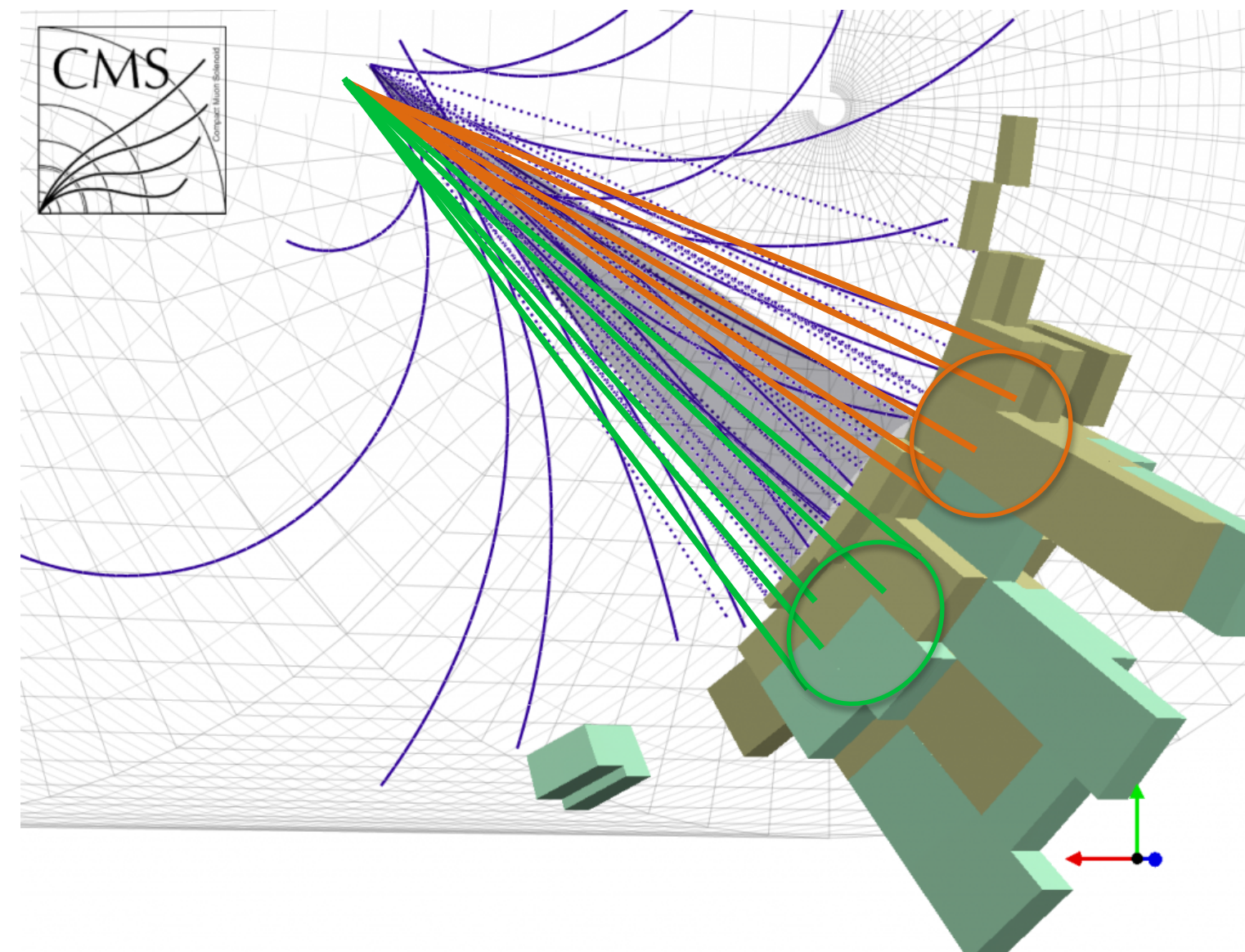


# Boosted resonance searches at CMS and their long-term impact

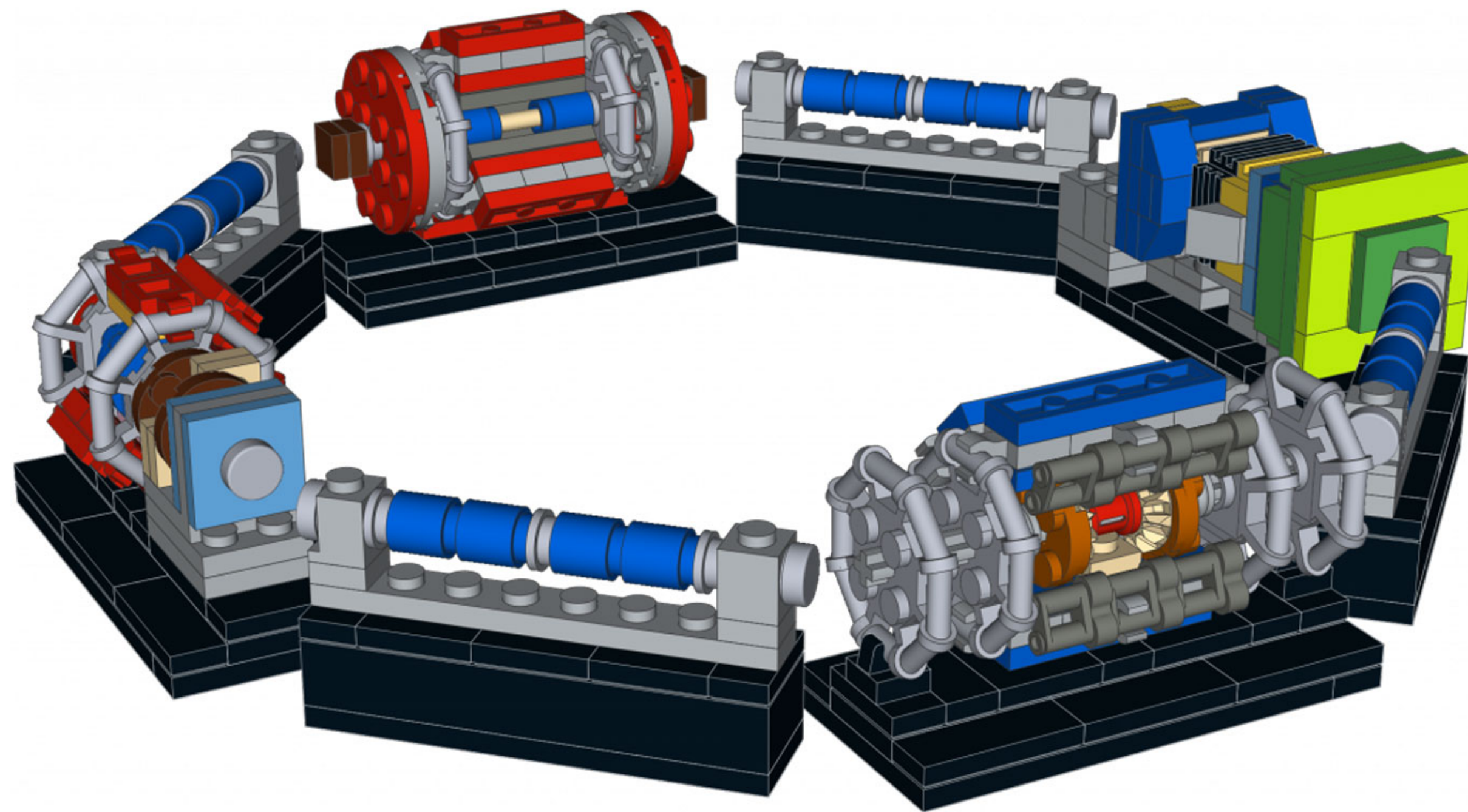


Clemens Lange (CERN)

Fermilab Wine & Cheese Seminar  
15<sup>th</sup> January 2021

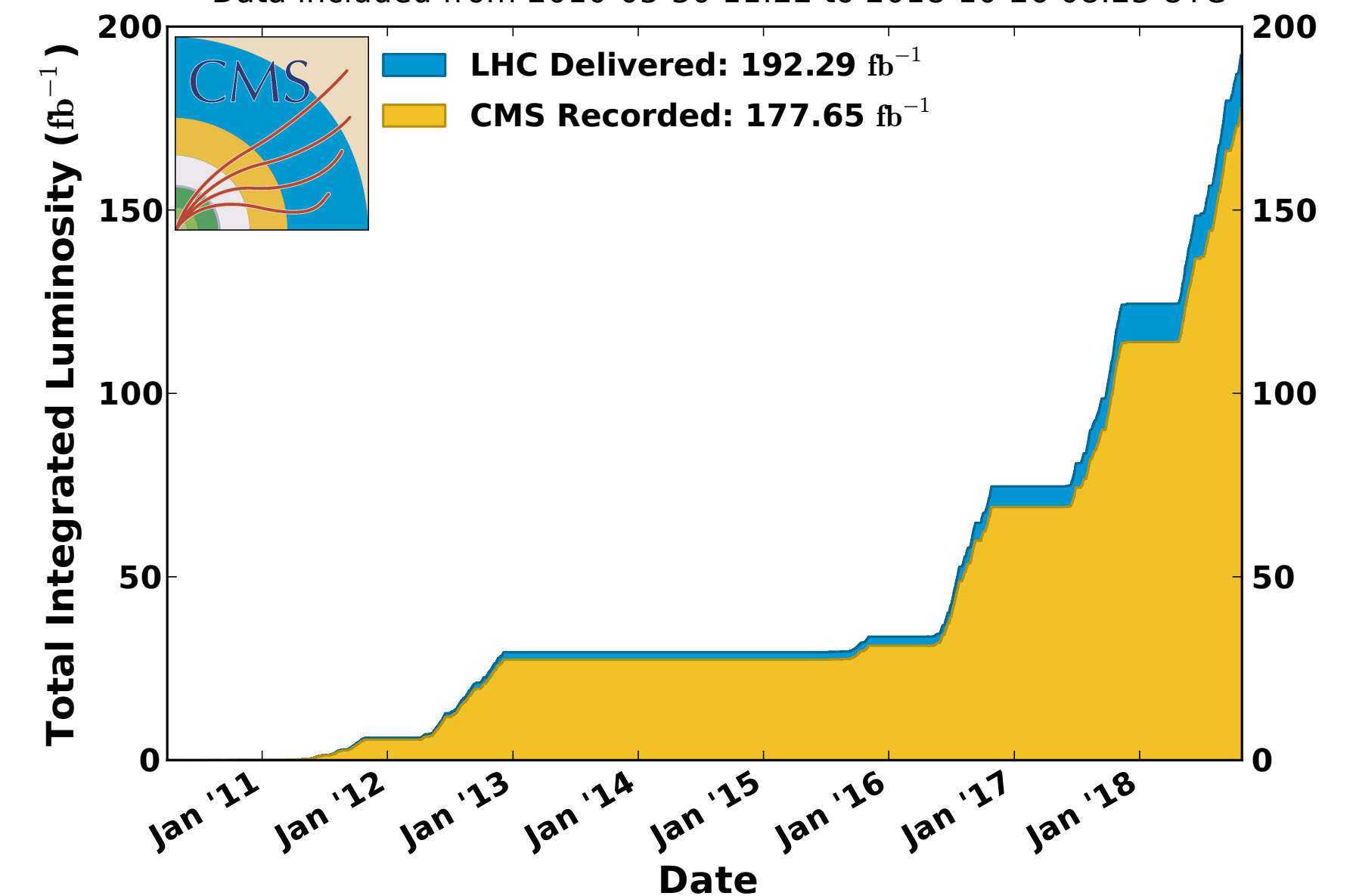


➤ The Large Hadron Collider (LHC) is the world's largest and **highest-energy** particle accelerator



CMS Integrated Luminosity, pp,  $\sqrt{s} = 7, 8, 13$  TeV

Data included from 2010-03-30 11:22 to 2018-10-26 08:23 UTC



- Delivered  $\mathcal{L} = 163 \text{ fb}^{-1}$  of proton-proton collisions at  $\sqrt{s} = 13 \text{ TeV}$
- Exceeded most of its design parameters, producing collisions 49% of the time in 2018

Image: [Nathan Readloff](#)

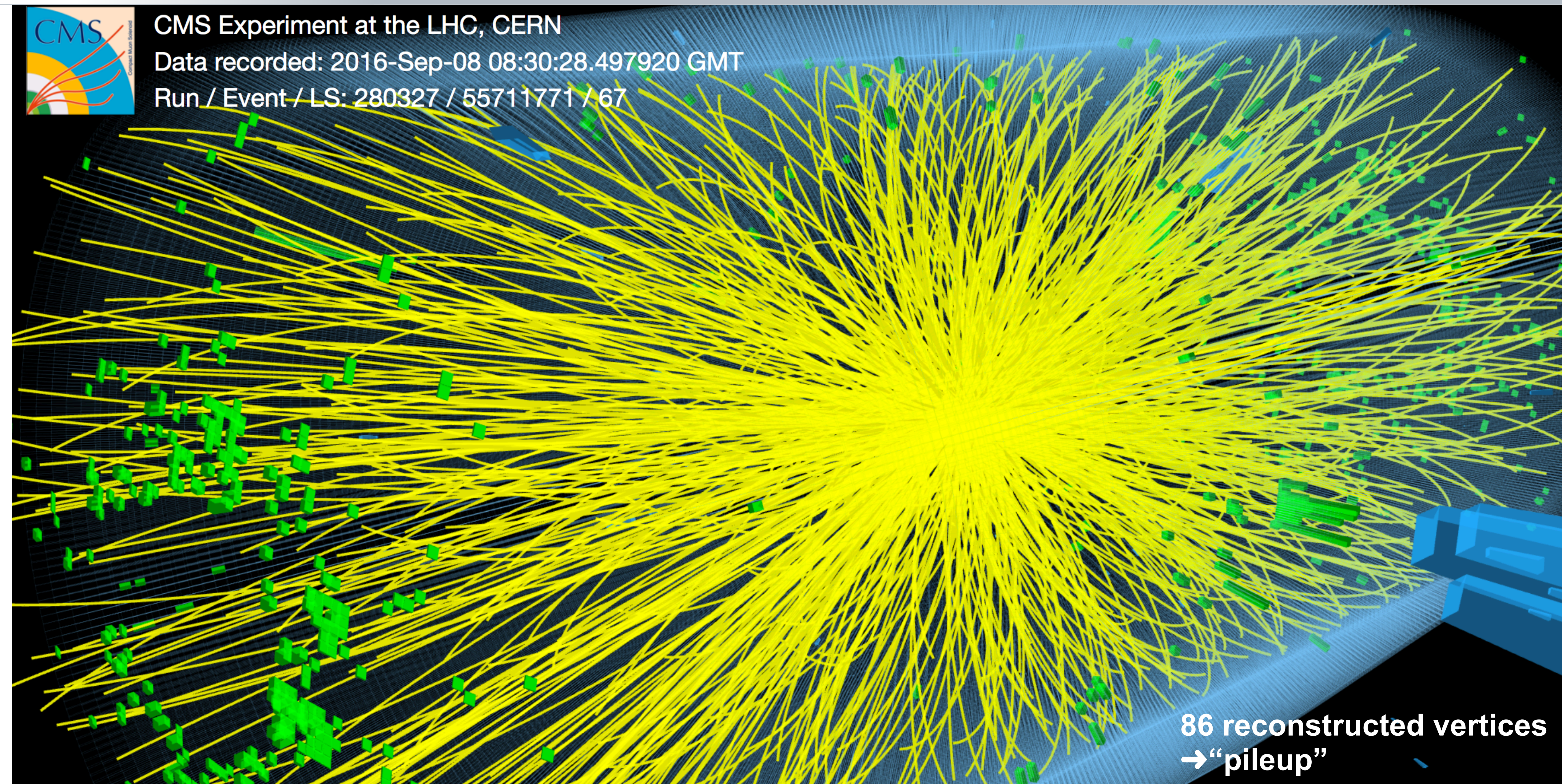
# ... creating a big mess



CMS Experiment at the LHC, CERN

Data recorded: 2016-Sep-08 08:30:28.497920 GMT

Run / Event / LS: 280327 / 55711771 / 67



86 reconstructed vertices  
→ "pileup"

➤ Finding a **very heavy and extremely rare resonance** in events like that

➤ Finding a **very heavy and extremely rare resonance** in events like that

Why?

➤ Finding a **very heavy and extremely rare resonance** in events like that

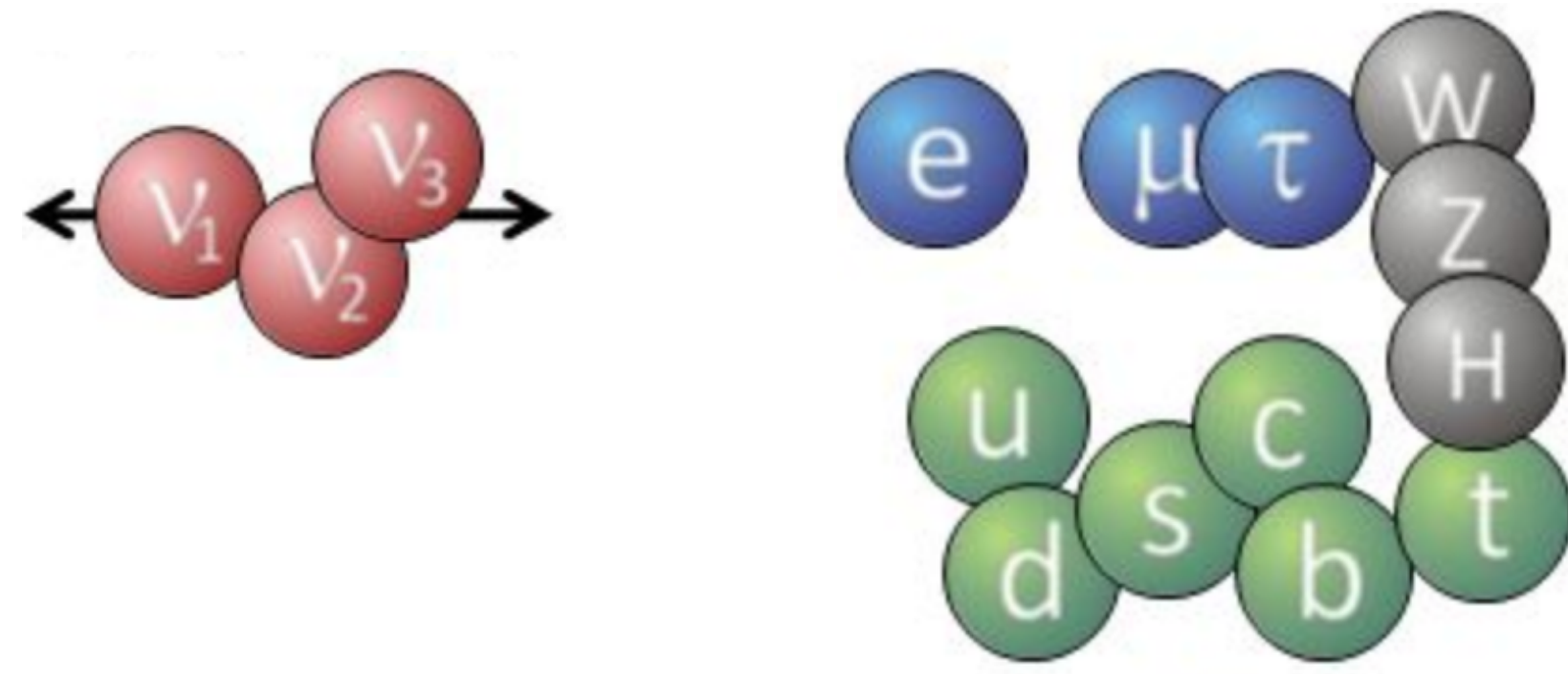
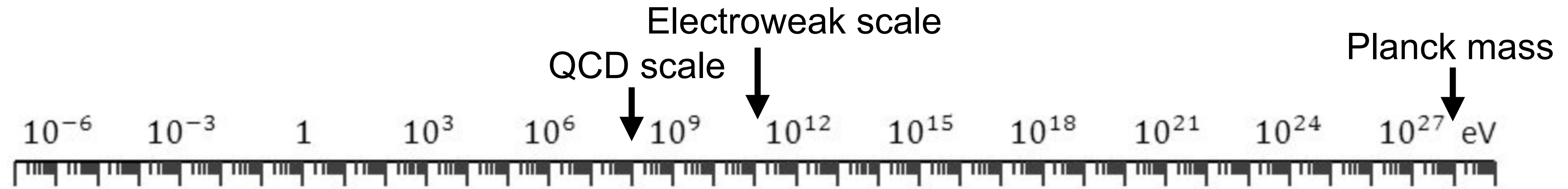
Why?

➤ Try to find a possible explanation to the big difference between **weak force** and **gravity**?

$$\mu^2 = \lambda v^2 = \frac{\lambda}{g^2} 4M_W^2 \sim \underbrace{10^4 \text{ GeV}^2}_{\text{Electroweak scale}} \ll M_{Pl} \sim \underbrace{10^{38} \text{ GeV}^2}_{\text{Planck scale}}$$

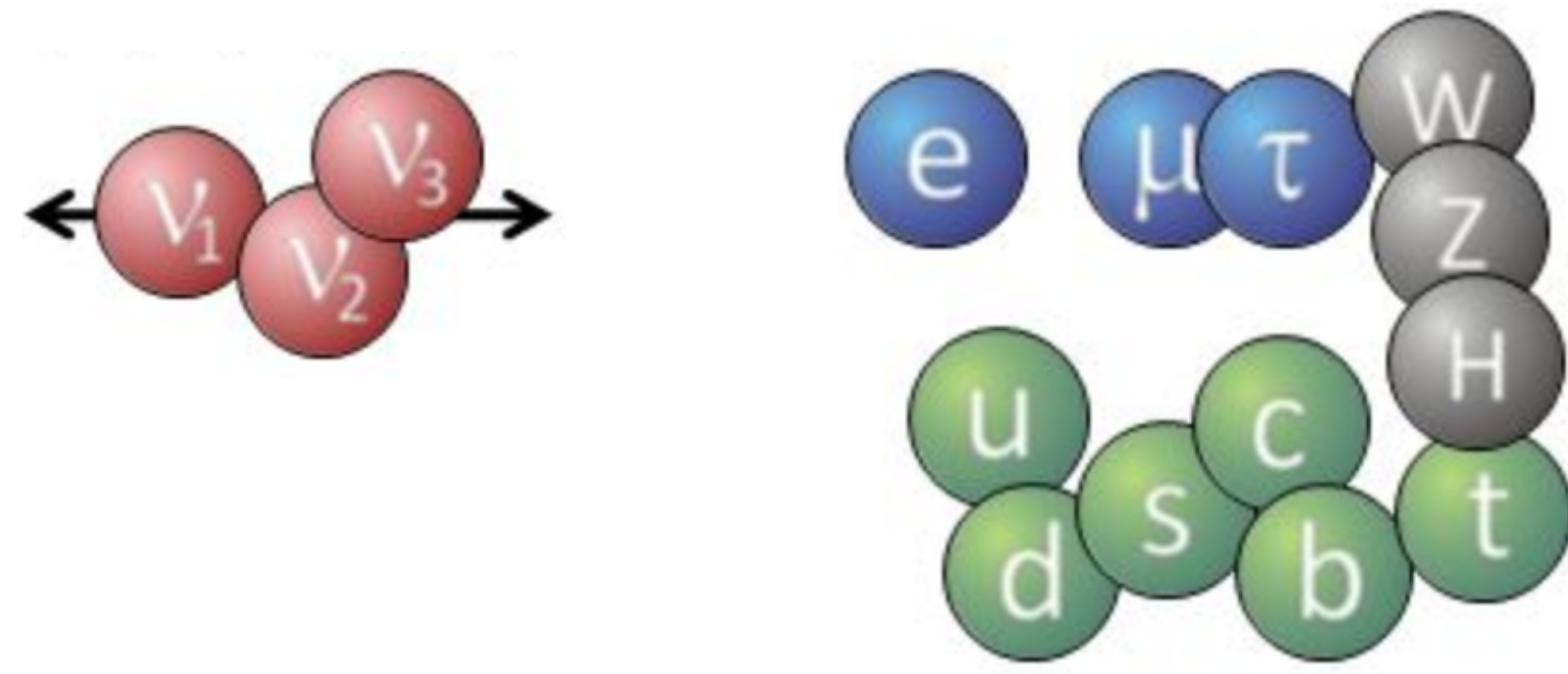
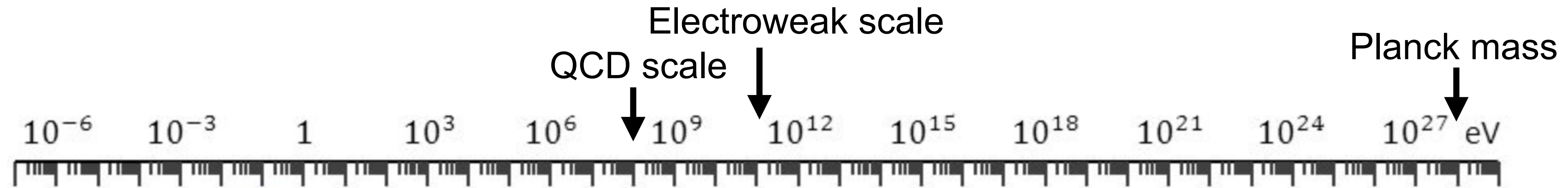
- Referred to as **hierarchy problem**
  - In other words — why is the **Higgs boson** so **light**?
- „Natural“ explanation would be that SM is replaced by another theory at the TeV scale:  $\mu^2 \sim (\text{heavier scale})^2 \rightarrow$  **new particles**

# More on the hierarchy problem



**No idea what's happening in this range**

# More on the hierarchy problem



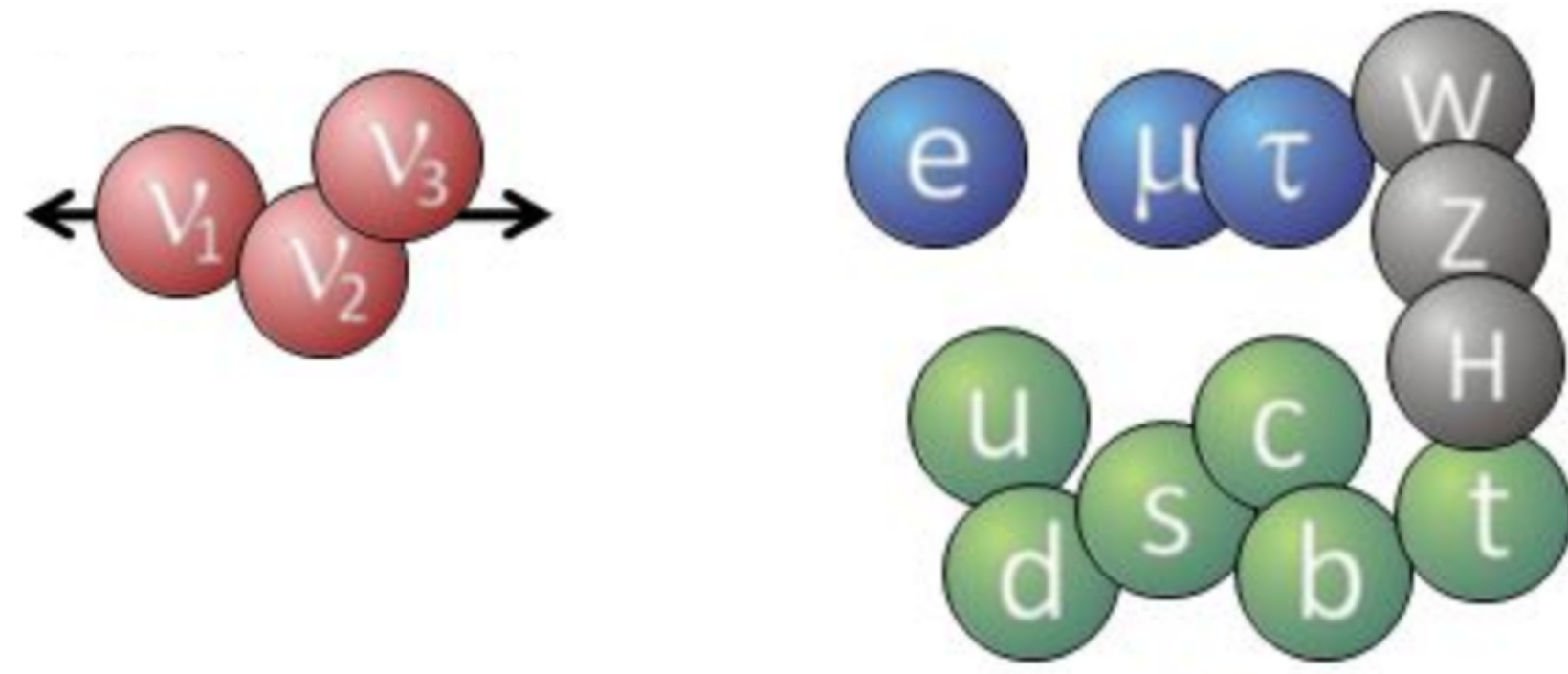
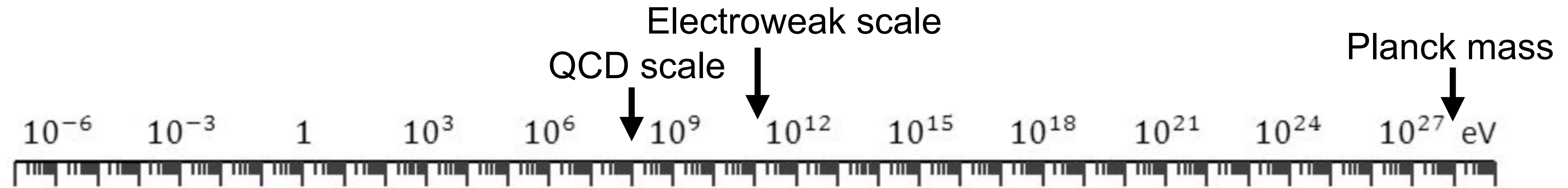
**SUSY?** Explaining the Higgs mass by an additional symmetry



No idea what's happening in this range



# More on the hierarchy problem

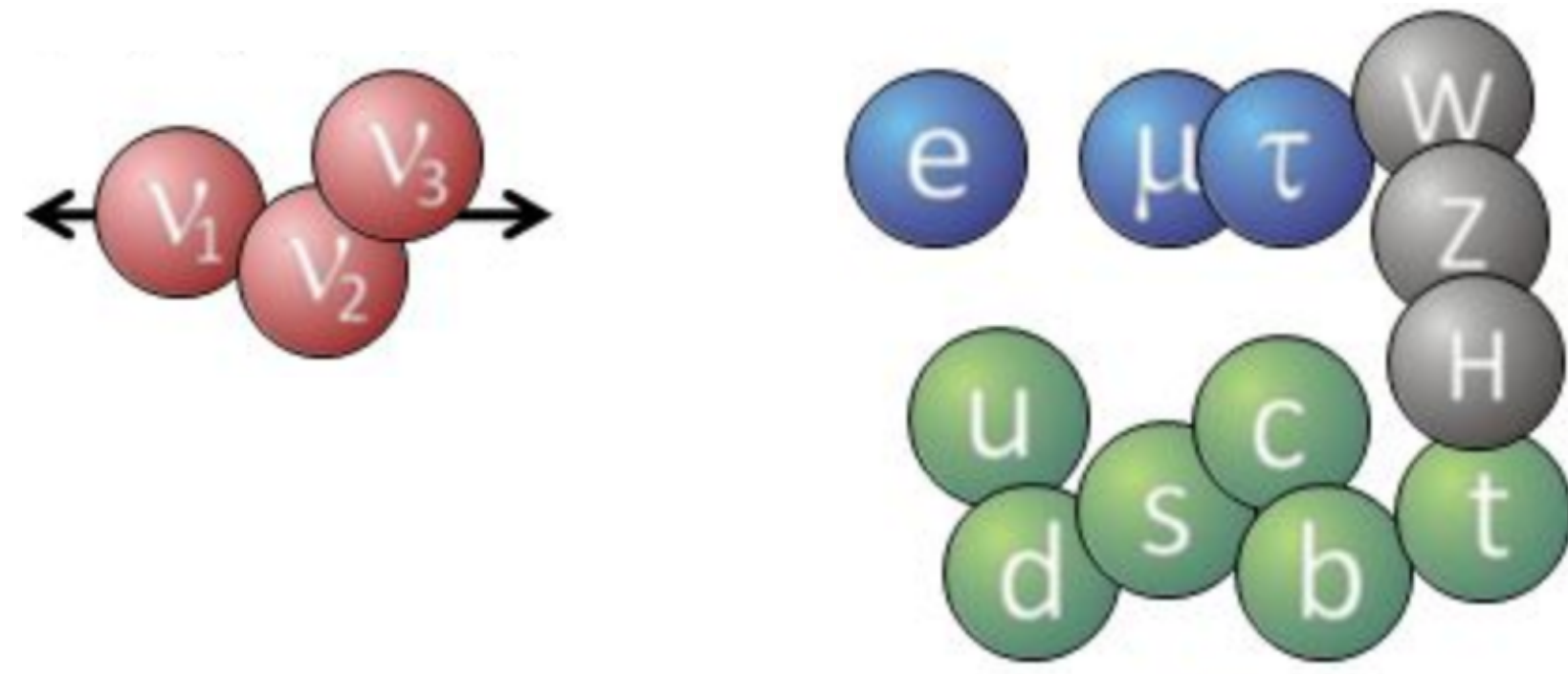
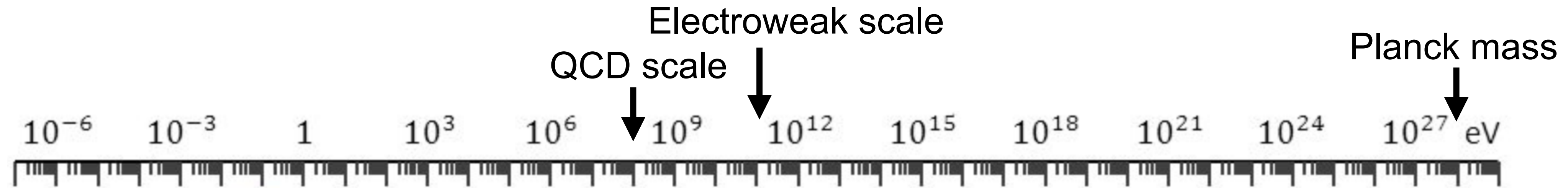


**SUSY?** Explaining the Higgs mass by an additional symmetry

**Composite Higgs?** The Higgs is not elementary

**No idea what's happening in this range**

# More on the hierarchy problem

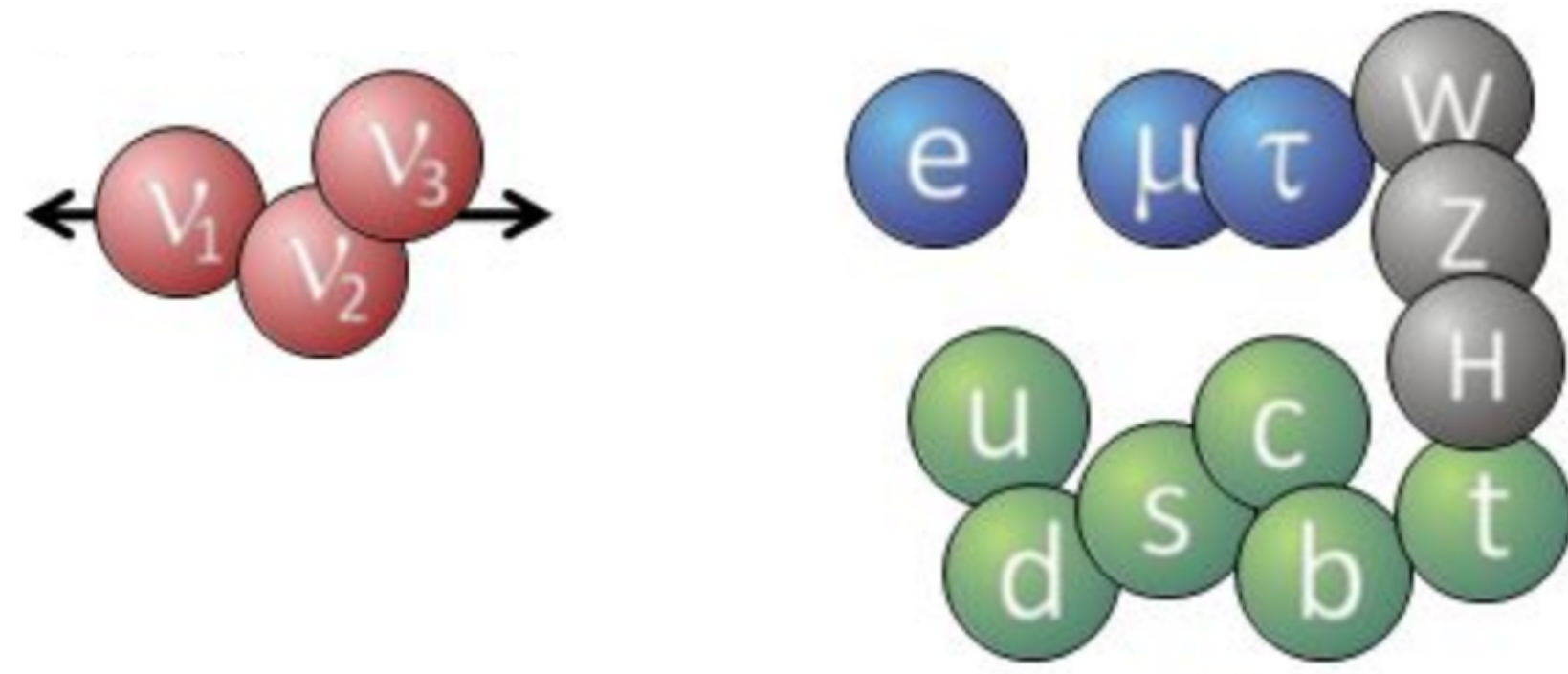
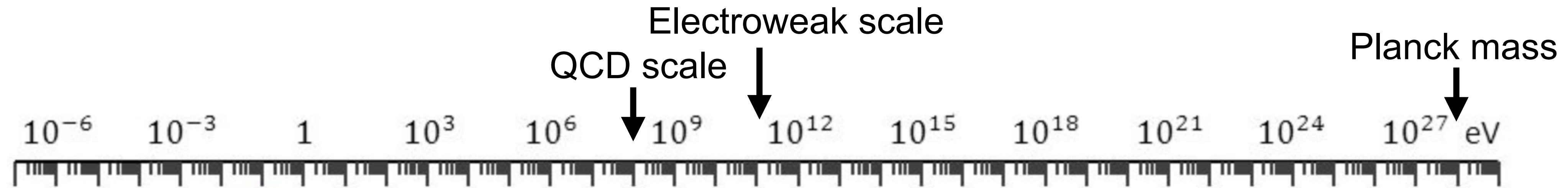


**SUSY?** Explaining the Higgs mass by an additional symmetry

**Composite Higgs?** The Higgs is not elementary

**Large/warped extra dimensions?** Gravity already strong at electroweak scale

# More on the hierarchy problem



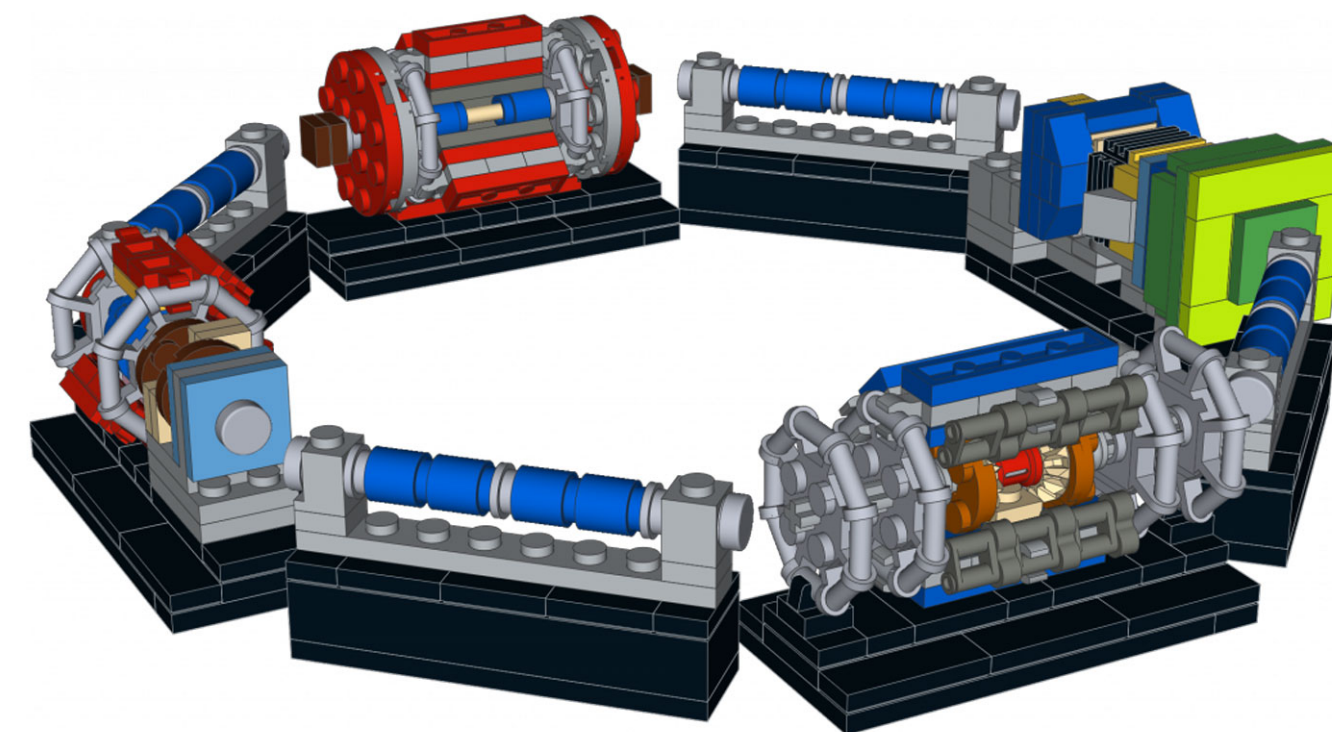
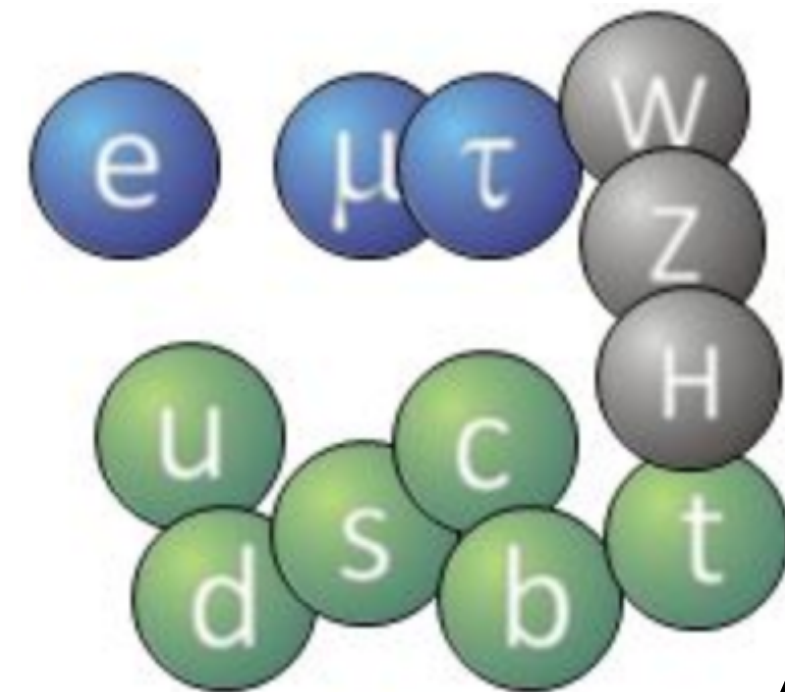
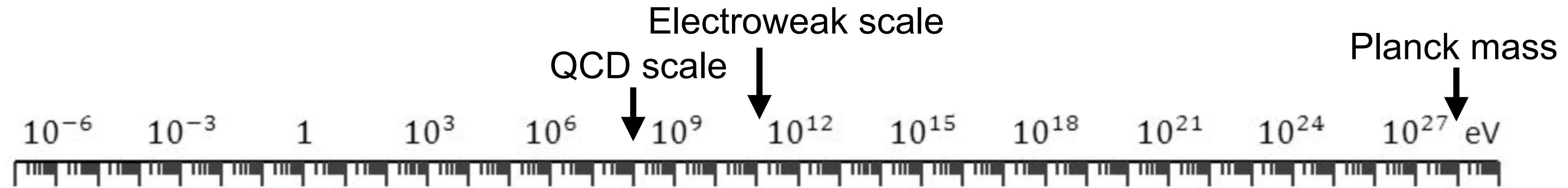
**SUSY?** Explaining the Higgs mass by an additional symmetry

**Composite Higgs?** The Higgs is not elementary

**Large/warped extra dimensions?** Gravity already strong at electroweak scale

**Need to test these experimentally!**

# More on the hierarchy problem

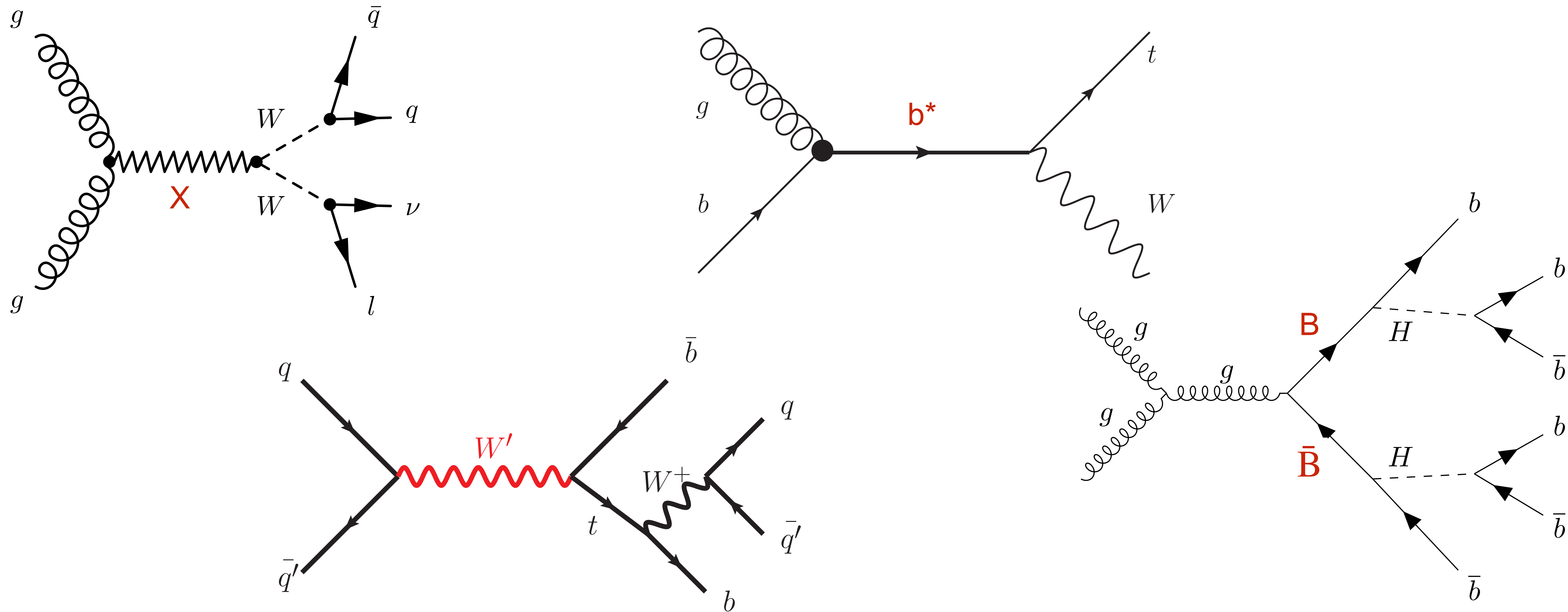


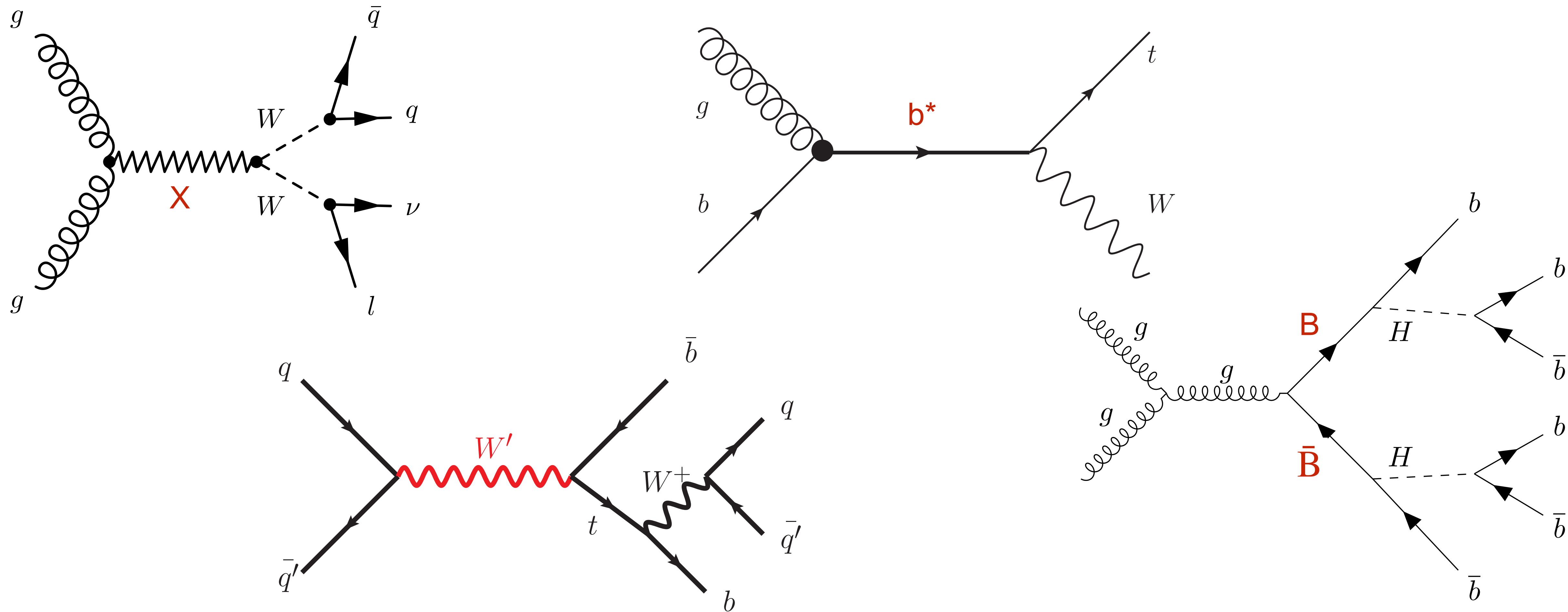
**SUSY?** Explaining the Higgs mass by an additional symmetry

**Composite Higgs?** The Higgs is not elementary

**Large/warped extra dimensions?** Gravity already strong at electroweak scale

**Need to test these experimentally!**

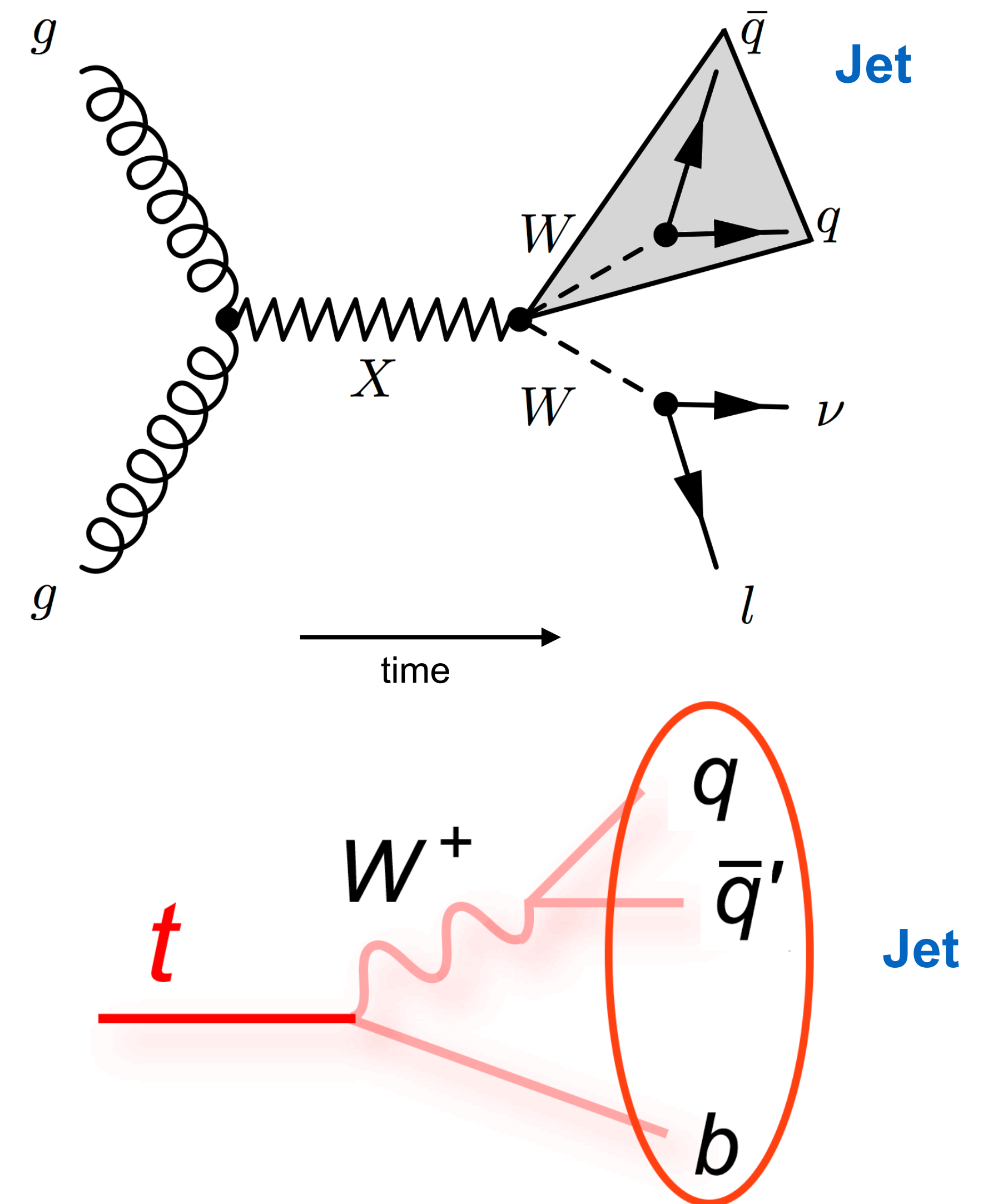




**All the unknown particles  $X$ ,  $W'$ ,  $b^*$ ,  $B$  etc. are very heavy:  $m \geq 1$  TeV**

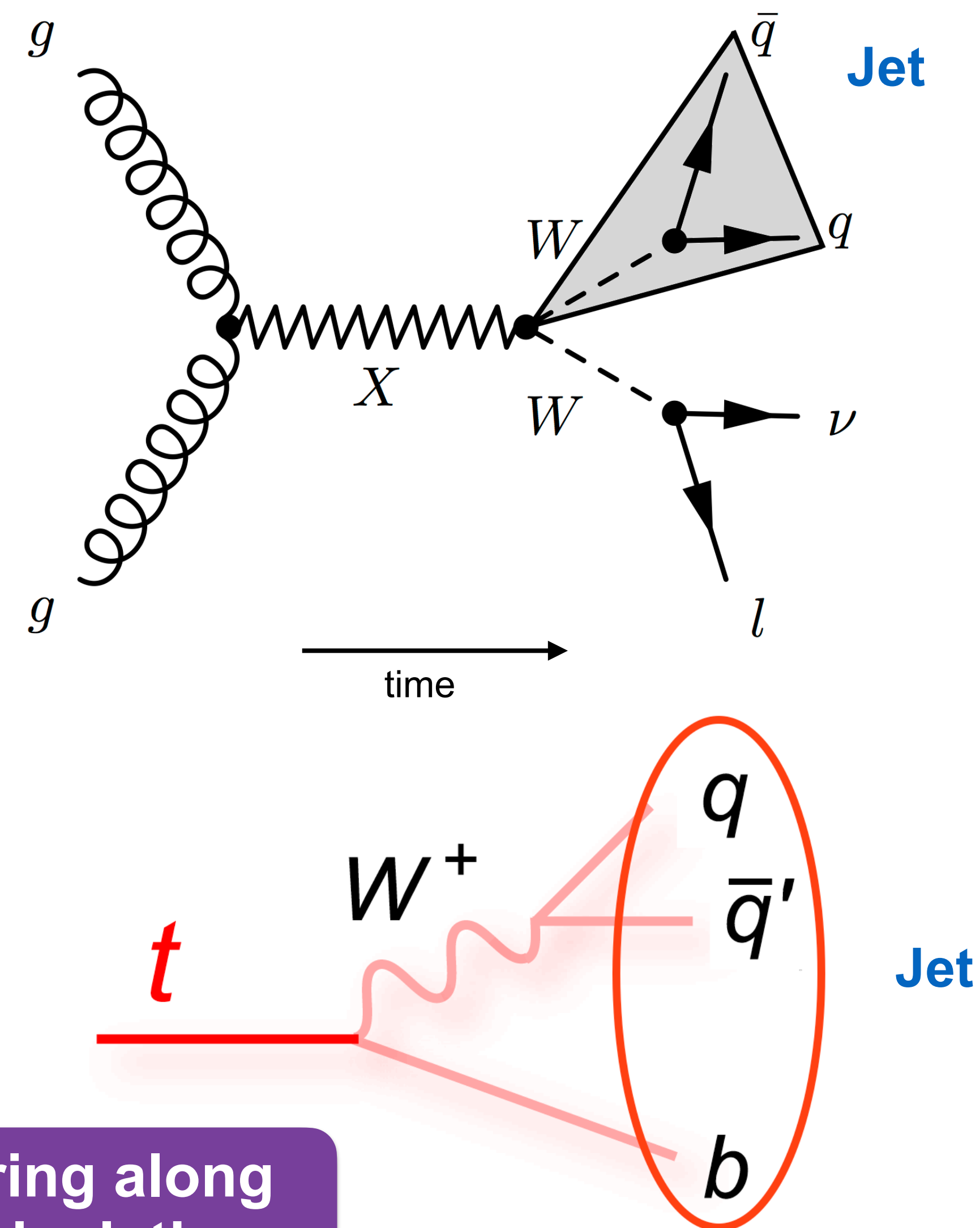
# A heavy resonance decaying

- > In the examples shown, resonance decays to **massive bosons (W, Z, H)** or also **top quarks**
- > These **decay further**, since they are not stable
- > They predominantly decay to a **pair of quarks** (bosons) or **three quarks** (top)
- > This leaves a lot of energy to the quarks due to  $E_{\text{decay}} \approx m_X c^2$  and they will be **close in space**
- > The quarks **hadronize** and form so-called **jets**



# A heavy resonance decaying

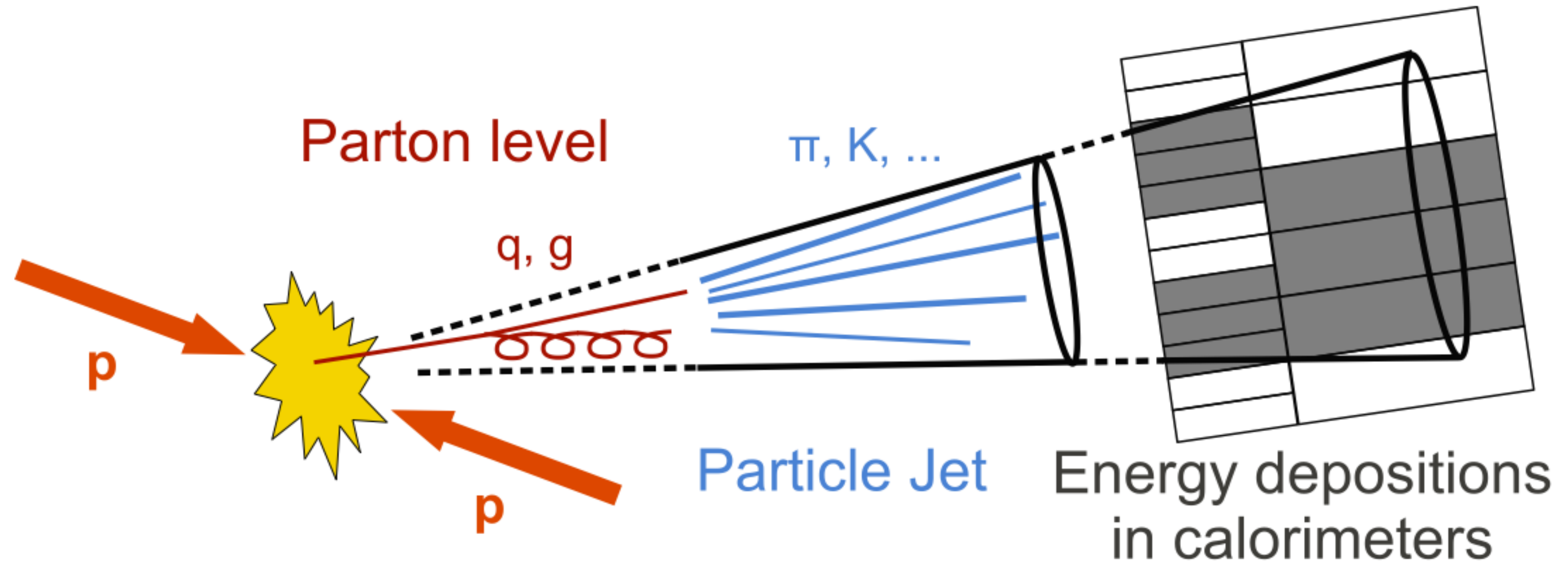
- > In the examples shown, resonance decays to **massive bosons (W, Z, H)** or also **top quarks**
- > These **decay further**, since they are not stable
- > They predominantly decay to a **pair of quarks** (bosons) or **three quarks** (top)
- > This leaves a lot of energy to the quarks due to  $E_{\text{decay}} \approx m_X c^2$  and they will be **close in space**
- > The quarks **hadronize** and form so-called **jets**



Note: leptonic decay channels bring along other challenges such as lepton isolation



# What is a jet?

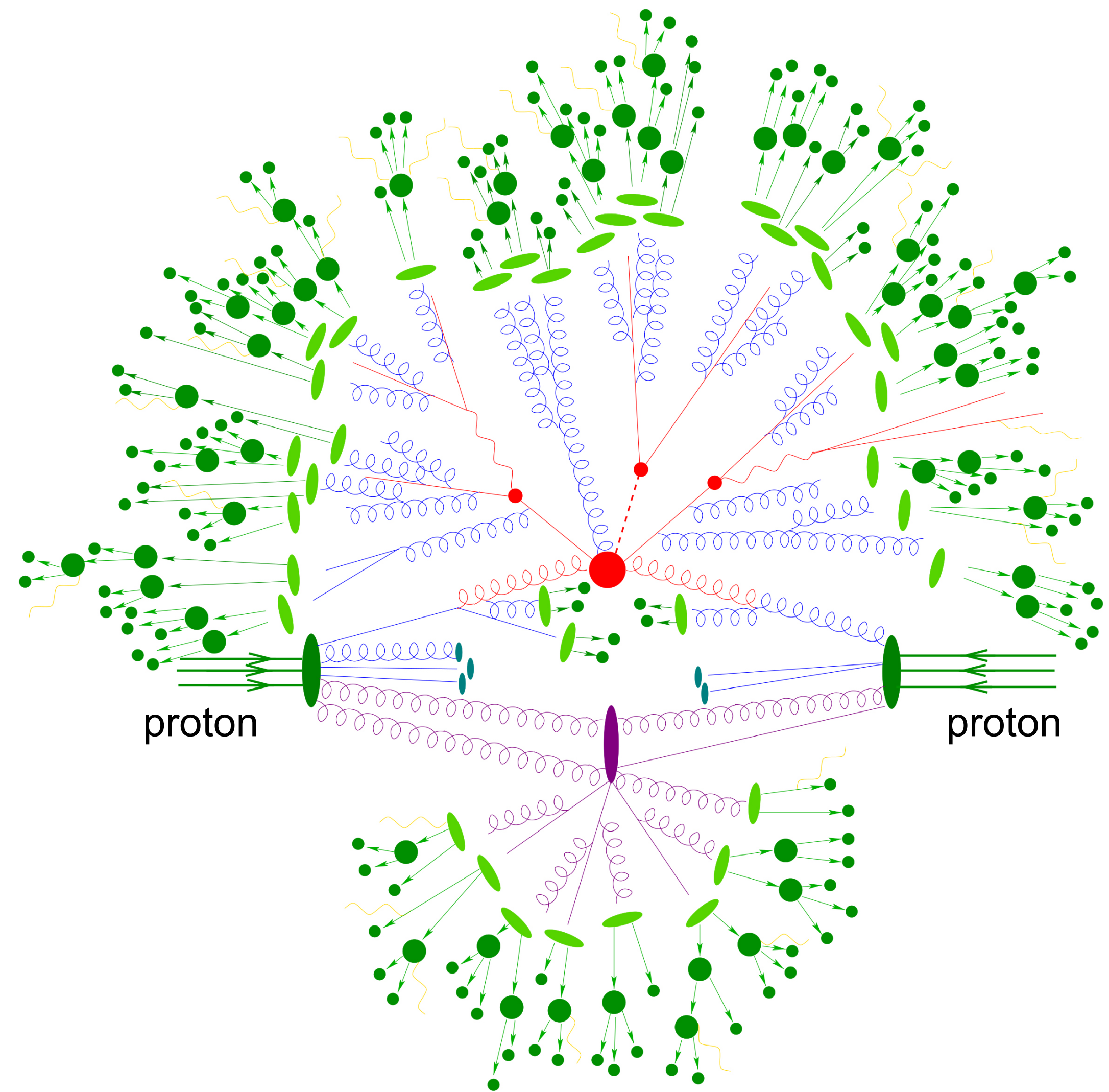


- > **Object** defined by jet **clustering algorithm**
- > Provides **link** between **theory predictions** and **experimental observations**
- > Theory: quarks/partons  $\rightarrow$  *hadronization*  $\rightarrow$  particles ( $p, n, \eta, \lambda, \pi, \dots$ )
- > Experiment: sensor signals  $\rightarrow$  reconstruction  $\rightarrow$  tracker hits, calorimeter entries ( $\rightarrow$  particles (neutral/charged hadrons,  $\gamma, \dots$ ))

# What's going on in a jet

- Jets are very messy objects
- This is due to a phenomenon called **confinement**
- A quark/gluon cannot exist on its own
- It “pulls” in other quarks and gluons to **form hadrons** - this is due to the **strong force**
- Several of the **particles** created this way **decay further** until stable particles have been created

$$(\tau_{\text{had}} = \Lambda_{\text{QCD}}^{-1} = 3 \cdot 10^{-24} \text{ s})$$



Example of a *single* proton-proton collision—now imagine more than 30 on average at the same time

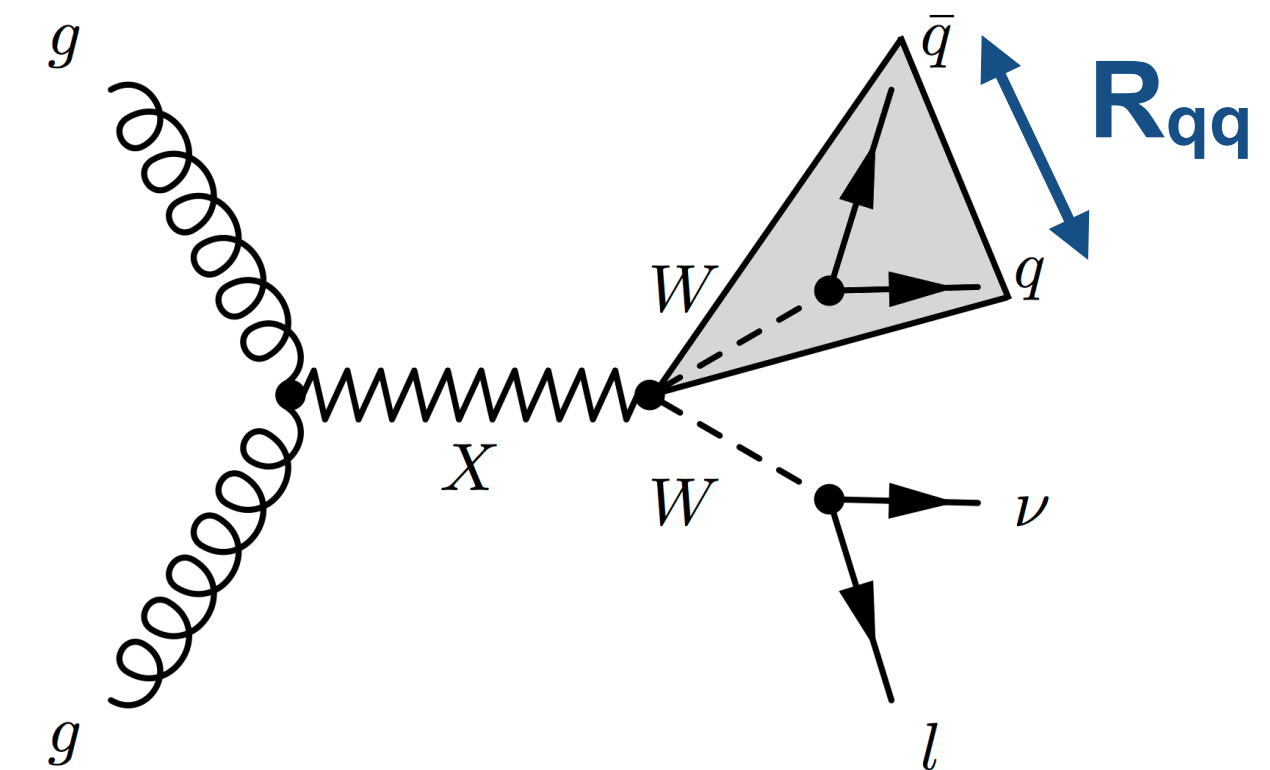
# Fat jet or not

- > “Standard” jets in CMS: use **anti- $k_T$  algorithm** with  $R = 0.4$  (“AK4 jets”)
- > Approximation: all particles within  $\Delta R := \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} = c$  will be **reconstructed as a single jet** with cut-off parameter  $R = c$

> “Standard” jets in CMS: use **anti- $k_T$  algorithm** with  $R = 0.4$  (“AK4 jets”)

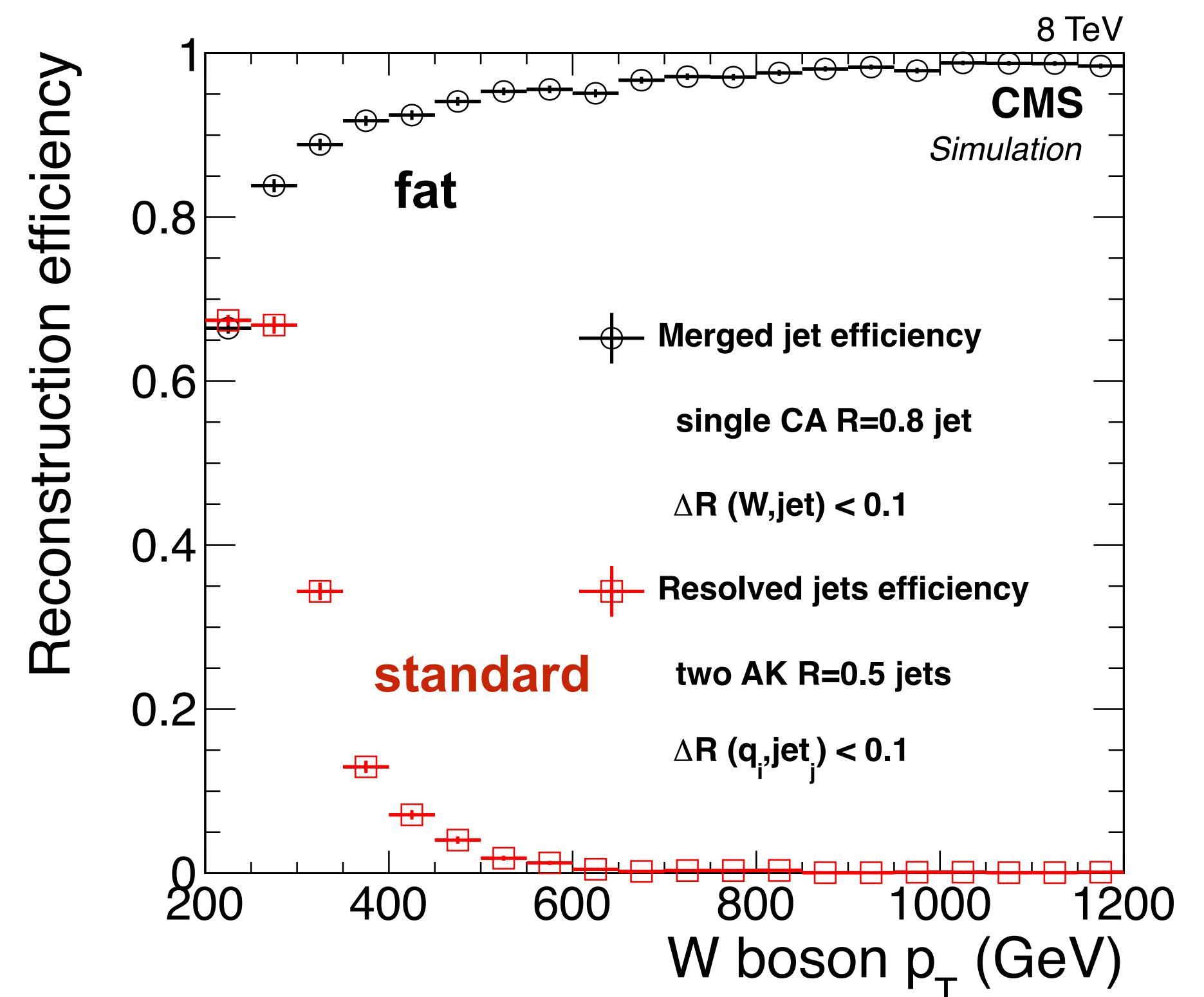
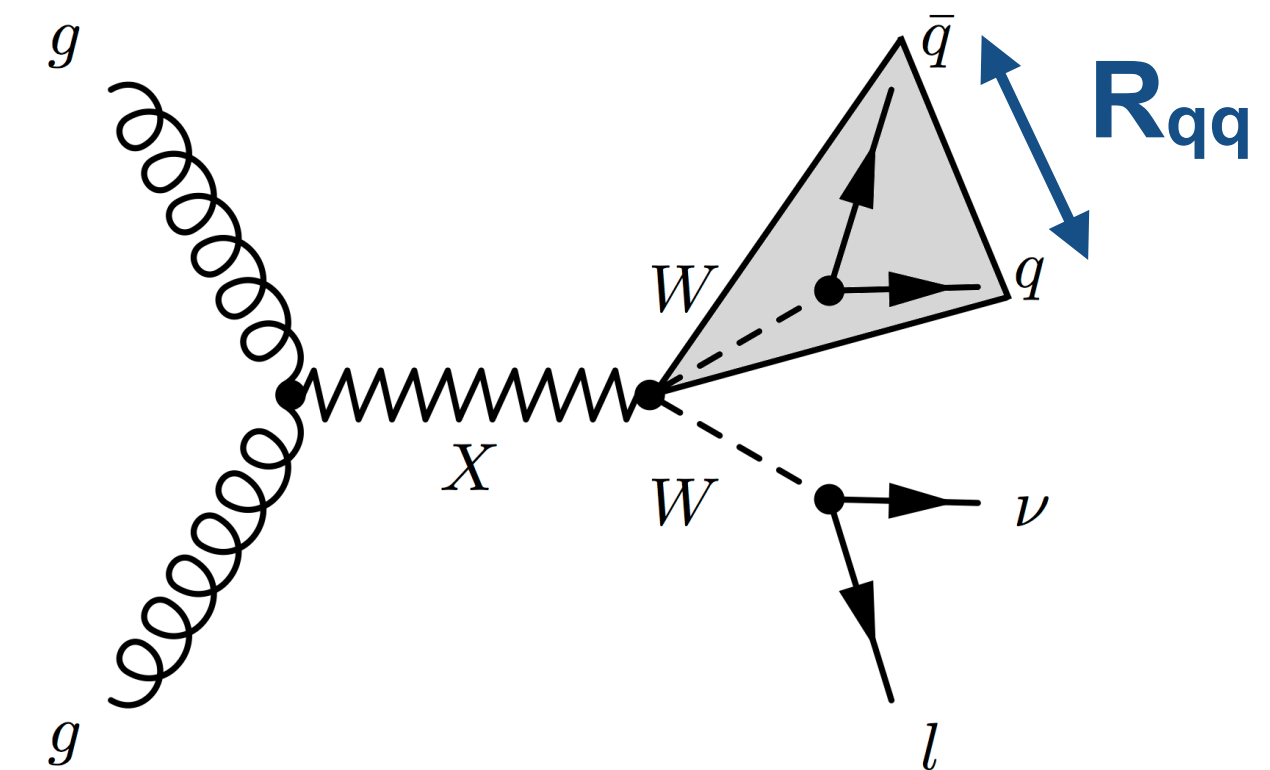
> Approximation: all particles within  $\Delta R := \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} = c$  will be **reconstructed as a single jet** with cut-off parameter  $R = c$

- > For a  $W$ -boson decay:  $R_{qq} \approx 2 \frac{m_W}{p_T^W}$
- Example: resonance of mass 1 TeV bosons ( $m = 100$  GeV) from the decay will on average have  $p_T \sim 0.4$  TeV  $\rightarrow R_{qq} \approx 0.5$
  - An AK4 jet could miss parts of the decay

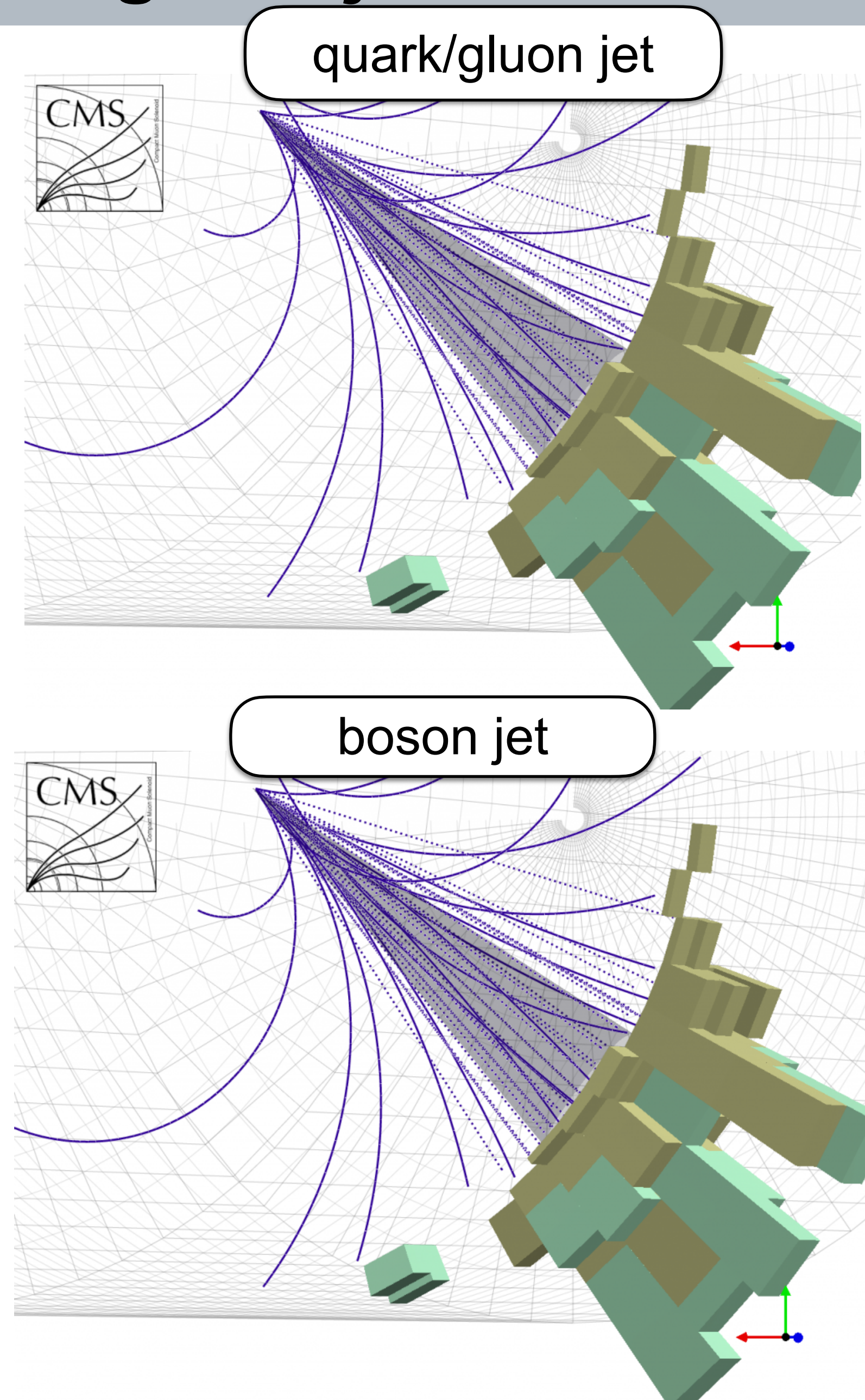


# Fat jet or not

- > “Standard” jets in CMS: use **anti- $k_T$  algorithm** with  $R = 0.4$  (“AK4 jets”)
- > Approximation: all particles within  $\Delta R := \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} = c$  will be **reconstructed as a single jet** with cut-off parameter  $R = c$
- > For a W-boson decay:  $R_{qq} \approx 2 \frac{m_W}{p_T^W}$ 
  - Example: resonance of mass 1 TeV bosons ( $m = 100$  GeV) from the decay will on average have  $p_T \sim 0.4$  TeV  $\rightarrow R_{qq} \approx 0.5$
  - An AK4 jet could miss parts of the decay
- > Use larger jet “radius” to **contain full decay** (usually  $R = 0.8$ ,  $\rightarrow$  “AK8”)

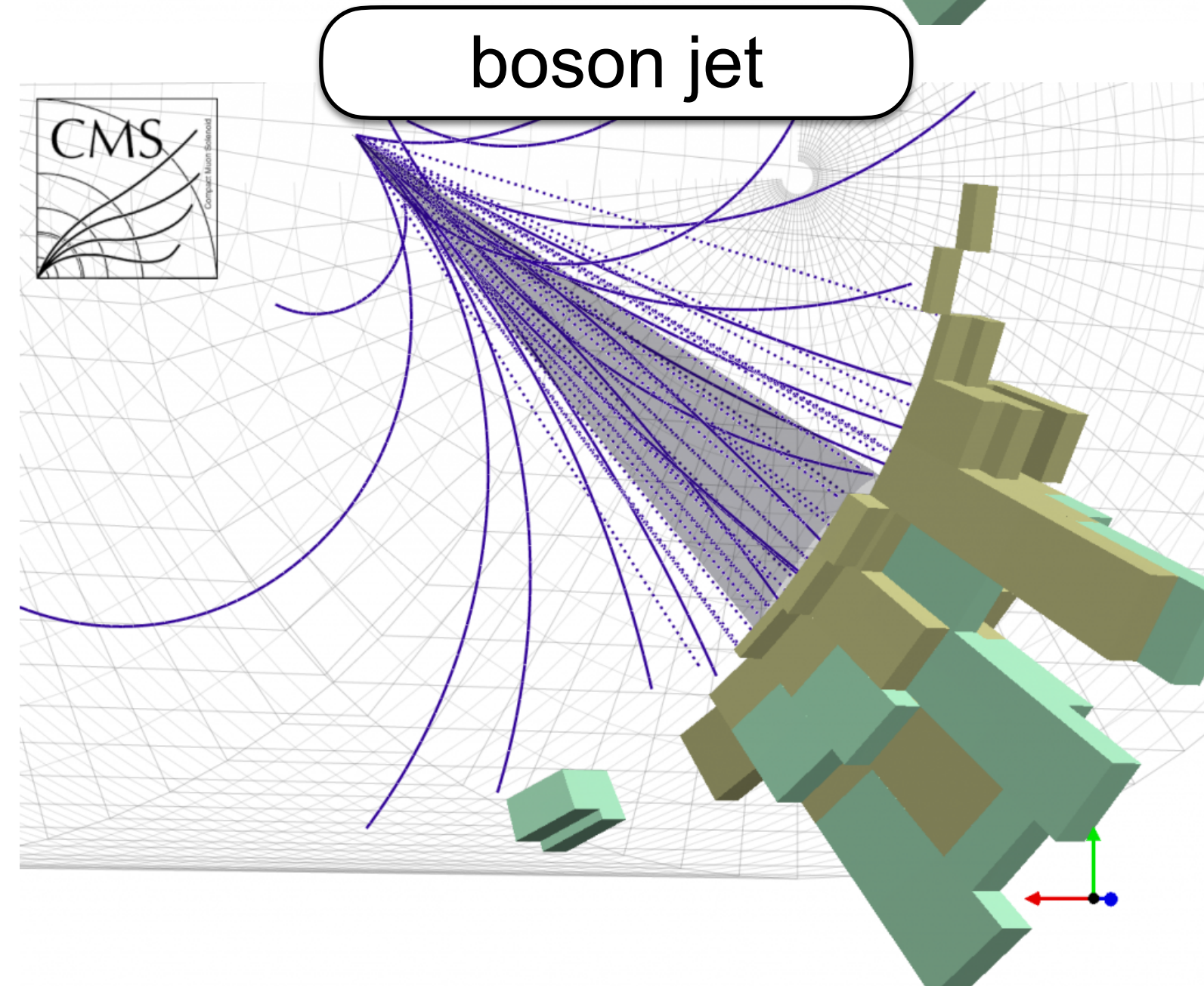
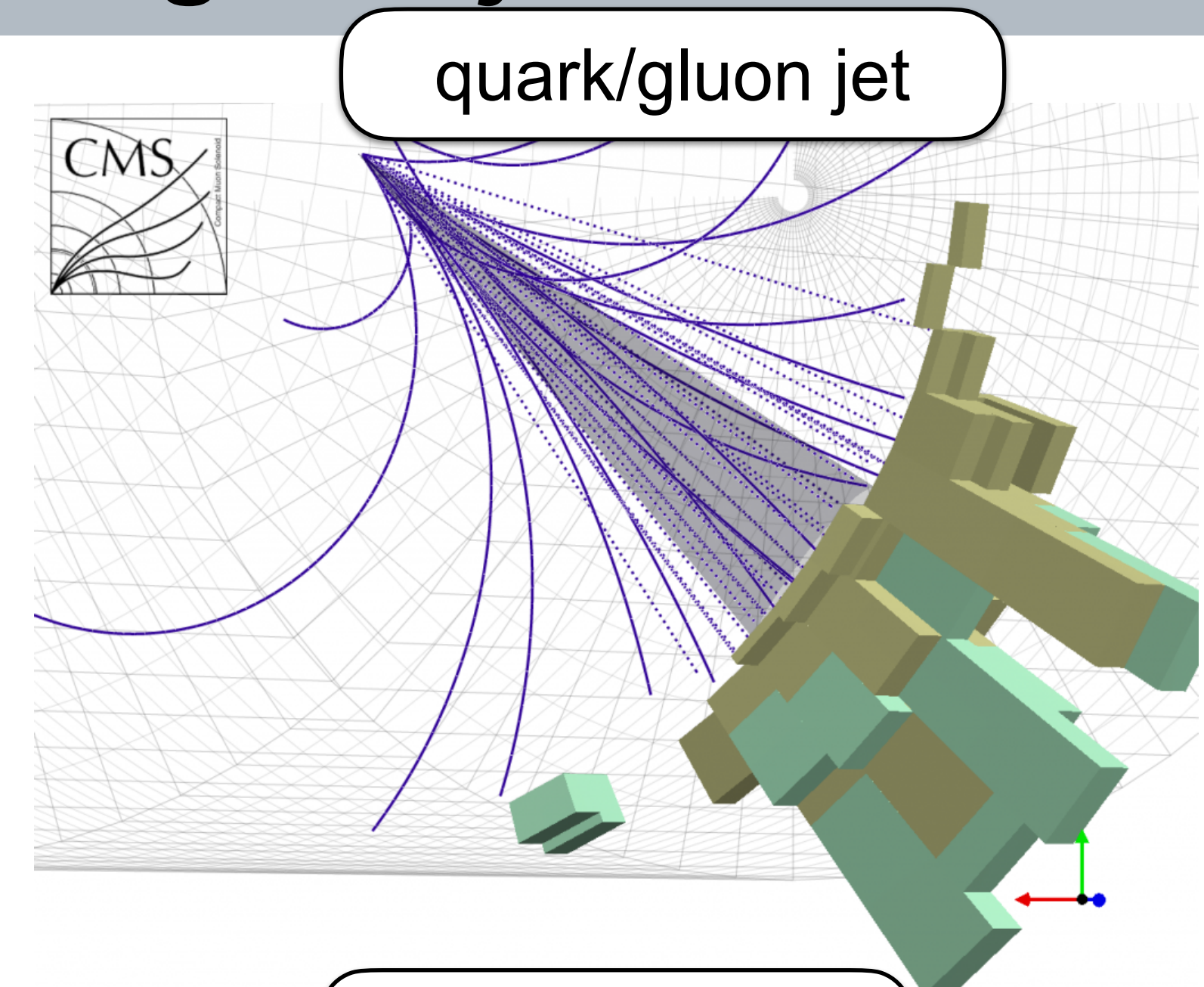


# Boson/top quark jets vs. quark/gluon jets



# Boson/top quark jets vs. quark/gluon jets

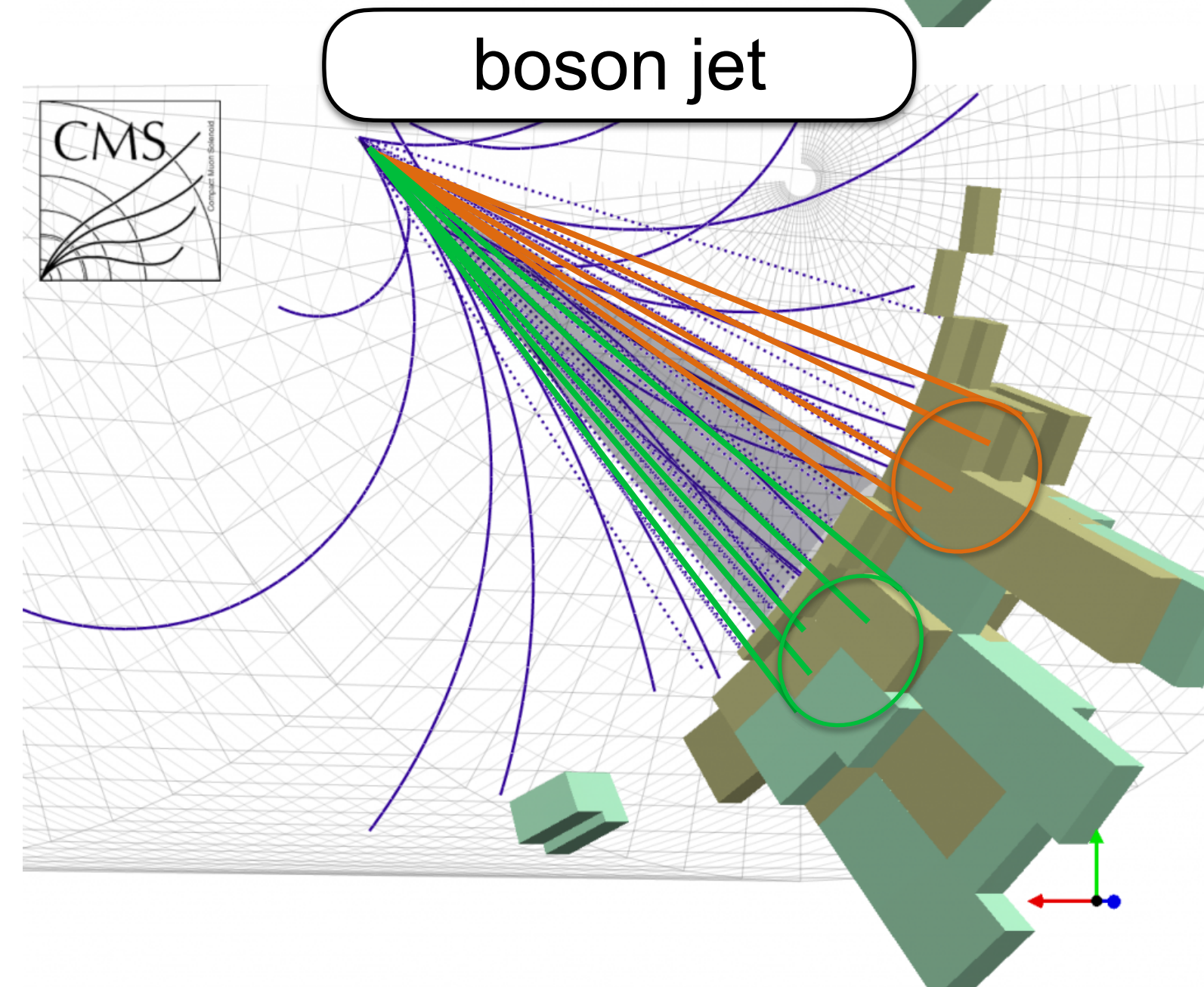
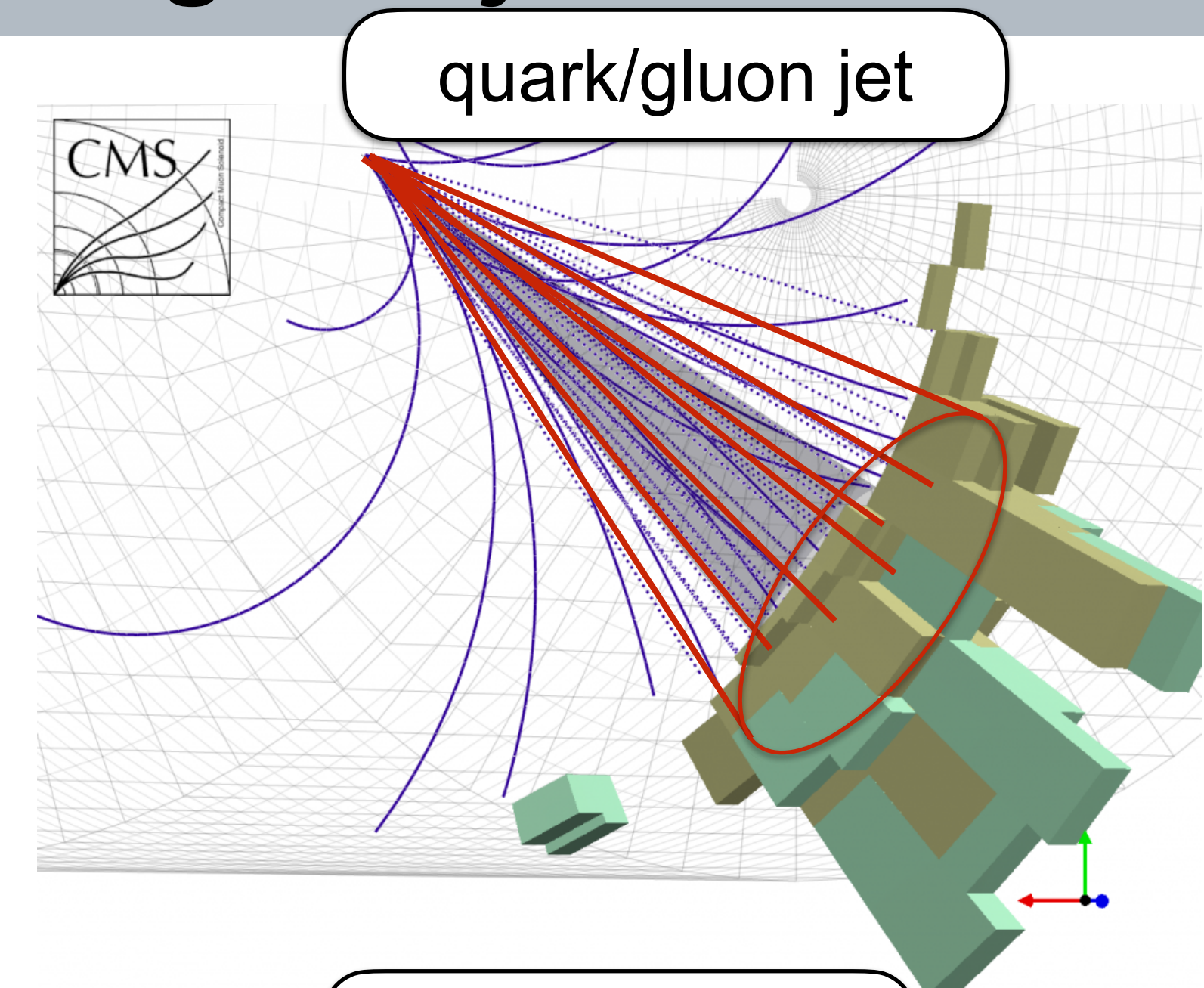
- > At first look, it's the same as any other jet
- > However, if you **look more closely**, you can find differences





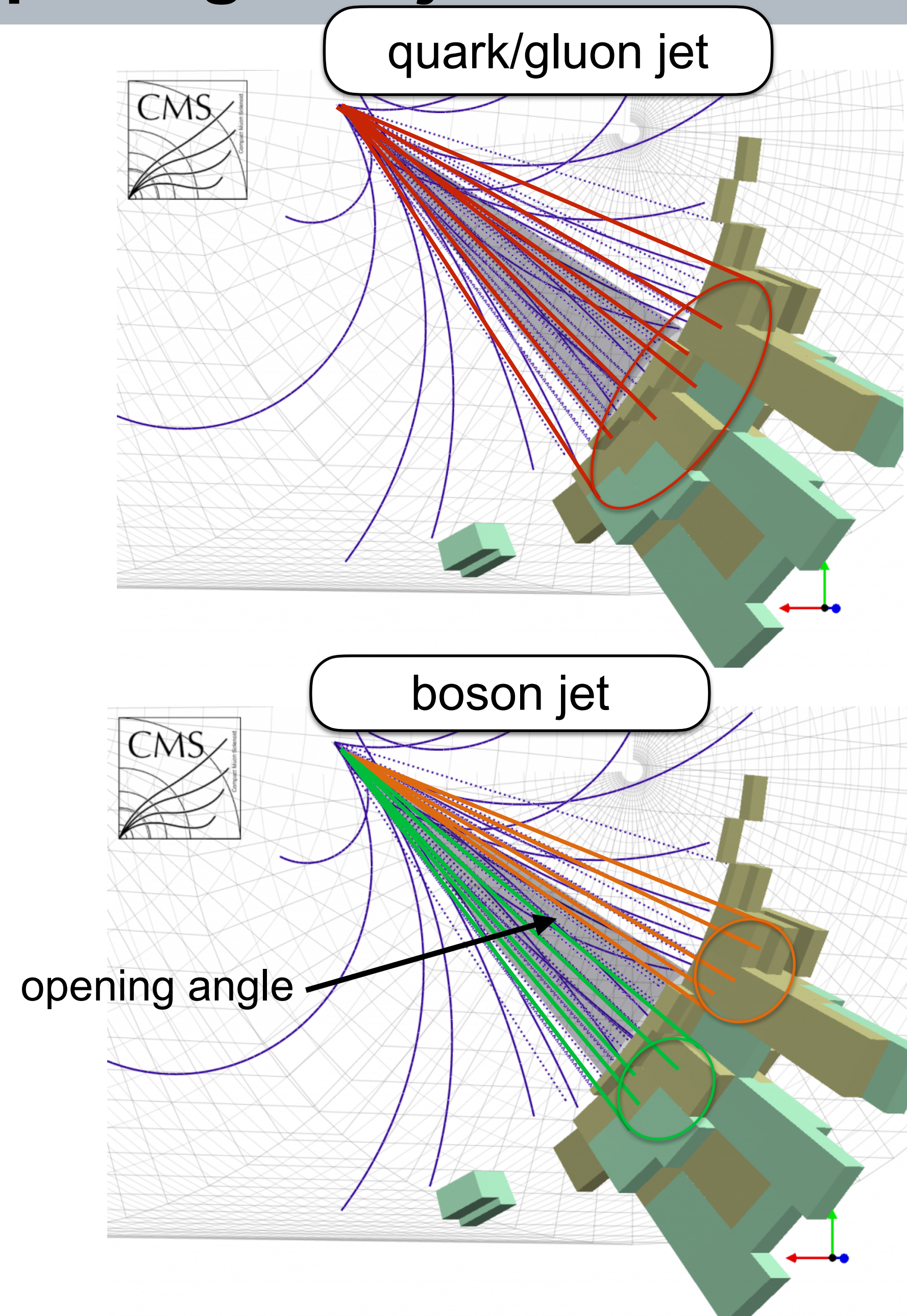
# Boson/top quark jets vs. quark/gluon jets

- > At first look, it's the same as any other jet
- > However, if you **look more closely**, you can find differences
- > You will find that the **energy deposits** inside the jet are centred around **two cores/axes** instead of just one



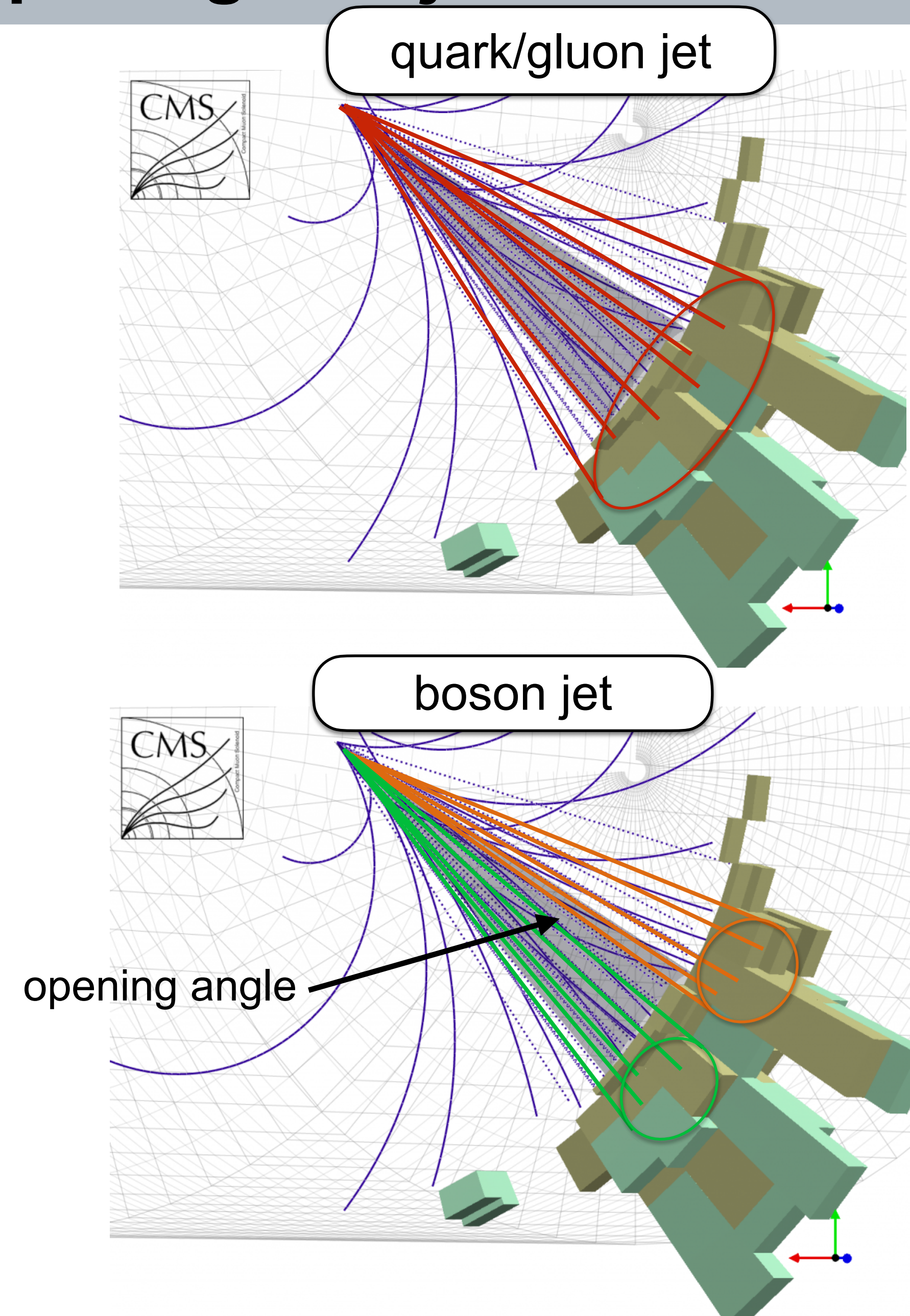
# Boson/top quark jets vs. quark/gluon jets

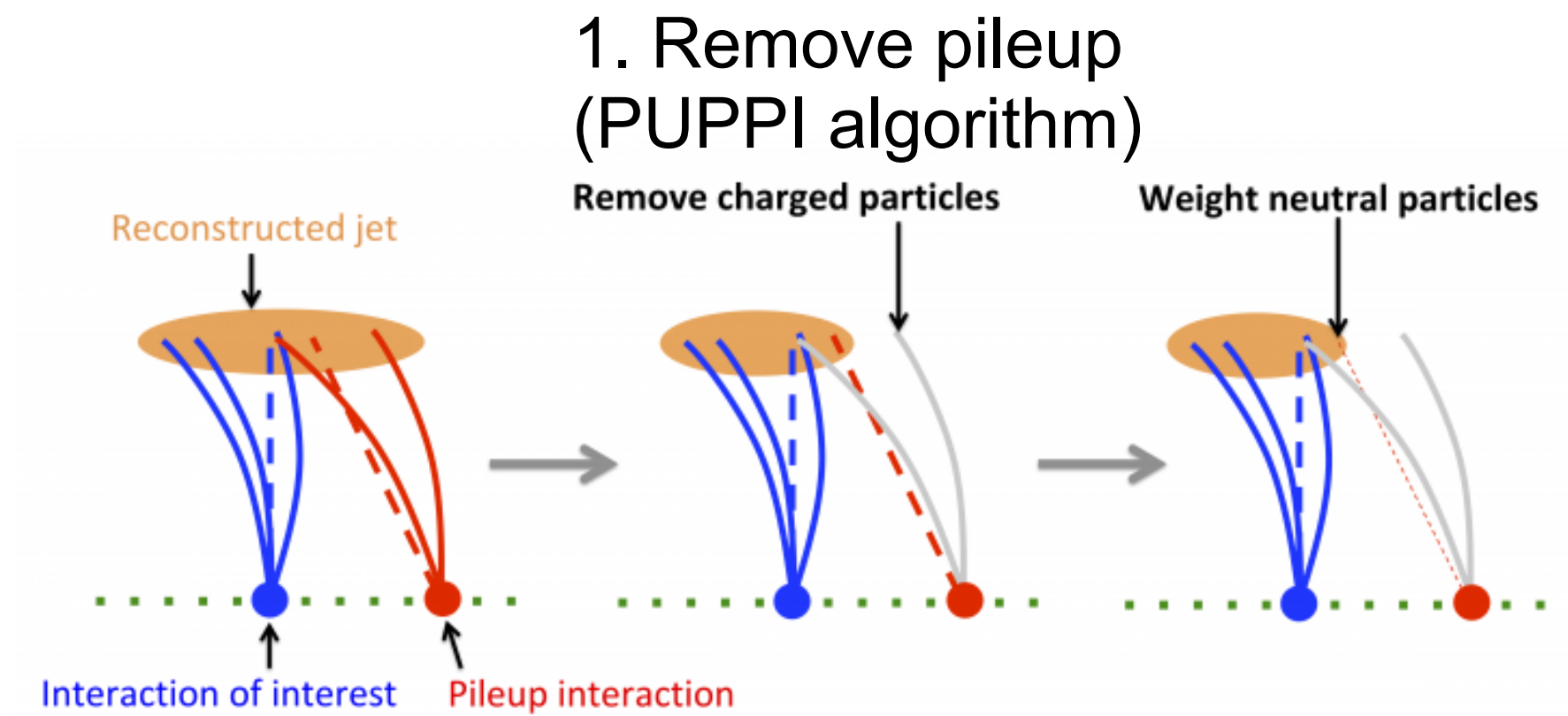
- > At first look, it's the same as any other jet
- > However, if you **look more closely**, you can find differences
- > You will find that the **energy deposits** inside the jet are centred around **two cores/axes** instead of just one
- > The **opening angle** between two energy deposits relates to the **mass of the original particle**



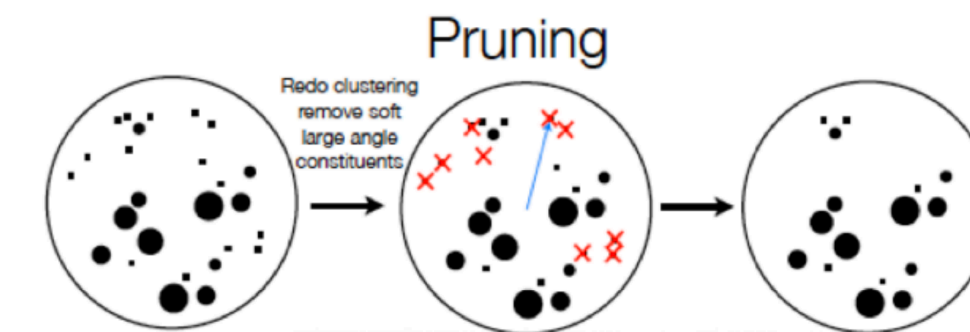
# Boson/top quark jets vs. quark/gluon jets

- > At first look, it's the same as any other jet
- > However, if you **look more closely**, you can find differences
- > You will find that the **energy deposits** inside the jet are centred around **two cores/axes** instead of just one
- > The **opening angle** between two energy deposits relates to the **mass of the original particle**
- > However, to be able to see that, we need to **clean up the jet**

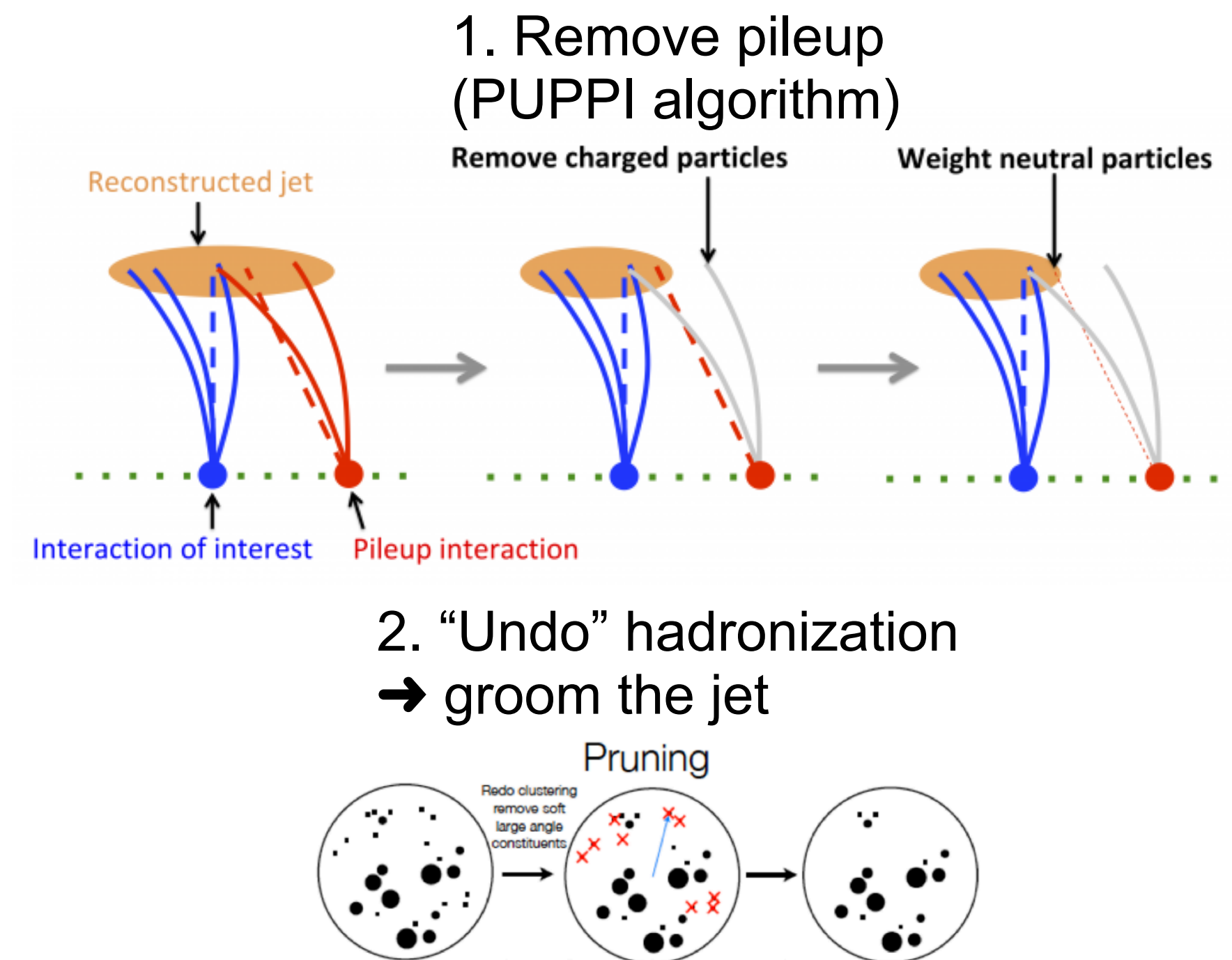




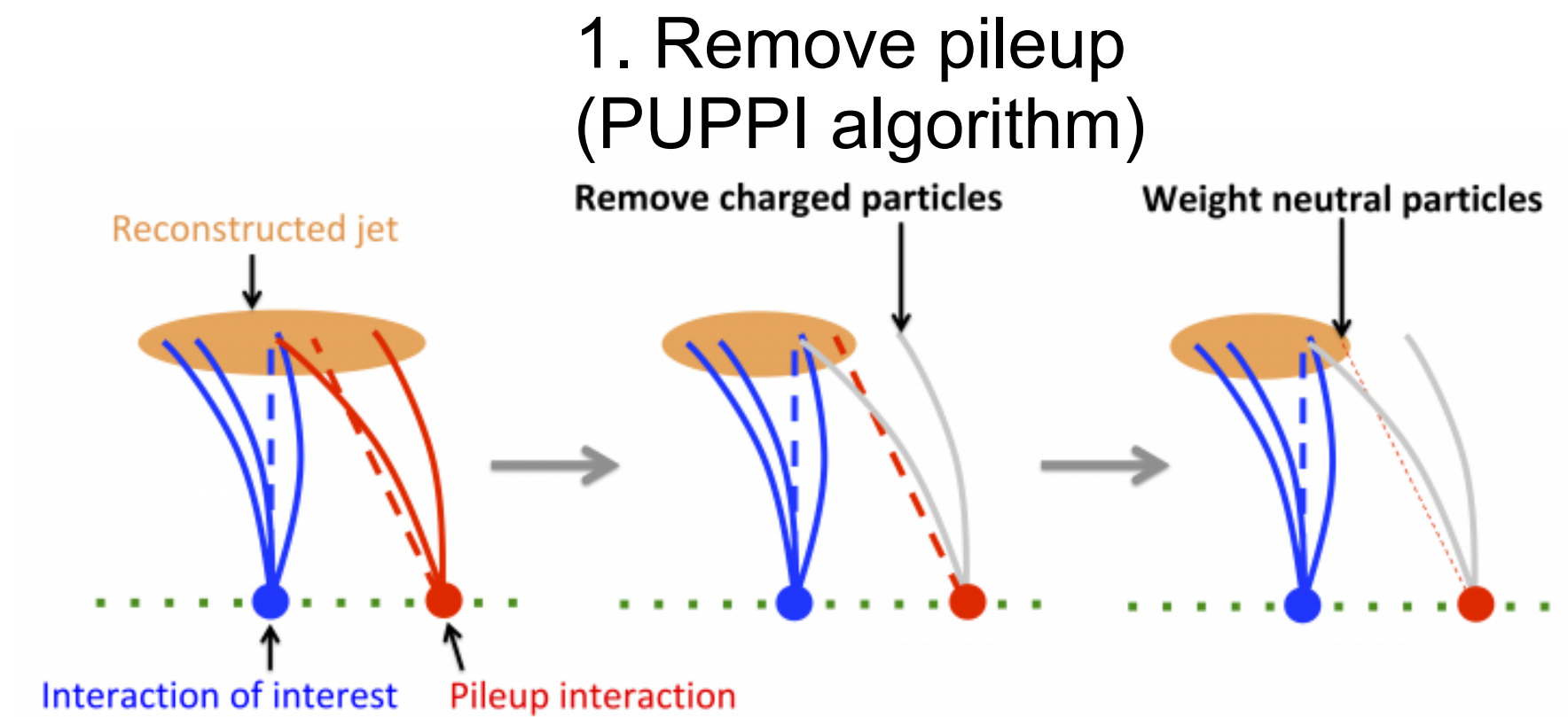
2. "Undo" hadronization  
 → groom the jet



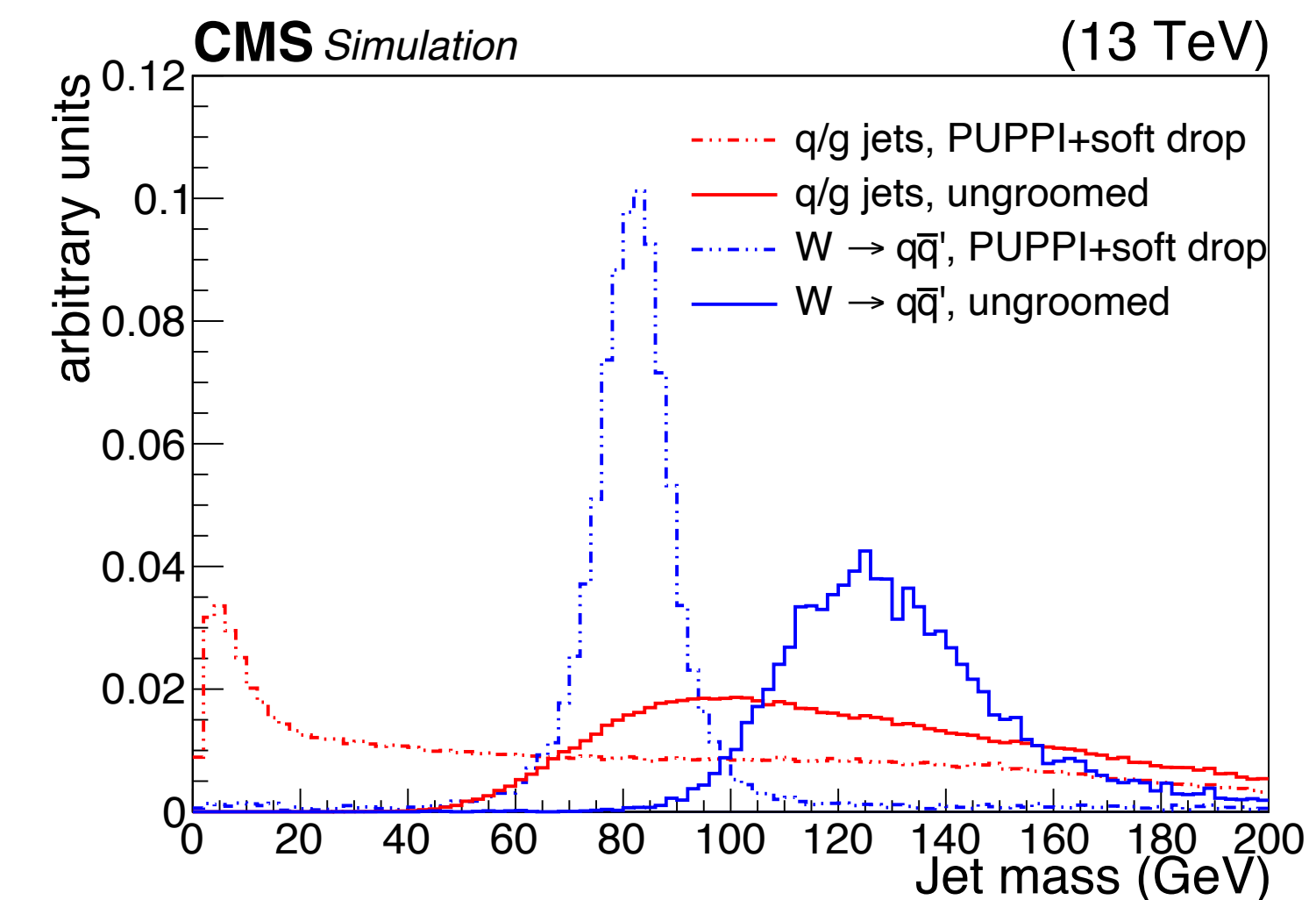
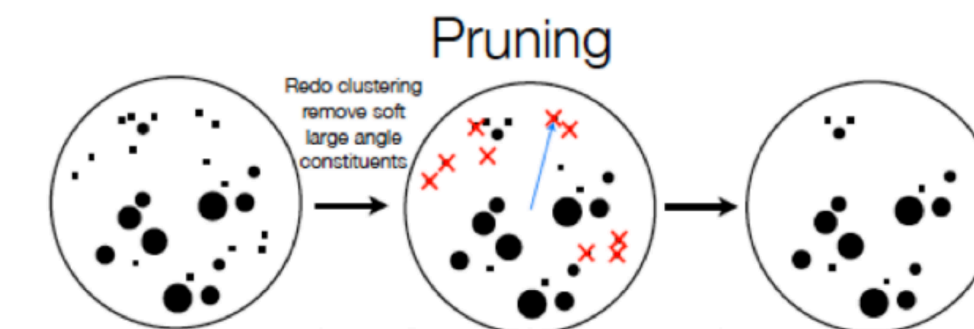
- > When looking at our **“massive” jets**, we are mostly interested in the **initial quarks**
- > Attempt to **throw away low energy and large angle radiation**  
 → **“undo” hadronization**
- > This process is called **grooming**
  - There are a few different algorithms to do that



- > When looking at our **“massive” jets**, we are mostly interested in the **initial quarks**
- > Attempt to **throw away low energy and large angle radiation**  
→ **“undo” hadronization**
- > This process is called **grooming**
  - There are a few different algorithms to do that
- > In CMS, the modified mass-drop tagger **“soft drop”** is commonly used

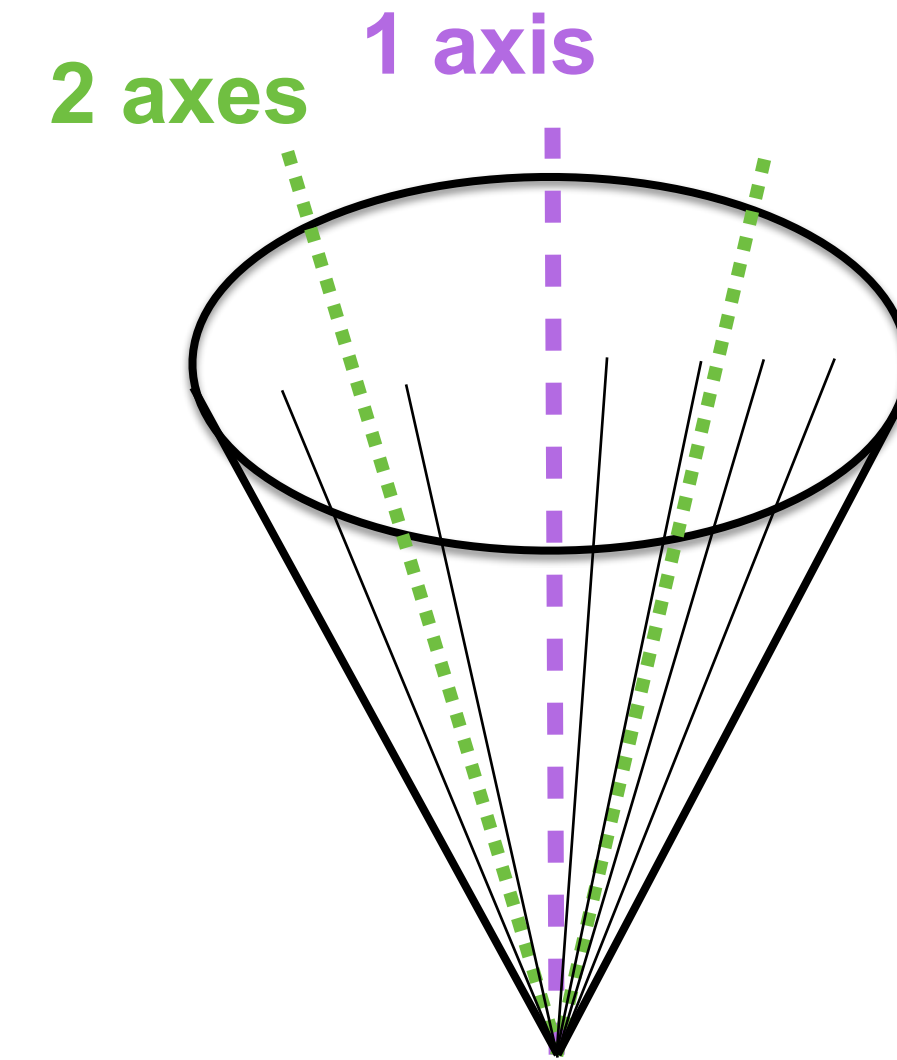


2. “Undo” hadronization  
→ groom the jet



# There is more than just mass

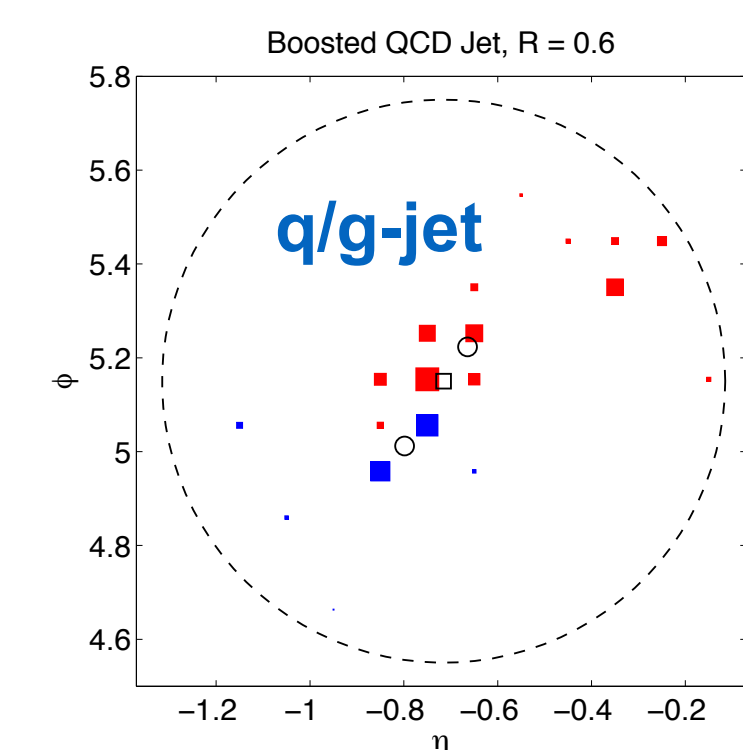
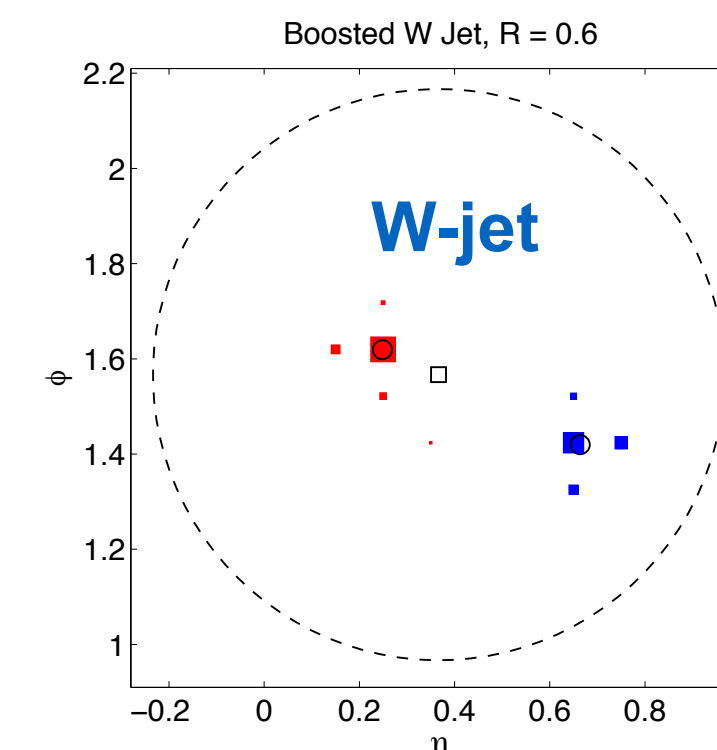
- > Remember that I told you something about an opening angle between the decay products?
- > We can also measure the **energy flow** inside a jet
- > Estimate to what extent it is aligned along 2 or 3 momentum axes (or just 1)
- > Again, there are a range of different algorithms
  - N-subjettiness ( $\tau_N$ ), energy correlation functions, machine-learned variables, ...
- > For  $\tau_N$  (by now somewhat outdated):
  - ratio  $\tau_2/\tau_1 \rightarrow$  W/Z boson tagging
  - ratio  $\tau_3/\tau_2 \rightarrow$  top quark tagging



Calculate for a given hypotheses of N subjects:

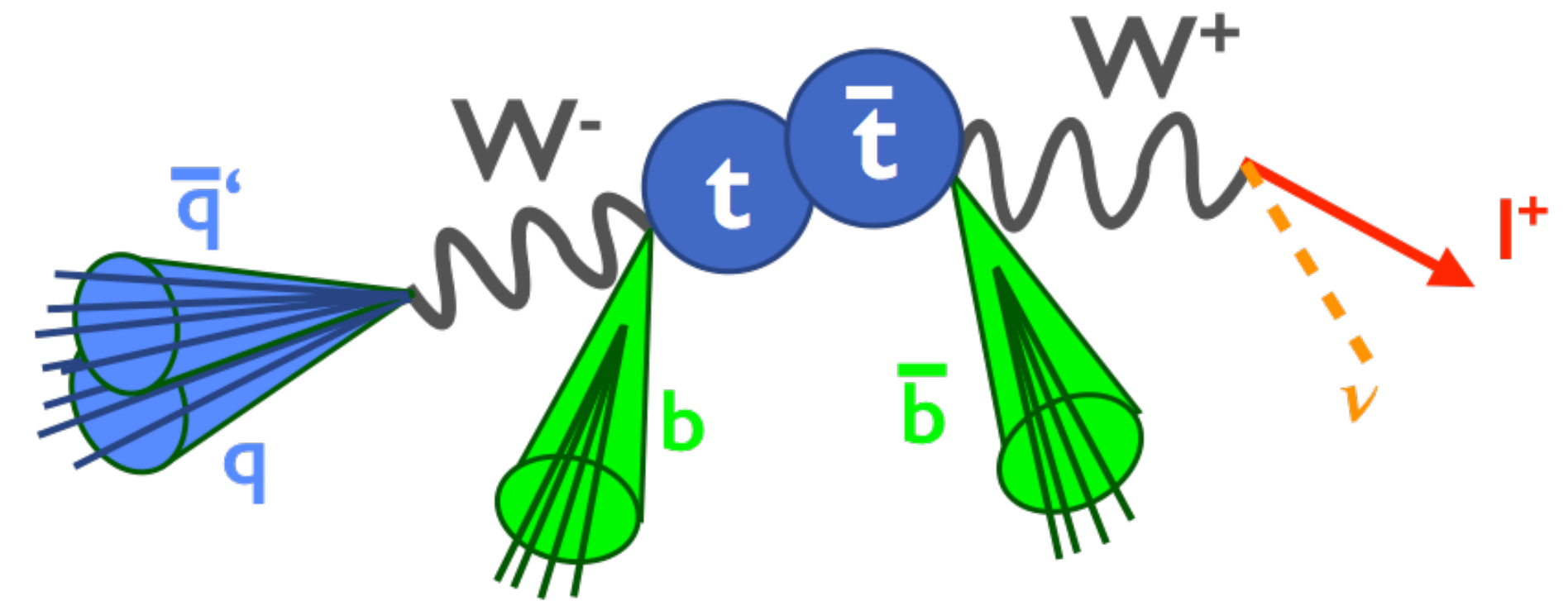
$$\tau_N = \frac{1}{d_0} \sum_k p_{T,k} \min(\Delta R_{1,k}, \Delta R_{2,k}, \dots, \Delta R_{N,k})$$

normalization    sum over particles    minimise distance to candidate subjts

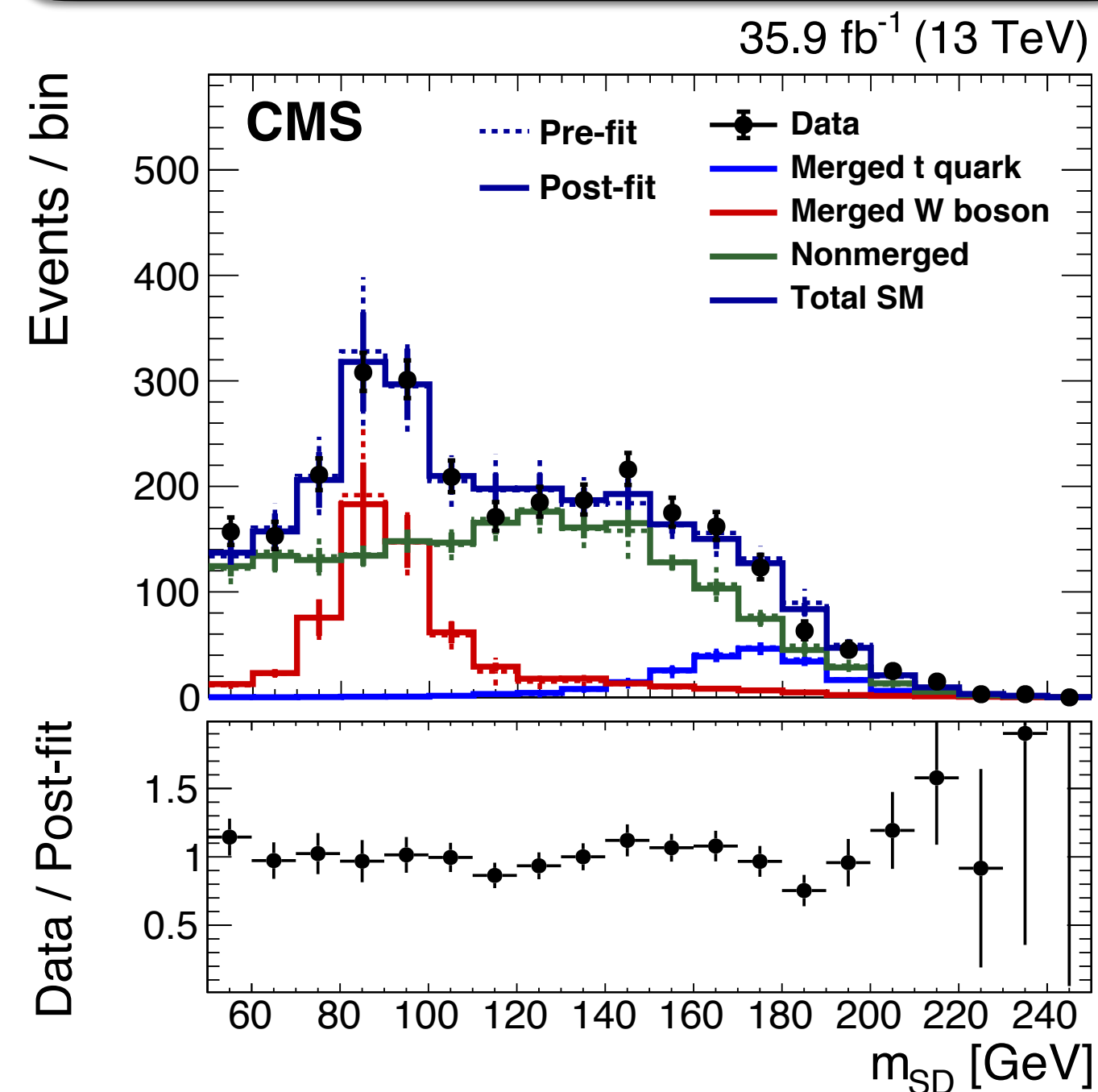


# Confirming that this works

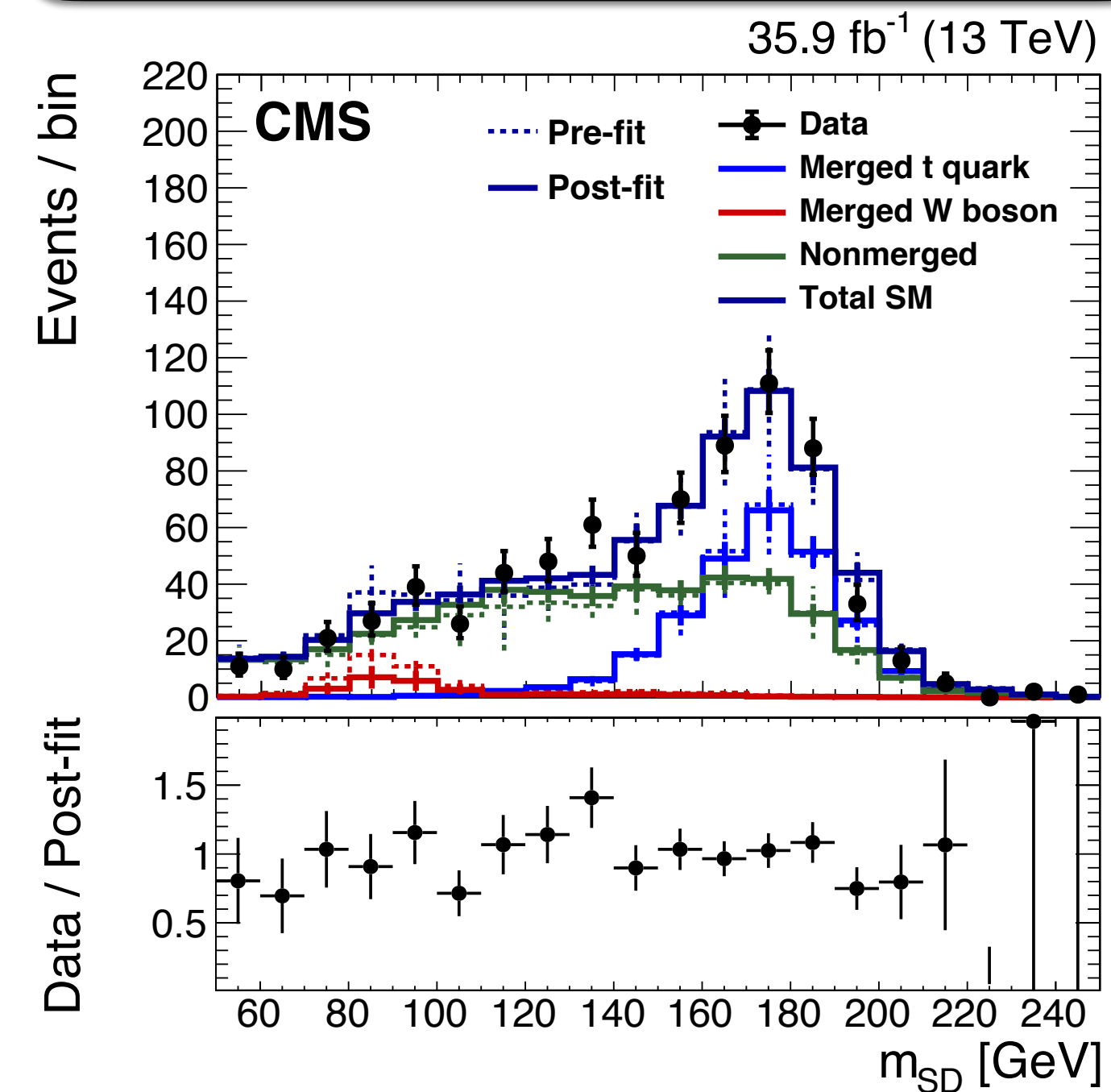
- Rather **complicated variables**, difficult to model → need to validate in data
- Clean sample of W-boson jets: **top-antitop quark pairs** used for calibration (W-boson jet  $p_T \sim 200$  GeV)



Pass W-boson discriminant



Pass top-quark discriminant







# Using jet substructure in resonance searches

Two hot-off-the-press examples





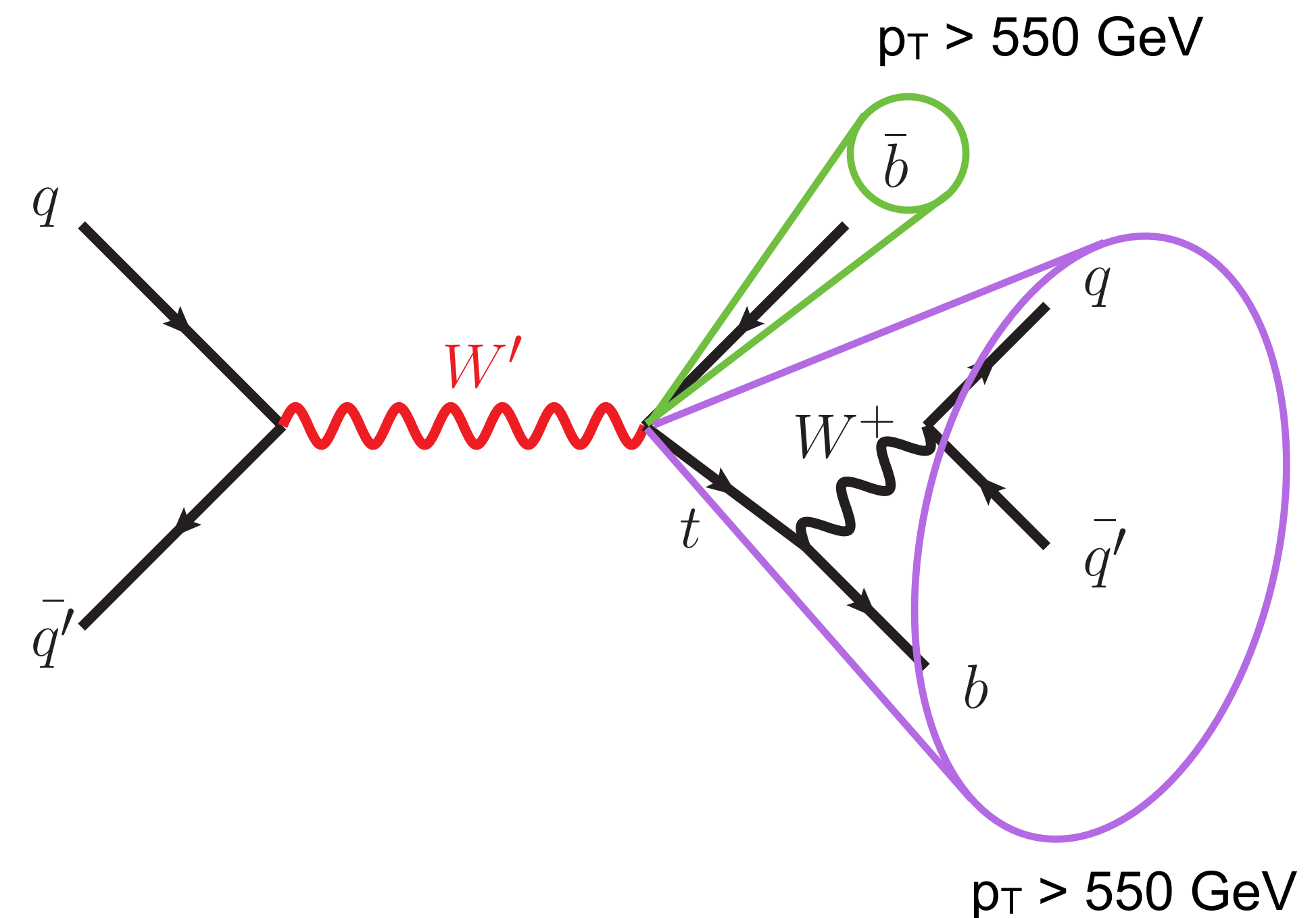
## > Topology:

- 1 high- $p_T$  bottom-quark jet
- 1 high- $p_T$  top-quark jet
- both are identified using dedicated deep neural network algorithms (DeepJet and DeepAK8)

## > Selection:

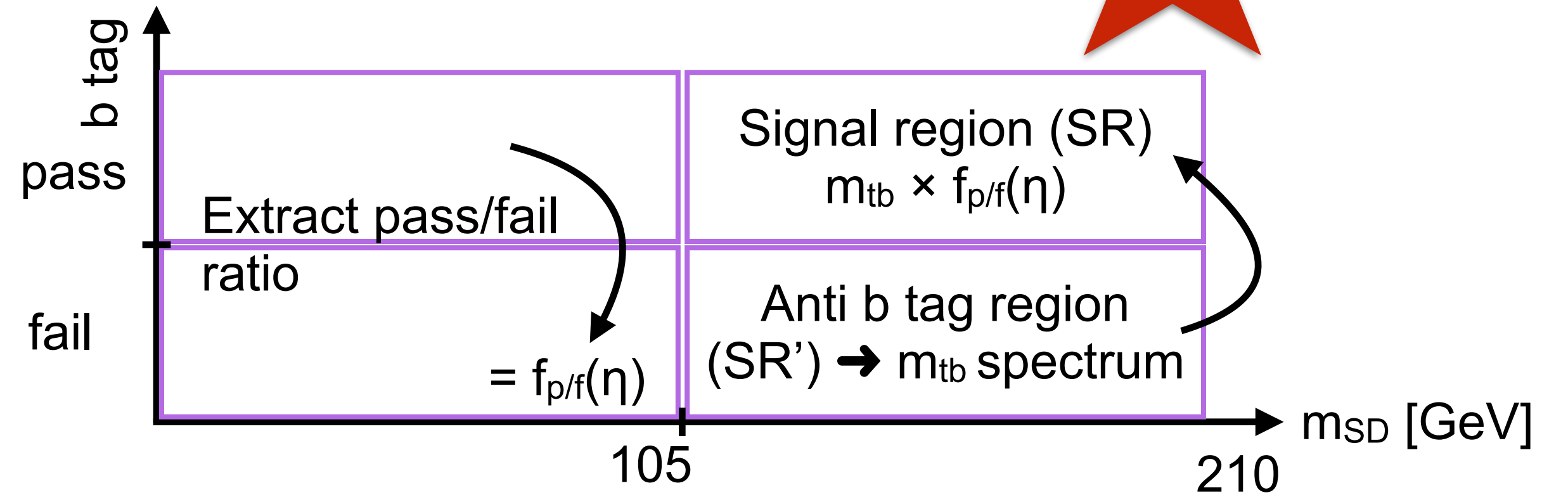
- One AK4 jet,  $p_T > 550$  GeV, b tagged
- One AK8 jet,  $p_T > 550$  GeV, top tagged,  $105 < m_{SD} < 210$  GeV
- Both well-separated from each other (back-to-back)

## > Define control and validation regions by inverting b/top tag requirements and using mass sidebands

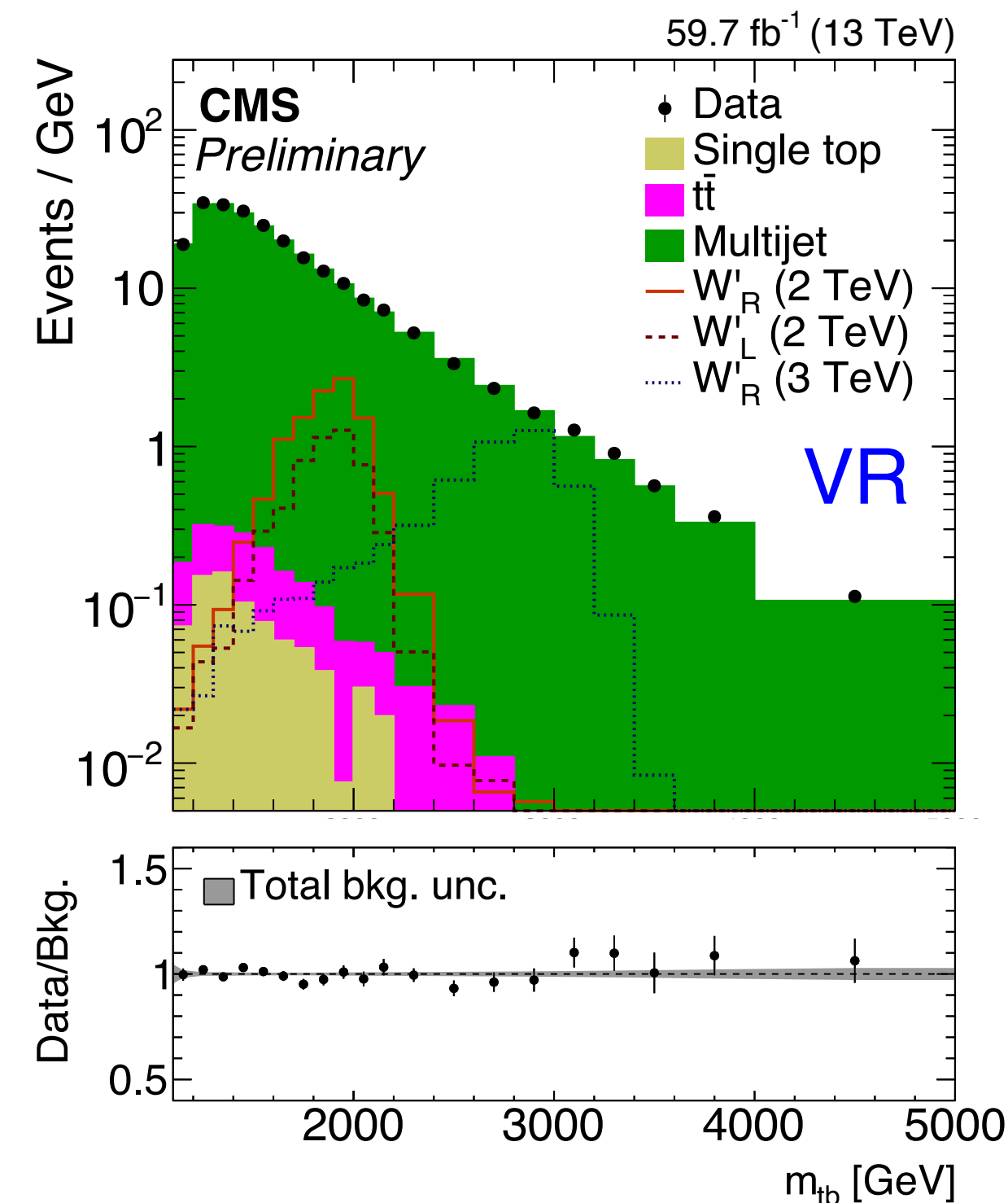




- > Final discriminant: invariant  $tb$  mass ( $m_{tb}$ )
- > Background estimation of dominant multijet production:
  - In mass sideband ( $m_{SD} < 105$  GeV), extract **b tag pass/fail ratio** as function of  $\eta$  of the AK4 jet
  - In signal mass window, invert b tag requirement (SR') and multiply  $m_{tb}$  spectrum by pass/fail ratio to **predict multijet in signal region** (SR)
  - Validate procedure in top tag fail region (VR)

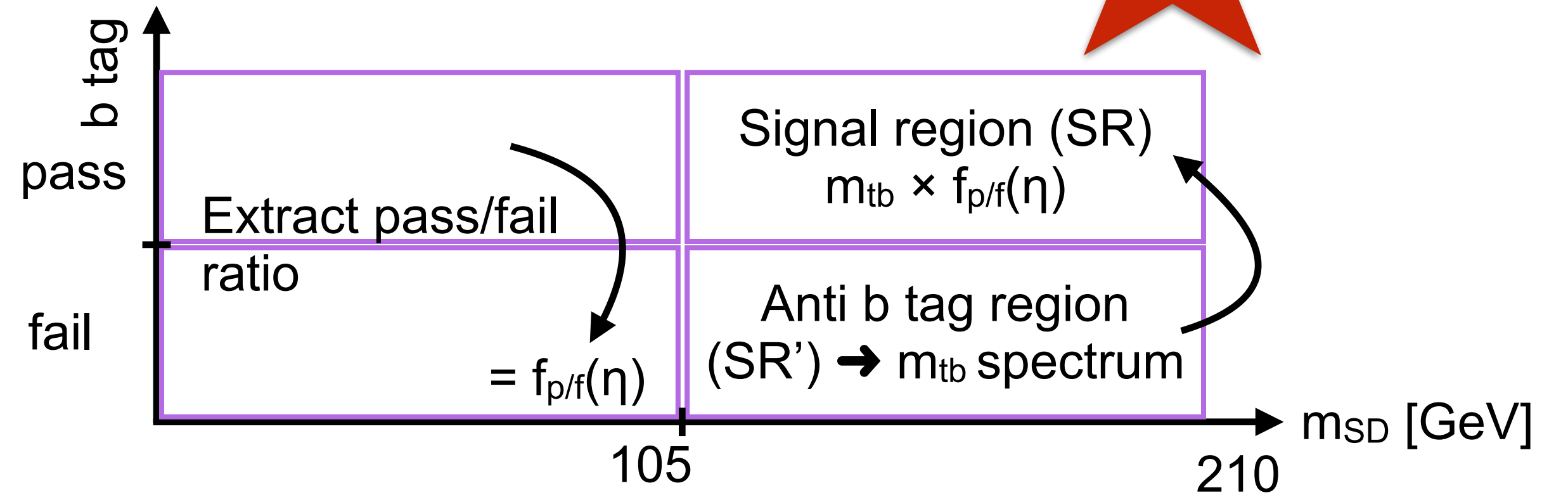


Multijet validation region



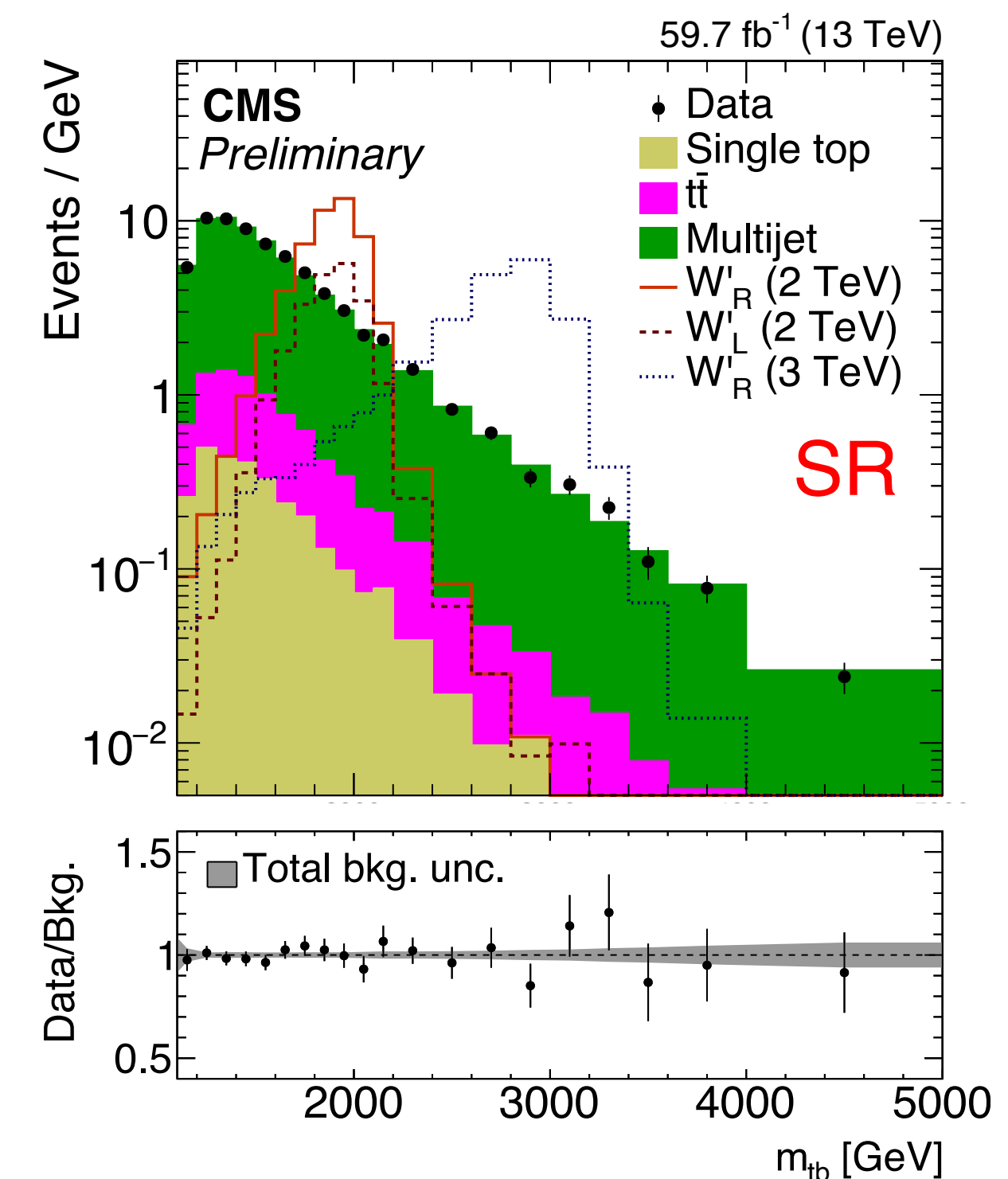
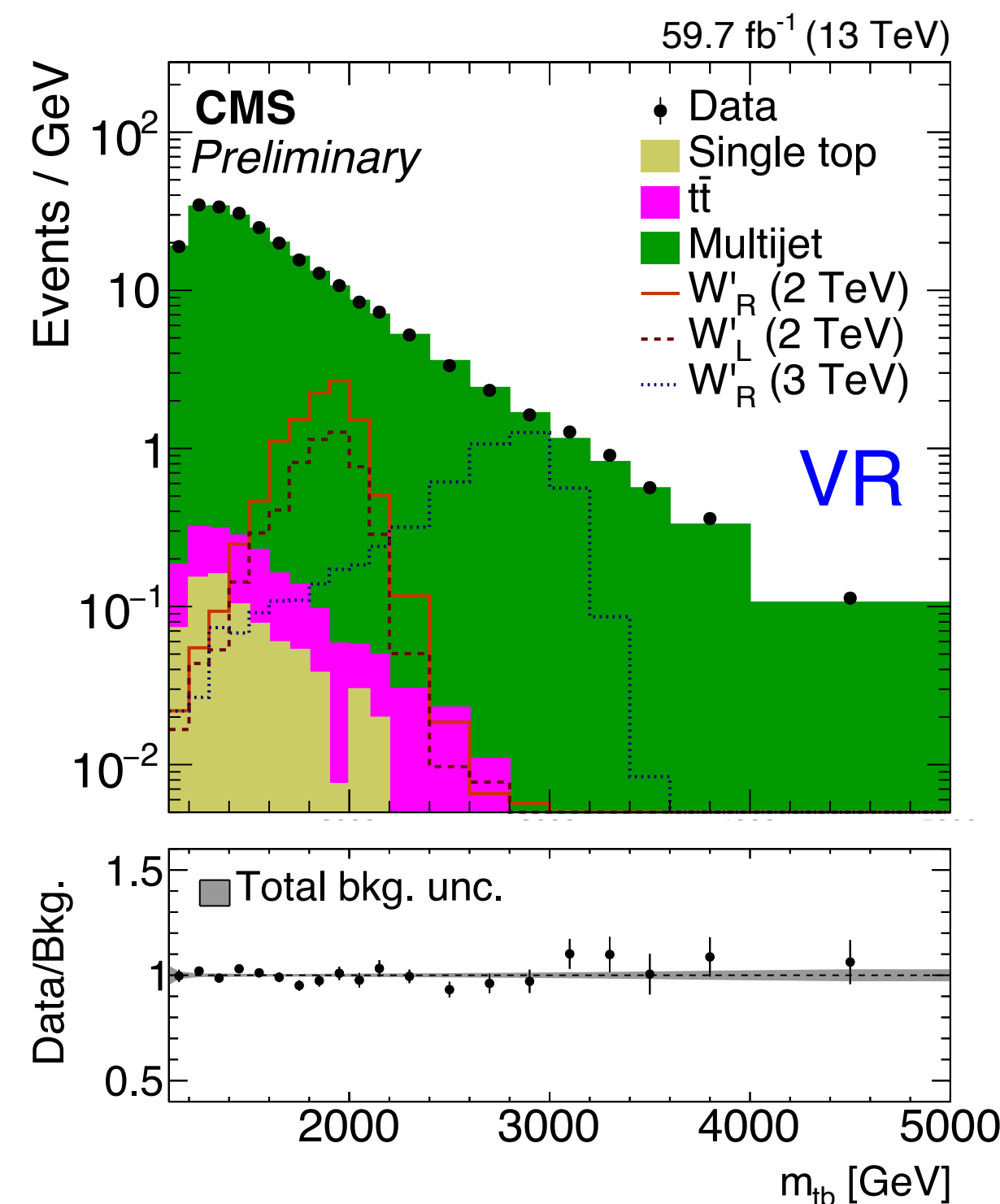


- Final discriminant: invariant  $tb$  mass ( $m_{tb}$ )
- Background estimation of dominant multijet production:
  - In mass sideband ( $m_{SD} < 105$  GeV), extract **b tag pass/fail ratio** as function of  $\eta$  of the AK4 jet
  - In signal mass window, invert b tag requirement (SR') and multiply  $m_{tb}$  spectrum by pass/fail ratio to **predict multijet in signal region** (SR)
  - Validate procedure in top tag fail region (VR)



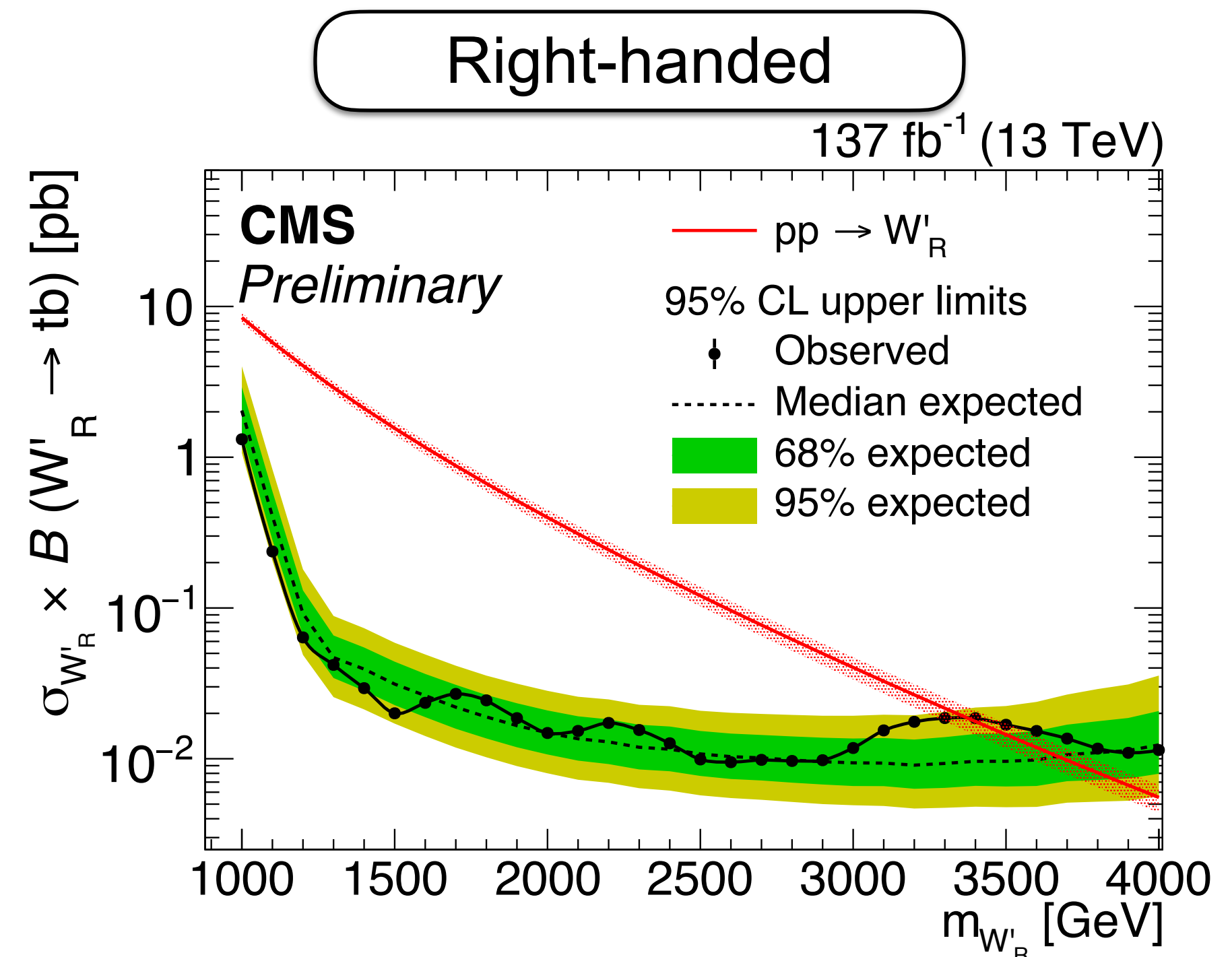
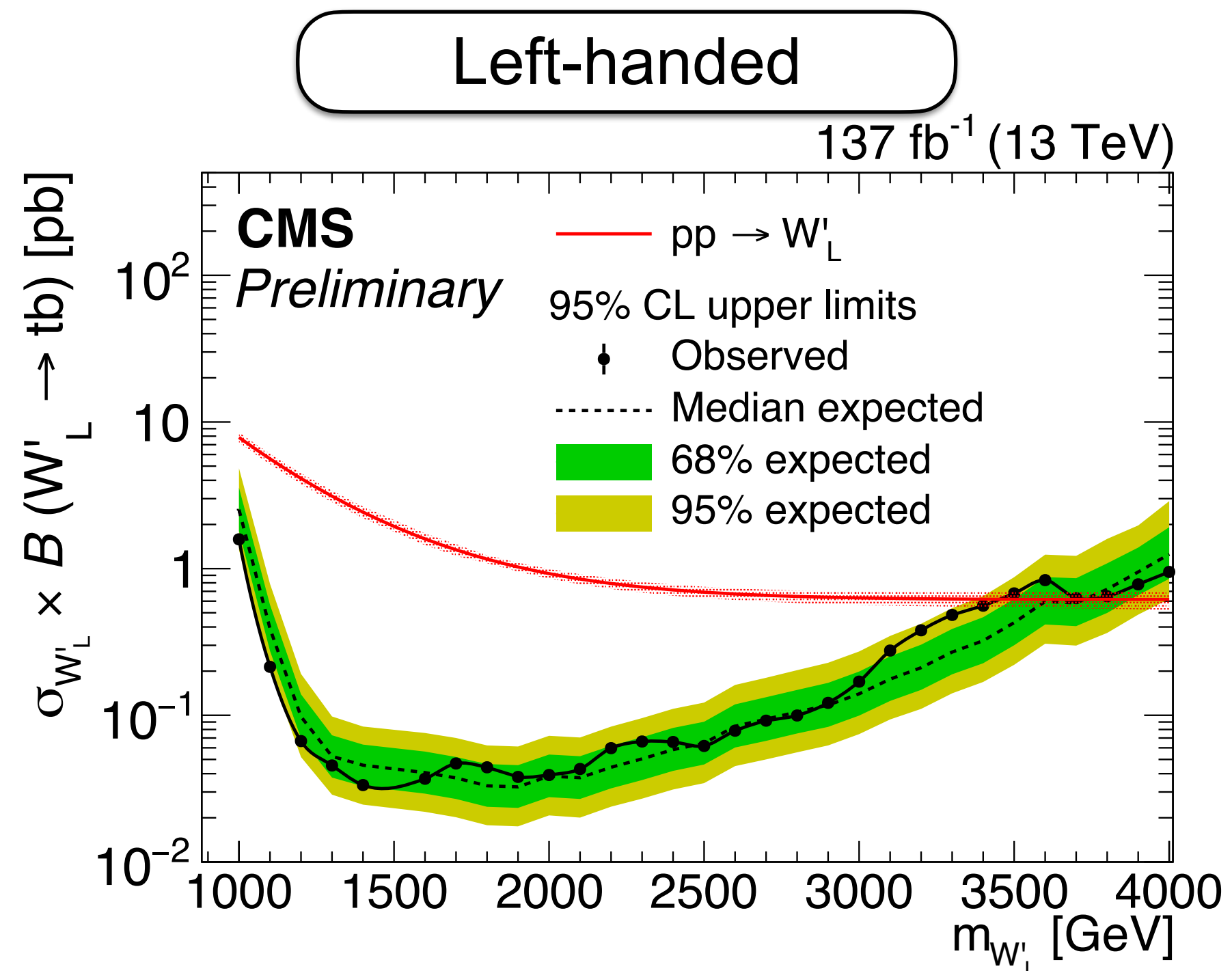
Multijet validation region

Signal region





- > Set upper limits on the production cross section of a  $W'$  decaying to  $tb$
- >  $W'$  can have different chiralities (left- and right-handed)
  - Different chiralities lead to different angular distributions of top quark decay products affecting tagger efficiency
  - Also taking into account interference with standard model



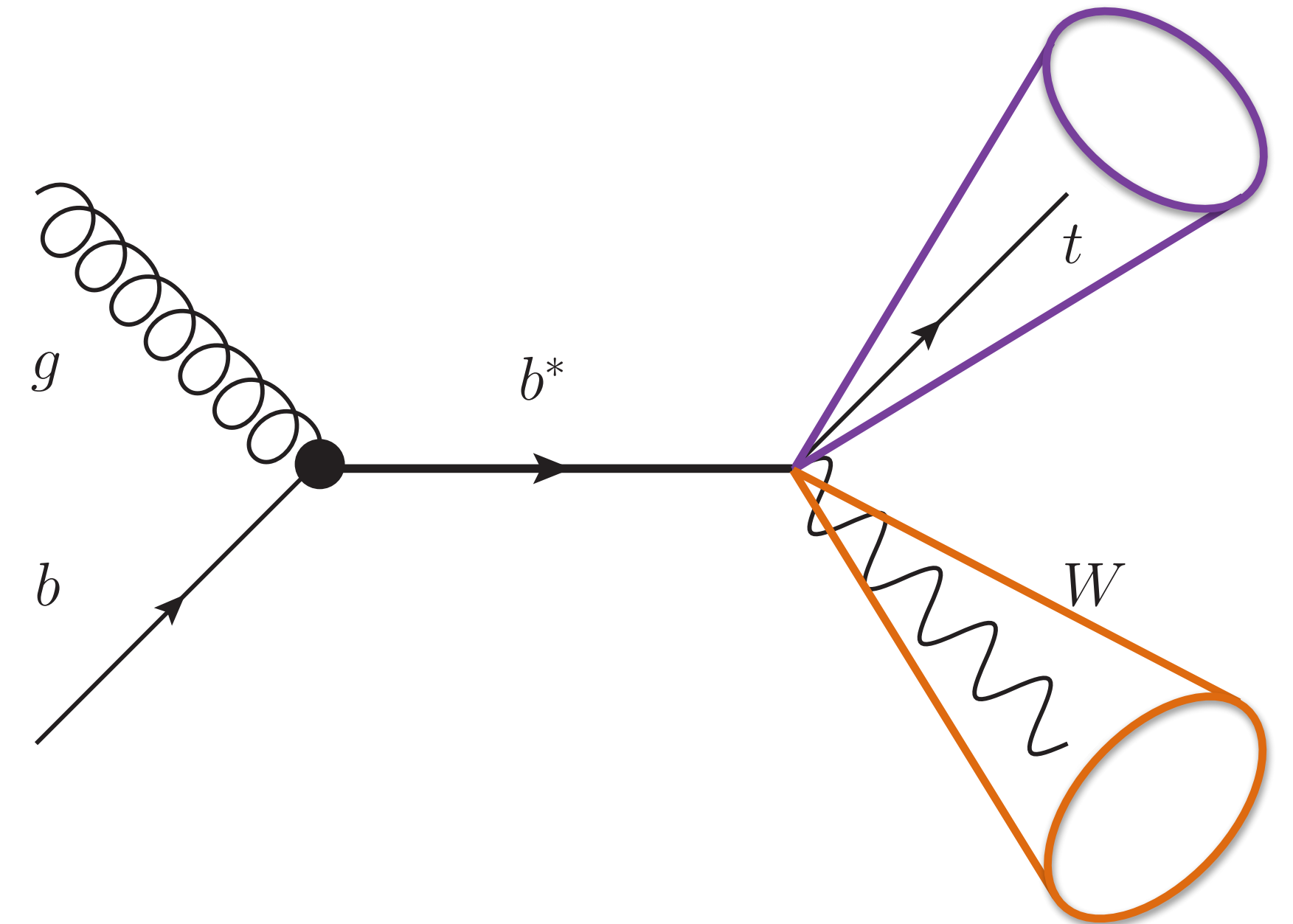
new!

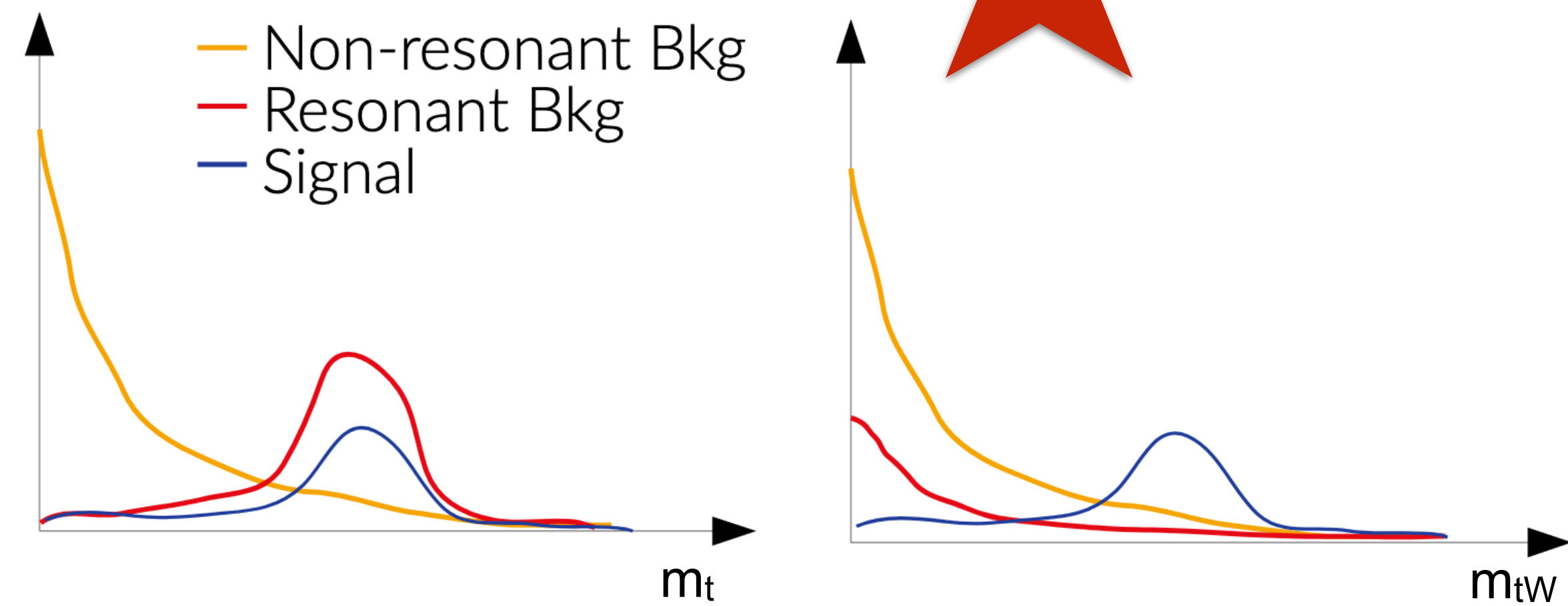
## > Topology:

- 1 high- $p_T$  **W-boson jet**
- 1 high- $p_T$  top-quark jet
- both are identified using N-subjettiness ratios ( $\tau_2/\tau_1$  and  $\tau_3/\tau_2$ ), additional subjet b tagging for top quark

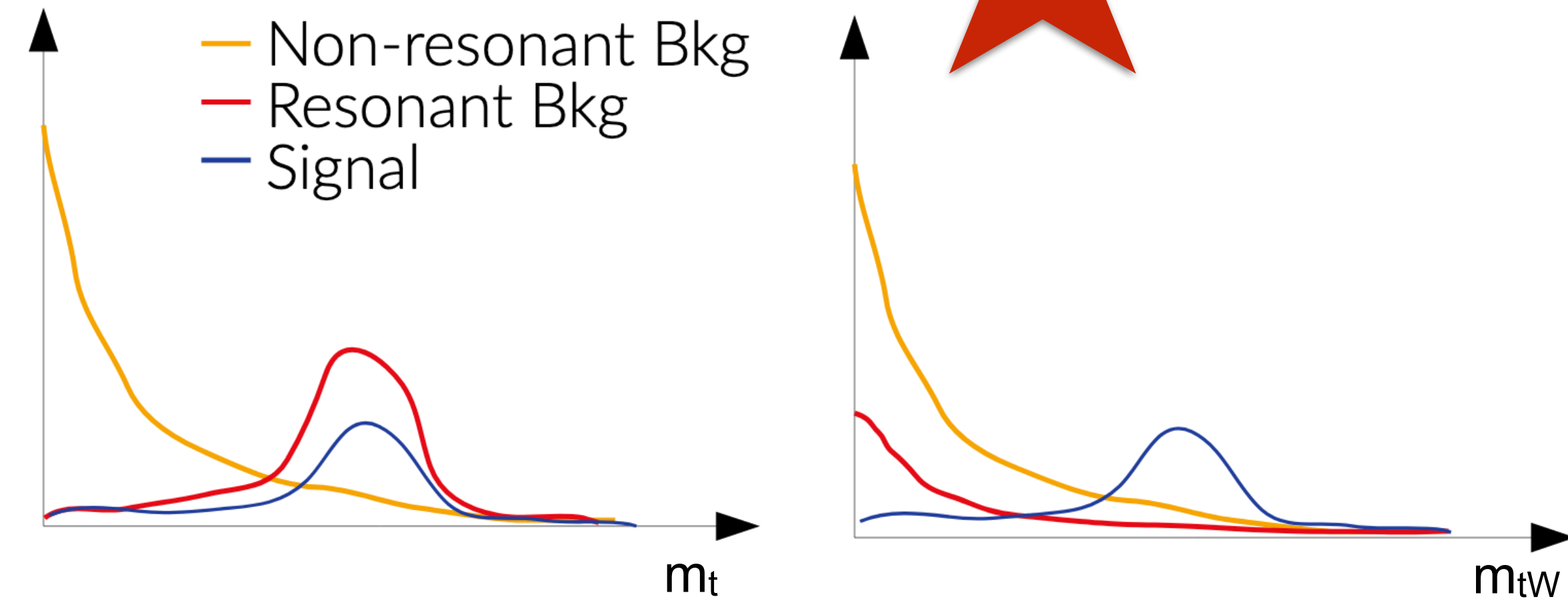
## > Selection:

- Two AK8 jets,  $p_T > 400$  GeV
- Select W-boson (and top-quark) mass windows  $65 (105) < m_{SD} < 105 (210)$  GeV
- Both well-separated from each other (back-to-back)





- > Parameterize bump hunt in  $(m_t, m_{tW})$ 
  - Smoothly falling nonresonant background (multijets,  $W$ +jets) estimated from data
  - Resonant backgrounds ( $tt$  and  $tW$ ) estimated via template fit from simulation
- > Perform a 2D likelihood fit in  $m_t = [65, 285]$  GeV and  $m_{tW} = [1200, 4000]$  GeV





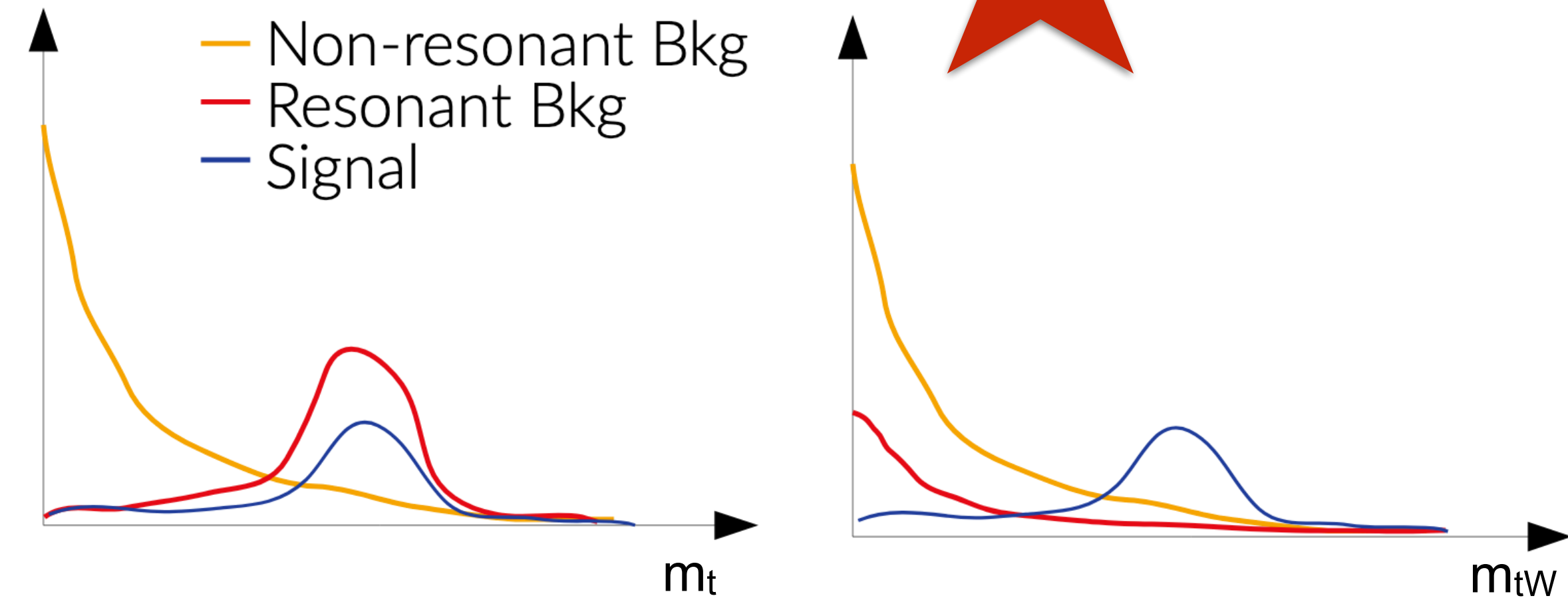
## > Parameterize bump hunt in $(m_t, m_{tW})$

- Smoothly falling nonresonant background (multijets,  $W$ +jets) estimated from data
- Resonant backgrounds ( $tt$  and  $tW$ ) estimated via template fit from simulation

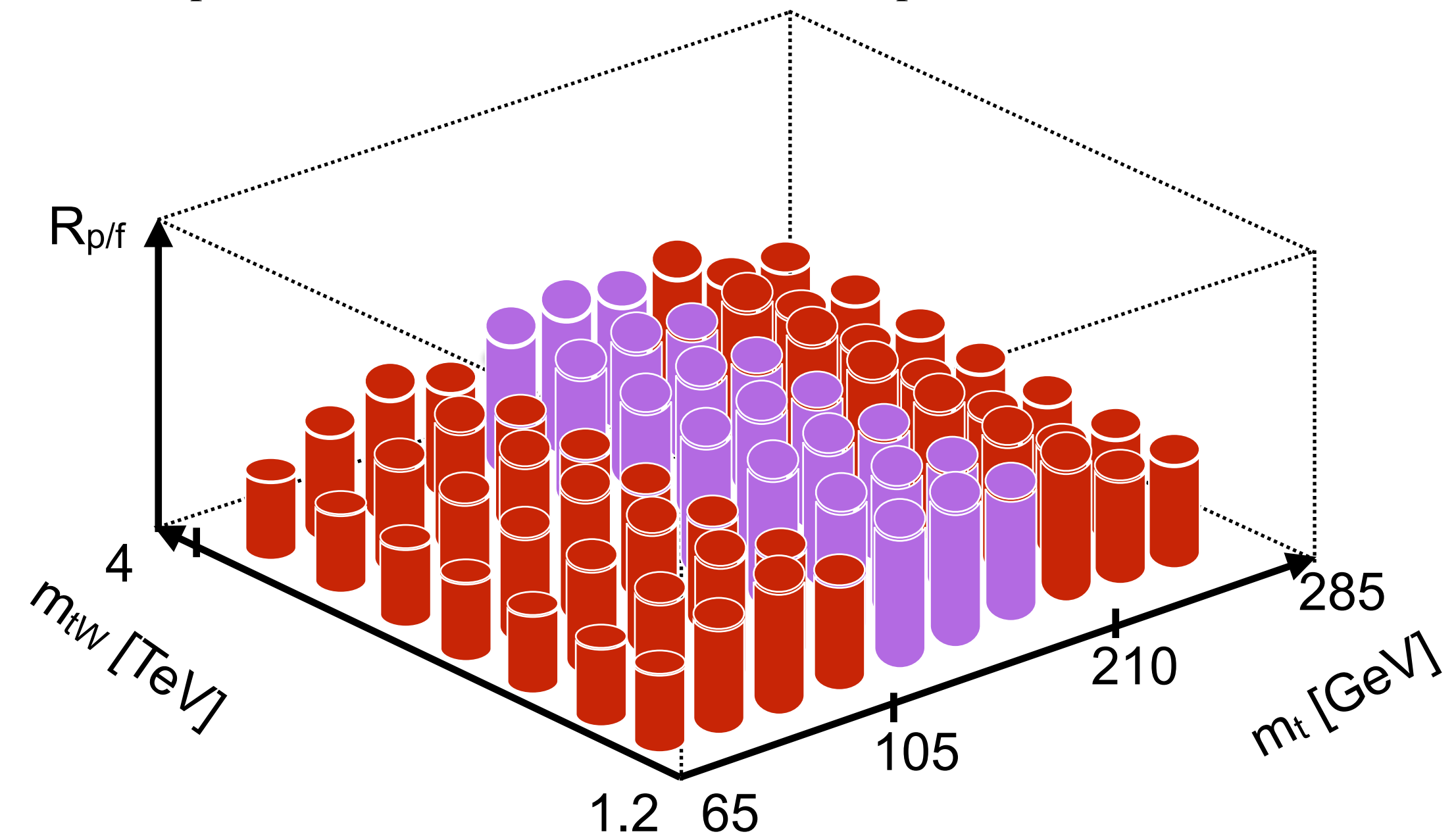
## > Perform a 2D likelihood fit in $m_t = [65, 285]$ GeV and $m_{tW} = [1200, 4000]$ GeV

## > Nonresonant background: top tag pass/fail ratio

- Smooth ratio, fit using 2D polynomials



$$N_p^{\text{nonres}}(\text{bin}) = N_f^{\text{nonres}}(\text{bin}) \times f_{p/f}(m_t, m_{tW})^\dagger$$



$\dagger$ actually,  $R_{p/f}^{\text{MC}}$  ratio is factored out and data/MC  $R_{p/f}$  is used

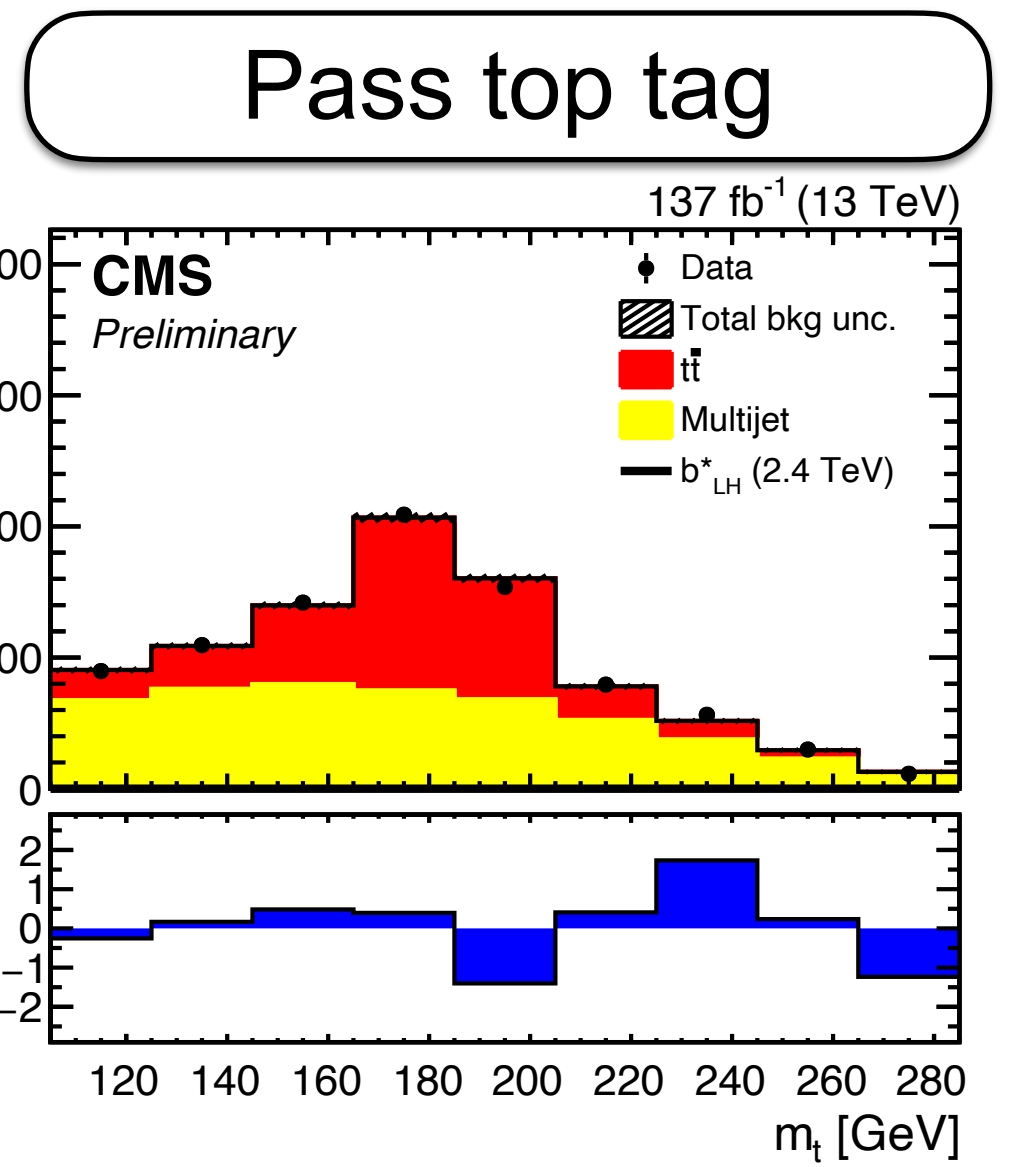
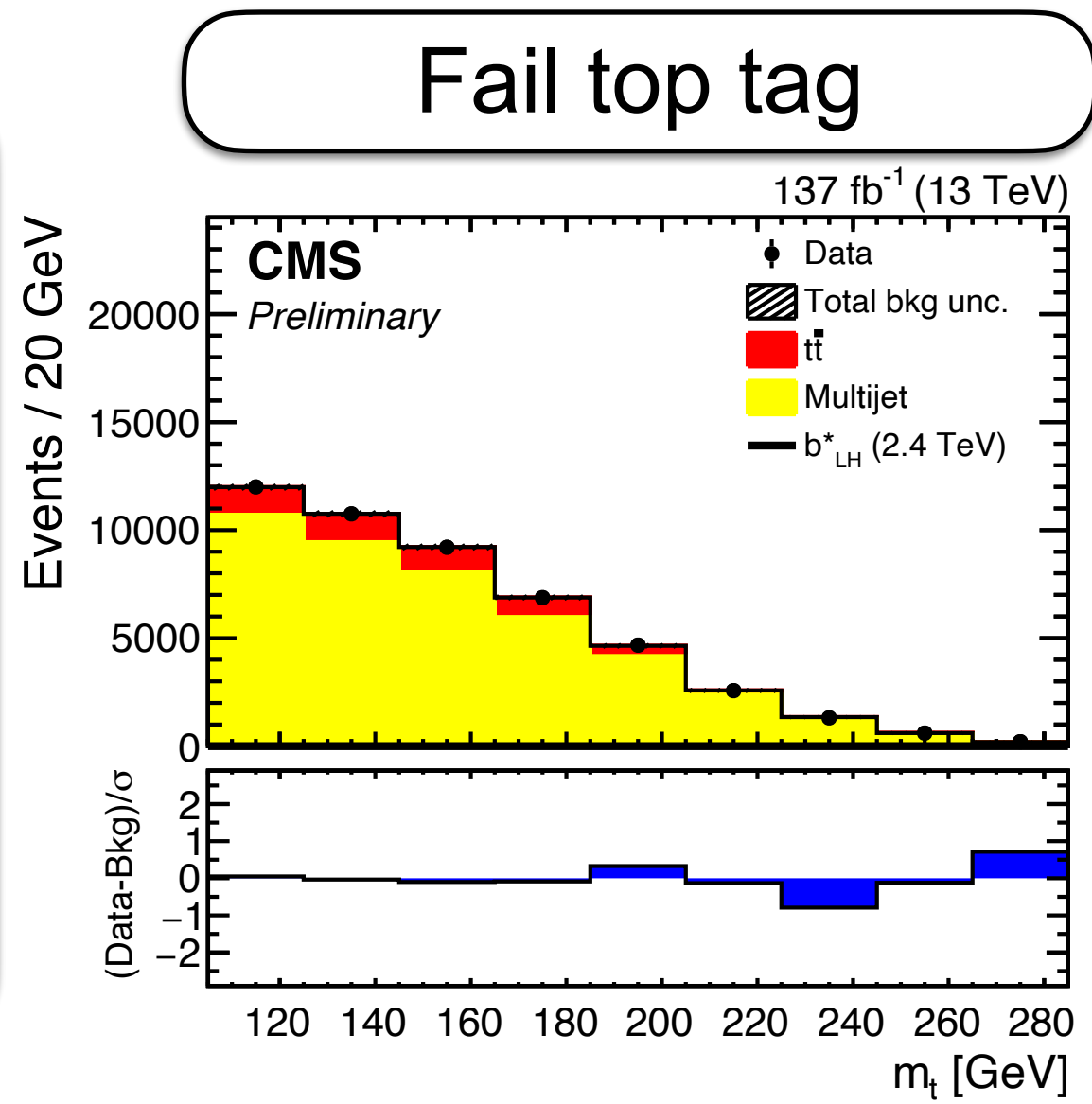


## ➤ Resonant $t\bar{t}$ and $tW$ background:

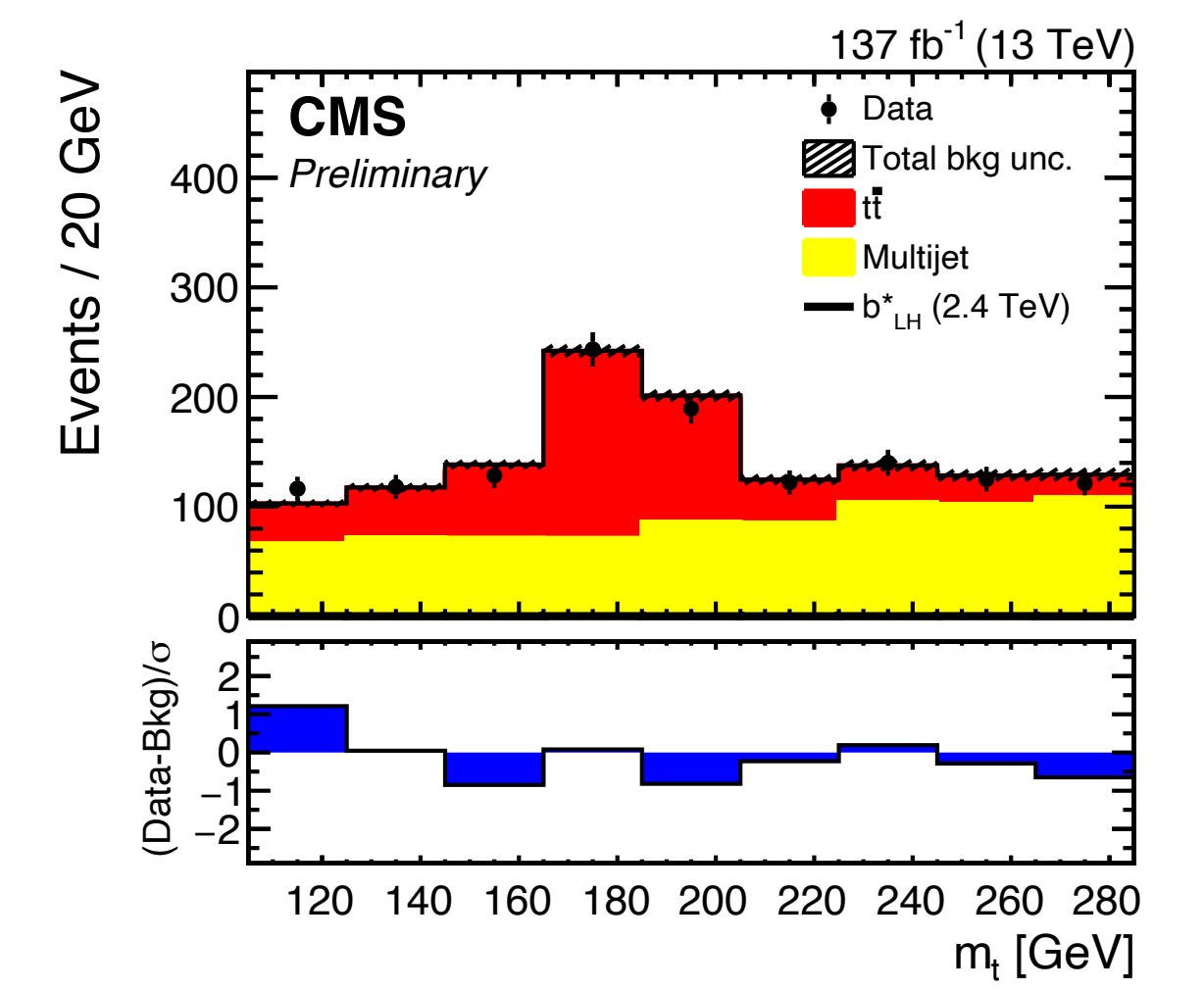
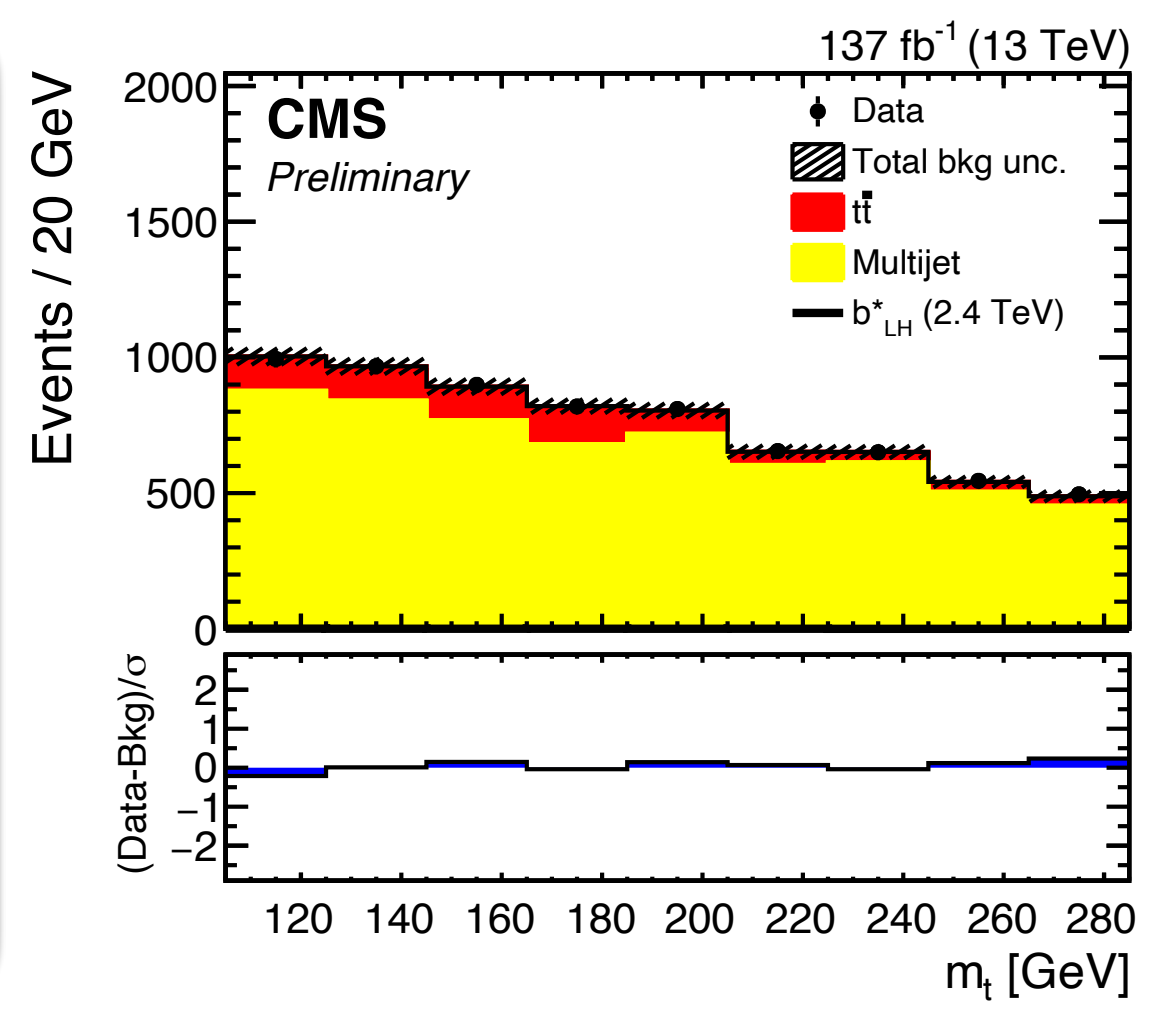
- Define dedicated measurement region by requiring a second top tag
- Estimate multijet background as for signal

## ➤ Constrain top mass scale simultaneously

1.2 <  $m_{t\bar{t}}$  < 1.3 TeV



1.8 <  $m_{t\bar{t}}$  < 3 TeV

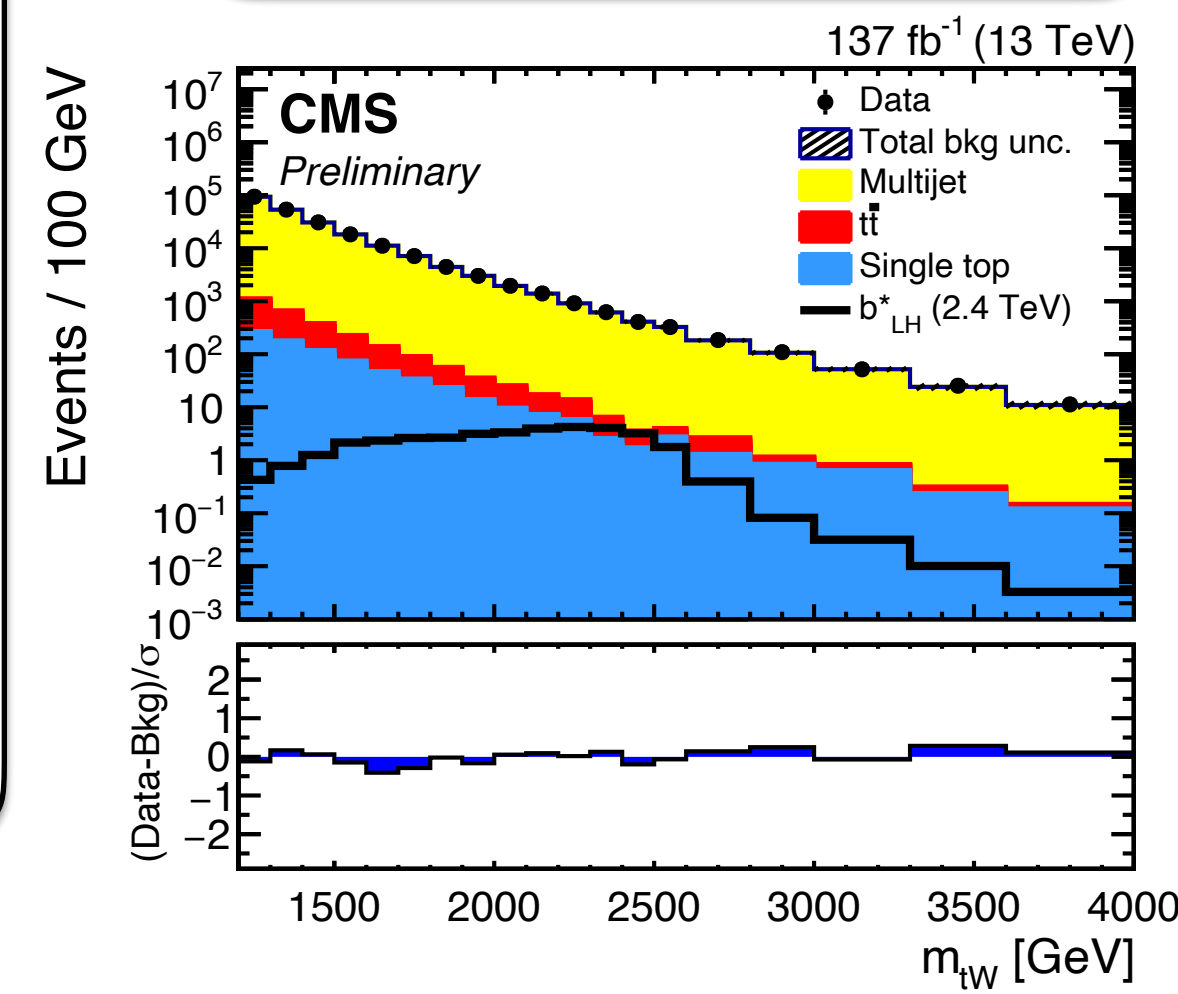




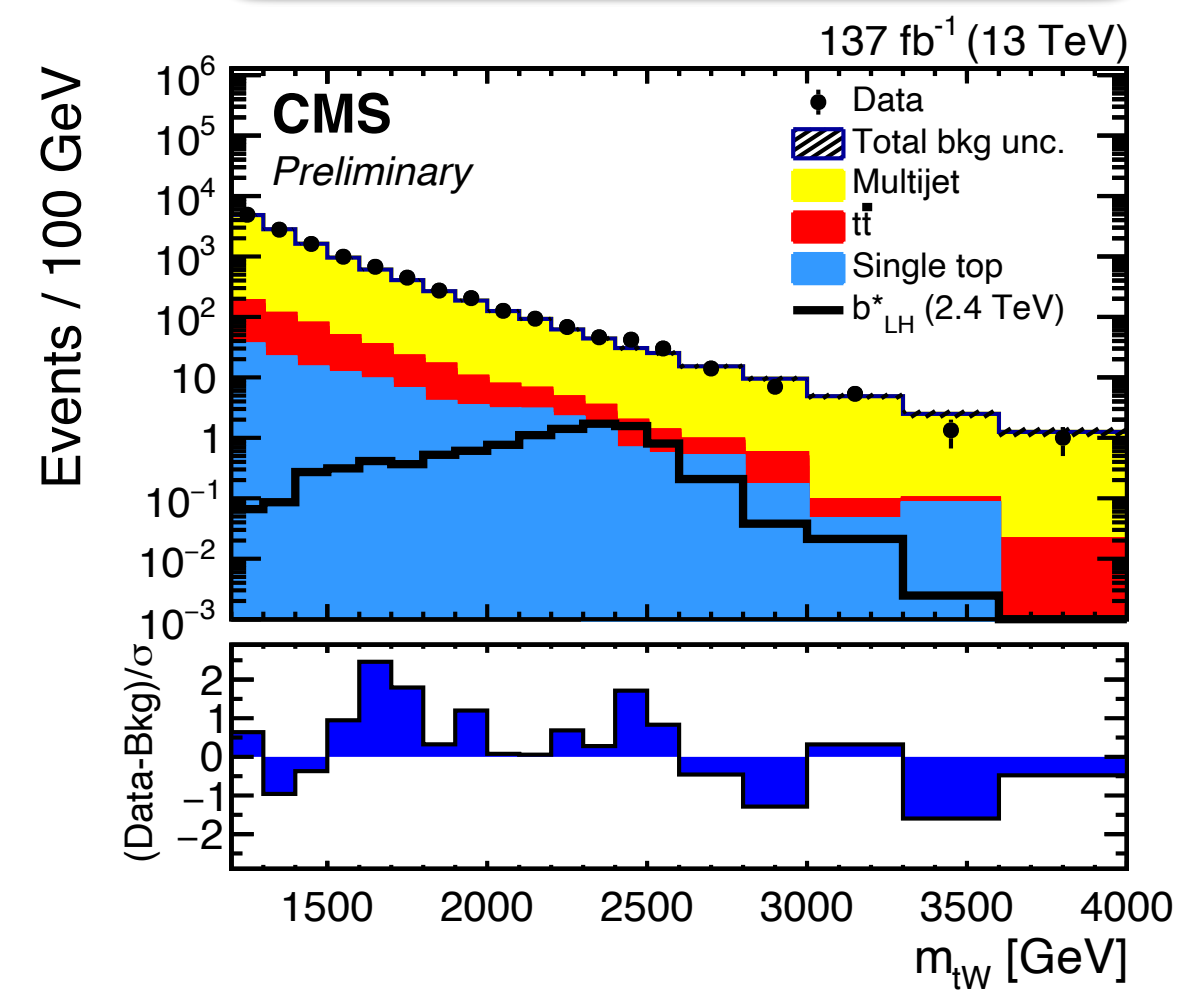
## ➤ Signal region post-fit spectra

65 <  $m_t$  < 105 GeV

Fail top tag

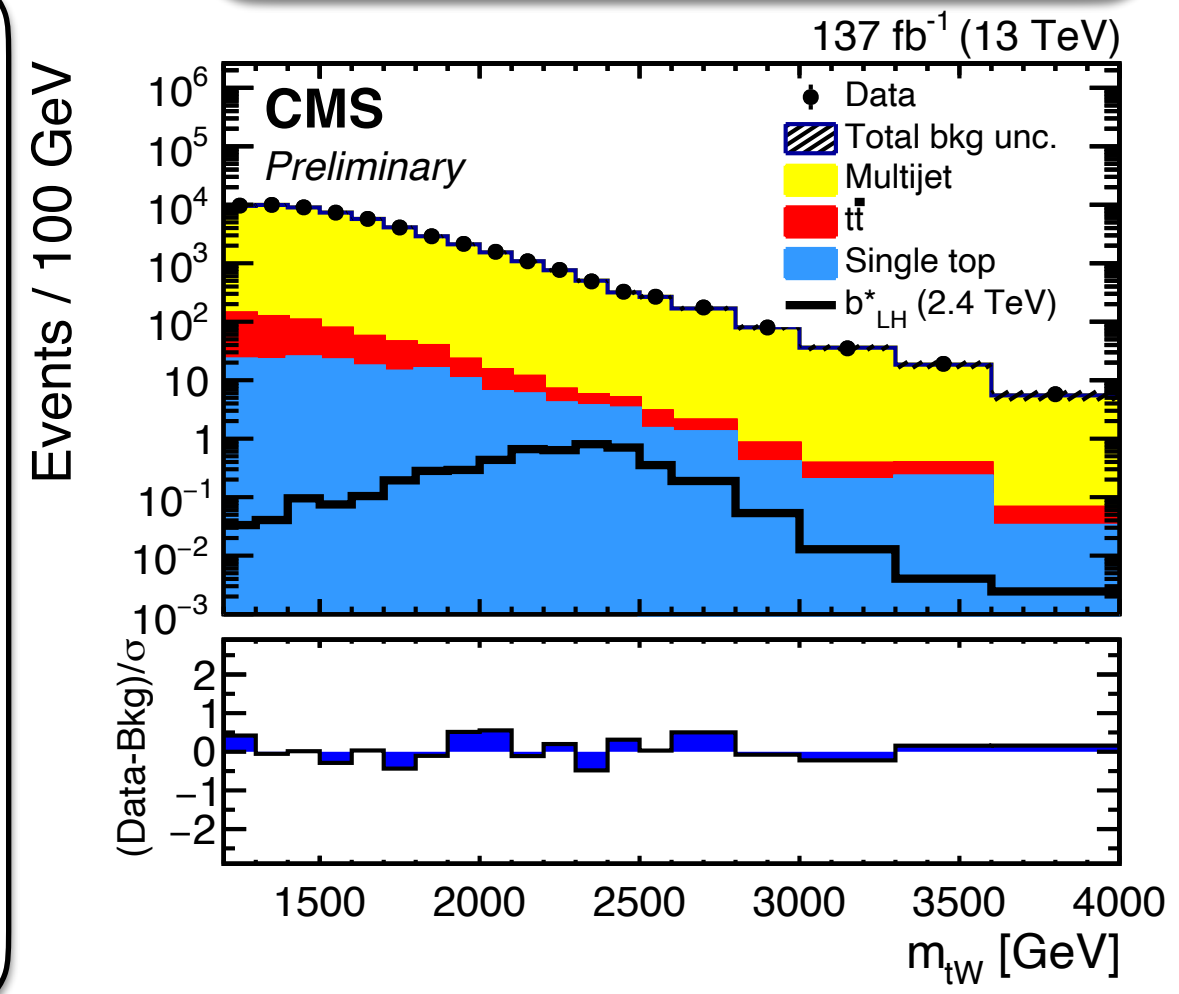


Pass top tag

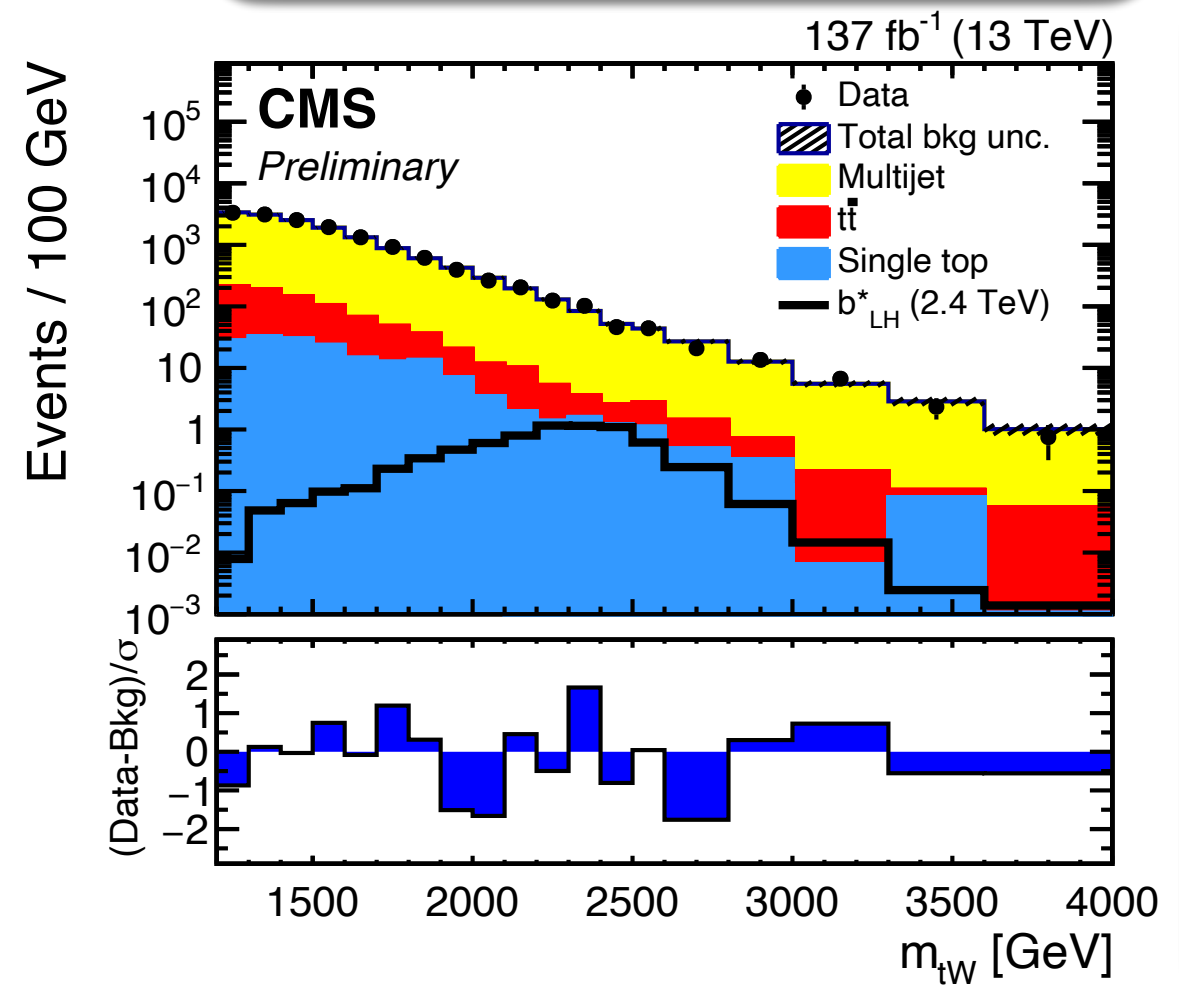


225 <  $m_t$  < 285 GeV

Fail top tag

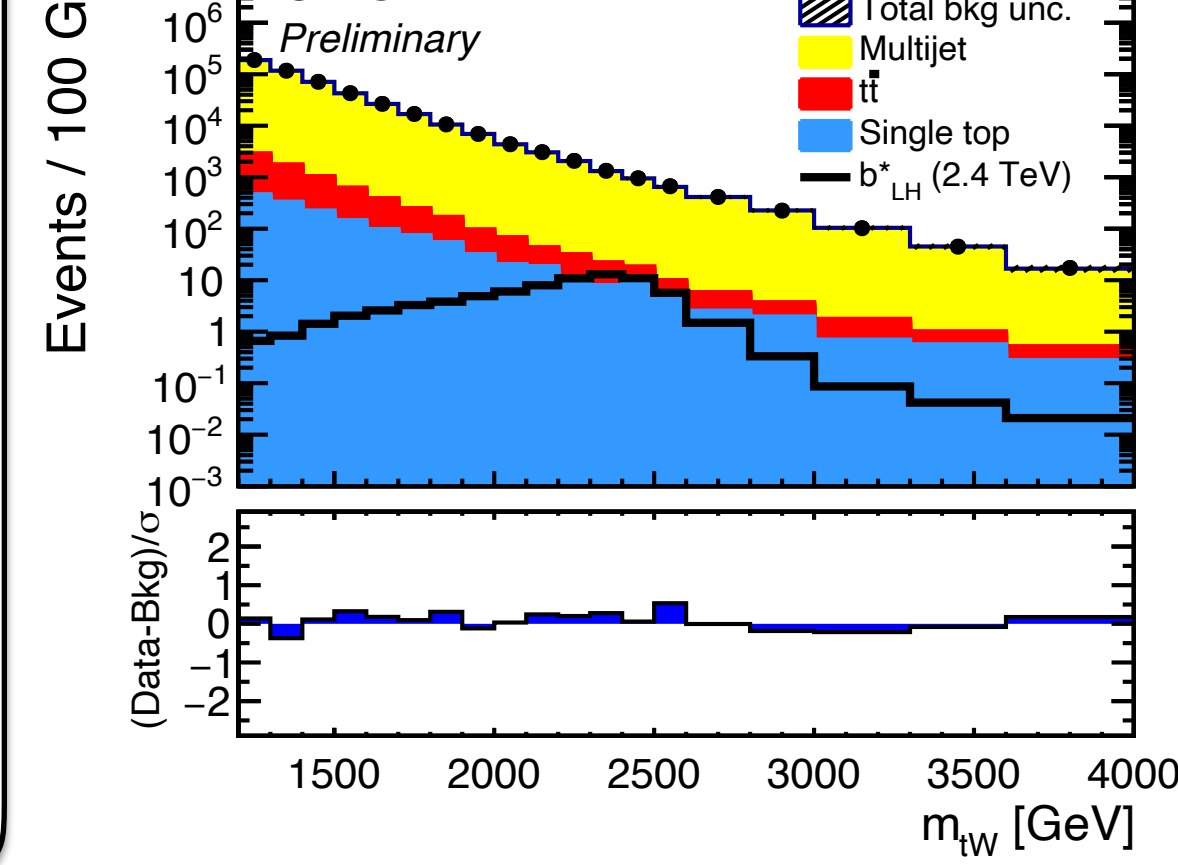


Pass top tag



105 <  $m_t$  < 225 GeV

Fail top tag

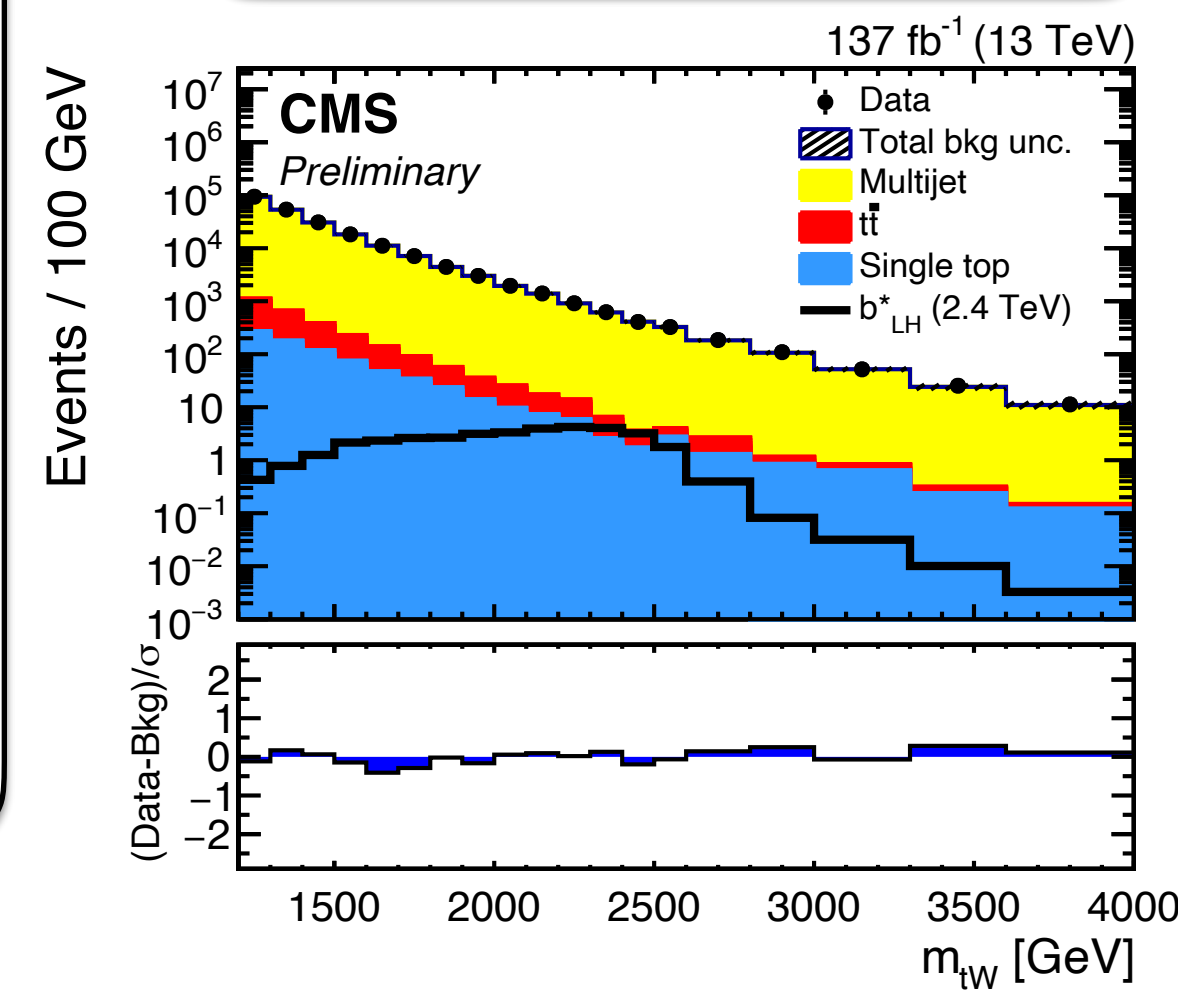




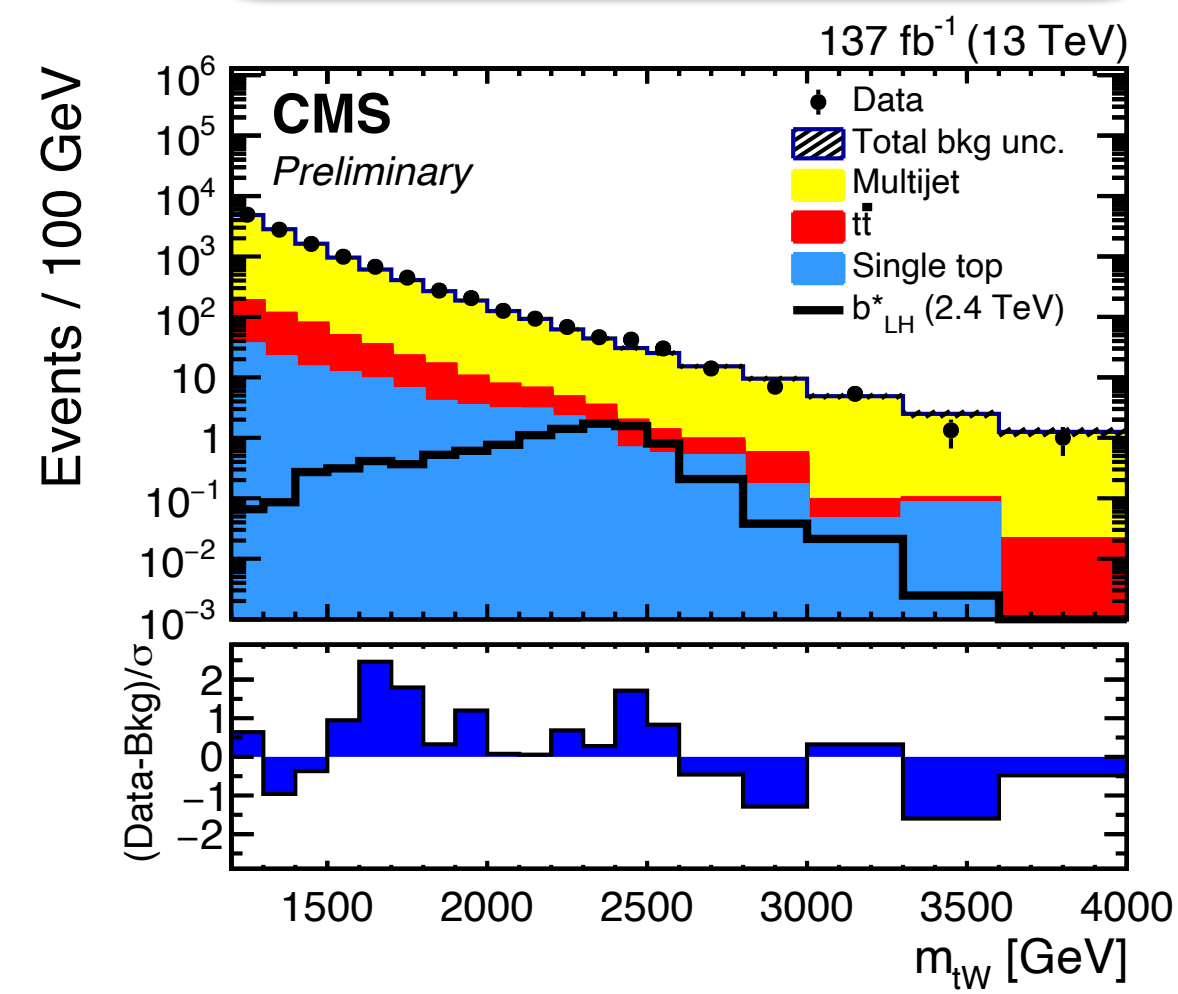
## ➤ Signal region post-fit spectra

65 < m<sub>t</sub> < 105 GeV

Fail top tag

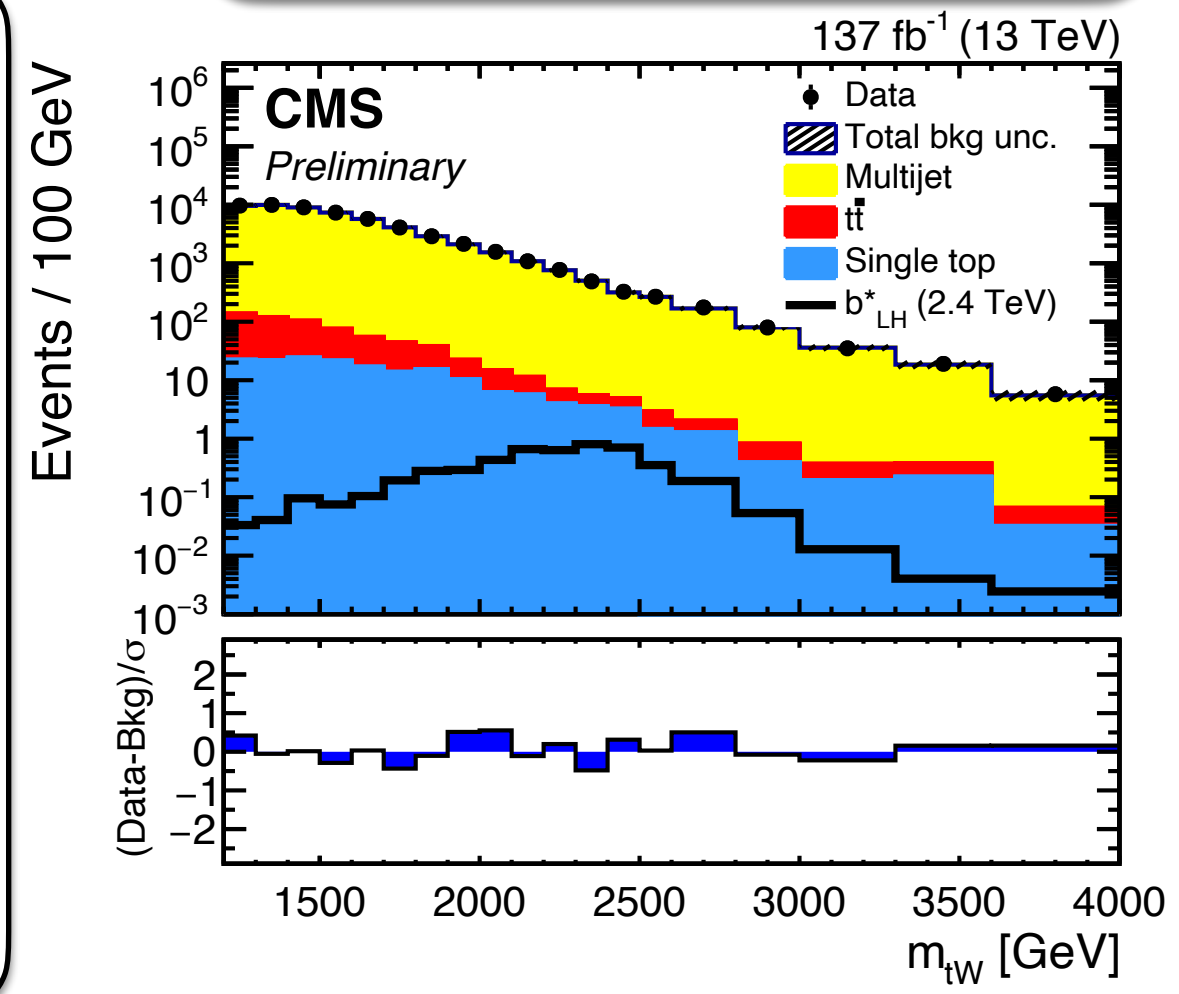


Pass top tag

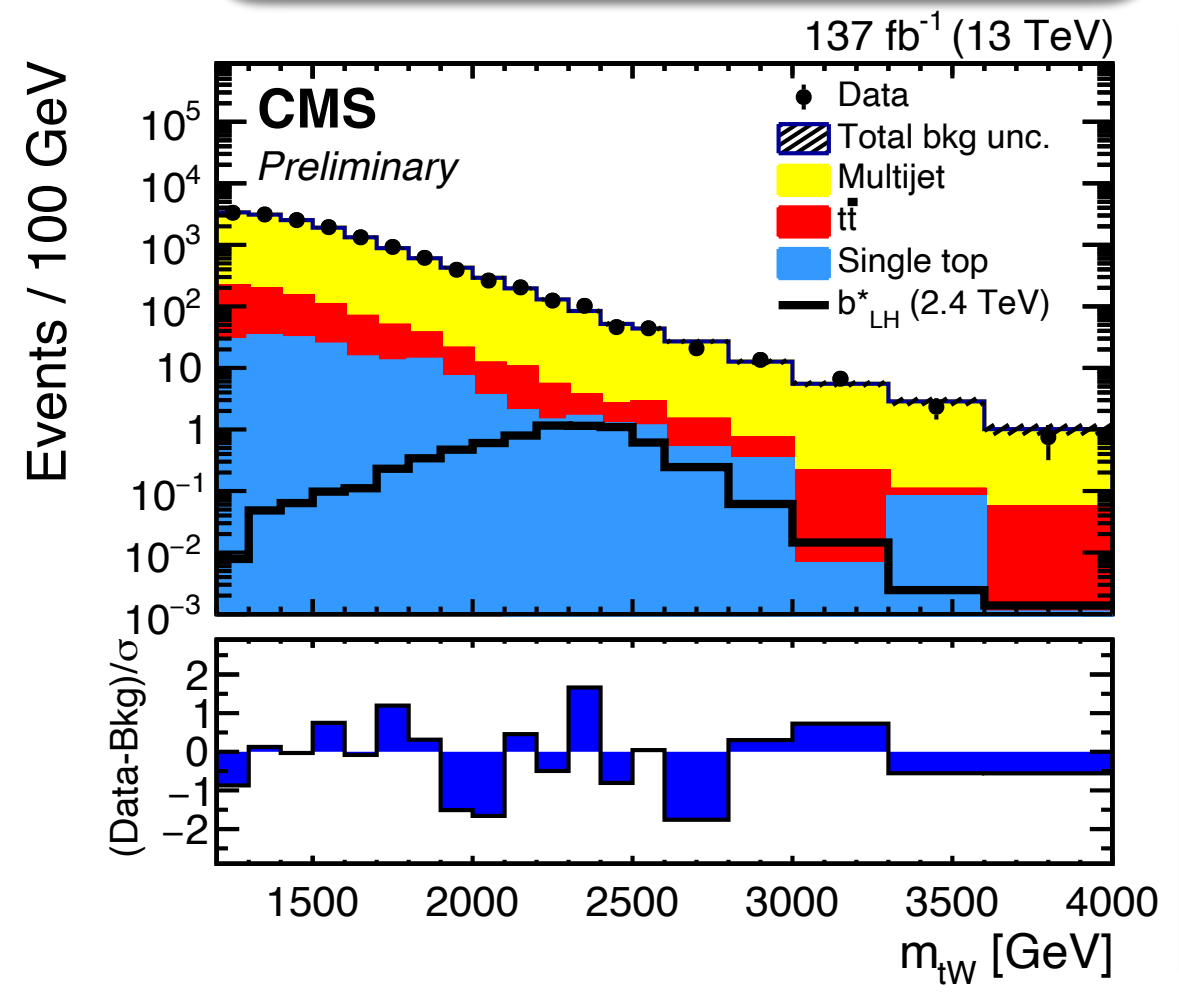


225 < m<sub>t</sub> < 285 GeV

Fail top tag

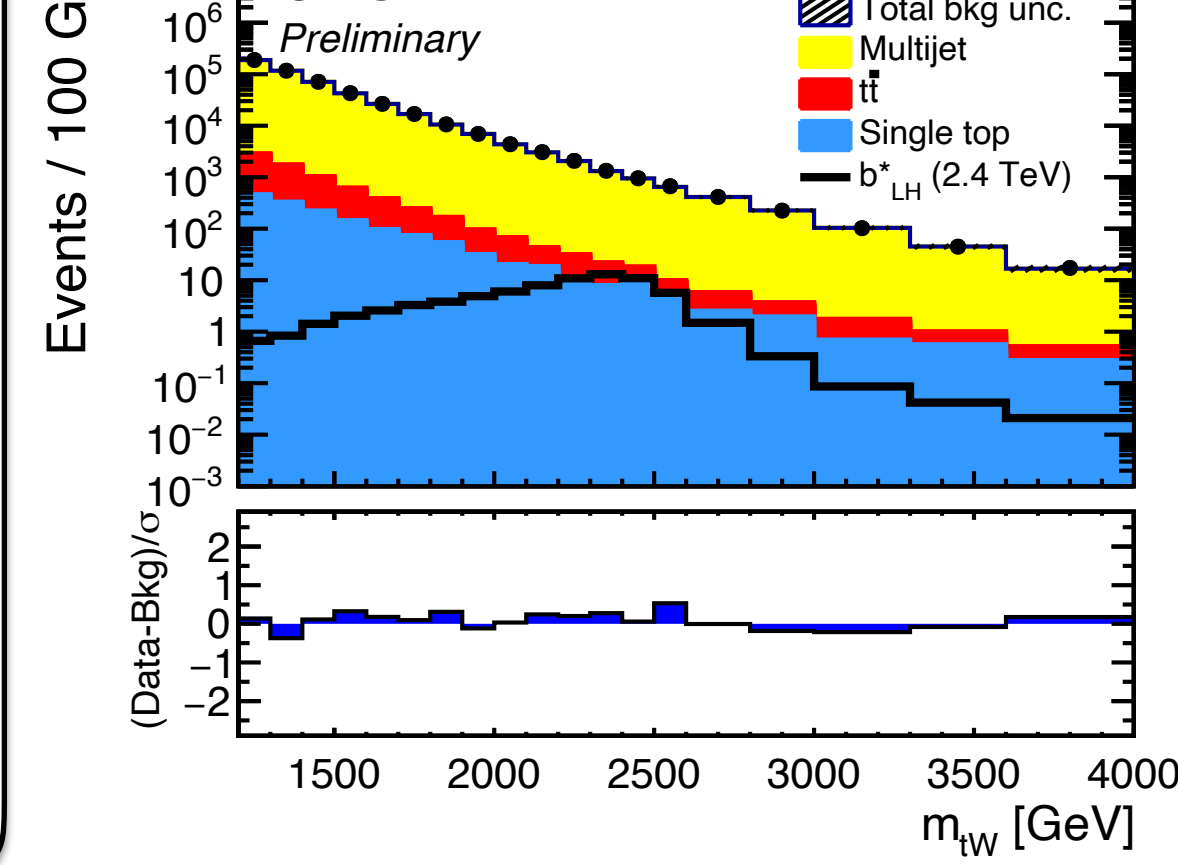


Pass top tag

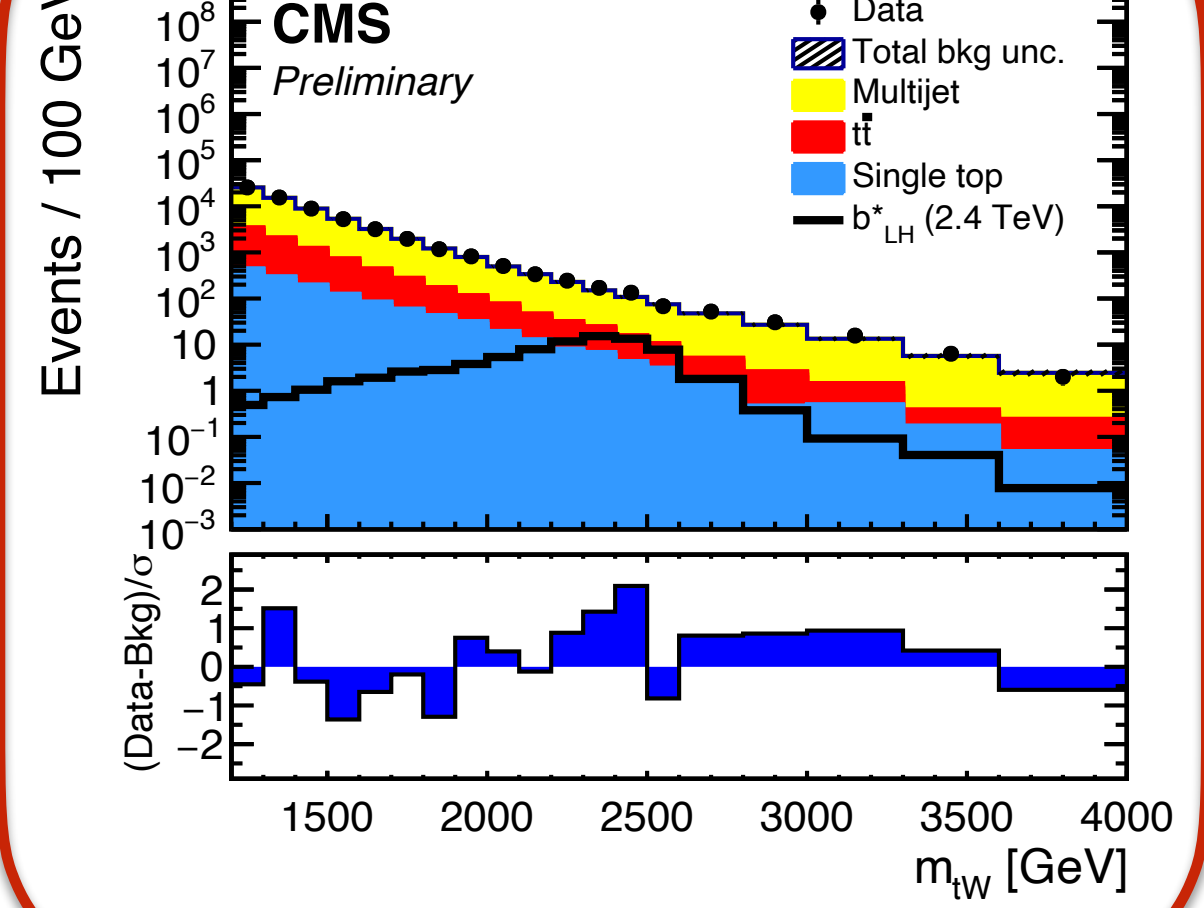


105 < m<sub>t</sub> < 225 GeV

Fail top tag



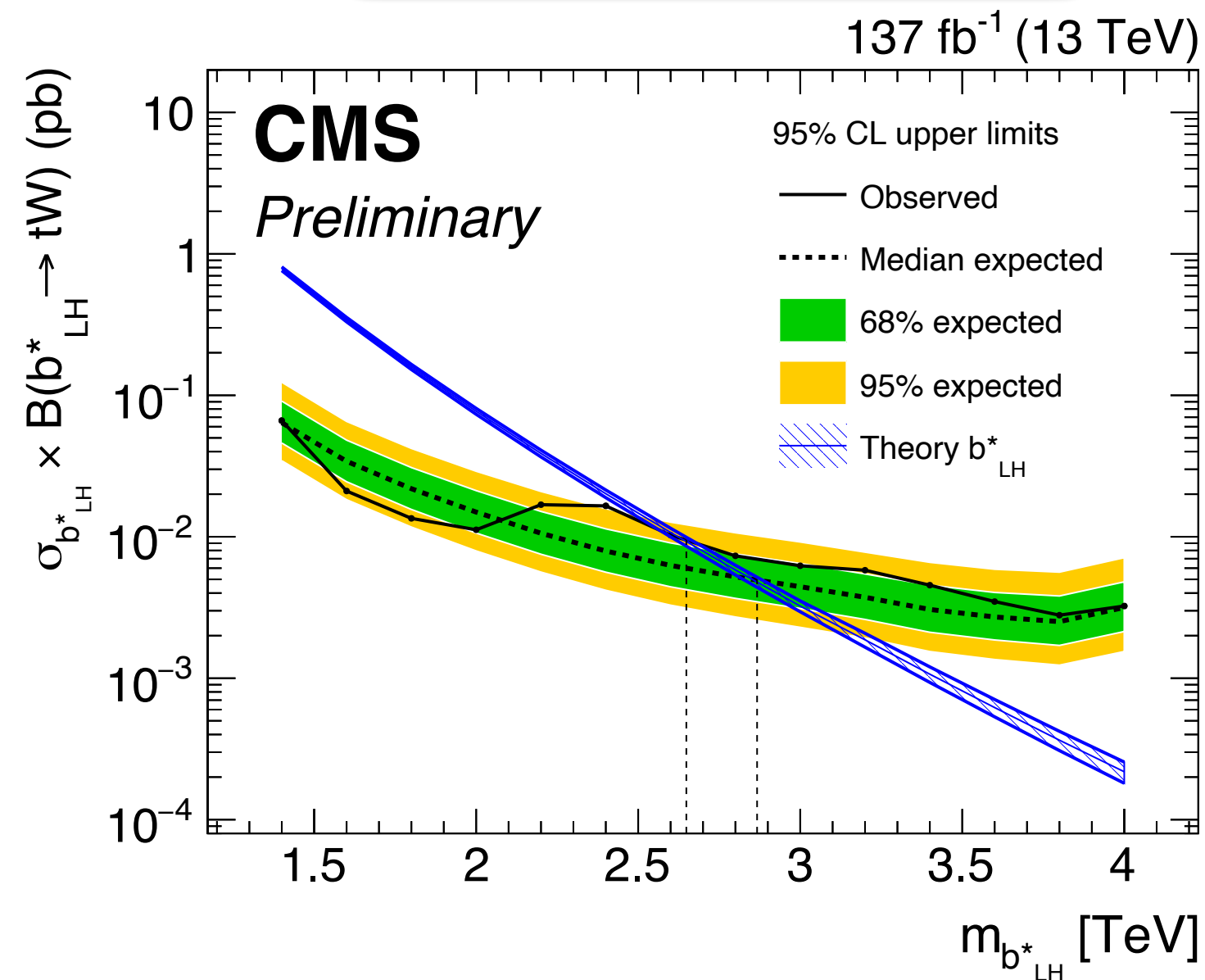
Pass top tag



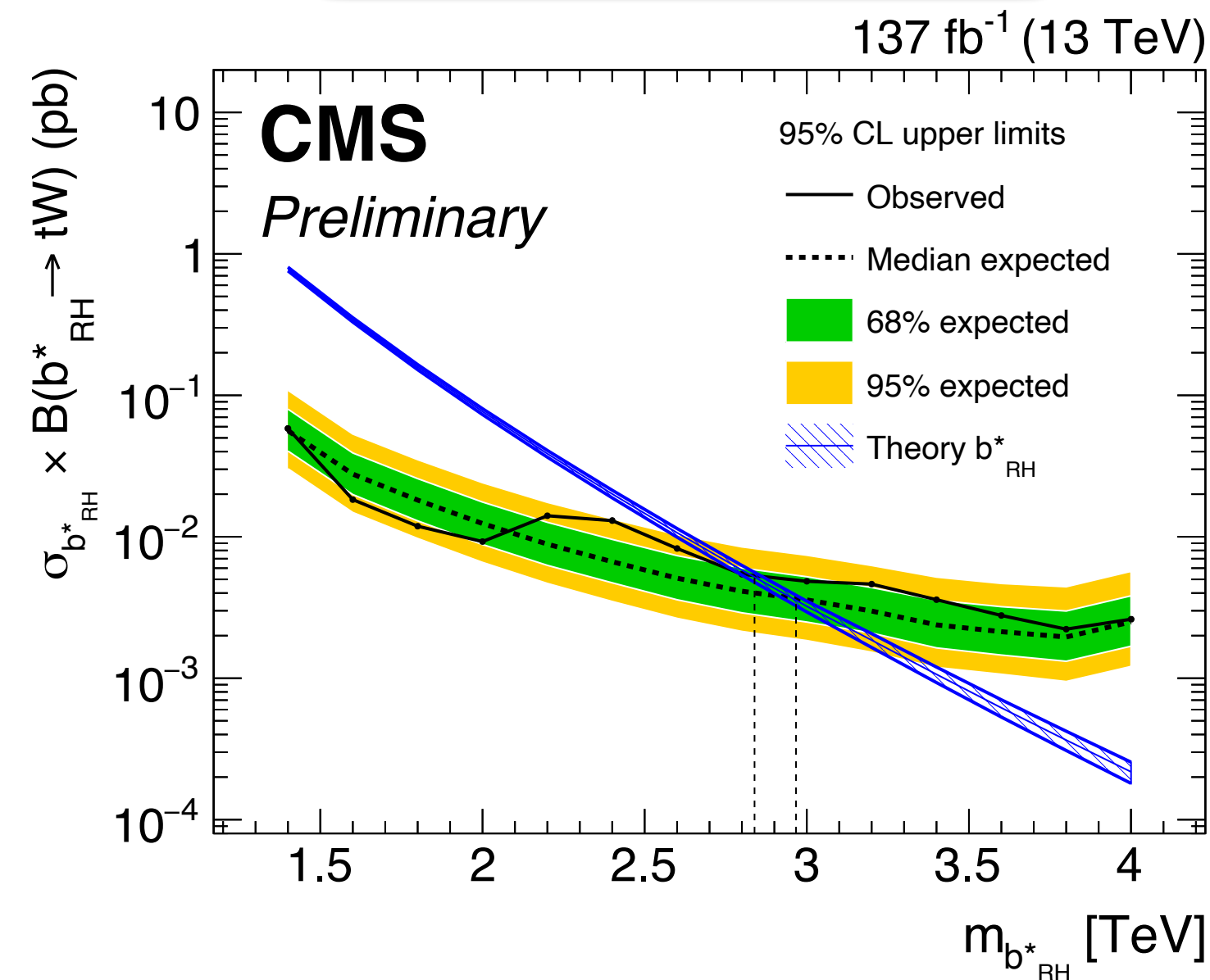


- >  $b^*$  can have different chiralities (left- and right-handed, vector-like)
- > Largest excess for left-handed  $b^*$  at 2.4 TeV ( $2.3\sigma$  local)
- > Interpret result in these models

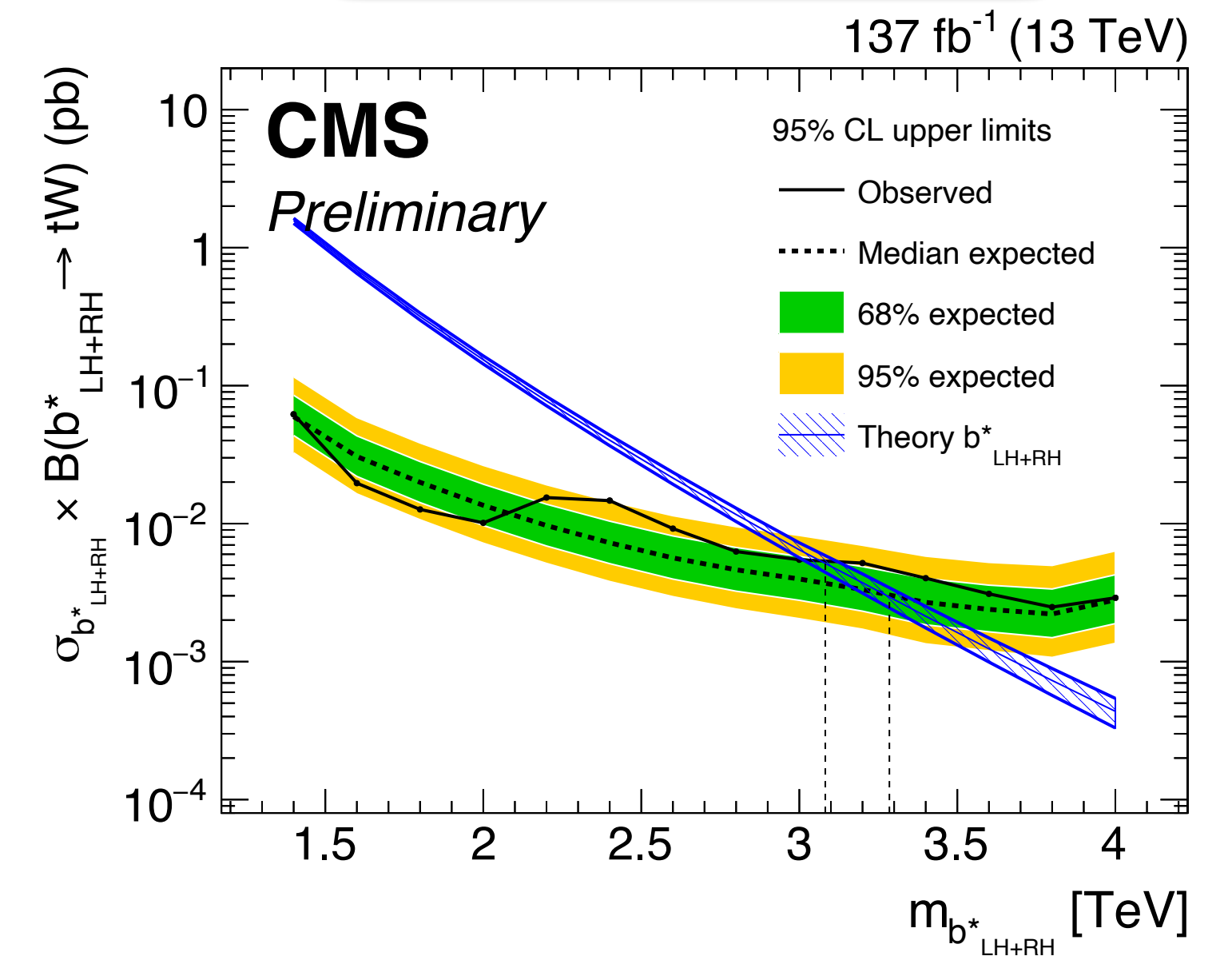
Left-handed



Right-handed

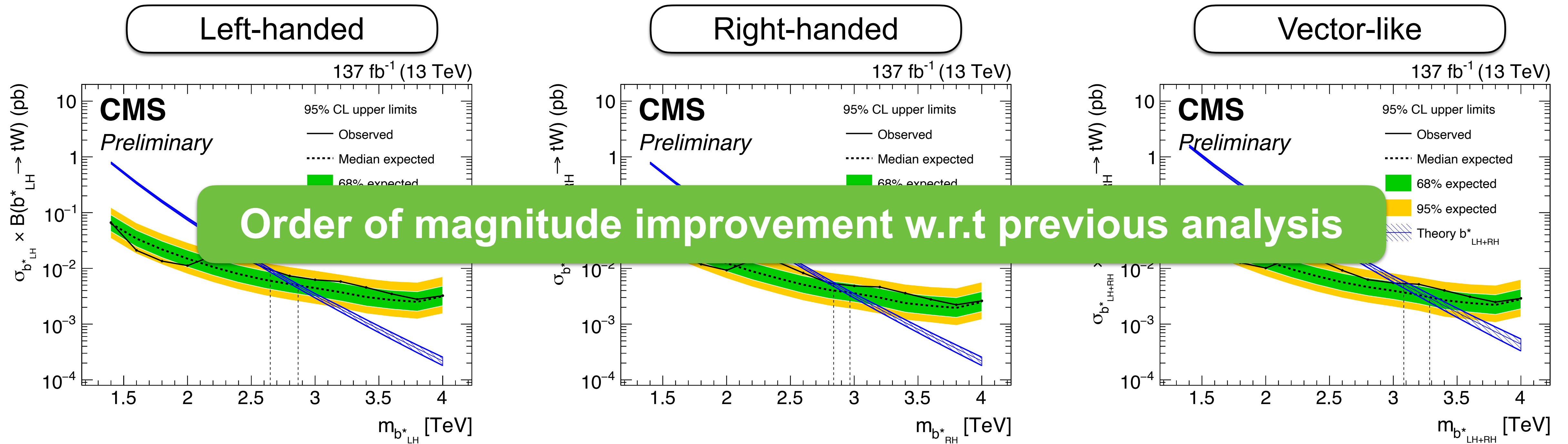


Vector-like





- >  $b^*$  can have different chiralities (left- and right-handed, vector-like)
- > Largest excess for left-handed  $b^*$  at 2.4 TeV ( $2.3\sigma$  local)
- > Interpret result in these models



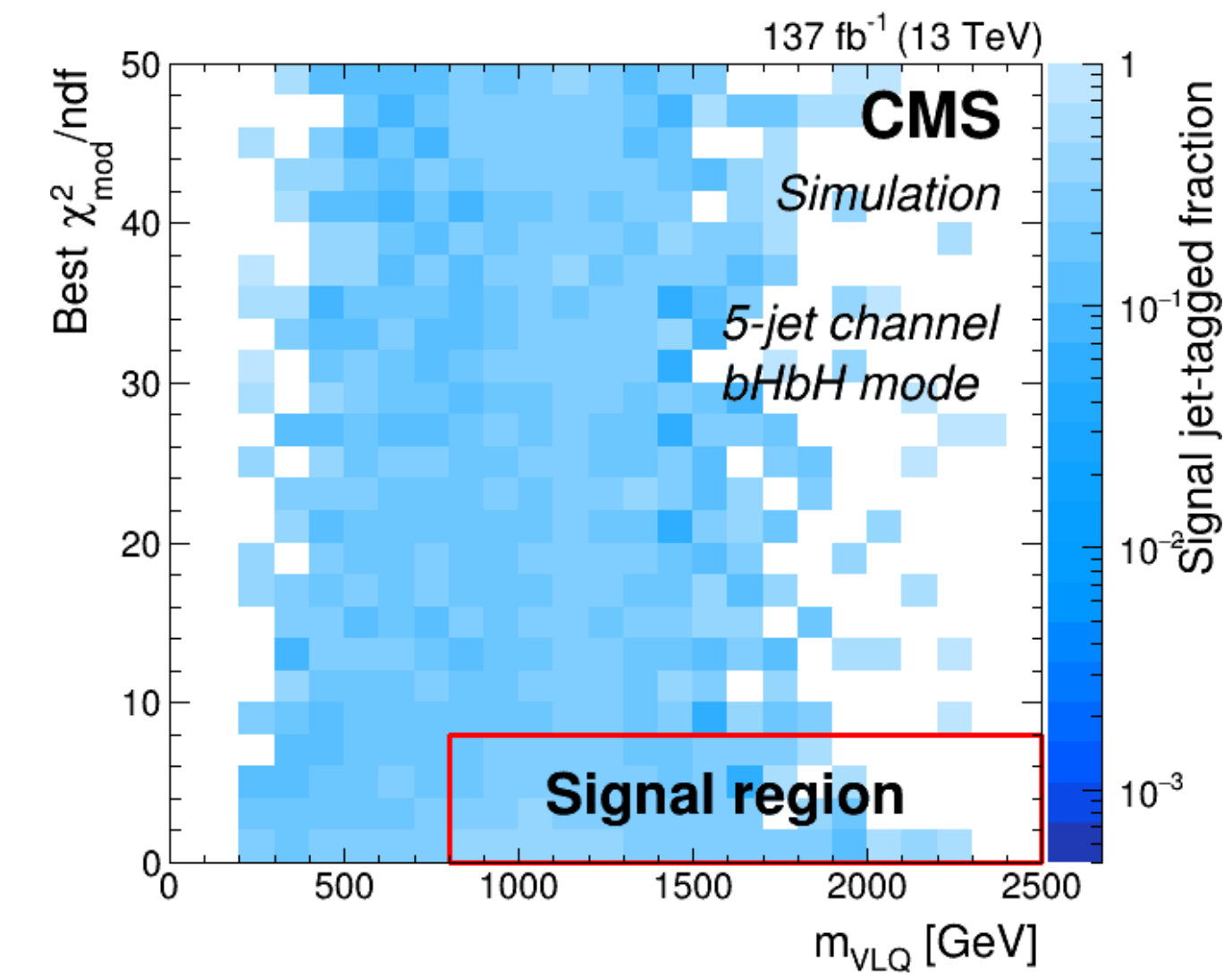


# Limits — and now what?

Ensuring analysis long-term impact and collaborating with theory



# Digitised results?

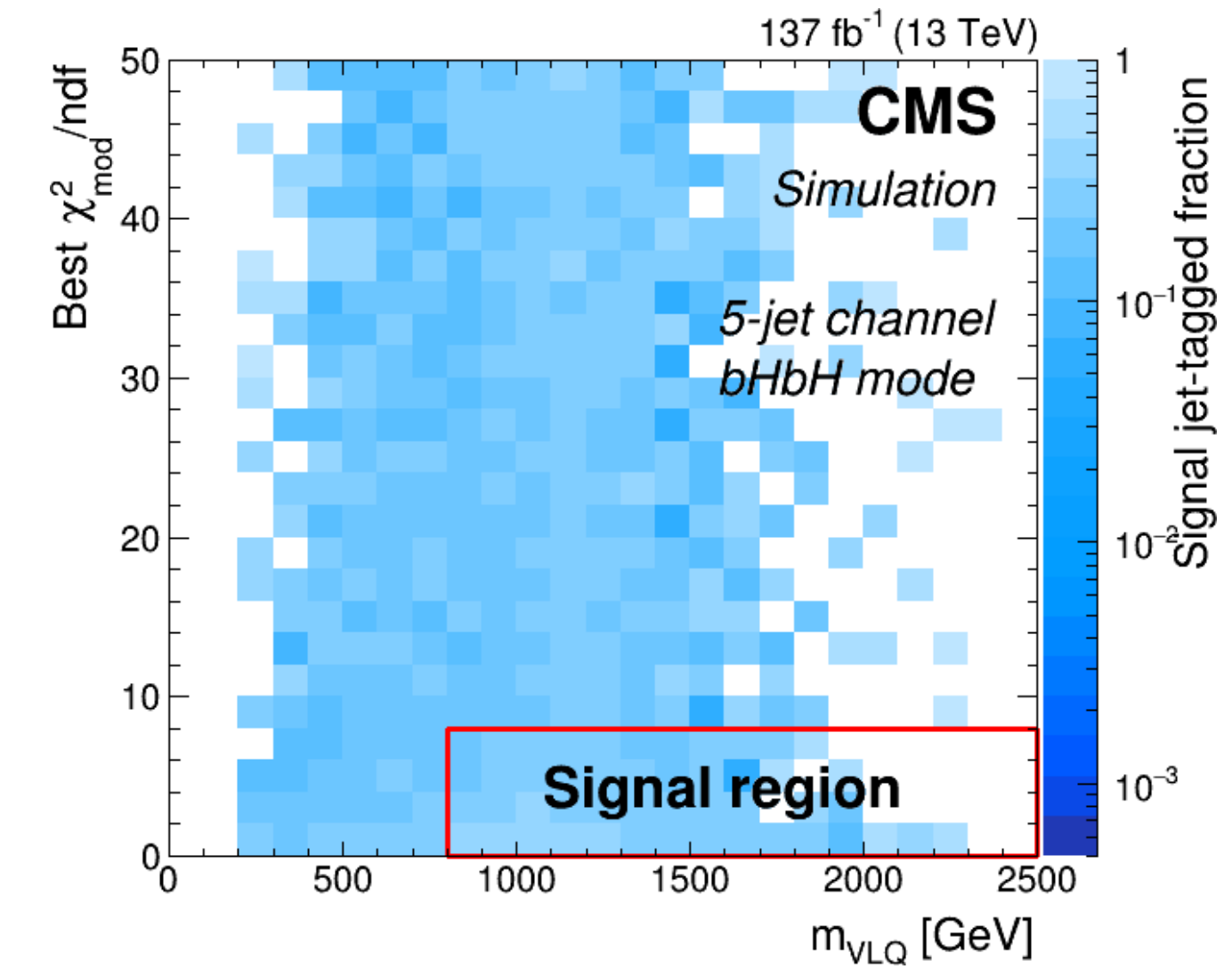


Note: Can also make Rivet analysis available



# Digitised results?

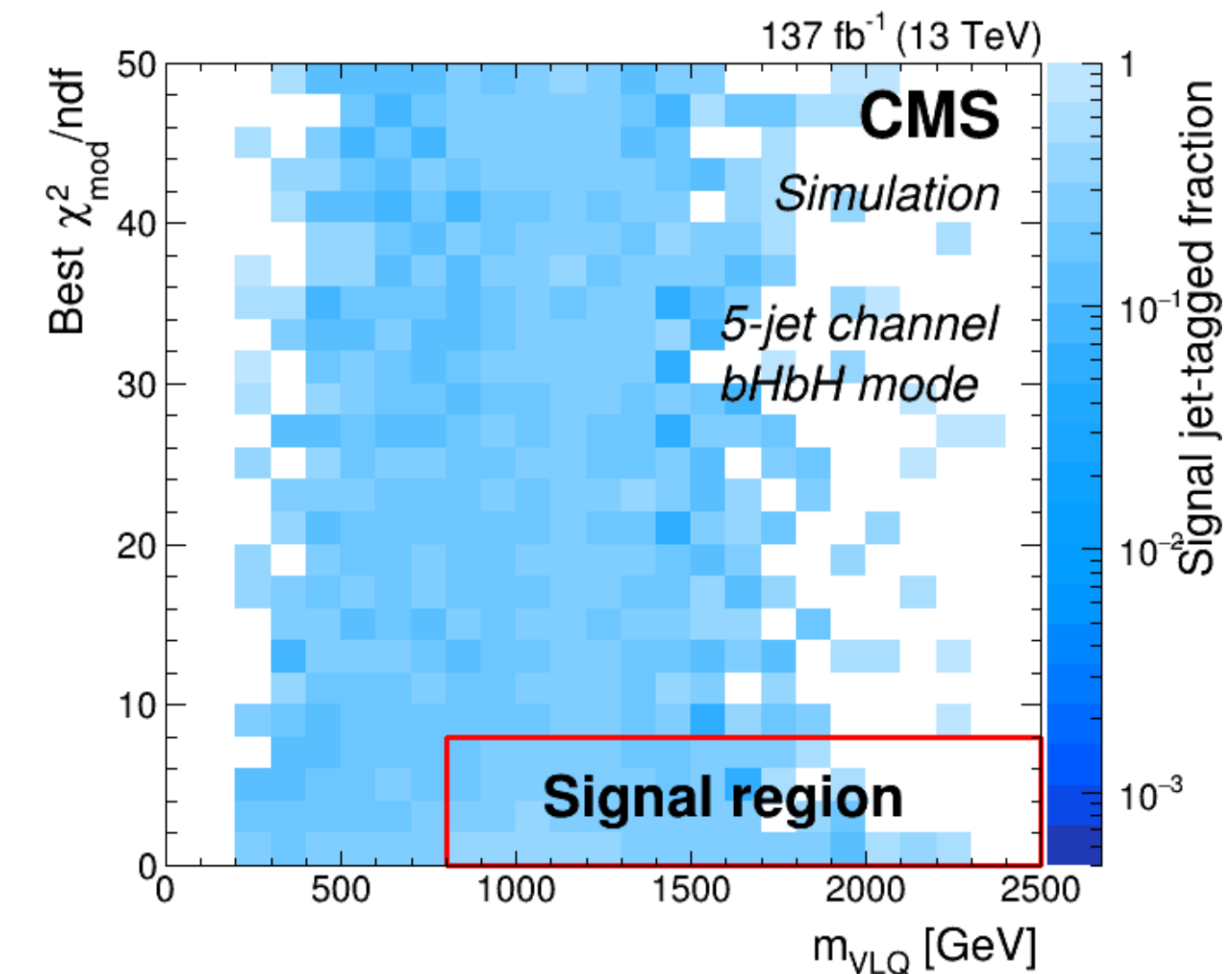
- The figures that are part of a paper are published as images
- Reading off values can be tedious
  - Note: There are tools such as [WebPlotDigitizer](#) that help with that



Note: Can also make Rivet analysis available

# Digitised results?

- The figures that are part of a paper are published as images
- Reading off values can be tedious
  - Note: There are tools such as [WebPlotDigitizer](#) that help with that
- Better: Provide digitised versions of plots and tables
  - Analyst most likely the only person with those at hand
- For High Energy Physics: [HEPData portal](#)
  - Use e.g. [hepdata\\_lib](#) Python library to create a submission

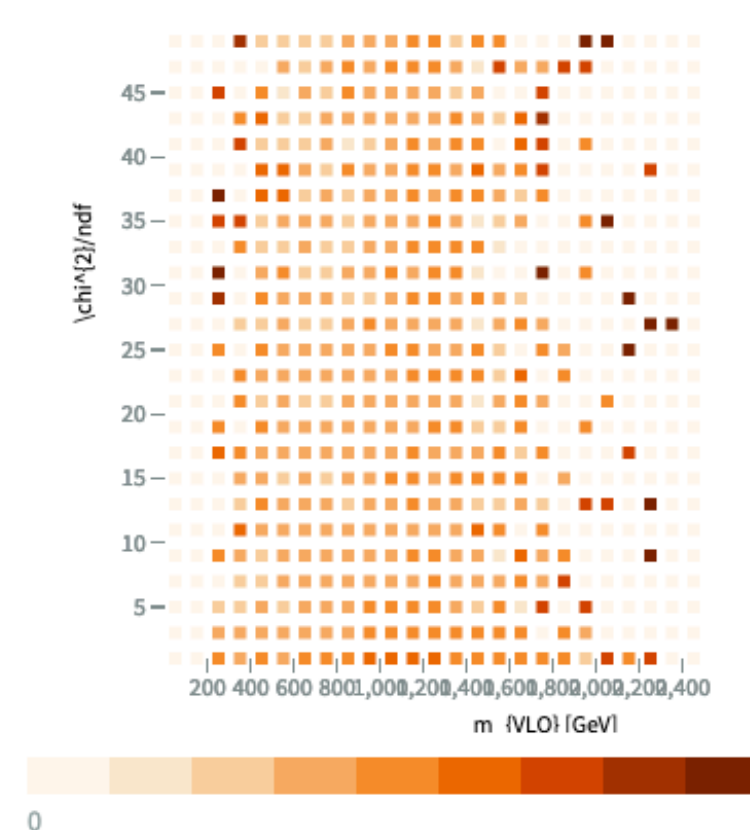


Showing 50 of 625 values

[Show All 625 values](#)

Visualize

SQRT(S)		13 TeV
LUMINOSITY		137 fb <sup>-1</sup>
$m_{VLQ}$ [GeV]	$\chi^2/\text{ndf}$	Jet Tag Efficiency
50.0	1.0	0.0
50.0	3.0	0.0
50.0	5.0	0.0
50.0	7.0	0.0
50.0	9.0	0.0
50.0	11.0	0.0
50.0	13.0	0.0



Note: Can also make Rivet analysis available

# Digitised results?

- > The figures that are part of a paper are published as images
- > Reading off values can be tedious

- Note: There are tools such as [WebPlotDigitizer](#) that help with that

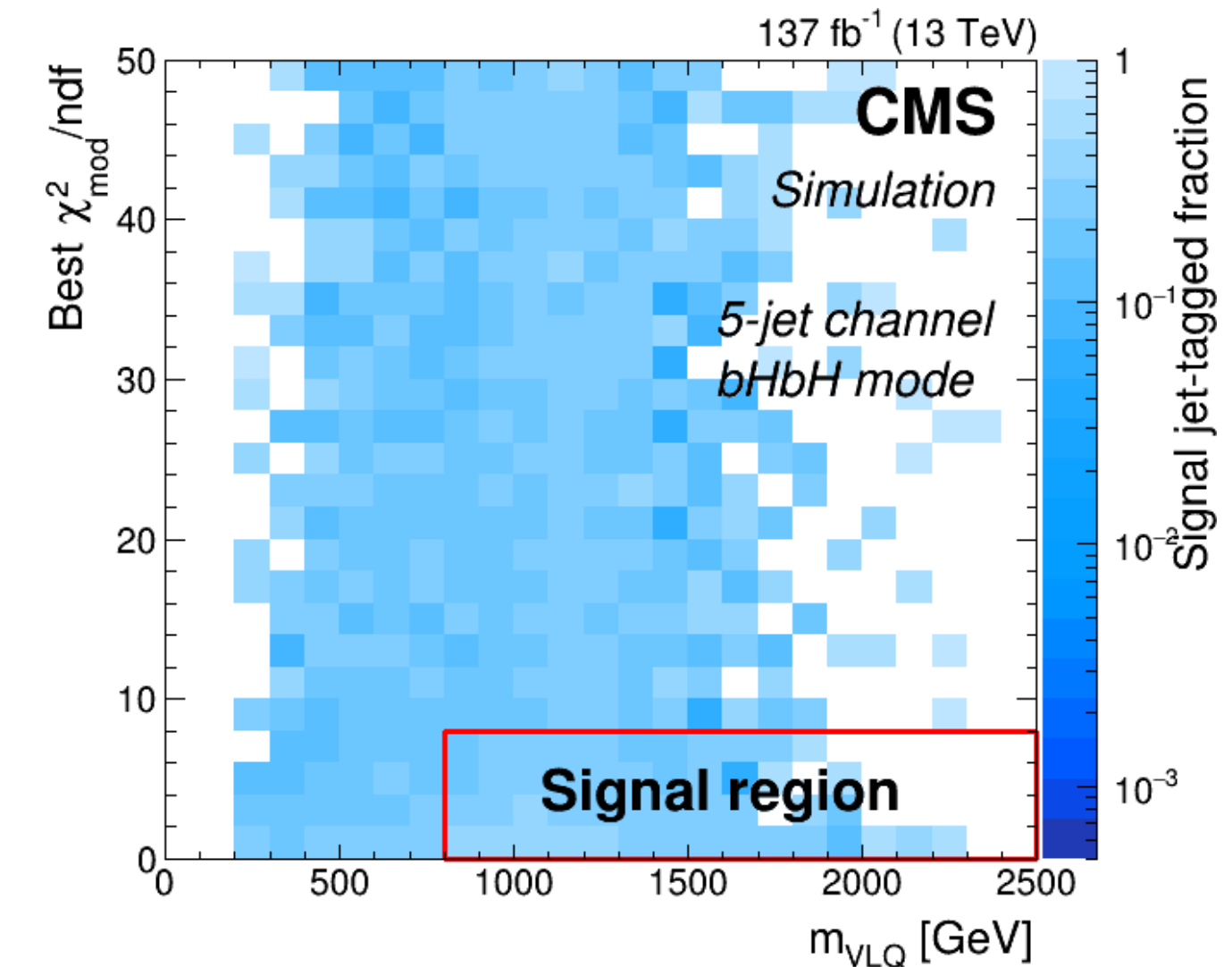
- > Better: Provide digitised versions of plots and tables

- Analyst more comfortable with those at hand

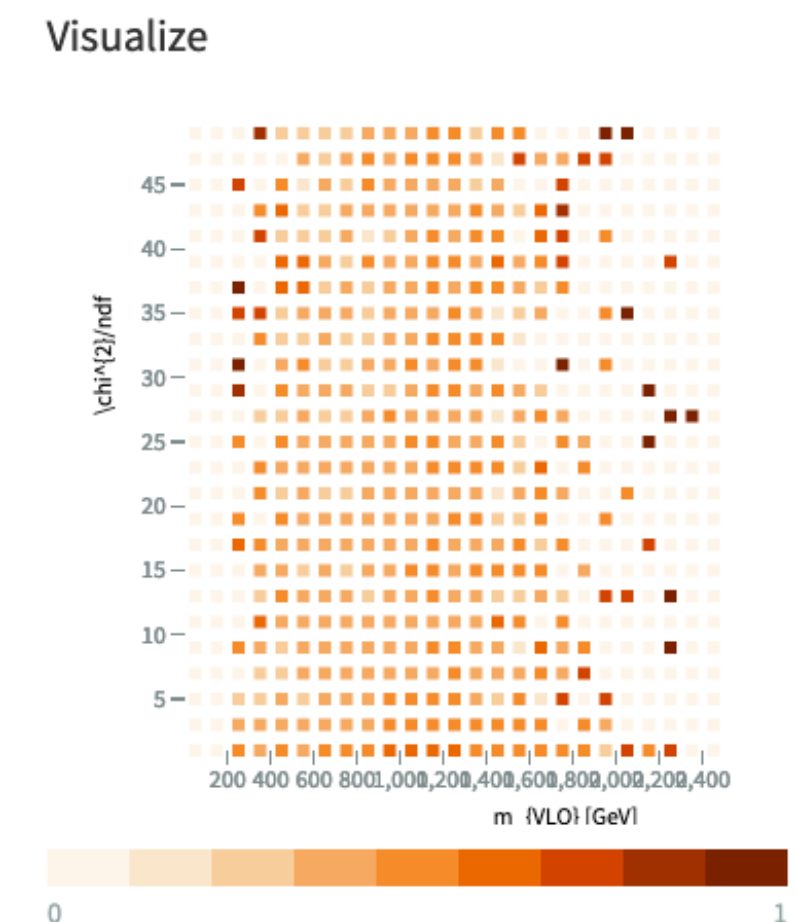
Anyone can reproduce the plot!

- > For High Energy Physics: [HEPData portal](#)

- Use e.g. [hepdata\\_lib](#) Python library to create a submission

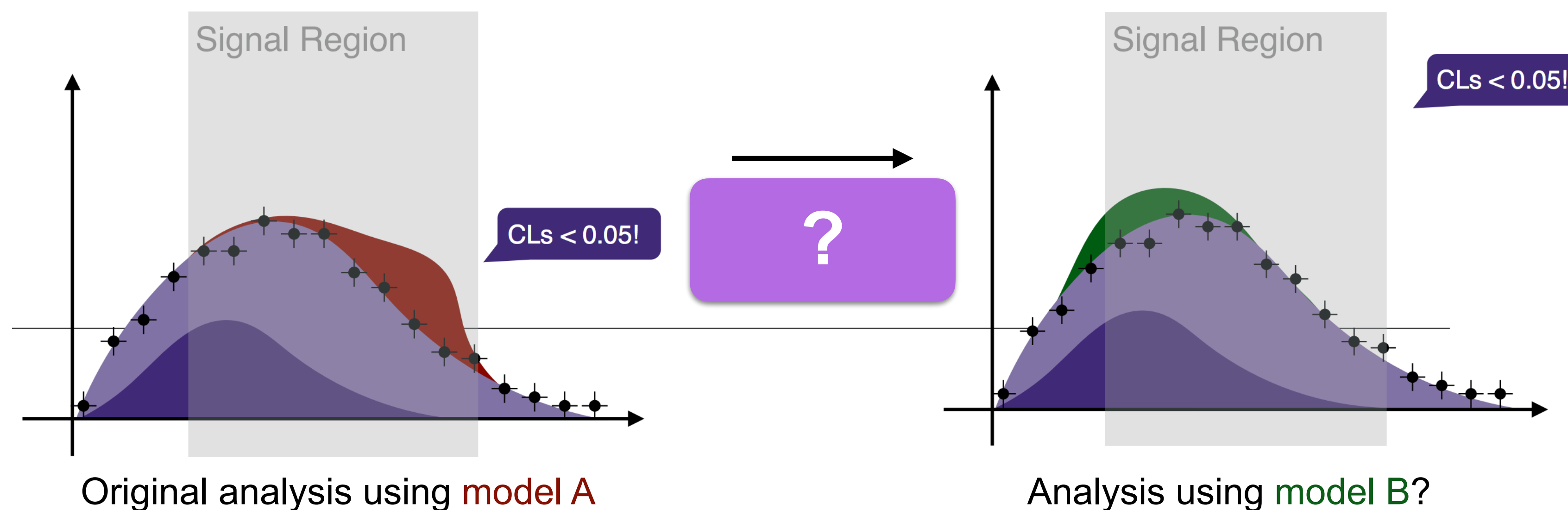


$m_{\text{VLQ}}$ [GeV]	$\chi^2_{\text{mod}} / \text{ndf}$	Signal jet-tagged fraction
50.0	1.0	0.0
50.0	3.0	0.0
50.0	5.0	0.0
50.0	7.0	0.0
50.0	9.0	0.0
50.0	11.0	0.0
50.0	13.0	0.0

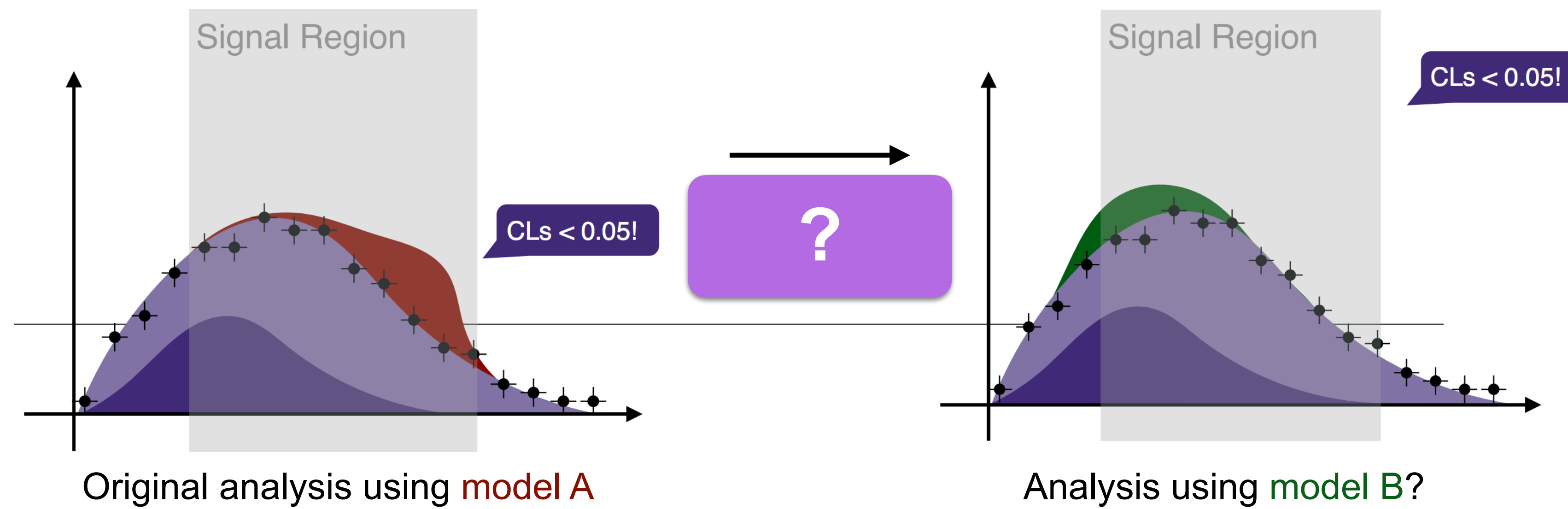


Note: Can also make Rivet analysis available

- > We try to interpret our experimental results in a breadth of theoretical models and frameworks
- > However:
  - New models are continuously being developed and could be quite different
  - There can be surprises in the data that “motivate” to take another look (remember the 2015  $\gamma\gamma$  excess?)



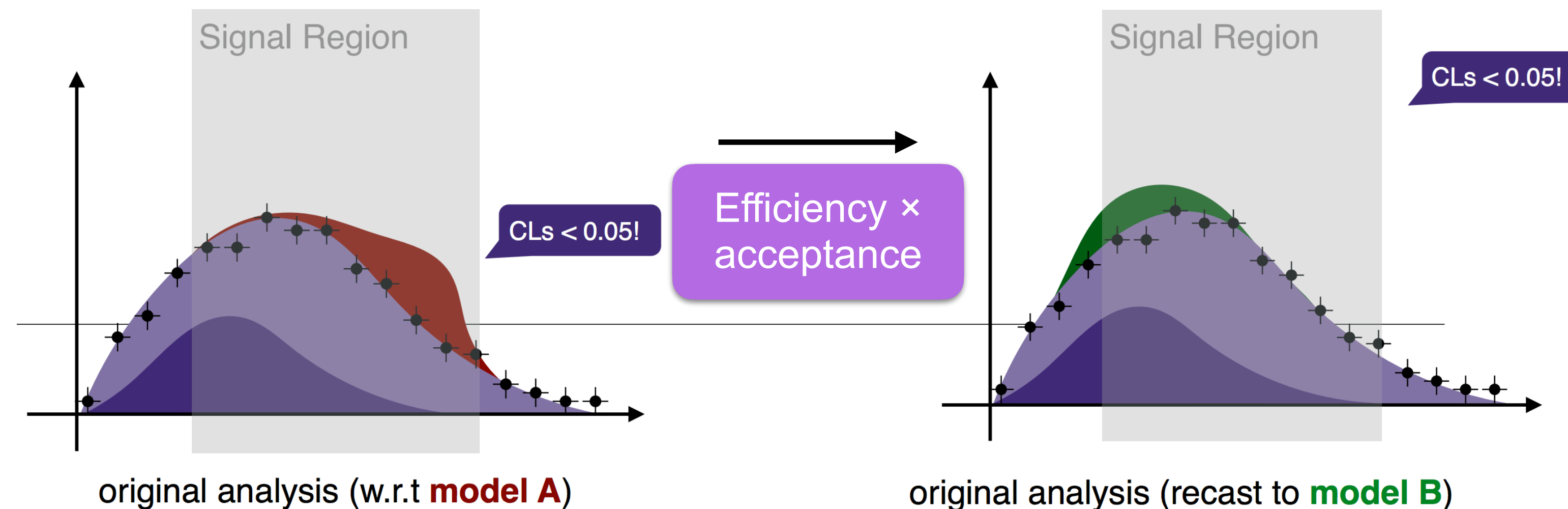
- > We try to interpret our experimental results in a breadth of theoretical models and frameworks
- > However:
  - New models are continuously being developed and could be quite different
  - There can be surprises in the data that “motivate” to take another look (remember the 2015  $\gamma\gamma$  excess?)



How to make sure a reinterpretation is possible?

# Preparing for reinterpretation

- > A new theory model only changes the posited signal, less often the background processes
  - Do not need to process the data and backgrounds again
  - Probably background model won't have to be changed either
- > Need to estimate new signal's selection efficiency  $\times$  acceptance
  - Does the paper publication contain enough information to do that?
- > Optimal approach: preserve overall analysis setup



# Tools for preservation and reusability

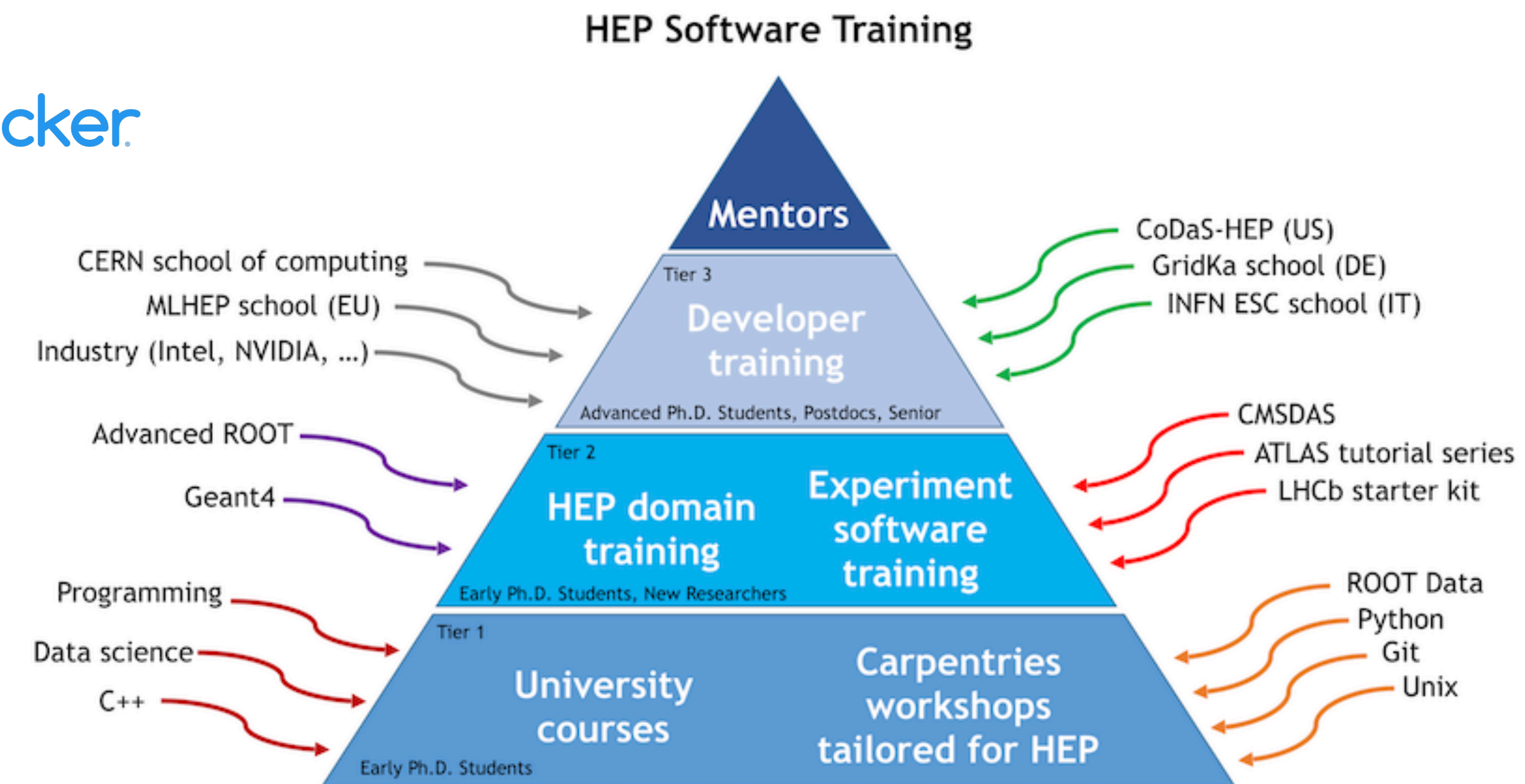
## > Tools for preservation/reusability:

- Version-controlled software (Git) including automated checks **git**
- Containerised software images (Docker) **docker**
- Automated workflows

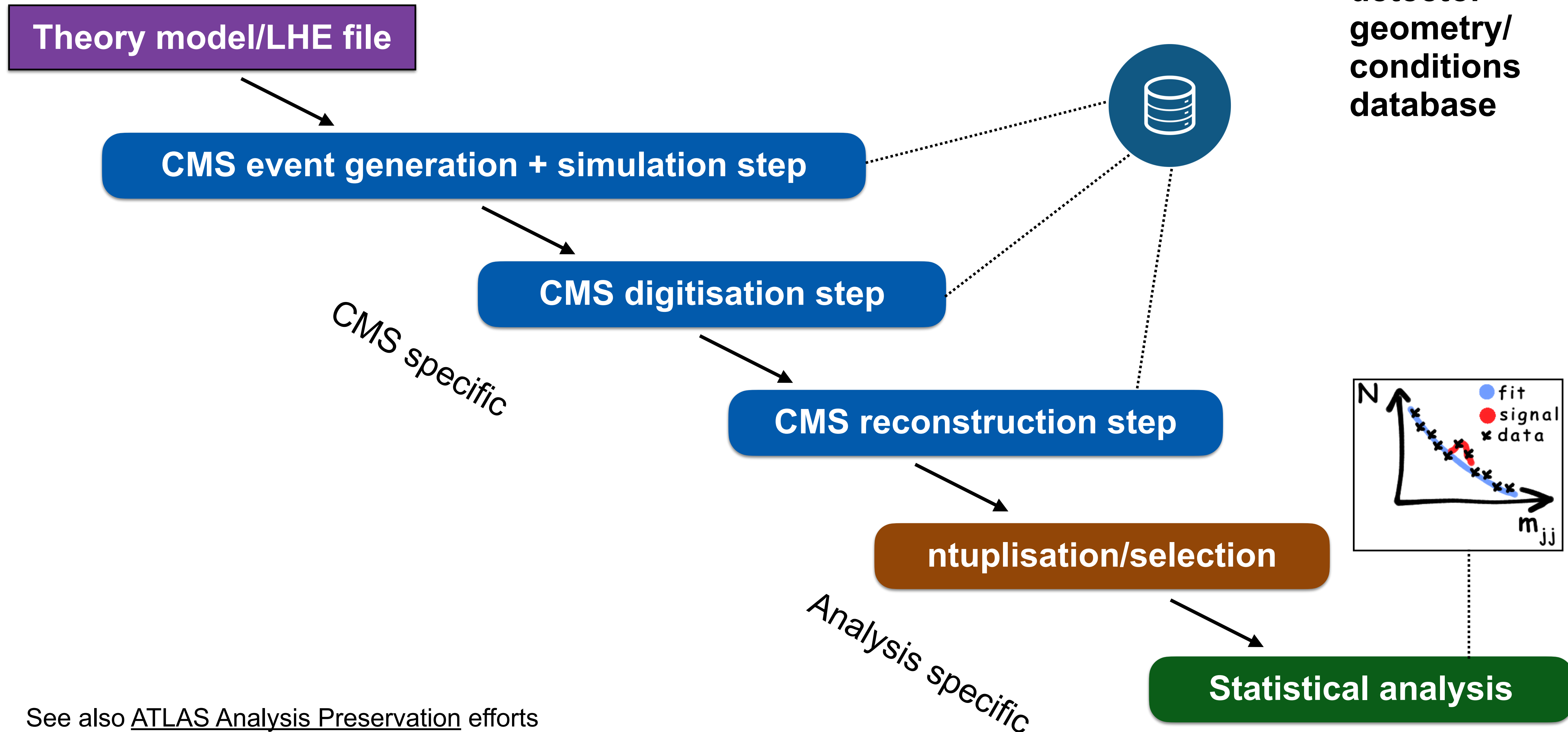
## > Training available via HEP Software Foundation, LPC hands-on training sessions (HATS), experiment-specific trainings

## > Tools being developed at CERN:

- CERN Analysis Preservation Portal
- REANA (Reusable analysis platform)



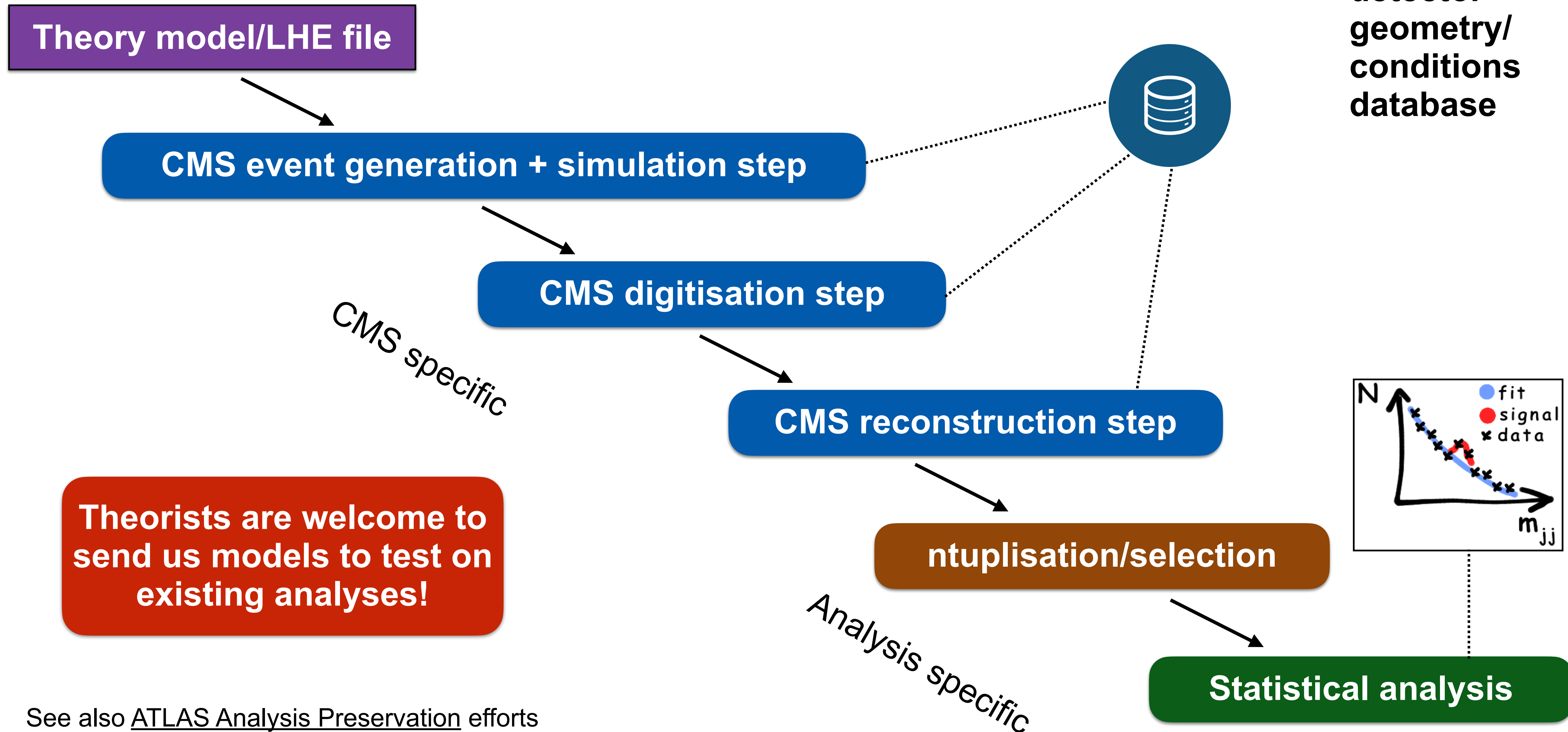
# Performing a reinterpretation



See also [ATLAS Analysis Preservation](#) efforts

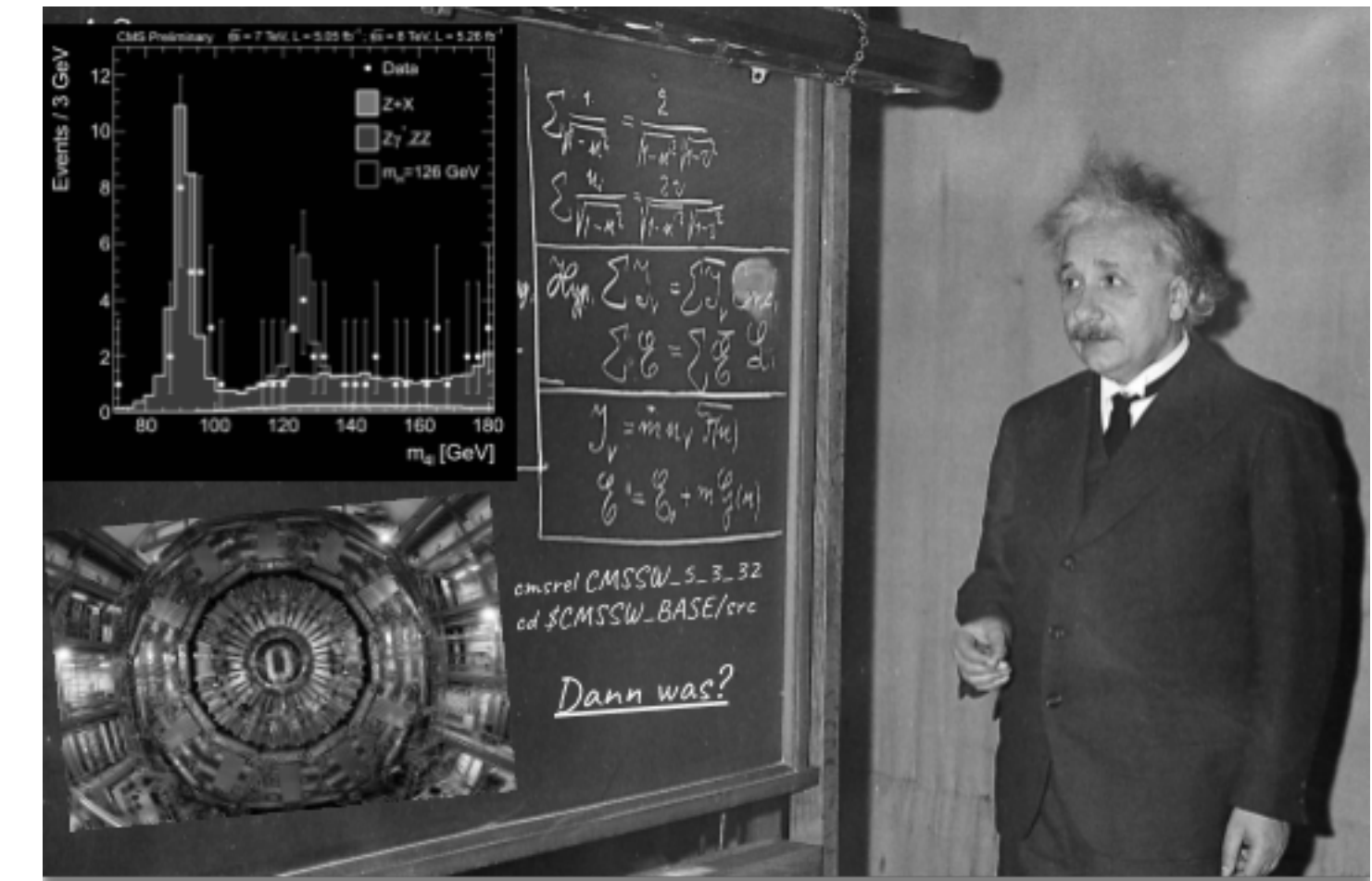


# Performing a reinterpretation

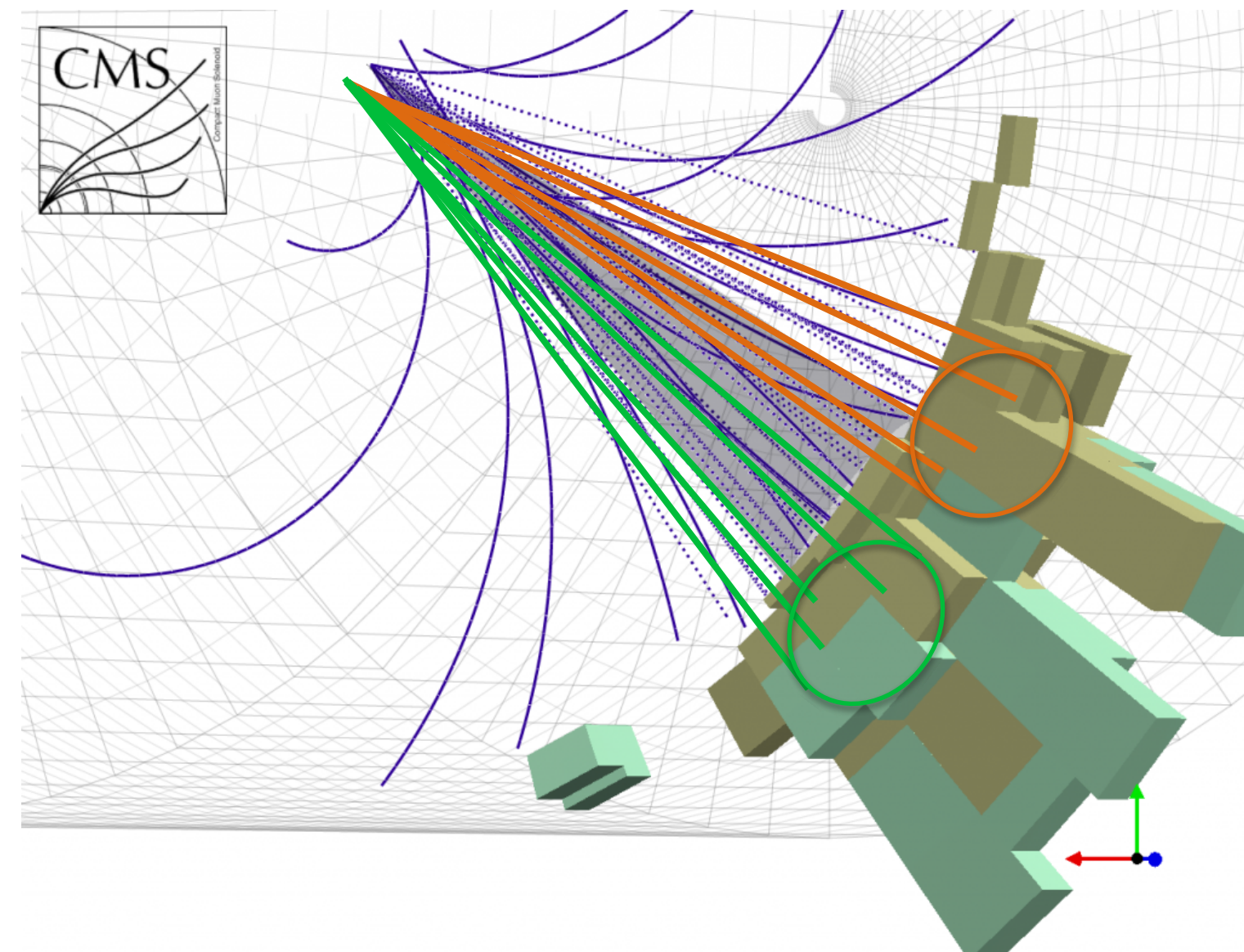


See also [ATLAS Analysis Preservation](#) efforts

- > Theorists (and anyone else) can also use CMS data
- > More than 2 PB available (mostly Run-1) from the CERN Open Data Portal
- > Using the data can be a challenge
  - Training available through CMS Open Data Workshop for Theorists (Sep/Oct 2020)
  - Includes using public cloud offerings for large-scale data analysis



- > More good news: New Open Data policy by the LHC experiments
  - All experiments will make data for scientific use available starting five years after data taking

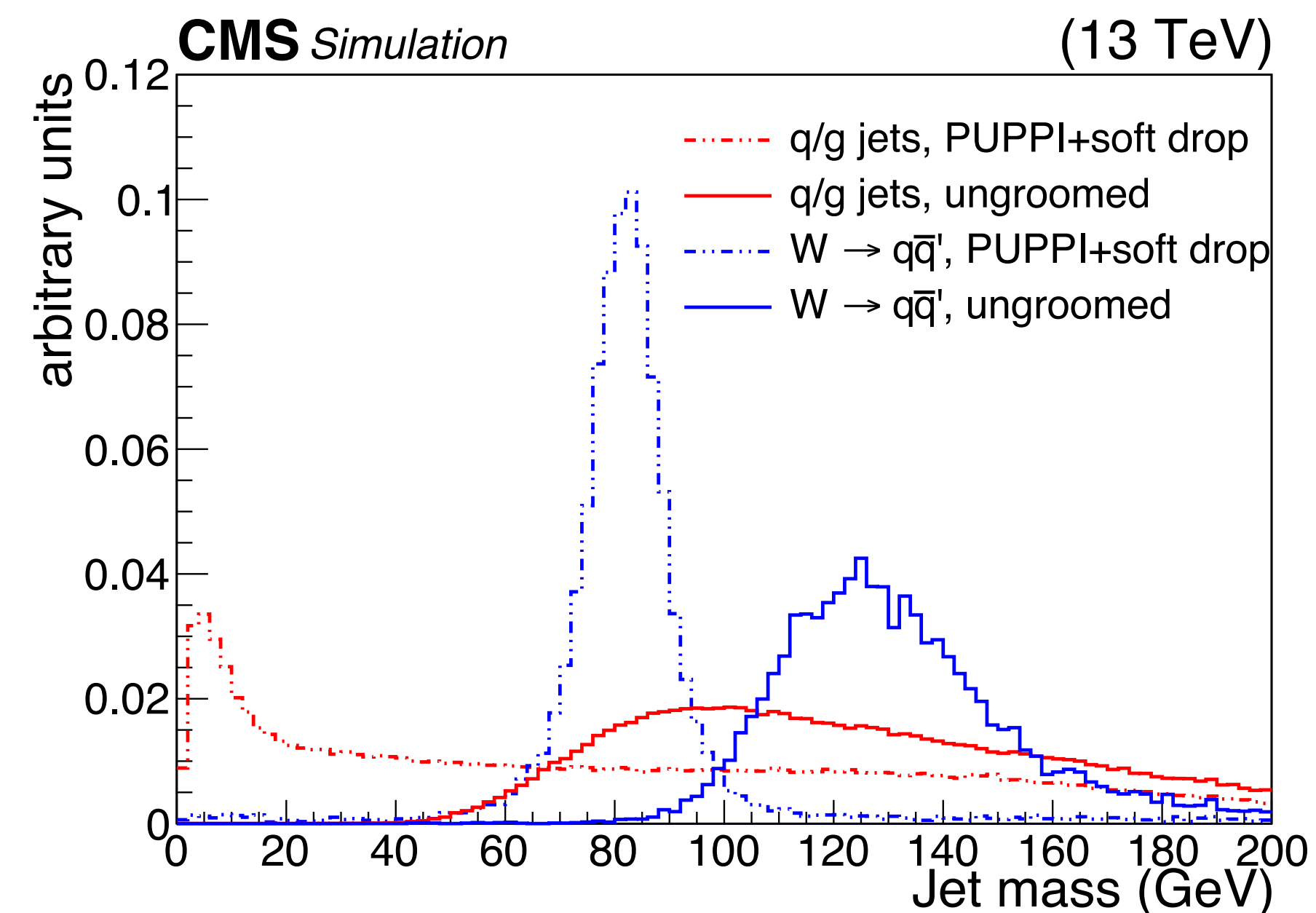


- Jet substructure enables the search for extremely rare and heavy resonances
- Several new CMS analyses using 2016-18 data becoming public pushing the boundaries
  - Only presented the latest two results
- Performing reusable analyses has a long-term impact on the field

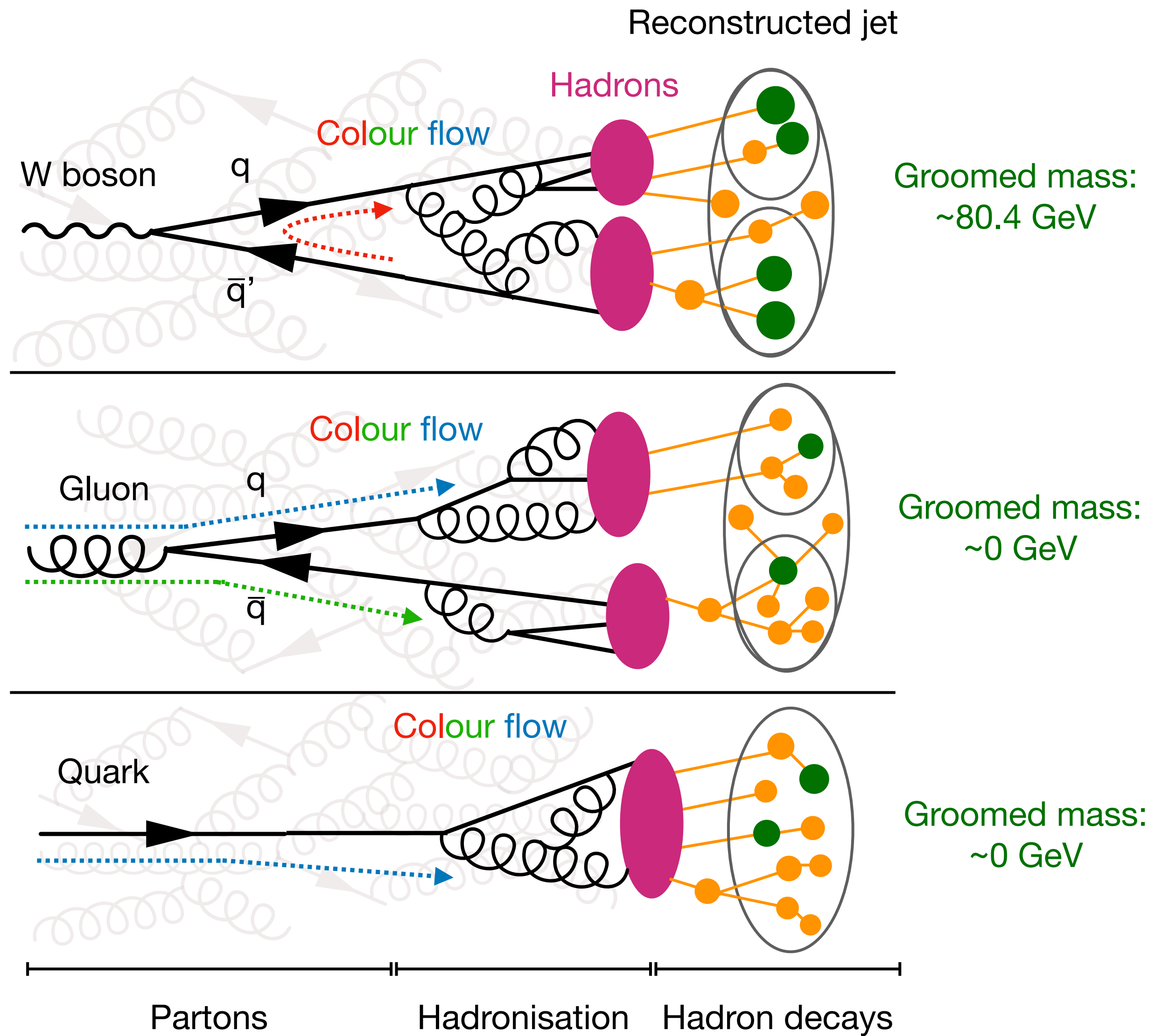


# Example: “modified mass-drop tagger”

- > Recluster jet constituents using Cambridge-Aachen jet algorithm (based on **spatial separation** only)
- > Iteratively break into two subjets
- > Remove softer contribution (and continue with harder one) if:
 
$$\frac{\min(p_{T_1}, p_{T_2})}{p_{T_1} + p_{T_2}} < 0.1 \text{ (CMS choice)}$$
- > Stop otherwise



# Undoing hadronisation



# Search for bottom-type, vector-like quark pair production

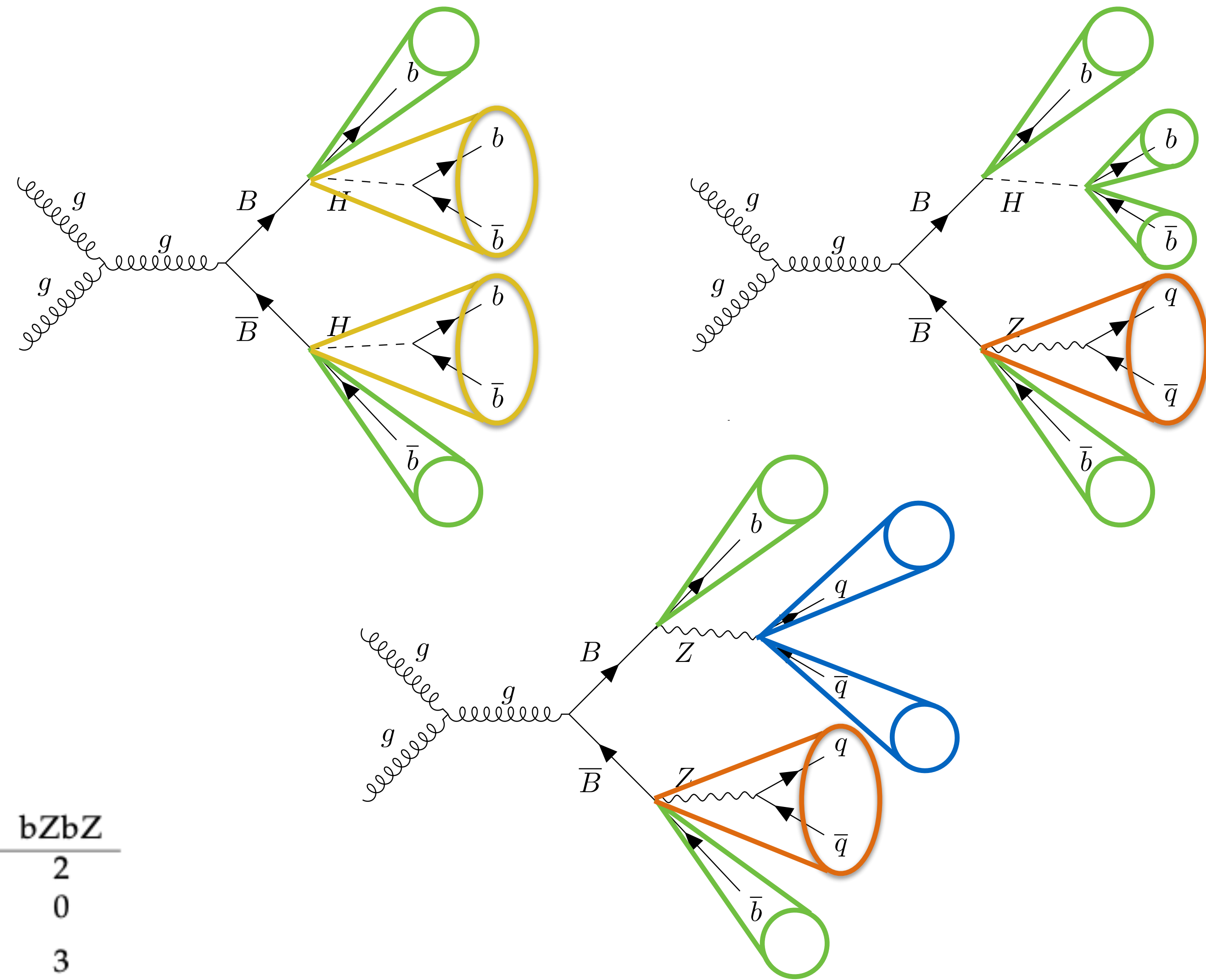
## > Topology:

- Each B decays to a b quark and a Z or Higgs boson
- Investigate  $H \rightarrow bb$  and  $Z \rightarrow qq$  (incl.  $bb$ )

## > Selection:

- Select at least 4 AK4 jets,  $p_T > 30$  GeV
- If AK8 jet ( $p_T > 200$  GeV) exists close to AK4 jet ( $\Delta R < 0.3$ ) and sufficiently far from a second AK4 jet ( $\Delta R > 0.6$ ), use AK8 jet instead
- Use DeepJet b tag algorithm for AK4 jets
- Double-b tagger (incl. substructure info) for AK8 jets

Jet multiplicity	Tag	bHbH	bHbZ	bZbZ
4 jets	Single b	2	2	2
	Double b	1	1	0
5 jets	Single b	3	3	3
	Double b	0	0	0
6 jets	Single b	4	4	3

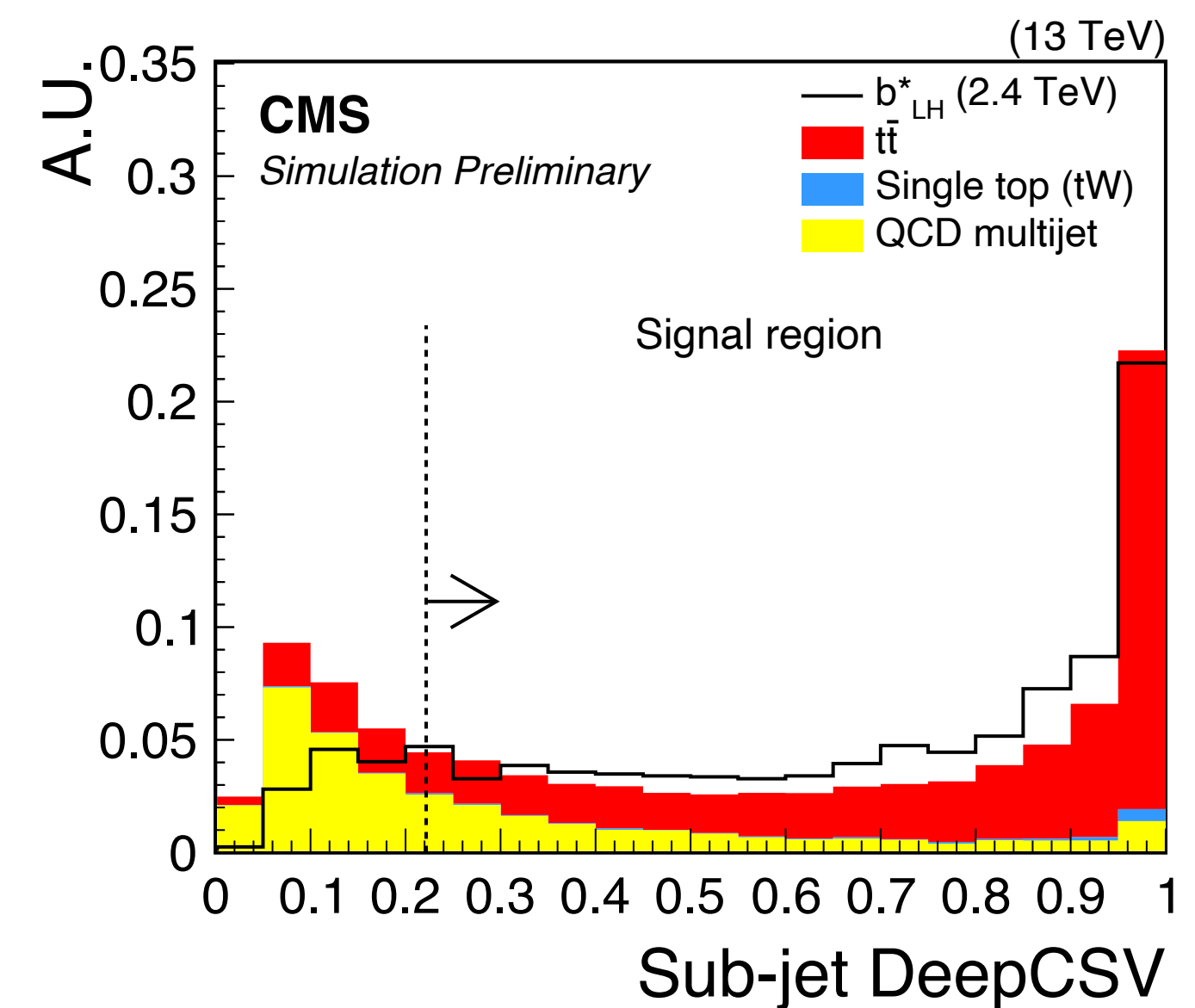
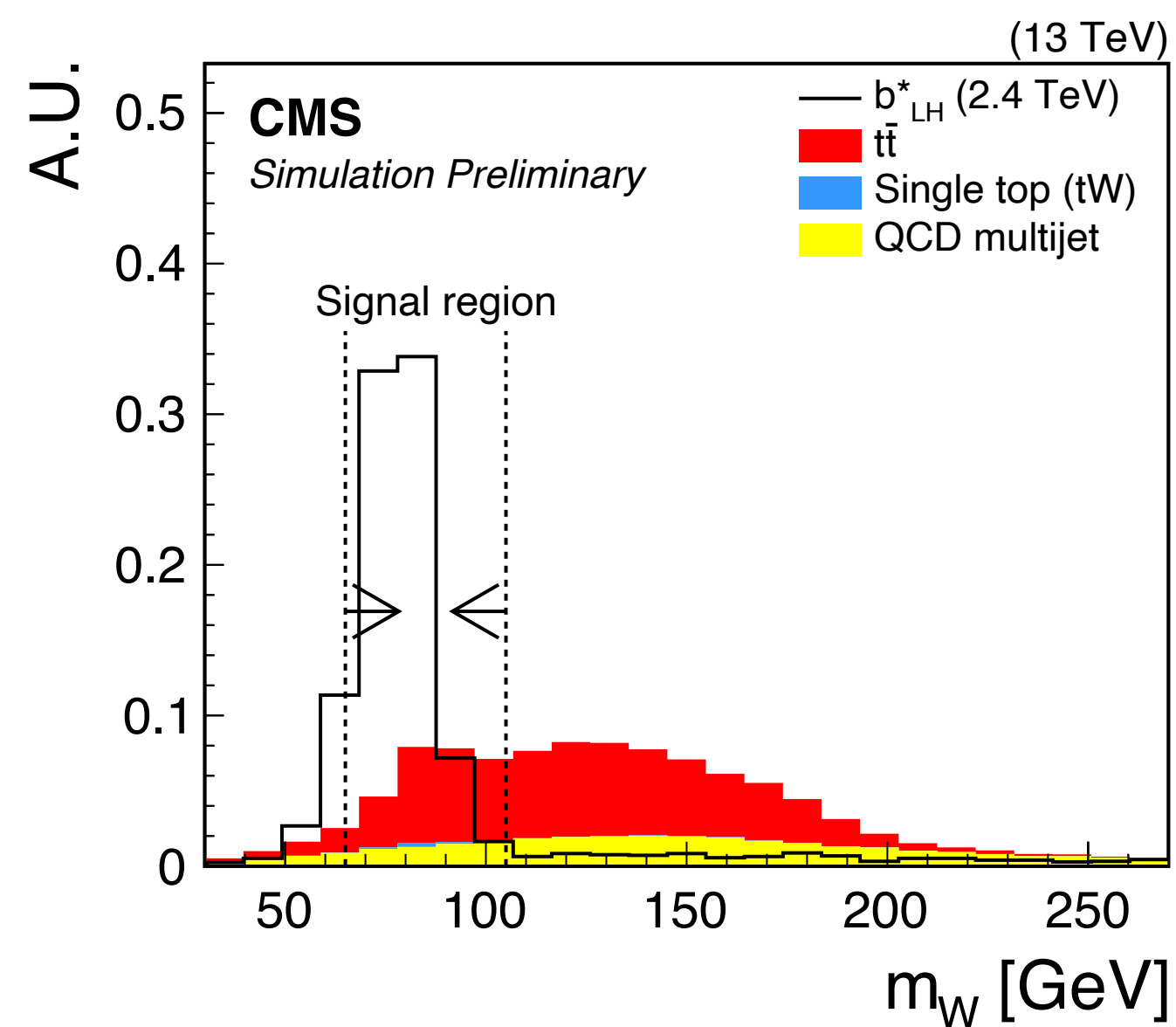
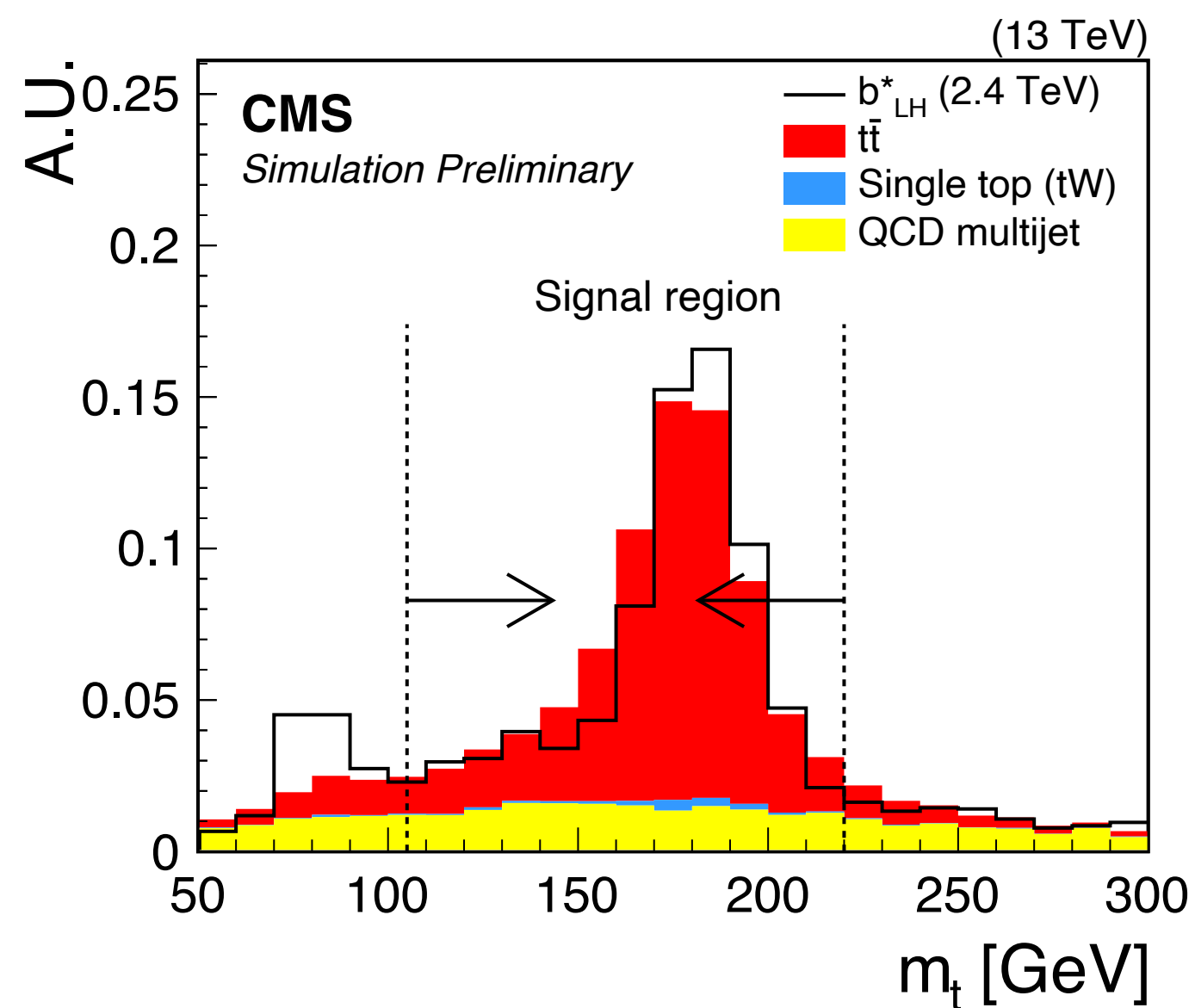
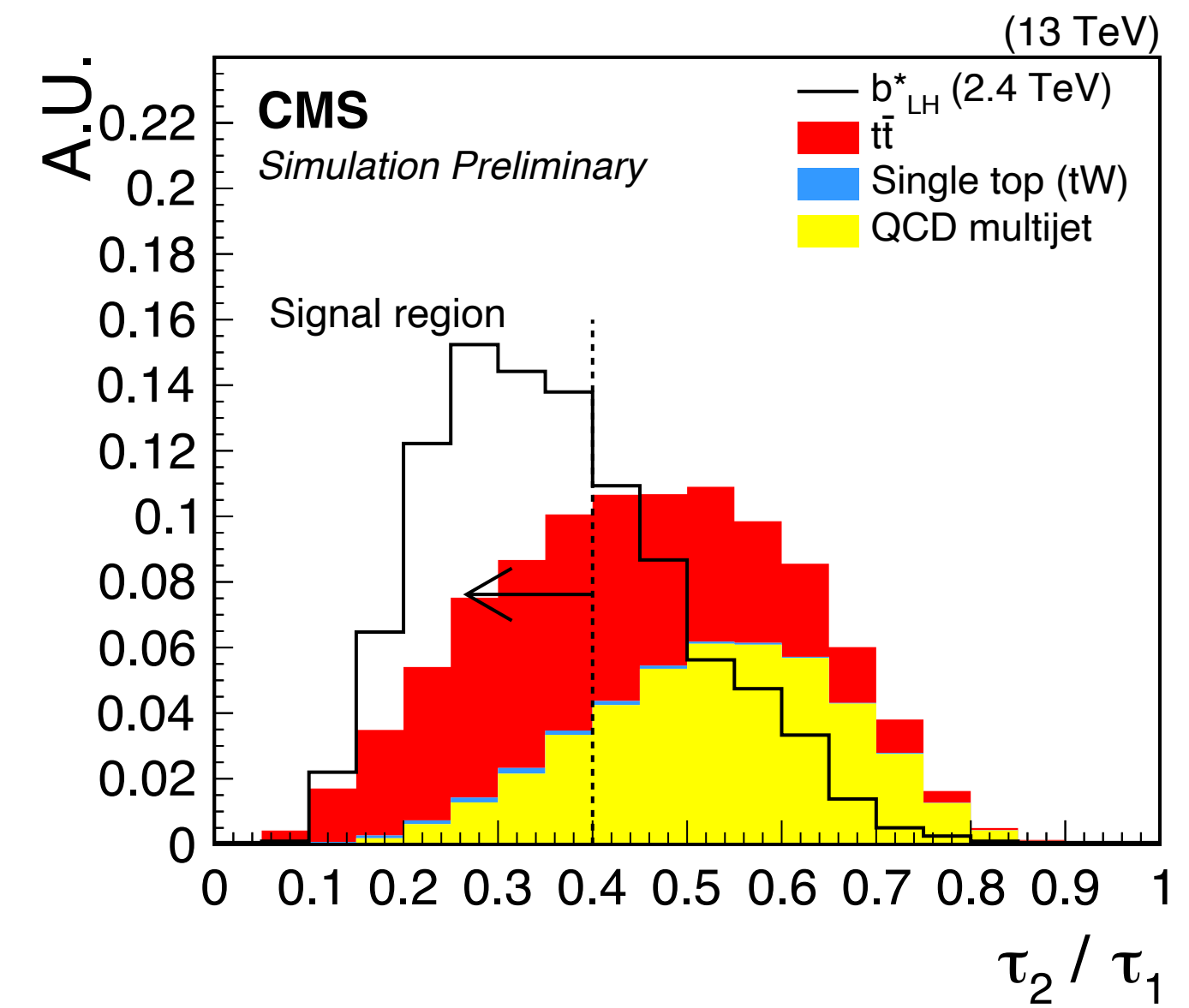
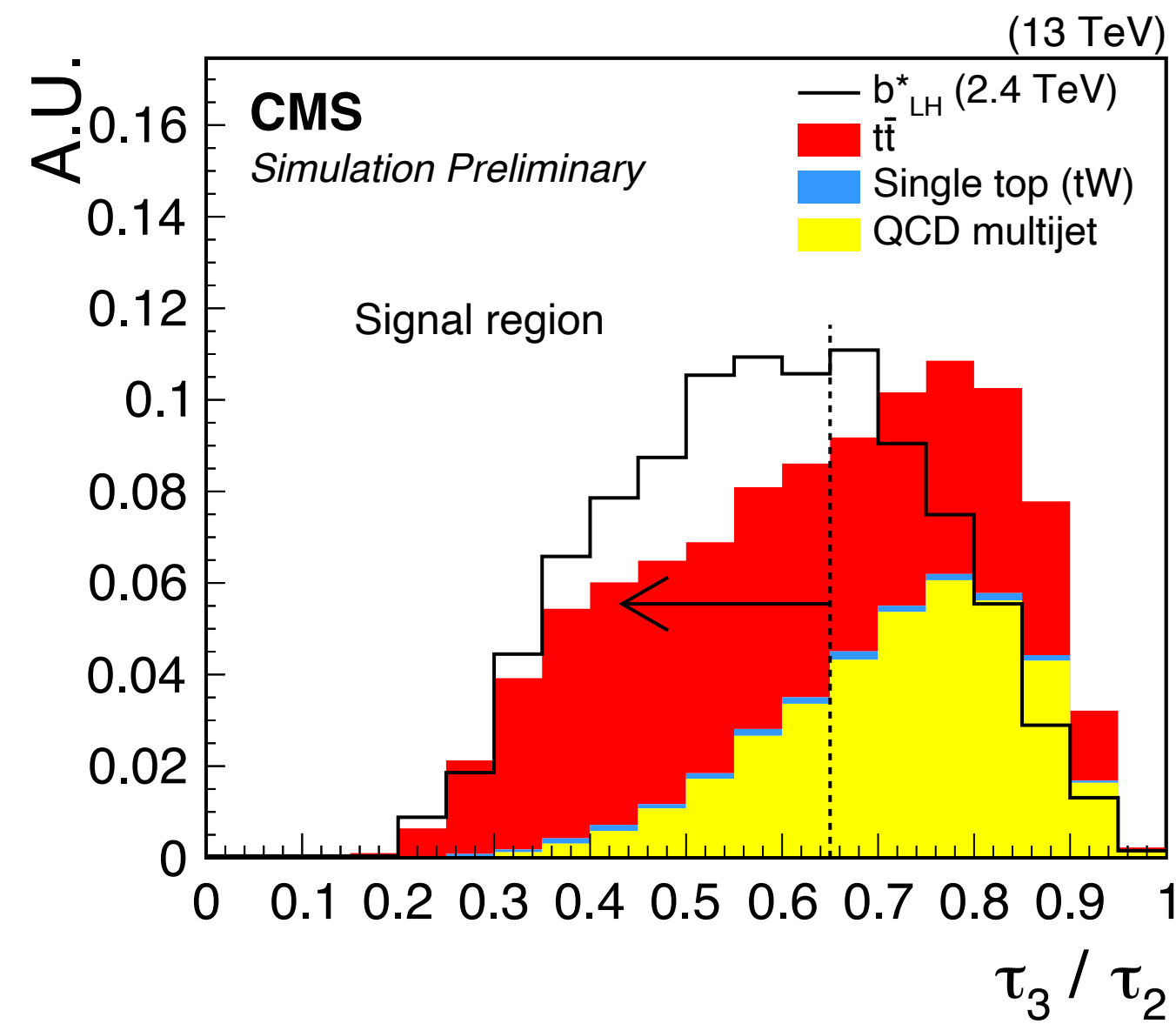
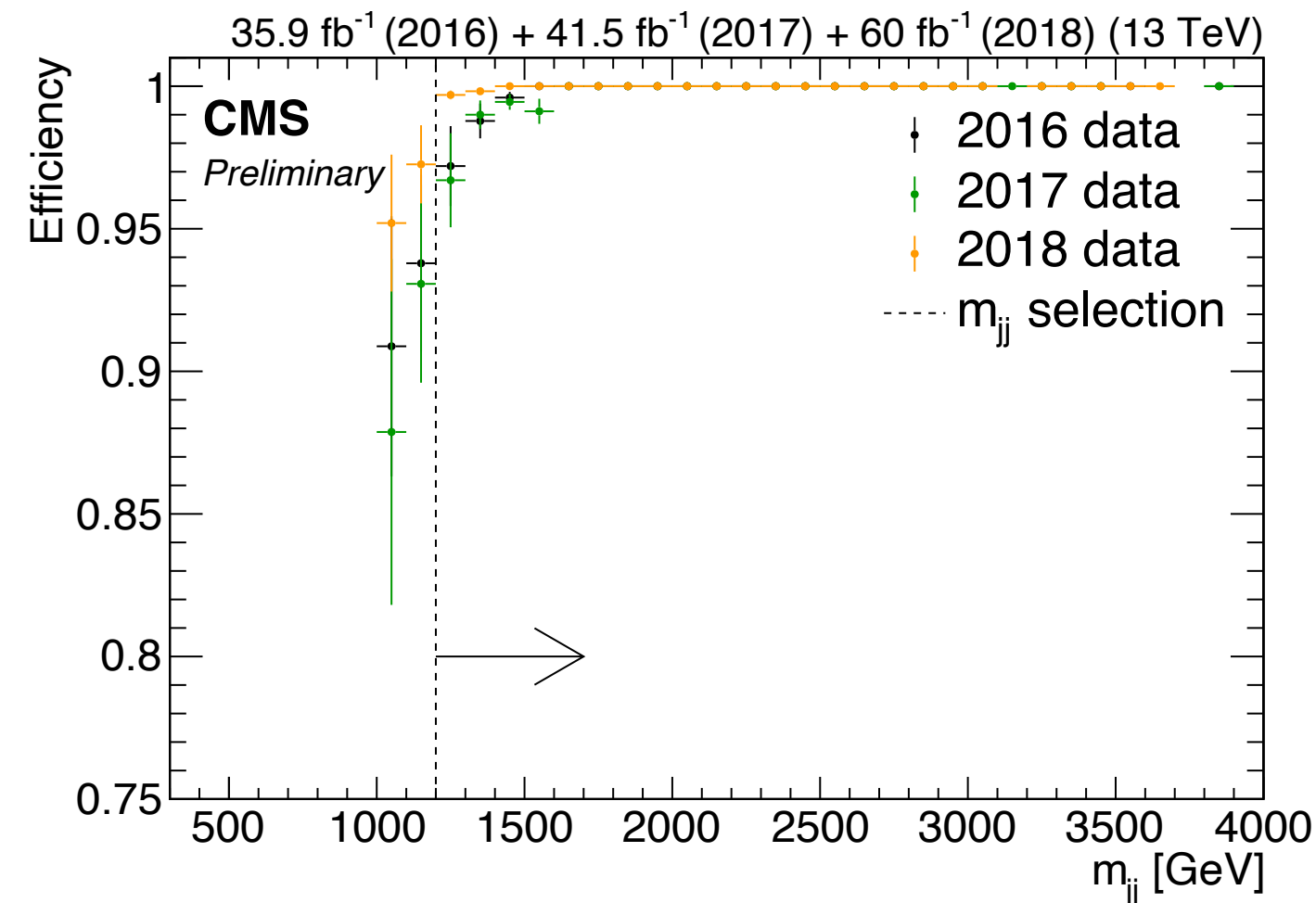


# Search for $W' \rightarrow tb$ : uncertainties

Systematic source	Correlation between different years	Impact
Luminosity	No correlation	0.5%
$t\bar{t}$ cross section	Full correlation	0.1%
Single top cross section	Full correlation	0.2%
JES	No correlation	0.8%
JER	No correlation	< 0.1%
B tagging scale factor	No correlation	< 0.1%
top quark tagging scale factor	No correlation	0.2%
Pileup	Full correlation	< 0.1%
Prefire correction	No correlation	< 0.1%
$t\bar{t}$ normalization and slope	No correlation	0.2%
Scale ( $\mu_R$ and $\mu_F$ )	Full correlation	0.3%
PDF	Full correlation	< 0.1%
Pass-to-fail ratio	No correlation	0.2%
Alternative function of pass-to-fail ratio	No correlation	0.1%
Non-closure uncertainty	No correlation	0.3%
B candidate $m_{SD}$ correction	No correlation	0.9%



# Search for $b^* \rightarrow tW$ : additional plots



# Search for $b^* \rightarrow tW$ : uncertainties

Source	Uncertainty	Samples	Impact (up/down)
$t\bar{t}$ cross section	$\pm 20\%$	$t\bar{t}$	-4.6/ +4.4%
Single top cross section	$\pm 30\%$	single top	+1.2/ -1.4%
Integrated Luminosity	$\pm 1.8\%$	$t\bar{t}$ , single top, signal	+1.6/ -1.1%
Pileup	Shape ( $\sigma_{mb}$ )	$t\bar{t}$ , signal, single top	+0.3/ -0.2%
Prefire	Shape ( $p_T, \eta$ )	$t\bar{t}$ , signal, single top	+0.0/ +0.1%
Jet energy scale	Shape ( $p_T$ )	$t\bar{t}$ , signal, single top	+0.3/ -0.6%
Jet energy resolution	Shape ( $p_T, \eta$ )	$t\bar{t}$ , signal, single top	-0.4/ -0.5%
Jet mass scale	Shape ( $m_W$ )	$t\bar{t}$ , signal, single top	-0.1/ -0.0%
Jet mass resolution	Shape ( $m_W$ )	$t\bar{t}$ , signal, single top	+0.0/ +0.9%
W tagging	Shape ( $p_T$ )	signal, single top	+0.9/ -0.9%
W tagging: $p_T$ extrapolation	Shape ( $p_T$ )	signal, single top	+4.9/ -4.9%
Top tagging, merged	Shape ( $p_T$ )	$t\bar{t}$ , signal, single top	+0.2/ -0.2%
Top tagging, semimerged	Shape ( $p_T$ )	$t\bar{t}$ , signal, single top	+1.1/ -0.9%
Top tagging, not merged	Shape ( $p_T$ )	$t\bar{t}$ , signal, single top	-0.1/ +0.1%
Trigger	Shape ( $H_T$ )	$t\bar{t}$ , signal, single top	+0.3/ -0.4%
Top quark $p_T$ correction - $\alpha$	Shape ( $p_T$ )	$t\bar{t}$	-0.3/ +0.3%
Top quark $p_T$ correction - $\beta$	Shape ( $p_T$ )	$t\bar{t}$	-3.9/ +3.5%
PDF	Shape ( $m_t, m_{tW}$ )	signal	+0.1/ -0.1%
KDE bandwidth	Shape ( $m_t, m_{tW}$ )	multijet (from simulation)	-1.2/ +0.2%
$R_{\text{ratio}}(m_t, m_{tW})^{SR} p_0$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	-4.4/ +0.0%
$R_{\text{ratio}}(m_t, m_{tW})^{SR} p_1$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	-2.0/ +2.2%
$R_{\text{ratio}}(m_t, m_{tW})^{SR} p_2$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	+0.9/ -0.8%
$R_{\text{ratio}}(m_t, m_{tW})^{SR} p_3$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	+18.6/ -18.8%
$R_{\text{ratio}}(m_t, m_{tW})^{t\bar{t}} p_0$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	-0.4/ +0.6%
$R_{\text{ratio}}(m_t, m_{tW})^{t\bar{t}} p_1$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	-0.4/ +0.6%
$R_{\text{ratio}}(m_t, m_{tW})^{t\bar{t}} p_2$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	+0.5/ -0.6%
$R_{\text{ratio}}(m_t, m_{tW})^{t\bar{t}} p_3$	Shape ( $m_t, m_{tW}$ )	multijet (from data)	-0.6/ +0.6%