

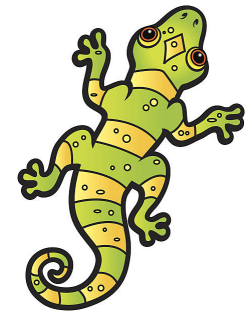
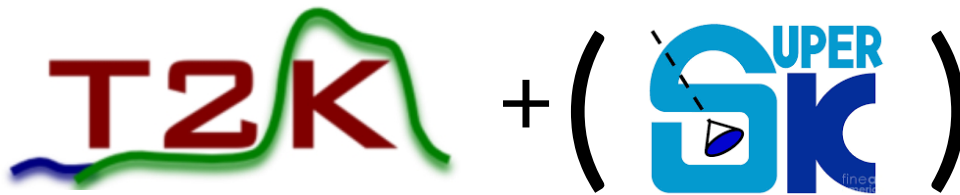
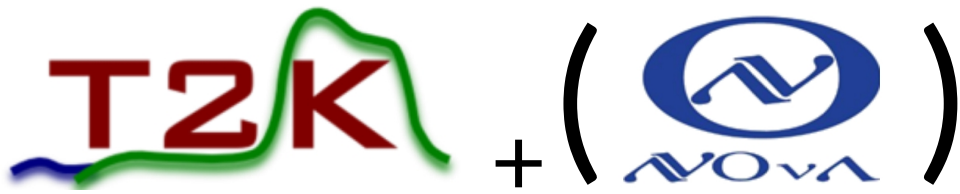
# Impact of neutrino interaction uncertainties on oscillation measurements

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Clarence Wret  
April 15 2024  
NuInt 2024, Sao Paulo

# Impact of neutrino interaction uncertainties on oscillation measurements

Bias declarations:

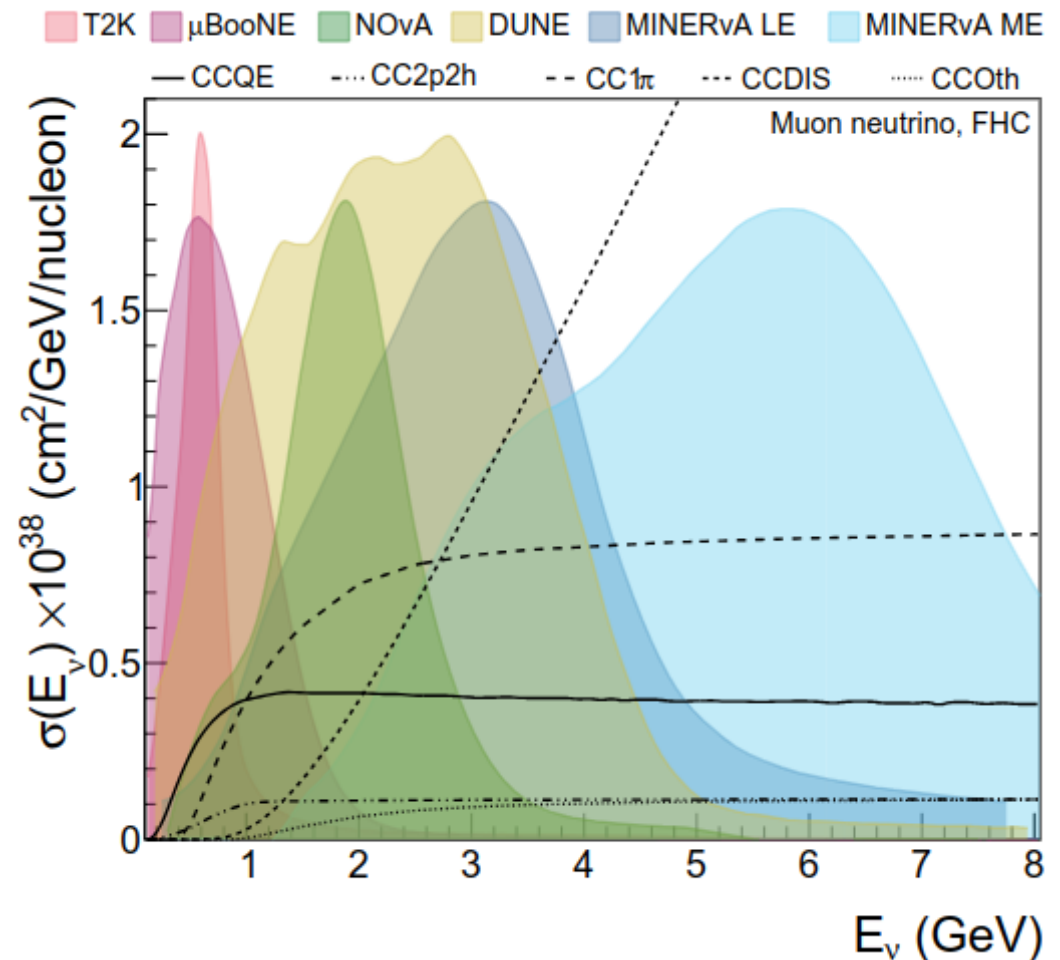


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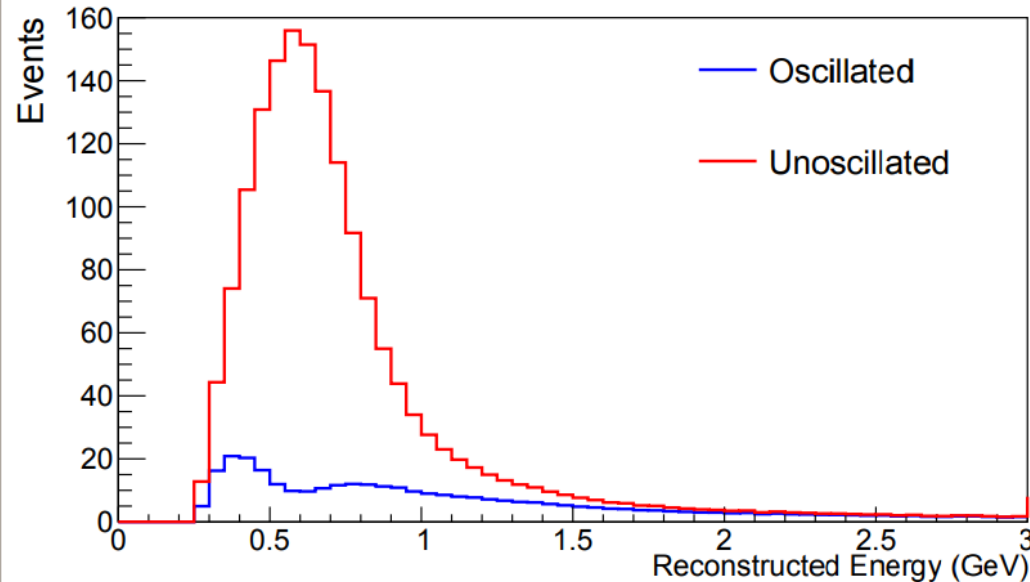
# Introduction

- Accelerator neutrino oscillation experiments generally in the **0.5-5 GeV** region
  - Some with wide, some with narrow band beam
- Studying (anti-) $\nu_\mu$  disappearance and (anti-) $\nu_e$  appearance in an (anti-) $\nu_\mu$  beam
- Complex scenario of which neutrino interactions matter
  - What matters for T2K, may not matter for NOvA, may not matter for DUNE
  - Measurements from a cross-section experiment may not extrapolate well to an oscillation experiment

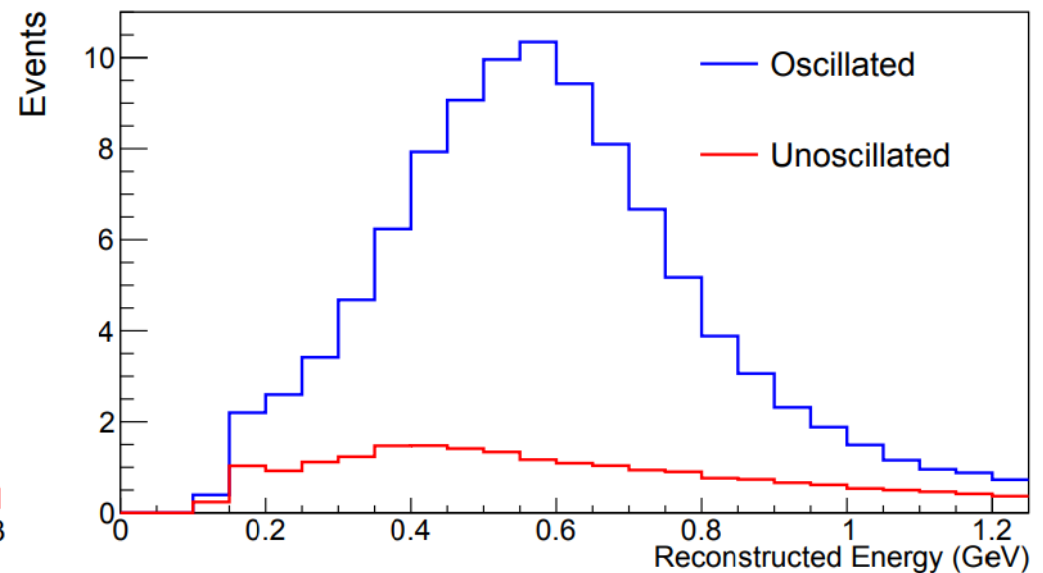


# Introduction

- Oscillation parameters change the rate and shape of the appearing and disappearing neutrinos

T2K FHC 1R $\mu$ 

T2K FHC 1Re

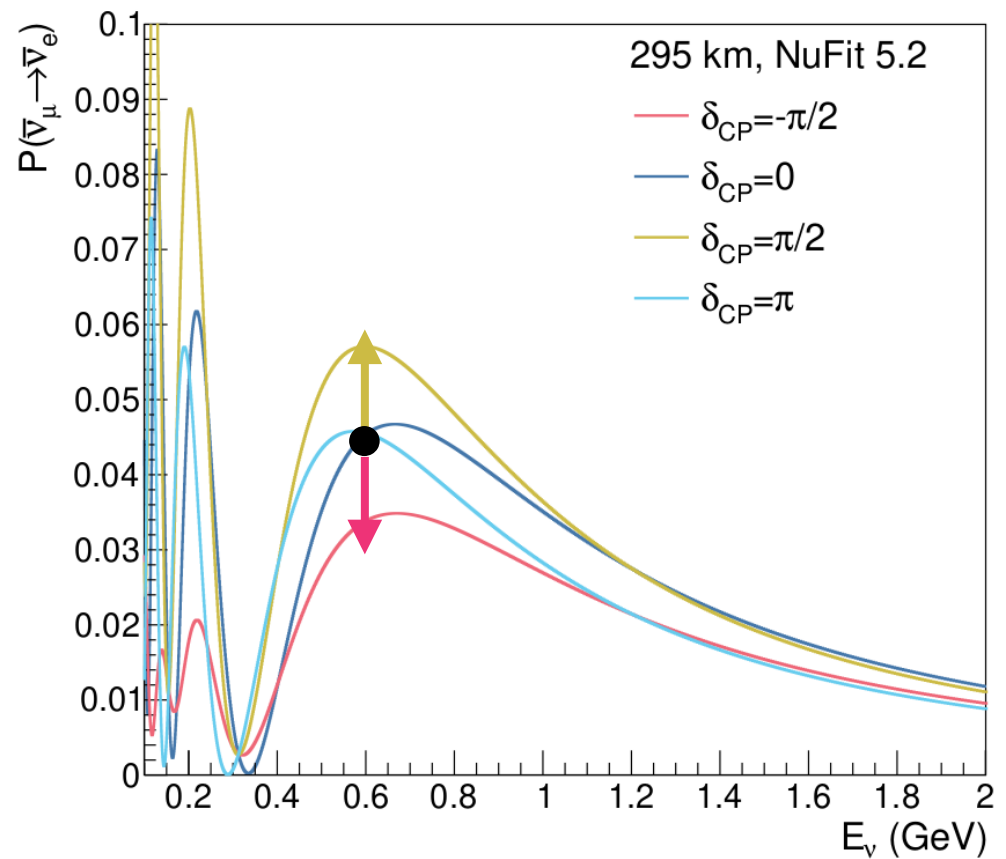
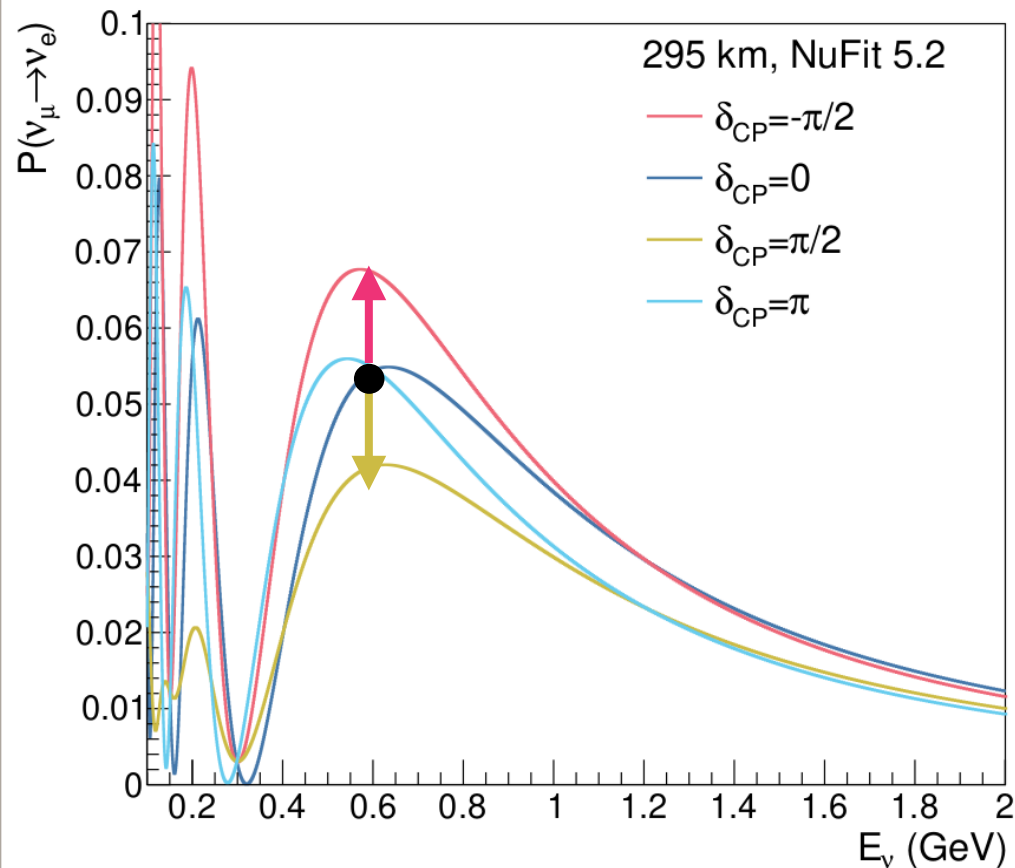


- Relies on the model prediction in the absence of oscillations
  - Constrain this model  $\rightarrow$  constrain your oscillation parameters!
- Finding cross-section effects which are degenerate with oscillation parameters is the **nightmare** scenario

# What can go wrong?

- **Flavour identification**

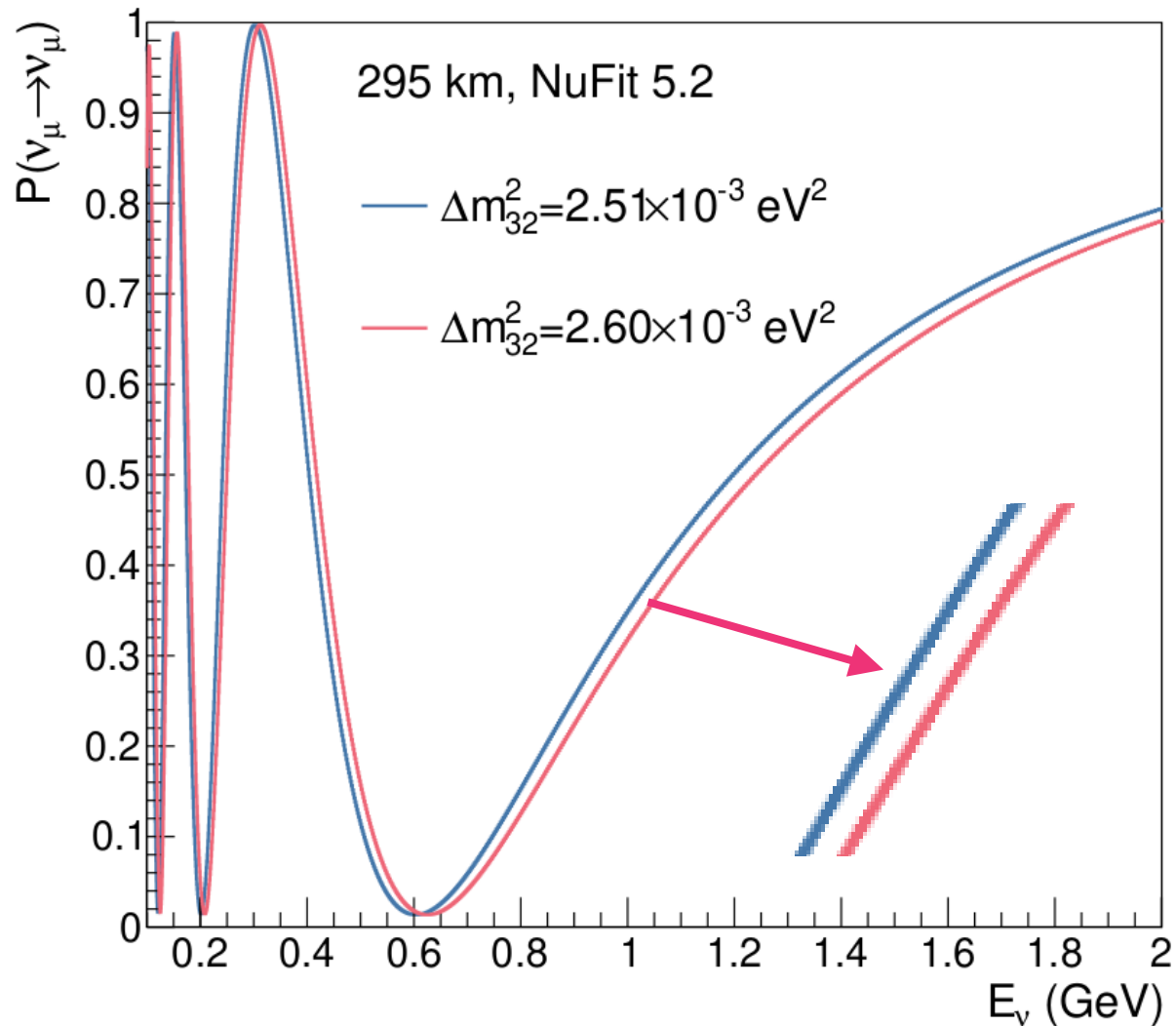
- Is the increased rate of CC1e from oscillations, or is it a poorly modelled NC1 $\pi^0$  background? Or NC1 $\pi^\pm$  mistaken for CC1 $\mu$ ?
- Attribute a cross-section effect of higher  $\nu_e$  rate to oscillations  $\rightarrow$  estimate a larger  $\delta_{CP}$  and  $\sin^2\theta_{13}$



# What can go wrong?

- **Neutrino energy estimation**

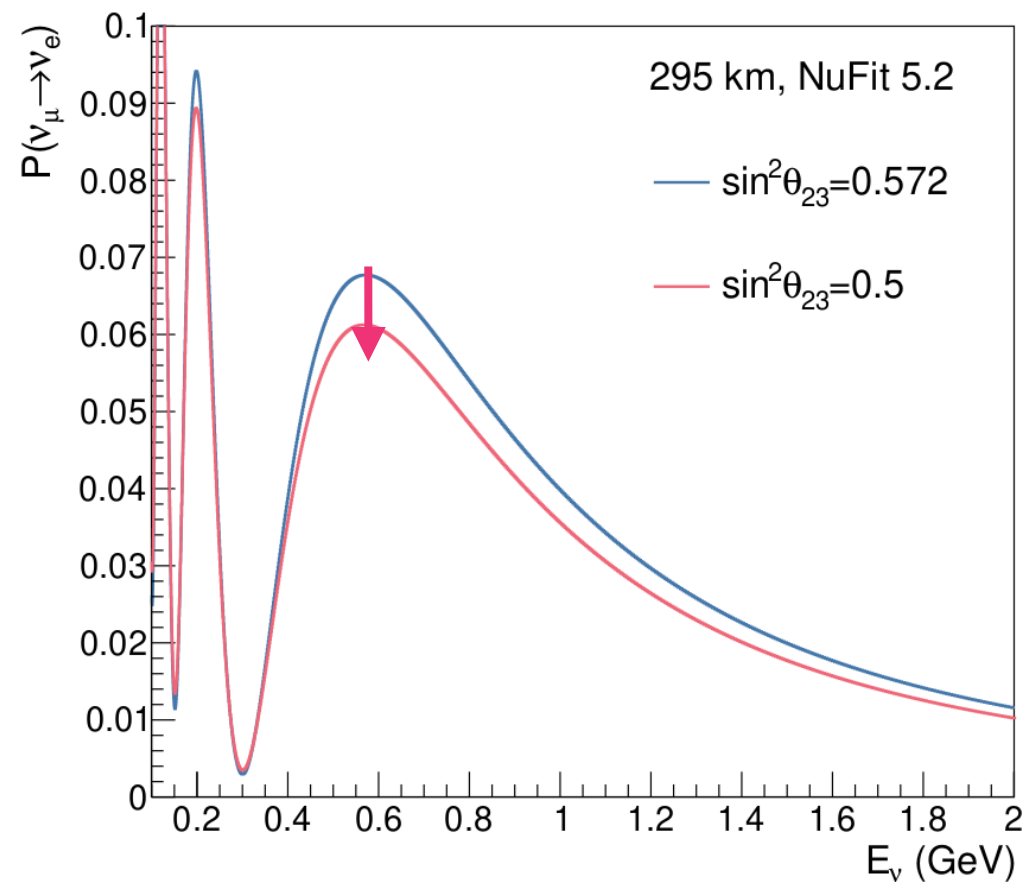
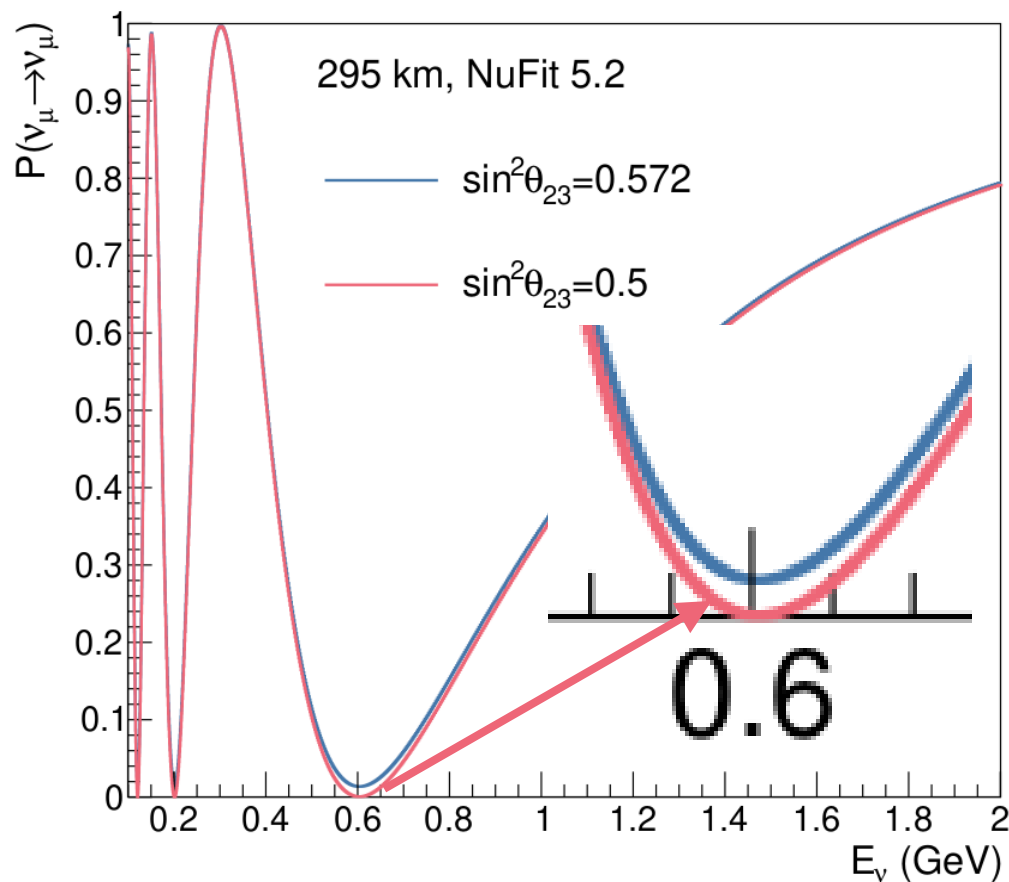
- Is the frequency of the oscillation due to  $\Delta m^2$ , or biases in neutrino energy reconstruction from mismodelling?



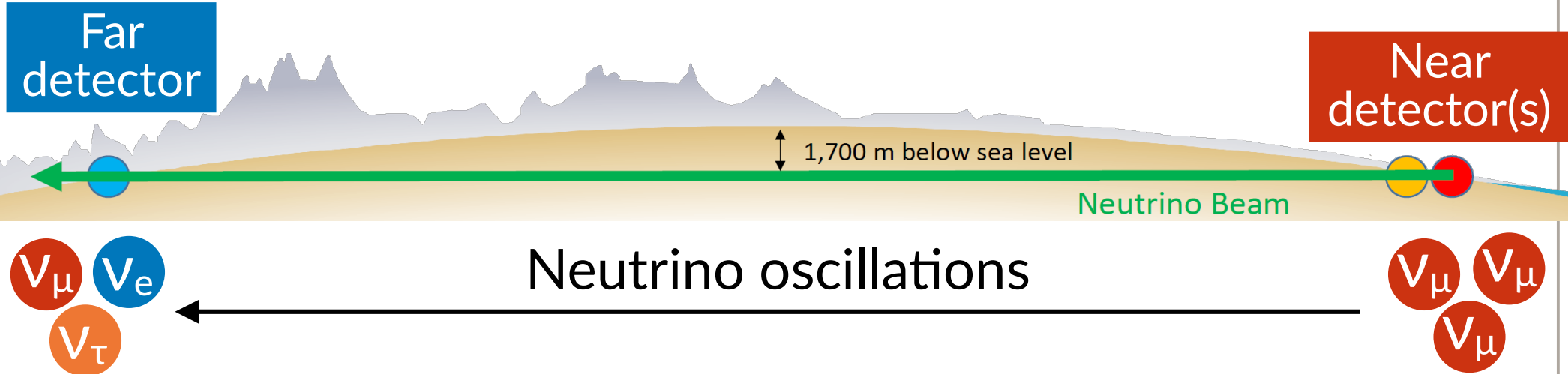
# What can go wrong?

- Rate of appearance and disappearance

- Is the  $\nu_e$  rate higher because of a larger value of  $\delta_{CP}$ , or is your model for  $\nu_e \rightarrow \nu_\mu$  wrong?
- Is the increased rate of  $\nu_\mu$  due to  $\sin^2\theta_{23}$ , or a larger cross section?



# Role of the near detector



- The beam is characterised by **high-statistics samples** at the **near detector(s)** before long baseline oscillations
- Events observed at the far detector have many **shared uncertainties** with the near detector
  - Constrain **flux and interaction model** using near detector data

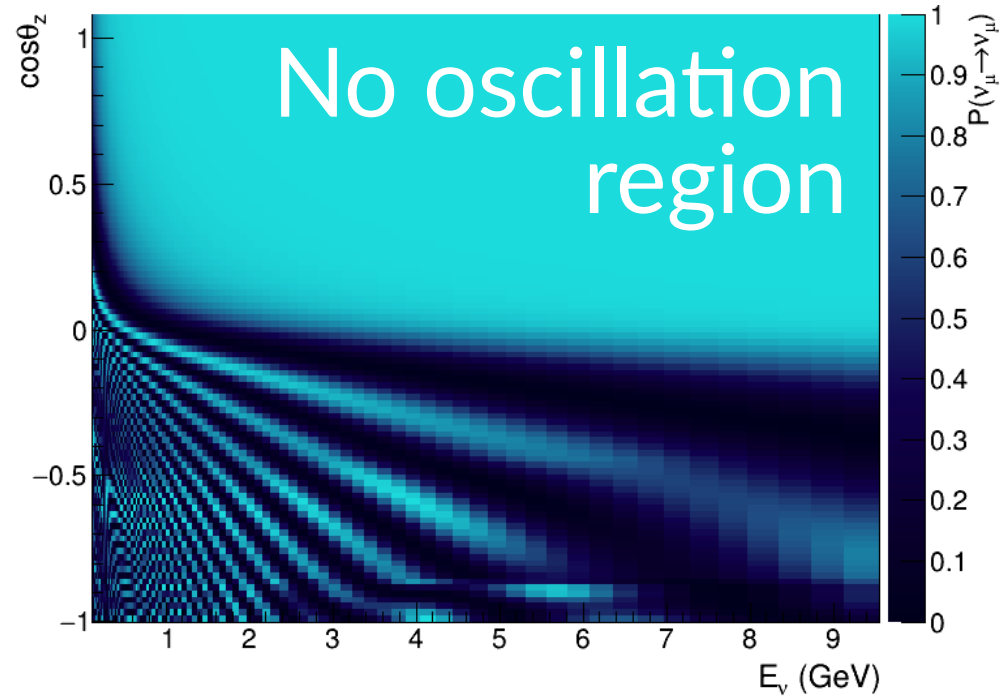
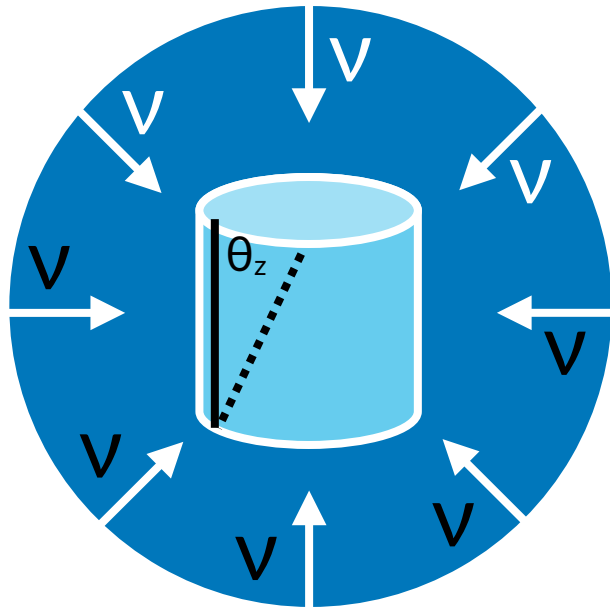
$$N_{\text{ND}}^\alpha(\vec{x}) = \Phi^\alpha(E_\nu) \times \sigma^\alpha(\vec{x}) \times \epsilon_{\text{ND}}^\alpha(\vec{x})$$

$$N_{\text{FD}}^\alpha(\vec{x}) = P(\nu_\alpha \rightarrow \nu_\alpha) \times \Phi^\alpha(E_\nu) \times \sigma^\alpha(\vec{x}) \times \epsilon_{\text{FD}}^\alpha(\vec{x})$$

- **Mitigates many of the issues**, e.g. size of cross sections



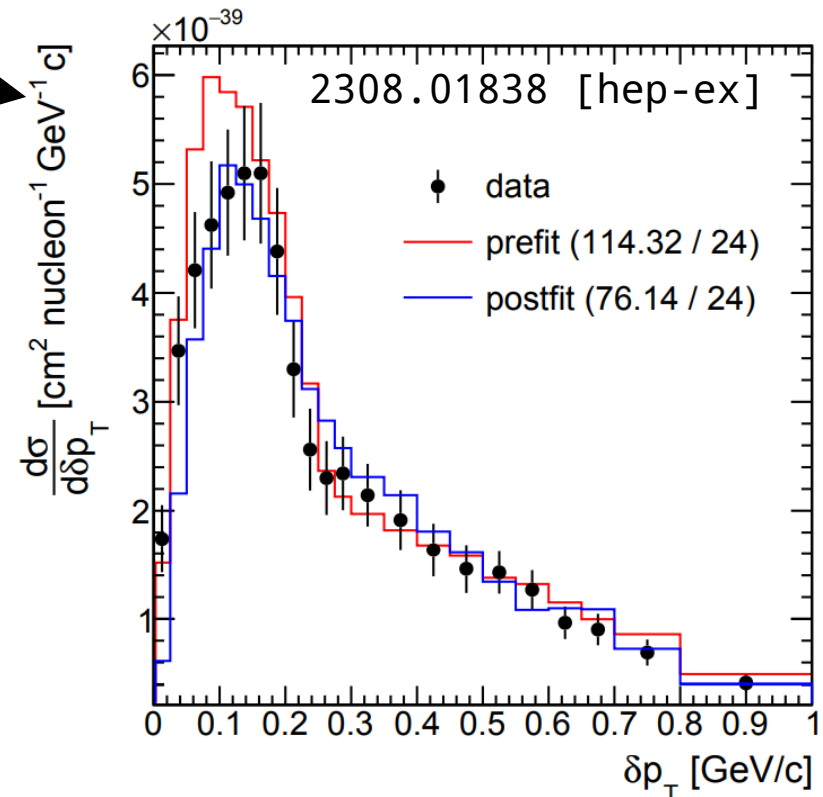
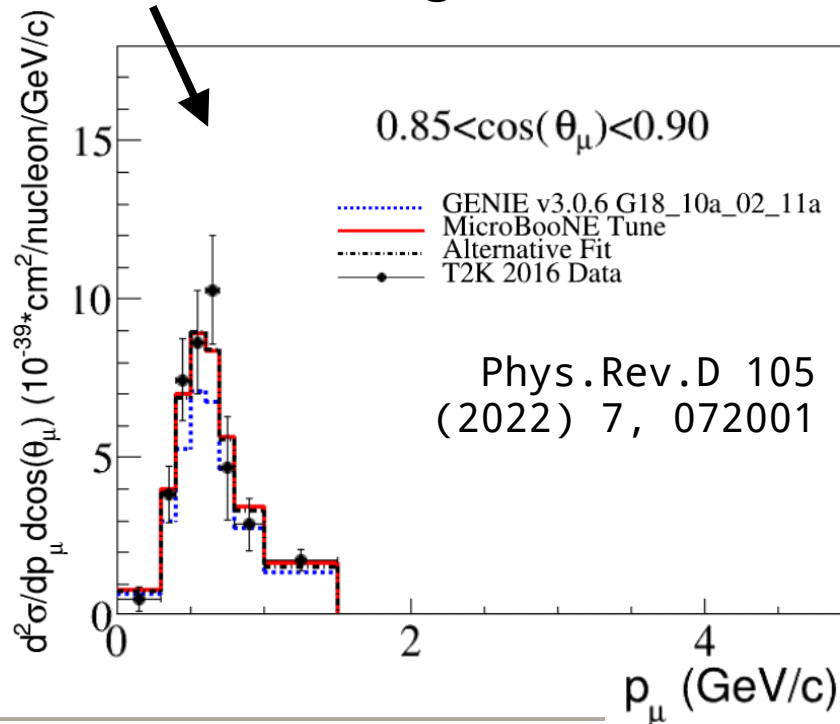
# Role of atmos. down-going events



- For **atmospheric** neutrinos, there is no near detector, but it is largely addressed by **down-going neutrinos**
  - Very small oscillation probability in region
  - **Effectively acting as a near-detector** constraint throughout a large neutrino energy range

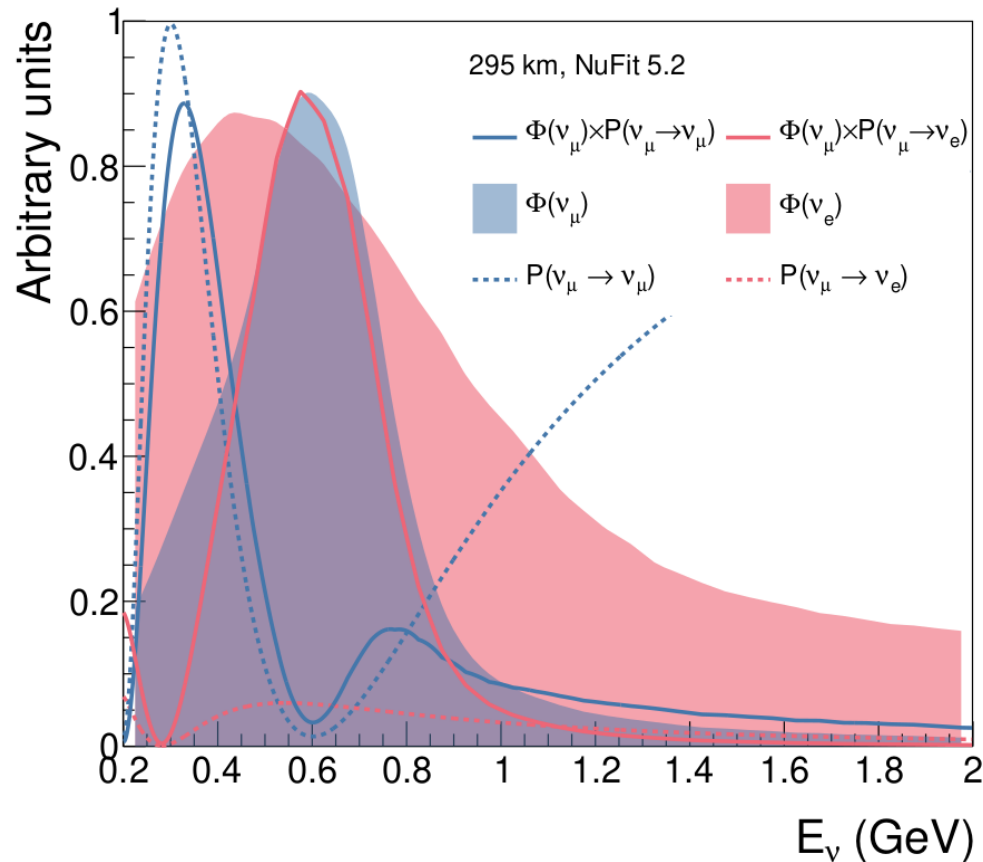
# Role of external data

- In some cases, data from the **near detector might not suffice**
  - e.g. unmagnetised detector, but want  $\text{NC}1\pi^+$  cross section to understand the background in  $\nu_\mu$  disappearance
- Or, you might not have a near detector!
- **External data is often used to estimate the cross section, and prevent a near-detector analysis from over-constraining the model**
  - T2K using MINERvA data
  - MicroBooNE using T2K data



# Issues with the near detector

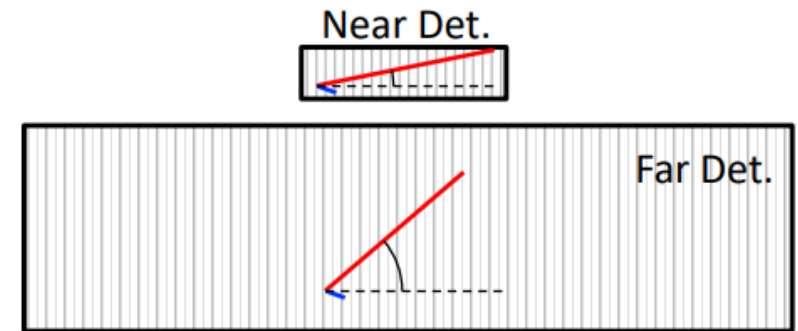
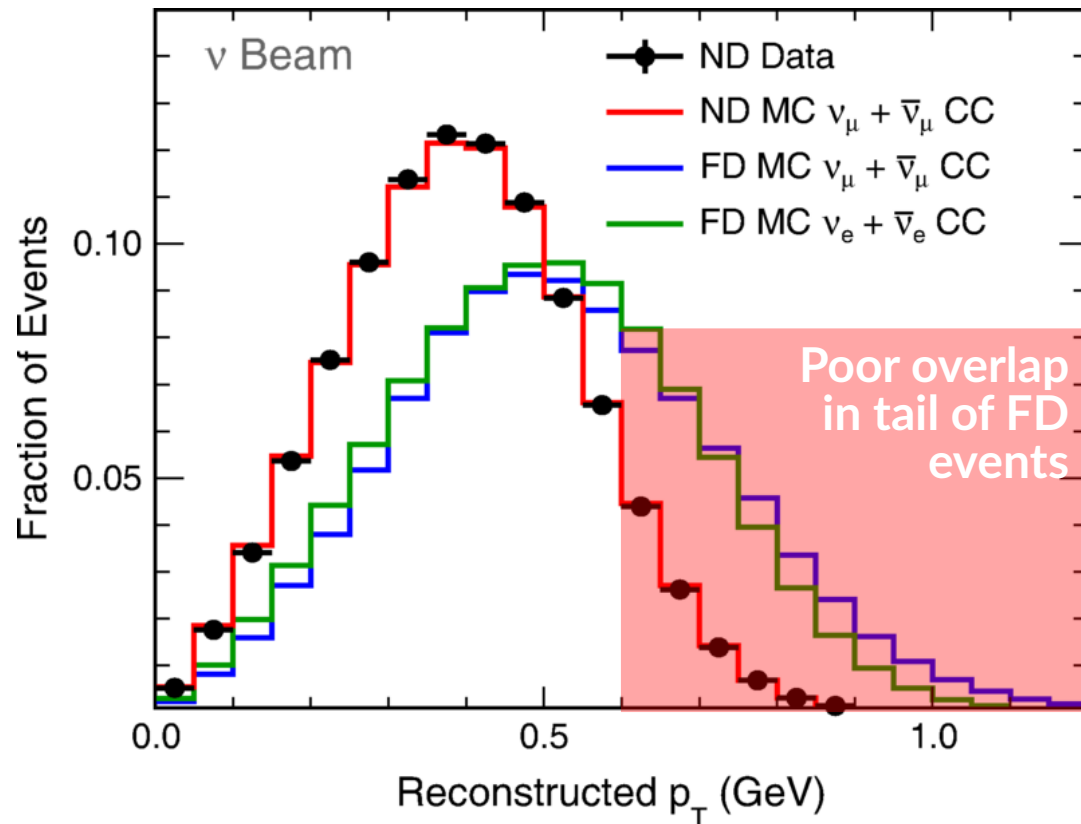
- The  $\nu_\mu$  flux at the **FD** has a **minimum** where the  $\nu_\mu$  flux at the **ND** has a **maximum**



- Oscillated  $\nu_\mu$  flux gives rise to  $\nu_e$  signal at the FD
- Intrinsic  $\nu_e$  at ND do not have same neutrino energy spectrum as the  $\nu_e$  signal at FD**
- Reliance on model for **extrapolating in neutrino energy**

# Issues with the near detector

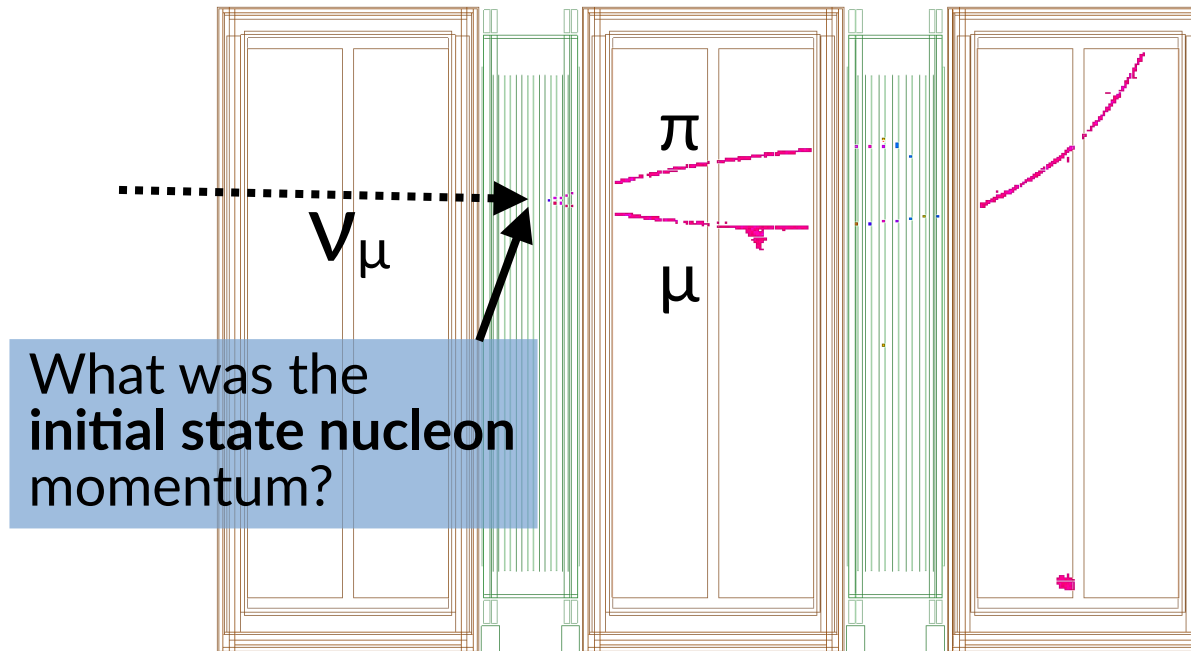
- Acceptance differences from **different size**
  - Functionally identical does not mean identical acceptance



- **Different target material** and **detector design** means additional model dependence in  $\text{CH} \rightarrow \text{H}_2\text{O}$
- **Different detector technologies** and **geometry** may mean different particle acceptance

# Energy reconstruction

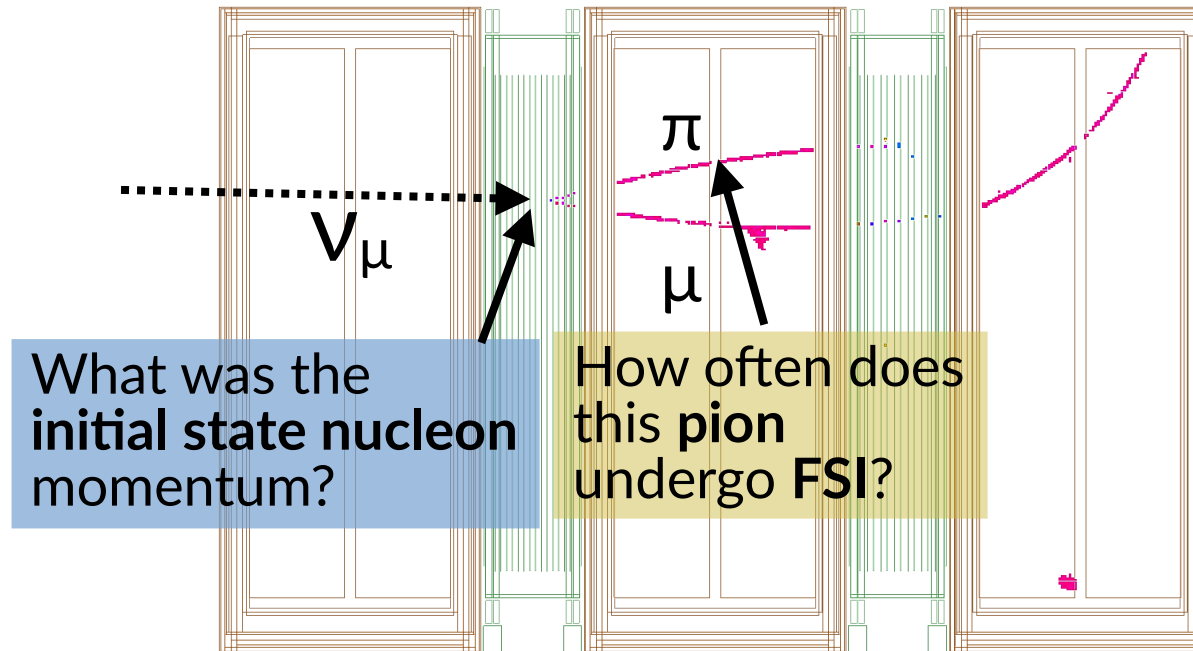
- Energy reconstruction method is function of **selection** and **detector technology**
- Need to understanding mapping between **observed events** and the **not-observed neutrino energy**



- All estimators are biased
  - Try to **reduce** the amount of bias
  - Understand the **uncertainty on the bias**

# Energy reconstruction

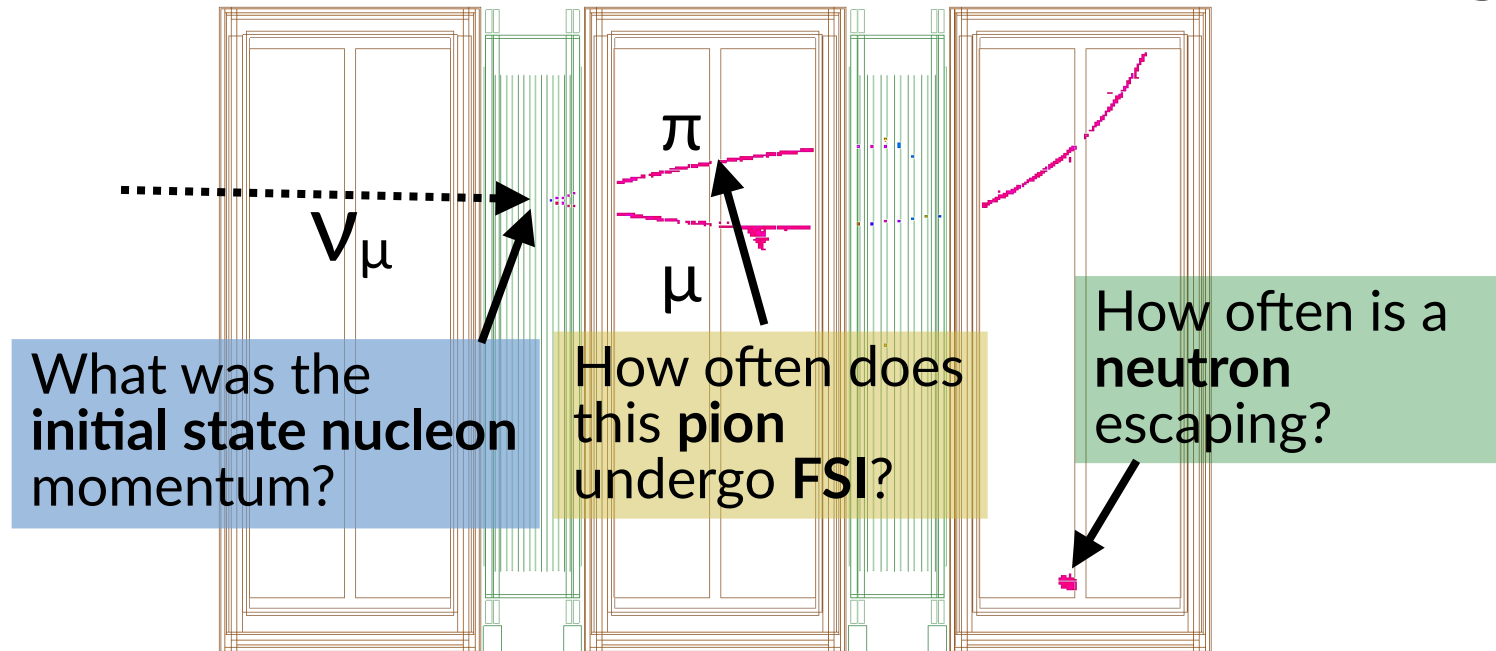
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# Energy reconstruction

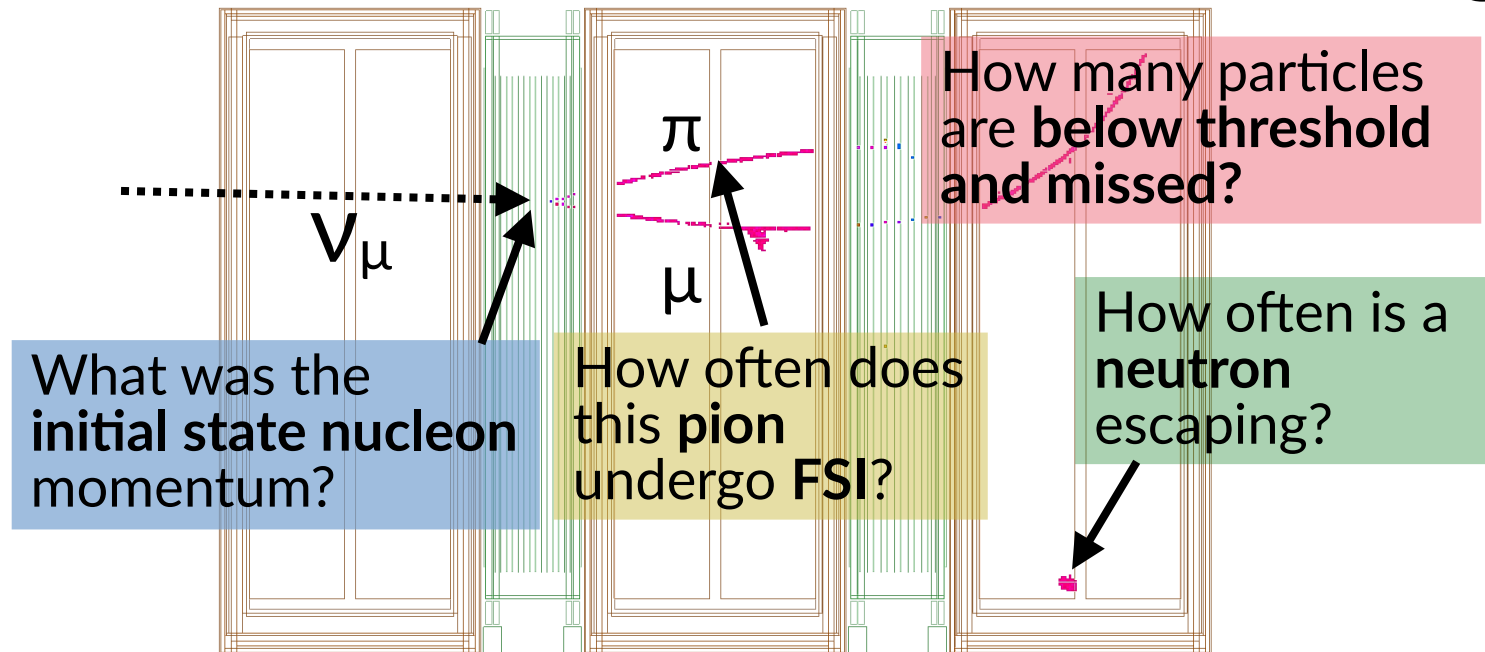
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# Energy reconstruction

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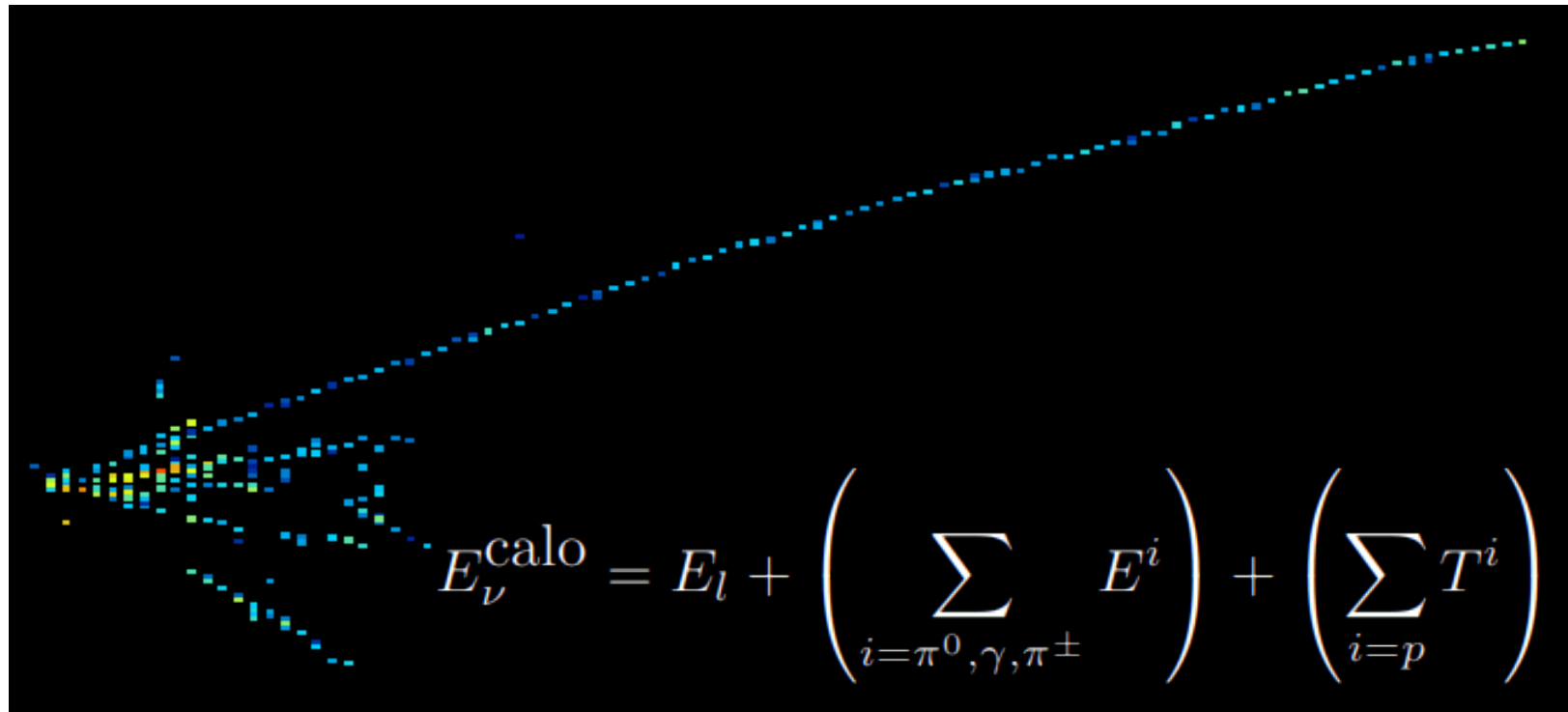


- All estimators are biased
  - Try to **reduce** the amount of bias
  - Understand the **uncertainty on the bias**



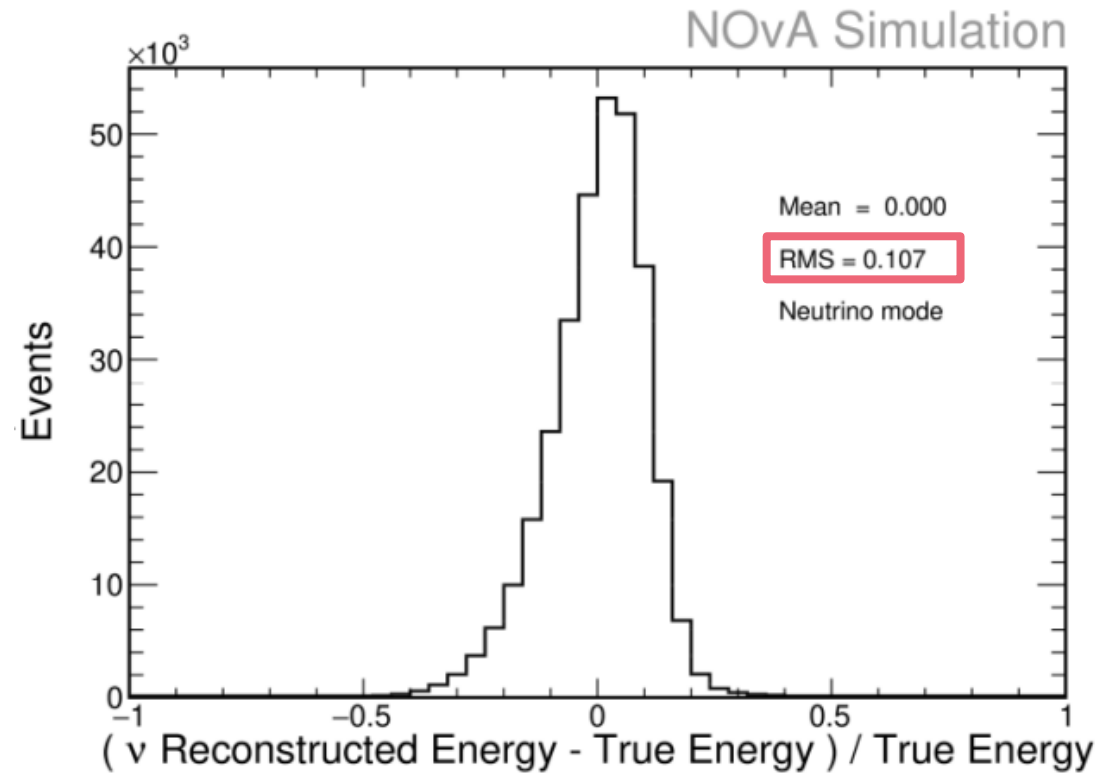
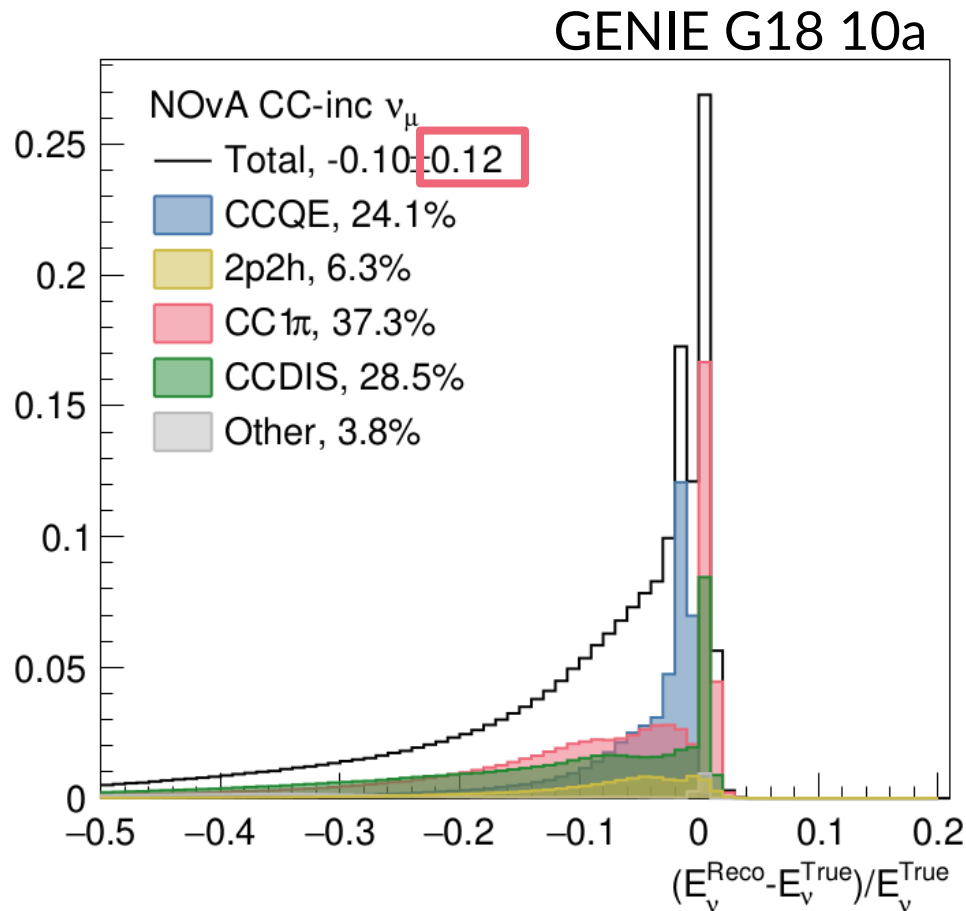
# Energy reconstruction

- Energy reconstruction method is function of **selection and detector technology**
- NOvA, DUNE and SBN have **sampling calorimeters** and often **events with multiple tracks**
  - **CC-inclusive** selection
  - Energy estimator which **sums up energy deposits**


$$E_{\nu}^{\text{calo}} = E_l + \left( \sum_{i=\pi^0, \gamma, \pi^{\pm}} E^i \right) + \left( \sum_{i=p} T^i \right)$$

# Calorimetric energy reconstruction

- Simple simulation result agrees well with NOvA official figure: ~11% RMS



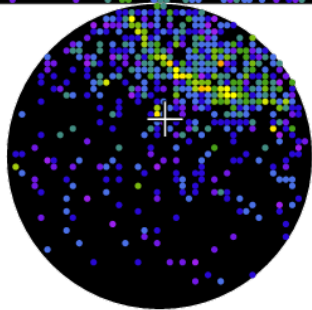
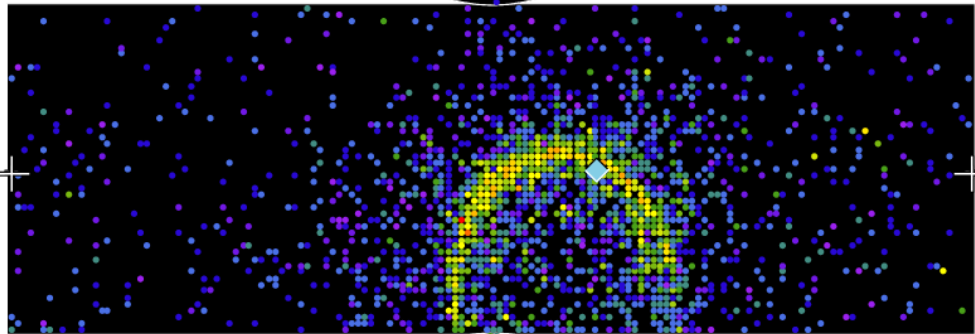
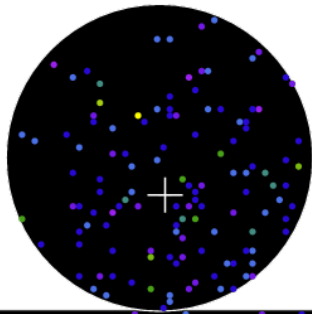
- Interaction modes bias differently, e.g. DIS has multiple missing neutrons and pion FSI

# Calorimetric energy reconstruction

- Generally more precise energy estimate than kinematic method
- Susceptible to missing neutrons and other particles
- **Final-state interactions** directly bias the estimator
- Relies on **correct PID of every track**, otherwise risk bias by rest mass (e.g. mistake proton for pion)
- Will always have bias from **initial state motion**
  - Smaller impact at higher energies, e.g. NOvA and DUNE
- CC-inclusive selection means **complex contributions from multiple interaction modes**

# Kinematic energy reconstruction

- Energy reconstruction method is function of **selection** and **detector technology**
- T2K and HK are dominated by **CC0 $\pi$  interaction**, and Cherenkov threshold for proton is  $>1$  GeV in H<sub>2</sub>O



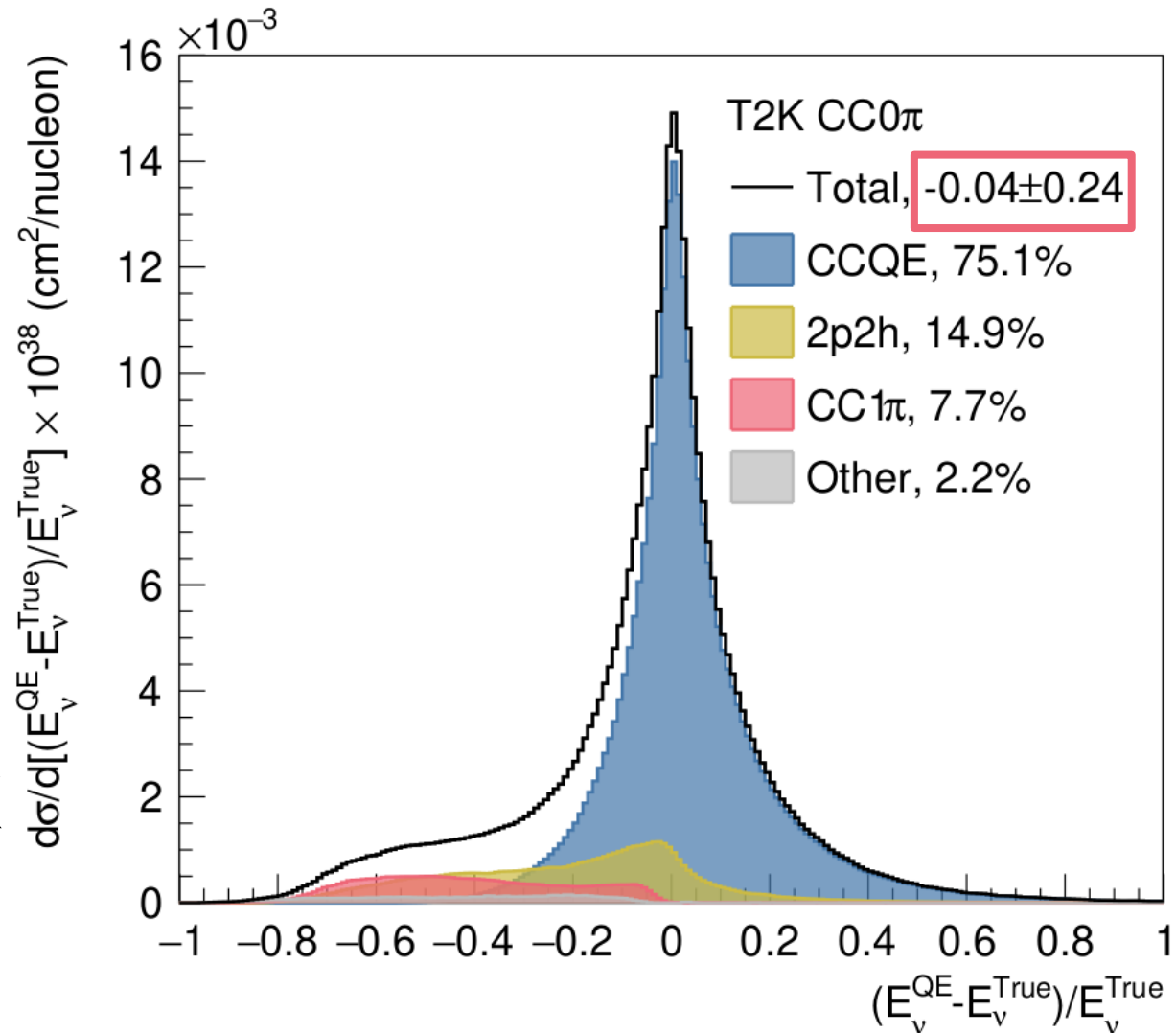
- **Single-track** events
- Kinematic reconstruction using **only lepton** information
- Assumes **4 legged CCQE** interaction, and **initial state nucleon at rest**

$$E_{\nu}^{\text{CCQE}} = \frac{2m_N E_l - m_l^2 + m_{N'}^2 - m_N^2}{2(m_N - E_l + p_l \cos \theta_{\nu,l})}$$

# Kinematic energy reconstruction

- **CCQE** contribution largely unbiased
- **20-25% RMS**
- CC1 $\pi$ +FSI and 2p2h contribution **less than 25% of total signal**
- When applied to CC1 $\pi$  sample, replace  $m_p$  with  $m_\Delta$ 
  - Works because T2K  $\Delta(1232)$  dominated





$$E_\nu^{\text{CCQE}} = \frac{2m_N E_l - m_l^2 + m_{N'}^2 - m_N^2}{2(m_N - E_l + p_l \cos \theta_{\nu,l})}$$



# Kinematic energy reconstruction

- Important to get the **CCQE, 2p2h and CC1 $\pi$  contributions correct**
  - They bias the estimator differently: mistaking non-CCQE for CCQE imposes a bias
- **Direct dependence on nuclear initial-state model**
  - Relatively large contribution at  $E_\nu=0.6$  GeV
- Only dependent on **FSI in the absorption**
  - Proton may lose energy to nucleus; does not matter in estimator
  - Secondary dependence on FSI through **missing particles**: think it's four-limbed interaction when it was not
- **Small contribution** from higher  $W$  resonances, SIS and DIS contributions

# Event counts at the FDs

Sample	 T2K	 NOVA	 Hyper-Kamiokande	 DUNE
$N_{\mu}^{\text{rec}}$ FHC	318	211	10000	7000
$N_{\mu}^{\text{rec}}$ RHC	137	105	14000	3500
$N_e^{\text{rec}}$ FHC	108	82	3000	1500
$N_e^{\text{rec}}$ RHC	16	33	3000	500

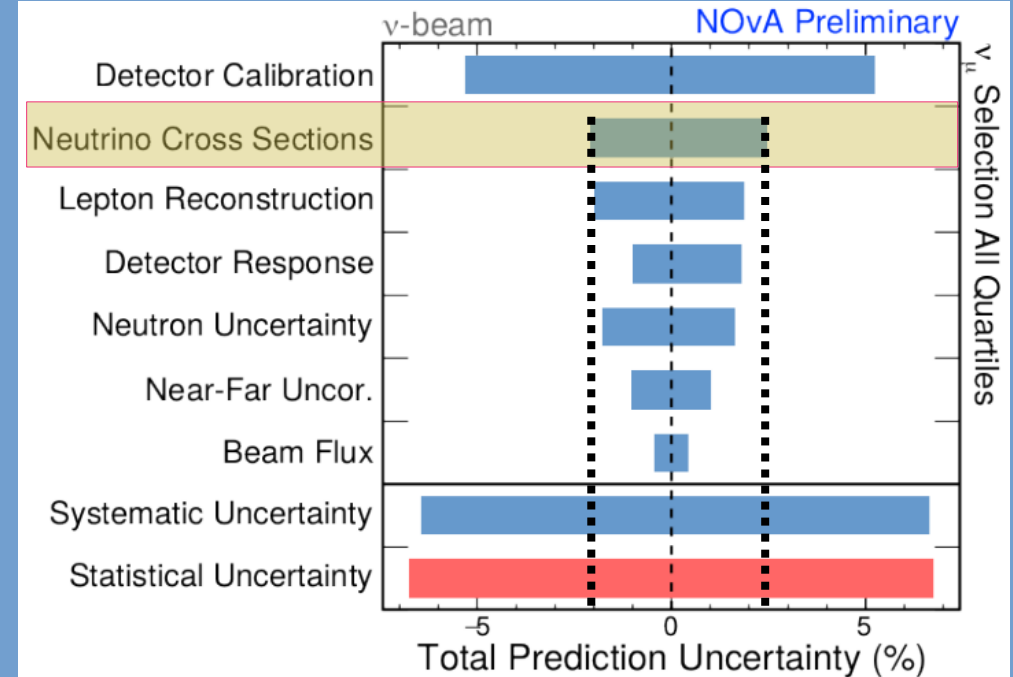
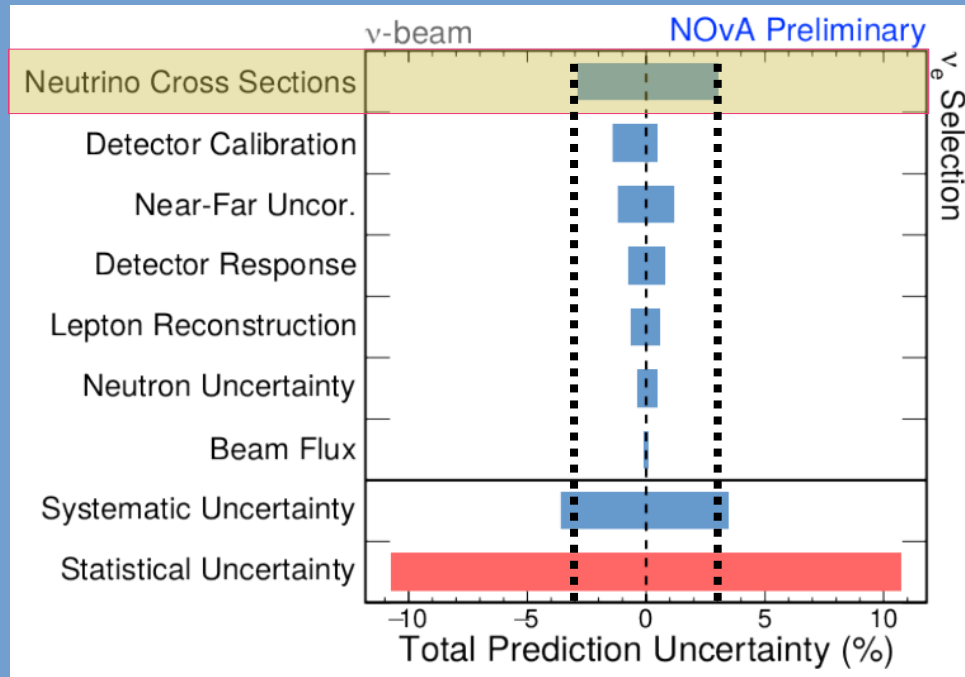
- HK and DUNE will have **enough events to be limited by the  $\sim 3\%$  (anti-) $\nu_e$  uncertainty**
- Current experiments at the **3-5% level uncertainties\***

\*Exception of T2K's single-pion-below-threshold sample (10-15%)

# Impact of systematics at the FD

- Neutrino cross-section uncertainties contribute ~3% to number of  $\nu_e$  on NOvA and T2K

M. Elkins, T. Nosek, Neutrino 2020 poster



Sample		Uncertainty source (%)			Flux ⊗ Interaction (%)	Total (%)
		Flux	Interaction	FD + SI + PN		
1Rμ	$\nu$	2.9 (5.0)	3.1 (11.7)	2.1 (2.7)	2.2 (12.7)	3.0 (13.0)
	$\bar{\nu}$	2.8 (4.7)	3.0 (10.8)	1.9 (2.3)	3.4 (11.8)	4.0 (12.0)
1Re	$\nu$	2.8 (4.8)	3.2 (12.6)	3.1 (3.2)	3.6 (13.5)	4.7 (13.8)
	$\bar{\nu}$	2.9 (4.7)	3.1 (11.1)	3.9 (4.2)	4.3 (12.1)	5.9 (12.7)
1Re1de	$\nu$	2.8 (4.9)	4.2 (12.1)	13.4 (13.4)	5.0 (13.1)	14.3 (18.7)

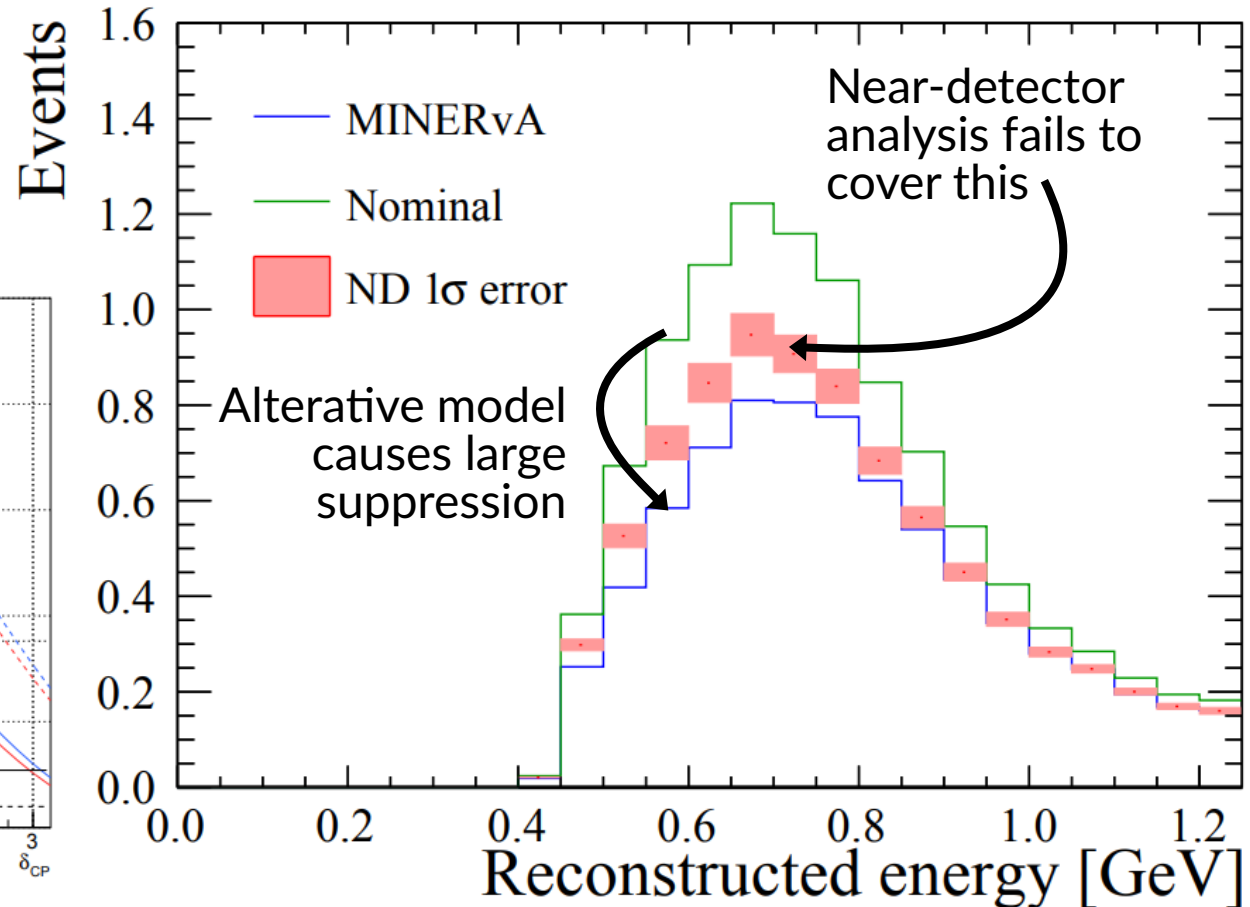
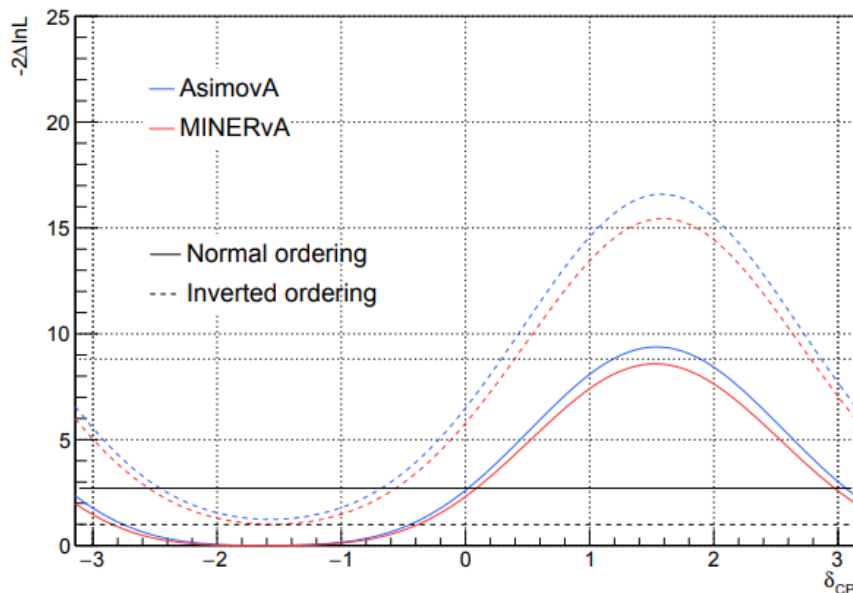


# Fake-data studies

- Realistically, won't have a perfect interaction model for a *timely* oscillation analysis
- Reasonable best case scenario: a model that fits the experimental data, but is not applicable to other experiments
  - The model is *effective*, but **not complete**
  - The physics is **not modelled exactly**, but **approximately**, with effects soaked up in the wrong part of the model
- What if nature is described by a different model; **what bias** is incurred on **oscillation parameters**?
- The bias this may cause is generally mitigated by “**fake-data studies**”
- **Can change exclusion statements and model choices**

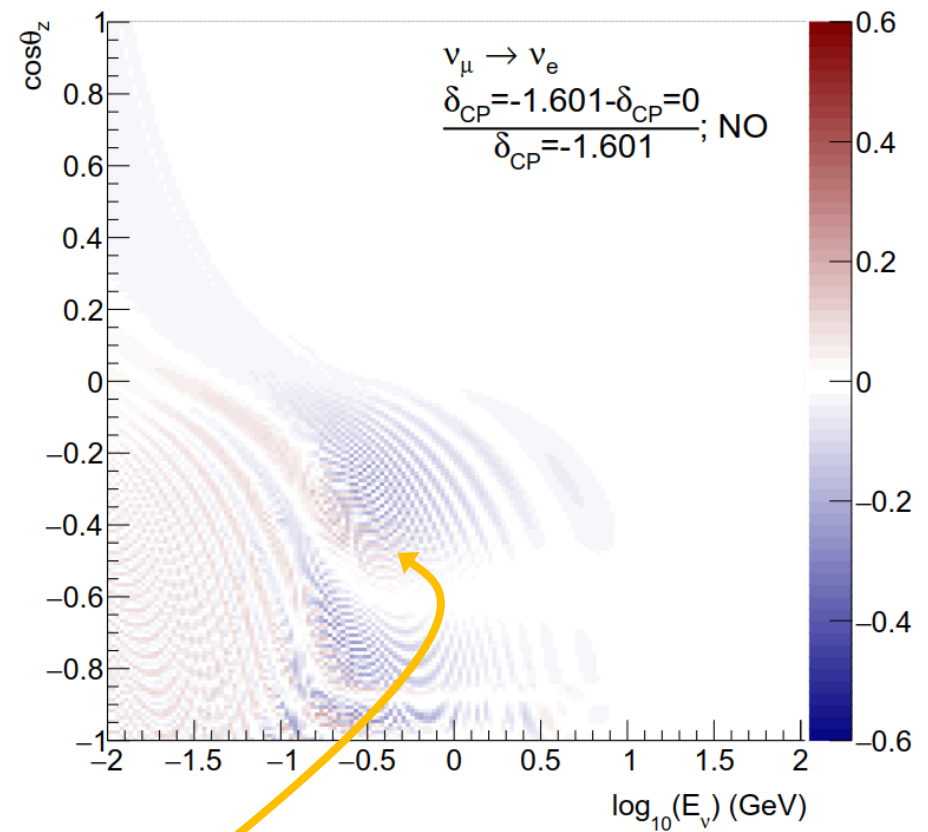
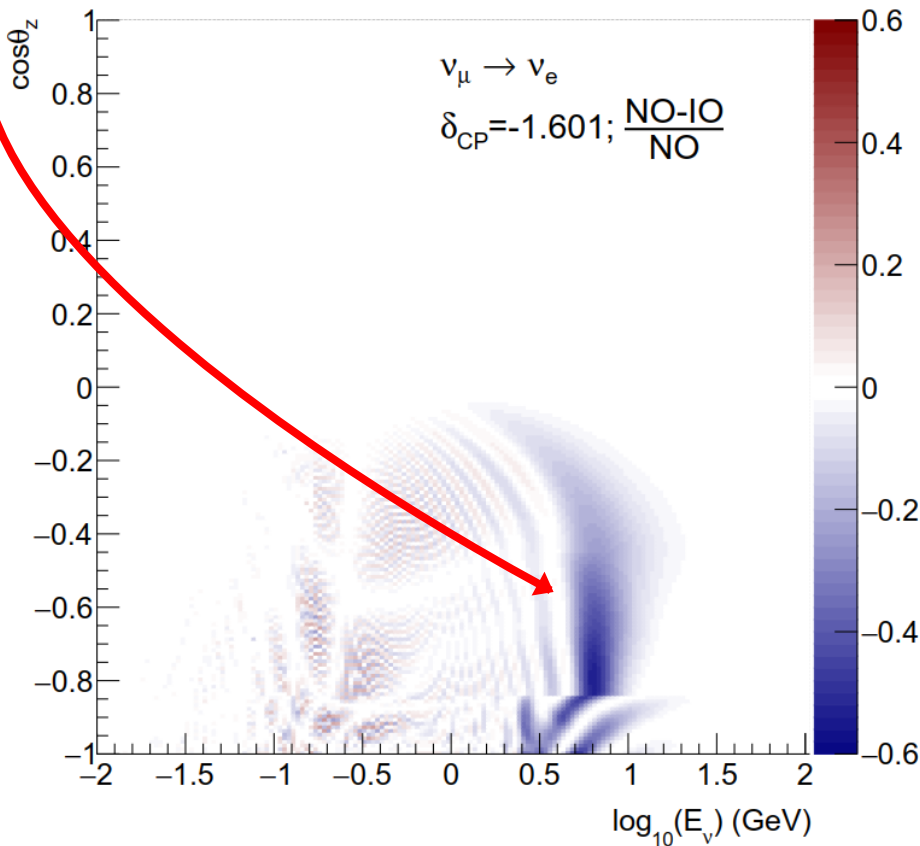
# Fake-data studies

- Use an alternative model to make a prediction for near and far detectors
- Fit to the alternative model at the near detector
  - Set of parameters that best describe the alternative model
- Propagate result to far detector, perform oscillation analysis



# Atmospheric neutrinos

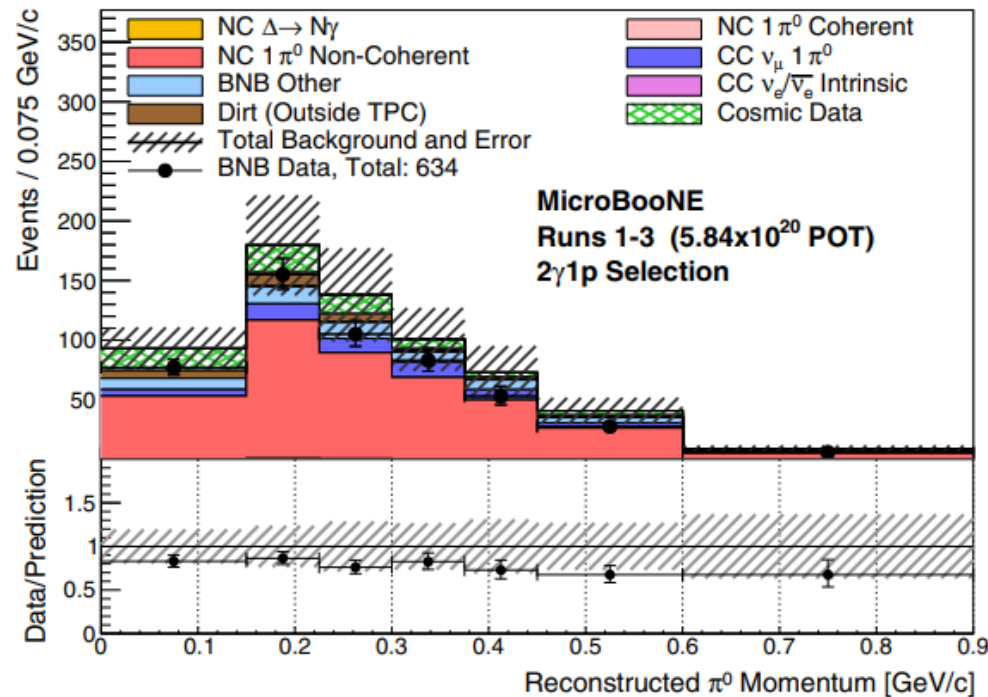
- Atmospheric neutrinos have sensitivity to mass ordering via 3-10 GeV resonance
  - Opposite effect for neutrino and anti-neutrinos: **need to separate**
  - Contribution from  $\nu_\mu \rightarrow \nu_\tau$ , where  $\nu_\tau$  enters multi-ring  $\nu_e$  sample



- $\delta_{CP}$  sensitivity from  $\nu_e$  below 1 GeV  $\rightarrow \nu_e/\nu_\mu$  important
- **Neutrino flavour differences** also limiting atmospheric results

# SBN

- For SBN programme and appearance searches, anything mimicking  $\nu_e$  appearance is important
  - e.g. NC1 $\gamma$ , NC1 $\pi^0$  DIS, NC1 $\pi^0$  resonant, NC1 $\pi^0$  coherent
  - Many constrained by dedicated measurements and sidebands



Phys. Rev. Lett.  
 128, 111801

- $\nu_e/\nu_\mu$  differences from nucleon and nuclear environment, especially considering  $^{40}\text{Ar}$

# What do I worry about?

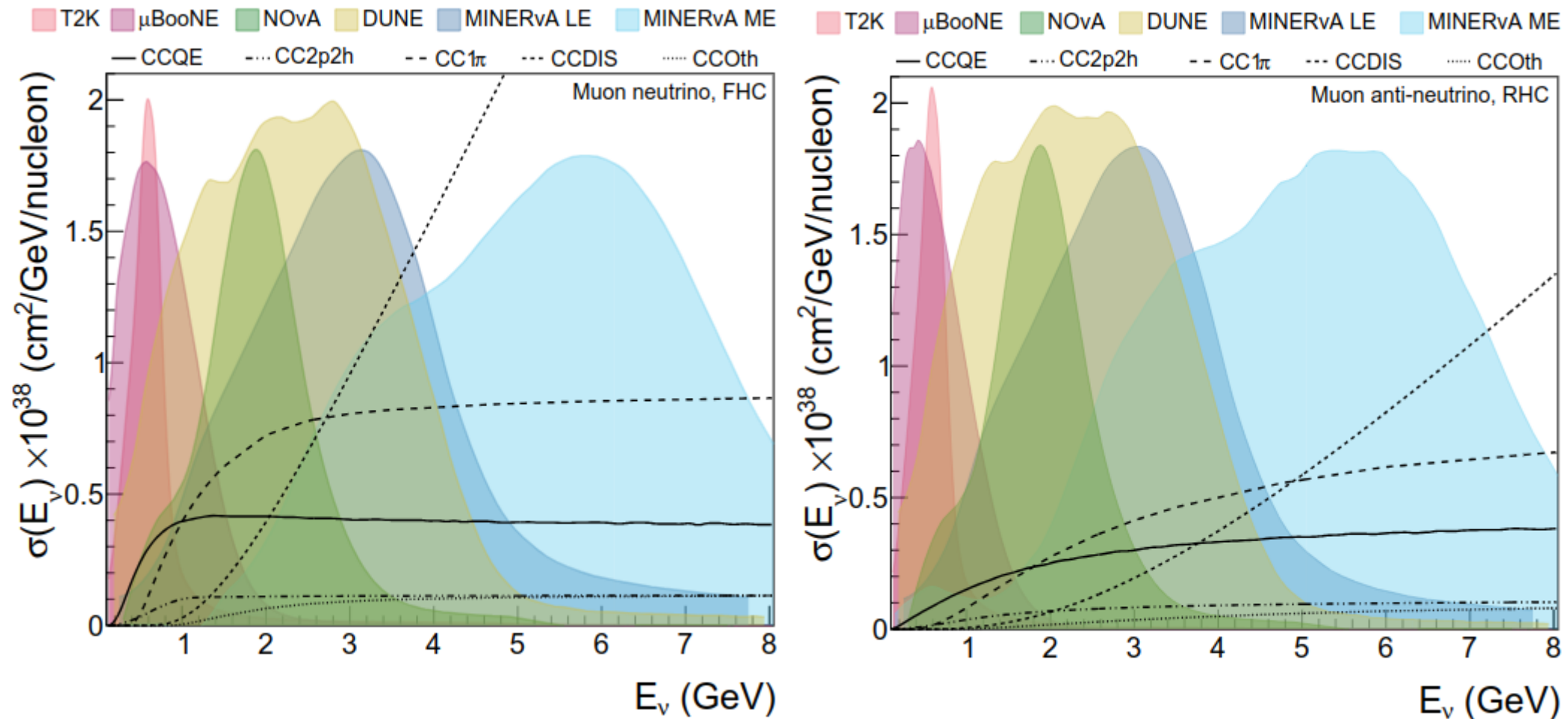
- Will **(anti-) $\nu_e$**  uncertainties fall below 2-3%?
  - Critical for  $\delta_{CP}$ , mass ordering, for both **atmospheric** and **accelerator** experiments, and **MiniBooNE LEE**
- Do we understand **transition, SIS and DIS** interactions sufficiently for **DUNE**?
  - Worry that the day DUNE ND turns on, it'll show how poorly we describe these samples
- Will we understand **nuclear effects in  $^{40}\text{Ar}$**  nuclear in 10 years time?
- Will we understand **neutron final-state interactions** sufficiently to use them for e.g. **energy estimators** and **tagging events**?
- **$\nu_\tau$  uncertainties** for **atmospheric neutrinos** and **mass ordering sensitivity**
- How do we diagnose **low momentum pion modelling**

# Summary

- Neutrino interactions are a central ingredient to the accelerator and atmospheric neutrino measurements
  - Starting to see importance on current-generation experiments like T2K, NOvA, SK
  - Critical for next-generation experiments HK and DUNE
- Experiments and generator groups are including latest model developments
- Theory community gaining people and working hard at developing modelling
  - e.g.  $^{40}\text{Ar}$  spectral functions, 2p2h models and uncertainties, single pion production, sophisticated nuclear models...
- Very exciting time for the field, and an excellent week to be in Sao Paolo!

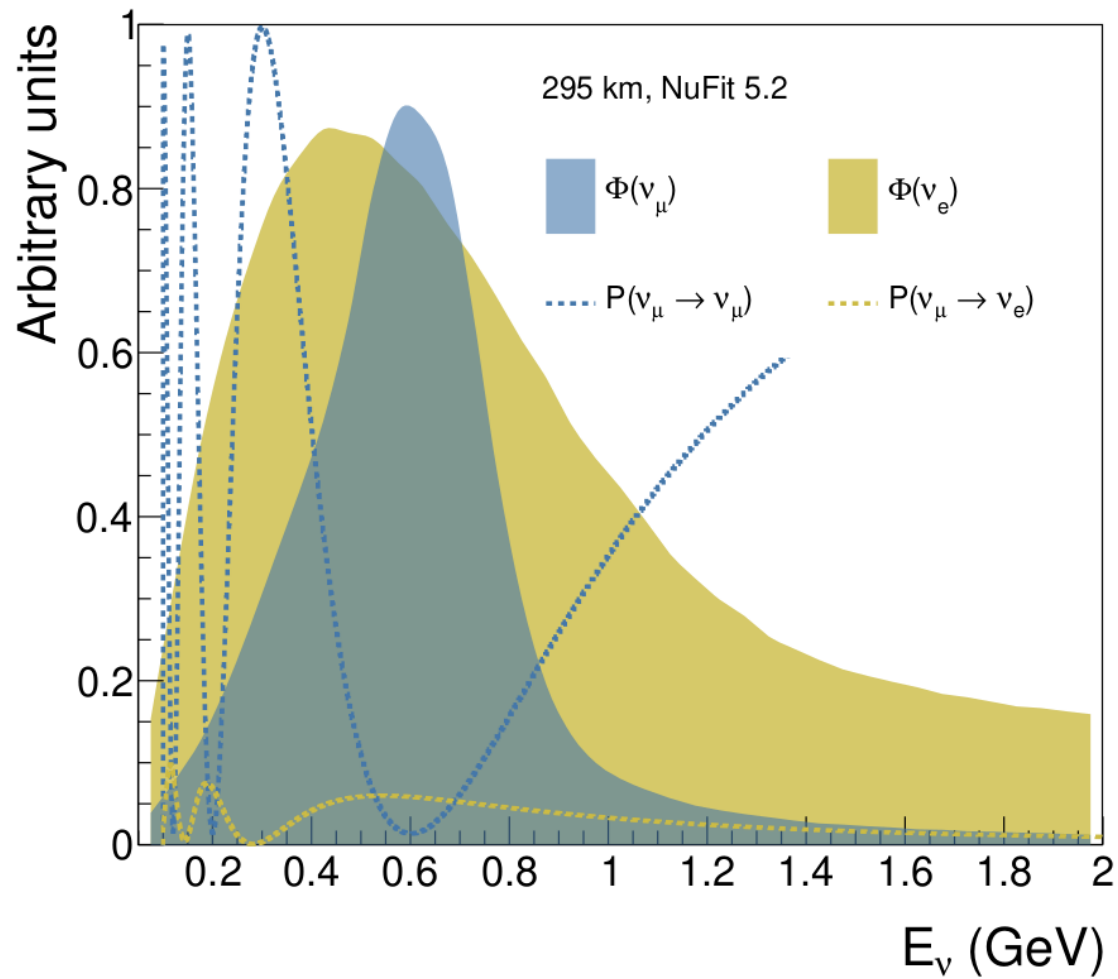
# Backups

# Neutrino fluxes



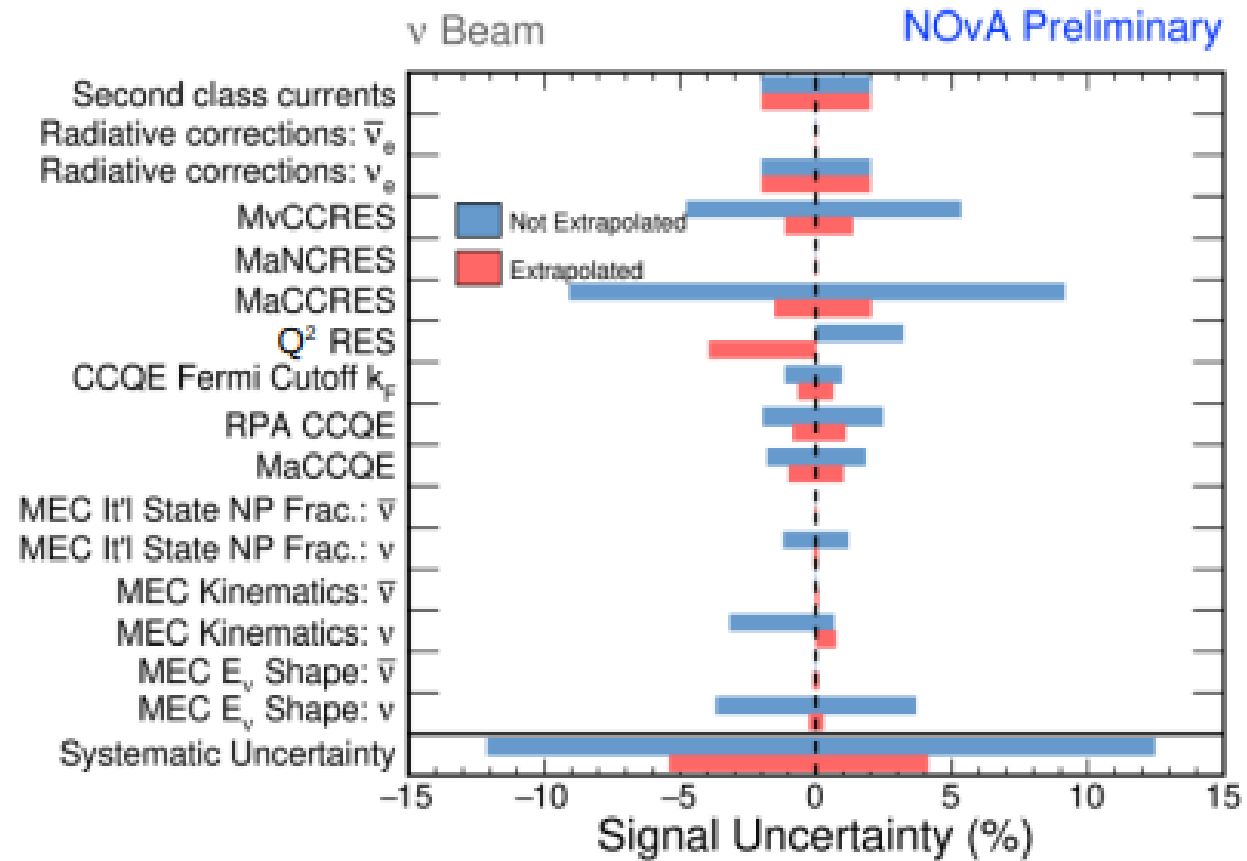


# Neutrino fluxes



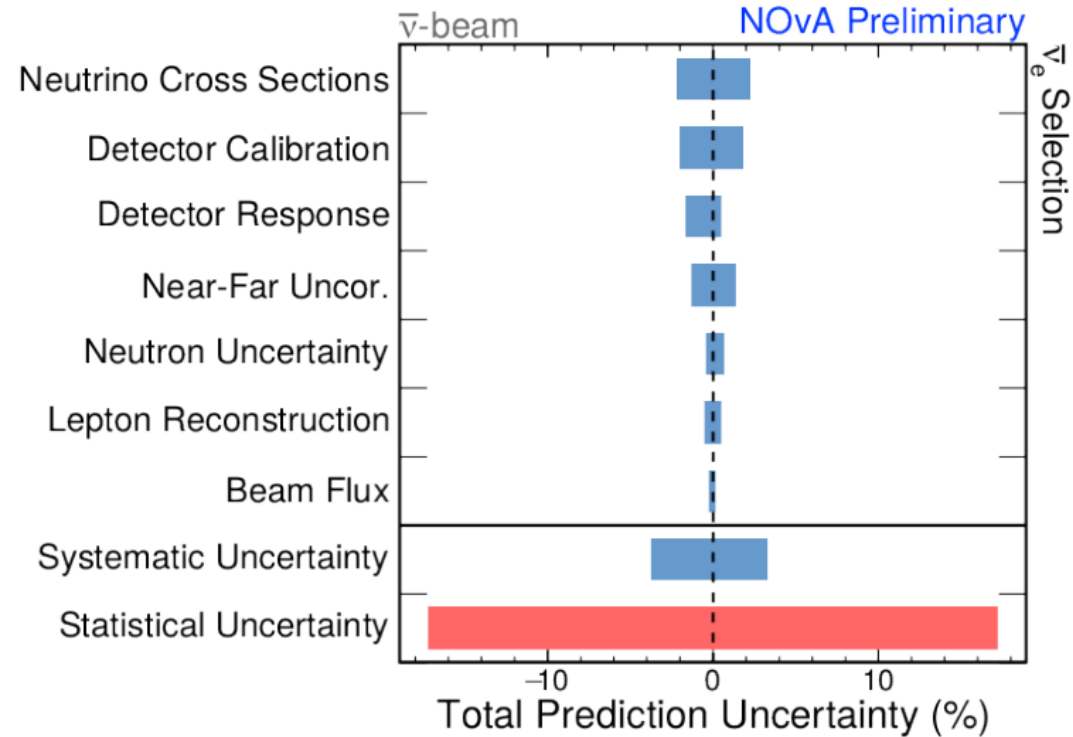
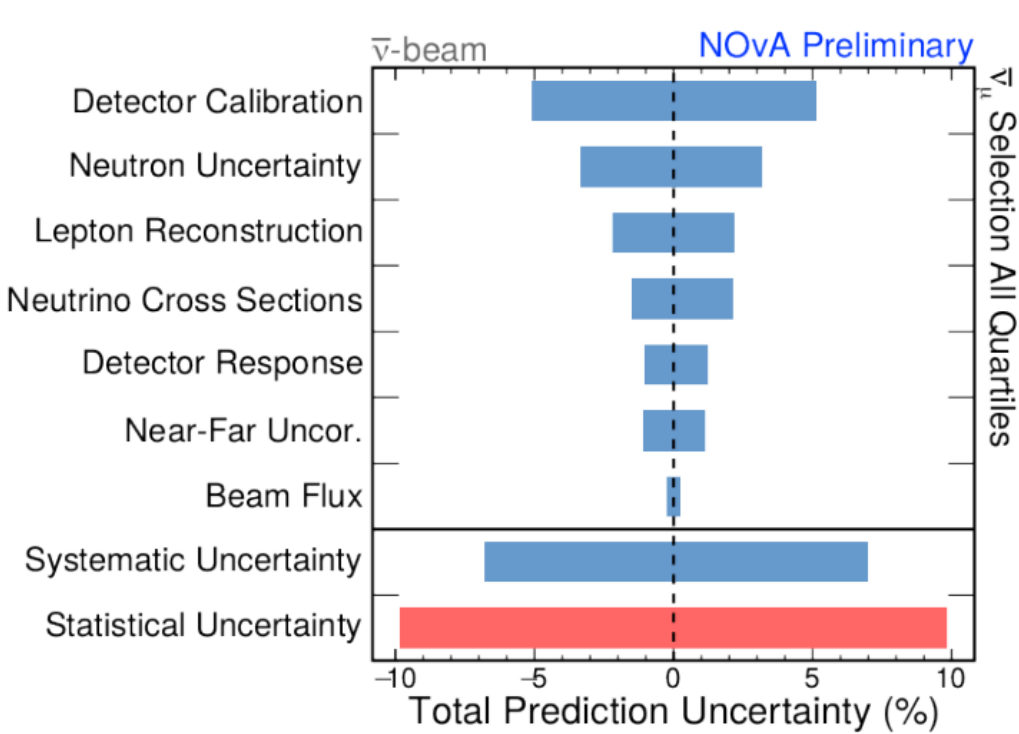
# NOvA

- Jeremy Wolcott, NuInt17



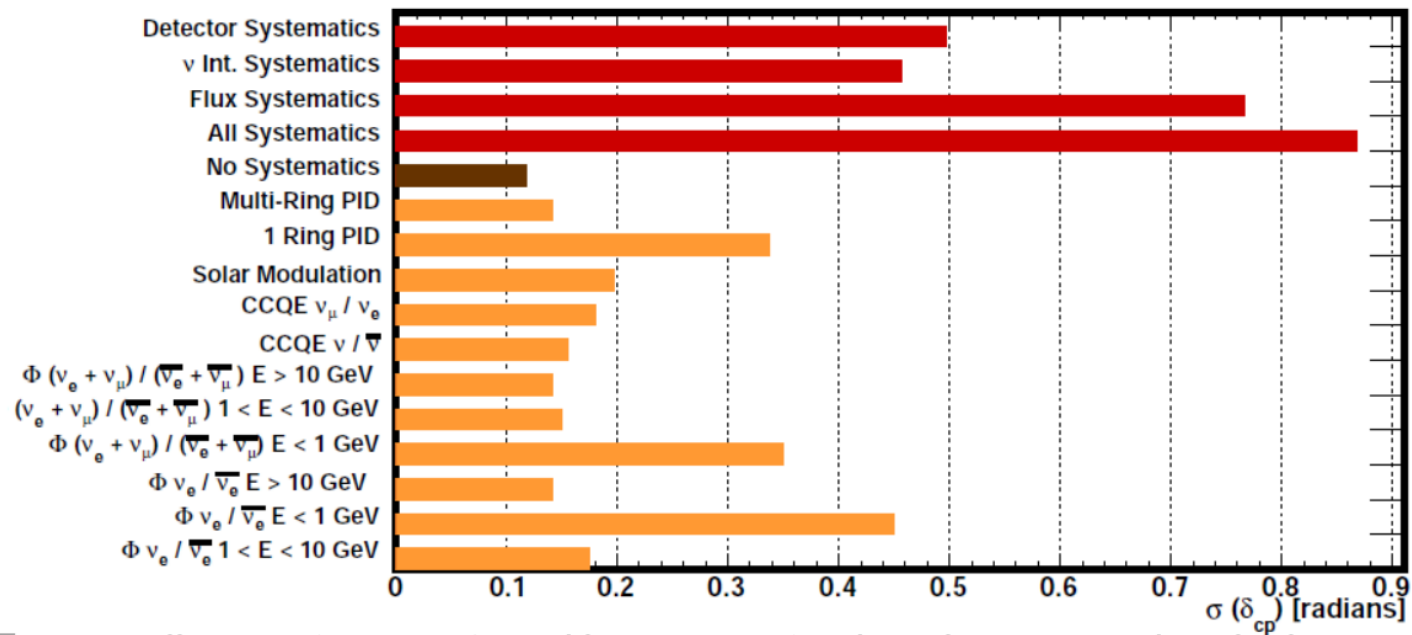
# NOvA

M. Elkins, T. Nosek, Neutrino 2020 poster



# Atmospheric

## Hyper-K's Sensitivity to $\delta_{cp}$ with Atmospheric neutrinos



## Systematic Effect on Hierarchy Sensitivity at Super-K

