



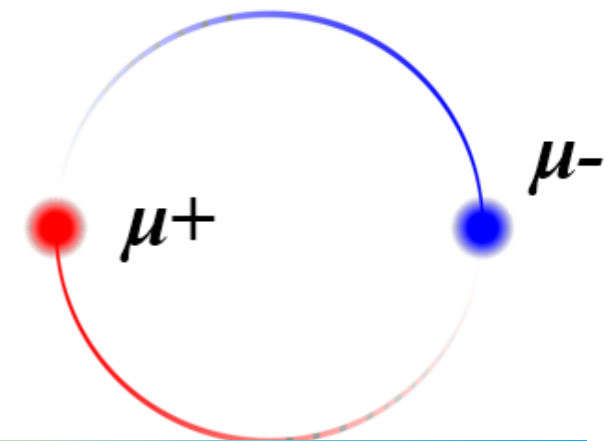
# DIMUS: Di-Muonium Spectroscopy Collider

Patrick Fox

(work with Sergo Jindariani and Vladimir Shiltsev)

Muons in Minneapolis

December 8, 2023

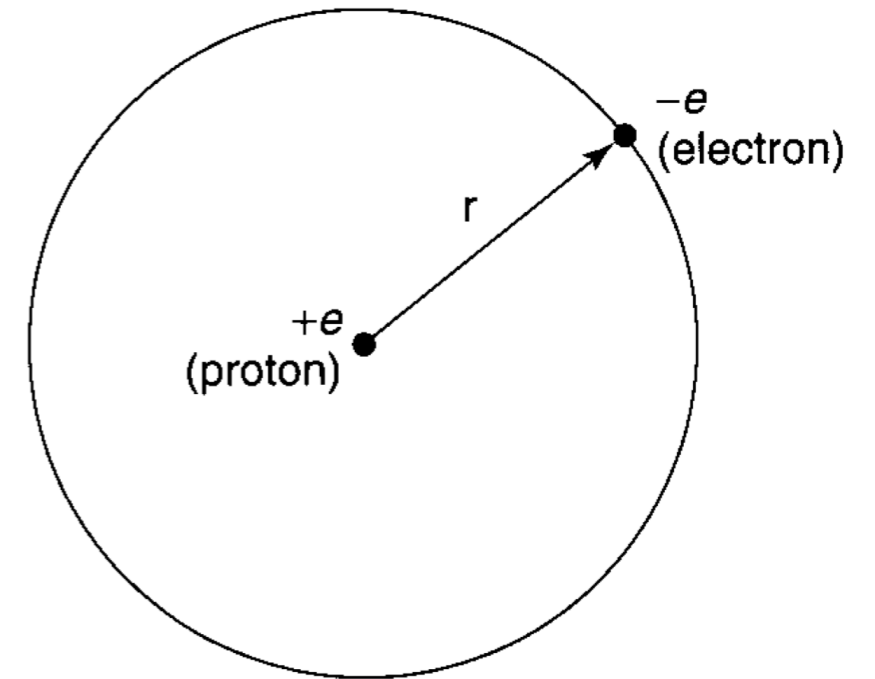


# Bound States of QED

- Hydrogen atom  $(p^+ e^-)$
- Positronium  $(e^+ e^-)$
- Muonium  $(\mu^\pm e^\mp)$
- “True” Muonium/Dimuonium  $(\mu^+ \mu^-)$
- More exotic di-leptonic resonances  $(\tau^\pm \ell^\mp), (\tau^+ \tau^-)$
- “Molecular systems”  $(e^+ e^-)(e^+ e^-)$
- Other atoms  $(\pi^\pm \mu^\mp)$

# Bound States of QED

The Bohr atom



$$E_n = -\frac{\alpha^2 \mu}{2n^2} \quad r_n = \frac{n^2}{\alpha \mu}$$

$$\psi_{nlm}(r, \theta, \varphi) = \sqrt{\left(\frac{2}{na_0^*}\right)^3 \frac{(n-l-1)!}{2n(n+l)!}} e^{-\rho/2} \rho^l L_{n-l-1}^{2l+1}(\rho) Y_l^m(\theta, \varphi)$$

Higher order corrections (fine and hyper-fine) e.g. relativistic, spin-orbit, Lamb shift, spin-spin, lift  $n^2$  degeneracy

# True muonium/Dimuonium

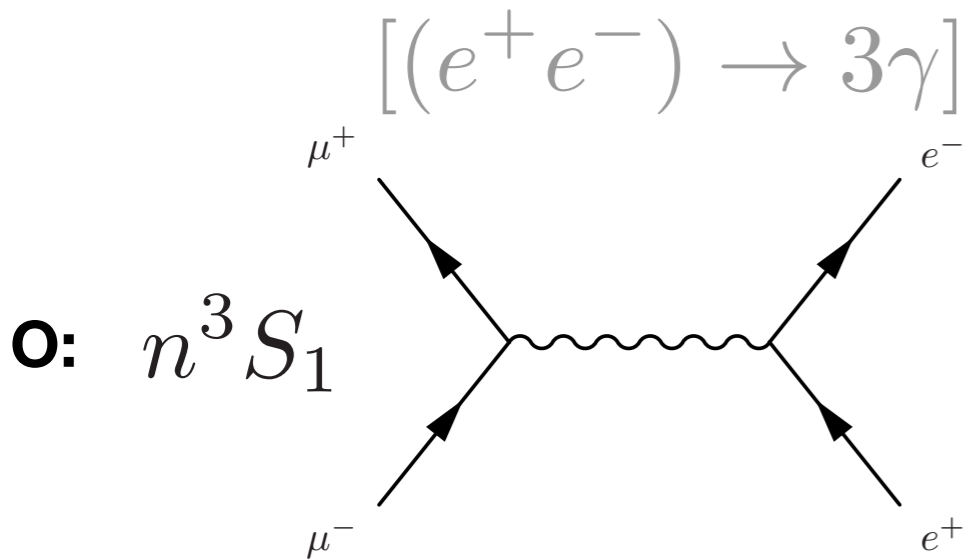
Rescale positronium. Mass is  $2m_\mu - E_1$

$$E_1(H) = -13.6 \text{ eV} \quad E_1(e^+e^-) = -6.8 \text{ eV} \quad \underline{E_1(\mu^+\mu^-) = -1407 \text{ eV}}$$

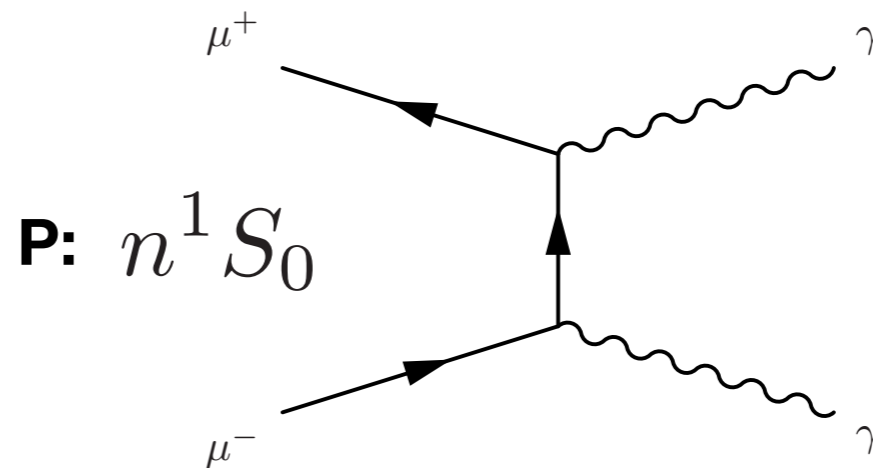
$$r_1(H) = a_0 = 53000 \text{ fm} \quad r_1(e^+e^-) = 2a_0 \quad \underline{r_1(\mu^+\mu^-) = 530 \text{ fm}}$$

Unlike positronium there are fermionic decays (for S levels)

$$\Gamma \propto |\psi(0)|^2$$



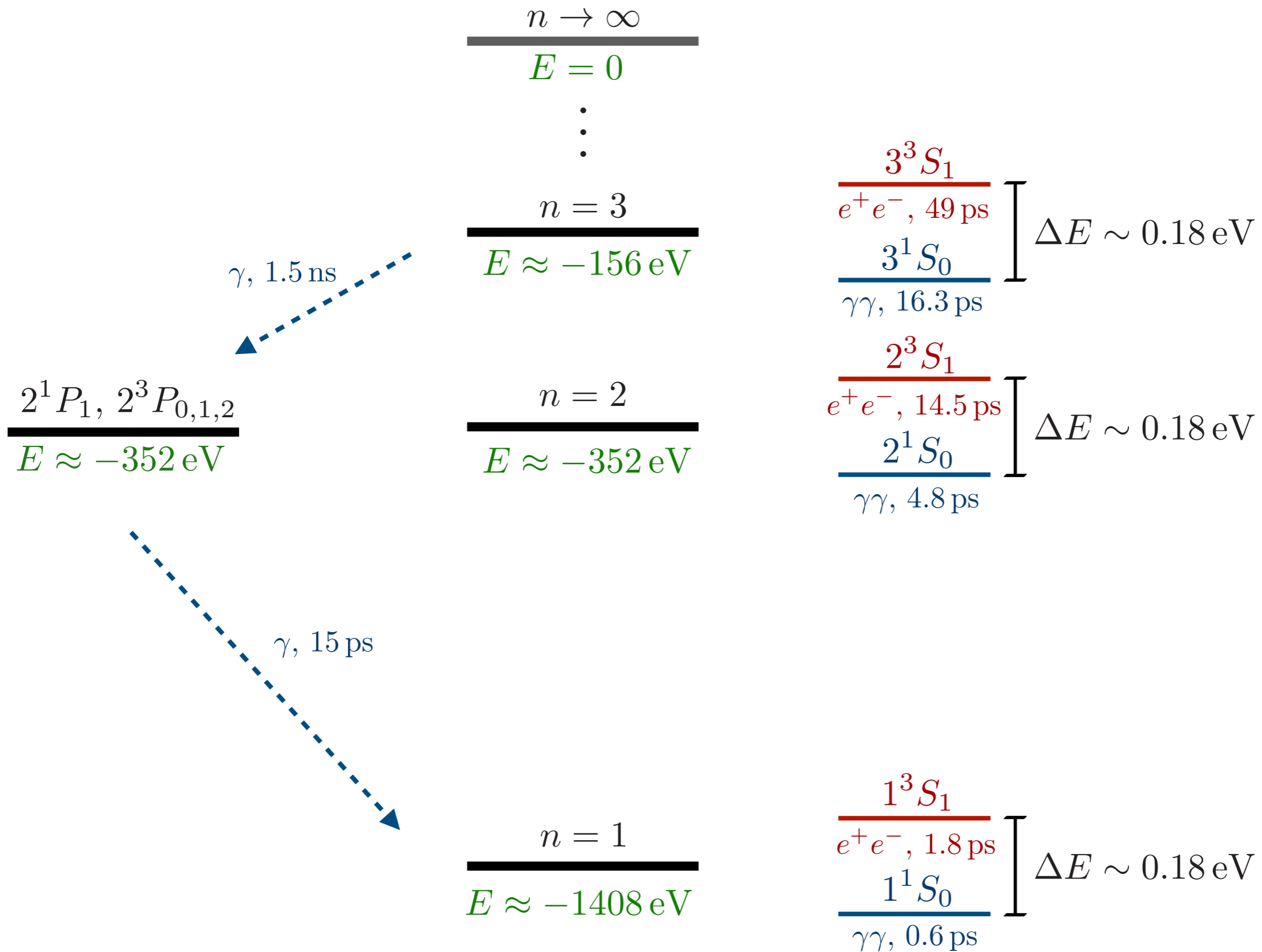
$$\tau = \frac{6n^3}{\alpha^5 m_\mu}$$



$$\tau = \frac{2n^3}{\alpha^5 m_\mu}$$

$$n^{2s+1}l_J$$

# Muonium spectrum and decays



$$n^{2s+1}l_J$$

# Possible TM Production Processes

- Storied history: pion collisions, electron beams, photon beams, RHIC...

More recently:

Banburski and Schuster [1206.3961]

- HPS, electron beam on a thin foil, production through 1/3 photon processes. Few hundred events

$$N_{TM} \sim \mathcal{O}(100) \times \left( \frac{I \times T}{450 \text{ nA} \times \text{month}} \right)$$

- Eta decays at LHCb

Vidal et al [1904.08458]

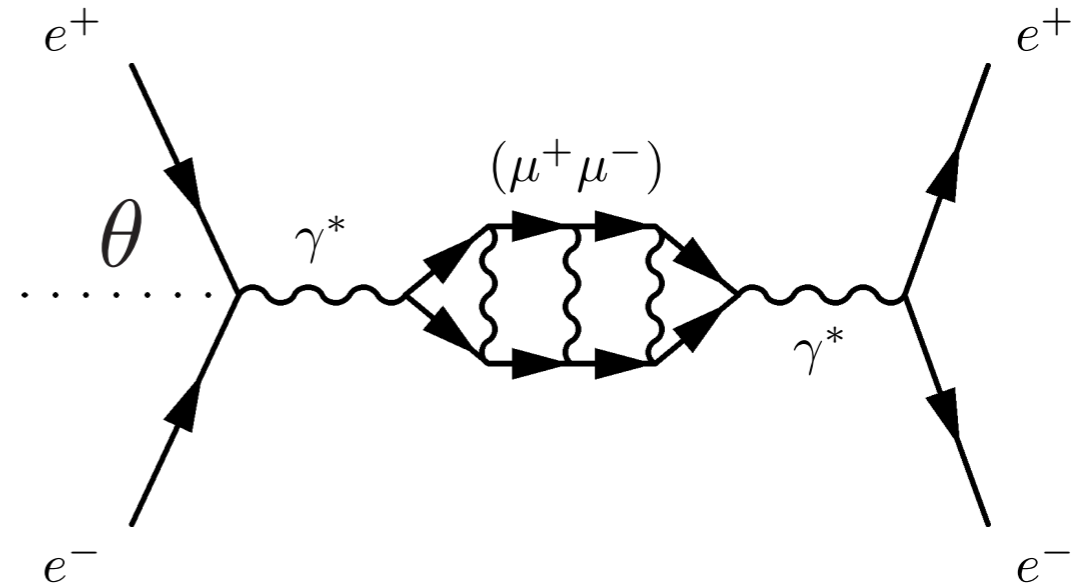
$$\text{BR}(\eta \rightarrow \gamma[\mu^+ \mu^-]) \sim 5 \times 10^{-10}$$

Look for displaced electron pair, w/ or w/o a photon  
Expect 100-1000 events after Run 3

# Another True Muonium Production

## Fool's Intersection Storage Ring

Brodsky & Lebed [0904.2225]



- Produces  $n^3S_1$  states with relative rate  $n^{-3}$

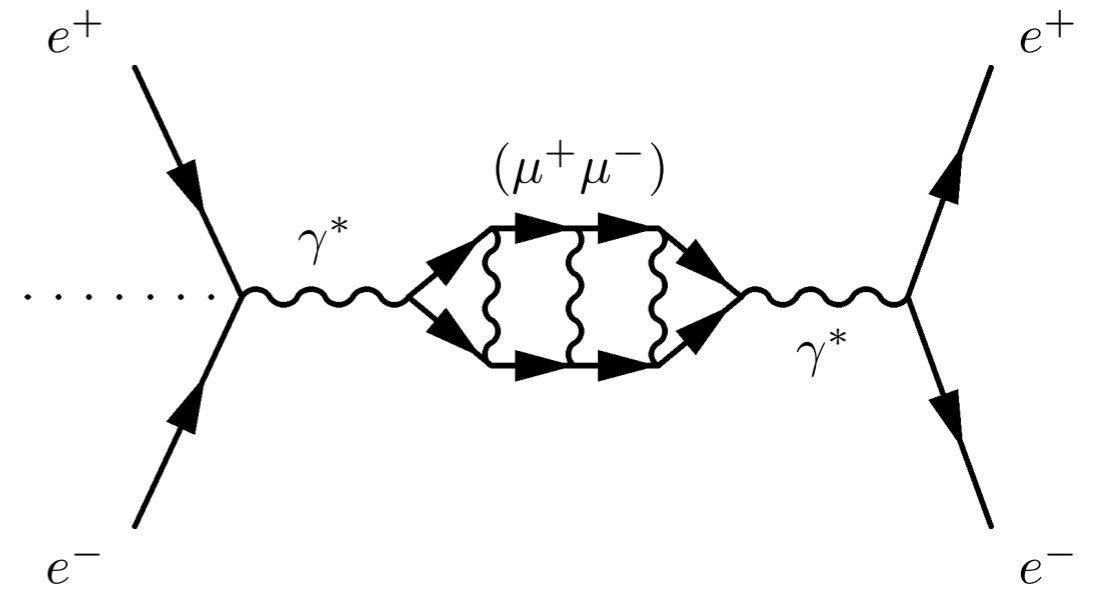
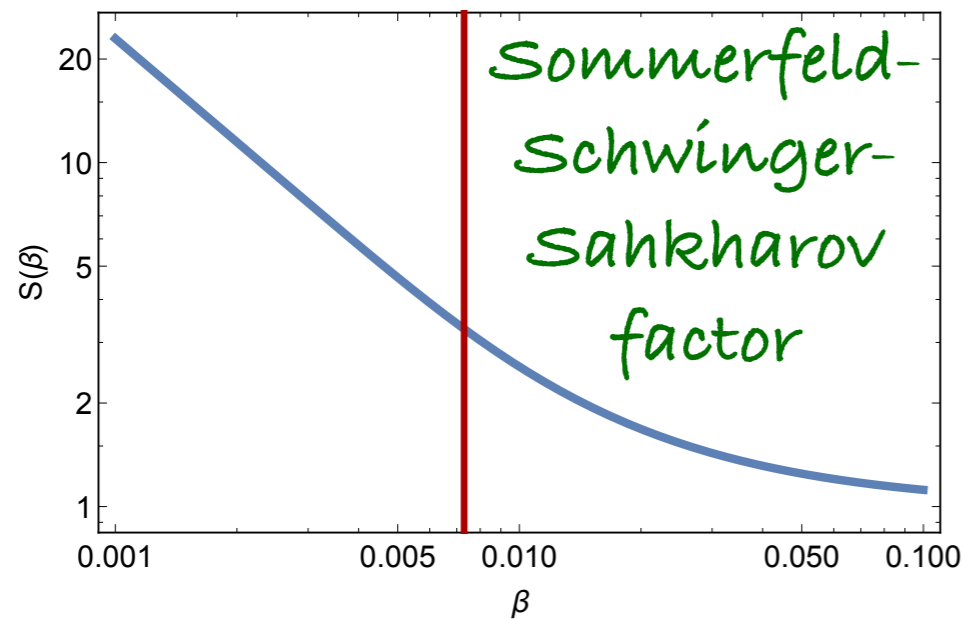
- For symmetric beam energies  $p_z = \frac{2m_\mu}{\tan \theta}$  and boost  $\gamma = \frac{1}{\tan \theta}$

- $E_{\text{beam}} = \frac{m_\mu}{\sin \theta}$

Boost is critical for separating signal from background (Bhabha)

$$c\tau(^3S_1) \approx 0.5 \text{ mm}$$

# Muonium Production



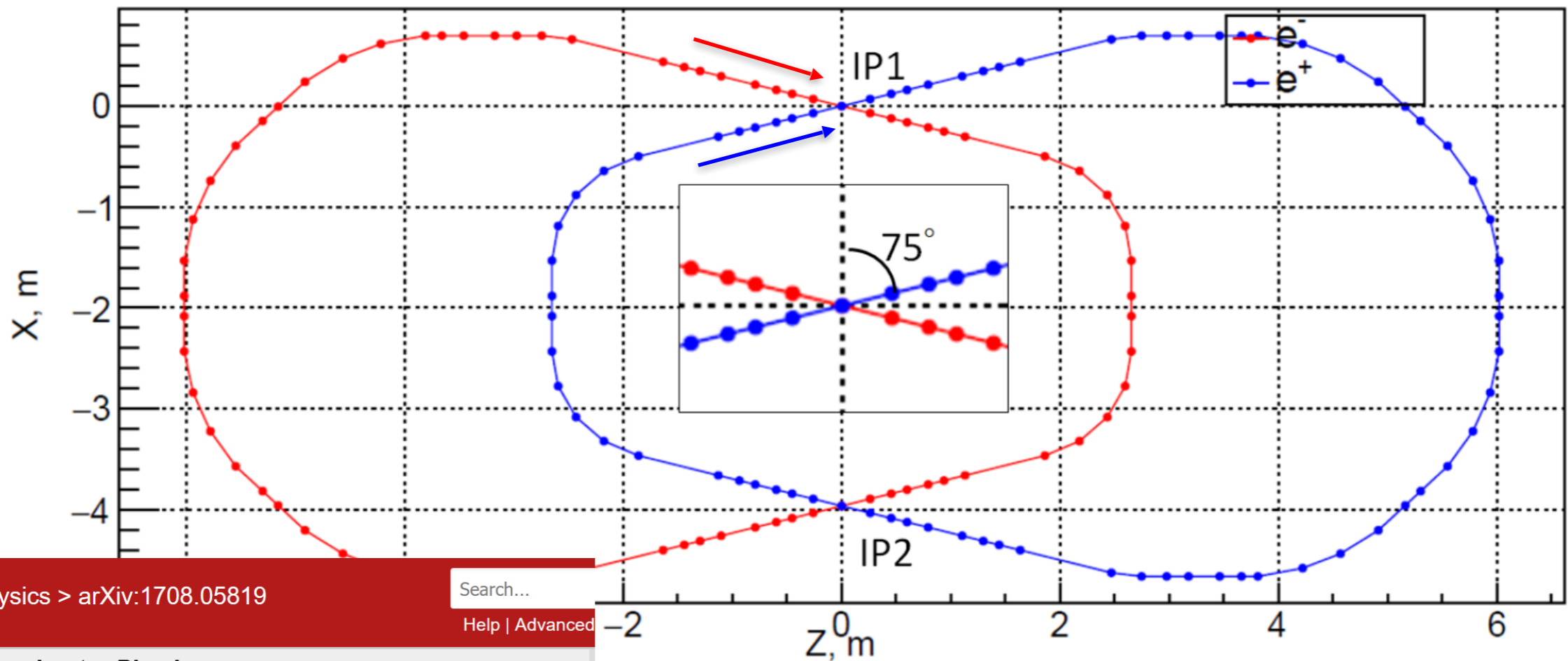
$$\sigma(e^+e^- \rightarrow \mu^+\mu^-) \Big|_{\beta \approx 0} = \frac{2\pi\alpha^2\beta}{s} \left(1 - \frac{\beta^2}{3}\right) S(\beta)$$

$$\sigma_{b.s} = \left(\frac{\pi^2\alpha^3}{2m_\mu^2}\right) \left(\frac{\alpha^2 m_\mu}{4\Delta E_e}\right) \sim \left(\frac{1\text{MeV}}{\Delta E_e}\right) 10^{-34} \text{cm}^2$$

$$\frac{\sigma_{b.s}}{\sigma_{Bhabha}} \sim \left(\frac{3\pi\alpha}{2}\right) \left(\frac{\alpha^2 m_\mu}{4\Delta E_e}\right) \sim \left(\frac{1\text{MeV}}{\Delta E_e}\right) 10^{-4}$$



# Novosibirsk “Mu-Mu-Tron” Design



arXiv.org > physics > arXiv:1708.05819

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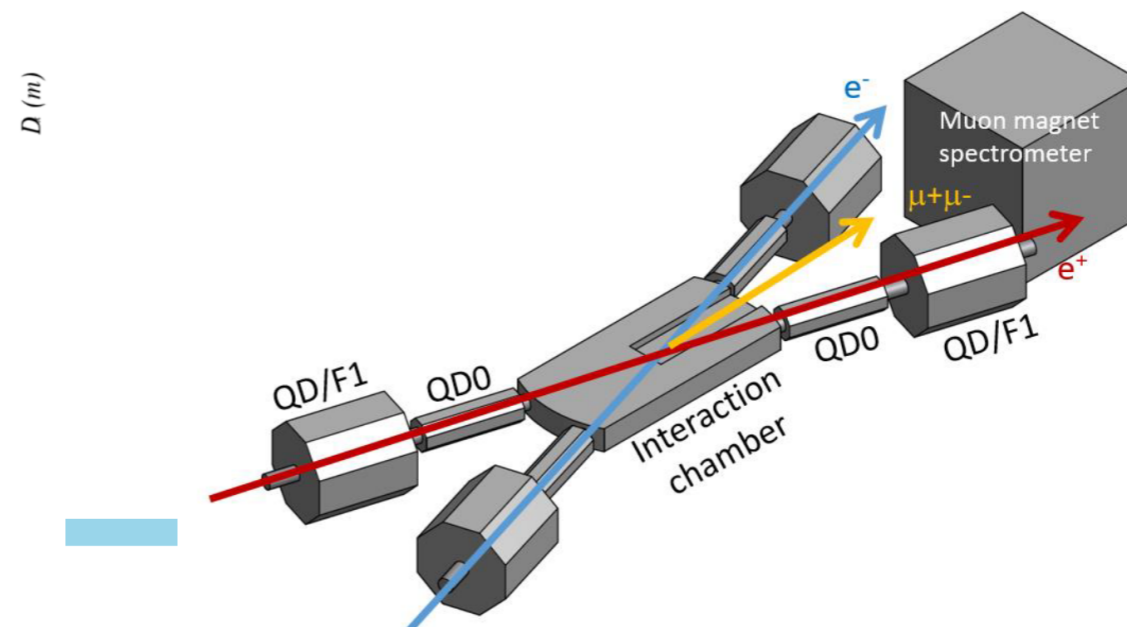
## Physics > Accelerator Physics

[Submitted on 19 Aug 2017]

### Low-energy electron-positron collider to search and study $(\mu^+\mu^-)$ bound state

A. Bogomyagkov, V. Druzhinin, E. Levichev, A. Milstein, S. Sinyatkin

We discuss a low energy  $e^+e^-$  collider for production of the not yet observed  $(\mu^+\mu^-)$  bound system (dimuonium). Collider with large crossing angle for  $e^+e^-$  beams intersection produces dimuonium with non-zero momentum, therefore, its decay point is shifted from the beam collision area providing effective suppression of the elastic  $e^+e^-$  scattering background. The experimental constraints define subsequent collider specifications. We show preliminary layout of the accelerator and obtained main parameters. High luminosity in chosen beam energy range allows to study  $\pi^\pm$  and  $\eta$ -mesons.



# Fermilab

- Public Areas
- not to scale



NORTH



Kirk Road

NML



Power Line Rd

Town Road

Wilson St.

Site 70

Wilson St

Road B

Site 37

Site 39

Site 65

Meson Area

Neutrino Area

Site 67

Proton Area

Site 50

Master Substation

Buffalo Farm

Technical Division

Road D

Bike Path

Fermilab Village

Lederman Science Center

Main Entrance

Feynman Computing Center

Pine St.

Bike Path  
NuMI/Minos  
MiniBoone

Antiproton Source

Wilson Hall & Ramsey Auditorium  
(Public Welcome)

CDF

C-Zero

Site 55

Dog Training Area

Bike Path

Batavia Rd

Lake Law  
Nature Area

A.E. Sea

East Gate  
to:  
Rt-59

Main Injector

Tevatron

D-Zero

Site 56

Site 3

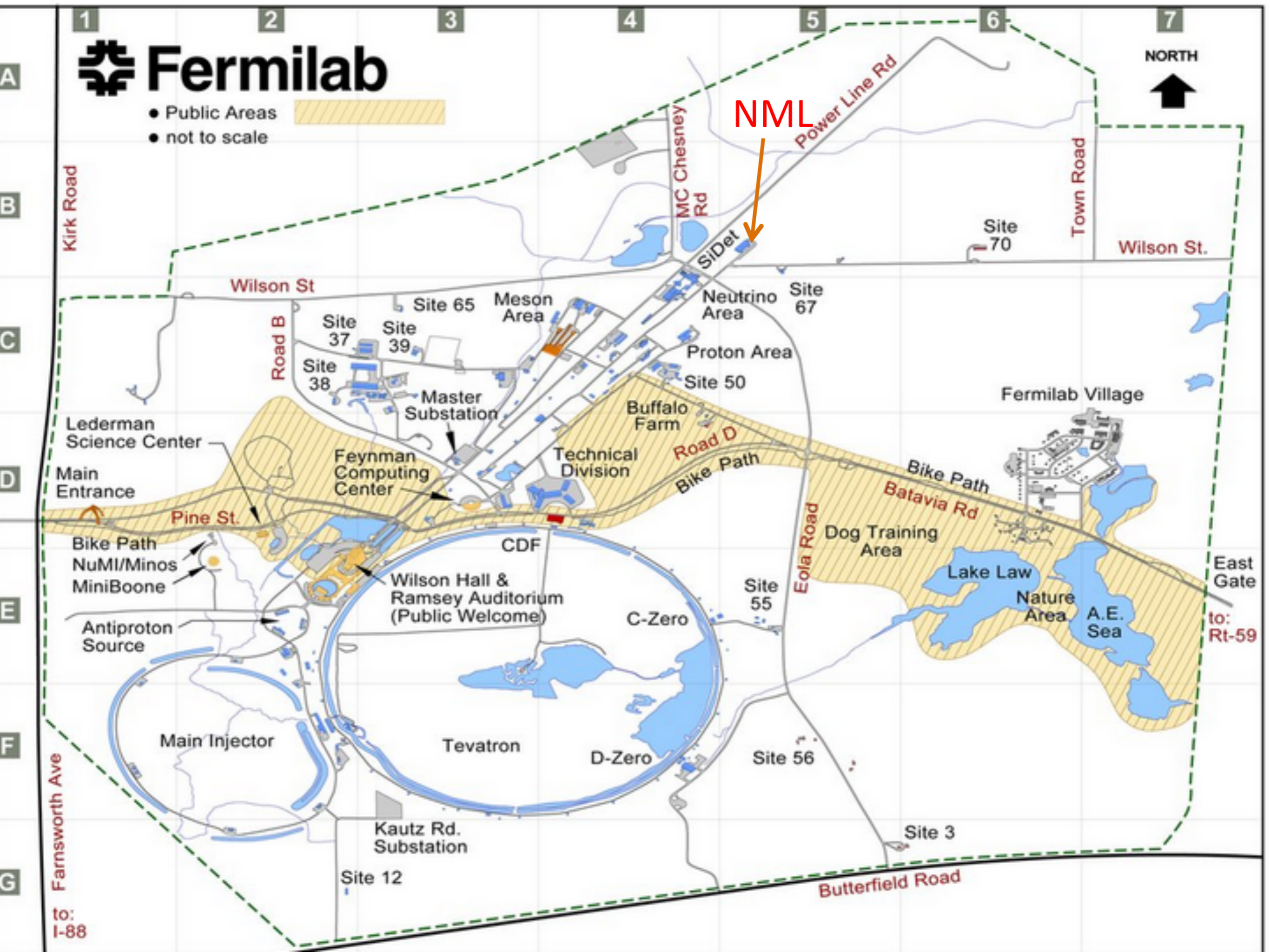
Kautz Rd.  
Substation

Site 12

Butterfield Road

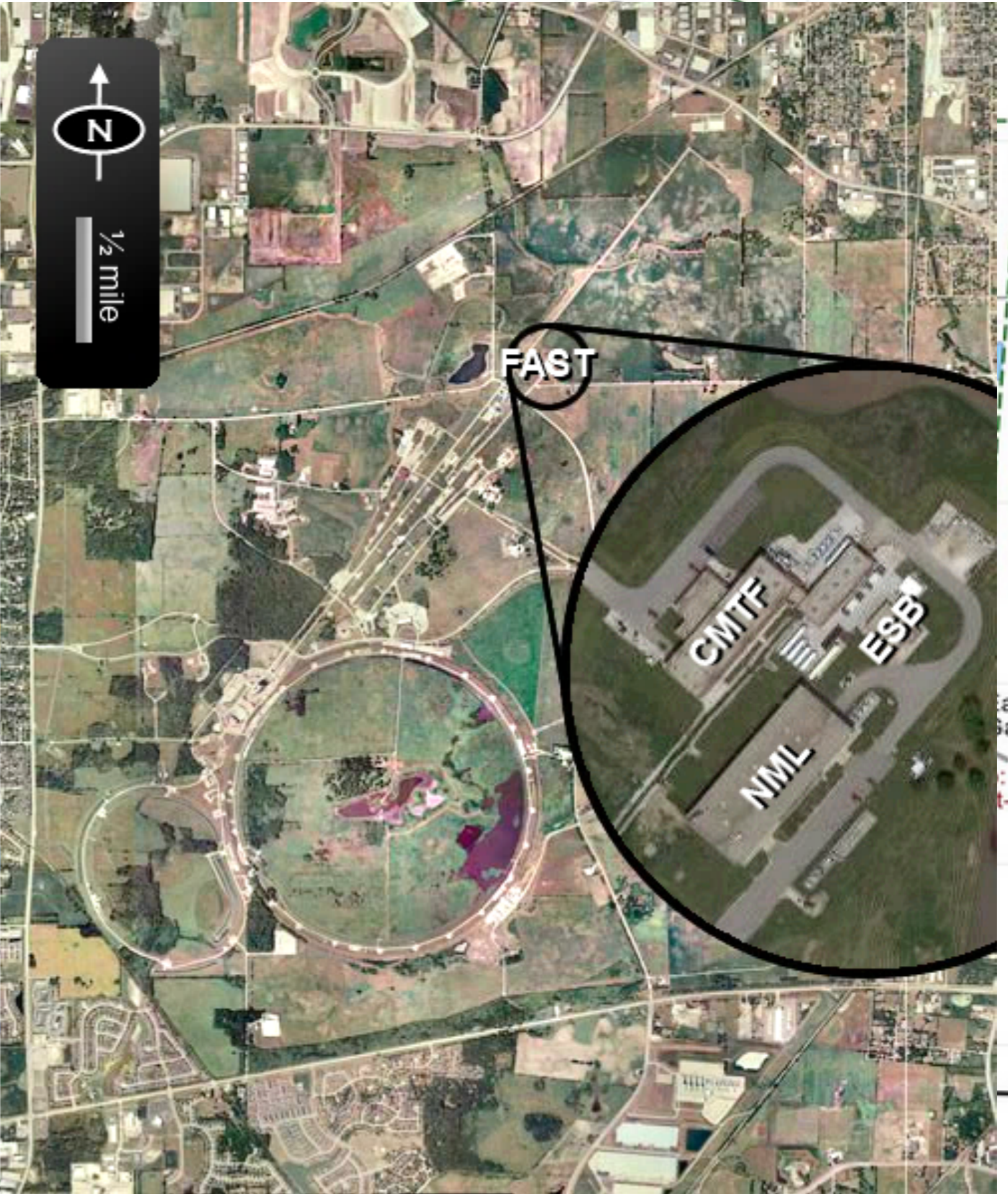
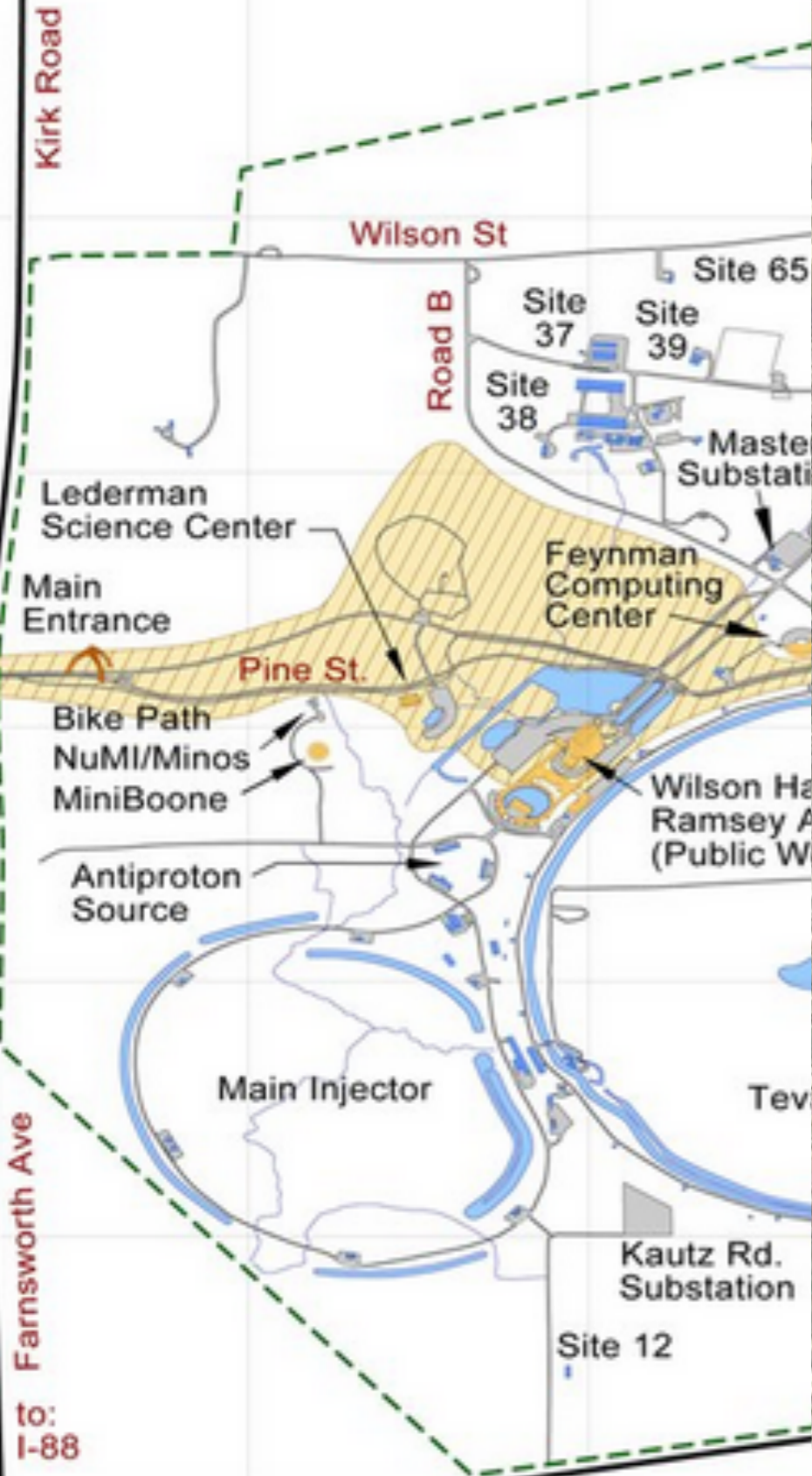
Farnsworth Ave

to:  
I-88



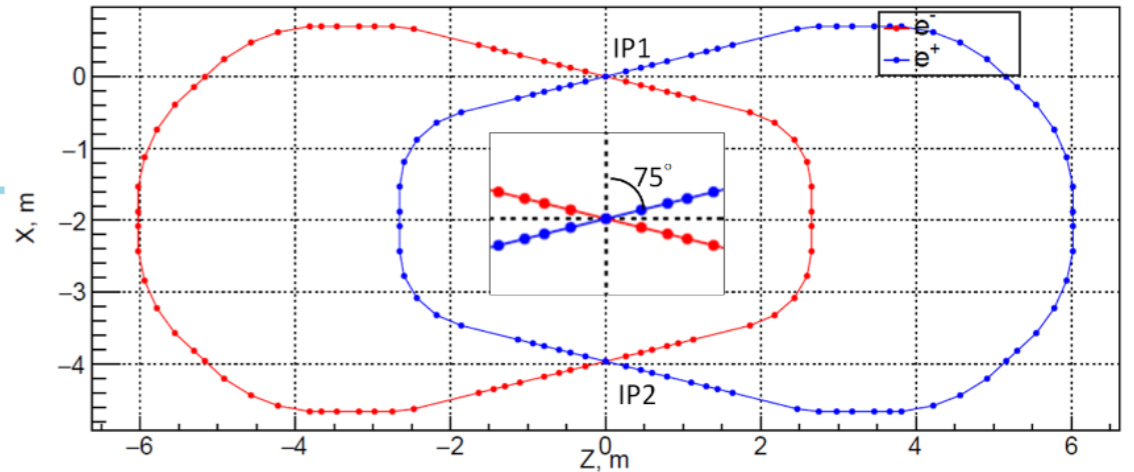
# Fermilab

- Public Areas
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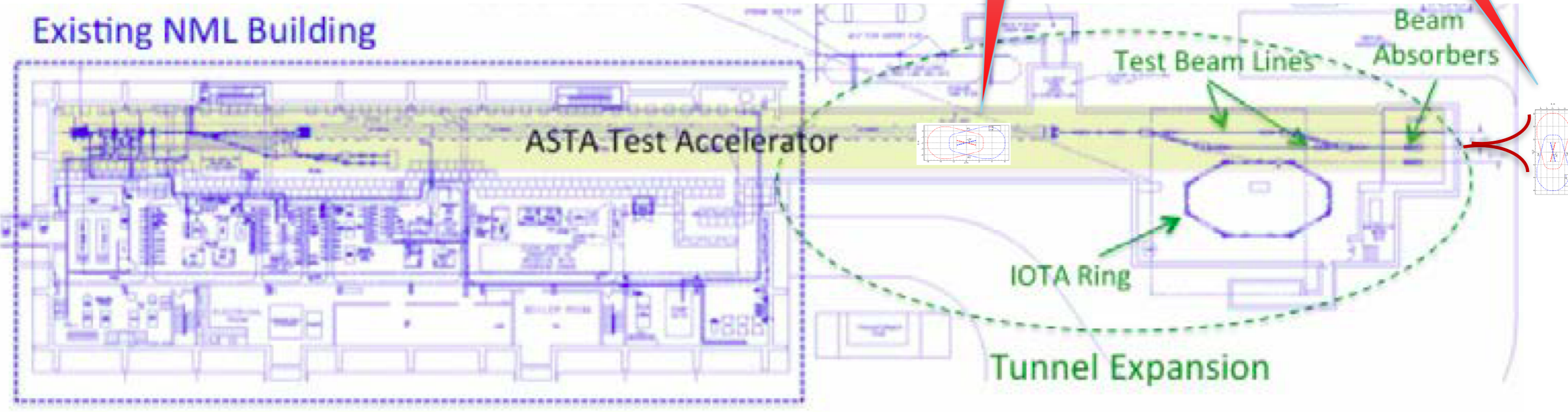


to:  
I-88

# Placement of the DIMUS Collider



~12m x 6m



# DIMUS Collider

For  $75^\circ$  crossing need beam energy of 408 MeV

Require high positron production rate  $10^{11}e^+/s$

Intra-beam scattering, beam lifetime, non-head-on collisions all leads to technical accelerator challenges...surmountable

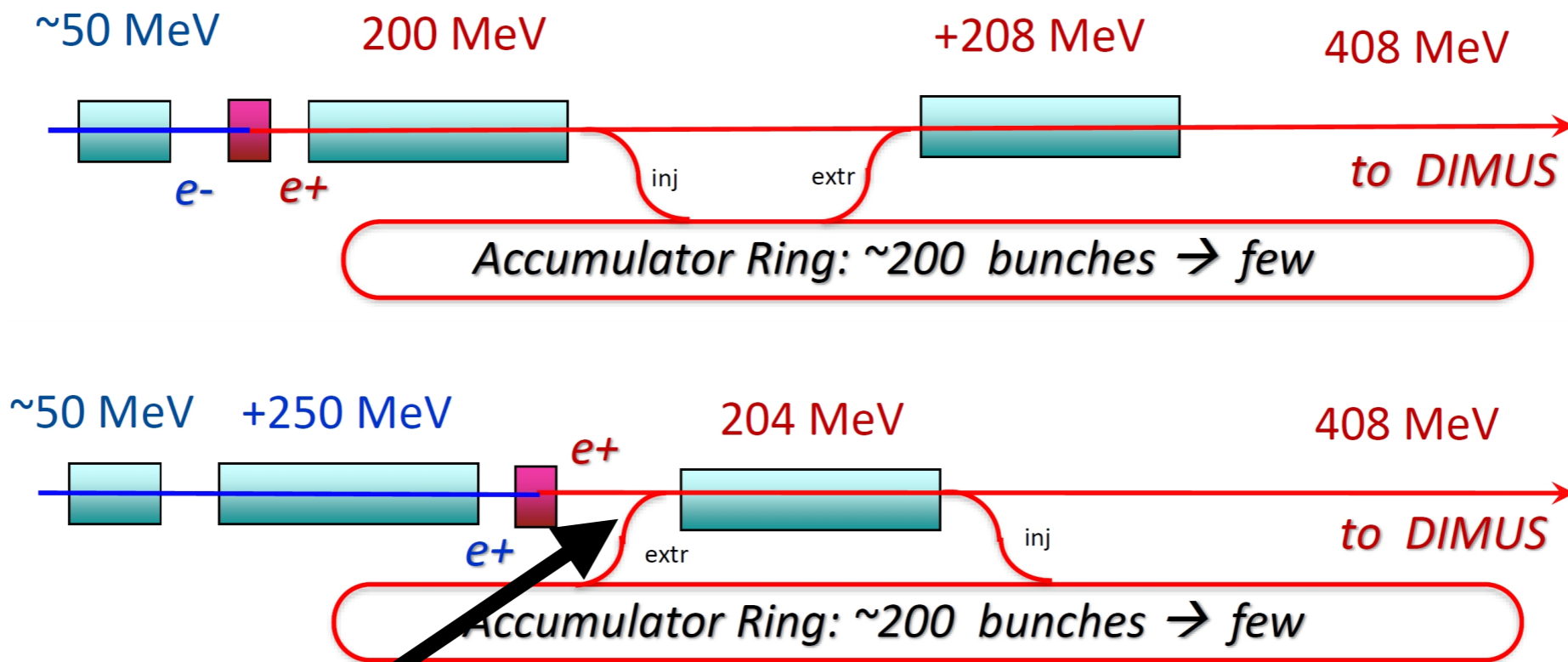
FAST has SRF that can deliver  $3 \times 10^{14}e^-/s$  up to 300 MeV

Need second cryomodule, plenty of space



# DIMUS Collider

Positron production: convert  $e^-$  on a Tungsten target, 2 possible configurations



Injection/extraction requires fast (4ns) kickers, similar to ones developed for ILC

# *DiMuonSpectroscopy (DiMuS) at NML : Opportunities*

---

- **Excellent source of high energy electrons:**
  - eg 3000 bunches x 5 Hz x  $2e10$  =  $3e14$  e-/s
  - at 1% conversion →  $3e12$  e+/s
- **DIMUS will probably need much less**
  - eg 200 bunches x 1 Hz x  $2e10$  =  $4e12$  e-/s
  - at 1% conversion →  $4e10$  e+/s
- **Efficient linac – now upto 300 MeV**
  - DIMUS will need extra  $\sim 108$  MeV → total of 408 MeV
- **Infrastructure and expertise:**
  - wide & (important) long tunnel, cryo, power, HCW, etc
  - knowledgeable people

# DiMuS at NML : Summary

---

- They can be created in  $e^+e^-$  collision with large longitudinal momentum (as they quickly decay)
  - e.g. 408 MeV/beam at  $75^\circ$
- **FAST/NML is perfectly suitable for DIMUS:**
  - SRF accelerators, plenty of  $e^-$ , wide/long tunnels
  - potential for  $O(1e32)$  luminosity and  **$\sim 0.5M$  dimuons** per year
- **Requires:**
  - second SRF CM, positron production and accumulation system, collider rings, detector(s)



# After production

If muonium transits material it can be destroyed

$$\sigma_{dissoc.} \approx 13Z^2 \text{ barn}$$

If muonium exposed to intense laser it can be put into P-state

If transits regions with strong B-field, level mixing can also populate other states

Spectroscopy: measure Lamb shift, hyperfine etc  
Decay lifetimes and branching ratios

# New Physics

Ongoing anomalies in muon sector:  $g-2$ , muonic Hydrogen,  $R_K$   
New physics coupled to muons?

Great probe of short distances, no nuclear effects to contend with

New forces can change size of muonium, altering production/  
**decay**

$$(\mu^+ \mu^-) \rightarrow V_{NP}^* \rightarrow e^+ e^-$$

and provide new **decay** channels

$$(\mu^+ \mu^-) \rightarrow \gamma X \qquad (\mu^+ \mu^-) \rightarrow XX$$

$$X \rightarrow SM \ SM$$

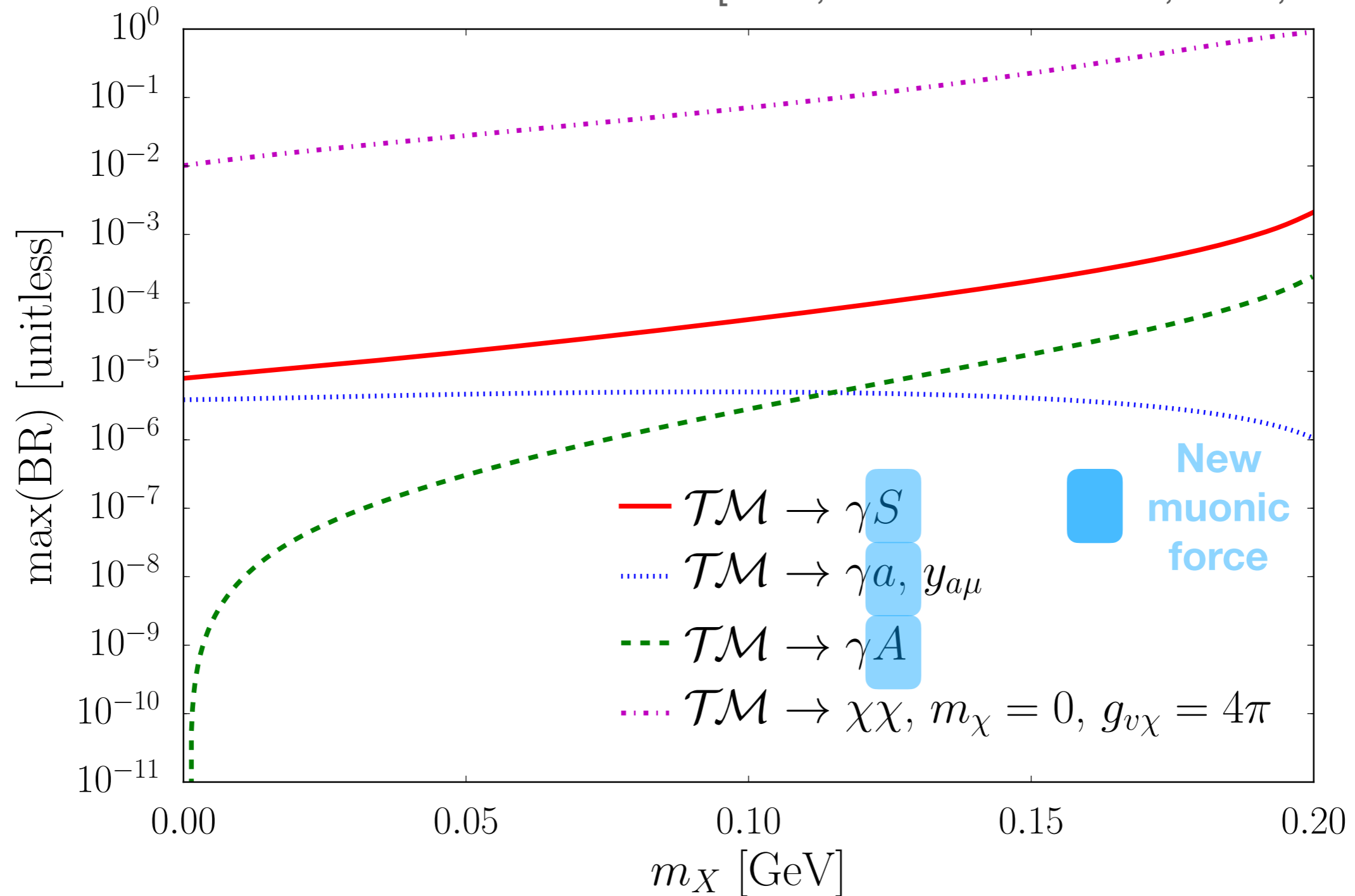
or change energy levels (**spectroscopy**)

2S-2P transition

Strong constraints from other measurements

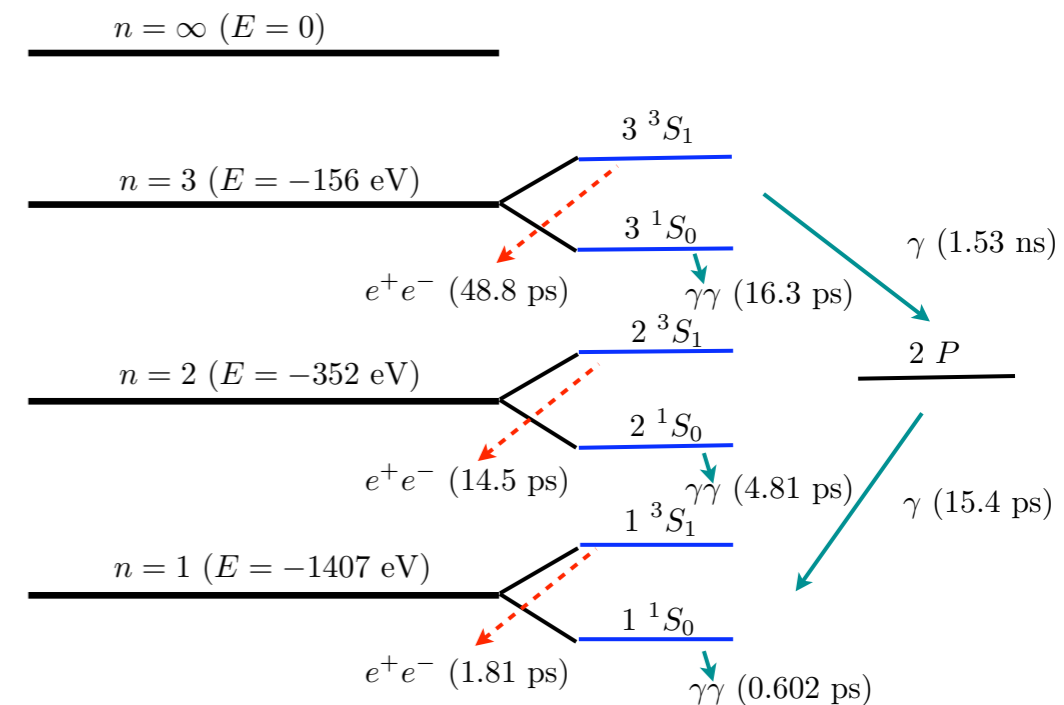
# New Decay Modes

[Vidal, Ilten et al PRD100, 2019; 1904.08458]



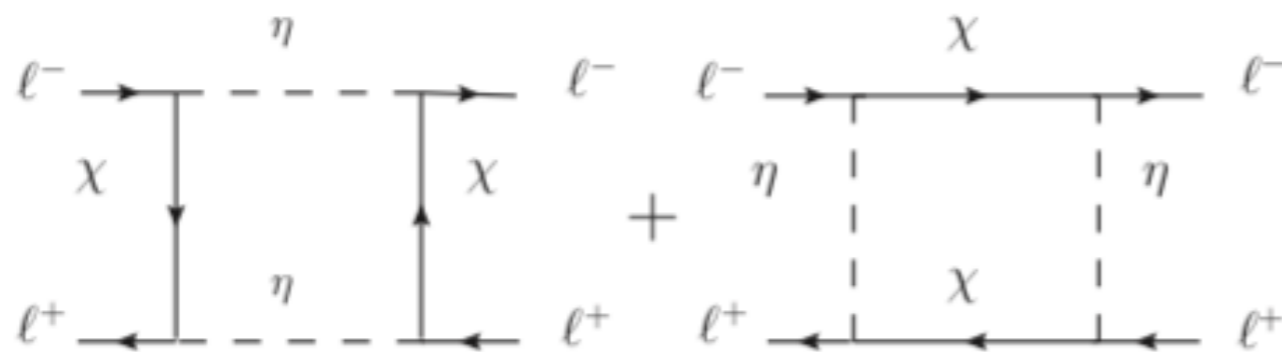
# Spectroscopy [Ji,Lamm; 1712.03429]

Transition	$E_{\text{theory}}$ [MHz]
$1^3S_1 - 1^1S_0$	$42329355(51)_{\text{had}}(700)$
$2^3S_1 - 1^3S_1$	$2.550014(16) \times 10^{11}$
$2^3P_0 - 2^3S_1$	$1.002(3) \times 10^7$
$2^3P_1 - 2^3S_1$	$1.115(3) \times 10^7$
$2^3P_2 - 2^3S_1$	$1.206(3) \times 10^7$
$2^1P_1 - 2^3S_1$	$1.153(3) \times 10^7$

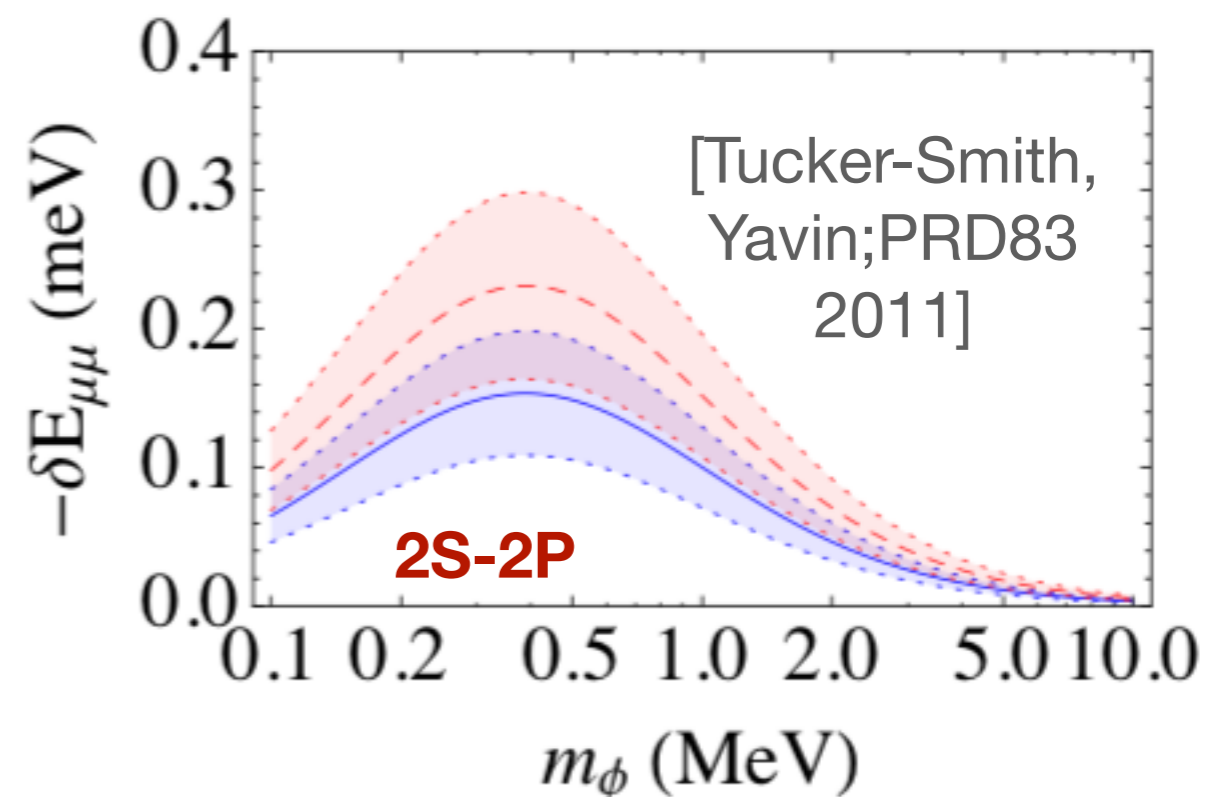


Muonic forces/contact interactions can alter energy levels: Lamb shift, hyperfine, 2P-2S, 2S-1S, etc

QED prediction known to  $\mathcal{O}(m_\mu \alpha^5)$  BSM  $\sim 100$  MHz



$$\Delta E_{\text{hfs}}^{\mu^+\mu^-} = -1.47 \text{ MHz} \times y^4 \left( \frac{100 \text{ GeV}}{m_\chi} \right)^2,$$



# Detection

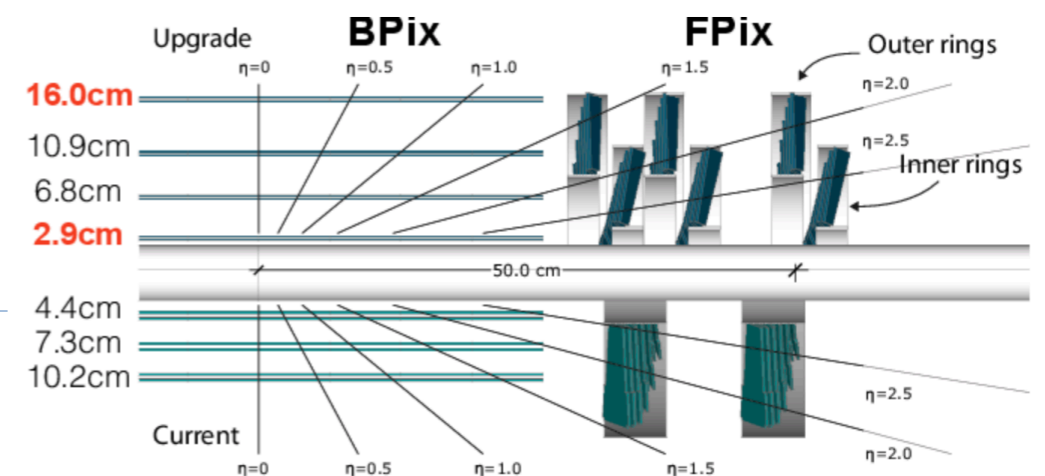
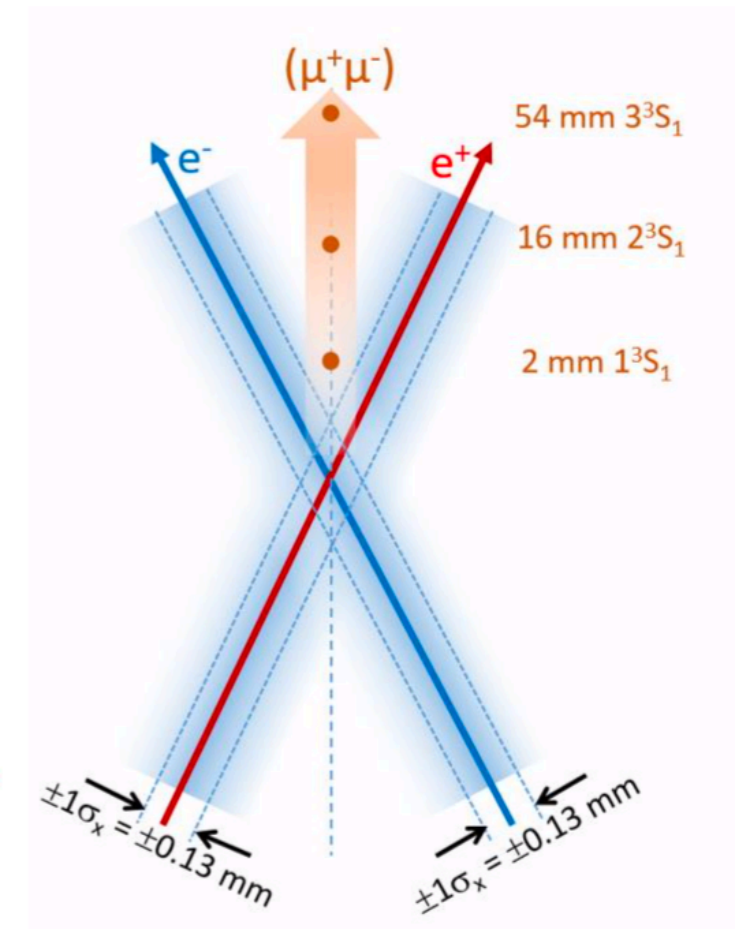
- ◆ **Detector requirements can depend on the physics goals**
- ◆ Can we observe True Muonium (TM) ?
- ◆ Can we perform spectroscopy analysis of TM ?
- ◆ Are there exotic decays of TM we should look for?
- ◆ Can we do other physics with this setup?

## The Challenge:

- $e^+e^- \rightarrow \text{TM} \rightarrow e^+e^-$
- The primary background is Bhabha events
- For  $\Delta(E_e) \sim 10$  keV, the signal x-section is  $\sim 5$  nb
- Bhabha  $\sim 22,000$  nb  $\rightarrow$  **S/B  $\sim 1/4,000$**

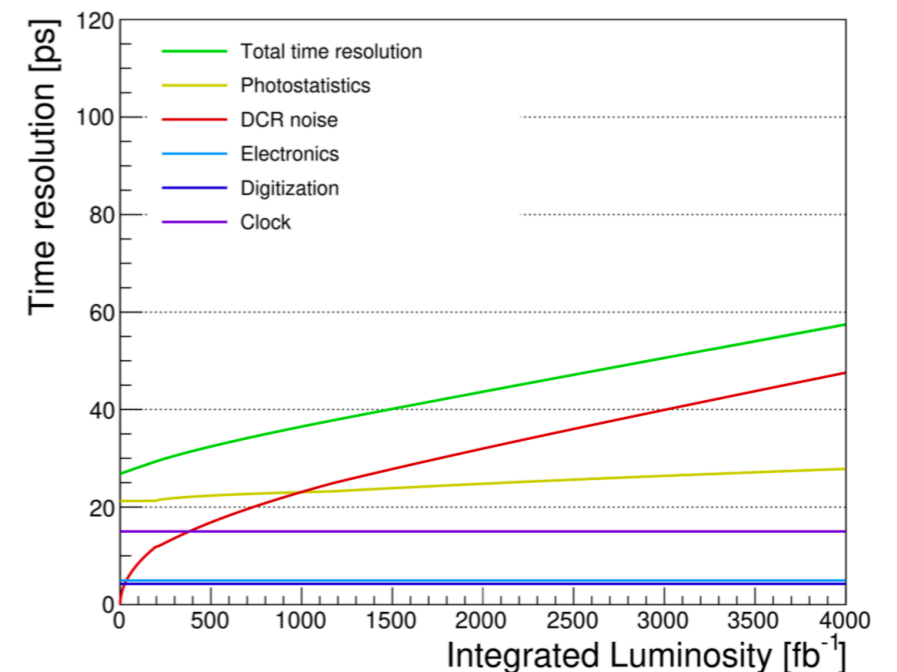
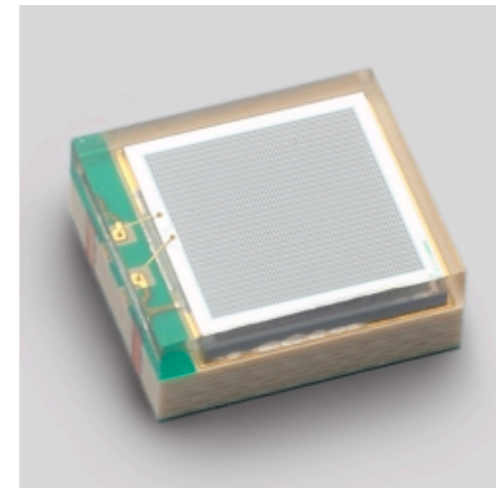
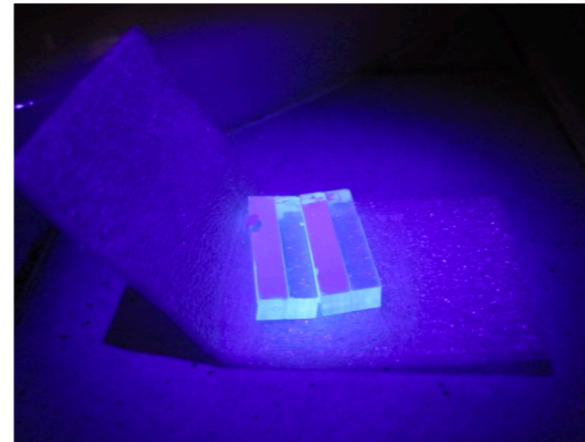
# Tracker Considerations

- ◆ For Dimuonium:  $\beta \gamma c \tau = 2 \text{ mm}$
- ◆ Interaction region spread  $\sim 300 \text{ microns}$ 
  - Detector resolution can be small ( $< 100 \text{ microns}$ )
  - Total vertex resolution  $< 400 \text{ microns}$
- ◆ Requiring  $z > 2 \text{ mm}$  would suppress Bhabba events
  - Prompt background free after the cut
- ◆ Extract 1S/2S/3S fractions from the vertex position
- ◆ Need a vertex detector:
  - Pixelated silicon
    - ★ – CMS Phase-0 had 100-150 micron pitch pixels and allowed  $z$  resolution of  $< 100 \text{ microns}$  in  $r$ - $z$  and  $< 30 \text{ microns}$  transverse plane. Good enough!
  - Drift chamber? Straw tracker?

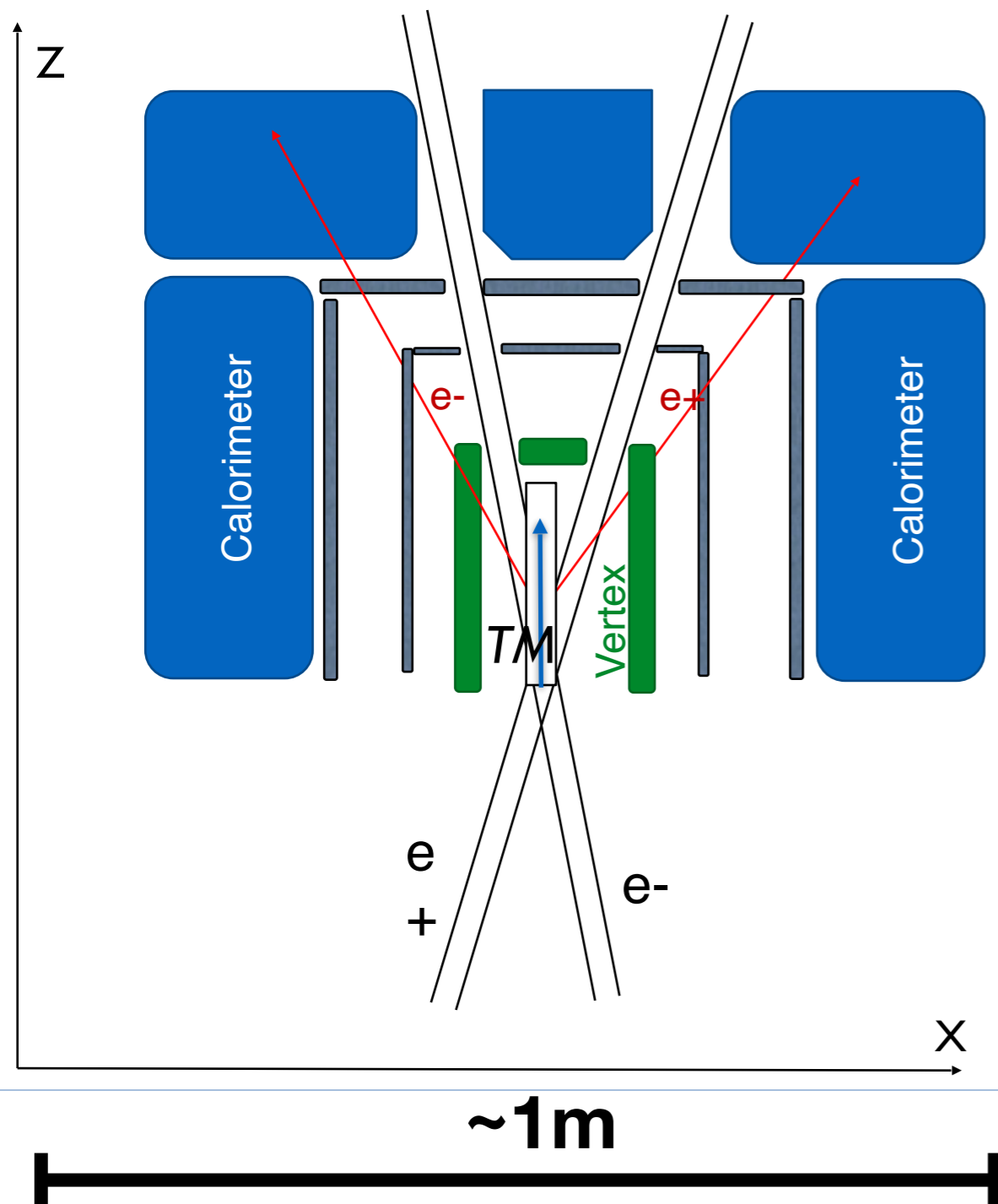


# Calorimeter Considerations

- ◆ Electron/positron energy  $\sim 100$  MeV
- ◆ Only few particles in the event – do not need fine segmentation, but do need good resolution and good coverage/acceptance
- ◆ A decently large crystal would contain the electron/positron and the right choice of crystal would give a lot of light
  - LYSO crystal read out by SiPM
  - PbWO<sub>4</sub> cheaper but probably not bright enough
  - Plastic is not going to work
- ◆ Precision timing desirable for further BG suppression and spectroscopy measurements?



# Detector Sketch



- ◆ Vertex: Pixelated silicon vertex detector
- ◆ LYSO calorimeter with excellent timing and energy resolution
- ◆ Directionality: Additional 2-3 tracking layers between the vertex detector and the calorimeter. Gas based (GEM) or silicon strips
- ◆ No magnetic field necessary
- ◆ Can probably achieve 50+% acceptance per track, 25% total.
- ◆ **100k-0.5M signal events per year**
- ◆ Integrated radiation dose small
- ◆ Devil is in the details...

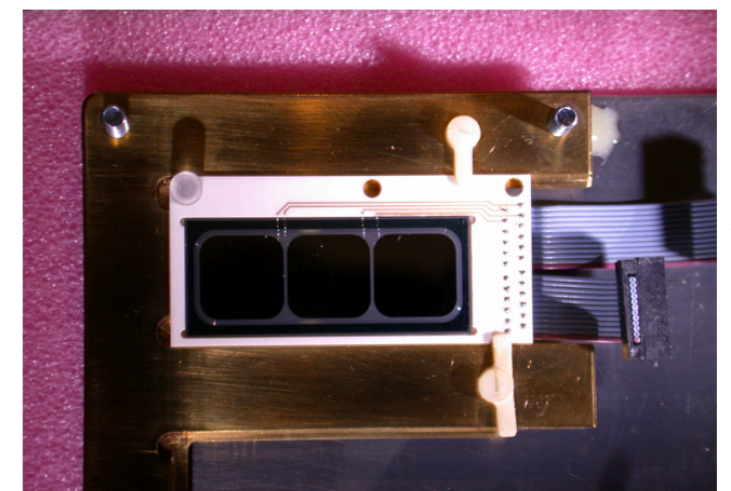


# X-ray Photon Detection

- ◆ Transition between the TM states happens with the emission of photons in the 100 eV – 10 KeV range.
- ◆ Can you infer this from the energy resolution of the electron/positron?
  - $\Delta E/E \sim 10 \text{ keV} / 100 \text{ MeV} < 10^{-4}$ , **very hard** even at the higher end of the spectrum
- ◆ Direct detection of KeV photons
  - Examples DEAR, SIDDHARTA experiments at DAFNE (kaon spectroscopy, ~6 KeV x-ray photons)
  - SDD a possibility. Beam backgrounds?
- ◆ What about Laser spectroscopy?

Detector	Si(Li)	CCD	<b>SDD</b>
Area [mm <sup>2</sup> ]	200	724	<b>100</b>
Thickness [mm]	5	0.03	<b>0.30</b>
$\Delta E$ (FWHM) [eV]	410	170	<b>185</b>
$\Delta t$ (FWHM) [ns]	290	-	<b>430</b>

200 SDDs with 1cm<sup>2</sup> per SDD



# Conclusions

- Dimuonium is a bound state of QED, never seen before!
- Provides a precision laboratory to test QED and muons
- Existing anomalies:  $g-2$ , proton radius,  $R_D$ ,  $R_K$
- FISR produces relativistic dimuonium in  $3S1$  states
- Proposal for DIMUS at NML/FAST, modest upgrades (eg 2nd cryo-module, fast kicker, positrons)
- Detection of TM in  $e^+e^-$  final state needs vertex detector, high resolution, good timing calorimeter
- Opportunity for detailed study of its properties — production rate, decays, transitions. Constraints on new physics.

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**Thank you!**

# Muons in Minneapolis Workshop

Fundamental Physics with Muons

University of Minnesota, Twin Cities Dec 6-8, 2023

Organizers:  
Yohei Ema  
Saarik Kalia  
Zhen Liu  
Kunfeng Lyu  
Maxim Pospelov



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Hot summer in Minneapolis

Photo by Andrey Shkerin

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Fundamental Physics with Muons



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Maxim Pospelov



Hot ~~Winter~~ in Minneapolis

Photo by Andrey Shkerin

Beam energy	408	MeV
C.m.e. $\sqrt{s}$	211	MeV
C.m.e. spread	0.4	MeV
Crossing angle	75	deg.
Circumference	23	m
Beta-functions at IP $(y, x)$	20/0.2	cm
Bunch length	1.2	cm
Bunch spacing	1.9	ns
Beam sizes at IP $(y, x)$	0.7/130	$\mu\text{m}$
Number of bunches	40	
Number of $e^+/e^-$ per bunch	$4 \cdot 10^{10}$	
Beam lifetime	$\geq 30$	sec
Max $e^+$ production rate	$4 \cdot 10^{10}$	$e^+/\text{s}$
Peak luminosity	$1.6 \cdot 10^{32}$	$\text{cm}^{-2}\text{s}^{-1}$

TABLE I. Main parameters of the DIMUS collider at Fermilab's NML/FAST.