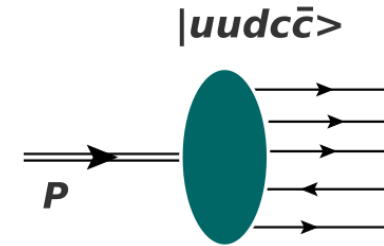
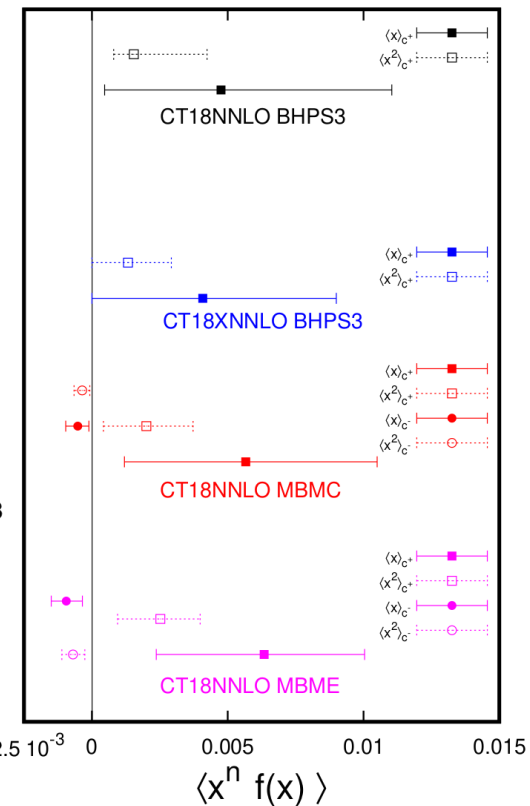
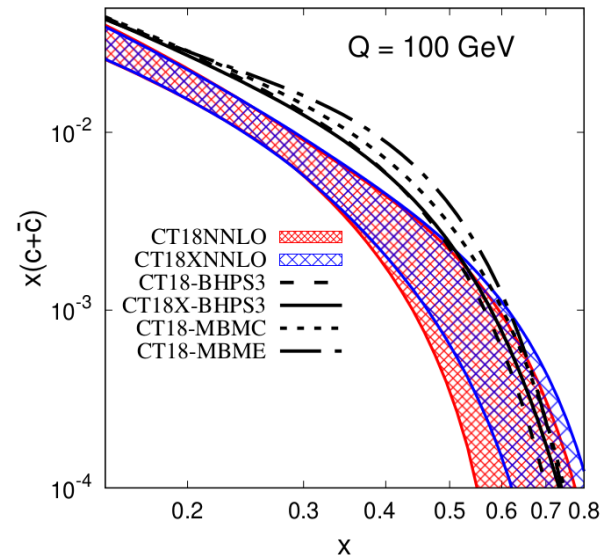


the proton's intrinsic charm remains concealed

Tim Hobbs – Argonne National Lab



$$\Delta\chi^2 \leq 10$$



NEW

arXiv: 2211.01387

CT18 FC: revisiting nonperturbative or *fitted charm* (FC)

CTEQ

- reassess status of FC, especially following recent LHC data

extended **talk tomorrow** (7:30am CST), International Light Cone Advisory Committee [ILCAC]

recent paper, arXiv: **2211.01387**

M. Guzzi, **T. Hobbs**, K. Xie, J. Huston, P. Nadolsky, and C.-P. Yuan

→ for the CTEQ-Tung et al. (CTEQ-TEA) Collaboration

this talk

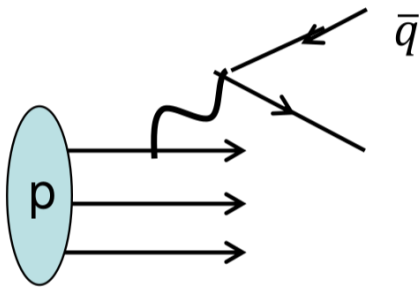
- i intrinsic charm (IC) vs. fitted charm (FC) in QCD
- ii treatment of key **expts** with potential FC sensitivity
- iii CT18 FC PDF analysis
- iv comparison with other recent FC studies

conclusion(s): necessary developments; high-impact data, calculations

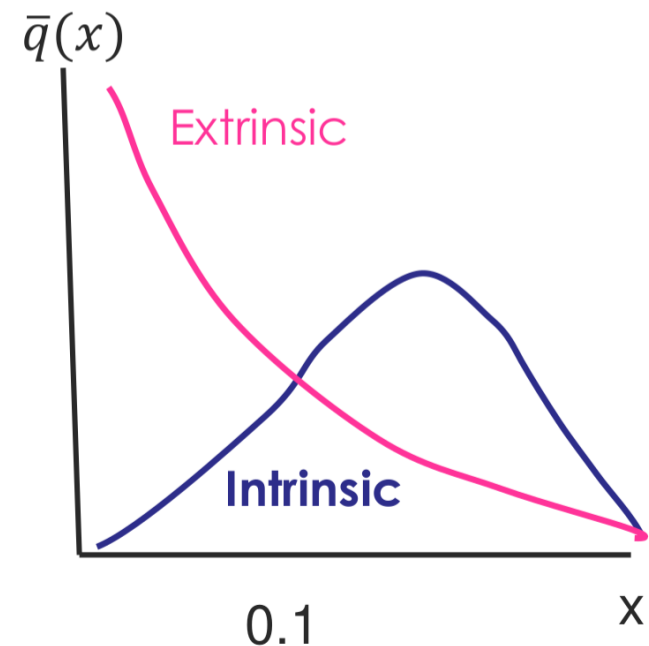
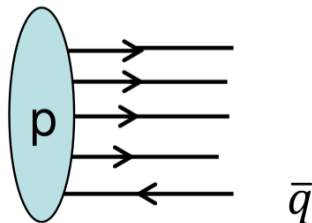
Extrinsic and intrinsic sea PDFs in nonperturbative models

“Extrinsic” sea

[maps on leading-power sea production from light flavors]



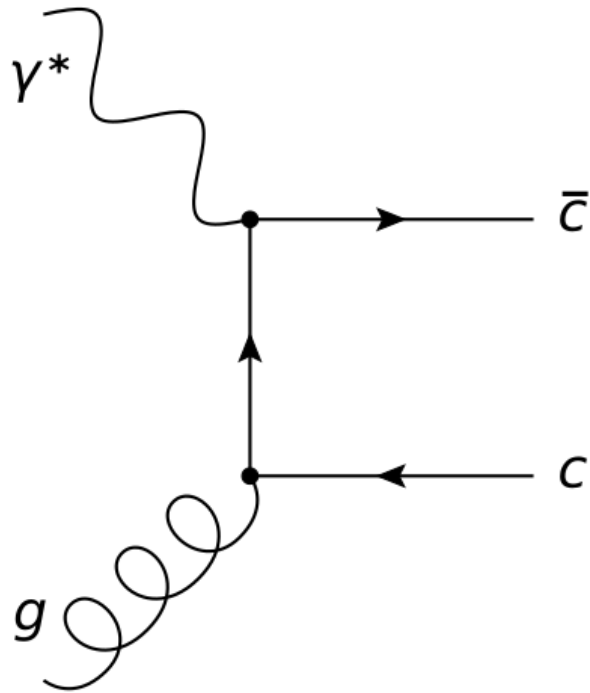
“Intrinsic” sea (excited Fock nonpert. states;
beyond the leading-power production)



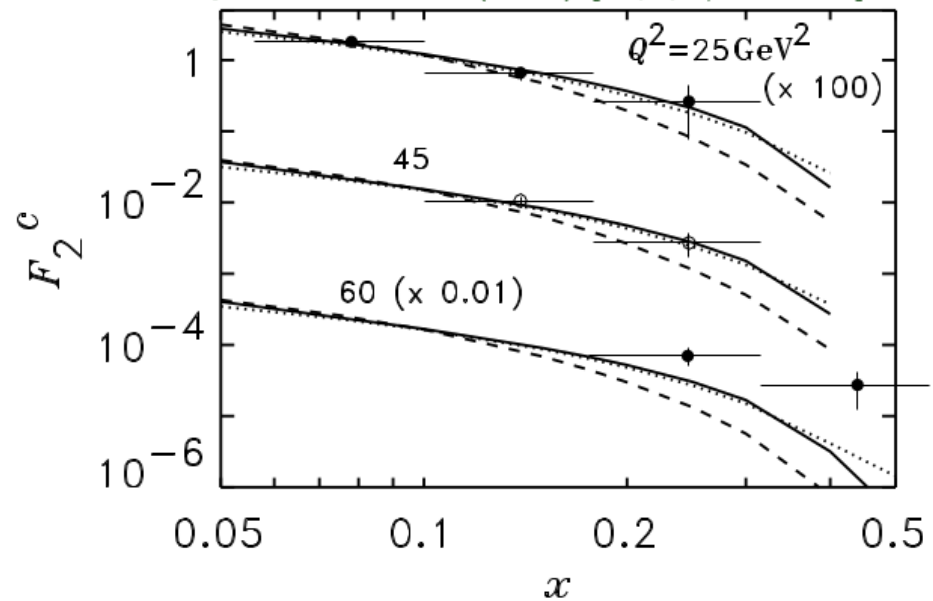
→ “intrinsic” charm (IC) from nucleon WF models based on this picture
...“extrinsic” generated radiatively; calculable in pQCD

implementations of perturbative ('extrinsic') charm in QCD analyses

- $c(x, Q^2 \leq m_c^2) = \bar{c}(x, Q^2 \leq m_c^2) = 0$ (a vanishing boundary condition for perturbative evolution)



F. M. Steffens, W. Melnitchouk and A. W. Thomas,
Eur. Phys. J. C **11**, 673 (1999) [hep-ph/9903441].



- *intermediate Q^2 :*

$$F_{2, \text{PGF}}^c(x, Q^2) = \frac{\alpha_s(\mu^2)}{9\pi} \int_x^{z'} \frac{dz}{z} C^{\text{PGF}}(z, Q^2, m_c^2) \cdot xg\left(\frac{x}{z}, \mu^2\right)$$

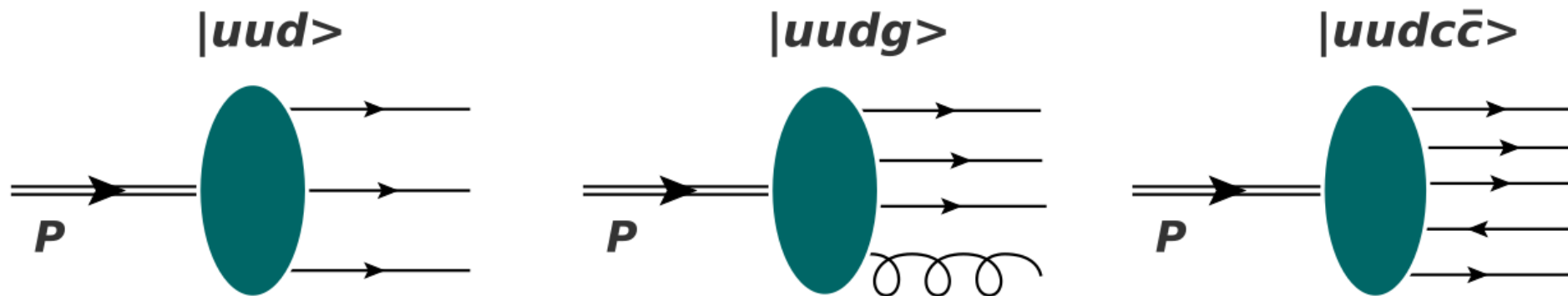
- *high Q^2 :*

massless **DGLAP** (i.e., *variable flavor-number schemes*)

nonperturbative QCD can generate a low-scale charm PDF

Fock expansion

Brodsky, Hoyer, Peterson, Sakai (BHPS); Phys. Lett. **B93** (1980) 451.



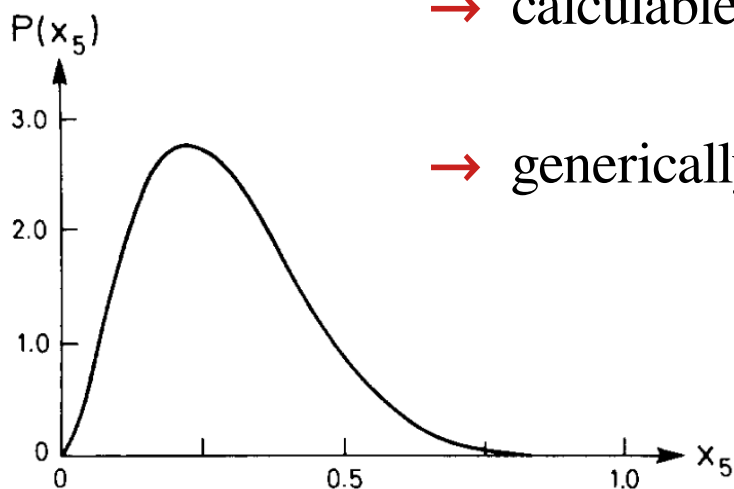
- IC PDF: transition matrix element, $|\text{proton}\rangle \rightarrow |uudc\bar{c}\rangle$

$$P(p \rightarrow uudc\bar{c}) \sim \left[M^2 - \sum_{i=1}^5 \frac{k_{\perp i}^2 + m_i^2}{x_i} \right]^{-2}$$

→ calculable in old-fashioned perturbation theory; **scalar** field theory

→ generically yields valence-like shape; governed by charm masses

$$m_c = m_{\bar{c}} \implies c^{\text{BHPS}}(x) = \bar{c}^{\text{BHPS}}(x)$$



- alternative but similar representations exist

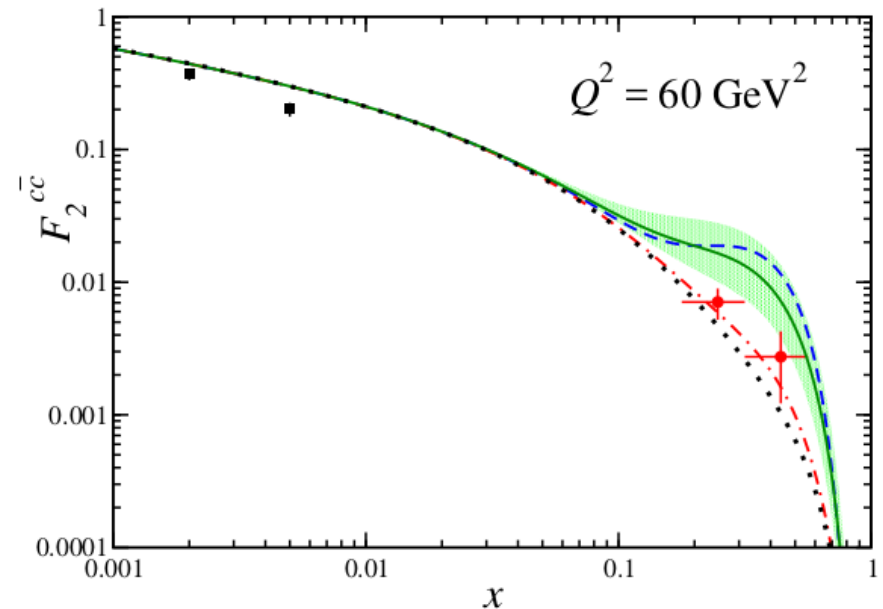
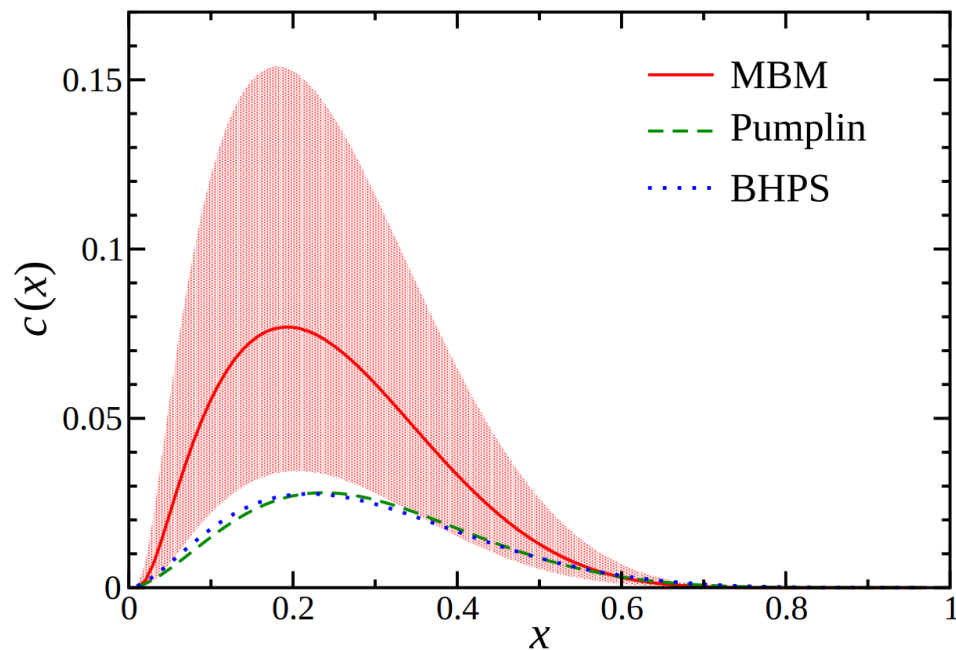
IC (MBM) depends on UV scale parameter, Λ ; predicts high- x excess

- tune **universal** cutoff $\Lambda = \hat{\Lambda}$ to fit **ISR** $pp \rightarrow \Lambda_c X$ collider data

multiplicities, momentum sum:

$$\langle n \rangle_{MB}^{(\text{charm})} = 2.40\% \quad {}^{+2.47}_{-1.36};$$

$$P_c := \langle x \rangle_{\text{IC}} = 1.34\% \quad {}^{+1.35}_{-0.75}$$



$$F_2^{c\bar{c}}(x, Q^2) = \frac{4x}{9} [c(x, Q^2) + \bar{c}(x, Q^2)]$$

→ evolve to **EMC** scale, $Q^2 = 60 \text{ GeV}^2$

low- x H1/ZEUS data check *massless* **DGLAP** evolution

IC models and **formal QCD**

- models simulate nucleon wave function; aim to *mimic* nonpert QCD
 - bound-state structure driven by constituent-quark masses
 - integrate away gluonic degrees-of-freedom
 - connect to SU(4) flavor-symm breaking (in meson-baryon models [MBMs])

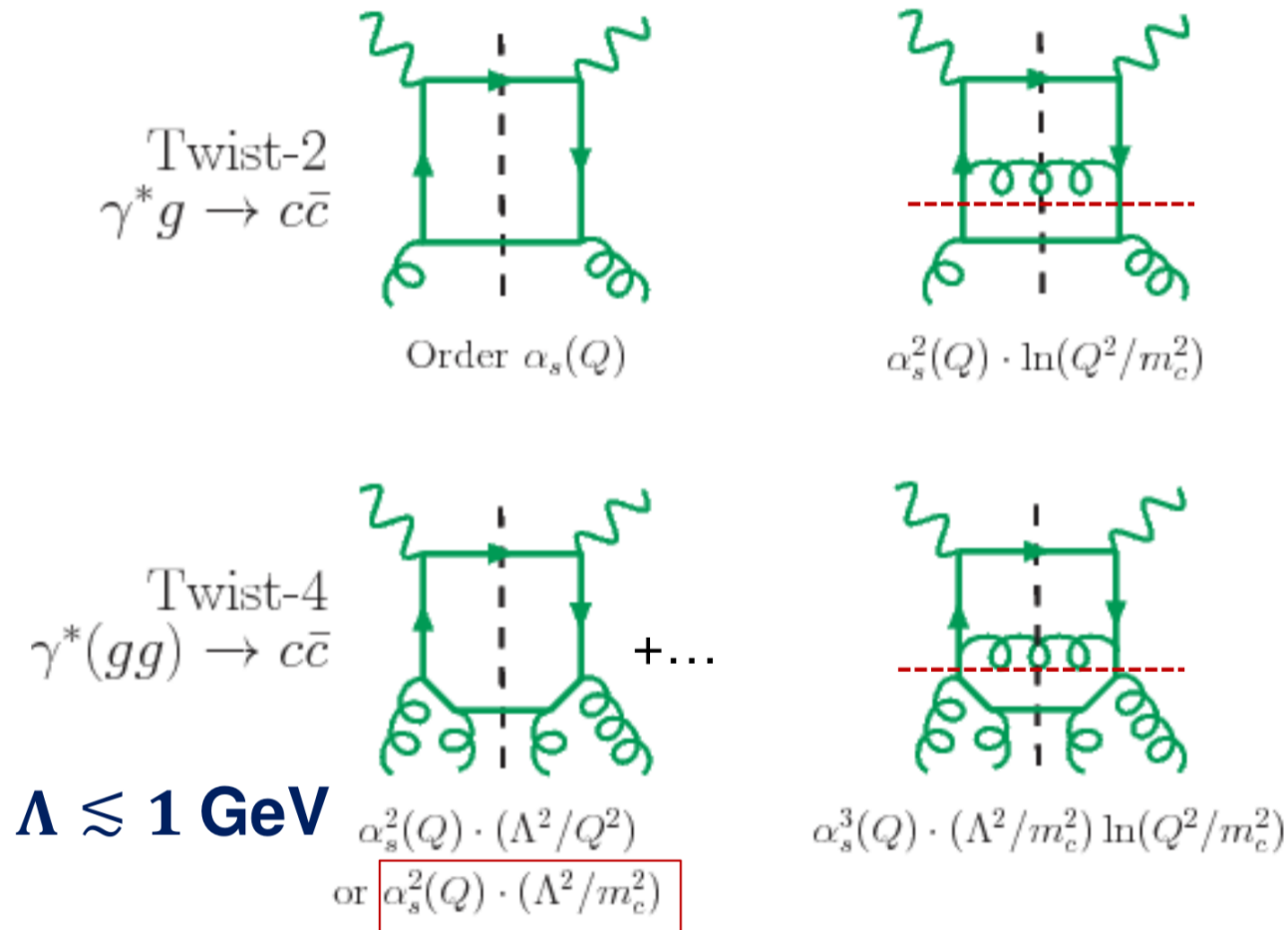
-
- **BUT:** IC models in systematically-improvable QCD calculations unclear
 - based on *truncated* Fock-state or similar wave function expansions
 - no obvious mapping onto factorization theorems
 - ambiguity regarding fact. scale, μ , in IC models

$$F(x, Q) = \sum_{a=0}^{N_f} \int_x^1 \frac{d\xi}{\xi} \mathcal{C}_a \left(\frac{x}{\xi}, \frac{Q}{\mu}, \frac{m_c}{\mu}; \alpha_s(\mu) \right) f_{a/p}(\xi, \mu) + \mathcal{O}(\Lambda^2/m_c^2, \Lambda^2/Q^2)$$

- PDF analyses extract fitted charm (FC) \neq intrinsic charm (IC)

IC may have complicated interplay with nonleading twist

- IC can be developed in twist expansion; systematic ordering of leading-, power-suppressed contributions



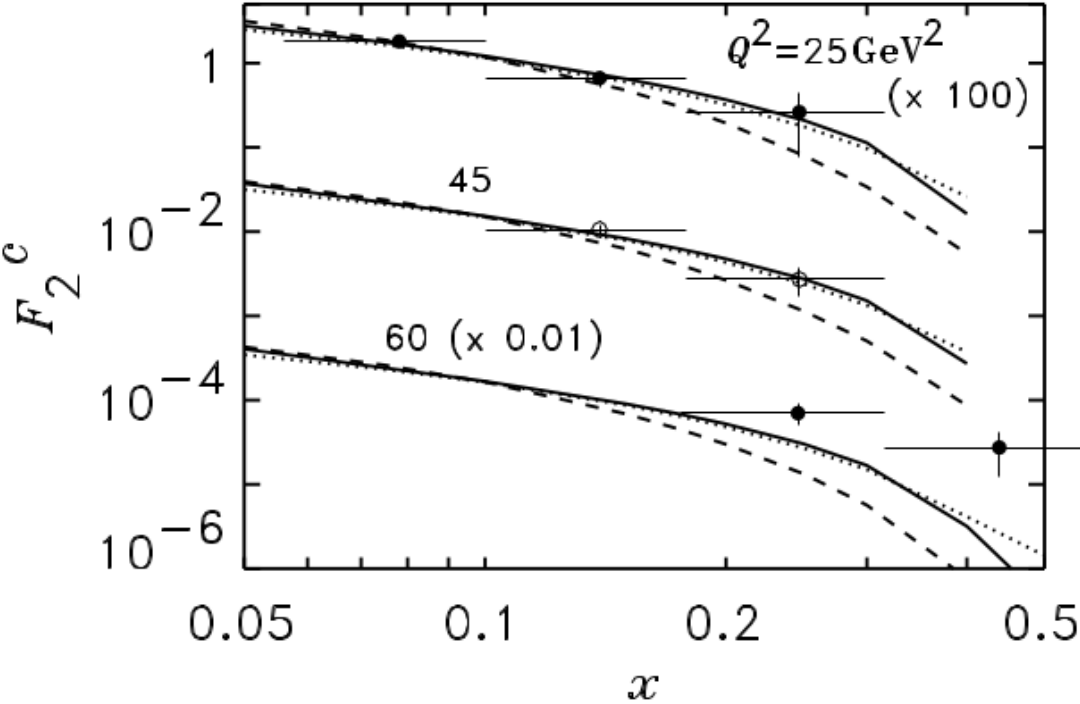
- control needed to avoid absorbing non-universal contributions into IC

few expts with ‘smoking gun’ sensitivity to FC; but **EMC data (?)**

J. J. Aubert *et al.* (EMC), NPB**213** (1983) 31–64.

- historically, charm structure function data, $F_2^{c\bar{c}}$, from EMC were suggestive

F. M. Steffens, W. Melnitchouk and A. W. Thomas, Eur. Phys. J. C **11**, 673 (1999) [hep-ph/9903441].



- hint of high- x excess in select Q^2 bins
- data were analyzed only at LO
- show anomalous Q^2 dependence
- EMC data fit poorly in CT14 IC study

we do not include EMC in CT18 FC

CT14 IC, arXiv: 1707.00657.

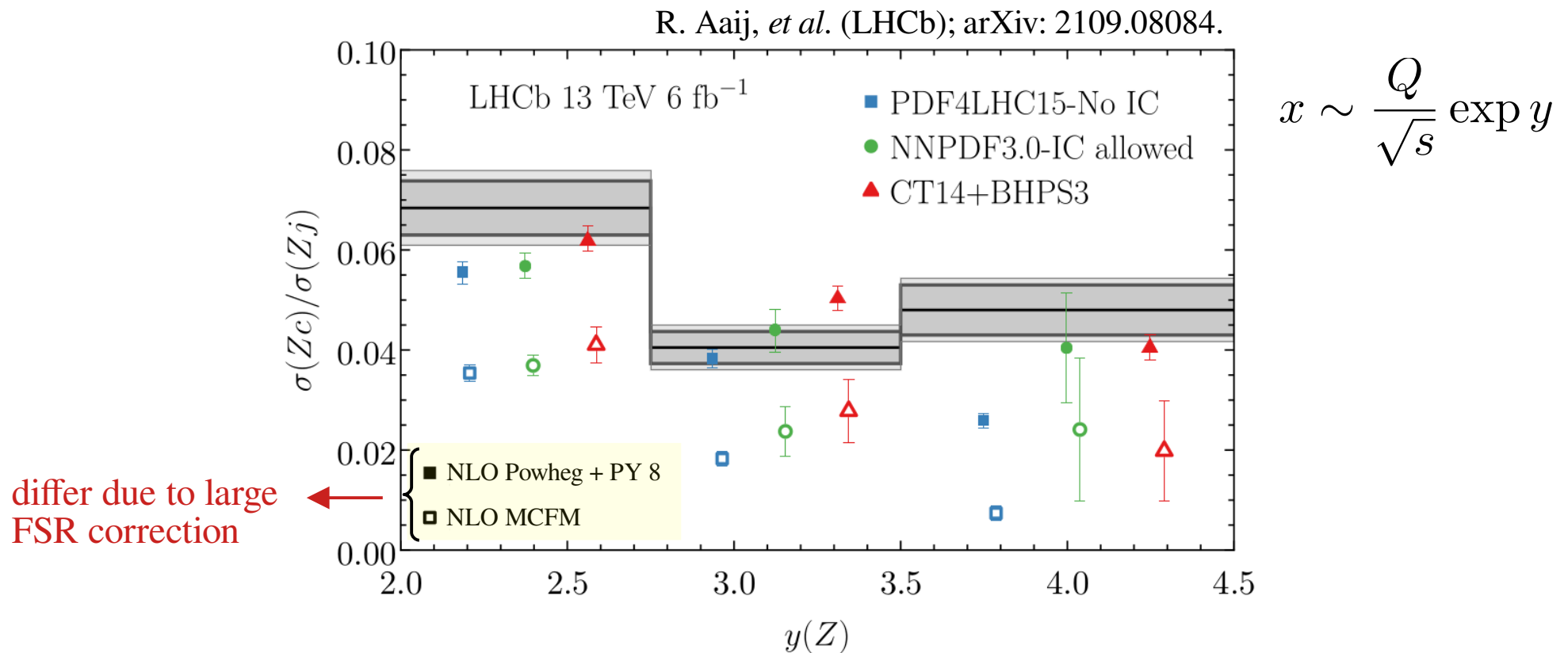
Candidate NNLO PDF fits	χ^2/N_{pts}			
	All Experiments	HERA inc. DIS	HERA $c\bar{c}$ SIDIS	EMC $c\bar{c}$ SIDIS
CT14 + EMC (weight=0), no IC	1.10	1.02	1.26	3.48
CT14 + EMC (weight=10), no IC	1.14	1.06	1.18	2.32
CT14 + EMC in BHPS model	1.11	1.02	1.25	2.94
CT14 + EMC in SEA model	1.12	1.02	1.28	3.46

$Z+c$ potentially sensitive to IC; sizable theory uncertainties

T. Boettcher, P. Ilten, M. Williams, 1512.06666

- 2022 LHCb 13 TeV data: $(Z+c) / (Z+jet)$ ratios; 3 rapidity bins

→ calculated **NLO** cross-section ratio similarly depends on showering, hadronization



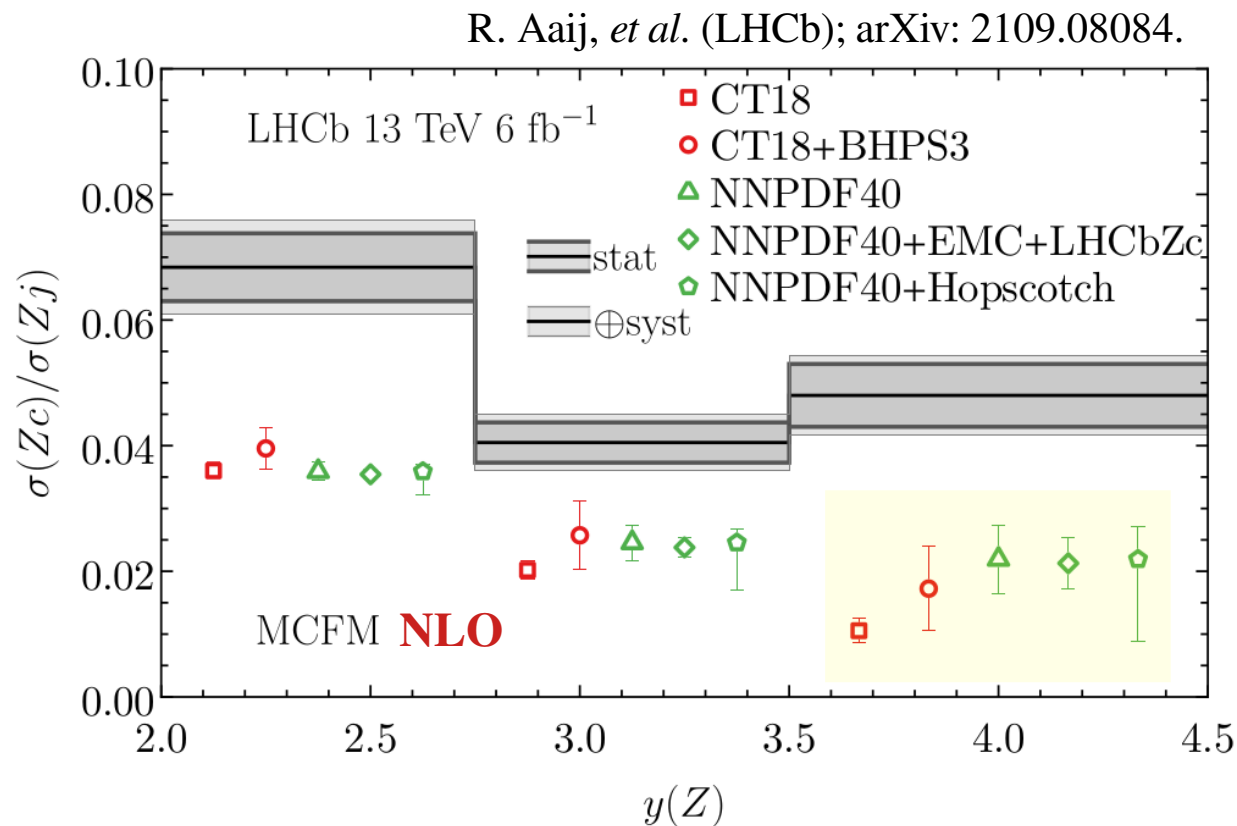
- NNLO calculations recently available, but not implemented in PDF fits

R. Gauld, *et al.*; arXiv: 2005.03016.

M. Czakon, *et al.*; arXiv: 2011.01011.

theory uncertainties currently larger than PDF variations

- assuming MCFM at NLO, can vary underlying PDFs, test inclusion of FC
 - FC slightly enhances ratio; not enough to improve agreement with data



$$x \sim \frac{Q}{\sqrt{s}} \exp y$$

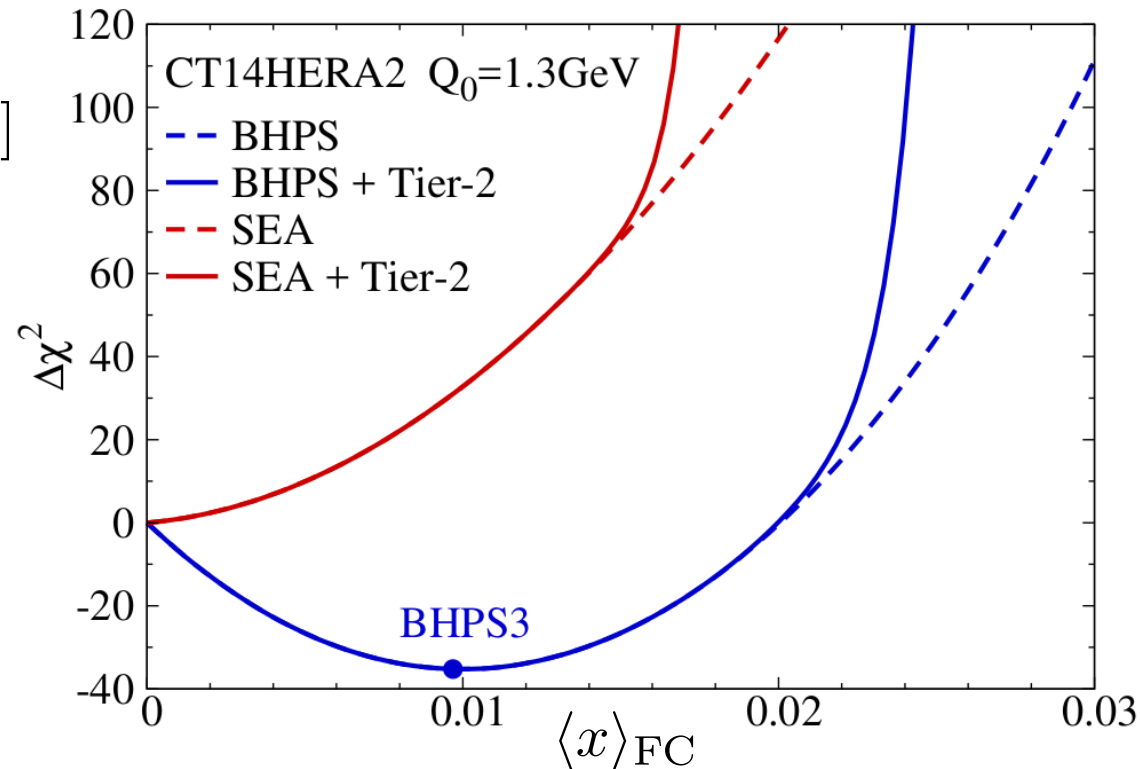
- theory accuracy not yet sufficient to leverage expt. precision for PDFs
 - need NNLO theory interface; control over showering, final-state effects

might other HEP experiments be sensitive to FC?

- must be assessed using comprehensive global QCD analysis of PDFs
- CT performed such an analysis, CT14 IC in [arXiv: 1707.00657](#)
 - found $\langle x \rangle_{\text{FC}} < 2\%$, but with large uncertainty consistent with zero FC

$$\langle x \rangle_{\text{FC}} = \int_0^1 dx x [c(x, Q_0) + \bar{c}(x, Q_0)]$$

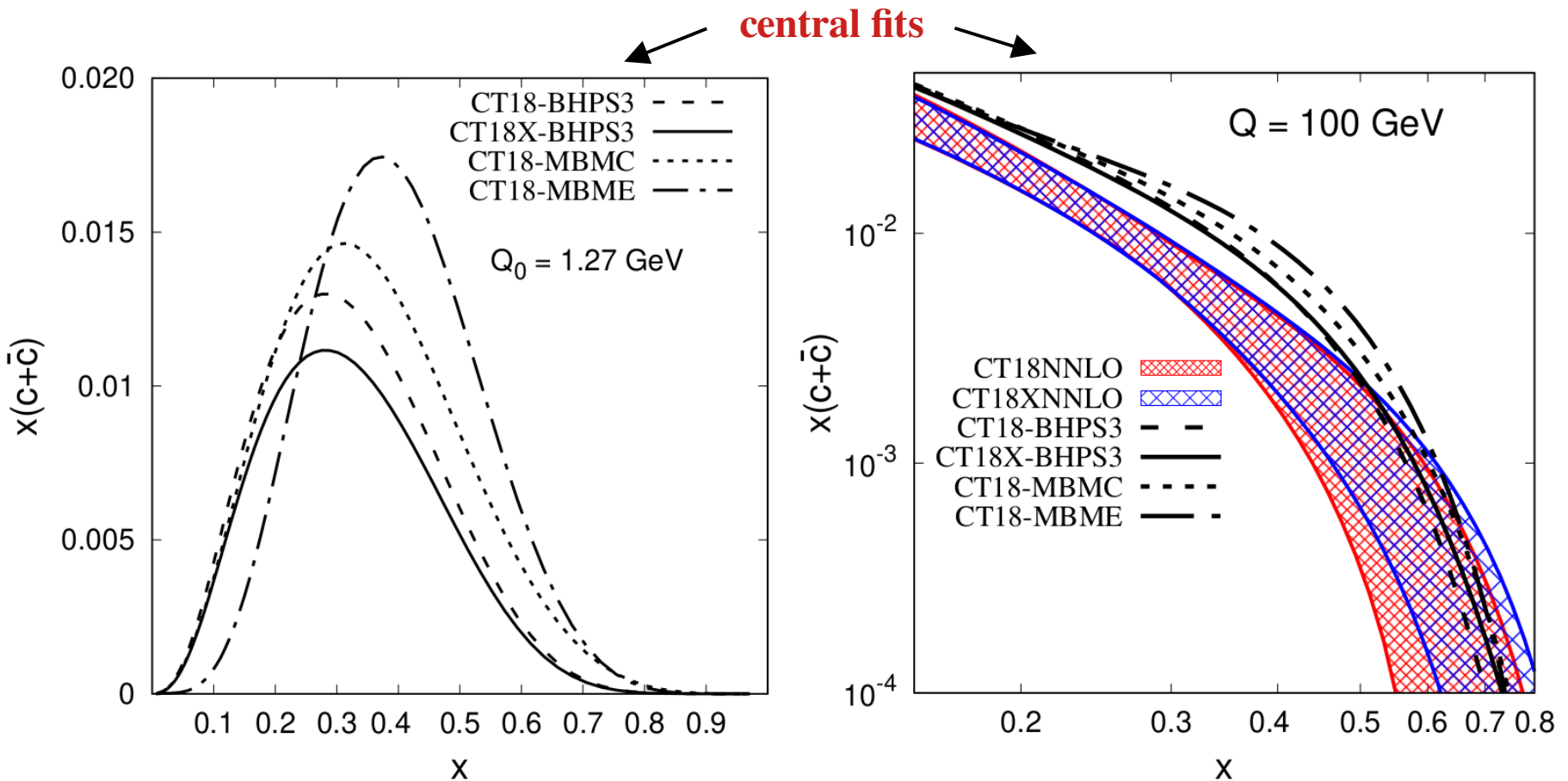
- included many details on theory and analysis of IC



- since CT14 IC, many LHC measurements have been released; natural to ask if these possess *collective* sensitivity to FC

CT18 FC total charm PDFs

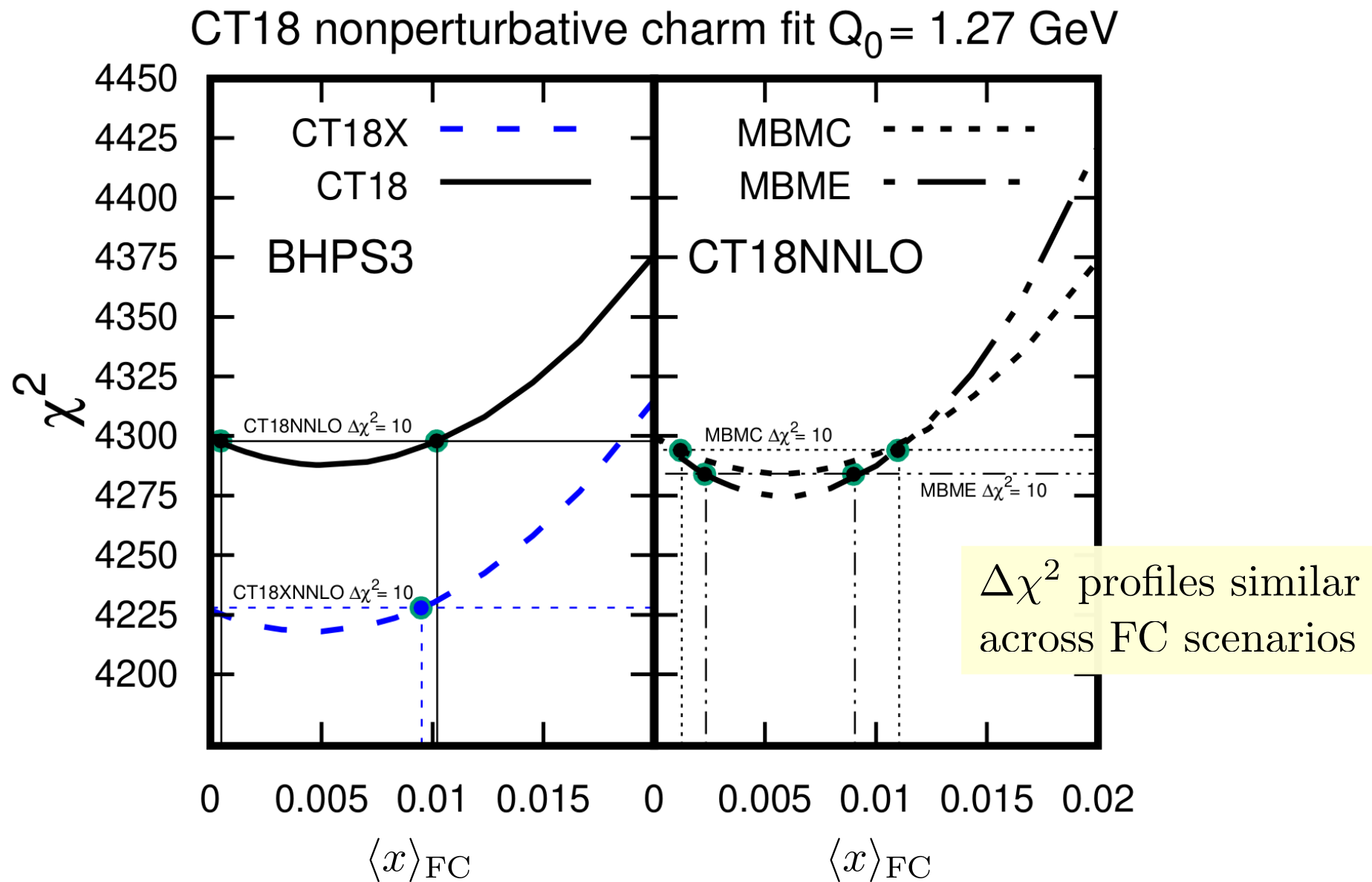
- FC scenarios traverse range of high- x behaviors from IC models
 - fit implementation of BHPS from CT14IC (BHPS3) on CT18 or CT18X (NNLO)
 - fit two MBMs: MBMC (confining), MBME (effective mass) on CT18
- investigate constraints from newer LHC data in CT18



iii

signal for FC in CT18 study, but with shallower $\Delta\chi^2$ than CT14 IC

- FC uncertainty quantified by normalization via $\langle x \rangle_{\text{FC}}$ for each input IC model
- $\langle x \rangle_{\text{FC}} \approx 0.5\%$ ($\Delta\chi^2 \gtrsim -25$) vs. $\langle x \rangle_{\text{FC}} \approx 0.8-1\%$ ($\Delta\chi^2 \gtrsim -40$) **CT14 IC**



iii

FC PDF moments as F.o.M.

- even restrictive uncertainties give moments consistent with zero

→ broaden further for default CT tol.

→ lattice may give $\langle x \rangle_{c+}$, $\langle x^2 \rangle_{c-}$

$$\langle x \rangle_{\text{FC}} \equiv \langle x \rangle_{c+} [Q_0 = 1.27 \text{ GeV}]$$

$$= 0.0048^{+0.0063}_{-0.0043} \quad (+0.0090, -0.0048), \text{ CT18 (BHPS3)}$$

$$= 0.0041^{+0.0049}_{-0.0041} \quad (+0.0091, -0.0041), \text{ CT18X (BHPS3)}$$

$$= 0.0057^{+0.0048}_{-0.0045} \quad (+0.0084, -0.0057), \text{ CT18 (MBMC)}$$

$$= 0.0061^{+0.0030}_{-0.0038} \quad (+0.0064, -0.0061), \text{ CT18 (MBME)}$$

$$\Delta\chi^2 \leq 10$$

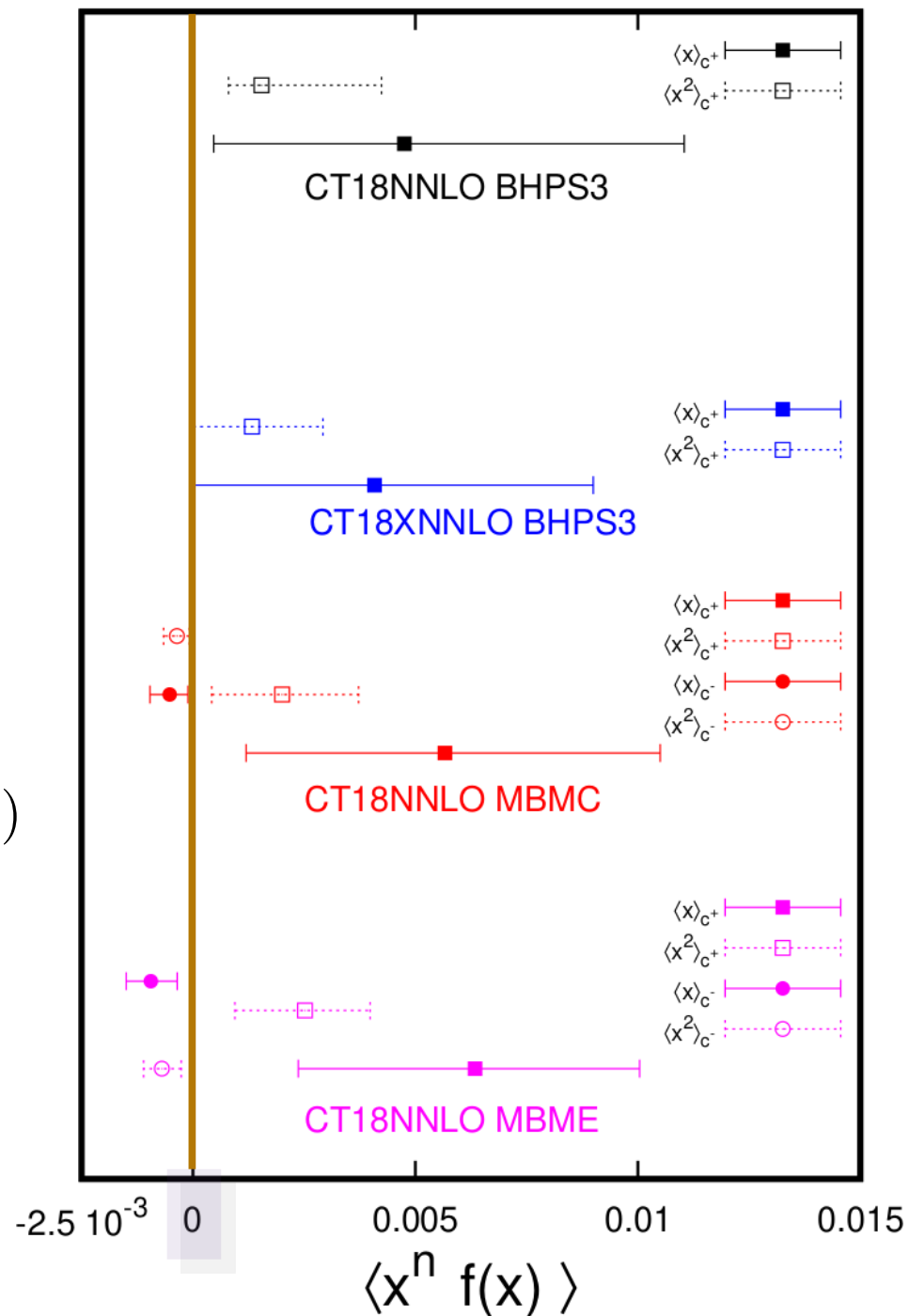
(restrictive tolerance)

$$\Delta\chi^2 \leq 30$$

(~CT standard tolerance)

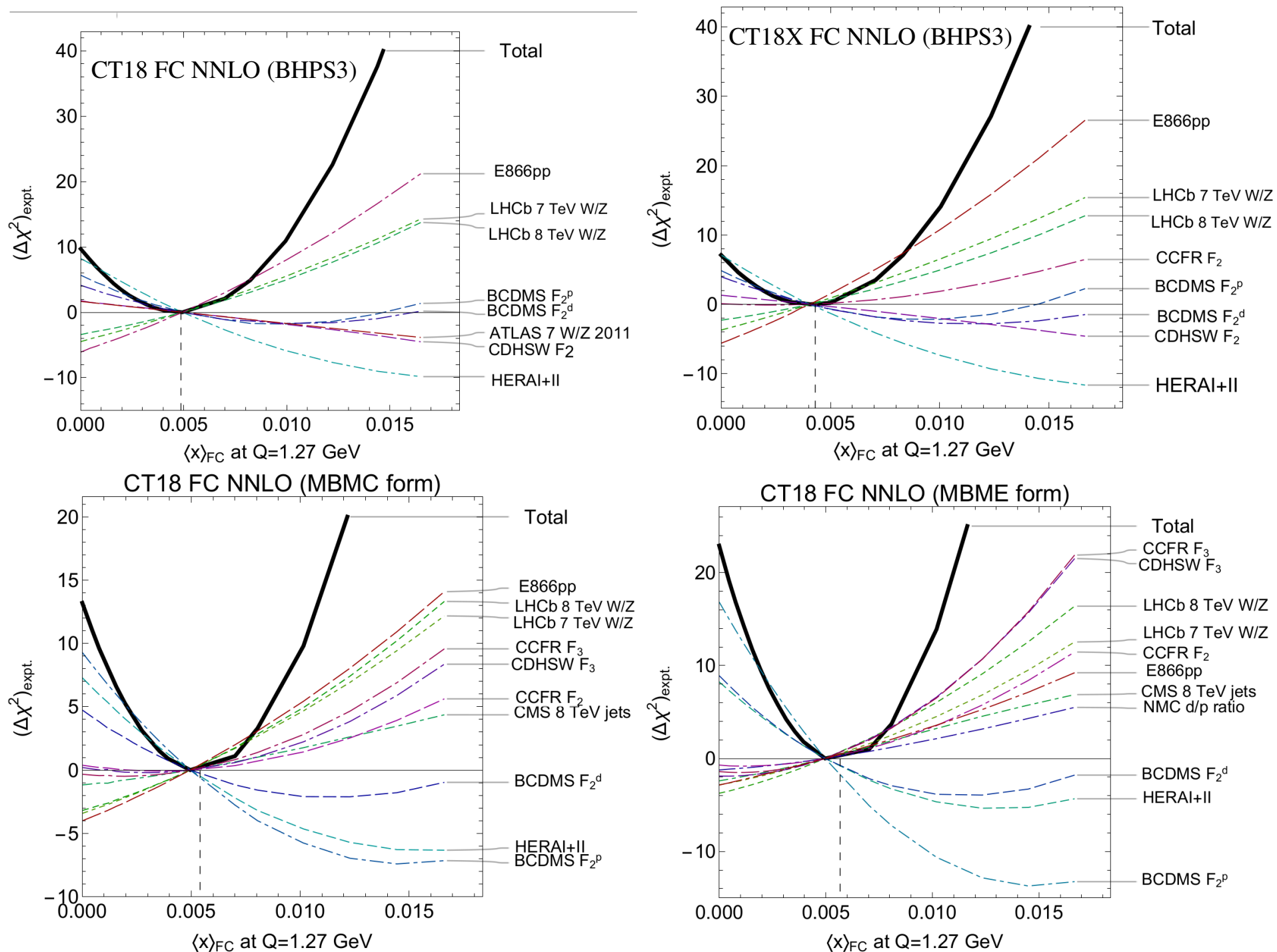
Nonperturbative charm moments $Q_0 = 1.27 \text{ GeV}$

Intervals of $\Delta\chi^2 < 10$



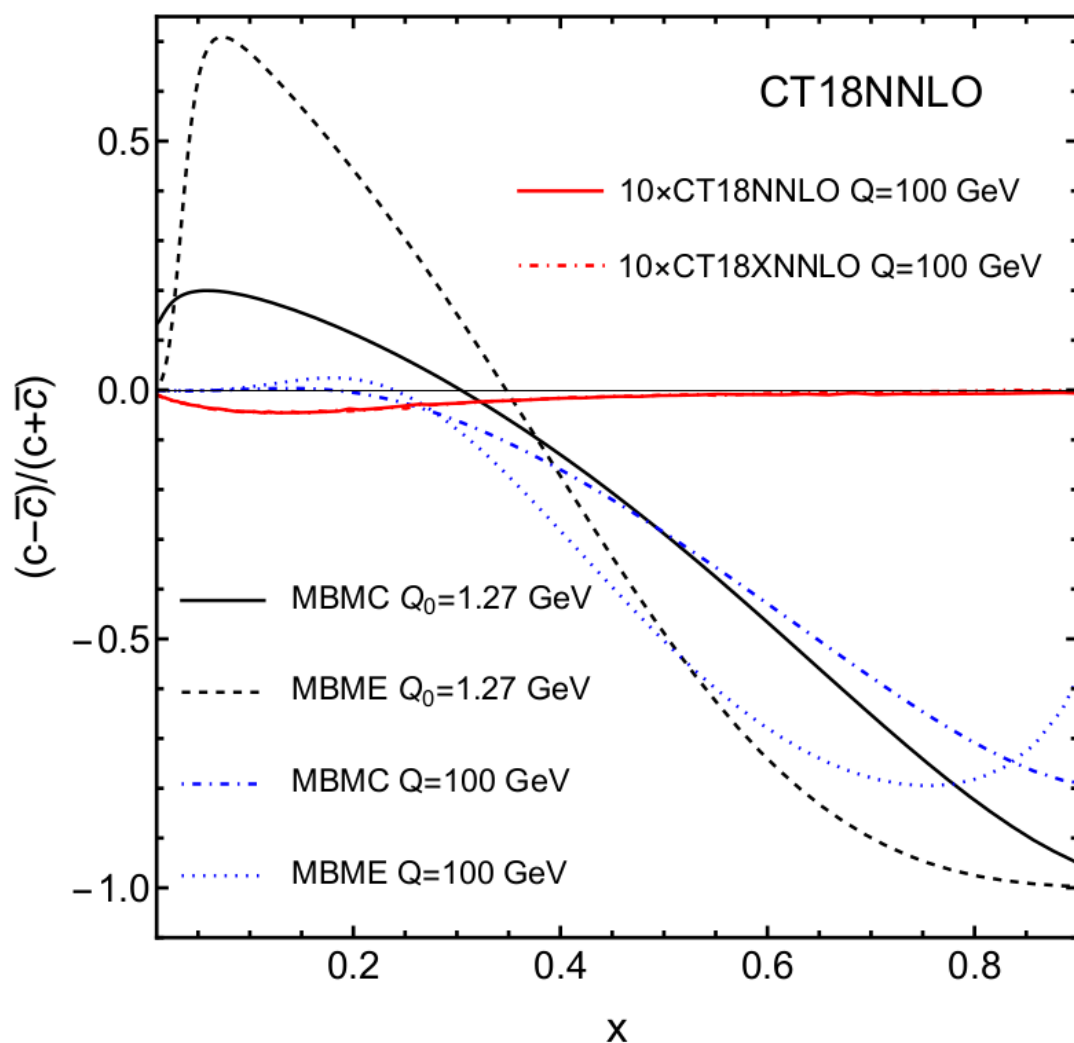
iii

data pull opposingly on $\langle x \rangle_{\text{FC}}$; depend on FC scenario, enhancing error



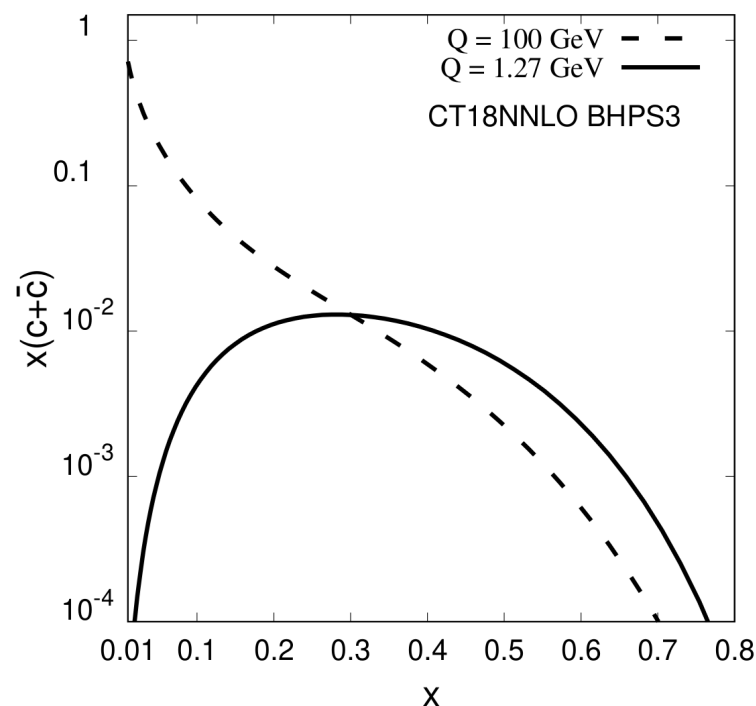
possible charm-anticharm asymmetries

- pQCD only very weakly breaks $c = \bar{c}$ through HO corrections
 - large(r) charm asymmetry would signal nonpert dynamics, IC
 - MBM breaks $c = \bar{c}$ through hadronic interactions

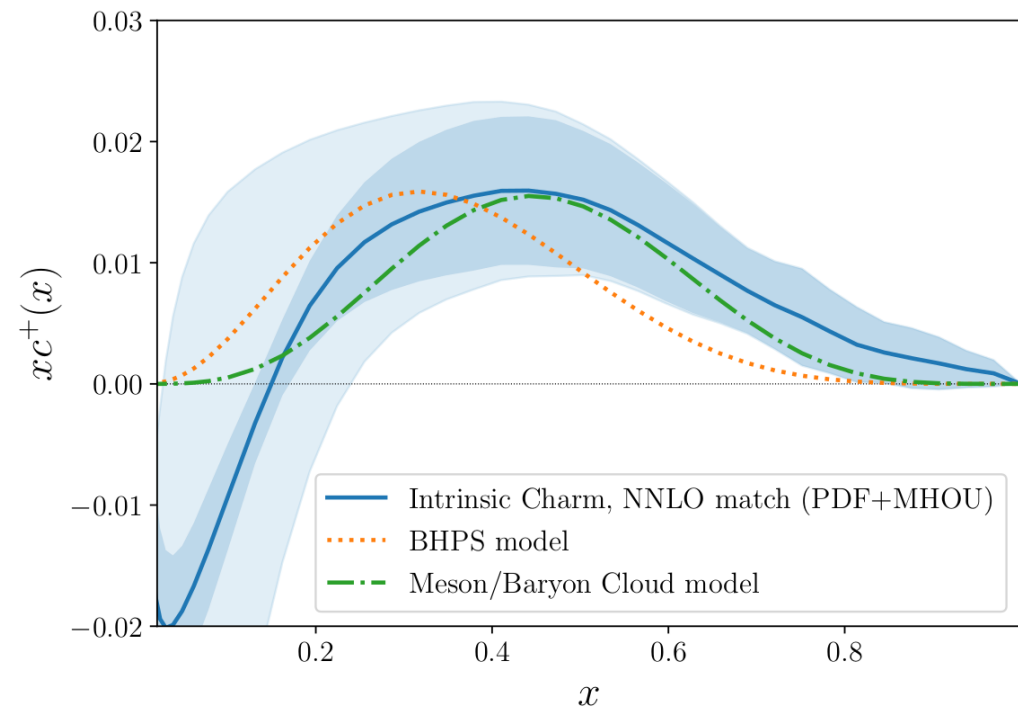
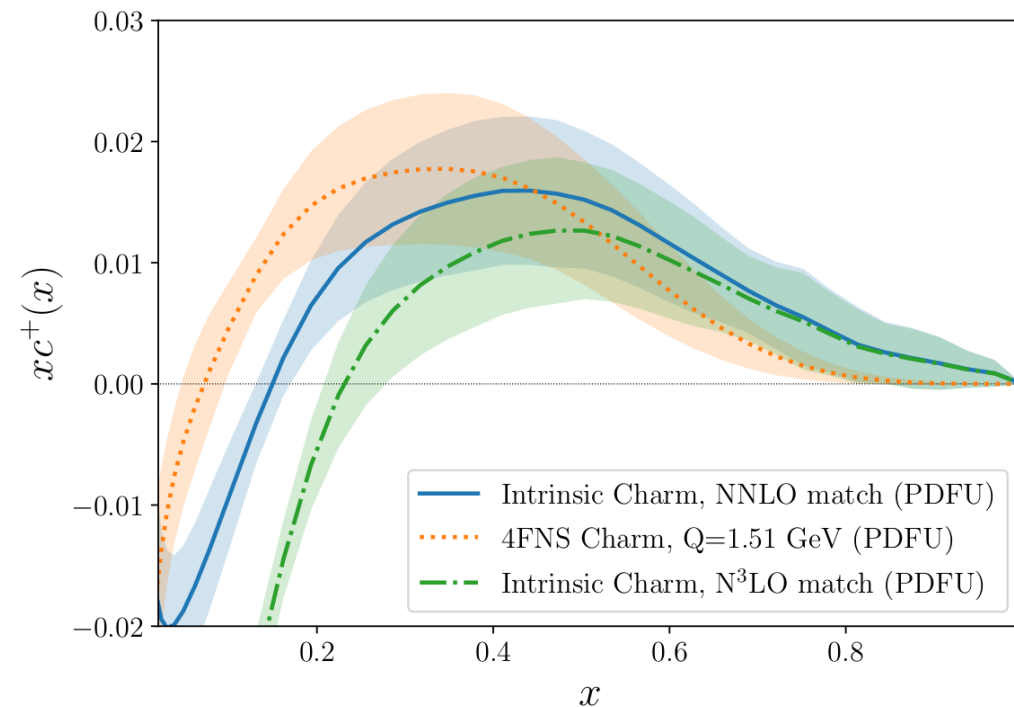


- consider two MBM models as *examples* (not predictions)

→ asym. small but ratio (left) can be bigger; will be hard to extract from data

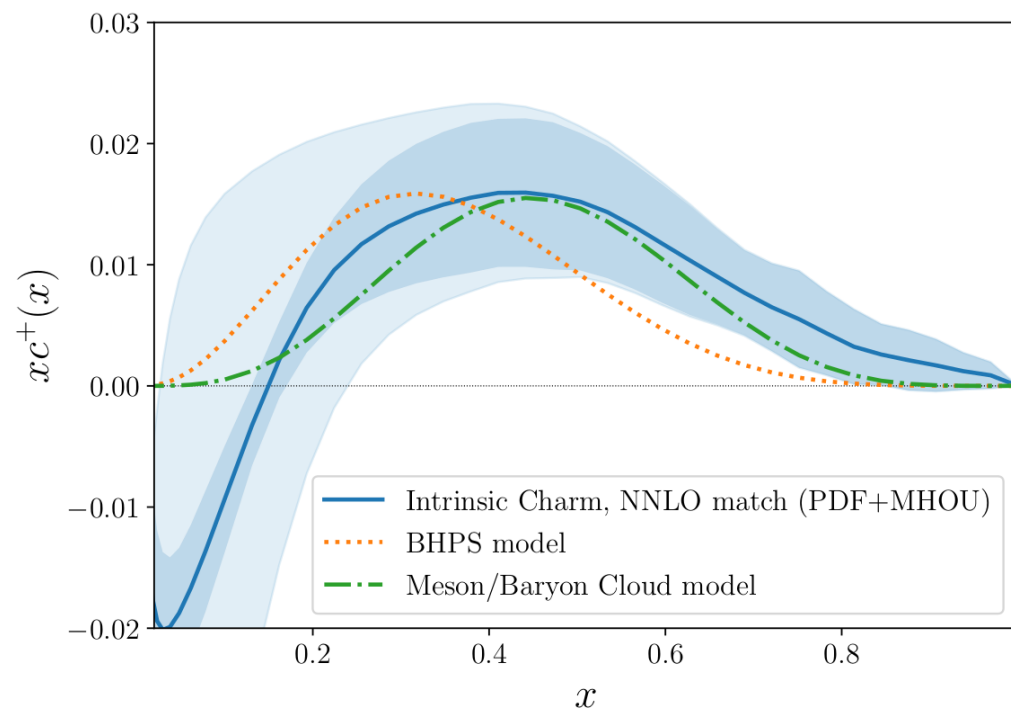
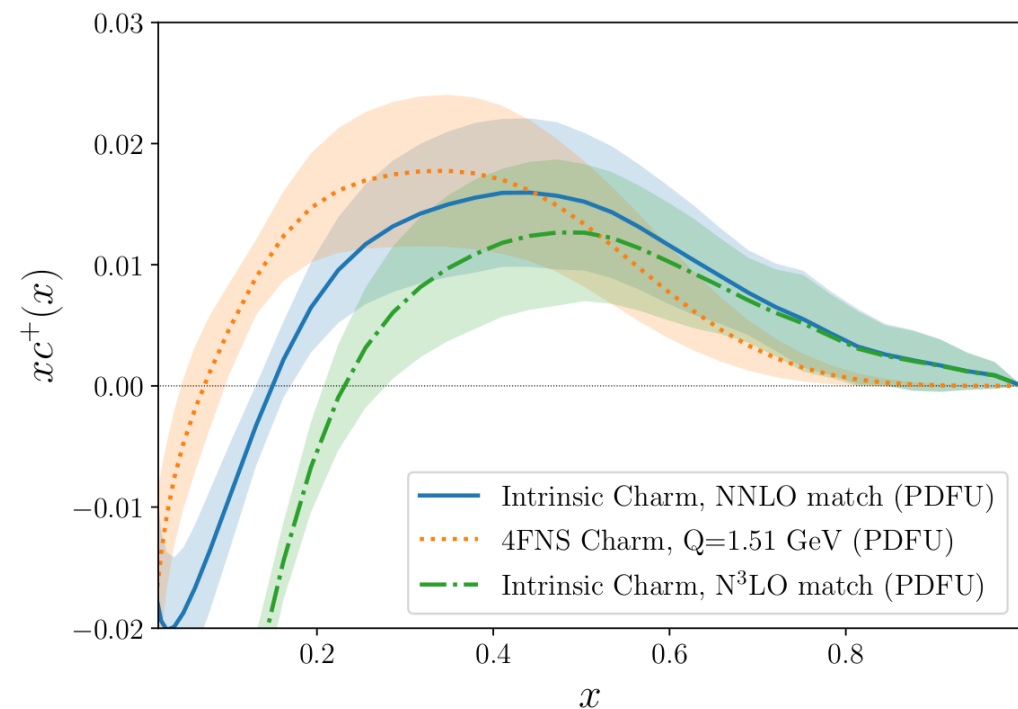


- NNPDF have recently claimed 3σ evidence for ‘IC’
 - based on local (x -dependent) deviation of FC PDF from perturbative scenario
 - implies crucial dependence on size and shape of PDF uncertainty



- NNPDF FC distribution is particularly hard, peaking at $x \gtrsim 0.4$
- intriguing behavior at low x

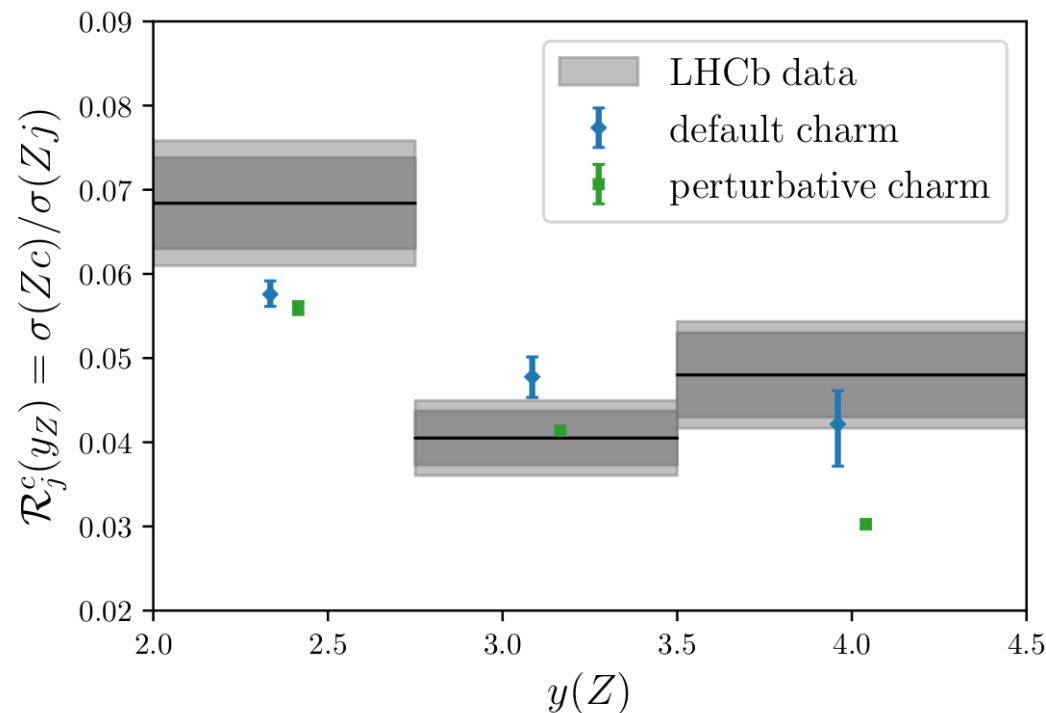
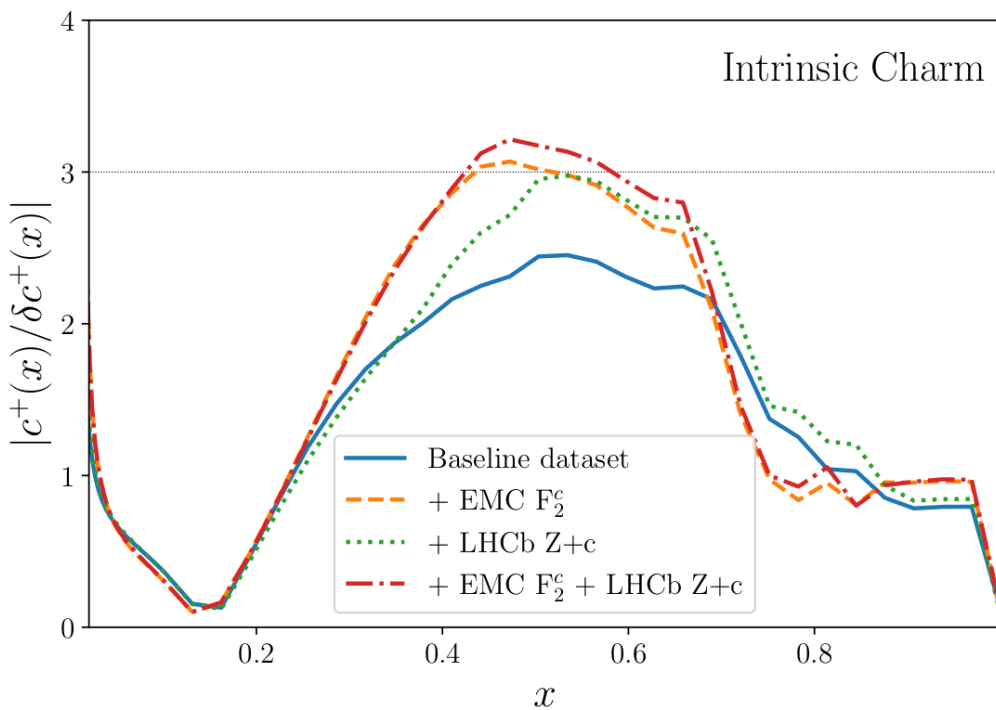
- large perturbative instability from MHOU affects low- x behavior
 - matching at fixed NNLO gives negative FC, unlike IC models
 - MHOU persists to quite high $x < 0.1$ or more



- MHOU excluded to obtain a nominal charm fraction, $\langle x \rangle_{\text{FC}} = 0.62 \pm 0.28\%$
- if MHOU is included, consistency with zero: $\langle x \rangle_{\text{FC}} = 0.62 \pm 0.61\%$

iv specific experiments in NNPDF IC

- 3σ significance reached with inclusion of LHCb $Z+c$ data
 - theory uncertainties for these data (*e.g.*, showering algorithms) remain large

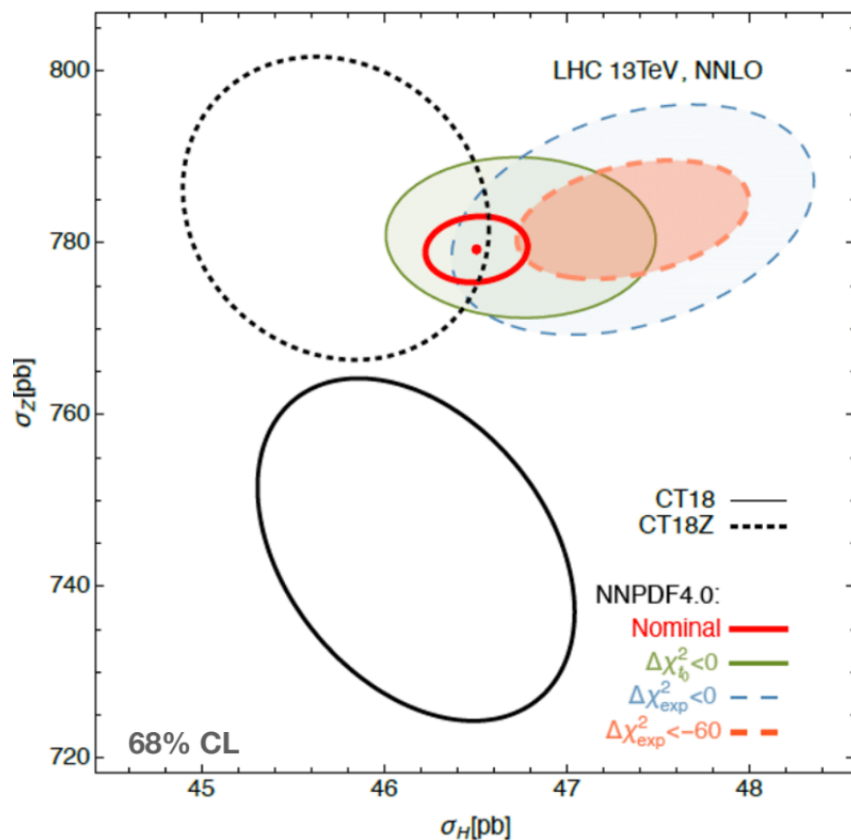


- NNPDF approach 3σ significance with baseline dataset
 - similar group of expts in CT18 FC do not yield strong signal
- connected to differing PDF uncertainty quantifications

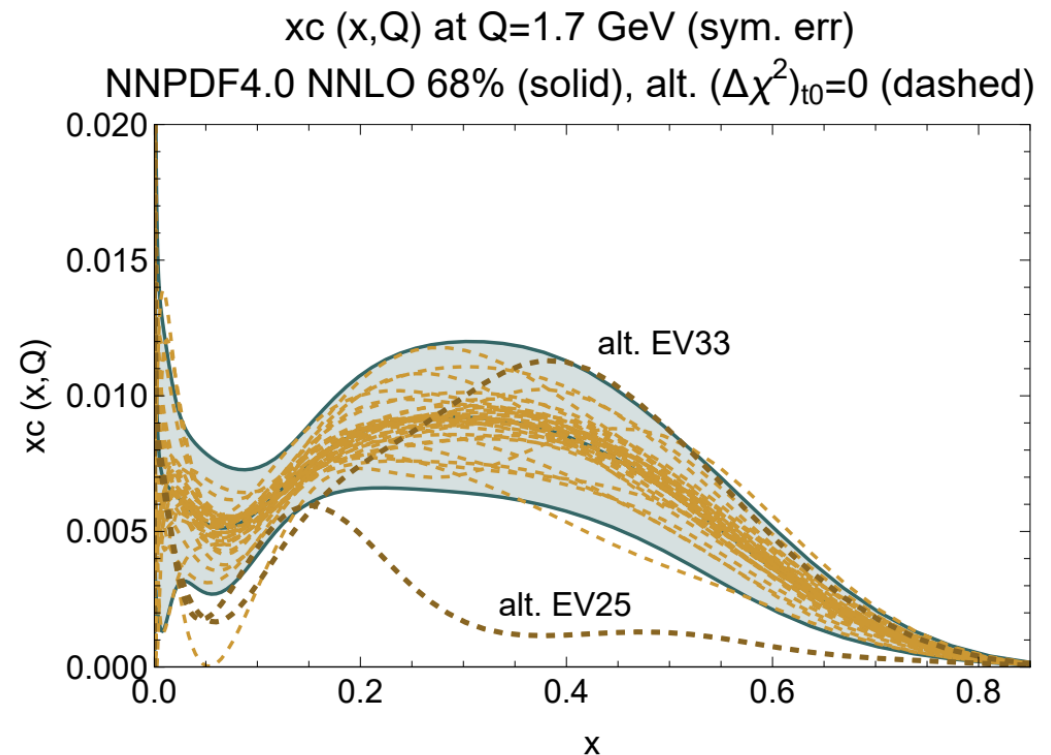
iv more representative sampling can enlarge MC uncertainties

Courtoy *et al.*, arXiv: 2205.10444.

- default replica-training in MC studies may omit otherwise acceptable solutions
- more comprehensive sampling impacts PDF errors of cross sections



- substantially broaden high- x FC error

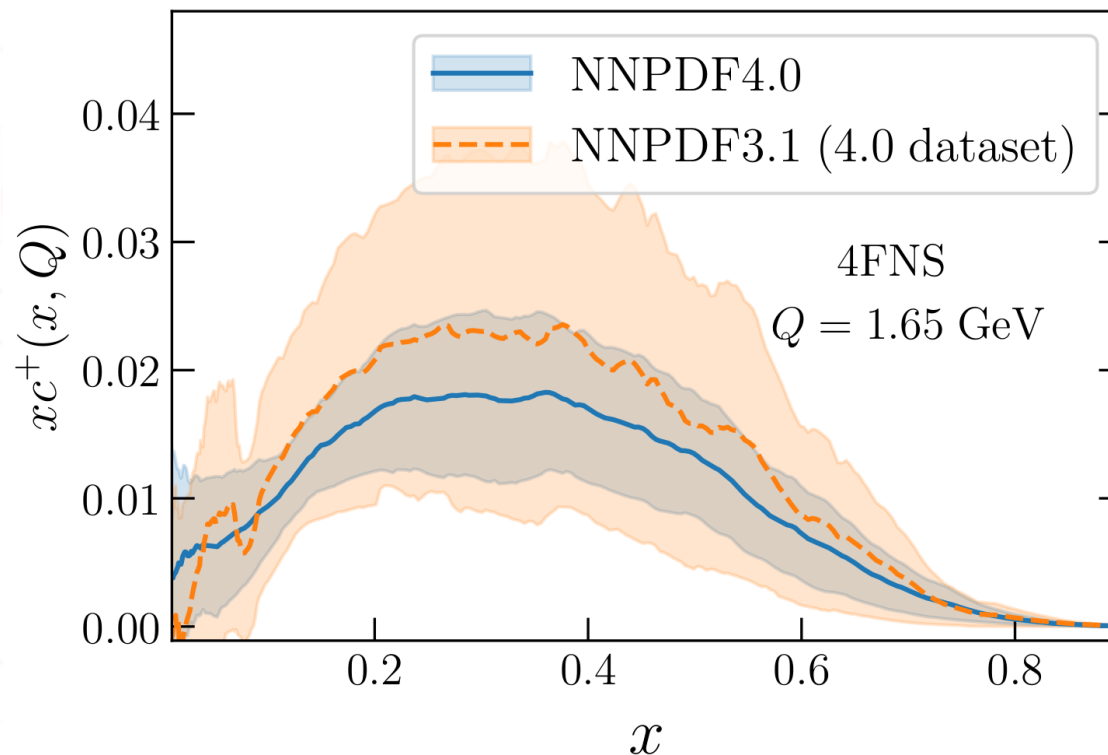


iv more representative sampling can enlarge MC uncertainties

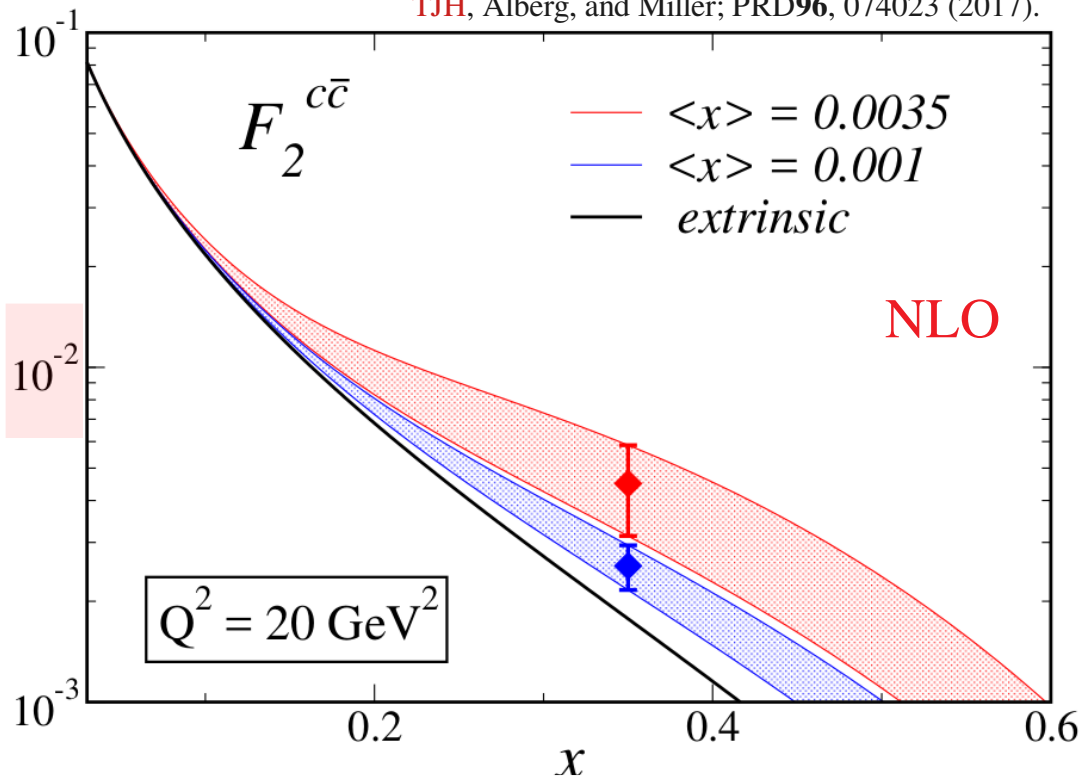
Courtoy *et al.*, arXiv: 2205.10444.

- default replica-training in MC studies may omit otherwise acceptable solutions

→ alternate fitting methodologies (NNPDF3.1 vs. 4.0) produce significant differences in PDF uncertainty



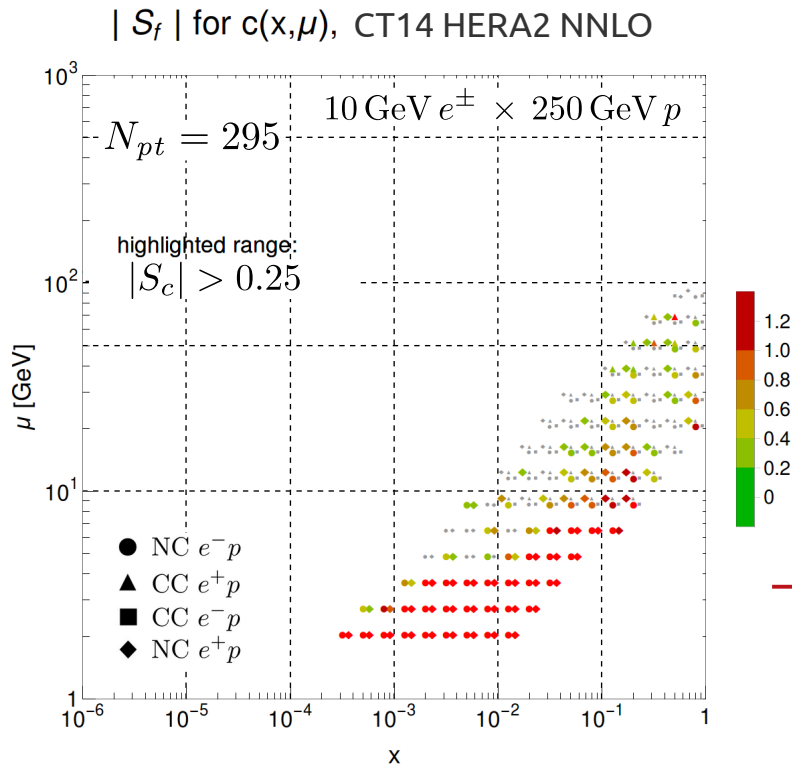
both curves based on same underlying data



future data will inform FC

EIC will constrain FC scenarios

enhanced FC momentum implied by EMC data \rightarrow small high- x effects in structure function; need high precision



■ essential complementary input from LHC; CERN FPF

EIC will measure precisely in the few-GeV, high- x region where FC signals are to be expected

conclusions

- **size, shape of nonpert charm remains indeterminate**
 - theoretical ambiguities in relation between FC/IC unresolved
 - need more sensitive data; FC currently consistent with zero

concordance with enlarged error estimates: $\langle x \rangle_{\text{FC}} \sim 0.5\%$, well below evidence-level

- need more NNLO and better showering calculations (*e.g.*, for $Z+c$)
- further progress in quantifying and estimating PDF uncertainties

-
- opportunities to improve knowledge of FC:
 - promising experiments at LHC; EIC; CERN FPF
 - lattice data on key charm PDF moments; quasi-PDFs
 - direct benchmarking of FC among PDF fitting groups