

Impact of neutrino interaction uncertainties on $T2K$ physics measurements



Laura Munteanu on behalf of the T2K experiment

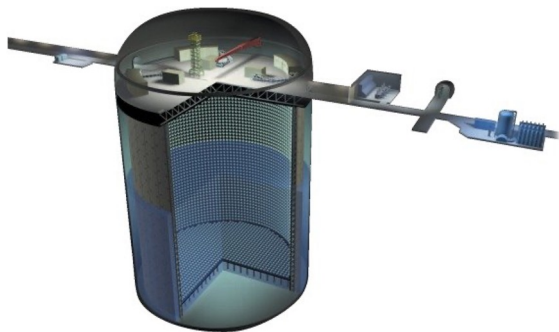
NuInt 2024, São Paulo, Brazil

15 April 2024

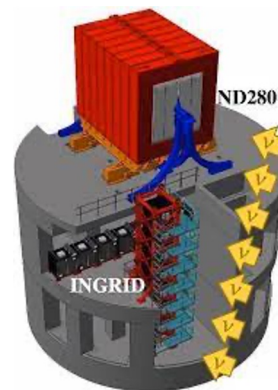


The T2K Experiment

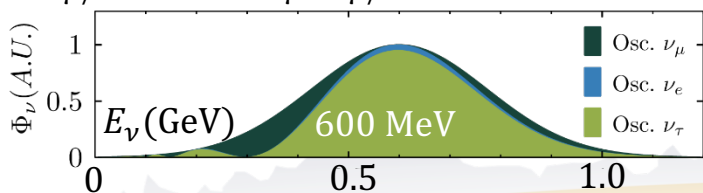
Far detector: Super-Kamiokande



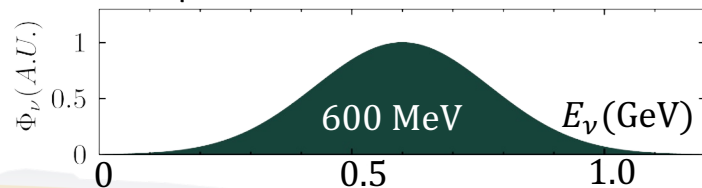
Near detector complex



$$N_{\nu_{\mu/e}}(E_\nu) = P_{\nu_\mu \rightarrow \nu_{\mu/e}}(E_\nu) \Phi(E_\nu) \sigma(E_\nu) \epsilon(E_\nu)$$



$$N_{\nu_\mu}(E_\nu) = \Phi(E_\nu) \sigma(E_\nu) \epsilon(E_\nu)$$



Baseline ~295 km

Neutrino beam

T2K physics program

Neutrino oscillations

Nature 580, 339–344 (2020)



Eur. Phys. J. C 83, 782 (2023)

Eur. Phys. J. C (2023) 83:782
<https://doi.org/10.1140/epjc/s10052-023-11819-x>

THE EUROPEAN
PHYSICAL JOURNAL C

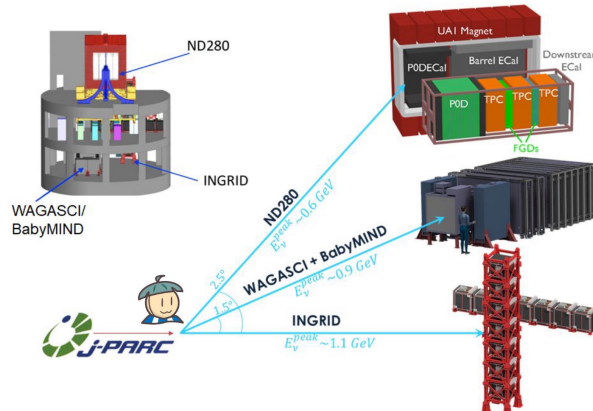


Regular Article - Experimental Physics

Measurements of neutrino oscillation parameters from the T2K experiment using 3.6×10^{21} protons on target

T2K Collaboration

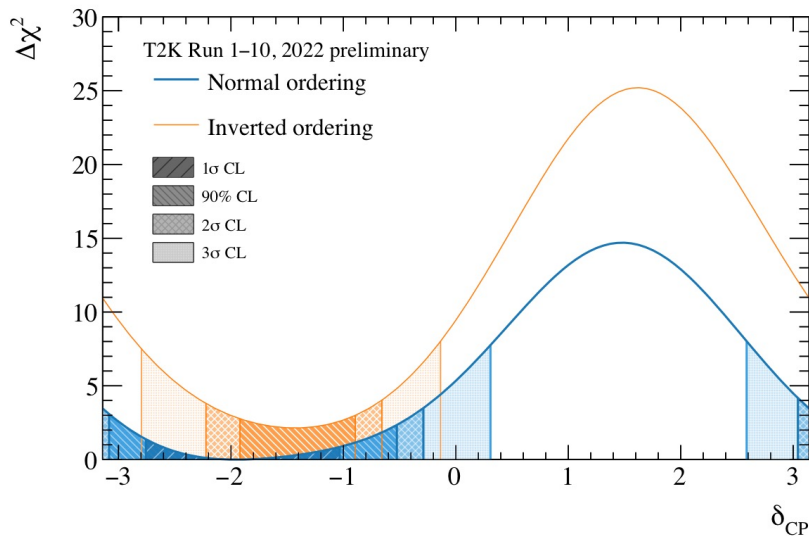
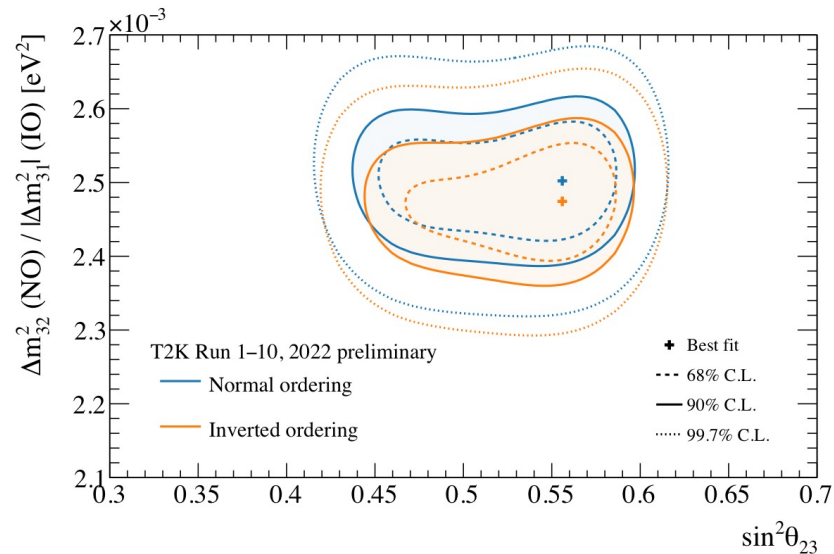
Neutrino cross-sections



Exotic searches

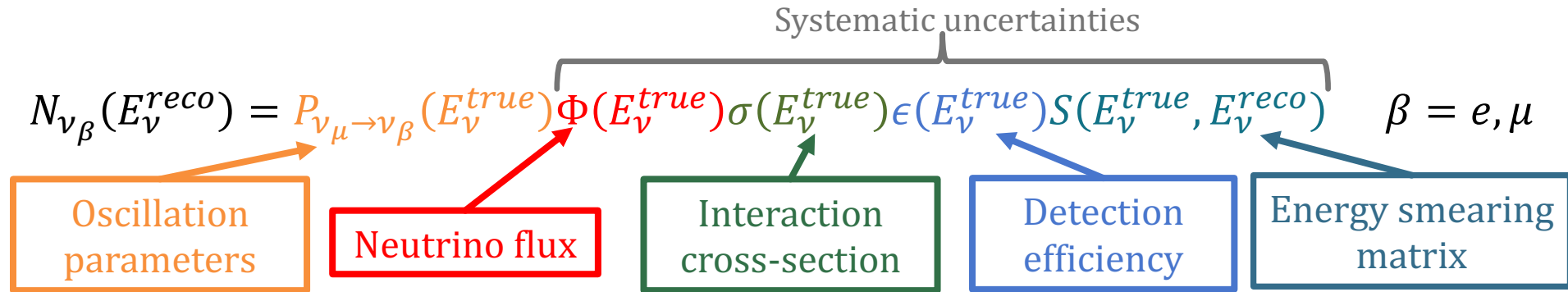
See talks by
S. Dolan
C. Jesús-Valls

Latest oscillation results



Measuring neutrino oscillations with T2K

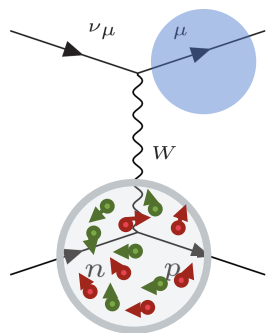
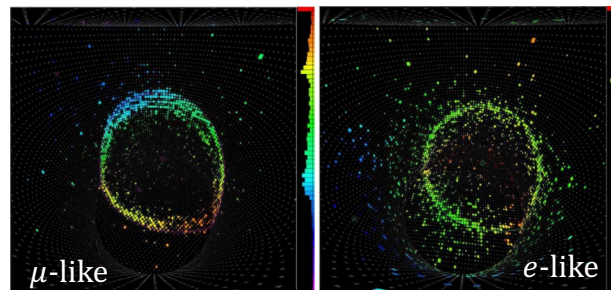
- Oscillation parameters are inferred from event spectra **as a function of reconstructed neutrino energy**



- Constrain systematics with **near detector**
- But **heavily rely on models** to predict near-to-far detector **extrapolation and neutrino energy smearing**

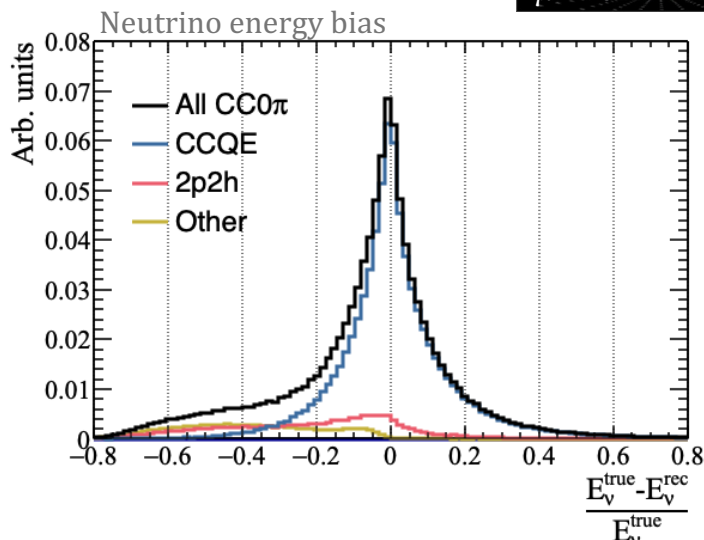
Measuring neutrino oscillations with T2K

Oscillated neutrino event rates as a function of neutrino energy measured with SK – water Cherenkov detector



Infer neutrino energy using **lepton information** under 2-body reaction assumption

15.04.2024



Laura Munteanu - NuInt 2024, São Paulo, Brazil

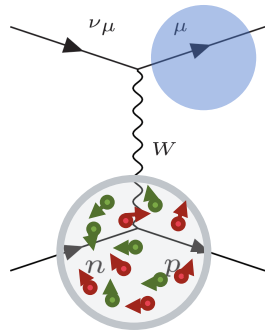
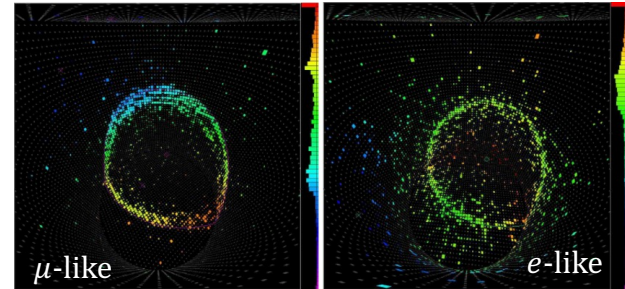
Need to control: (1st order)

- Shape of **Fermi motion**
- Proportion of **QE vs non-QE** processes
- **Physics beyond PWIA**
- **Energy dependence** of the cross-section (due to oscillations)
- **A-scaling** (C and O)

PWIA: Plane Wave Impulse Approximation 6

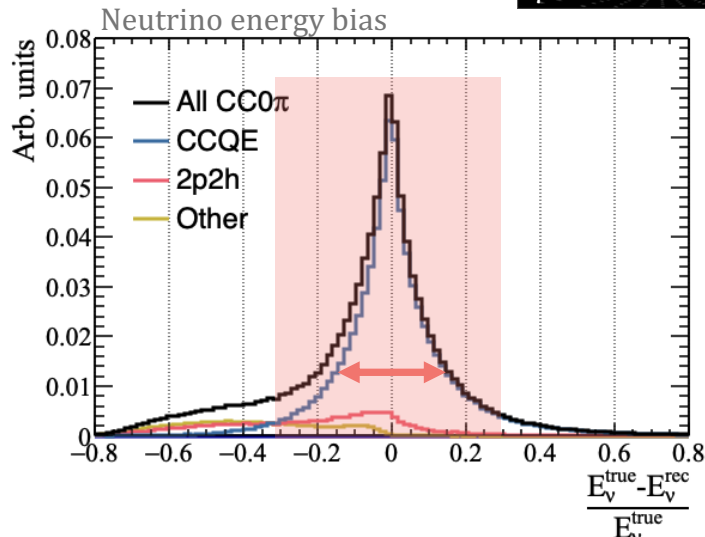
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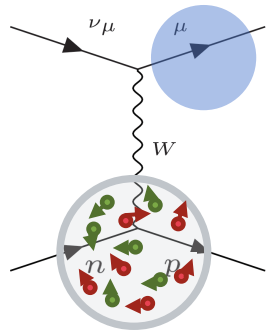
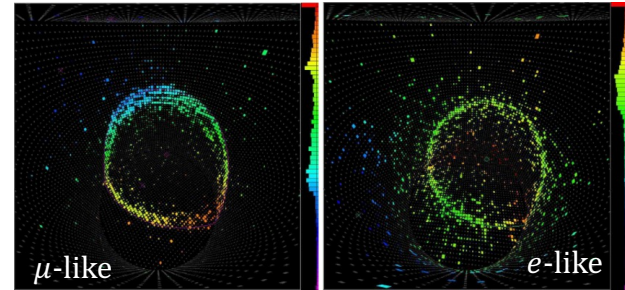
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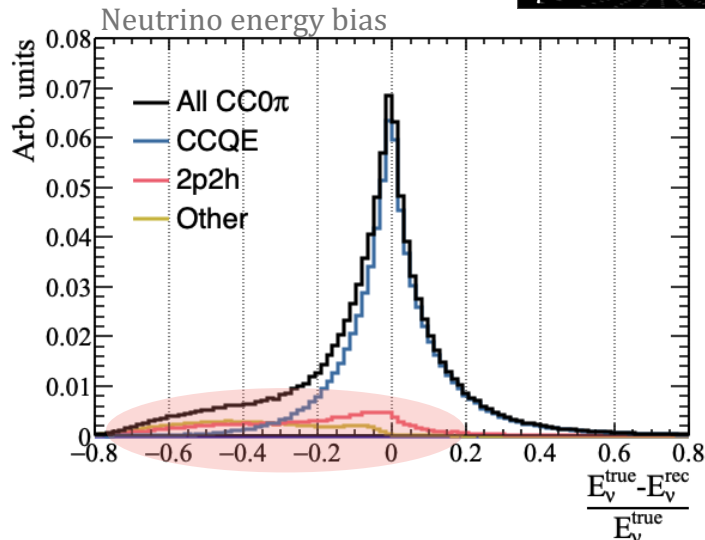
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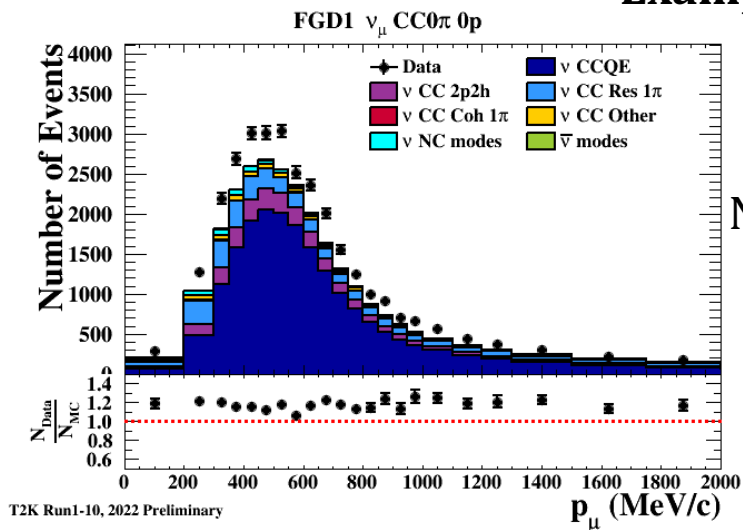
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PWIA: Plane Wave Impulse Approximation 8

Constraining uncertainties with near detector data

- 22 near detector samples
- 4000+ bins in $(p_\mu, \cos\theta_\mu)$
- ~ 700 parameters (~ 70 for cross-section uncertainties)

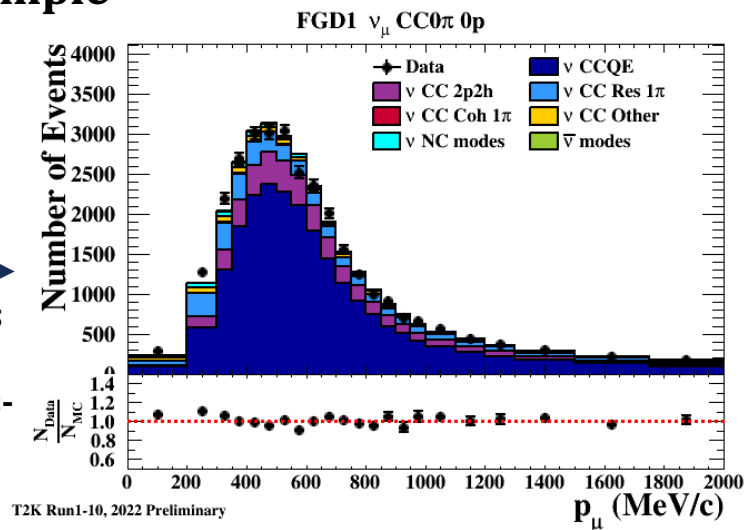
Example: $\text{CC}0\pi0p$ sample



Near detector fit



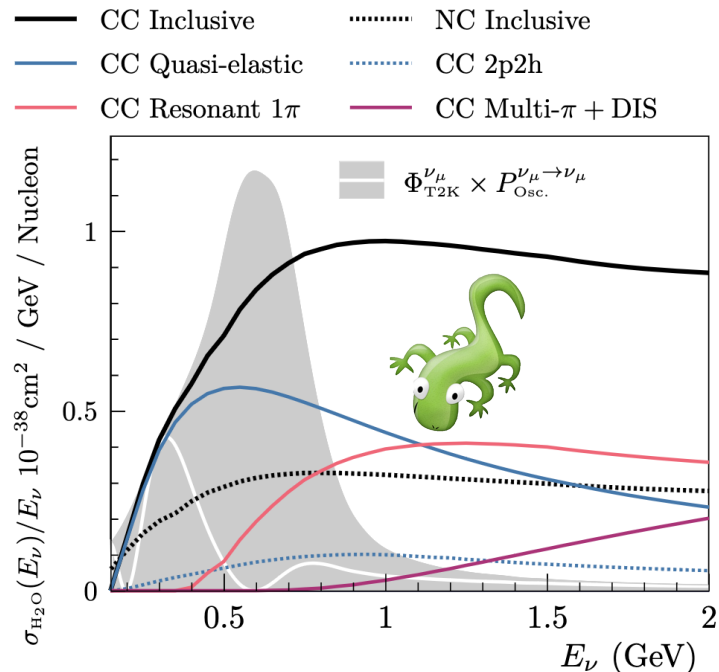
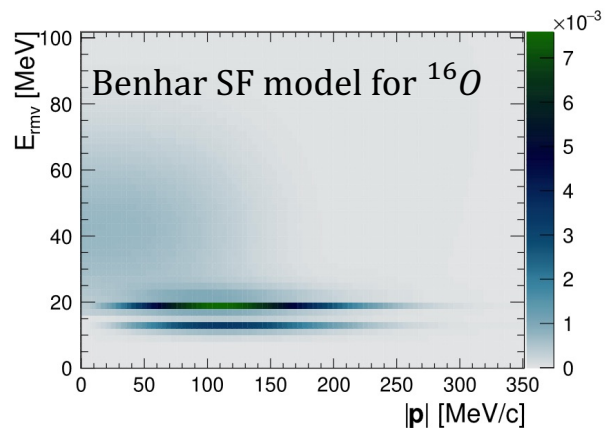
Varies parameters related to flux, detector and **cross-section model**



Baseline model and simulation

T2K uses the NEUT neutrino event generator

Process	Model
CCQE (1p1h)	Benhar Spectral Function (SF)
CC 2p2h	Nieves et al. 2p2h
CC Resonant	Rein Sehgal
Final State Interactions	NEUT cascade (based on Salcedo & Oset)



See talk by P. Stowell

CCQE uncertainties – intrinsic degrees of freedom

T2K is the first neutrino oscillation experiment to use a non-Fermi gas model

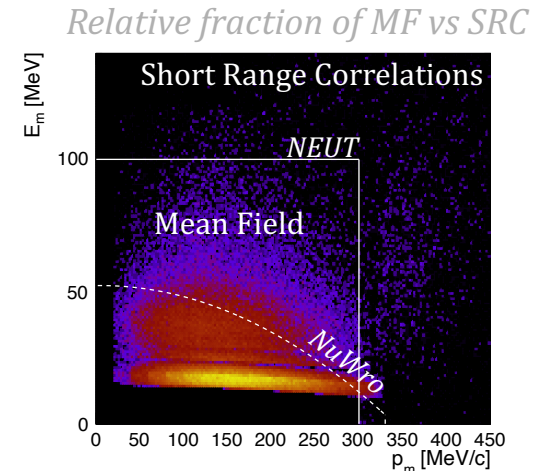
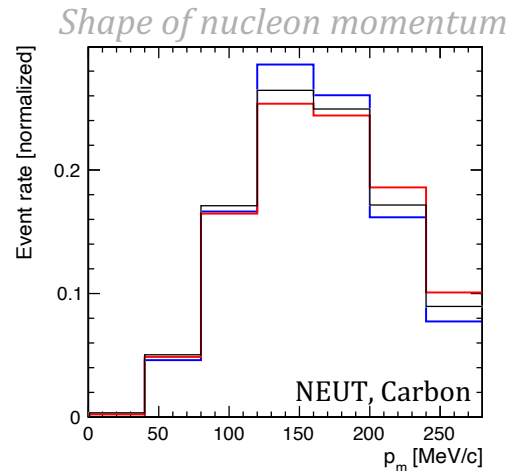
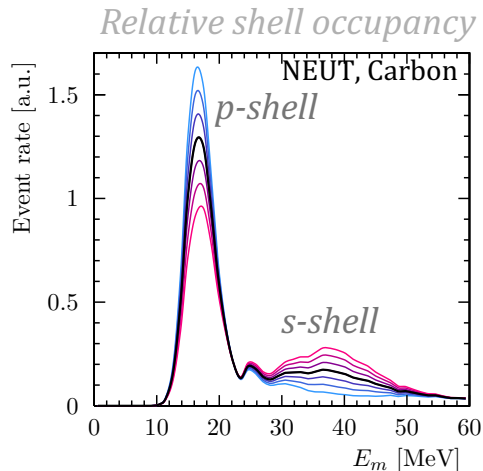
- ✓ Tuned to $ee'p$ data
- ✓ More powerful at predicting hadron kinematics than other available models
- ✓ Possibility to vary physically meaningful degrees of freedom

CCQE uncertainties – intrinsic degrees of freedom

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* E_m, p_m – missing energy and momentum



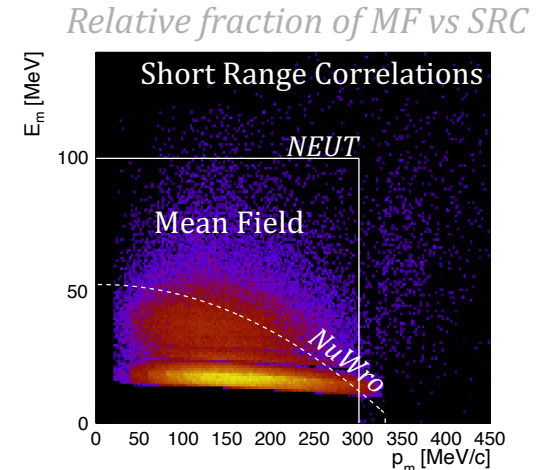
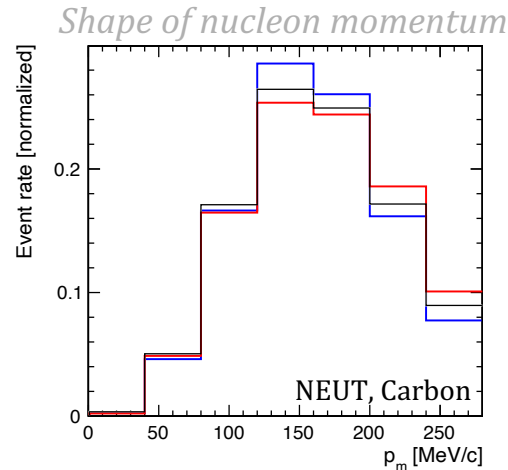
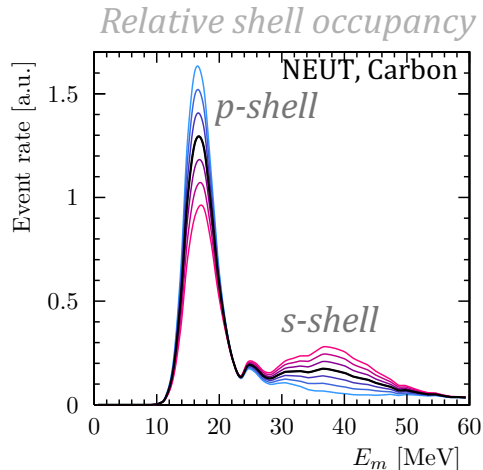
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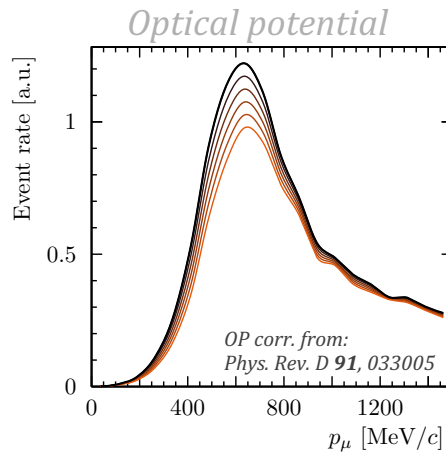
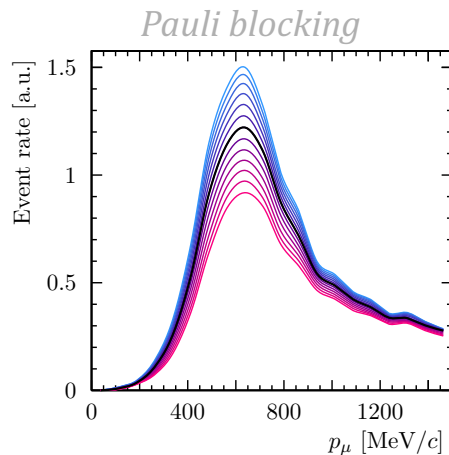
- ✗ Relies on factorization approach
- ✗ Does not include FSI effects on the lepton
- ✗ Simplistic description of Pauli blocking

* E_m, p_m – missing energy and momentum

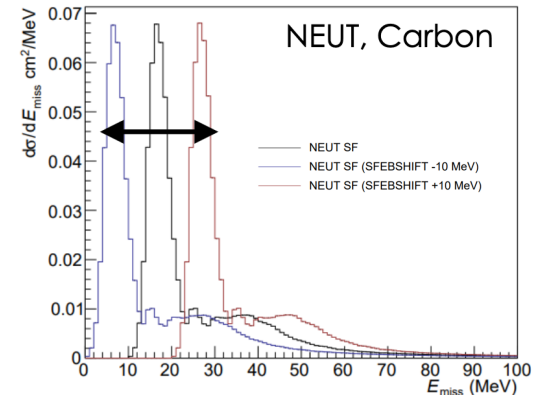


CCQE uncertainties – effective degrees of freedom

Current near detector fit is performed as a function of **lepton kinematics only**
 → Include **effective** d.o.f. which alter the shape of lepton kinematic distributions



Shift in removal energy distribution

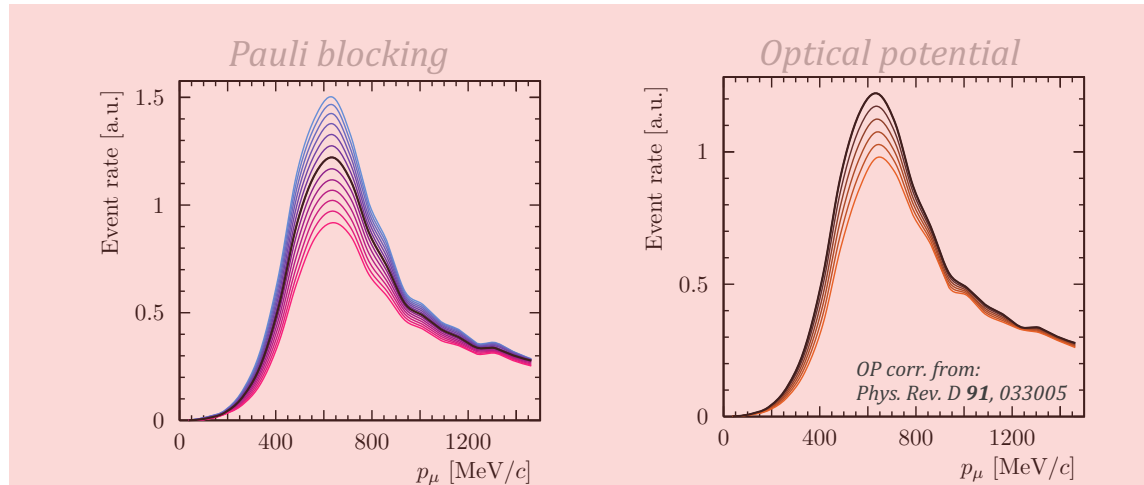


CCQE uncertainties – effective degrees of freedom

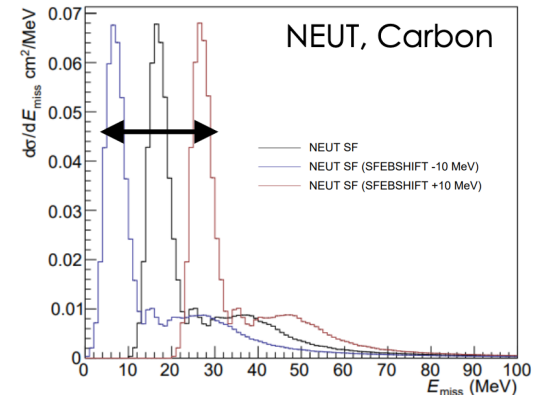
Current near detector fit is performed as a function of **lepton kinematics only**
 → Include **effective** d.o.f. which alter the shape of lepton kinematic distributions

Target low- ω region ($\sim 15\%$ of CCQE events)
 where effects beyond PWIA are important

PWIA: Plane Wave Impulse Approximation



Shift in removal energy distribution

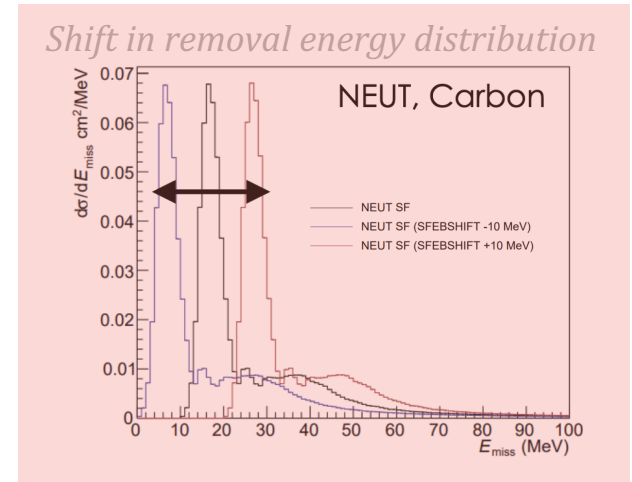
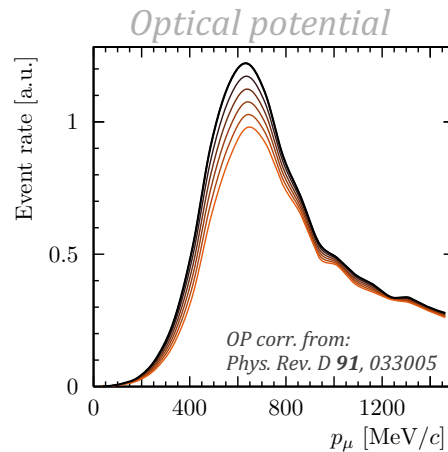
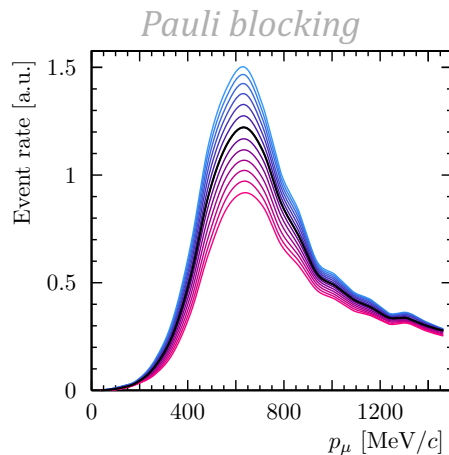


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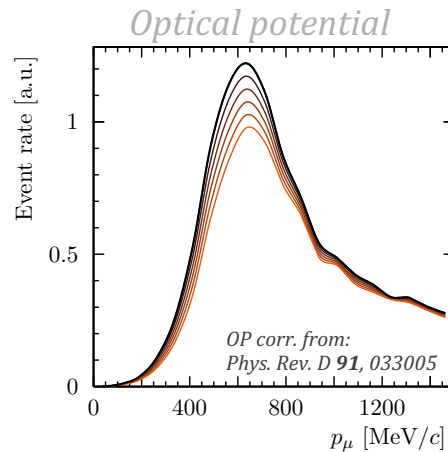
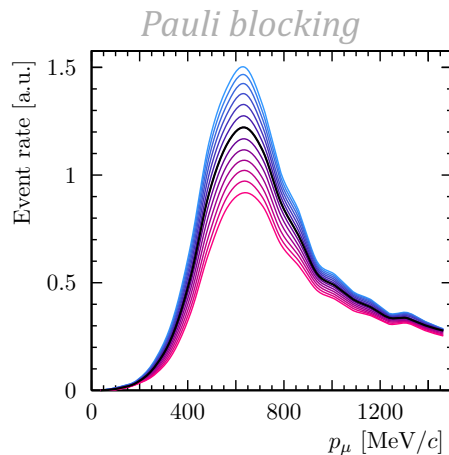
Account for uncertainties in shell positions
Previously dominant source of systematic uncertainty on Δm_{32}^2
(now subdominant thanks to use of SF model and $ee'p$ constraints)



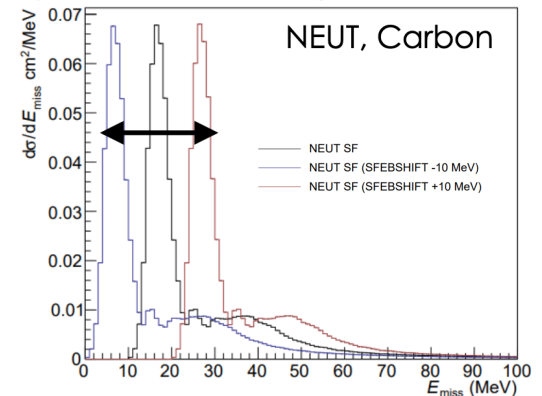
CCQE uncertainties – effective degrees of freedom

Current near detector fit is performed as a function of **lepton kinematics only**
 → Include **effective** d.o.f. which alter the shape of lepton kinematic distributions
 + Effective Q^2 shape freedom for deviations from dipole M_A prediction

Will need revisiting once we include hadron kinematics in the ND analysis



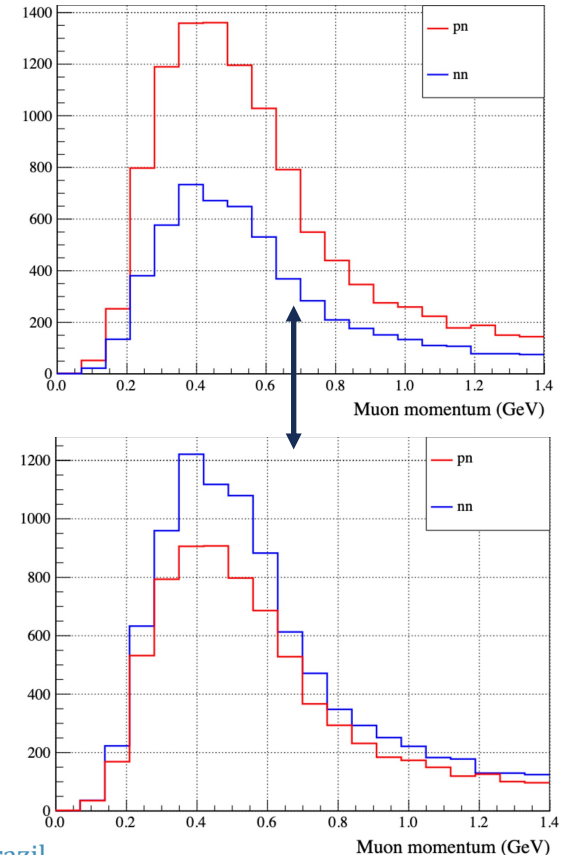
Shift in removal energy distribution



2p2h uncertainties

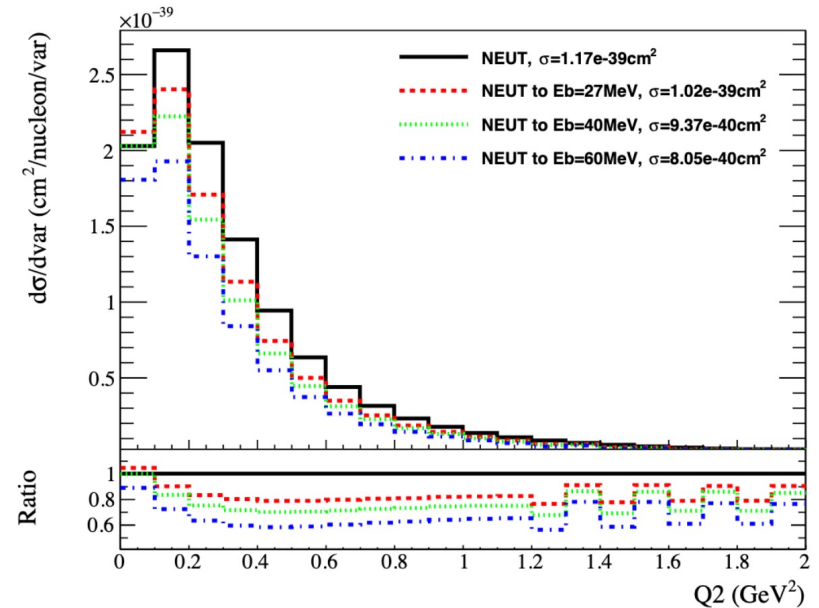
- Dominant non-QE contrib. in $CC0\pi$ samples
- Simulated using Nieves et al. 2p2h model
- Freedoms include:
 - Normalization
 - Shape (Δ vs non- Δ components)
 - nn vs np pair fractions
 - Energy dependence of different models
- Lacking freedom in nucleon kinematics
 - Not very impactful for current analyses
 - But will become critical in future analyses

Impact of varying the fraction of 2p2h nn and np initial states



Pion production uncertainties

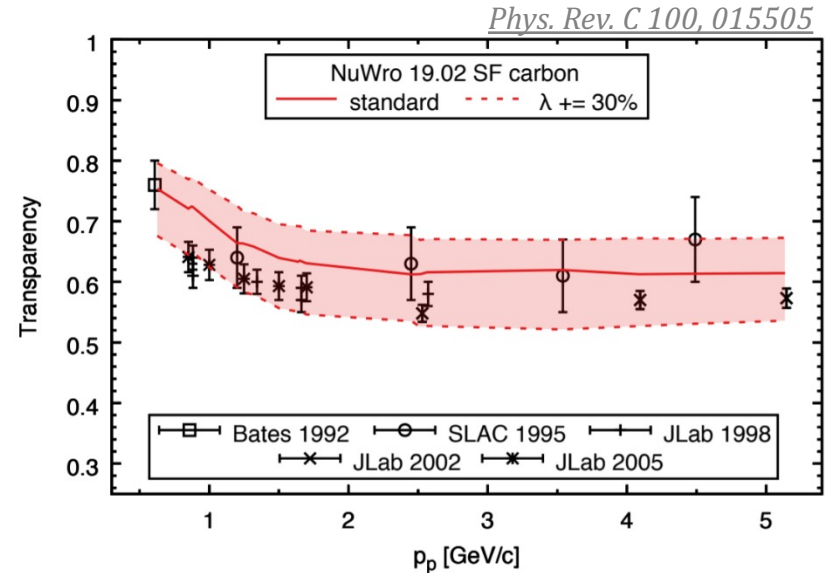
- Baseline model: Rein-Sehgal + Graczyk-Sobczyk form factors
- Dominated by Δ resonance, but 17 resonances + interferences included
- Non-resonant pion production but no interference with resonant production
- Parameters which control:
 - Form factors (M_{RES}^A and C_5^A) – newly tuned
 - Non-resonant contributions
 - Removal energy in π -production events
 - Resonance decay kinematics



Impact of varying the removal energy for π -production events

Final State Interactions

- Salcedo-Oset intra-nuclear cascade
 - 6 meson FSI parameters tuned to π -C and π -O scattering data *Phys. Rev. D* **99**, 052007
- Simple parameter to control probability of proton FSI



Robustness studies

Our uncertainty model is not complete due to

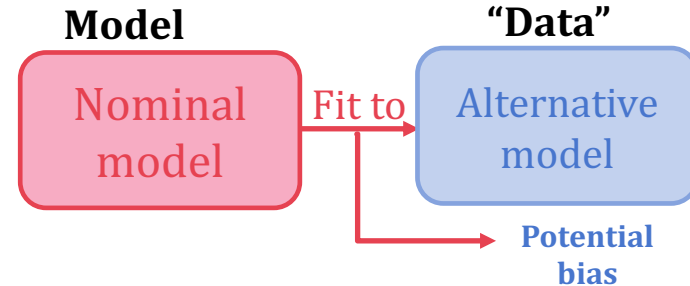
- unknown unknowns
- lack of theoretical guidance
- lack of tools/challenges in propagating some effects

We test the robustness of our analysis by assessing its performance against alternative models or tunes

Examples: (non-exhaustive, 16 total tests)

1. Alternative CCQE models (LFG, CRPA)
2. Varying the proportion of non-QE events
3. Alternative π -production models (e.g. Martini 1π)
4. Hard photon emission

Principle:

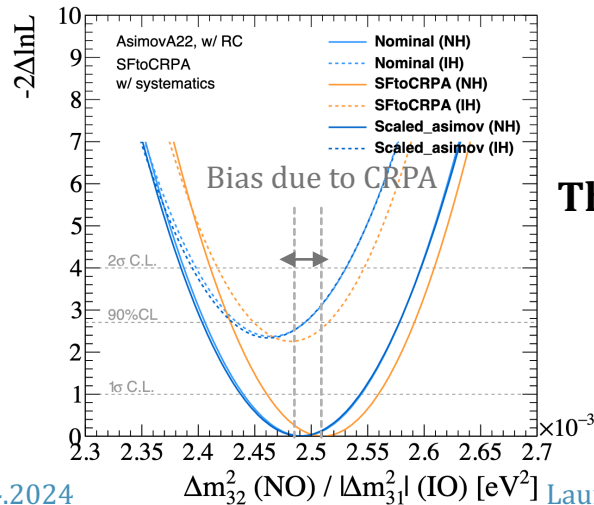


Robustness studies

- All robustness checks show deviations which are far below the *total* uncertainty on oscillation parameters

But notable cases where sizable deviations were seen:

1. **CRPA** alternative model shows a bias comparable to the size of the total systematic uncertainty on Δm_{32}^2
2. Attributing the data-MC discrepancy to **non-QE** events only shows a bias of $\sim 70\%$ of the systematic uncertainty on Δm_{32}^2



Accounted for by applying an additional smearing to Δm_{32}^2

This smearing is the dominant systematic uncertainty on Δm_{32}^2

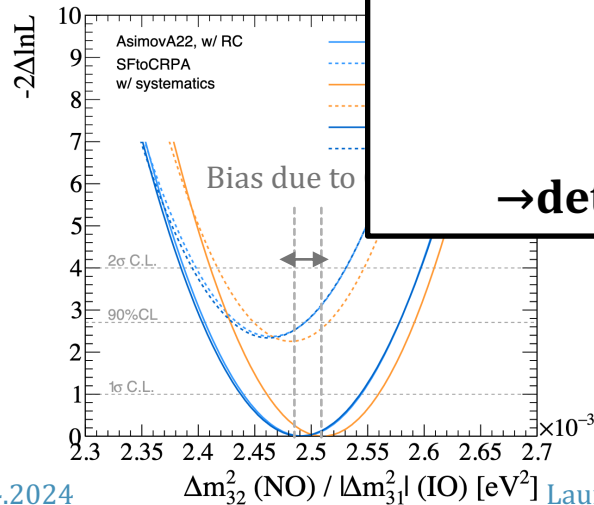
Highlights aspects of the model which need improvement

Robustness studies

- All robustness checks show deviations which are far below the *total* uncertainty on oscillation parameters

But notable cases where sizable deviations were seen:

1. CRPA alternative model
2. Attributing the data uncertainty on Δm_{32}^2



For a full description of

- full baseline model
- uncertainty model
- robustness studies
- near detector fit

→ detailed paper in preparation

atic uncertainty on Δm_{32}^2
0% of the systematic

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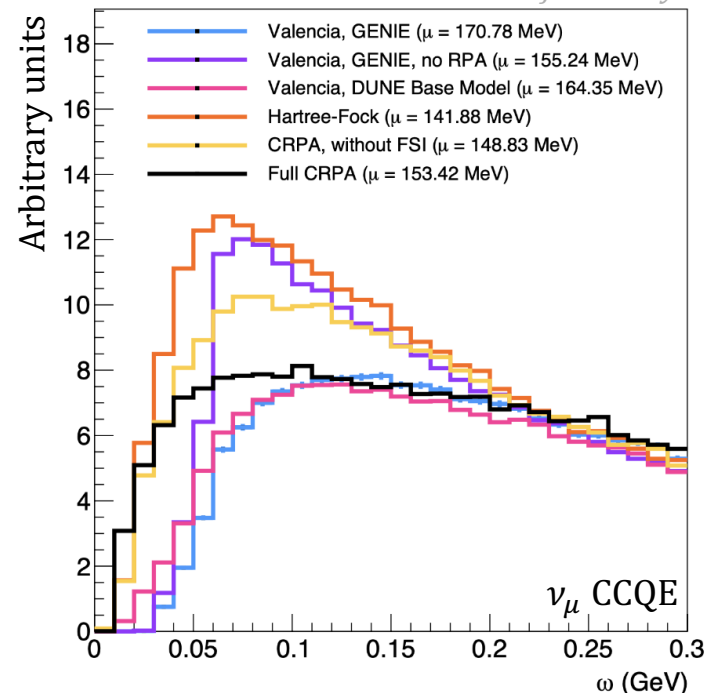
tic uncertainty on Δm_{32}^2

Highlights aspects of the model which need improvement

Lessons learned – towards the next analysis

- **Low- ω physics** (RPA, optical potential, Pauli blocking...) are the **dominant source of systematic uncertainty on atmos. parameters for T2K** (and T2K+SK atmospheric) oscillation analyses
 - Currently developing new freedoms to target these effects
- Lacking freedom in **nucleon kinematics**
 - Ok for now but unacceptable once we include hadron kinematics in the analysis
 - Next analysis will include freedom to control SRC pair fractions & cascade nucleon FSI
 - Ongoing work to even better describe nucleon FSI
- Emission of **radiative photons** now simulated in NEUT for next analysis

Work of T. Holvey



Additional future improvements

- Ongoing (very promising!) implementation of ED-RMF model in NEUT
 - Opens up the possibility of physically motivated uncertainties relatable to a **fully microscopic model**
- Addition of new freedoms for **hadron kinematics in 2p2h processes**
 - E.g. inclusion of MicroBooNE-inspired decay angle freedom for 2p2h events
- Wider phase space of **robustness studies**
 - 2p2h alternative models
 - Pion multiplicities
- ...and many more!

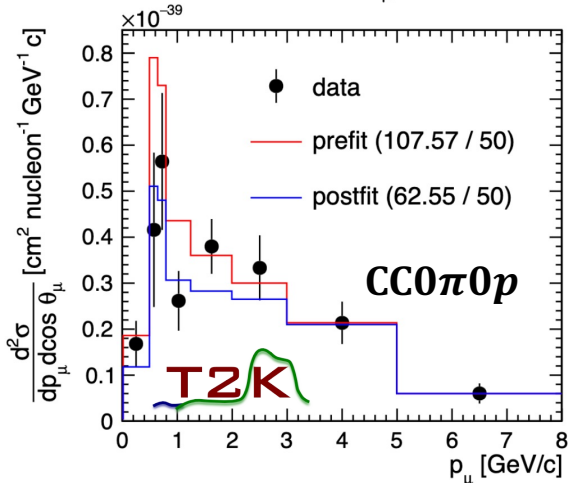
Benchmarking with cross-section measurements

The T2K uncertainty model has enough freedom to describe T2K inclusive and some semi-inclusive measurements

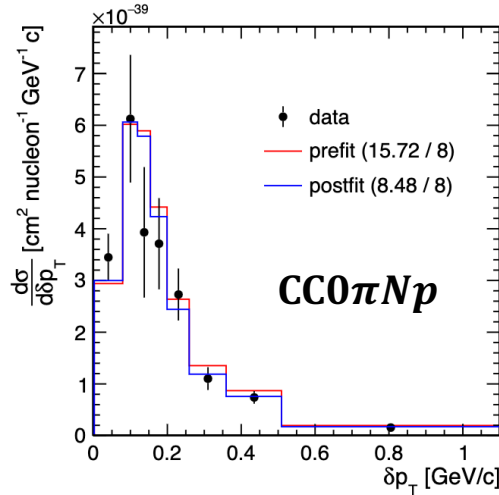
Fits performed using



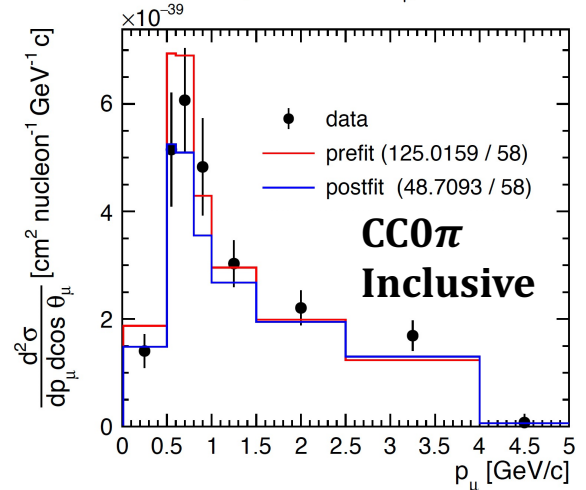
$0.98 < \cos \theta_\mu < 1.00$



Measurement from [Phys. Rev. D 98, 032003 \(2018\)](https://arxiv.org/abs/1803.03200)




C, $0.93 < \cos \theta_\mu < 1.00$



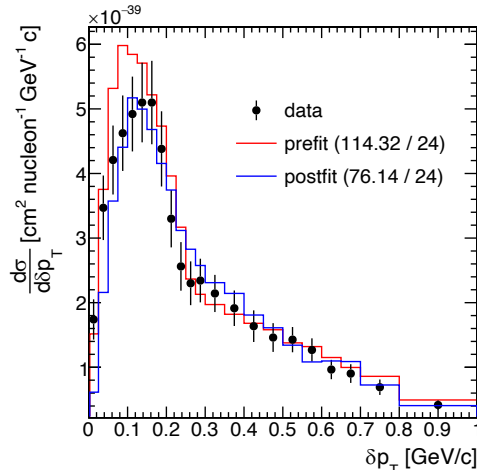
Measurement from [Phys. Rev. D 101, 112004 \(2020\)](https://arxiv.org/abs/2004.112004)

Benchmarking with cross-section measurements

The T2K uncertainty model has enough freedom to describe T2K inclusive and some semi-inclusive measurements

Fits performed using 

...improves agreement with MINERvA measurements but doesn't describe it quantitatively



Measurement from [Phys.Rev.Lett. 121 \(2018\) 2, 022504](https://doi.org/10.1103/PhysRevLett.121.022504)

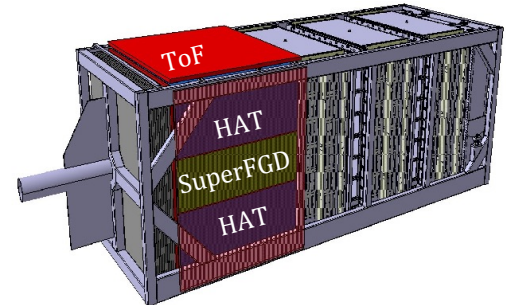
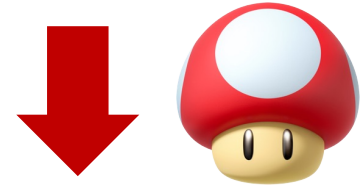
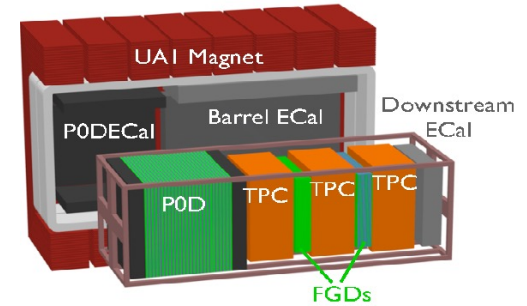
Possible lacking freedoms:

- Energy dependence
- Hadron kinematics
- Nucleon FSI
- Resonant pion production

Summary & prospects

- T2K has developed a sophisticated neutrino interaction uncertainty model for its oscillation analyses
- **~70 d.o.f. for relevant effects**
- Robustness of the model is assessed through dedicated studies
 - **Dominant source of systematic uncertainty on atmos. parameters** currently related to **beyond-PWIA effects**
 - Help identify shortcomings of the model which we are currently addressing
- Iterative work currently done in preparation for the first data with the new **Upgraded ND280**
 - Will open up a world of possibilities for new and robust measurements
 - Needs dedicated, new uncertainties **for including hadronic observables** in the oscillation analysis

See talk by U. Virginet



Summary & prospects

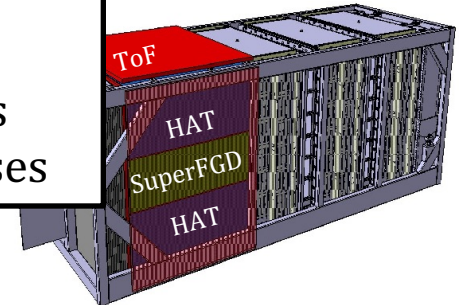
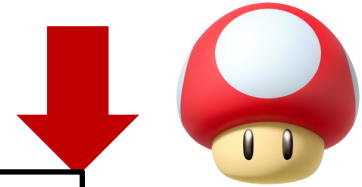
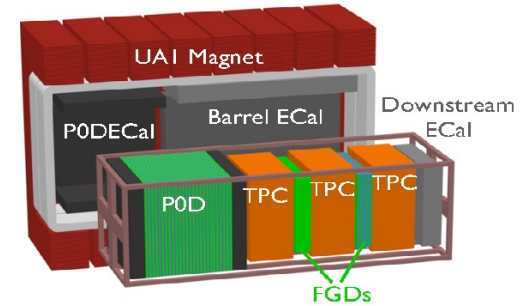
- T2K has developed a sophisticated neutrino interaction uncertainty model for its oscillation analyses
- **~70 d.o.f. for relevant effects**
- Robustness of the model is assessed through dedicated studies
 - Dependence of systematic uncertainty on atmos. parameters is strongly related to **beyond-PWIA effects**
 - Identification of shortcomings of the model which we are currently addressing
- Iterative analysis of data with improved models
 - Will open new measurement channels
 - Needs development of **observables** in the oscillation analysis

SOS

Key challenges:

- C/O correlations
- Nucleon kinematics in 2p2h interactions
- Nuclear effects in pion production processes

See talk by U. Virginet

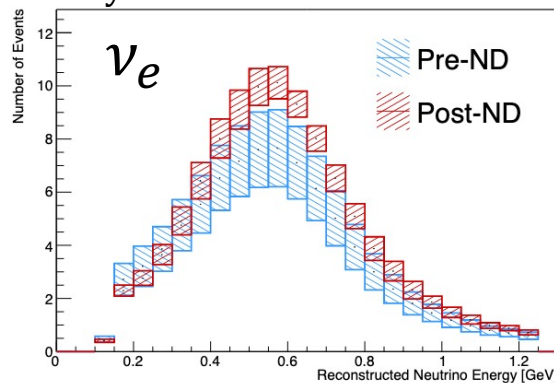
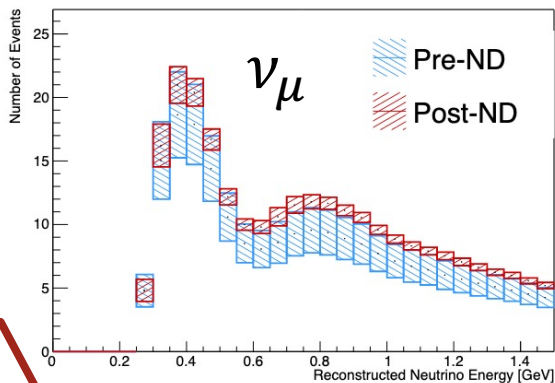




Supplementary material

Impact of ND constraint on FD spectra and errors

T2K preliminary



Systematic errors

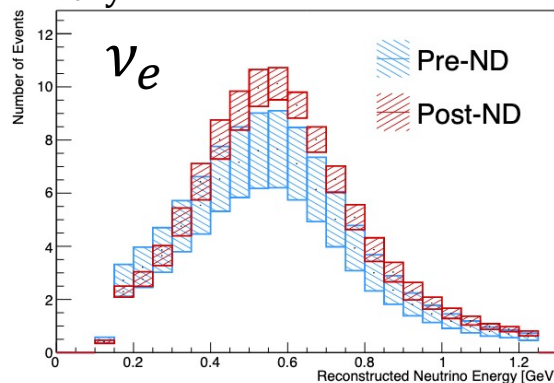
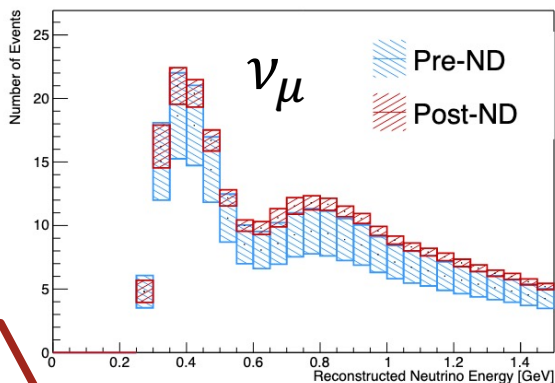
Before ND fit

Error source (units: %)	1R		MR		1Re				
	FHC	RHC	FHC	CC1 π^+	FHC	RHC	FHC	CC1 π^+	FHC/RHC
Flux	5.0	4.6	5.2		4.9	4.6	5.1		4.5
Cross-section (all)	15.8	13.6	10.6		16.3	13.1	14.7		10.5
SK+SI+PN	2.6	2.2	4.0		3.1	3.9	13.6		1.3
Total All	16.7	14.6	12.5		17.3	14.4	20.9		11.6

T2K Run 1-10, preliminary

Impact of ND constraint on FD spectra and errors

T2K preliminary



Systematic errors

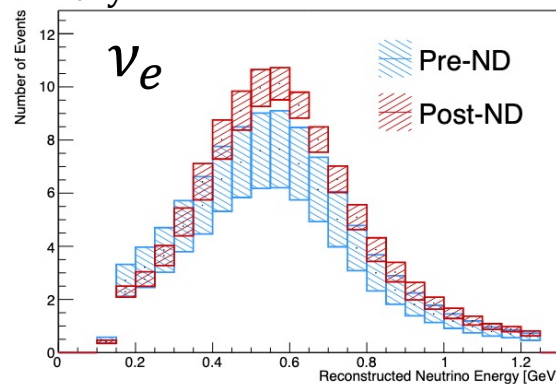
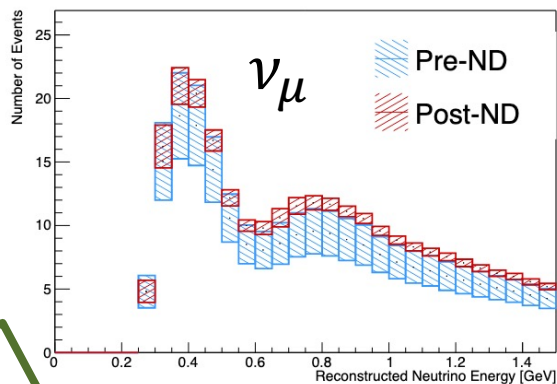
Before ND fit

Error source (units: %)	1R		MR		1Re			
	FHC	RHC	FHC	CC1 π^+	FHC	RHC	FHC	CC1 π^+ FHC/RHC
Flux	5.0	4.6	5.2		4.9	4.6	5.1	4.5
Cross-section (all)	15.8	13.6	10.6		16.3	13.1	14.7	10.5
SK+SI+PN	2.6	2.2	4.0		3.1	3.9	13.6	1.3
Total All	16.7	14.6	12.5		17.3	14.4	20.9	11.6

T2K Run 1-10, preliminary

Impact of ND constraint on FD spectra and errors

T2K preliminary



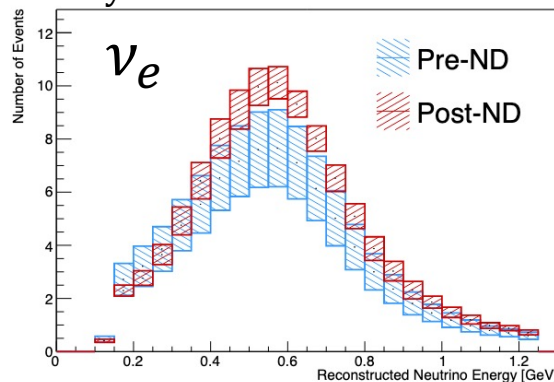
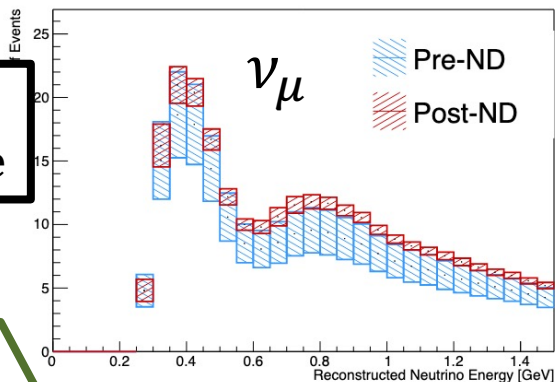
Systematic errors

After ND fit

Error source (units: %)	1R		MR		1Re			
	FHC	RHC	FHC	CC1 π^+	FHC	RHC	FHC/RHC	
Flux	2.8	2.9	2.8		2.8	3.0	2.8	2.2
Xsec (ND constr)	3.7	3.5	3.0		3.8	3.5	4.1	2.4
Flux+Xsec (ND constr)	2.7	2.6	2.2		2.8	2.7	3.4	2.3
Xsec (ND unconstr)	0.7	2.4	1.4		2.9	3.3	2.8	3.7
SK+SI+PN	2.0	1.7	4.1		3.1	3.8	13.6	1.2
Total All	3.4	3.9	4.9		5.2	5.8	14.3	4.5

Impact of ND constraint on FD spectra and errors

T2K preliminary



But also tuned spectrum shape

After ND fit

Systematic errors

Error source (units: %)	1R		MR		1Re			
	FHC	RHC	FHC	CC1π ⁺	FHC	RHC	FHC	CC1π ⁺ FHC/RHC
Flux	2.8	2.9	2.8		2.8	3.0	2.8	2.2
Xsec (ND constr)	3.7	3.5	3.0		3.8	3.5	4.1	2.4
Flux+Xsec (ND constr)	2.7	2.6	2.2		2.8	2.7	3.4	2.3
Xsec (ND unconstr)	0.7	2.4	1.4		2.9	3.3	2.8	3.7
SK+SI+PN	2.0	1.7	4.1		3.1	3.8	13.6	1.2
Total All	3.4	3.9	4.9		5.2	5.8	14.3	4.5