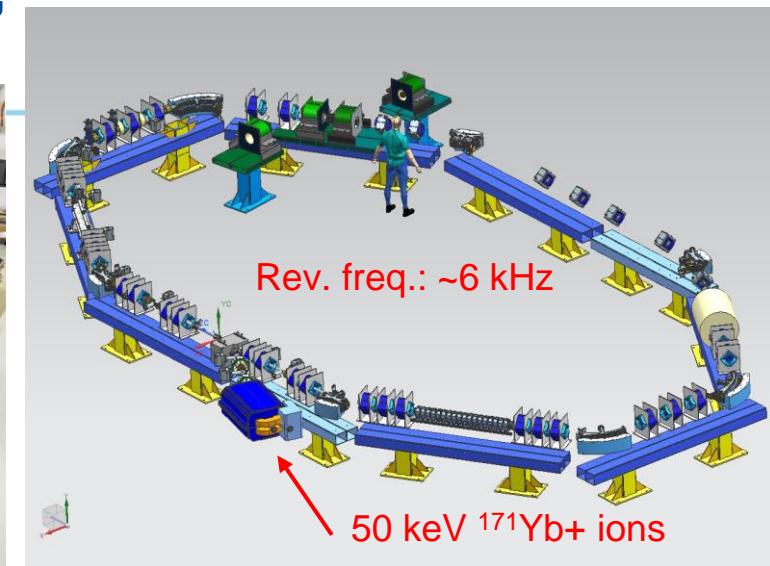
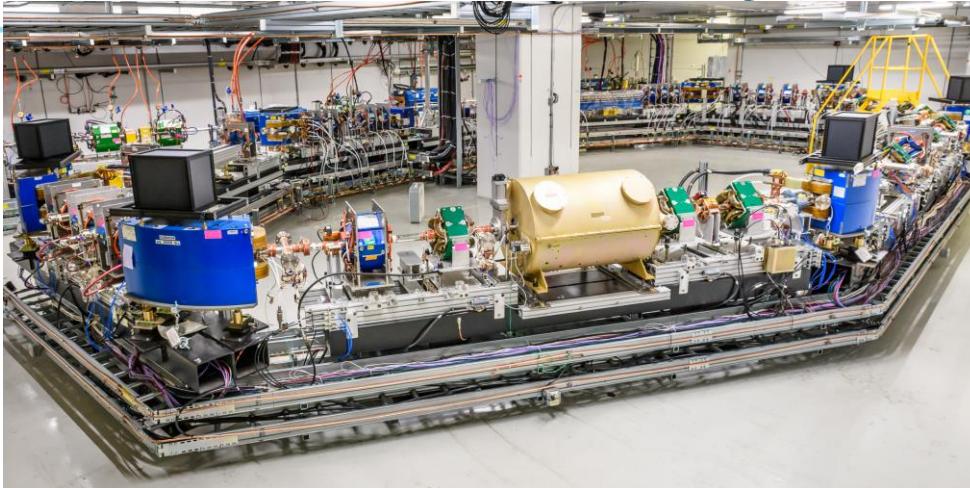

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Ion coulomb crystals in the Fermilab IOTA ring: lifetime estimates

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Fermilab IOTA ring (40-m circumference, 50 – 150 MeV/c momentum range)



- Present status: operating with relativistic electrons (~100-150 MeV)
- **This proposal:** add a 50-keV (120-MeV/c momentum) $^{171}\text{Yb}^+$ ion source, install counter-propagating lasers for Doppler laser cooling and extra ion diagnostics.

Basic parameters

Ions: $^{171}\text{Yb}^+$

$$A := 171 \quad M := 931.5 \quad T := 300 \quad k := 1.38 \cdot 10^{-23}$$

$$c := 3 \cdot 10^{10} \quad L := 4000 \text{ m -- IOTA circumference}$$

$$K := 50 \cdot 10^{-3} \quad \text{MeV -- kinetic energy}$$

$$\gamma := \frac{K + A \cdot M}{A \cdot M} \quad \beta := \sqrt{1 - \frac{1}{\gamma^2}}$$

$$\beta \cdot c = 2.377 \times 10^7 \text{ cm/s -- ion velocity}$$

$$\frac{\beta \cdot c}{L} = 5.943 \times 10^3 \text{ Hz}$$

$$\beta \cdot A \cdot M = 126.209 \text{ MeV/c}$$

$$\frac{K \cdot 10^6}{A} = 292.398 \text{ eV/amu -- kinetic energy per nucleon}$$

Charge-exchange cross section (example)

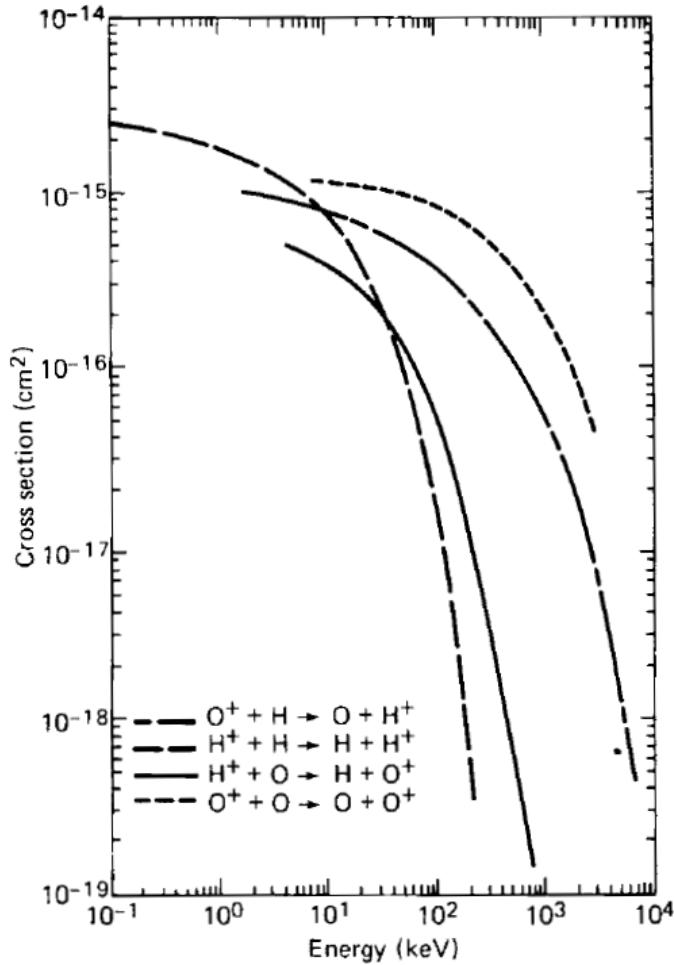


Fig. 1: Charge-exchange cross sections of energetic H⁺ and O⁺ ions as a function of total ion energy for electron pickup from cold neutral hydrogen and oxygen (figure is taken from a compilation by McEntire and Mitchell, 1989).

- From: Detection of Energetic Neutral Atoms, Peter Wurz
http://wurz.space.unibe.ch/paper_bad_honnef.pdf

Lifetime estimates

- Assume that the main loss mechanism is the charge exchange with residual (neutral) atoms/molecules:
 - $A^+ + B \rightarrow A + B^+$
 - In our case the kinetic energy is about 300 eV/nucleon
 - Cross-section is estimated at $1e-16 \text{ cm}^{-2}$

$$\text{Pressure: } p := 1 \cdot 10^{-10} \text{ torr}$$

$$n := \frac{p \cdot 133.3}{k \cdot T \cdot 10^6} \quad n = 3.22 \times 10^6 \text{ 1/cm}^3$$

$$\sigma := 1 \cdot 10^{-16} \text{ cross-section, cm}^{-2}$$

$$\tau := (n \cdot \sigma \cdot \beta \cdot c)^{-1} \quad \tau = 130.659 \text{ seconds}$$

: Fermilab