

Electron-Nucleus Scattering for Neutrino Interactions and Oscillations

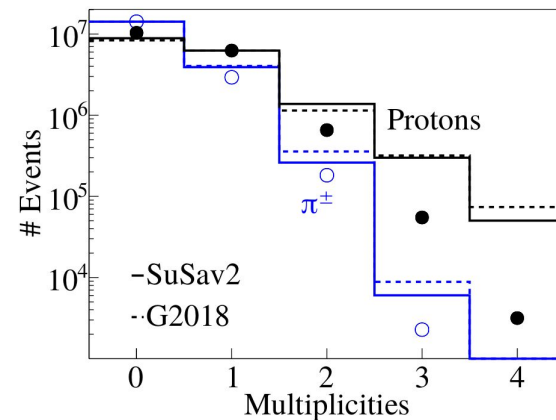
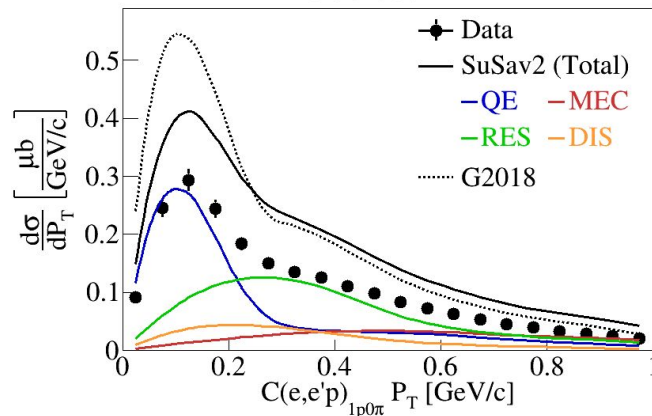
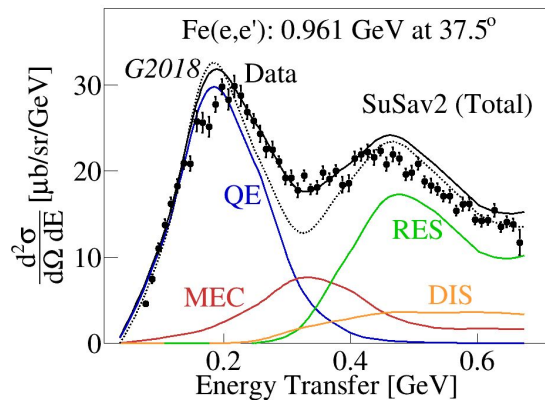
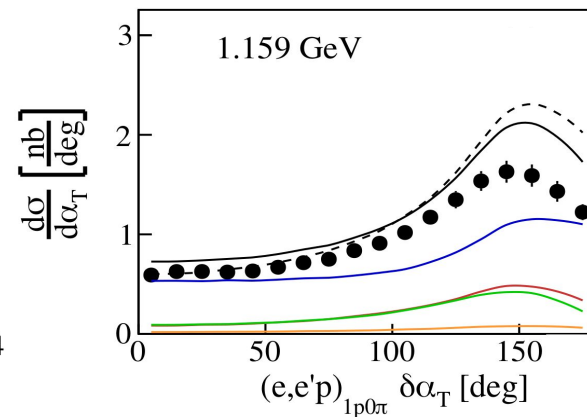
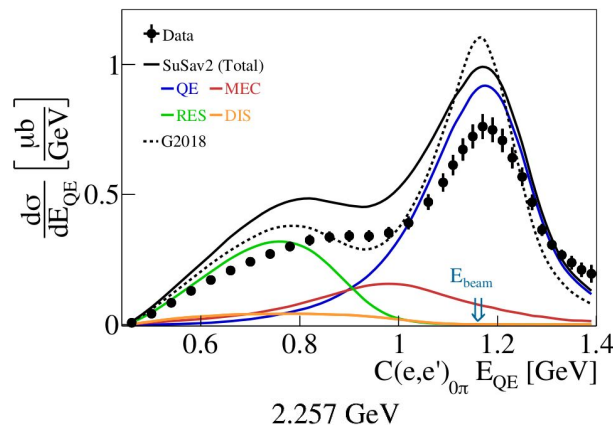
Afrodit Papadopoulou
On behalf of the *e4ν* collaboration

Generator Workshop

The e4ν Result Factory

Many

- nuclei
- beam energies
- channels
- variables



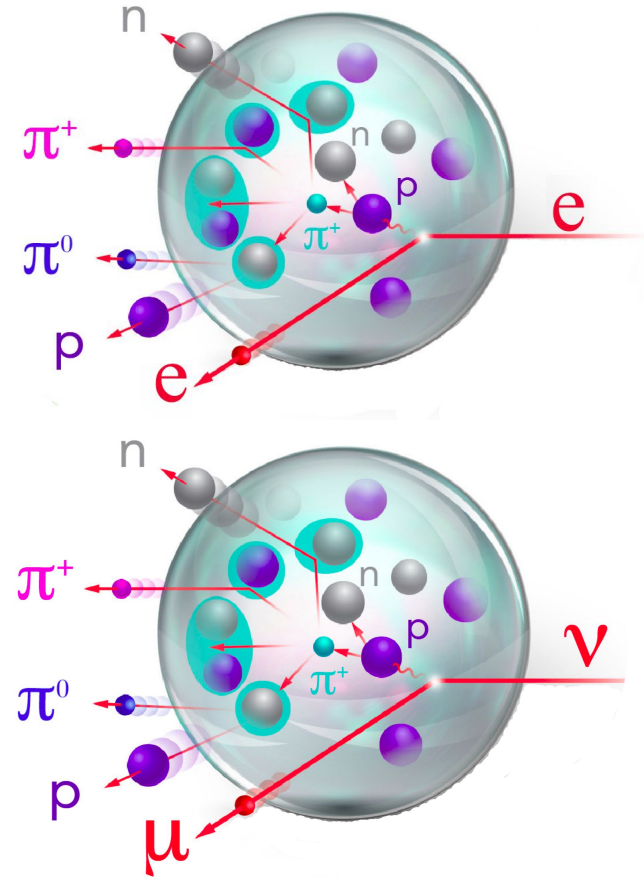
Nature 599, 565–570 (2021)

Phys. Rev. D 103, 113003 (2021)

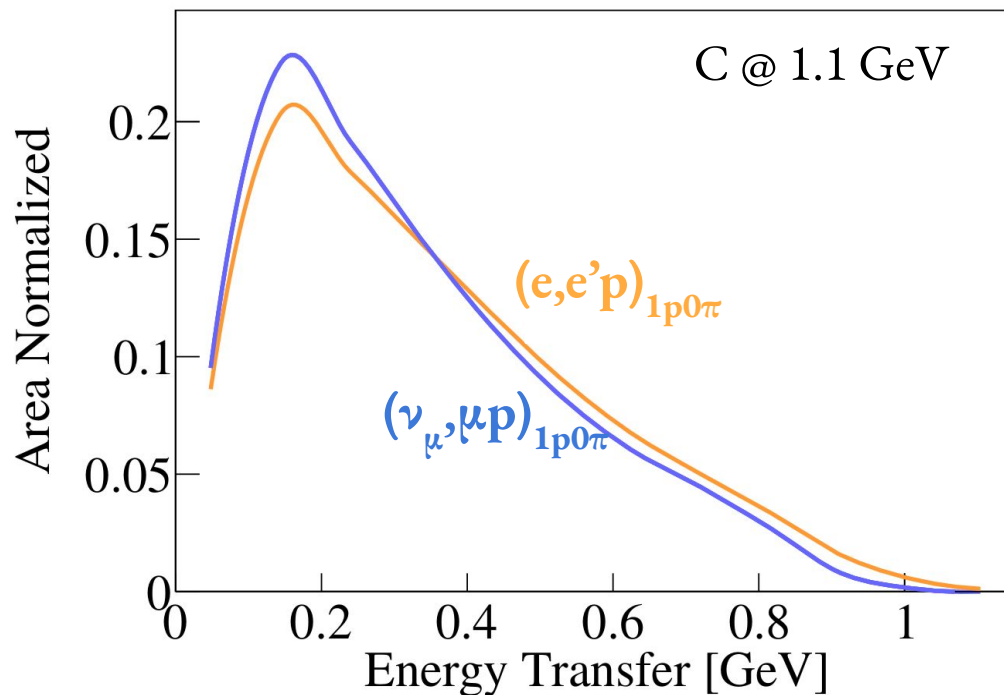
Why electrons?

- Common vector current
- Identical nuclear effects
- Monoenergetic beams
- High statistics
 - Precision measurements

Any model must work for electrons,
or it won't work for neutrinos !



Similar ν & e Distributions

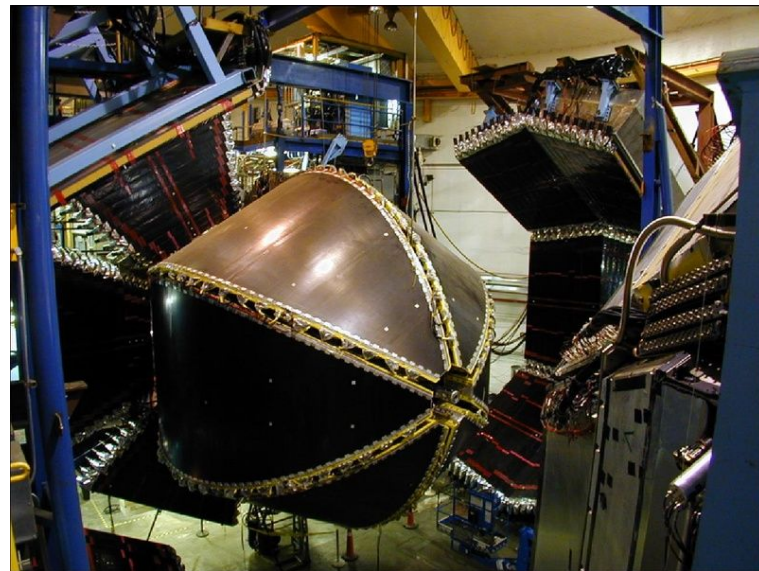


Accounting for propagator mass (γ vs W) via Q^4 scaling of the electron side

Jefferson Laboratory

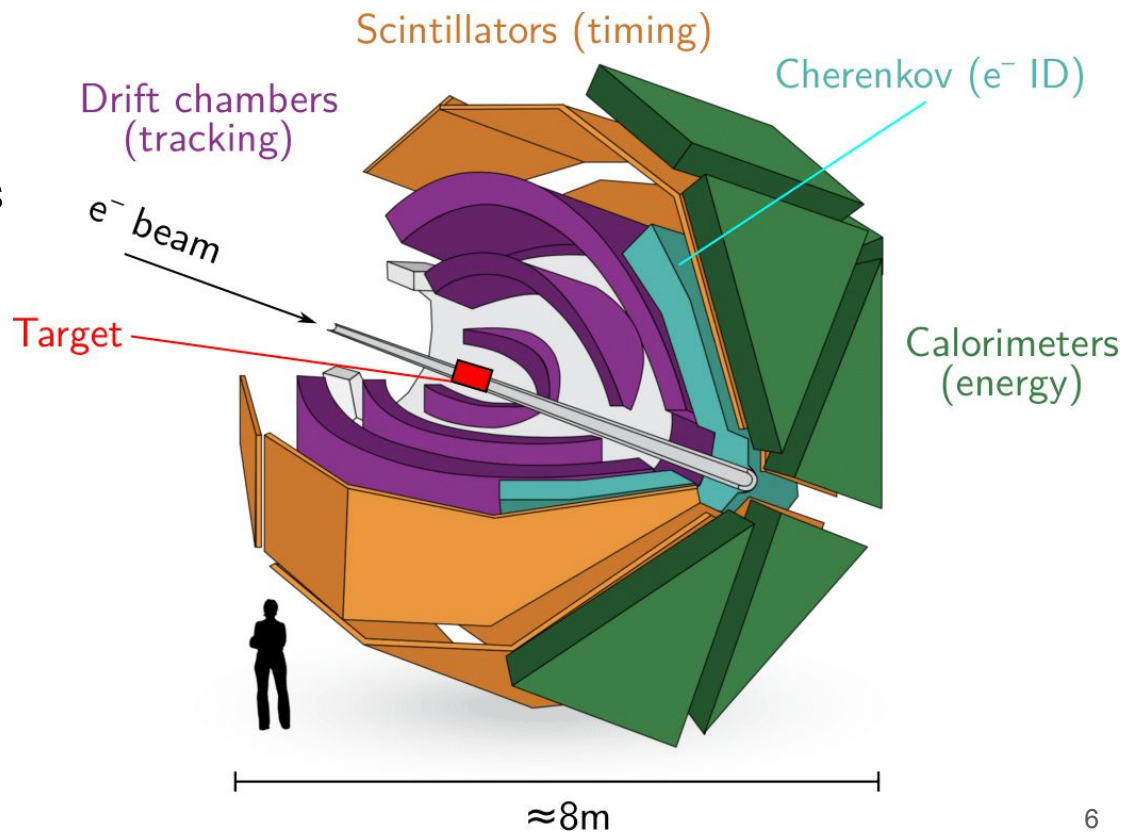


- Electron beam accelerator facility
- Energies up to 12 GeV
- Using Hall B & CLAS detector



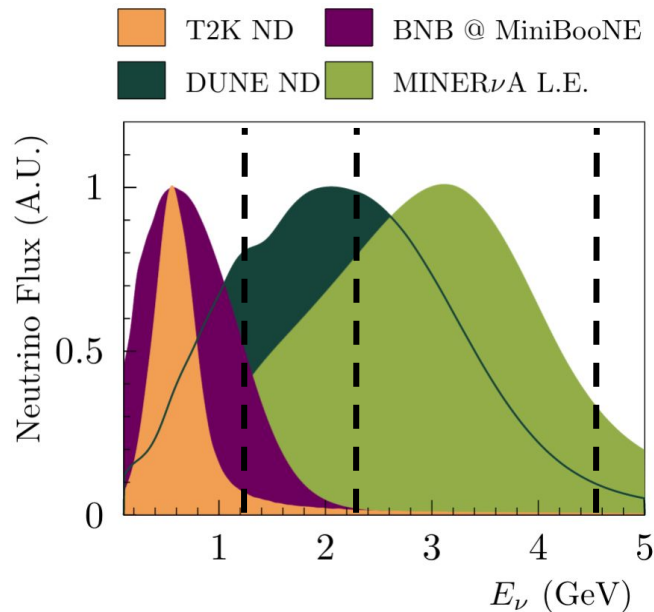
e4 ν Data-Mining With CLAS

- Charged particle threshold similar to ν tracking detectors
- ~50% of “ 4π ” coverage



e4 ν Data-Mining With CLAS

- Charged particle threshold similar to ν tracking detectors
- $\sim 50\%$ of “ 4π ” coverage
- Energies: 1, 2 & 4 GeV
- Targets: ^4He , ^{12}C , ^{56}Fe



H₂O

CH

Ar

Playing The QE-like Neutrino Game



- 1 proton ($> 300 \text{ MeV/c}$)
- No π^\pm ($> 70 \text{ MeV/c}$)

[Phys. Rev. Lett. 125, 201803 \(2020\)](#)

[arXiv:2301.03706](#)

[arXiv:2301.03700](#)

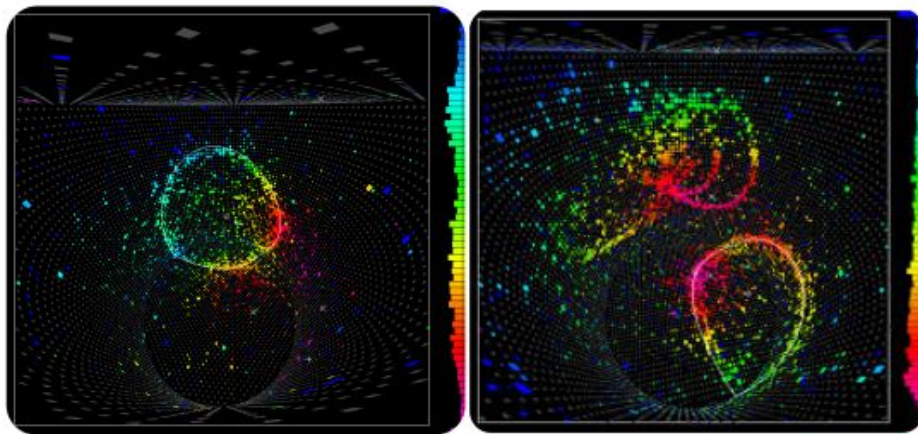


- 1 proton ($> 300 \text{ MeV/c}$)
- No π^\pm ($> 150 \text{ MeV/c}$)
- Scale by $\sigma_{\nu N} / \sigma_{eN} \propto Q^4$

[Nature 599, 565–570 \(2021\)](#)

- Study energy reconstruction
- Test against GENIE event generator

QE Energy Reconstruction

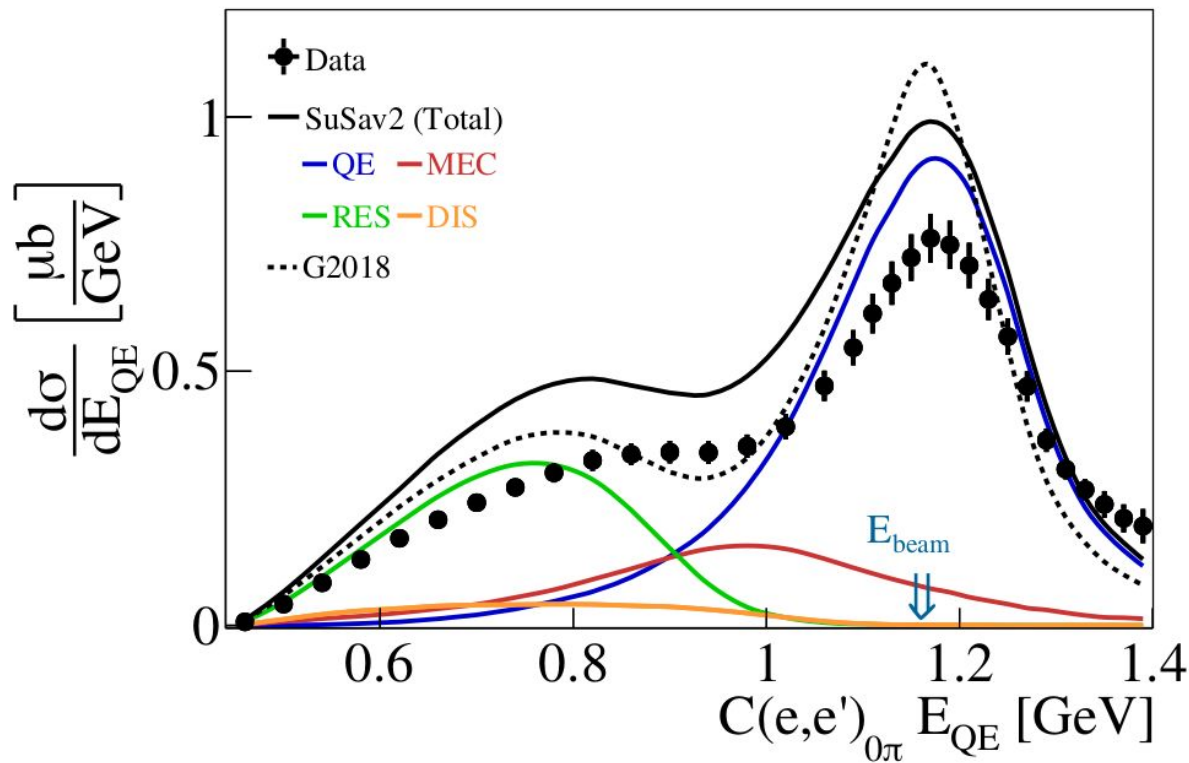


Cherenkov detectors
Assuming QE interaction
Using lepton kinematics

$$E_{QE} = \frac{2M\epsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|\cos\theta_l)}$$

QE Energy Reconstruction

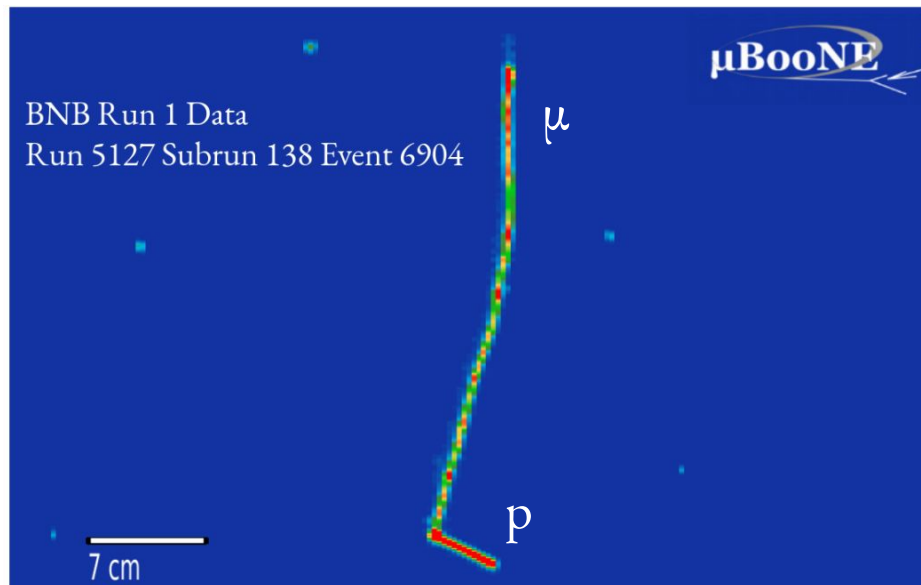
C @ 1.16 GeV



- Relevant for T2K
- Overestimation of
QE peak & RES tail

$$E_{QE} = \frac{2M\epsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|\cos\theta_l)}$$

Calorimetric Energy Reconstruction



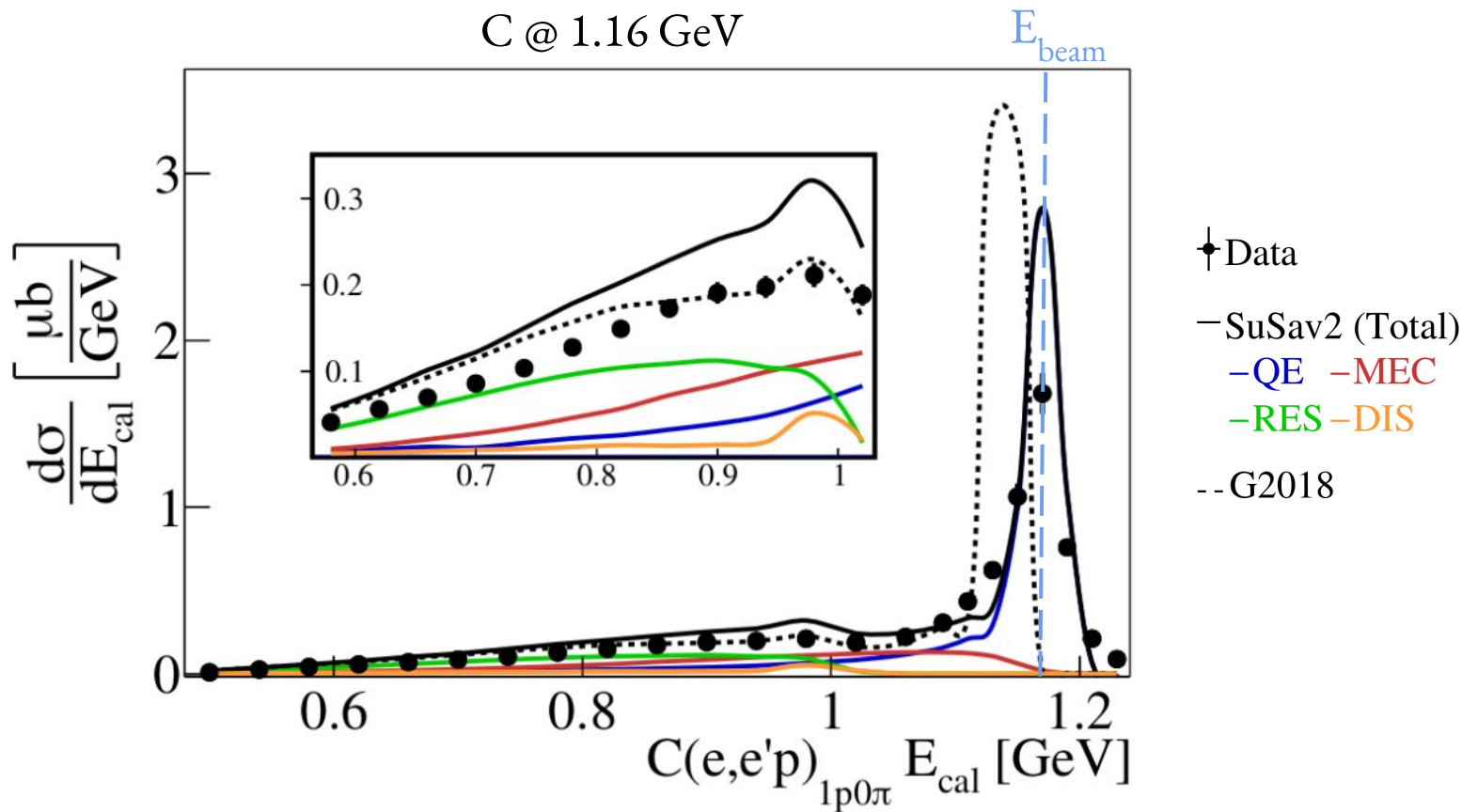
Tracking detectors

Calorimetric sum

Using all detected particles

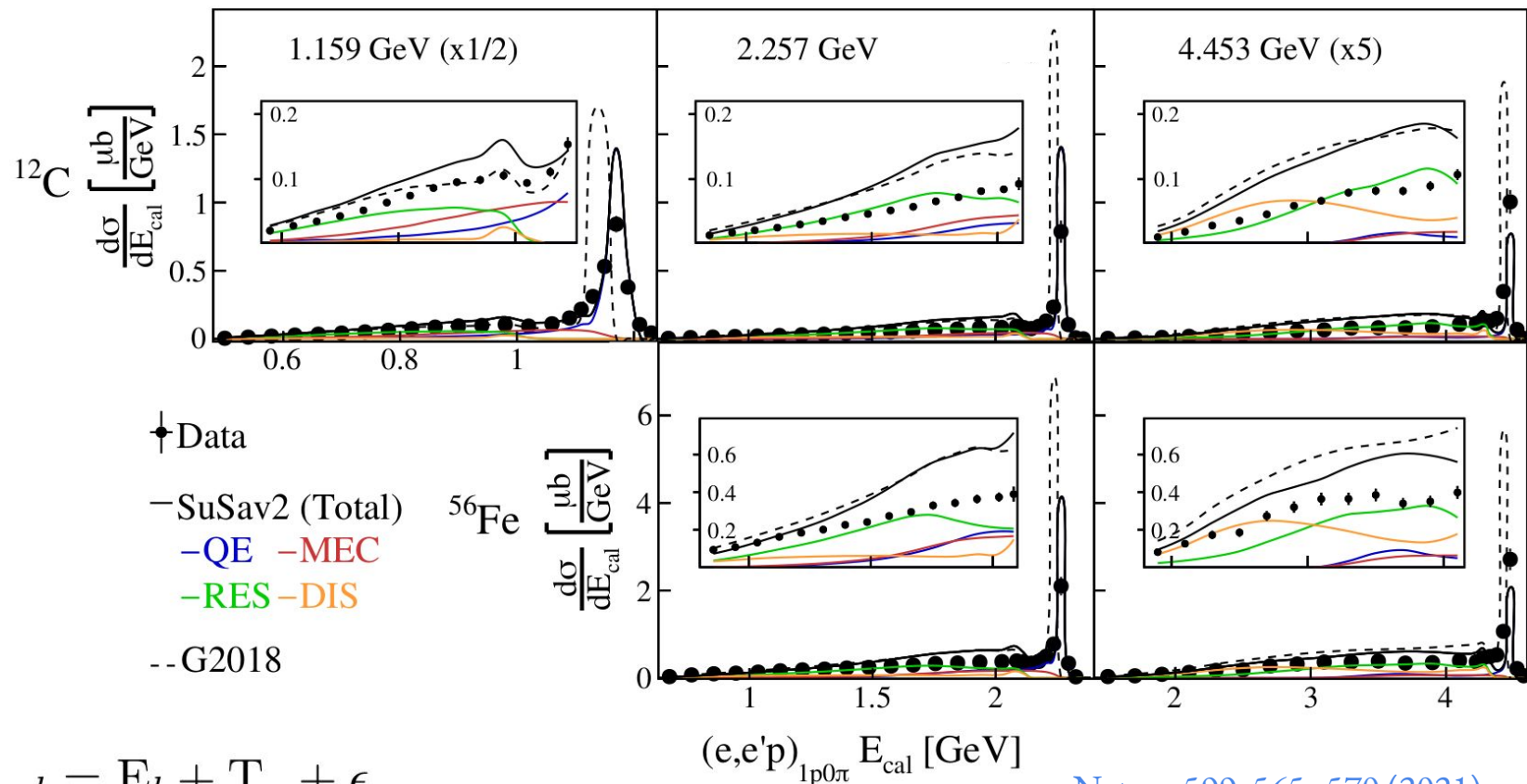
$$E_{cal} = E_l + T_p + \epsilon_B$$

Calorimetric Energy Reconstruction



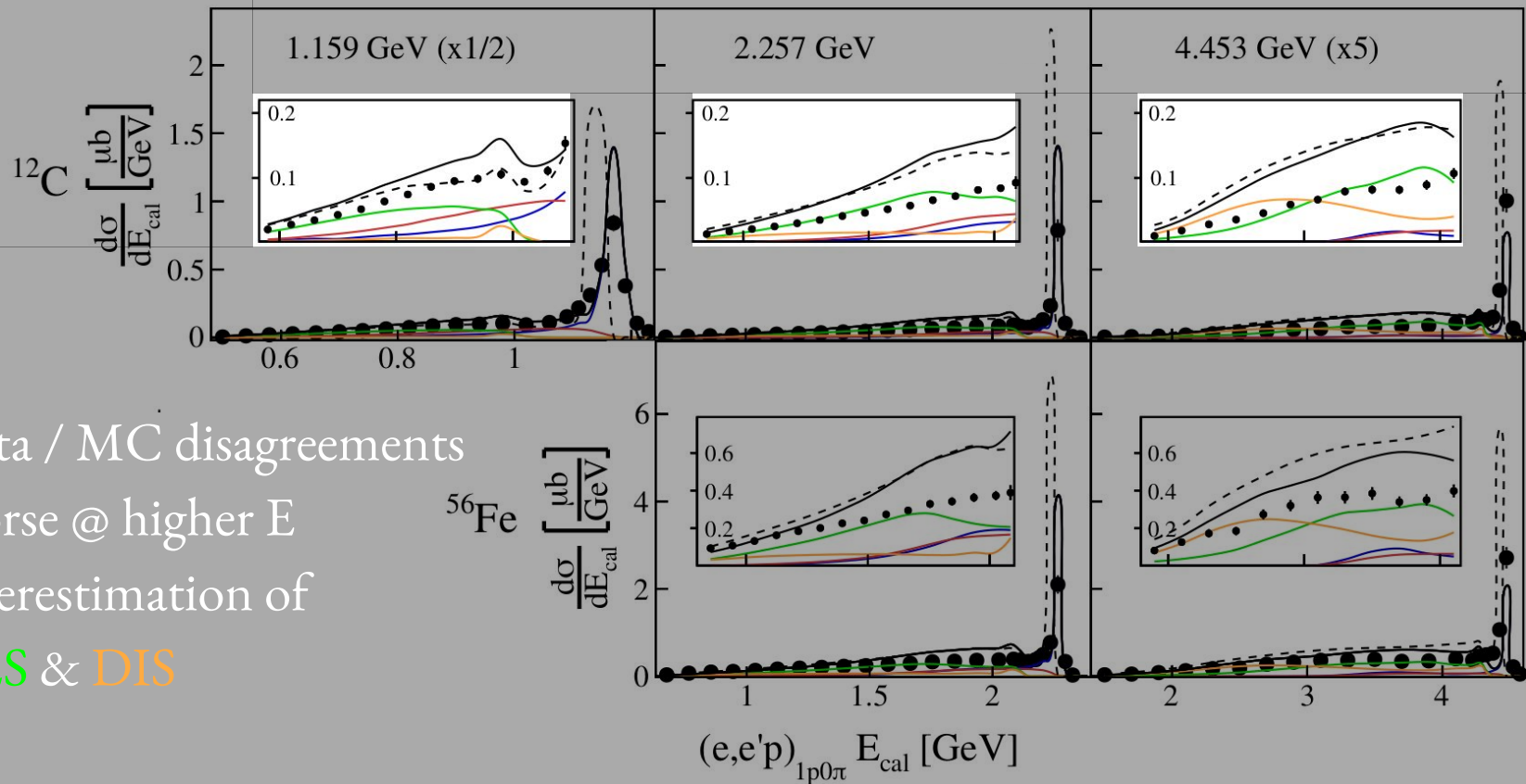
$$E_{cal} = E_l + T_p + \epsilon$$

E_{cal} Nucleus & Energy Dependence



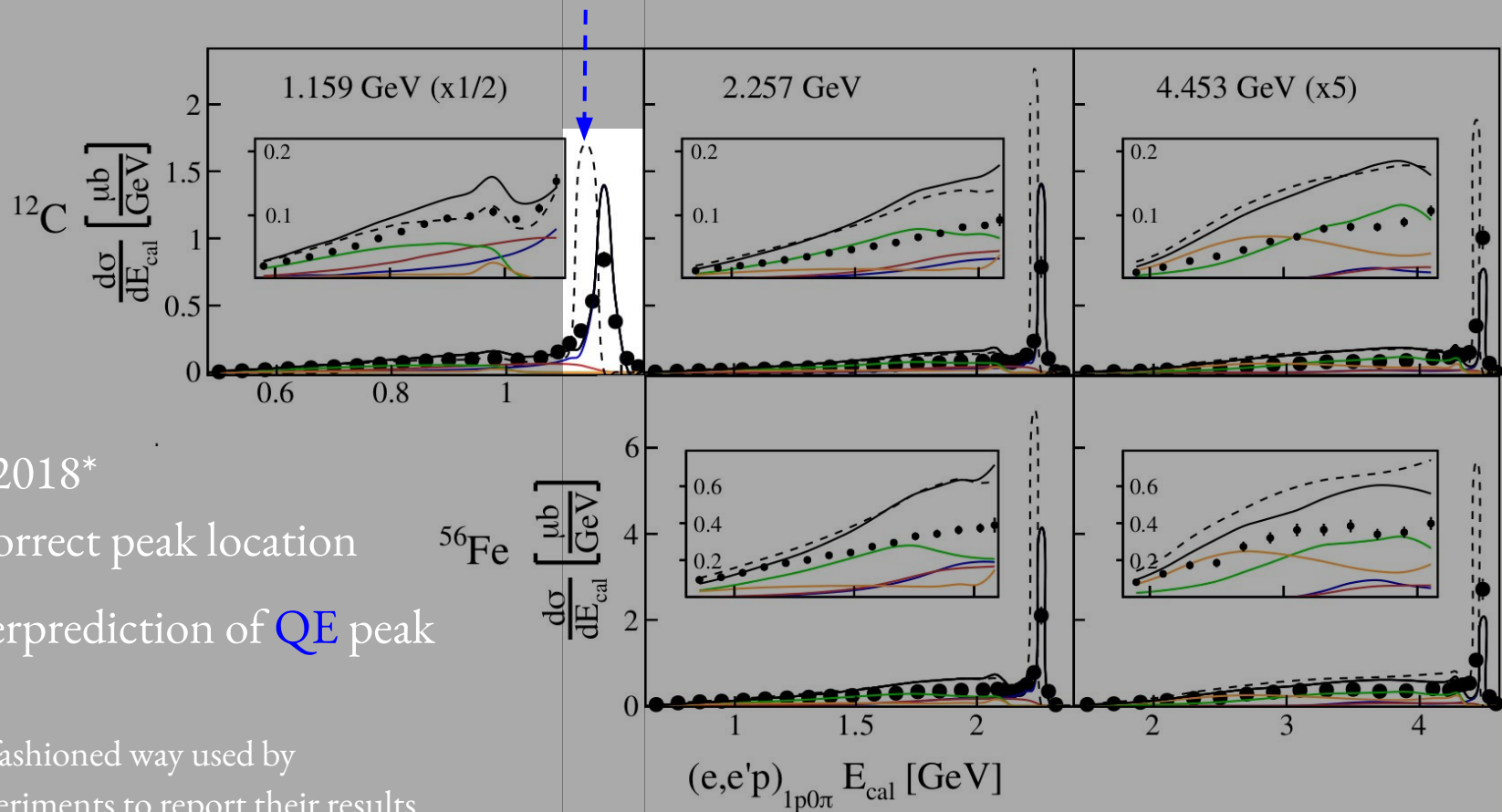
$$E_{cal} = E_l + T_p + \epsilon$$

Nucleus & Energy Dependence



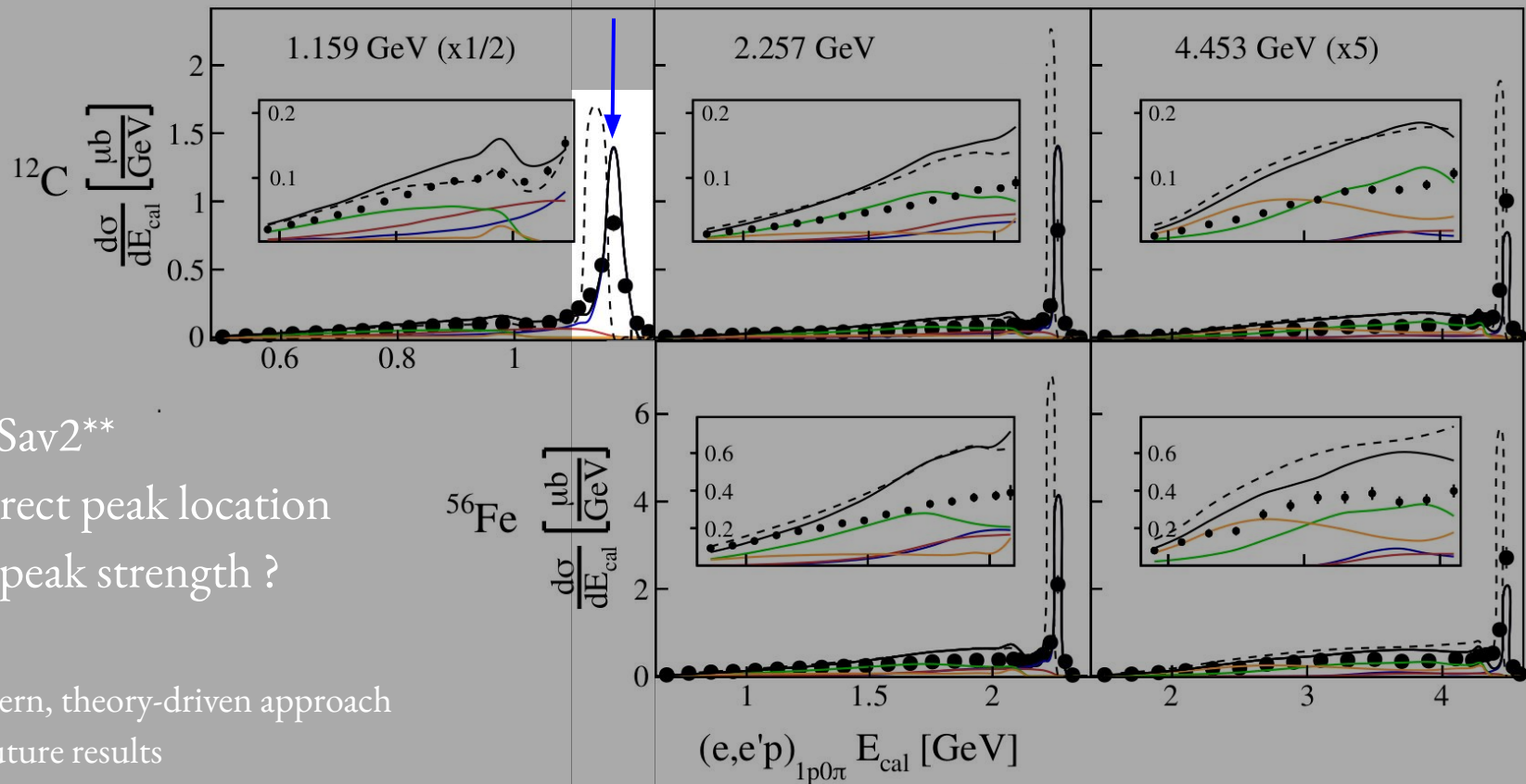
- Data / MC disagreements
- Worse @ higher E
- Overestimation of
RES & DIS

Nucleus & Energy Dependence



* Old-fashioned way used by ν experiments to report their results

Nucleus & Energy Dependence

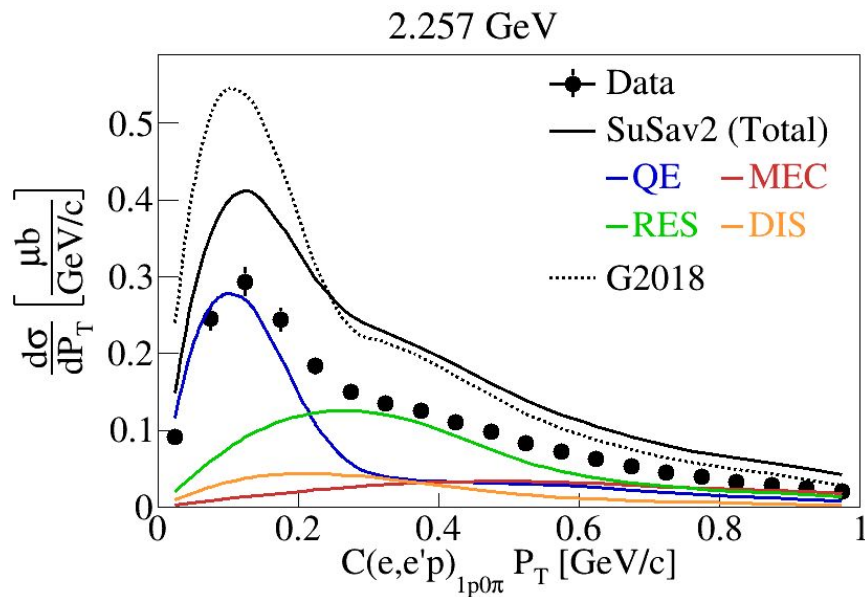


— SuSav2**

- Correct peak location
- QE peak strength ?

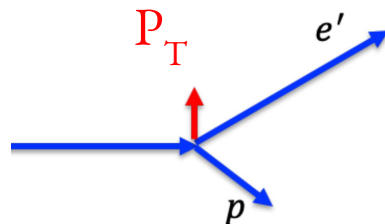
** Modern, theory-driven approach
for future results

Transverse Momentum



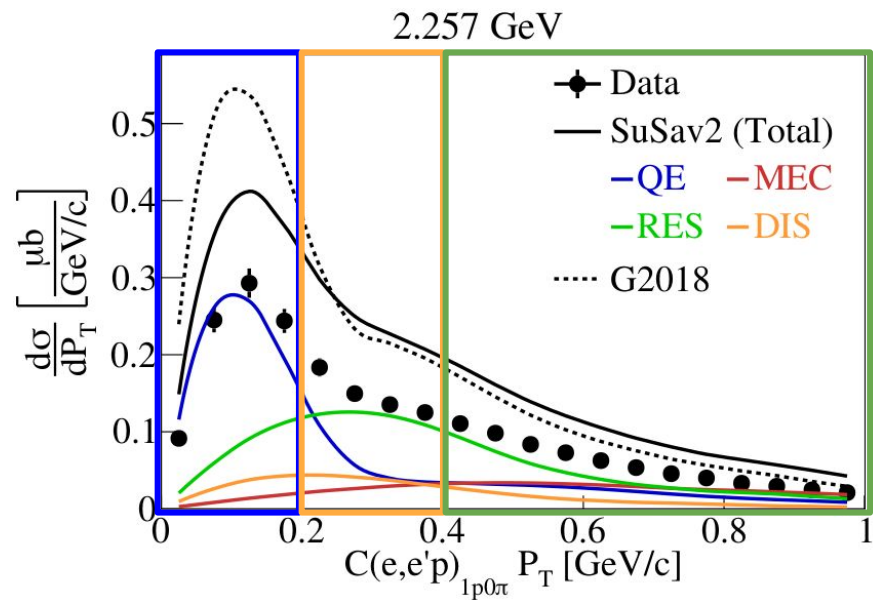
Nature 599, 565–570 (2021)

$$P_T = | \mathbf{P}_T^{e'} + \mathbf{P}_T^p |$$

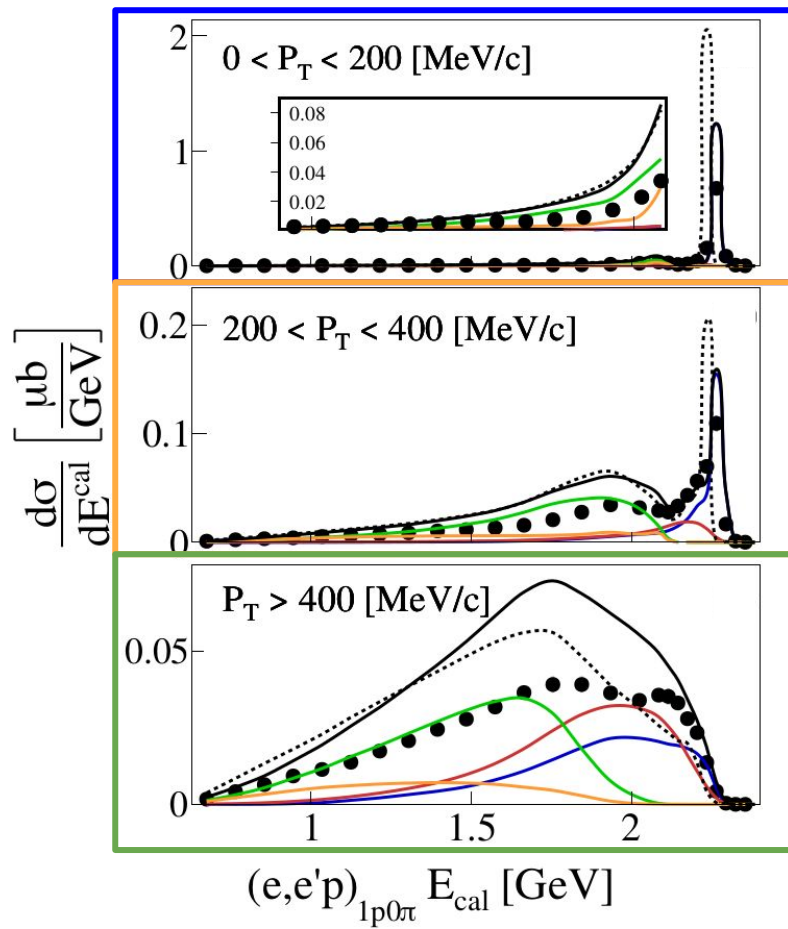


- P_T sensitivity to nuclear effects (fermi motion, final-state interactions, ...)
- Overestimation of QE peak & RES tail

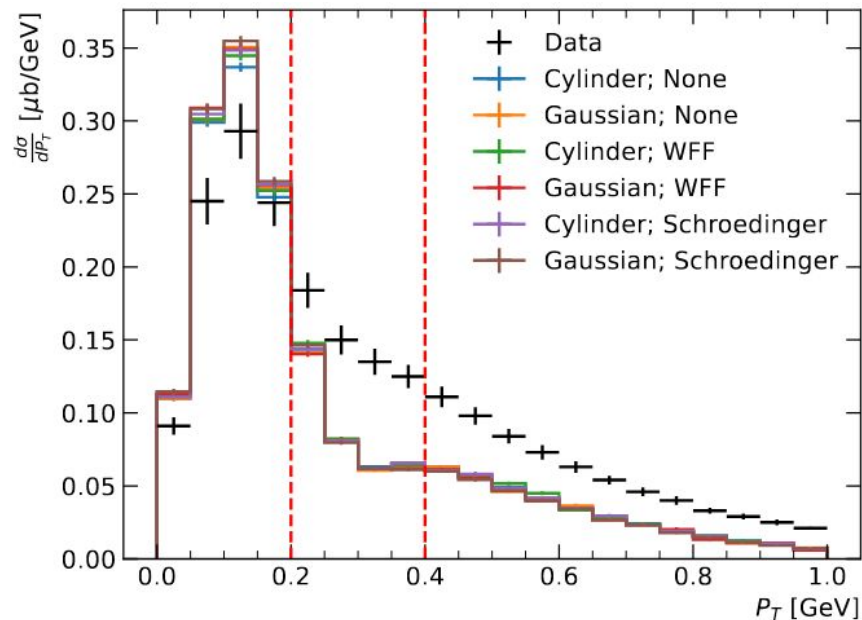
Energy Reconstruction In P_T Slices



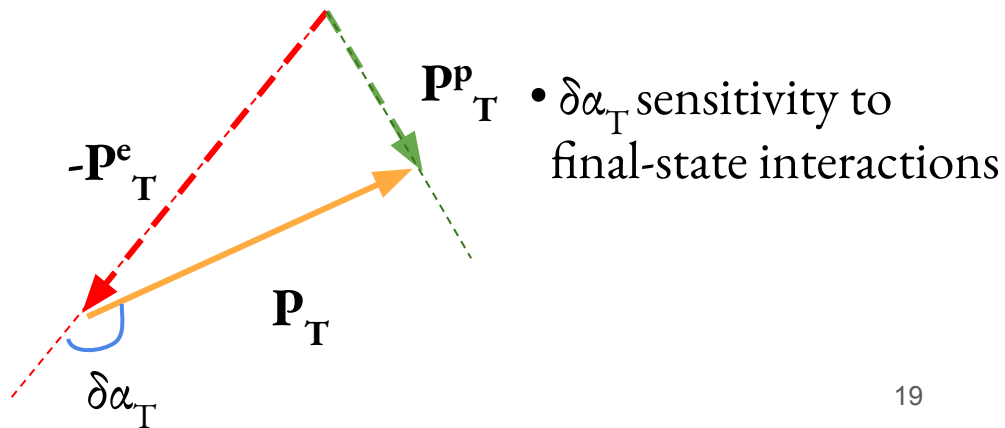
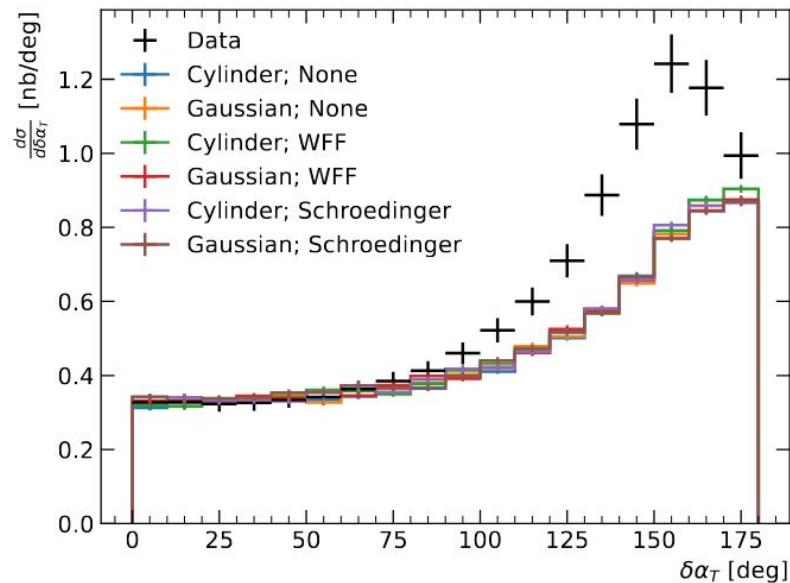
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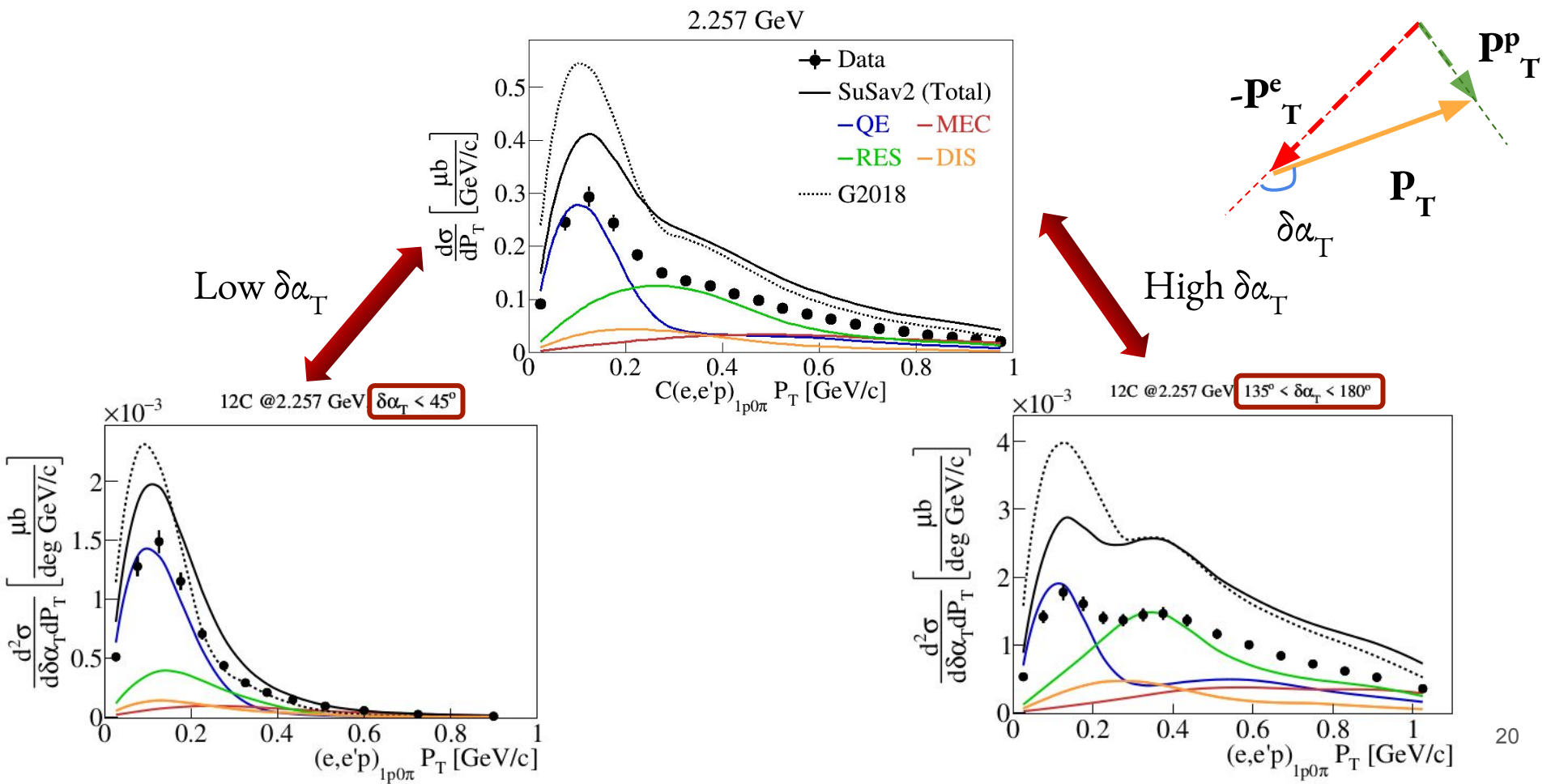
Example: Benchmarking New Generators & Kinematic Variables!



First step: only QE & FSI
 ACHILLES arXiv: 2205.06378

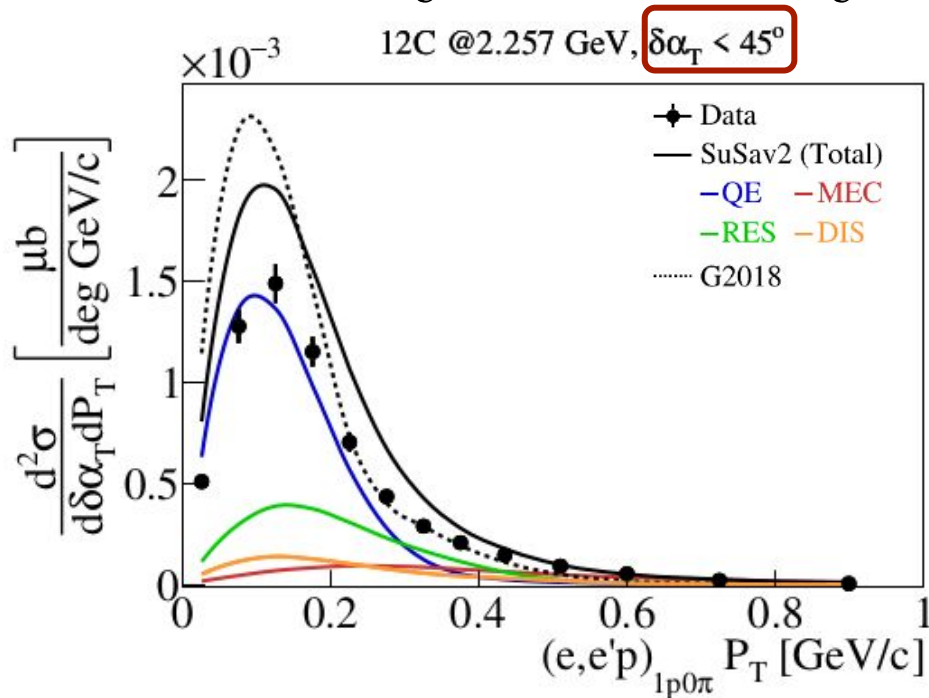


Example: 2D Kinematic Imbalance

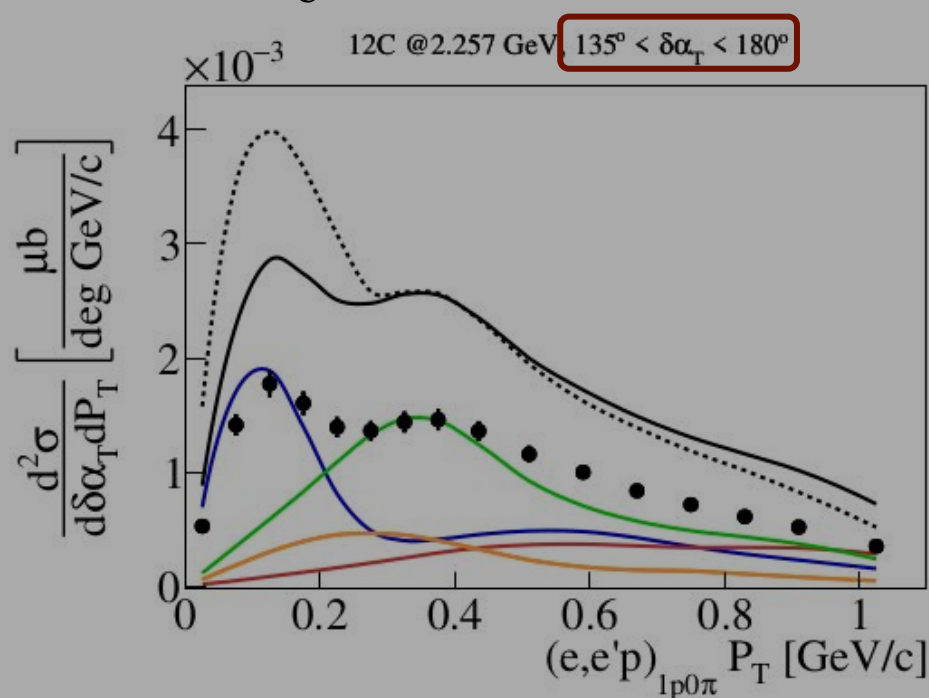


Example: 2D Kinematic Imbalance

Low $\delta\alpha_T$
QE-enhanced region
Sensitive to ground-state modeling

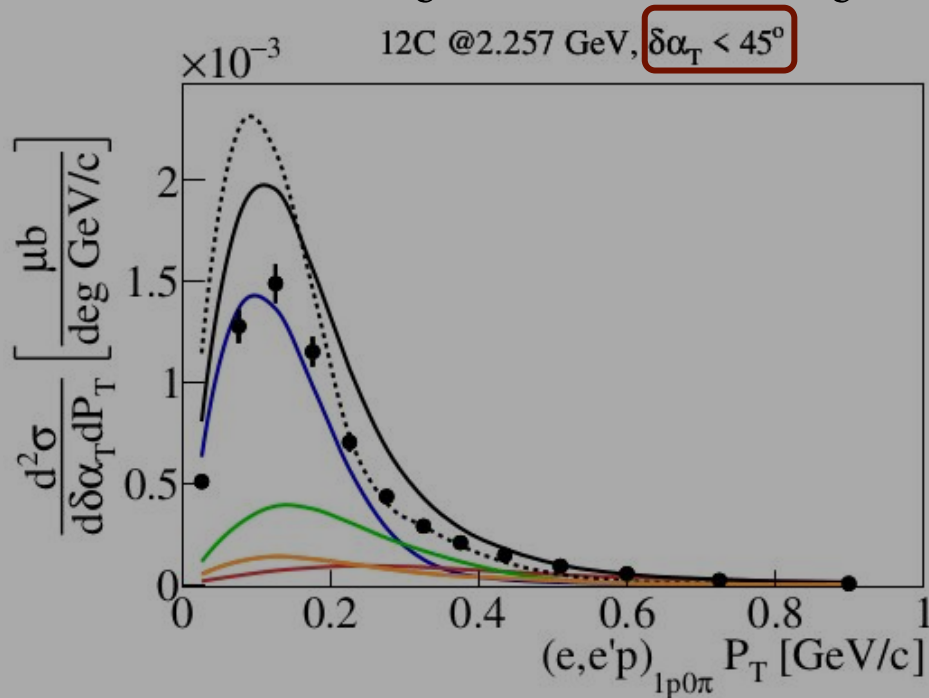


High $\delta\alpha_T$
Large non-QE contributions
Strong final-state interaction effects

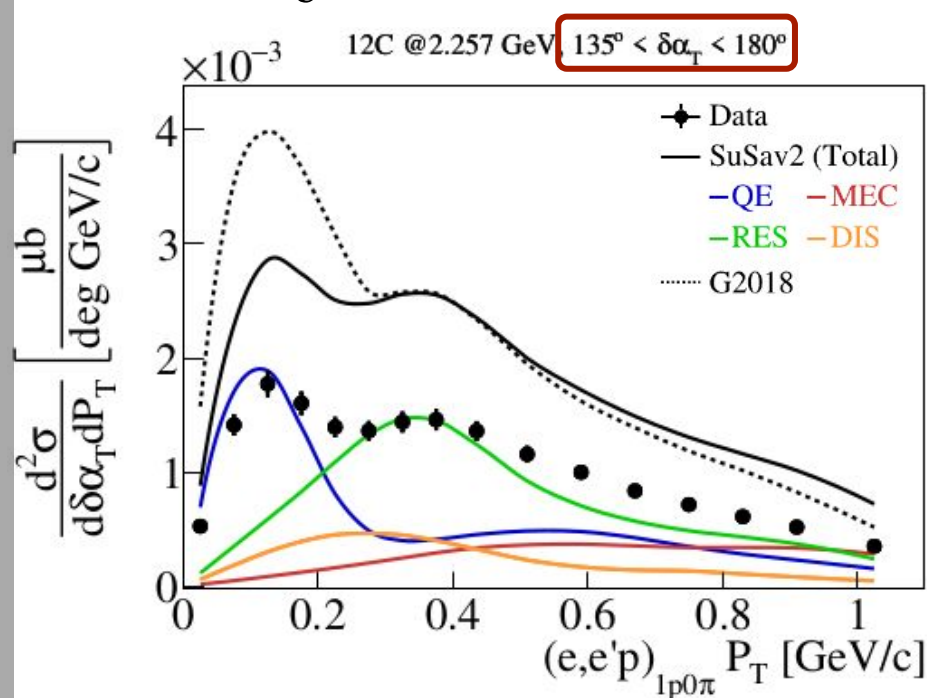


Example: 2D Kinematic Imbalance

Low $\delta\alpha_T$
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Complementarity To “Sister” Neutrino Analysis

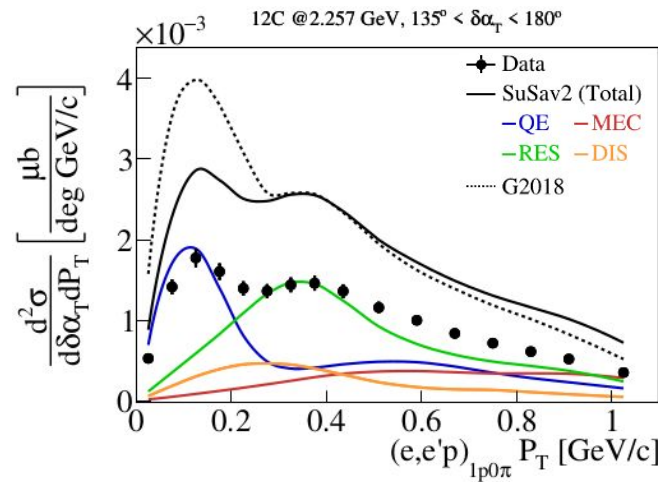
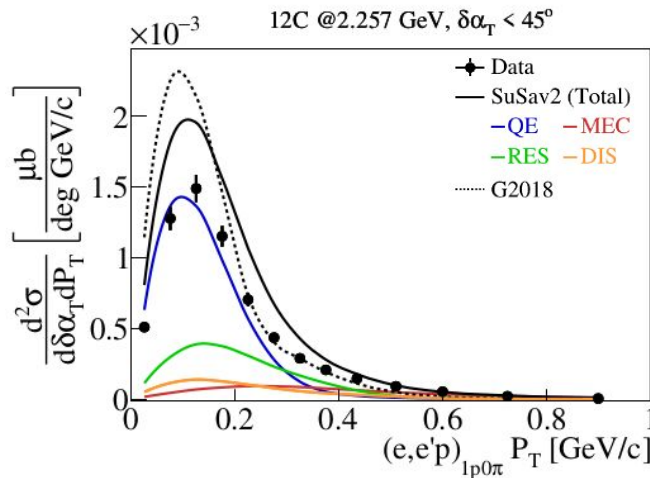
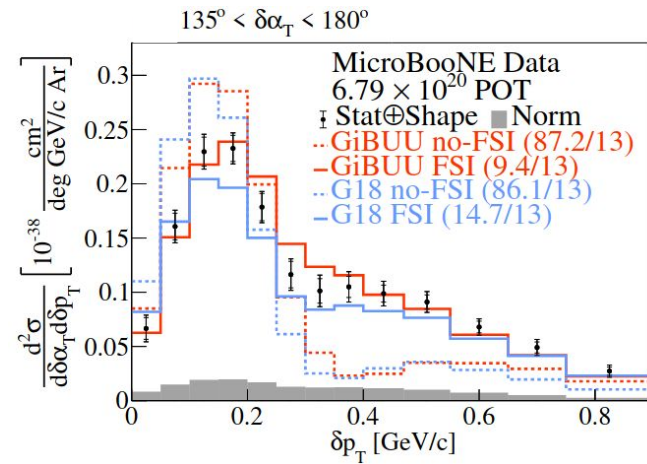
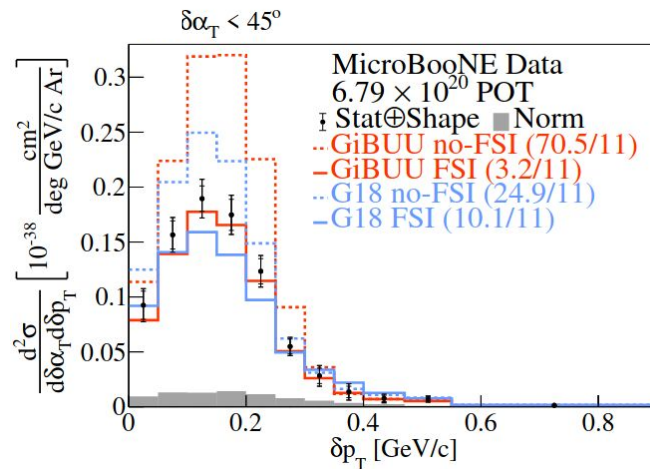
μBooNE



arXiv:2301.03706

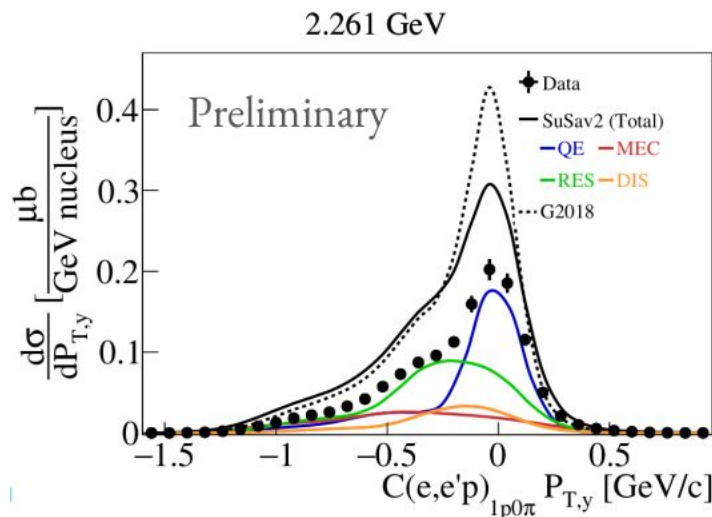
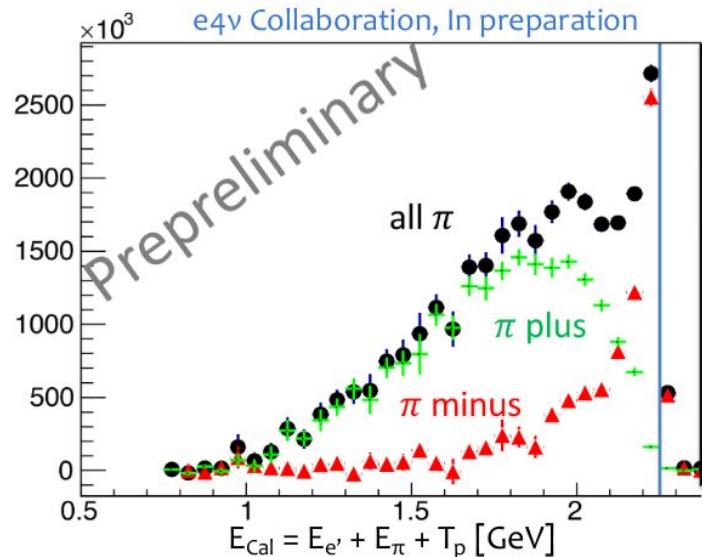
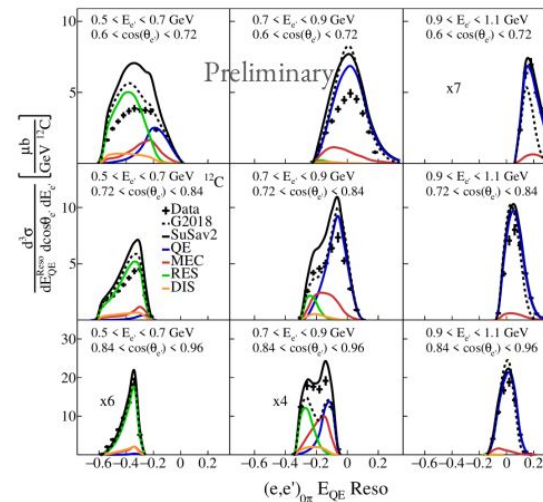
arXiv:2301.03700

e4ν



Next Steps

- Even more differential! Into the 3D multiverse
Taking advantage of massive statistics
- More nuclear sensitivity variables
Help decide what to tune
- $1p1\pi$ exclusive cross sections



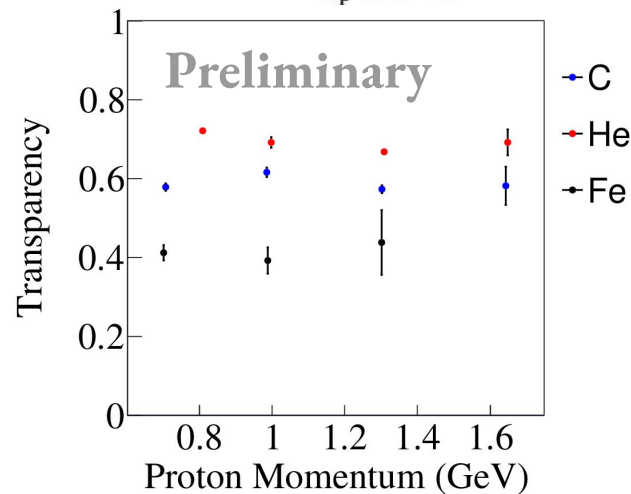
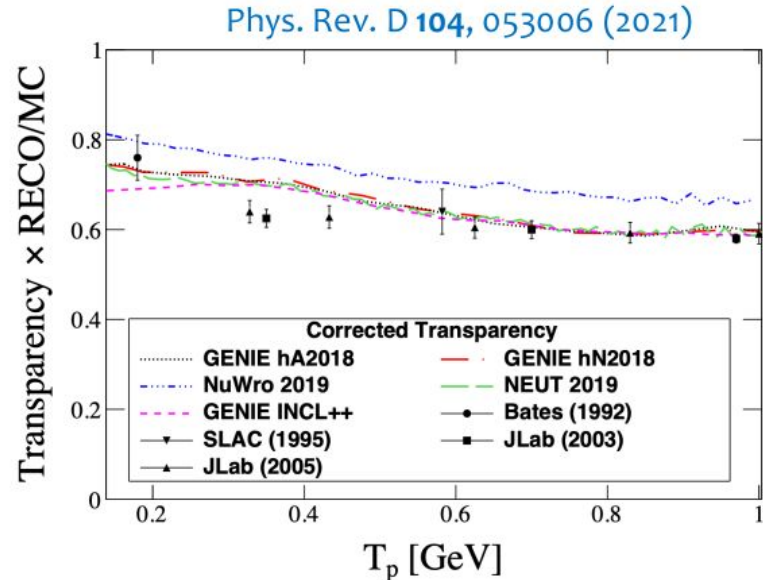
Next Steps

- More with CLAS6



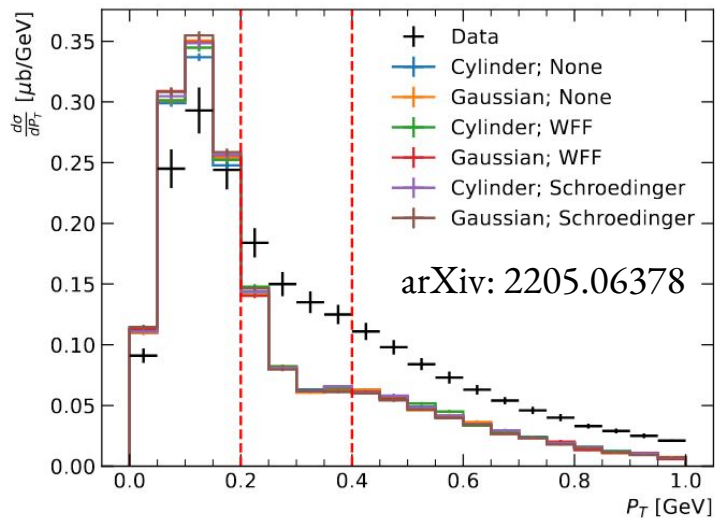
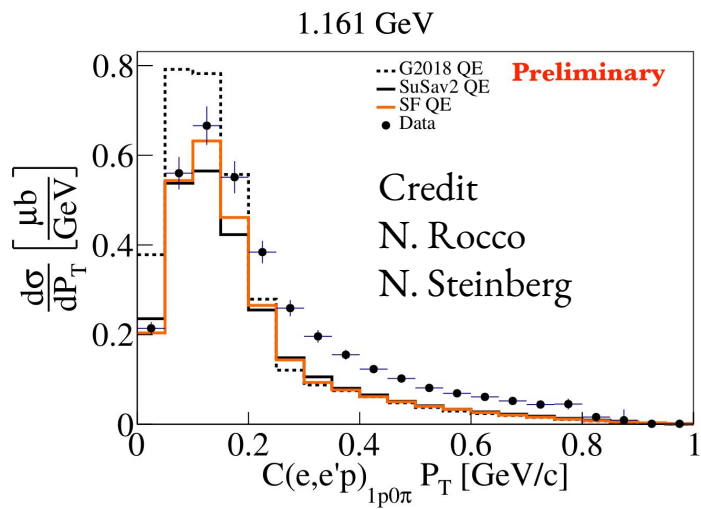
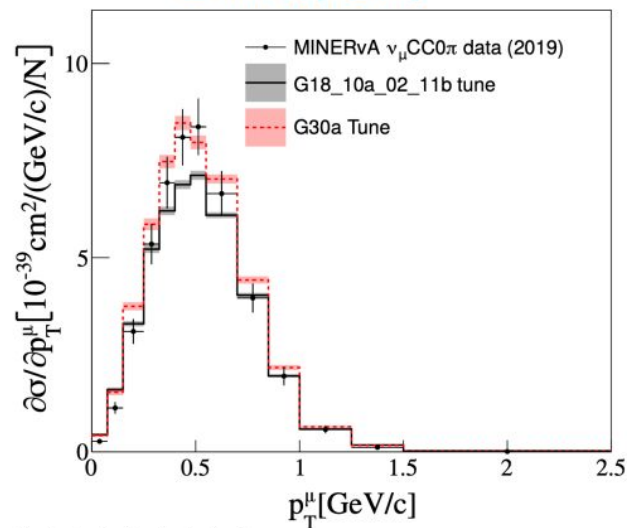
Proton transparency studies

- Observable that summarizes strength of intranuclear rescattering
- Measurement study
$$T = N_{\text{prot}}^{\text{detected}} / N_{\text{prot}}^{\text{PWIA}}$$
- Test event generator FSI models in GENIE across multiple nuclear targets
- Testing dependency of transparency calculations on PWIA normalization



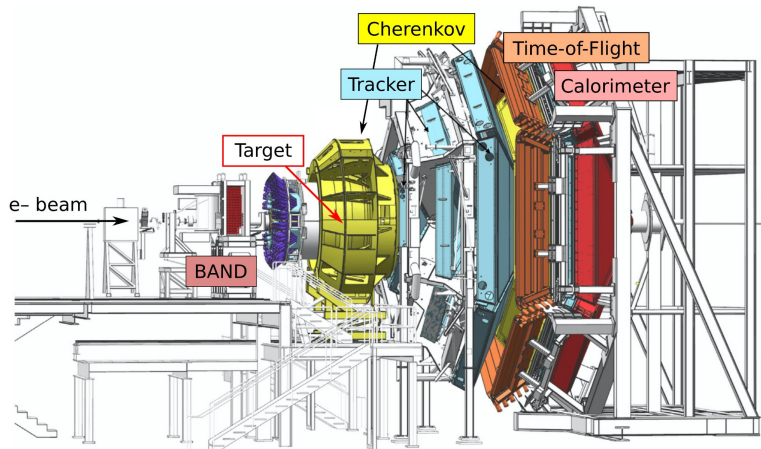
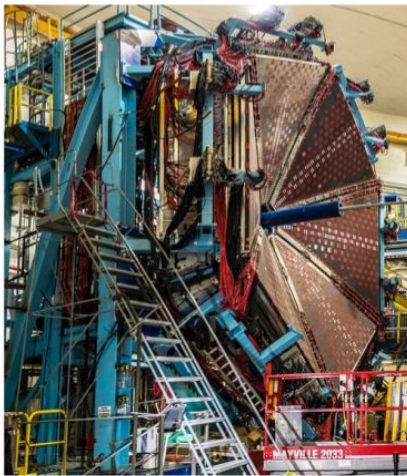
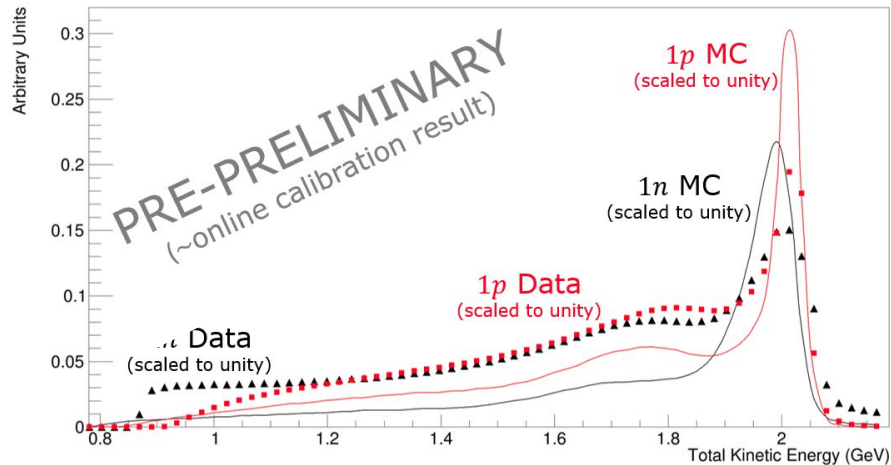
Next Steps

- More with CLAS6
- ❑ Prepare suite of cross sections in same variables as neutrinos for first e-GENIE tune
 - Compare with neutrino CC0 π tune
- $e4\nu$ data already being used to validate event generators



Next Steps

- New data with CLAS12
Targets: ^4He , ^{12}C , ^{40}Ar , ^{120}Sn
- 2 - 6 GeV beam energies
- More phase-space coverage ($\theta_e > 5^\circ$)
- Neutrons!

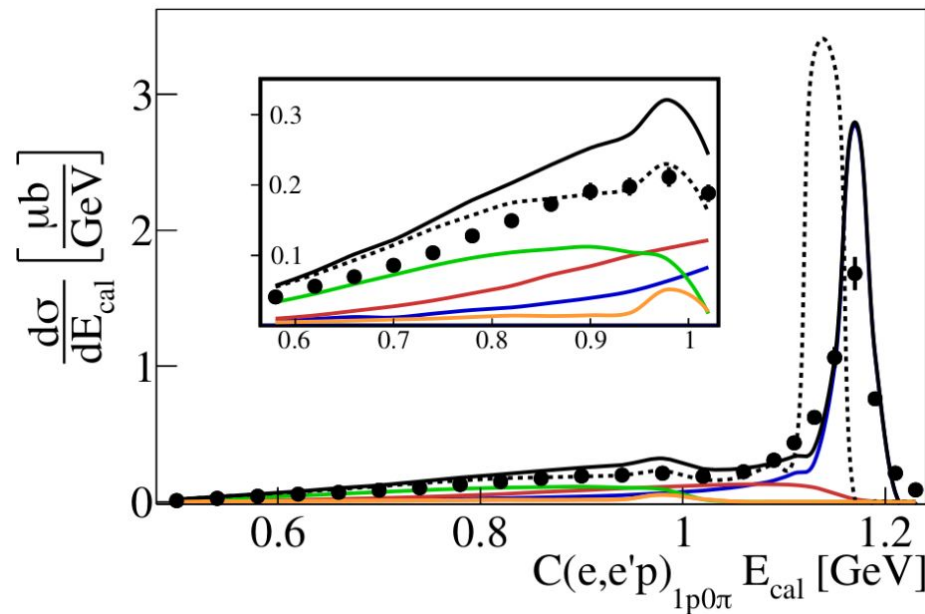


Summary

- First use of electron data to test ν event generators

www.e4nu.com

- Data/MC disagreement even for simple $1p0\pi$ events
- Identified regions requiring modeling improvements
- Excited for new results and new interpretations
- *e4ν* result factory continuing to churn!

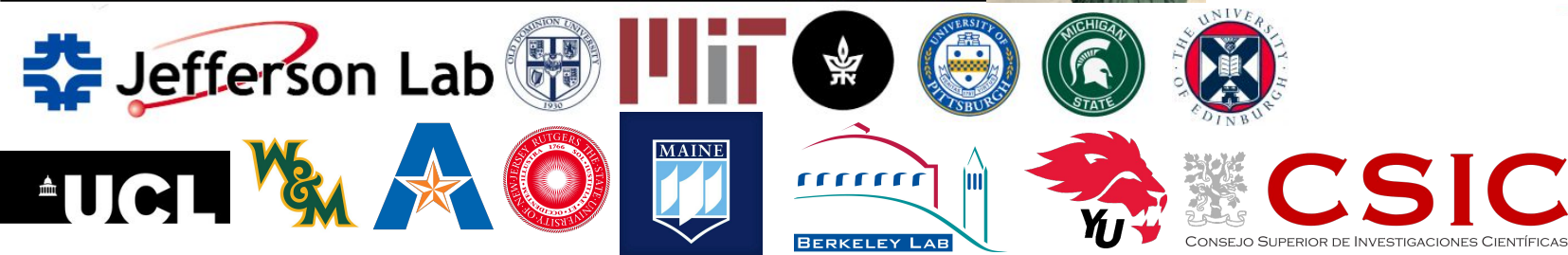


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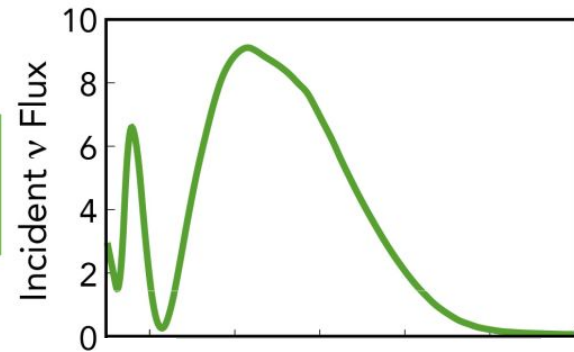
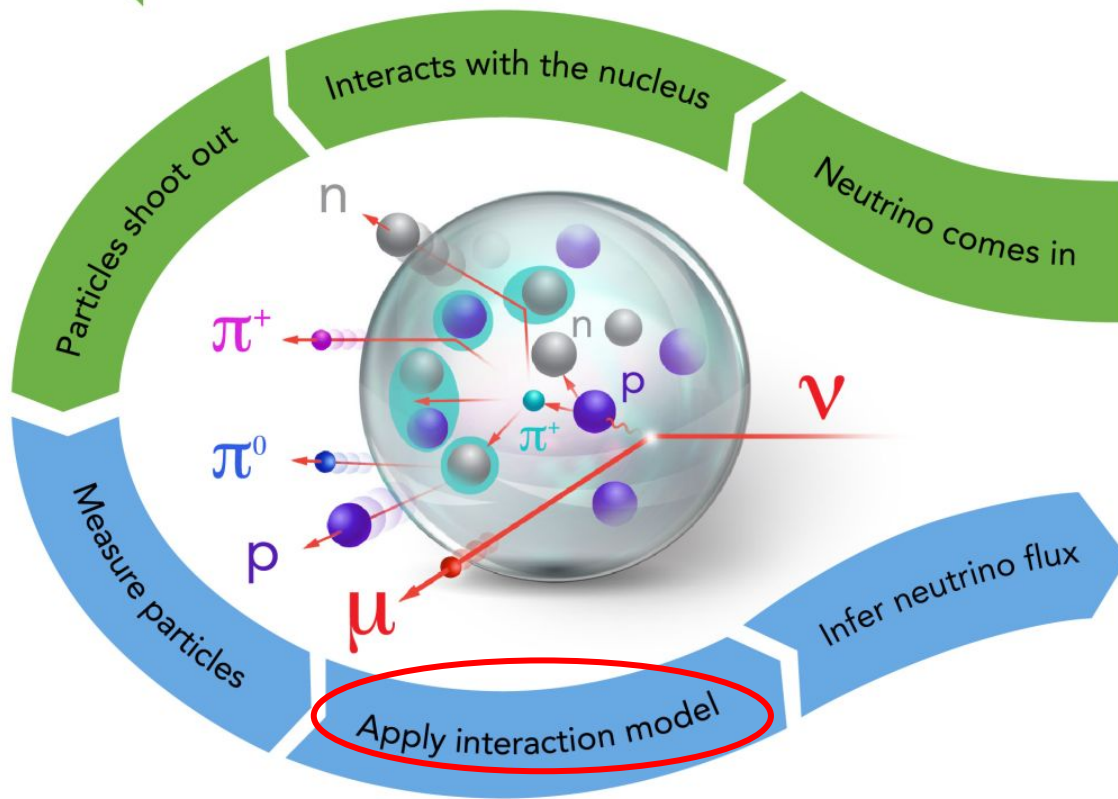
Thank you !

e4V



Backup Slides

PHYSICS PROCESS

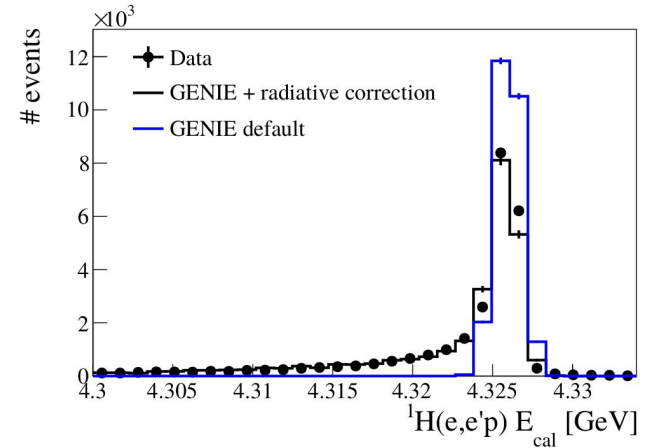


EXPERIMENTAL ANALYSIS

Cross-Section Extraction

- Subtract backgrounds
- Scale counts by luminosity
- Correct for detector acceptance & radiation

Systematic uncertainties on each correction plus variation among detector sectors

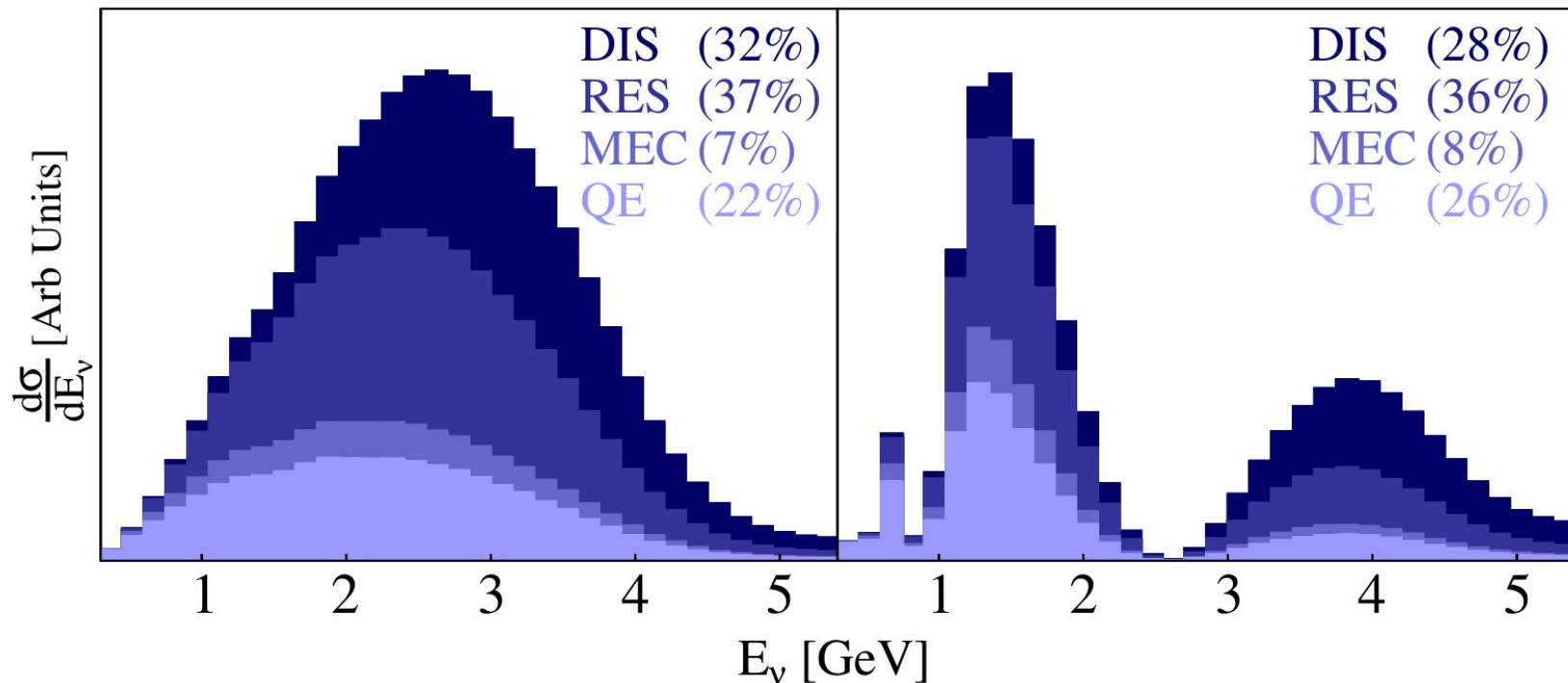


Hall A@ JLab

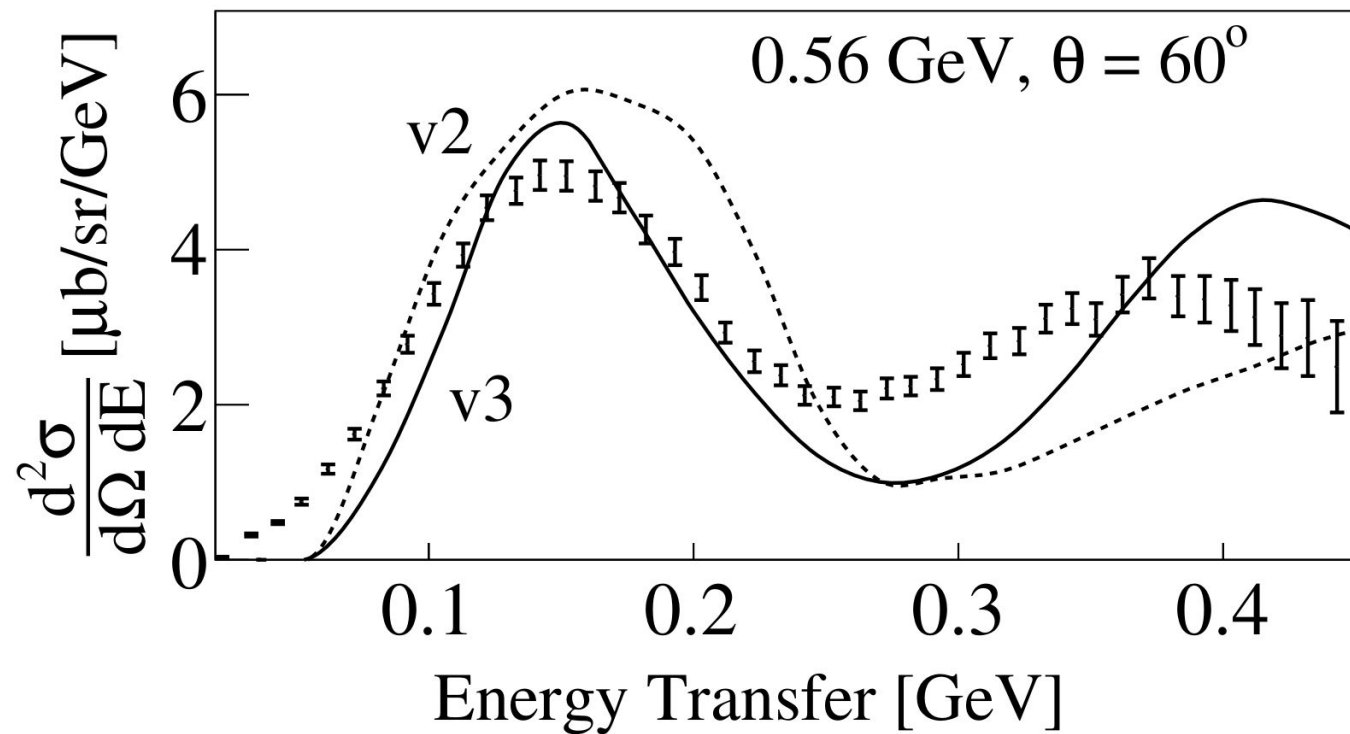
$\text{H}(e,e'p)$ @ 4.32 GeV

Mismodelling Impact On Mixing Parameters

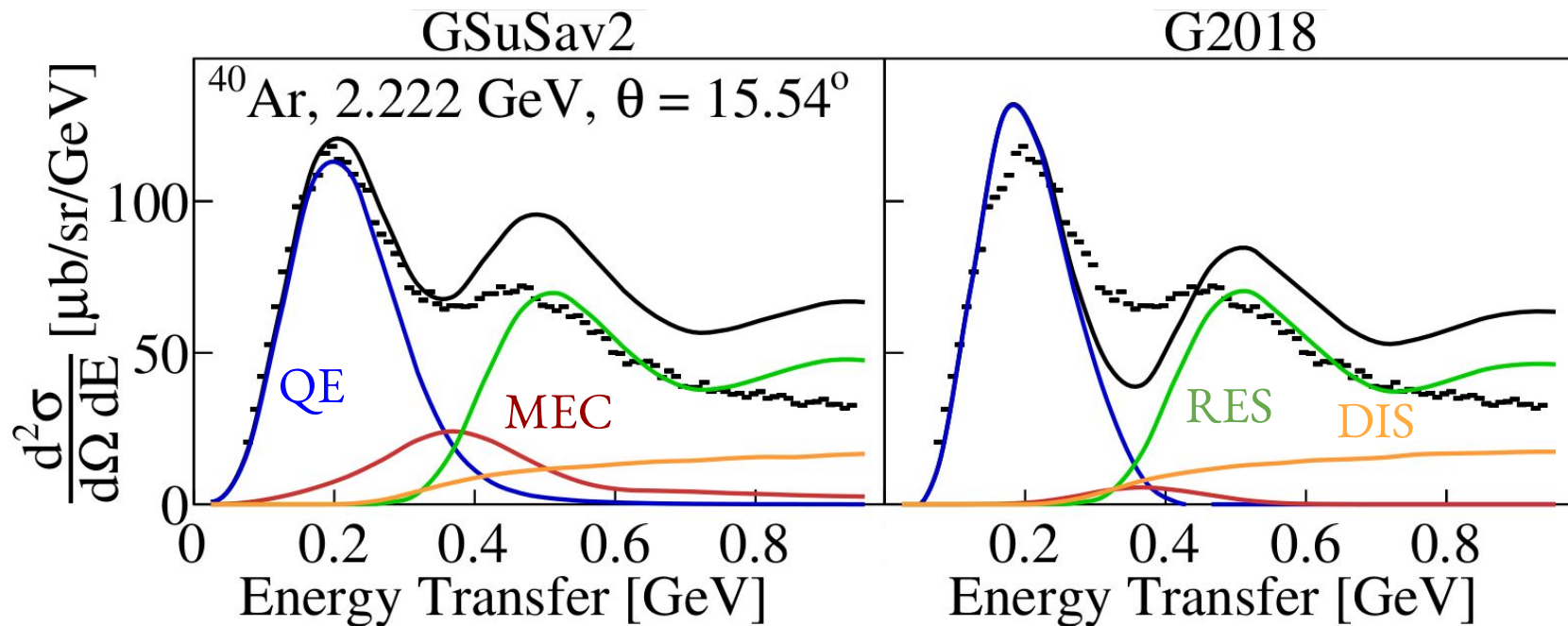
Charged current cross sections obtained using GENIE for the DUNE near detector (left) and far detector (right) oscillated fluxes



(e,e') ^{12}C with G2018

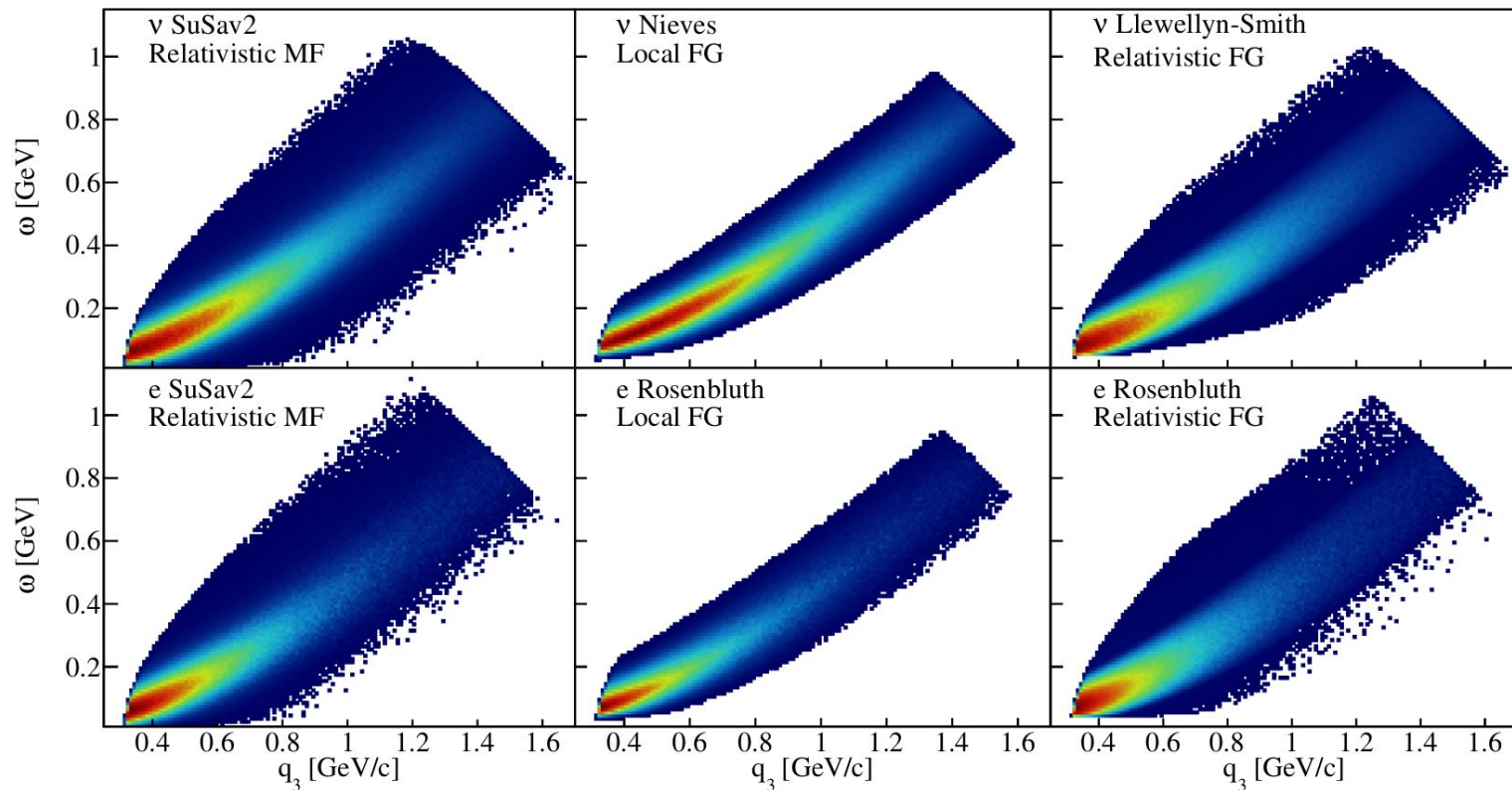


SuSav2 Offers More Accurate Prediction



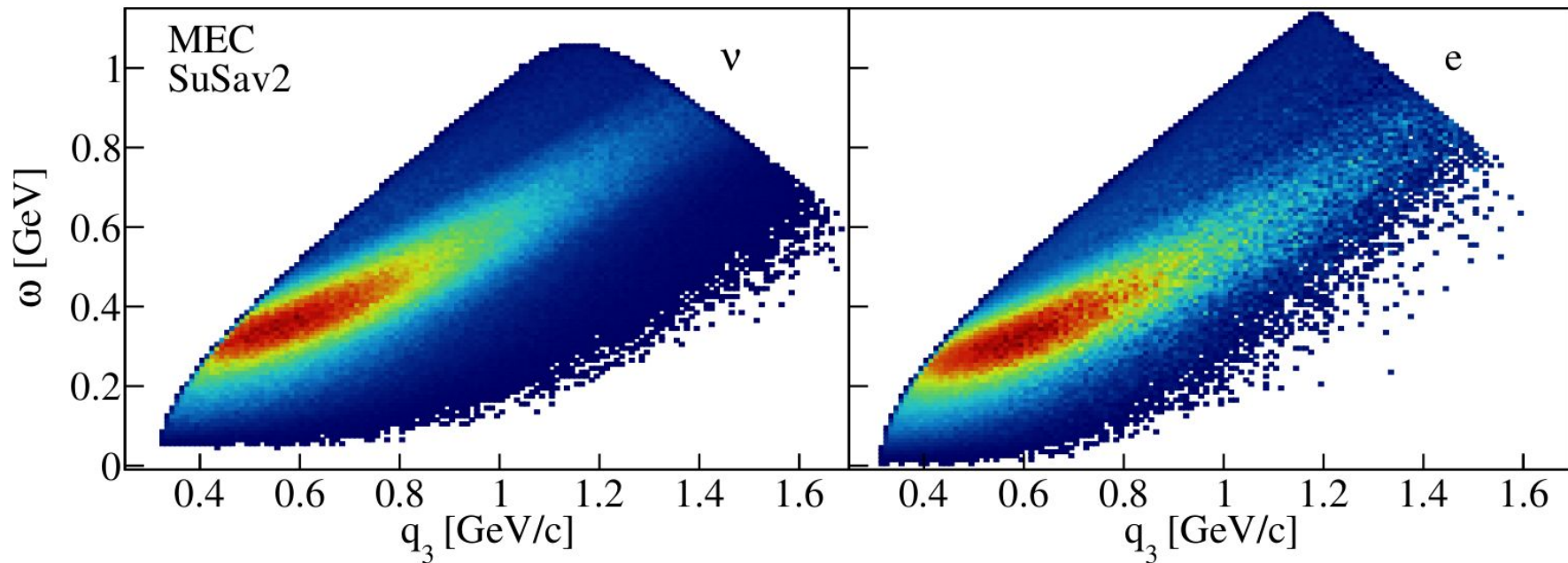
Probing The Neutrino Phase-Space With Electrons

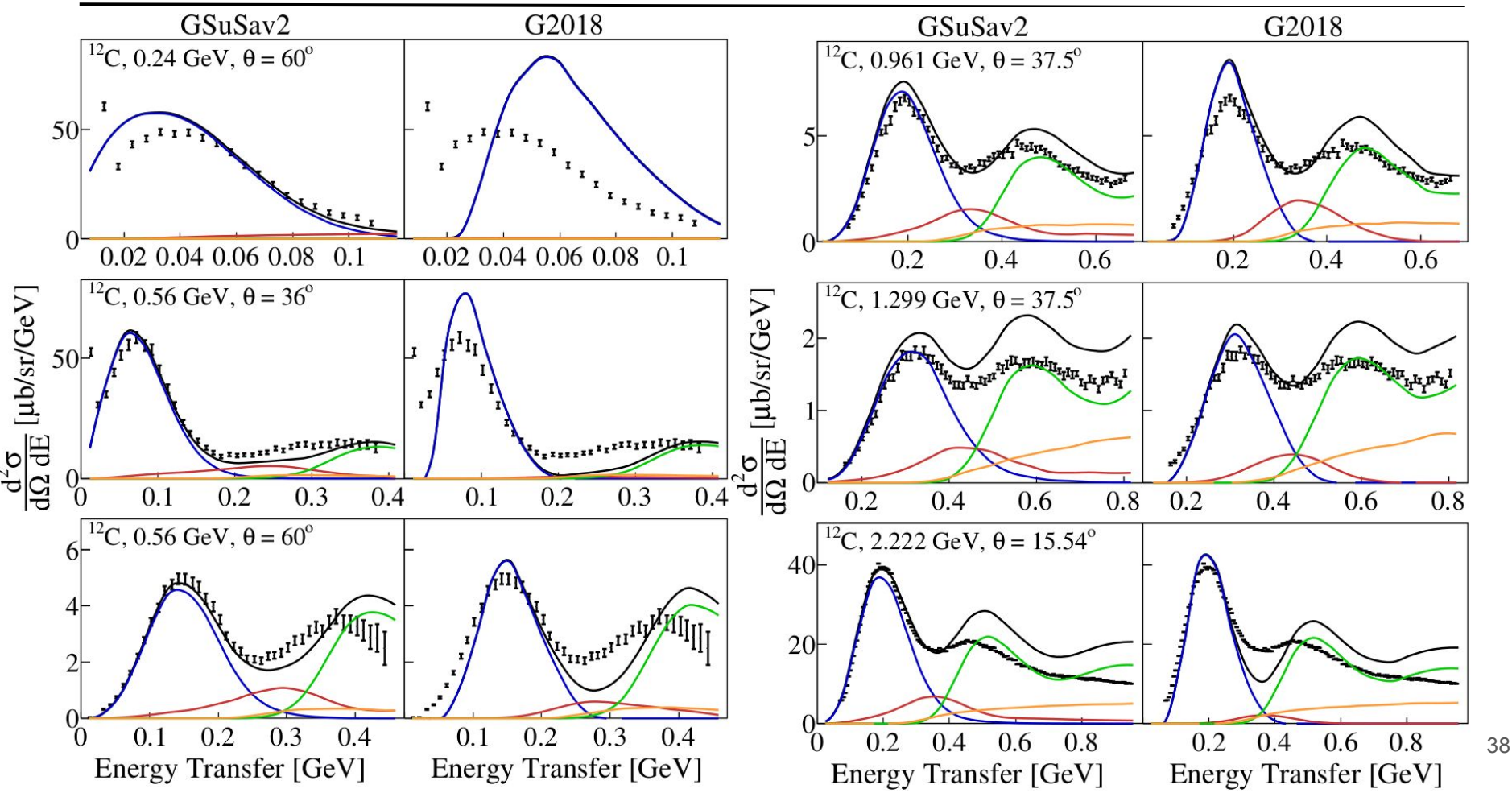
QE Events

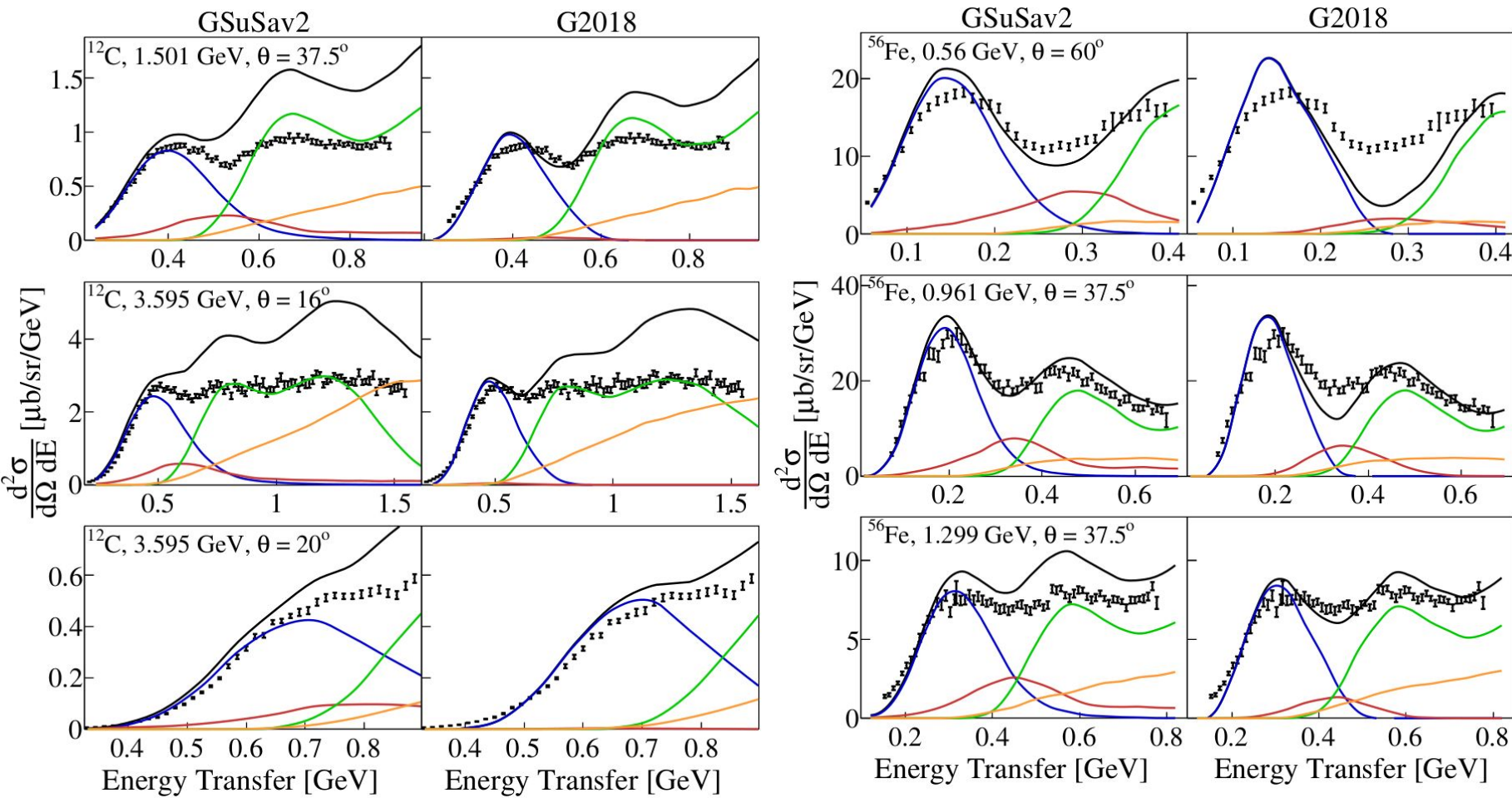


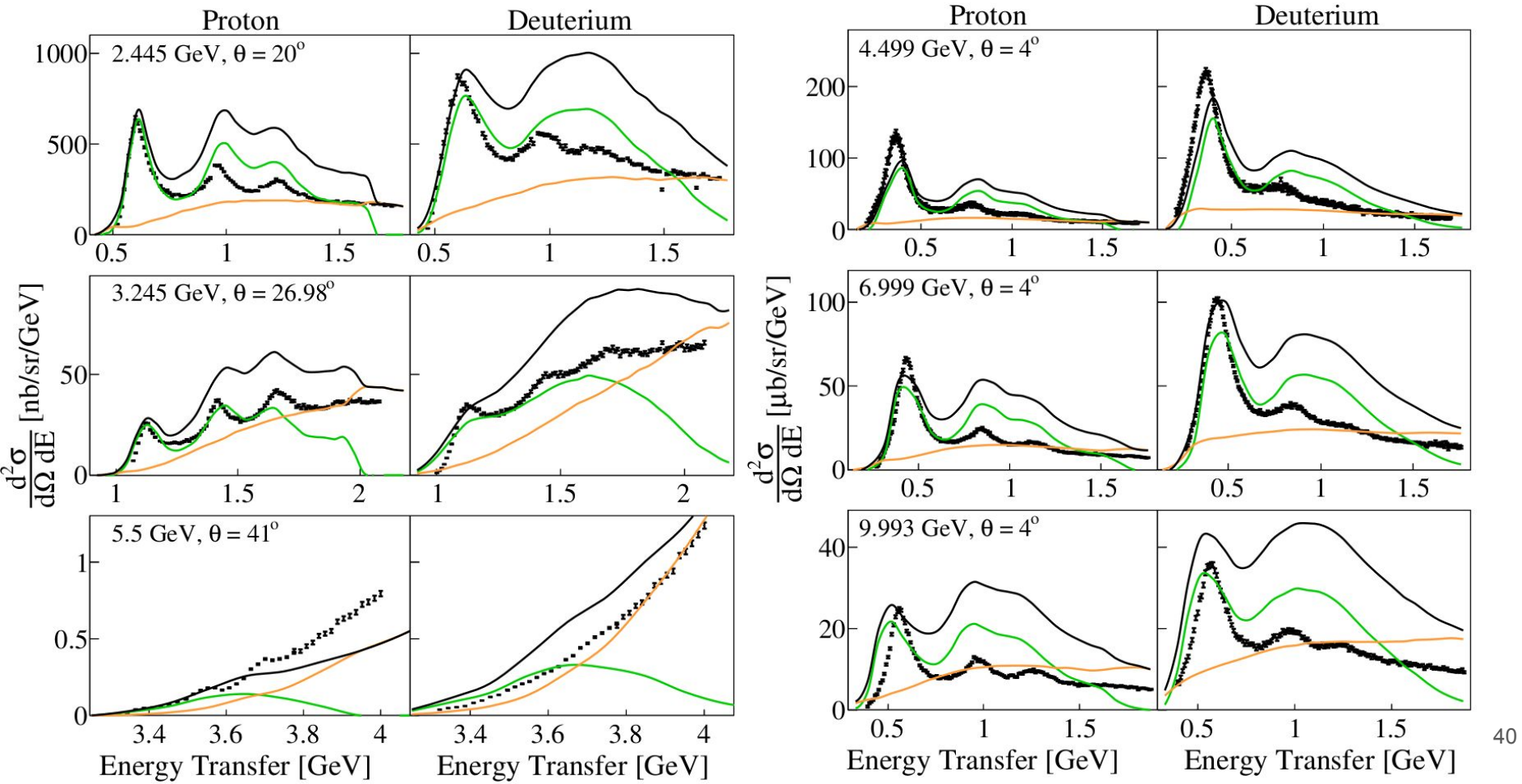
Consistent Treatment Of MEC Events With SuSav2

Unique chance to constraint one of least understood interaction channels

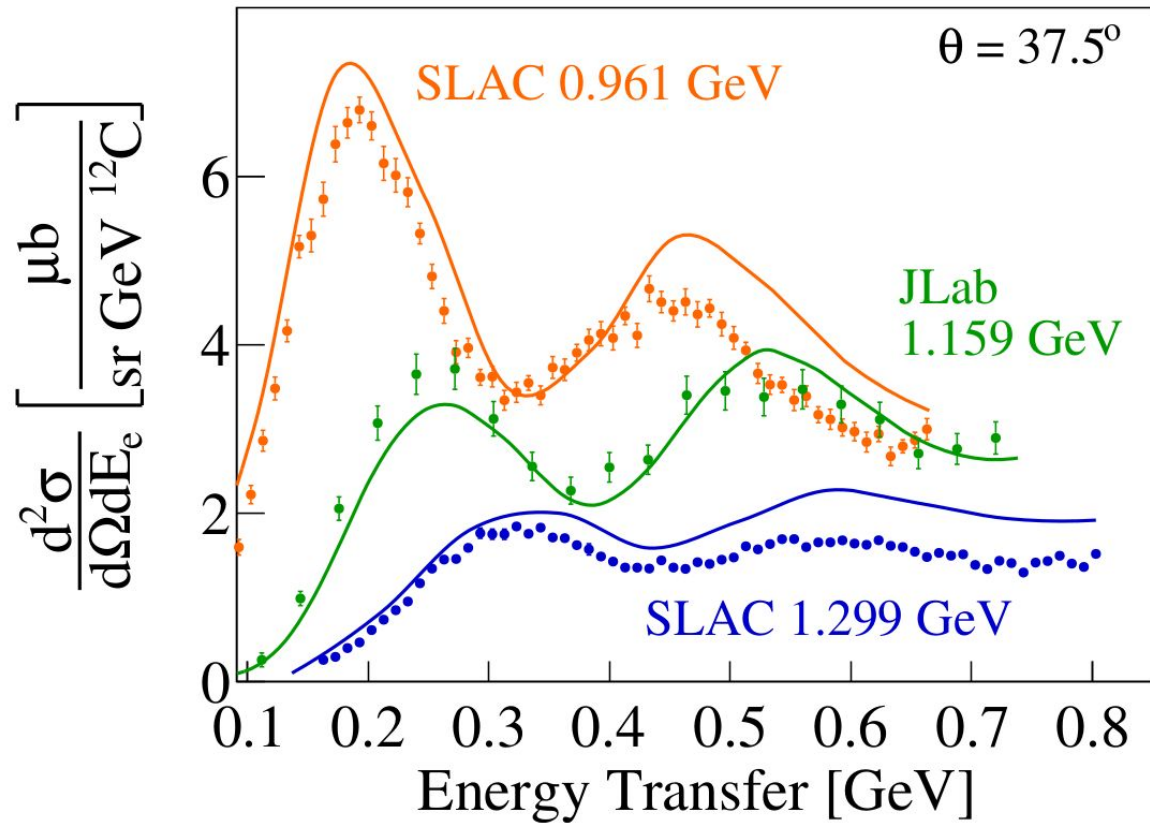




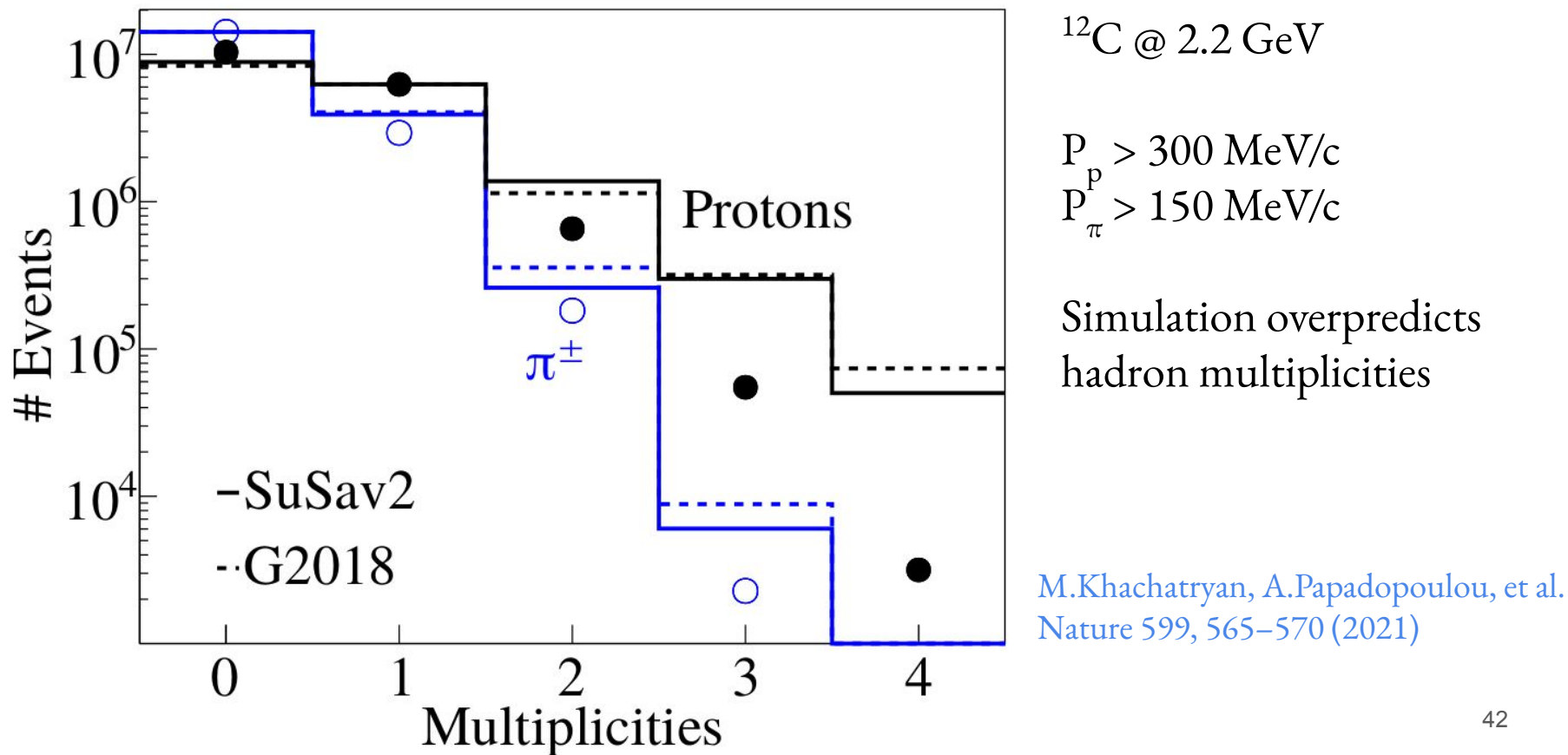




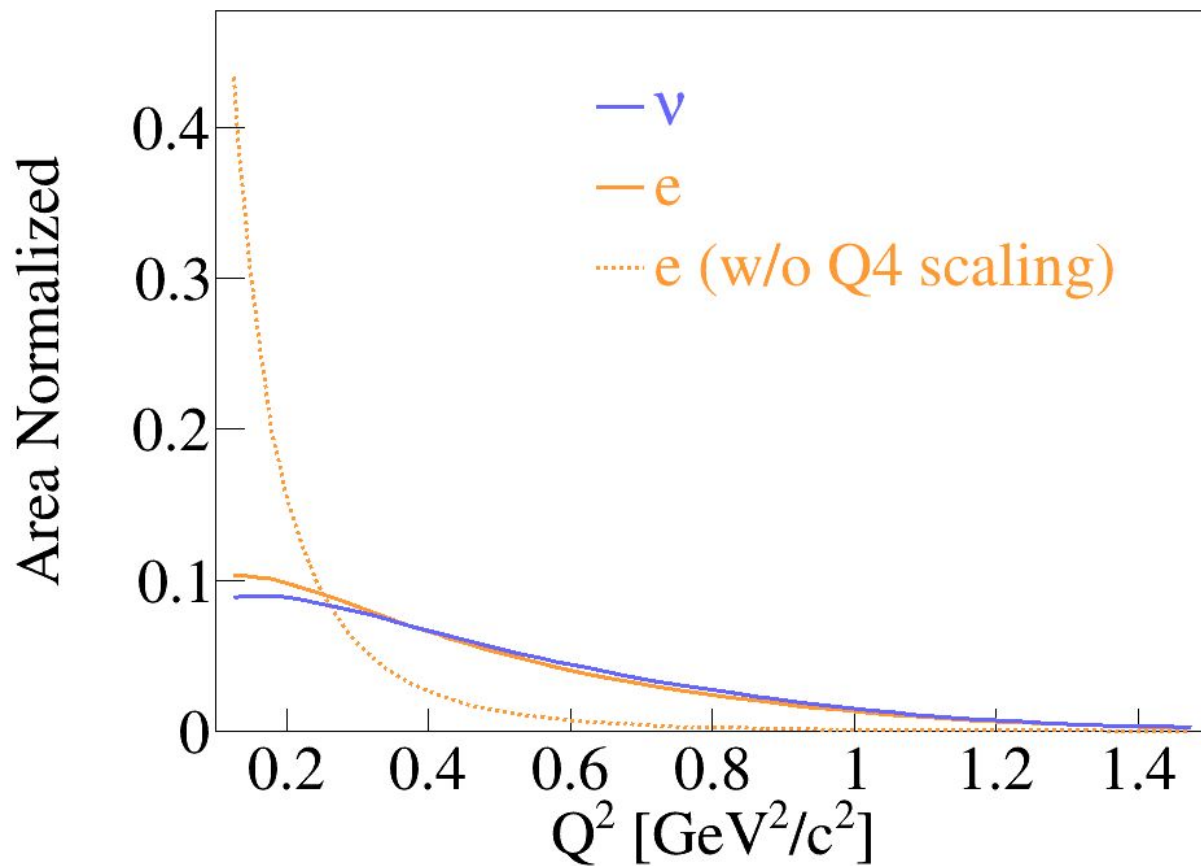
Sanity Check With Inclusive Cross Sections

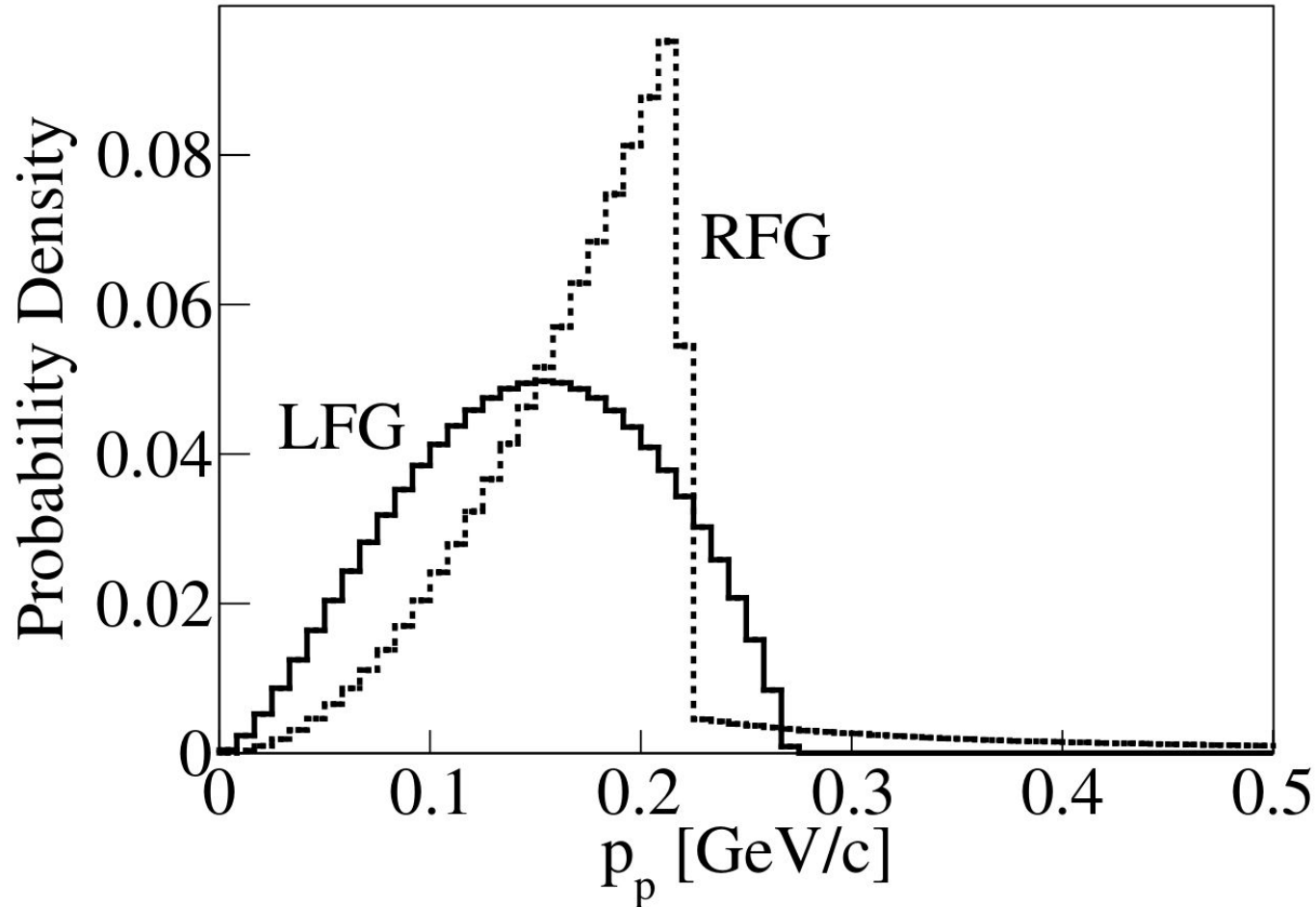


Detected Hadron Multiplicities



Q^4 Scaling Effect





SuSav2 Configuration / GEM21_11b_00_000

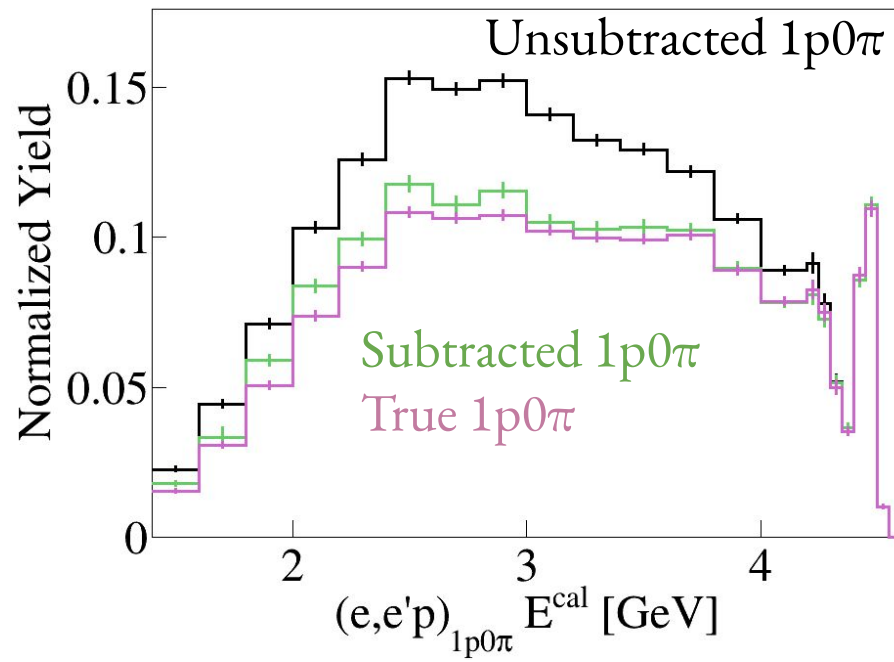
	Electrons	Neutrinos
QE	SuSav2	SuSav2
MEC	SuSav2	SuSav2
RES	Berger-Sehgal	Berger-Sehgal
DIS	AGKY	AGKY
FSI	hN2018	hN2018
Nuclear Model	Relativistic Mean Field	Relativistic Mean Field

G2018 Model Configuration

	Electrons	Neutrinos
QE	Rosenbluth	Nieves
MEC	Empirical	Nieves
RES	Berger-Sehgal	Berger-Sehgal
DIS	AGKY	AGKY
FSI	hA2018	hA2018
Nuclear Model	Local Fermi Gas	Local Fermi Gas

Closure Test

- Use GENIE files
- Filter specific topologies (e.g. $1p0\pi p + 1p1\pi$)
- **Subtracted** & **True** $1p0\pi$ are in good agreement



Well defined signal definition: Min θ_e Cut

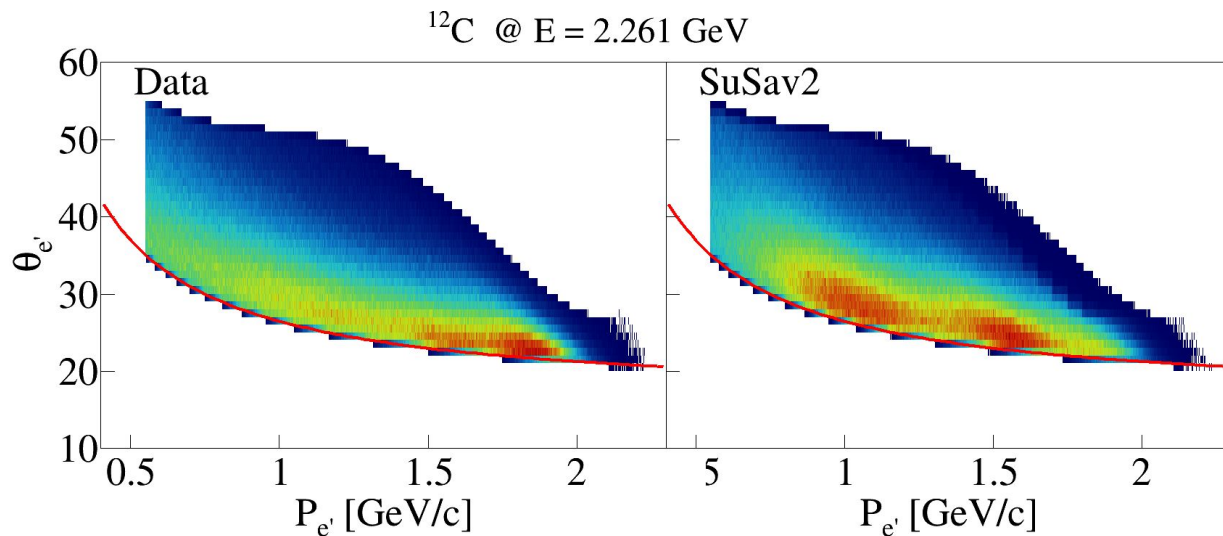
@ 1.1 GeV: $\theta = 17 + 7 / P$

@ 2.2 GeV: $\theta = 16 + 10.5 / P$

@ 4.4 GeV: $\theta = 13.5 + 15 / P$

See backup for $p / \pi^{+/-}$ definitions

- We do not acceptance correct below min θ



Well defined signal definition: Min θ_e Cut

@ 1.1 GeV: $\theta = 17 + 7 / P$

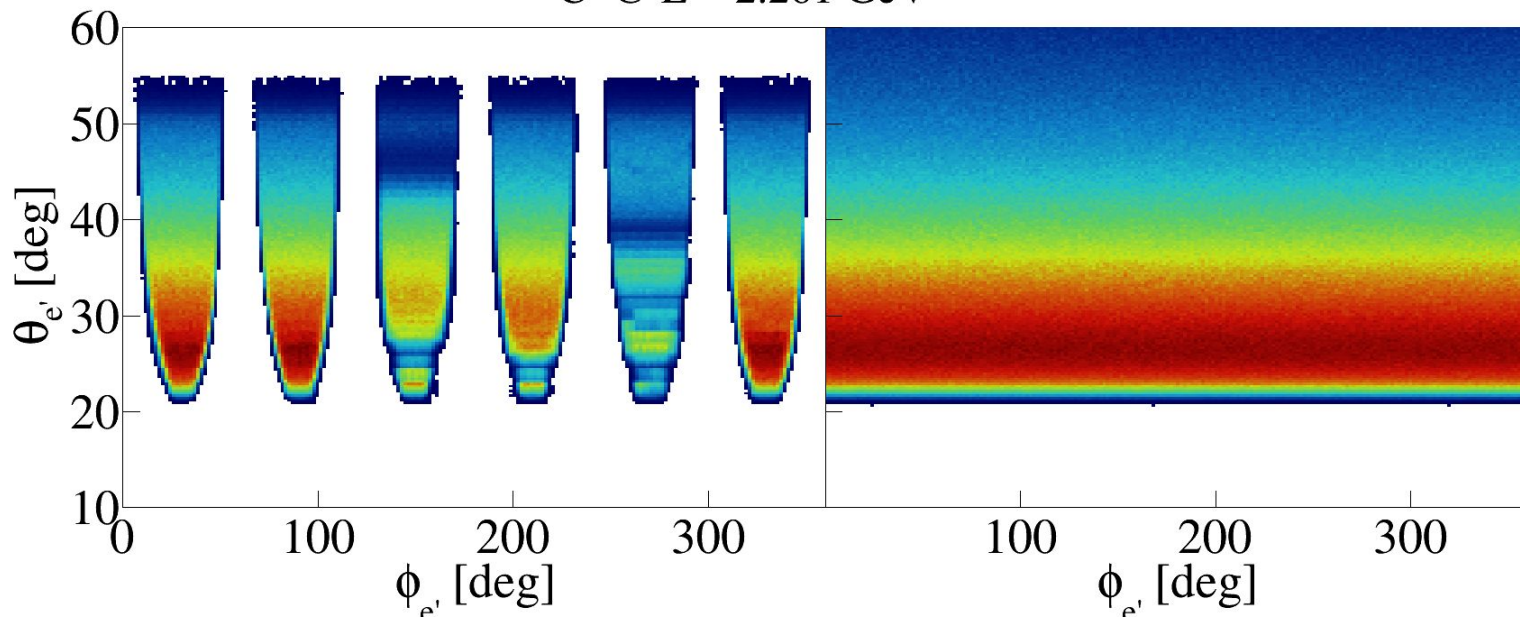
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See backup for $p / \pi^{+/-}$ definitions

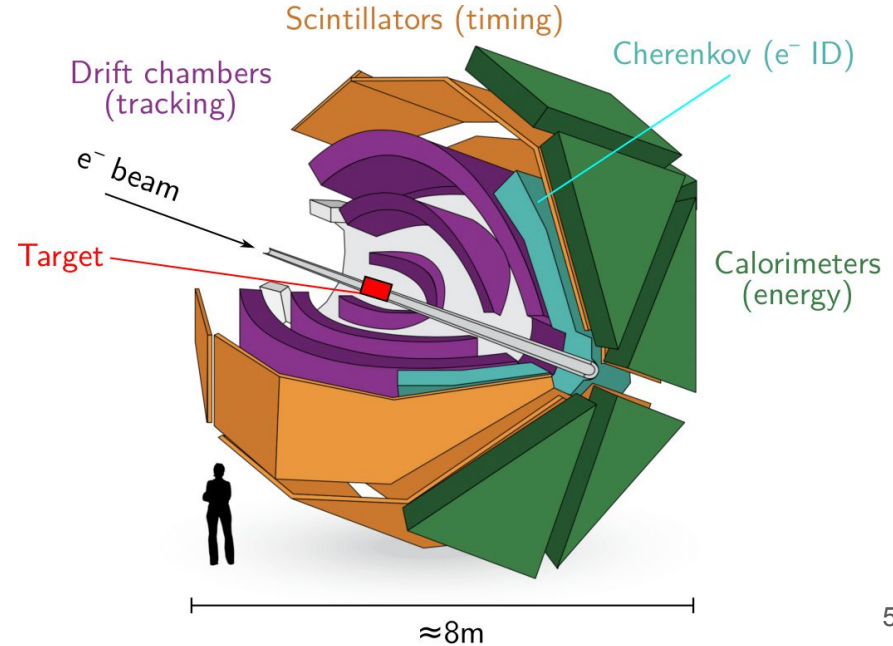
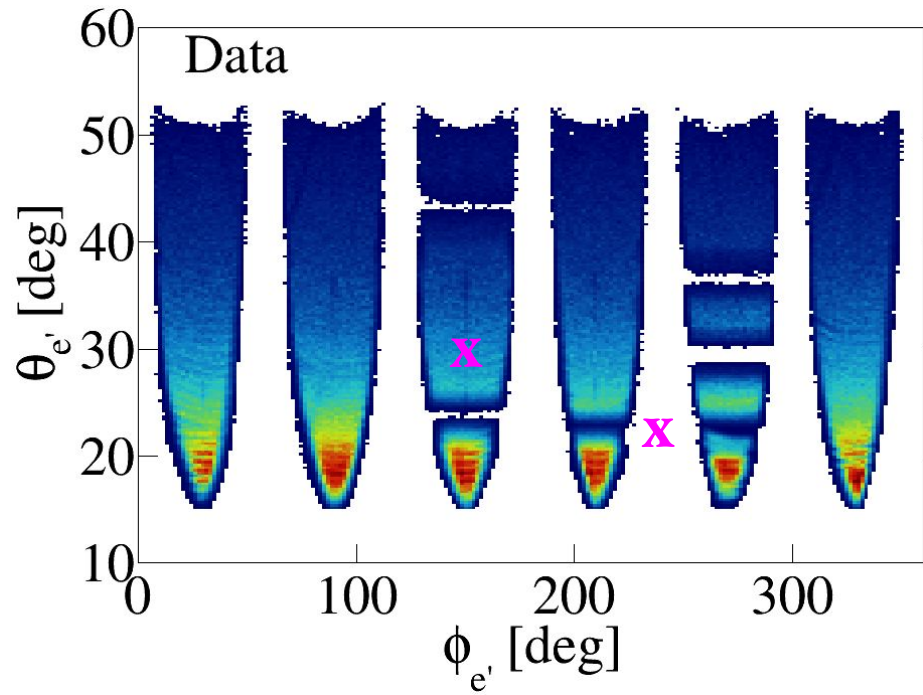
- We do not acceptance correct below min θ

^{12}C @ $E = 2.261$ GeV



Background Subtraction

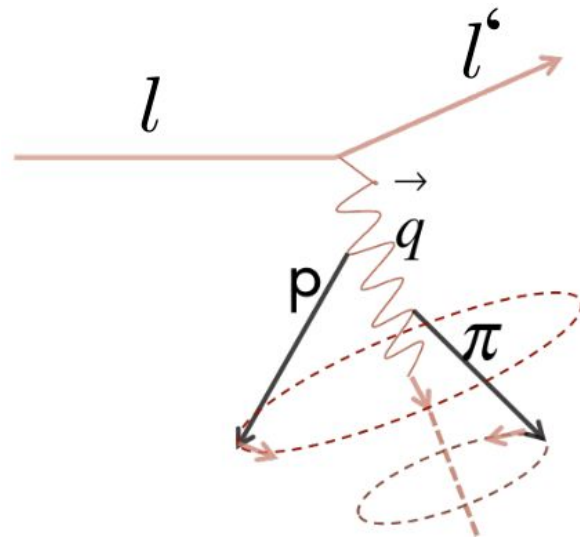
Non-($e,e'p$) interactions lead to multi-hadron final states
Gaps can make them look like ($e,e'p$) events



Data Driven Correction

Non- $(e,e'p)$ interactions lead to multi-hadron final states
Gaps make them look like $(e,e'p)$ events

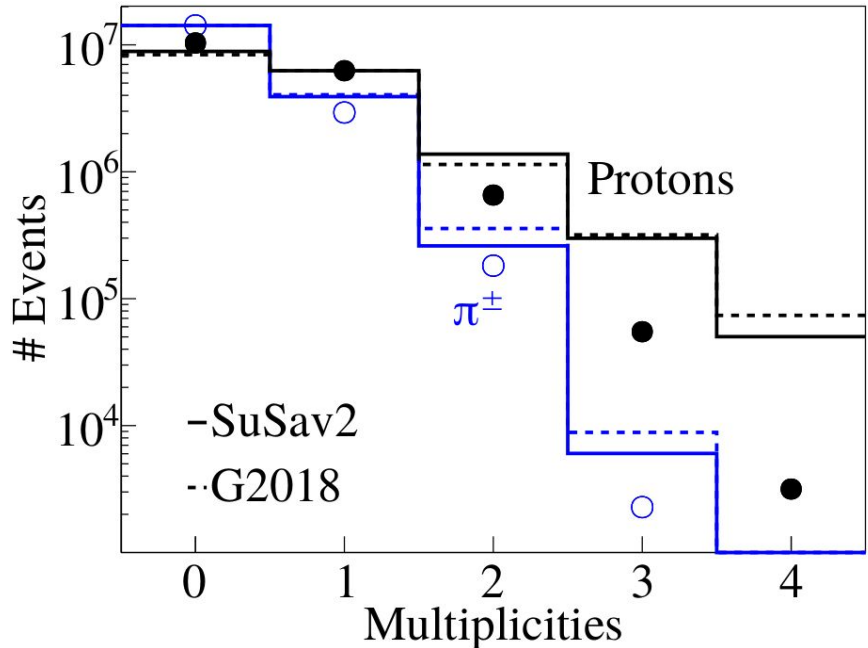
- Use measured $(e,e'p\pi)$ events
- Rotate p, π around q to determine π detection efficiency
- Subtract undetected $(e,e'p\pi)$
- Repeat for higher hadron multiplicities



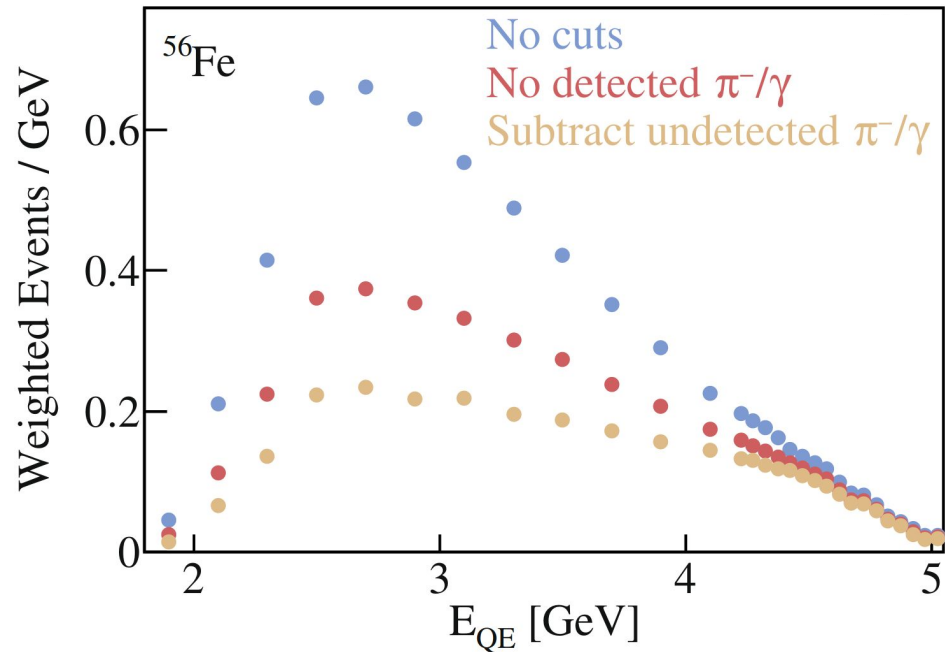
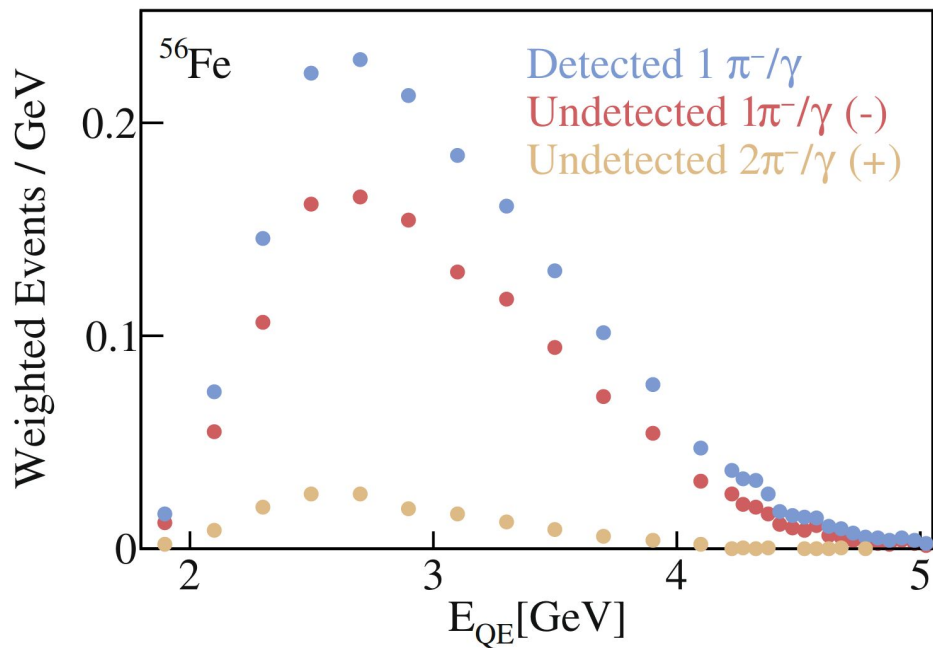
Data Driven Correction

Non-(e,e'p) interactions lead to multi-hadron final states
Gaps can make them look like (e,e'p) events

- Use measured (e,e'p π) events
- Rotate p, π around q to determine π detection efficiency
- Subtract for undetected (e,e'p π)
- Repeat for higher hadron multiplicities (2p, 3p, 2p+1 π , ...)

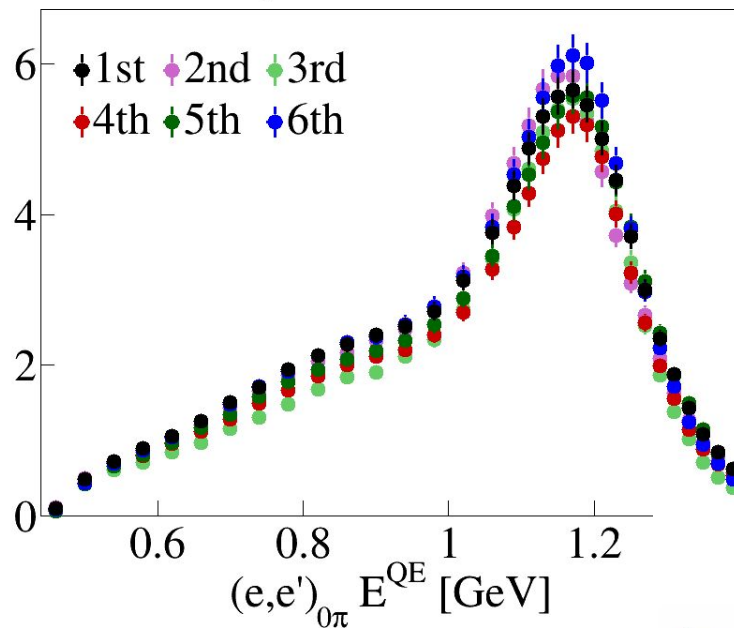


Subtraction Effect

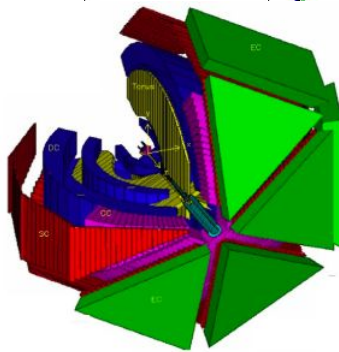
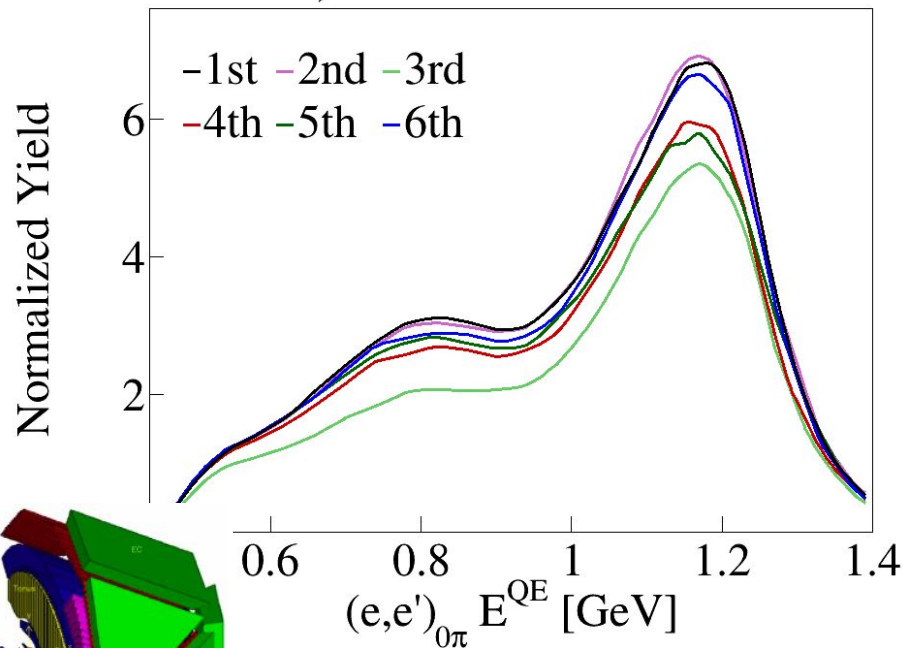


Systematics: Sector Dependence

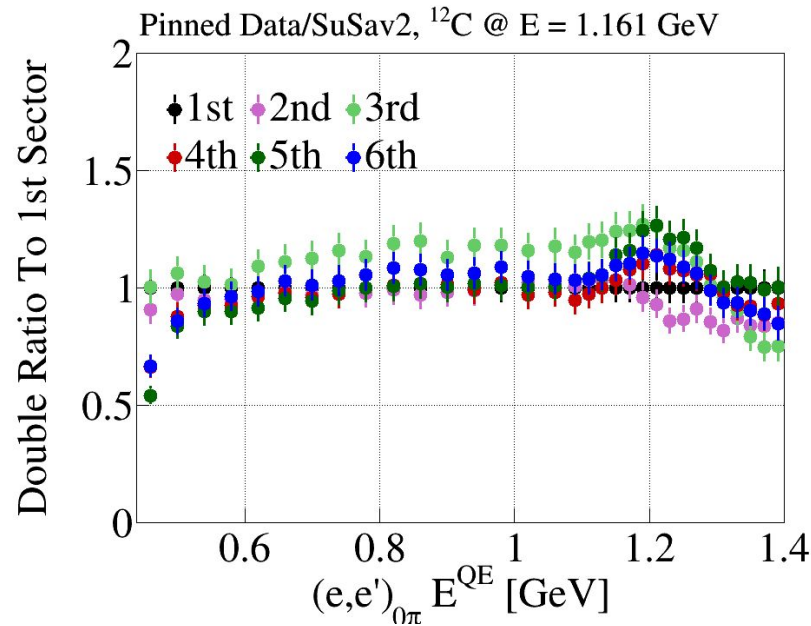
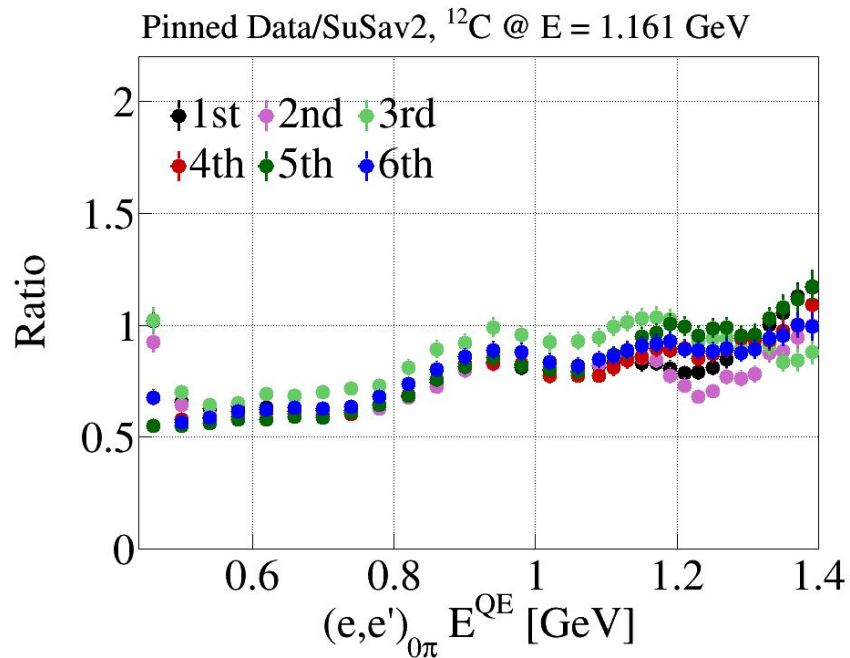
Pinned Data, ^{12}C @ $E = 1.161$ GeV



SuSav2, ^{12}C @ $E = 1.161$ GeV

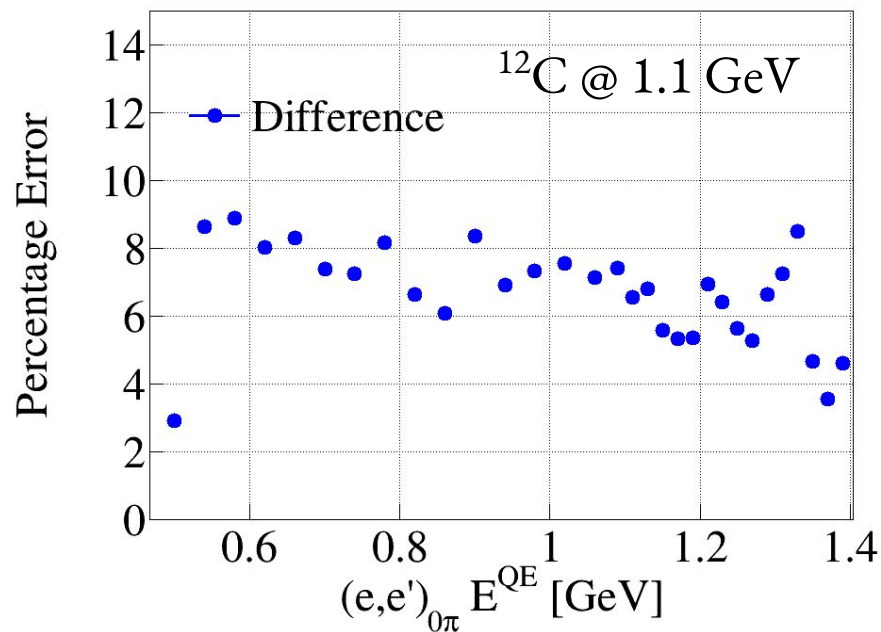


Systematics: Sector Dependence



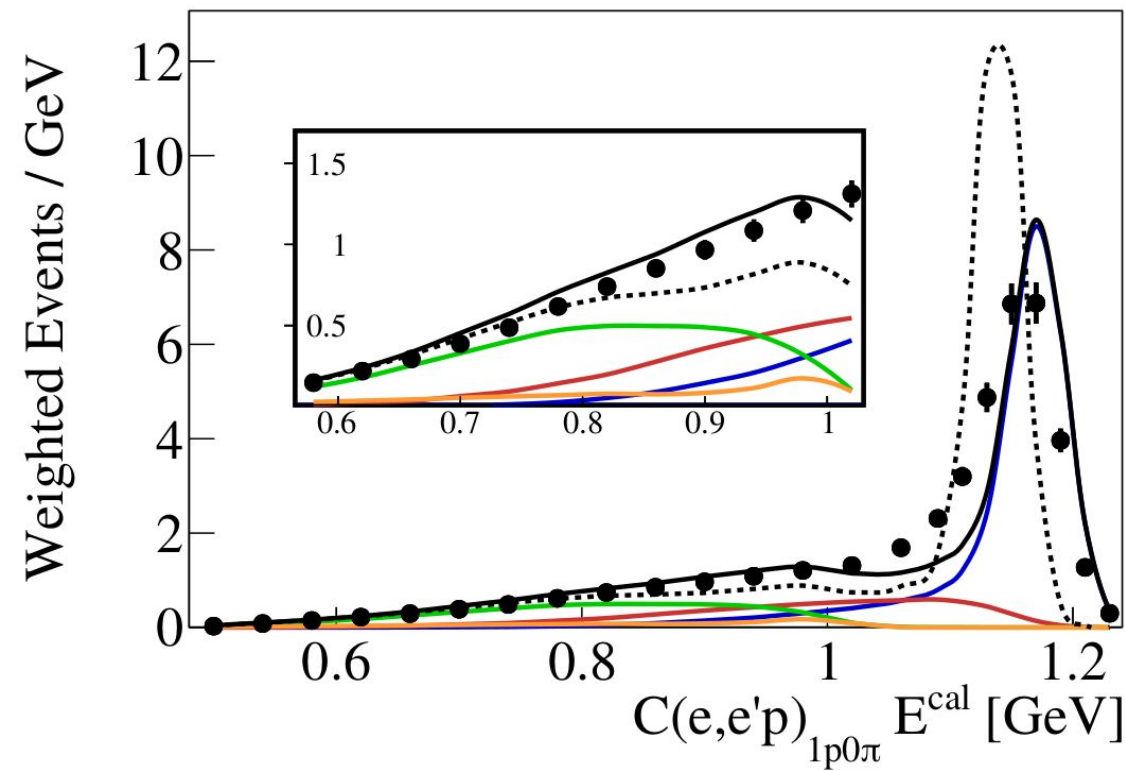
Systematics: Sector Dependence

Quantifying uncertainty by using
unweighted variance & by subtracting variance from statistical uncertainty



- Playing this game across all nuclei & energies
- Division by $\sqrt{N_{\text{sectors}}}$
- Flat uncertainty of 6%

Calorimetric energy reconstruction using the 1p0 π channel



- Area normalized results
- No information with respect to absolute scale
- G2018 offset potentially due to binding energy issue

• Data

— SuSav2 (Total)

— QE — MEC

— RES — DIS

-- G2018

Step #2: Normalized Yield

Data

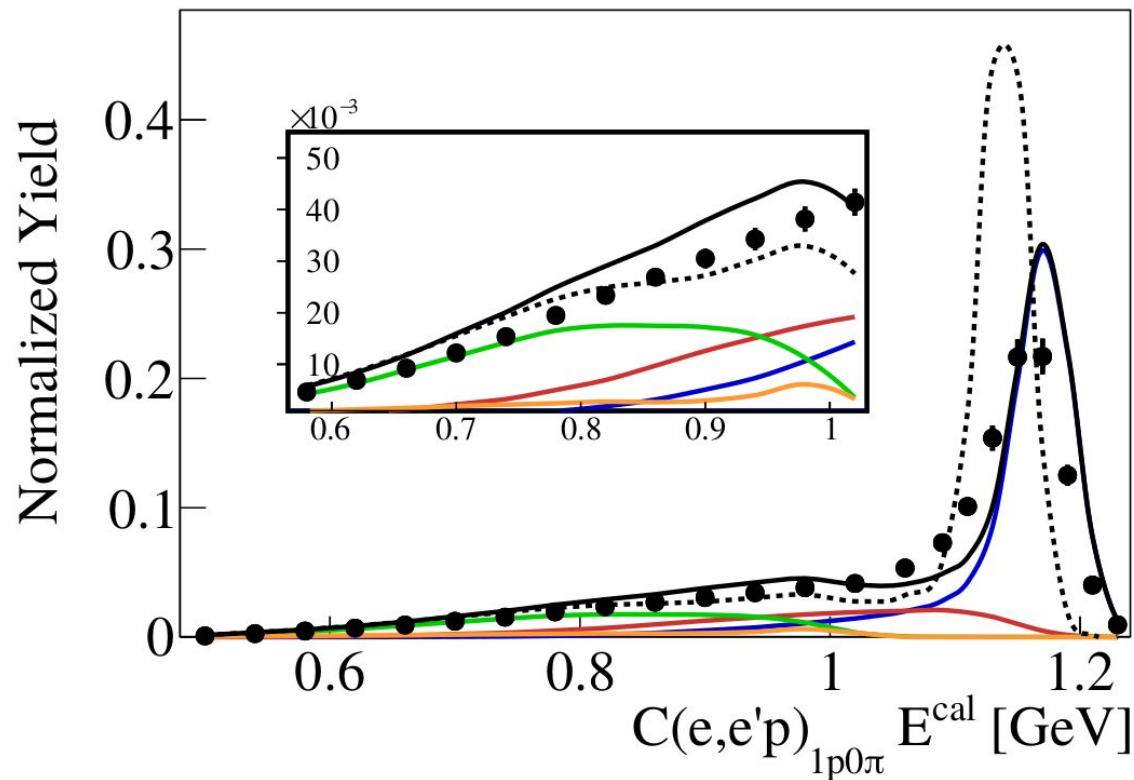
- Divide # events by integrated charge & target thickness to get xsec in μb
- Divide by bin width to get $\mu\text{b}/\text{GeV}$

Simulation

- Get GENIE total cross section for E_e / target A & $Q^2 > Q^2_{\text{min}}$
- $\text{xsec} = (\text{Selected detected events} / \text{all generated events}) * \text{total xsec} / \text{bin width}$

No corrections for CLAS acceptance or for bremsstrahlung radiation

Step #2: Normalized Yield



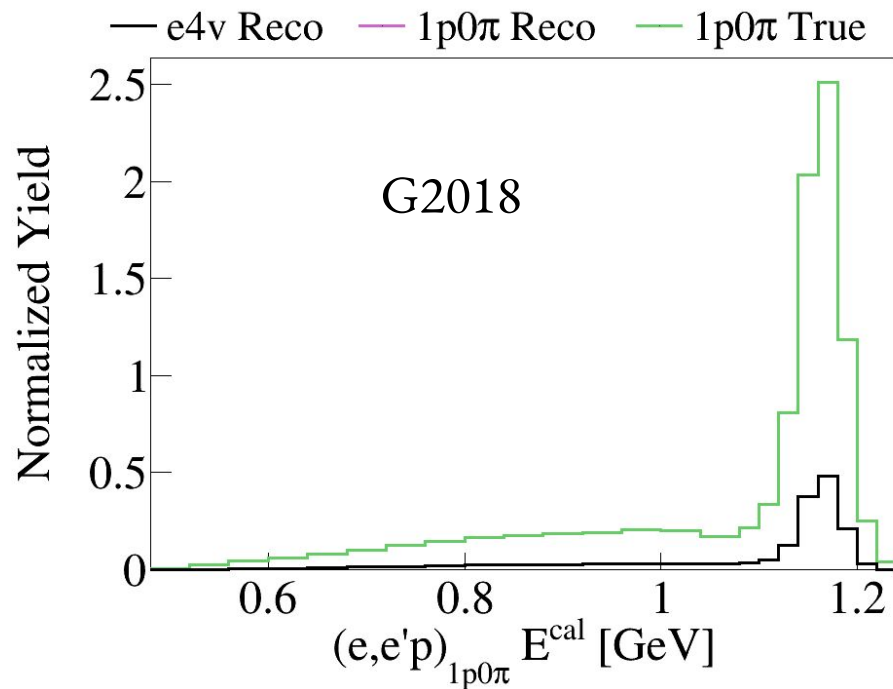
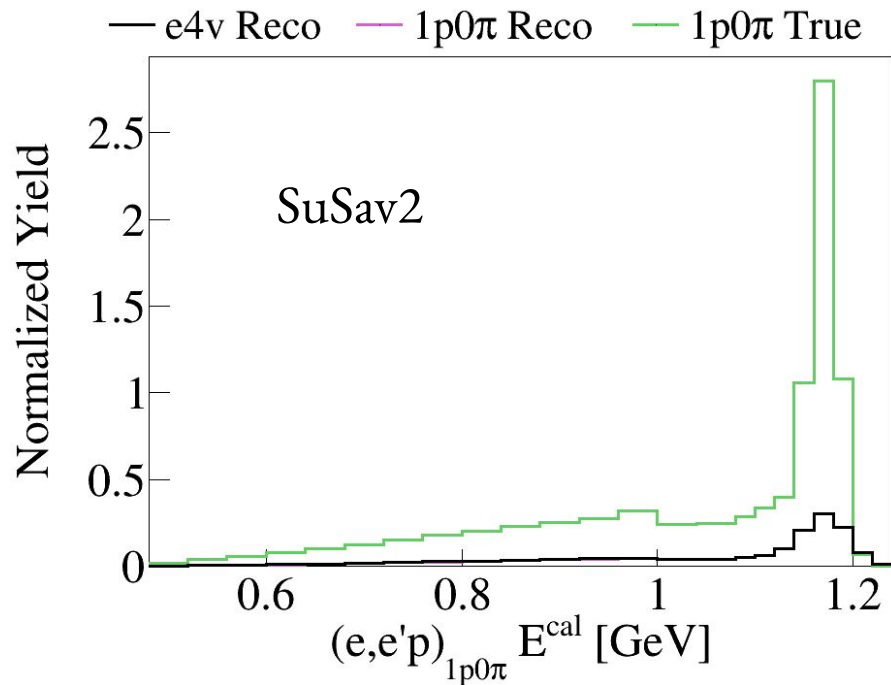
- Absolute scale comparison
- Small effect @ 1 GeV

• Data
— SuSav2 (Total)
— QE — MEC
— RES — DIS
-- G2018

Step #3a: Acceptance Correction

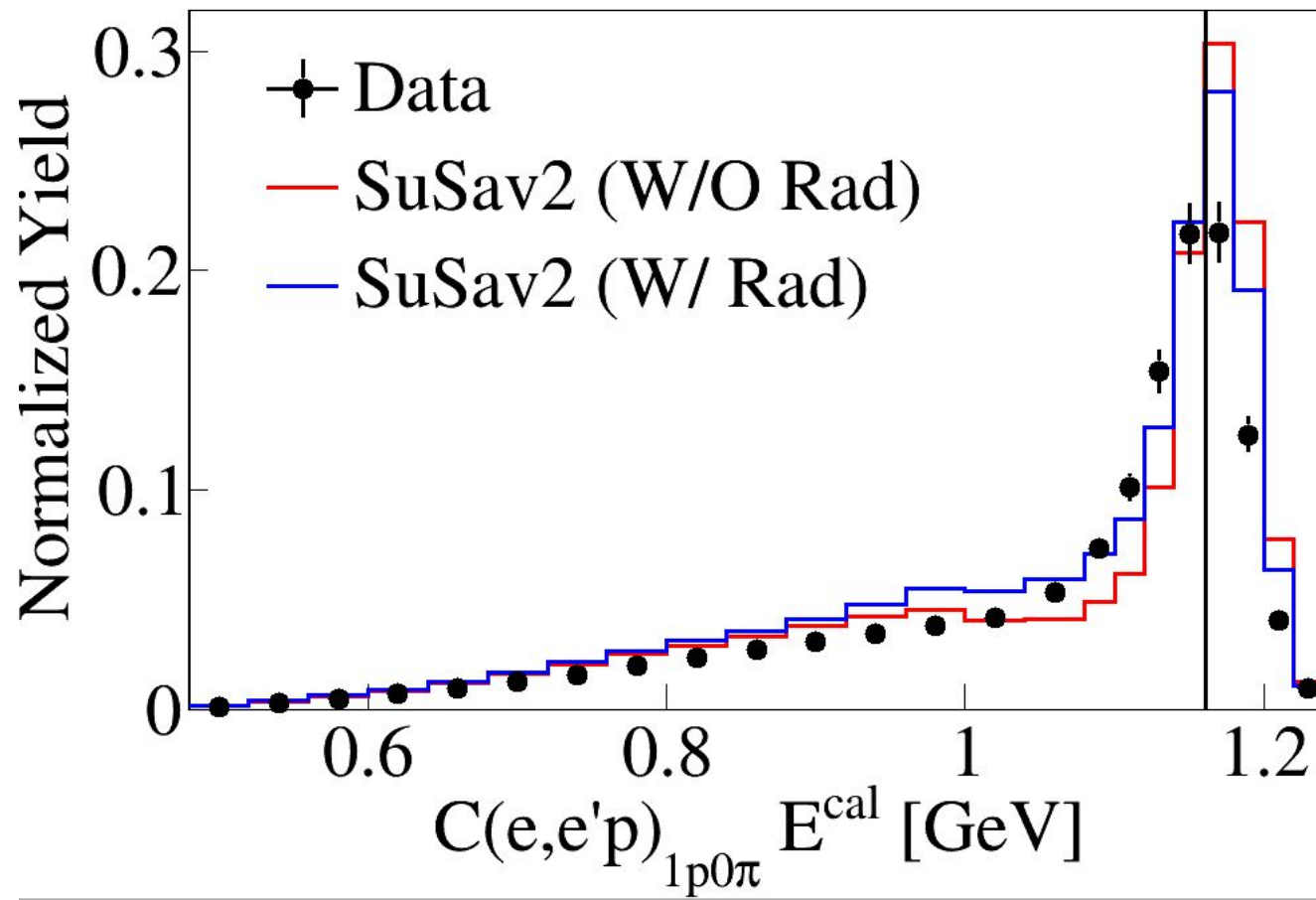
- Start from reco / true ratio w/o radiation to obtain acceptance correction
- Average on a bin-by-bin basis $x = |\text{SuSav2} + \text{G2018}| / 2$
- Due to offset, G2018 Ecal predictions have been shifted by
10/25/36 MeV for $^4\text{He}/^{12}\text{C}/^{56}\text{Fe}$ respectively

Step #3a: Example 12C @ 1.1 GeV



Use reco / true ratio to obtain acceptance correction

Step #3b: Radiation Correction



Use ratio of **red** / **blue**
to correct for radiation

Averaged Acceptance Correction Uncertainty Over True Beam Energy

On a bin-by-bin basis

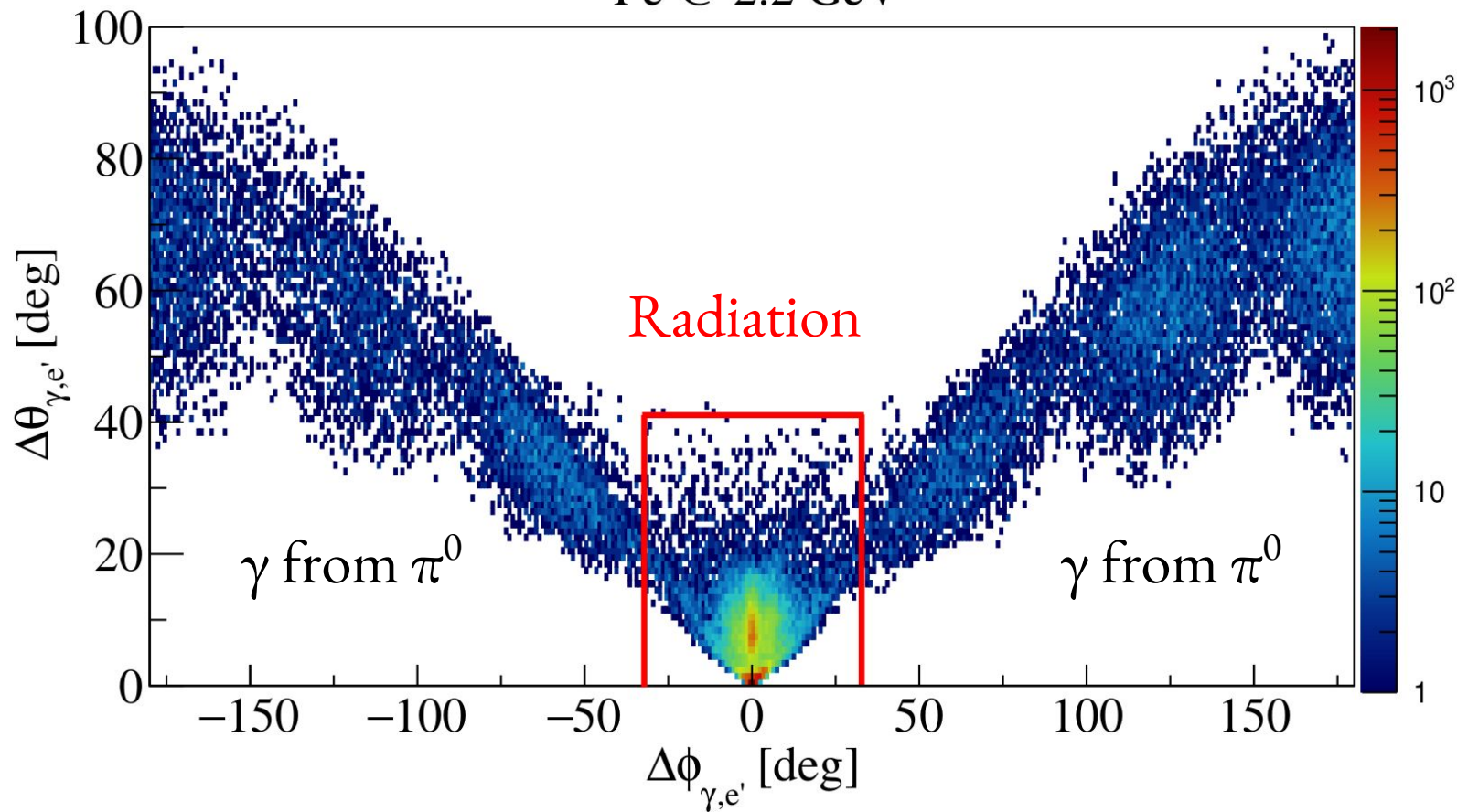
$$x = |\text{SuSav2} - \text{G2018}| / \text{Sqrt}(12)$$

$$\text{Bin Entry} = x / \text{Average} * 100 \%$$

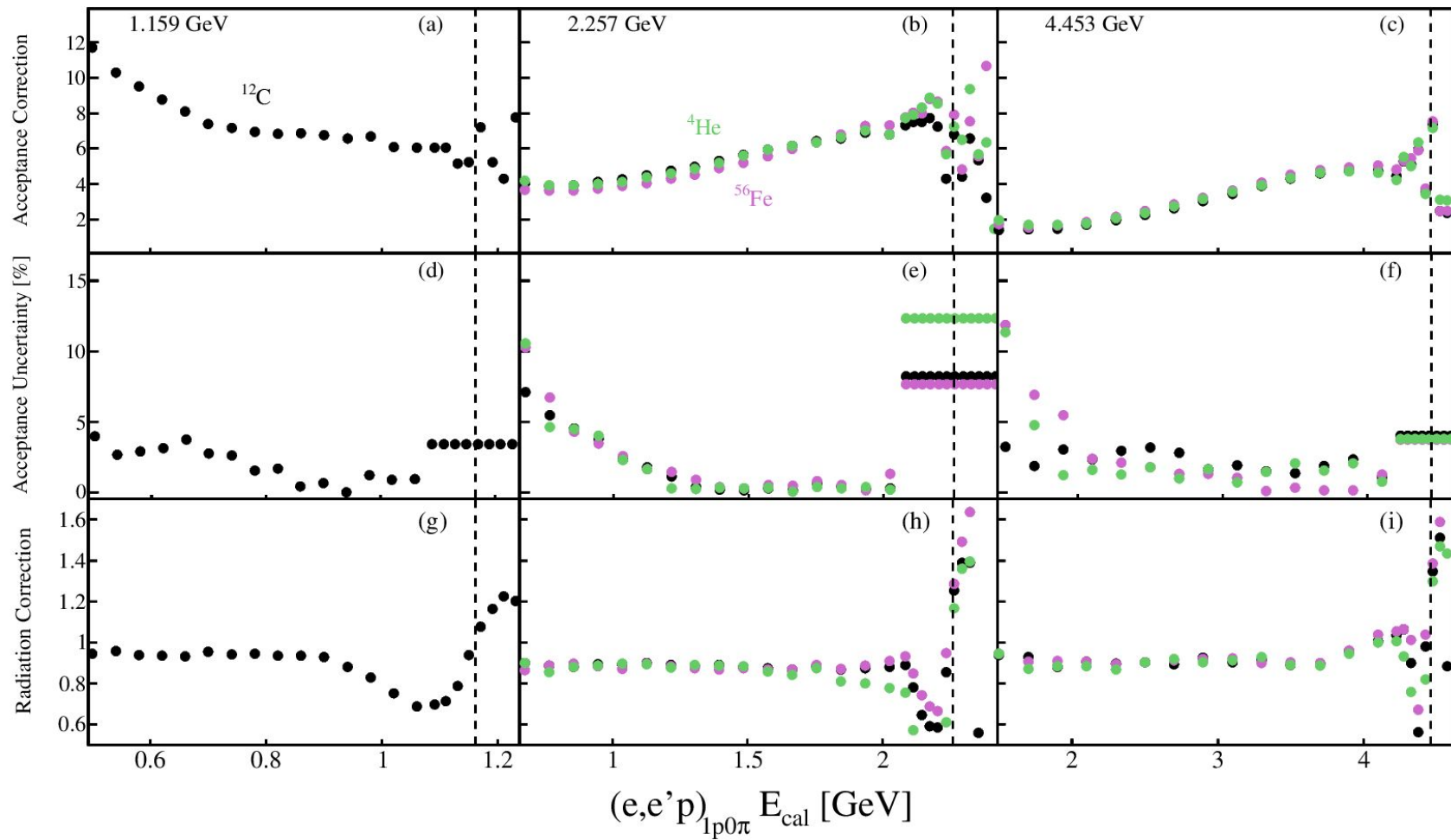
Same recipe as for acceptance correction but,
to avoid infinities, will use average (1 bin) around the peak and
 $\text{average}(\text{reco}) / \text{average}(\text{true})$ for correction factor

Excluding Radiation

^{56}Fe @ 2.2 GeV

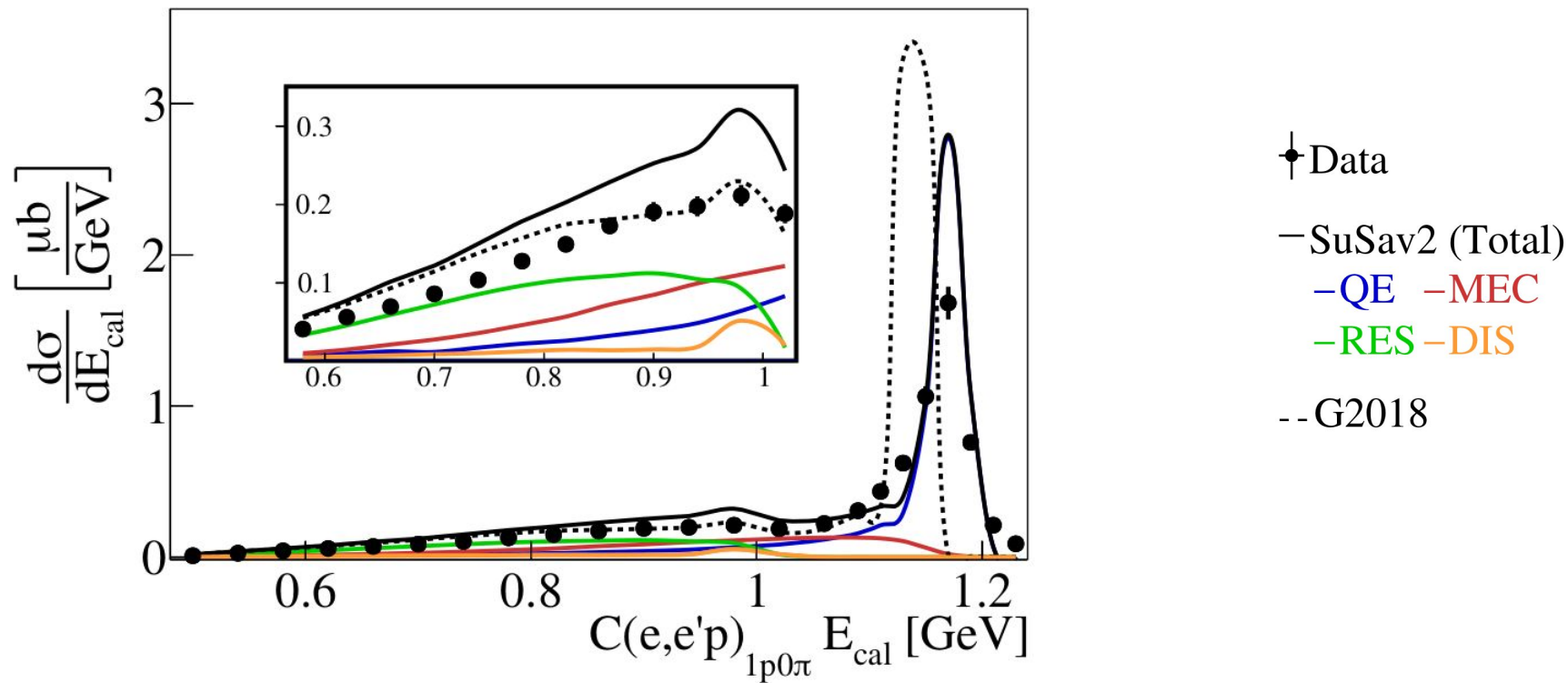


Correction Factors



Step #4: Absolute Cross Sections

After both acceptance & radiation corrections, without systematics yet



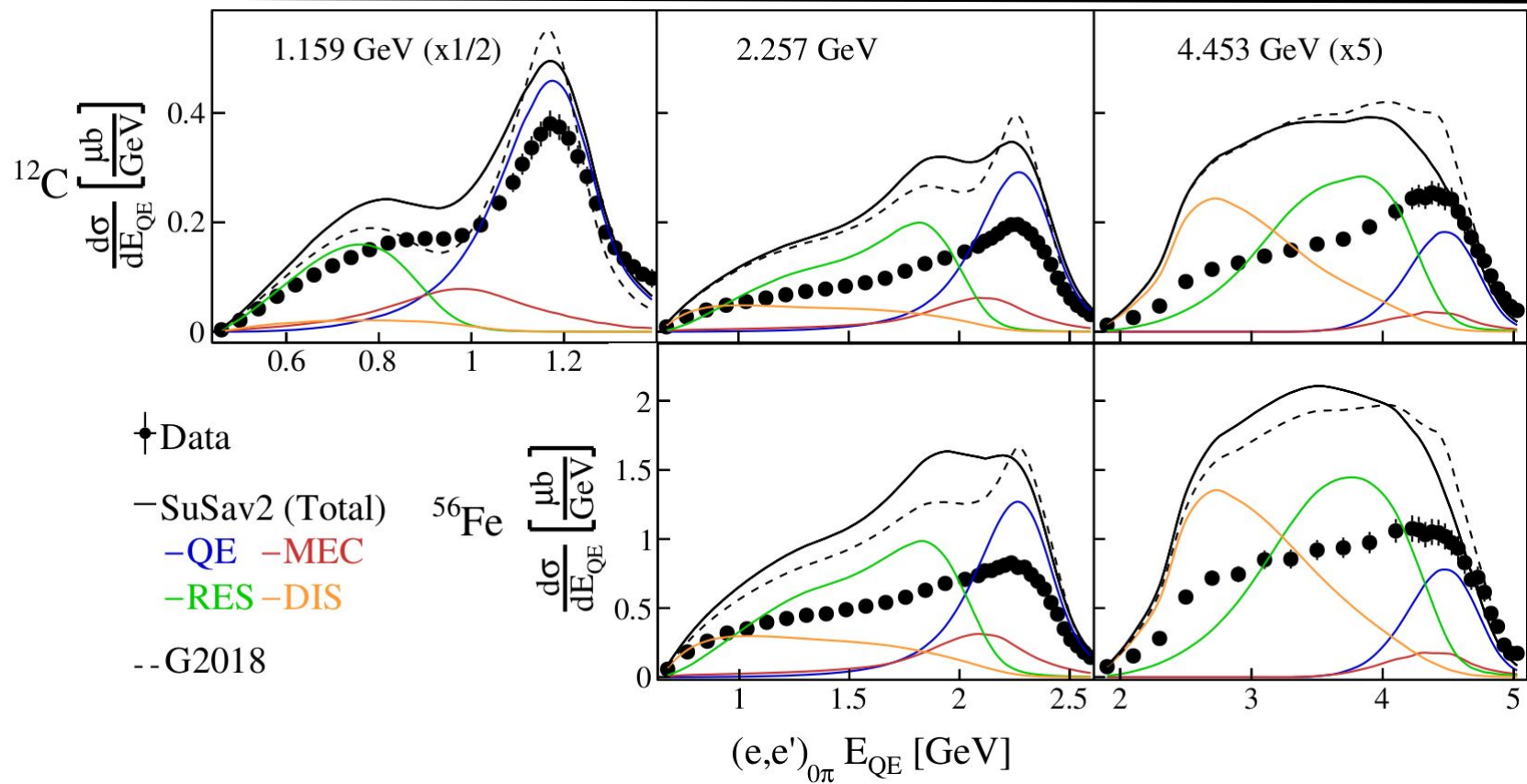
Systematics

Source	Uncertainty (%)
Detector acceptance Identification cuts $\phi_{q\pi}$ cross section dependence Number of rotations	2,2.1,4.7 (@ 1.1,2.2,4.4 GeV)
Sector dependence	6
Acceptance correction	2-15
Overall normalization	3
Electron inefficiency	2

Energy Reconstruction Accuracy

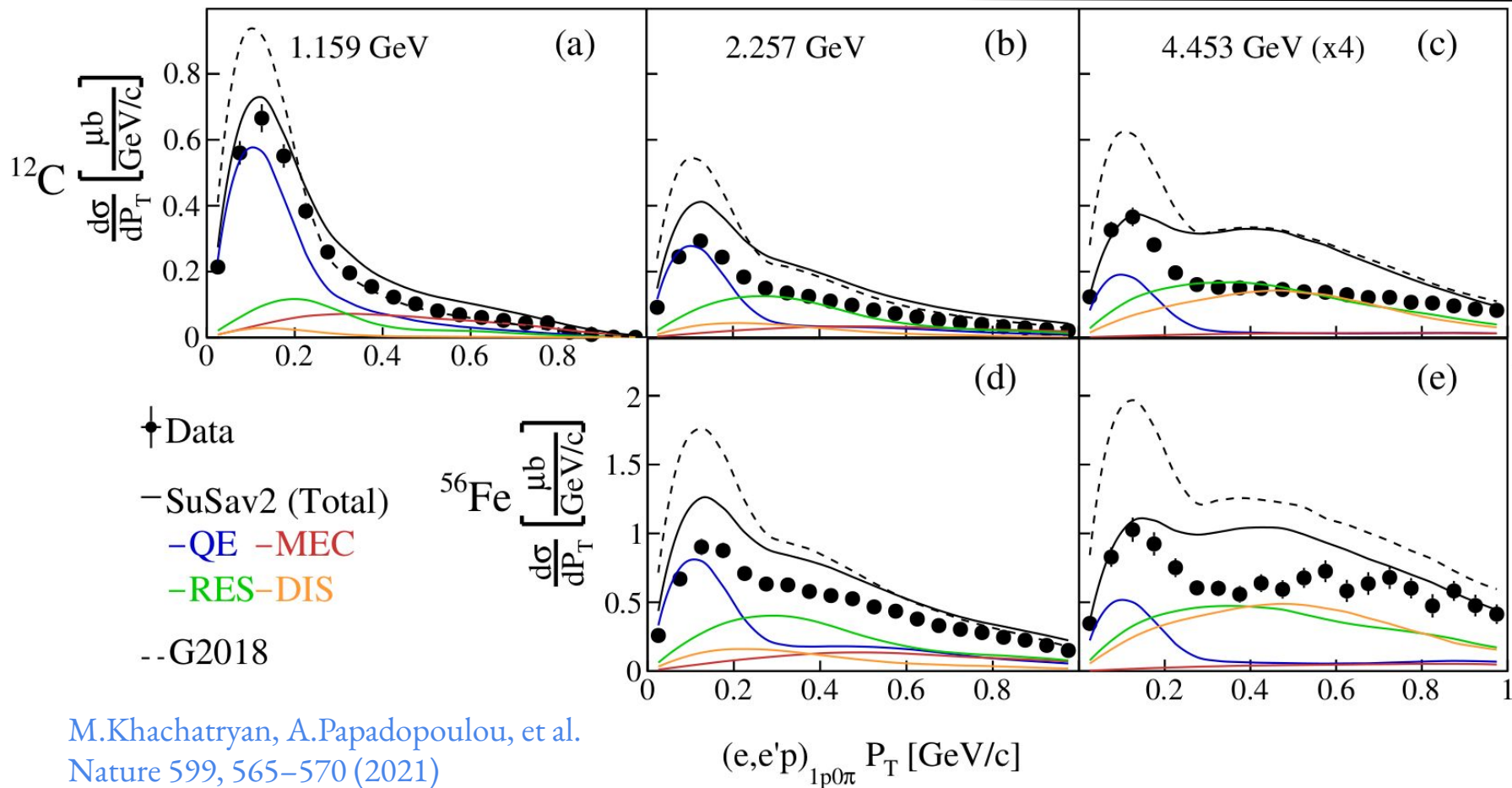
		1.159 GeV		2.257 GeV		4.453 GeV	
		Peak	Peak	Peak	Peak	Peak	Peak
		Fraction	Sum [μb]	Fraction	Sum [μb]	Fraction	Sum [μb]
^4He	Data	-	-	41	0.48	38	0.15
	SuSAv2	-	-	45	1.31	22	0.14
	G2018	-	-	39	0.93	24	0.16
^{12}C	Data	39	4.13	31	1.26	32	0.34
	SuSAv2	44	5.33	27	1.76	12	0.20
	G2018	51	6.53	37	2.44	23	0.43
^{56}Fe	Data	-	-	20	3.73	23	1.01
	SuSAv2	-	-	21	5.28	10	0.58
	G2018	-	-	30	8.22	19	1.48

E_{QE} Nucleus & Energy Dependence



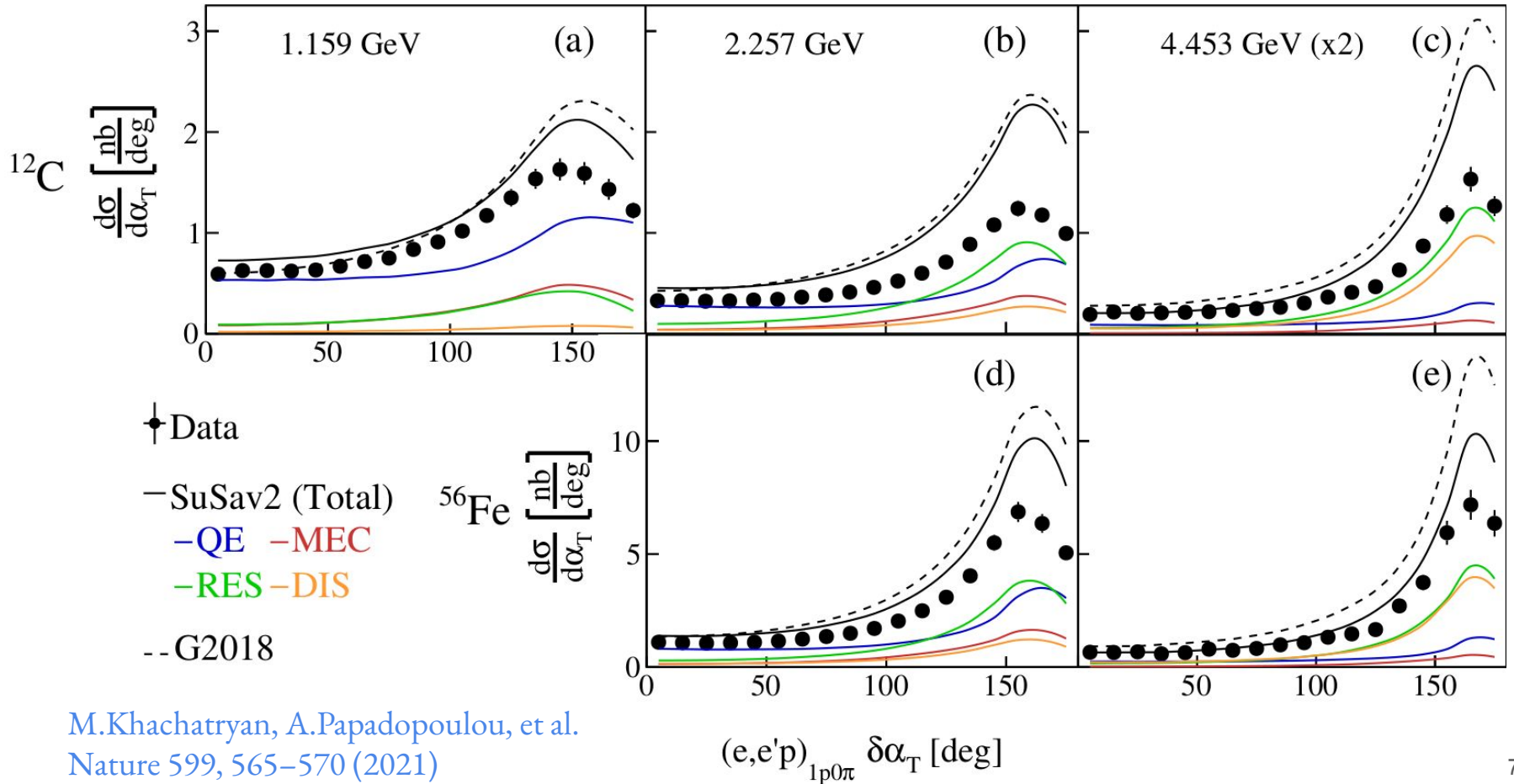
$$E_{QE} = \frac{2M\epsilon + 2ME_l - m_l^2}{2(M - E_l + |k_l|\cos\theta_l)}$$

P_T Nucleus & Energy Dependence



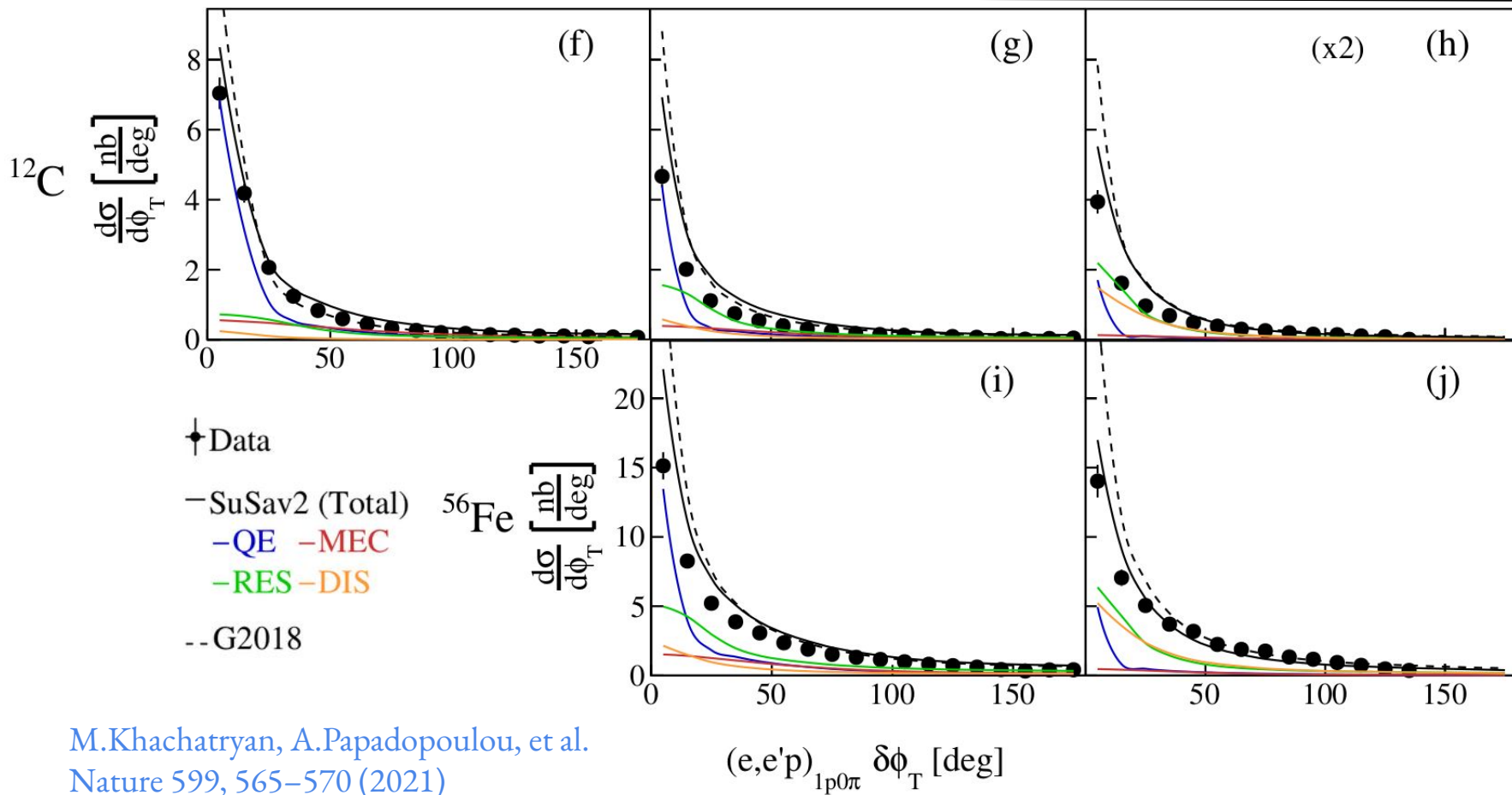
M.Khachatryan, A.Papadopoulou, et al.
Nature 599, 565–570 (2021)

$\delta\alpha_T$ Nucleus & Energy Dependence



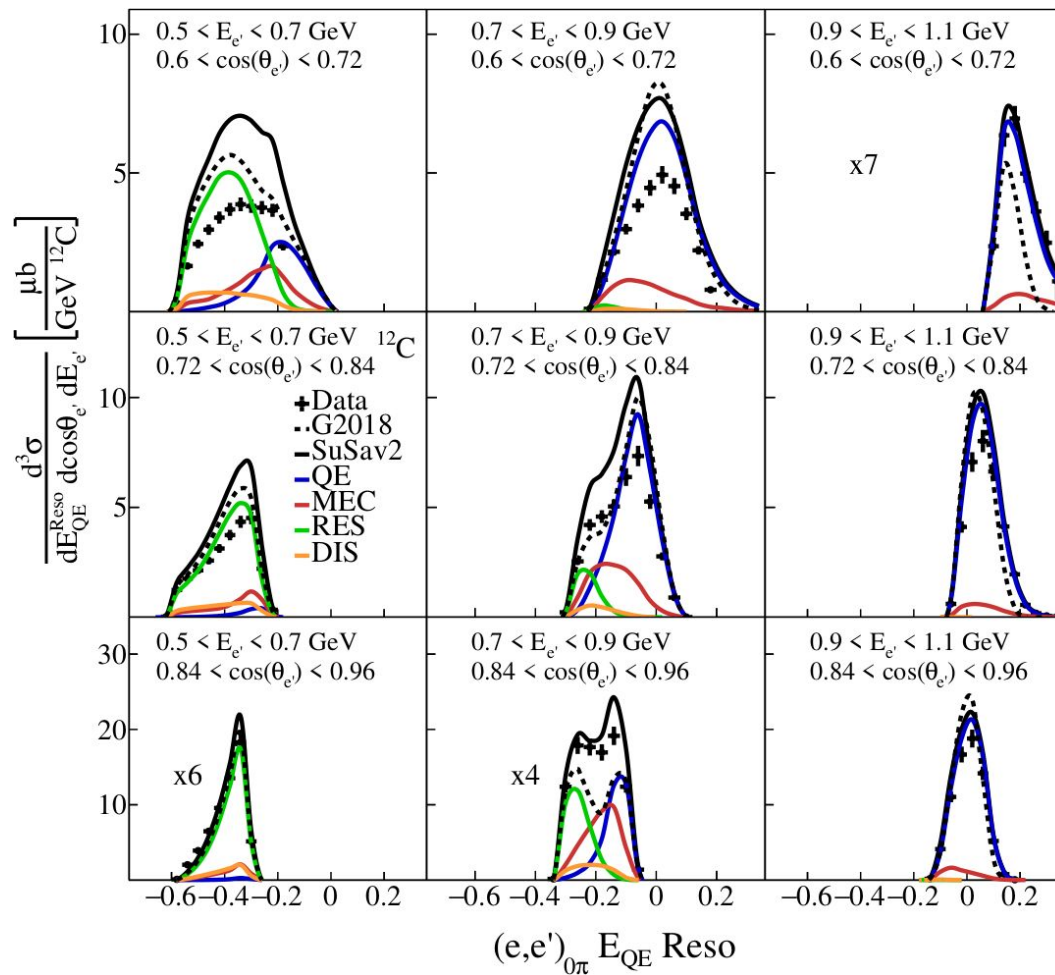
M.Khachatryan, A.Papadopoulou, et al.
 Nature 599, 565–570 (2021)

$\delta\phi_T$ Nucleus & Energy Dependence



M.Khachatryan, A.Papadopoulou, et al.
Nature 599, 565–570 (2021)

Into The 3D e4ν Multiverse!

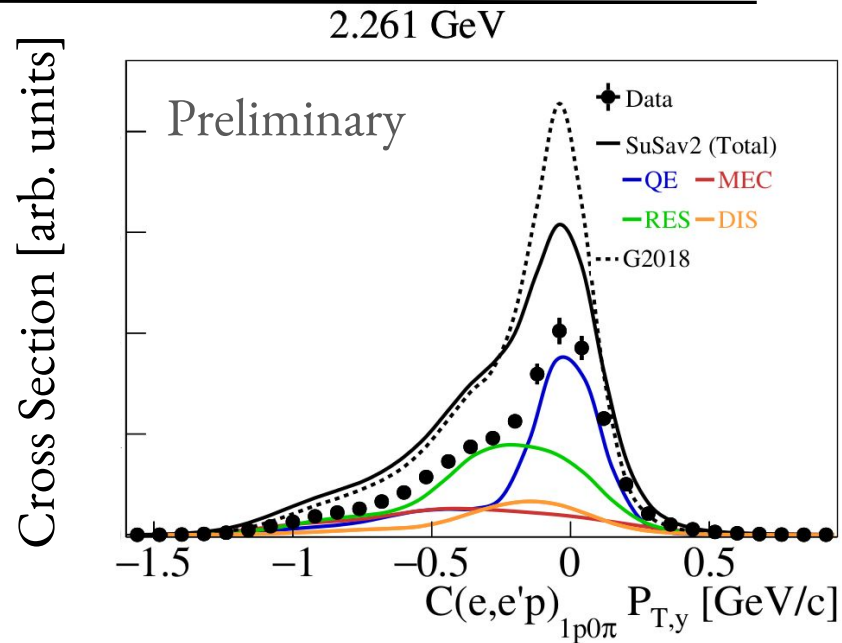
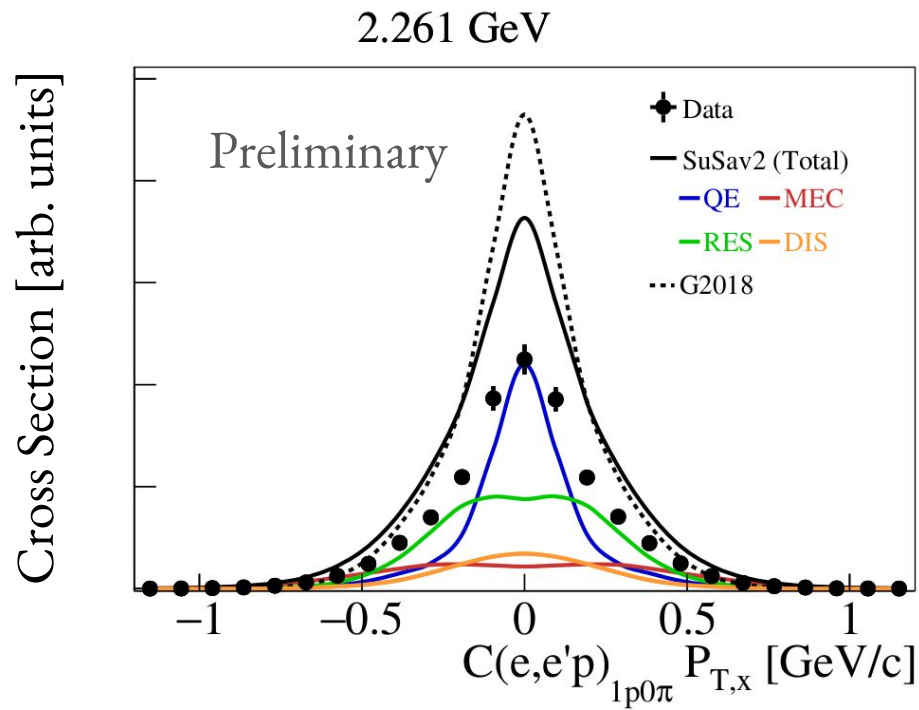


A.Papadopoulou, et al,
In preparation

Nuclear Sensitivity Variables

$$\delta \mathbf{p}_{T_x} = (\hat{\mathbf{p}}_v \times \hat{\mathbf{p}}_T^l) \cdot \delta \vec{\mathbf{p}}_T = |\delta \vec{\mathbf{p}}_T| \sin(\delta \alpha_T)$$

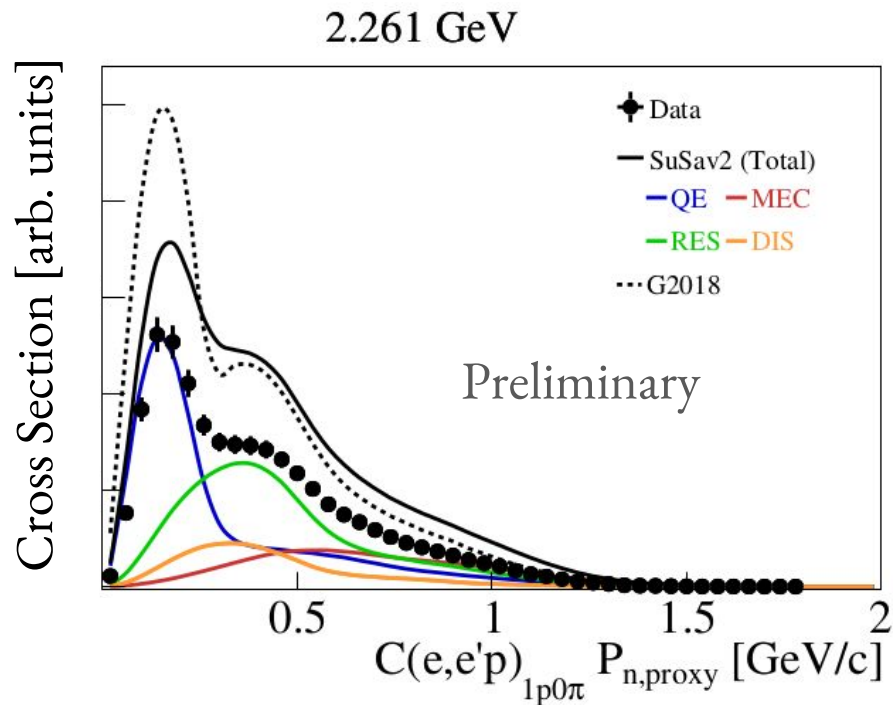
Sensitivity to Fermi motion



$$\delta \mathbf{p}_{T_y} = -\hat{\mathbf{p}}_T^l \cdot \delta \vec{\mathbf{p}}_T = |\delta \vec{\mathbf{p}}_T| \cos(\delta \alpha_T)$$

Sensitivity to final state interactions

Missing Momentum Approximation



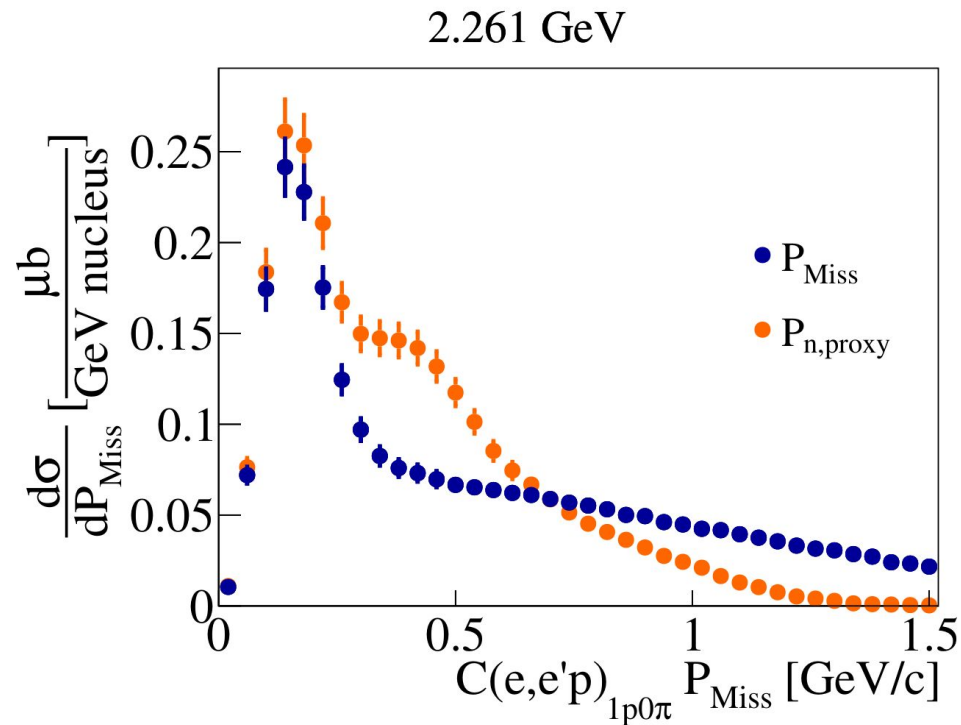
$$P_{n,proxy} = \sqrt{\delta p_L^2 + \delta p_T^2}$$

Under QE assumption

[Phys. Rev. Lett. 121, 022504 \(2018\)](#)

[A.Papadopoulou, et al, In preparation](#)

Fails To Reproduce True Missing Momentum



$$P_{\text{n,proxy}} = \sqrt{\delta p_L^2 + \delta p_T^2}$$

Under QE assumption

[Phys. Rev. Lett. 121, 022504 \(2018\)](#)

True missing momentum

$$P_{\text{miss}} = |p - q|$$

p = proton 3-vector

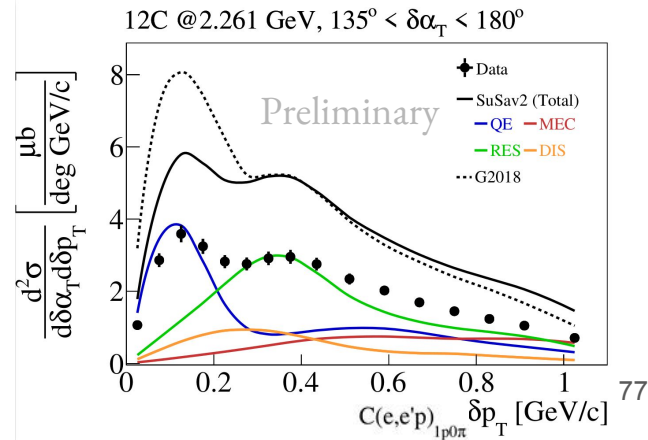
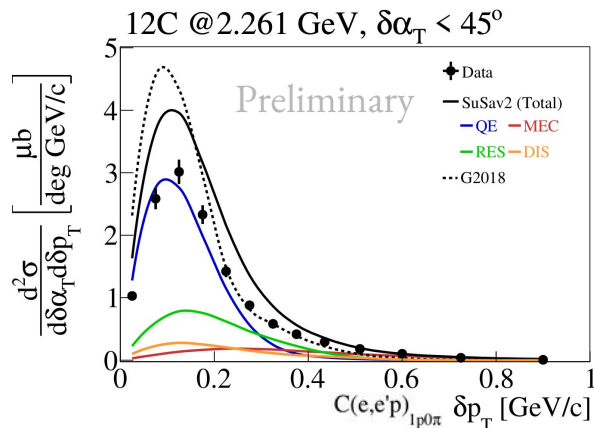
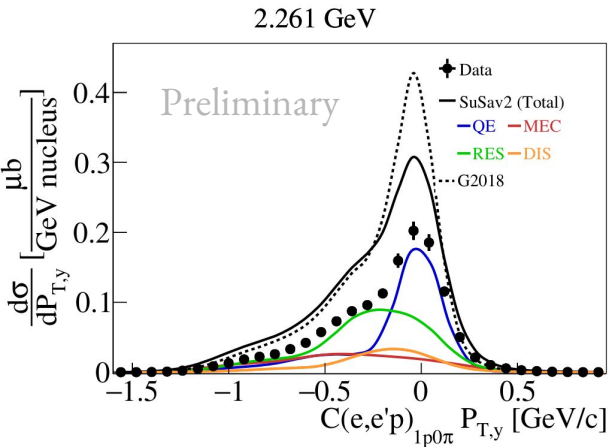
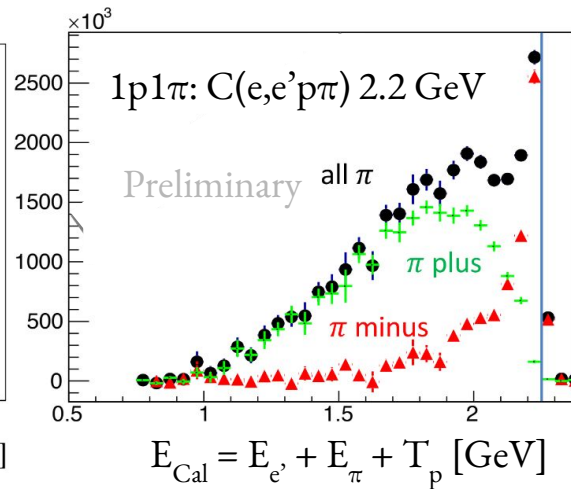
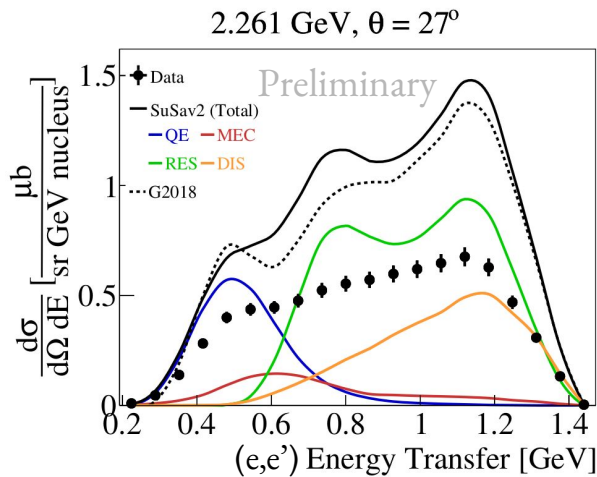
q = momentum transfer

[A.Papadopoulou, et al, In preparation](#)

The e4ν Result Factory Continued!

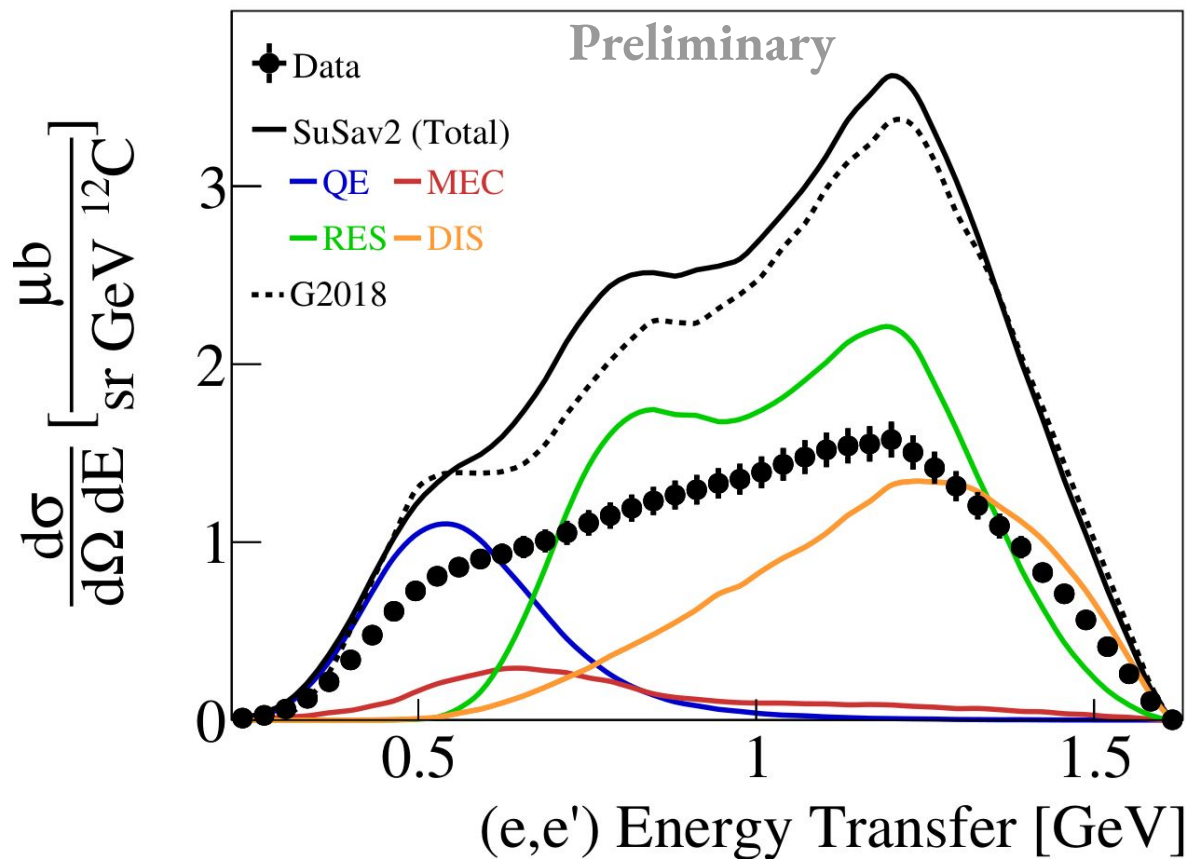
- More inclusive results
- More complex channels
- Nuclear sensitivity variables
- Multi-differential results

e4ν Collaboration, In preparation



Inclusive Results

2.261 GeV, $\theta = 28^\circ$



The e4ν Result Factory
Continued!

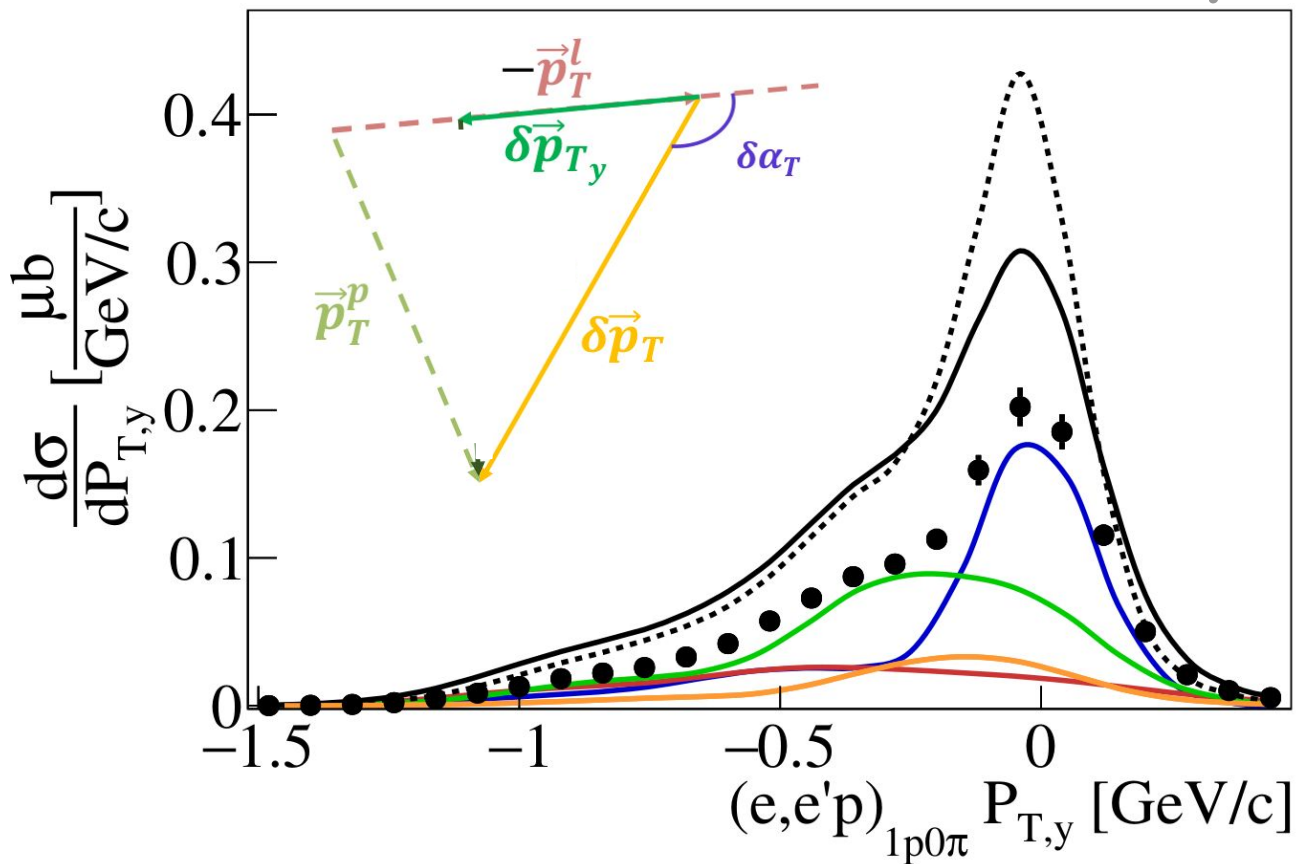
- Scan over multiple angles
- Results on Argon soon

e4ν Collaboration
In preparation

Nuclear Sensitivity Variables

12C @ 2.261 GeV

Preliminary



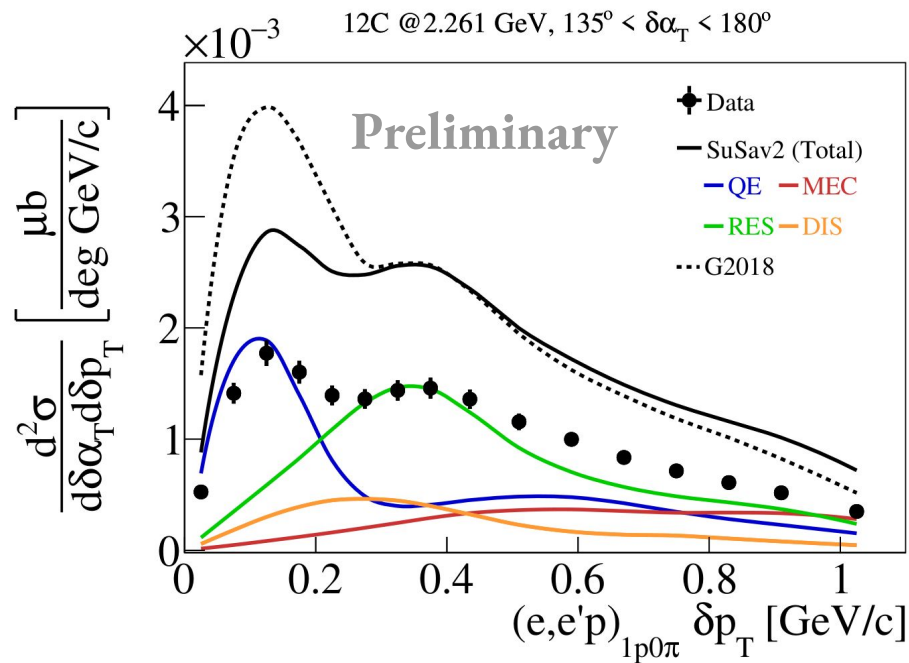
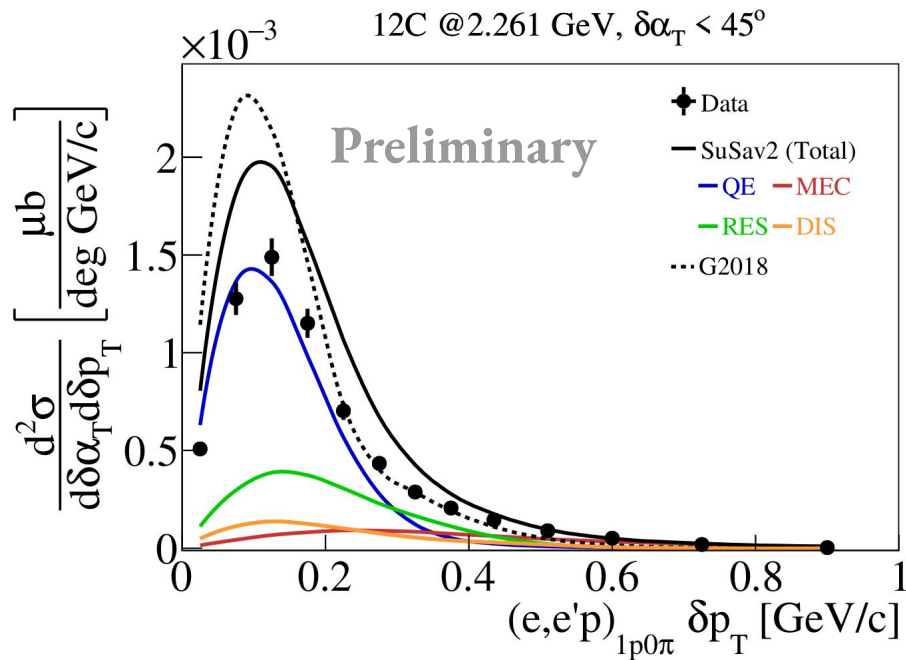
$$\delta p_{T,y} = -\hat{p}_T^l \cdot \delta \vec{p}_T = |\delta \vec{p}_T| \cos(\delta \alpha_T)$$

The e4ν Result Factory
Continued!

- Fermi motion
- Final state interactions (FSI)

e4ν Collaboration
In preparation

Double Differential Results



The e4ν Result Factory
Continued!

e4ν Collaboration
In preparation

- Handle over FSI / initial state effects
- Tuning potential