

# Scaling of e+e- Ring Collider

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# $e^+e^-$ Ring Colliders

- Lots of proposals since LEP3 proposal a year ago
- Except for the local issues
  - Can be accommodated in existing tunnel? (LHC)
  - If new tunnel, does it fit with future plans of the lab? (LHeC, HELHC, VLHC, etc)
- Problems are common to all the proposals
- The only parameters are
  - Ring size
  - site power limitation

# Common Features of $e^+e^-$ Ring Colliders

- High luminosity  $\sim 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  causes short beam life time due to radiative Bhabha scattering
  - Top-up injection needed
  - one more ring
- Bunch collision frequency (5-50kHz) much lower than in B factories (10-100MHz)
  - because synch.rad.power must be reduced
    - reduce total current , keeping luminosity
    - increase bunch charge & decrease # of bunches
  - hence, LC-like collision frequency and bunch charge
    - beamstrahlung similar to LC

# Limitation of $e^+e^-$ Ring Colliders

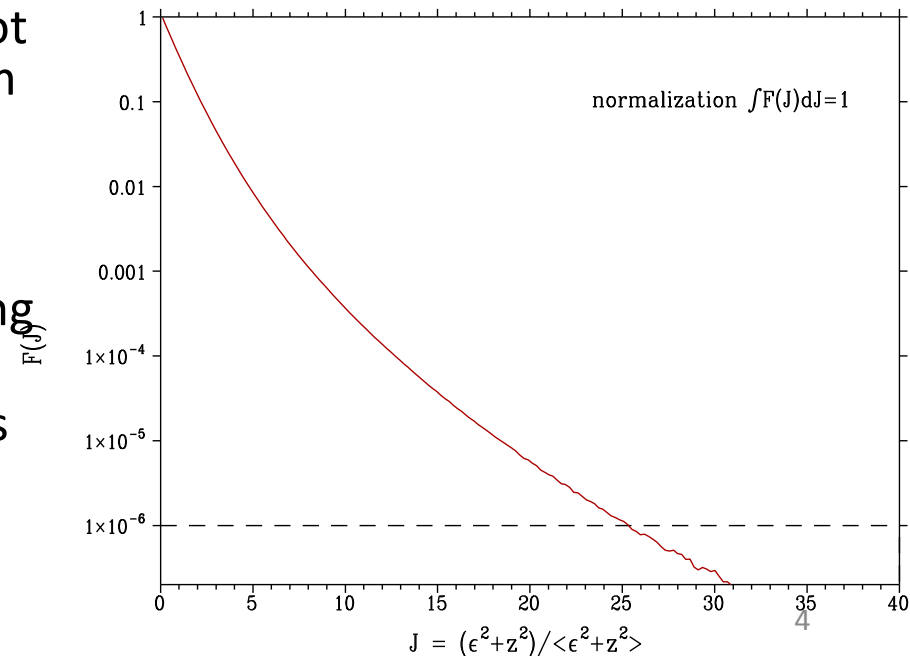
- Beamstrahlung at high-energy tail causes significant energy loss of electrons/positron

$$\Upsilon_{max} \approx \frac{2Nr_e^2\gamma}{\alpha\sigma_z\sigma_x}, \quad (\sigma_x \gg \sigma_y)$$

$$\frac{dW}{d\omega} \propto \exp\left[-\frac{2\omega}{3\Upsilon E_e}\right], \quad (\Upsilon E_e \ll \omega \ll E_e)$$

Distribution of Longitudinal Action J

- Particles with large energy loss cannot circulate around the ring (momentum band-width)
- Affects the beam life time
- Hence, ring colliders are much more fragile than LCs against beamstrahlung
  - Once accelerator is OK, then beamstrahlung in ring colliders is milder than in LC for physics



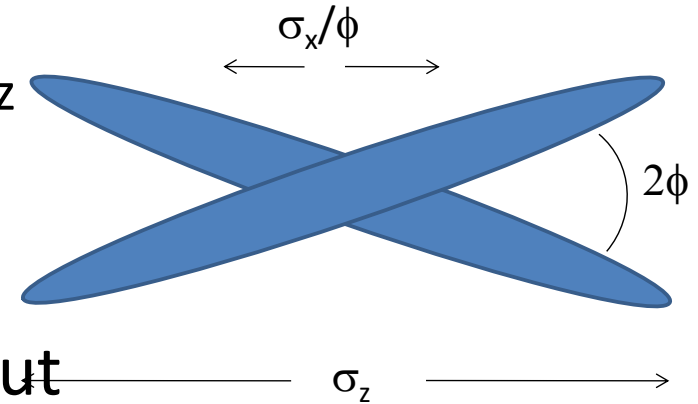
# Nanobeam Scheme (or Crab Waist)

- large crossing angle  $\gg \sigma_x/\sigma_z$   
(no crab cavity compensation)

- merits

- effectively short bunch without using high RF voltage
- this makes smaller beta possible

- But does not help in solving the beamstrahlung issue



# Luminosity Scaling of $e^+e^-$ Ring Colliders

V. Telnov, arXiv:1203.6563v, 29 March 2012

- For given Upsilon, the momentum band width must be

$$\eta \equiv [\Delta p/p]_{max} \gtrsim 15 \Upsilon$$

- Then, the luminosity at beamstrahlung limit and tune-shift limit is given by

$$\mathcal{L} \propto \frac{\rho P_{SR}}{E^{13/3}} \left( \frac{\xi_y \eta^2}{\varepsilon_{g,y}} \right)^{1/3}$$

$P_{SR}$  : syn.rad.power

$\rho$  : bending radius

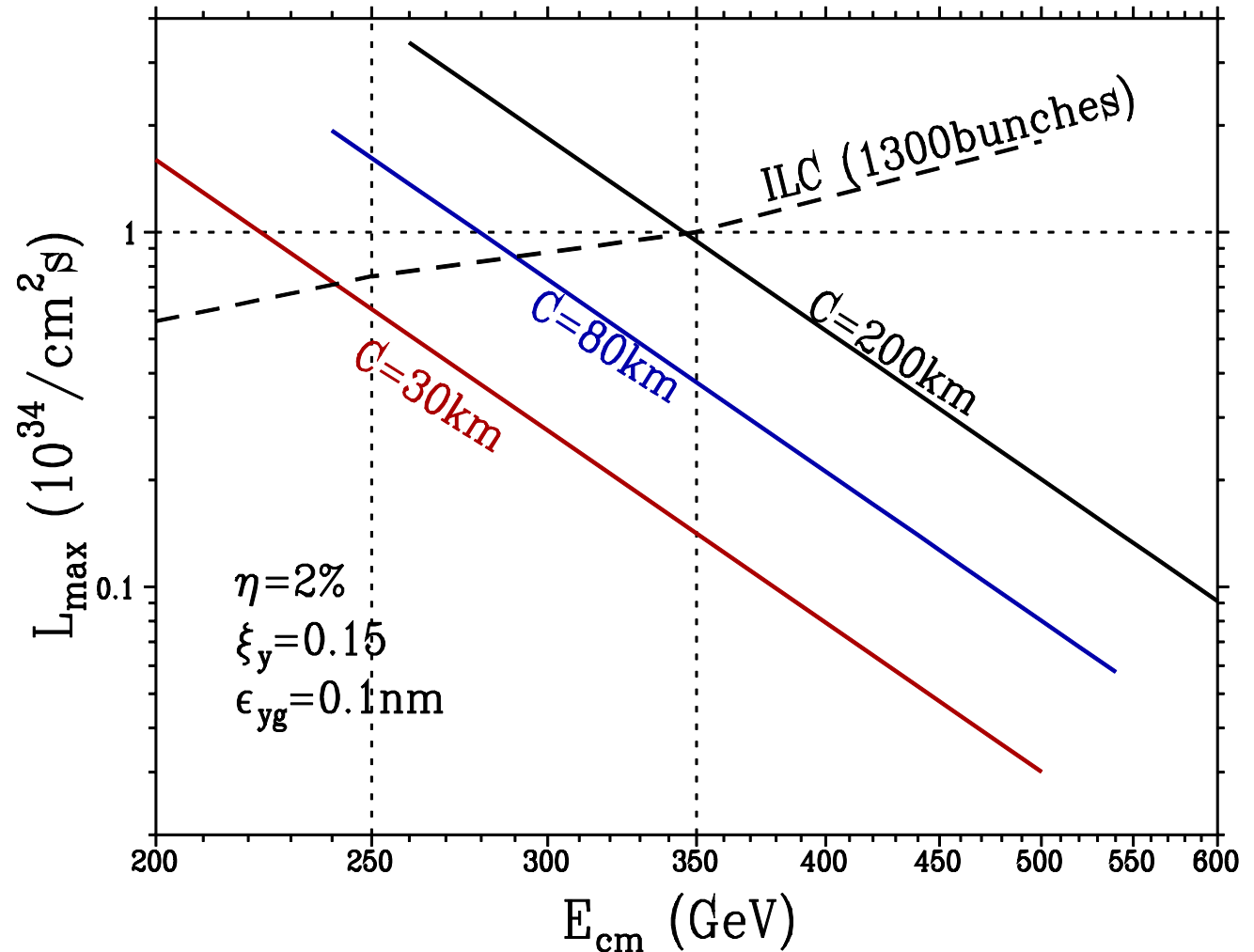
$\xi_y$  : tune-shift

$\varepsilon_{g,y}$  : geometric emit.

# Luminosity vs. Energy

example with

- $\eta=2\%$
- $\xi_y=0.15$
- $\epsilon_{gy}=0.1\text{nm}$



# R&D Items of Ring Colliders (1)

- Momentum band-width
  - RF bucket height must be  $> \eta$  (OK with a higher  $V_{RF}$ )
  - Transverse acceptance of off-momentum particles is an issue
  - Arc is OK (light sources accept  $> 4\%$ )
  - FFS is not easy
    - chromaticity  $L*\eta/\beta_y*$  large
    - 2% is perhaps feasible (non-educated guess)
- But what is “momentum band width”?
  - Usually, track particles with given amplitude (constant energy or constant synchrotron oscillation amplitude) over several damping times.
  - Synchrotron tune very high
  - Damping is very fast
  - It does not make much sense to track particles with constant energy or constant synchrotron/betatron amplitude
  - Possible tracking to guarantee beamlife
    - track 10-100 particles over desired life ( $10^7$  turns)
    - including
      - exact lattice
      - synchrotron oscillation
      - synchrotron radiation in the arc
      - beam-beam kick by Erskine-Basetti
      - Beamstrahlung by Erskine-Basetti
    - And see how many particles survive



# R&D Items of Ring Colliders (2)

- Vertical emittance
  - light sources can reach  $\varepsilon_{gy} \sim 1\text{pm}$  at low energy
  - still far above the fundamental limit due to radiation opening angle ( $1/\gamma$ )
  - but what about colliders at high energy?
- Synchrotron radiation power  $O(100\text{MW})$ 
  - 4x LEP2
  - critical energy  $> \text{MeV}$
  - How large is the AC power?
  - RF coupler
  - Vacuum
  - cryogenics
- IR region design
  - very small beta
  - different beam energy for  $e^+$  and  $e^-$  due to beamstrahlung  $O(0.1\%)$

# (personal) Conclusions

- ILC/CLIC Higgs factory are obvious if 500GeV is feasible
  - cost and staging issues
  - CLIC has maturity problem for early start
- $e^+e^-$  Ring Colliders
  - Technology not trivial
    - Good exercise of accelerator physics (till an LC starts)
  - LEP3 (27km, 240GeV) & TLEP (80km, 350GeV) are just at the border of feasibility
  - Can be a choice if higher energy with  $e^+e^-$  is not needed at all
- $\gamma\text{-}\gamma$  Colliders
  - technology immature
  - good target as a second stage of linear colliders
- Those who are not satisfied with personal conclusions, go to FNAL →