DUNE Oscillation Sensitivities using MaCh3

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How Do Long-baseline Analyses Work?

$N(\text{Observables}) = \int \frac{\text{Flux}(E_{\nu}, \text{time}) \times \text{Interaction prob}(E_{\nu}, \text{final state})}{\times \text{Detector Efficiency}(\text{final state}) \times \frac{\text{Osc}(E_{\nu})}{\text{Osc}(E_{\nu})}}$

- We have a large number of events (ND + FD) at DUNE need to constrain our systematics
- How do we do that? Near Detector! O(100 million), no oscillations!
- Far detector has far fewer events and oscillations -> apply systematic constraints



Why is this difficult?

- Systematic model needs to be complex extrapolating between very precise ND complex
 huge FD with different systematic uncertainties
 - **True energy -> reco energy map** key to extracting true parameter values
- Simplified model will cause bias/over-constraints
- Uncertainties are degenerate with each other
- ND data will pin down each systematic -> encountered by Technical Design Report (TDR) analysis





• Systematic X applies to ND and FD events



Toy Example:

• Systematic X applies to ND and FD events





Toy Example:

• Systematic X applies to ND and FD events



ND will work out exact value of systematic X!



Toy Example:

• Systematic X applies to ND and FD events



• Add systematic Y which only affects ND also shifts events from A->B = degeneracy

• Now ND can't work out value of systematic X



MaCh3 - A Markov Chain Monte Carlo Fitter with a built-in Likelihood Calculator



Binned Likelihood Analysis

• We need to model this complex/degenerate likelihood space -> different types of systematics:



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Splines



- Continuous response functions using piecewise cubic interpolation
- Binned or event-by-event
- Cross-section parameters



Binned Likelihood Analysis

Splines

• We need to model this complex/degenerate likelihood space -> different types of systematics:



Normalisation

- Continuous response functions using piecewise cubic interpolation
 Weigh to para
- Binned or event-by-event
- Cross-section parameters



- Weights events up and down relative to parameter movement
- Apply to specific kinematic ranges and events
- Flux parameters





Binned Likelihood Analysis

• We need to model this complex/degenerate likelihood space -> different types of systematics:



• Cross-section parameters

Flux parameters



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Binned Likelihood Analysis

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How do we explore this complicated likelihood space...?

- Likely 500+ parameters total
- Discontinuous
 - Events moving between bins and samples
- Multiple minima



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* MCMC has entered the chat *



MCMC - Markov Chain Monte Carlo

- Semi-random walk around the full parameter space
- Metropolis-Hastings algorithm for accepting or rejecting steps
- Builds up distribution of steps in each parameter -> proportional to target distribution
- Scales well with dimensions
- Can deal with discontinuous likelihoods (caused by event shifting)





Bayesian Inference

- MCMC let's evaluate a nearly impossible integral to get the posterior distribution
- Multi-dimensional posterior... we only want oscillation parameters
- Marginalisation integrate out nuisance parameters
- MCMC gives us this integral for free

theorem:
$$A \mid B) = rac{P(B \mid A) \cdot P(A)}{P(B)}$$



b





Bayes'

Current motivations for this analysis

- Sensitivity studies can DUNE do what it hopes to do?
- Motivate design choices for DUNE
 - How will this complex Near Detector affect our sensitivity?
 - Prove that we do need it!
- Check how systematics behave in these large fits
- Check out our fits behave with much larger statistics





FD-only Sensitivities



FD-only Asimov fits

• Fits were run with **27 million** steps for **stats-only** & **104 million** steps w/ **flux+xsec systs**

- NuFit 4.0 NH Asimov point chosen for comparisons with DUNE TDR
- Uses simple TDR model (and no detector systs) -> would look worse with full syst model
- Using nominal 7 year exposure -> 336 ktMWyr and without reactor constraint
- Step sizes for systematic parameters have been tuned
- Reweighting binned in mode and true energy



FD-only Stat-Only: 2D Contours



- Asimov point and best-fit point lie in close agreement
- 1σ contour only in correct octant



FD-only w/Systs: 2D Contours



- Best fit point and Asimov point show good agreement
- Both θ₂₃ octants being evaluated correct octant chosen
- Some degeneracy between θ_{13} and θ_{23}
- No posterior in IH as expected

FD-only w/Systs: FD w/Systs Asimov Fit: Stats-only Comparison



- Contours with systematics are **wider** than stats-only
- Systematics are doing their job!



FD w/Systs Asimov Fit: Cross-section Constraints



- Little constraining power from FD as expected
- Parameters which appear to have strong constraints have almost flat priors within bounds
- Some systematics end up wider posteriors than priors -> likely due to correlations with flux

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FD w/Systs Asimov Fit: Jarlskog Invariant

- The Jarlskog invariant indicates the magnitude of CP violation
- Value of 0 indicates **no CP violation**
- MaCh3 can produce a Jarlskog invariant posterior distribution without running another fit
- Plan to produce unitarity triangle plots -> Marvin Pfaff (ICL)





What about ND?



ND Progress

- Added ND-LAr samples used in FD TDR analysis
- Replicated FHC CC inclusive and RHC CC inclusive sample cuts
- Produced varied spectra on samples with TDR xsec and flux systematics
- Produced splines for TDR samples binned in reco energy, true energy and Bjorken y
- Joint FD + ND fits running with xsec and flux systematics -> chains need to be tuned





ND_FHC_CCnumu

Conclusion and Plans

- MaCh3 can perform the accurate systematic treatment needed to handle DUNE's statistics
- FD-only Asimov fits look as we'd expect
 - Adding detector systematics -> full FD-only comparison with TDR
- ND-LAr samples added -> xsec + flux fits need tuning
- UK students playing a leading role in DUNE LBL analysis using MaCh3
 - Naseem Khan (ICL) will be adding ND-GAr samples to this analysis

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And that's MaCh3 in a nutshell...

A Markov Chain Monte Carlo Fitter with a built-in Likelihood Calculator



Already successfully used on data from T2K and NOvA, in progress for DUNE and Hyper-K





What is MaCh3

- Markov Chain Monte Carlo-based Bayesian fitter with integrated likelihood calculator capable of predicting event rates and distributions at near and far detectors
- Fit distributions at ND and FD to constrain models
- Core functionality is straightforward to adapt to other experiments
- In use for T2K, T2K+NOvA, T2K+SK atmospherics, and in progress for DUNE and Hyper-K
- We usually perform a joint ND+FD fit but can also fit ND separately and use post-ND-fit-constrains in a FD fit



MaCh3 code release

Code stripped of T2K internal version

• CPU-only and CPU+GPU versions available

• Multi-threading

- Using CMake build system, Root 6
- Successfully built at DUNE gpvms, CERN, Royal Holloway, Imperial, ETH, etc. systems
- Release planned on github after initial phase





Existing MaCh3 features: reweighting capability

- MaCh3 has full access to event-by-event kinematics during the fit
 - Enables reweights at each parameter step with functional forms on any event variable
 - Also enables shifts of variable at each step, e.g. events can be put in different bins as a result of shift in momentum
- Also infrastructure for standard bin-by-bin response functions and linear normalisations implemented
- Response can be broken down also by interaction mode, oscillation channel, true variable bins, etc.





FHC nue selection per mode Total variation from MaQE





FD Asimov Fit

• New refactored MaCh3 DUNE **significantly improved step time** allowing us to run longer chains

- Spline evaluation improvements made in **T2K** reduced step time by ~ **8x!**
- Maximal δ_{CP} violation Asimov point chosen
- Fits were run with **17 million** steps for **stats-only** & **23 million** steps w/ **flux+xsec systs**

 Typically takes O(18k) steps to get an independent step so we have O(1k) independent points were evaluated for both



CUDAProb3 Speed

- Checked chain step time by running dummy fits with both CUDAProb3 and Prob3++ calculators
- GPU step time is very similar
- Step time in MaCh3 is generally: oscillation calculation + spline evaluation
- When using GPU osc calc almost all the steptime is CPU spline eval





CUDAProb3 Speed - CPU



- CPU step time improves drastically when osc calc is multi-threaded comparable to GPU!
- CPU osc calc allows us to run significantly more chains in parallel
- Available to the wider DUNE collaboration!

