

# Measuring Neutrino Flux at Low Energies: The Low $\nu$ Method

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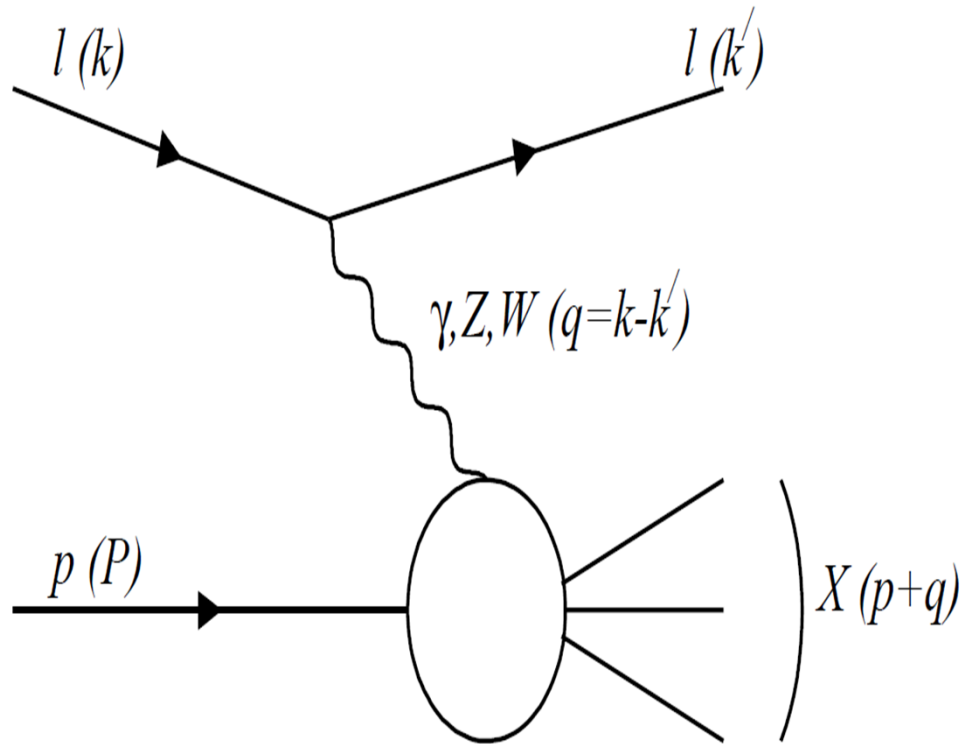
arXiv: 1201.3025

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# Why Do We Need to Determine the Flux at Low Energies?

- Total cross section should be well understood for neutrino oscillation experiments such as T2K, NOvA and MINOS at 500 MeV – 3 GeV.
- MINERvA can investigate cross sections above 500 MeV.
- Flux uncertainty accounts for about 10% of the systematic uncertainty in  $|\Delta m^2|$  [1] and in MINERvA.

# The General Process



$$Q^2 = -q^2 = -(k - k')^2 > 0,$$

$$s = (P + k)^2,$$

$$W^2 = (P + q)^2,$$

$$x = \frac{Q^2}{2P \cdot q},$$

$$y = \frac{P \cdot q}{P \cdot k},$$

$$\nu = \frac{P \cdot q}{M}.$$

$$\left( v = \frac{Q^2 + W^2 - M^2}{2M} \right)$$

Source:

Yang, Un Ki. «A Measurement of differential cross-sections in charged current neutrino interactions on iron and a global structure functions analysis.» FERMILAB-THESIS-2001-09, UMI-99-98273.3-4 (2001).

# Cross Section Equation and Definitions

$$\begin{aligned}
 \frac{d\sigma^{ud}}{dQ^2 d\nu} = & S_{cos} \frac{1}{2E^2} \mathcal{W}_1 [Q^2 + m_\mu^2] \\
 & + S_{cos} \mathcal{W}_2 \left[ \left(1 - \frac{\nu}{E}\right) - \frac{(Q^2 + m_\mu^2)}{4E^2} \right] \\
 & + S_{cos} \mathcal{W}_3 \left[ \frac{Q^2}{2ME} - \frac{\nu}{4E} \frac{Q^2 + m_\mu^2}{ME} \right] \\
 & + S_{cos} \mathcal{W}_4 \left[ m_\mu^2 \frac{(Q^2 + m_\mu^2)}{4M^2 E^2} \right] \\
 & - S_{cos} \mathcal{W}_5 \left[ \frac{m_\mu^2}{ME} \right]
 \end{aligned}$$

$$\left( \nu = \frac{Q^2 + W^2 - M^2}{2M} \right)$$

$$\sigma_{tot}(E) = \sigma_{W_2}(\infty) [f_C]$$

$$f_C = [f_{W_2} + f_2 + f_1 + f_3 + f_4 + f_5]$$

$$f_{W_2} = \frac{\sigma_{W_2}}{\sigma_{W_2}(\infty)} (\approx 1)$$

$$f_2 = \frac{\sigma_2}{\sigma_{W_2}(\infty)} (= \textit{kinematic correction})$$

$$f_1 = \frac{\sigma_1}{\sigma_{W_2}(\infty)} (= \textit{important})$$

$$f_3 = \frac{\sigma_3}{\sigma_{W_2}(\infty)} (= \textit{important})$$

$$f_4 = \frac{\sigma_4}{\sigma_{W_2}(\infty)} (= \textit{very small})$$

$$f_5 = \frac{\sigma_4}{\sigma_{W_2}(\infty)} (= \textit{very small})$$



# The Low $\nu$ Method for High Energies

- At high E, cross section for DIS dominates.

$$\frac{d\sigma}{d\nu} = A \left( 1 + \frac{B \nu}{A E} - \frac{C \nu^2}{A 2E^2} \right)$$

Multiply both sides by flux  $\rightarrow$

$$\frac{dN}{d\nu} = \phi A \left( 1 + \frac{B \nu}{A E} - \frac{C \nu^2}{A 2E^2} \right)$$

As  $\nu \rightarrow 0$ ,

$$\frac{dN}{d\nu} \approx \phi A$$

# The Low $\nu$ Method for High Energies

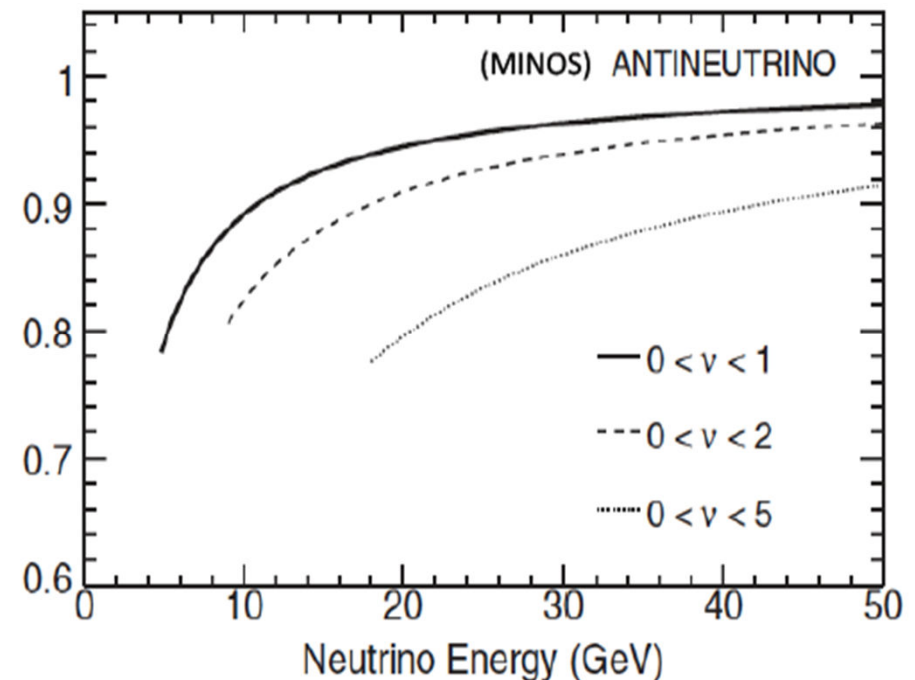
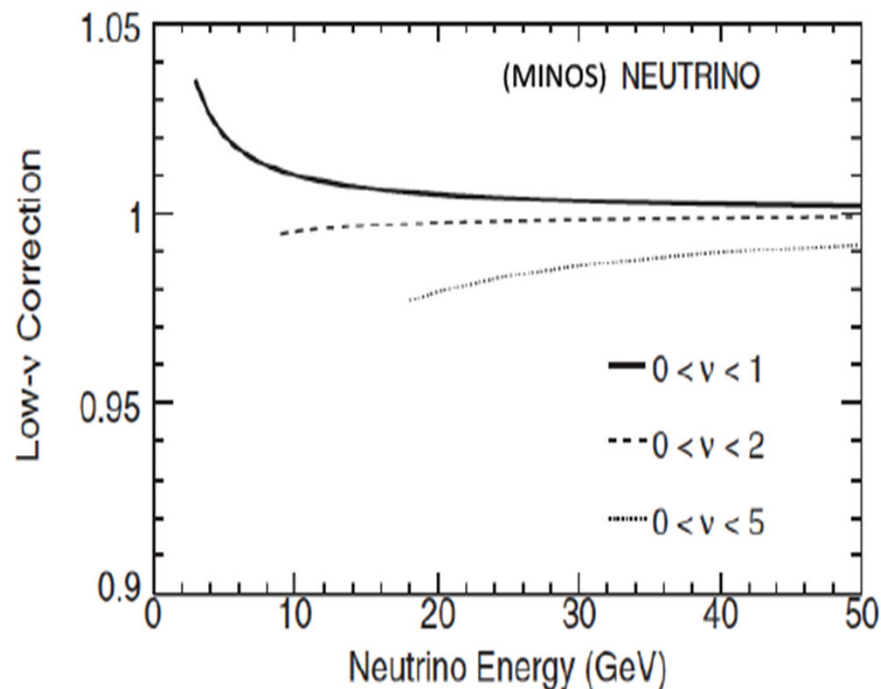
$$f_{C:\nu < \nu_{max}}(E) := \frac{\sigma(E, \nu < \nu_{max})}{\sigma(E \rightarrow \infty, \nu < \nu_{max})}$$

$$\phi(E) = \frac{\int_{\nu_{min}(E)}^{\nu_{max}} \frac{dN(E)}{d\nu} d\nu}{f_C(E) * A(E)}$$

$\nu_{min}$  is known from kinematics, but what determines  $\nu_{max}$ ?

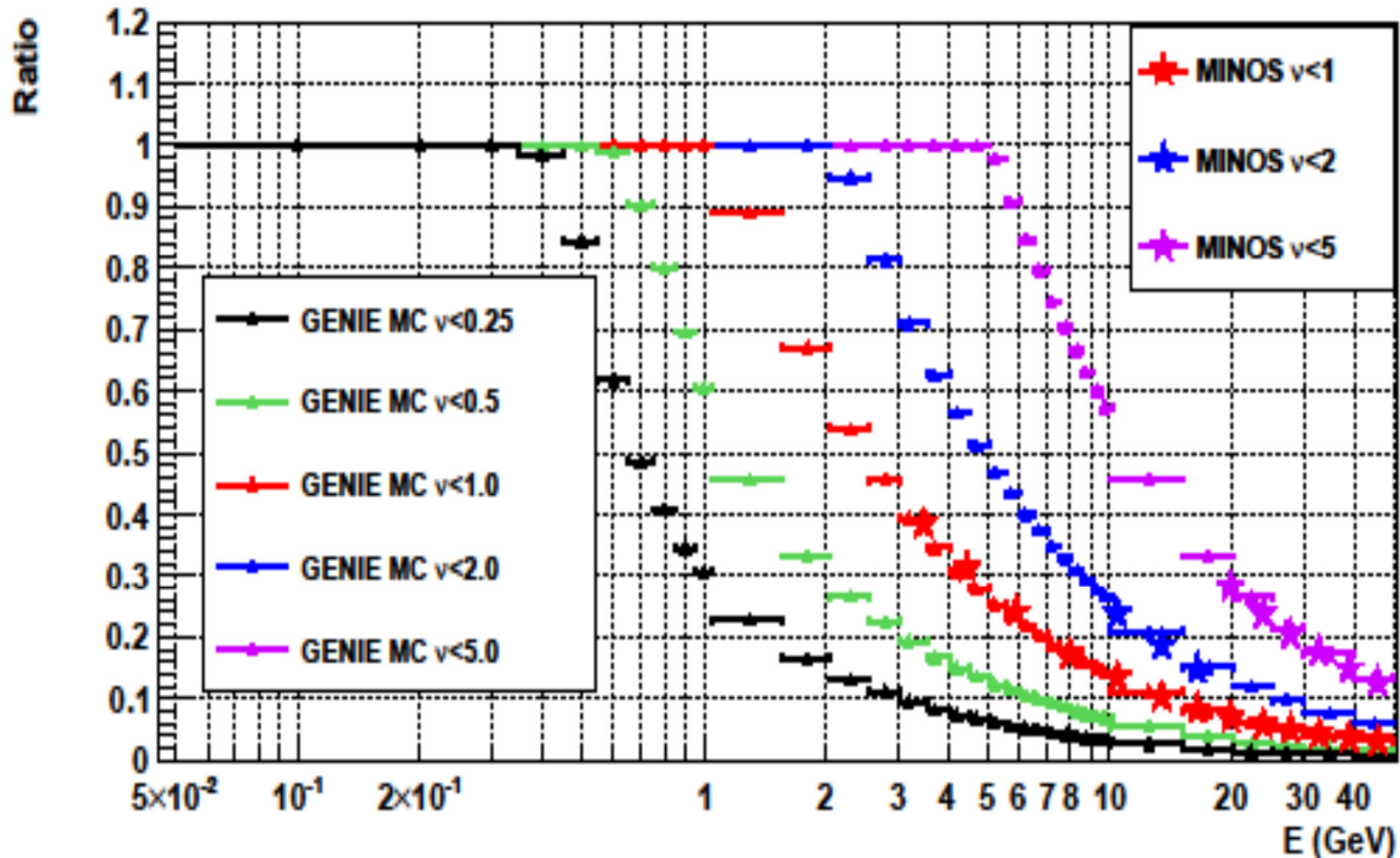
# Criteria

- The MINOS Collaboration suggested the number of low  $\nu$  events should not exceed 60% of the total cross section
- However, this number should also be statistically significant.
- Hence, MINOS used  $\nu < 1$  GeV for  $E > 3$  GeV for neutrinos and  $E > 5$  GeV for antineutrinos;  $\nu < 2$  GeV and  $\nu < 5$  GeV for  $E > 9$  GeV and  $E > 18$  GeV, respectively.



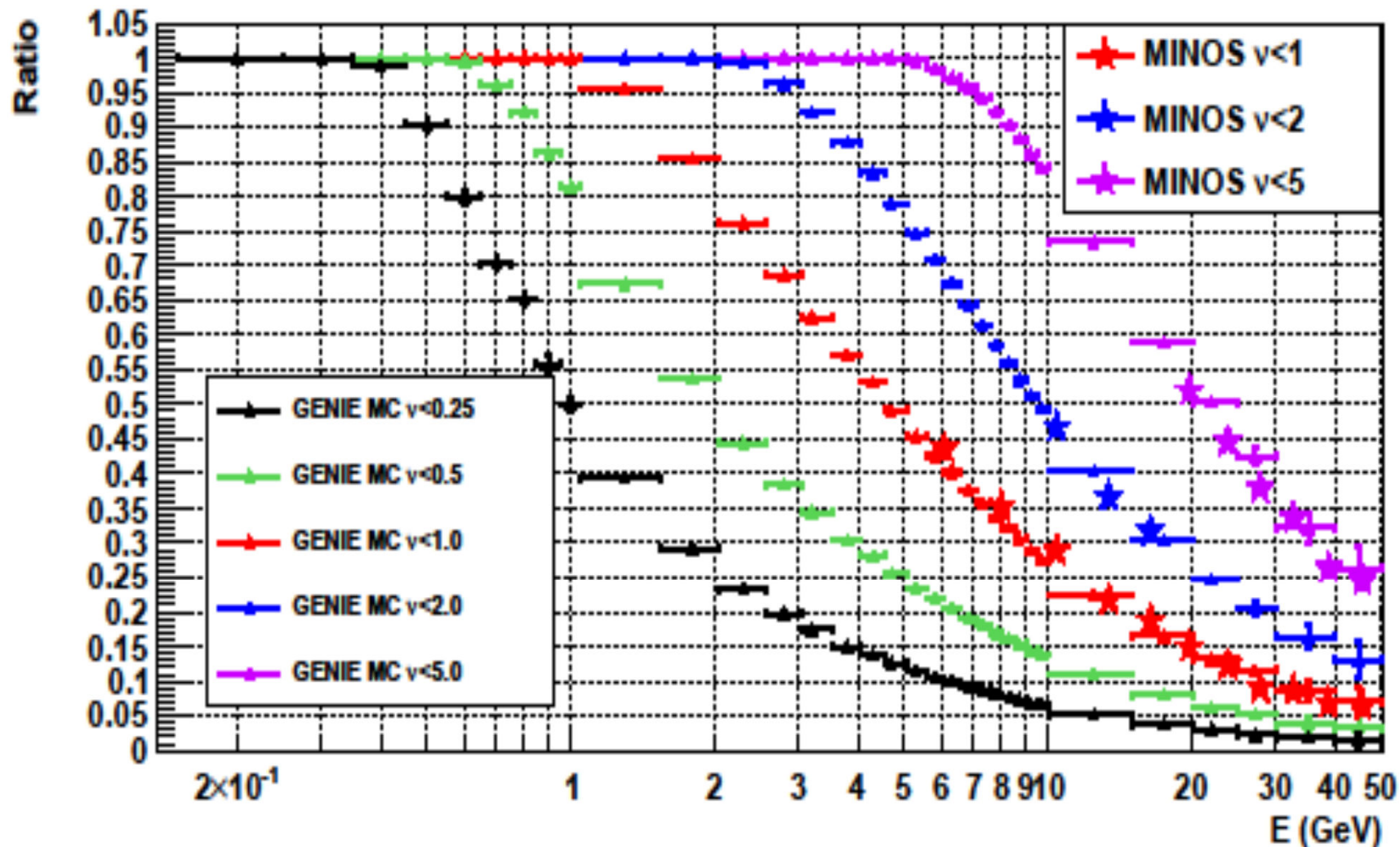
# The Low $\nu$ Method for Low Energies

Fraction of Events with  $\nu$  Cut for Neutrino on Carbon



# The Low $\nu$ Method for Low Energies

Fraction of Events with  $\nu$  Cut for Antineutrino on Carbon



# The Low $\nu$ Method for Low Energies

- As the energy decreases, lower  $\nu$  events should be selected so that their cross section remains below 60%.

# The Low $\nu$ Method for Low Energies

- We examine the use of
  - a)  $\nu < 0.25$  GeV for  $E_\nu > 0.7$  GeV,  $E_{\bar{\nu}} > 1$  GeV  
and
  - b)  $\nu < 0.5$  GeV for  $E_\nu > 1.2$  GeV,  $E_{\bar{\nu}} > 2$  GeVon CC events.

$$\dots \nu_{max}=0.25\dots$$



## ... $\nu_{max}=0.25$ : Methodology...

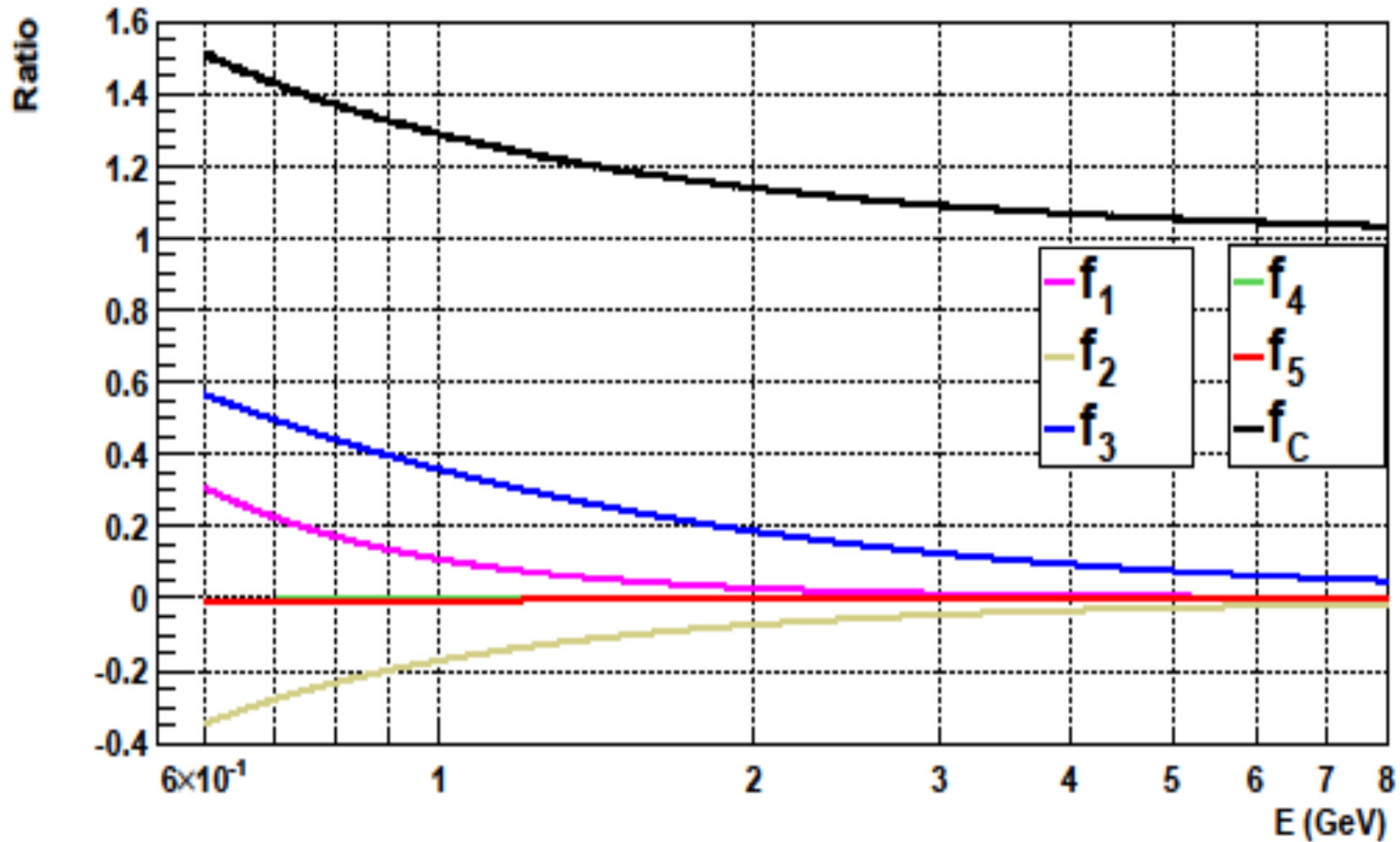
- The cross section for  $\nu_{max}=0.25$  is almost entirely QE:

$$\nu n \rightarrow \mu^- p / \bar{\nu} p \rightarrow \mu^+ n$$

- Structure function ratios are well known for QE on free nucleons, so  $f_C$  should have very small systematic uncertainties on hydrogen and deuterium.
- $^{12}_6C$  targets: Cross section corrections for nuclear effects are necessary: Pauli suppression (Paschos and Yu, 2002) on the differential cross section.
- Recent update from Bodek, Budd and Christy with QE transverse enhancement at low energy for nuclear targets.

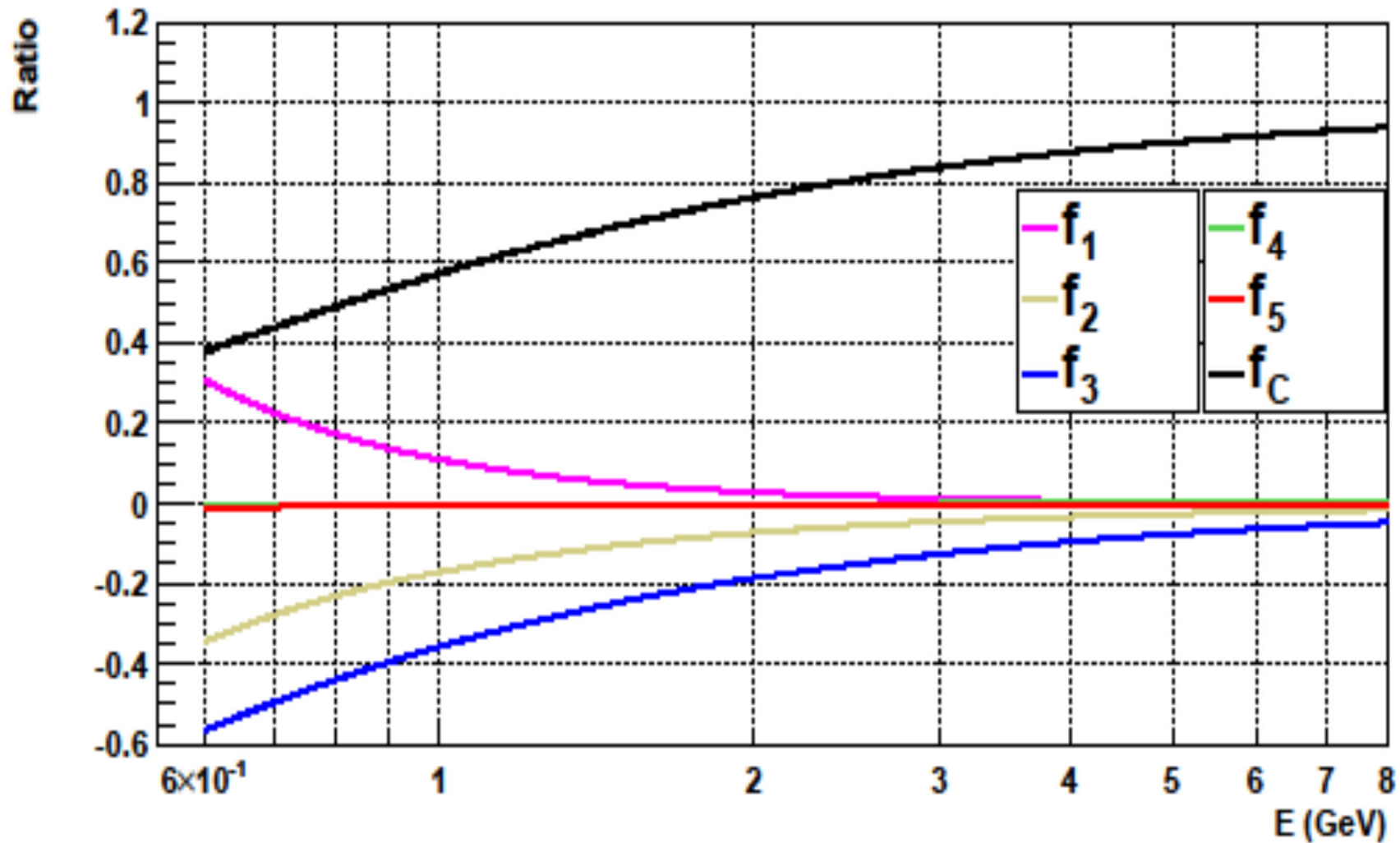
... $\nu_{max}=0.25: f_c$ ...

Contributions to  $f_c$  for Neutrino ( $\nu < 0.25$ )



... $\nu_{max}=0.25: f_C$ ...

Contributions to  $f_C$  for Antineutrino ( $\nu < 0.25$ )



... $\nu_{max}=0.25$ : Conclusion...

- If we apply the MINOS criterion of 60%, the method works for  $E > 0.7$  GeV for  $\nu_{\mu}$  and  $E > 1$  GeV for  $\bar{\nu}_{\mu}$  with model uncertainties 3.8% and 5%, respectively.

$$\dots \nu_{max}=0.5\dots$$

$$\dots \nu_{max} = 0.5 \dots$$

- Primary contributors: QE + Single-pion  $W < 1.4$  GeV
- Single-pion major contributor: Delta ( $J = \frac{3}{2}, P_{33}(1232)$ ) resonance
  - $\nu p \rightarrow \mu^- \Delta^{++} / \bar{\nu} n \rightarrow \mu^+ \Delta^-:$ 
    - $\nu p \rightarrow \mu^- p \pi^+ / \bar{\nu} n \rightarrow \mu^+ n \pi^-$
  - $\nu n \rightarrow \mu^- \Delta^+ / \bar{\nu} p \rightarrow \mu^+ \Delta^0:$ 
    - $\nu n \rightarrow \mu^- n \pi^+ / \bar{\nu} p \rightarrow \mu^+ p \pi^-$
    - $\nu n \rightarrow \mu^- p \pi^0 / \bar{\nu} p \rightarrow \mu^+ n \pi^0$
- Some higher resonances and the non-resonant continuum
- Almost negligible coherent (below,  $A = \text{nucleus}$ ):
  - $\nu A \rightarrow \mu^- A \pi^+ / \bar{\nu} A \rightarrow \mu^+ A \pi^-$

## ... $\nu_{max}=0.5$ : Methodology...

- Cross section fits of delta resonance differ for high and low energy experiments.
- For the resonance region calculation, we define the delta interactions for  $W < 1.4$  as the single-pion final-state interactions. Therefore, our definition includes the non-resonant continuum even though we will collectively call it delta.
- We use Paschos 2011 equations for delta resonance on free nucleons, apply absolute cross section scaling of  $1/1.2$  to exclude  $W > 1.4$  GeV and vary  $M_A$  and  $C_5^A$  to fit BEBC90 single-pion  $W < 1.4$  GeV results.
- For carbon, we again apply Pauli suppression.

## ... $\nu_{max}=0.5$ : Plots with GENIE MC...

- The total  $\nu < 0.5$  GeV cross section flattens as  $E$  increases: Reasonably flat for 10-20 GeV
- In order to compare our predictions to GENIE and make the method accessible for future experimental application, we normalize to 10-20 GeV (average 15.1 GeV for GENIE) and define:

$$\bar{f}_{C:\nu<\nu_{max}}(15.1)(E) := \frac{f_{C:\nu<\nu_{max}}(E)}{f_{C:\nu<\nu_{max}}(15.1 \text{ GeV})}$$



$$\dots \nu_{max}=0.5\dots$$

- Curve legend for the following plots (carbon targets, applying Pauli blocking to differential cross section):

$$\nu p \rightarrow \mu^- \Delta^{++} / \bar{\nu} n \rightarrow \mu^+ \Delta^-$$

Paschos 2011:  $M_A = 1.05$ ;  $C_5^A = 1.2$  (Original values used by Paschos and Lalakulich, fitting ANL and BNL low energy data)

FIT-A1:  $M_A = 1.93$ ;  $C_5^A = 0.62$  (BEBC90  $\bar{\nu} n \rightarrow \mu^+ \Delta^-$  differential and total cross section fit)

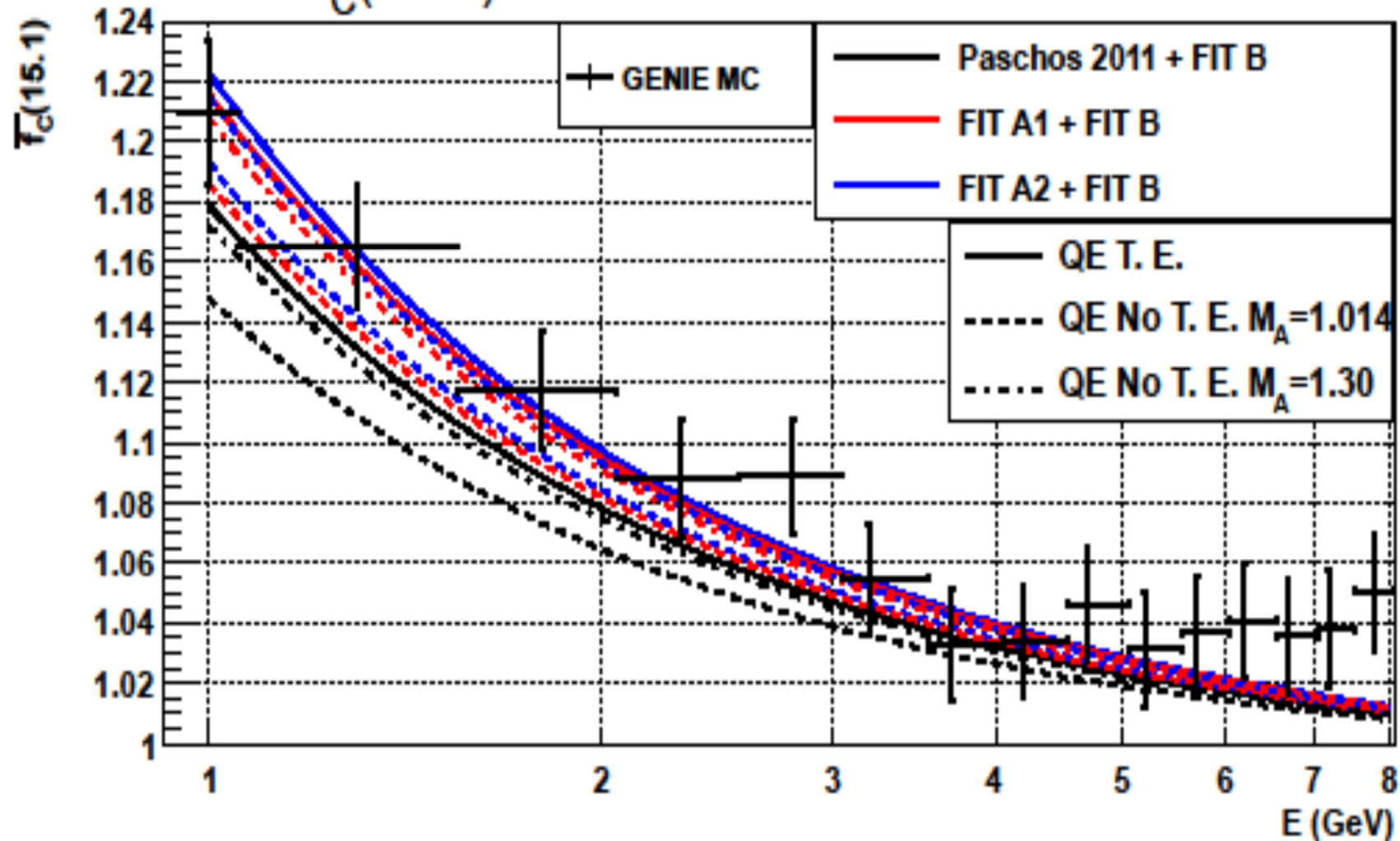
FIT-A2:  $M_A = 1.75$ ;  $C_5^A = 0.49$  (BEBC90  $\nu p \rightarrow \mu^- \Delta^{++}$  differential and total cross section fit)

$$\nu n \rightarrow \mu^- \Delta^+ / \bar{\nu} p \rightarrow \mu^+ \Delta^0$$

FIT-B:  $M_A = 1.62$ ;  $C_5^A = 1.27$  (BEBC90  $\nu n \rightarrow \mu^- \Delta^+$  differential and total cross section fit)

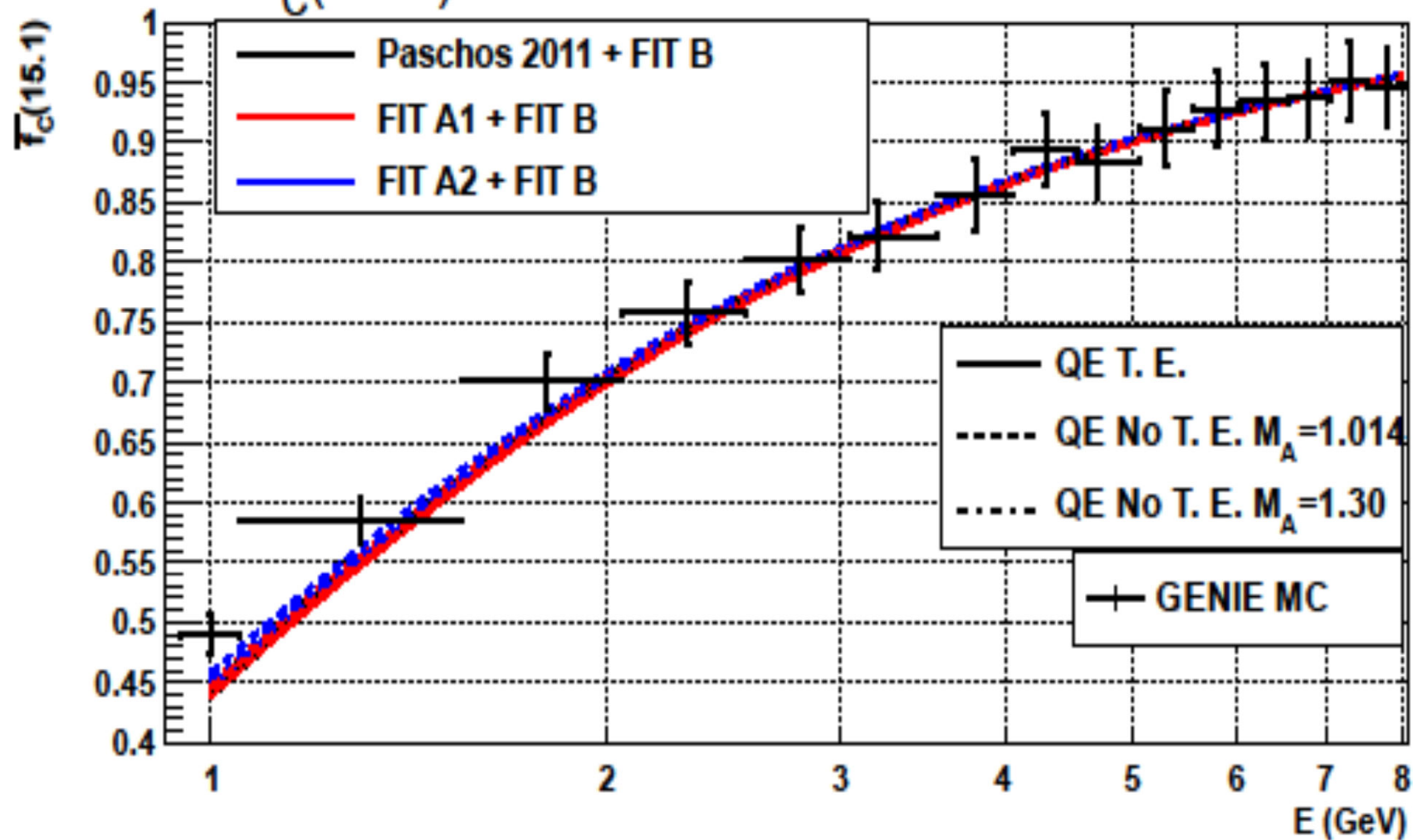
... $\nu_{max}=0.5: \bar{f}_C...$

$\bar{f}_C(15.1)$  for Neutrino on Carbon  $\nu < 0.5$



... $\nu_{max}=0.5: \bar{f}_C...$

$\bar{f}_C(15.1)$  for Antineutrino on Carbon  $\nu < 0.5$



## ... $\nu_{max}=0.5$ : Conclusion

- Depending on the model used,  $\Delta f_C$  is within 2.6% for  $\nu_\mu$  above 1.2 GeV and 1.4% for  $\bar{\nu}_\mu$  above 2 GeV.
- Above these energies, the ratios to total cross section are below 60%.

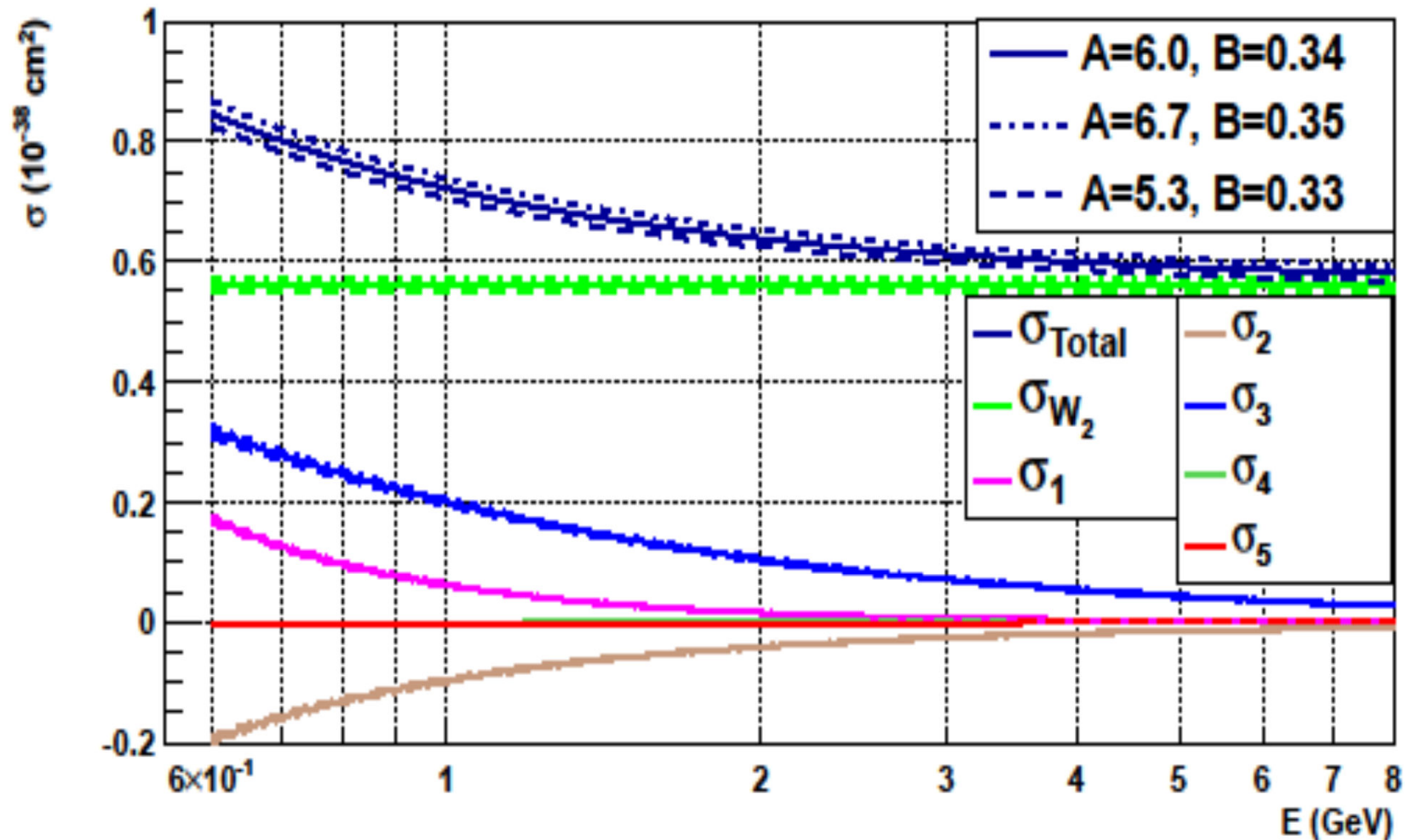
# Back-up Slides

# Other Methods Available for MINERvA

- Modeling the production of pions and kaons produced from the proton beam, tracking them along the horn magnetic focus and modeling their decay:
  - > Differential cross section over a thick target and a reliable model for the magnetic field
- Measuring the muon flux that exits the decay pipe:
  - > Response of detectors at the end of the decay pipe
  - > Muon energy not measured
- Monitoring inverse muon decay:
  - > Above around 12 GeV, no antineutrinos, useful to constrain flux at high energies
- Monitoring muon neutrino-electron scattering:
  - > Useful only for total flux since calorimetric detectors cannot distinguish the leptons' charge

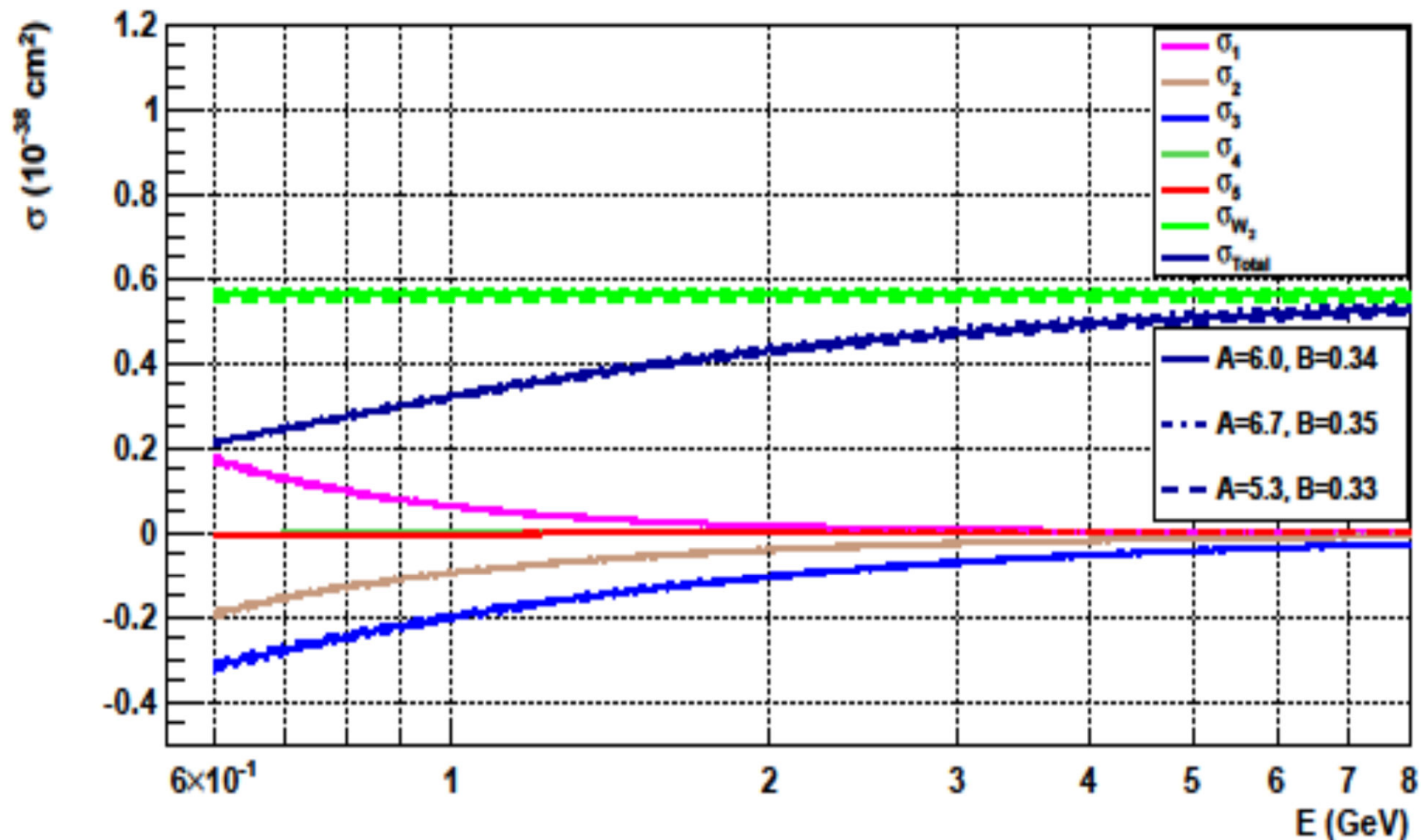
... $\nu_{max}=0.25$ : Cross sections...

Contributions to Quasi-elastic  $\sigma_{Total}$  for Neutrino ( $\nu < 0.25$ )



... $\nu_{max}=0.25$ : Cross sections...

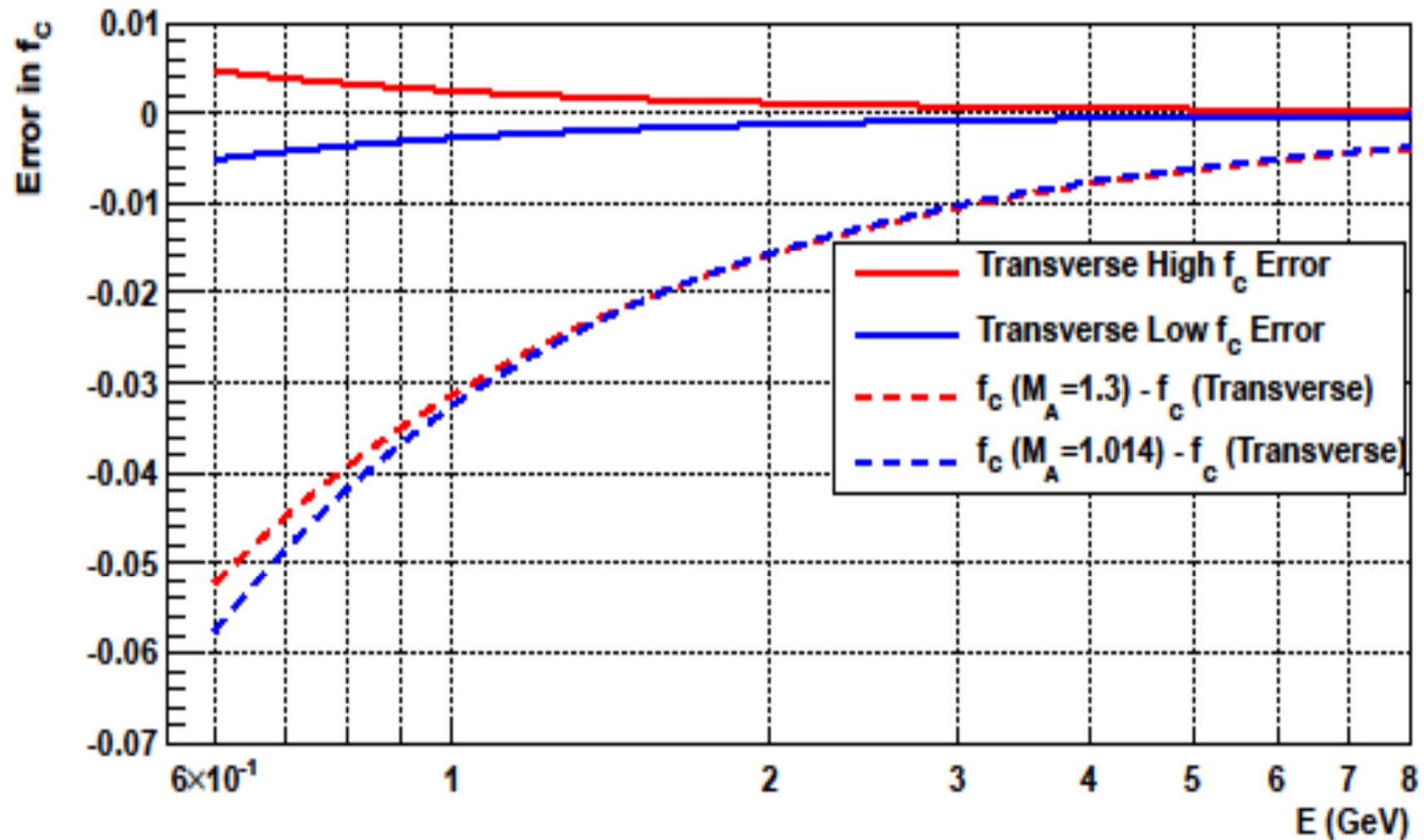
Contributions to Quasi-elastic  $\sigma_{Total}$  for Antineutrino ( $\nu < 0.25$ )





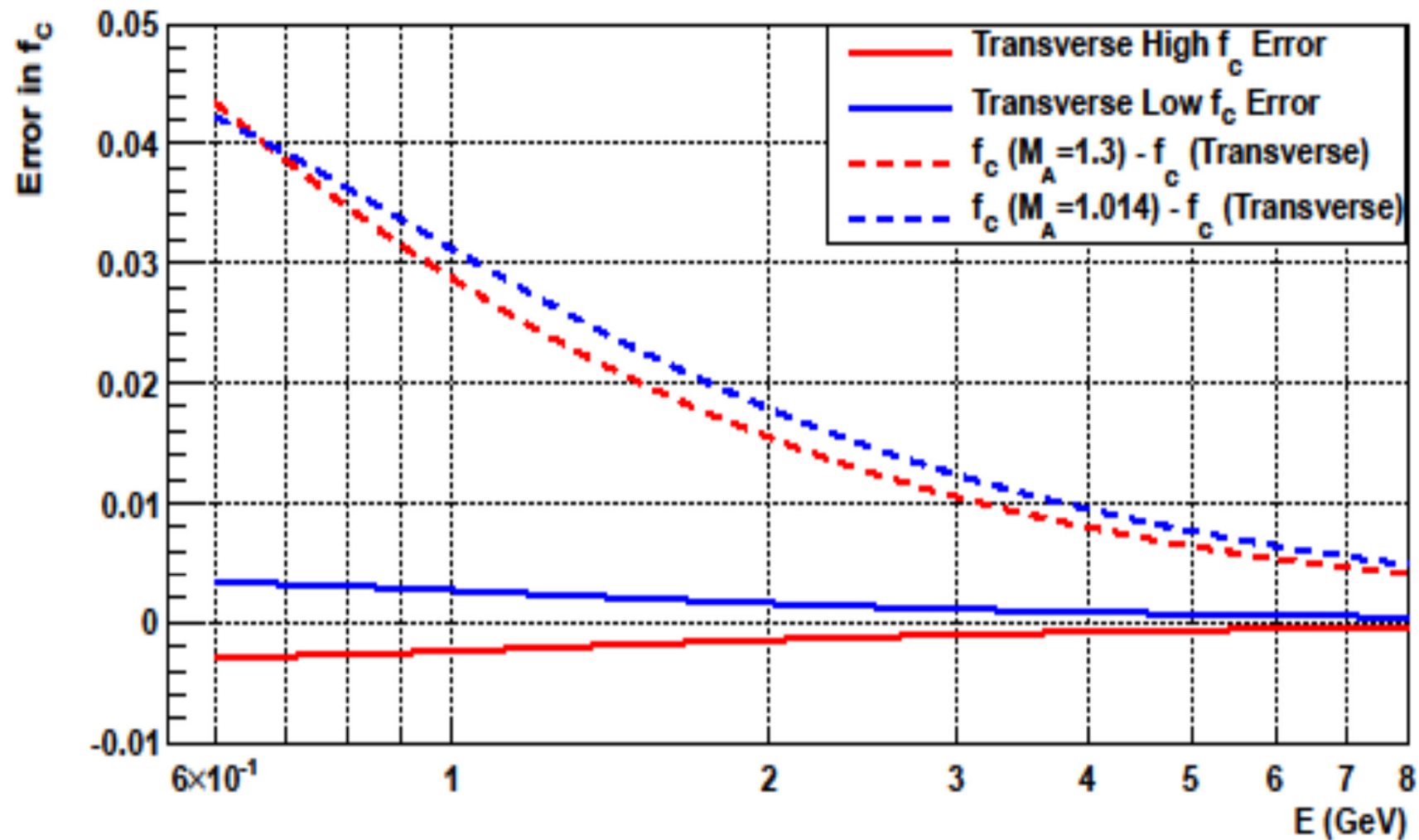
... $\nu_{max}=0.25$ :  $f_c$  Error...

Error in  $f_c$  for Neutrino ( $\nu < 0.25$ )



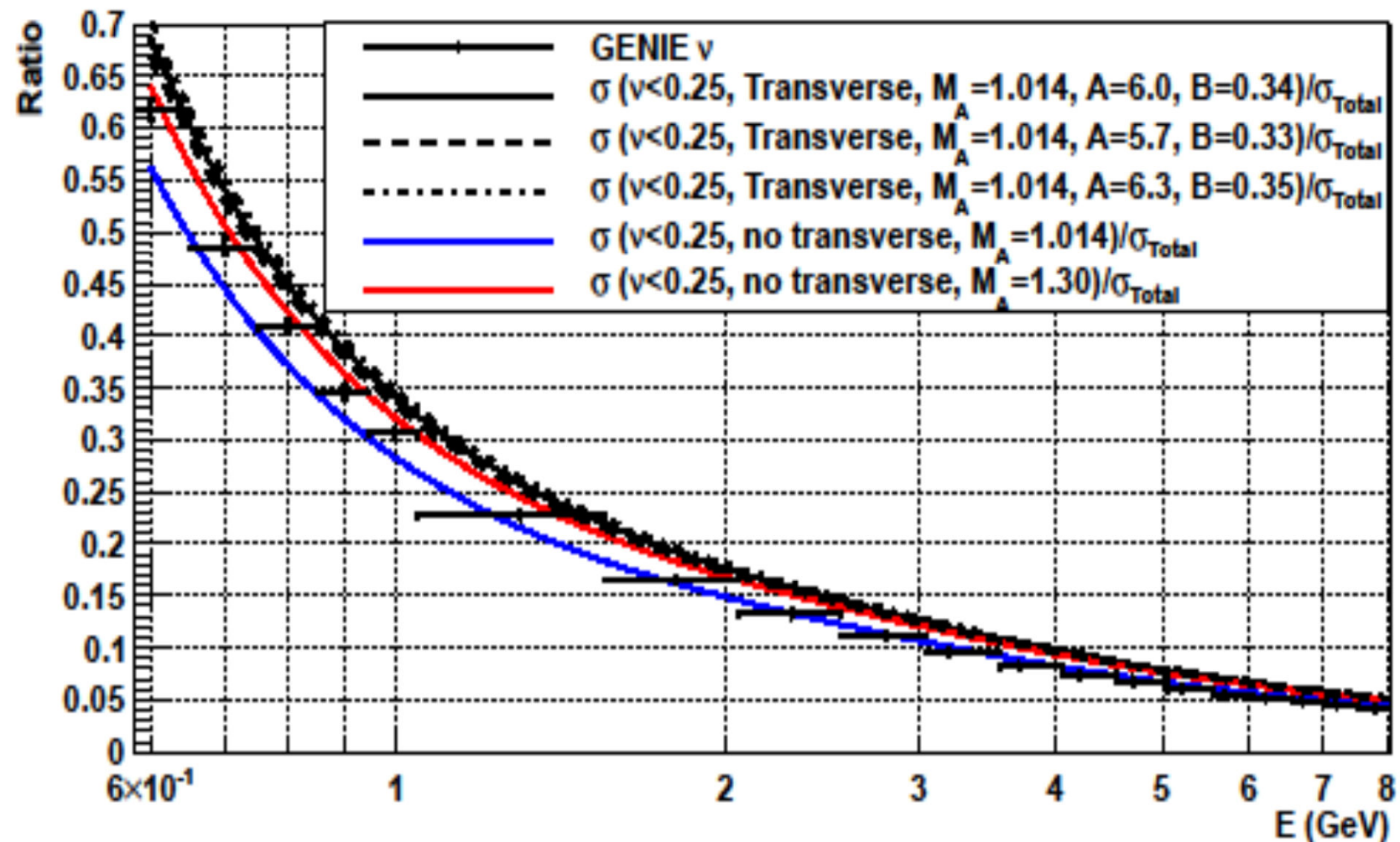
... $\nu_{max}=0.25$ :  $f_C$  Error...

Error in  $f_C$  for Antineutrino ( $\nu<0.25$ )



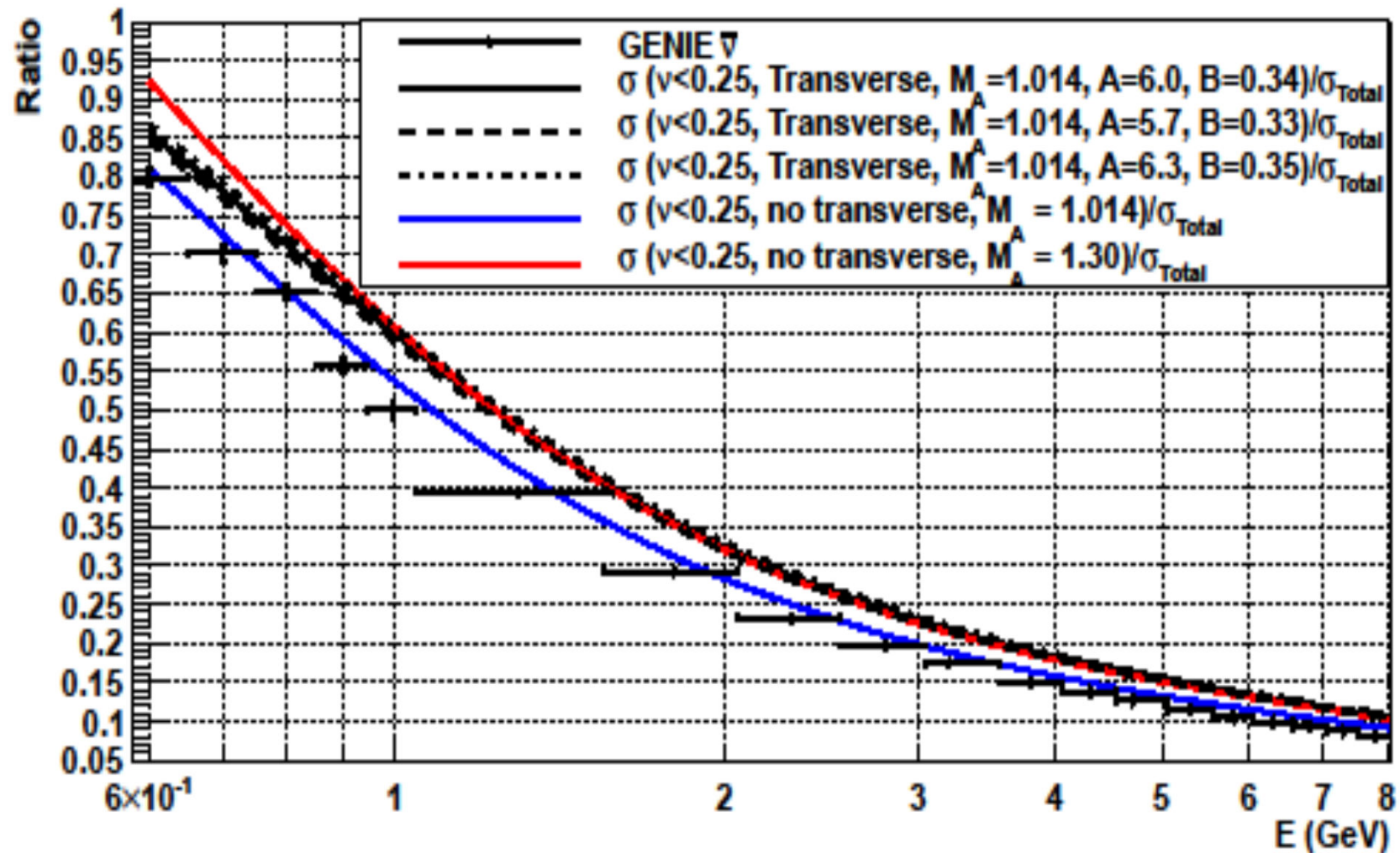
... $\nu_{max}=0.25$ : Ratio to Total  
Parameterization...

Fraction of  $\nu<0.25$  Cross Section to Total Cross Section for Neutrino



... $\nu_{max}=0.25$ : Ratio to Total  
Parameterization...

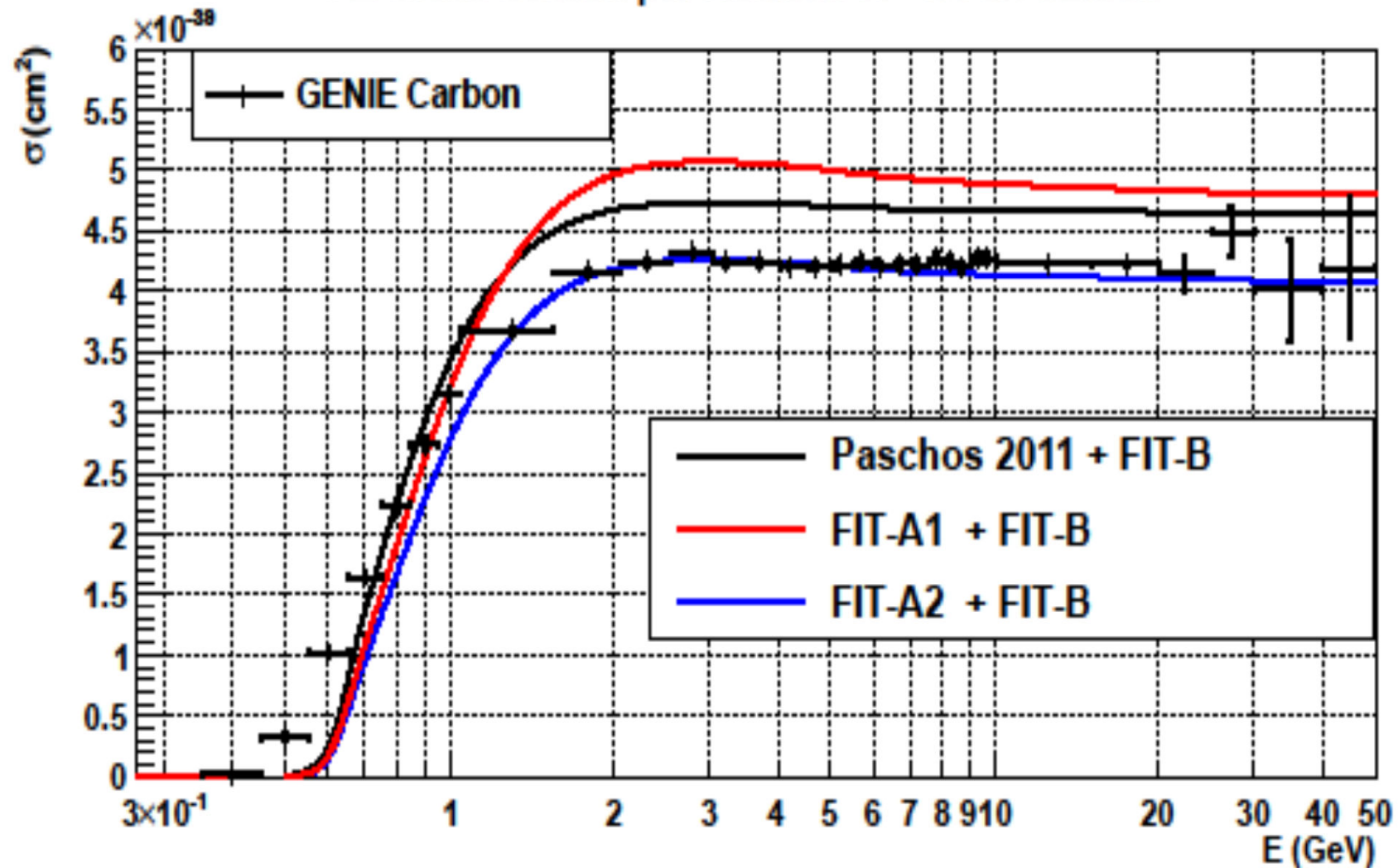
Fraction of  $\nu < 0.25$  Cross Section to Total Cross Section for Antineutrino





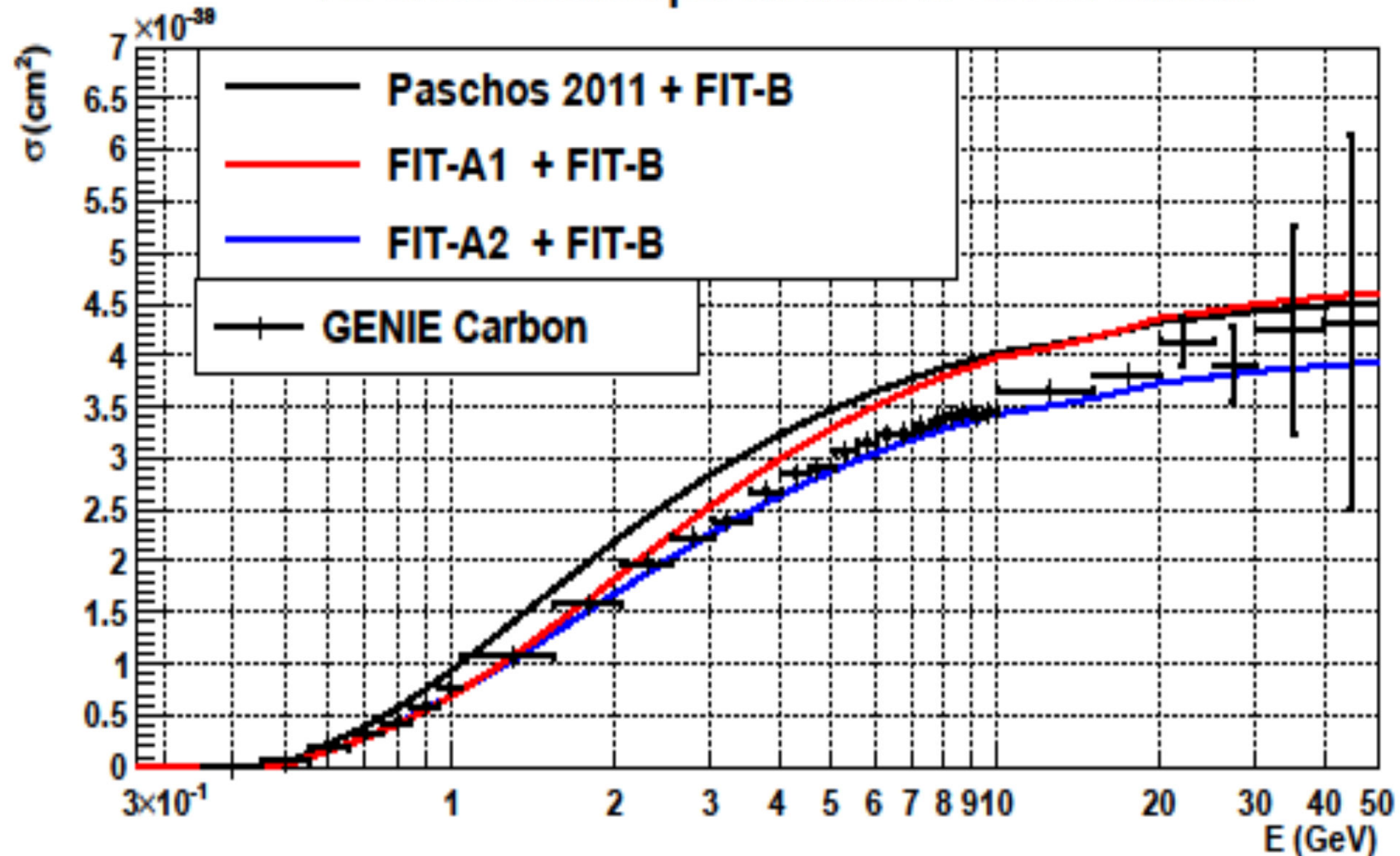
... $\nu_{max}=0.5$ : Cross sections...

$\nu$   $\Delta$  Cross Section per Nucleon  $W < 1.4$  on Carbon



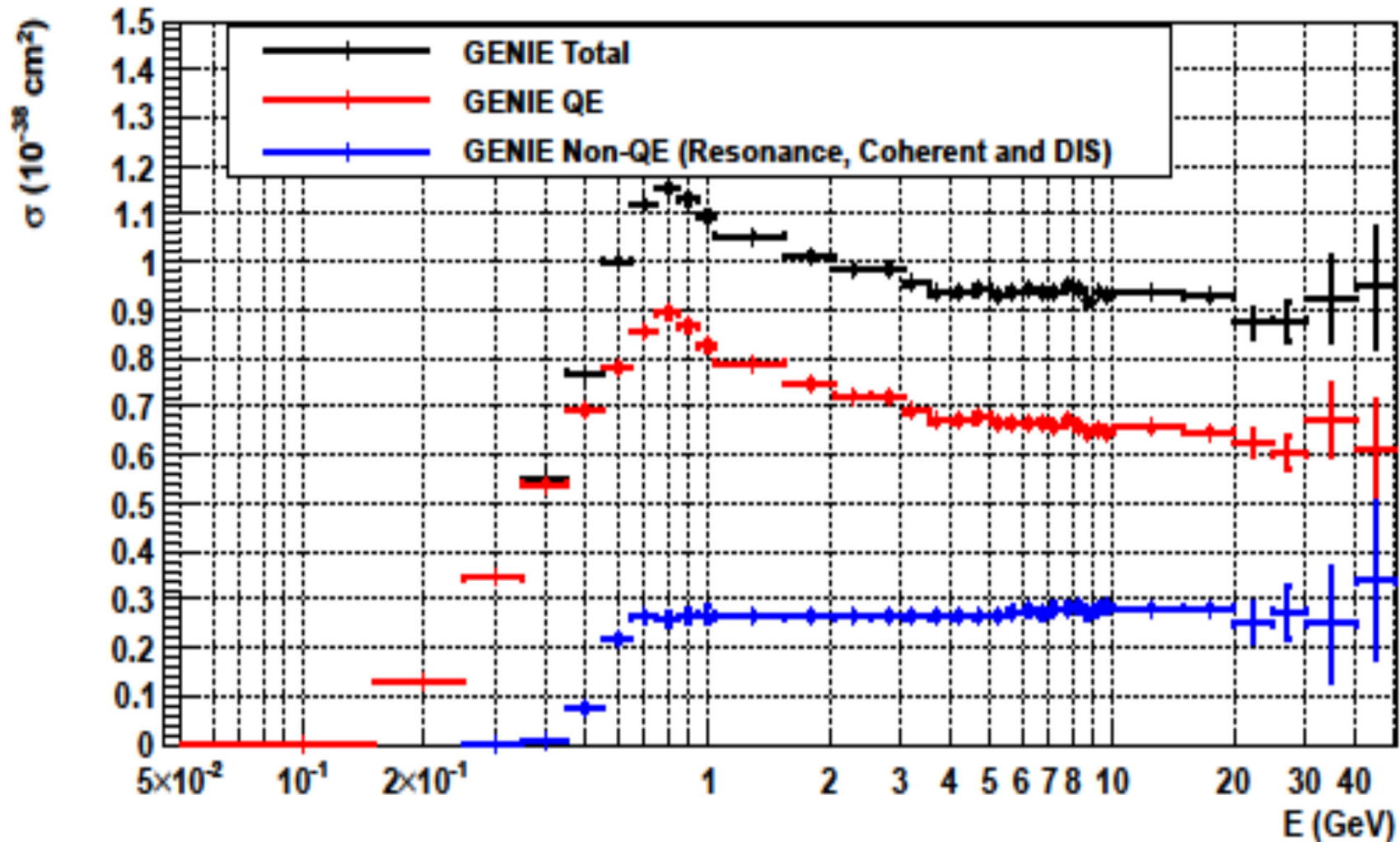
... $\nu_{max}=0.5$ : Cross sections...

$\nabla \Delta$  Cross Section per Nucleon  $W < 1.4$  on Carbon



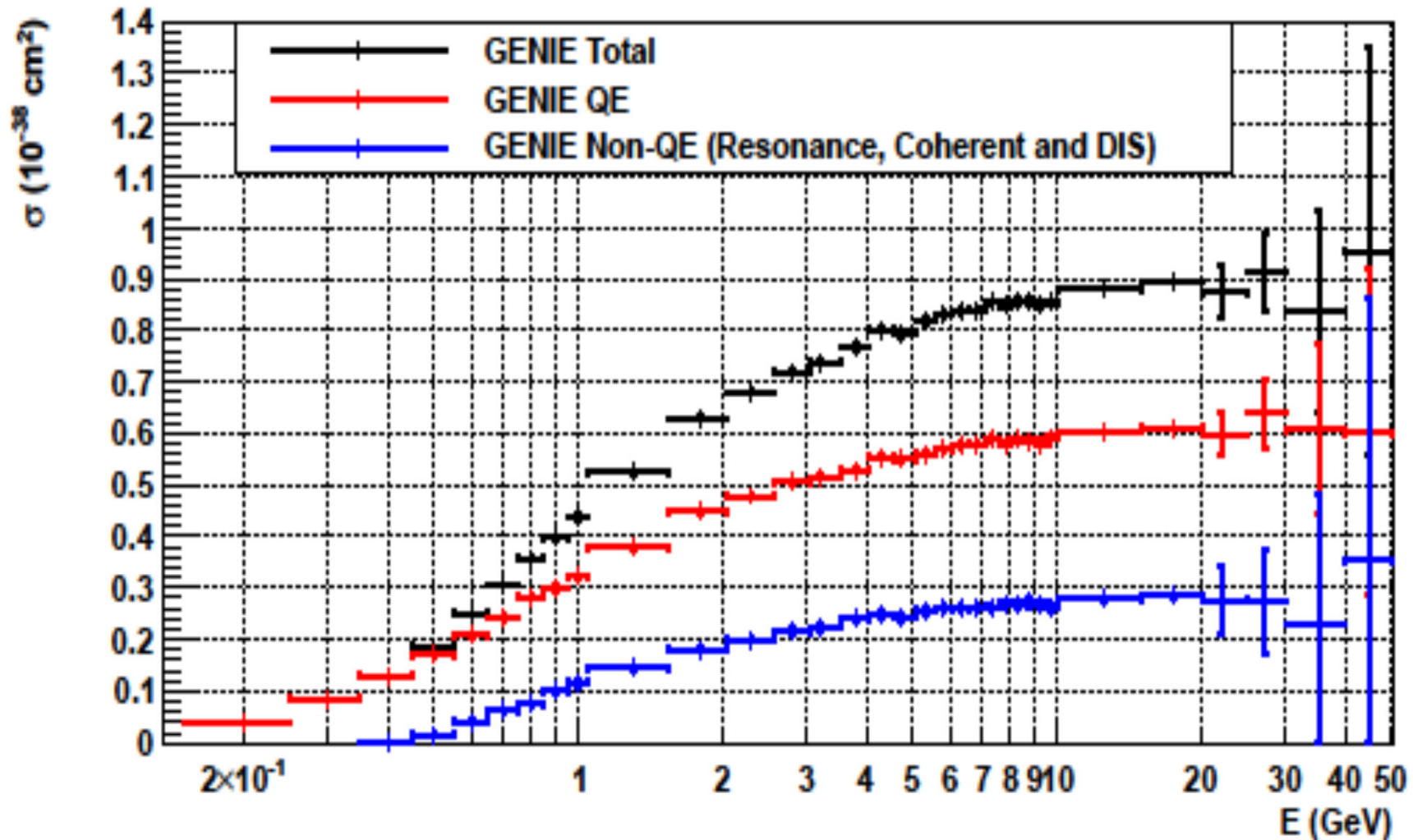
... $\nu_{max}=0.5$ : Cross sections...

$\sigma(\nu<0.5)$  Components for Neutrino on Carbon



... $\nu_{max}=0.5$ : Cross sections...

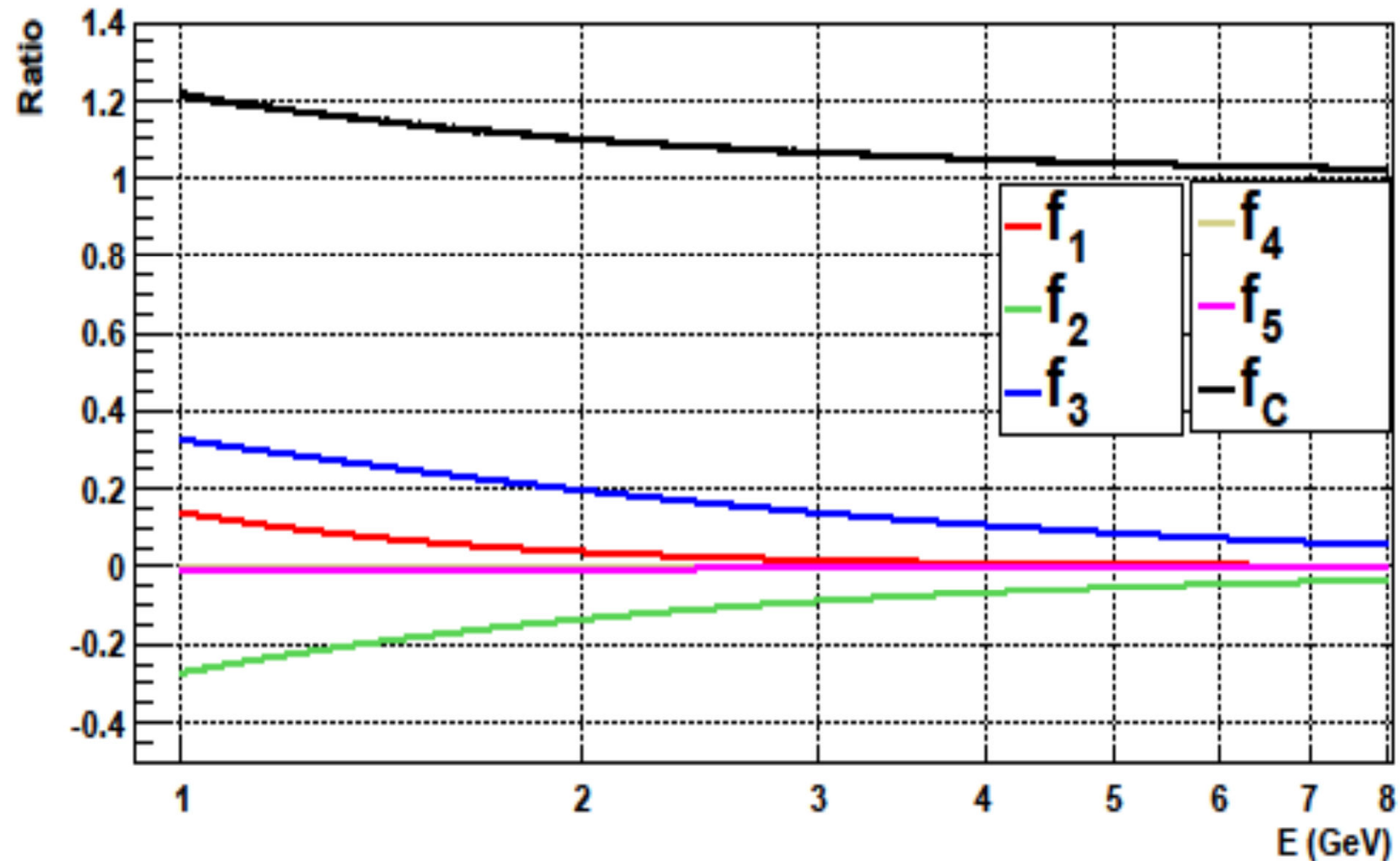
$\sigma(\nu<0.5)$  Components for Antineutrino on Carbon





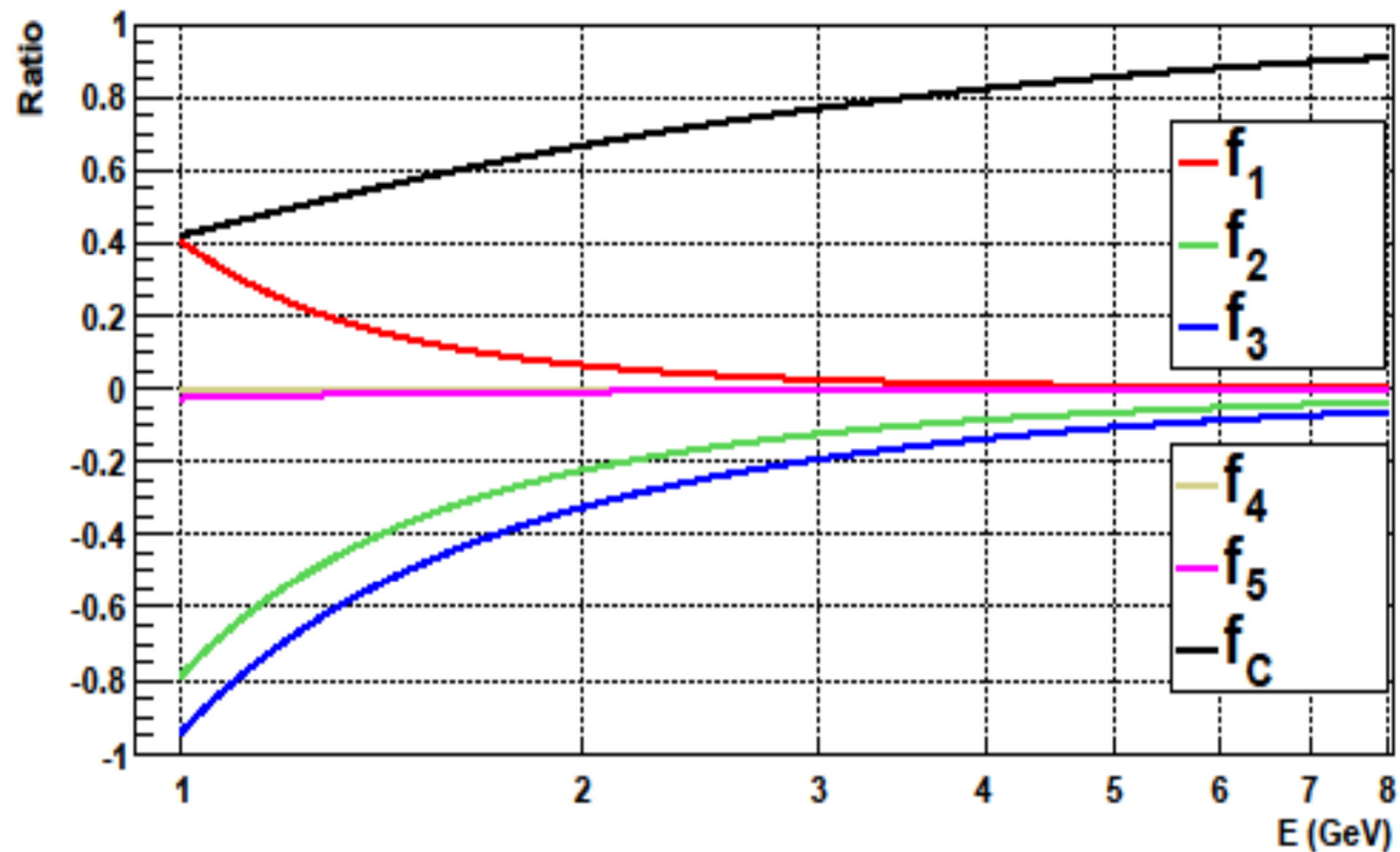
... $\nu_{max}=0.5$ : Total = QE T.E. + Paschos 2011 + FIT-B...

Total Contributions to  $f_c$  for Neutrino ( $\nu < 0.5$ ,  $W < 1.4$ )



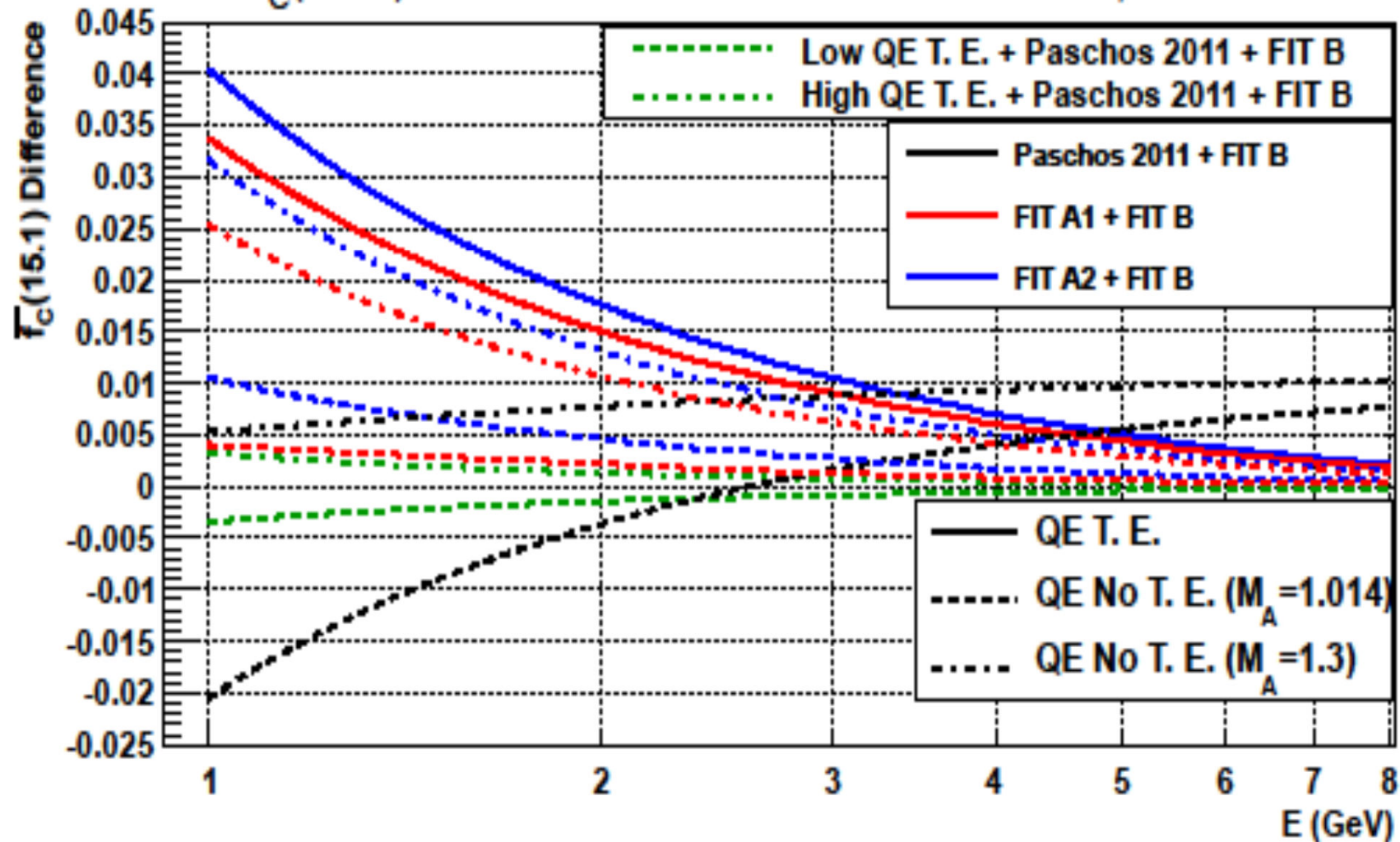
... $\nu_{max}=0.5$ : Total = QE T.E. + Paschos 2011 + FIT-B...

Total Contributions to  $f_c$  for Antineutrino ( $\nu < 0.5$ ,  $W < 1.4$ )



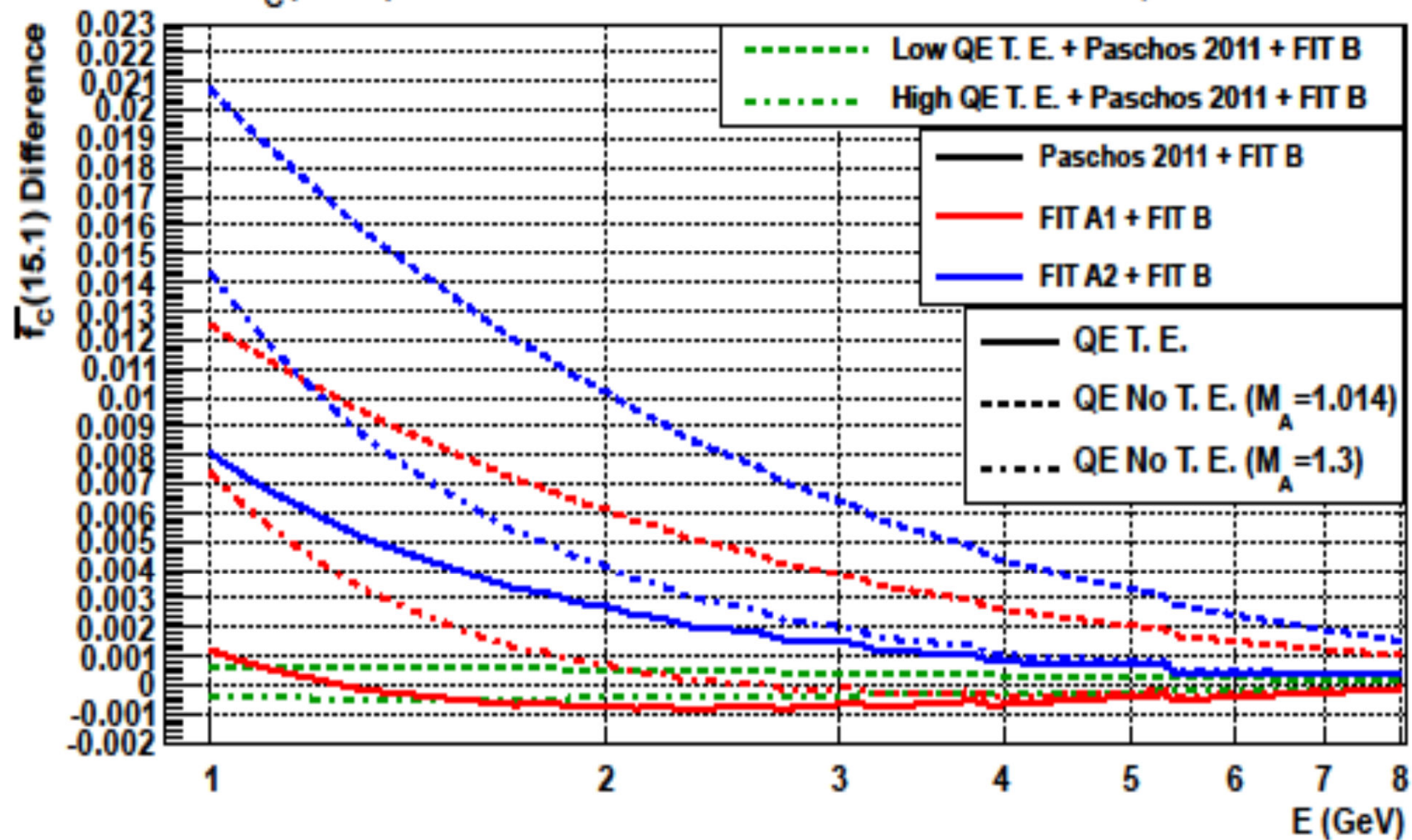
$$\dots \nu_{max}=0.5\dots$$

$\overline{f}_C(15.1)$  Error for Neutrino on Carbon  $\nu < 0.5$ ,  $W < 1.4$



... $\nu_{max}=0.5$ ...

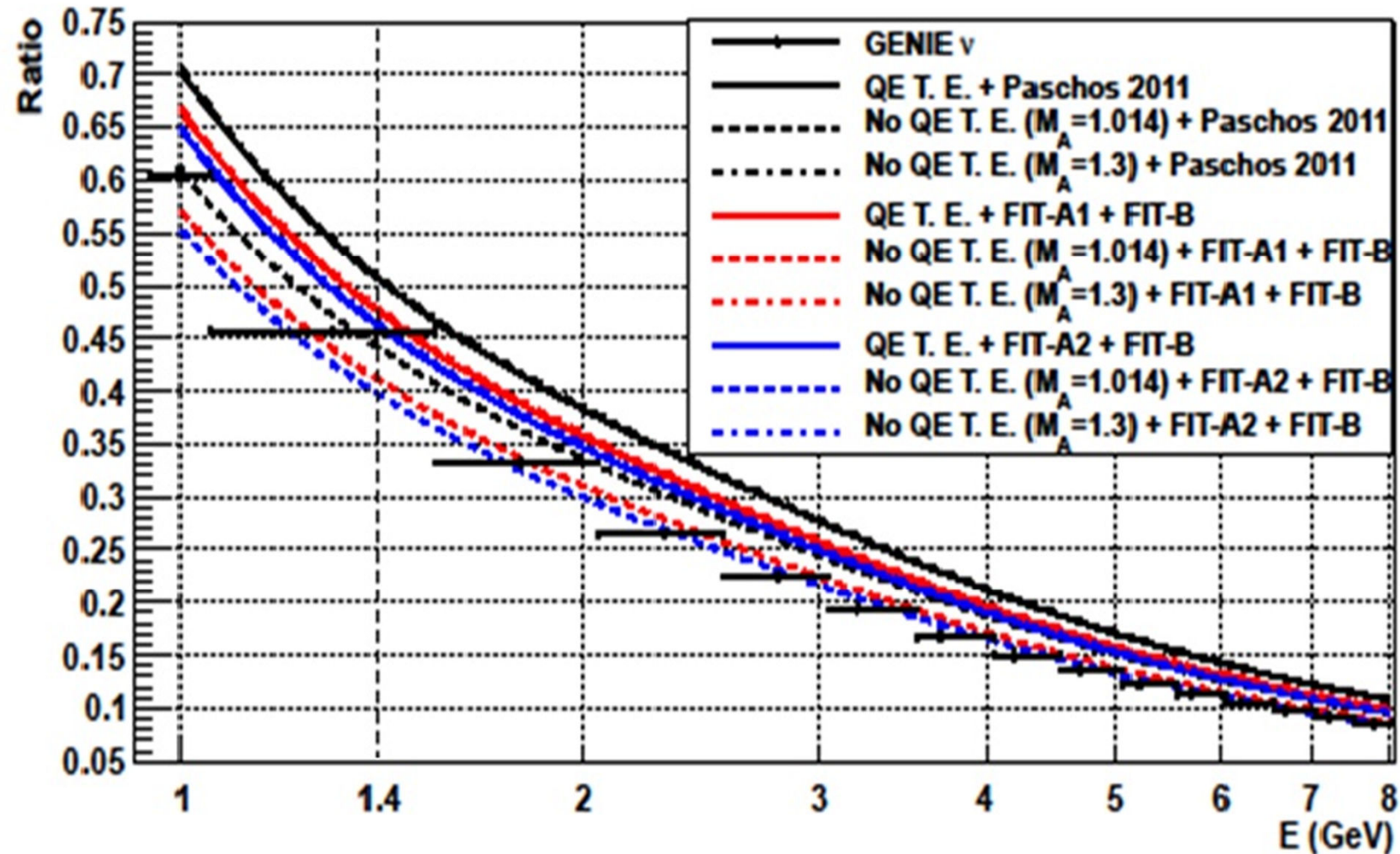
$\bar{f}_C(15.1)$  Error for Antineutrino on Carbon  $\nu < 0.5$ ,  $W < 1.4$





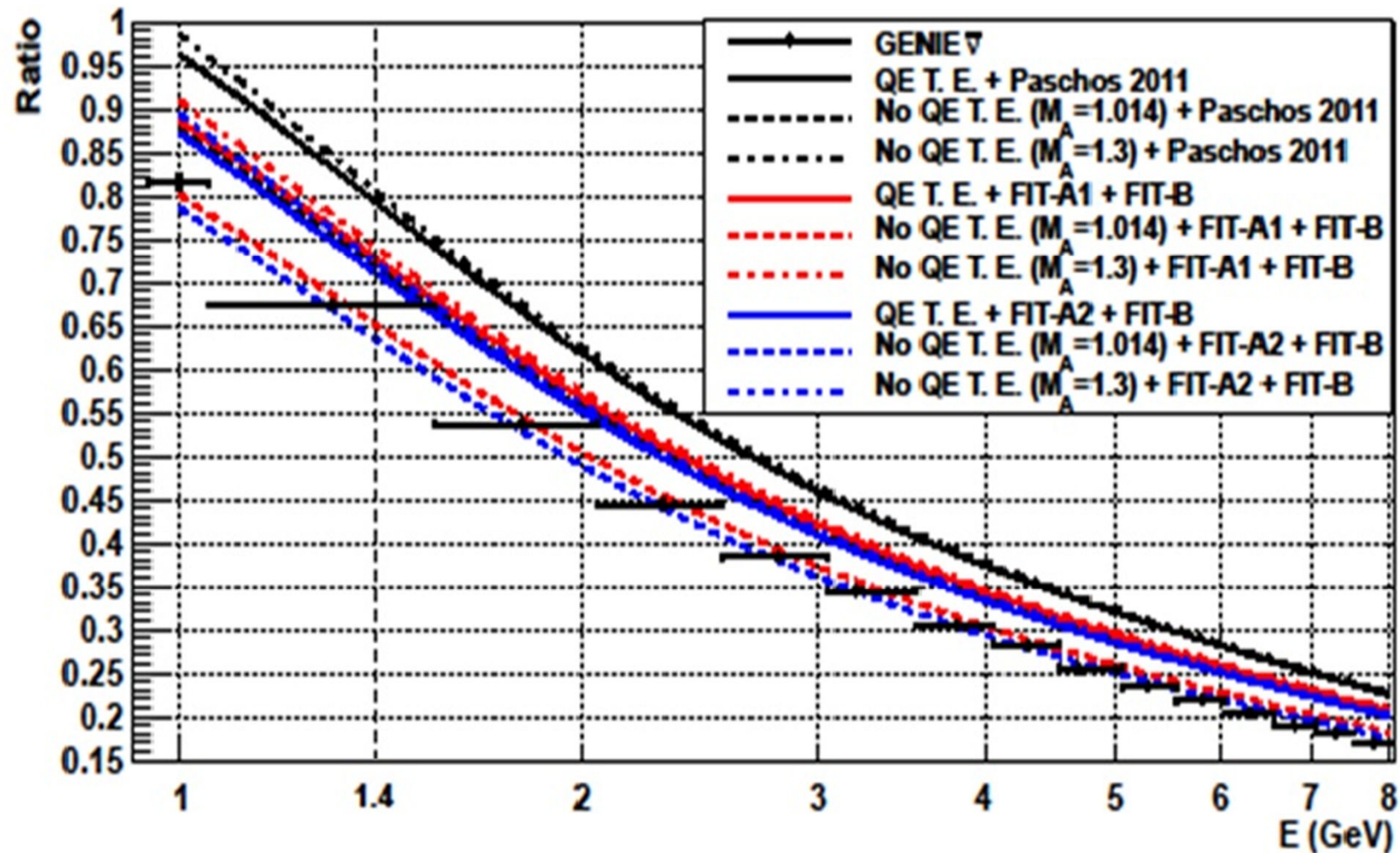
... $\nu_{max}=0.5$ ...

Fraction of  $\nu < 0.5$ ,  $W < 1.4$  Cross Sections for Neutrino



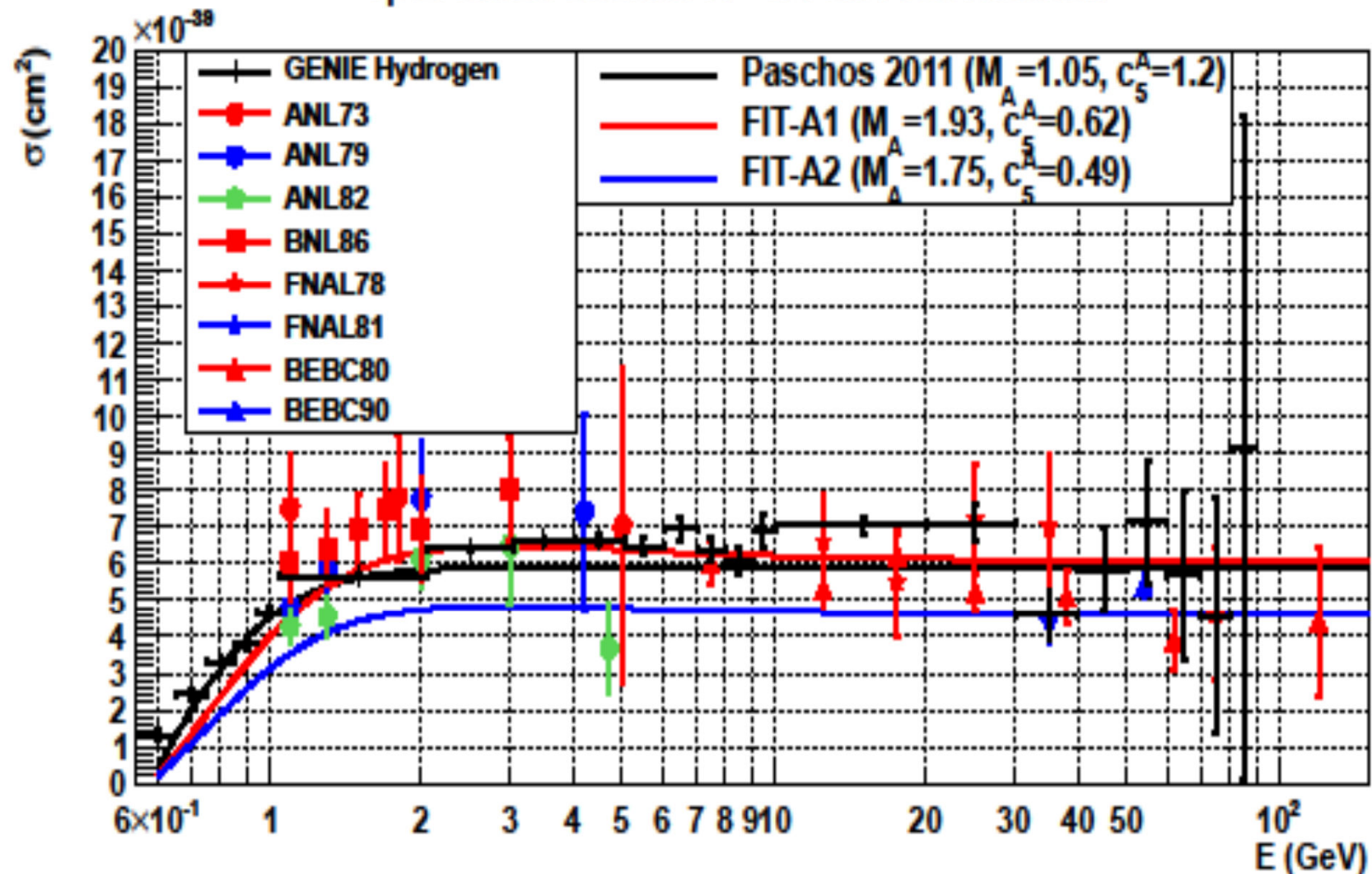
$$\dots \nu_{max}=0.5\dots$$

Fraction of  $\nu < 0.5$ ,  $W < 1.4$  Cross Sections for Antineutrino



# $\nu p$ Delta Cross Section on Free Nucleon

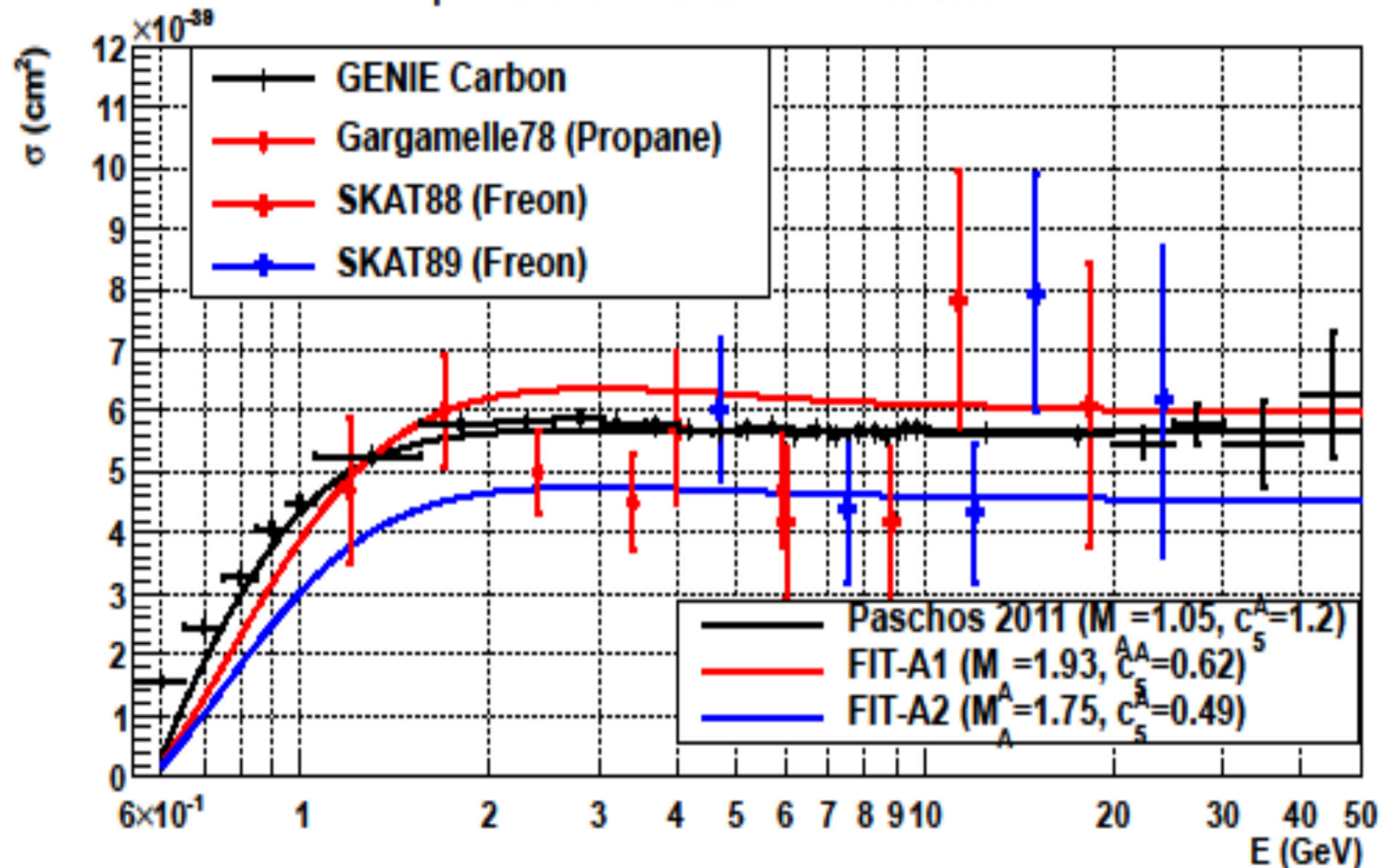
$\nu p$   $\Delta$  Cross Section  $W < 1.4$  on Free Nucleon





# $\nu p$ Delta Cross Section on Carbon

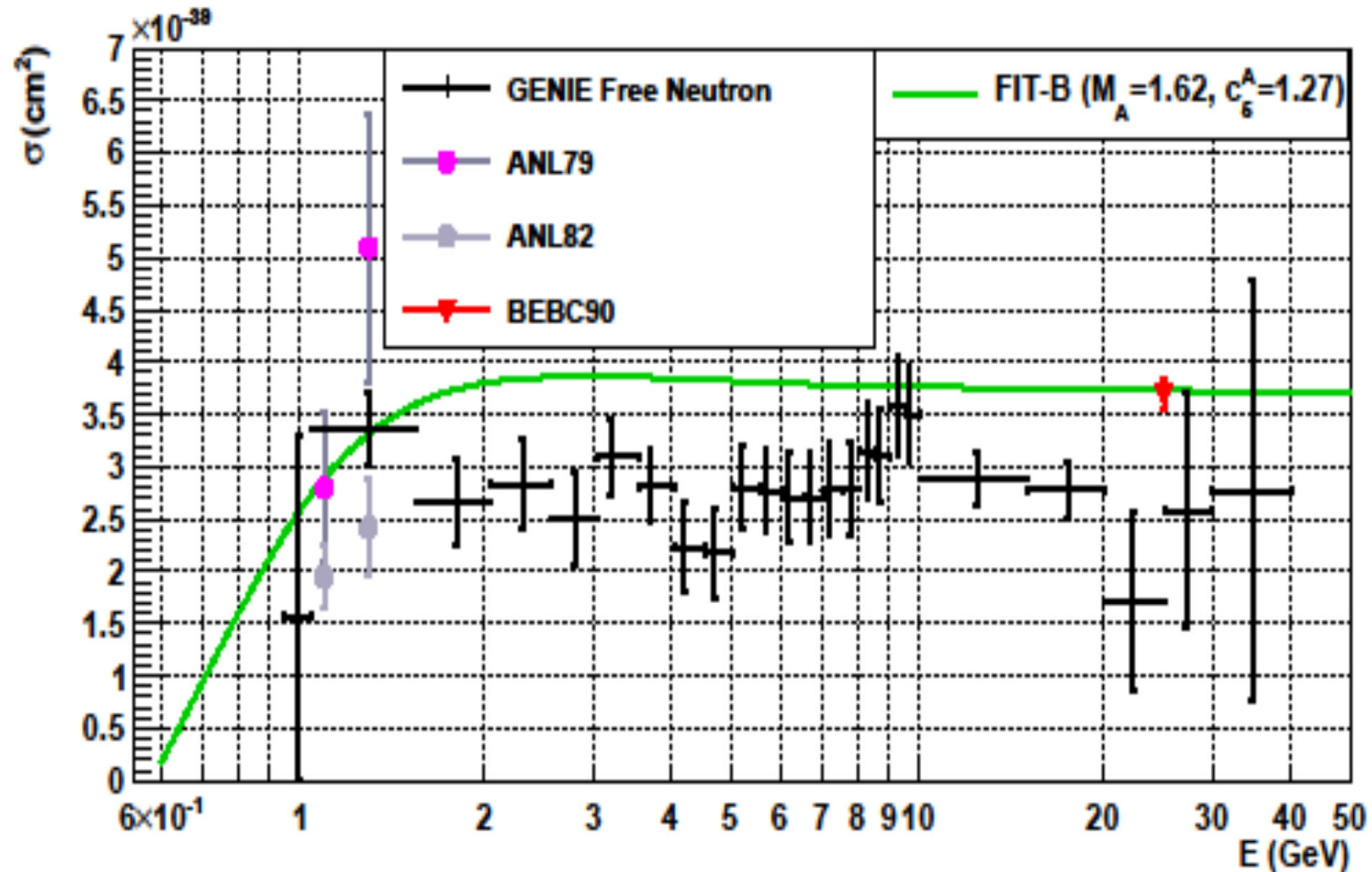
$\nu p$   $\Delta$  Cross Section  $W < 1.4$  on Carbon





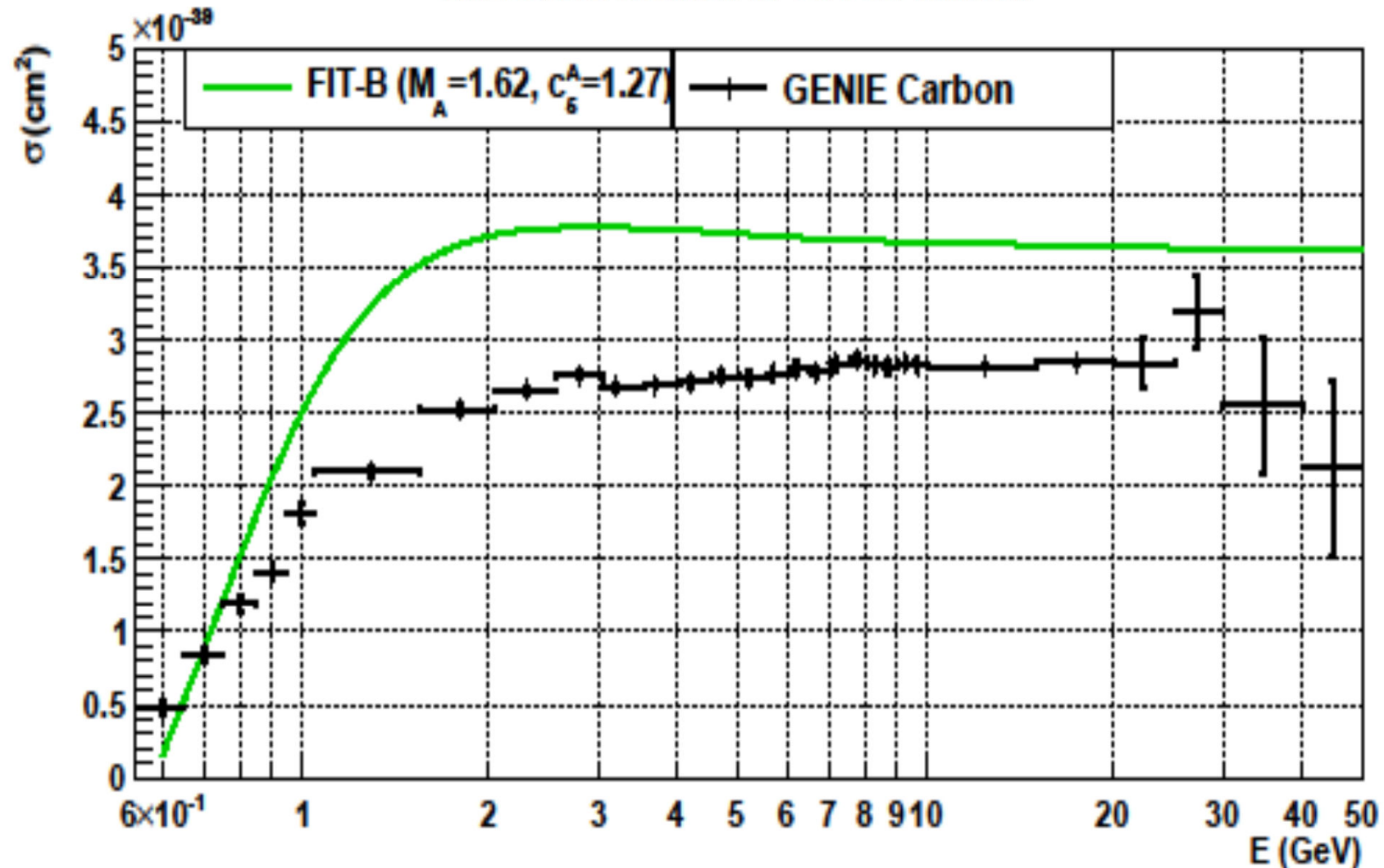
# $\nu n$ Delta Cross Section on Free Nucleon

vn  $\Delta$  Cross Section  $W < 1.4$  on Free Nucleon

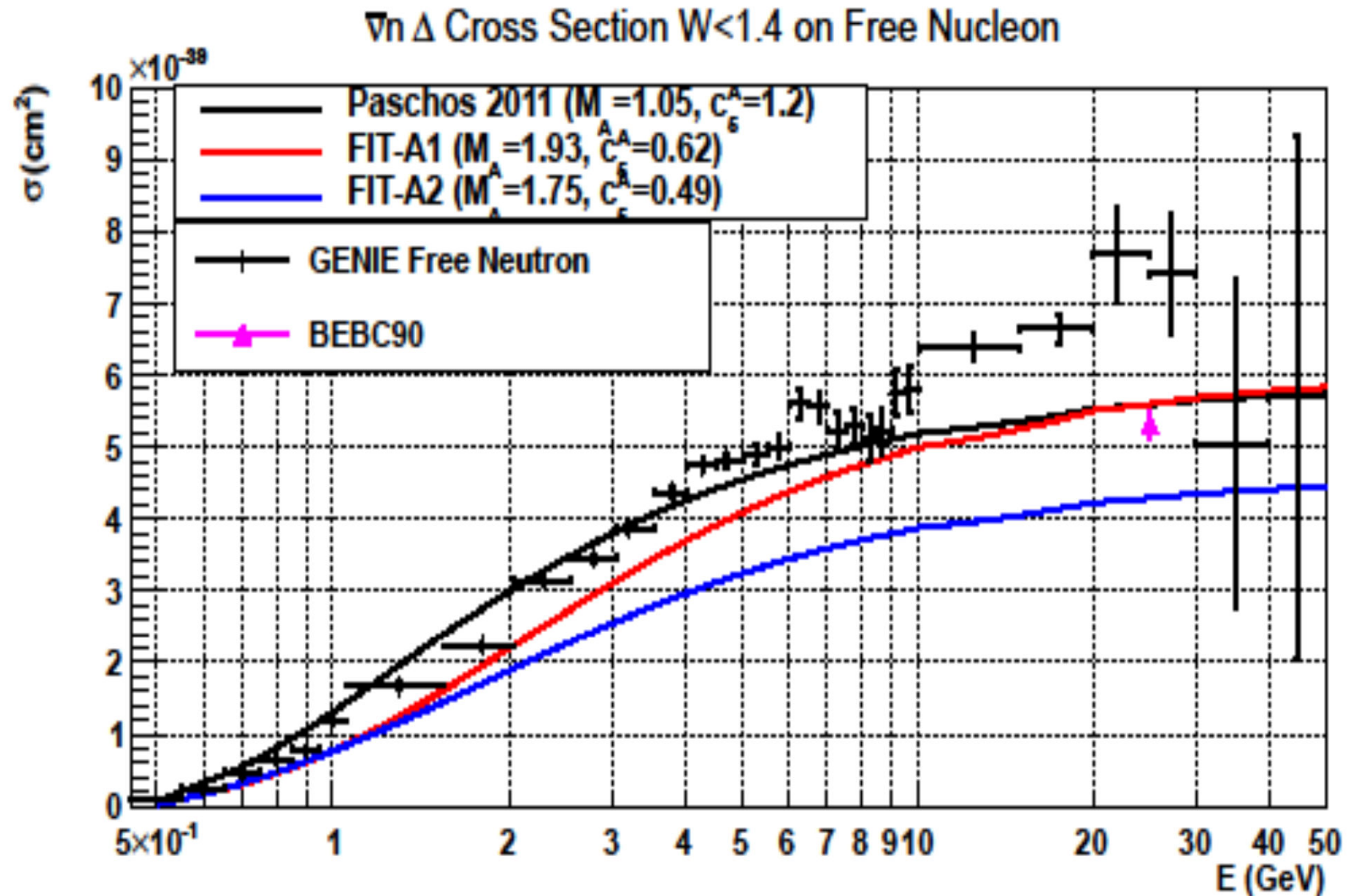


# $\nu n$ Delta Cross Section on Carbon

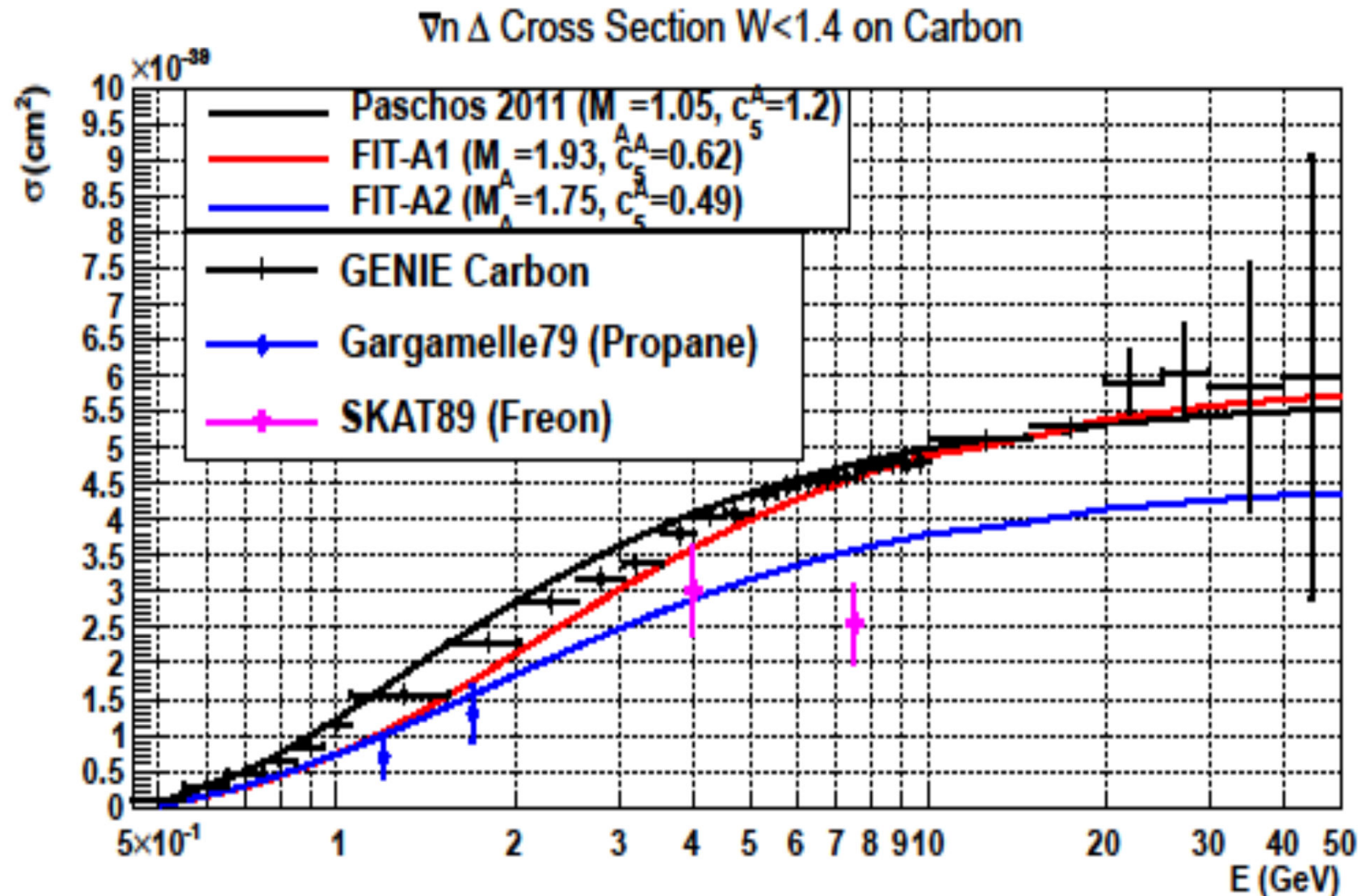
$\nu n$   $\Delta$  Cross Section  $W < 1.4$  on Carbon



# $\bar{\nu}n$ Delta Cross Section on Free Nucleon



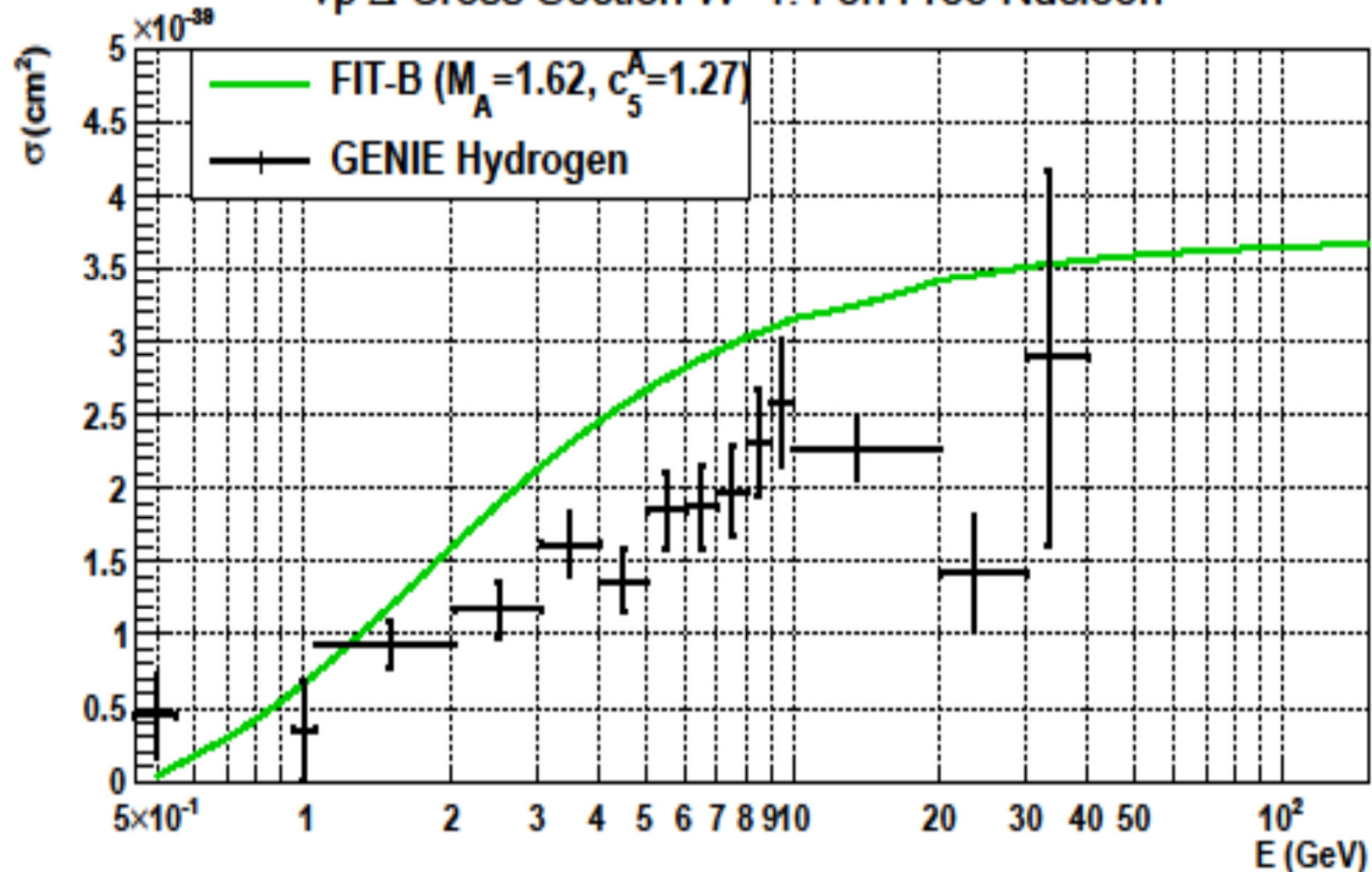
# $\bar{\nu}n$ Delta Cross Section on Carbon



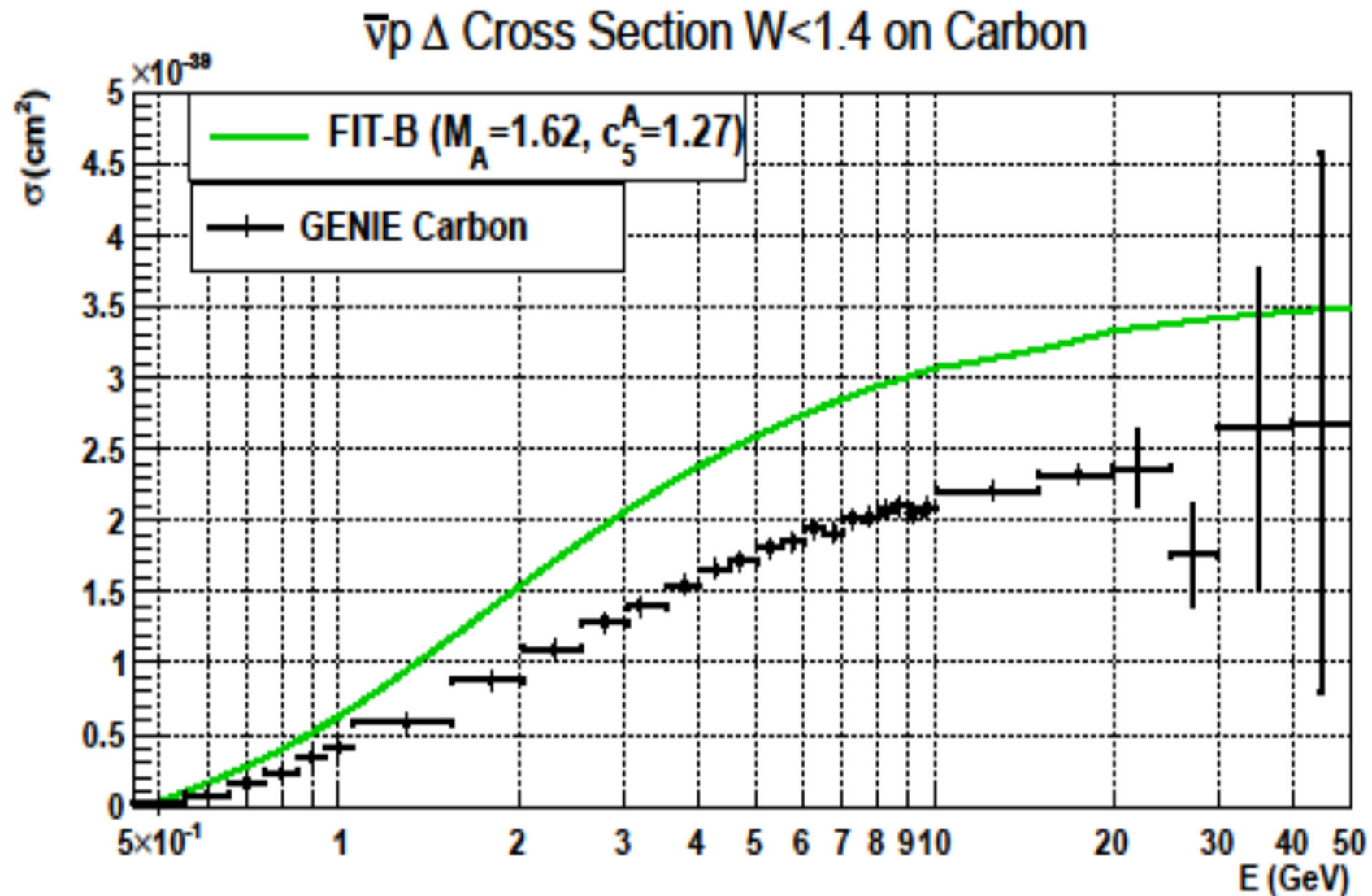


# $\bar{\nu}p$ Delta Cross Section on Free Nucleon

$\bar{\nu}p$   $\Delta$  Cross Section  $W < 1.4$  on Free Nucleon

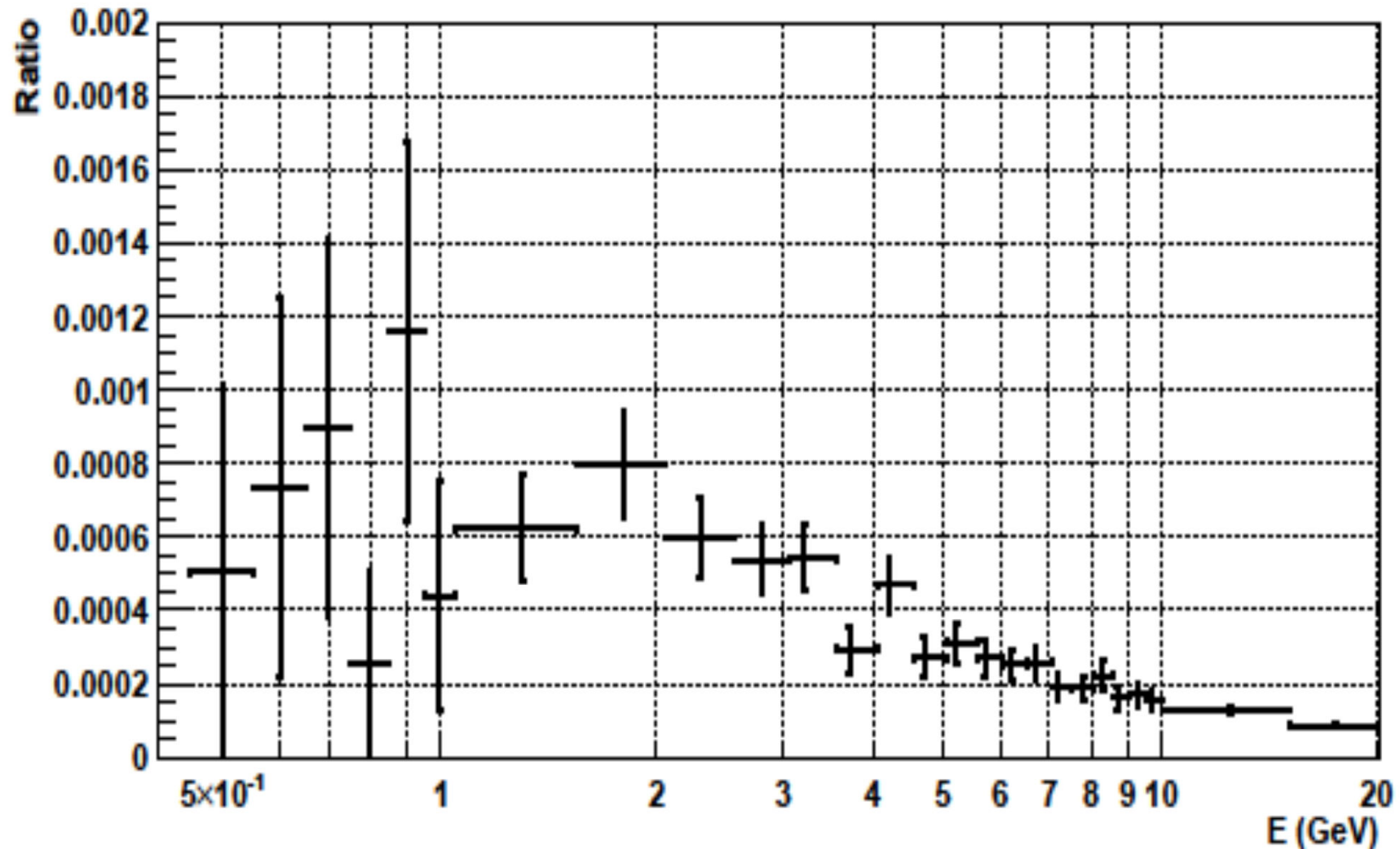


# $\bar{\nu}_p$ Delta Cross Section on Carbon



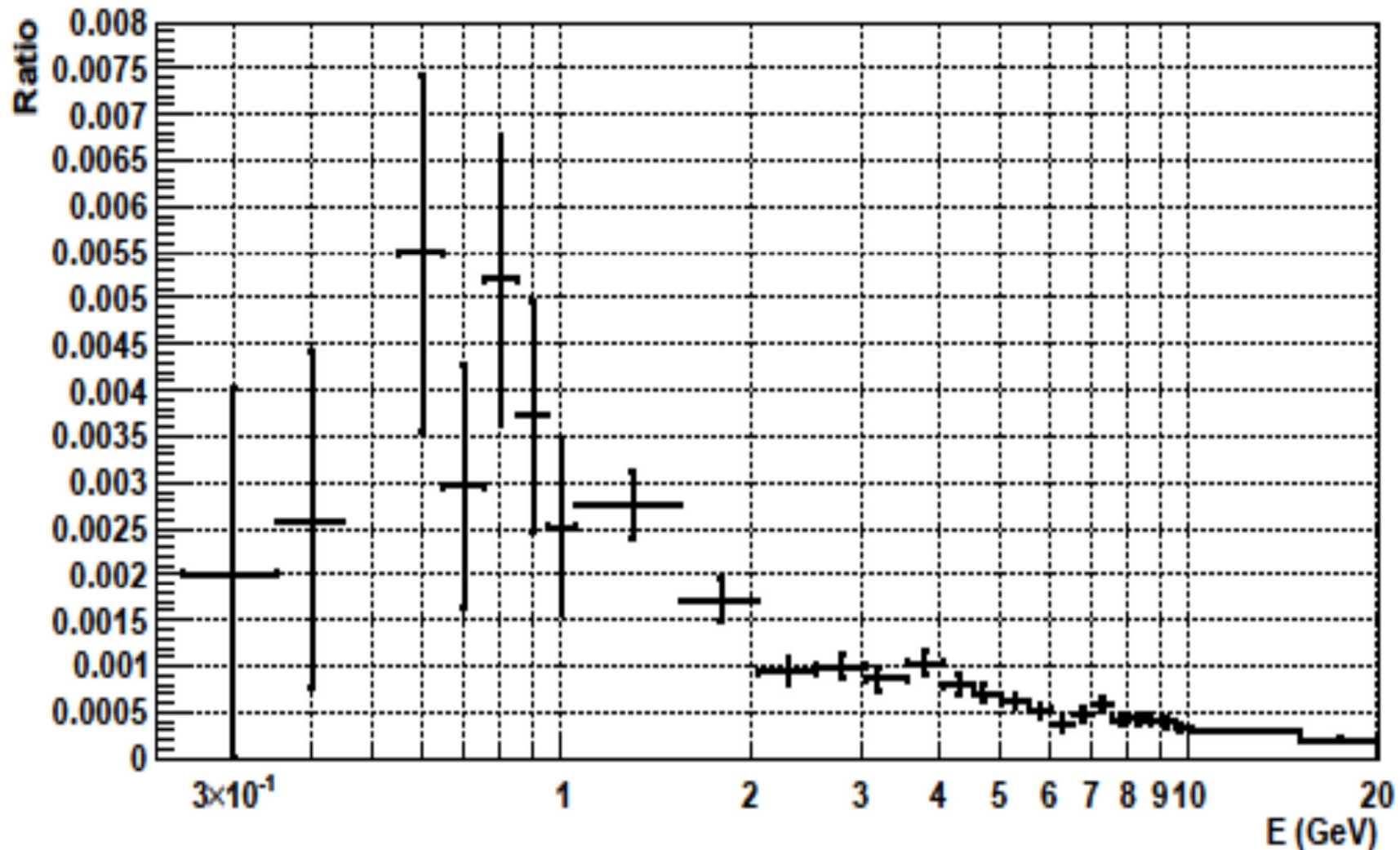
# CC Coherent Fraction on Carbon for $\nu < 0.25 \text{ GeV}$

CC Coherent Pion Fraction on Carbon for  $\nu$  ( $\nu < 0.25$ )



# CC Coherent Fraction on Carbon for $\nu < 0.25 \text{ GeV}$

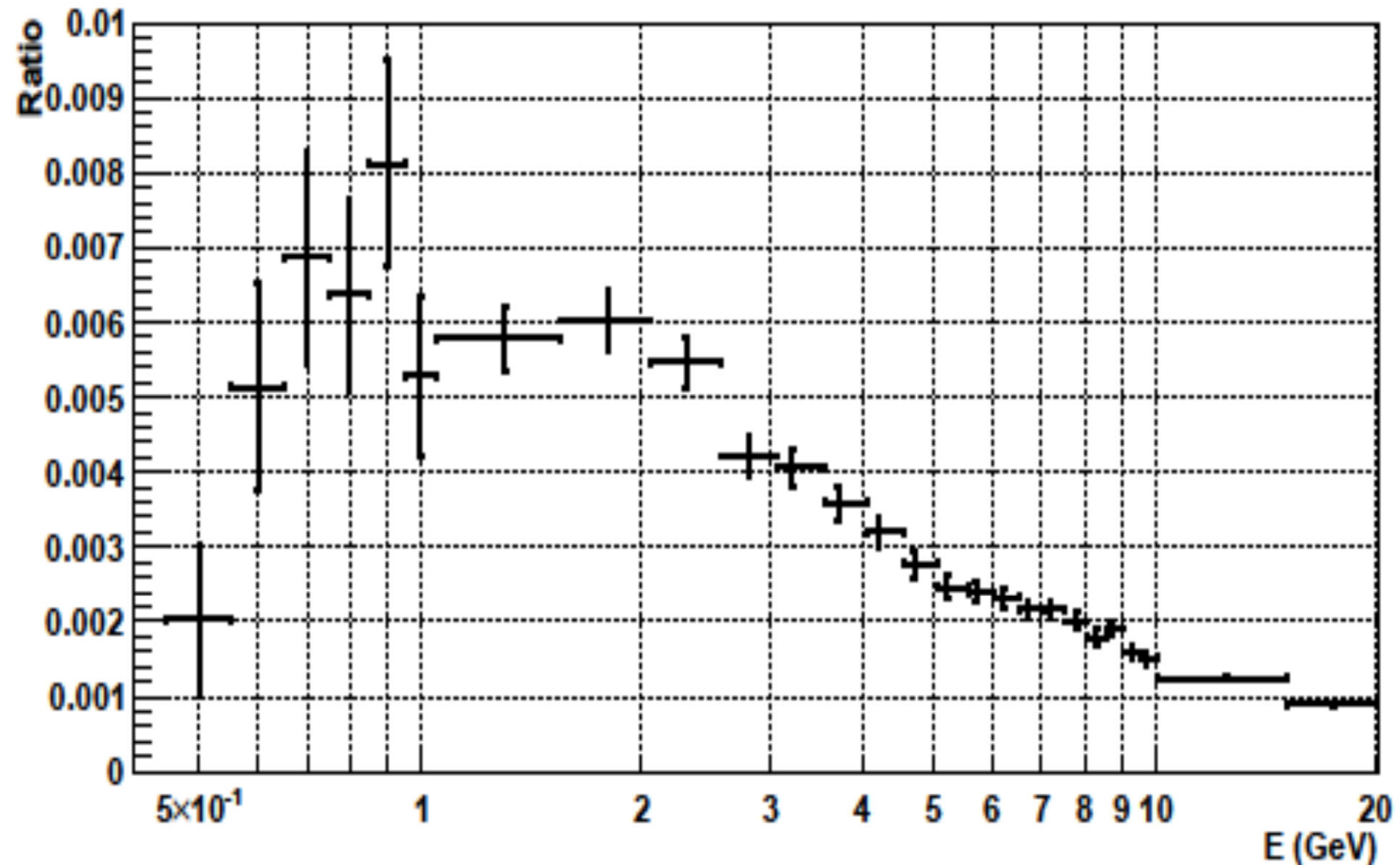
CC Coherent Pion Fraction on Carbon for  $\nabla$  ( $\nu < 0.25$ )





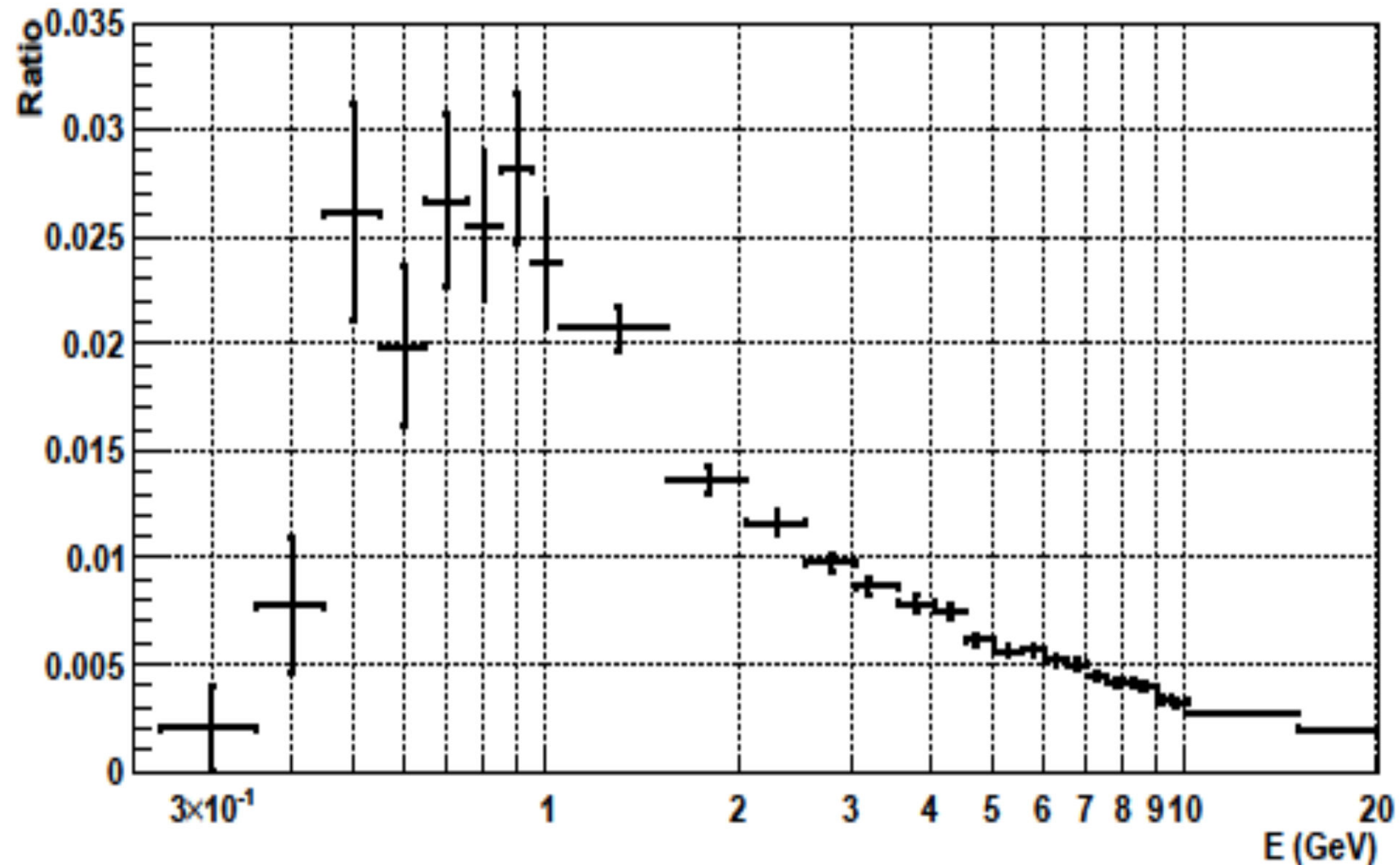
# CC Coherent Fraction on Carbon for $\nu < 0.5 \text{ GeV}$

CC Coherent Pion Fraction on Carbon for  $\nu$  ( $\nu < 0.5$ )



# CC Coherent Fraction on Carbon for $\nu < 0.5 \text{ GeV}$

CC Coherent Pion Fraction on Carbon for  $\bar{\nu}$  ( $\nu < 0.5$ )



# Additional References

- [1] P. Adamson et al. Phys. Rev. Lett. 101. 131802. 4 (2008).
- [2] Un Ki Yang, Ph.D. thesis, University of Rochester [FERMILAB-THESIS-2001-09, 2001].