bai et al 1512.05357

Dentler et al 1911.01427,
de Gouvea et al 1911.01447,
Hostert & Pospelov 2008.11851

Heavy $O(100\text{MeV})$ decay to ν_e

Fisher et al 1909.0956,
CA, Foppiani, Hostert 2109.03831

Heavy $O(100\text{MeV})$ decay to photon

Oscillations+X

Assadi et al 1712.08019

Resonant matter effect

Moss et al 1711.05921, Moulai et al 1910.13456

Steriles +decay

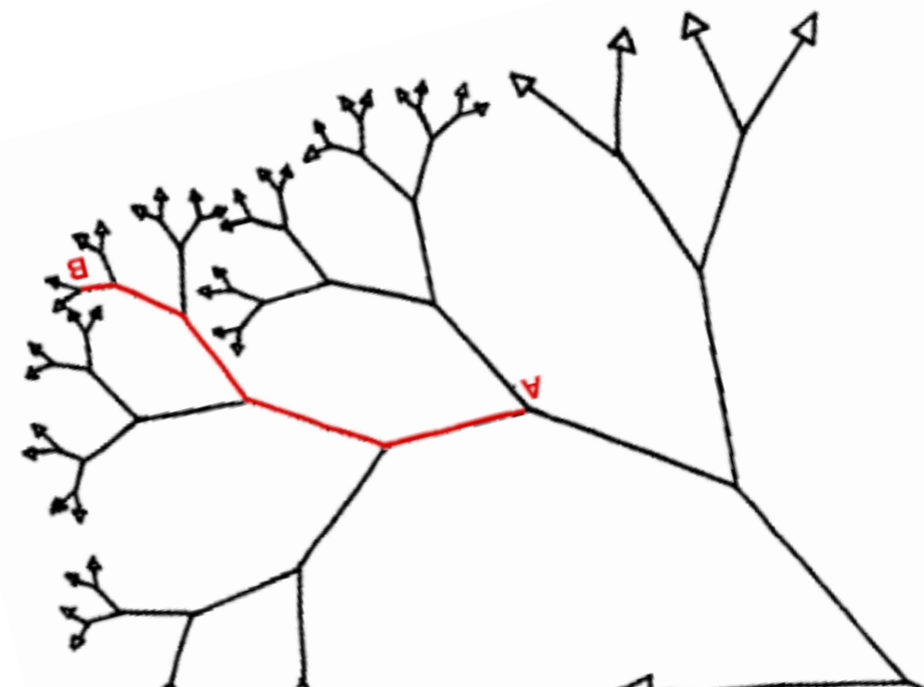
Liao et al 1810.01000

Steriles + NCNSI + CCNSI

More than one at a time

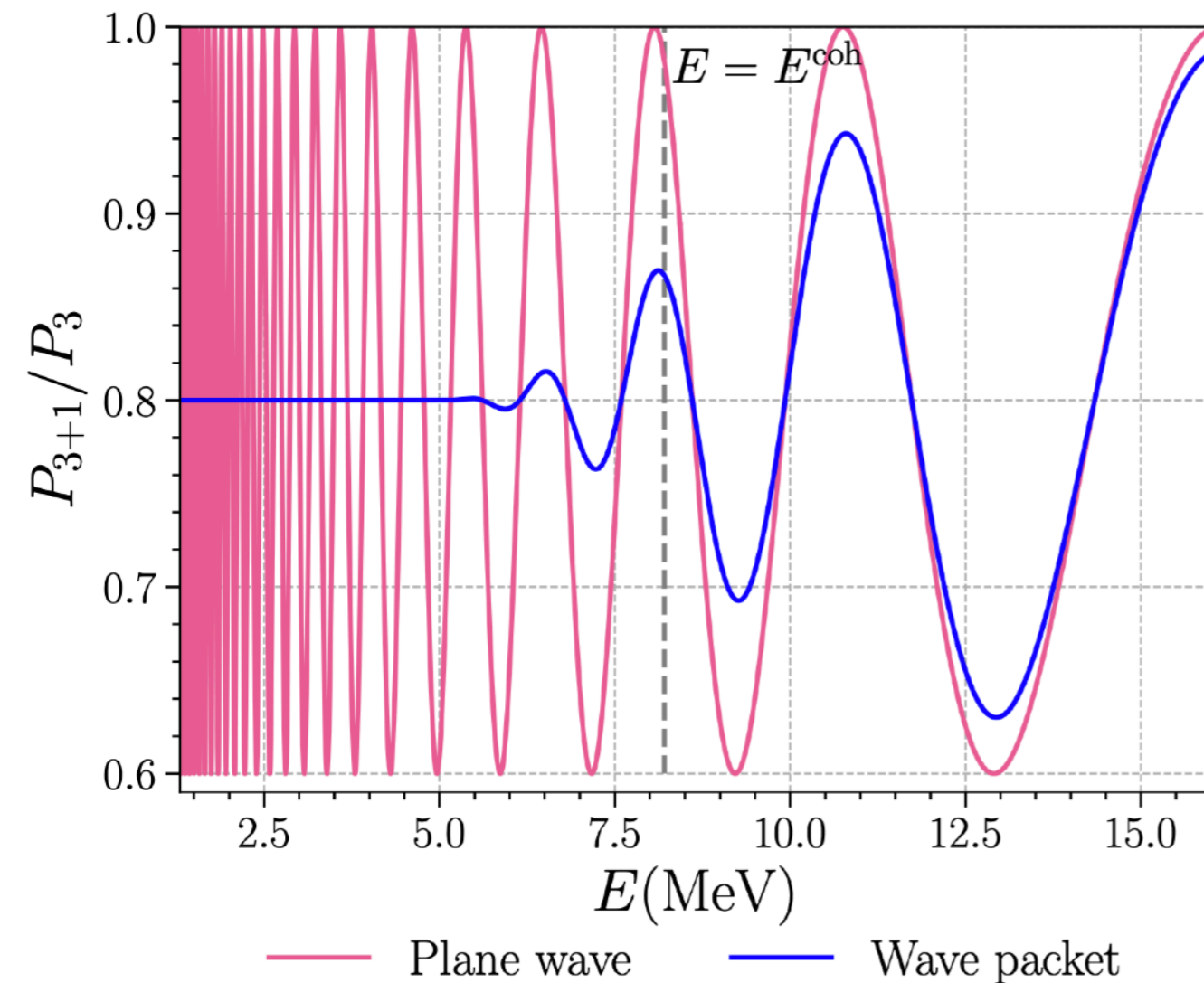
S. Vergani et al arXiv:2105.06470

Light Sterile + Heavy neutrino $O(100\text{MeV})$,
magnetic moment



Oscillation probability in the Wave Packet formalism

$$L \cdot \Delta m_{41}^2 = 80 \text{ m} \cdot \text{eV}^2, \sin^2 2\theta_{14} = 0.4$$



$$P_{\alpha\beta} = \sum_{i=1}^n |U_{\alpha i}|^2 |U_{\beta i}|^2 + 2\text{Re} \sum_{j>i} U_{\alpha i} U_{\alpha j}^* U_{\beta i}^* U_{\beta j} \times$$

$$\times \exp \left\{ -2\pi i \frac{L}{L_{\text{osc}}^{ij}} - 2\pi^2 \left(\frac{\sigma_x}{L_{\text{osc}}^{ij}} \right)^2 - \left(\frac{L}{L_{\text{coh}}^{ij}} \right)^2 \right\}$$

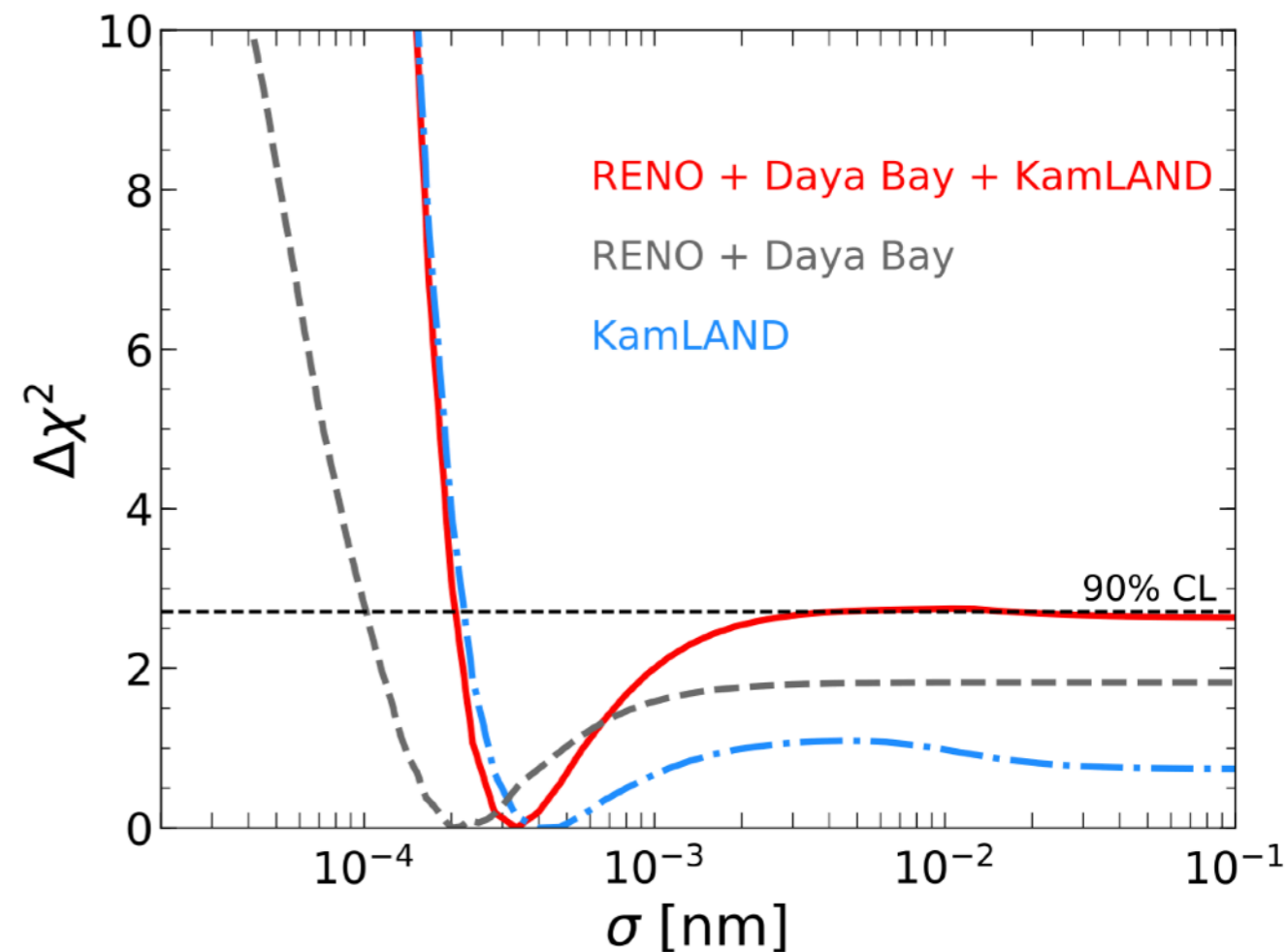
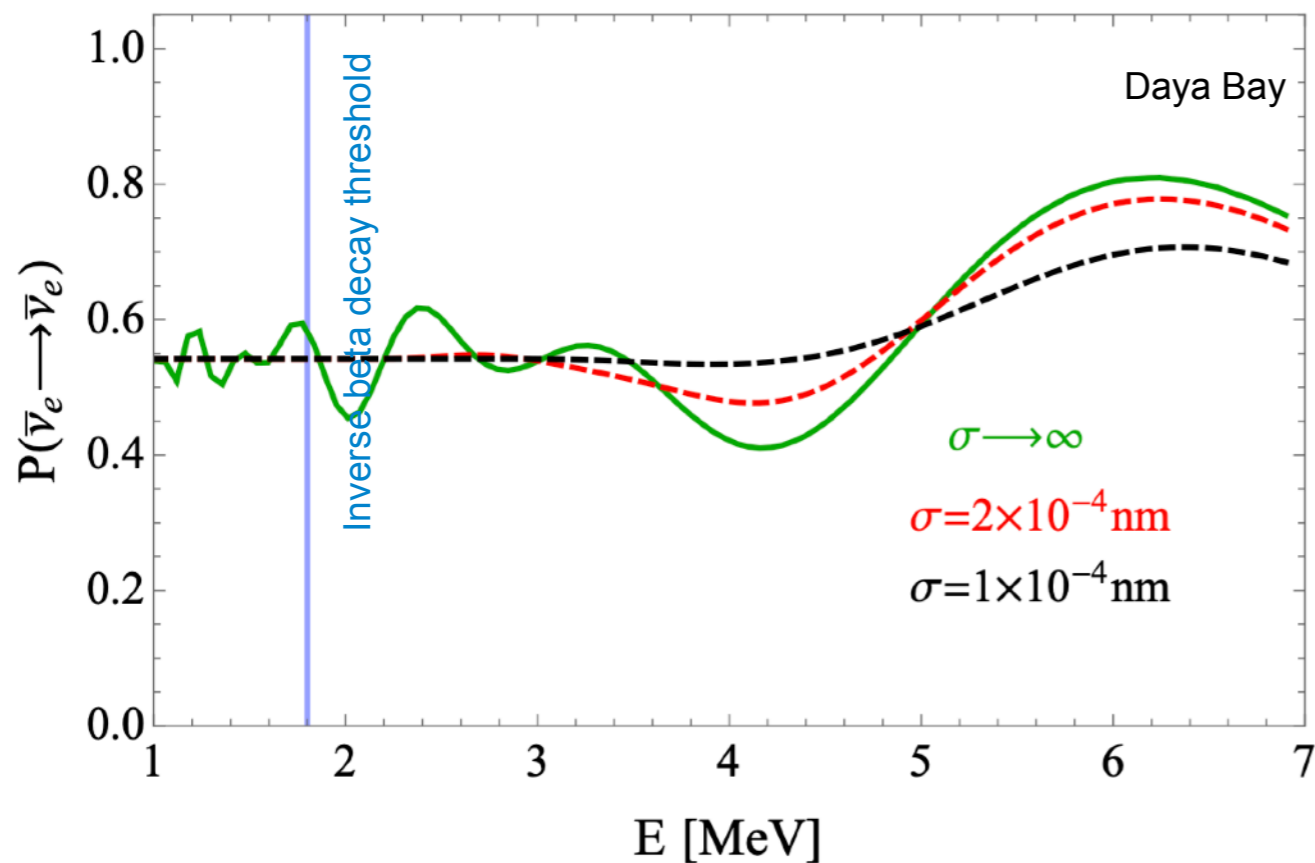
$$L_{\text{osc}}^{ij} = \frac{4\pi E}{\Delta m_{ji}^2} \quad \text{and} \quad L_{\text{coh}}^{ij} = \frac{4\sqrt{2}E^2\sigma_x}{\Delta m_{ji}^2}$$

σ_x is the wave packet size

Oscillations are damped due to the added uncertainty in the neutrino energy

Can we measure/constraint its size?

Yes! We can look at the distortions on the reactor neutrino measurements of standard oscillations!



Reactor wave packet size to be constraint to be greater than 2.1×10^{-4} nm at 90% CL.

What is the size of the wave packet?

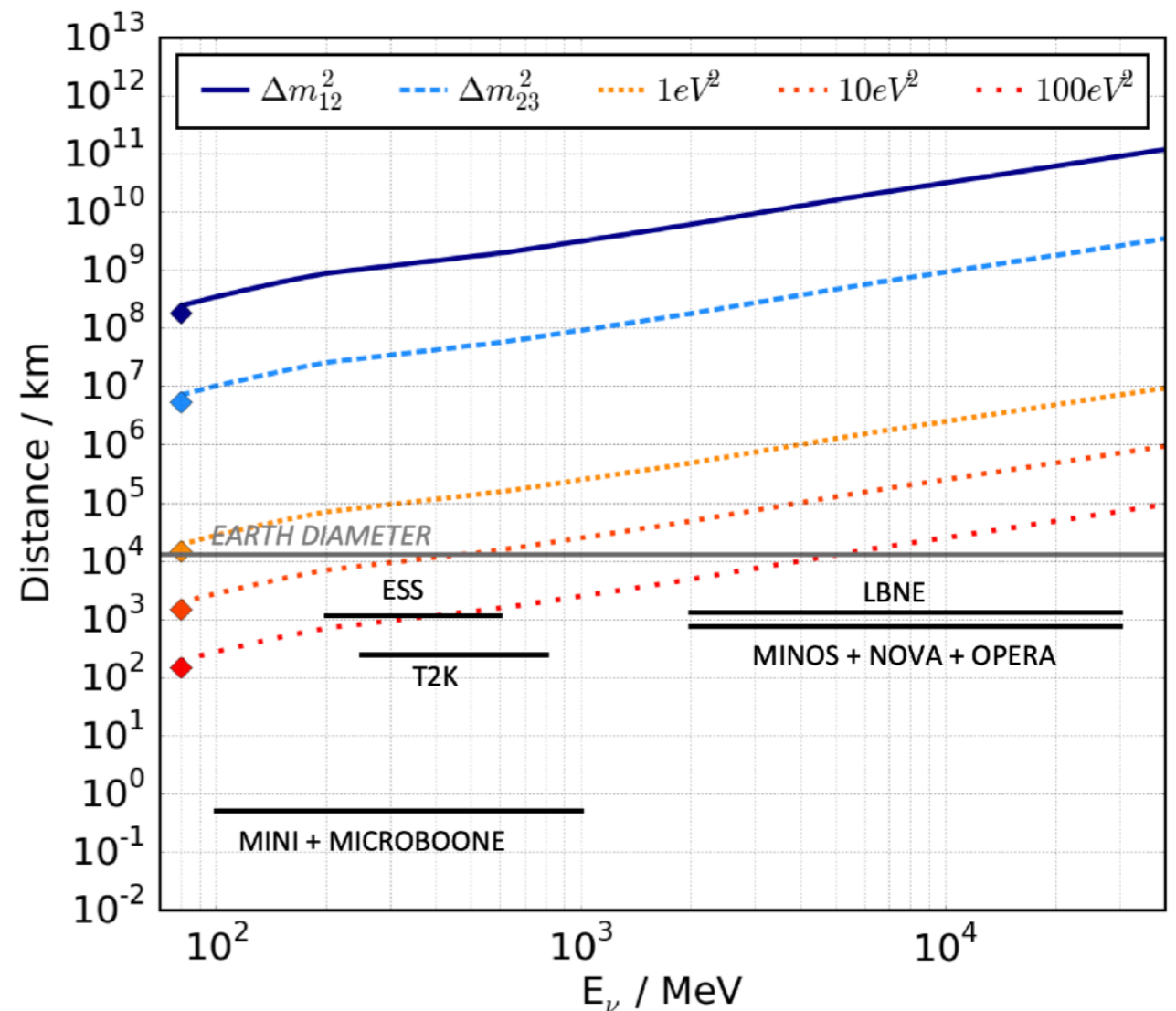
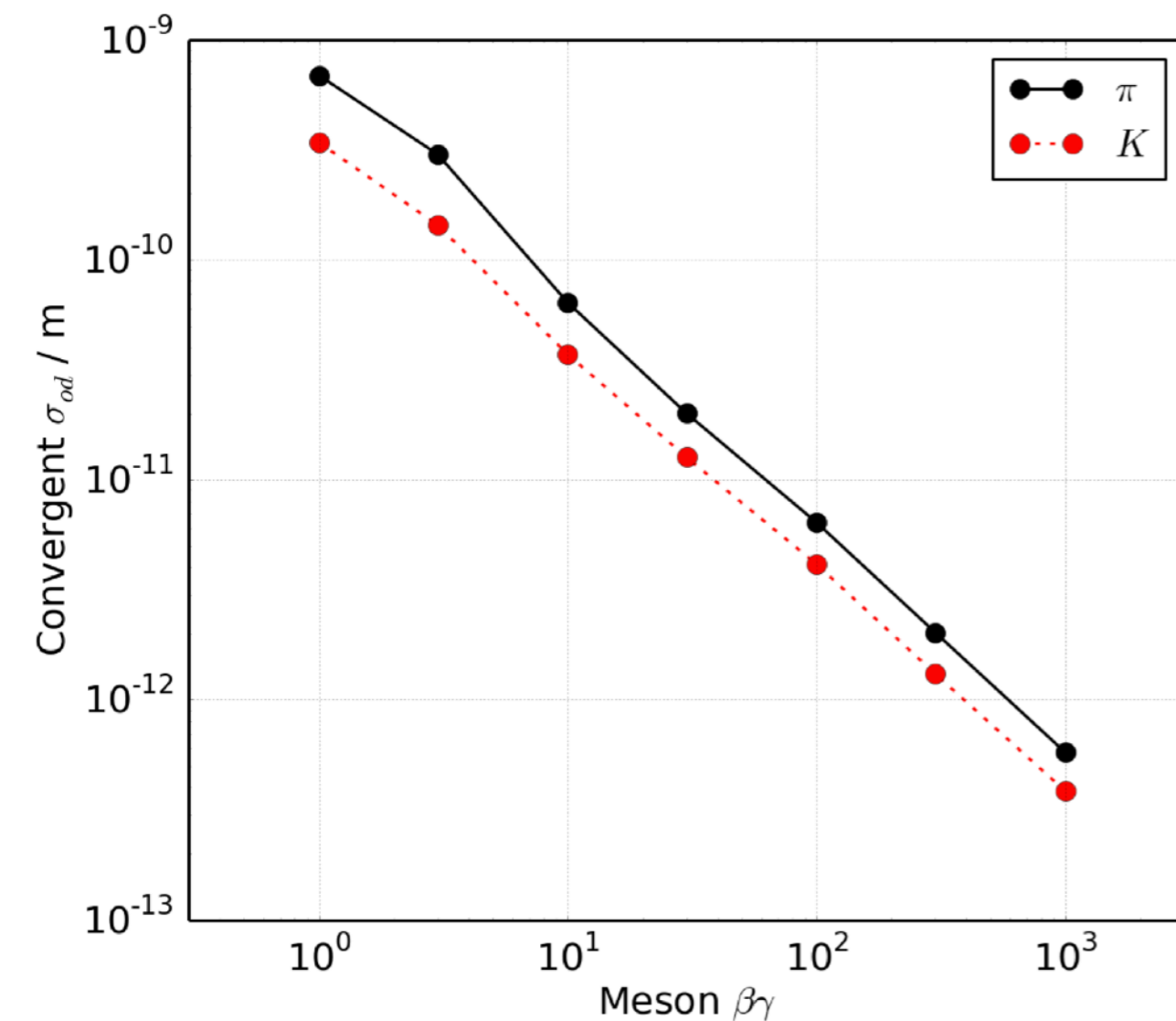
No detail calculation exists for neutrinos produced in reactors or radioactive sources. The following scales seem plausible:

- Typical size of beta-decaying nuclei (10^{-5} nm)
- Interatomic spacing on reactor fuel (0.1 – 1 nm for uranium)
- Inverse of the neutrino energy (10^{-4} nm)
- Inverse of detector energy resolution

The smaller the scale of the neutrino wave packet the larger the neutrino energy resolution effect.

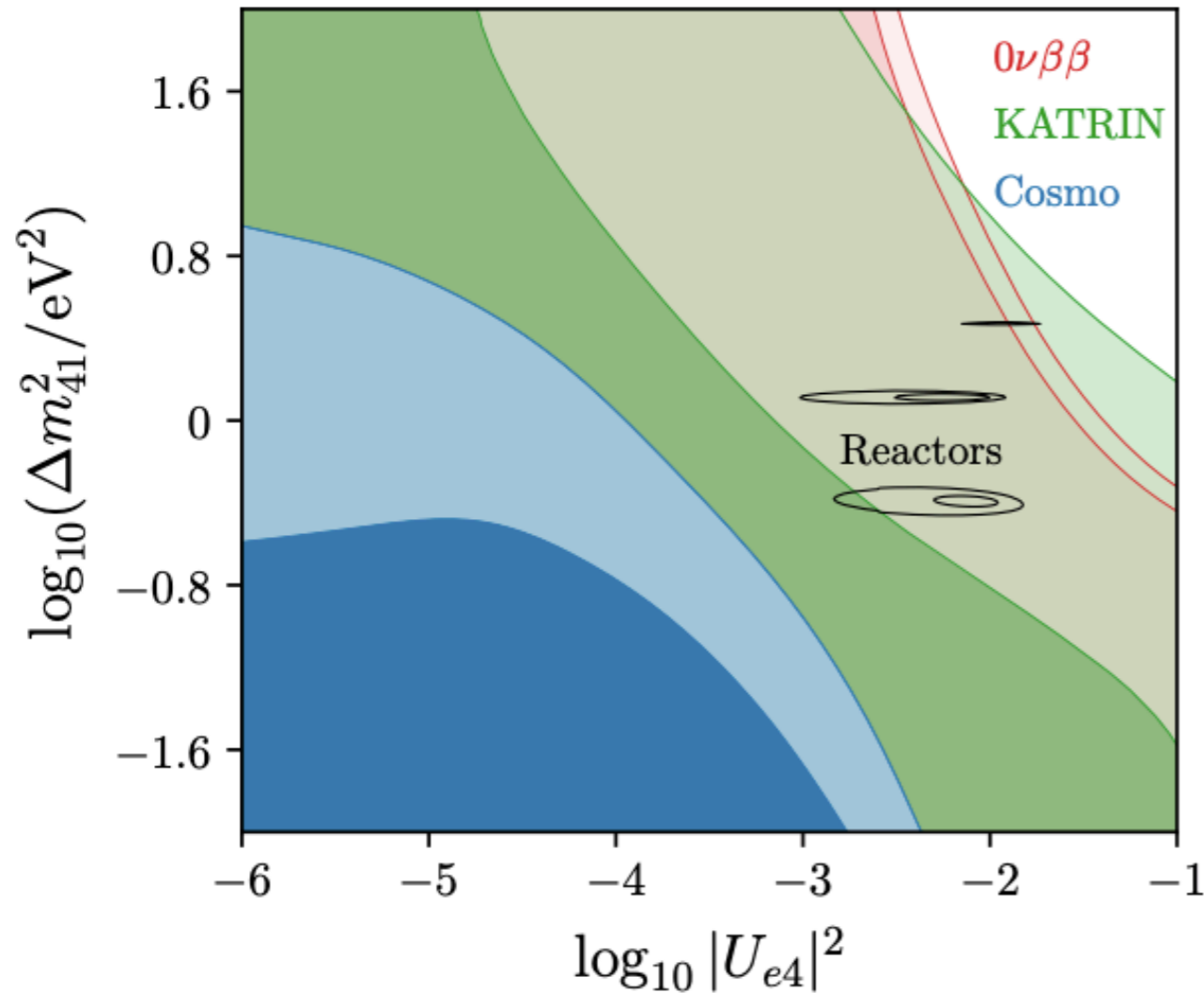
What is the size of the wave packet?

Depends on production and detection process. This has been computed for pion decay in flight.



Let's not forget cosmology!

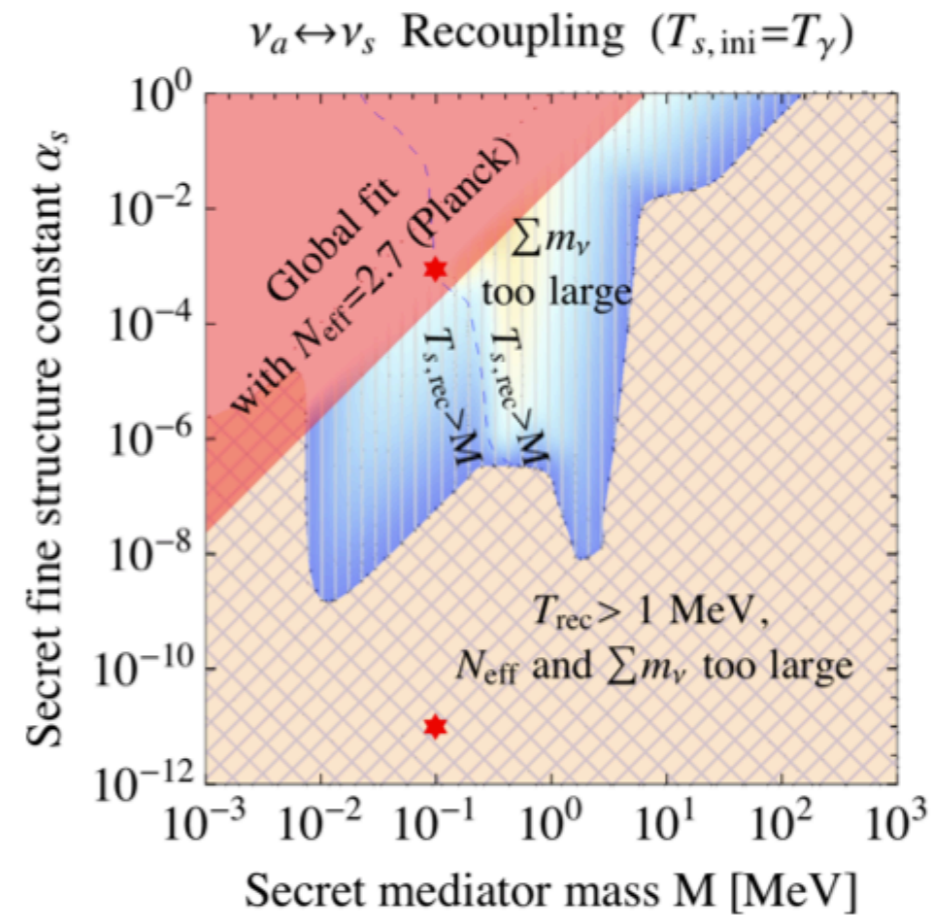
Hagztoz et al/ <https://arxiv.org/pdf/2003.02289.pdf>



Effective mixing $\rightarrow \sin^2 2\theta_m = \frac{\sin^2 2\theta_0 \text{ (Vacuum mixing)}}{\left(\cos^2 2\theta_0 + \frac{2E}{\Delta m^2} V_m\right) + \sin^2 2\theta_0} \rightarrow \text{Keeps } N_{\text{eff}} \text{ at 3}$

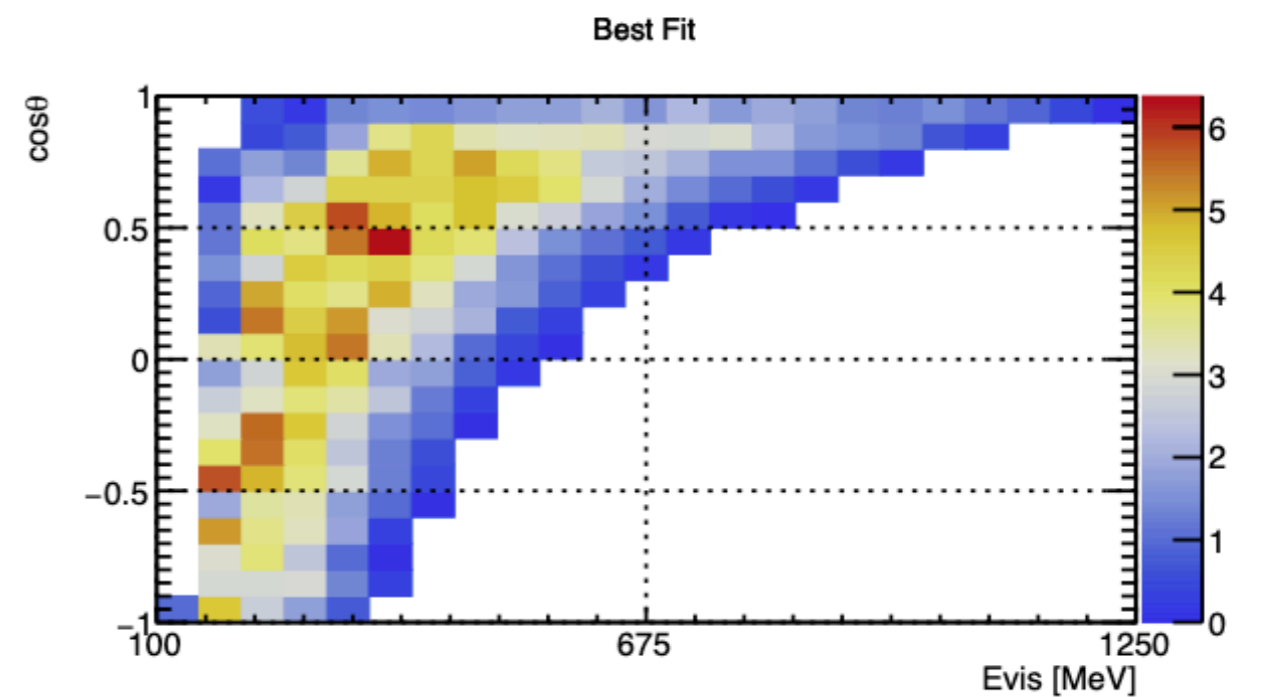
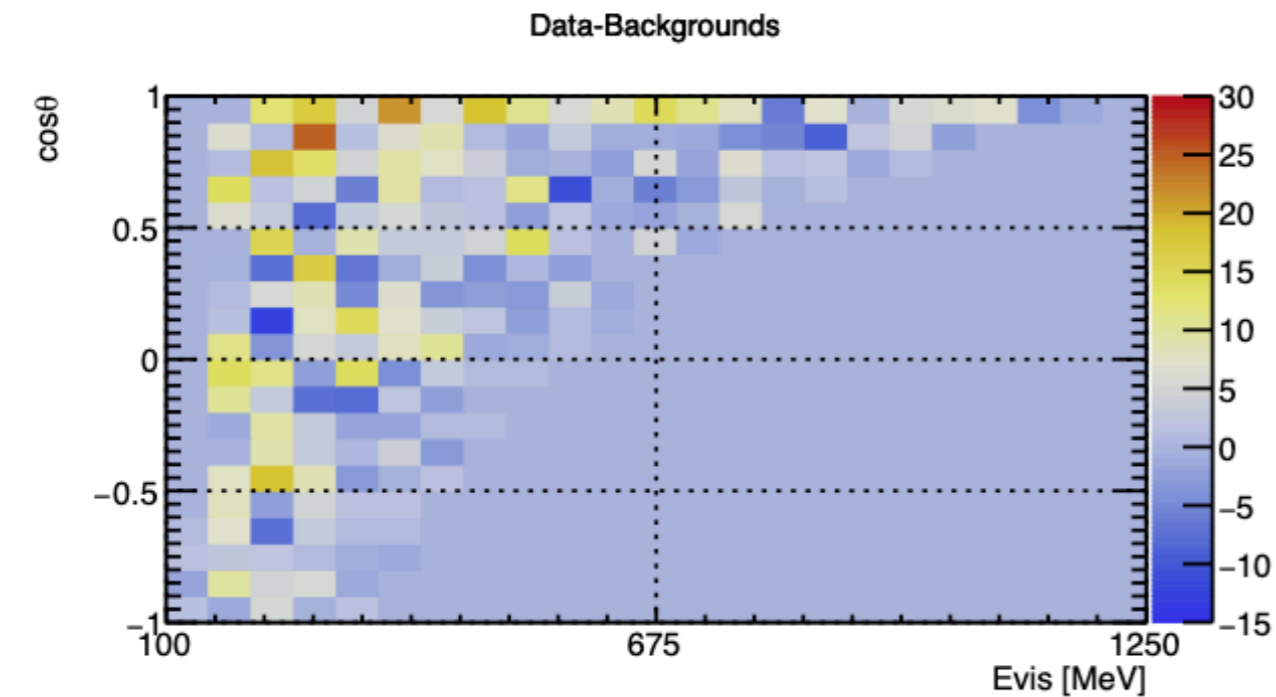
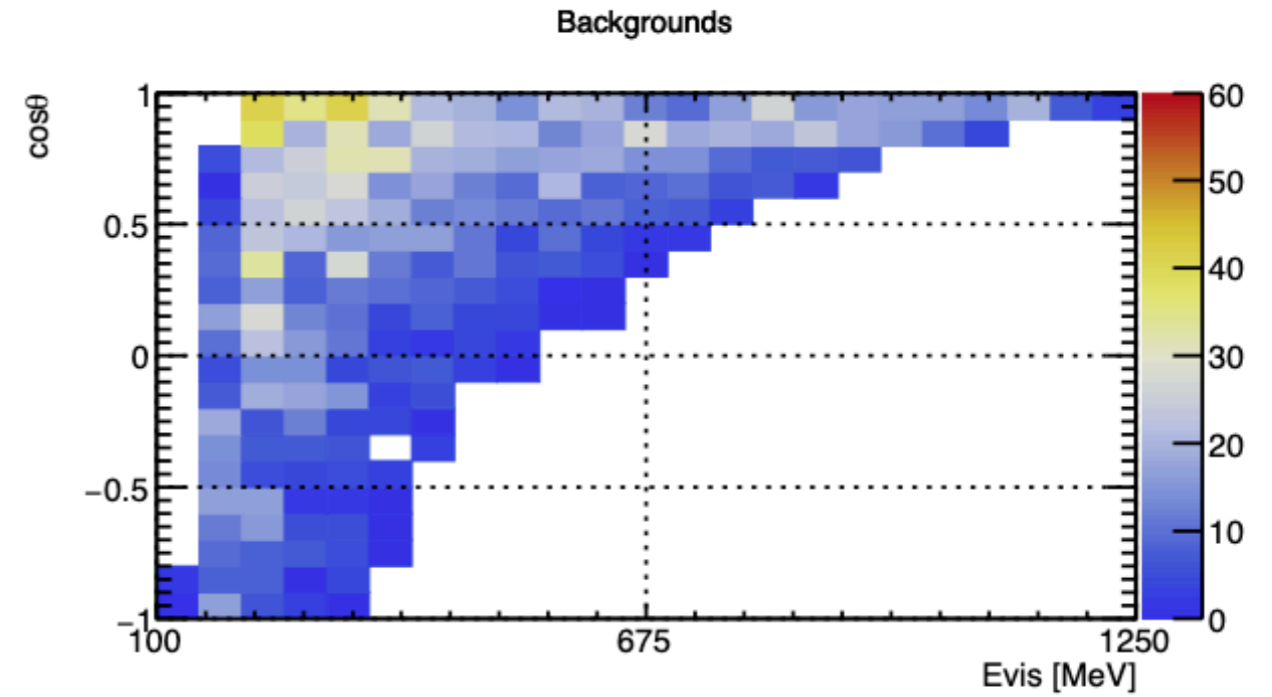
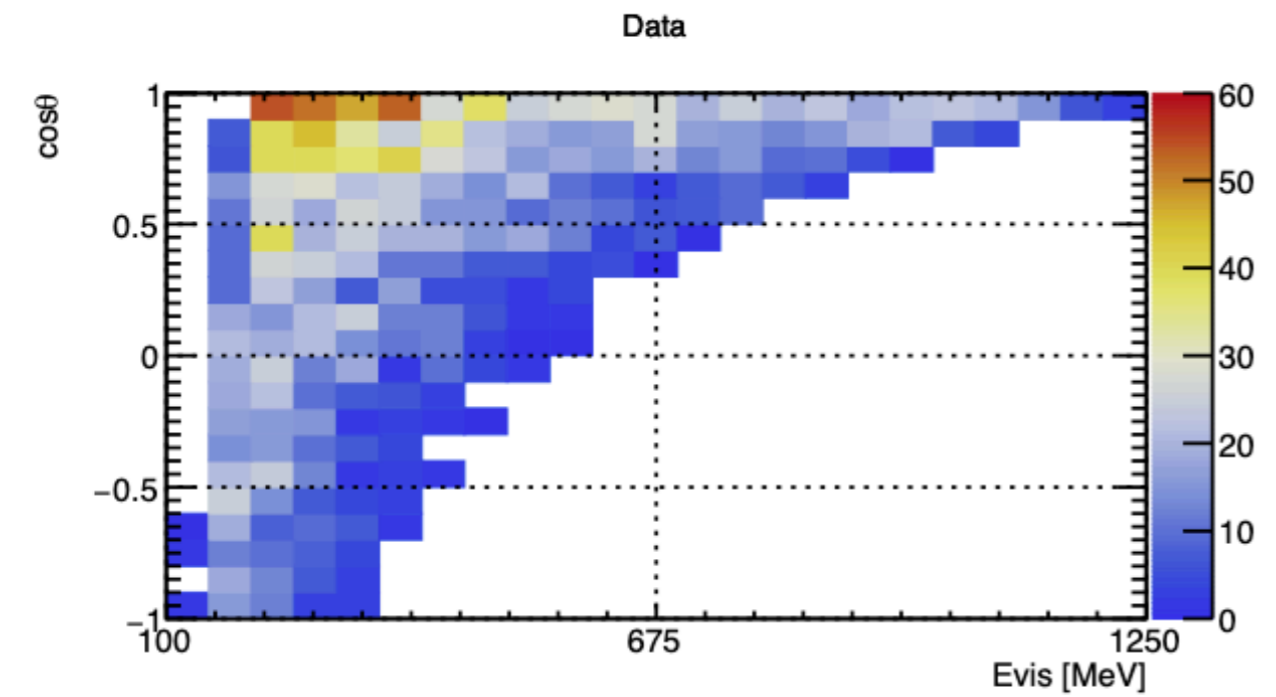
Large

Chu et al. <https://arxiv.org/pdf/1806.10629.pdf>



Dasgupta & Kopp 2014; Chu, Dasgupta & Kopp 2015 Saviano et al. 2014; Mirrizi et al. 2015;
Cherry, Friedland & Shoemaker 2016; Chu et al. 2018
See talk by Yvonne Y. Y. Wong at Neutrino 2020 for summary

More information & a new perspective!



$$d_{\tau\mathcal{N}} = 0$$

