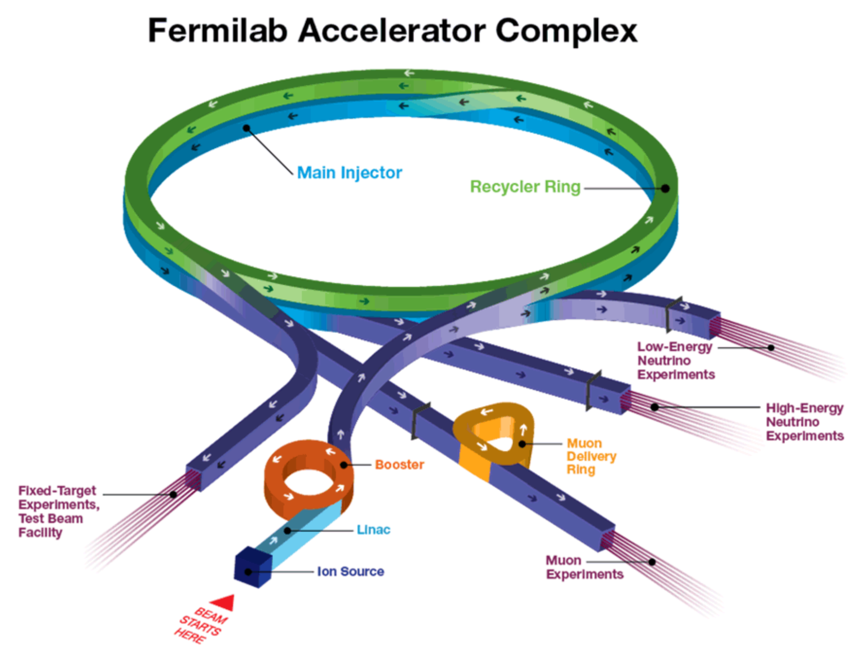
Muon Collider Physics

- Ian Low
- Argonne/Northwestern

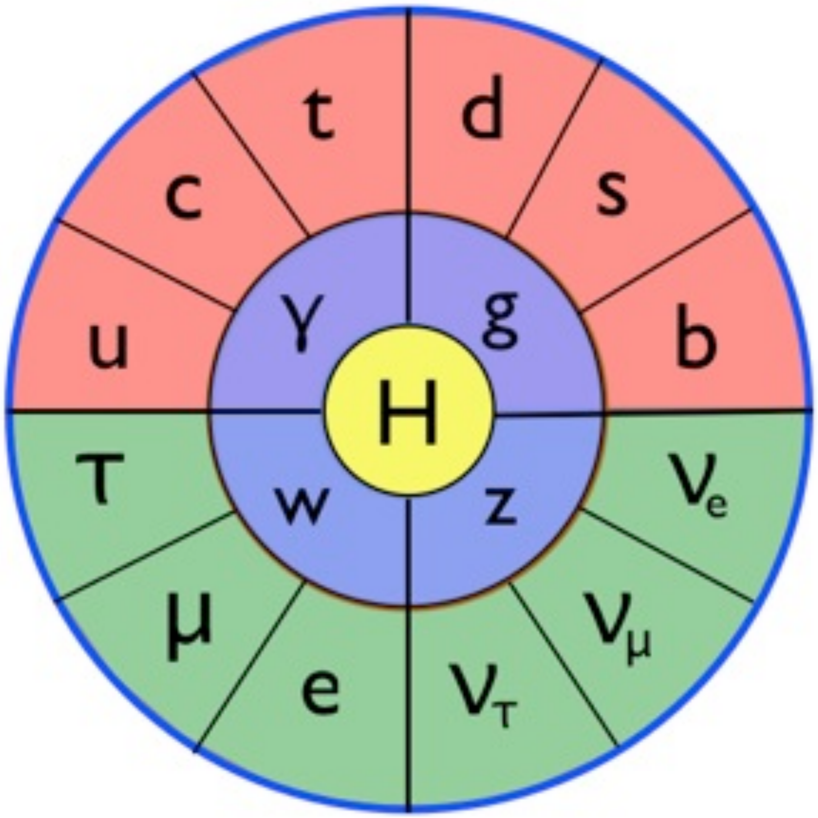
- June 14, 2023

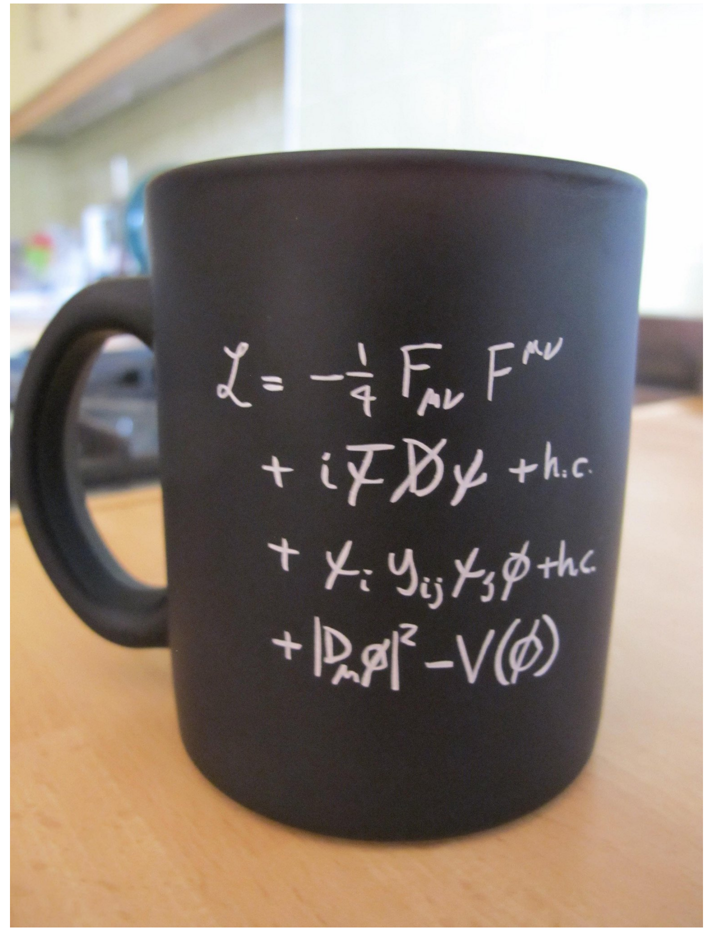


ACE Science Workshop

Fermilab

The Standard Model is UV-complete after the discovery of the Higgs:





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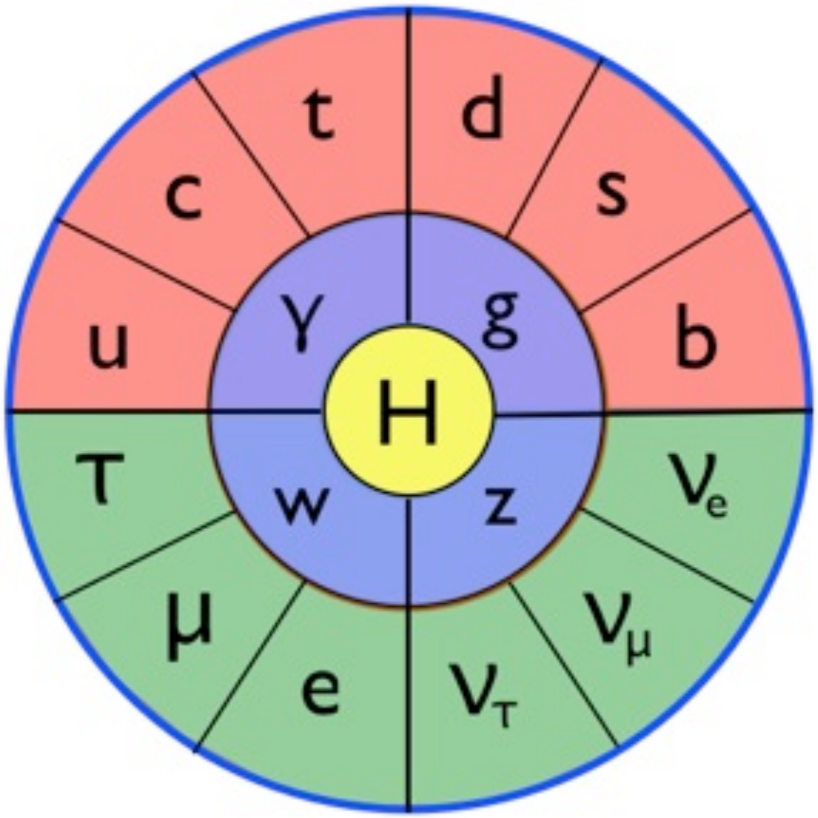

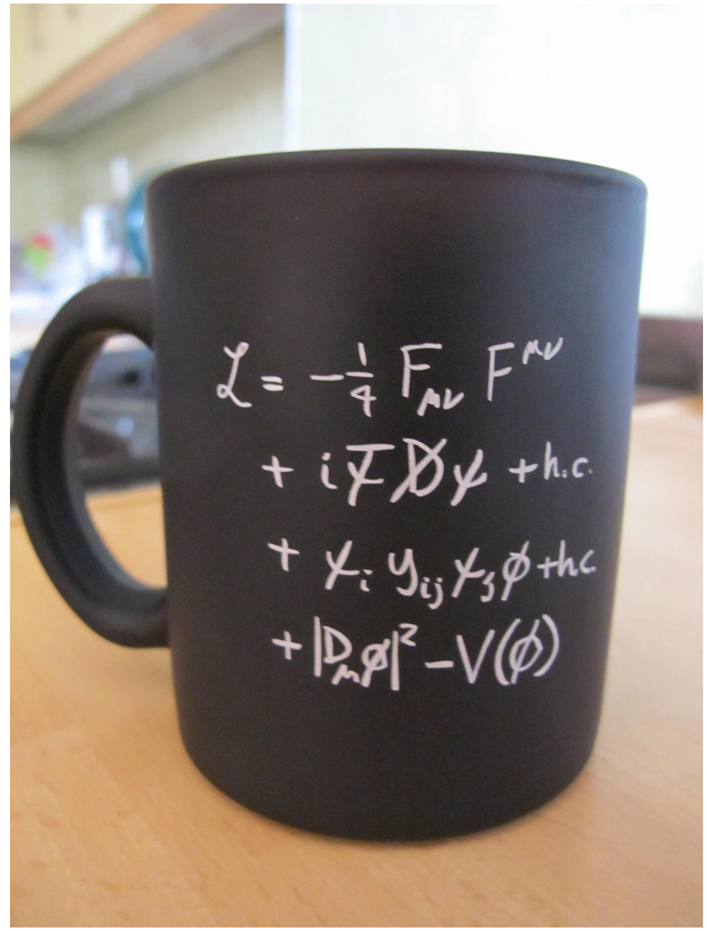

Why a 10 TeV Muon Collider then?

A reminder:

throughout the course of history, UV completion always fails to predict the completeness of the theory!

- QED (photons+electrons) is UV-complete. But physics didn't stop there.
- QCD (gluons+quarks) is UV-complete. Again physics didn't stop there.
- SM with one generation of fermion is UV-complete. "WHO ORDERED THAT?"

Why a 10 TeV Muon Collider?

- Questions unanswered
- Predictions untested
- A New Regime of Quantum Field Theories
- Strong Synergies with the Neutrino Frontier

Questions unanswered

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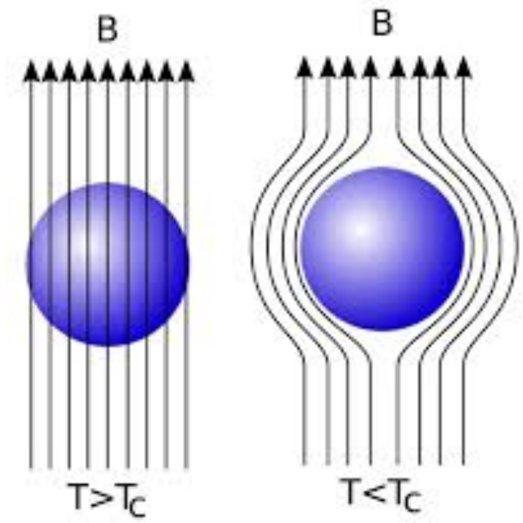
A physics Ph.D could rephrase the question in a slightly more sophisticated fashion:

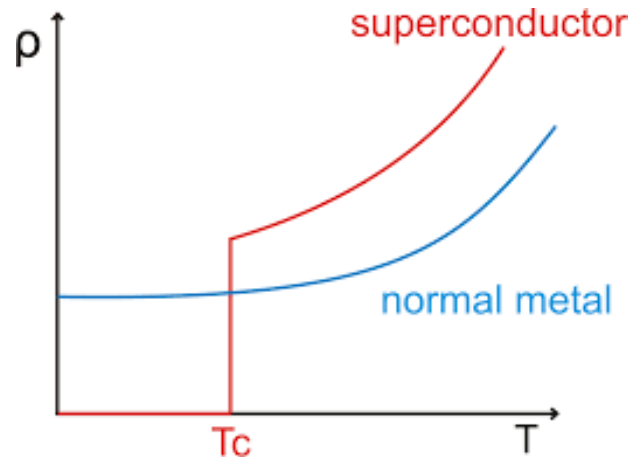
What is the microscopic theory that gives rise to the Higgs boson and its potential?

$$V(H) = -\mu^2|H|^2 + \lambda|H|^4$$

Our colleagues in condensed matter physics are very used to asking, and studying, this kind of questions.

One of the most beautiful examples is the superconductivity discovered in 1911:





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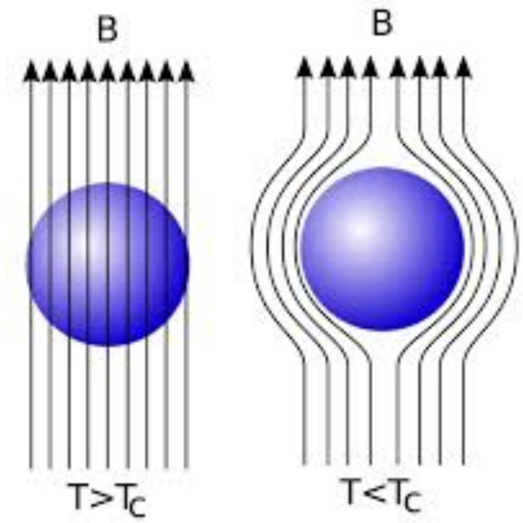

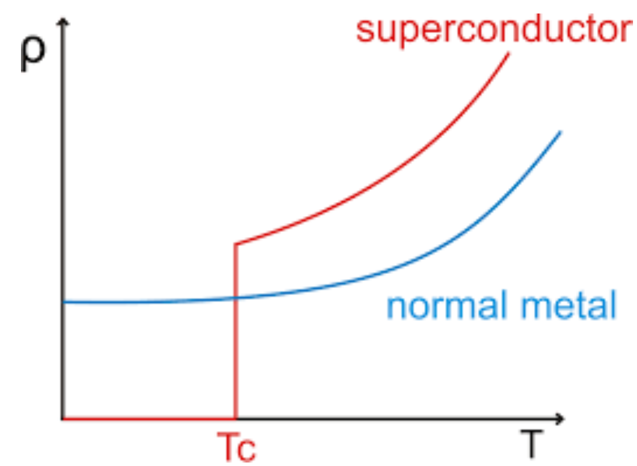

Ginzburg-Landau theory from 1950 offered a **macroscopic** (ie effective) theory for conventional superconductivity,

$$V(\Psi) = \alpha(T)|\Psi|^2 + \beta(T)|\Psi|^4 \qquad \alpha(T) \approx a^2(T - T_c) \qquad \text{and} \qquad \beta(T) \approx b^2$$

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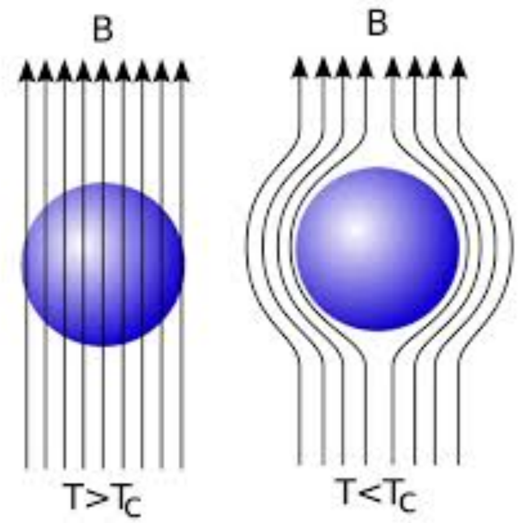

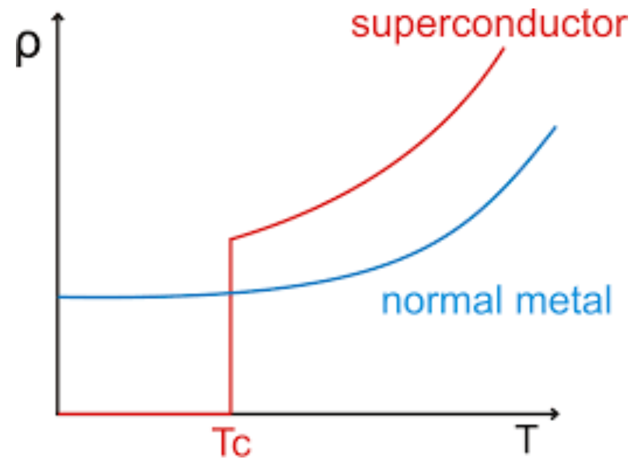

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What is the **microscopic** origin of the Ginzburg-Landau potential for superconductivity?

In 1957 Bardeen, Cooper and Schrieffer provided the **microscopic** (fundamental) theory that allows one to

1) interpret $|\Psi|^2$ as the number density of Cooper pairs

2) calculate coefficients of $|\Psi|^2$ and $|\Psi|^4$ in the potential.

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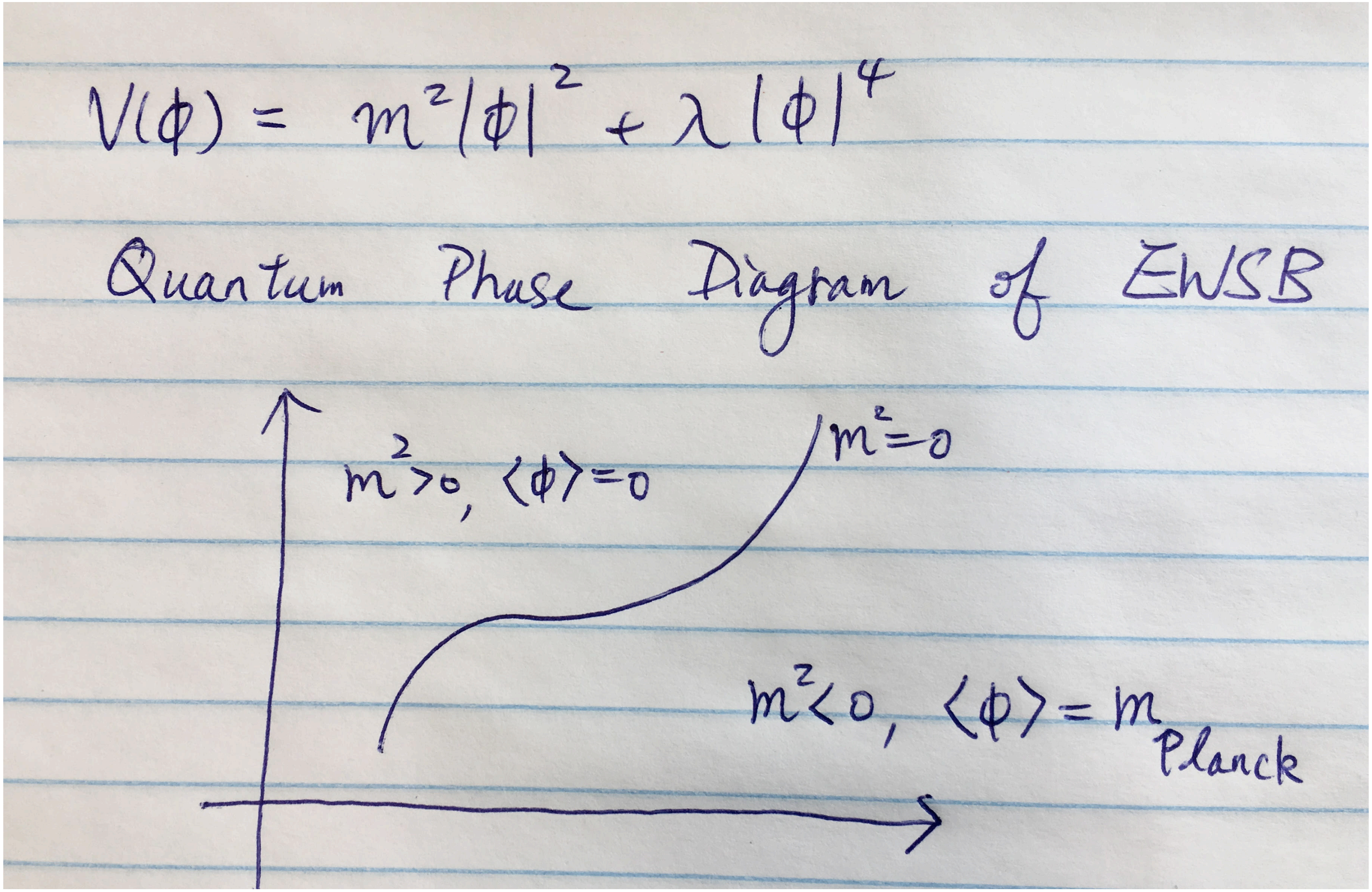
1) interpret $|\Psi|^2$ as the number density of Cooper pairs

2) calculate coefficients of $|\Psi|^2$ and $|\Psi|^4$ in the potential.

We do not have the corresponding **microscopic** theory for the Higgs boson.

In fact, we have NOT even measured the Ginzburg-Landau potential of the Higgs!

The question can be reformulated in terms of **Quantum Criticality**:



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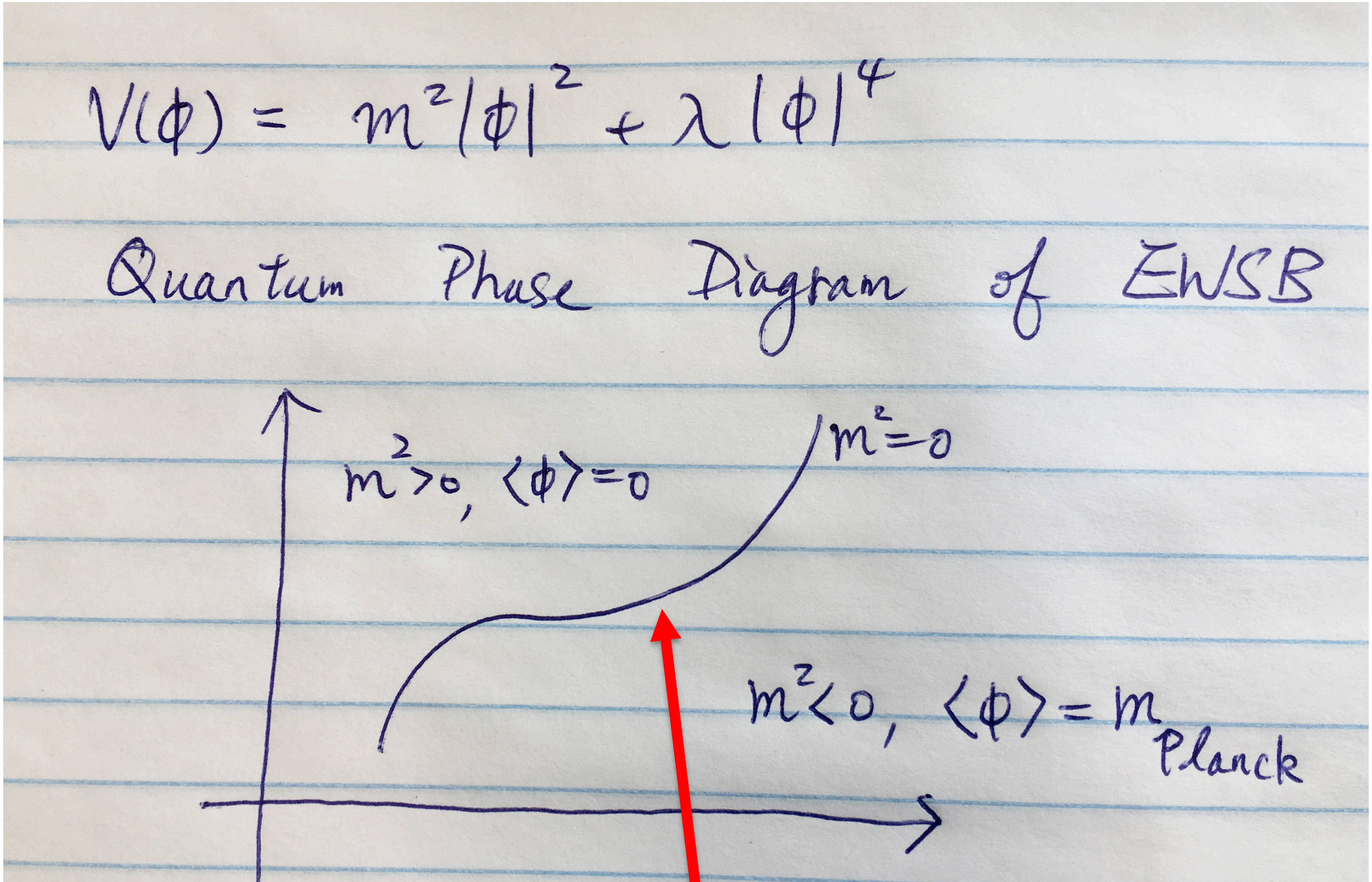


Mh=125 GeV. We are sitting extremely close to the criticality. **WHY??**

One appealing possibility – the critical line is selected dynamically.

This is the analogy of BCS theory for electroweak symmetry breaking. It goes by the name of “technicolor,” which is strongly disfavored experimentally.

“The Universe is not a piece of crappy metal!”

by a prominent HEP theorist.

Every day we don't observe any signs of new physics, the mystery deepens and the plot thickens:

Why are we sitting close to the critical line of EWSB??

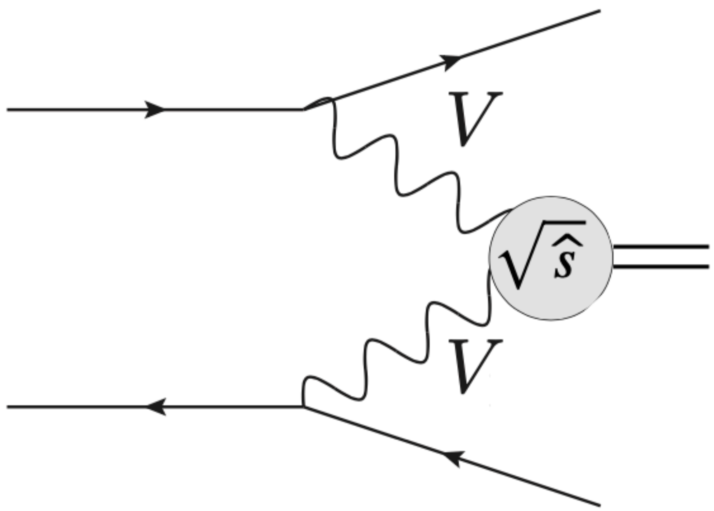
An esteemed condensed matter colleague once told me "I have a microscopic theory for EWSB!"

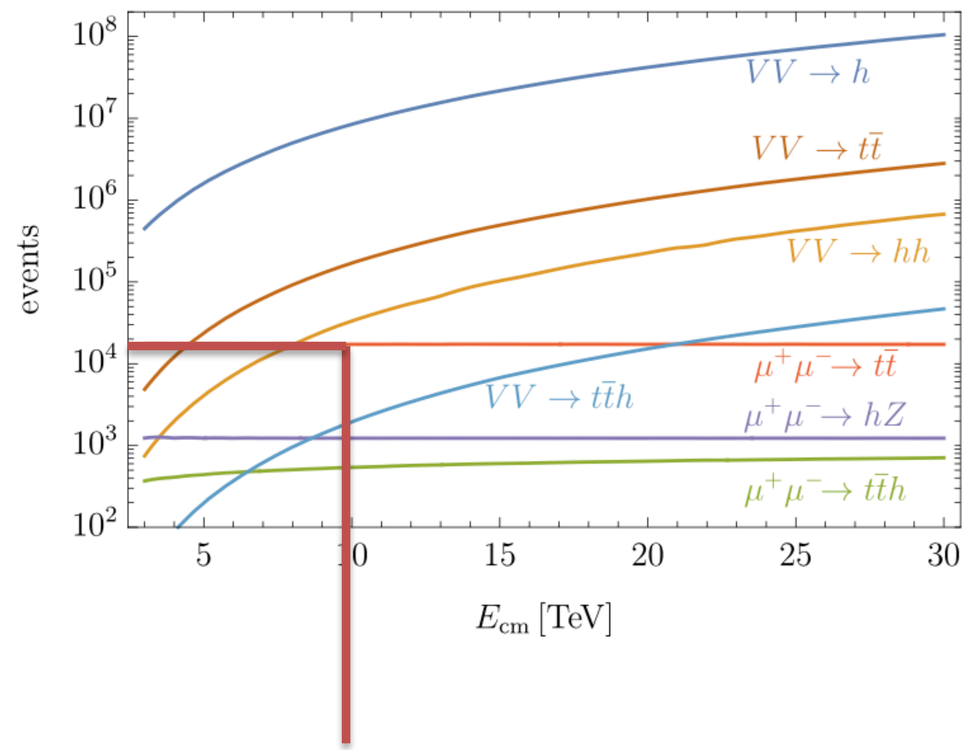
I asked him "So tell me, do you have Higgs and nothing else?"

Then he shut up…

EWSB is the most exotic state of quantum criticality.

A 10 TeV muon collider would be a super-Higgs factory, producing ~ 10 million Higgs bosons with 10 /ab:



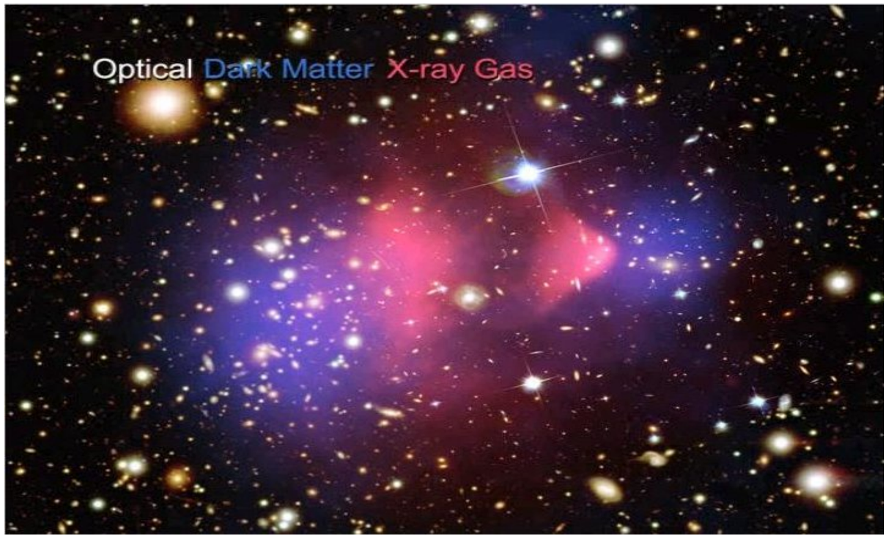


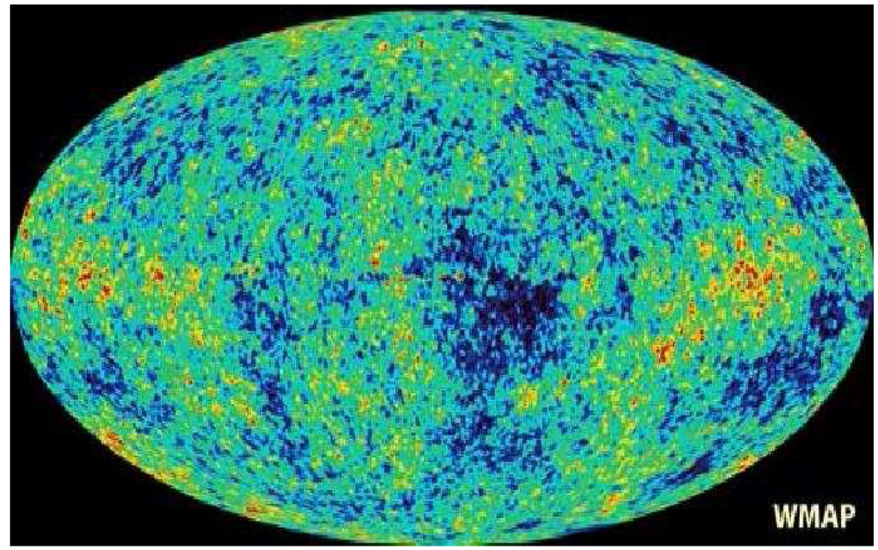
This would allow us to study the microscopic properties of the Higgs!

(By comparison, an "ordinary" Higgs factory produces ~ 1 million Higgses.)

Some excellent empirical questions SM cannot answer:

- Dark matter/Dark sector:





We (most people) are convinced about the existence of dark matter. What is it??

In principle, a high energy collider could produce dark matter particles with mass around E_{CM} /2.

For the simplest WIMP scenarios, the thermal target is well above 1 TeV:

Thermal targets

Model (color, n, Y)		Therm. target
(1,2,1/2)	Dirac	1.1 TeV
(1,3,0)	Majorana	2.8 TeV
(1,3,ϵ)	Dirac	2.0 TeV
(1,5,0)	Majorana	14 TeV
(1,5,ϵ)	Dirac	6.6 TeV
(1,7,0)	Majorana	48.8 TeV
(1,7,ϵ)	Dirac	16 TeV

Correct relic abundance
$\Rightarrow$ Thermal targets

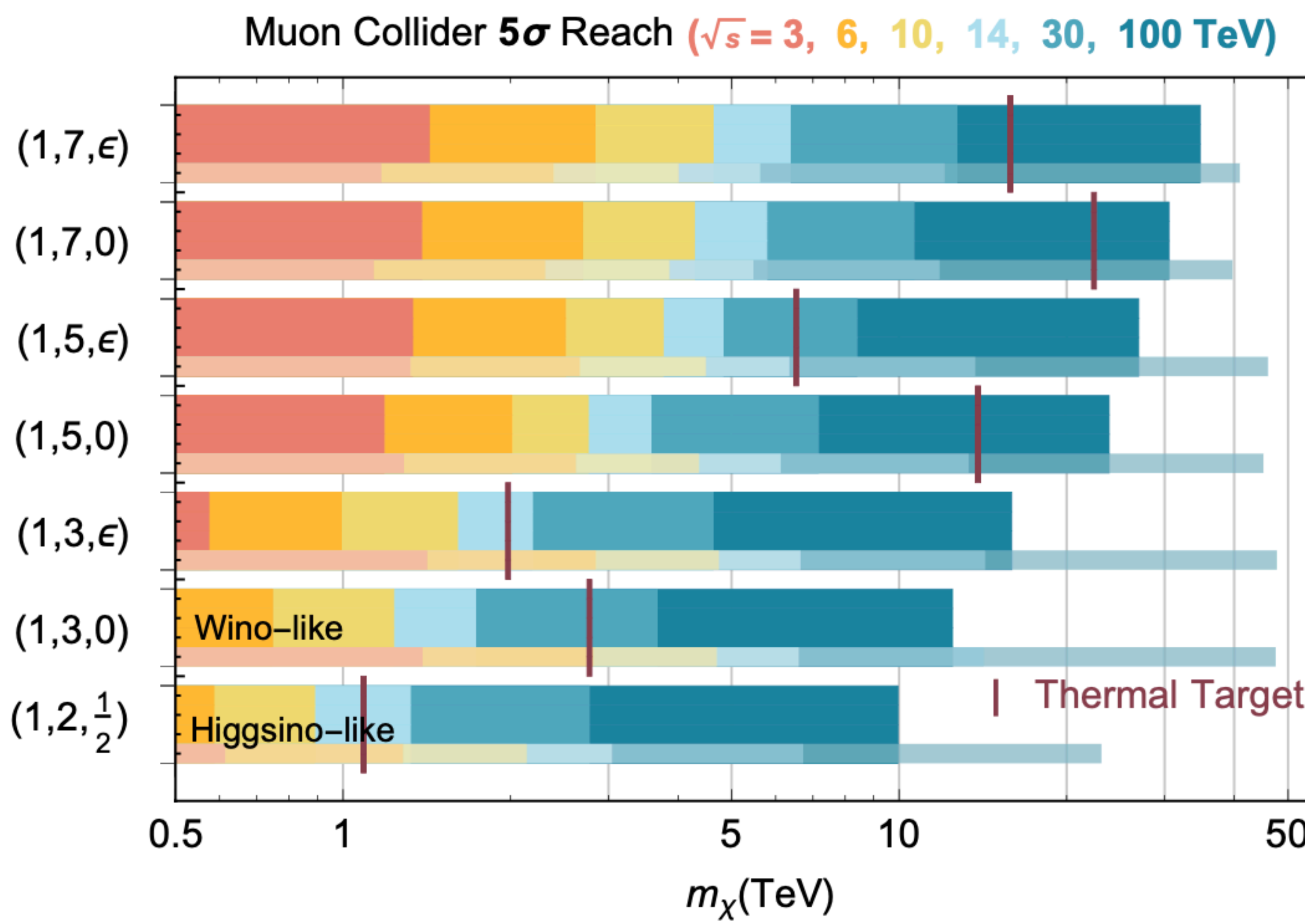
Reach up to thermal target
$\approx$
complete coverage for WIMP candidate

Mitridate, Redi, Smirnov, Strumia, 1702.01141

S. Bottaro, D. Buttazzo, M. Costa, R. Franceschini, P. Panci, D. Redigolo, L. Vittorio, 2107.09688

Slide from L.-T. Wang

Preliminary study of searching for “minimal” WIMPs:

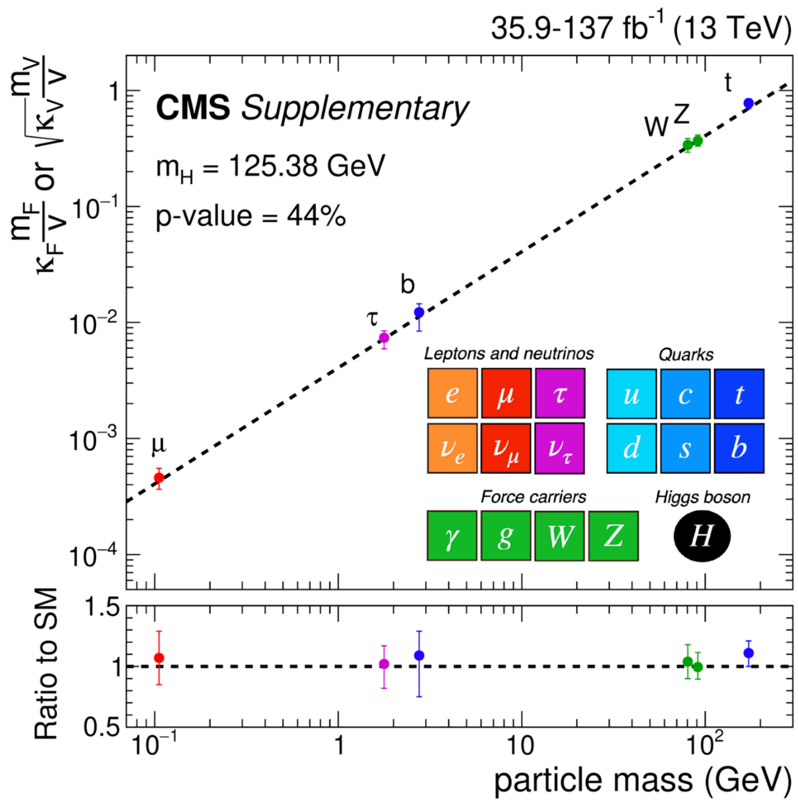


T. Han, Z. Liu, L.-T. Wang, X. Wang: 2009.11287

Predictions untested

- **Prioritize couplings which have yet to be established experimentally:**

Yukawa couplings to 1st and 2nd generation fermions.



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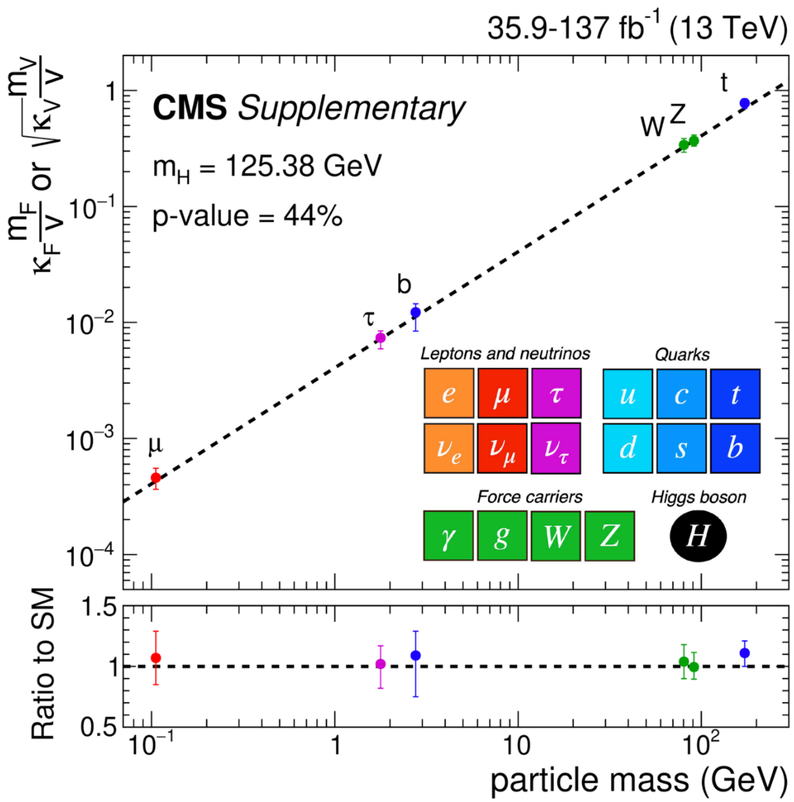
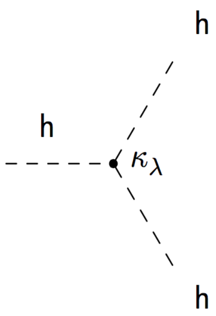


Trilinear Higgs self-coupling – we have NOT measured the Higgs potential.



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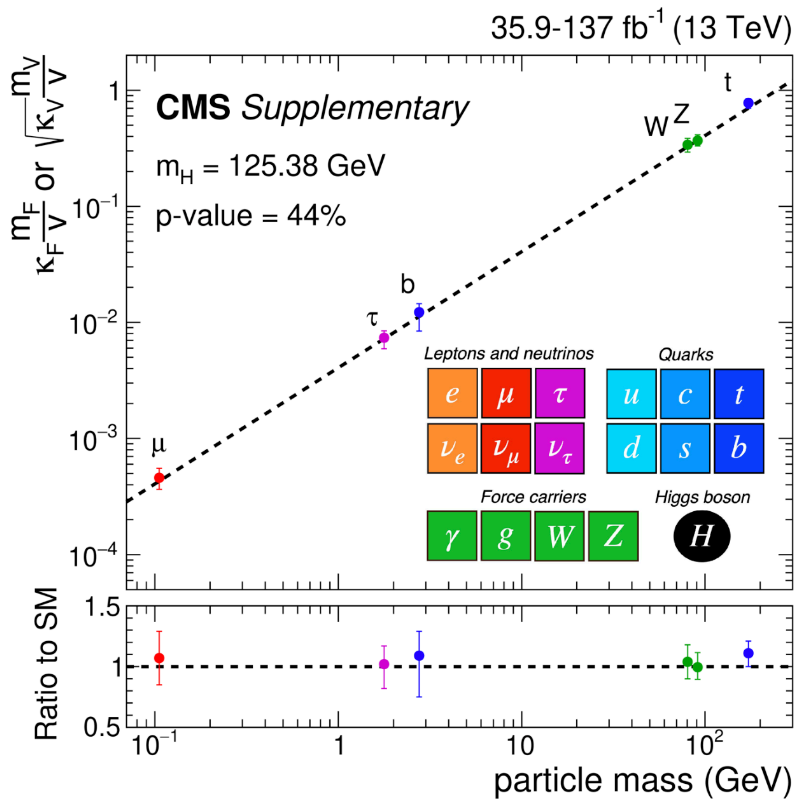

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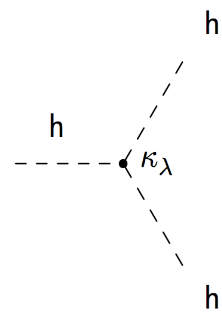
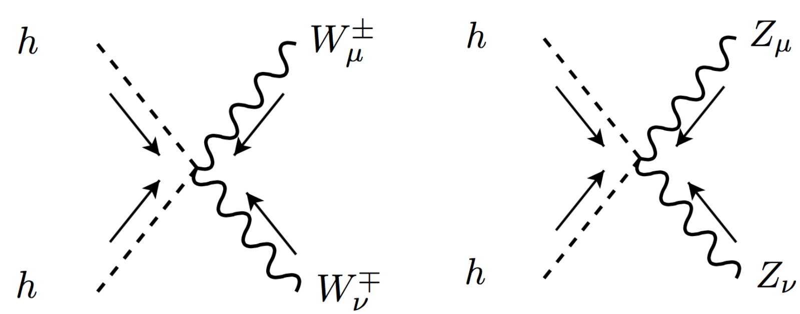
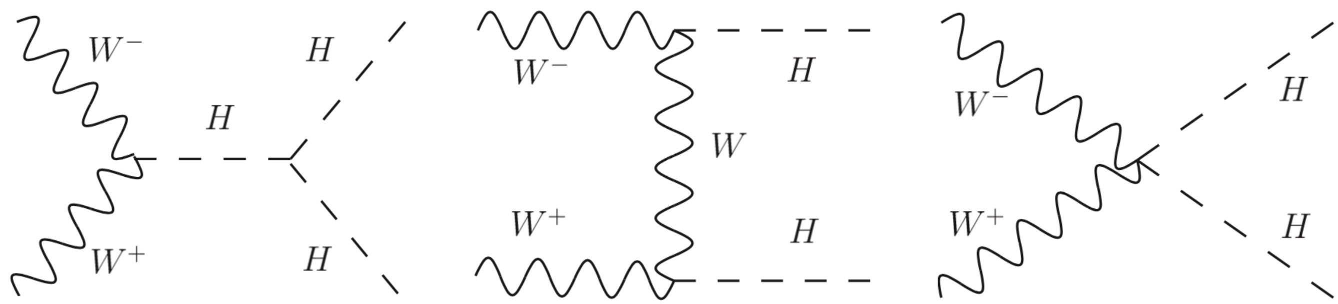


4-pt HHVV coupling – prediction of gauge invariance.

$$D_\mu H^\dagger D^\mu H \supset g^2 h^2 V_\mu V^\mu$$



- At a lepton collider, both the trilinear and quartic couplings can be probed in double Higgs production through VBF:



(a) (b) (c)

Notice the process is sensitive to **both** HHH and WWHH couplings!

- Using the M_{HH} shape information, it is possible to constrain both couplings at the same time:

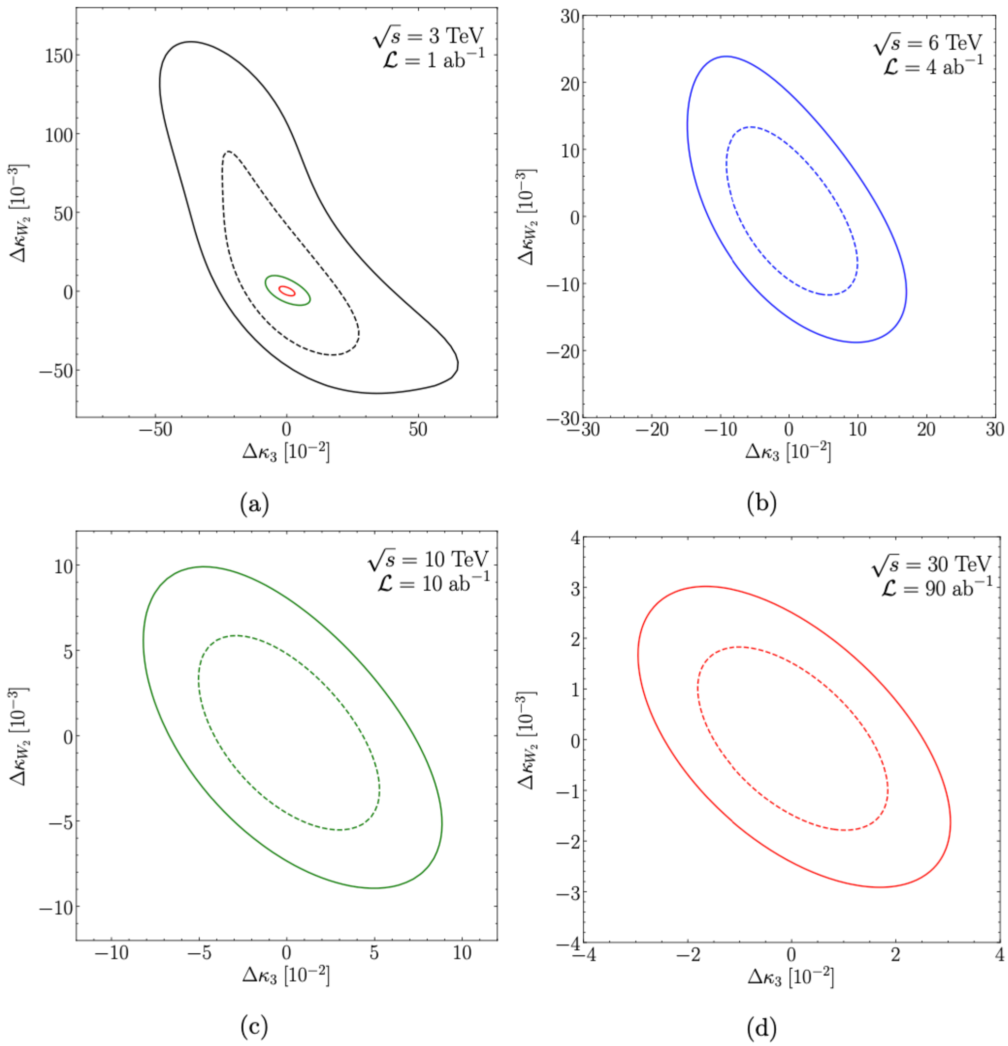


Figure 7: Correlated bounds with 95% C.L. (solid) and 68% C.L. (dashed) in the $\Delta\kappa_{W_2}$-$\Delta\kappa_3$ plane for $\sqrt{s} = 3, 6, 10, 30$ TeV, respectively. In (a), inner ellipses (solid) include the 95% C.L. results for 10 TeV and 30 TeV for comparison.

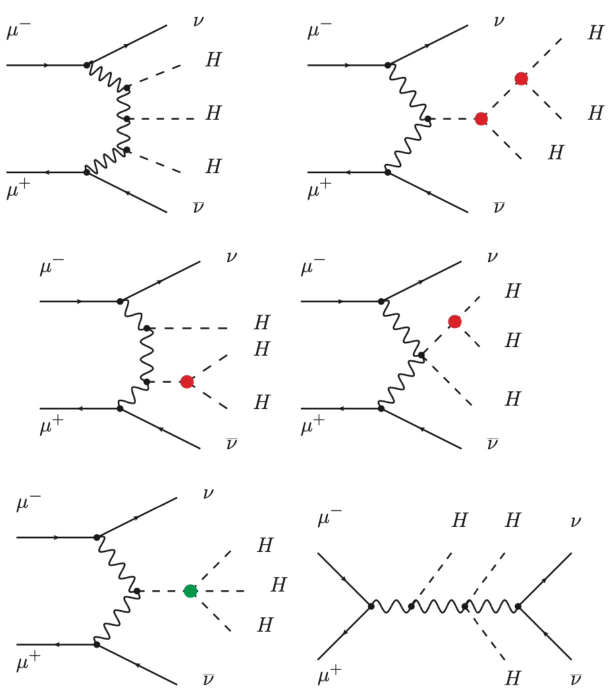
T. Han, D. Liu, IL, X. Wang: 2008.12204

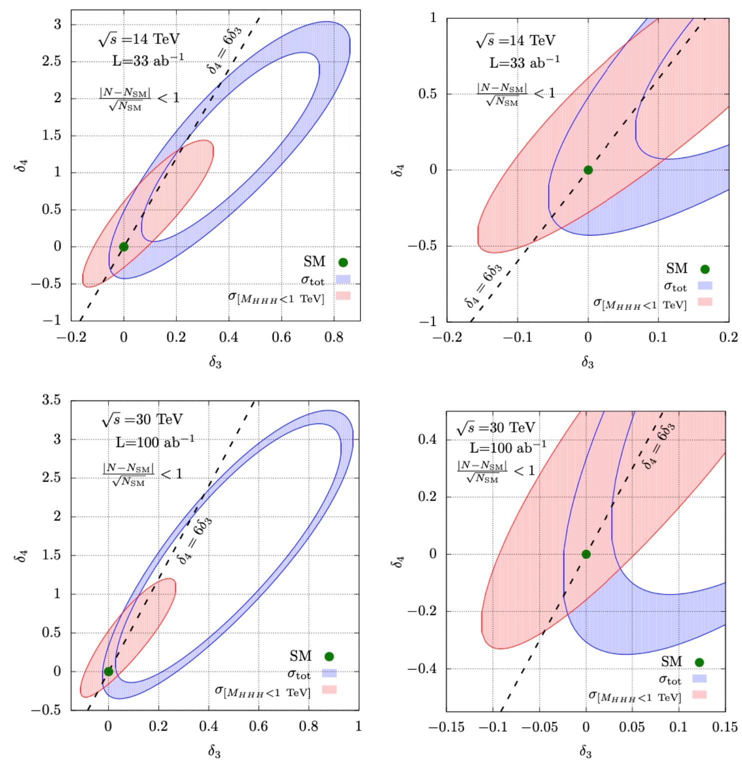
As we go to very high energies, we can even produce triple and quadruple Higgses!

- HHH and HHHH final states have not been searched for experimentally. **What are the SM predictions??**

This is a new frontier waiting to be explored further. There's a study on HHH final state at the Muon collider:

Chiesa et al: 2003.13628

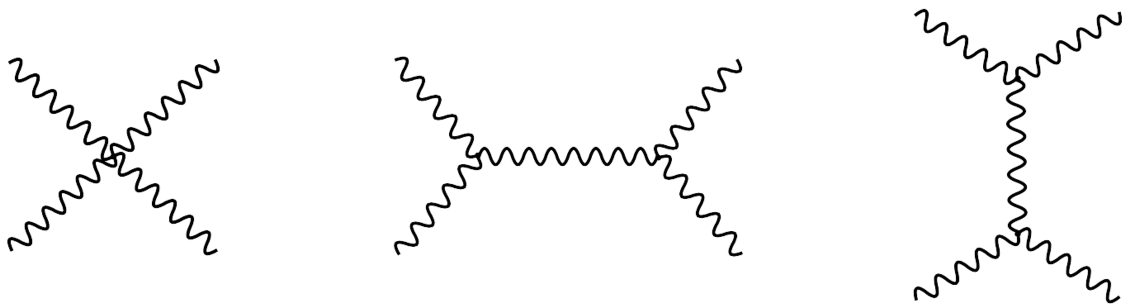




See also: IL, N. Shah, X. Wang: 2012.00773; Egana-Ugrinovic, Homiller, Meade: 2101.04119
C.-W. Chiang, T.-K. Kuo, IL: 2202.02954

- Would like to single out one very important prediction of SM Higgs to be tested precisely:

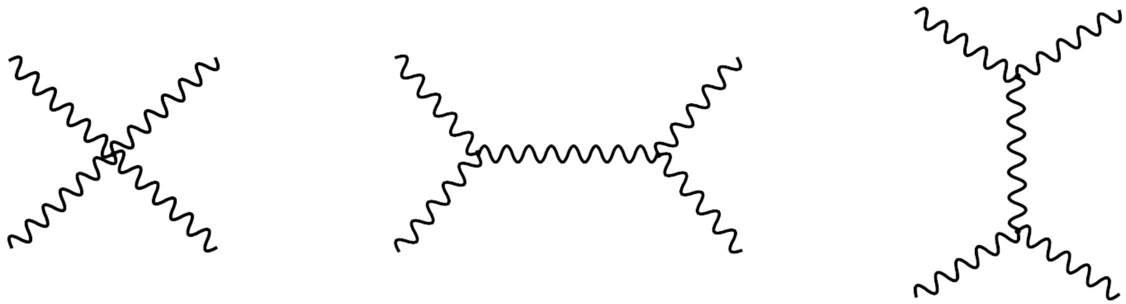
  Without the Higgs, WW scattering amplitude violates unitarity:

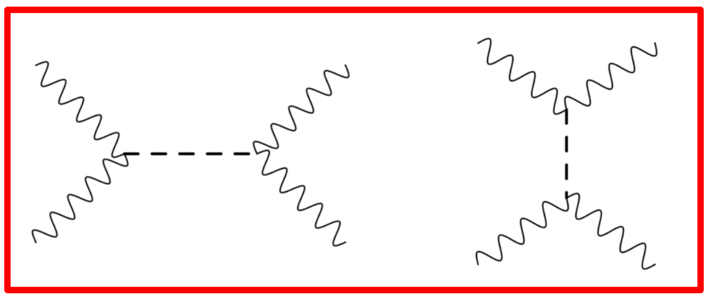


$$\mathcal{A}(W_L^+ W_L^- \to W_L^+ W_L^-) \simeq \frac{g^2}{4m_W^2}(s+t) \ .$$

- Would like to single out one very important prediction of SM Higgs to be tested precisely:

  Including the Higgs contribution allows the growth to be cancelled completely,





provided the HWW coupling have precisely the form in the SM!

This is an extremely simple and economical solution, except…

Nature has never chosen this simple solution before…

(Recall we have NOT observed a fundamental scalar previously!)

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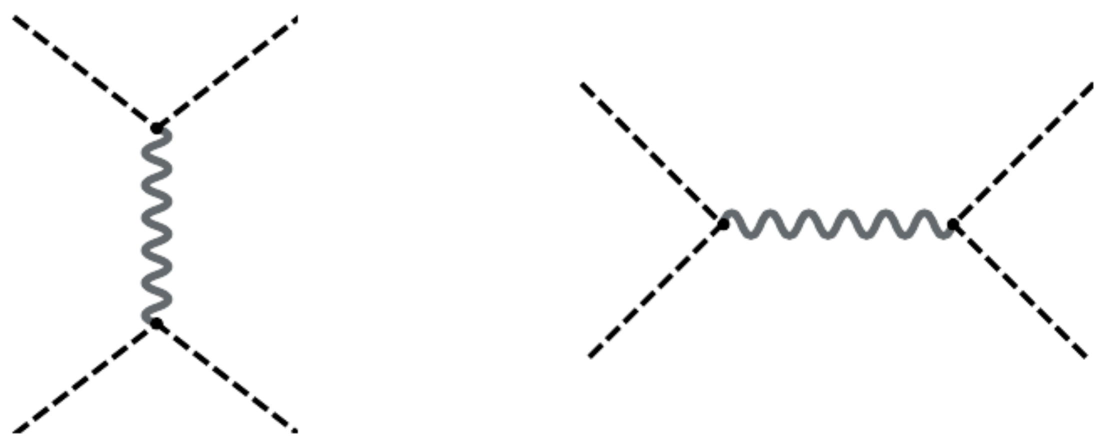
For example, pi-pi scattering in low-energy QCD is unitarized by a series of heavy resonances, including the spin-1 rho meson:



Each resonance only partially unitarizes the pi-pi scattering.

If the 125 GeV Higgs only partially unitarize the VV scattering

→ the HVV coupling will deviate from the SM expectation!!

Unitarization in VV scattering is only tested with O(10%) uncertainty.

→ Clearly not sufficient!

How precise is precise enough?

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How precise is precise enough?

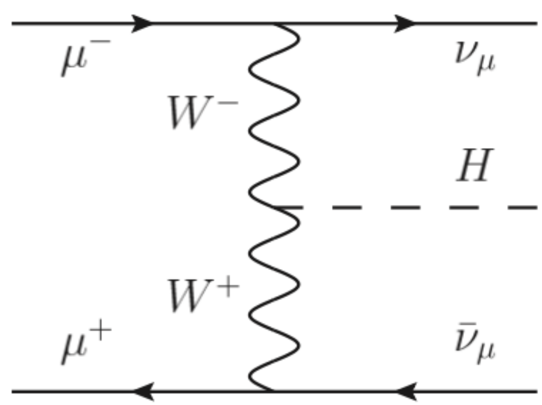
By accident, generic deviations from SM are quadratic in $1/M_{new}$:

$$\mathcal{O}\left(\frac{v^2}{M_{\rm new}^2}\right) \sim 5\% \times \left(\frac{1\ \mathrm{TeV}}{\Lambda}\right)^2$$

To establish credible deviations we need percent level precision!

At a high energy muon collider, single Higgs production goes through the VBF topology. Moreover, both WW and ZZ fusion need to be considered:

$$\mu^+\mu^- \to \nu_\mu\bar{\nu}_\mu\, H \qquad (WW \text{ fusion}),$$
$$\mu^+\mu^- \to \mu^+\mu^-\, H \qquad (ZZ \text{ fusion}).$$



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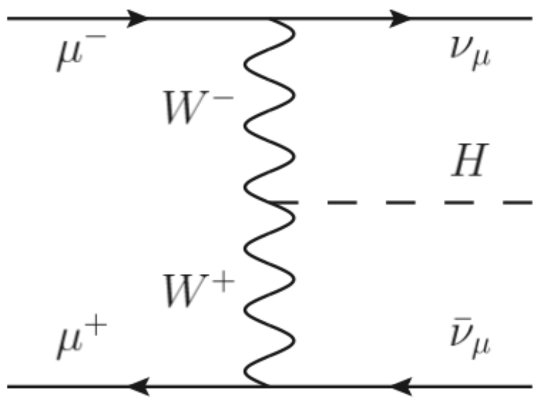

However, in the ZZ fusion channel, the outgoing muons are very forward and may escape detections. This led to the notion of a "inclusive process,"

- Inclusive channel: events from WW fusion and from ZZ fusion without detecting muons;

Similar to that in a hadron collider!

A preliminary study using the "kappa" formalism at the muon collider:

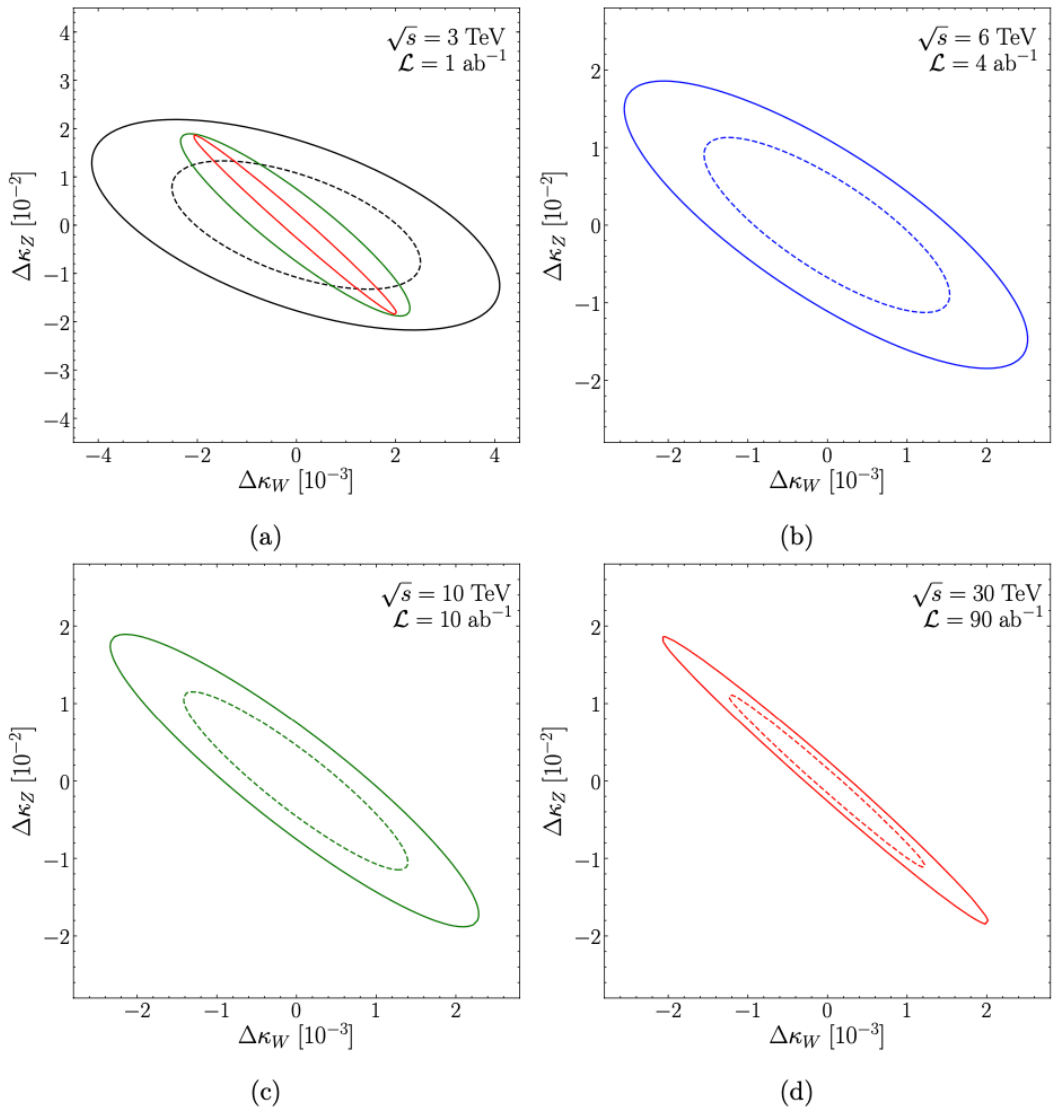

Figure 6: Correlated bounds with 95% C.L. (solid) and 68% C.L. (dashed) in the $\Delta\kappa_W$-$\Delta\kappa_Z$ plane for $\sqrt{s} = 3, 6, 10, 30$ TeV, respectively. In (a), inner ellipses (solid) include the 95% C.L. results for 10 TeV and 30 TeV for comparison.

A New Regime of QFT

At 10 TeV, the SM enters into a new regime of QFT which has never been studied/observed previously:

$$E \gg m_W \qquad\qquad (\text{Casimir}) \times \frac{\alpha_2}{\pi} \log^2 \frac{E}{m_W} \sim \mathcal{O}(1)$$

We will observe enhanced electroweak radiations in a *nearly* massless non-abelian gauge theory!

This is not dissimilar to QCD and QED in the high energy regime (E>> Λ_{QCD} and E >>μ_{IR}), with one crucial difference:

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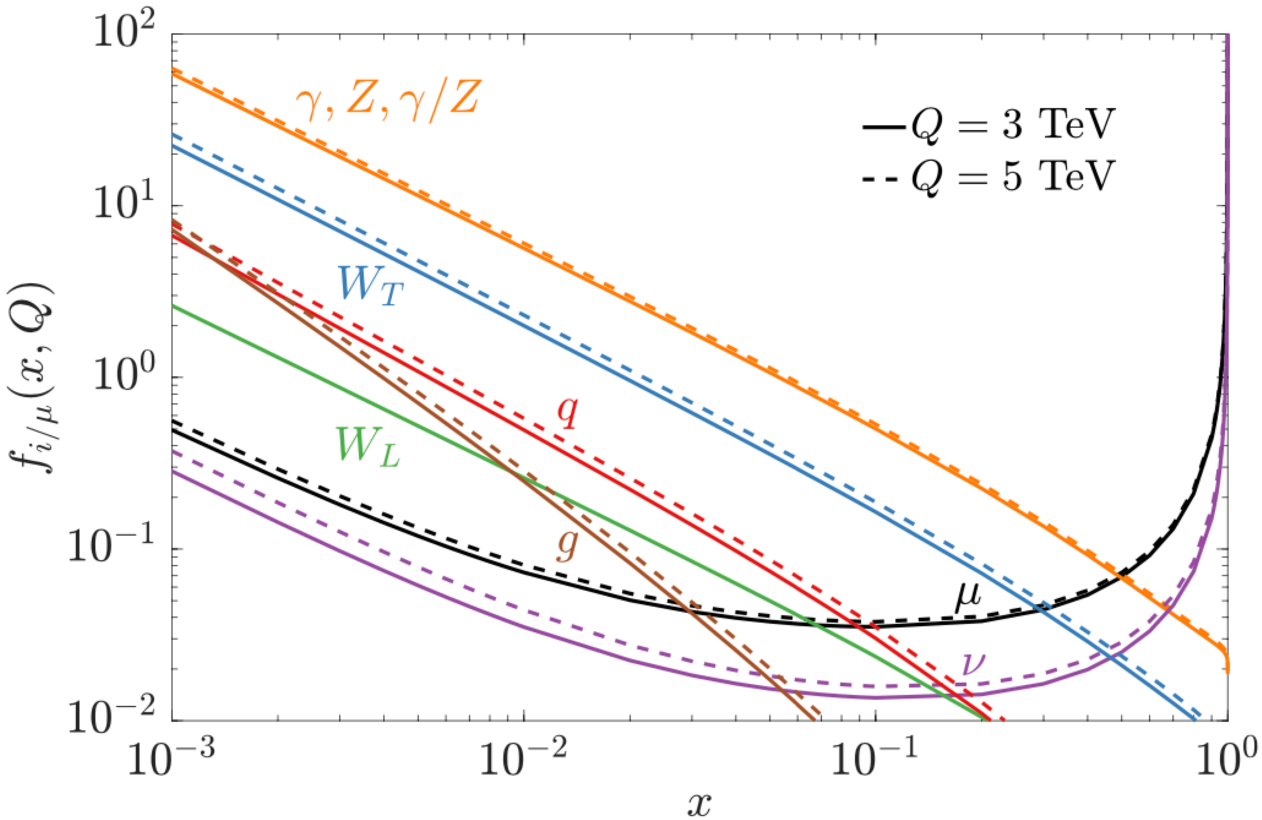
Electroweak symmetry is broken and electroweak "color" is observable!

This is a new phase of non-abelian gauge theory we would not be able to study/observe at lower energies or elsewhere!

There are several novel features in this regime of broken gauge theory:

- The muon effectively becomes a composite particle and the collision is described by electroweak parton distribution functions:

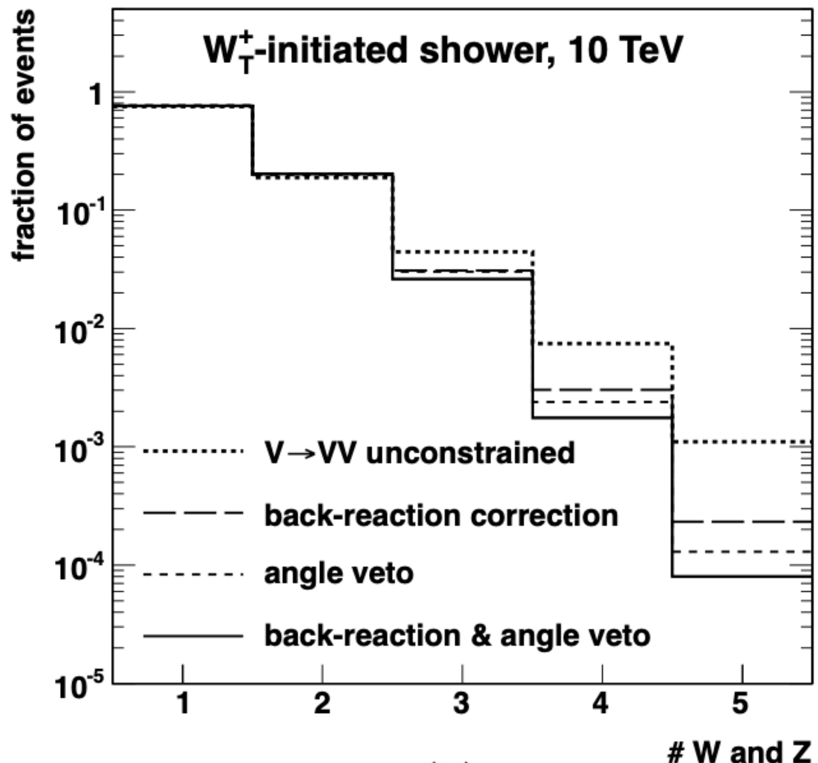


T. Han, Y. Ma, K. Xie: 2007.14300; 2103.09844

(See also A. Constantini et. al.: 2005.10289; S. Chen et. al.: 2202.10509.)

The need to consider electroweak "parton showering" gives rise to the concept of "weak jets."

One example is multiple collimated EW bosons initiated from transverse gauge bosons:

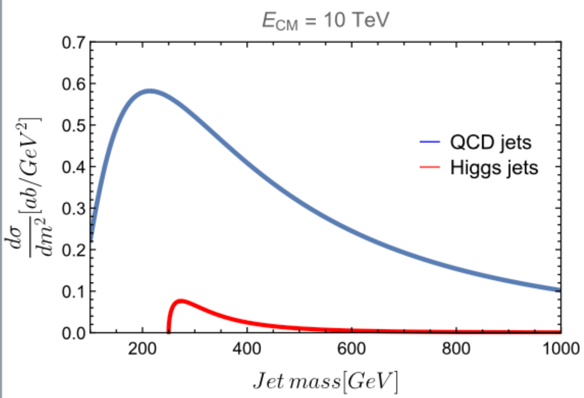


(b)

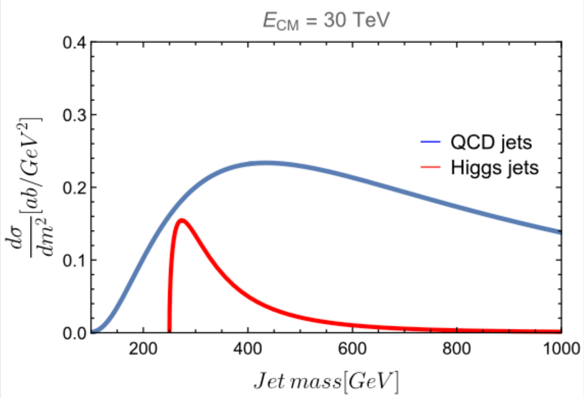
J. Chen, T. Han, B. Tweedie: 1611.00788

One could also have "Higgs jet," which have distinct features due to the presence of "super-renormalizable" trilinear coupling:

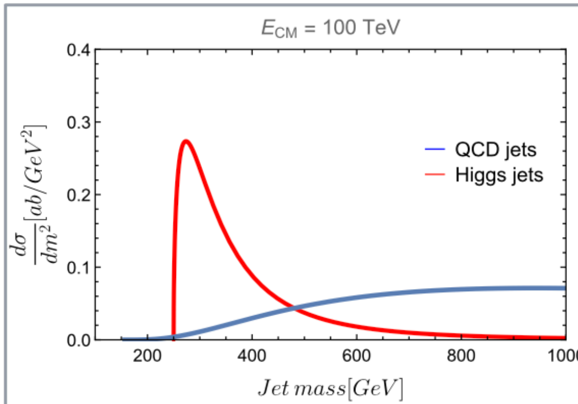
COMPARISON PLOTS



$C_{EW}^{(1)}\ (10\ TeV) = -1.178$



$C_{EW}^{(1)}\ (30\ TeV) = -1.984$



$C_{EW}^{(1)}\ (100\ TeV) = -3.108$

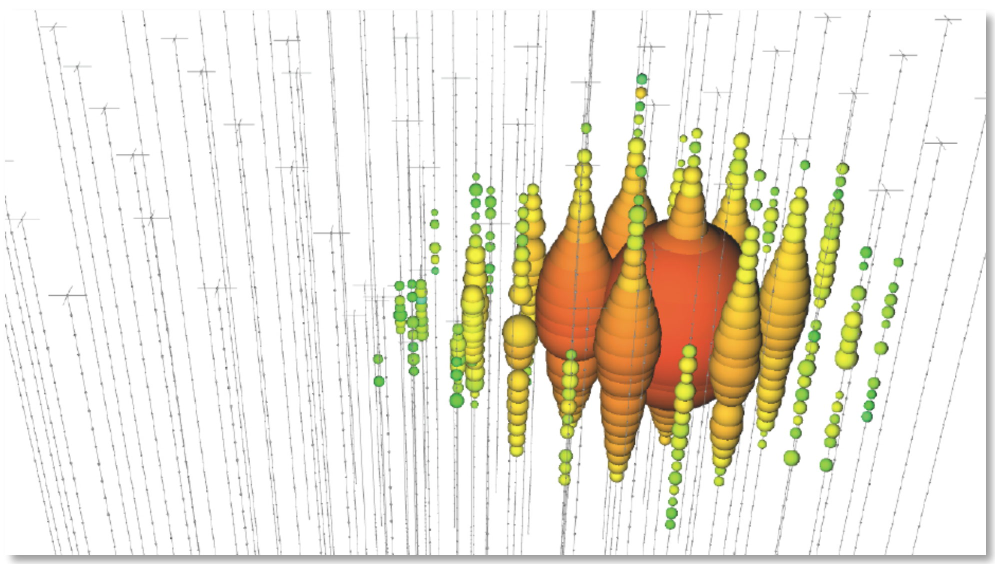
Preliminary work by J. Desai and G. Sterman

Strong Synergies with the Neutrino Frontier

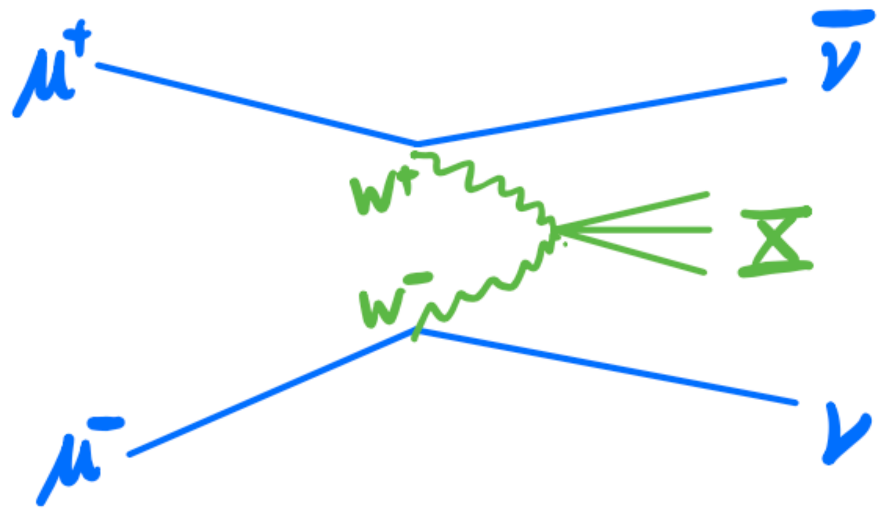
One of the most interesting questions (benchmarks) is the electroweak parton showering of a high energy neutrino:

- Can a very energetic neutrino be "seen" via the final state radiation? (A ν-jet ?)

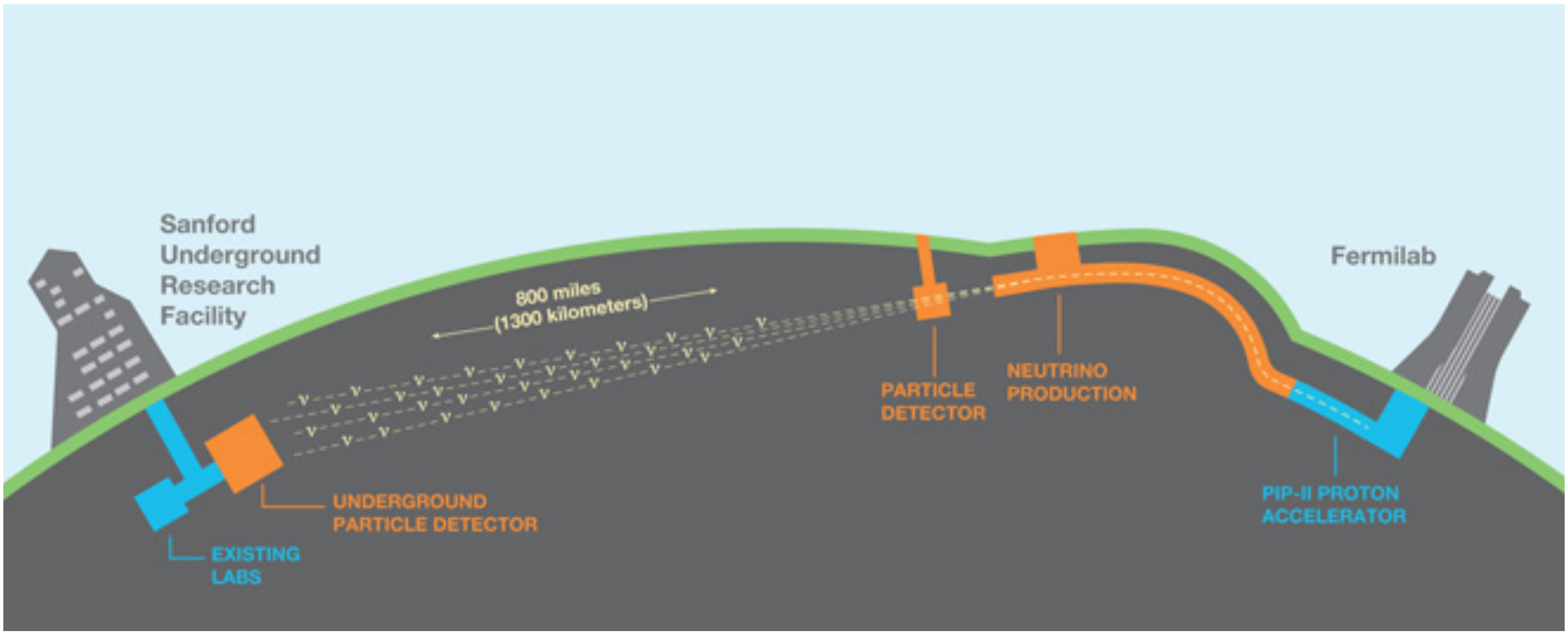
- What about through its interactions with detector materials ?? (A ν-calorimeter?)



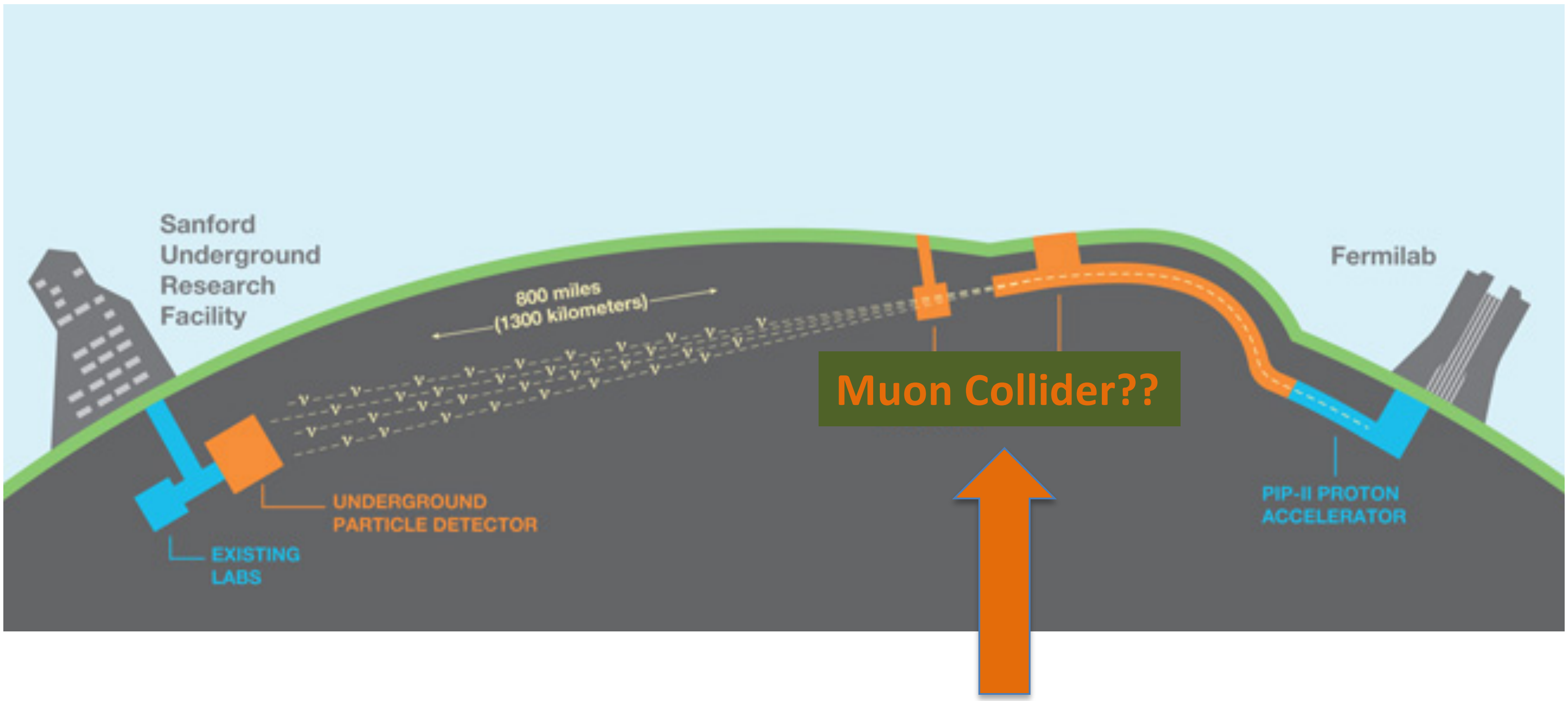
- A high energy muon beam is also a high energy neutrino beam:



Can we direct the neutrino beam somewhere and do some neutrino physics?

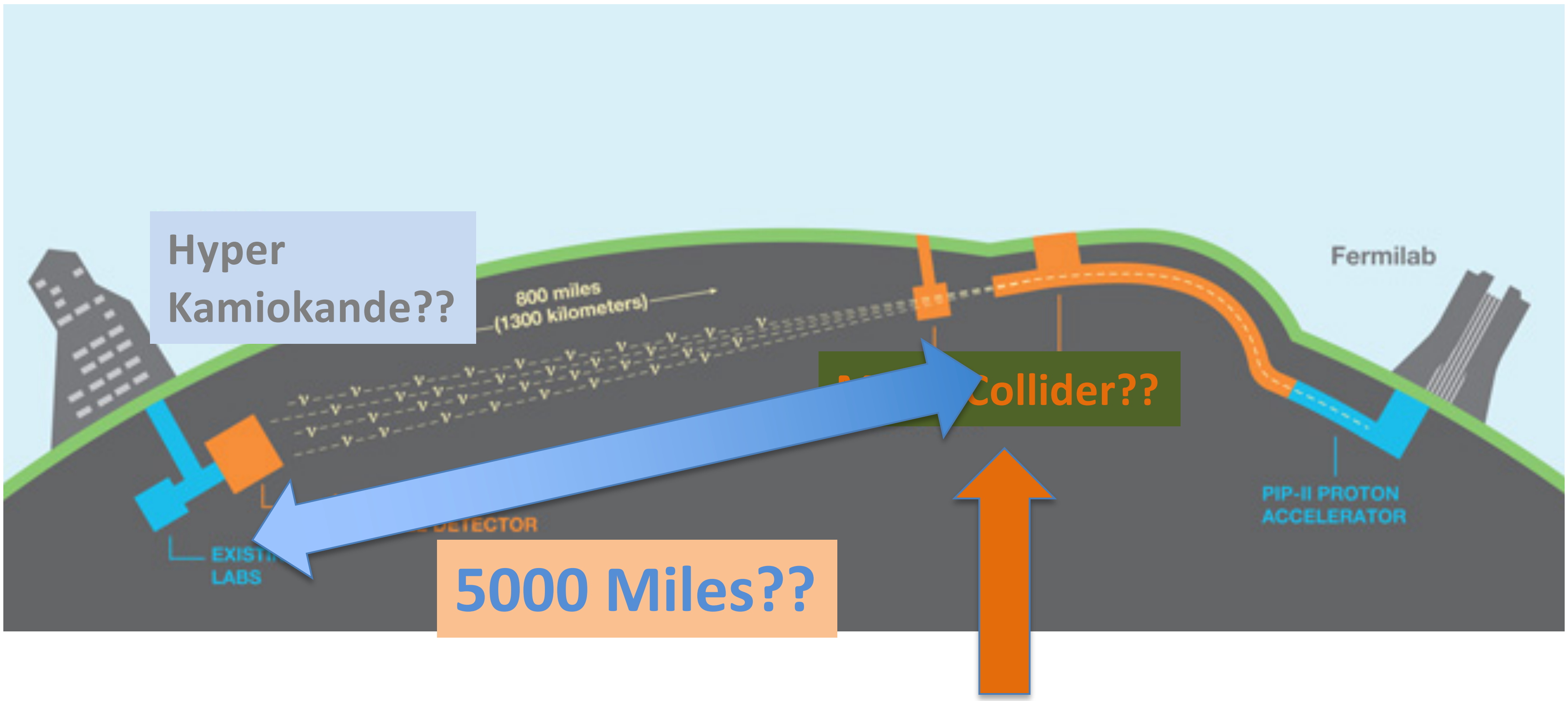


Sanford Underground Research Facility
800 miles (1300 kilometers)
Fermilab
PARTICLE DETECTOR
NEUTRINO PRODUCTION
UNDERGROUND PARTICLE DETECTOR
EXISTING LABS
PIP-II PROTON ACCELERATOR



Much higher energy neutrino beam.
Matter effects are more important!

A suggestion by R. Kitano, a colleague at KEK:



Much higher energy neutrino beam.
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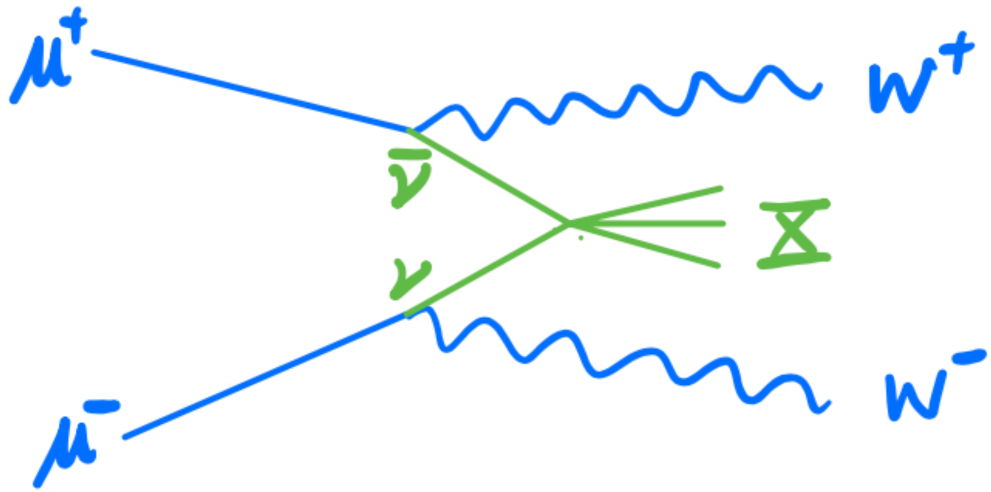
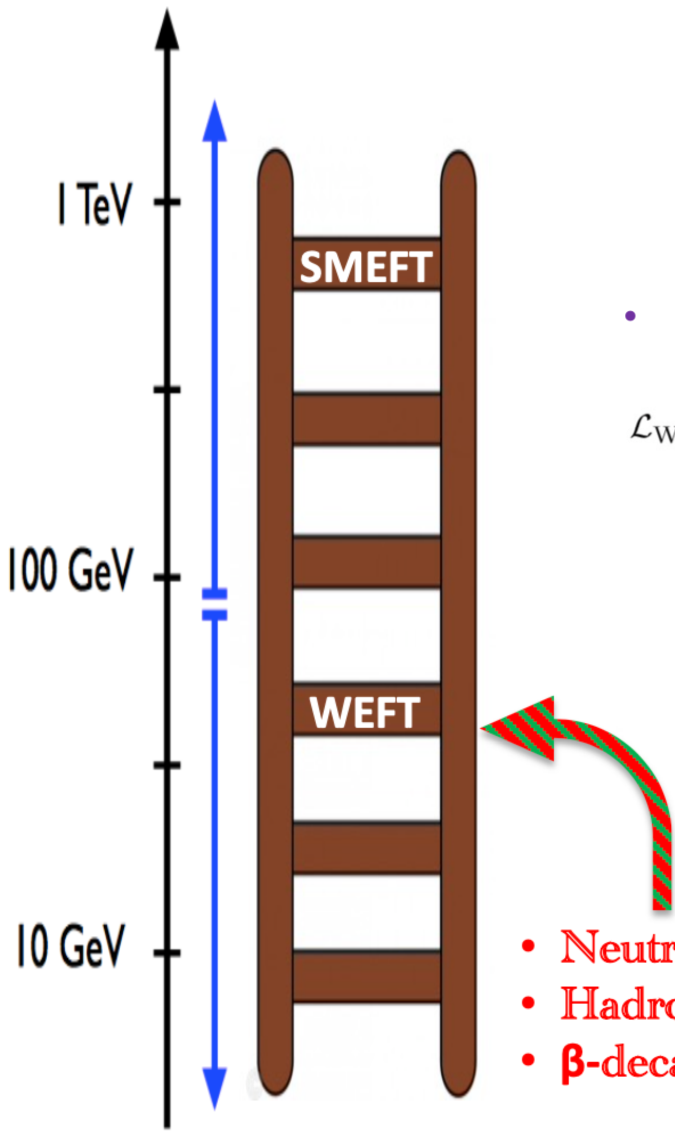
- A high energy muon collider is also a high energy neutrino collier:



Could provide constraints to Non-standard Interactions that are complementary to low-energy probes!

EFT ladder

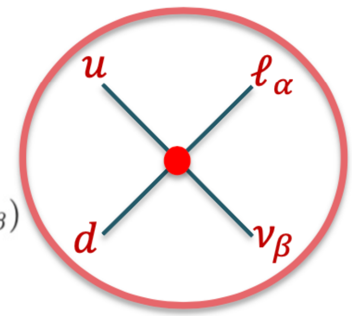


- Neutrino experiments
- Hadron Decays
- **β-decays**

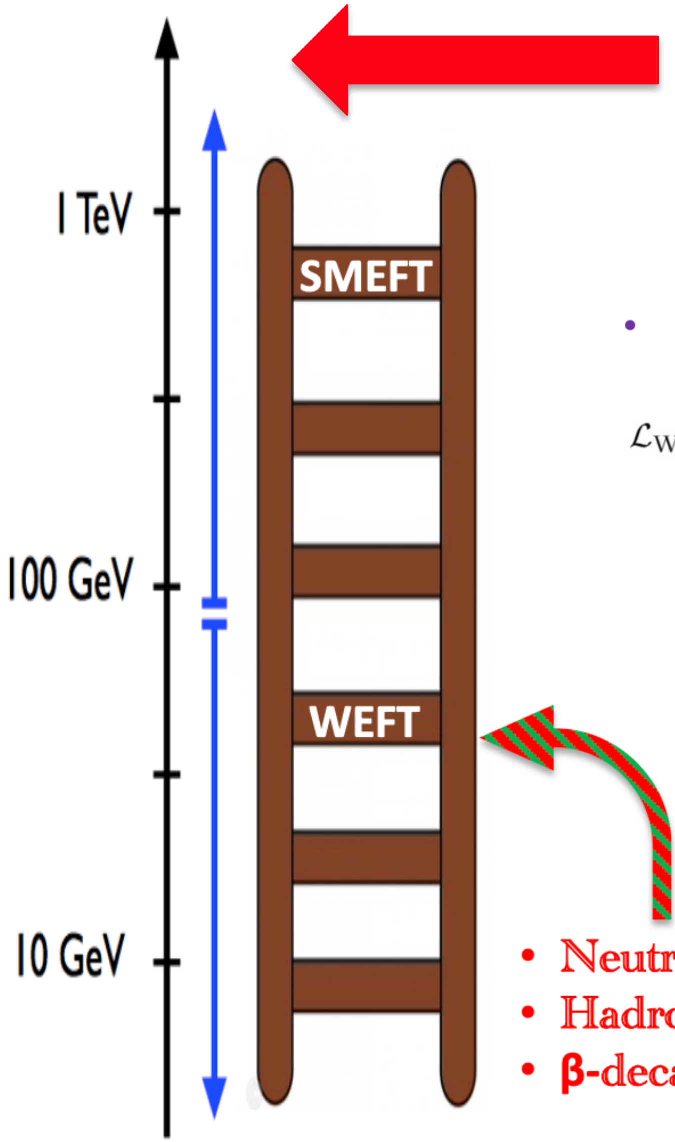
Art work by Z. Tabrizi

- CC: New left/right handed, (pseudo)scalar and tensor interactions

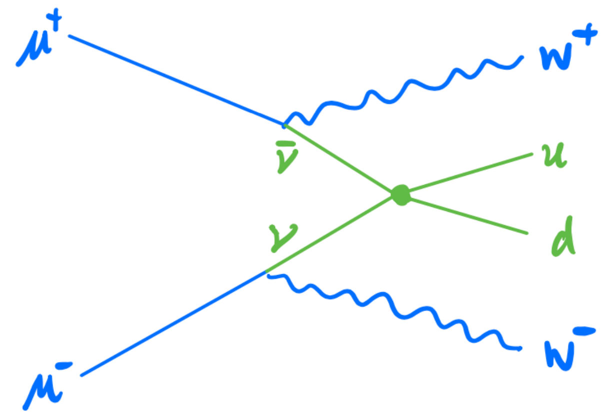
$$\begin{aligned}\mathcal{L}_{\rm WEFT} \supset\; & -\frac{2V_{ud}}{v^2}\{\,[\mathbf{1}+\epsilon_L]_{\alpha\beta}(\bar{u}\gamma^\mu P_L d)(\bar{\ell}_\alpha\gamma_\mu P_L\nu_\beta) \\ & +[\epsilon_R]_{\alpha\beta}(\bar{u}\gamma^\mu P_R d)(\bar{\ell}_\alpha\gamma_\mu P_L\nu_\beta) \\ & +\frac{1}{2}[\epsilon_S]_{\alpha\beta}(\bar{u}d)(\bar{\ell}_\alpha P_L\nu_\beta)-\frac{1}{2}[\epsilon_P]_{\alpha\beta}(\bar{u}\gamma_5 d)(\bar{\ell}_\alpha P_L\nu_\beta) \\ & +\frac{1}{4}[\hat{\epsilon}_T]_{\alpha\beta}(\bar{u}\sigma^{\mu\nu}P_L d)(\bar{\ell}_\alpha\sigma_{\mu\nu}P_L\nu_\beta)+\text{h.c.}\}\end{aligned}$$



EFT ladder

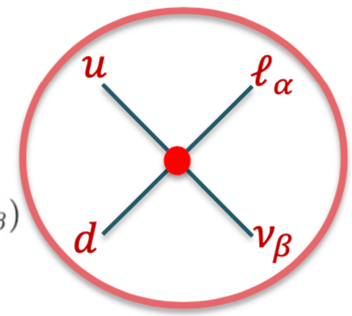


10 TeV MuC:



- CC: New left/right handed, (pseudo)scalar and tensor interactions

$$\mathcal{L}_{\rm WEFT} \supset -\frac{2V_{ud}}{v^2}\Big\{ [\mathbf{1}+\epsilon_L]_{\alpha\beta}(\bar{u}\gamma^\mu P_L d)(\bar{\ell}_\alpha\gamma_\mu P_L\nu_\beta) + [\epsilon_R]_{\alpha\beta}(\bar{u}\gamma^\mu P_R d)(\bar{\ell}_\alpha\gamma_\mu P_L\nu_\beta) + \frac{1}{2}[\epsilon_S]_{\alpha\beta}(\bar{u}d)(\bar{\ell}_\alpha P_L\nu_\beta) - \frac{1}{2}[\epsilon_P]_{\alpha\beta}(\bar{u}\gamma_5 d)(\bar{\ell}_\alpha P_L\nu_\beta) + \frac{1}{4}[\hat{\epsilon}_T]_{\alpha\beta}(\bar{u}\sigma^{\mu\nu}P_L d)(\bar{\ell}_\alpha\sigma_{\mu\nu}P_L\nu_\beta) + \text{h.c.}\Big\}$$



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Art work by Z. Tabrizi

A 10 TeV Muon Collider could:

- Study the microscopic nature of the Higgs boson as the most exotic state of matter in Nature.
- Testing unverified predictions of the SM.
- Explore the last vestiges of WIMP dark matter.
- Observe a new regime of quantum field theories.
- Strong synergies with the neutrino frontier.

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Standard Model is our no-lose theorem for Muon Collider!