



# $\mu$ TRISTAN

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Based on 2201.06664, Yu Hamada (KEK -> DESY), RK, Ryutaro Matsudo (KEK -> NTU),  
Hiromasa Takaura (KEK -> YITP), Mitsuhiro Yoshida (KEK)

2210.11083, Yu Hamada (KEK -> DESY), RK, Ryutaro Matsudo (KEK -> NTU),  
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2304.14020, Kåre Fridell (KEK/Florida State U.), RK, Ryoto Takai (KEK/Sokendai)

Also, study in progress with Koji Nakamura (KEK), Sayuka Kita (Tsukuba U.),  
Toshiaki Kaji (Waseda U.), Taiki Yoshida (Waseda U.), Kohei Yorita (Waseda U.)

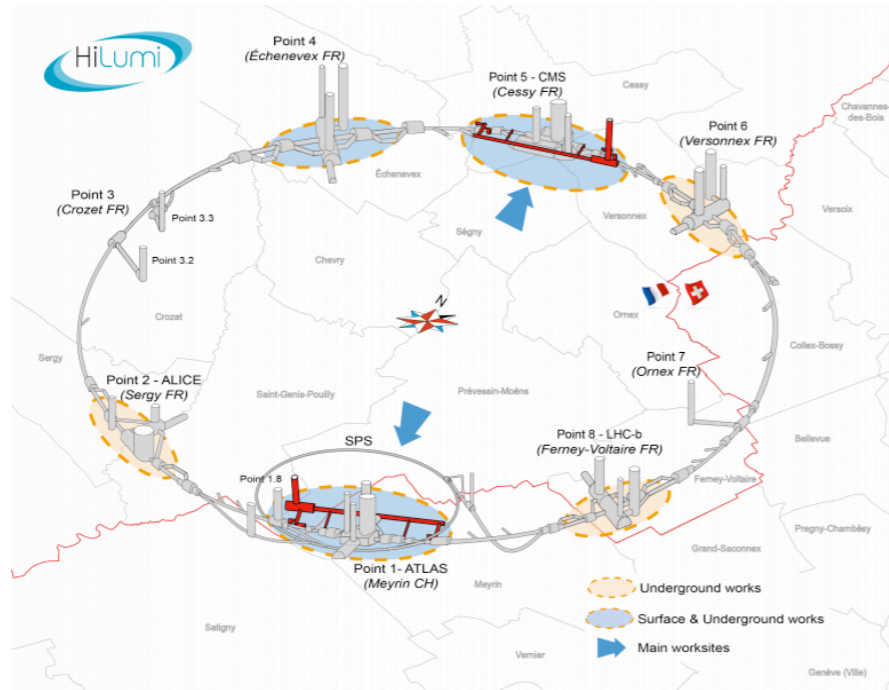
**Muons in Minneapolis Workshop@Minneapolis, December 6-8, 2023**

# Clearly, we need next generation colliders.

1. We must investigate **the form of the Higgs potential** by the observation of self-interactions.
2. We must check the possibility that one can actually produce **dark matter** artificially.
3. We must look for **new physics** at least up to about 10TeV (~ a loop factor higher than the EW scale).

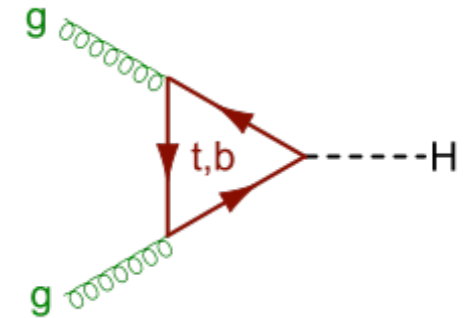
We cannot stop here.

# Higgs factories



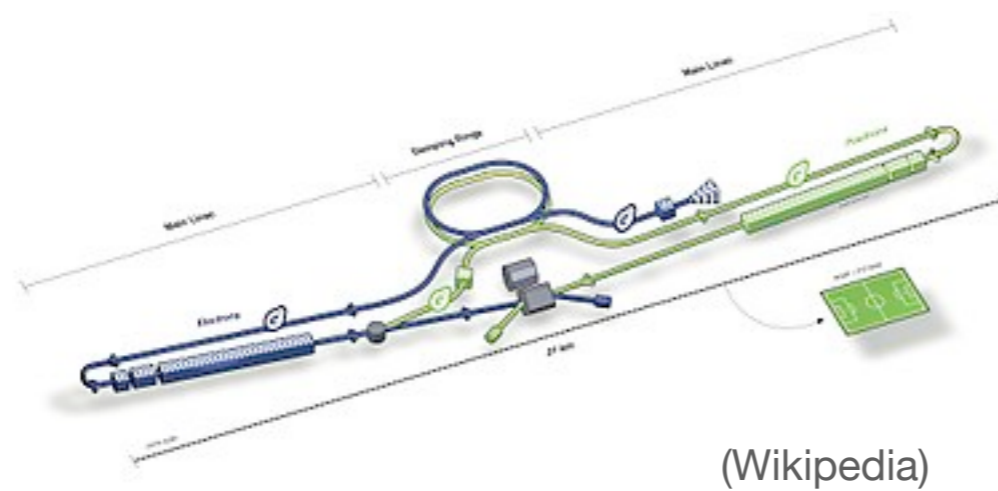
## HL-LHC (2029?-)

14TeV pp collider,  $3ab^{-1}$   
 $O(100M)$  Higgs bosons  
 (Although hard to identify)



## Higgs coupling at 1% level.

(LHC measures at a few - 10% level)



## ILC250 (20.5km $e^+e^-$ linear collider)

$\sim ab^{-1}$

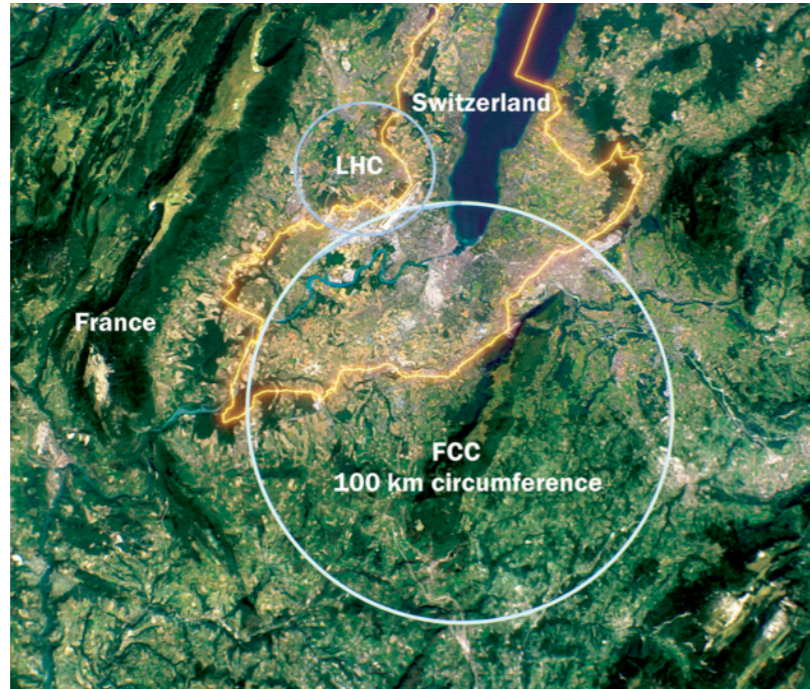
Extendable to 500GeV, 1TeV



$O(1M)$  Higgs bosons

Measurements of Higgs couplings at the level of 0.1%.

# Future colliders?



$e^+e^-$  (90-365 GeV)  $\longrightarrow$  pp (100 TeV)

Higgs/top factory      New physics searches

O(1M) Higgs

[muon smasher's guide]

10 TeV @  $10 \text{ ab}^{-1}$

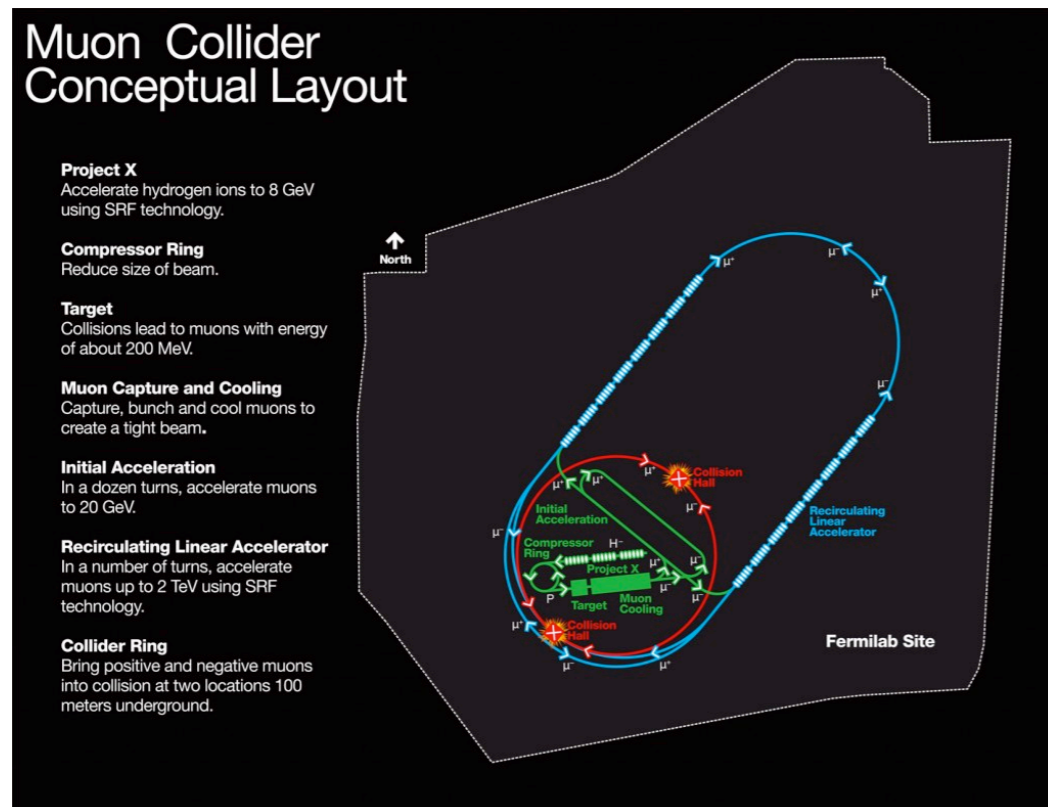
| Production     | Decay                  | Rate [fb] | $A \cdot \epsilon$ [%] | $\Delta\sigma/\sigma$ [%] |
|----------------|------------------------|-----------|------------------------|---------------------------|
| W-fusion       | $bb$                   | 490       | 7.4                    | 0.17                      |
|                | $cc$                   | 24        | 1.4                    | 1.7                       |
|                | $jj$                   | 72        | 37                     | 0.19                      |
|                | $\tau^+\tau^-$         | 53        | 6.5                    | 0.54                      |
|                | $WW^*(jj\ell\nu)$      | 53        | 21                     | 0.30                      |
|                | $WW^*(4j)$             | 86        | 4.9                    | 0.49                      |
|                | $ZZ^*(4\ell)$          | 0.1       | 6.6                    | 12                        |
|                | $ZZ^*(jj\ell^+\ell^-)$ | 2.1       | 8.9                    | 2.3                       |
|                | $ZZ^*(4j)$             | 11        | 4.6                    | 1.4                       |
|                | $\gamma\gamma$         | 1.9       | 33                     | 1.3                       |
|                | $Z(jj)\gamma$          | 0.9       | 27                     | 2.0                       |
| Z-fusion       | $\mu^+\mu^-$           | 0.2       | 37                     | 0.37                      |
|                | $bb$                   | 51        | 8.1                    | 0.49                      |
| W-fusion $tth$ | $WW^*(4j)$             | 8.9       | 6.2                    | 1.3                       |
|                | $bb$                   | 0.06      | 12                     | 12                        |

$\mu^+\mu^-$  (10 TeV?)

Fantastic!

A lot of Higgs bosons through WW fusion.

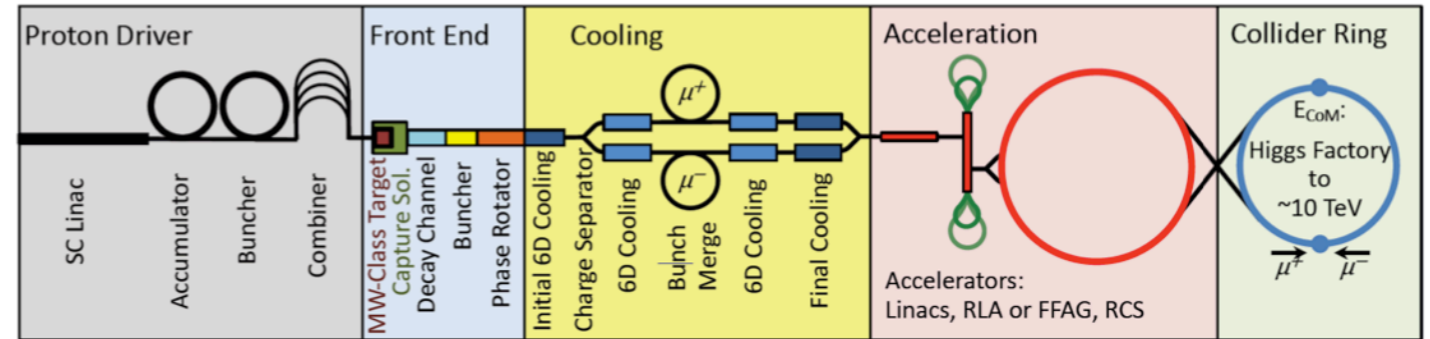
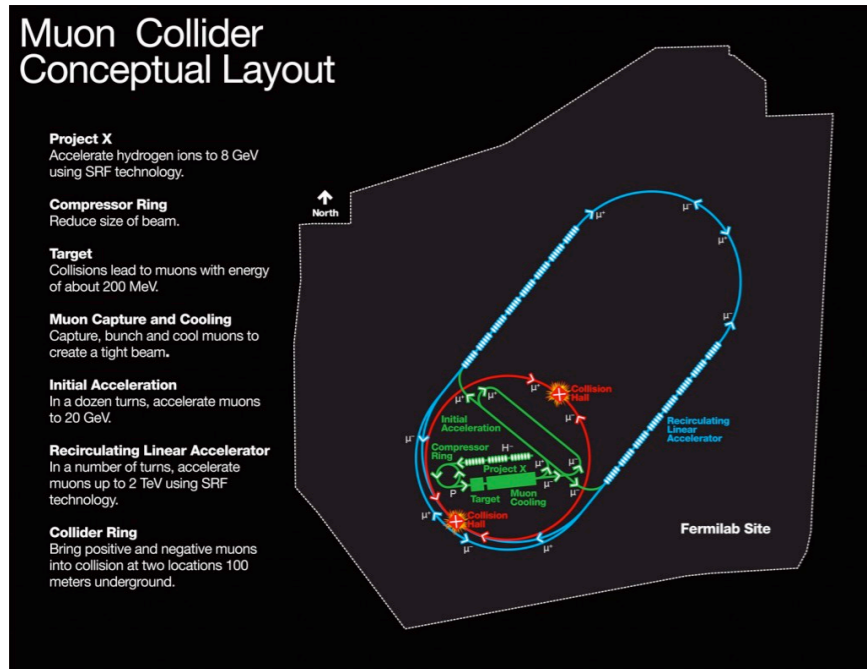
Direct reach to 10 TeV physics!



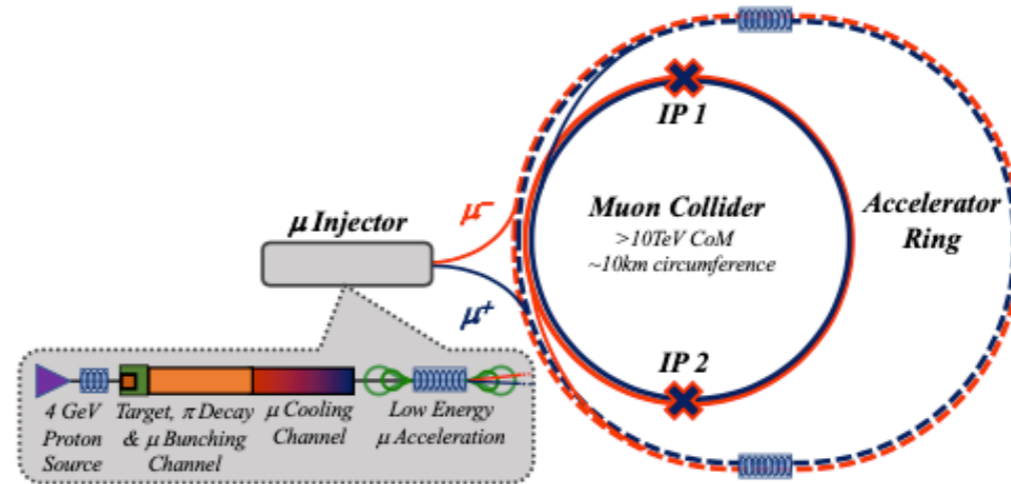
from symmetry

# muon collider

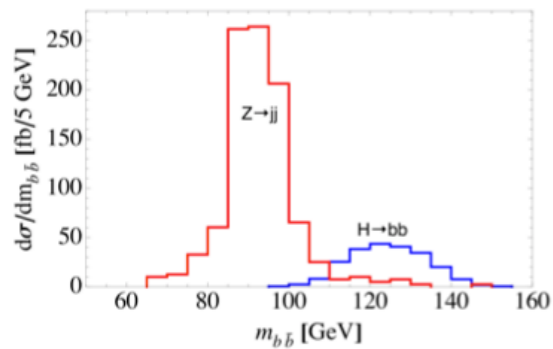
this is what we want!



from symmetry



[MAP collaboration]

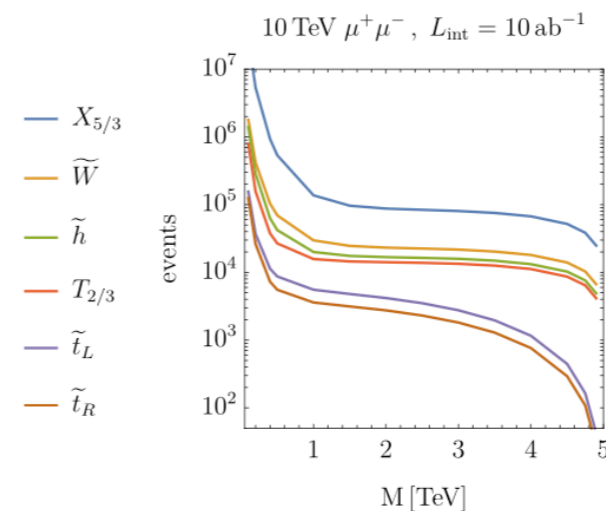


[Han, Liu, Low, Wang '20]

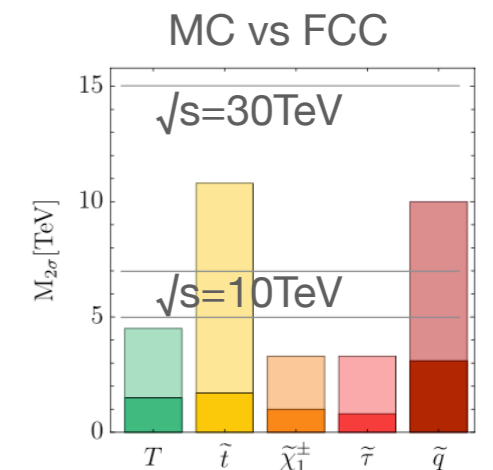
10 TeV @  $10\text{ab}^{-1}$

| Production             | Decay                  | Rate [fb] | $A \cdot \epsilon$ [%] | $\Delta\sigma/\sigma$ [%] |
|------------------------|------------------------|-----------|------------------------|---------------------------|
| W-fusion               | $bb$                   | 490       | 7.4                    | 0.17                      |
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|                        | $jj$                   | 72        | 37                     | 0.19                      |
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|                        | $\mu^+\mu^-$           | 0.2       | 37                     | 0.37                      |
| W-fusion $t\bar{t}$    | $bb$                   | 51        | 8.1                    | 0.49                      |
|                        | $WW^*(4j)$             | 8.9       | 6.2                    | 1.3                       |
| $W$ -fusion $t\bar{t}$ | $bb$                   | 0.06      | 12                     | 12                        |

[muon smasher's guide]



[Buttazzo, Franceschini, Wulzer '20]



[Snowmass report '22]

# Very nice. Why don't we just do it now!

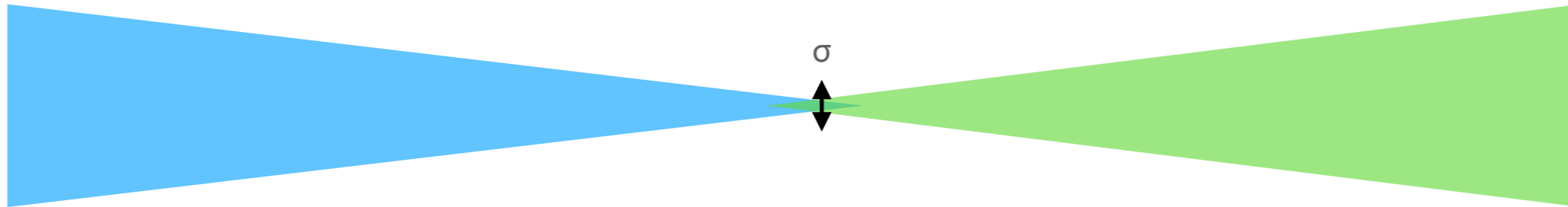
of course, there are technical challenges to realize this collider.

The most challenging part is to obtain enough **luminosities**.

Today, I talk about possibly a realistic scenario of  **$\mu^+$  based** colliders.

# Luminosity

$$\mathcal{L} = \frac{N_{\text{beam1}} N_{\text{beam2}}}{4\pi\sigma_x\sigma_y} f_{\text{rep}}$$



We need a large number of muons and/or narrow beams.

As a reference,

$N_{\text{beam}}=10^{10}$  (1.6nC) / bunch

$\sigma=1\mu\text{m}$

$f_{\text{rep}}=1\text{MHz}$



$\sim 8 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1} \sim 25 \text{ fb}^{-1}/\text{year}$

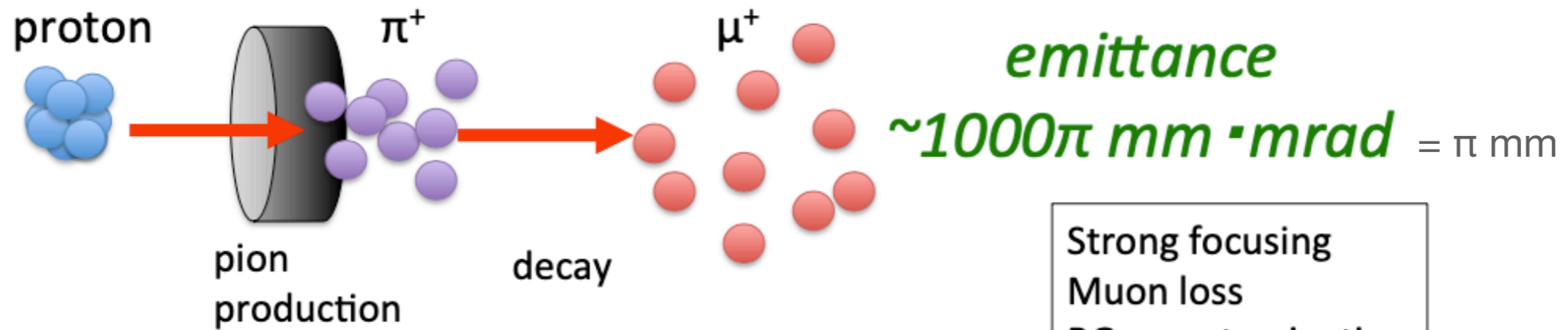
We want  $\text{ab}^{-1}$  level luminosity for physics  
(HL-LHC, ILC)

$\sigma$  is the most difficult part. The **cooling** is the key.

# Muon beam

## Conventional muon beam

Too much spread.



Taken from Mibe-san's lecture slide

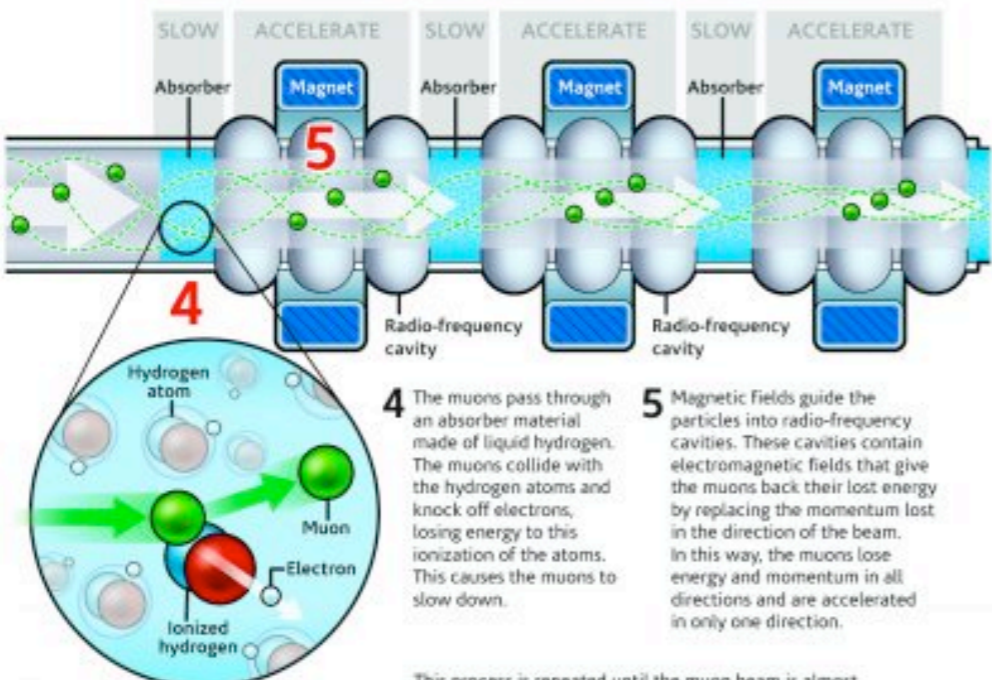
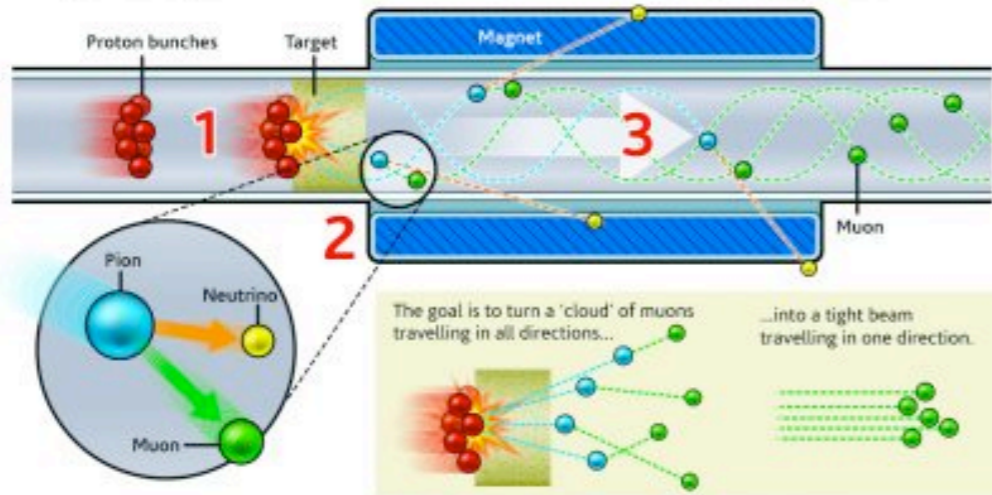


# Muon cooling

## MICE Muon Ionization Cooling Experiment

MICE has made the first ever demonstration of the ionization cooling of muons – a major step in the journey to create the world's most powerful particle accelerator.

- 1 Bunches of protons are accelerated into a target of dense material (such as tungsten or mercury). The atoms within the target emit a particle called a pion.
- 2 Pions are unstable and they quickly decay into a muon and a neutrino.
- 3 The neutrinos, being virtually massless and without charge, pass out of the experiment. Magnets direct charged muons of the correct energy moving in the right direction.

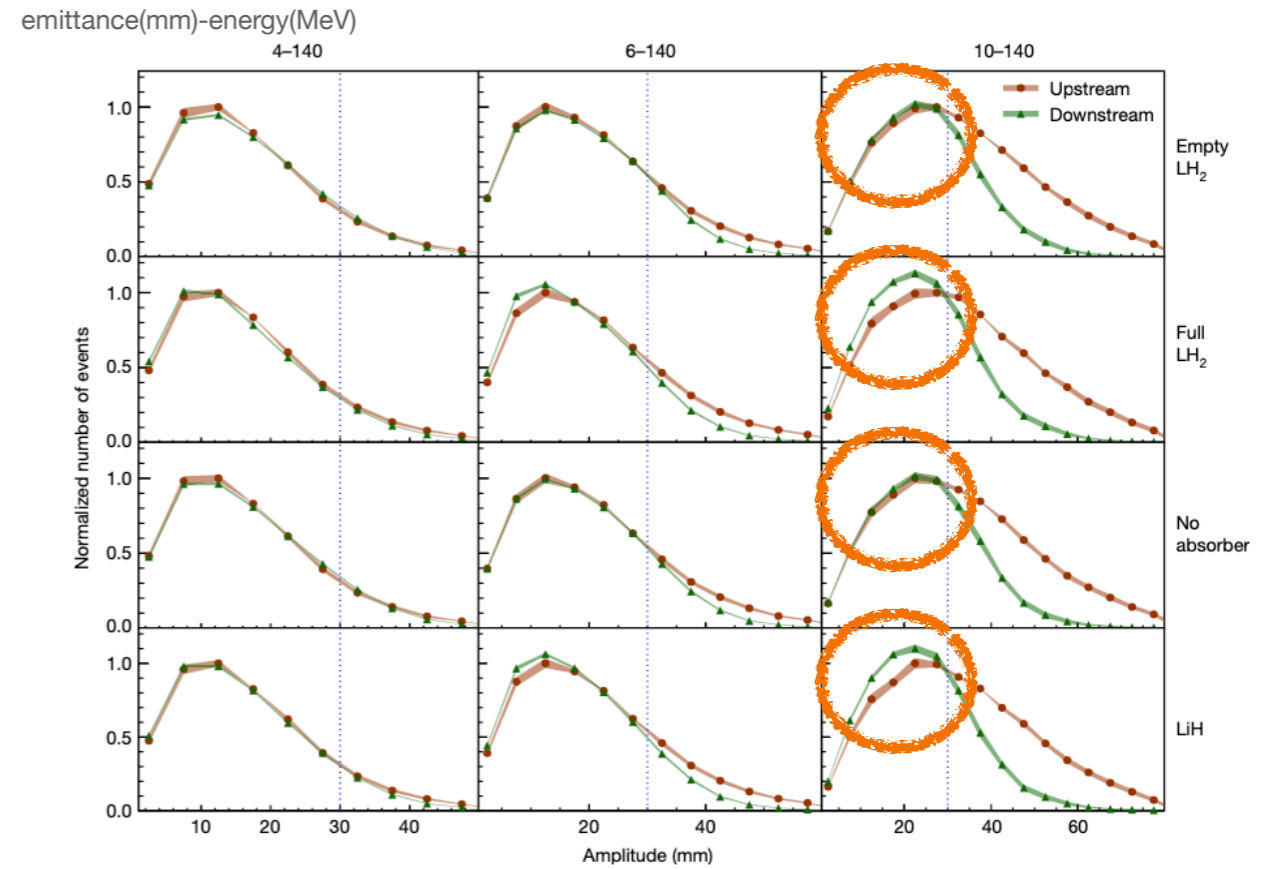


Infographic: STFC, Ben Gilliland

This process is repeated until the muon beam is almost laser-like, ready for injection into the main accelerator.

Principle works.

[Nature 2020, MICE collaboration]



simulation and plan for muon cooling of the MAP design

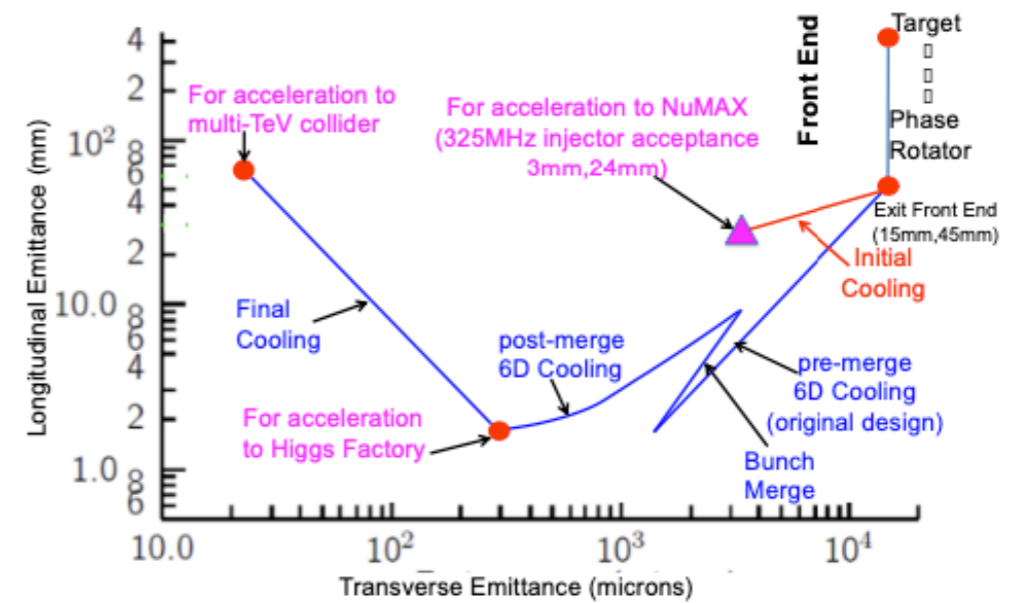


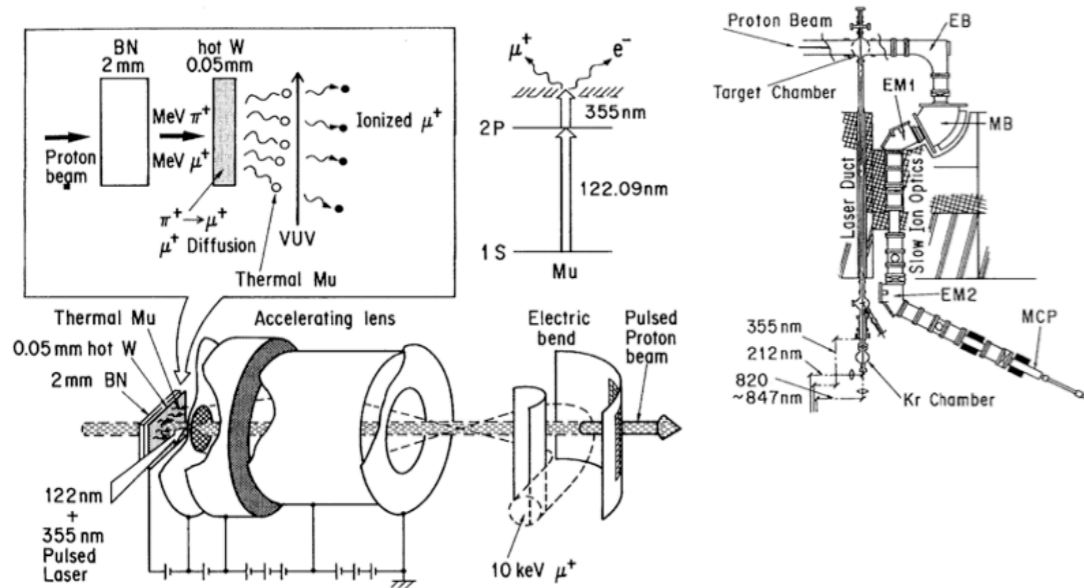
Figure 3. Ionization Cooling path in the 6D phase space.

# Muon cooling which works for $\mu^+$

There is a rather matured(?) technology only works for  $\mu^+$ .

Ultracold muon technology

[K.Nagamine et al. 1995]



This has been the key technology for the J-PARC muon g-2 experiment.

ultra-cold muon is here. ●

## ミュオンg-2/EDMと極冷ミュオンビーム

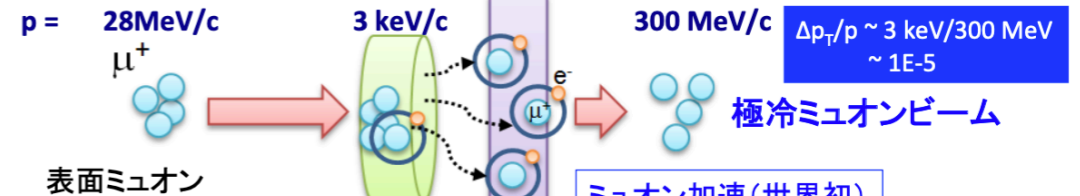
J-PARCで行う新しいミュオンg-2/EDM精密測定 [www.g-2.kek.jp](http://www.g-2.kek.jp)

- BNLが報告した標準模型からのズレ(3 $\sigma$ )の検証(0.1ppm)
- 全く新しいコンセプトで主要系統誤差要因を払拭
  - ゼロ電場
  - コンパクトな蓄積磁石(0.7 m << 14 m)
- 通常に比べてエミッタンスが1/1000程度小さいミュオンビーム (極冷ミュオンビーム)が必須

ミュオニウムMu ( $\mu^+e^-$ )のレーザー共鳴イオン化

Nagamine et al. PRL 74 (1995)  
P. Bakule et al. INM B266(2008)

Laser 122nm, 355nm



ミュオニウム生成・放出

従来 : 高温金属(タングステン箔)  
本研究: シリカエアロゲルを用いて  
室温で高効率生成に成功

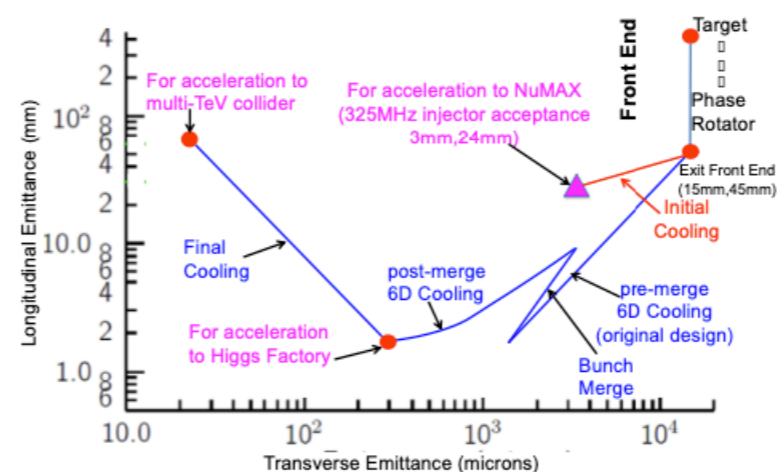


Figure 3. Ionization Cooling path in the 6D phase space.

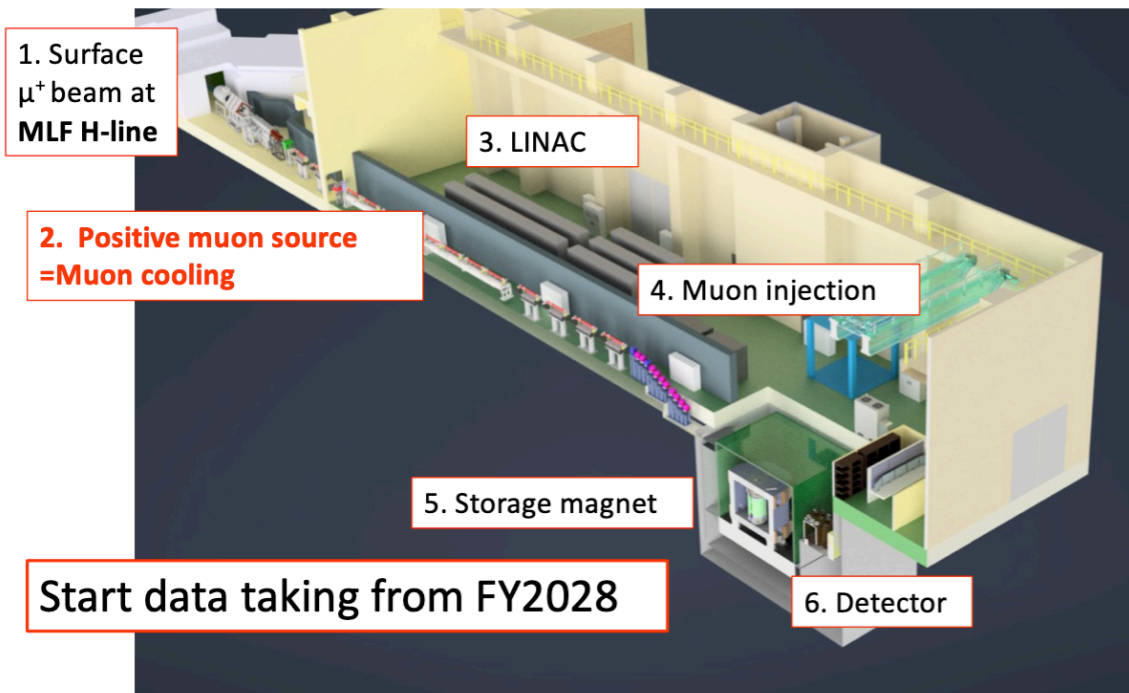
Mibe-san's slide

Looks like there is a good chance of realizing a low-emittance  $\mu^+$  beam!

# g-2/EDM experiment @ KEK J-PARC

## Muon g-2/EDM experiment at J-PARC

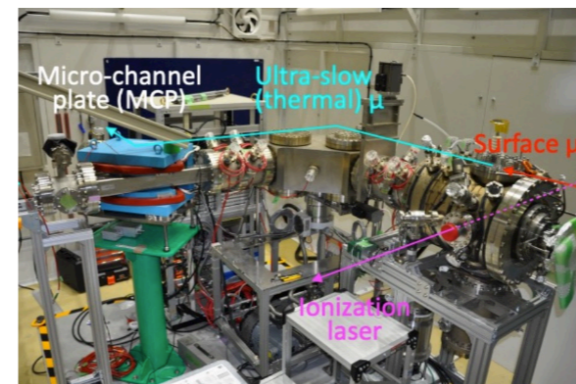
A new muon g-2/EDM measurement featuring a low emittance  $\mu^+$  beam



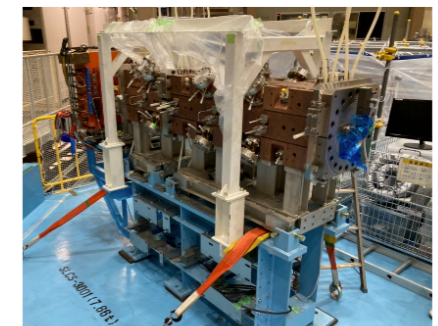
## Demonstration @ MLF S-line

- Collaborating with Muonium 1S-2S spectroscopy experiment.
  - A 244-nm pulsed laser developed by Okayama univ.
- Q-scan measurement is underway to evaluate the initial phase space.
- RFQ acceleration of cooled muon will be performed after in 2024.

MCP for counting event rate & Beam profile monitor to measure USM beam size after extraction



World 1st acceleration of USM will be performed soon



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S. Kamioka (talk@muon acceleration workshop, Nov. 2, 2023)

Yes, it has already been cooled and to be accelerated soon!!

(Actually, the acceleration of the  $\mu^+e^-e^-$  bound state has already been demonstrated!!)

# $\mu$ TRISTAN

$\mu^+e^-/\mu^+\mu^+$  collider with 1 TeV  $\mu^+$  beam.

**PTEP**

Prog. Theor. Exp. Phys. **2022** 053B02(16 pages)  
DOI: 10.1093/ptep/ptac059

30 GeV  $e^-$  / 1 TeV  $\mu^+$  : Higgs factory,  $\sqrt{s}=346\text{ GeV}$   
1 TeV  $\mu^+$  / 1 TeV  $\mu^+$  : new physics search,  $\sqrt{s}=2\text{ TeV}$

## $\mu$ TRISTAN

Yu Hamada<sup>1</sup>, Ryuichiro Kitano<sup>1,2</sup>, Ryutaro Matsudo<sup>1</sup>, Hiromasa Takaura<sup>1,\*</sup>, and Mitsuhiro Yoshida<sup>2,3</sup>

<sup>1</sup>KEK Theory Center, Tsukuba 305-0801, Japan

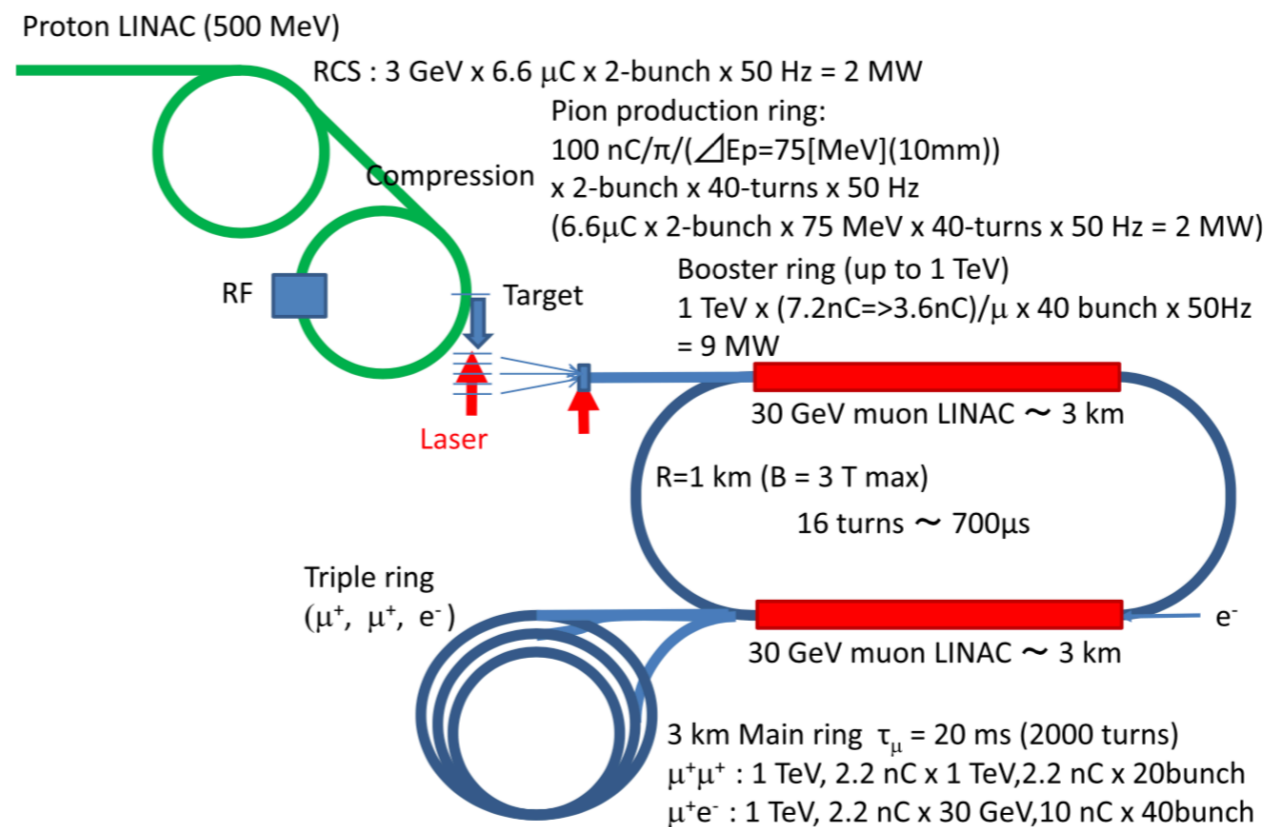
<sup>2</sup>Graduate University for Advanced Studies (Sokendai), Tsukuba 305-0801, Japan

<sup>3</sup>KEK Accelerator Department, Tsukuba 305-0801, Japan

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The ultra-cold muon technology developed for the muon  $g-2$  experiment provides a low-emittance  $\mu^+$  beam which can be accelerated and used for experiments. We consider the possibility of new collider experiments by  $\mu^+$  beam up to 1 TeV. Allowing the  $\mu^+$  beam to collide with a high-intensity TRISTAN energy,  $E_{e^-} = 30\text{ GeV}$ , in a storage ring with the same size as TRISTAN (circumference of 3 km), one can realize a collider experiment with the center-of-mass energy  $\sqrt{s} = 346\text{ GeV}$ , which allows the production of Higgs bosons through vector boson fusion processes. We estimate the deliverable luminosity with existing accelerator technology.  $\mu^+\mu^+$  colliders up to  $\sqrt{s} = 2\text{ TeV}$  are also possible using the same storage ring. They have the capability of producing the superpartner of the muon up to TeV energy.



**Fig. 1.** Conceptual design of the  $\mu^+e^-/\mu^+\mu^+$  collider.

# How many cold muons?

1/(20ms) where 20ms is the lifetime of the 1TeV muon

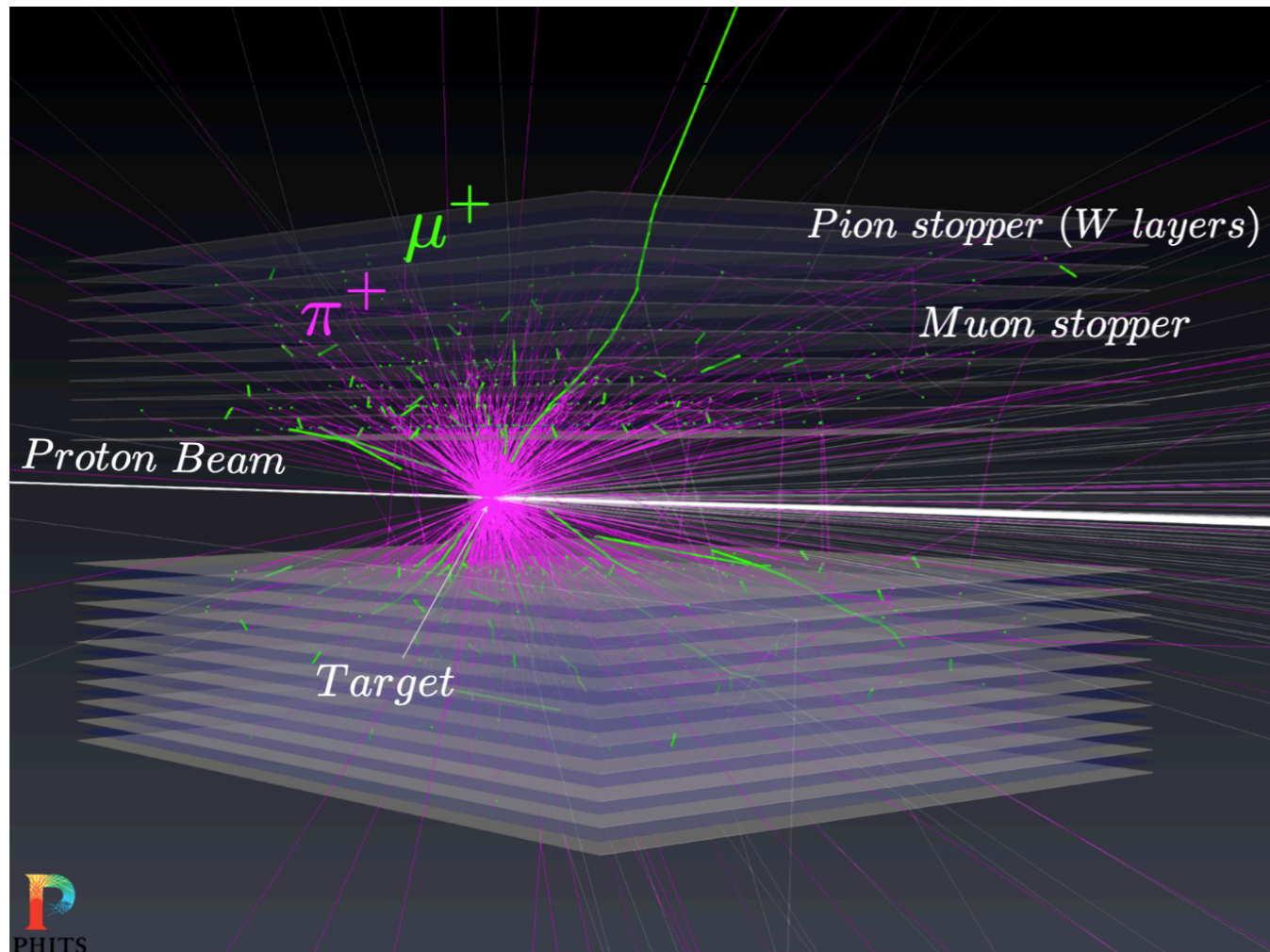
J-PARC like proton driver:  $6.6 \mu\text{C} * 50 \text{ Hz} * 2 \text{ bunches} = 4.1 \times 10^{15} \text{ protons/s}$

pion production target: 40 hits/bunch 0.016  $\pi^+$ /proton  $2.6 \times 10^{15} \pi^+/\text{s}$

pion stopping target: 0.5 stopping efficiency \* 0.07 muons/ $\pi^+$   $9 \times 10^{13} \mu^+/\text{s}$

simulation: (Yoshida, Sakaki ... in progress)

$10^5$  larger than J-PARC MLF.  
Super muon factory!



(Thermal muon production rate)

= (Muon stopping number on the layers)

× (MC correction for pion production)

× (Muonium formation)

× (Vacuum yield)

× (Loss of muoniums due to the decay)

PTEP 2022 (2022) 5, 053B02

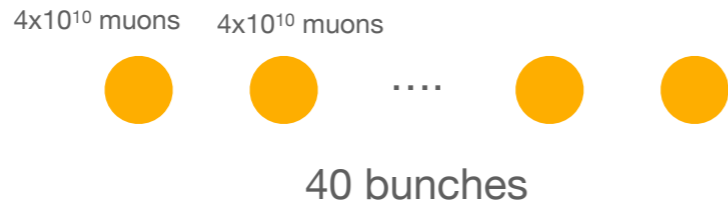
=  $1.4 * 10^{-3} \mu/p$

→  **$2.4 * 10^{14} \mu/s$**  (J-PARC RCS: 6.6  $\mu\text{C}$ , 2bunch 40 turns)

**$O(10^{13} \mu/s)$  will be available for collider experiment**

# Luminosity?

$$6.6 \mu\text{C} \times 2 \times 0.016 \times 0.5 \times 0.07 \sim 7 \text{ nC} / \text{bunch} \sim 4 \times 10^{10} \text{ muons/bunch}$$



accelerate up to 1TeV → bunch charge reduced to half by decay  
 storage ring → 2000 turns. further reduced by half

$$N_\mu \sim 10^{10} \quad N_e \sim 6 \times 10^{10}$$

$$\sigma \sim 2\text{-}3 \mu\text{m} \quad (\beta^* \sim \text{cm})$$

$$f_{\text{rep}} \sim (c/3\text{km}) \times 40 \text{ bunches} \\ \sim 100 \text{ kHz} \times 40 \text{ bunches} = 4 \text{ MHz}$$

storage ring  
 1μs for one turn.  
 2000 turns before next beam  
 is coming.

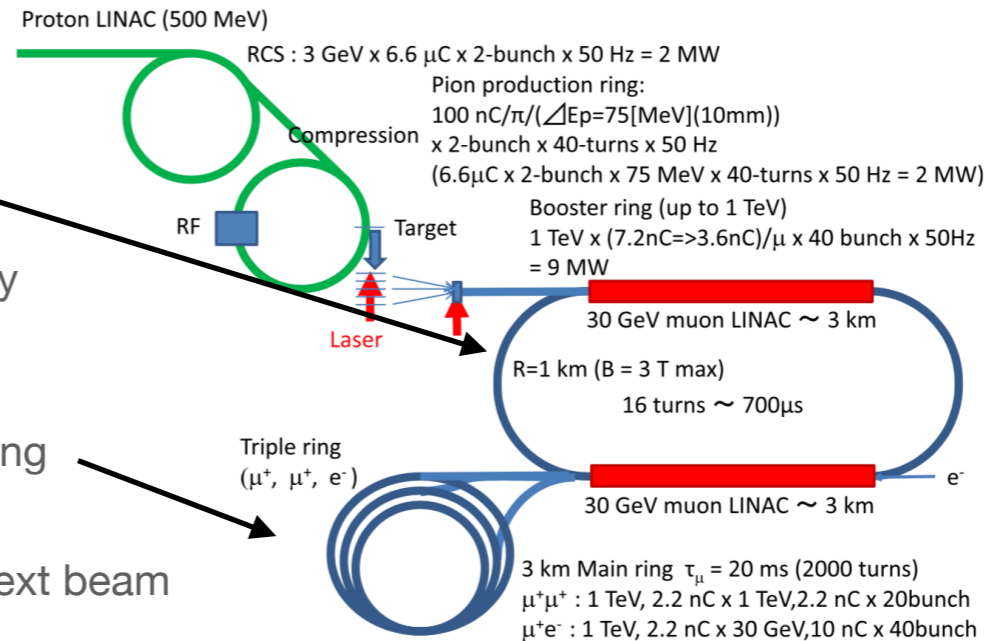
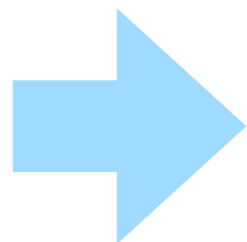


Fig. 1. Conceptual design of the μ<sup>+</sup>e<sup>-</sup>/μ<sup>+</sup>μ<sup>+</sup> collider.



$$\mathcal{L}_{\mu^+e^-} = 4.6 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}.$$

$$\mathcal{L}_{\mu^+\mu^+} = 5.7 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}.$$

ab<sup>-1</sup> level for 10yrs running.

not bad.

Actually, these numbers are pretty much conservative ones compared to MAP estimates.

# Luminosity comparison

|                                     | <b>MAP</b>       | <b><math>\mu</math>TRISTAN(<math>\mu^+\mu^+</math>)</b> |
|-------------------------------------|------------------|---|
| <b>normalized emittance</b>         | 25 $\pi$ mm mrad | 0.1-1 $\pi$ mm mrad                                     |
| <b>bunch length</b>                 | 1 cm             | 0.01-0.1 cm   |
| <b>efficiency</b>                   | 0.1              | 0.01 - 0.07   |
| <b>total luminosity (arb. unit)</b> | 1                | 2.5 - 10000   |

(eff)<sup>2</sup> / (emittance \* bunch length)

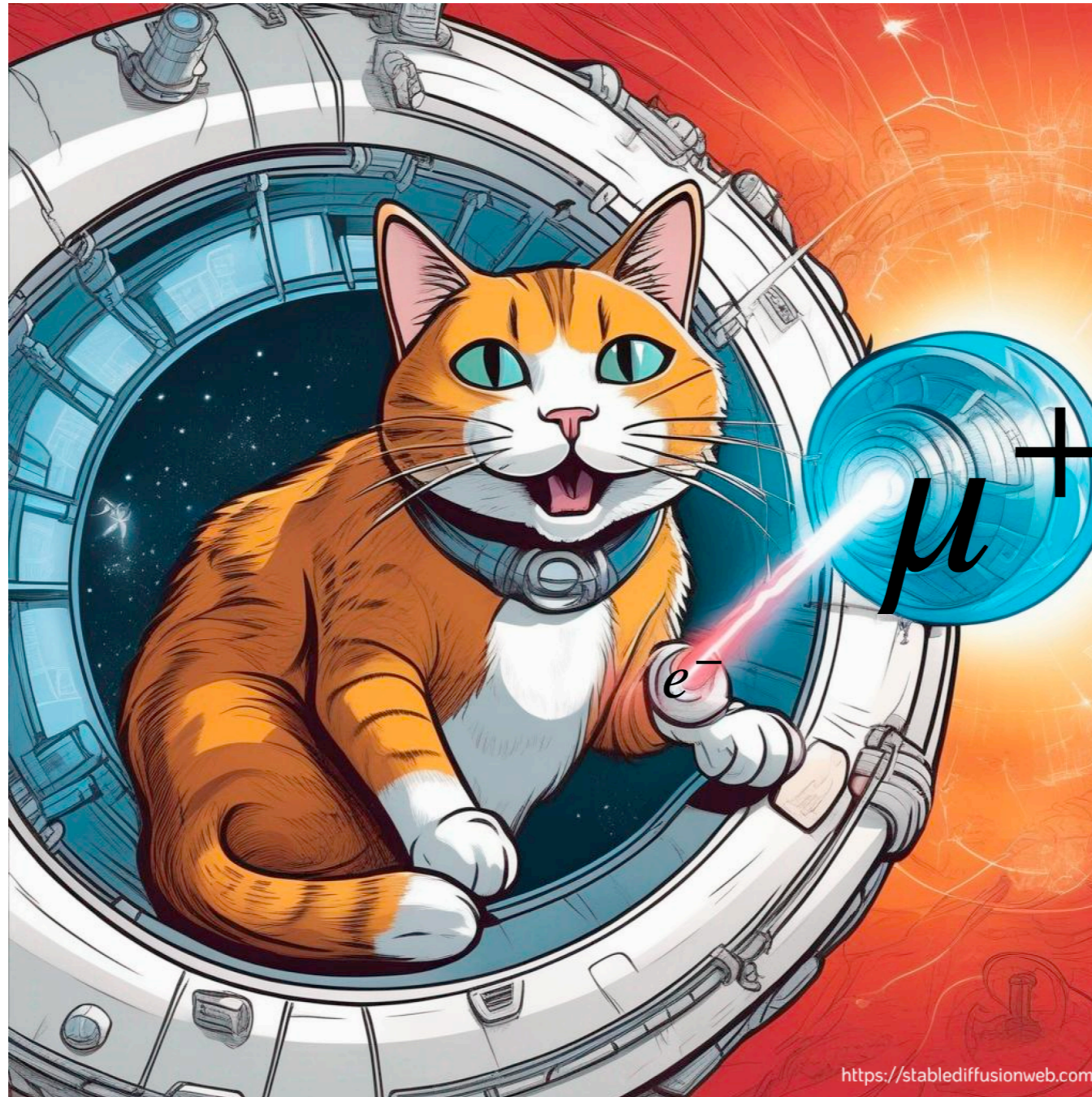
(could be much better for  $\mu^+e^-$ )

Number of muons may be smaller, but

we see that if we only use  $\mu^+$ , we can have (much) better luminosities.

And, the technology is more matured! Express ticket for muon colliders?

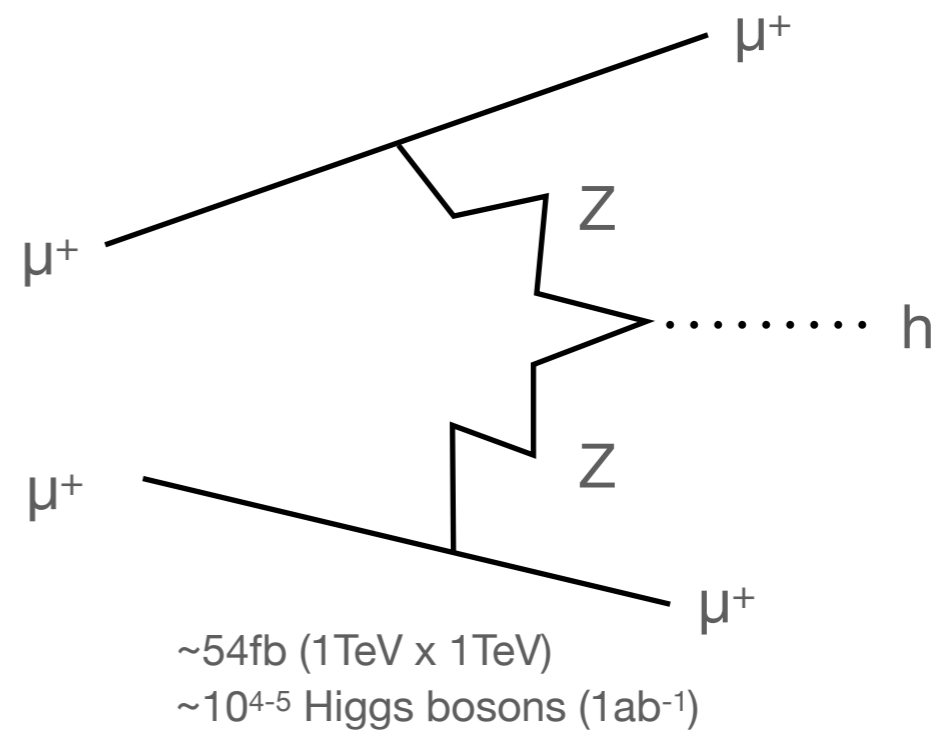
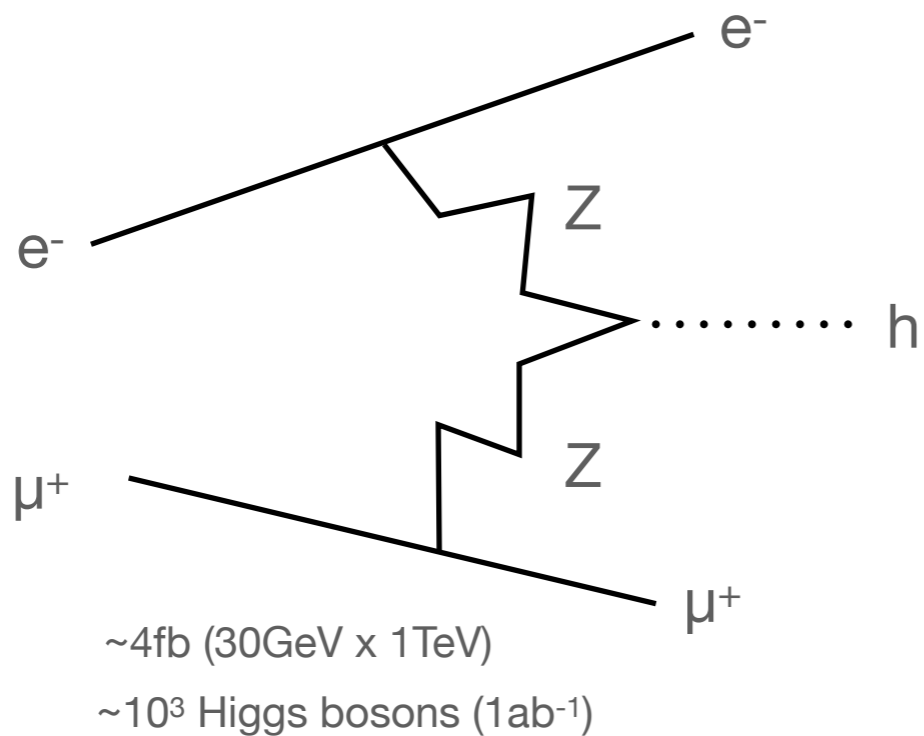
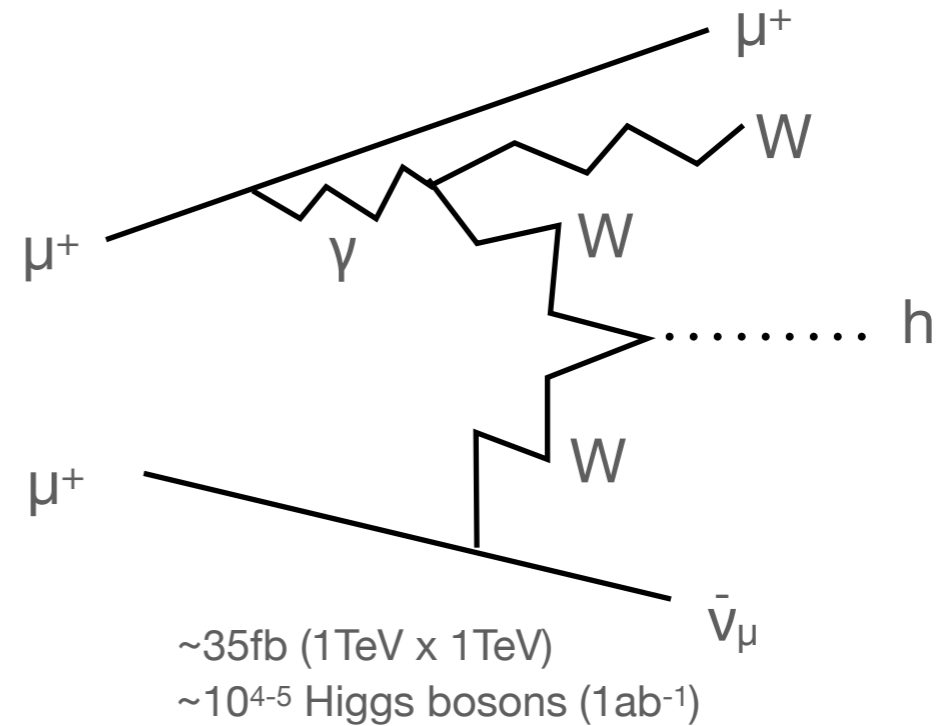
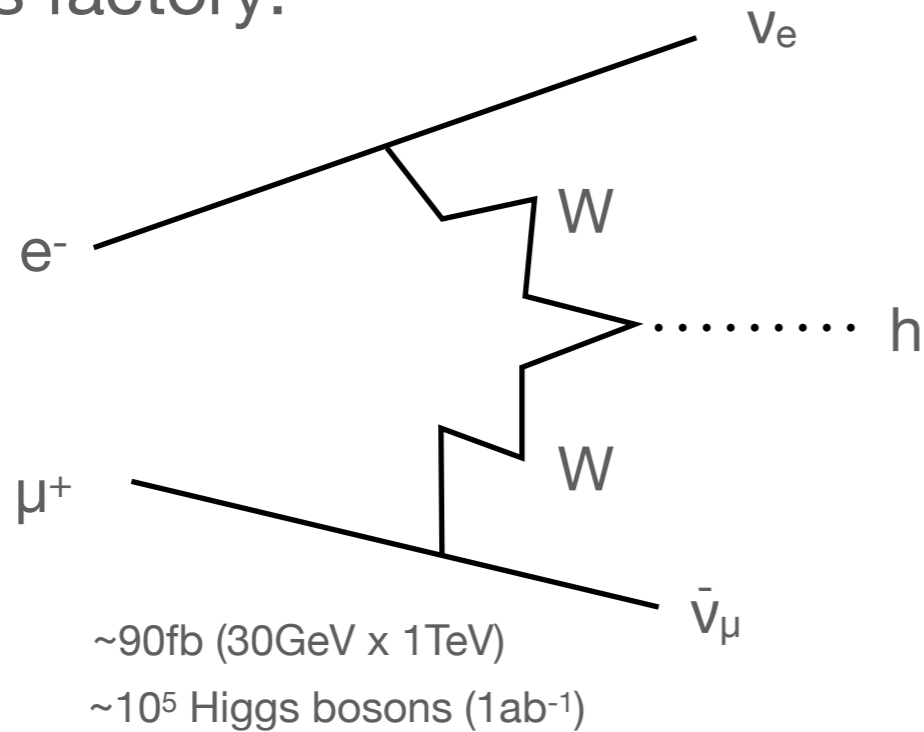
mewTRISTAN



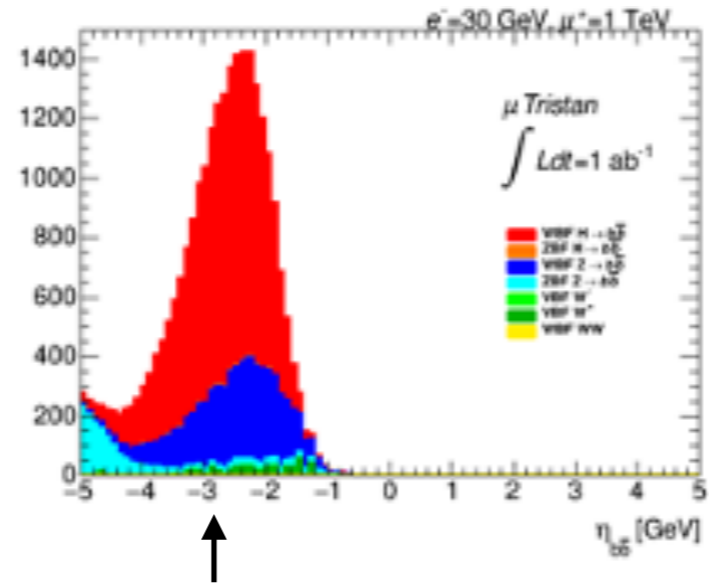


# What can we do at $\mu$ TRISTAN?

Higgs factory:

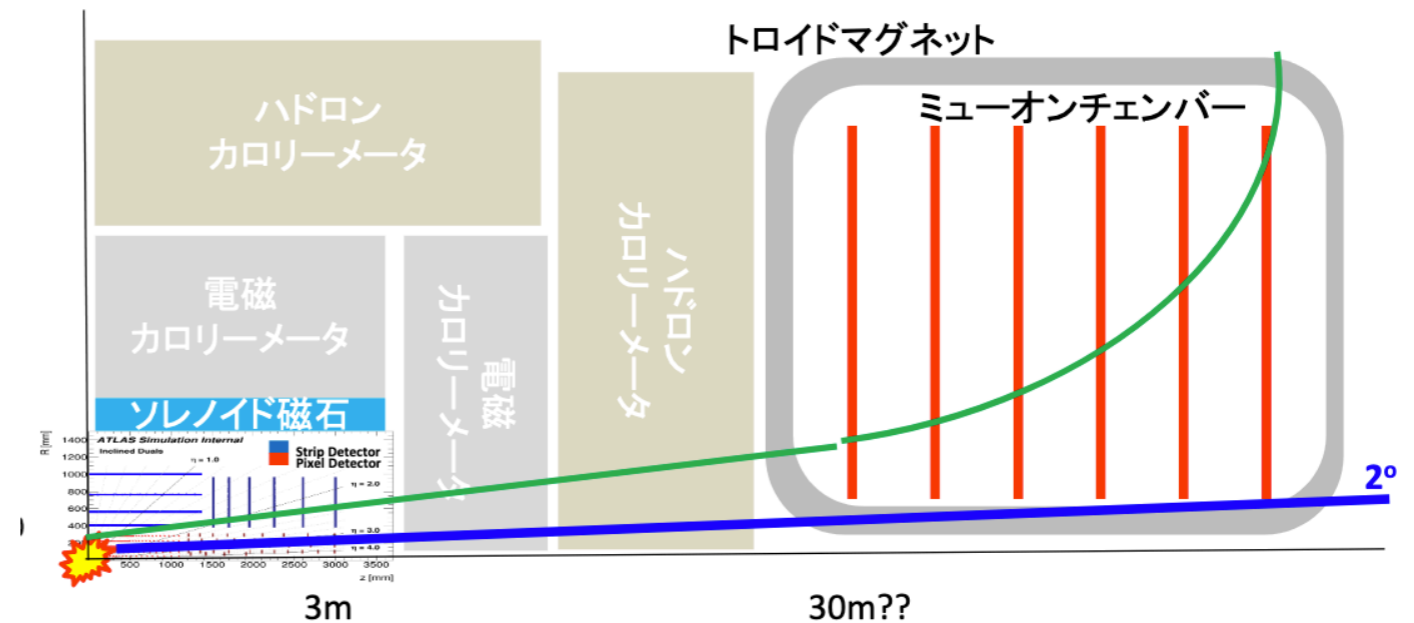
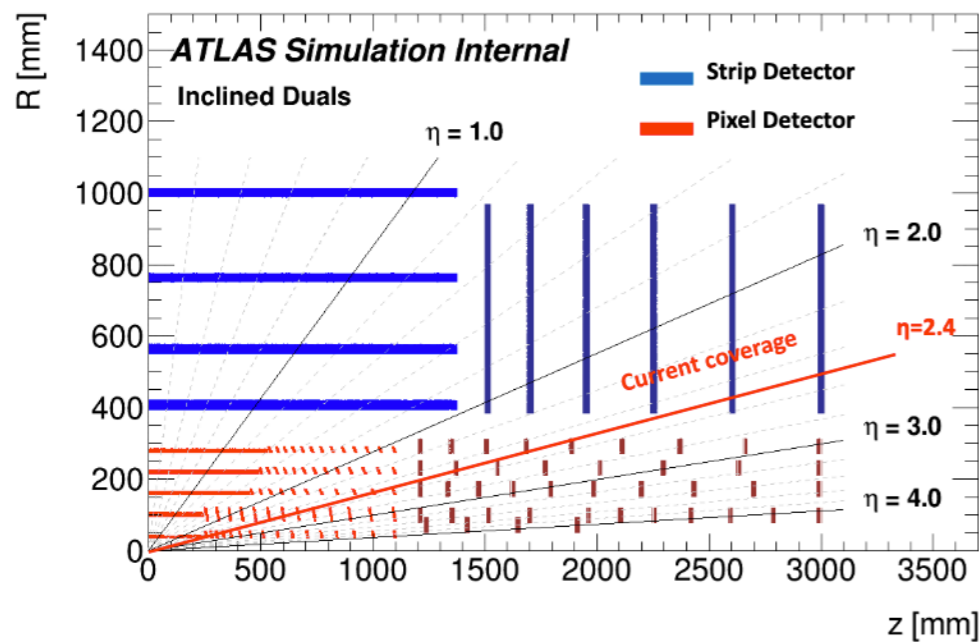


# $\mu^+e^-$ : Very asymmetric



All the particles go to the direction of the muon.

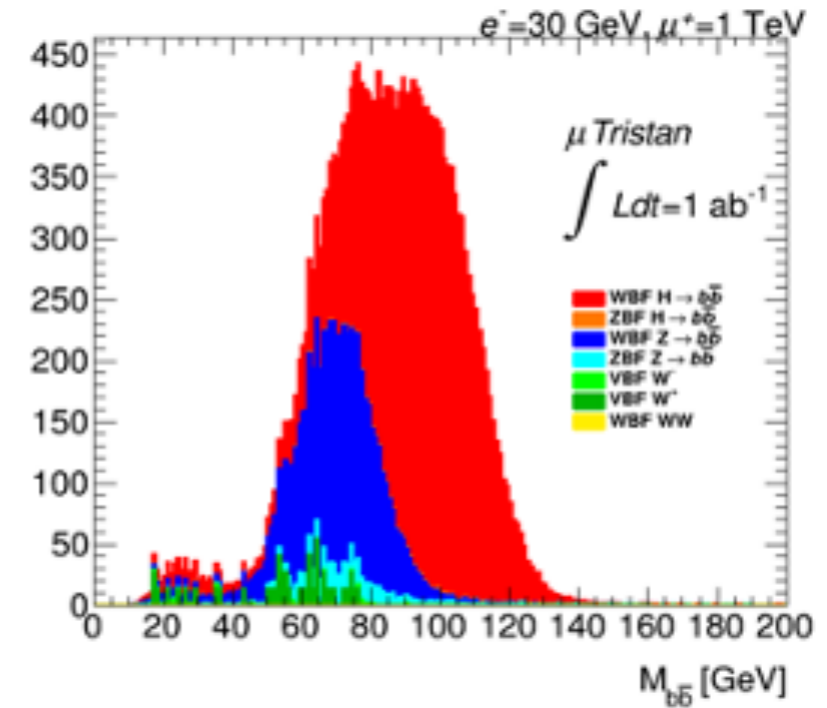
We need a coverage of  $\eta \sim -4$  ( $2^\circ$ ), which is the same level as the design of the ATLAS at HL-LHC.



# Higgs coupling

Study in progress in collaboration with Koji Nakamura and Sayuka Kita.

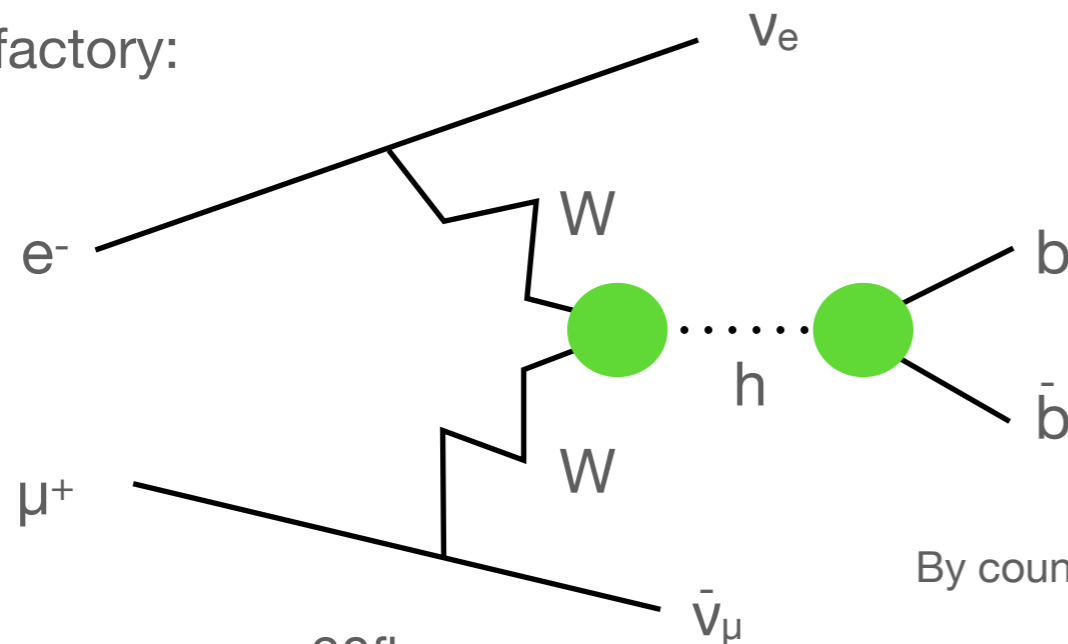
simulation with the ATLAS detector for HL-LHC



acceptance  $\sim 23\%$

(This should improve a lot with a detector designed for this collider.)

Higgs factory:



$\sim 90\text{fb}$

$\sim 10^5$  Higgs bosons

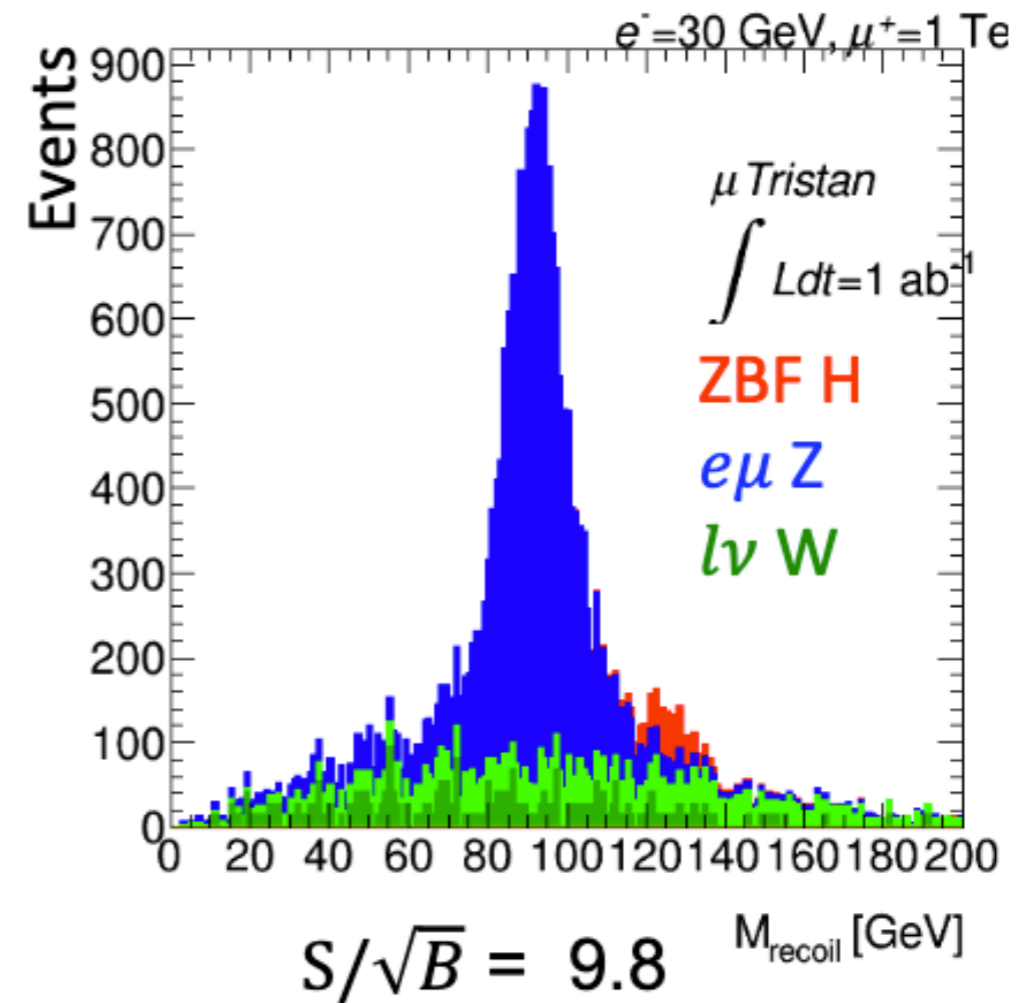
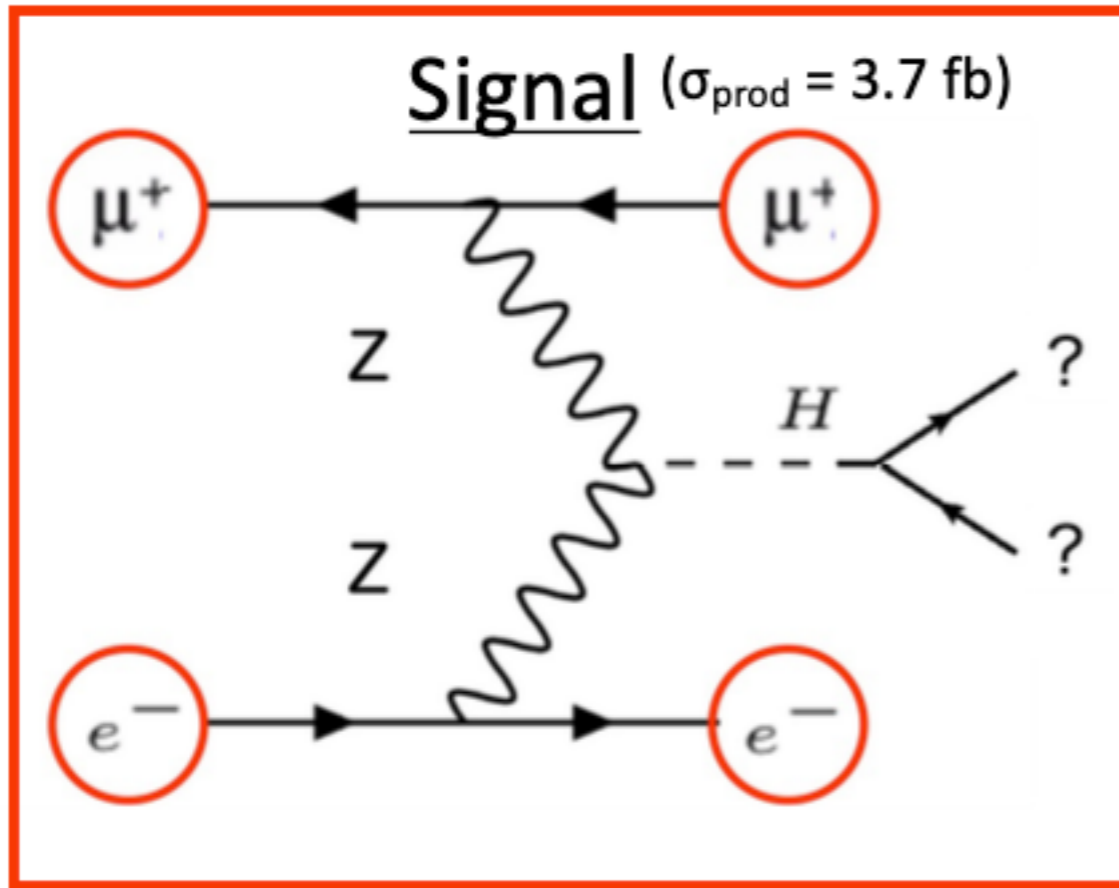
By counting the number of events and compare with the SM prediction

$$\Delta(\kappa_W + \kappa_b - \kappa_H)_{\text{stat}} = \frac{1}{2} \frac{1}{\sqrt{N(\text{WBF}) \times \text{Br}(h \rightarrow b\bar{b}) \times \text{efficiency}}}$$

$$= 3.1 \times 10^{-3} \times \left( \frac{\text{integrated luminosity}}{1.0 \text{ ab}^{-1}} \right)^{-1/2} \left( \frac{\text{efficiency}}{0.5} \right)^{-1/2}$$

sub percent level measurements.

# Z boson fusion recoil mass



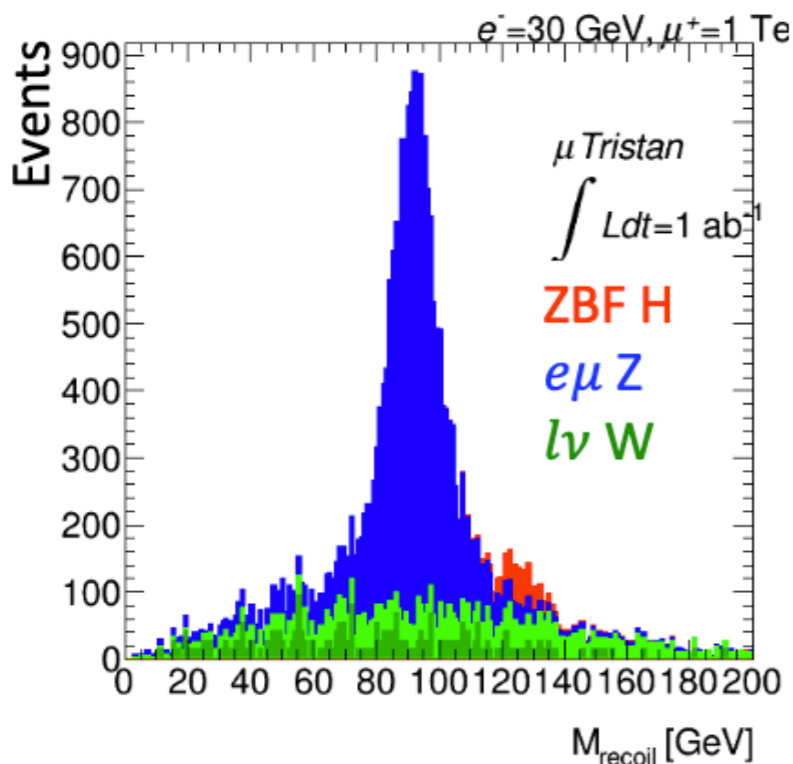
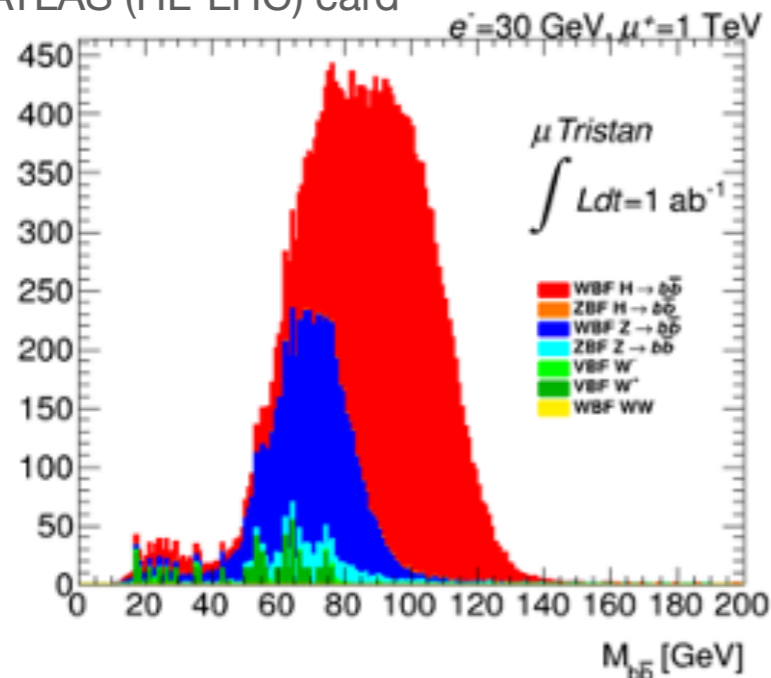
→ 1k events @ 1  $\text{ab}^{-1}$

Total width may be measured.

# Detector matters

Delphes

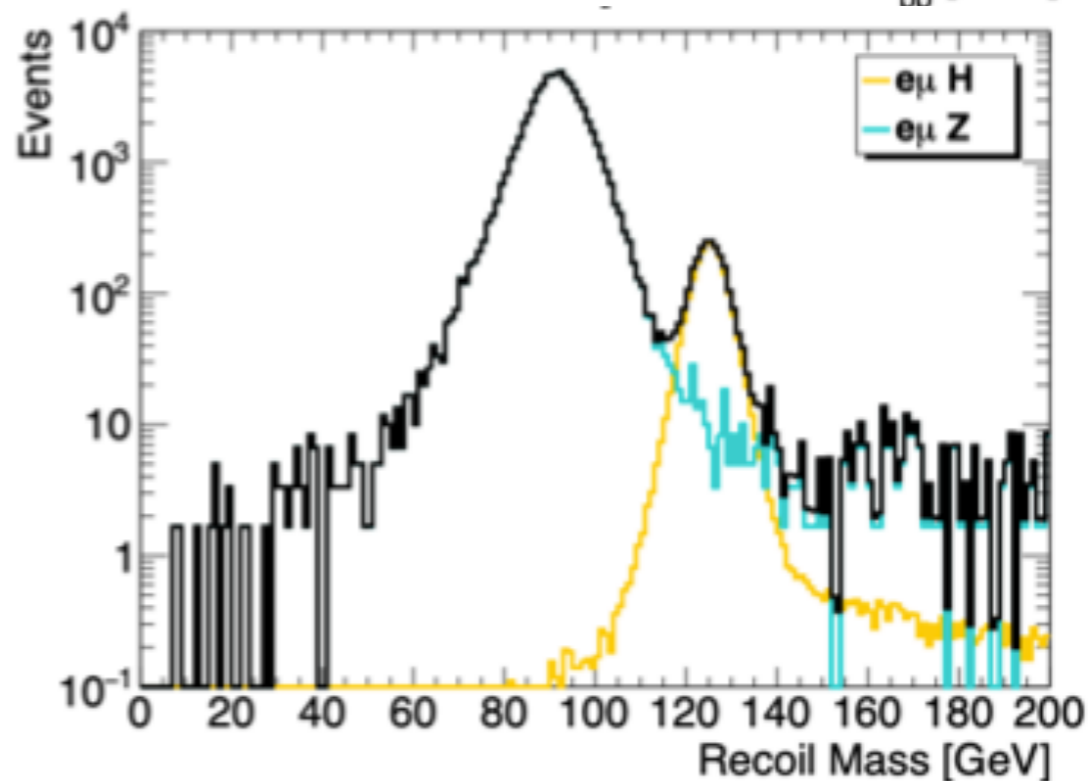
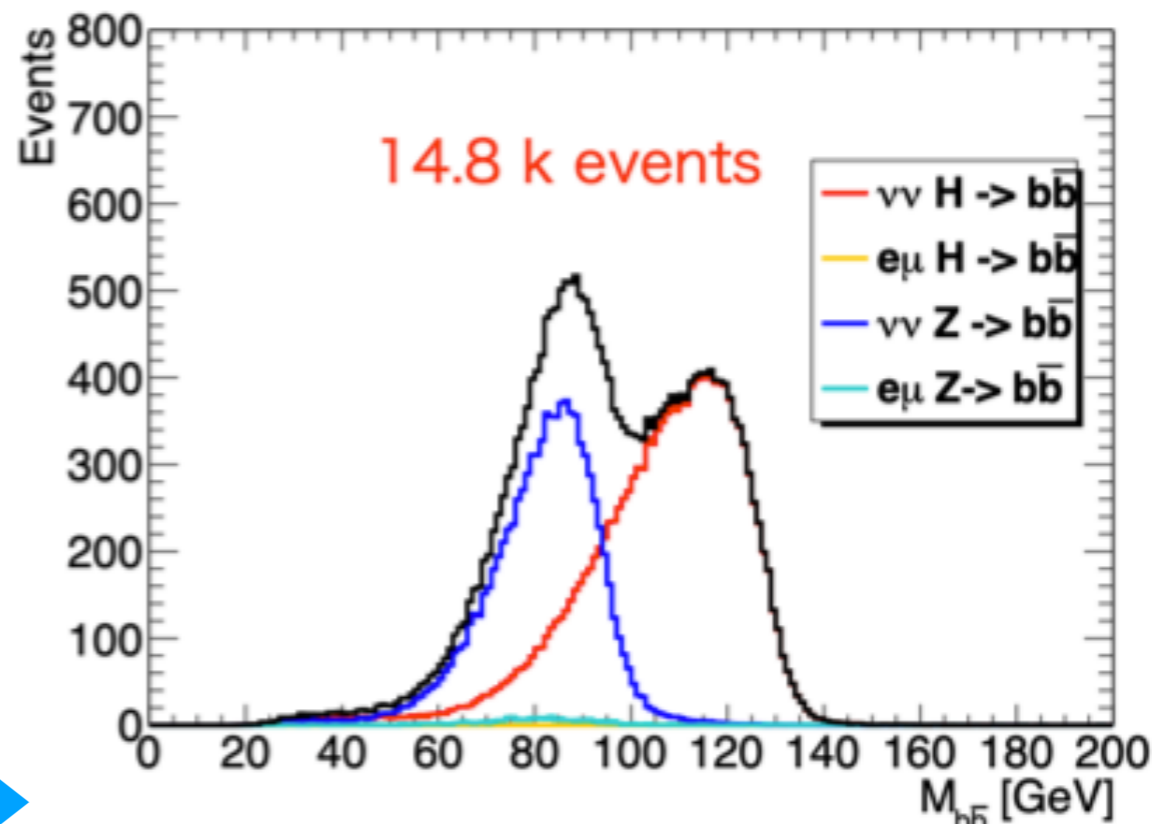
ATLAS (HL-LHC) card



Delphes

Much better!

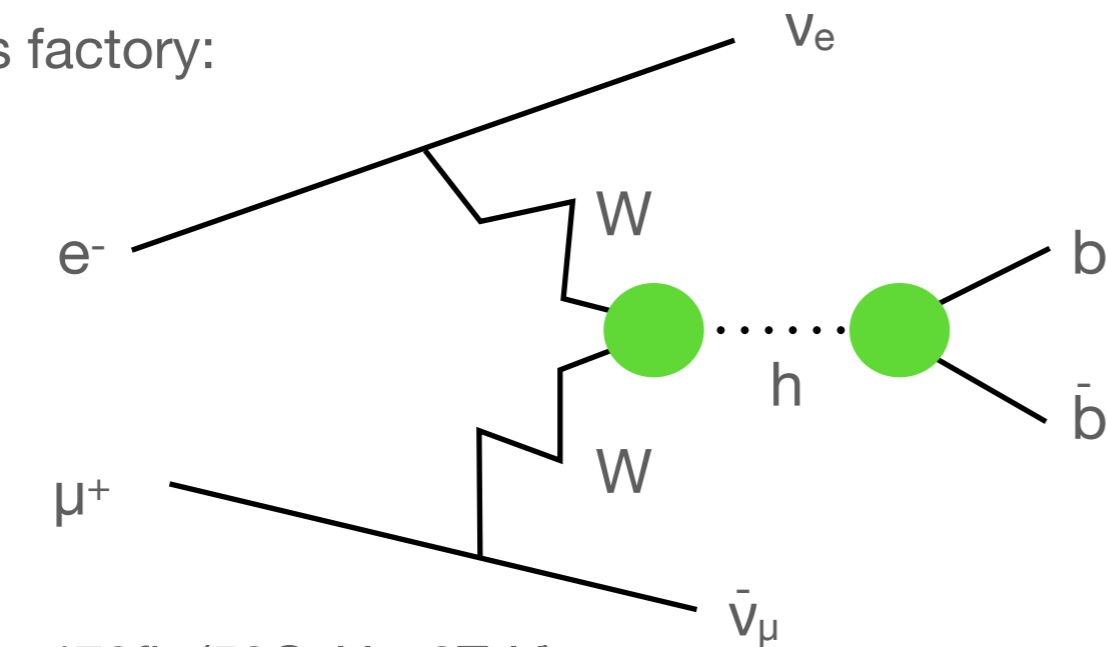
ATLAS (LHC) card with a larger forward coverage



Studies underway.

# Higher energy? $\mu$ Tevatron?

Higgs factory:



$\sim 472 \text{ fb}$  ( $50 \text{ GeV} \times 3 \text{ TeV}$ )

$\sim 5 \times 10^5$  Higgs bosons ( $\text{ab}^{-1}$ )

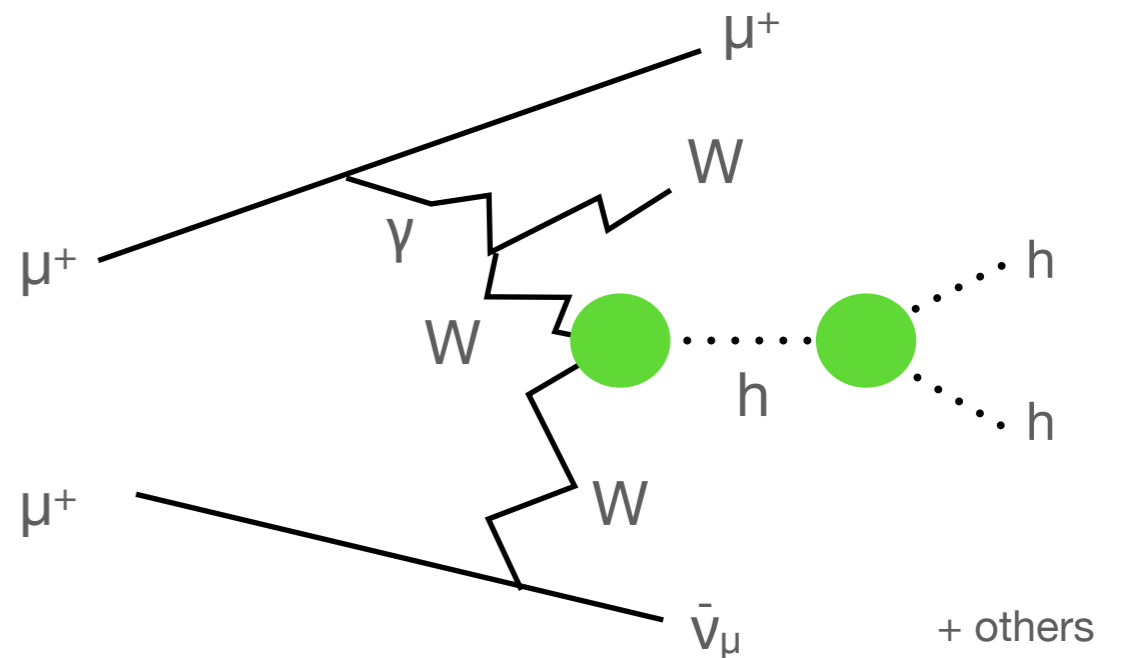
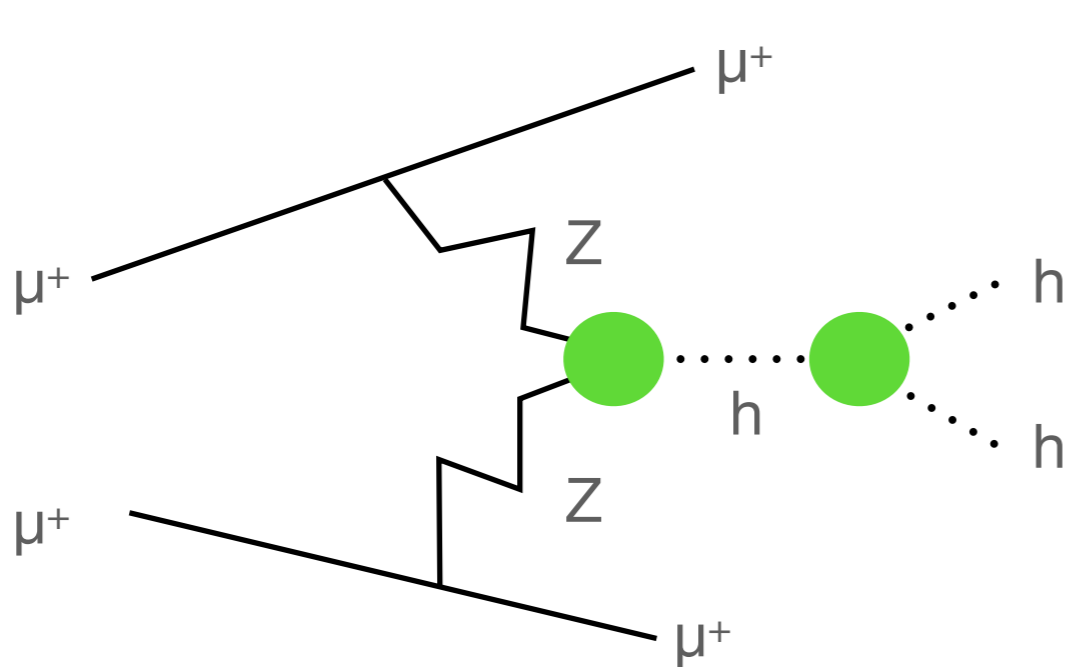
50 GeV electron + 3 TeV muon at a **6 km** ring

$$\sqrt{s} = 775 \text{ GeV}$$

hh production:  $89 \text{ events/ab}^{-1}$  (maybe we need more for coupling measurements)



# Higgs production@ $\mu^+\mu^+$

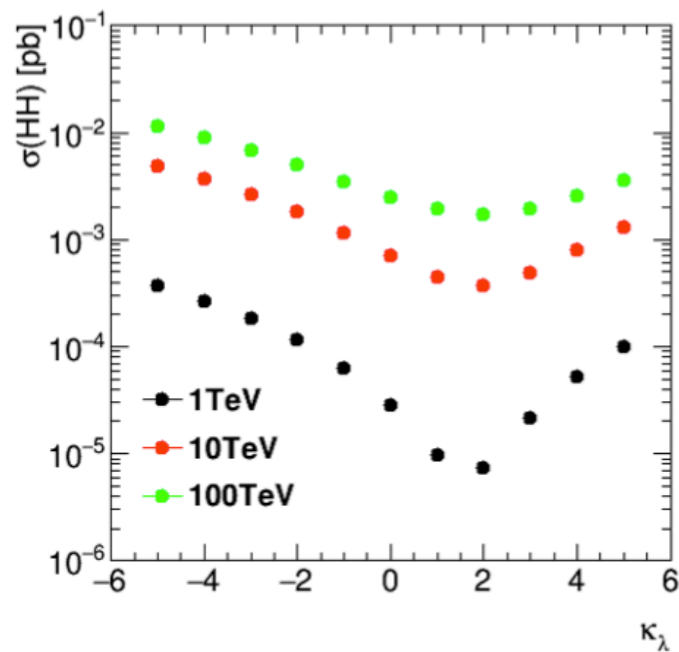


about 1/3 of  $\mu^+\mu^-$

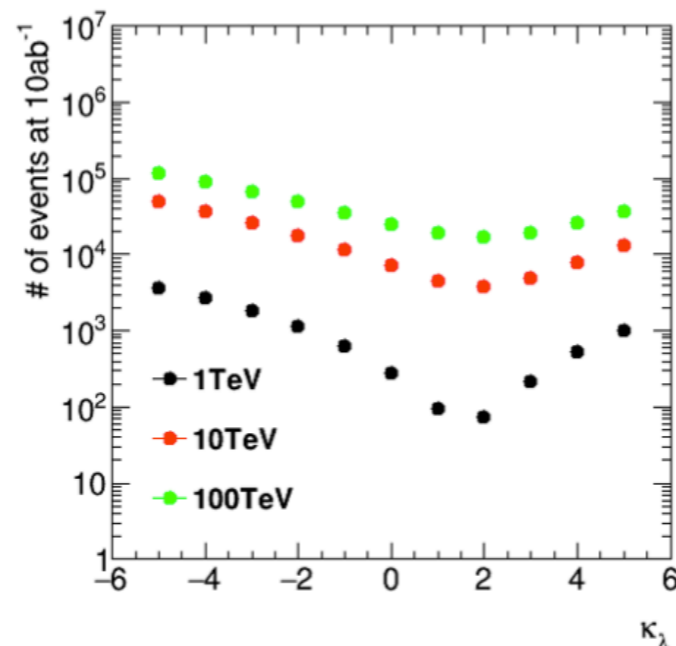
| $\sqrt{s}$ [TeV] | ZBF [fb] | Photon emission [fb] |
|------------------|----------|----------------------|
| 2                | 0.075    | 0.010                |
| 10               | 0.62     | 0.30                 |
| 20               | 1.1      | 0.75                 |

ZBF:

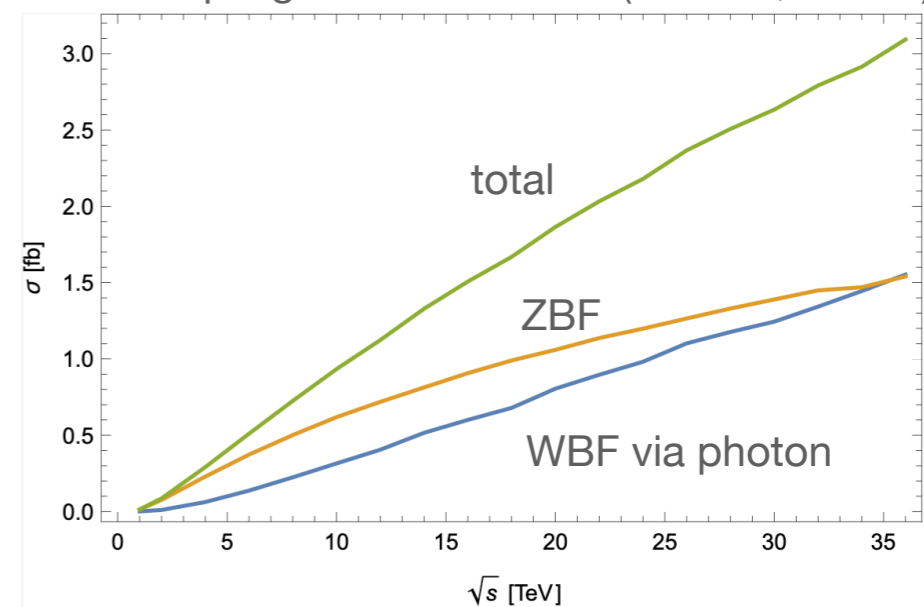
## Cross section



## # of Events in 10ab<sup>-1</sup>



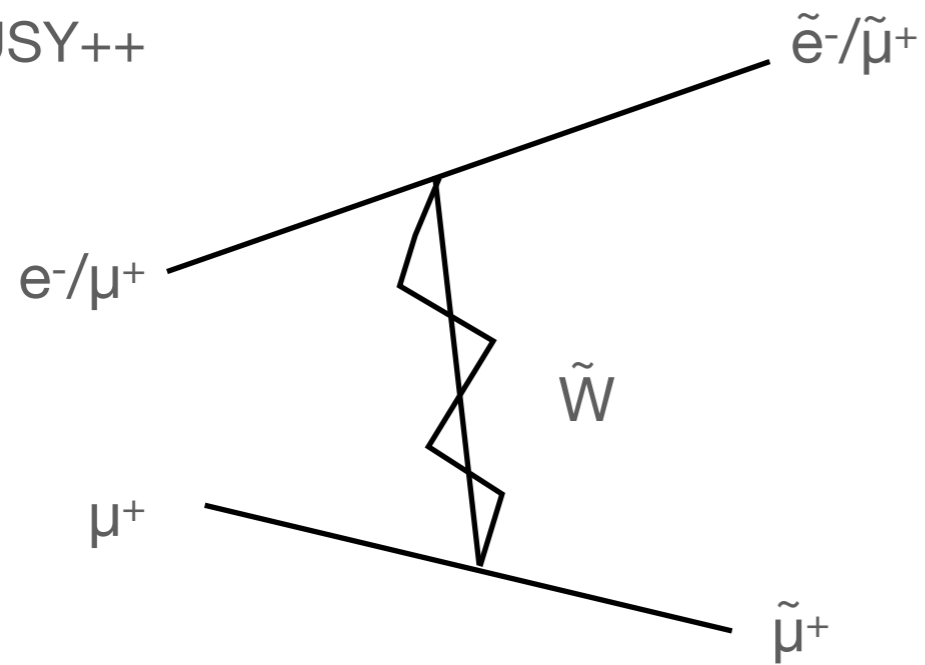
hhh coupling at 5-10% level? (@10TeV, 10ab<sup>-1</sup>)





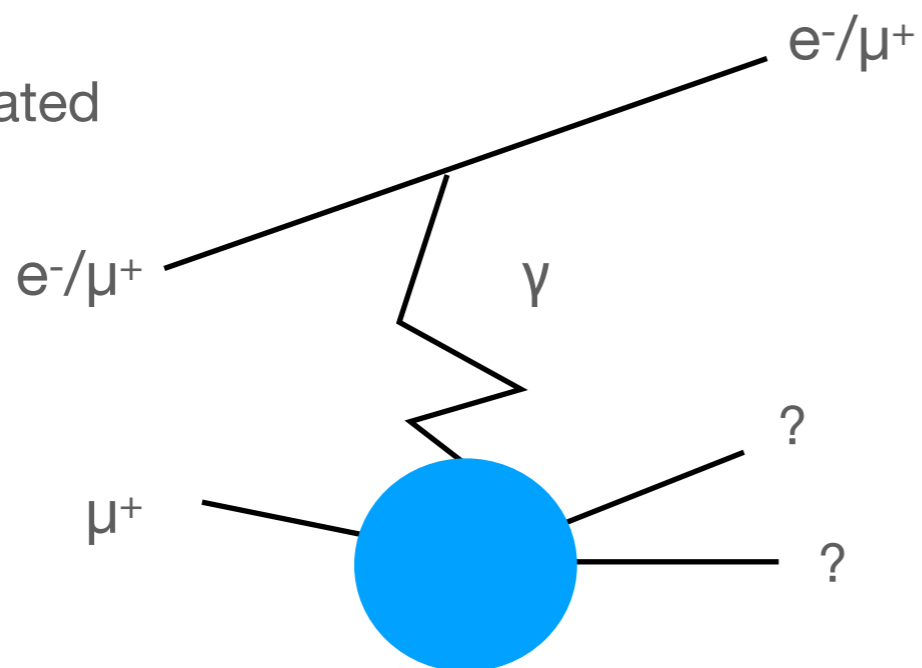
# New physics?

SUSY<sub>++</sub>

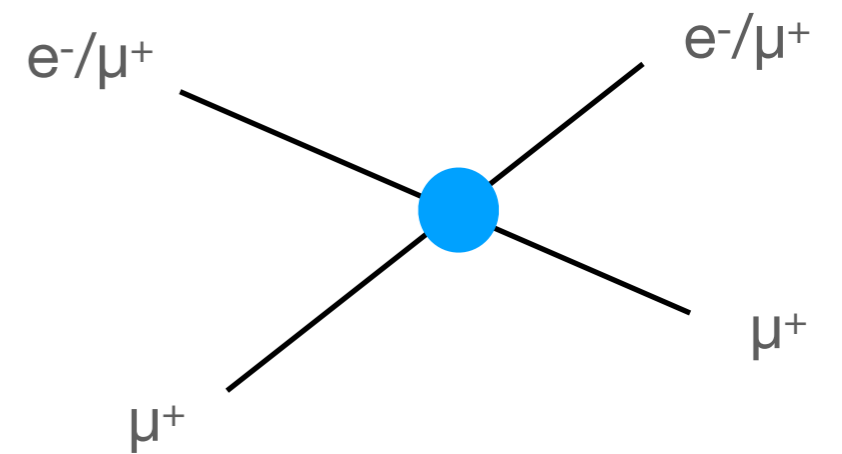
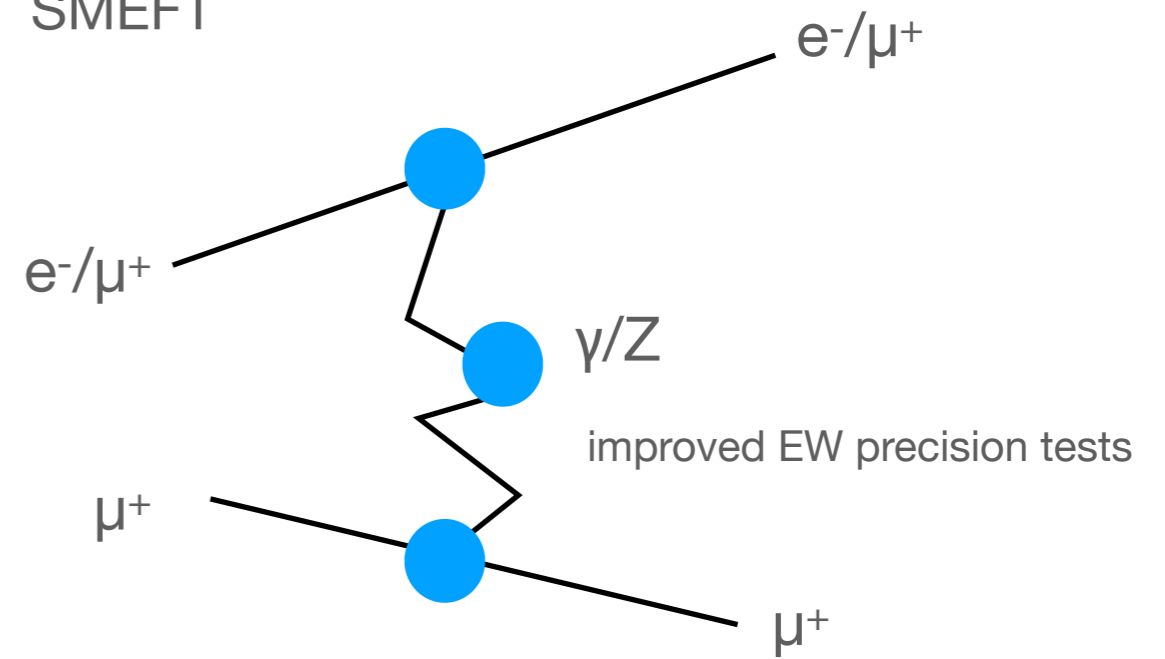


TeV mass new particles

$g-2$  motivated



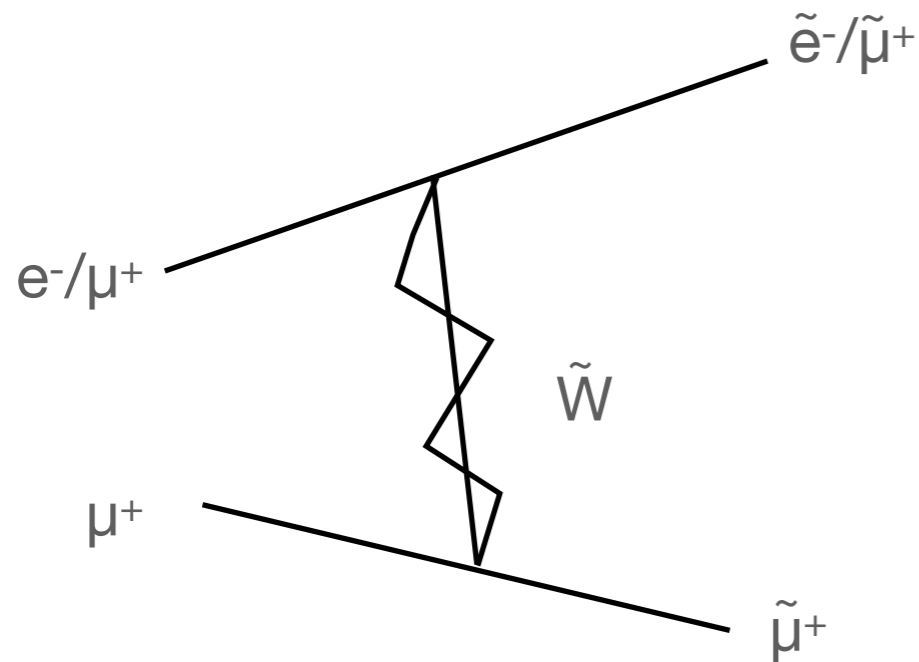
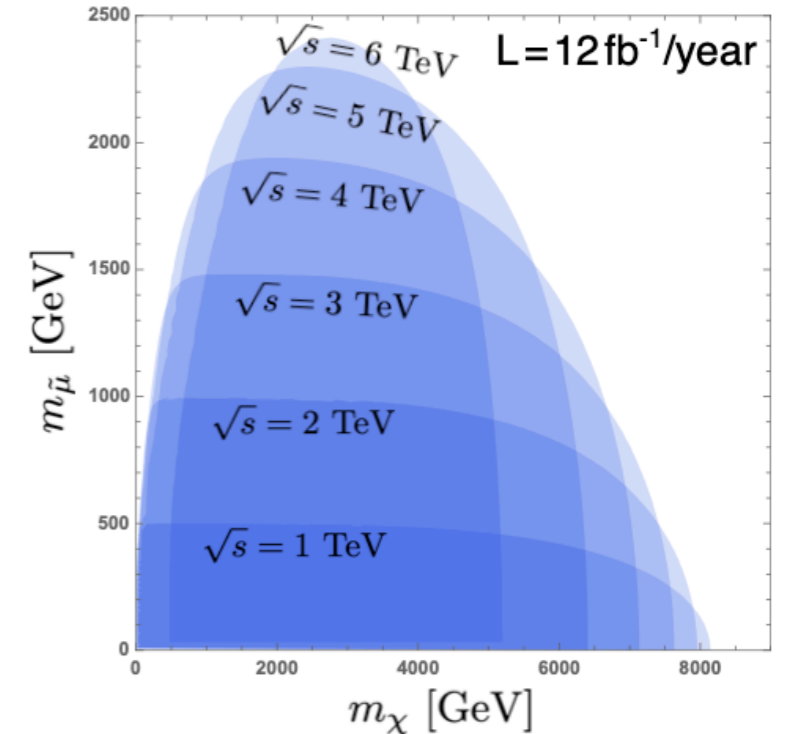
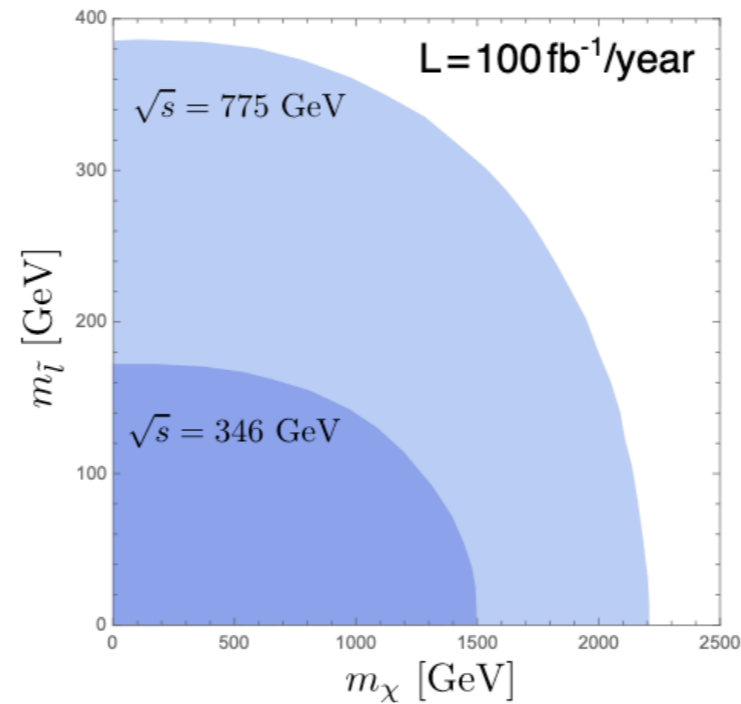
SMEFT



probe 100TeV scale physics!?

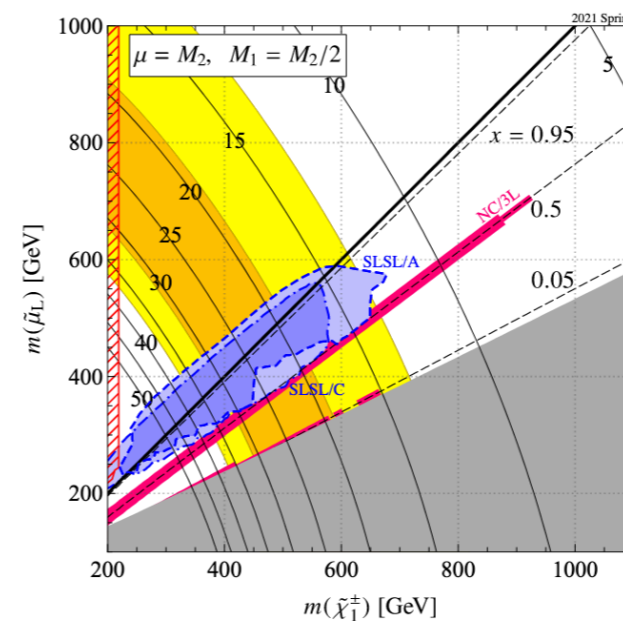
# Supersymmetry

Regions for  $N_{\text{event}}/\text{year} > 100$ .

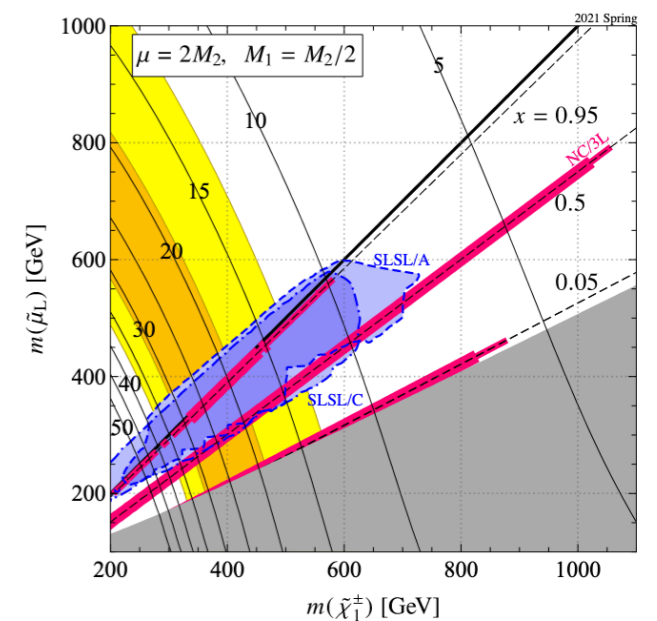


Scalar muons up to TeV even for very heavy gauginos.  
Almost completely cover the muon  $g-2$  motivated region.

[Endo, Hamaguchi, Iwamoto, Kitahara '21]



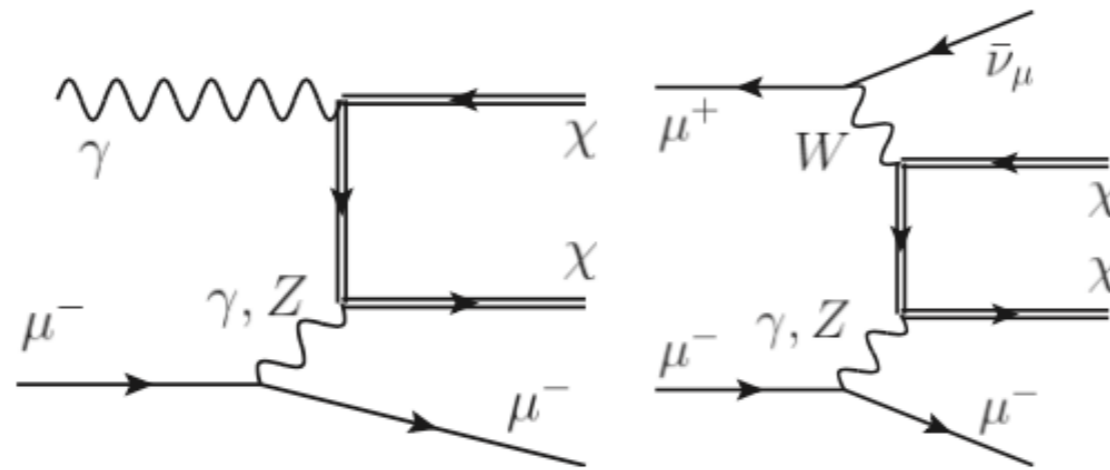
(A)  $\mu = M_2, M_1 = M_2/2$ .



(B)  $\mu = 2M_2, M_1 = M_2/2$ .

# DM?

study@ $\mu^+\mu^-$  [Han et al. '20]



same search is possible at  $\mu^+\mu^+$

mono- $\mu$

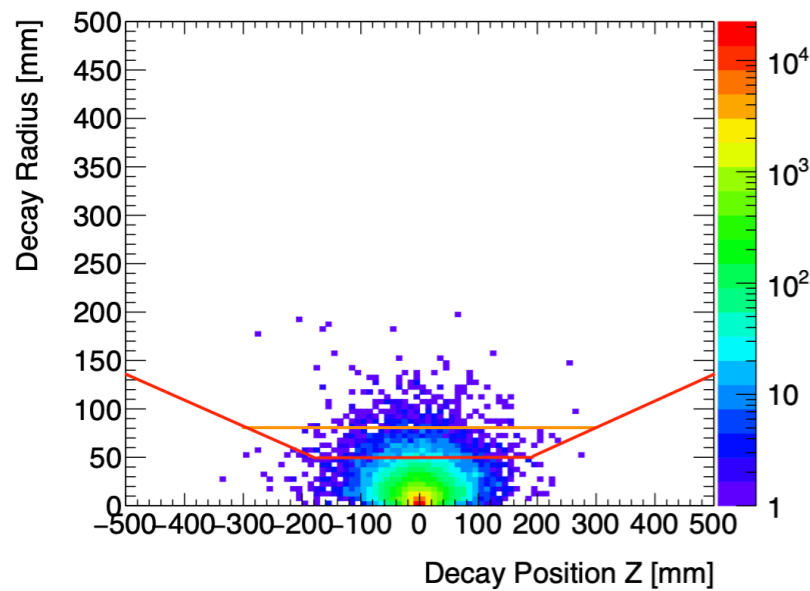
S/B is good in this process.

10TeV machine can cover 1TeV Higgsino and 1-2TeV Wino.

track + VBF search?

indirect search: [Fukuda, Moroi, Niki, Wei '23]

$\sqrt{s} = 10$  TeV, 質量 1 TeV Higgsino の崩壊マップ



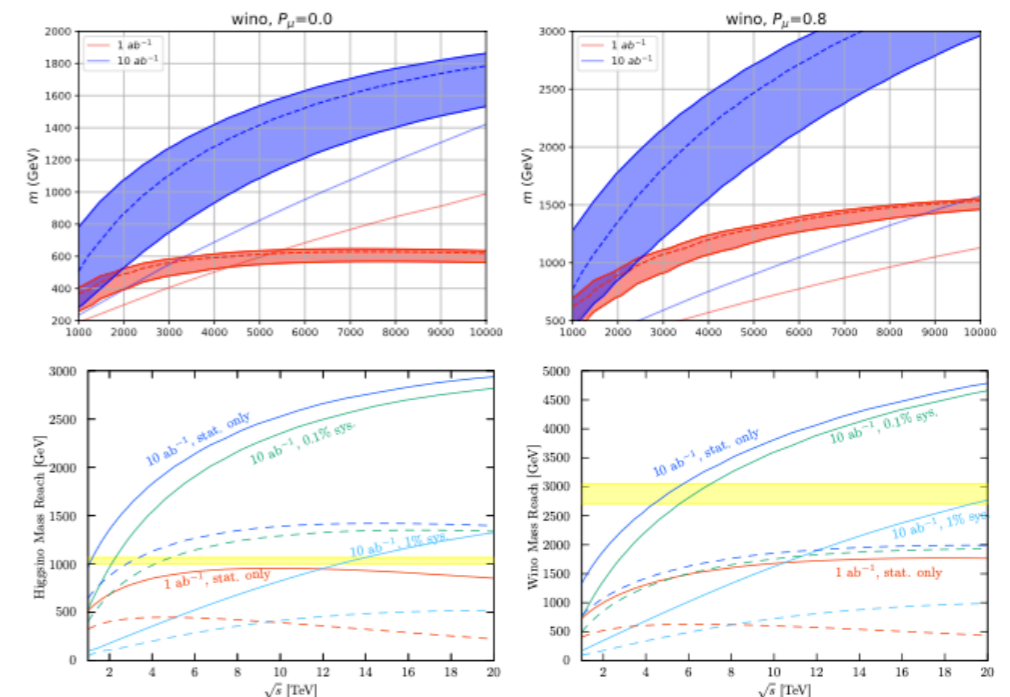
崩壊半径

- Case A > 80 mm
- Case B > 50 mm

$|\eta| < 2.0$

を再構成できると仮定

[with T. Kaji, T. Yoshida, K. Yorita in progress]

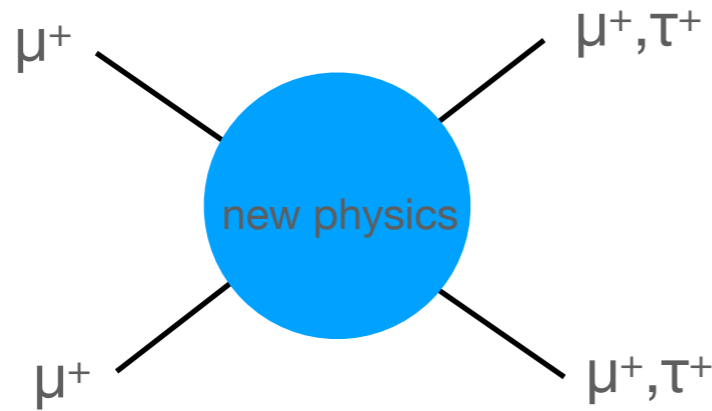


(a) Higgsino

(b) Wino

[Okabe, Shirai '23]

# muon specific



elastic scattering and lepton flavor violating scattering.

$\mu^+\mu^+$  has a big advantage in looking for new physics associated with the muon.

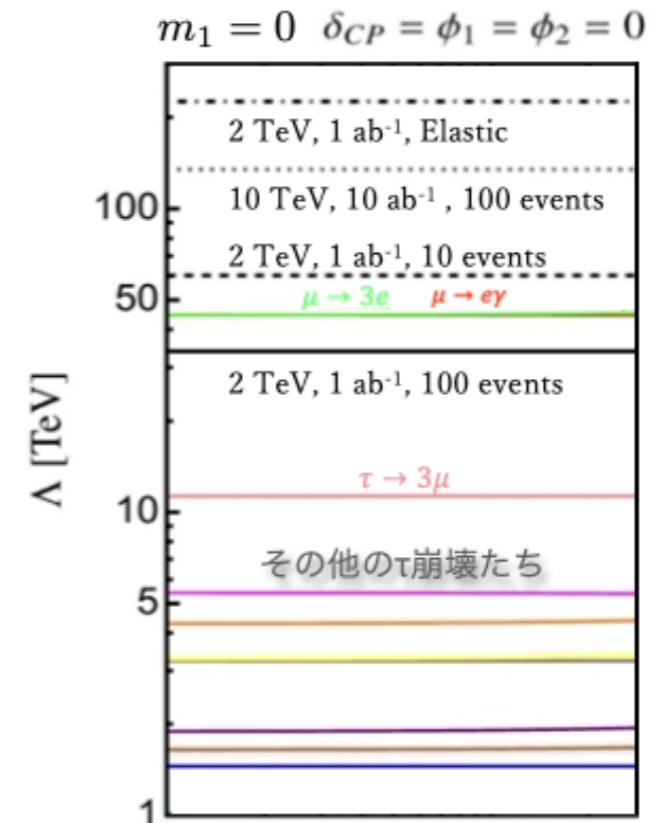
reach to O(100)TeV physics!

[Fridell, RK, Takai '23]

[Hamada, RK, Matsudo, Takaura '22]

|                               | RR      | LL      | RL      |
|-------------------------------|---------|---------|---------|
| $C_{HWB}$                     | 10 TeV  | 9.4 TeV | 2.3 TeV |
| $C_{HD}$                      | 5.5 TeV | 3.5 TeV | 2.3 TeV |
| $C_{H\ell}^{(1)}$             | 8.0 TeV | 0       | 4.9 TeV |
| $C_{H\ell}^{(3)}$             | 14 TeV  | 7.0 TeV | 6.7 TeV |
| $C_{H\tau}$                   | 0       | 7.5 TeV | 5.3 TeV |
| $C_{\ell\ell}$                | 7.7 TeV | 5.0 TeV | 3.3 TeV |
| $C_{\ell\ell}^{\mu\mu\mu\mu}$ | 100 TeV | 0       | 0       |
| $C_{ee}^{\mu\mu\mu\mu}$       | 0       | 100 TeV | 0       |
| $C_{le}^{\mu\mu\mu\mu}$       | 0       | 0       | 46 TeV  |

Table 1: Constraints on SMEFT operators at 2-sigma level.  $\sqrt{s} = 2$  TeV. The bin size for  $\theta$  is taken as  $1^\circ$  and each bin covers the range  $\theta_i - 0.5^\circ < \theta < \theta_i + 0.5^\circ$ . The considered range of  $\theta_i$  is  $16^\circ \leq \theta_i \leq 164^\circ$ .



# Summary

$\mu^+$  may have a better chance. Interesting to consider a km size experiment as a relatively near future project.

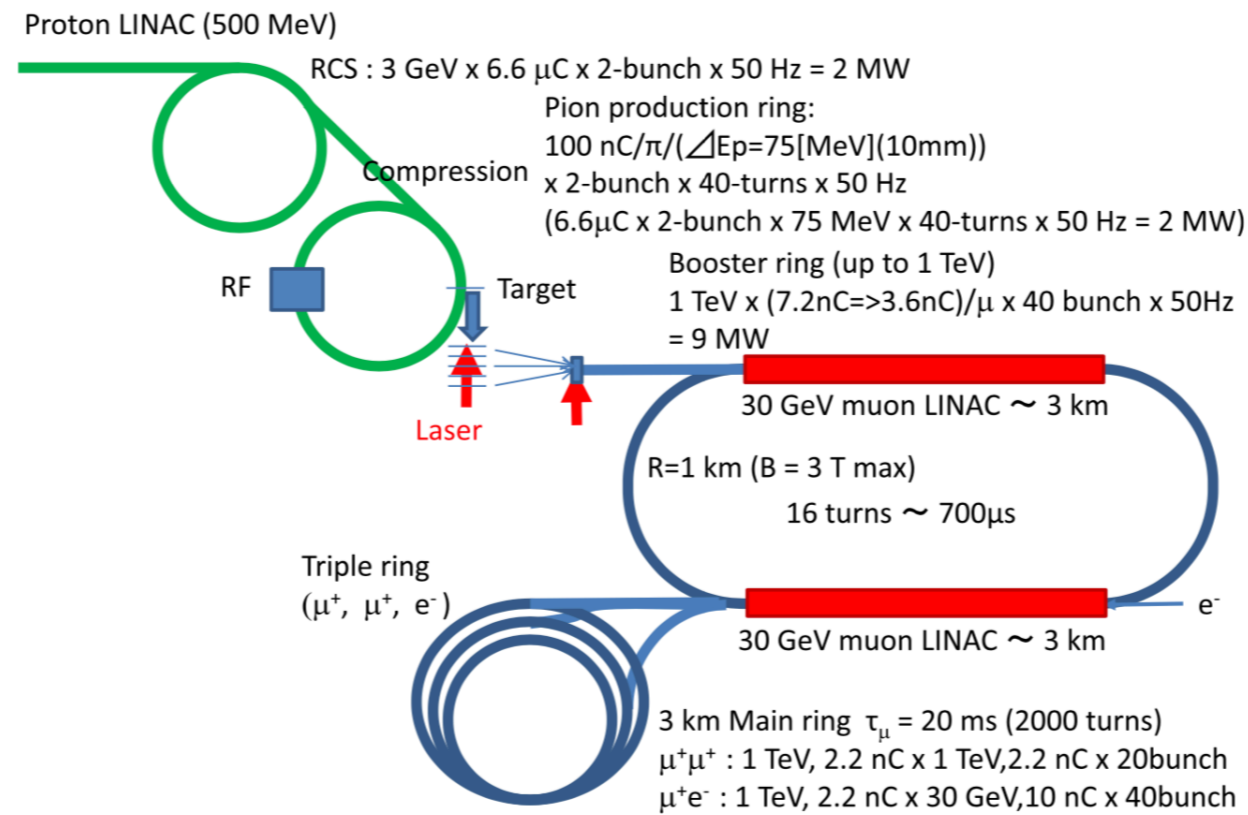


Fig. 1. Conceptual design of the  $\mu^+e^-/\mu^+\mu^+$  collider.

