

Muon Collider: Proton Driver

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About ODU and me

- Old Dominion University (Norfolk, VA) is presently one of three US universities with a fully signed IMCC MoC
 - Our interests are in the MC Accelerator R&D: beam dynamics, cooling, SRF,...
 - Graduate student engagement through our DOE-funded accelerator traineeship program (VITA)
- I am presently at Jefferson Lab (EIC Principal Accelerator Scientist) and a Jefferson Lab professor at ODU
 - JLab is already collaborating with IMCC and was an important part of MAP; preparing to play a key role in a future US MC program (after the upcoming P5 report)



Acknowledgements

- Many thanks to Mark Palmer (BNL) and Natalia Milos (ESS) for providing materials from previous (MAP) and on-going design studies (IMCC)
- Materials used in this talk:
 - “The Future Prospects of Muon Colliders and Neutrino Factories”, M. Boscolo, J.-P. Delahaye and M. Palmer, RAST 10, 189-214 (2019)
 - “Proton driver scenarios at CERN and Rutherford Appleton Laboratory”, J. W. G. Thomason, R. Garoby, S. Gilardoni, L. J. Jenner, and J. Pasternak, PRST AB 16, 054801 (2013)
 - MuCol EU Kick-off meeting, <https://indico.cern.ch/event/1219912/> , Mar 28, 2023
 - MAP 2014 Spring Meeting, <https://indico.fnal.gov/event/8326/>

Introduction

- Several detailed studies have looked at MC Proton Drivers in the past.
 - Concepts based on SPL, Project X, ESS, PIP-II

Table 3. Main parameters of the various phases of an MC as developed by the MAP effort.

Parameter	Units	Higgs	Top-high resolution	Top-high luminosity	Multi-TeV		
CoM energy	TeV	0.126	0.35	0.35	1.5	3.0	6.0*
Avg. luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.008	0.07	0.6	1.25	4.4	12
Beam energy spread	%	0.004	0.01	0.1	0.1	0.1	0.1
Higgs production/ 10^7 sec		13,500	7000	60,000	37,500	200,000	820,000
Circumference	km	0.3	0.7	0.7	2.5	4.5	6
Ring depth [1]	m	135	135	135	135	135	540
No. of IPs		1	1	1	2	2	2
Repetition rate	Hz	15	15	15	15	12	6
$\beta_{x,y}^*$	cm	1.7	1.5	0.5	1 (0.5–2)	0.5 (0.3–3)	0.25
No. muons/bunch	10^{12}	4	4	3	2	2	2
Norm. trans. emittance, ε_T	π mm-rad	0.2	0.2	0.05	0.025	0.025	0.025
Norm. long. emittance, ε_L	π mm-rad	1.5	1.5	10	70	70	70
Bunch length, σ_s	cm	6.3	0.9	0.5	1	0.5	0.2
Proton driver power	MW	4	4	4	4	4	1.6
Wall plug power	MW	200	203	203	216	230	270

*Accounts for off-site neutrino radiation

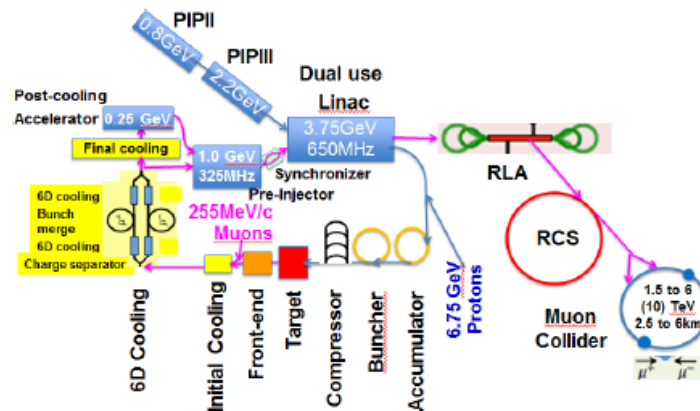


Fig. 13. Layout of a muon-based multi-TeV MC.

TABLE I. Proton-driver requirements. A proton kinetic energy in the range 5 to 15 GeV has been shown to provide adequate performance. The number of protons, beam radius, β^* , and geometric emittance correspond to the values for an 8 GeV proton beam.

Parameter	Value
Kinetic energy	5–15 GeV
Average beam power	4 MW (3.125×10^{15} protons/s)
Repetition rate	50 Hz
Bunches per train	3
Total time for bunches	240 μ s
Bunch length (rms)	1–3 ns
Beam radius	1.2 mm (rms)
Rms geometric emittance	$< 5 \mu$ m
β^* at target	≥ 30 cm

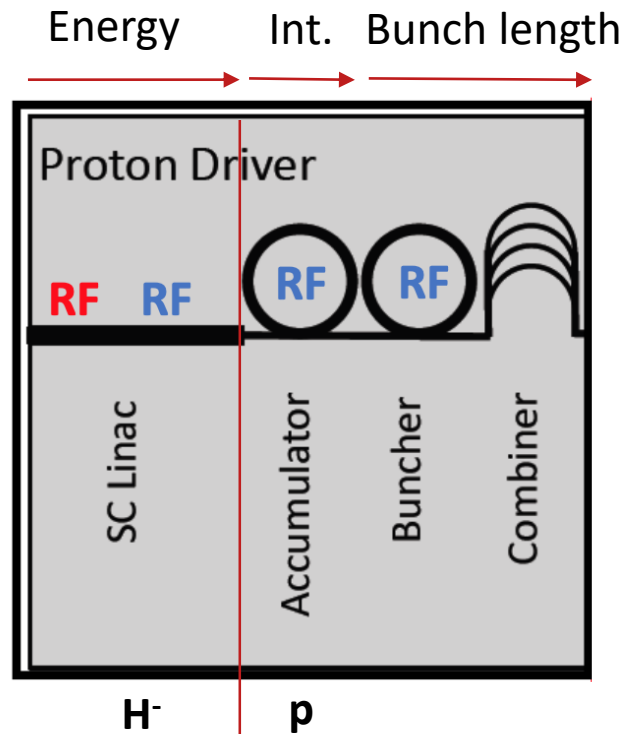
TABLE II. Parameters of the accumulator and compressor rings for the CERN proton-driver scenario.

Parameter	Value
Accumulator ring	
Circumference	185 m
No. of turns for accumulation	640
Working point (H/V)	7.37/5.77
Total bunch length	120 ns
rms momentum spread	0.863×10^{-3}
Compressor ring	
Circumference	200 m
No. of turns for compression	86
rf voltage	1.7 MV
Gamma transition	2.83
Working point	4.21/2.74

Proton Driver: Essential Elements

H⁻ source and accumulator and combiner complex
10¹⁴-10¹⁵ protons in ns-long bunch

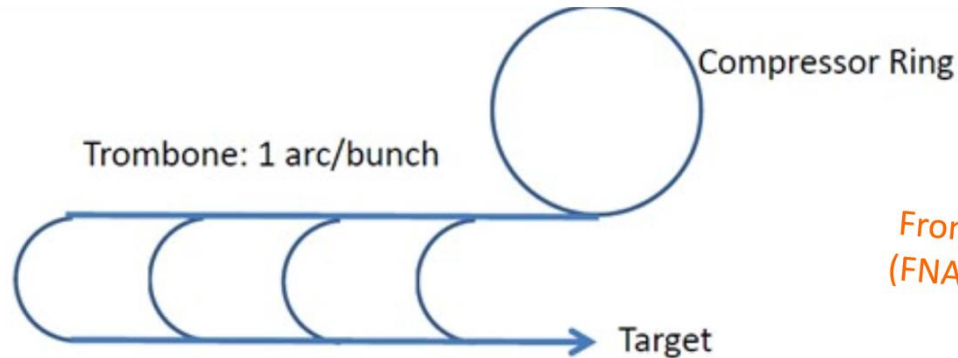
The concept is based on a Muon Collider with single (mu⁺ and mu⁻) colliding bunches



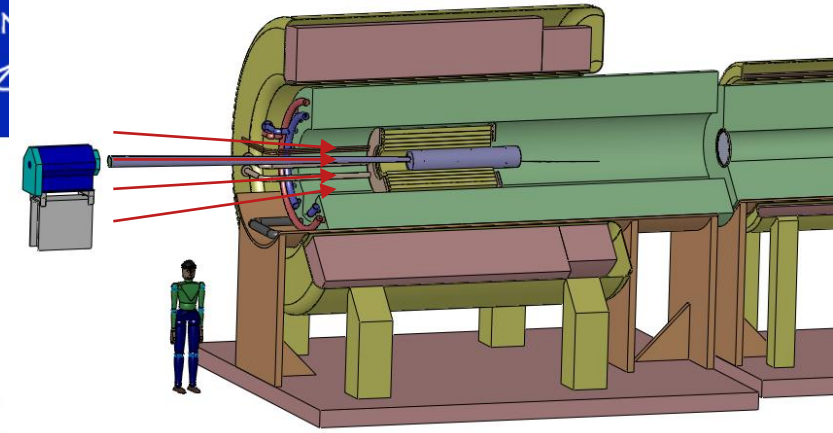
- H⁻ source → high intensity
- ~10 GeV → Superconducting Linac (similar to SNS, ESS)
- Accumulator
- Buncher/Compressor
- Combiner → beam-to-target delivery system
- **Challenge:**
High intensity short bunches @ low rep. rate

Proton Driver Proposals

FNAL MAP with 8 GeV H- Linac with Accumulator and Compressor Rings



From DOE Review of MAP
(FNAL, August 29-31, 2012)



Muon Collider Proton Driver Trombone Schematic

(not to scale; bunches arrive simultaneously on target)

- Different version of accumulator & compressor rings designed by different people
 - Accumulator with moderate RF voltage and far from transition
 - Compressor with large (120 kV) RF voltage close to transition to generate short bunches
- Combiner after extraction out of compressor ring
 - Combination of four bunches extracted from compressor to one bunch on target
 - ◆ Different path lengths such that bunches arrive simultaneously
 - ◆ Different incidence angles for different bunches
 - (Scheme useful to adopt any neutrino factory proton driver to muon collider)

C. Carli

Motivation

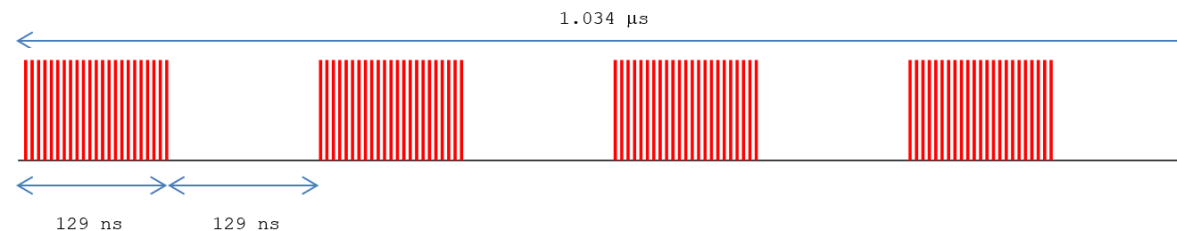
D. Neuffer proposed a two-ring scenario: one for accumulation with sufficiently large slippage factor η to increase the microwave instability threshold, the other for bunch compression with small $|\eta|$ to reduce the required RF voltage

Parameters	AR	CR
Circumference, m	308.23	308.23
Momentum compaction	-0.052	0.001
Slippage factor	-0.063	-0.01
RF frequency, MHz	3.87	3.87
RF voltage, kV	10	240
Synchrotron tune	$2.1 \cdot 10^{-4}$	$4.2 \cdot 10^{-4}$
Peak current, A	100	1040
Final r.m.s. bunch length, ns	29.2	3.2
Final r.m.s. energy spread	$5.2 \cdot 10^{-4}$	$6.9 \cdot 10^{-3}$
Threshold impedance, Ohm	20	3 \rightarrow 53
R.m.s. emittance, μm	5	5
Space charge tunes, h/v	0.02/0.02	0.14/0.16
Betatron tunes, h/v	7.94/6.91	6.76/8.44

Two major problems with Accumulator/Compressor rings - space-charge and microwave instability - can be mitigated with the Flexible Momentum Compaction (FMC) lattice design:

- Large (and negative) momentum compaction factor α_c increases the microwave instability threshold
- Large dispersion (characteristic to FMC lattices) reduces the space-charge tunes

Micro-structure of "pre-chopped" injected beam for 4 bunches :



Present IMCC Baseline parameters



- Beam Power: 2 MW
- Rep. rate: 5 Hz
- Beam spot size: ~ 5 mm (1σ)
- Bunch length: 2 ns (rms)
- Beam Energy: 5 and 10 GeV
- Linac + 2 rings (initial design)

This talk

- Beam Power: 2 MW
- Rep. rate: **10 Hz**
- Beam spot size: ~ 5 mm (1σ)
- Bunch length: 2 ns = 0.6 m (rms)
- Beam Energy: **8 GeV**
- Linac + 2 rings (initial design)
 - **Combine 4 bunches on target**

What's important?

- Accumulator (accumulates 4 proton bunches):

$$P = 4N_b q E f_0 = 2 \text{ MW}$$

- Stripping injection and painting
- Injection-related beam losses
- Instabilities
 - Landau damping and feed-backs
- Extraction kicker and septum magnet

- Buncher (rotates bunches by 90-degrees in the long phase-space):

- Space-charge effects
- Large energy spread (~1% rms)
- Instabilities
 - Landau damping and feed-backs
- Extraction kicker and septum magnet

$$\delta v \approx - \frac{3N_b r_p}{2\pi\beta\gamma^2 \varepsilon_{n,rms}} \frac{C}{\sqrt{2\pi}\sigma_s} = - \frac{3r_p P}{4\sqrt{(2\pi)^3 \beta\gamma^2 \sigma_s q E f_0} \varepsilon_{n,rms}} \frac{C}{\varepsilon_{n,rms}}$$

$\approx 2 \times 10^{-7}$???

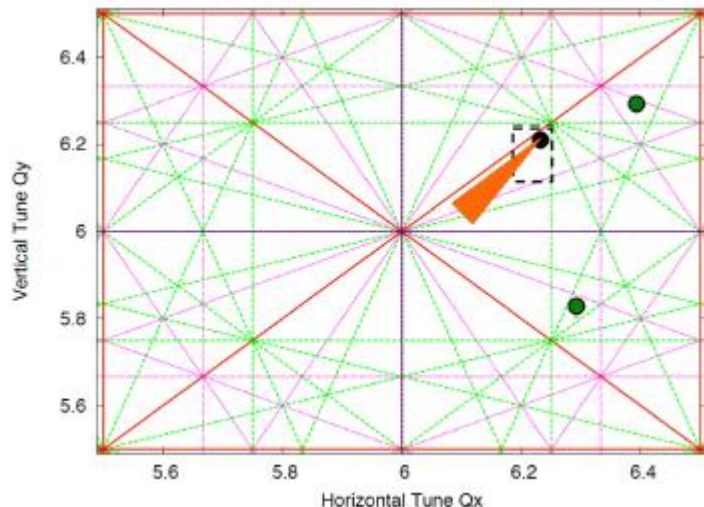
$$\delta v \approx -0.2 \quad \text{-- Conservative approach}$$

Tension: larger beam emittance makes magnets, kickers, rf systems more expensive, a shorter circumference, C, leads to superconducting magnets (also more expensive)

SNS ring experience

- SNS ring: 1.2 GeV, 1.4e14 at 60 Hz → 1.5 MW
- Single bunch ~1 us long
- Emittance (rms, norm): ~60 μm
 - Painting (non-gaussian)
- Fixed energy, storage for ~1000 turns (1 ms)
- Beam losses are acceptable for operations
 - Fully controlled by collimators
 - Relatively small space-charge tune shift (~0.2)

$$\delta\nu \approx -\frac{3N_b r_p B_F}{2\pi\beta\gamma^2 \epsilon_{n,rms}}$$



Feature	Cost	Payoff So Far
Large Aperture	\$\$\$\$	High ←
Injection Painting	\$\$\$	High ←
Collimation	\$\$\$	High ←
TiN coating	\$\$\$	Unknown
2 nd harmonic RF	\$\$	Medium+
Main sextupoles	\$\$	Low - None
Main octupoles	\$\$	None
Sextupole correctors	\$	None
Octupole correctors	\$	None
Clearing solenoids	\$	None
Beam in gap kicker	\$	None
Clearing electrodes	\$	None

Vacuum chamber: stainless steel, 20 cm diam
 Large aperture → high cost of magnets and other devices.

Courtesy of S. Cousineau (SNS)

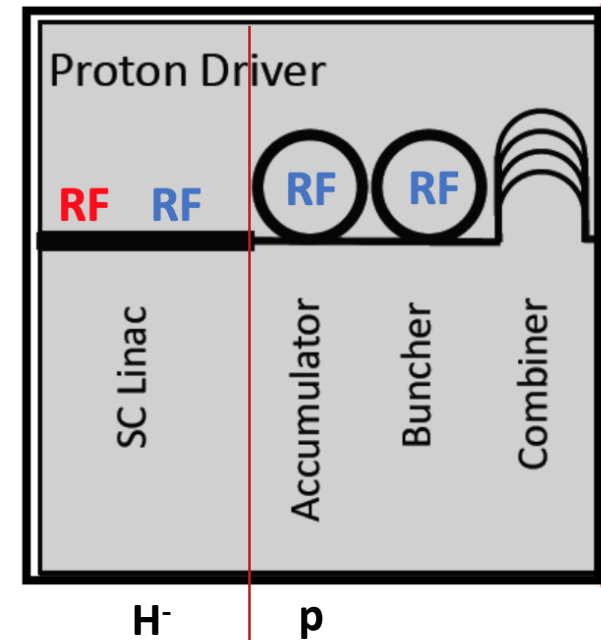
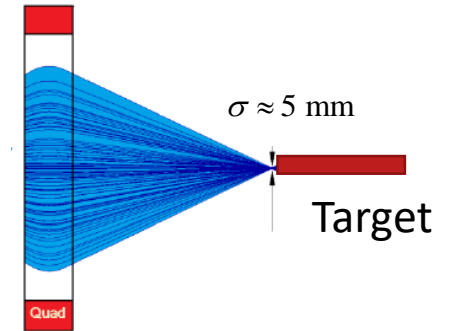
Start from **beam-on-target** considerations and proceed upstream

- Assume beta-function β_T on target: ~ 1 m
 - Combiner must accommodate large energy spread (~ 1 %)
- Assume a gaussian transverse beam distribution:

$$\varepsilon_{n,rms} = \frac{\beta_T \sigma^2}{\beta_T} \approx 240 \mu\text{m}$$

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- This emittance is about 100 greater than the present Booster emittance
- We will assume that there are 4 proton bunches in the Buncher ring
 - These bunches are extracted in one turn and are combined on the target
- Beam intensity for 2 MW at 10 Hz (4 bunches)

$$N_T \approx 1.6 \times 10^{14} \quad \text{or} \quad N_b \approx 0.4 \times 10^{14} \quad \text{per bunch}$$



Discussion about beam emittance

- Large emittance means large beam size and, thus, a large vacuum chamber and magnets

$$\sigma_x = \sqrt{\frac{\beta_x \varepsilon_{n,rms}}{\beta\gamma} + \left(D_x \frac{\delta p}{p} \right)^2}$$

- Using SNS ($\beta\gamma \approx 1.8$) as our example (vacuum chamber diam 20 cm), we should limit the MC Proton Driver emittance to

$$\varepsilon_{n,rms} \approx 100 \mu\text{m}$$

Space-charge tune shift

- SC tune shift $\delta\nu \approx -2 \times 10^{-7} \frac{C}{\mathcal{E}_{n,rms}}$ (this expression ignores the dispersive beam size)

- Emittance: $\mathcal{E}_{n,rms} \approx 100 \mu\text{m}$

- Dispersive beam size helps with reducing the effective tune shift and may be important

$$\delta\nu_x \sim \left\langle \frac{\beta_x}{\sigma_x (\sigma_x + \sigma_y)} \right\rangle_s \quad \sigma_x = \sqrt{\frac{\beta_x \mathcal{E}_{n,rms}}{\beta\gamma} + \left(D_x \frac{\delta p}{p} \right)^2}$$

- We would like to limit the SC tune shift to ~ 0.2 at extraction from the Buncher
 - This gives us $C \approx 100 \text{ m}$ -- Buncher circumference
 - Dispersion may help with space-charge but we must remember that the ring must have a large momentum acceptance ($\sim \text{few}\%$)
- Thus, our first conclusion:
 - The Buncher ring should be about 100 m in circumference with 4 bunches

Buncher ring

- Typically, in a ring, about 60% of circumference is occupied by dipole magnets
 - 100-m ring -> 60 m of dipoles for a 8.9 GeV/c beam gives the magnetic field of 3 T
- Thus, such a Buncher ring is going to be based on SC magnets with a large aperture (~20-cm) and a low-frequency rf system, likely $h = 4$ (~10 MHz)
 - Higher frequency rf may not be compatible with a large aperture (~20 cm diam)

Accumulator ring

- The main purpose of the Accumulator ring is to convert a long (~ 1 ms) linac pulse of H-ions to 4 bunches of protons in a ring
 - Bunches should be ~ 6 -m (20-ns) long (rms) with a small momentum spread ($< 1E-3$ rms) at extraction.
 - Space-charge effects are 10 times lower than the Buncher ring
- Ideally, the Accumulator ring should be the same circumference as the Buncher
 - However, this would also mean that the Accumulator would be based on 3-T SC magnets and it implies no ramping (not at 10 Hz anyway)
 - This would also mean that the Linac must be an 8-GeV linac
- Since the space-charge is 10 times smaller, one can envision room-temperature RCS-style magnets (~ 1 -T max), and the Accumulator could be a 300-m ring
 - This scenario requires a separate analysis

Accumulator ring: challenges

- H- stripping at 8-GeV (foil or laser) is only ~96-98% efficient thus we will have to deal with 40-80 kW of beam losses
 - ~3000-turn injection
 - To compare: the total Fermilab Booster beam power is ~80 kW
- Large-aperture SC curved magnets with $R = 10$ m
 - Same for the Buncher ring
- Extraction kicker for a large aperture
 - Same for the Buncher ring

Linac

- Ideally, we would want an SNS-like linac, extended to 8 GeV
 - Deliver 1.6×10^{14} protons in ~ 1 ms, or ~ 30 mA ave beam current during pulse
 - 3000-turns stripping injection
- It might be possible to adopt/adjust the PIP-II linac design but requires a detailed study
 - The present PIP-II linac current (2 mA) is too low for the MC Proton Driver

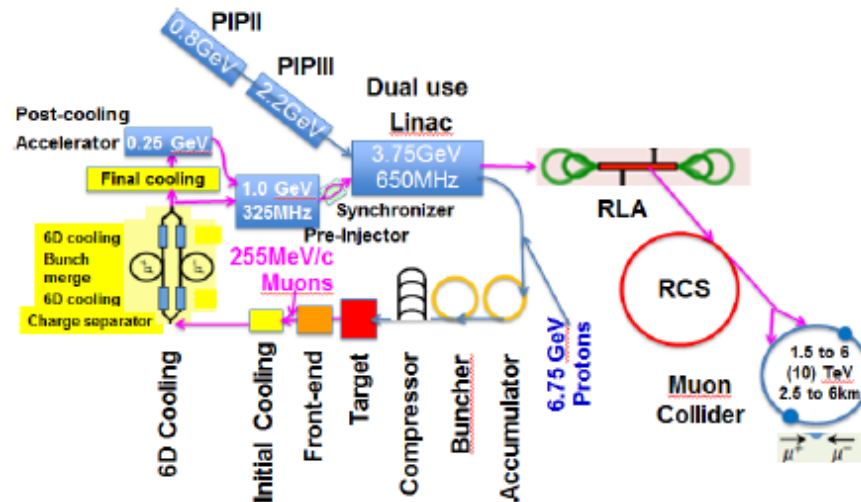


Fig. 13. Layout of a muon-based multi-TeV MC.

“The Future Prospects of Muon Colliders and Neutrino Factories”, M. Boscolo, J.-P. Delahaye and M. Palmer, RAST 10, 189-214 (2019)

Summary

- I believe it is possible (with work and resources) to design a Proton Driver, compatible with the Muon Collider requirements
- Much work has been done already by the MAP and IMCC teams
 - Much R&D is still needed and many physics challenges remain: optimal beam optics, beam dynamics, space-charge, instabilities, H⁻ injection, loss mitigation
- None of the 6 Fermilab Booster replacement options (submitted to P5 as part of ACE) are optimized for an MC design or an MC Demonstrator
 - All 6 concepts were focused largely on how to achieve 2.4 MW for DUNE
- Main ingredients for a successful design:
 - High-current ~8-GeV H⁻ linac
 - Two fixed-energy large-aperture (~100 m circumference) rings
 - Low-loss stripping injection
 - Large-aperture SC magnets (~3 T)
 - Low-frequency rf systems
 - High-field extraction septum magnets
 - High-field large-aperture extraction kickers
 - A 4-bunch combiner, delivering 4 bunches to the target