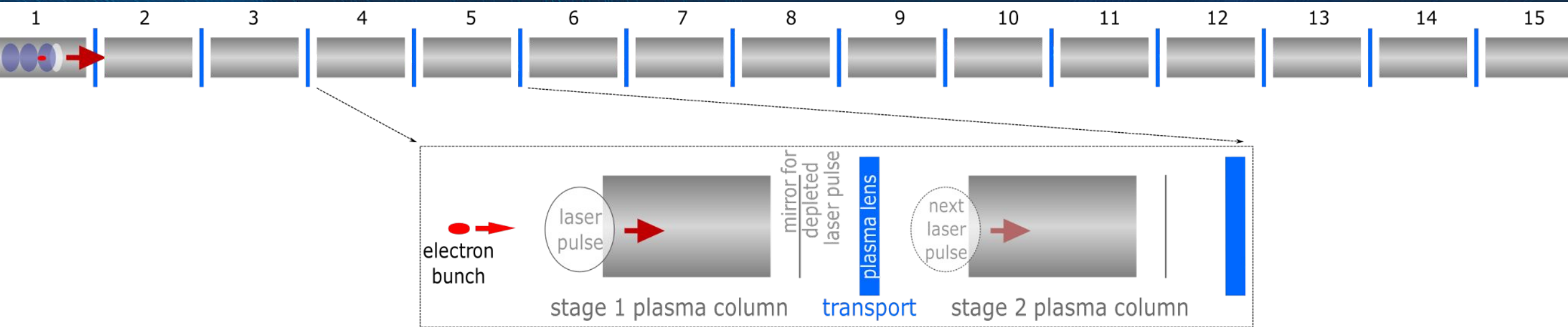


# Data-Driven Modeling for Wakefield Colliders – New Capabilities for Integrated RF & Wakefield Modeling in BLAST

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Marco Garten, Andrew Myers, Ji Qiang, Jean-Luc Vay



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# Abstract (12' + 3' Q&A)

Kinetic simulations of relativistic, charged particle beams and advanced plasma accelerator elements are often performed with high-fidelity particle-in-cell simulations, some of which fill the largest GPU supercomputers. **Self-consistent modeling of wakefield accelerators for colliders includes many elements beyond plasma acceleration.** The integrated Beam, Plasma & Accelerator Simulation Toolkit (**BLAST**) provides high-performance simulation codes suitable to model different parts of a beamline on the latest and world's largest GPU supercomputers. Yet, for some workflows such as **start-to-end modeling and coupling with experimental operations** (digital twins), it is desirable to integrate and model all accelerator elements with **very fast, effective models**. Traditionally, analytical and reduced-physics models fill this role, usually at a cost of lower fidelity and/or reduced dynamics.

Here, we show that the **vast data from high-fidelity simulations** and the power of **GPU-accelerated computation** open a new opportunity to **complement traditional modeling: data-driven surrogate modeling** through **machine learning (ML)**. We present the new capabilities for fully GPU-accelerated, **in-the-loop ML workflows in BLAST** and how they complement and fill a need alongside first-principles modeling and reduced models and **pair** well with recently established out-of-the-loop machine-learning workflows (i.e., **optimization**). We demonstrate that the high-quality data from WarpX simulations can train **low-error surrogate data models**, which are seamlessly integrated into a **GPU beamline simulation using ImpactX**, with the purpose of **minimizing chromatic emittance growth during acceleration and transport in a staged laser-wakefield accelerator** of low beam charge.

# Outline

## **Approaches to wakefield collider modeling**

theoretical, first-principle & reduced physics simulation, data

## **BLAST Codes for Accelerator Modeling**

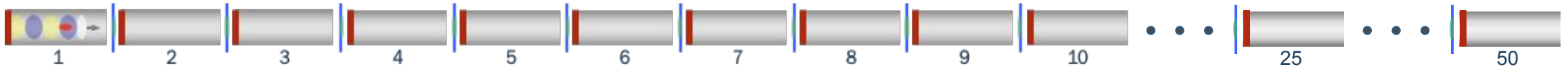
Exascale & ML Technology in WarpX and ImpactX

## **Staging of LWFA for future HEP colliders**

Hybrid beamlines: plasma & transport modeling, ML integration & evaluation



# Level of Realism: 50 multi-GeV Stages Modeled in 3D



first 3D simulation of a chain of 50 plasma accelerator stages

## LWFA lattice:

- Plasma channels: 28cm
- Gaps: 3cm
- Plasma lens model: linear thick lens (3 mm) w/ "residence correction"

## Electron beam:

- Charge: -1 fC
- Size:  $0.75 \mu\text{m} \times 0.75 \mu\text{m} \times 0.1 \mu\text{m}$
- Emittance: 1 mm.mrad

## Analytical expression to set plasma lens strength:

$$\frac{dB_{\perp}}{dr} = \frac{\langle \gamma \rangle mc^2}{e} k^2 \quad \tan(kL_{lens}) = \frac{2\langle xx' \rangle}{k\langle x^2 \rangle - \langle x'^2 \rangle / k}$$

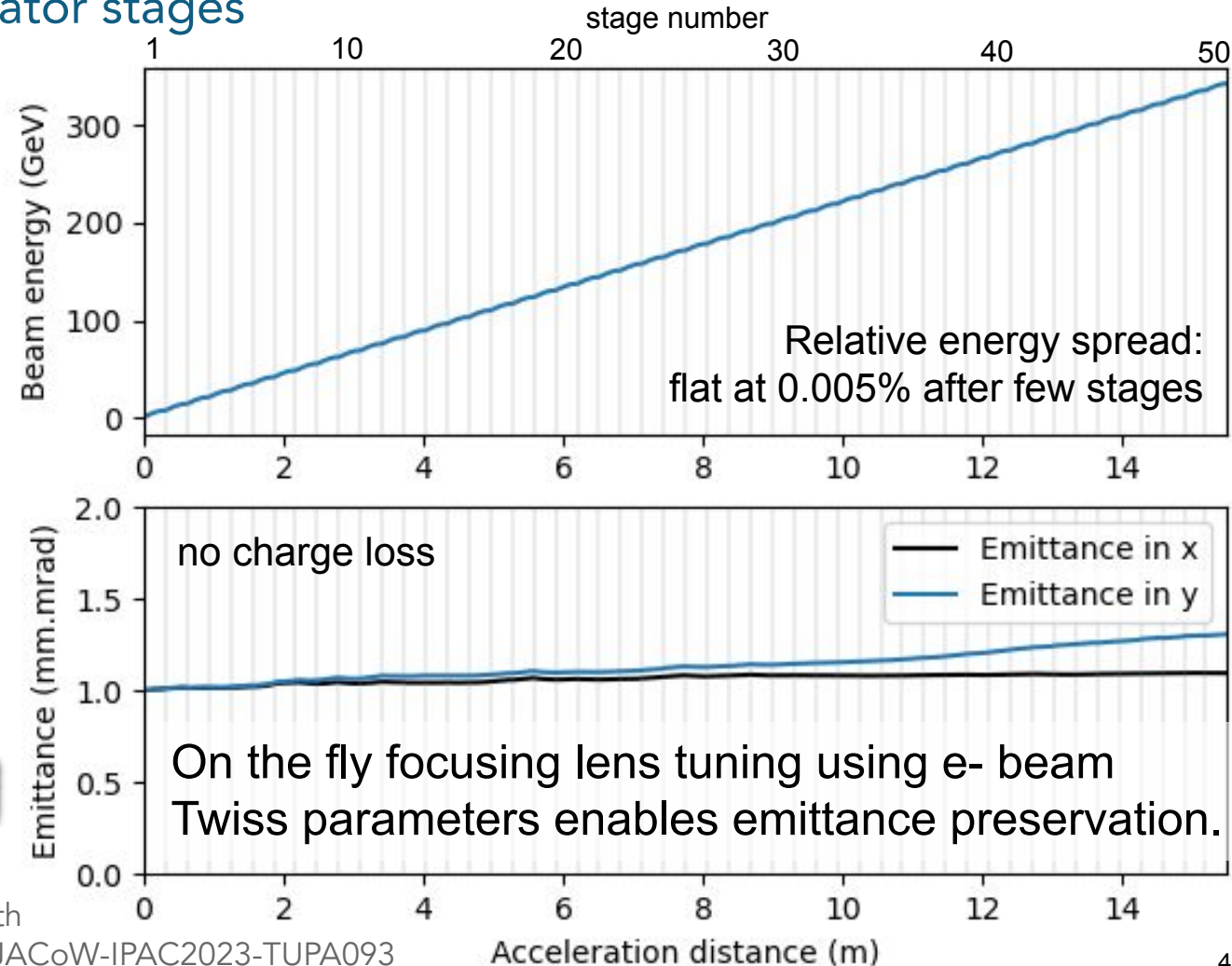
$k$  lens strength,  $\langle \cdot \rangle$  moment

## Grid size/resolution:

- $128 \times 128 \times 17664$ , boosted frame
- $2 \mu\text{m} \times 2 \mu\text{m} \times 0.01 \mu\text{m}$

## Computer: 256 GPUs for 8h

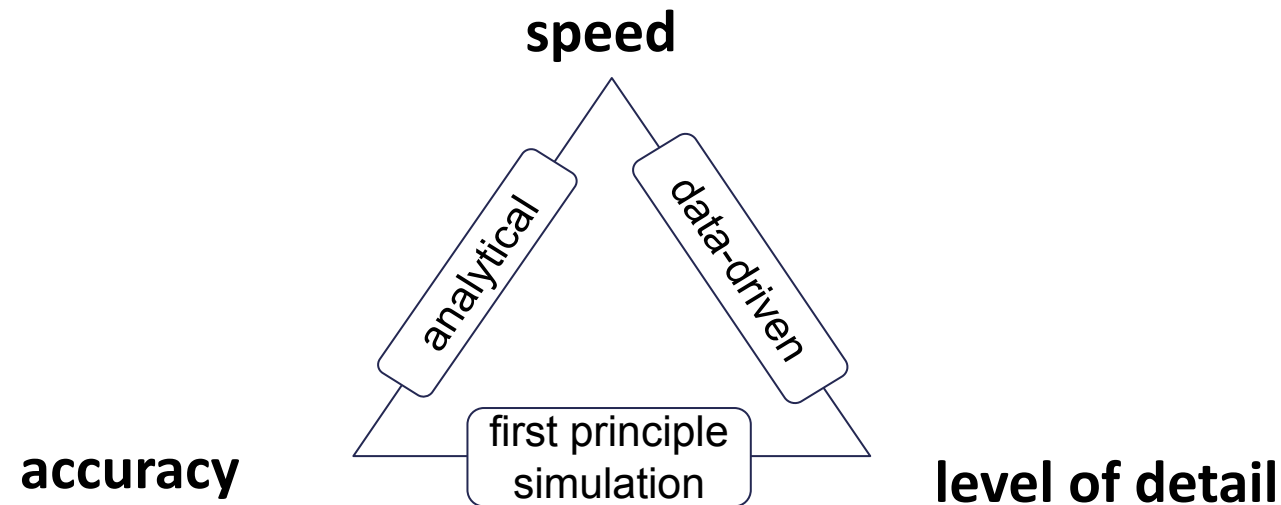
WarpX





# Approaches to Wakefield Collider Modeling

For theoretical modeling of complex, nonlinear many-body systems *such as a collider* we develop and evaluate models that have the following **characteristics** - and appear to do at best *two of those well*:



Is *data-driven modeling* via machine-learning surrogates *accurate and fast enough* for

- collider *design*: optimization and/or
- collider *operations*: digital twins ?

# BLAST Codes for Accelerator Modeling

## Exascale & ML Technology in WarpX and ImpactX







# Developed by an international, multidisciplinary team

WarpX open governance



Jean-Luc Vay



Ji Qiang



Arianna Forment



Marco Garten



Axel Huebl



Rémi Lehe



Chad Mitchell



Ryan Sandberg



Olga Shapoval



Edoardo Zoni



Kale Weichmann



Ann Almgren



Kevin Gott



Junmin Gu



Revathi Jambunathan



Andrew Myers



Weiqun Zhang



David Grote



Justin Angus



Eric Clark



Germany  
Maxence Thévenet



Severin Diederichs



Alexander Sinn



Ángel Ferran Pousa



Rob Shalloo



France  
Igor Andriyash



Switzerland  
Lorenzo Giacomel



Lixin Ge



France  
Henri Vincenti



Luca Fedeli



Thomas Clark



Pierre Bartoli



Franz Poeschel



Roelof Groenewald



over 80 contributors, incl. from the private sector





Integrated through Standards & Workflows

Data

Input

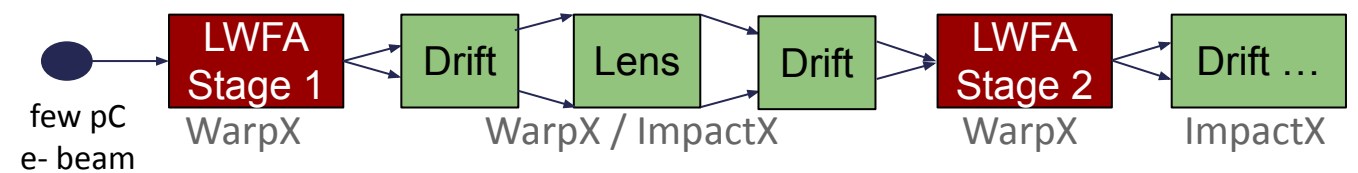
Lasers

Optimize

Code	Year started	Dimensionality	Independent variable	Solver	Symplectic maps	ML surrogate elements	Language	Parallel (multinode)	CPU and GPU	Multi-vendor GPU	Linac	Ring	Source	Wakefield accelerators	Beam-Beam	QED	E-cloud	IBS	CSR	Spin tracking	...
Warp	1989	2/3/RZ++	t/s/ξ	ES/EM/QS			For./Python	✓		✓	✓	✓	✓			✓				3D	...
Impact-Z	1999	3	s	ES	✓		Fortran	✓		✓	✓							✓		1D	...
Impact-T	2002	3	t	ES			Fortran	✓				✓						✓			...
Marylie/IMPACT	2006	3	s	ES	✓		Fortran	✓		✓	✓										...
Posinst	2002	2	t	ES			Fortran										✓				...
BeamBeam3D	2003	2.5	t,s	ES	✓		Fortran	✓			✓				✓						...
FBPIC	2015	RZ++	t	EM			Python	✓	✓				✓							✓	...
LW3D	2018	3	t	LW			Fortran	✓												3D	...
Wake-T	2019	RZ	ξ	QS			Python				✓		✓							1D	...
WarpX	2016	1/2/3/RZ++	t	ES/EM	**		C++/Python	✓	✓	✓	*	**	✓	✓	✓	✓		**		3D	**
HiPACE++	2022	3	ξ	QS			C++/Python	✓	✓	✓			✓								✓
ImpactX	2022	3	s	ES	✓	✓	C++/Python	✓	✓	✓	✓	✓						**		1D*, ML*	**

\* in development      ES=Electrostatic; EM=Electromagnetic; QS=Quasistatic; LW=Lienard-Wiechert; ML=Machine Learning Model  
 \*\* planned, seeking additional funding

## Model Speed: for accelerator elements



## Simulation time: full geometry, full physics

hrs      <sec  
 256 GPUs      1 GPU



# Augmenting & GPU-accelerating PIC Simulations & ML Models

## GPU Workflows are blazingly fast

- first-principle models: PIC simulations
- data-driven models: machine learning

*We augmented & accelerated on-GPU PIC simulations with on-GPU ML models!*

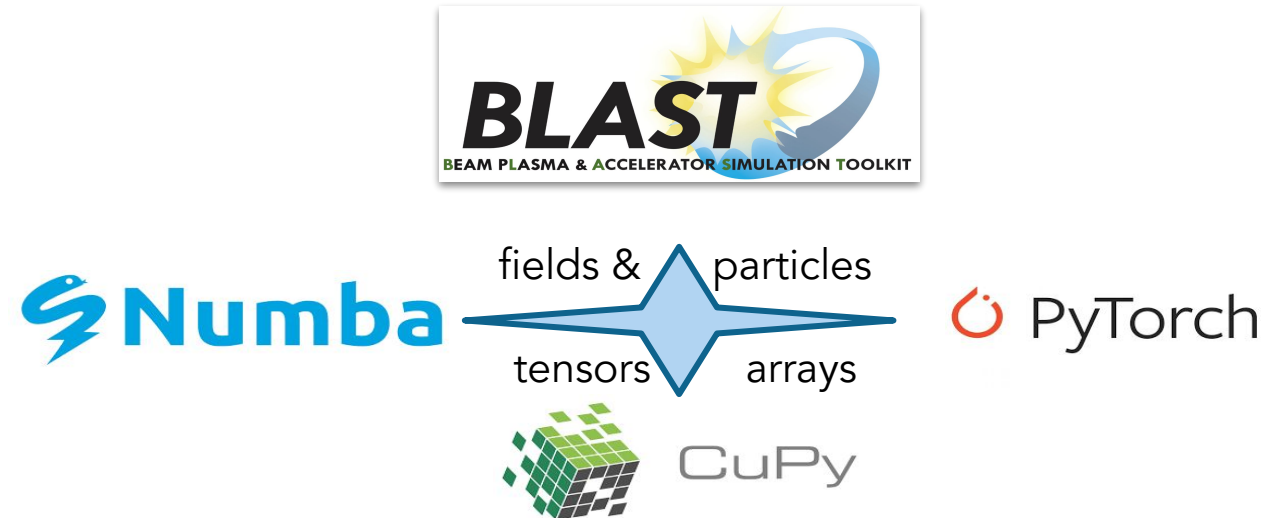
```
from impactx import ImpactXParIter
import torch

# loop over AMReX particle tiles
for pti in ImpactXParIter(...):
    soa = pti.soa().to_xp() # view
    x = soa.real["x"]      # alias
    # ... y, t, py, pt ...

    data_arr = torch.tensor( # SoA -> Tensor AoS
        stack([x, y, t, px, py, pt], axis=1),
        device=device,
        dtype=torch.float64,
    )
    # ... normalize data_arr ...

    with torch.no_grad(): # apply NN in-memory
        surrogate_model(data_arr)
```

## Compatible ecosystem between:



## Persistent GPU data placement

- read+write access, no CPU transfer



*Cross-Ecosystem, In Situ Coupling:  
Consortium for Python Data API  
Standards* [data-apis.org](https://data-apis.org)



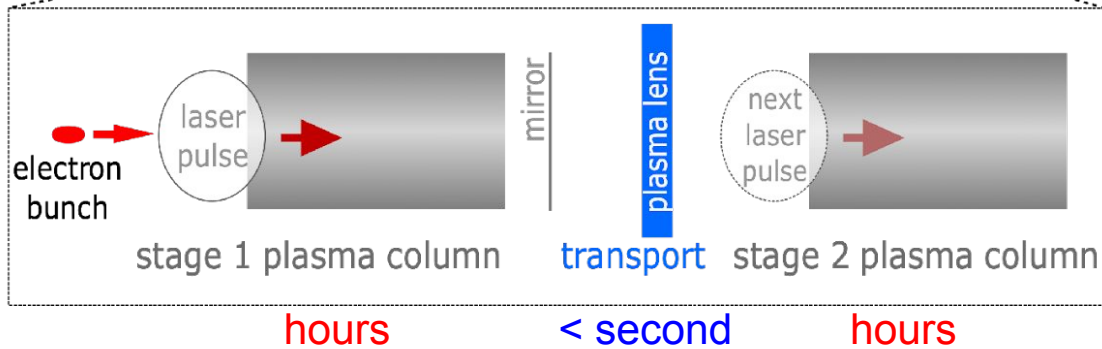
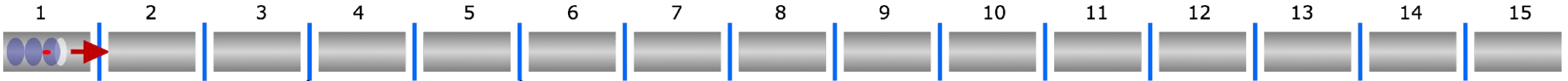
# Staging of LWFA for future HEP colliders

Hybrid beamlines: plasma & transport modeling,  
ML integration & evaluation



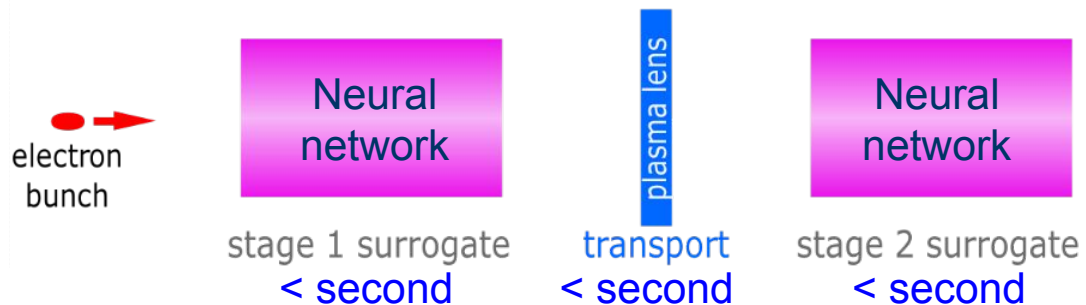
# LPA surrogate models bridge runtime gap

Our goal is to find better **transport**: Combine Plasma & RF Accelerator Elements for start-to-end modeling



- *high-quality plasma simulation can be expensive*
  - 15 stages: **1,316 A100 GPUhrs**
  - 3D electromagnetic, fully kinetic, 128x128x35328 cells
- *optimization challenge*
  - usually 1000s of runs (derivative-free)
  - repeated evaluation *in 3D* would be **very expensive**

**tightly-coupled LPA-neural networks** inside **ImpactX**



- approach: **specialized replacements**
  - *in situ* coupling of **ImpactX** simulation with **data-driven surrogates**
  - train surrogate models from **high-quality WarpX data**

# Surrogate models learn initial $\rightarrow$ final phase space map from LPA stage data generated by a high-fidelity WarpX simulation

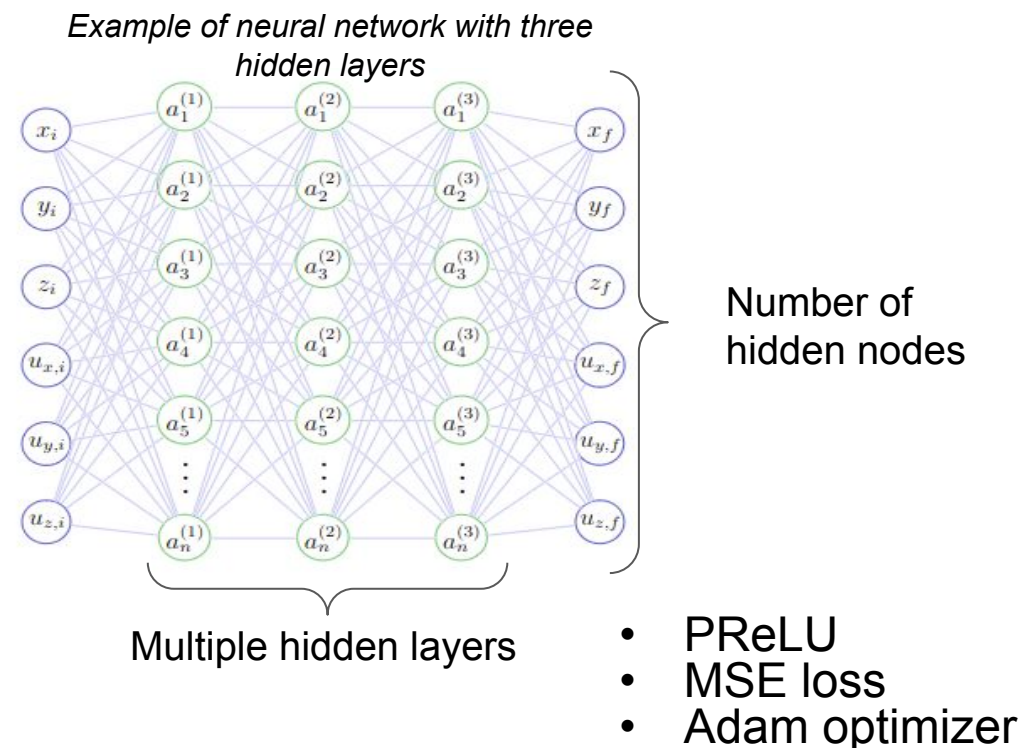
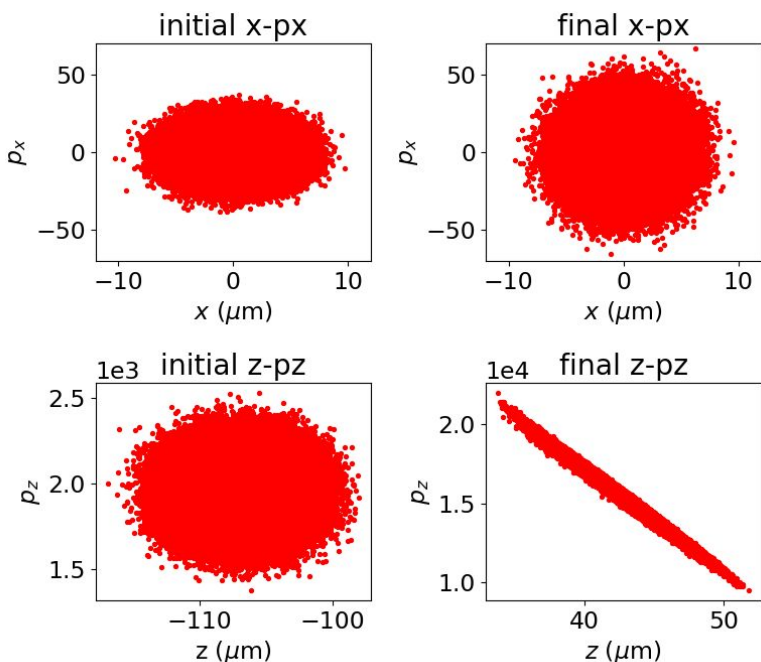
## Surrogate model: Generic Transport Map

Initial  $\rightarrow$  final  
phase space

$$f : \mathbb{R}^6 \rightarrow \mathbb{R}^6$$

$$\begin{pmatrix} x \\ y \\ z \\ p_x \\ p_y \\ p_z \end{pmatrix}_i$$

example: stage 1 training data



Stages 1-3: 5 hidden layers, 900 nodes per layer  
Stages 4-15: 3 hidden layers, 700 nodes per layer



# Surrogate models learn initial $\rightarrow$ final phase space map from LPA stage data generated by a high-fidelity WarpX simulation

## Surrogate model: Generic Transport Map

Initial  $\rightarrow$  final phase space

$$f : \mathbb{R}^6 \rightarrow \mathbb{R}^6$$

supports beams with

- ✓ arbitrary profiles
- ✓ chromatic effects
- ✗ collective effects

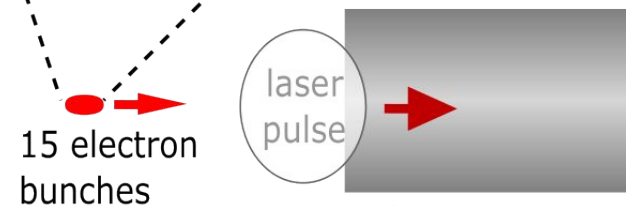
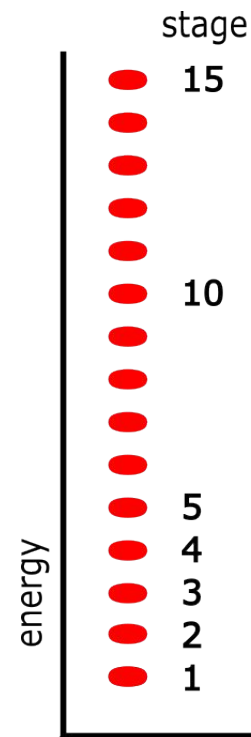


Notes:

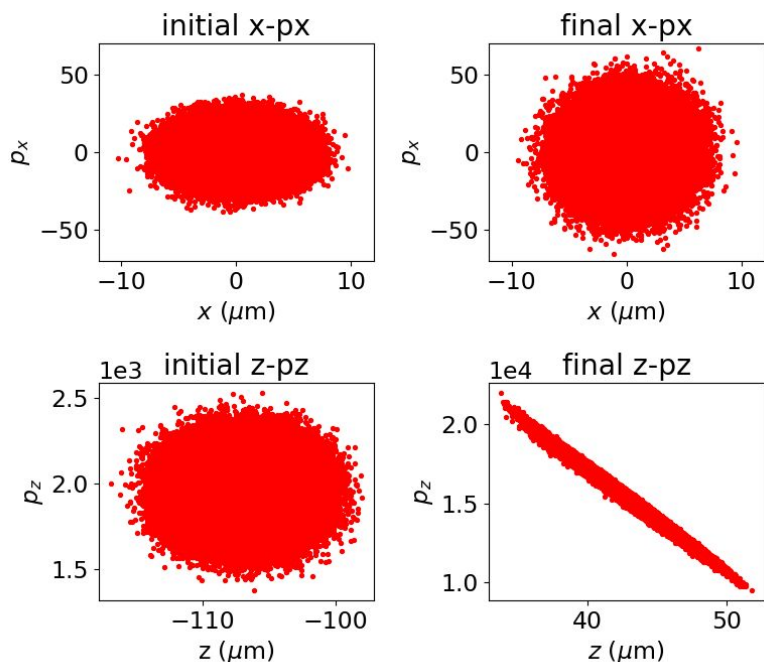
- *intentional* choice
- very easy to modify models from Python
- *ideal ground for ML model development*

## Training Data generation with WarpX

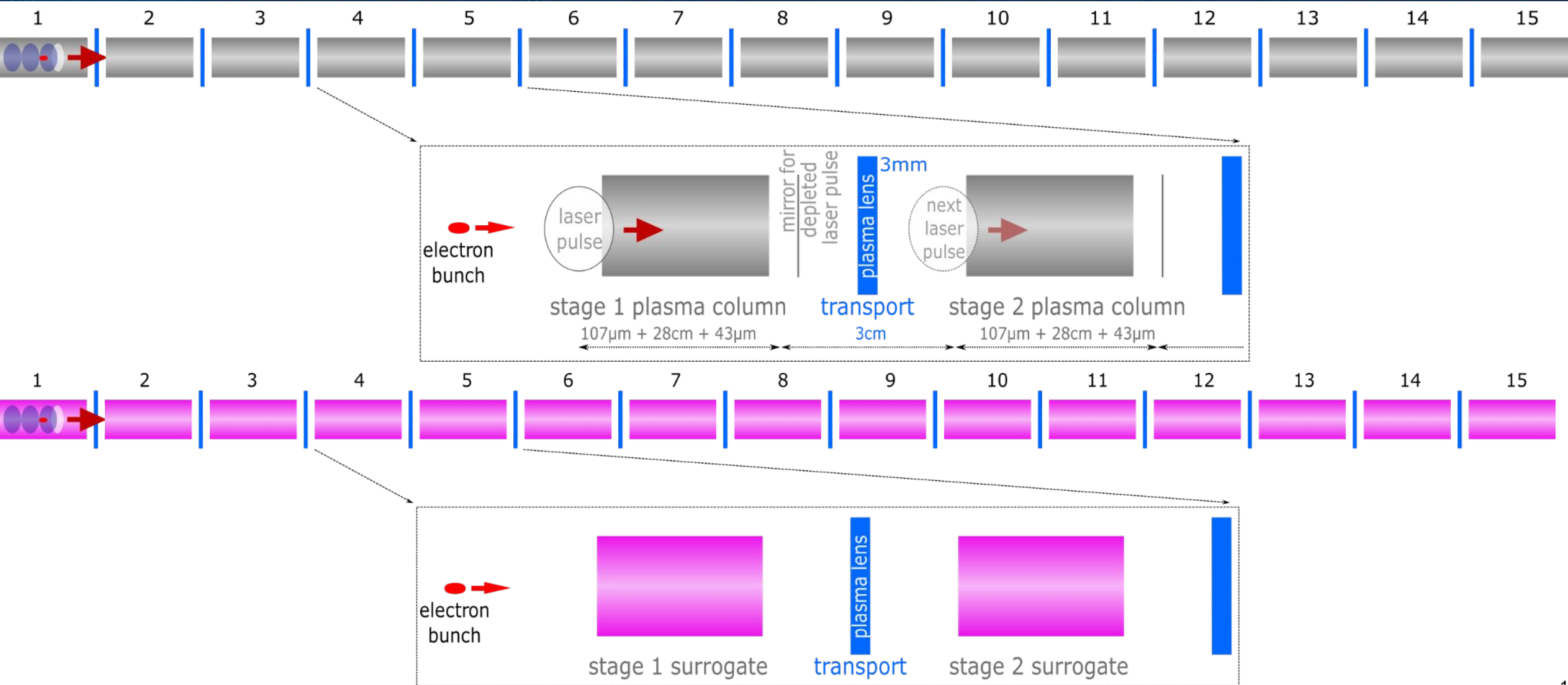
- 1 plasma column
- 15 diluted beams
- 404 A100 GPUhrs (once!)



example: stage 1 training data

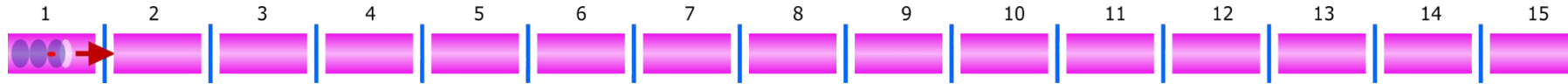


# Evaluation: Synthesis of ImpactX and WarpX-trained surrogate models

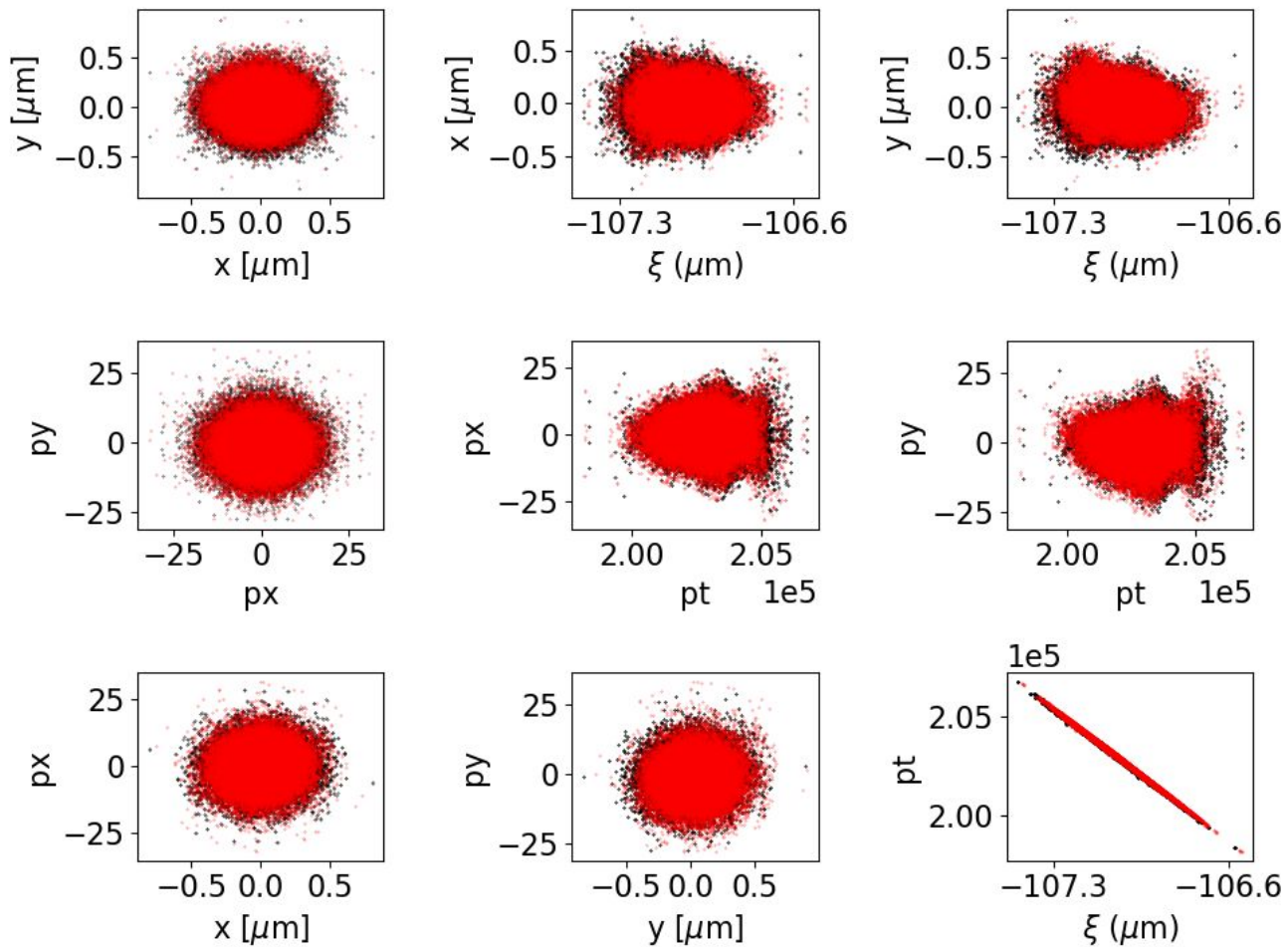




# ImpactX+WarpX surrogate agrees with WarpX reference after 15 stages



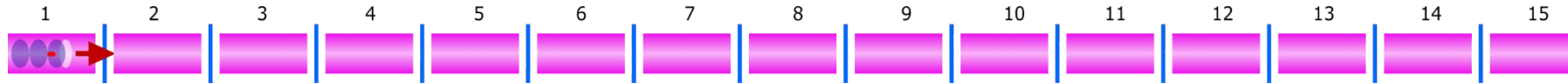
15th stage, ct=4.62e+00  
 Black: WarpX reference  
 Red: ImpactX+surrogate



Relative errors in beam moments

	stage 1	stage 2	stage 15
$\sigma_x$	0.12%	1.8%	3.2%
$\sigma_{px}$	0.54%	2.1%	2.8%
$\epsilon_x$	0.43%	0.38%	0.39%
$\sigma_y$	0.03%	1.5%	1.2%
$\sigma_{py}$	0.3%	1.9%	3.2%
$\epsilon_y$	0.3%	0.44%	2.1%

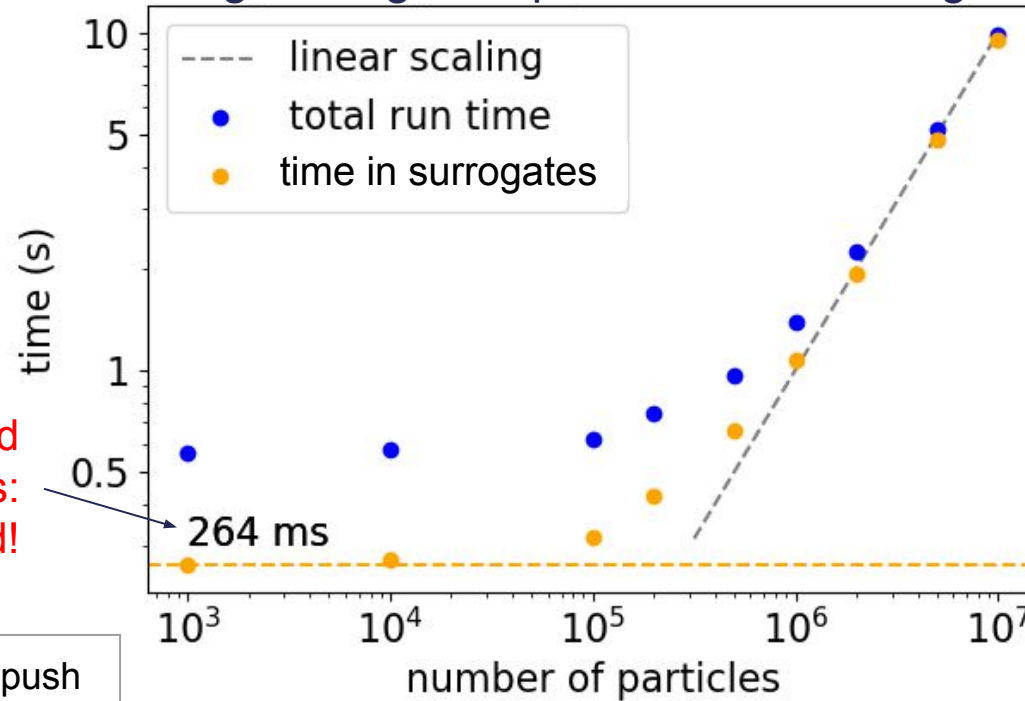
# Modeling + ML Inference are fully GPU accelerated, approaches linear strong scaling in number of particles



Note: NN inference needs significant memory. Surrogates of 15 stages did fit into 80GB A100 GPU memory.

ImpactX with WarpX-trained surrogates:  
2-4 simulations / second!

strong scaling of ImpactX+15 NN surrogates



ImpactX with WarpX-trained surrogates: 10 GPU sec for 15 stages

$10^7$ particles	Time (ms)	% of push
Stage 15 Push	495	100
Inference	477	96.4
Data Preparation	18	3.6

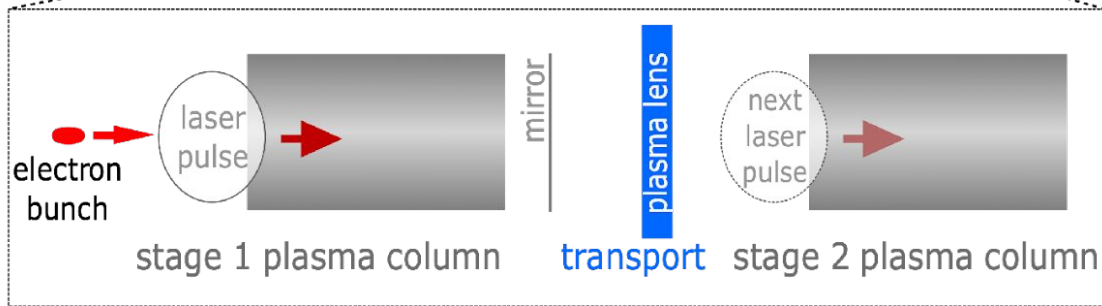
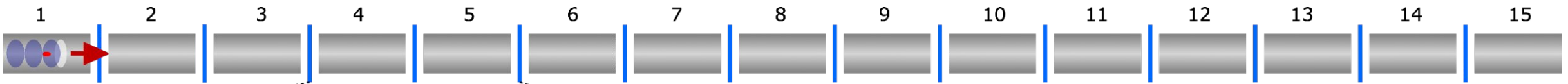
$10^3$ particles	Time (ms)	% of push
Stage 15 Push	2.77	100
Inference	0.77	27.8
Data Preparation	2.00	72.2

GPU inference time: 63ns / particle / stage  
ImpactX tracking >1M particles

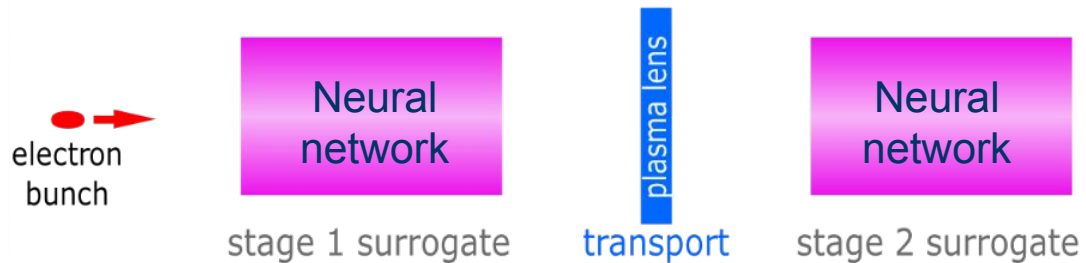


# Rapid Optimization with Surrogates: Results Transfer to 3D WarpX

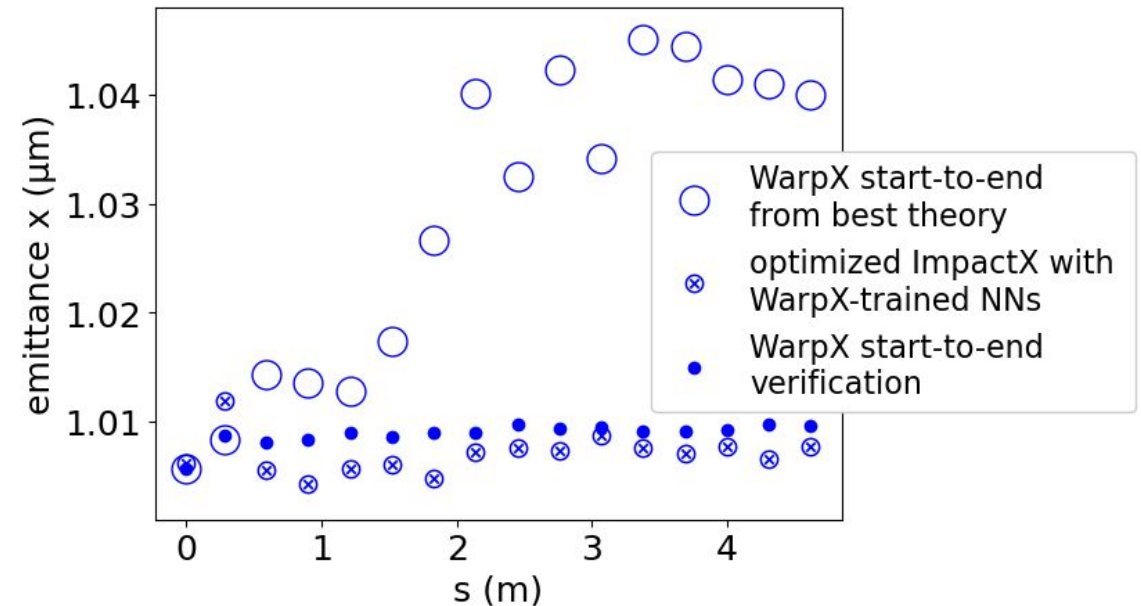
**Central BLAST Code Interoperability:** Combine Plasma & RF Accelerator Elements for start-to-end modeling high-quality, first-principle *WarpX data* used for *ImpactX* ML surrogate training



**tightly-coupled LPA-neural networks inside ImpactX**



**LPA + Transport Optimization**  
with  $\approx 1000$  evaluations



# ≈752x estimated cost savings with in-the-loop ML optimization workflow

## Previously (Estimate)

1500 GPU hours simulation  
x 1000 iterations

+ 1500 GPU hours validation simulation

= 1 501 500 GPU hours

## Optimization with in-the-loop ML surrogate model

450 GPU hours training simulation  
+ 3 GPU hours PyTorch training  
x 15 stages

+ 10 GPU seconds ImpactX+NN  
x 1000 iterations

+ 1500 GPU hours validation simulation




= 1 998 GPU hours



# In-the-loop Machine Learning Surrogates Beyond Single-Particle Tracking Maps

- **$R^6 \rightarrow R^6$  surrogate**: intentional choice, for the detailed study of **chromatic effects**
  - high level of detail, *arbitrary* low-charge phase spaces, conserves the *phase* of each particle
  - *drop-in* replacement for single-particle, first-principle models

Examples to **include collective effects** in ML surrogates:

-  **double down**: trajectory + collective beam parameters  $R^{6+m} \rightarrow R^{6+m}$ 
  - how: expose additionally  $m$  collective beam parameters to ML model for various beam charges
  - note: very costly learning phase, unless constrained (e.g., only change 1D current profile)
-  **project**: learn & predict phase spaces
  - how: learn & predict selected 2D phase spaces for various beam charges
  - note: less detailed; resampling loses phase, e.g., for tune calculations in rings
  - e.g., Emma et al, PRAB 21, 112802 (2018); Edelen et al., TUPS72, IPAC24 (2024)
-  **simplify**: work with beam moments and simpler distributions
  - how: learn & predict *only* collective beam parameters, learn simpler distributions (e.g., KV)
  - note: little detail; resampling loses phase, e.g., for tune calculations in rings
  - e.g., Edelen et al., PRAB 23, 044601 (2020); Garcia-Cardona & Scheinker, PRAB 27, 024601 (2024)

**These and your own ML ideas can now easily be implemented (Python) & studied in BLAST codes WarpX/ImpactX - see our documentation and detailed examples on how to get started** 

# In-the-loop Machine Learning Surrogates Beyond Single-Particle Tracking Maps

The screenshot shows the ImpactX documentation website. The left sidebar contains navigation links for 'Code of Conduct', 'Acknowledge ImpactX', 'INSTALLATION', 'Users', 'Developers', 'HPC', 'USAGE', and 'Run ImpactX'. Below these are 'Examples' including 'Single Particle Dynamics', 'Space Charge', 'Beam Distributions', 'Lattice Design & Optimization', 'Virtual Test Stands' (Cyclotron, Fermilab IOTA storage ring, Positron Channel), and '15 Stage Laser-Plasma Accelerator Surrogate'. The main content area is titled '15 Stage Laser-Plasma Accelerator Surrogate' and includes a search bar, a 'Search docs' input, and a 'Edit on GitHub' link. The text describes the surrogate model and lists references. A schematic diagram shows 15 stages of the accelerator, with a detailed view of two stages: 'stage 1 plasma column' (107μm + 28cm + 43μm) and 'stage 2 plasma column' (107μm + 28cm + 43μm), separated by a 'transport' section (3cm). The diagram shows an 'electron bunch' and 'laser pulse' interacting with 'plasma' and 'laser pulse' in each stage.

## 15 Stage Laser-Plasma Accelerator Surrogate

This example models an electron beam accelerated through fifteen stages of laser-plasma accelerators with ideal plasma lenses providing the focusing between stages. For more details, see:

- Sandberg R T, Lehe R, Mitchell C E, Garten M, Myers A, Qiang J, Vay J-L and Huebl A. **Synthesizing Particle-in-Cell Simulations Through Learning and GPU Computing for Hybrid Particle Accelerator Beamlines**. Proc. of Platform for Advanced Scientific Computing (PASC'24), submitted, 2024. [arXiv:2402.17248](https://arxiv.org/abs/2402.17248)
- Sandberg R T, Lehe R, Mitchell C E, Garten M, Qiang J, Vay J-L and Huebl A. **Hybrid Beamline Element ML-Training for Surrogates in the ImpactX Beam-Dynamics Code**. 14th International Particle Accelerator Conference (IPAC'23), WEPA101, 2023. DOI:10.18429/JACoW-IPAC2023-WEPA101

A schematic with more information can be seen in the figure below:

Fig. 10 Schematic of the 15 stages of laser-plasma accelerators.

The laser-plasma accelerator elements are modeled with neural networks as surrogates. These networks are trained beforehand. In this example, pre-trained neural networks are downloaded from a [Zenodo archive](#) and saved in the `models` directory. For more about how these neural network surrogate models were created, see this [description of a workflow for training neural networks from WarpX simulation data](#).

The screenshot shows the 'Training a Surrogate Model from WarpX Data' page in the ImpactX documentation. The left sidebar contains navigation links for 'Developers', 'HPC', 'USAGE', 'Run WarpX', 'Examples', 'Parameters: Python (PICMI)', and 'Parameters: Inputs File'. Below these are 'Workflows' including 'Extend a Simulation with Python', 'Domain Decomposition', 'Visualizing a distribution mapping', 'Debugging the code', 'Generate QED lookup tables using the standalone tool', 'Plot timestep duration', 'Predicting the Number of Guard Cells for PSATD Simulations', and 'Archiving'. Below these are 'Training a Surrogate Model from WarpX Data' including 'Data Cleaning', 'Create Normalized Dataset', 'Neural Network Structure', 'Train and Save Neural Network', 'Evaluate', and 'Optimizing with Optimas'. Below these are 'FAQ' and 'DATA ANALYSIS' including 'Output formats'. The main content area is titled 'Training a Surrogate Model from WarpX Data' and includes a 'Python Input for Training Simulation' section. The text describes the workflow for data processing and model training. Three plots show the final phase space of the particle beam: a scatter plot of Y (μm) vs x (μm), a scatter plot of x (μm) vs z-0.28 m (μm), and a scatter plot of Y (μm) vs z-0.28 m (μm). The plots show a dense cluster of particles with some outliers.

## Training a Surrogate Model from WarpX Data

Suppose we have a WarpX simulation that we wish to replace with a neural network surrogate model. For example, a simulation determined by the following input script

```
Python Input for Training Simulation
```

In this section we walk through a workflow for data processing and model training, using data from this input script as an example. The simulation output is stored in an online [Zenodo archive](#), in the `lab_particle_diags` directory. In the example scripts provided here, the data is downloaded from the Zenodo archive, properly formatted, and used to train a neural network. This workflow was developed and first presented in Sandberg *et al.* [1], Sandberg *et al.* [2]. It assumes you have an up-to-date environment with PyTorch and openPMD.

### Data Cleaning

It is important to inspect the data for artifacts, to check that input/output data make sense. If we plot the final phase space of the particle beam, shown in Fig. 18, we see outlying particles. Looking closer at the z-pz space, we see that some particles were not trapped in the accelerating region of the wake and have much less energy than the rest of the beam.

The three plots show the final phase space of the particle beam. The first plot shows Y (μm) vs x (μm) with a dense cluster of particles and some outliers. The second plot shows x (μm) vs z-0.28 m (μm) with a dense cluster of particles and some outliers. The third plot shows Y (μm) vs z-0.28 m (μm) with a dense cluster of particles and some outliers.

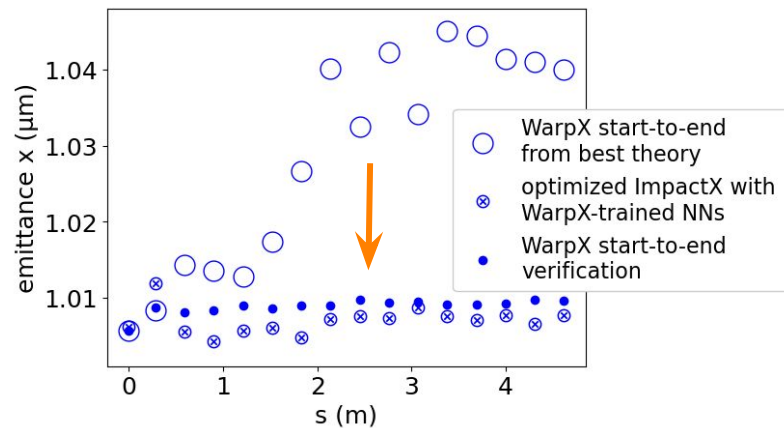
These and your own ML ideas can now easily be implemented (Python) & studied in BLAST codes WarpX/ImpactX - see our documentation and detailed examples on how to get started 



# Summary

## A fast, high-fidelity, data-driven LPA staging workflow with ImpactX+surrogate models

- **neural network surrogates** reproduce unloaded LPA simulations with % level error
- runs in **seconds** – optimization workflow gets  $\mathcal{O}(1000)$  speedup
- best ImpactX+surrogate transport parameters **readily transfer** to 3D WarpX simulations
  - **emittance significantly improved** ● for 15 stages to ○ prior best results



## Established data-driven methods in BLAST codes WarpX & ImpactX

- kinetic codes & in situ ML elements: easy to **test & study** new data models
- fully **accelerated** (GPU or CPU), fully **documented**
- vibrant, friendly & helpful **open source community** - we invite you to join

**bring your own  
lattice & ML model**



# Thank you for your attention!

## Try it yourself:



ECP-WarpX/WarpX  
ECP-WarpX/impactX  
AMReX-Codes/pyamrex



Paper: R. Sandberg et al.,  
*PASC24 Best Paper (2024)*

[DOI:10.1145/3659914.3659937](https://doi.org/10.1145/3659914.3659937)

Documented example links:

[WarpX ML training from openPMD](#)

[ML Surrogates in ImpactX](#)

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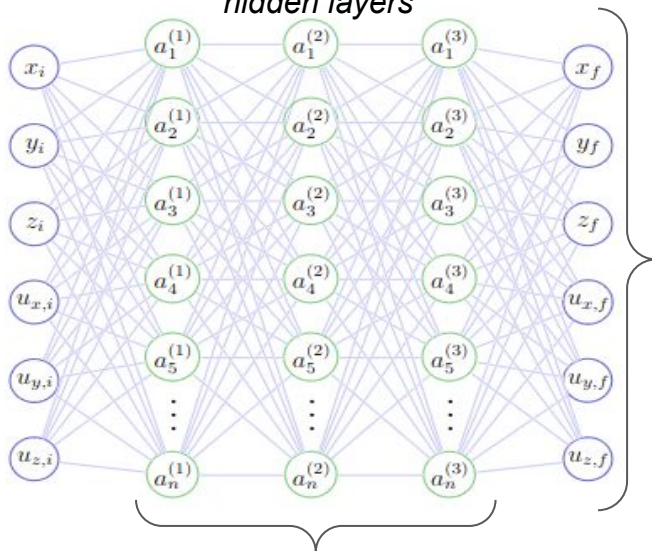


Backup Slides

# Hyperparameter tuning indicated that relatively simple neural networks were sufficiently accurate

## Model of a single stage

Example of neural network with three hidden layers

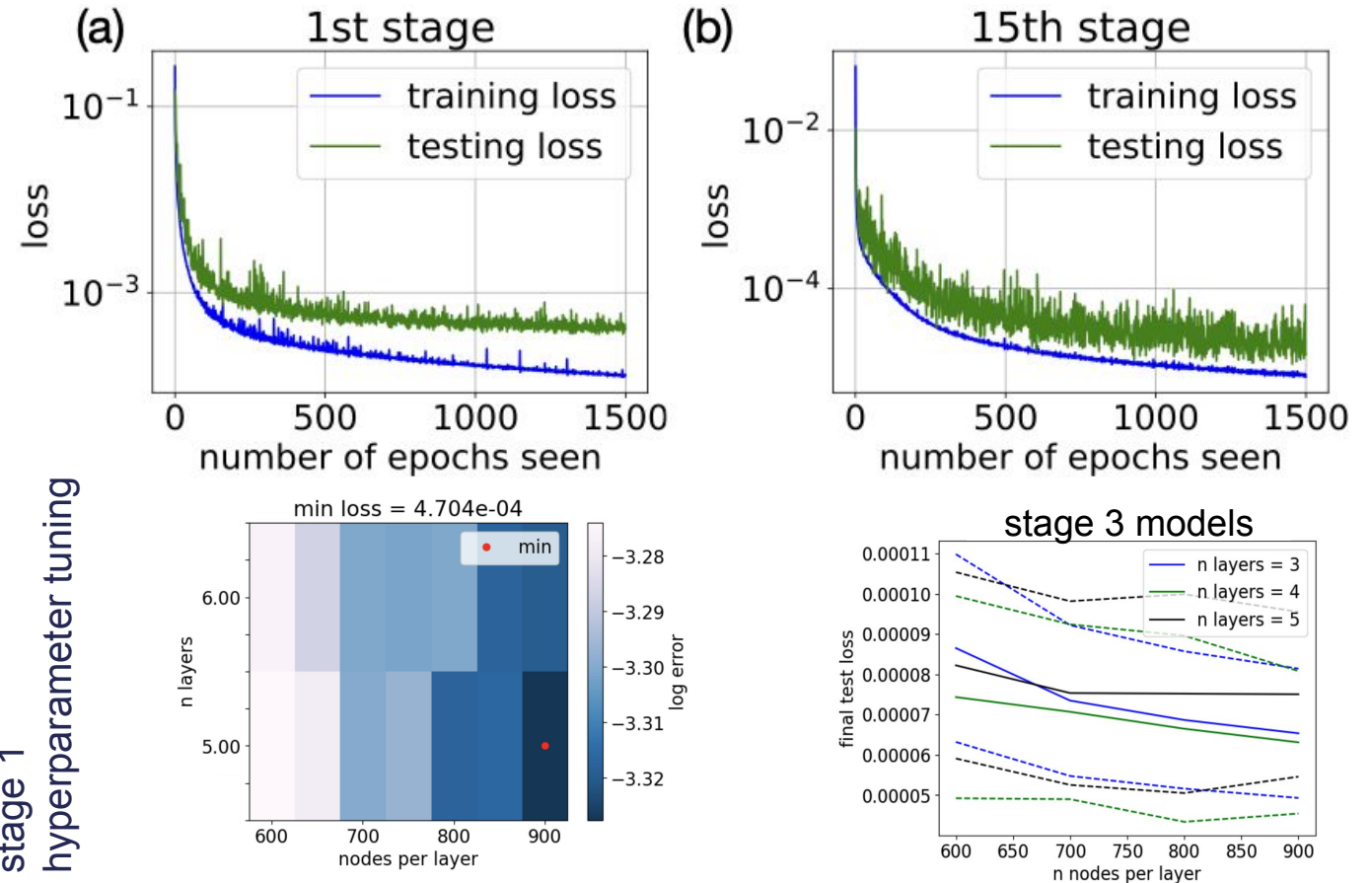


Multiple hidden layers

Number of hidden nodes

implemented in PyTorch

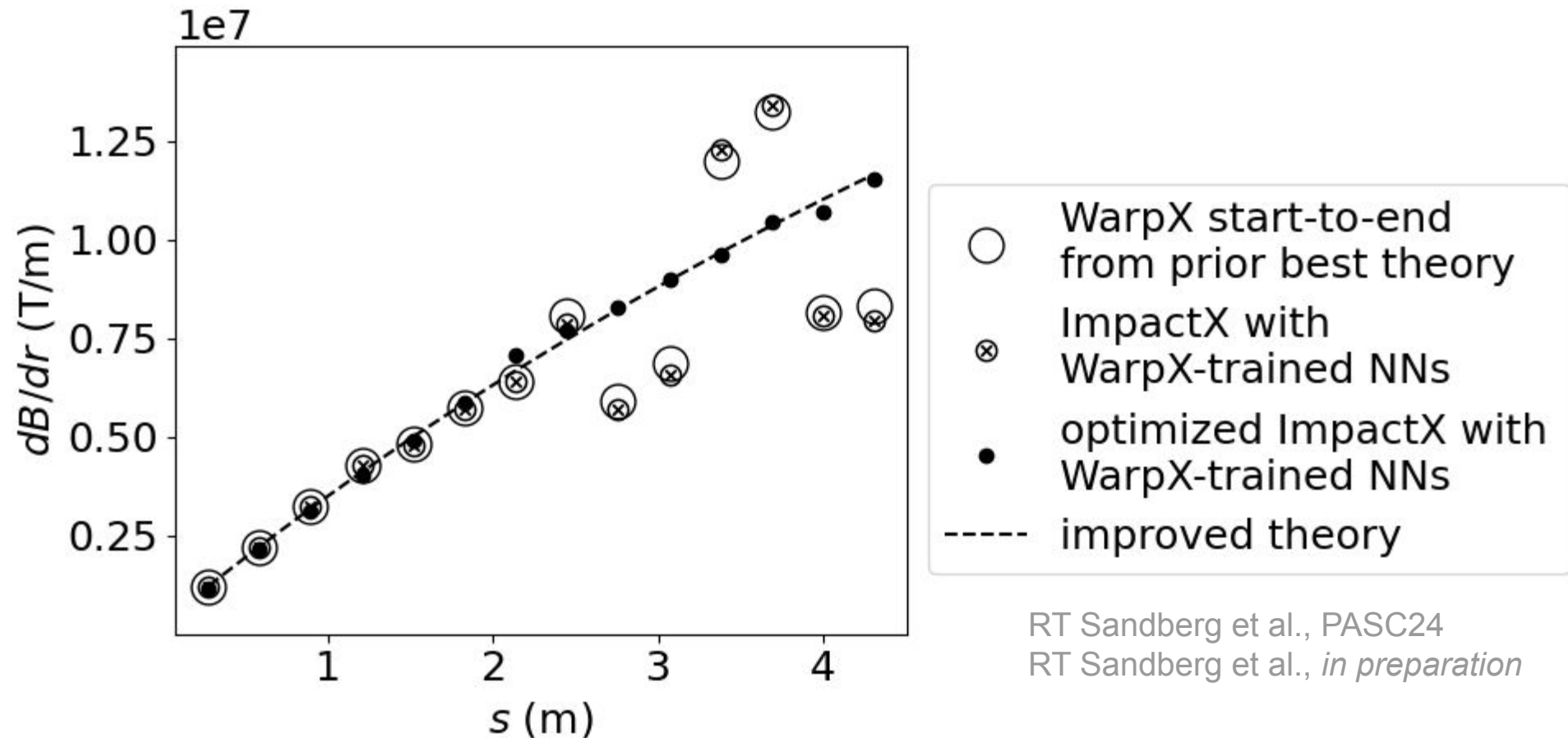
- PReLU
- MSE loss
- Adam optimizer



Stages 1-3: 5 hidden layers, 900 nodes per layer  
 Stages 4-15: 3 hidden layers, 700 nodes per layer



# Synthesized Simulation with Optimized Lenses Enabled Development of an Improved Analytical Theory



- before: **analytically**-motivated in situ tuning of lens strength
- now: **automated** tuning of **multiple** lens parameters
- enables: development & validation of **new theoretical** models



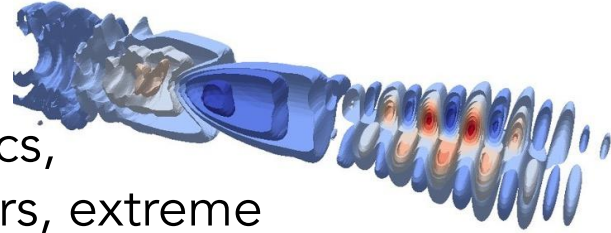


# WarpX is a Community Exascale Particle-in-Cell Code



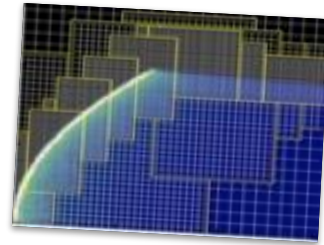
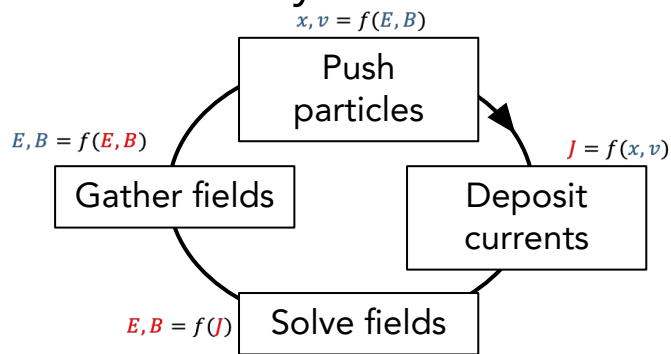
## Applications

laser-plasma physics,  
particle accelerators, extreme  
light sources, fusion devices & plasmas, ...



## Exascale Particle-in-Cell Code

- electromagnetic or electro/magnetostatic
- PIC-fluid hybrid
- time integration: explicit, implicit



International Contributors incl. private sector



## Award-Winning Code & Science



## Portable, Multi-Level Parallelization

- MPI: 3D MR decomposition
  - dynamic load balancing
- GPU: CUDA, HIP and SYCL
- CPU: OpenMP



## Scalable & Standardized

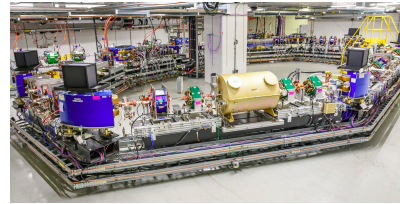
- Python APIs, openPMD data
- In situ processing
- Open community ecosystem



# ImpactX: We leverage WarpX Technology for RF Accelerator Modeling

## Beam-Dynamics in Linacs, Rings, Colliders

- intense beams, long-term dynamics
- HEP science: FNAL complex evolution, FCC-ee, FCC-hh, muon collider
- **s-based, electrostatic**
  - relative to a reference particle
  - elements: symplectic maps

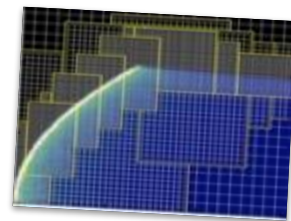


## Advanced Numerics

symplectic, based on IMPACT-Z, space charge, soon: radiative effects (CSR & ISR)

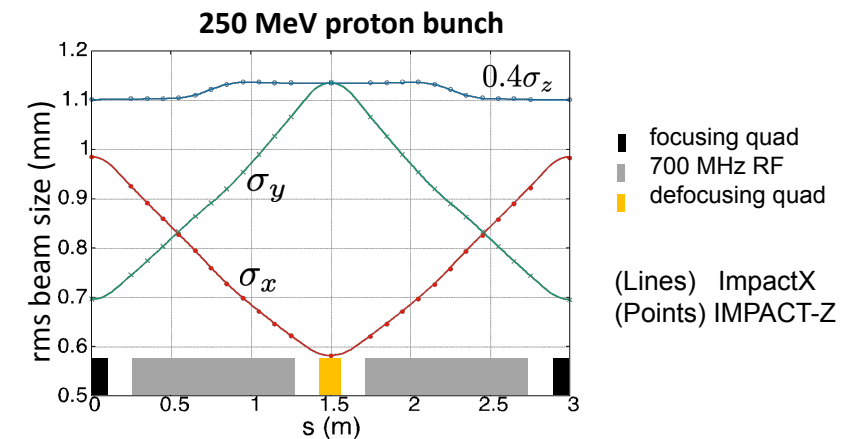
## Triple Acceleration Approach

- GPU support
- Adaptive Mesh Refinement
- AI/ML & Data Driven Models



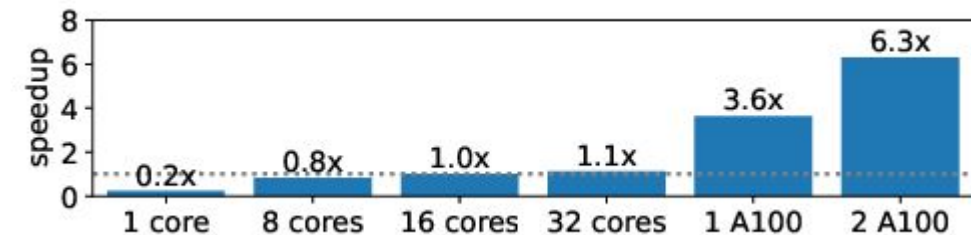
## Benchmarks & Validations

- 86 continuously run benchmarks
- code-to-code comparisons



## Performance

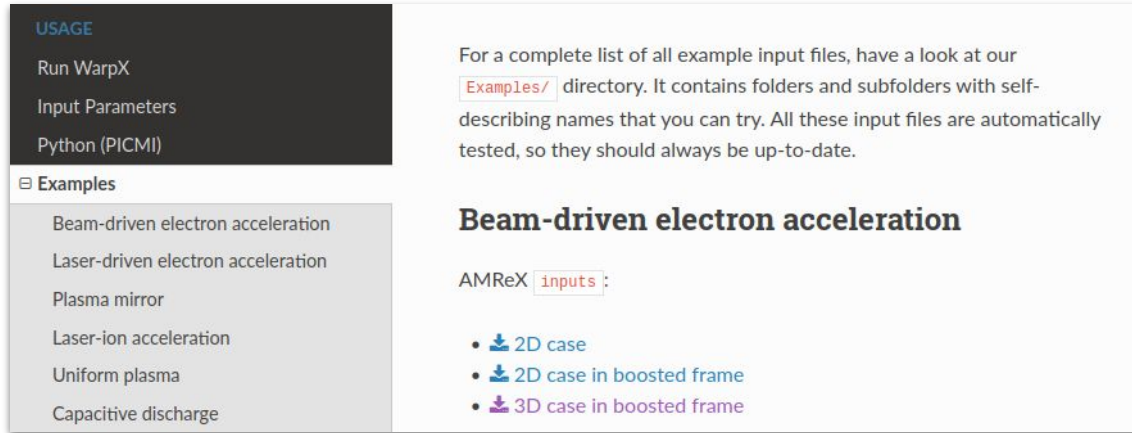
- order-of-magnitude perf.  $\nearrow$  from GPUs



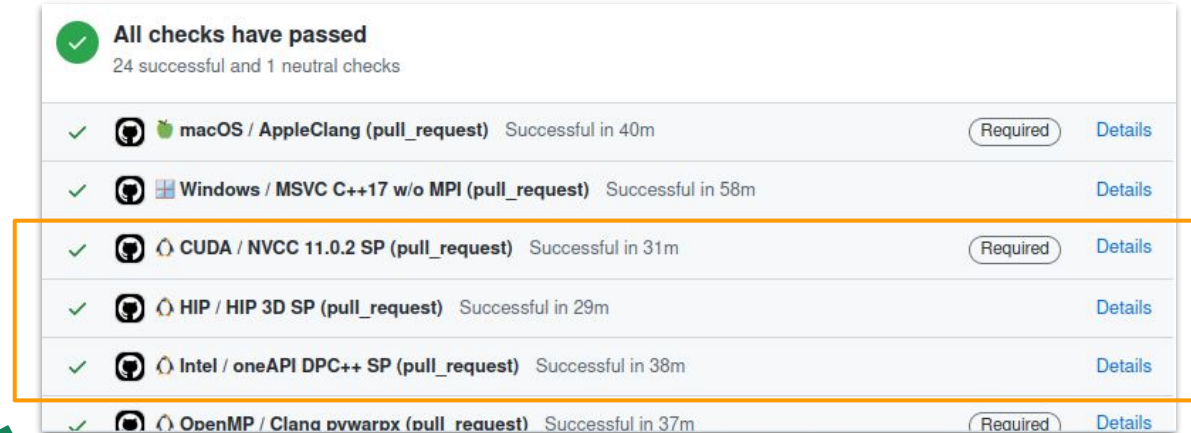


Online Documentation:  
[warpx|hipace|impactx.readthedocs.io](https://warpx.readthedocs.io)

Open-Source Development & Benchmarks:  
[github.com/ECP-WarpX](https://github.com/ECP-WarpX)



The screenshot shows the documentation page for WarpX. On the left, there is a sidebar with 'USAGE' (Run WarpX, Input Parameters, Python (PICMI)) and 'Examples' (Beam-driven electron acceleration, Laser-driven electron acceleration, Plasma mirror, Laser-ion acceleration, Uniform plasma, Capacitive discharge). The main content area has a heading 'Beam-driven electron acceleration' and lists 'AMReX inputs' with links to '2D case', '2D case in boosted frame', and '3D case in boosted frame'.



The screenshot shows a GitHub Actions workflow summary. At the top, it says 'All checks have passed' with '24 successful and 1 neutral checks'. Below are several job entries, each with a green checkmark, a platform icon, and a status: 'macOS / AppleClang (pull\_request) Successful in 40m', 'Windows / MSVC C++17 w/o MPI (pull\_request) Successful in 58m', 'CUDA / NVCC 11.0.2 SP (pull\_request) Successful in 31m', 'HIP / HIP 3D SP (pull\_request) Successful in 29m', 'Intel / oneAPI DPC++ SP (pull\_request) Successful in 38m', and 'OpenMP / Clang on warpX (pull\_request) Successful in 37m'. A green arrow points from the bottom of this screenshot towards the benchmark text below.

**230 physics benchmarks** run on every code change of WarpX  
**34 physics benchmarks** for ImpactX

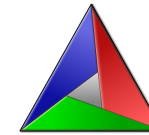
Rapid and easy installation on any platform:



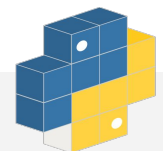
**conda install**  
**-c conda-forge warpX**



**spack install warpX**  
**spack install**  
**py-warpX**



**cmake -S . -B build**  
**cmake --build build --target**  
**install**



**python3 -m pip install .**



**brew tap ecp-warpX/warpX**  
**brew install warpX**

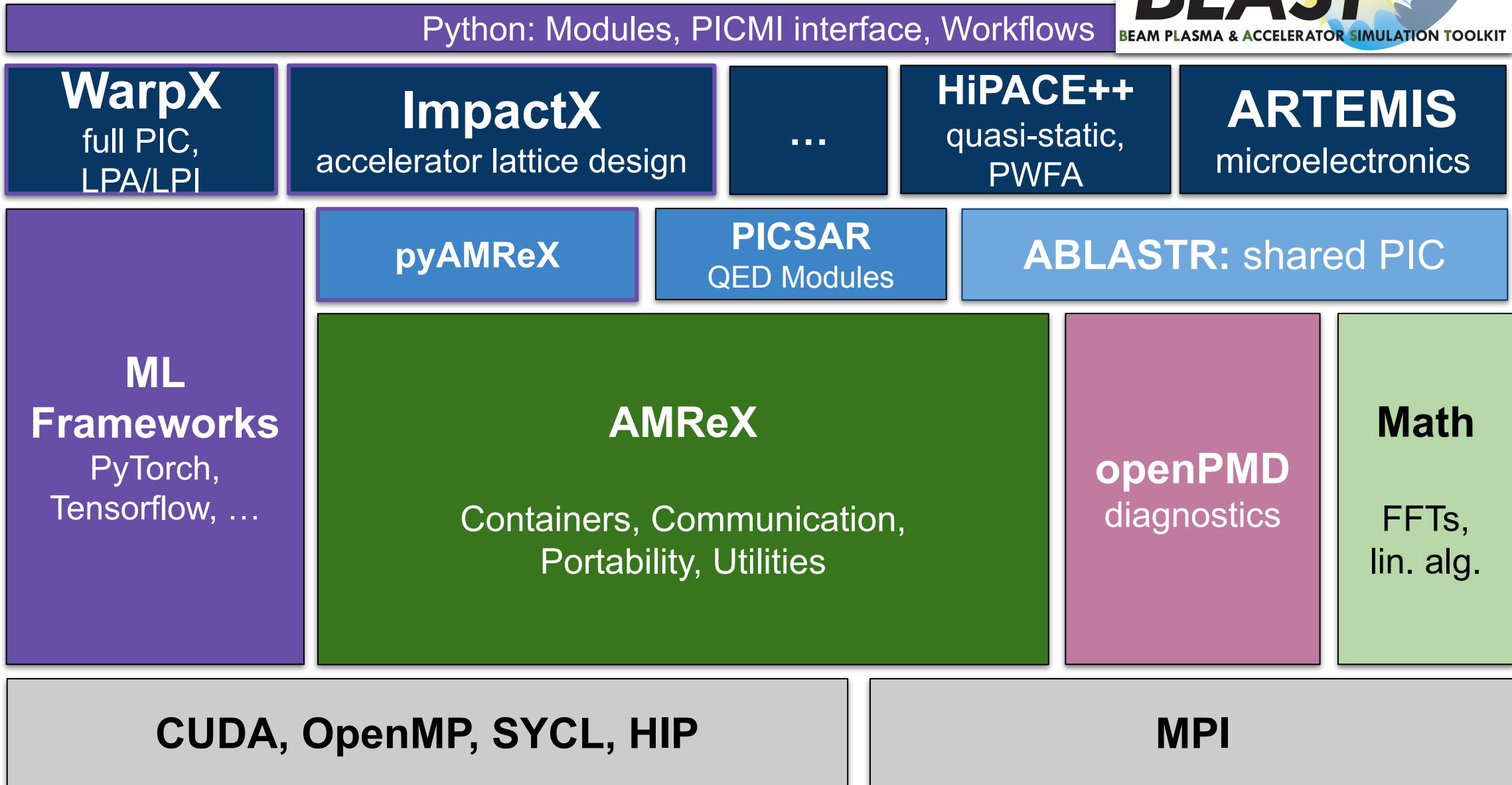


**module load warpX**  
**module load py-warpX**

# Modular Software Architecture



Desktop  
to  
HPC





# GPU-accelerated Synthesis: PIC Simulations & ML Models

## Demonstrated profits from GPUs

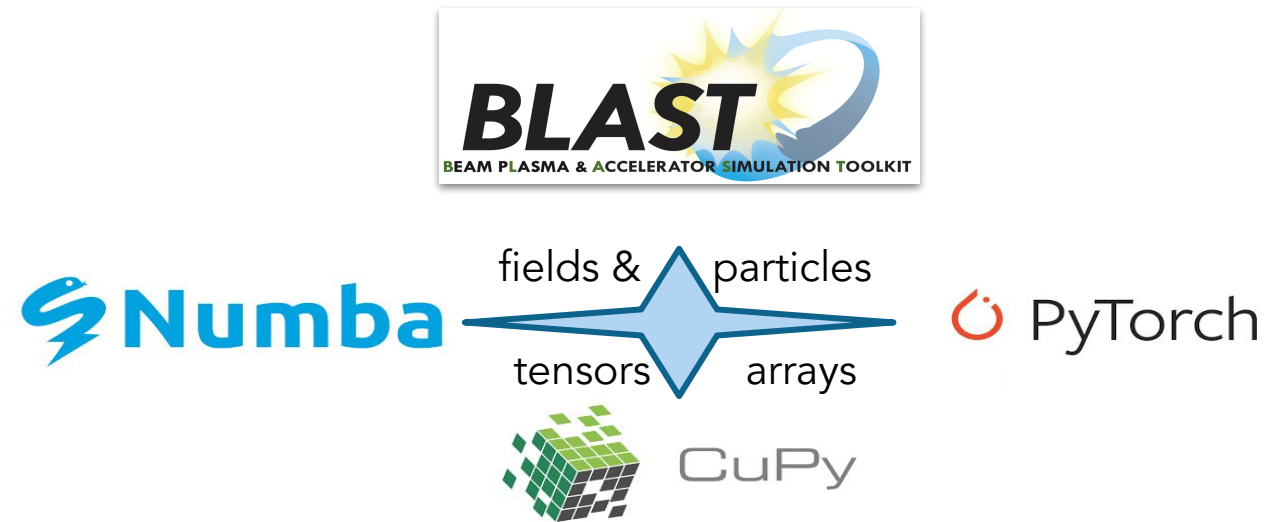
- *first-principle models:*  
Particle-in-Cell simulations
- *data-driven models:*  
neural network training & inference

## Implementation Goals

- **augment & accelerate *on-GPU* PIC simulations with *on-GPU* ML models**
- support many **HPC C++ compilers**
- **rapid ML model design "plug-and-play"**

## Approach

- Creation of a *compatible ecosystem*
- C++ core, Python control/glue
- pure C++ Python bindings: pybind11



W Jakob et al., pybind11 – Seamless operability between C++11 and Python (2017)

A Huebl et al., pyAMReX: GPU-Enabled, Zero-Copy AMReX Python Bindings including AI/ML (2023)

A Myers et al., AMReX and pyAMReX: Looking Beyond ECP, under review, arXiv:2403.12179 (2024)

# Augmenting & GPU-accelerating PIC Simulations & ML Models

## Embracing Emerging API Standards

- here: `__cuda_array_interface__`

```
{
  'shape': (1,),
  'typestr': '<f8',
  'descr': [('', '<f8')],
  'stream': 1,
  'version': 3,
  'strides': None,
  'data': (136661631501920, False)
}
```

- more general: DLPack

**Cross-Ecosystem, In Situ Coupling**  
Consortium for Python Data API  
Standards [data-apis.org](https://data-apis.org)



## Compute example

- data shared as views, stays on device
- enables in-memory updates

```
from impactx import ImpactXParIter
import torch

# loop over AMReX particle tiles
for pti in ImpactXParIter(...):
    soa = pti.soa().to_xp() # view
    x = soa.real["x"]      # alias
    # ... y, t, py, py, pt ...

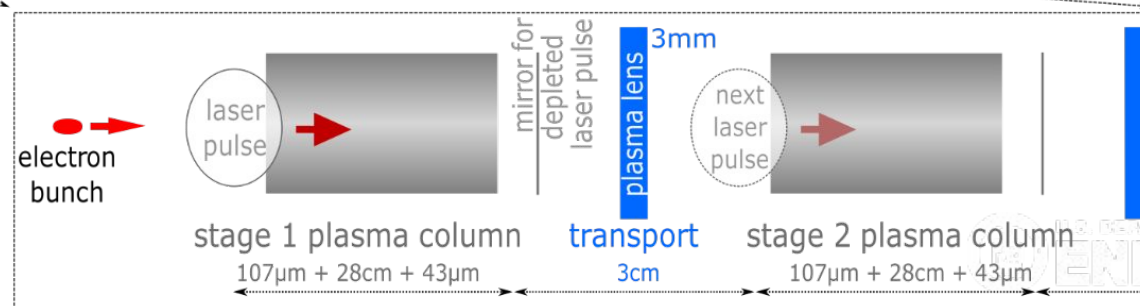
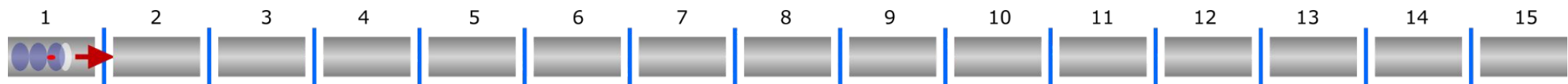
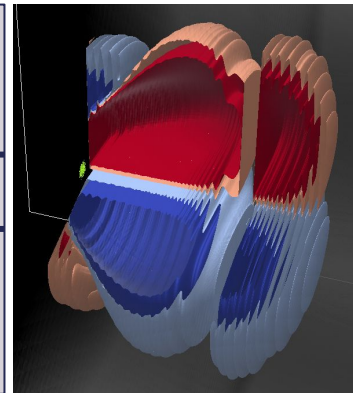
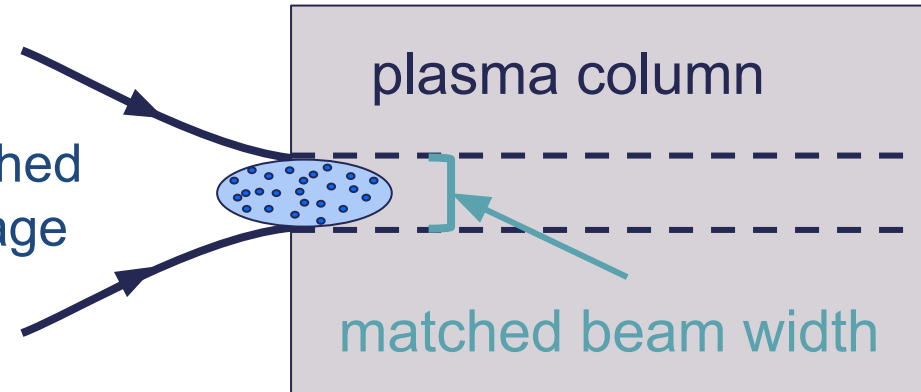
    data_arr = torch.tensor( # SoA -> Tensor AoS
        stack([x, y, t, px, py, pt], axis=1),
        device=device,
        dtype=torch.float64,
    )
    # ... normalize data_arr ...

    with torch.no_grad(): # apply NN in-memory
        surrogate_model(data_arr)
```



# A key challenge to particle accelerator design: suppress emittance growth

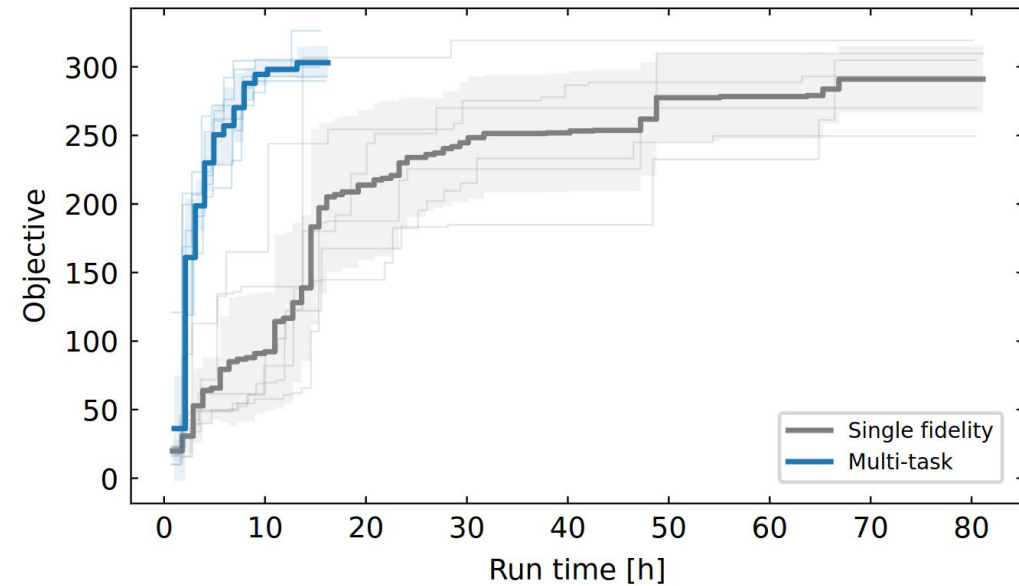
- Within plasma stage
  - emittance preserved if beam width is matched to *transverse focusing forces* in plasma stage
- Transport between stages
  - focus beam to matching conditions of subsequent stage
  - transport complex beams, e.g., with energy spread (chromaticity) without degrading beam quality (emittance, particle loss, energy spread) ...
- Demonstrator problem: control emittance growth through 15 stages



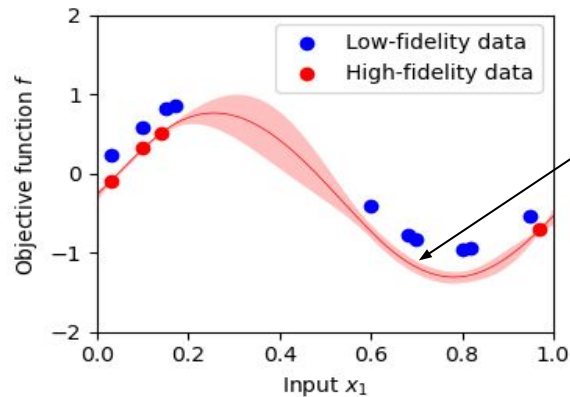
# ML-Guided Optimization: Automate Scans & Design Workflows

## Design Optimization:

- ML finds optima rapidly, e.g. *Gaussian Processes, Bayesian Optimization*
- **Multi-Fidelity** (think: multi-resolution): Learn trends from fast simulations and add precision with large costly sims

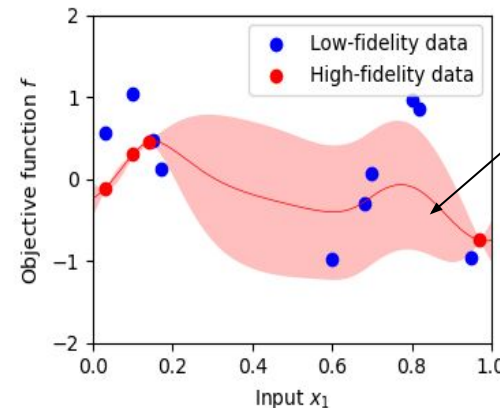


## Strongly-correlated case:



Low uncertainty, despite the absence of high-fidelity data

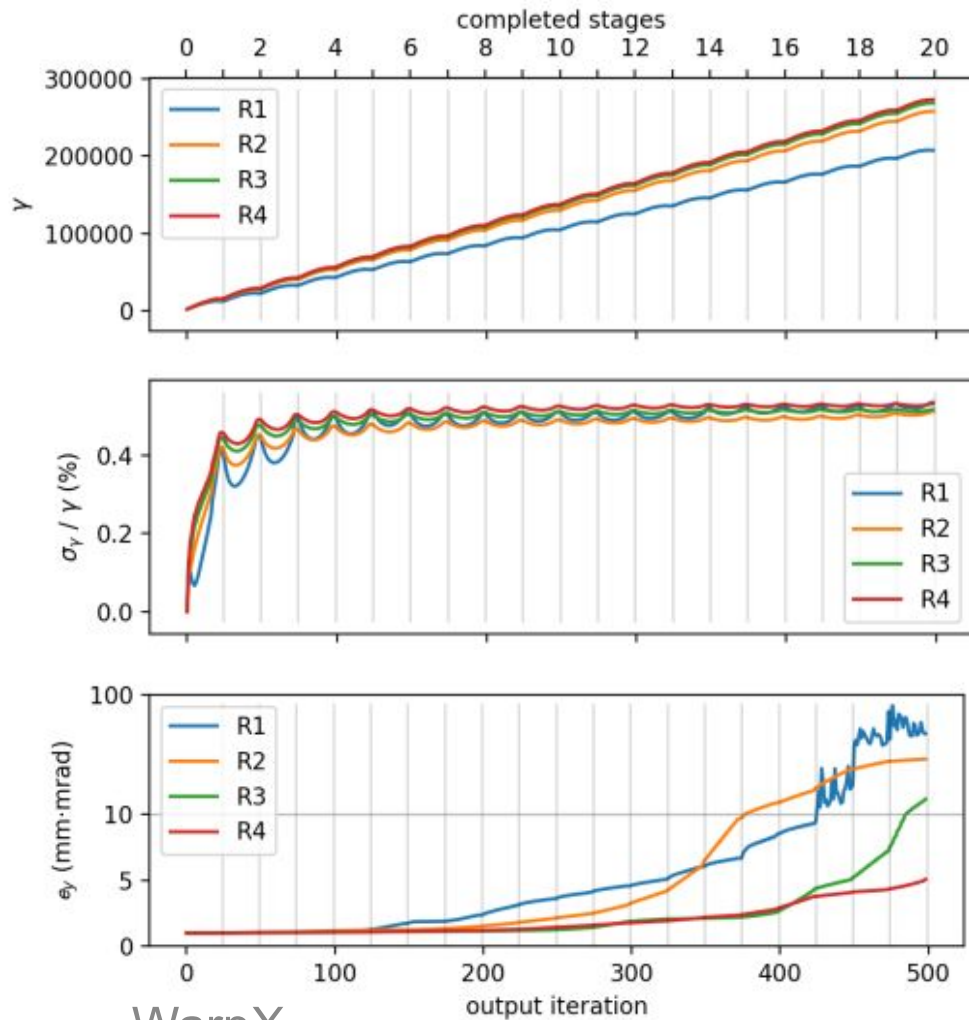
## Un-correlated case:



High uncertainty; low-fidelity data is ignored



# libEnsemble: Design Optimization with Reduced Models



WarpX

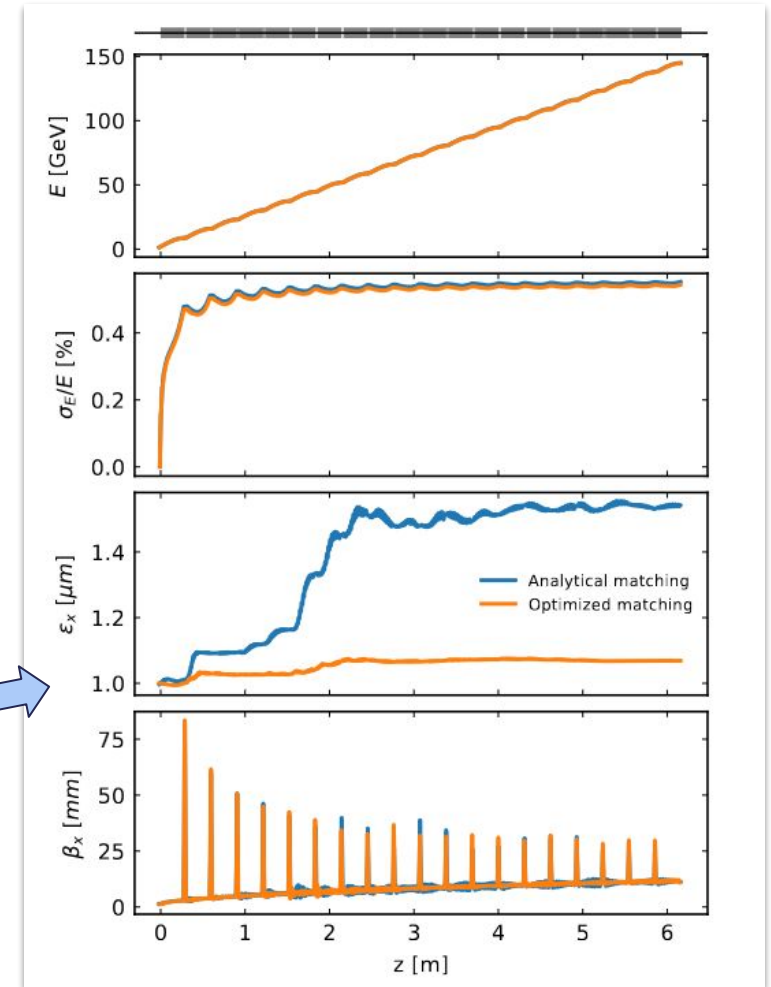
## Staged LPA

### Beam Emittance Preservation

3. converge 3D
4. optimize

1. optimize low-D, redu.

2. inform 3D



Wake-T, libEnsemble

# Functional examples of cleaning and training can be found on-line

[https://warpX.readthedocs.io/en/latest/usage/workflows/ml\\_dataset\\_training.html](https://warpX.readthedocs.io/en/latest/usage/workflows/ml_dataset_training.html)

- USAGE
  - Run WarpX
  - Examples
  - Parameters: Python (PICMI)
  - Parameters: Inputs File
- Workflows
  - Extend a Simulation with Python
  - Domain Decomposition
  - Visualizing a distribution mapping
  - Debugging the code
  - Run LibEnsemble on WarpX
  - Plot timestep duration
  - Predicting the Number of Guard Cells for PSATD Simulations
  - Archiving
- Training a Surrogate Model from WarpX Data
  - Data Cleaning
  - Create Normalized Dataset
  - Neural Network Structure
  - Train and Save Neural Network
  - Evaluate
- FAQ
- DATA ANALYSIS
  - Output formats
  - yt-project
  - openPMD-viewer
- Read the Docs v: latest

[https://warpX.readthedocs.io/en/latest/usage/workflows/python\\_extend.html](https://warpX.readthedocs.io/en/latest/usage/workflows/python_extend.html)

Home / Workflows / Training a Surrogate Model from WarpX Data

[Edit on GitHub](#)

## Training a Surrogate Model from WarpX Data

Suppose we have a WarpX simulation that we wish to replace with a neural network surrogate model. For example, a simulation determined by the following input script

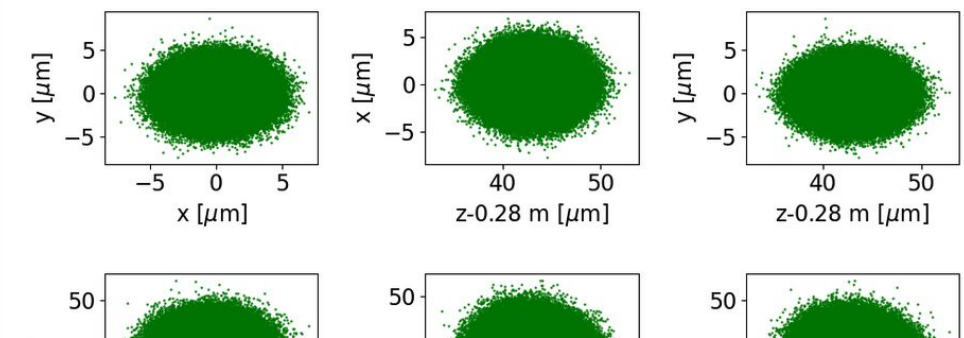
**Python Input for Training Simulation**

In this section we walk through a workflow for data processing and model training. This workflow was developed and first presented in Sandberg *et al.* [1], Sandberg *et al.* [2].

This assumes you have an up-to-date environment with PyTorch and openPMD.

### Data Cleaning

It is important to inspect the data for artifacts to check that input/output data make sense. If we plot the final phase space for beams 1-8, the particle data is distributed in a single blob, as shown by Fig. 18 for beam 1. This is as we expect and what is optimal for training neural networks.





# Functional examples of surrogates in ImpactX can also be found on-line

[https://impactx.readthedocs.io/en/latest/usage/examples/pytorch\\_surrogate\\_model/README.html](https://impactx.readthedocs.io/en/latest/usage/examples/pytorch_surrogate_model/README.html)

The screenshot shows a web browser displaying the ImpactX documentation page for the '9 Stage Laser-Plasma Accelerator Surrogate'. The page title is '9 Stage Laser-Plasma Accelerator Surrogate' and it includes a 'Read the Docs' button and a 'v: latest' dropdown menu. The main content area features a section titled '9 Stage Laser-Plasma Accelerator Surrogate' with a brief description: 'This example models an electron beam accelerated through nine stages of laser-plasma accelerators with ideal plasma lenses providing the focusing between stages. For more details, see:'. Below this, there are two bullet points listing references: 'Sandberg R T, Lehe R, Mitchell C E, Garten M, Qiang J, Vay J-L and Huebl A. Synthesizing Particle-in-Cell Simulations Through Learning and GPU Computing for Hybrid Particle Accelerator Beamlines. Proc. of Platform for Advanced Scientific Computing (PASC'24), submitted, 2024.' and 'Sandberg R T, Lehe R, Mitchell C E, Garten M, Qiang J, Vay J-L and Huebl A. Hybrid Beamline Element ML-Training for Surrogates in the ImpactX Beam-Dynamics Code. 14th International Particle Accelerator Conference (IPAC'23), WEPA101, 2023. DOI:10.18429/JACoW-IPAC2023-WEPA101'. At the bottom, there is a schematic diagram showing a sequence of 9 stages, with a red arrow pointing to the first stage.

[Examples](#) / [9 Stage Laser-Plasma Accelerator Surrogate](#) [Edit on GitHub](#)

## 9 Stage Laser-Plasma Accelerator Surrogate

This example models an electron beam accelerated through nine stages of laser-plasma accelerators with ideal plasma lenses providing the focusing between stages. For more details, see:

- Sandberg R T, Lehe R, Mitchell C E, Garten M, Qiang J, Vay J-L and Huebl A. **Synthesizing Particle-in-Cell Simulations Through Learning and GPU Computing for Hybrid Particle Accelerator Beamlines.** Proc. of Platform for Advanced Scientific Computing (PASC'24), *submitted*, 2024.
- Sandberg R T, Lehe R, Mitchell C E, Garten M, Qiang J, Vay J-L and Huebl A. **Hybrid Beamline Element ML-Training for Surrogates in the ImpactX Beam-Dynamics Code.** 14th International Particle Accelerator Conference (IPAC'23), WEPA101, 2023. DOI:10.18429/JACoW-IPAC2023-WEPA101

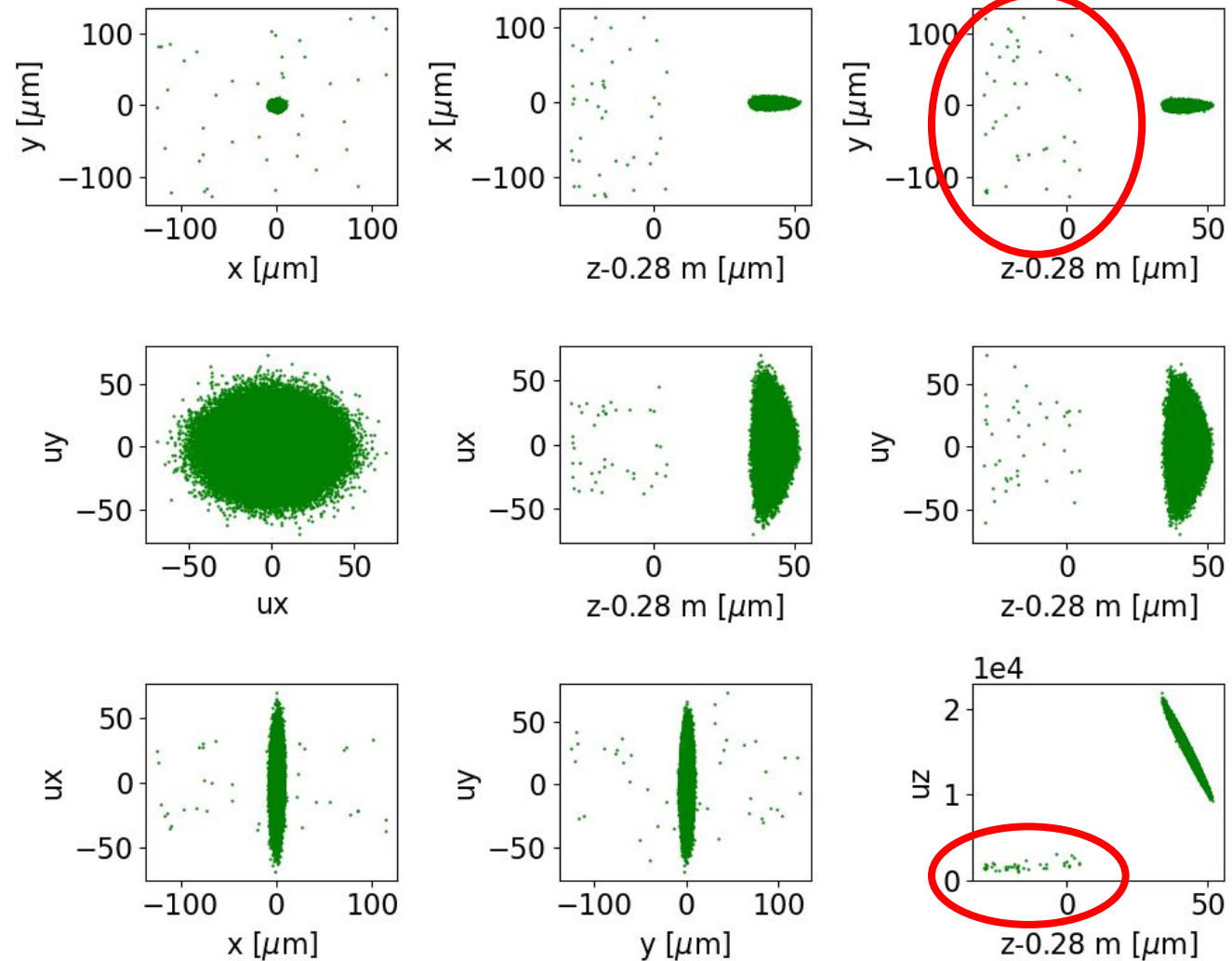
A schematic with more information can be seen in the figure below:

The schematic diagram shows a horizontal sequence of 9 stages, numbered 1 through 9. Each stage is represented by a grey rectangular block. Stage 1 is highlighted with a red arrow pointing to it from the left. Above each stage is a small blue circle, and a red arrow points from the first stage to the second stage, indicating the direction of the electron beam.

# Data preparation and cleaning

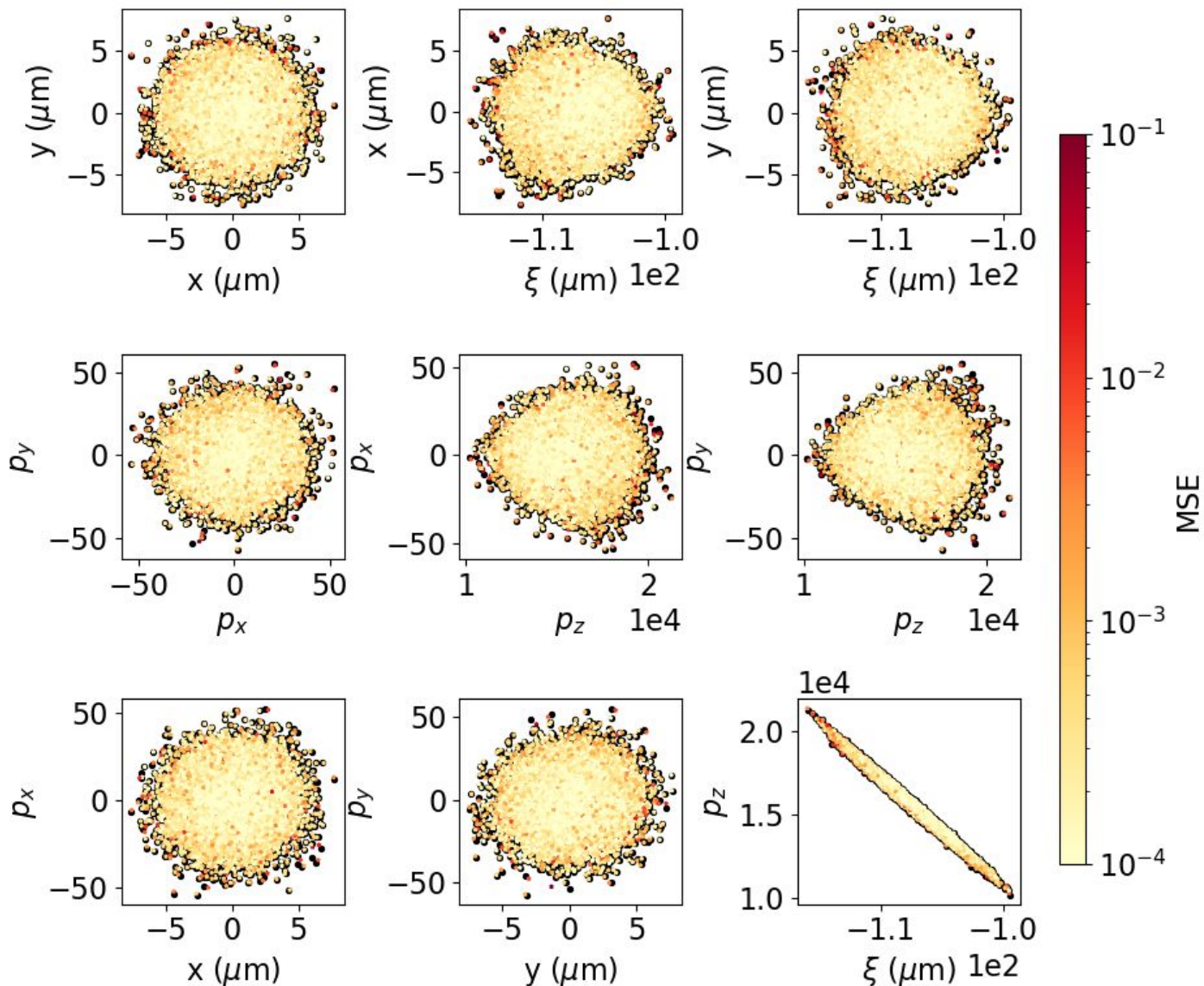
Beam at Stage 1 end

- Remove clear outliers
- 70/30% train/test split
- Normalize by training bunch mea





# Model learns training data very well



Stage 1

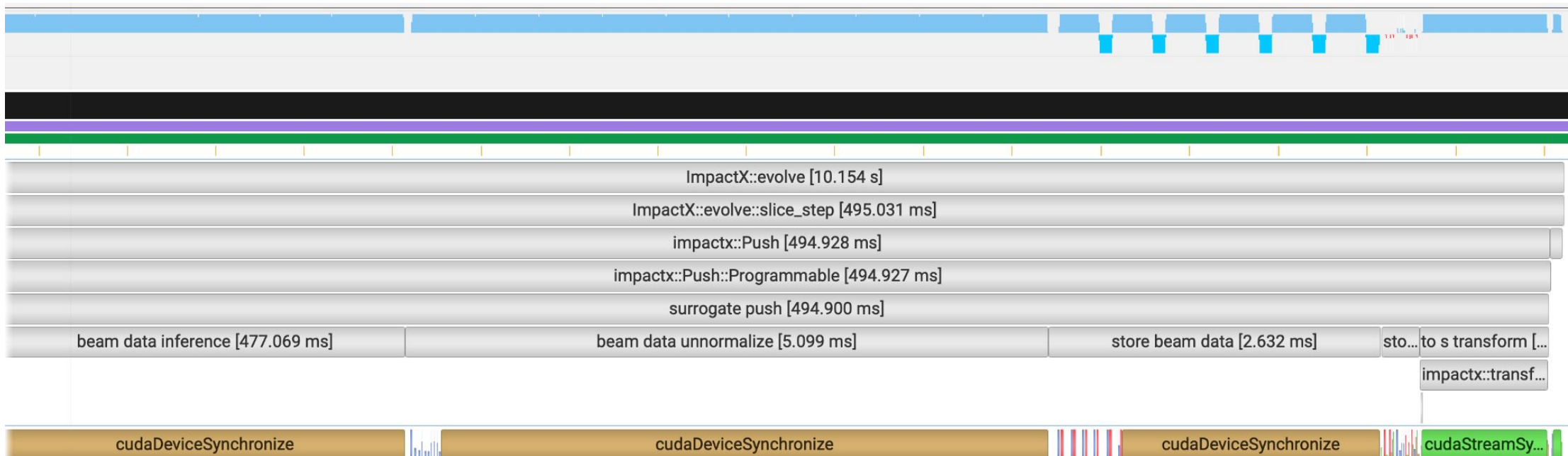
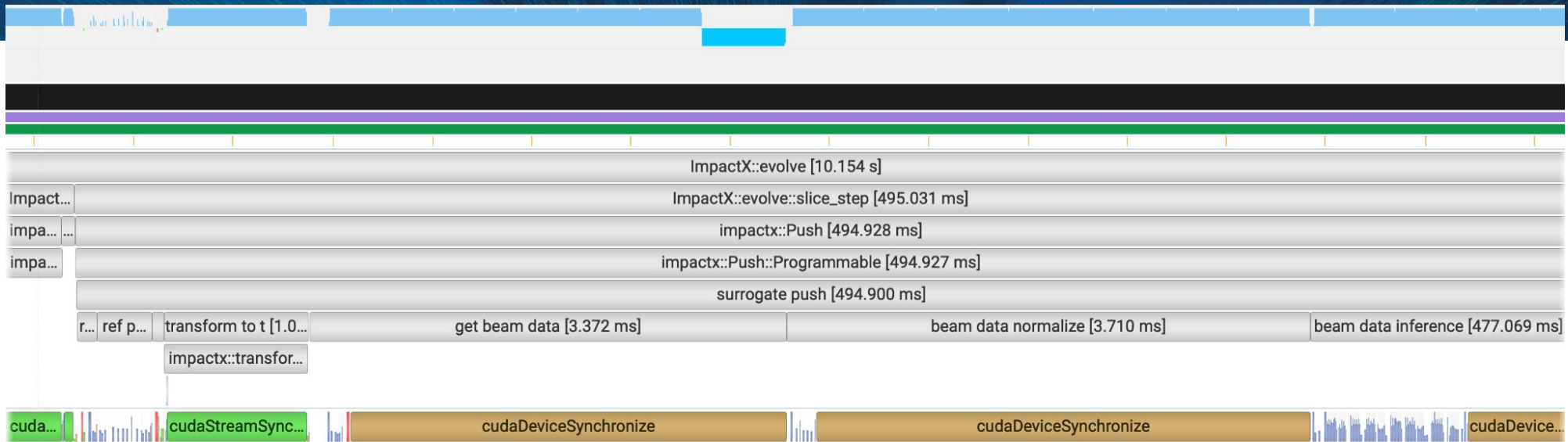
Black dots: training beam

Colored dots: predicted beam

Training data: 1M particles / beam

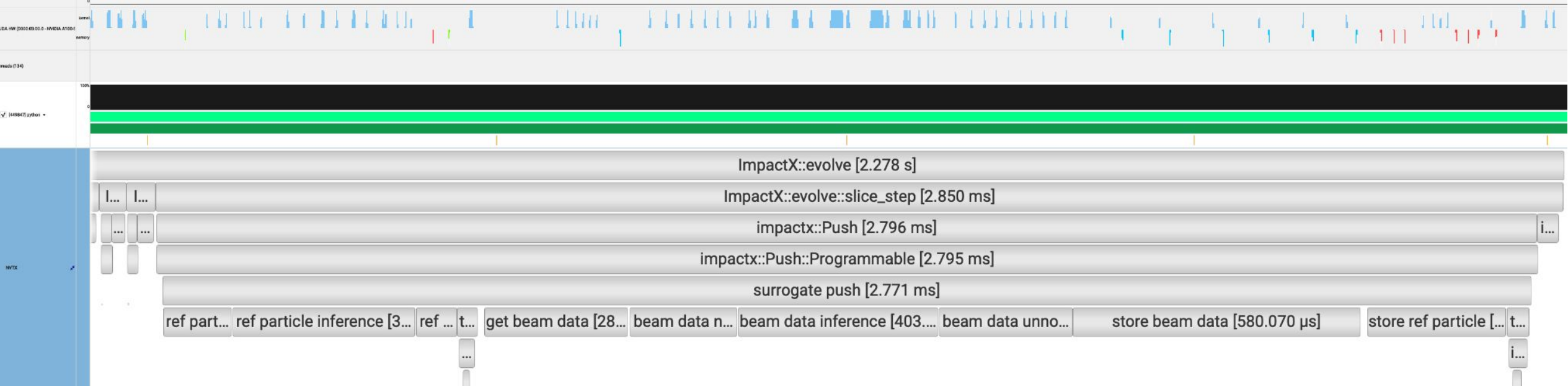
Training time: 2-2.2 hrs on 1 GPU

# 10 million particles



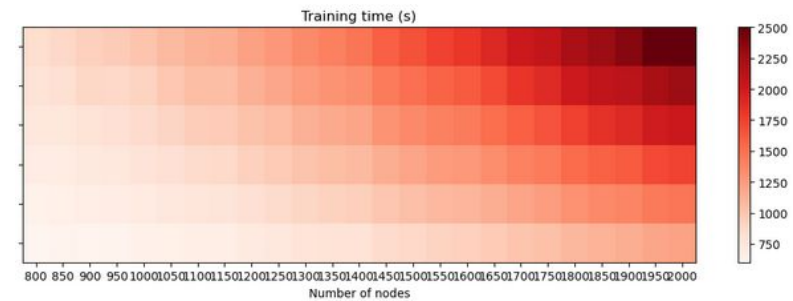
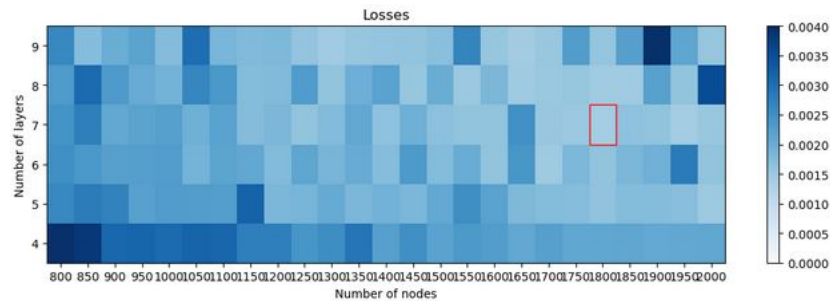


# 1000 particles



## What was accomplished

- Incorporated dropout layers
- Manage NN training with Ray Tune
- Used torch.compile (but it didn't speed things up)
- Continue the learning rate scan
- Learn that Ray Tune is the tool we want
- **Speedup > 2x** & smaller, less-noisy final loss-function with tf32 & PReLU

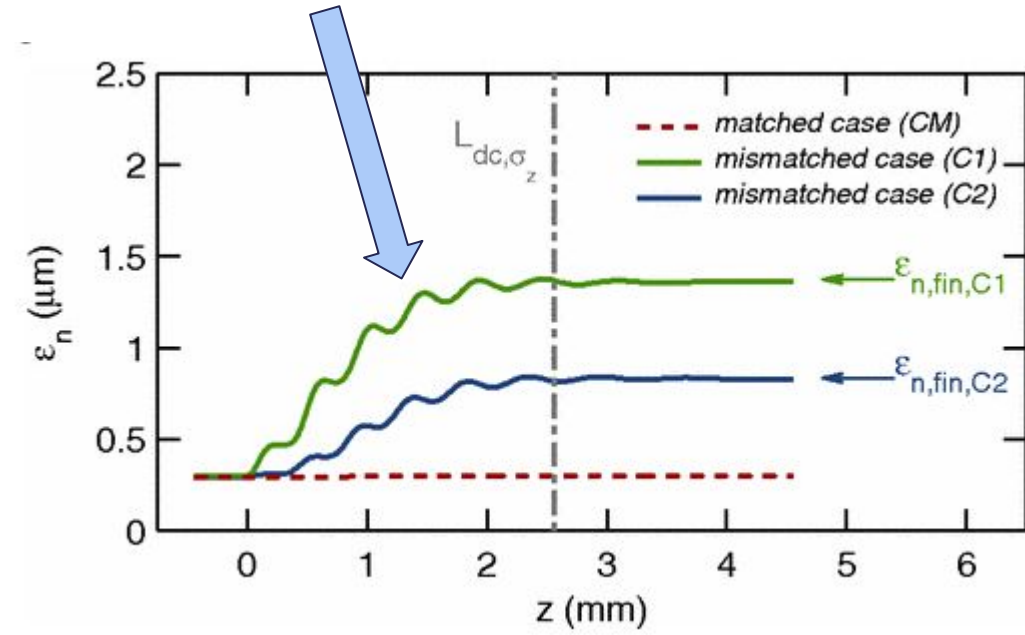
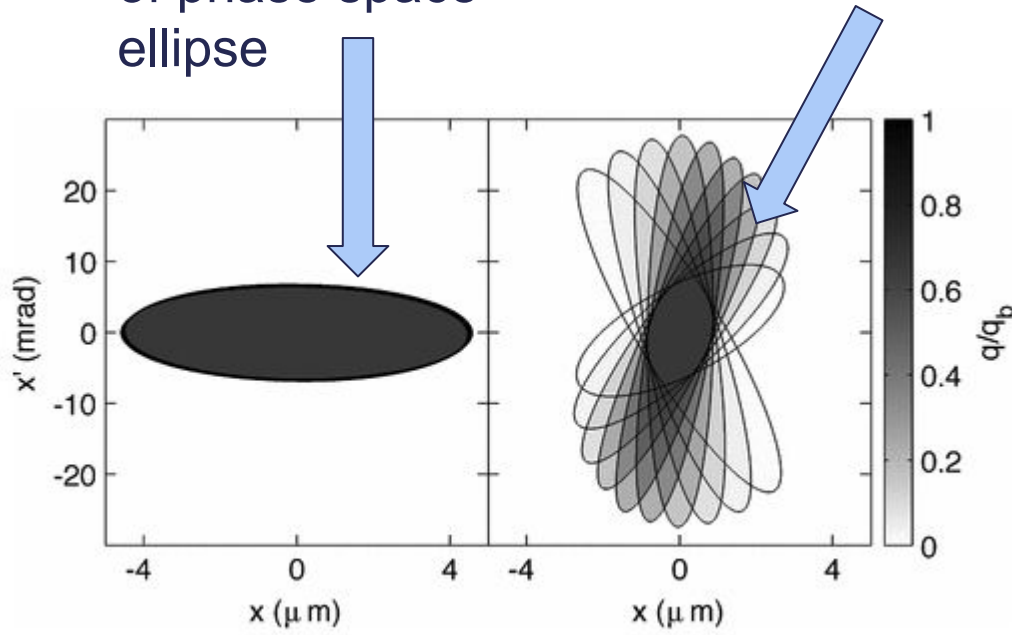






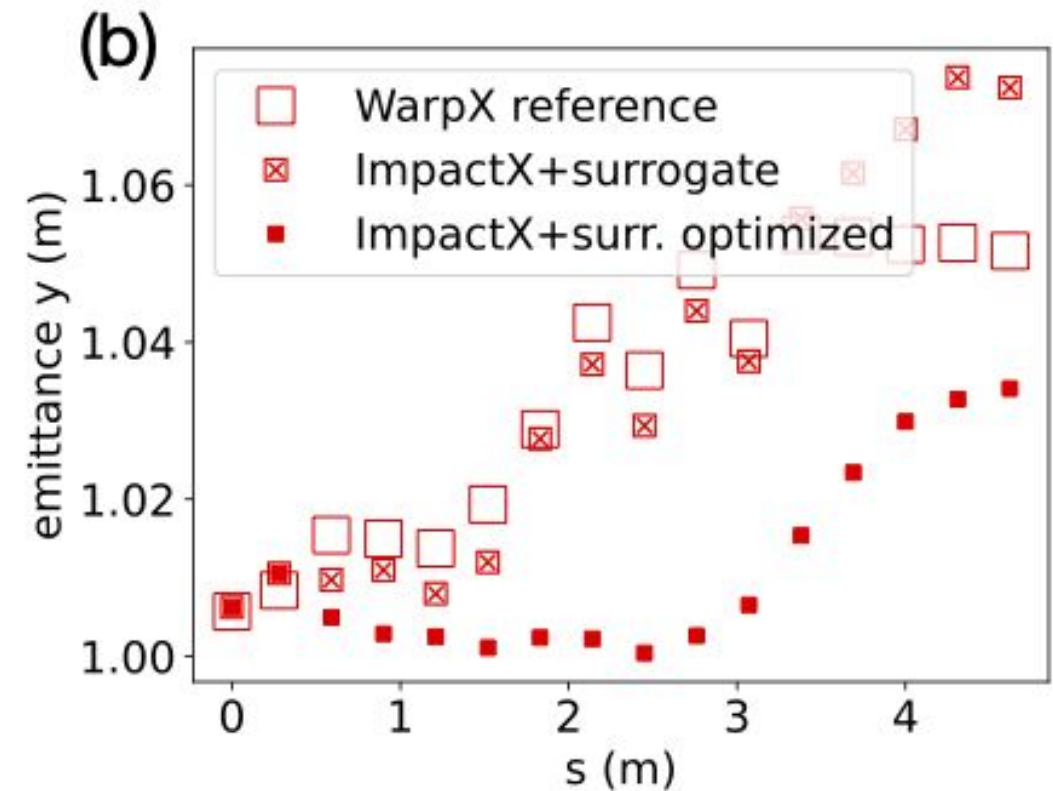
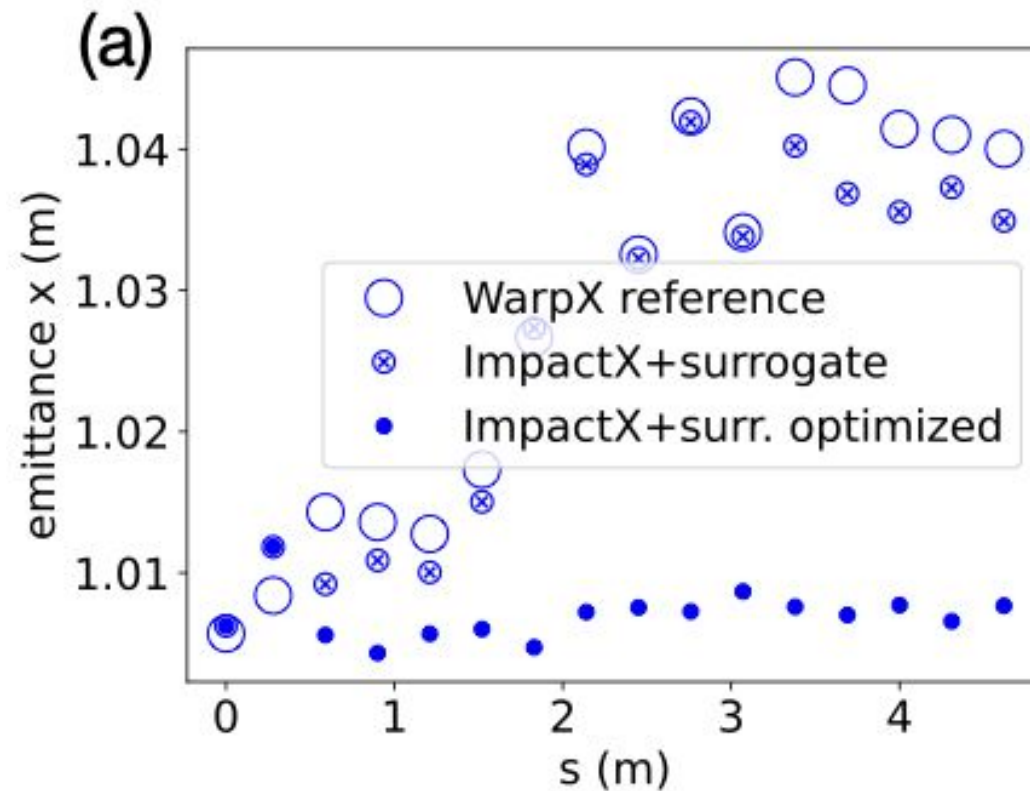
Emittance: area of phase space ellipse

Emittance increases if beam is not matched and "smeared out"



## Example usage: Find lens strengths that minimize x emittance

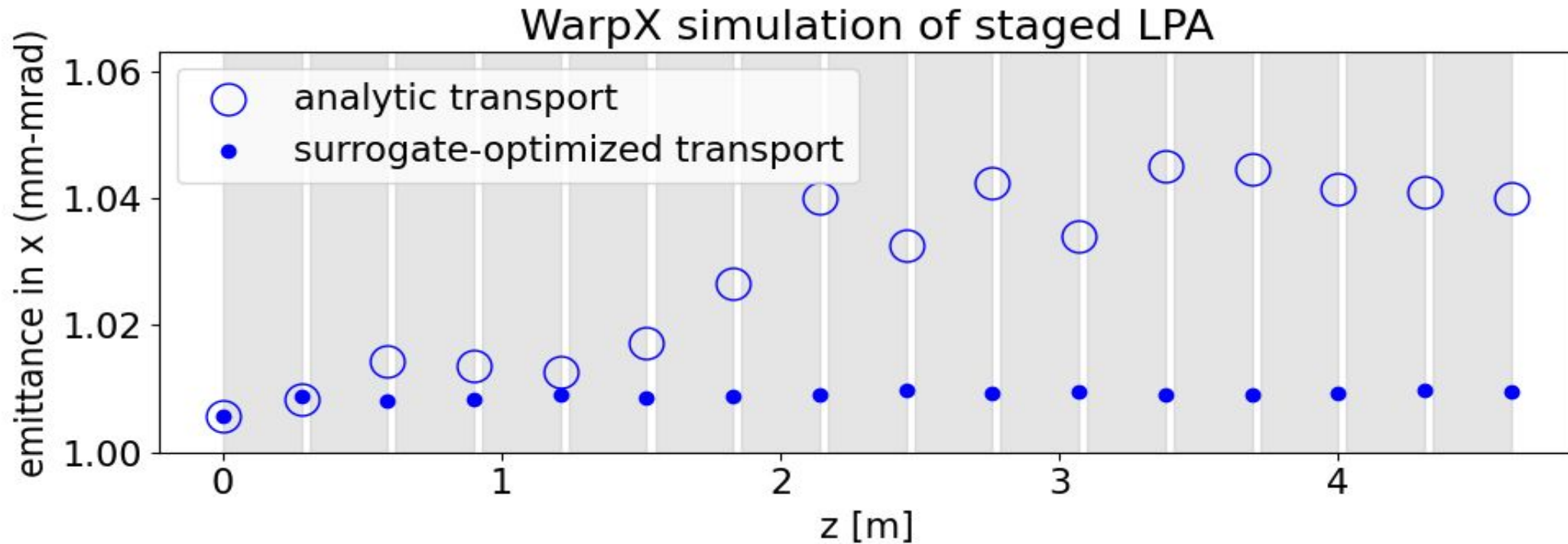
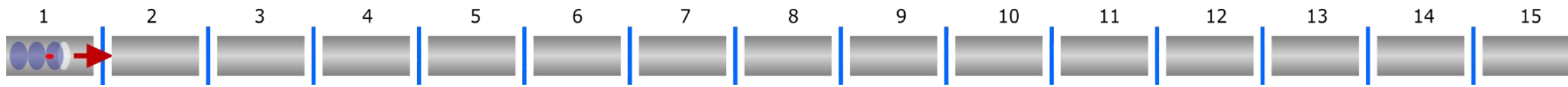
- Stage-by-stage optimization of transport parameters
- Emittance in x is kept constant, emittance growth in y reduced



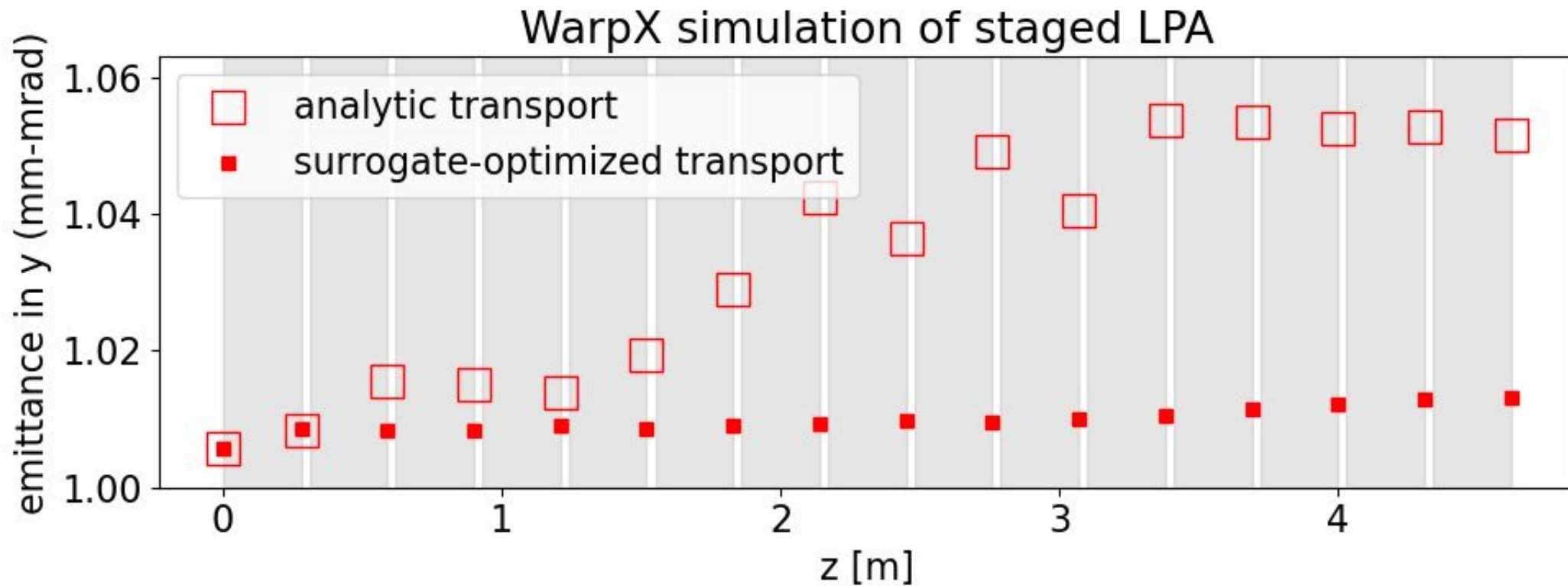
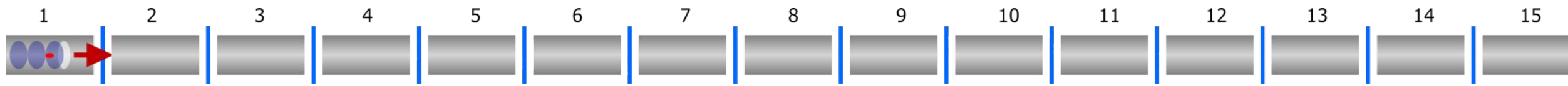
scipy.optimize.minimize with Nelder-Mead (simplex) optimization



# Close the loop: use ImpactX+WarpX-optimized transport to improve transport in WarpX

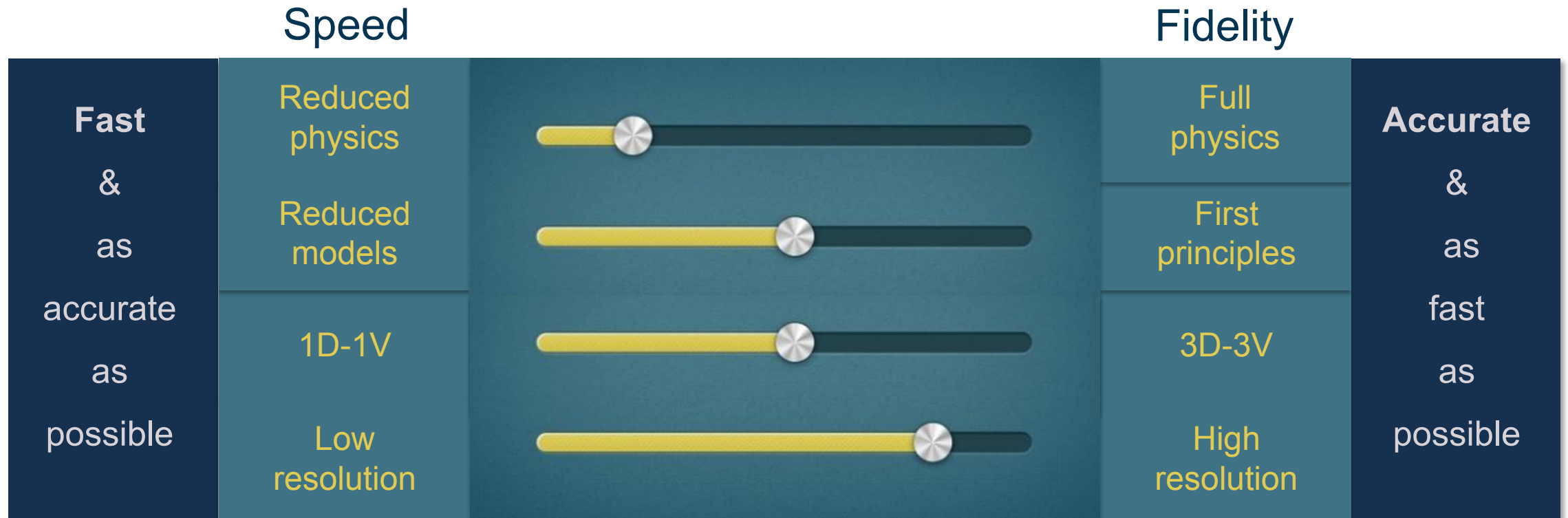


# Close the loop: use ImpactX+WarpX-optimized transport to improve transport in WarpX





# Toward an integrated ecosystem of codes with on-the-fly tunability



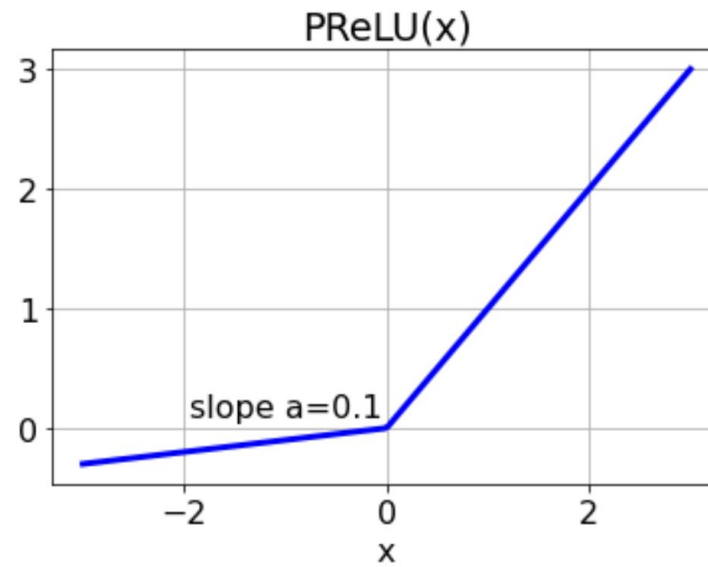
e.g., optimization & operations

e.g., exploration, training data

## Ecosystem of codes

- share models & data between codes
- works best when **standardized**

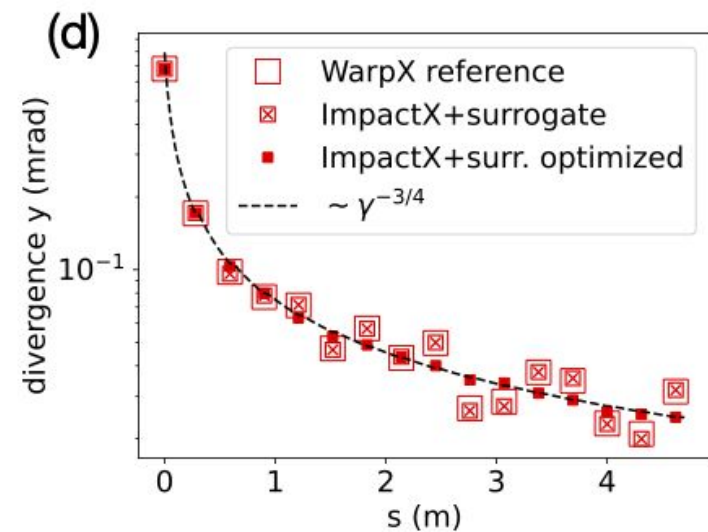
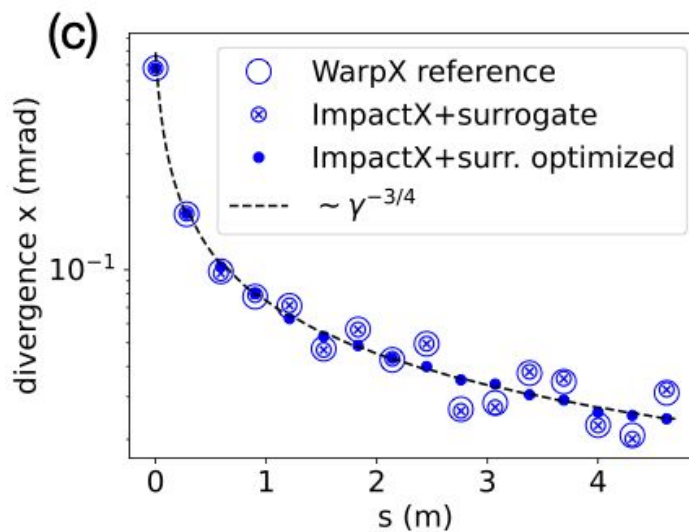
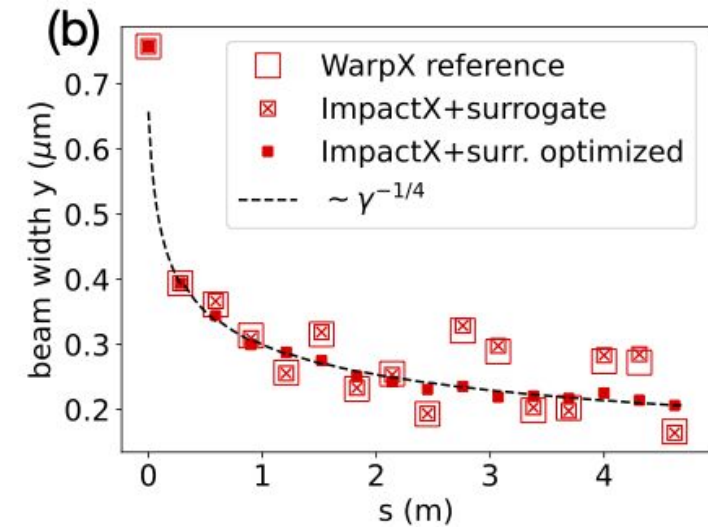
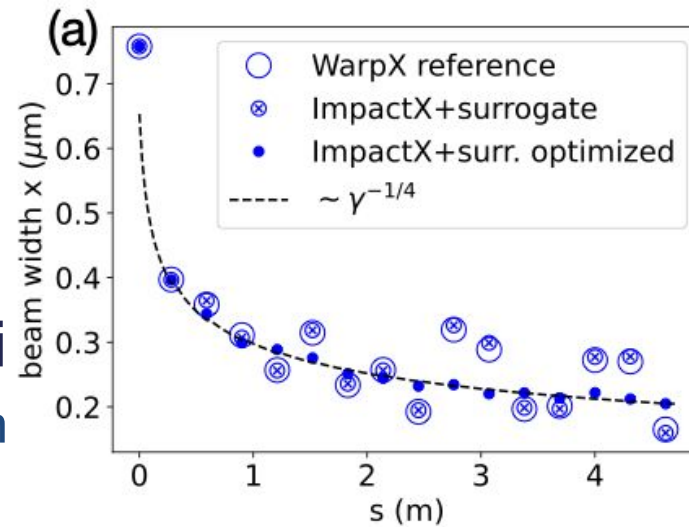
# PReLU activation function

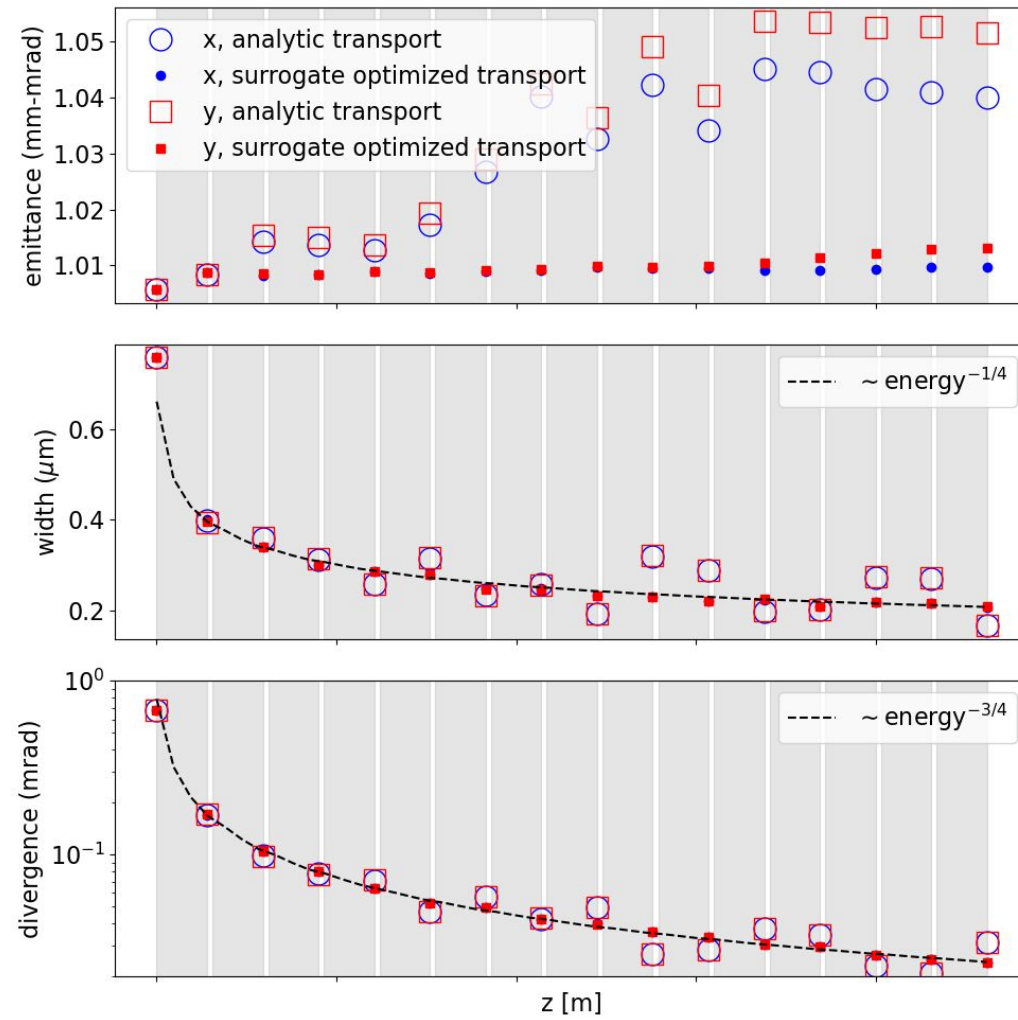




# Optimal lens strengths improve beam match

- Beam is better matched
  - Optimized beam width, divergence fit theory
- Recall: objective is emittance  $\epsilon$ 
  - Optimizer “learns” to find better  $m$   
In order to improve emittance

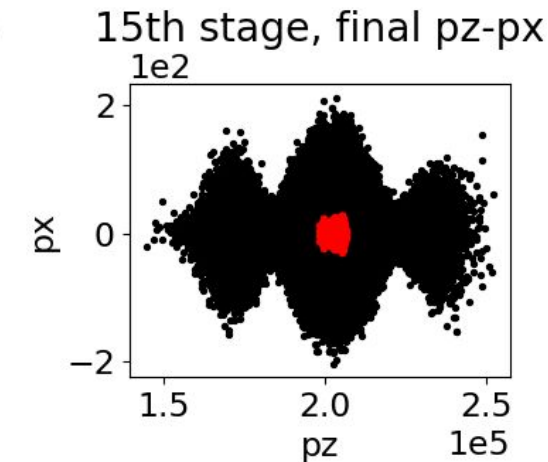
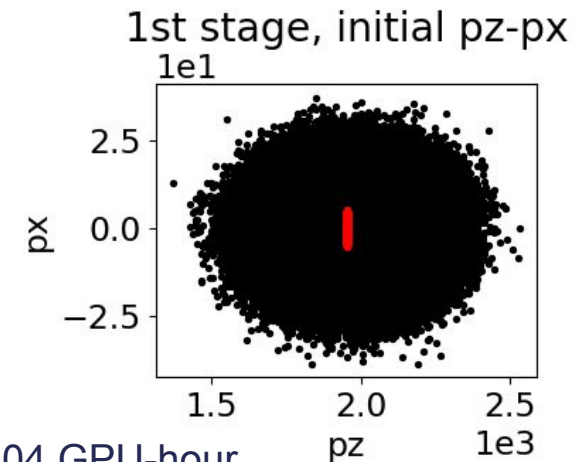
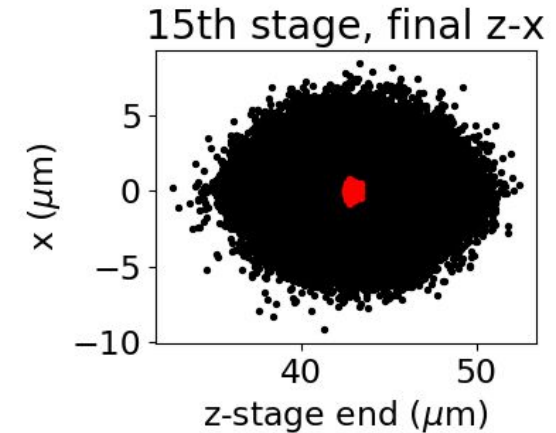
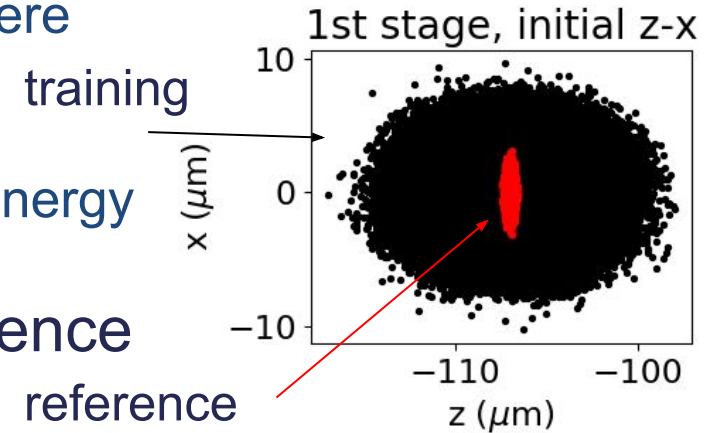






# A high-fidelity WarpX simulation provides training data

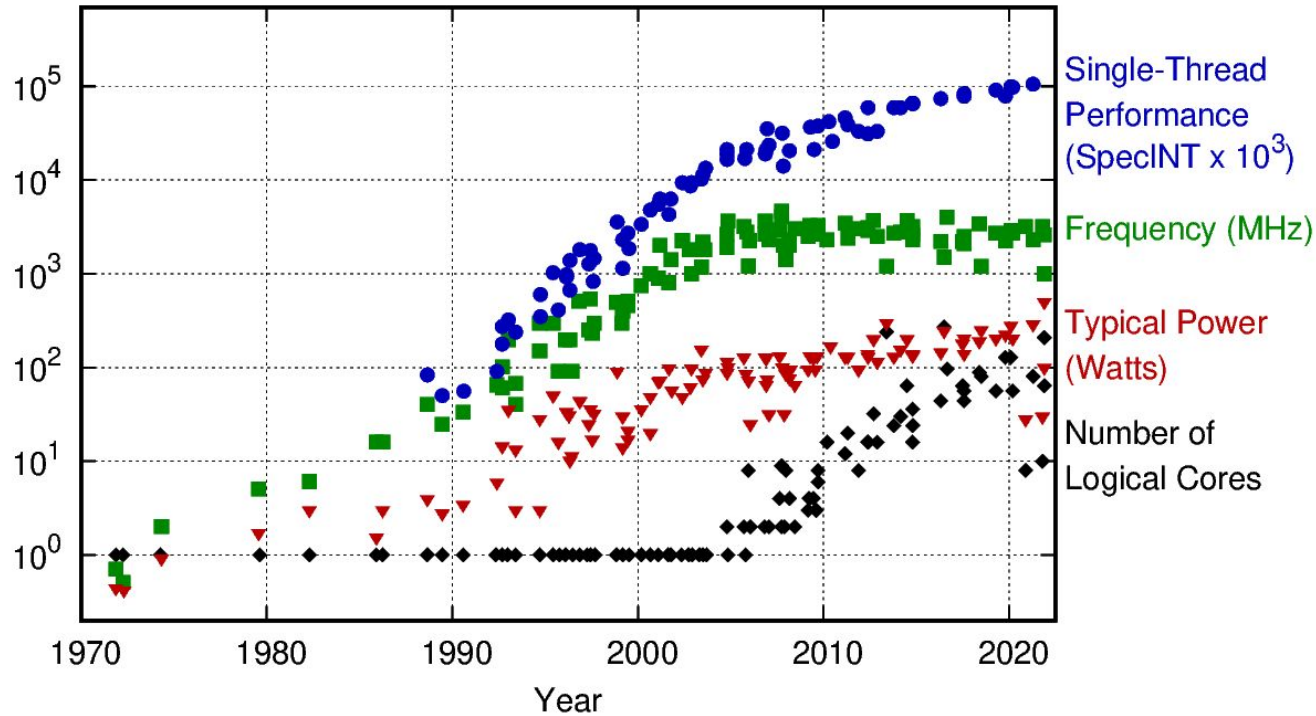
- Single simulation / single stage
  - Low space charge – beams do not interfere
- 1 electron beam / stage
  - identical except in energy
  - beam  $i$  mean energy = expected mean energy reference beam at stage  $i$
- Training beam  $\sim 3\text{-}5\text{x}$  larger than reference
  - Larger region of phase space
    - More general
    - Harder to learn
  - Smaller region of phase space
    - Could miss region of interest
    - Less general
    - More efficient training



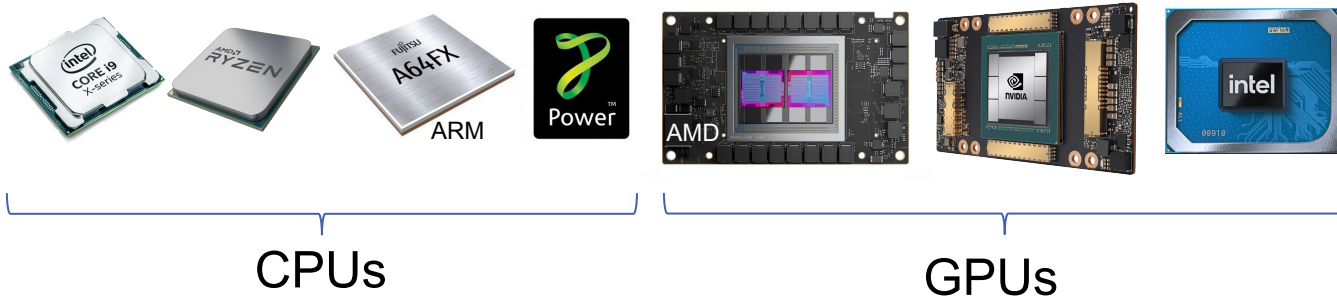
Training simulation: 404 GPU-hour  
WarpX simulation on Perlmutter

# Power-Limits Seeded a Cambrian Explosion of Compute Architectures

50 Years of Microprocessor Trend Data



Original data up to the year 2010 collected and plotted by M. Horowitz, F. Labonte, O. Shacham, K. Olukotun, L. Hammond, and C. Batten  
 New plot and data collected for 2010-2021 by K. Rupp



## Top 500



Frontier (USA): 1.2 EFlops  
 • AMD GPUs



Fugaku (Japan): 0.44 EFlops  
 • Fujitsu ARM CPUs



Lumi (Finland): 0.3 EFlops  
 • AMD GPUs



Leonardo (Italy): 0.24 EFlops  
 • Nvidia GPUs



Summit (USA): 0.15 EFlops  
 • Nvidia GPUs

## Upcoming

(under acceptance testing)



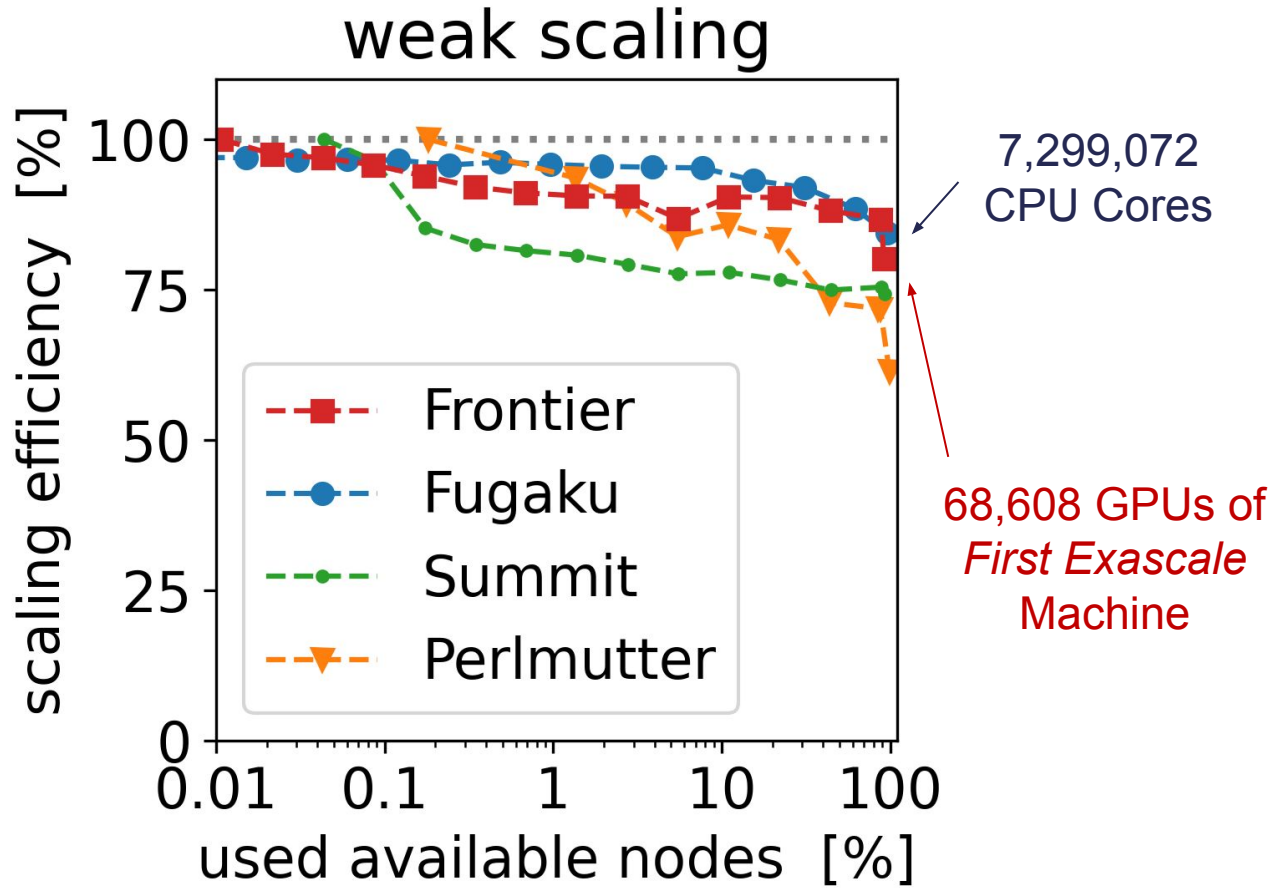
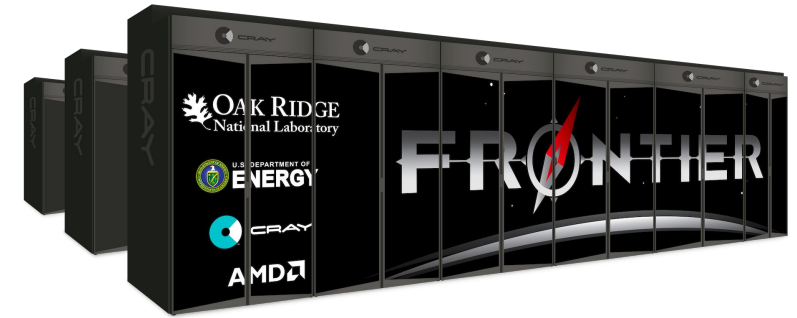
Aurora (USA): ~2 EFlops  
 • Intel GPUs



# WarpX is now 500x More Performant than its Pre-Exascale Baseline

April-July 2022: WarpX on world's largest HPCs

L. Fedeli, A. Huebl et al., *Gordon Bell Prize Winner* in SC'22, 2022



Note: Perlmutter & Frontier in pre-acceptance at the time!

Figure-of-Merit: weighted updates / sec

Date	Code	Machine	$N_c$ /Node	Nodes	FOM
3/19	Warp	Cori	0.4e7	6 625	2.2e10
3/19	WarpX	Cori	0.4e7	6 625	1.0e11
6/19	WarpX	Summit	2.8e7	1 000	7.8e11
9/19	WarpX	Summit	2.3e7	2 560	6.8e11
1/20	WarpX	Summit	2.3e7	2 560	1.0e12
2/20	WarpX	Summit	2.5e7	4 263	1.2e12
6/20	WarpX	Summit	2.0e7	4 263	1.4e12
7/20	WarpX	Summit	2.0e8	4 263	2.5e12
3/21	WarpX	Summit	2.0e8	4 263	2.9e12
6/21	WarpX	Summit	2.0e8	4 263	2.7e12
7/21	WarpX	Perlmutter	2.7e8	960	1.1e12
12/21	WarpX	Summit	2.0e8	4 263	3.3e12
4/22	WarpX	Perlmutter	4.0e8	928	1.0e12
4/22	WarpX	Perlmutter†	4.0e8	928	1.4e12
4/22	WarpX	Summit	2.0e8	4 263	3.4e12
4/22	WarpX	Fugaku†	3.1e6	98 304	8.1e12
6/22	WarpX	Perlmutter	4.4e8	1 088	1.0e12
7/22	WarpX	Fugaku	3.1e6	98 304	2.2e12
7/22	WarpX	Fugaku†	3.1e6	152 064	9.3e12
7/22	WarpX	Frontier	8.1e8	8 576	1.1e13

