

The logo for MicroBooNE, featuring the text "μBooNE" in a bold, black, sans-serif font. The Greek letter mu is smaller than the other characters. A blue oval highlights the "BooNE" part of the text. A black arrow points to the right from the end of the oval.

# The Impact of Neutrino Interaction Uncertainties on MicroBooNE and SBN Physics Measurements

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On behalf of the MicroBooNE Collaboration

April 15th, 2024

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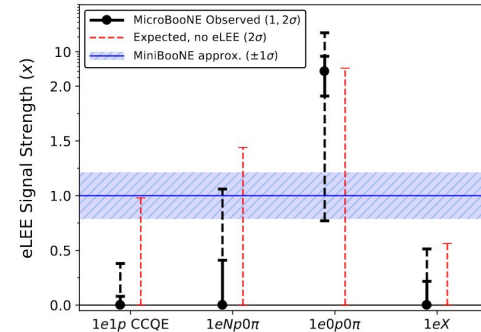


# It's an Exciting Time for Neutrino Physics

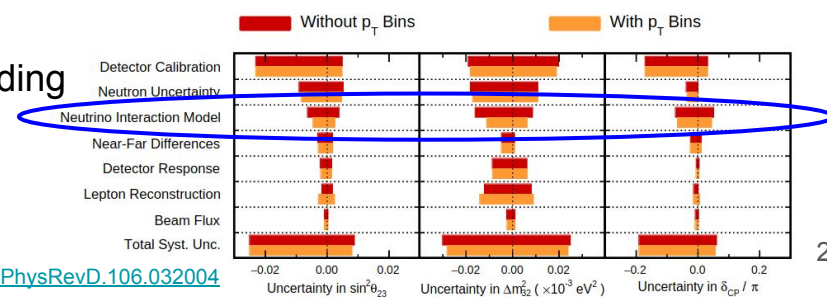
- MicroBooNE is a well established experiment with 65 published papers since 2017
  - Produced e-like and  $\gamma$ -like low energy excess searches
  - Cross section measurements on a diverse range of interactions and in multiple dimensions
- SBN is ramping up to provide a 2-detector oscillation search and even higher statistics
  - DUNE is on the horizon with even more precise requirements
  - Neutrino interaction modeling is a potential leading source of uncertainty



MicroBooNE eLEE Search



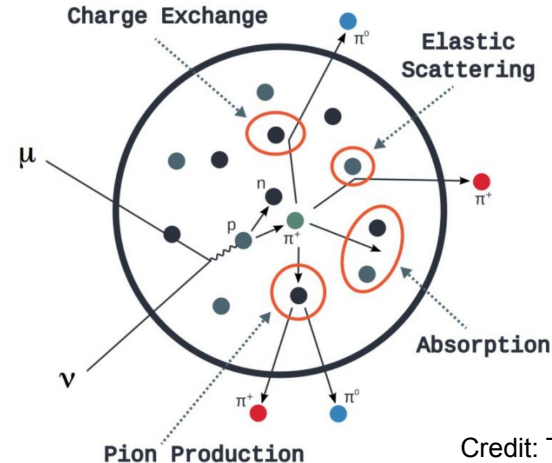
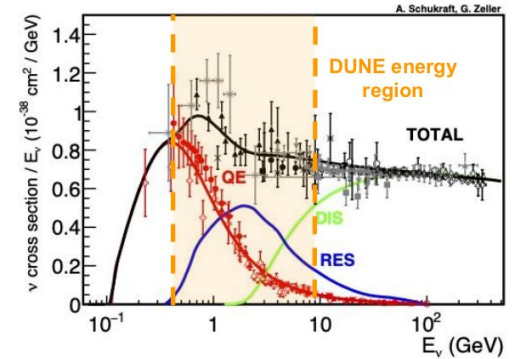
NOvA Uncertainties Breakdown



# Challenges in Neutrino Interaction Modeling

[RevModPhys.84.1307](#)

- Wide range of energies
  - Spans QE, RES, DIS
- Range of nuclear targets across experiments
  - Hydrogen, Deuterium, Carbon, Argon, Iron, Lead
- Complex QCD physics inside nucleus
  - Nuclear initial state
  - Nucleon-nucleon correlations
  - Final state interactions



Credit: T. Golan

# Cross Section Modeling with GENIE



| Parameter                                  | Central value          | 1 $\sigma$ | 1 $\sigma$ |
|--|------------------------|------------|------------|
| <i>CCQE event generator parameters</i>     |                        |            |            |
| CCQE_C0shape                               | Delta                  | Z equation | N/A        |
| NUCCQEshape                                | BR007                  |            | N/A        |
| NUCCQEshape                                | BR007                  |            | N/A        |
| MANTLE                                     | 0.00122 GeV            | -12%       | -12%       |
| DISFCTE                                    | 0.0                    | 1.0%       | -1.0%      |
| <i>RES Form factors and decays</i>         |                        |            |            |
| MCCHIS                                     | 1.00047 GeV            | -20%       | -20%       |
| MCCHIS                                     | 0.446 GeV              | -10%       | -10%       |
| MCCHIS                                     | 1.139 GeV              | -10%       | -10%       |
| MCCHIS                                     | 0.446 GeV              | -10%       | -10%       |
| RES01Lpenta                                | Normal                 | -10%       | -10%       |
| RES01Rta                                   | Normal                 | 10%        | 10%        |
| Tera_LAM2Ns                                | Normal                 | Interp     | N/A        |
| <i>gM1 interaction model</i>               |                        |            |            |
| gM1V1g                                     | -0.003                 | -20%       | -20%       |
| gM1V1p                                     | 16.923 GeV             | 1.0%       | 1.0%       |
| <i>Normalization of new RES decal mass</i> |                        |            |            |
| NeutrinoE1CC2p                             | 0.00713                | -10%       | -10%       |
| NeutrinoE1CC2p                             | 0.30999                | -10%       | -10%       |
| NeutrinoE1CC2p                             | 0.12708                | -10%       | -10%       |
| NeutrinoE1CC2p                             | 2.1252                 | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.12708                | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 2.1252                 | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.00713                | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.30999                | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| NeutrinoE1nonCC2p                          | 0.1                    | -10%       | -10%       |
| <i>Atomic energy correction functions</i>  |                        |            |            |
| AMBY                                       | 0.934 GeV <sup>2</sup> | -25%       | -25%       |
| RMRY                                       | 0.345 GeV <sup>2</sup> | -15%       | -15%       |
| CMRY                                       | 0.294 GeV <sup>2</sup> | -10%       | -10%       |
| CV24T                                      | 0.199 GeV <sup>2</sup> | -40%       | -40%       |
| <i>Photon interactions</i>                 |                        |            |            |
| MFP_p                                      | NA2018                 | -20%       | -20%       |
| MFP_n                                      | NA2018                 | -20%       | -20%       |
| FPAU_p                                     | NA2018                 | -40%       | -40%       |
| FPAU_n                                     | NA2018                 | -40%       | -40%       |
| FPPNU_p                                    | NA2018                 | -20%       | -20%       |
| FPPNU_n                                    | NA2018                 | -20%       | -20%       |
| FPAU_N                                     | NA2018                 | -40%       | -40%       |
| FPPNU_N                                    | NA2018                 | -20%       | -20%       |
| FPAU_N                                     | NA2018                 | -20%       | -20%       |

**Historical: RFG, Llewellyn Smith  
CCQE, Rein-Sehgal RES, hA FSI**

**LFG, Valencia CCQE, Berger-Sehgal  
improved RES modeling**

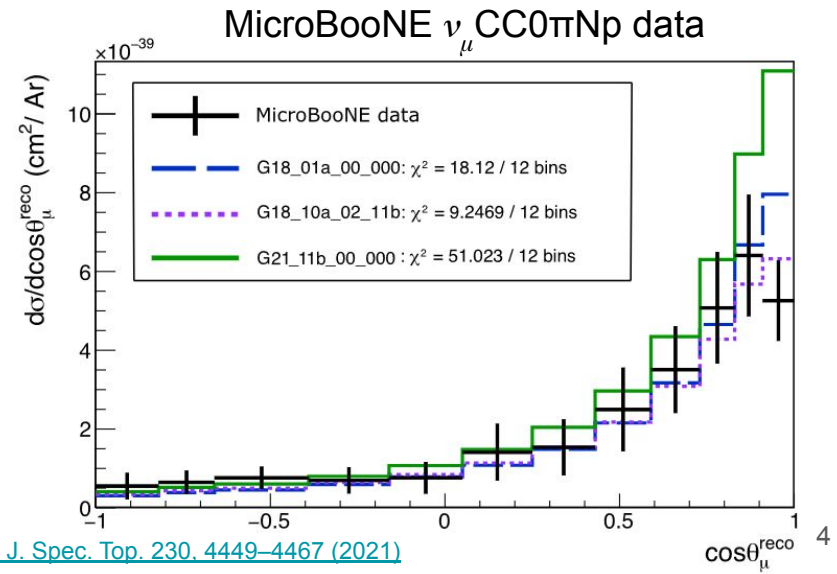
**SuSAv2 CCQE, hN FSI**

See Steven Gardiner's  
talk for new results!

- GENIE is the primary  $\nu$  interaction event generator for Fermilab experiments
  - Development is huge effort, tons of knobs
  - Lots of approx/estimates - room for improvement

- GENIE v3 is the latest major release
  - Genie v2 is also in use by other experiments
  - Many configurations possible within Genie v3. Details in [Eur. Phys. J. Spec. Top. 230, 4449–4467 \(2021\)](https://arxiv.org/abs/2105.04449)

- MicroBooNE uses GENIE v3.0.6 G18\_10a\_02\_11a
  - MicroBooNE tune discussed later
  - MicroBooNE was the first experiment to adopt GENIE v3

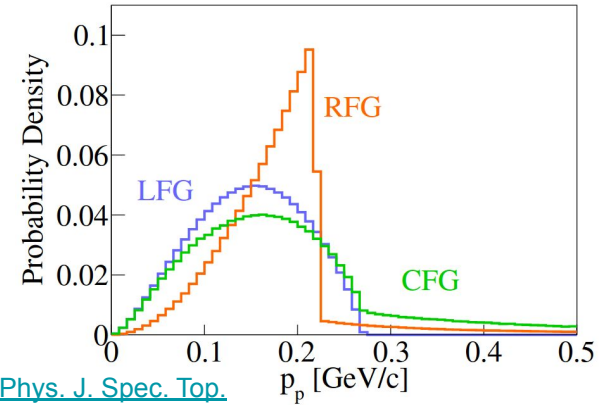


[Eur. Phys. J. Spec. Top. 230, 4449–4467 \(2021\)](https://arxiv.org/abs/2105.04449)

# Modeling the Nuclear Initial State

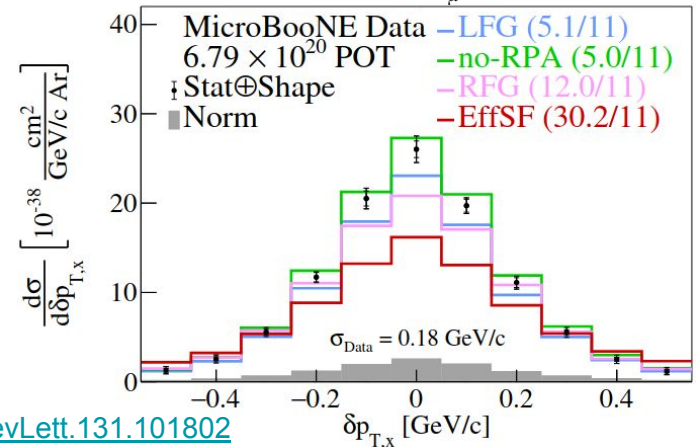
- Historical model: **Relativistic Fermi Gas (RFG)**
  - Non-interacting nucleons with momentum up to Fermi momentum  $k_F$
  - Non-zero momentum tail above  $k_F$  to account for short-range nucleon-nucleon correlations
- **Local Fermi Gas (LFG) model**
  - $k_F$  is a function of radius, derived from nucleon density distribution
  - Underpins Valencia CCQE and CCMEC modeling with shared use of density distribution
- **Correlated Fermi Gas (CFG) model**
  - Re-introduces non-zero momentum tail above  $k_F$
  - Included in GENIE 3.2

Nuclear Initial State Modeling In GENIE



[Eur. Phys. J. Spec. Top. 230, 4449–4467 \(2021\)](#)

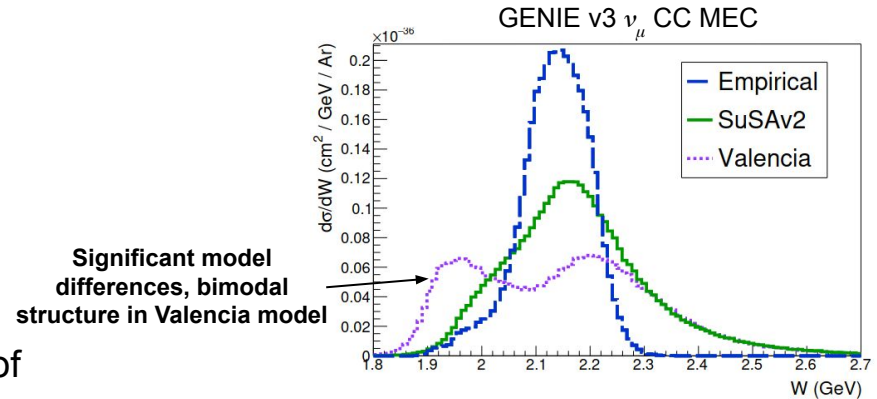
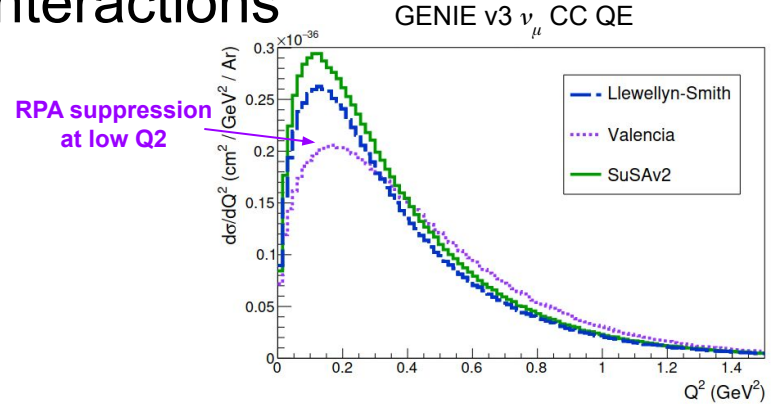
Impact of Initial State Modeling in  
MicroBooNE  $\nu_\mu$  CC  $1p0\pi$



[PhysRevLett.131.101802](#)

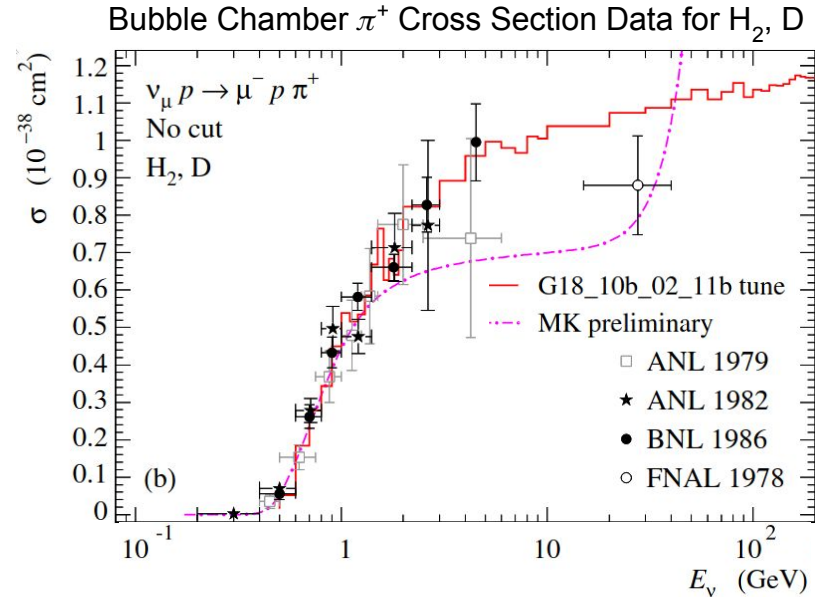
# Modeling of Charged Current Quasi-Elastic (CCQE) and Meson-Exchange Current (CCMEC) interactions

- Historical model: **Llewellyn-Smith**
  - Free nucleon model with corrections for Pauli blocking and binding energy
  - Accurate at higher energies ( $>2$  GeV)
- **Valencia** model for CCQE and CCMEC interactions
  - **RPA corrections** for long range correlations
  - Corrections for Coulomb interactions of outgoing lepton
- **SuperScaling Approach (SuSAv2)** model
  - RFG model predicts lepton cross section scales  $\sim \psi(q, \omega)$
  - SuSAv2 combines scaling in  $(e, e')$  data longitudinal channel with RMF prediction of significant transverse channel scaling



# Modeling of $\Delta$ -Resonance (RES) Interactions

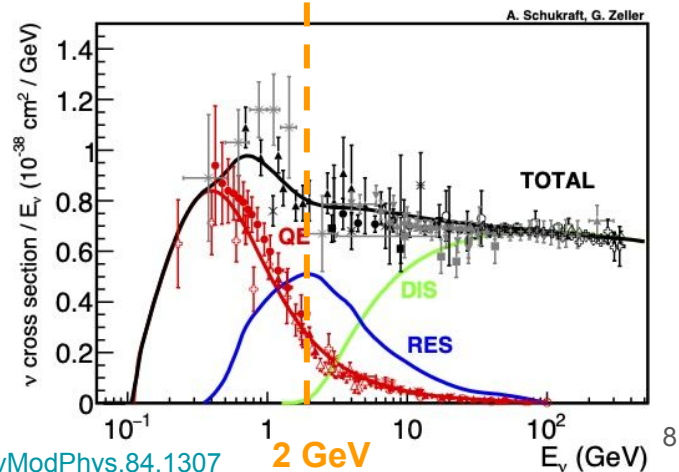
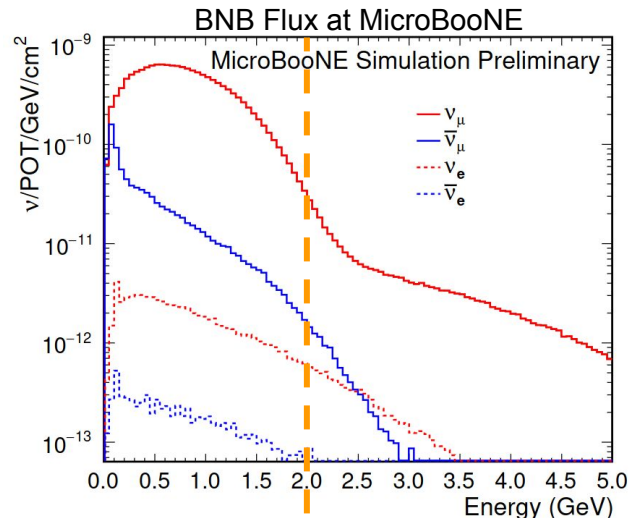
- Historical model: Rein-Sehgal
  - Dipole expansion of axial form factor with axial-vector mass  $M_A^{\text{RES}} = 1.12 \text{ GeV}$
- Berger-Sehgal model
  - Includes modeling improvements of nonzero lepton mass, lepton polarization, pion pole contribution
- To first-order, bubble chamber data gives good constraints
  - Small A means fewer FSI effects
  - Multi-dimensional phase space



[Eur. Phys. J. Spec. Top. 230, 4449–4467 \(2021\)](#)

# Modeling of Deep Inelastic Scattering (DIS) Interactions

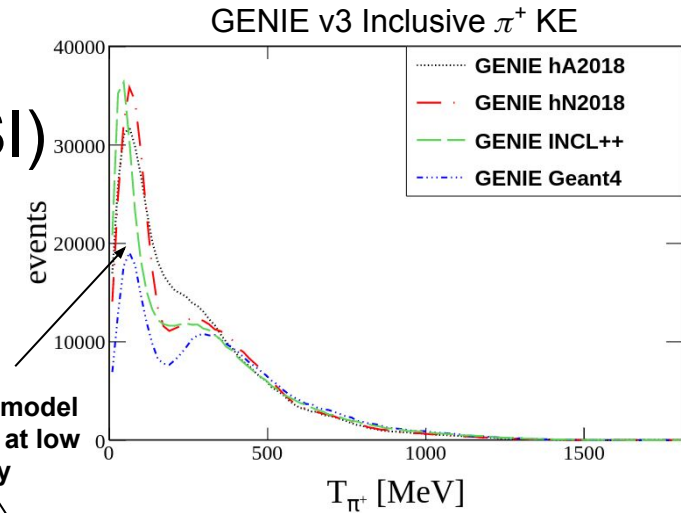
- Significant for DUNE, not as much MicroBooNE / SBN
- Bodek-Yang model for CCDIS interactions
- GENIE default has large uncertainties on non-RES  $\pi$  (50%) and DIS (25-40%) parameters





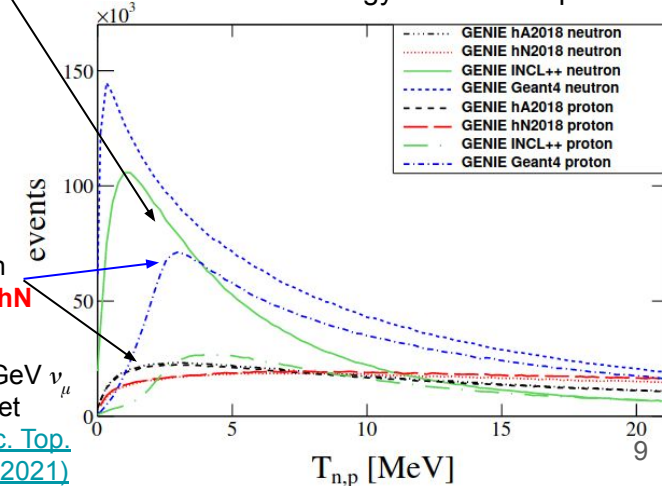
# Modeling of Final State Interactions (FSI)

- FSI models final state particles exiting nucleus
  - Processes include charge exchange, absorption, hadron knockout
  - More important for larger nuclei such as  $^{40}\text{Ar}$
- MicroBooNE FSI modeled with **hA** approximation
  - Approximates cascade of interactions with total cross sections
  - Data-driven, gives good agreement
- GENIE v3.0 also contains **hN intranuclear cascade** model
  - Models multiple interactions in nuclear cascade
  - Similar to implementations in NuWro and NEUT



Significant model differences at low energy

GENIE v3 Low-Energy Hadron Responses

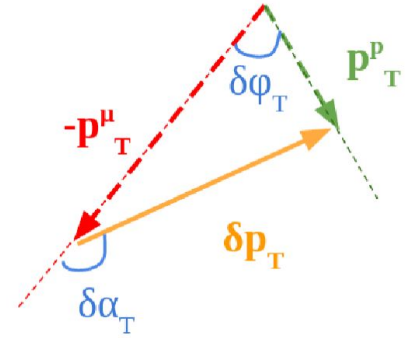


Proton suppression from Coulomb effects shown in **INCL**, **Geant4**, but not **hA**, **hN**

Predictions for 2 GeV  $\nu_\mu$  on argon target  
[Eur. Phys. J. Spec. Top. 230, 4449–4467 \(2021\)](#)

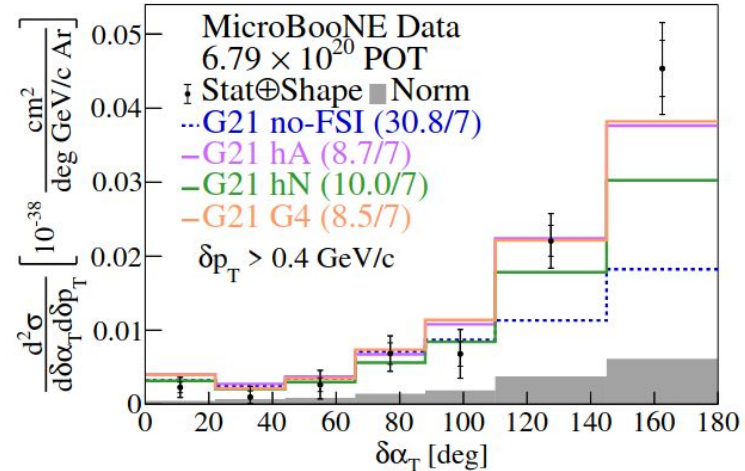
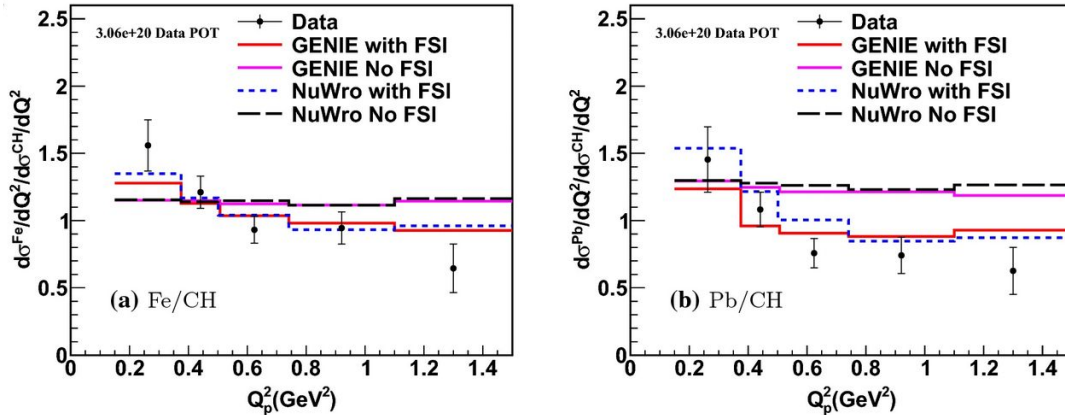
# Modeling of Final State Interactions (FSI)

- Impact of FSI is well demonstrated in published measurements
  - FSI sensitivity varies greatly with interaction channel and across phase space
  - Large impact at high  $\delta p_T$
  - FSI impact increases with nuclear size A



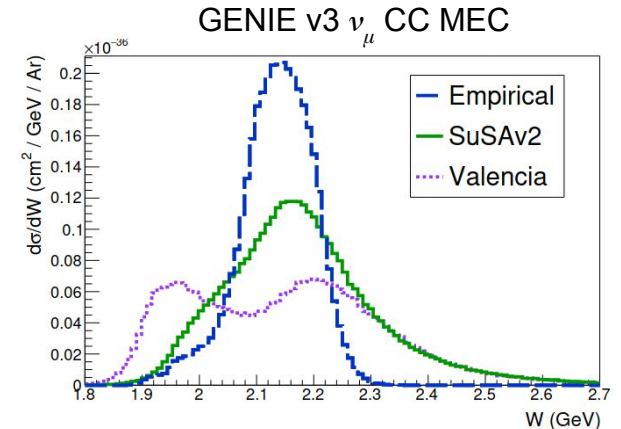
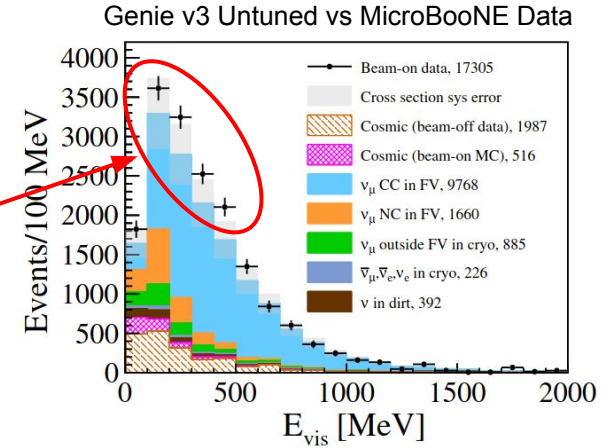
Impact of FSI in MicroBooNE  $\nu$  CC  $1p0\pi$   
[PhysRevLett.131.101802](https://arxiv.org/abs/1310.1802)

Impact of FSI in MINERvA ([Eur. Phys. J. Spec. Top. 230, 4243–4257](https://arxiv.org/abs/1306.4243))



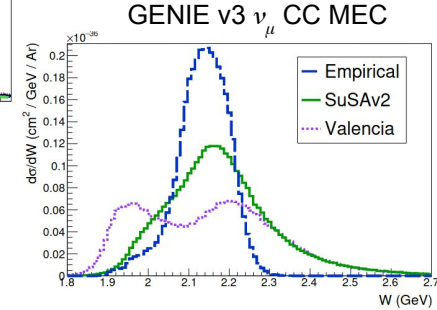
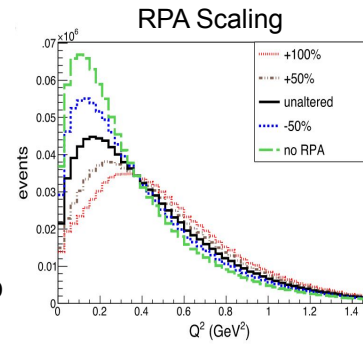
# MicroBooNE tune of GENIE v3

- Out-of-box GENIE v3.0.6 G18\_10a\_02\_11a under-predicted data
  - Particularly prevalent at low energy (<600 MeV)
- Tuned to T2K CC0 $\pi$  data (CH target)
  - Independent detector and beam
  - CCQE physics at a similar energy range
- Tuned 2 CCQE and 2 CCMEC parameters
  - Reflect known uncertainties in models of CC0 $\pi$  cross sections
  - Cannot easily be constrained by electron scattering data
  - Can be constrained by T2K data



# MicroBooNE tune of GENIE v3

- CCQE tuned parameters
  - CCQE  $M_A$  - low nominal value of  $\sim 0.96$  GeV contributes to underpredicting data
  - RPA strength - implemented by interpolating between Valencia model and no RPA correction
- CCMEC tuned parameters
  - CCMEC normalization - proportionally scales CCMEC contribution
  - CCMEC shape - implemented by interpolating between Valencia model and GENIE empirical model



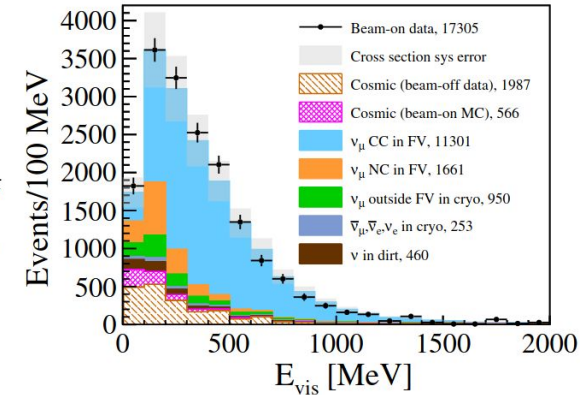
Fitted Parameters

|                | CCQE $M_A$                          | RPA Strength                     | CCMEC Norm                        | CCMEC Shape                                  |
|----------------|-------------------------------------|----------------------------------|-----------------------------------|--|
| <b>Nominal</b> | <b>0.961242 GeV</b>                 | <b>1</b>                         | <b>1</b>                          | <b>0 (Valencia)</b>                          |
| <b>Fitted</b>  | <b><math>1.1 \pm 0.1</math> GeV</b> | <b><math>0.85 \pm 0.4</math></b> | <b><math>1.66 \pm 0.50</math></b> | <b>1 (Empirical) <math>^{+0}_{-1}</math></b> |

All Non-Default Parameters

| Parameter             | Central value          | +1 $\sigma$              | -1 $\sigma$           |
|-----------------------|------------------------|--------------------------|-----------------------|
| MaCCQE <sup>a</sup>   | 1.10 GeV               | +0.1 GeV                 | -0.1 GeV              |
| RPA_CCQE <sup>b</sup> | 85%                    | +40%                     | -40%                  |
| Normccmec             | 166%                   | +50%                     | -50%                  |
| XSecShape_CCMEC       | Empirical <sup>c</sup> | N/A                      | Valencia <sup>d</sup> |
| Coulomb_CCQE          | Nominal                | +30%                     | -30%                  |
| DecayAngMEC           | Isotropic              | Alternative <sup>e</sup> | N/A                   |
| FracPN_CCMEC          | Valencia               | +20%                     | -20%                  |
| FracDelta_CCMEC       | Valencia               | +30%                     | -30%                  |
| NormNCMEC             | Nominal                | +100%                    | -100%                 |
| ThetaDelta2NRad       | Isotropic              | Alternative <sup>e</sup> | N/A                   |
| NormCCCOH             | Nominal                | +100%                    | -100%                 |
| NormNCCOH             | Nominal                | +100%                    | -100%                 |

Genie v3 Tuned vs MicroBooNE Data

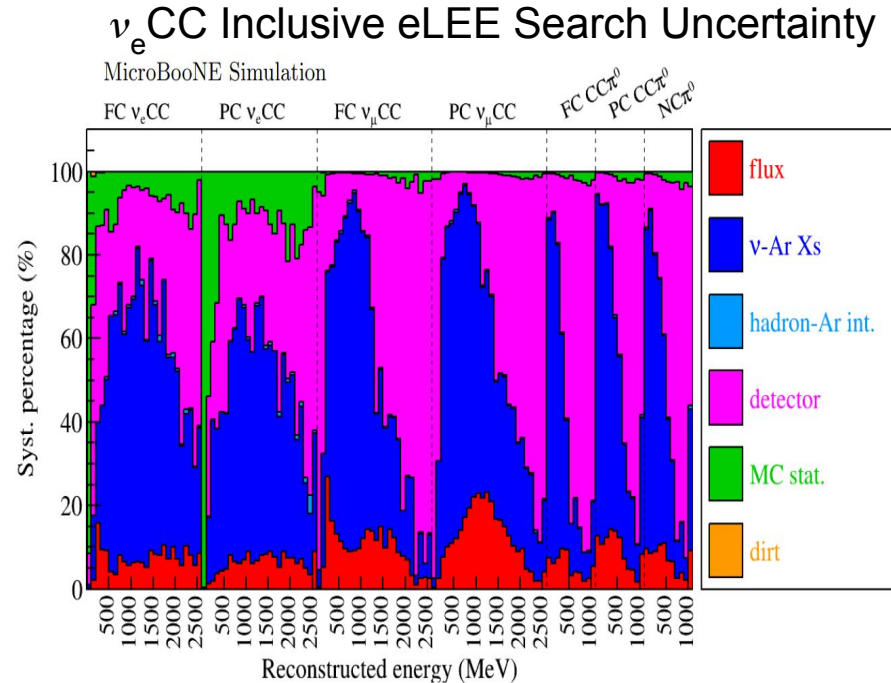


# Impact of Cross Section Uncertainties on Oscillation Measurements

- Inclusive signal
  - Not concerned with final state composition (eg: particle multiplicity, charge exchange)
- Requires  $E_\nu$  measurement
  - Transfer energy contains invisible portion in LArTPC (eg: neutrons)
  - Potential source of model dependence
- **Cross section uncertainties**

dominant at low  $E_\nu$  for both  $\nu_e$  and  $\nu_\mu$

  - MicroBooNE uses sideband constraints in place of 2-detector setup

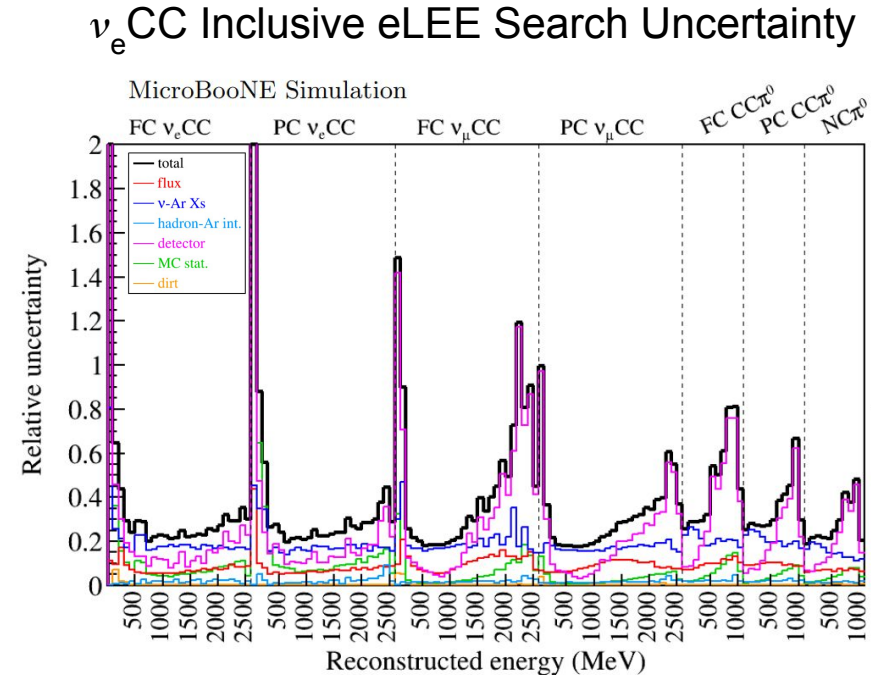


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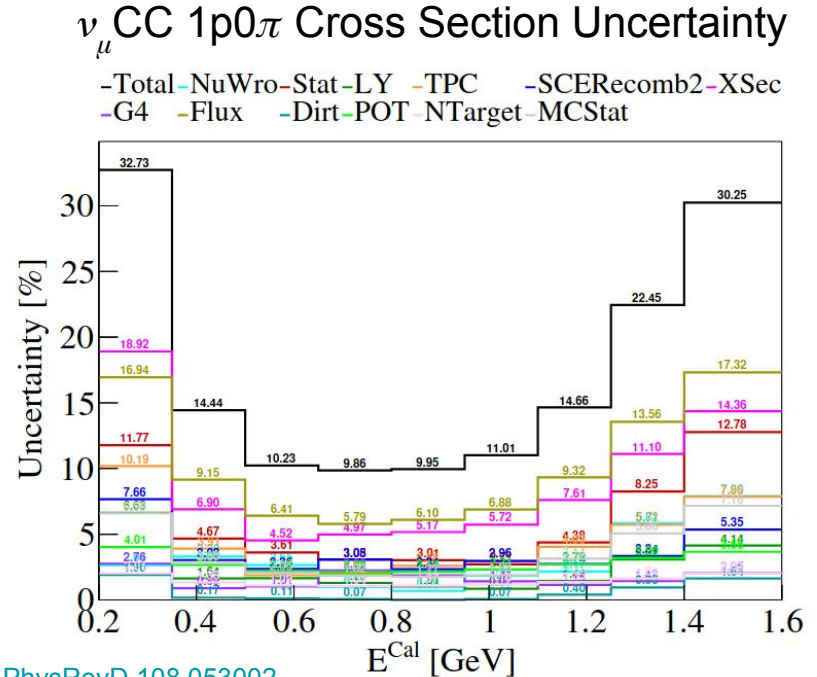
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# Impact of Cross Section Uncertainties on Cross Section Measurements

- Often exclusive signal
  - Backgrounds from interaction channels such as MEC
  - Impact varies between signal definitions
- Unfolding naturally suppresses **cross section uncertainties**
- Impact of **cross section uncertainties** depends on kinematic distribution
  - Sub-dominant across  $E_{\text{Cal}}$
  - Dominant at high  $\delta p_T$



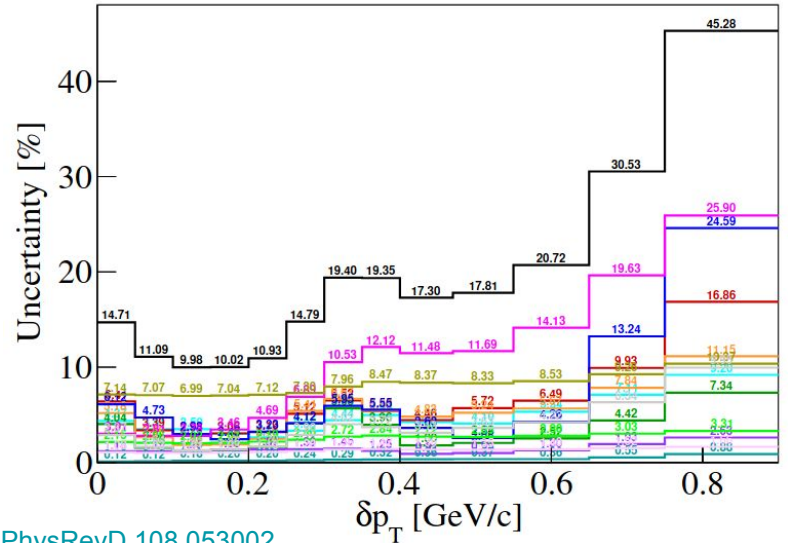
[PhysRevD.108.053002](#)  
[Supplemental Material](#)

# Impact of Cross Section Uncertainties on Cross Section Measurements

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$\nu_{\mu}$  CC  $1p0\pi$  Cross Section Uncertainty

-Total -NuWro -Stat -LY -TPC -SCERecomb2 -XSec  
 -G4 -Flux -Dirt -POT -NTarget -MCStat



[PhysRevD.108.053002](#)  
[Supplemental Material](#)



# Impact of Cross Section Parameter Uncertainties on $\nu$ CC $1p0\pi$ **1-Bin** Cross Section Measurement

[PhysRevD.108.053002](#)  
[Supplemental Material](#)

\*Largest uncertainties shown here;  
full list in backup slides

## CCQE Parameters

|              | $1\sigma$ Genie<br>Uncertainty | Fractional<br>Contribution<br>to Meas |
|--------------|--------------------------------|---------------------------------------|
| RPA Strength | 40 %                           | 2.1 %                                 |

## CCMEC Parameters

|                    | $1\sigma$ Genie<br>Uncertainty | Fractional<br>Contribution<br>to Meas |
|--------------------|--------------------------------|---------------------------------------|
| CCMEC Norm         | 50 %                           | 1.832 %                               |
| MEC Decay<br>Angle | Isotropic vs<br>$\cos^2\theta$ | 0.693 %                               |

## RES Parameters

|                                  | $1\sigma$ Genie<br>Uncertainty | Fractional<br>Contribution<br>to Meas |
|----------------------------------|--------------------------------|---------------------------------------|
| $M_A$ CCRES                      | 20%                            | 0.986 %                               |
| $M_V$ CCRES                      | 10%                            | 0.775 %                               |
| $M_A$ NCRES                      | 20%                            | 0.969 %                               |
| $\Delta \rightarrow N+\pi$ Angle | Rein-Sehgal<br>vs Isotropic    | 1.533 %                               |

## FSI Parameters

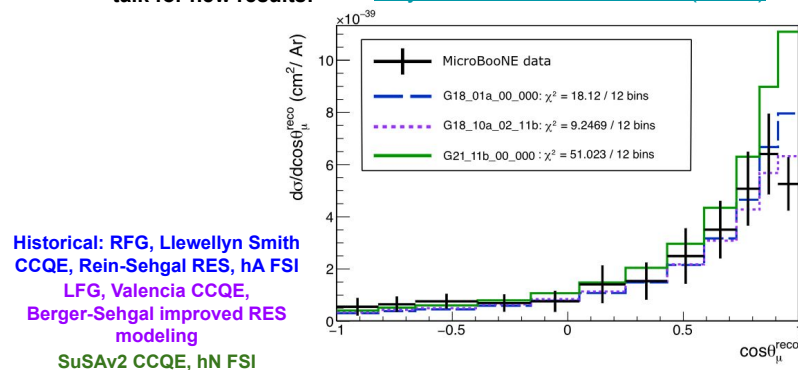
|                            | $1\sigma$ Genie<br>Uncertainty | Fractional<br>Contribution<br>to Meas |
|----------------------------|--------------------------------|---------------------------------------|
| Nucleon Mean<br>Free Path  | 20 %                           | 1.212 %                               |
| $\pi$ Absorption           | 30 %                           | 0.906 %                               |
| Nucleon Charge<br>Exchange | 20 %                           | 0.953 %                               |
| Nucleon<br>Absorption      | 40 %                           | 0.906 %                               |

# Summary

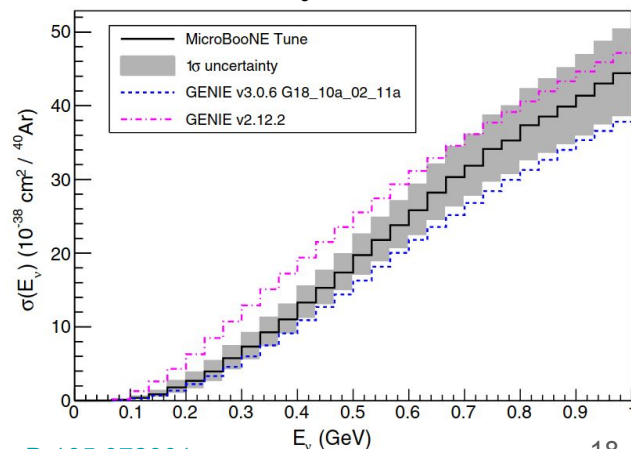
- Neutrino interaction modeling is important for precision oscillation measurements
  - Modeling is adequate for MicroBooNE, must do better for future experiments
- Many new model developments in recent years
  - Initial state models, CCQE models (SuSAv2, RPA correction), FSI models, ...
- Areas of significant model disagreement
  - RPA corrections, MEC contribution, FSI, ...
- Cross section measurements can continue to guide model development
  - Multi-dimensional phase spaces, high statistics, new detectors and unfolding methods, new kinematics being measured

See Steven Gardiner's talk for new results!

MicroBooNE  $\nu_\mu$  CC0 $\pi$ Np Data  
[Phys. Rev. D 102, 112013 \(2020\)](#)



MicroBooNE Tune  $\nu_e$  CC Inclusive Cross Section



[PhysRevD.105.072001](#)

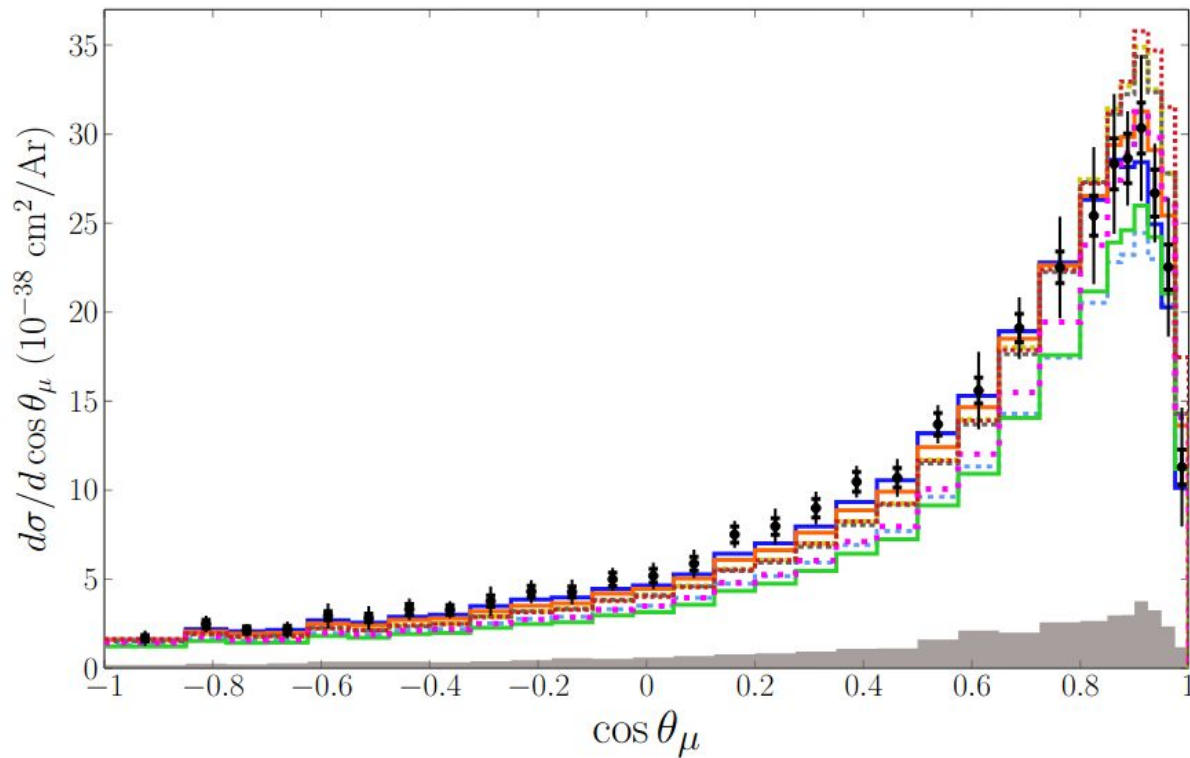
# Backup

TABLE IX. GENIE model parameters used with default settings in the “MicroBoONE tune.”

| Parameter                                    | Central value            | +1 $\sigma$ | -1 $\sigma$ |
|--|--------------------------|-------------|-------------|
| <i>CCQE form factor parametrization</i>      |                          |             |             |
| AxFCCQEshape                                 | Dipole                   | Z expansion | N/A         |
| VecFFCCQEshape                               | BBA07                    | Dipole      | N/A         |
| <i>NC elastic form factors</i>               |                          |             |             |
| MaNCEL                                       | 0.961242 GeV             | +25%        | -25%        |
| EtaNCEL                                      | 0.12                     | +30%        | -30%        |
| <i>RES form factors and decays</i>           |                          |             |             |
| MaCCRES                                      | 1.065047 GeV             | +20%        | -20%        |
| MvCCRES                                      | 0.840 GeV                | +10%        | -10%        |
| MaNCRES                                      | 1.120 GeV                | +20%        | -20%        |
| MvNCRES                                      | 0.840 GeV                | +10%        | -10%        |
| RDecBR1gamma                                 | Nominal                  | +50%        | -50%        |
| RDecBR1eta                                   | Nominal                  | +50%        | -50%        |
| Theta_Delta2Npi                              | Nominal                  | Isotropic   | N/A         |
| <i>AGKY hadronization model</i>              |                          |             |             |
| AGKYxF1pi                                    | -0.385                   | +20%        | -20%        |
| AGKYpT1pi                                    | 1/6.625 GeV <sup>2</sup> | +3%         | -3%         |
| <i>Normalization of non-RES final states</i> |                          |             |             |
| NonRESBGvpCC1pi                              | 0.007713                 | +50%        | -50%        |
| NonRESBGvpCC2pi                              | 0.787999                 | +50%        | -50%        |
| NonRESBGvnCC1pi                              | 0.127858                 | +50%        | -50%        |
| NonRESBGvnCC2pi                              | 2.11523                  | +50%        | -50%        |
| NonRESBGvbarpCC1pi                           | 0.127858                 | +50%        | -50%        |
| NonRESBGvbarpCC2pi                           | 2.11523                  | +50%        | -50%        |
| NonRESBGvbarnCC1pi                           | 0.007713                 | +50%        | -50%        |
| NonRESBGvbarnCC2pi                           | 0.787999                 | +50%        | -50%        |
| NonRESBGvpNC1pi                              | 0.1                      | +50%        | -50%        |
| NonRESBGvpNC2pi                              | 1                        | +50%        | -50%        |
| NonRESBGvnNC1pi                              | 0.3                      | +50%        | -50%        |
| NonRESBGvnNC2pi                              | 1                        | +50%        | -50%        |
| NonRESBGvbarpNC1pi                           | 0.3                      | +50%        | -50%        |
| NonRESBGvbarpNC2pi                           | 1                        | +50%        | -50%        |
| NonRESBGvbarnNC1pi                           | 0.1                      | +50%        | -50%        |
| NonRESBGvbarnNC2pi                           | 1                        | +50%        | -50%        |
| <i>Bodek-Yang structure functions</i>        |                          |             |             |
| AhtBY  | 0.538 GeV <sup>2</sup>   | +25%        | -25%        |
| BhtBY  | 0.305 GeV <sup>2</sup>   | +25%        | -25%        |
| CV1uBY                                       | 0.291 GeV <sup>2</sup>   | +30%        | -30%        |
| CV2uBY                                       | 0.189 GeV <sup>2</sup>   | +40%        | -40%        |
| <i>Final-state interactions</i>              |                          |             |             |
| MFP_pi                                       | hA2018                   | +20%        | -20%        |
| MFP_N  | hA2018                   | +20%        | -20%        |
| FrCEx_pi                                     | hA2018                   | +50%        | -50%        |
| FrInel_pi                                    | hA2018                   | +40%        | -40%        |
| FrAbs_pi                                     | hA2018                   | +30%        | -30%        |
| FrPiProd_pi                                  | hA2018                   | +20%        | -20%        |
| FrCEx_N                                      | hA2018                   | +50%        | -50%        |
| FrInel_N                                     | hA2018                   | +40%        | -40%        |
| FrAbs_N                                      | hA2018                   | +20%        | -20%        |
| FrPiProd_N                                   | hA2018                   | +20%        | -20%        |

| Parameter                       | Description  | CV           | $1\sigma$ Uncertainty            | Contributing Uncertainty (%) Total (Sig/Bkg) |
|---------------------------------|--|--------------|----------------------------------|--|
| <b>Quasi-Elastic Parameters</b> |  |              |                                  |  |
| MaCCQE                          | CCQE axial mass  | 1.10 GeV     | $\pm 0.1$ GeV                    | 0.038 (0.256, 0.218)                         |
| RPA CCQE                        | Strength of the RPA correction   | 0.151        | $\pm 0.4$                        | 2.094 (1.989, 0.104)                         |
| MaNCEL                          | Axial mass for NCEL  | 0.961242 GeV | $\pm 25\%$                       | 0.348 (0.010, 0.348)                         |
| EtaNCEL                         | Empirical parameter used to account for sea quark contribution to NCEL form factor   | 0.12         | $\pm 30\%$                       | 0.010 (0.010, 0.010)                         |
| AxFFCCQEshape                   | Parametrisation of the nucleon axial form factor                                     | Dipole       | z-expansion                      | 0.022 (0.016, 0.031)                         |
| VecFFCCQEshape                  | Parametrisation of the nucleon vector form factors                                   | BBA07        | Dipole                           | 0.051 (0.186, 0.137)                         |
| <b>MEC Parameters</b>           |  |              |                                  |  |
| NormCCMEC                       | Energy-independent normalization for CCMEC   | 1.66         | $\pm 0.5$                        | 1.832 (0.514, 1.319)                         |
| NormNCMEC                       | Energy-independent normalization for NCMEC   | 1            | $\pm 20\%$                       | 0.129 (0.010, 0.129)                         |
| FracPNCCMEC                     | Fraction of initial nucleon pairs that are pn (0 = Valencia)                         | 0            | $\pm 20\%$                       | 0.041 (0.333, 0.293)                         |
| FracDeltaCCMEC                  | Relative contribution of $\Delta$ diagrams to total MEC cross section (0 = Valencia) | 0            | $\pm 30\%$                       | 0.124 (0.124, 0.158)                         |
| XSecShape CCMEC                 | Changes shape of differential cross section  | 1.0          | 0.0                              | 2.273 (1.762, 0.511)                         |
| DecayAngMEC                     | Changes angular distribution of nucleon cluster                                      | Isotropic    | $\cos^2 \vartheta$ in rest frame | 0.693 (0.290, 0.404)                         |
| <b>Resonant Parameters</b>      |  |              |                                  |  |
| MaCCRES                         | CCRES axial mass   | 1.120 GeV    | $\pm 0.2$                        | 0.986 (0.119, 1.103)                         |
| MvCCRES                         | Shape-only CCRES axial mass  | 0.840 GeV    | $\pm 0.1$                        | 0.775 (0.121, 0.896)                         |
| MaNCRES                         | NCRES axial mass   | 1.120 GeV    | $\pm 0.2$                        | 0.969 (0.010, 0.969)                         |
| MvNCRES                         | NCRES vector mass.   | 0.840 GeV    | $\pm 0.1$                        | 0.395 (0.010, 0.395)                         |
| ThetaDelta2Npi                  | Interpolates angular distribution for $\Delta \rightarrow N + \pi$                   | Rein-Sehgal  | Isotropic                        | 1.533 (0.142, 1.392)                         |
| ThetaDelta2NRad                 | Interpolates angular distribution for $\Delta \rightarrow N + \gamma$                | Rein-Sehgal  | $\cos^2 \vartheta$               | 0.016 (0.016, 0.016)                         |

| Parameter                                 | Description   | CV         | $1\sigma$ Uncertainty | Contributing Uncertainty (%) Total (Sig/Bkg) |
|---|---|------------|-----------------------|--|
| <b>Non-Resonant Parameters</b>            |   |            |                       |  |
| NonRESBGvpNC1pi                           | Non-resonant background normalization for vp NC1 $\pi$                      | 0.1        | $\pm 0.5$             | 0.041 (0.010, 0.041)                         |
| NonRESBGvpNC2pi                           | Non-resonant background normalization for vp NC2 $\pi$                      | 1          | $\pm 0.5$             | 0.096 (0.010, 0.096)                         |
| NonRESBGvnNC1pi                           | Non-resonant background normalization for vn NC1 $\pi$                      | 0.3        | $\pm 0.5$             | 0.390 (0.010, 0.390)                         |
| NonRESBGvnNC2pi                           | Non-resonant background normalization for vn NC2 $\pi$                      | 1          | $\pm 0.5$             | 0.022 (0.010, 0.022)                         |
| NonRESBGvbarpNC1pi                        | Non-resonant background normalization for vp NC1 $\pi$                      | 0.3        | $\pm 0.5$             | 0.010 (0.010, 0.010)                         |
| NonRESBGvbarpNC2pi                        | Non-resonant background normalization for vp NC2 $\pi$                      | 1          | $\pm 0.5$             | 0.010 (0.010, 0.010)                         |
| NonRESBGvbarvNC1pi                        | Non-resonant background normalization for vn NC1 $\pi$                      | 0.1        | $\pm 0.5$             | 0.010 (0.010, 0.010)                         |
| NonRESBGvbarvNC2pi                        | Non-resonant background normalization for vn NC2 $\pi$                      | 1          | $\pm 0.5$             | 0.010 (0.010, 0.010)                         |
| NonRESBGvpCC1pi                           | Non-resonant background normalization for vp CC1 $\pi$                      | 0.007713   | $\pm 0.5$             | 0.014 (0.010, 0.019)                         |
| NonRESBGvpCC2pi                           | Non-resonant background normalization for vp CC2 $\pi$                      | 0.787999   | $\pm 0.5$             | 0.059 (0.010, 0.063)                         |
| NonRESBGvnCC1pi                           | Non-resonant background normalization for vn CC1 $\pi$                      | 0.127858   | $\pm 0.5$             | 0.217 (0.034, 0.250)                         |
| NonRESBGvnCC2pi                           | Non-resonant background normalization for vn CC2 $\pi$                      | 2.11523    | $\pm 0.5$             | 0.079 (0.010, 0.077)                         |
| NonRESBGvbarpCC1pi                        | Non-resonant background normalization for vp CC1 $\pi$                      | 0.127858   | $\pm 0.5$             | 0.013 (0.010, 0.013)                         |
| NonRESBGvbarpCC2pi                        | Non-resonant background normalization for vp CC2 $\pi$                      | 2.11523    | $\pm 0.5$             | 0.010 (0.010, 0.010)                         |
| NonRESBGvbarvCC1pi                        | Non-resonant background normalization for vn CC1 $\pi$                      | 0.007713   | $\pm 0.5$             | 0.010 (0.010, 0.010)                         |
| NonRESBGvbarvCC2pi                        | Non-resonant background normalization for vn CC2 $\pi$                      | 0.787999   | $\pm 0.5$             | 0.010 (0.010, 0.010)                         |
| AhtBY                                     | AHT higher-twist parameter in the Bodek-Yang model scaling variable $\xi_w$ | 0.538      | $\pm 0.25$            | 0.010 (0.010, 0.010)                         |
| BhtBY                                     | BHT higher-twist parameter in the Bodek-Yang model scaling variable $\xi_w$ | 0.305      | $\pm 0.25$            | 0.010 (0.010, 0.010)                         |
| CV1uBY                                    | CV1u valence GRV'98 PDF correction parameter in the Bodek-Yang model        | 0.291      | $\pm 0.3$             | 0.010 (0.010, 0.010)                         |
| CV2uBY                                    | CV2u valence GRV'98 PDF correction parameter in the Bodek-Yang model        | 0.189      | $\pm 0.4$             | 0.010 (0.010, 0.010)                         |
| <b>Hadronisation Parameters</b>           |   |            |                       |  |
| AGKYxF1pi                                 | Hadronization parameter, applicable to true DIS interactions only           | -0.385     | $\pm 0.2$             | 0.108 (0.013, 0.120)                         |
| AGKYpT1pi                                 | Hadronization parameter, applicable to true DIS interactions only           | 1/6.625    | $\pm 0.03$            | 0.034 (0.014, 0.046)                         |
| <b>Final State Interaction Parameters</b> |   |            |                       |  |
| MFP $_{\pi}$                              | $\pi$ mean free path  | 0          | $\pm 0.2$             | 0.032 (0.010, 0.028)                         |
| MFP $_N$                                  | Nucleon mean free path  | 0          | $\pm 0.2$             | 1.212 (1.067, 0.147)                         |
| FrCE $_{\pi}$                             | Fractional cross section for $\pi$ charge exchange                          | 0          | $\pm 0.5$             | 0.159 (0.025, 0.184)                         |
| FrInel $_{\pi}$                           | Fractional cross section for $\pi$ inelastic scattering                     | 0          | $\pm 0.4$             | 0.133 (0.042, 0.091)                         |
| FrAbs $_{\pi}$                            | Fractional cross section for $\pi$ absorption                               | 0          | $\pm 0.3$             | 0.906 (0.066, 0.019)                         |
| FrCE $_{N}$                               | Fractional cross section for nucleon charge exchange                        | 0          | $\pm 0.2$             | 0.953 (0.411, 0.542)                         |
| FrInel $_N$                               | Fractional cross section for nucleon inelastic scattering                   | 0          | $\pm 0.5$             | 0.289 (0.228, 0.061)                         |
| FrAbs $_N$                                | Fractional cross section for nucleon absorption                             | 0          | $\pm 0.4$             | 0.906 (0.526, 0.380)                         |
| <b>Delta Resonant Decay Parameters</b>    |   |            |                       |  |
| RDecBR1gamma                              | Normalization for $\Delta \rightarrow \gamma$ decays                        | Nominal BR | $\pm 0.5$             | 0.042 (0.017, 0.025)                         |
| RDecBR1eta                                | Normalization for $\Delta \rightarrow \eta$ decays                          | Nominal BR | $\pm 0.5$             | 0.513 (0.198, 0.324)                         |
| <b>Coherent Parameters</b>                |   |            |                       |  |
| NormCCCOH                                 | Scaling factor for CCCOH $\pi$ production total cross section               | Nominal    | 100% increase         | 0.027 (0.016, 0.027)                         |
| NormNCCOH                                 | Scaling factor for NCCOH $\pi$ production total cross section               | Nominal    | 100% increase         | 0.016 (0.016, 0.016)                         |



**MicroBooNE  $6.79 \times 10^{20}$  POT**

|                       |           |
|-----------------------|-----------|
| ◆ BNB data            | Norm unc. |
| ■ GENIE 2.12.10       | 27.4/30   |
| ■ GENIE 3.0.6         | 20.4/30   |
| ■ GiBUU 2021.1        | 7.35/30   |
| ■ NEUT 5.6.0          | 11.4/30   |
| ■ NuWro 19.02.2       | 30.5/30   |
| ■ MicroBooNE Tune     | 28.7/30   |
| ■ GENIE 3.2.0 G18_02a | 32.2/30   |
| ■ GENIE 3.2.0 G21_11b | 32.8/30   |

