

Lepton Flavor Violation — theory

Vincenzo Cirigliano

University of Washington



INSTITUTE for
NUCLEAR THEORY

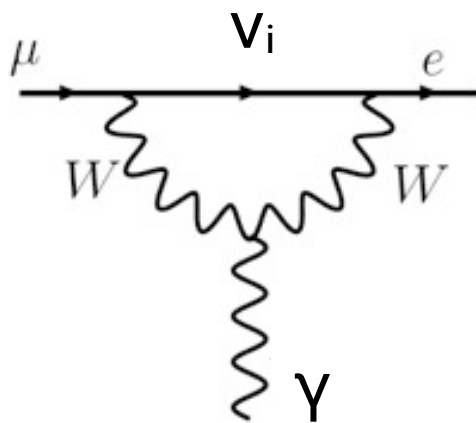
Outline

- Introduction: Lepton Flavor Violation & BSM physics
- LFV probes across energy scales
 - Reach in mass scale
 - Model-diagnosing power
- Conclusion and outlook — key opportunities in muon physics

Vast literature — apologies in advance for incomplete referencing.
Snowmass white papers are a great resource.

LFV and new physics (I)

- ν oscillations $\Rightarrow L_{e,\mu,\tau}$ not conserved
- In SM + massive ν , Charged-LFV decays suppressed to unobservable level



$$\mathcal{L}_{\nu\text{SM}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\nu\text{-mass}}$$

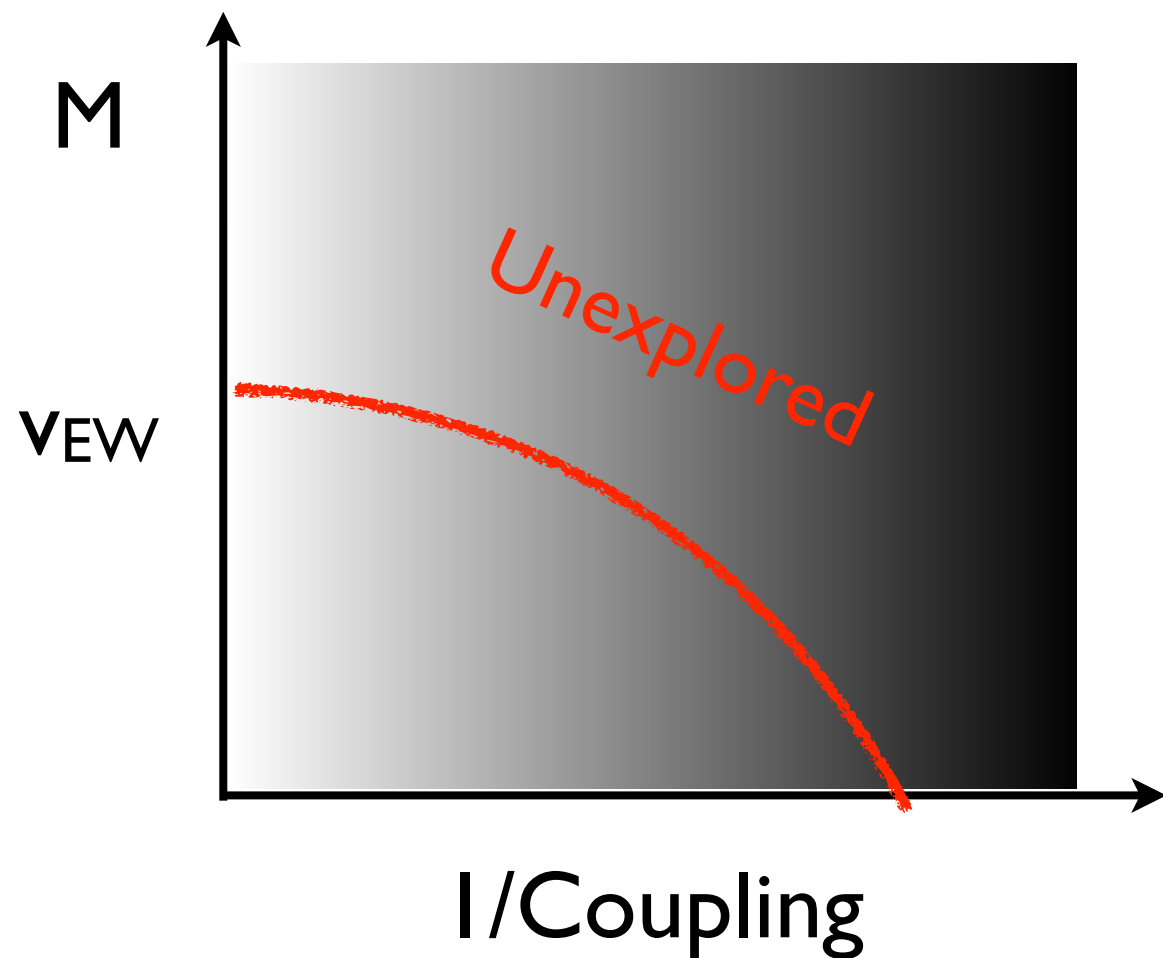
$$Br(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{M_W^2} \right|^2 < 10^{-54}$$

Petcov '77, Marciano-Sanda '77, Shrock '77...

- Observation of CLFV processes would unambiguously indicate BSM physics, related to the origin of leptonic 'flavor' & possibly neutrino mass

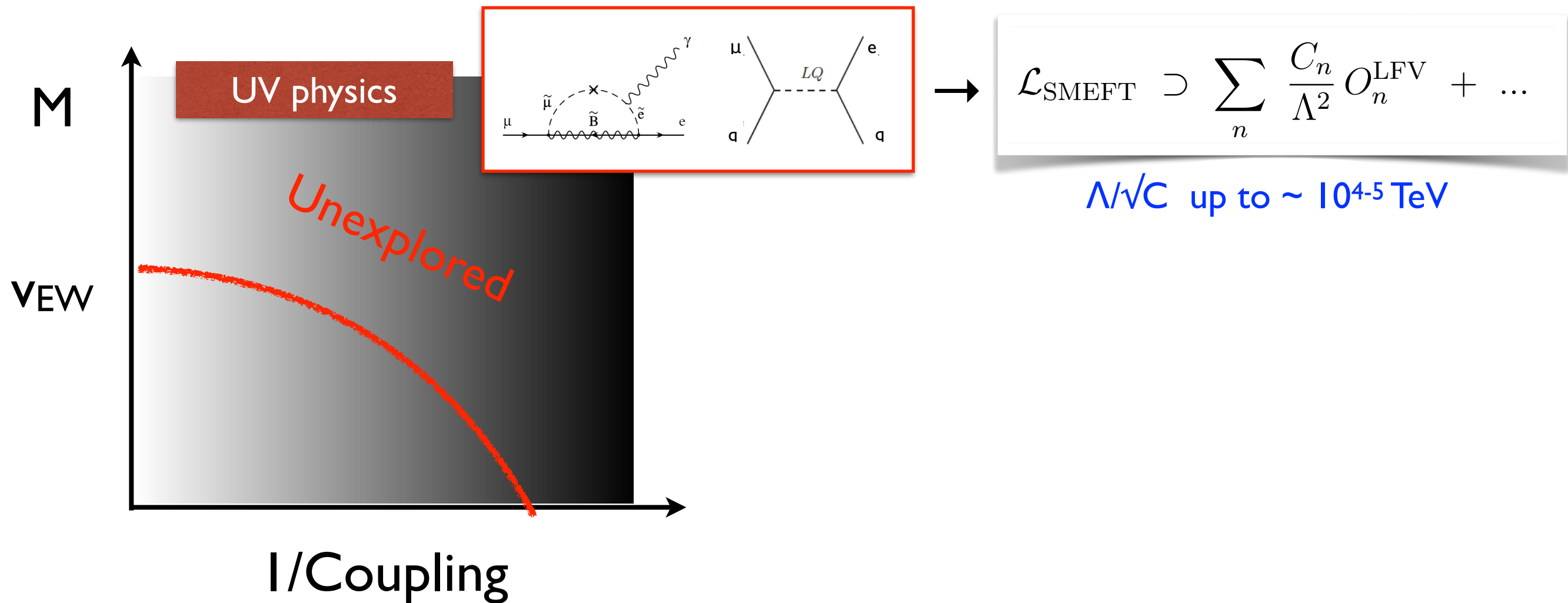
LFV and new physics (2)

- Sensitivity to broad spectrum of new physics: both heavy and light + weakly coupled



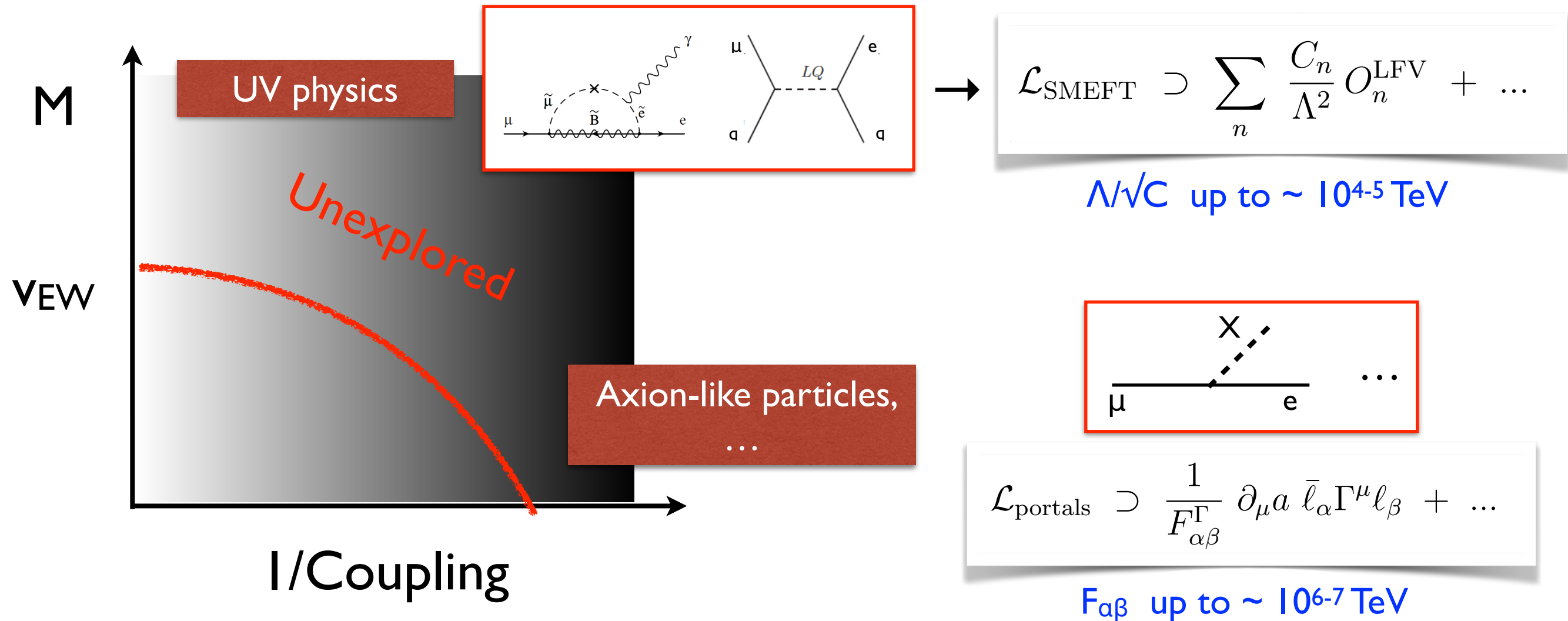
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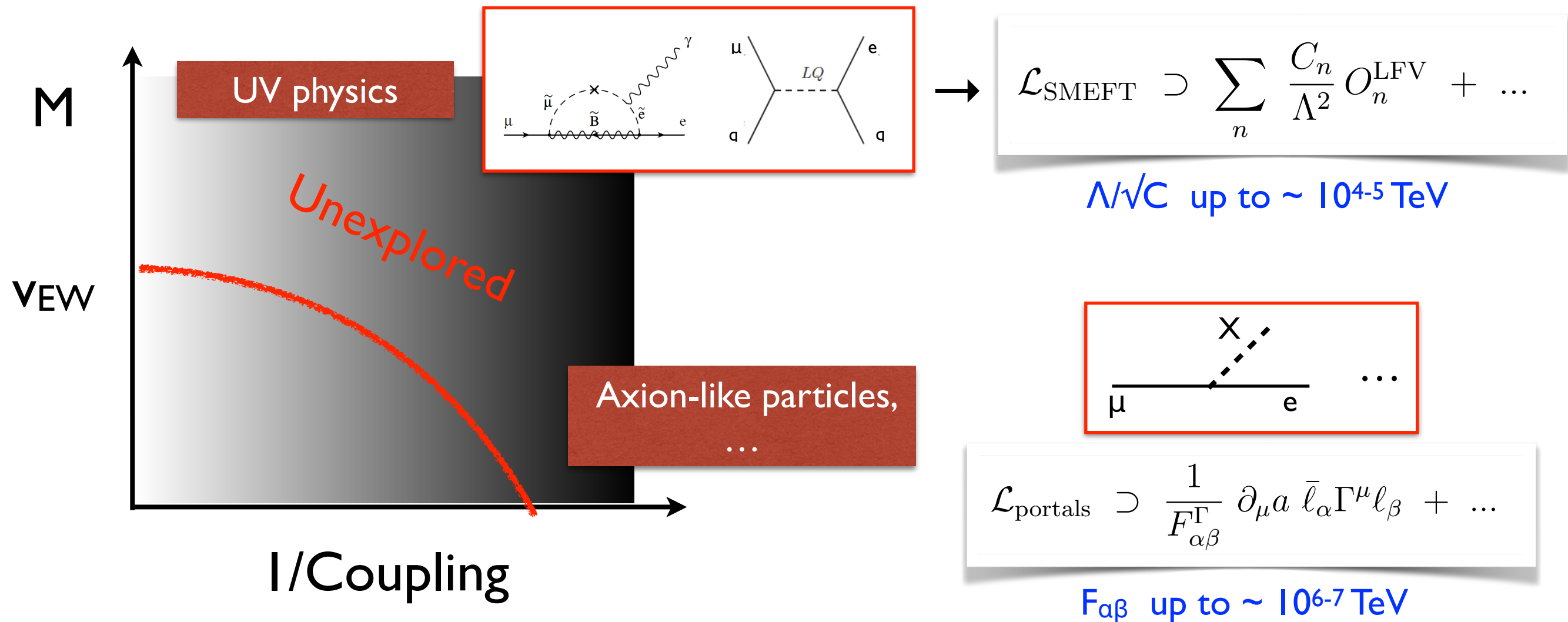
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LFV and new physics (2)

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We can probe LFV dynamics through a combination of low-energy and collider searches

LFV probes across energy scales

- Decays of μ , τ (and mesons)

($K \rightarrow \pi \mu e$; $B \rightarrow K \mu \tau, K \mu e$; $B_s \rightarrow \mu \tau, \mu e$, quarkonia, ... not discussed in detail in this talk)

$$\mu \rightarrow e \gamma, \quad \mu \rightarrow e \bar{e} e, \quad \mu(A, Z) \rightarrow e(A, Z) \quad M_\mu - \bar{M}_\mu \quad \mu \rightarrow e a$$

$$\tau \rightarrow l \gamma, \quad \tau \rightarrow l_\alpha \bar{l}_\beta l_\beta, \quad \tau \rightarrow l Y \quad Y = P, S, V, P\bar{P}, \dots$$

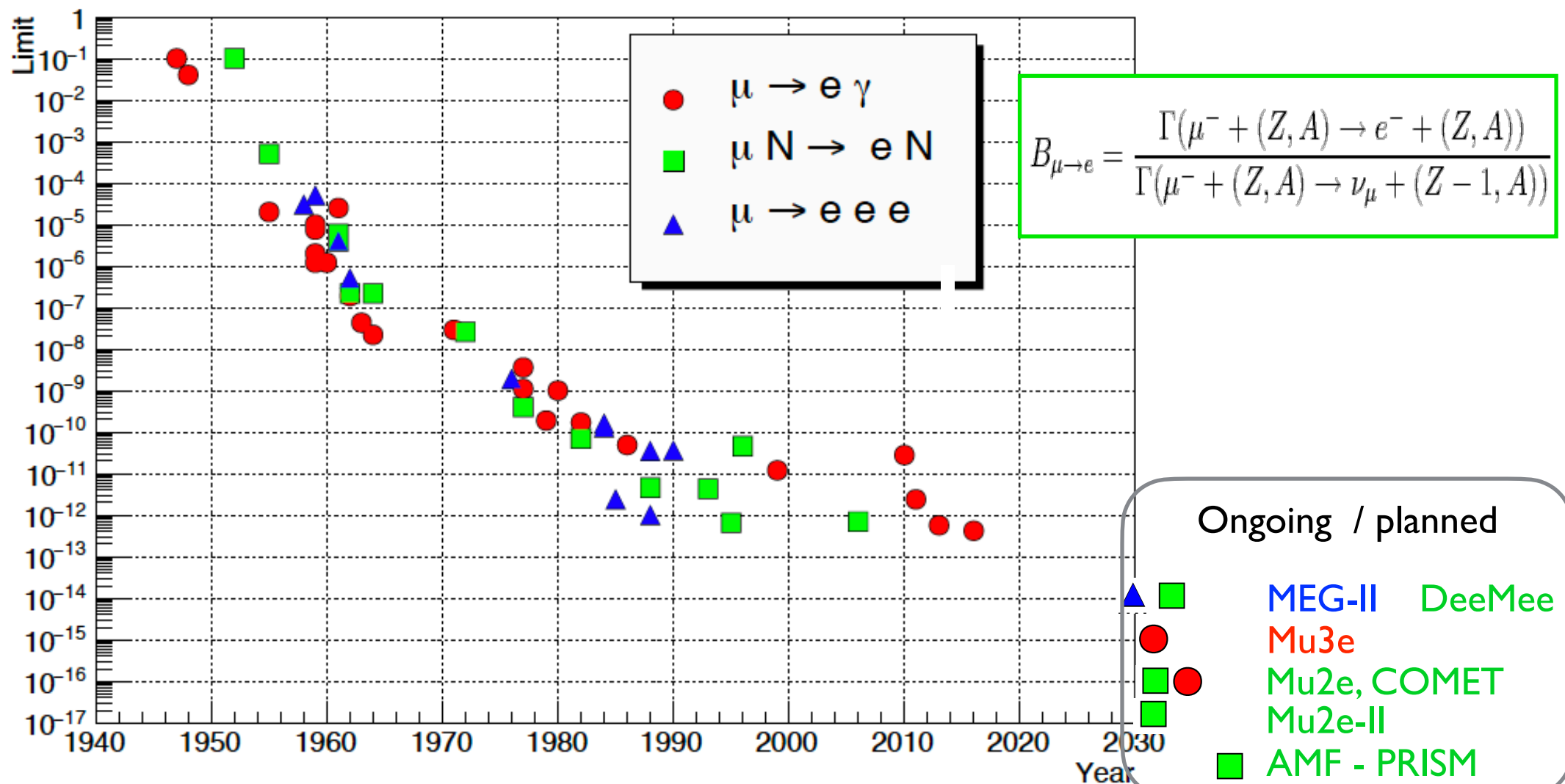
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Modified from
Calibbi-Signorelli
1709.00294

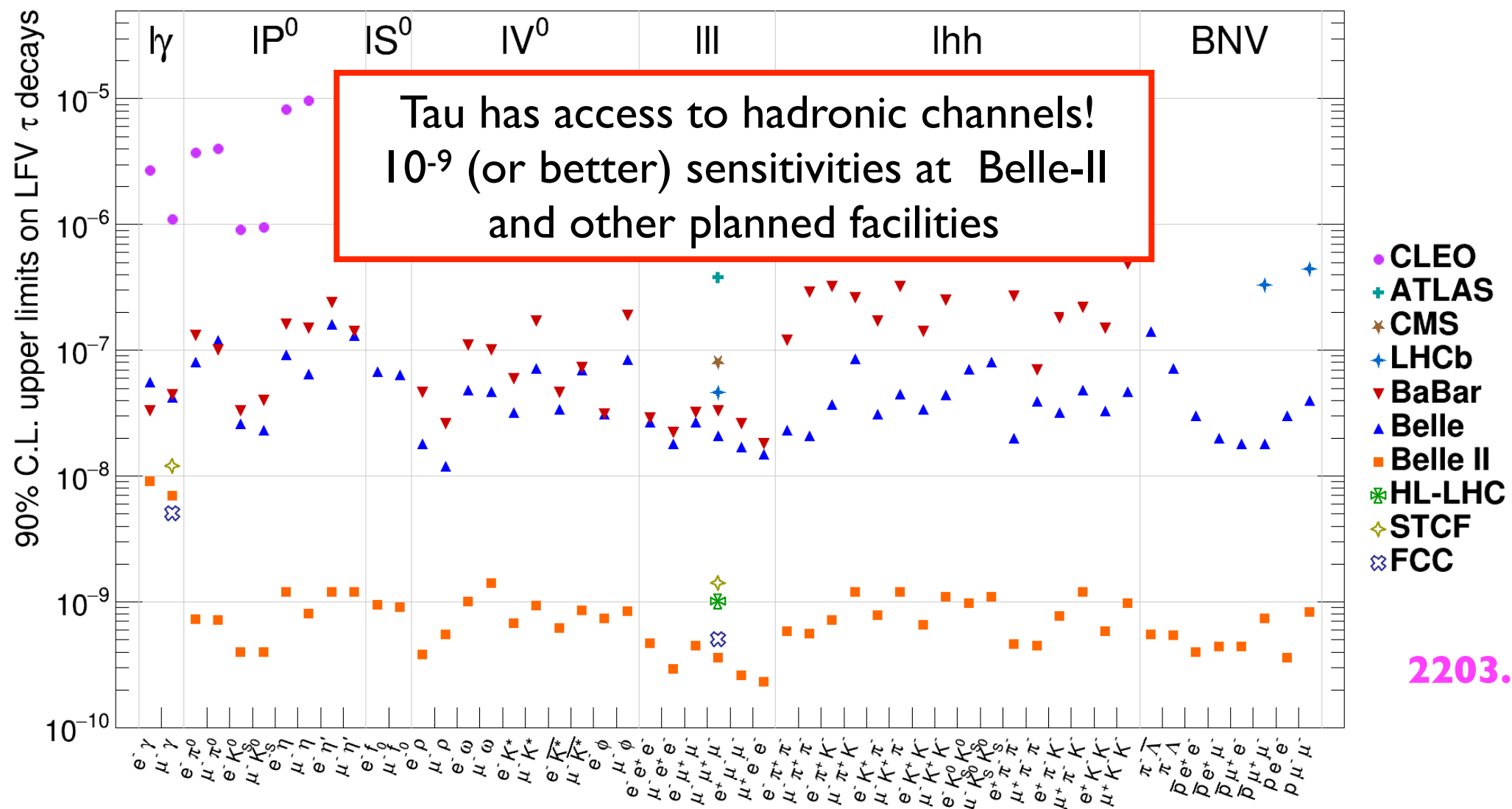
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2203.14919

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- Collider processes:

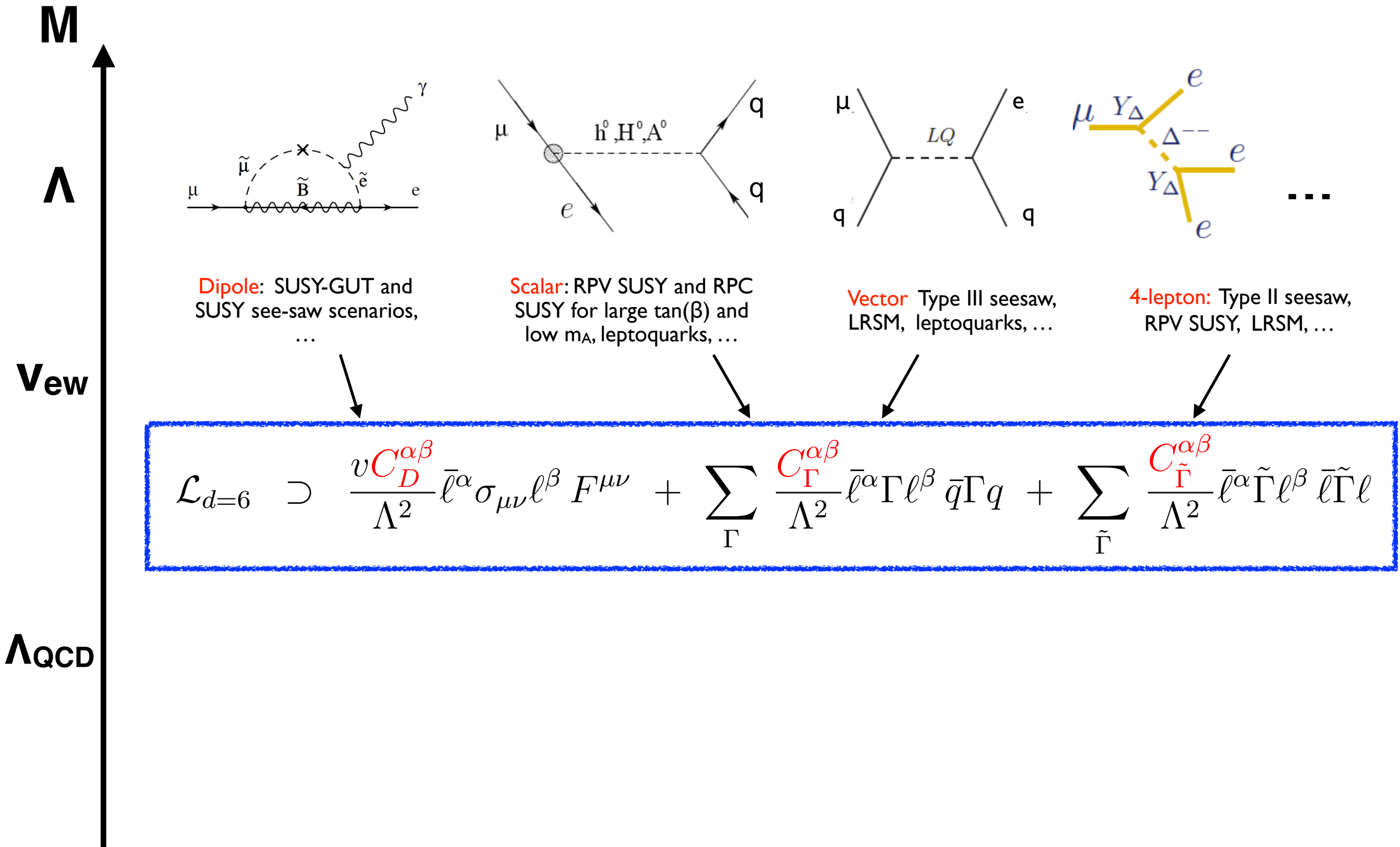
LHC

$$pp \rightarrow R \rightarrow l_\alpha \bar{l}_\beta + X \quad R = Z, h, \tilde{\nu}, \dots$$
$$pp \rightarrow l_\alpha \bar{l}_\beta + X$$

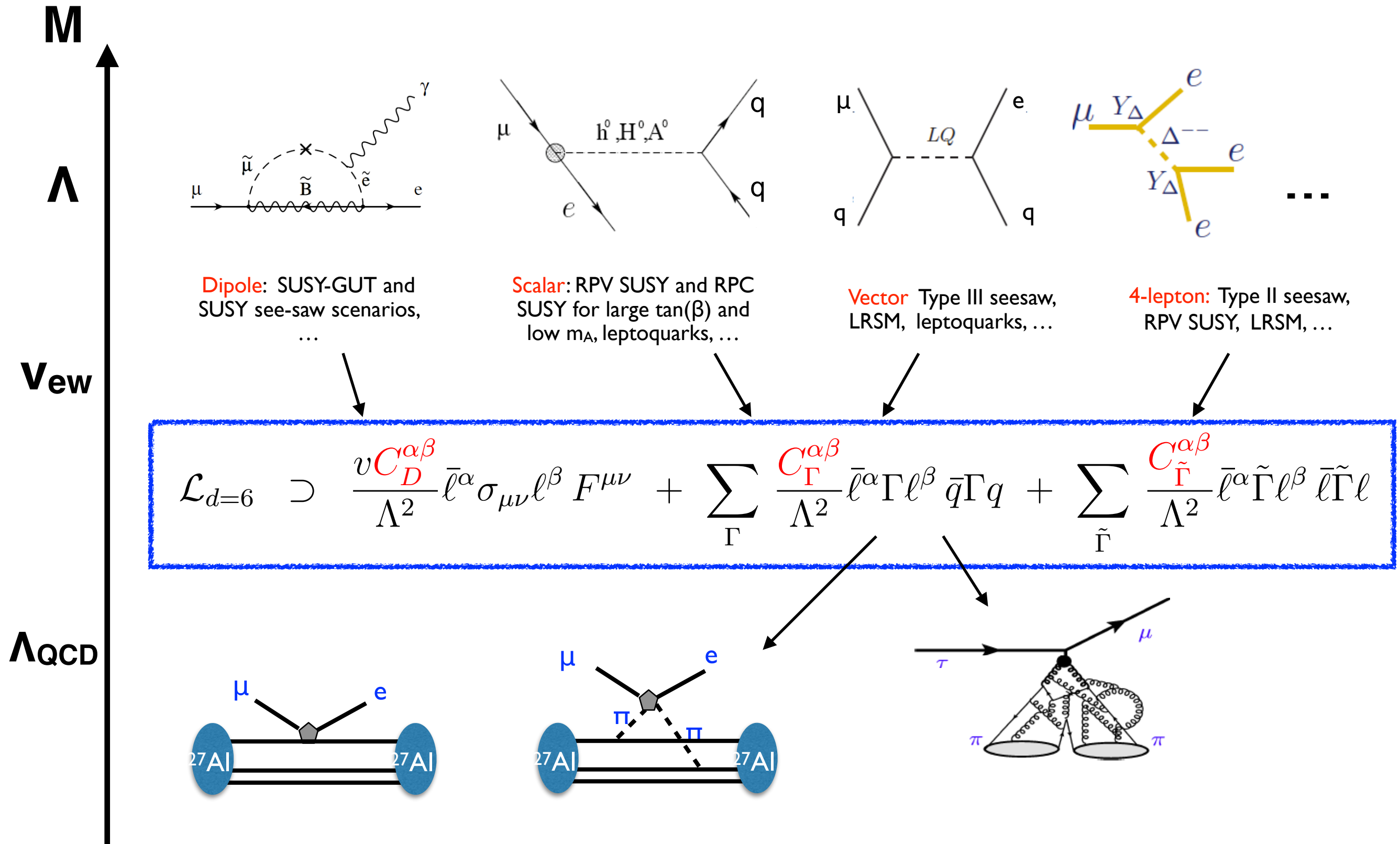
HERA,
EIC

$$ep \rightarrow l + X$$

Connecting scales with EFT



Connecting scales with EFT



CLFV phenomenology

$$\mathcal{L}_{\text{LFV}} \supset \frac{v C_D^{\alpha\beta}}{\Lambda^2} \bar{l}^\alpha \sigma_{\mu\nu} l^\beta + \sum_{\tilde{\Gamma}} \frac{C_{\tilde{\Gamma}}^{\alpha\beta}}{\Lambda^2} \bar{l}^\alpha \tilde{\Gamma} l^\beta \bar{l} \tilde{\Gamma} l + \sum_{\Gamma} \frac{C_{\Gamma}^{\alpha\beta}}{\Lambda^2} \bar{l}^\alpha \Gamma l^\beta \bar{q} \Gamma q + \frac{1}{F_{\alpha\beta}^{\Gamma}} \partial_\mu a \bar{l}^\alpha \Gamma^\mu l^\beta$$

Each model generates a specific pattern of operators

→ multiple CLFV measurements needed to extract the **underlying physics**

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→ multiple CLFV measurements needed to extract the **underlying physics**

- New physics **mass scale** through **any process**

$$\text{BR}_{\alpha \rightarrow \beta} \sim (v_{\text{ew}}/\Lambda)^4 * |(C_n)^{\alpha\beta}|^2$$

μ-e sector:	$\Lambda/\sqrt{C} \sim 10^{4-5} \text{ TeV}$	(Muon decays)
τ-μ(e) sector:	$\Lambda/\sqrt{C} \sim 10^2 \text{ TeV}$	(Tau decays)

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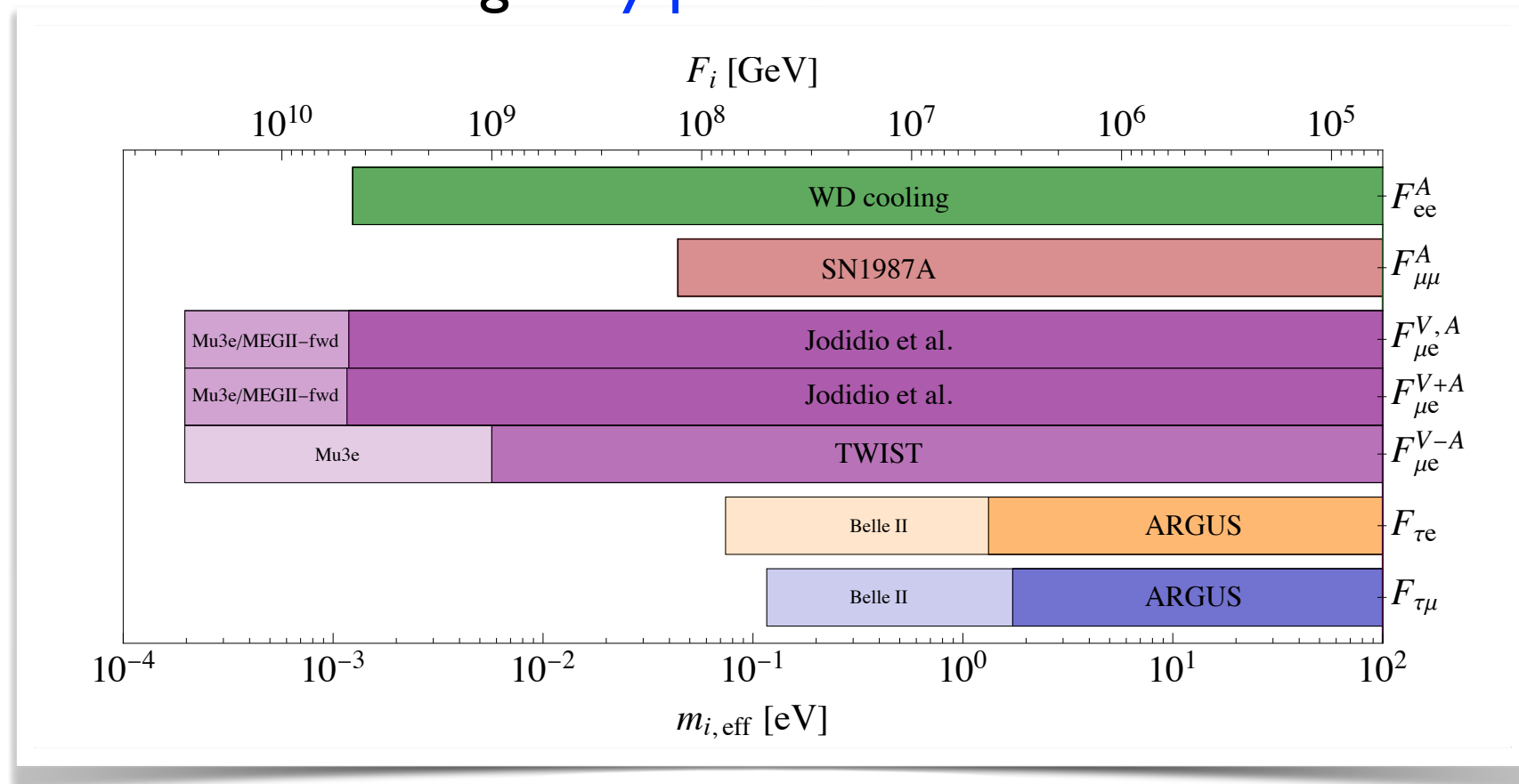
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$$\text{BR}(l_\alpha \rightarrow l_\beta a) \sim \left(\frac{v_{ew}}{(m_a F_{\alpha\beta})} \right)^2$$

Calibbi-Redigolo-
Ziegler-Zupan
2006.04795



CLFV phenomenology

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- Relative strength of operators ($[C_D]^{e\mu}$ vs $[C_S]^{e\mu} \dots$) through $\mu \rightarrow 3e$ versus $\mu \rightarrow e\gamma$ versus $\mu \rightarrow e$ conversion \Rightarrow **Mediators, mechanism**

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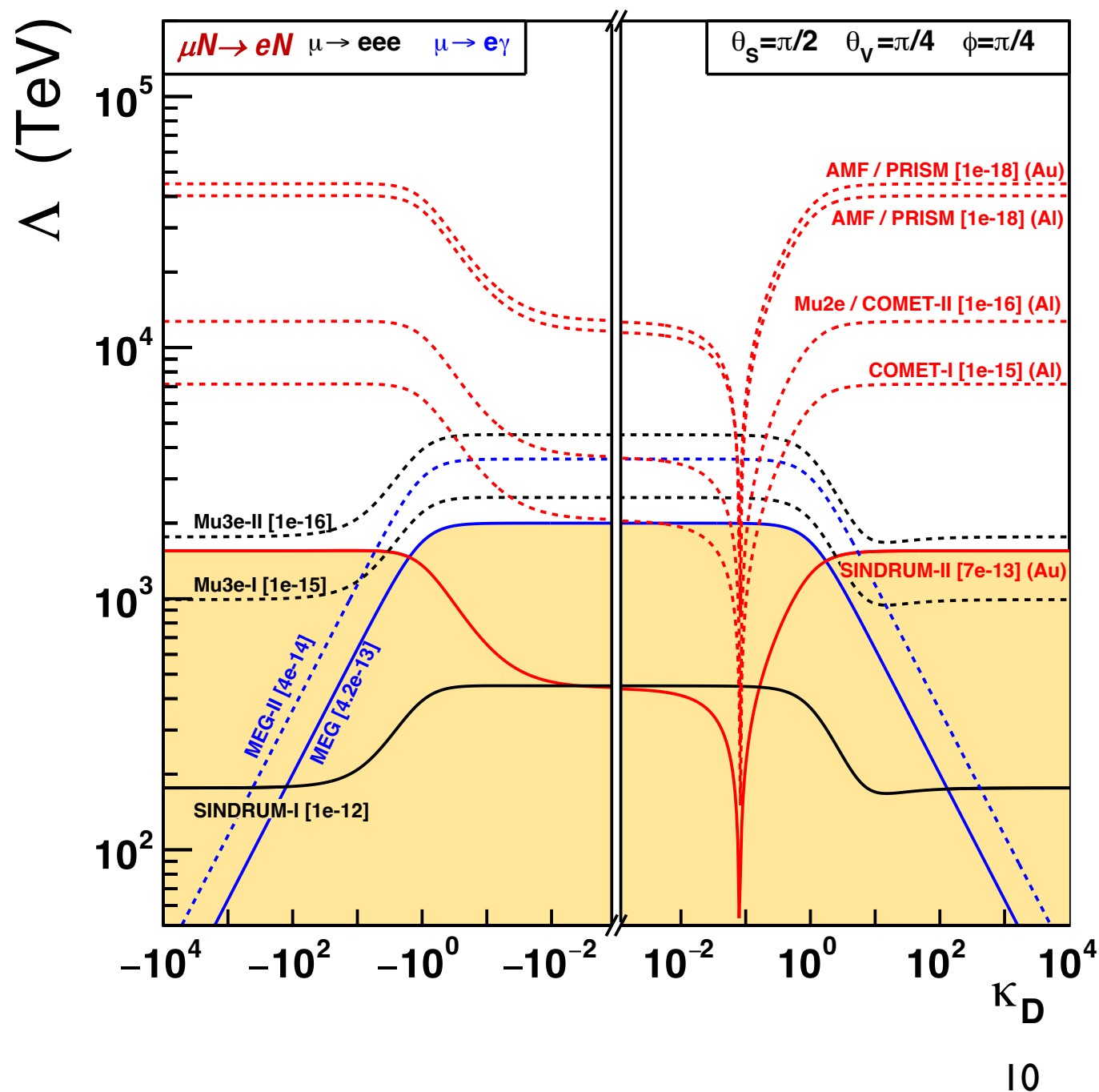
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- Flavor structure of couplings ($[C_D]^{e\mu}$ vs $[C_D]^{\tau\mu} \dots$) through $\mu \rightarrow e$ versus $\tau \rightarrow \mu$ versus $\tau \rightarrow e \Rightarrow$ **Sources of flavor breaking**

μ -e sector: mass reach

- Sensitivity is dominated by low-energy muon decay / conversion

Davidson-Echenard 2204.00564



$$\kappa_D = \cotan(\theta_D - \pi/2)$$

κ_D : relative strength of dipole vs four-fermion operators (inspired from the "κ parameterization" in 1303.0497)

$|\kappa_D| \ll 1$ dipole dominant

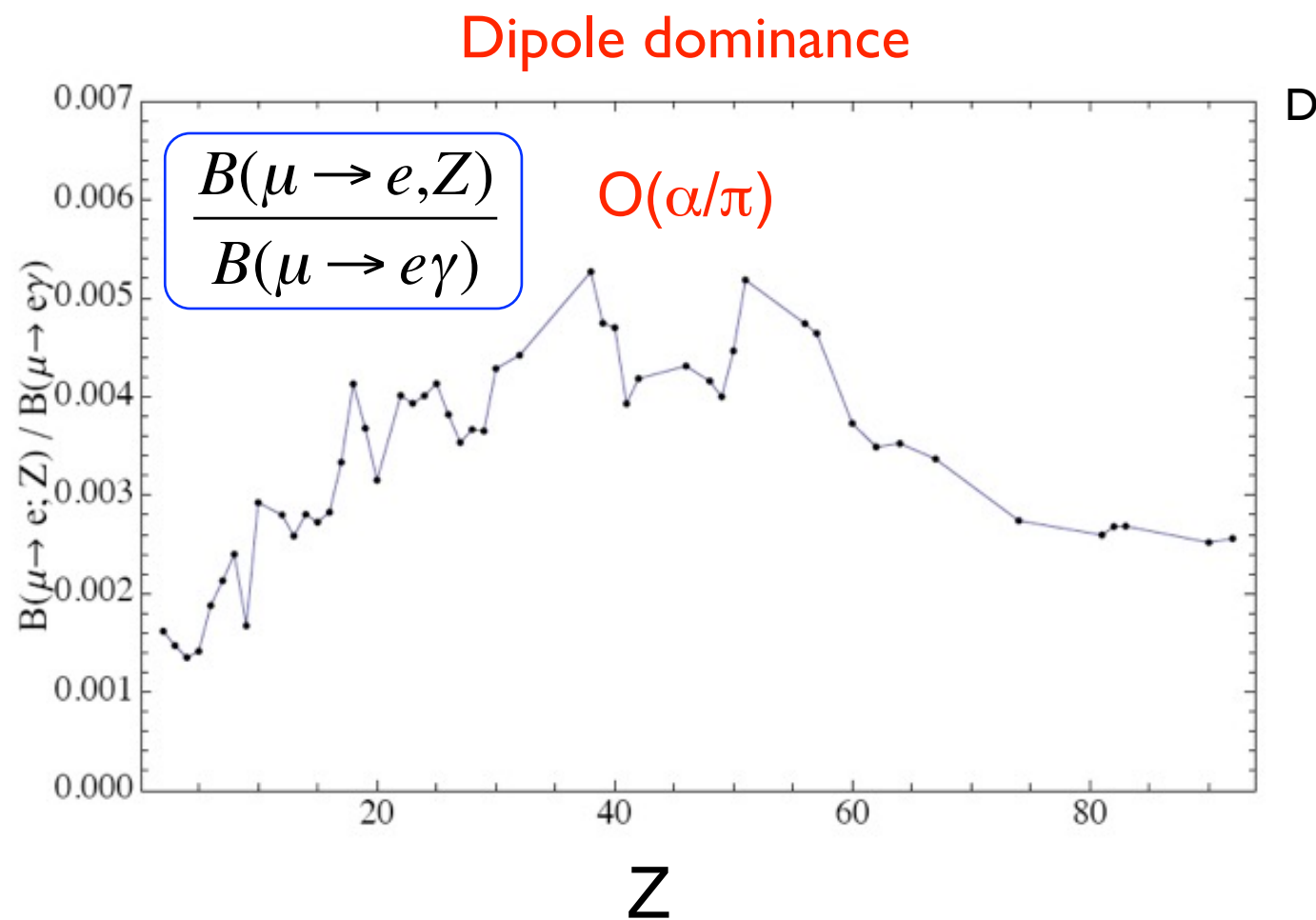
$|\kappa_D| \gg 1$ four-fermion dominant

- Very high scale probed!
Discovery opportunities in current and planned searches
- Notion of 'best probe' is model-dependent

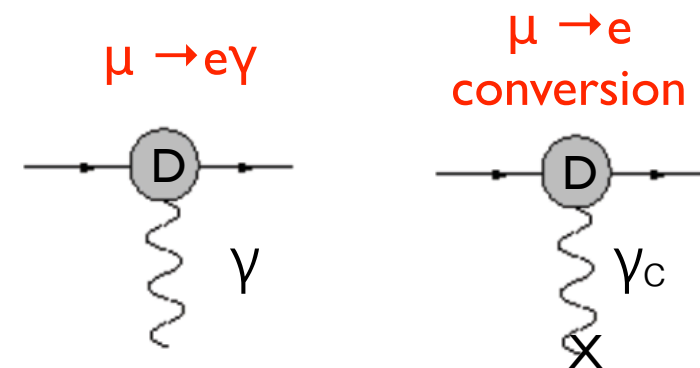
μ -e sector: diagnosing tools (I)

- Extract info on effective couplings from pattern of BRs:

$\mu \rightarrow e$ vs $\mu \rightarrow e\gamma$



D



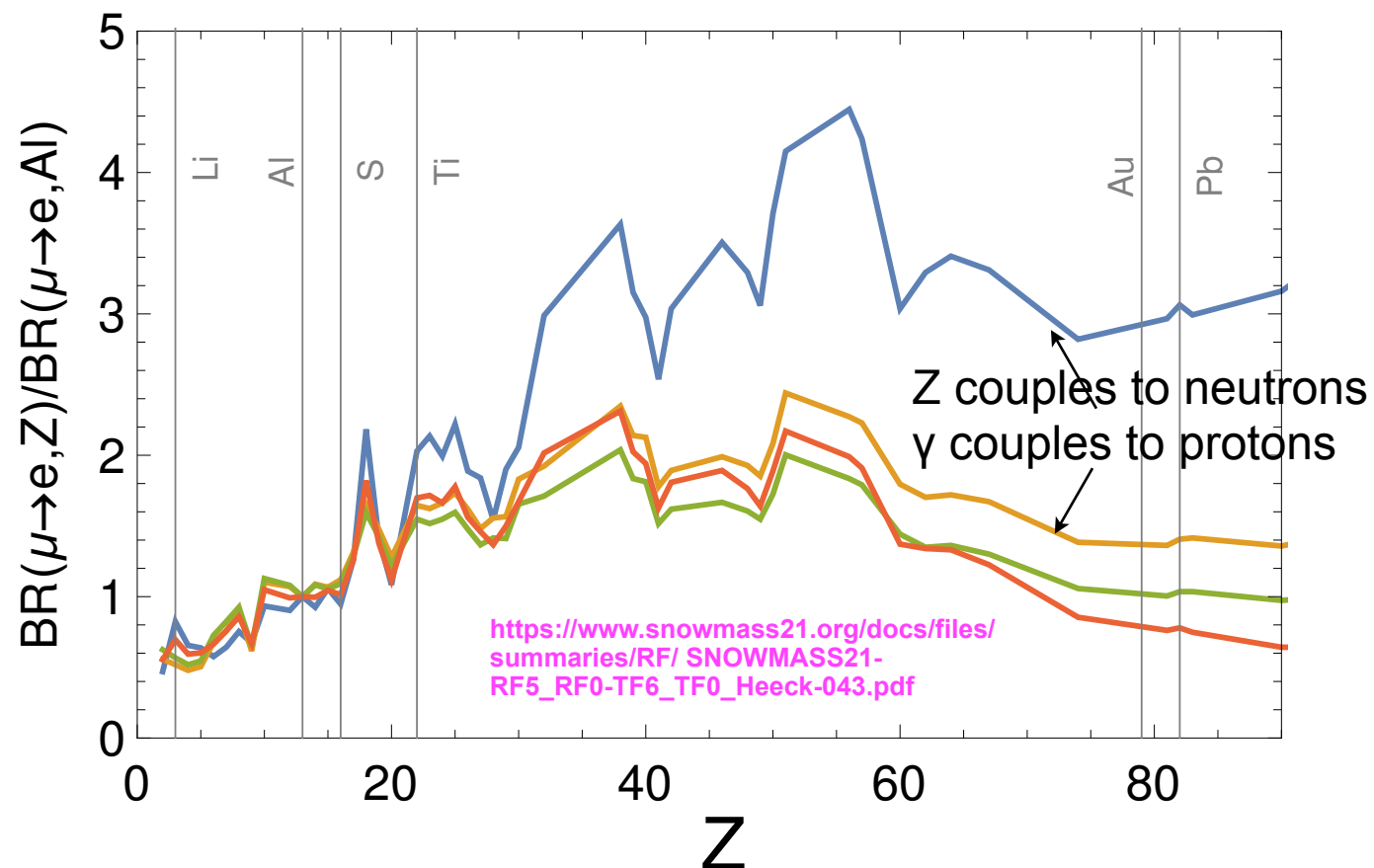
- Pattern controlled by
 - Behavior of overlap integrals
 - Total capture rate

Kitano-Koike-Okada [hep-ph/0203110](https://arxiv.org/abs/hep-ph/0203110), VC-Kitano-Okada-Tuzon 0904.0957, ...

μ -e sector: diagnosing tools (2)

- Extract info on effective couplings from pattern of BRs:
target-dependence of $\mu \rightarrow e$ conversion

— Z Penguin — Charge Radius — Dipole — Scalar



- Model diagnosing requires:

~5% measurement of Ti/Al
~20% measurement of Au/Al

- Ideal world: use Al and a large-Z target

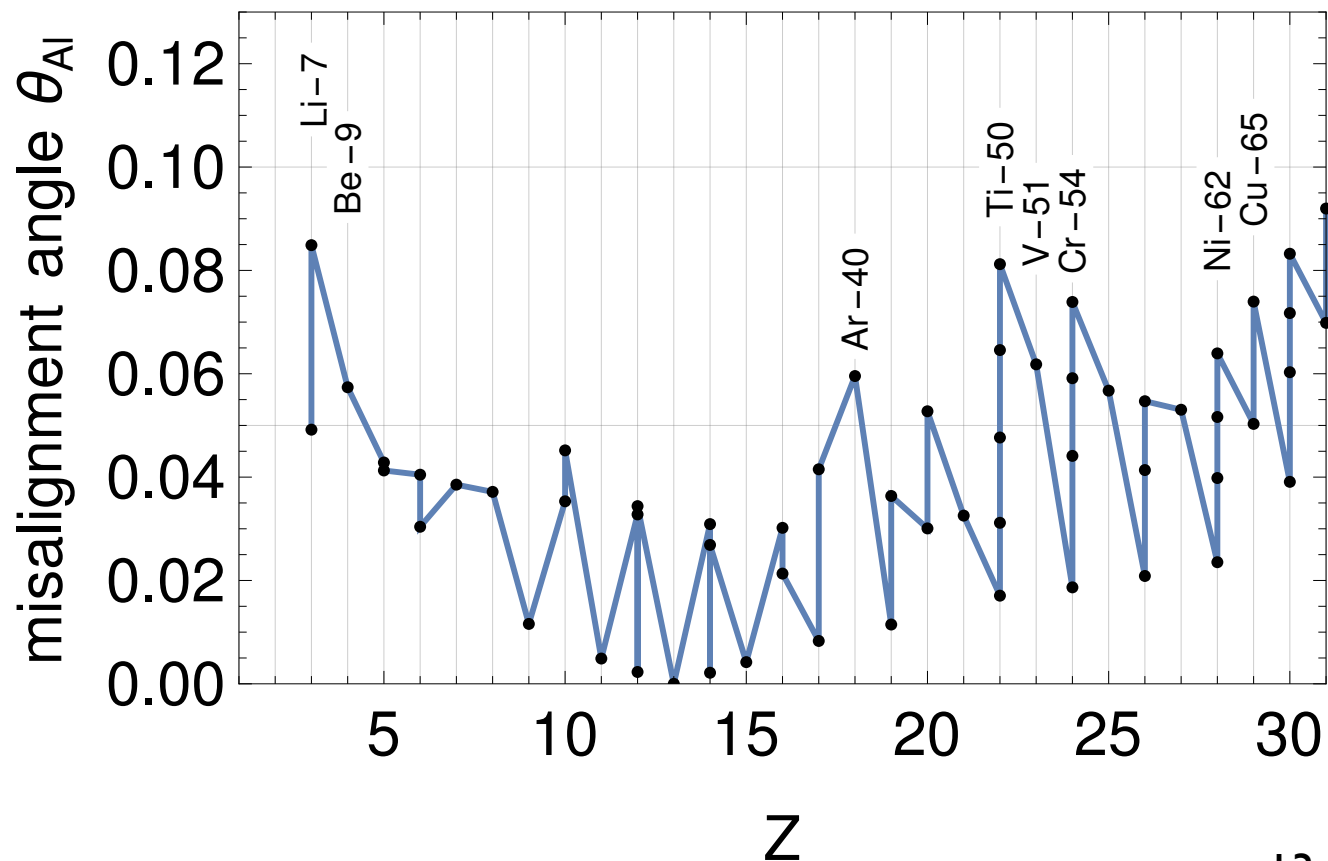
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μ -e sector: diagnosing tools (2)

- Extract info on effective couplings from pattern of BRs:
target-dependence of $\mu \rightarrow e$ conversion
- Conversion rate characterized by a target-dependent ‘vector’ of amplitudes

$$R_{\mu e} = \frac{32G_F^2}{\Gamma_{\text{capture}}} \left[|\vec{v} \cdot \vec{C}_L|^2 + |\vec{v} \cdot \vec{C}_R|^2 \right] \quad \vec{v} \equiv \left(\frac{D}{4}, V^{(p)}, S^{(p)}, V^{(n)}, S^{(n)} \right)$$

Heek-Szafron-Uesaka 2203.00702, ...



- Misalignment angle among targets quantifies the ‘complementarity’

$$\theta_{A1} = \arccos \left(\frac{\vec{v} \cdot \vec{v}_{A1}}{|\vec{v}| |\vec{v}_{A1}|} \right)$$

- Among low-Z target, ${}^7\text{Li}$ and ${}^{51}\text{V}$ stand out (large nat. abundance)

μ -e sector: diagnosing tools (3)

- Illustration: Higgs-mediated LFV, e.g. from dim-6 operator

Harnik-Kopp-Zupan 1209.1397, ...

- $\mu \rightarrow e \gamma$ is currently probing $|Y_{\mu e}| \sim 10^{-6}$ ($\text{BR}(h \rightarrow \mu e) < 10^{-9}$)

- Correlated signals in $\mu \rightarrow e$ transitions**

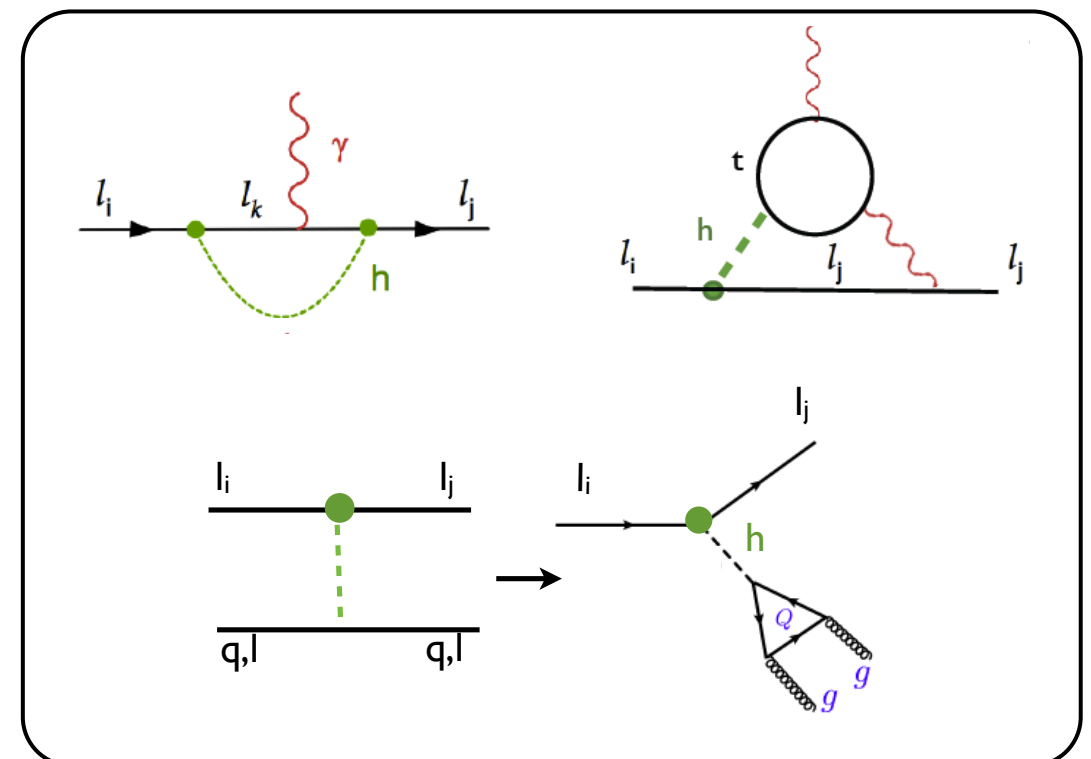
$$\text{BR}(\mu \rightarrow e, \text{Al}) / \text{BR}(\mu \rightarrow e \gamma) = 8.7(3) \cdot 10^{-3}$$

$$\text{BR}(\mu \rightarrow e, \text{Ti}) / \text{BR}(\mu \rightarrow e, \text{Al}) = 1.5(1)$$

VC, Fuyuto, Ramsey-Musolf, Rule 2203.09547

(See also Crivellin et al. 1404.7134)

$$\Delta \mathcal{L} \supset Y_{ij} \bar{e}_L^i e_R^j h + \text{H.c.}$$



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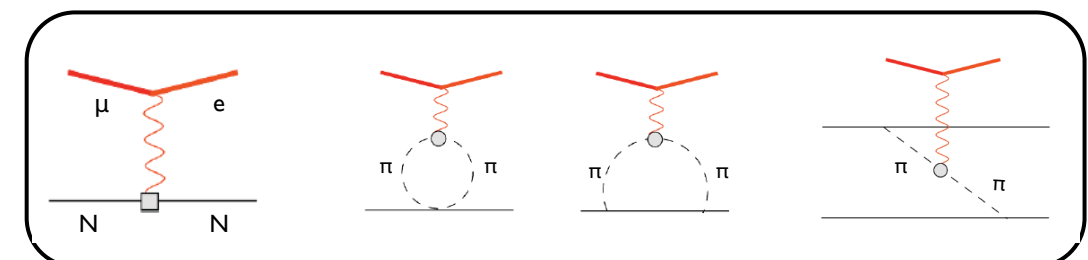
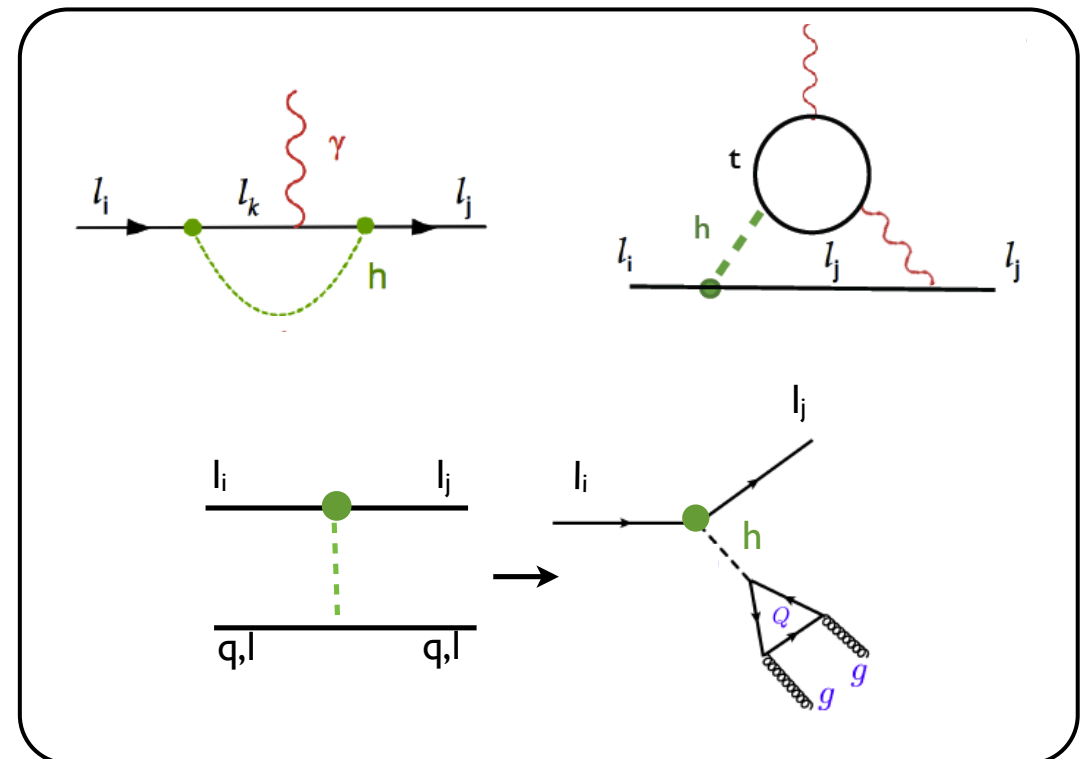
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** Included NLO chiral EFT corrections in computation of conversion rate.

For NR nuclear EFT approach see Rule et al, 2109.13503

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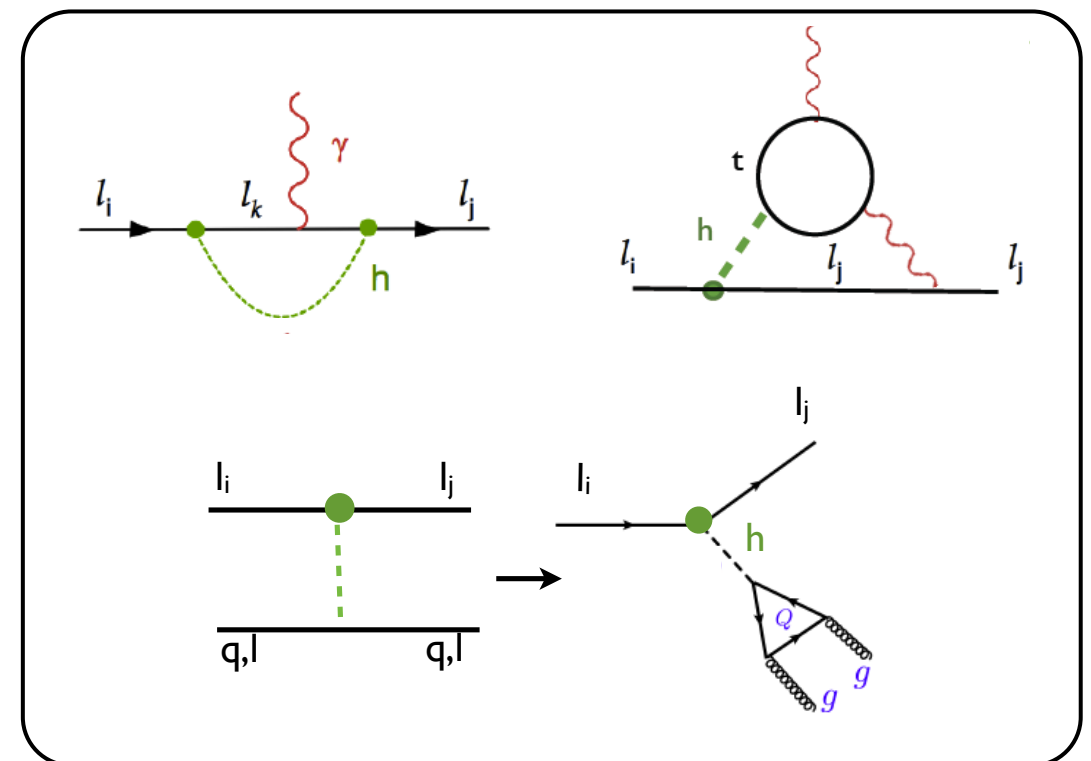
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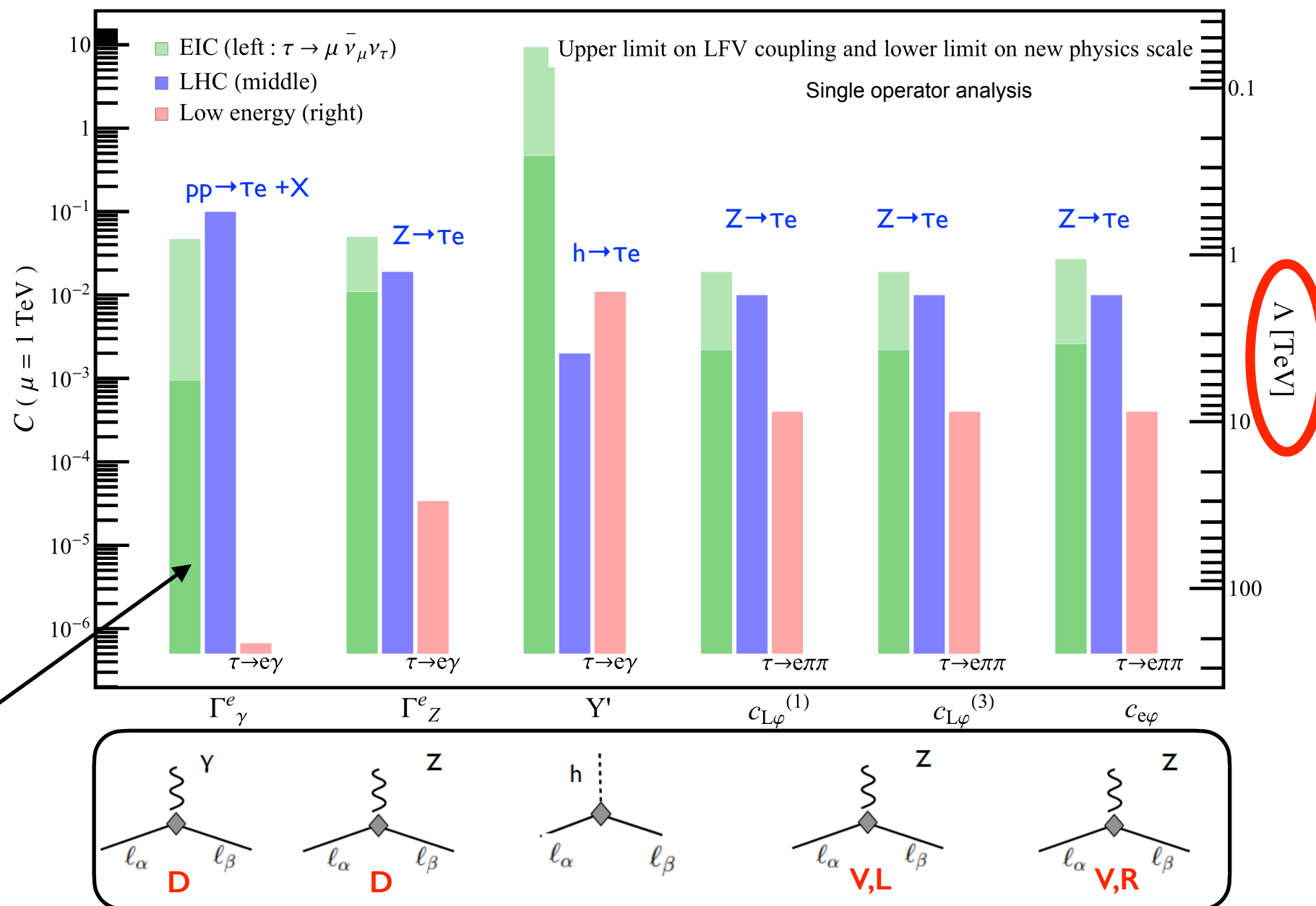


- Muon decays provide clean probe of LFV Higgs couplings

τ - $e(\mu)$ sector: mass reach (I)

- Bounds dominated by τ decays, with few exceptions from Higgs decay, LFV Drell-Yan, and B decays

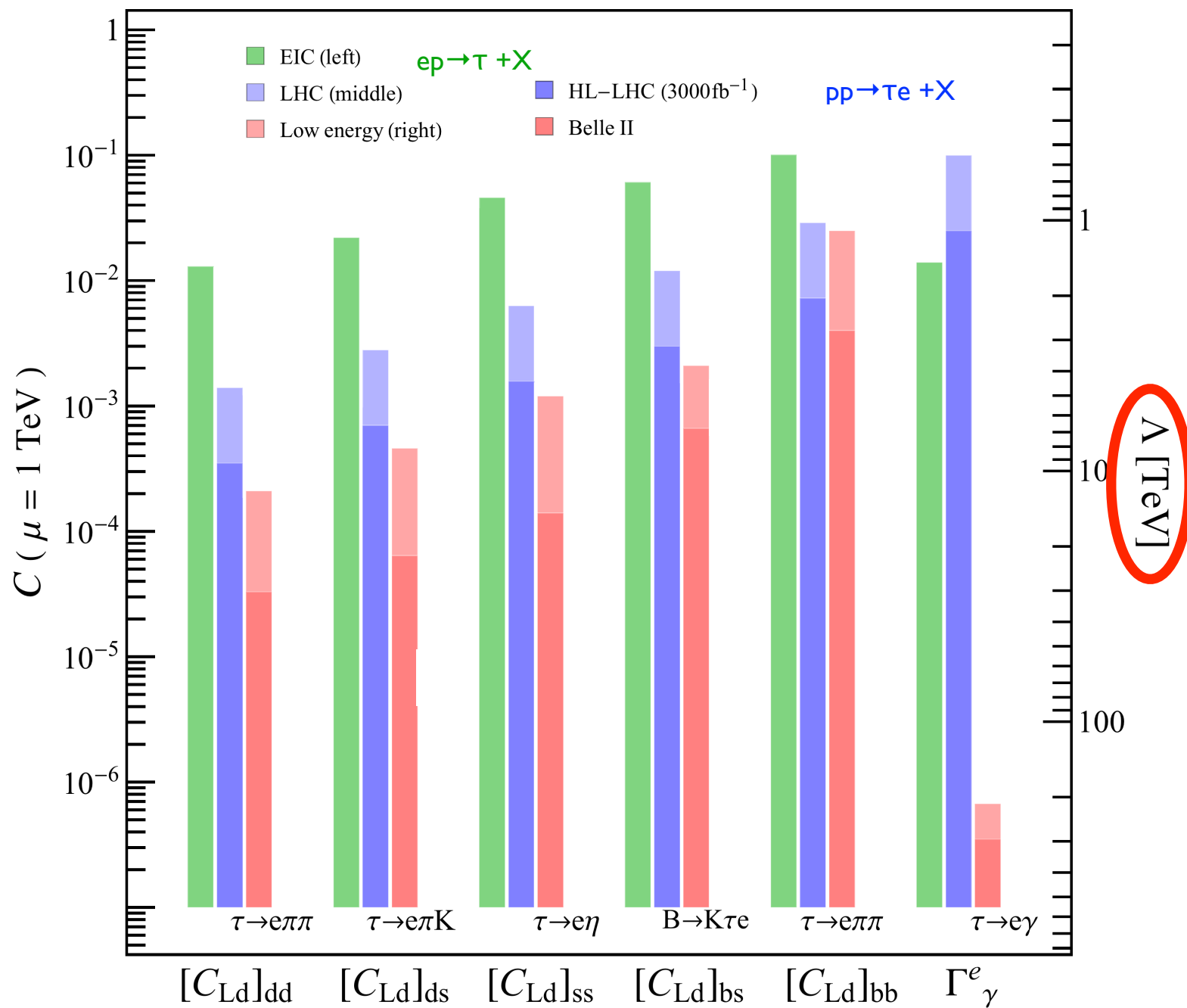
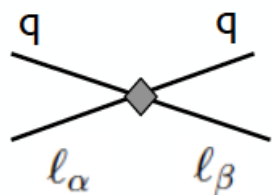
VC-Fuyuto-Lee-Mereghetti-Yan 2102.06176



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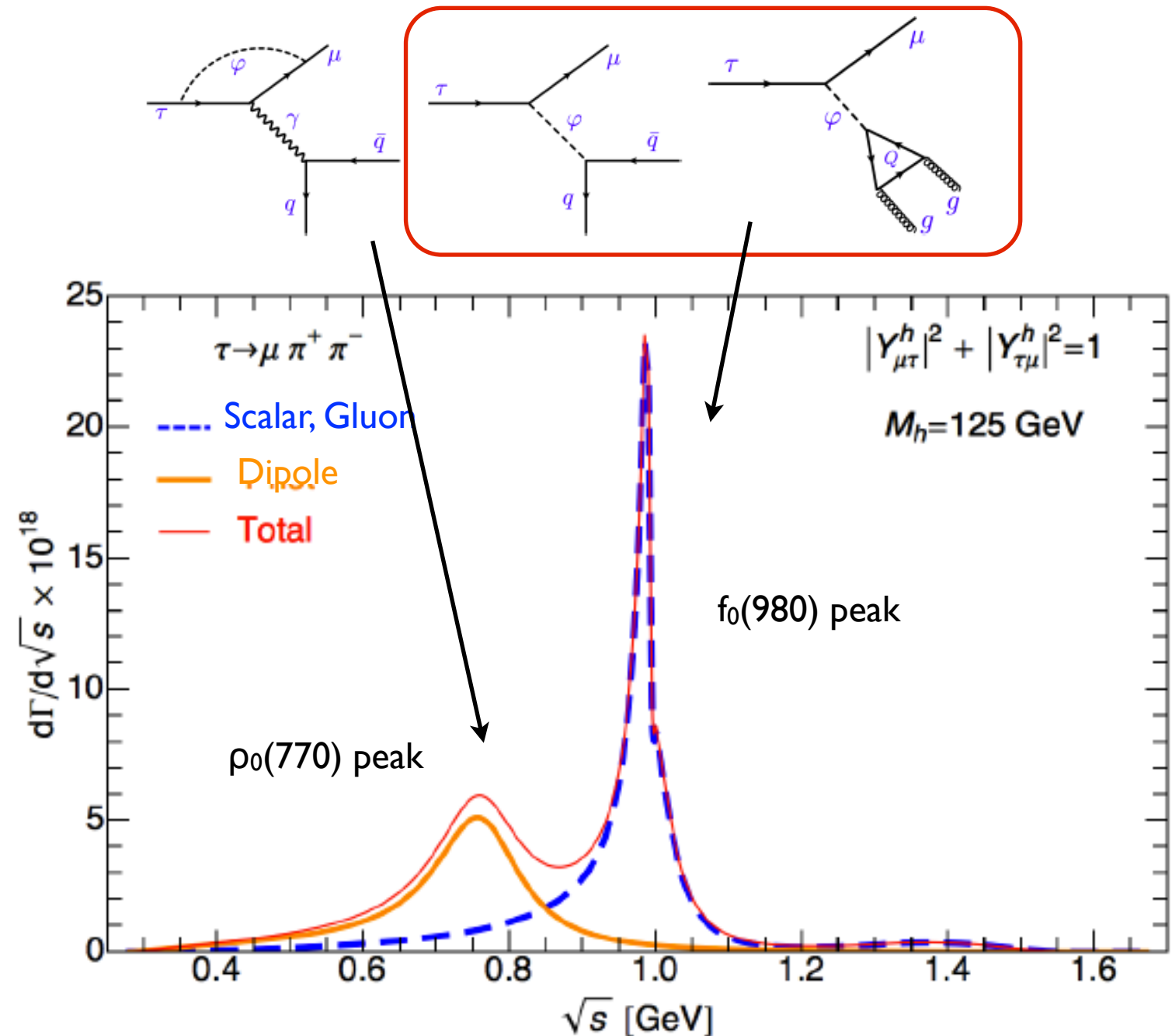
$$\bar{l}_\tau \gamma^\mu l_e \bar{d}_i \gamma_\mu d_j$$



τ - $\mu(e)$ sector: diagnosing tools

- Pattern of BRs and differential distributions. Illustration via **Higgs-mediated LFV**

- Given $\text{BR}(h \rightarrow \mu\tau) < 0.15\%$, $\tau \rightarrow \mu\pi\pi$ is observable at Belle-II if $Y_{u,d,s} \sim Y_b$
- Higgs-specific combination of D, S, G \rightarrow **unique signature in $\pi\pi$ spectrum**



Probing the flavor-breaking pattern: μ vs τ

- Smaller samples of taus compared to muons \Rightarrow $BR_{\tau} \sim 10^{-8}$ while $BR_{\mu} \sim 10^{-13}$
- Well motivated flavor-breaking patterns (leptonic MFV, GUTs, U(2) symmetries, ...) suppress $\mu \rightarrow e$ compared to $\tau \rightarrow \mu$:

Leptonic MFV**:

$$BR(\mu \rightarrow e\gamma) / BR(\tau \rightarrow \mu\gamma) \sim s_{13}^2 \sim 10^{-2}$$

GUT models:

$$BR(\mu \rightarrow e\gamma) / BR(\tau \rightarrow \mu\gamma) \sim |V_{us}|^6 \sim 10^{-4}$$

[VC-Grinstein-Isidori-Wise, hep-ph/0507001, hep-ph/0608123, ...](#)

[Barbieri-Hall-Strumia, hep-ph/9501334](#)

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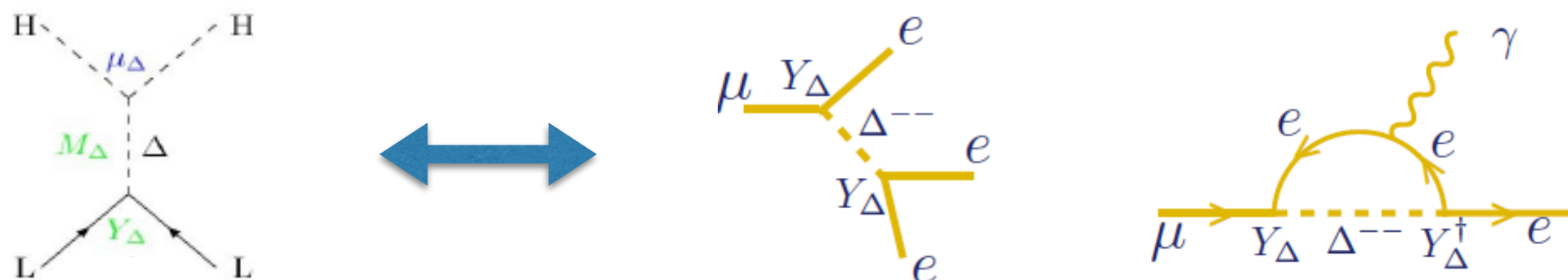
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VC-Grinstein-Isidori-Wise, [hep-ph/0507001](#), [hep-ph/0608123](#), ...

Barbieri-Hall-Strumia, [hep-ph/9501334](#)

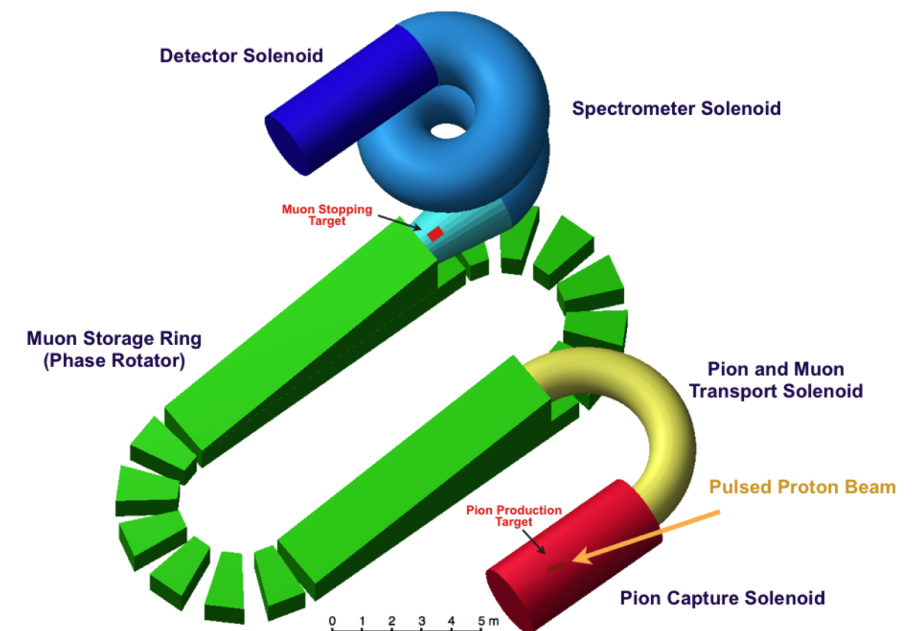
** Explicitly realized in Type-II seesaw (scalar triplet) CLFV controlled by $Y_\Delta \propto m_\nu$



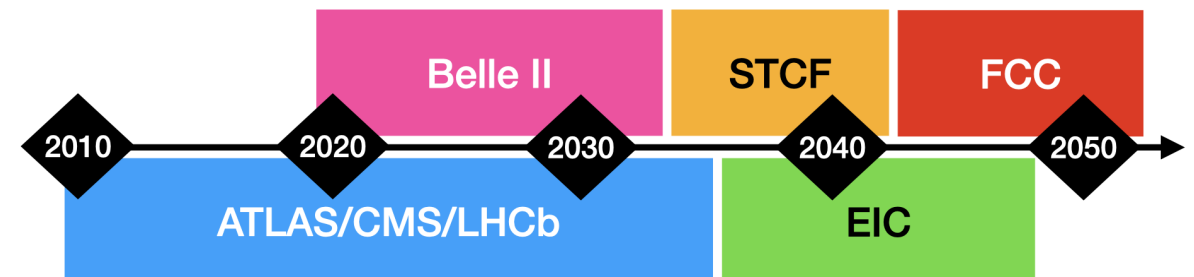
Experimental prospects

- Key facilities for **muons**: FNAL, J-PARC, PSI
- Next generation muon experiments at FNAL:
 - **Mu2e-II**, 10x better sensitivity
 - **Advanced Muon Facility**:
 - PRISM concept: **100x improvement μ -to-e conversion and high-Z target**
 - Muonium-antimuonium, muon EDM,...

PRISM concept
(Phase Rotated Intense Slow Muon beam)
[Kuno, Mori]

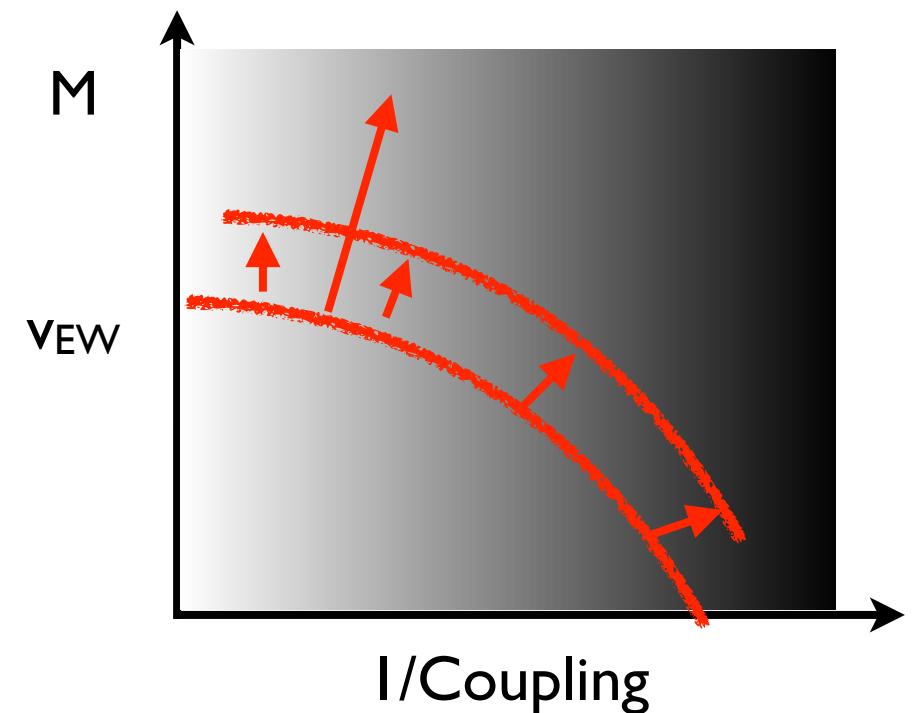


- Current / next gen. experiments relevant for CLFV in **tau** (and mesons)



Conclusions & Outlook

- Charged LFV processes probe a broad spectrum of new physics
 - *Discovery* tools: clean, very high scale reach
 - *Model-diagnosing* tools: mediators, sources of flavor breaking
- ‘Win-win’ situation
 - Should new physics appear (at the LHC or elsewhere) LFV will provide unique input on its symmetry structure
 - Should new physics NOT appear (at the LHC or elsewhere), LFV will be for a while one of the strongest tools to probe the mass scale of new physics



Conclusions & Outlook

- Charged LFV processes probe a broad spectrum of new physics
 - *Discovery* tools: clean, very high scale reach
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Exciting experimental prospects

- ★ 4-6 (1-2) orders of magnitude improvement in μ (τ) decays
- ★ LHC & EIC will be competitive in τ - μ and τ - e transitions ($h \rightarrow \tau\mu$, $e \rightarrow \tau$)
- ★ Muon processes have unmatched sensitivity in μ - e transitions.
Great opportunity for the Fermilab muon program