

# Determination of the Argon Spectral Functions at JLab

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NuInt 2024

14th International Workshop on Neutrino-Nucleus Interactions  
Principia Institute, São Paulo, Brazil

April 15-20, 2024

# OUTLINE

## ★ The nuclear spectral function

- ▶ Definition and physical interpretation
- ▶ Experimental determination from the  $(e, e'p)$  cross section
  - Plane Wave Impulse Approximation (PWIA)
  - Factorisation of the nuclear cross sections
  - Corrections: Final State Interactions and processes involving two-nucleon currents (MEC)

## ★ The E12-14-012 Experiment at Jefferson Lab

- ▶ Measurements of the  ${}^{40}_{18}\text{Ar}(e, e'p)$  and  ${}^{48}_{22}\text{Ti}(e, e'p)$  cross sections
- ▶ Data analysis

## ★ Applications

## ★ Outlook

# THE NUCLEAR SPECTRAL FUNCTION

- ★ fundamental quantity describing single-particle dynamics in interacting many-particle systems
- ★ trivially related to the two-point Green's function through

$$P(\mathbf{k}, E) = -\frac{1}{\pi} \text{Im} G(\mathbf{k}, E)$$

implying

$$P(\mathbf{k}, E) = \sum_n |\langle (A-1)_n | a_{\mathbf{k}} | A_0 \rangle|^2 \delta(E + E_n - E_0)$$

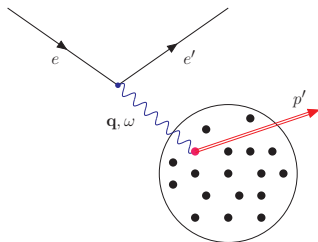
- ★ describes the probability of removing a nucleon of momentum  $\mathbf{k}$  from the nuclear ground state leaving the residual system with excitation energy  $E = E_0 - E_{\text{thr}}$ ,  $E_{\text{thr}}$  being the nucleon emission threshold

## THE $(e, e'p)$ REACTION

- ▶ Consider the process  $e + A \rightarrow e' + p + (A - 1)$  in which both the outgoing electron and the proton, carrying momentum  $p'$ , are detected in coincidence, and the recoiling nucleus can be left in either a bound or a continuum state

Define missing momentum  
and missing energy

$$\begin{aligned}\mathbf{p}_m &= \mathbf{p}' - \mathbf{q} \\ E_m &= \omega - T_{p'} - T_{A-1} \\ &\approx \omega - T_{p'}\end{aligned}$$



- ▶ Within the Plane Wave Impulse Approximation (PWIA), which amounts to assuming that Final State Interactions (FSI) be negligible, the *measured*  $\mathbf{p}_m$  and  $E_m$  can be identified with the initial energy and momentum of the knocked-out nucleon, the distribution of which is described by the target spectral function



## FACTORISATION OF THE $(e, e'p)$ CROSS SECTION

- ★ under the assumptions
  - ▶  $J_A^\mu(q) \approx \sum_i j_i^\mu(q)$  (single nucleon coupling)
  - ▶  $|X\rangle \approx |(A-1)_n, \mathbf{p}_n\rangle \otimes |\mathbf{p}'\rangle$   $\langle(A-1)_n, \mathbf{p}'| \approx \langle(A-1)_n| \otimes \langle\mathbf{p}'|$   
(factorization of the final state)

expected to be valid at large momentum transfer, the nuclear transition amplitude reduces the simple form

$$\langle(A-1)_n, \mathbf{p}'|J_A^\mu|0\rangle \rightarrow \sum_i M_n(\mathbf{k})\langle\mathbf{p}'|j_i^\mu|\mathbf{k}\rangle$$

- ★ The nuclear amplitude  $M_n$  is independent of momentum transfer, and can be accurately calculated using many-body theory and a state-of-the-art model of the nuclear Hamiltonian
- ★ The matrix element of the current between free-nucleon states can be computed using the fully relativistic expression. Constrained by proton and deuteron data
- ★ The resulting  $(e, e'p)$  cross section takes the simple and transparent form

$$\frac{d\sigma_A}{dE_{e'}d\Omega_{e'}dE_p d\Omega_p} \propto \sigma_{ep}P(p_m, E_m)$$

# COMMENTS OF FACTORISATION AND THE SPECTRAL FUNCTION

- ★ The  $y$ -scaling analysis of inclusive data provides clear cut and model independent evidence of factorisation of the  $eA$  cross section
- ★ The spectral function is an intrinsic property of the target, independent of both the nature of the beam particle and the kinematics of the scattering process
- ★ To the extent to which FSI and interactions involving two-nucleon currents can be treated as corrections, the spectral function formalism can be used to describe any

$$e + A \rightarrow e' + X \quad , \quad \nu_\ell + A \rightarrow \ell + X$$

processes, provided a reliable description of the elementary cross sections  $\sigma_{eN}$  and  $\sigma_{\nu N}$  is available

## ANALYTIC STRUCTURE OF $P(\mathbf{k}, E)$ AND CORRELATIONS

- ★ The analytic structure of the spectral function is dictated by the Källèn-Lehman representations of the Green's function

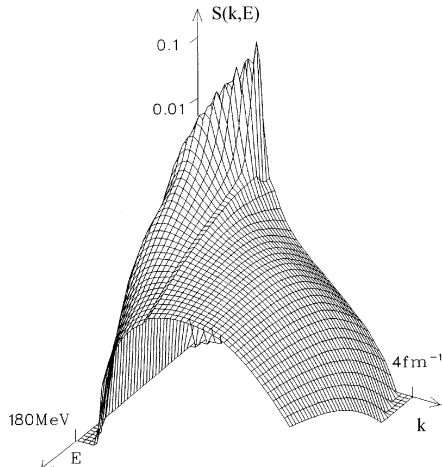
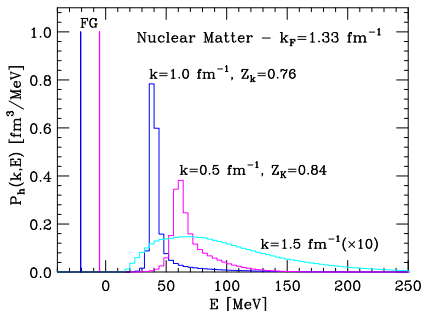
$$P(\mathbf{k}, E) = \sum_{h \in \{F\}} Z_h |M_h(\mathbf{k})|^2 F_h(E - E_h) + P_B(\mathbf{k}, E)$$

$F_h(E - E_h)$  features a collection of peaks of width  $\Gamma_h$ , located at energies  $E = E_h$  corresponding to the poles of  $G(\mathbf{k}, E)$ .

- ★ In independent-particle models based on the mean-field approximation (MFA) such as the nuclear shell model
  - ▷ Spectroscopic factors  $Z_h \rightarrow 1$
  - ▷  $M_h(\mathbf{k}) = \langle h | a_{\mathbf{k}} | 0 \rangle \rightarrow \phi_h(\mathbf{k})$ , the momentum-space wave function of the single-particle state  $h$
  - ▷ Energy distribution  $F_h(E - E_h) \rightarrow \delta(E - E_h)$
  - ▷ Smooth contribution  $P_B(\mathbf{k}, E) \rightarrow 0$ . Correlation effects not taken into account in MFA

# $P(k, E)$ OF ISOSPIN-SYMMETRIC NUCLEAR MATTER

Equilibrium density, full microscopic calculation based on a realistic nuclear Hamiltonian

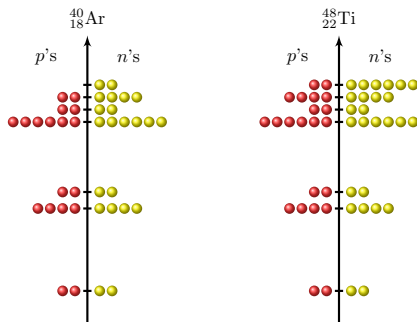


- ▶ The spectral functions of many medium-heavy nuclei have been obtained from the analysis of  $(e, e'p)$  cross sections within the Distorted-Wave-Impulse-Approximation (DWIA)

# The E12-14-012 Experiment at Jefferson Lab

## WHY ARGON AND TITANIUM?

- ★ The proton and neutron spectral functions of Argon are both needed, to describe neutrino and antineutrino interactions in liquid Argon detectors
- ★ The  $\text{Ar}(e, e'p)$  cross section only provides information on protons
- ★ Useful information on the neutron energy and momentum distribution can be obtained from  $\text{Ti}(e, e'p)$  data, by exploiting the similarity between the proton spectrum of  $^{48}\text{Ti}$  and the neutron spectrum of  $^{40}\text{Ar}$



- ★ Experiment E12-14-012—approved by PAC42 in 2014—measured the  ${}^{40}_{18}\text{Ar}(e, e'p)$  and  ${}^{48}_{22}\text{Ti}(e, e'p)$  cross sections in Jefferson Lab Hall A  
Data were collected in February and March 2017

Measurement of the Spectral Function of  ${}^{40}\text{Ar}$  through  
the  $(e, e'p)$  reaction

Proposal (PR12-14-012) submitted to the  
Jefferson Lab Program Advisory Committee PAC 42  
July 2014

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## Publications & Theses

- ▶ H. Dai *et al.*, Phys. Rev. C **98**, 014617 (2018)
- ▶ H. Dai *et al.*, Phys. Rev. C **99**, 054608 (2019)
- ▶ M. Murphy *et al.*, Phys. Rev. C **100**, 054606 (2019)
- ▶ L. Gu *et al.*, Phys. Rev. C **103**, 034604 (2021)
- ▶ L. Jiang *et al.*, Phys. Rev. D **105**, 112002 (2022)
- ▶ L. Jiang *et al.*, Phys. Rev. D **107**, 012025 (2023)
- ▶ 4 PhD Theses (3 @ VT + 1 @ UVA)

- ★ Argon & Titanium target
- ★ Beam energy  $E_e = 2.222$  GeV; parallel kinematics
- ★ Five kinematic settings

	$E'_e$ (GeV)	$\theta_e$ (deg)	$ \mathbf{p}' $ (MeV)	$\theta_{p'}$ (deg)	$ \mathbf{q} $ (MeV)	$p_m$ (MeV)	$E_m$ (MeV)
kin1	1.777	21.5	915	-50.0	865	50	73
kin2	1.716	20.0	1030	-44.0	846	184	50
kin3	1.799	17.5	915	-47.0	741	174	50
kin4	1.799	15.5	915	-44.5	685	230	50
kin5	1.716	15.5	1030	-39.0	730	300	50

kin1			kin3		
Collected Data	Hours	Events(k)	Collected Data	Hours	Events(k)
Ar	29.6	43955	Ar	13.5	73176
Ti	12.5	12755	Ti	8.6	28423
Dummy	0.75	955	Dummy	0.6	2948
kin2			kin4		
Collected Data	Hours	Events(k)	Collected Data	Hours	Events(k)
Ar	32.1	62981	Ar	30.9	158682
Ti	18.7	21486	Ti	23.8	113130
Dummy	4.3	5075	Dummy	7.1	38591
Optics	1.15	1245	Optics	0.9	4883
C	2.0	2318	C	3.6	21922
kin5			kin5 - Inclusive		
Collected Data	Hours	Events(k)	Collected Data	Minutes	Events(k)
Ar	12.6	45338	Ar	57	2928
Ti	1.5	61	Ti	50	2993
Dummy	5.9	16286	Dummy	56	3235
Optics	2.9	160	C	115	3957

- ★ Overall kinematic coverage

$$15 \leq p_m \leq 300 \text{ MeV} \quad , \quad 12 \leq E_m \leq 80 \text{ MeV}$$



# DETERMINATION OF THE TARGET SPECTRAL FUNCTION

- ★ The reduced measured cross-section defined as

$$P_D(p_m, E_m) = \frac{1}{|\mathbf{p}'|E_{\mathbf{p}'}} \frac{1}{\sigma_{ep}} \frac{d\sigma_A}{dE_{e'}d\Omega_{e'}dE_p d\Omega_p},$$

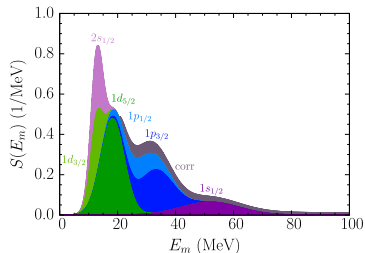
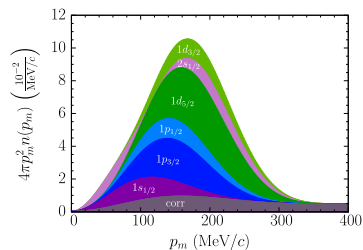
obtained using the off-shell extrapolation of the electron-proton cross section of De Forest (cc1 model), has been fitted using the model *distorted* spectral function

$$P_D(p_m, E_m) = \sum_h Z_h |\phi_h^D(\mathbf{p}_m)|^2 F_h(E_m - E_h) + P_{\text{corr}}^D(p_m, E_m),$$

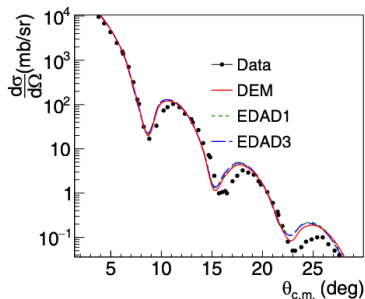
- ★ The unit normalised distorted momentum distributions,  $|\phi_h^D(\mathbf{p}_m, \mathbf{p})|^2$  are obtained from Relativistic Mean Field calculations (code provided by Carlotta Giusti)
- ★ The energy distributions  $F_h(E_m - E_h)$ , of width  $\Gamma_h$ , have been assumed to have Maxwell-Boltzmann shape
- ★ Correlation contribution, accounting for 20% of the strength, described following a simple model developed by Ciofi degli Atti & Simula

# MAIN ELEMENTS OF THE ARGON ANALYSIS

Missing momentum (top) and missing energy (bottom) distributions



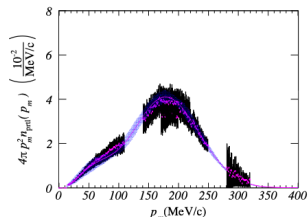
Differential cross section for elastic scattering of 800 MeV protons on Argon. Theoretical results obtained from the optical potential employed in the analysis



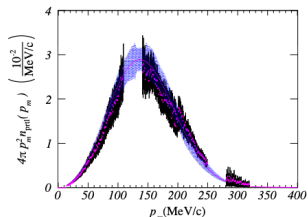
# STEP 1: ANALYSIS OF MOMENTUM DISTRIBUTION

- ★ The spectroscopic factors have been determined from momentum distributions—obtained from integration over three missing energy ranges—using constraints from previous experiments

$\alpha$	$N_\alpha$	All priors	w/o $p_m$	w/o corr.
		$S_\alpha$		
$1d_{3/2}$	2	$0.89 \pm 0.11$	$1.42 \pm 0.20$	$0.95 \pm 0.11$
$2s_{1/2}$	2	$1.72 \pm 0.15$	$1.22 \pm 0.12$	$1.80 \pm 0.16$
$1d_{5/2}$	6	$3.52 \pm 0.26$	$3.83 \pm 0.30$	$3.89 \pm 0.30$
$1p_{1/2}$	2	$1.53 \pm 0.21$	$2.01 \pm 0.22$	$1.83 \pm 0.21$
$1p_{3/2}$	4	$3.07 \pm 0.05$	$2.23 \pm 0.12$	$3.12 \pm 0.05$
$1s_{1/2}$	2	$2.51 \pm 0.05$	$2.05 \pm 0.23$	$2.52 \pm 0.05$
Corr.	0	$3.77 \pm 0.28$	$3.85 \pm 0.25$	Excluded
$\sum_\alpha S_\alpha$		$17.02 \pm 0.48$	$16.61 \pm 0.57$	$14.12 \pm 0.42$
d.o.f		206	231	232
$\chi^2/\text{d.o.f.}$		1.9	1.4	2.0



(a)  $0 < E_m < 30$  MeV



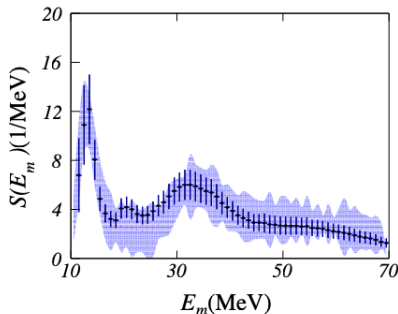
(b)  $30 < E_m < 54$  MeV

## STEP 2: ANALYSIS OF MISSING ENERGY DISTRIBUTION

- ★ The energies and widths of the shell-model states have been determined from the missing energy distributions, using the priors obtained from the momentum distribution analysis

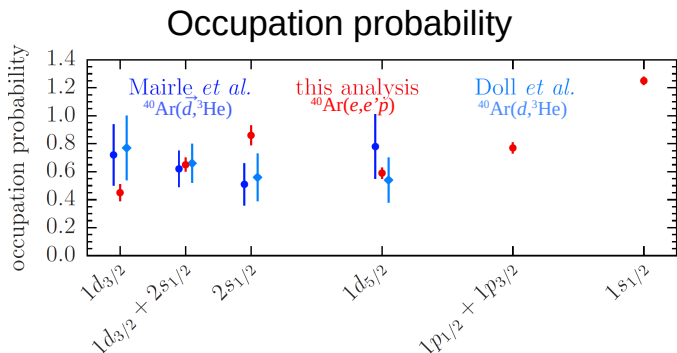
$\alpha$	$E_\alpha$ (MeV)		$\sigma_\alpha$ (MeV)	
	w/ priors	w/o priors	w/ priors	w/o priors
$1d_{3/2}$	$12.53 \pm 0.02$	$10.90 \pm 0.12$	$1.9 \pm 0.4$	$1.6 \pm 0.4$
$2s_{1/2}$	$12.92 \pm 0.02$	$12.57 \pm 0.38$	$3.8 \pm 0.8$	$3.0 \pm 1.8$
$1d_{5/2}$	$18.23 \pm 0.02$	$17.77 \pm 0.80$	$9.2 \pm 0.9$	$9.6 \pm 1.3$
$1p_{1/2}$	$28.8 \pm 0.7$	$28.7 \pm 0.7$	$12.1 \pm 1.0$	$12.0 \pm 3.6$
$1p_{3/2}$	$33.0 \pm 0.3$	$33.0 \pm 0.3$	$9.3 \pm 0.5$	$9.3 \pm 0.5$
$1s_{1/2}$	$53.4 \pm 1.1$	$53.4 \pm 1.0$	$28.3 \pm 2.2$	$28.1 \pm 2.3$
Corr.	$24.1 \pm 2.7$	$24.1 \pm 1.7$	...	...

$$15 \leq p_m \leq 110 \text{ MeV}$$



## COMPARISON WITH PREVIOUS ARGON DATA

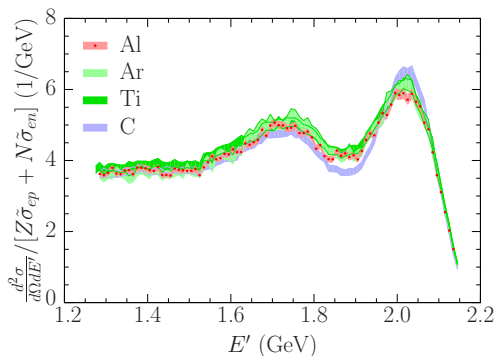
- ▶ Nucleon knock-out from Argon has been also studied in the proton pick-up reaction  $^{40}\text{Ar}(^2\text{H}, ^3\text{He})$  using both in-polarised and polarised deuteron beams



- ▶ The results of present analysis turn out to be largely compatible with previous data (figure courtesy of A. Ankowski)

## APPLICATIONS: INCLUSIVE CROSS SECTIONS

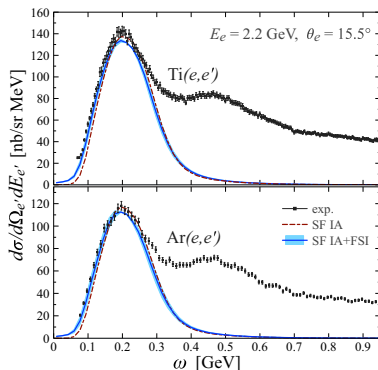
- ▶ inclusive data have been collected at beam energy  $E = 2.22 \text{ GeV}$  and electron scattering angle  $\theta_e = 15.54 \text{ deg}$  using different targets.  
H. Dai *et al.*, PRC **98**, 014617 (2018); PRC **99**, 054608 (2019)  
M. Murphy *et al.*, PRC **100**, 054606 (2019)



- ▶ Consistency with previous inclusive data confirmed by  $y$ -scaling and superscaling analyses

## COMPARISON TO THE RESULTS OF THEORETICAL STUDIES

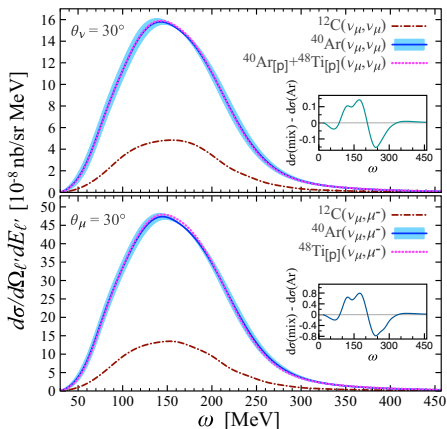
- ▶ The proton and neutron spectral functions of  $^{40}\text{Ar}$  and  $^{48}\text{Ti}$  have been calculated by C. Barbieri, N. Rocco, and G. Somà using the self-consistent Green's function formalism and a chiral nuclear Hamiltonian [PRC **100**, 062501(R) (2019)]



- ▶ Position and width of the quasi elastic peak are described to remarkable accuracy

# COMPARING ARGON AND TITANIUM

- ▶ Theoretical calculations of Barbieri *et al.* [PRC **100**, 062501(R) (2019)]



- ▶ Results obtained by replacing the neutron spectral function of  $^{40}\text{Ar}$  with the experimentally accessible proton spectral function of  $^{48}\text{Ti}$  are quite encouraging.



# IMPLEMENTATION IN NUWRO

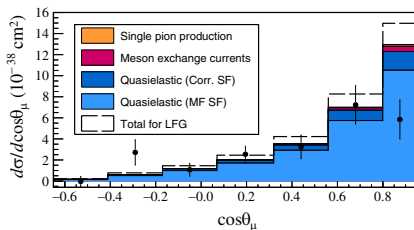
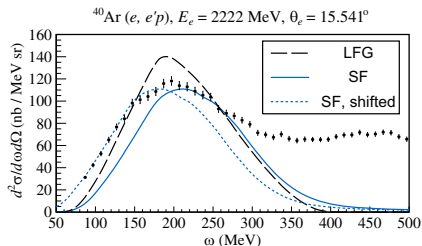
- ▶ First implementation of the Argon spectral functions obtained from the JLab data [PRD **109**, 073004 (2024)]

PHYSICAL REVIEW D **109**, 073004 (2024)

## JLab spectral functions of argon in $\text{NaWro}$ and their implications for MicroBooNE

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<sup>✉</sup> (Received 21 December 2023; accepted 6 March 2024; published 8 April 2024)



## SUMMARY & OUTLOOK

- ★ The **Ar and Ti( $e, e'p$ )** cross-sections measured at Jefferson Lab by the E12-14-012 collaboration have allowed a reliable determination of the Argon and Titanium spectral functions
- ★ In addition to being interesting in their own right, the information obtained from JLab data —e.g. spectroscopic factors and width of the single-nucleon states—will be useful to derive *realistic* spectral functions from *simplified* nuclear models
- ★ The results of early applications of the E12-14-012 data set—including theoretical studies of the inclusive cross sections, and analyses of electron and neutrino data based on the implementation in NuWro—are encouraging
- ★ The extent to which a proton in Titanium is a good proxy for a neutron in Argon, as well as the feasibility of a neutron knockout experiment, need to be carefully investigated
- ★ Electron scattering experiments may provide new insight into other outstanding issues, such as the determination of the nucleon axial form factor

# MEASUREMENT OF THE AXIAL FORM FACTOR AT JLAB

- ▶ Bogdan Wojtsekhowski's talk at the Winter Hall A Collaboration Meeting at JLab (January 16-17, 2024)

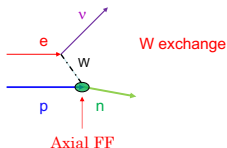


## Weak Axial-vector Form Factor

B. Wojtsekhowski, JLab

in collaboration with

P. Degtiarenko, A. Deur, J. Golak,  
D. Jones, C. Keppel, E. King, J. Napolitano



1/16/24

Hall A collaboration

Bogdan Wojtsekhowski

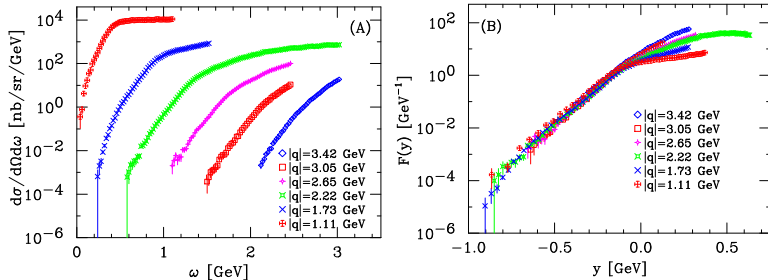
slide 1

- ▶ Studies aimed at submitting a proposal to the JLab PAC are under way

## Backup slides

## $y$ -SCALING OF INCLUSIVE DATA

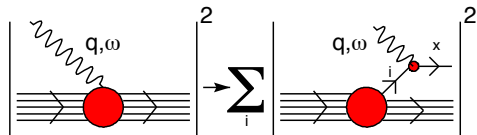
- ★ JLab data of Arrington *et al.*, PRL **82**, 2056 (1999). Iron target evidence of factorisation of the  $eA$  cross section. PRL **82**, 2056 (1999)



- ★ in the kinematical region in which scaling is observed the dominant reaction mechanism is quasi elastic single-nucleon knock out. Scaling violations originate from inelastic processes (at  $y > 0$ ) and FSI (at  $y \ll 0$ )

# FACTORISATION OF THE NUCLEAR CROSS SECTION

- ★ In the PWIA regime, corresponding to  $\lambda \ll d_{NN} \sim 1.5 \text{ fm}$ , nuclear scattering reduces to the incoherent sum of scattering processes involving individual nucleons



- ★ Basic assumptions
  - ▷  $J_A^\mu(q) \approx \sum_i j_i^\mu(q)$  (single-nucleon coupling)
  - ▷  $|(A-1)_n, \mathbf{p}'\rangle \approx |(A-1)_n\rangle \otimes |\mathbf{p}'\rangle$  (factorization of the final state)
- ★ As a zero-th order approximation, Final State Interactions (FSI) and processes involving two-nucleon Meson-Exchange Currents (MEC) are neglected. Their effects are included as corrections.

## THE FACTORISED $(e, e'p)$ CROSS SECTION

- ★ Factorisation allows to rewrite the nuclear transition amplitude in the simple form

$$\langle (A-1)_{n, \mathbf{p}'} | J_A^\mu | 0 \rangle \rightarrow \sum_i M_n(\mathbf{k}) \langle \mathbf{p}' | j_i^\mu | \mathbf{k} \rangle$$

- ▶ The nuclear amplitude  $M_n$  is independent of momentum transfer
- ▶ The matrix element of the current between free-nucleon states can be computed using the fully relativistic expression

- ★  $(e, e'p)$  cross section

$$\frac{d\sigma_A}{dE_{e'} d\Omega_{e'} dE_p d\Omega_p} \propto \sigma_{ep} P(p_m, E_m)$$

- ★ The spectral function describing the probability of removing a nucleon of momentum  $\mathbf{p}$  from the nuclear ground state, leaving the residual system with excitation energy  $E$ , is trivially related to the two-point Green's function through

$$P(\mathbf{k}, E) = -\frac{1}{\pi} \text{Im} G(\mathbf{k}, E)$$

## FSI CORRECTIONS WITHIN THE DWIA

- ▶ The effects of FSI are described by a *distorted* mean-field spectral function

$$P_{MF}^D(\mathbf{p}_m, \mathbf{p}, E_m) = \sum_h Z_h |\phi_h^D(\mathbf{p}_m, \mathbf{p})|^2 F_h(E_m - E_h)$$
$$\sqrt{Z_h} \phi_h^D(\mathbf{p}_m, \mathbf{p}) = \int d^3 p_i \chi_p^*(\mathbf{p}_i + \mathbf{q}) \phi_h(\mathbf{p}_i)$$

where the *distorted wave*  $\chi_p^*(\mathbf{p}_i + \mathbf{q})$  is obtained from a *complex* optical potential

- ▶ The analysis of the large body of  $(e, e'p)$  data shows that the effects of FSI can be strongly suppressed by measuring the cross section in *parallel kinematics*, that is with  $\mathbf{p} \parallel \mathbf{q}$ .
- ▶ In parallel kinematics, *factorisation of the nuclear cross section is preserved to very high accuracy*, the distorted momentum distribution only depends on missing momentum

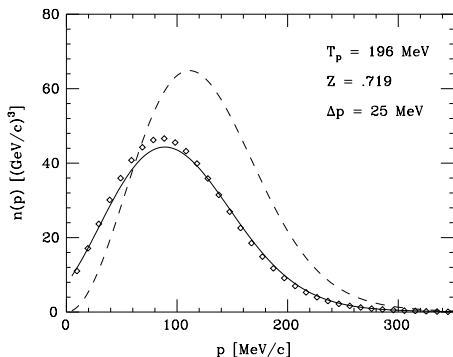
$$n_h^D(p_m) = Z_h |\phi^D(p_m)|^2,$$

and *the effects of FSI can be easily identified*



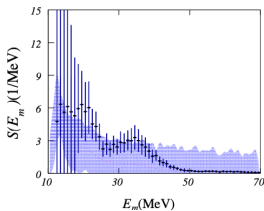
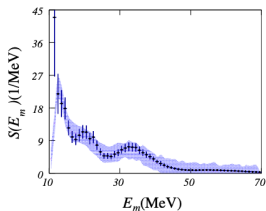
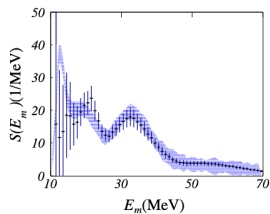
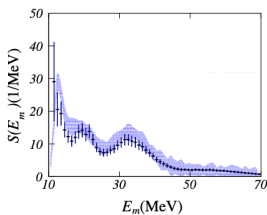
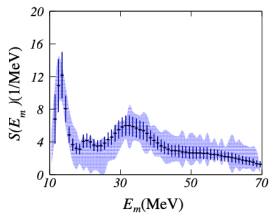
## DISTORTED MOMENTUM DISTRIBUTION

- ▶ consider knock out of a  $p$ -shell proton with kinetic energy  $T_p = 196$  MeV in parallel kinematics
- ▶ Distortion described by a *complex* optical potential (OP)

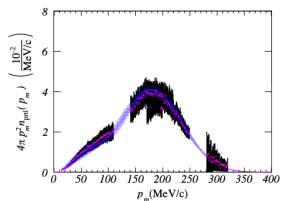


- ▶ FSI lead to a shift in missing momentum (real part of OP), and a significant quenching, typically by a factor  $\sim 0.7$  (imaginary part of OP).

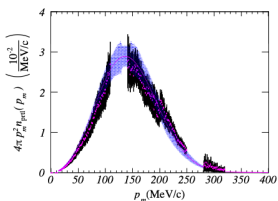
# ARGON MISSING ENERGY DISTRIBUTIONS



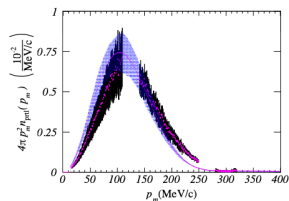
# ARGON MISSING MOMENTUM DISTRIBUTIONS



(a)  $0 < E_m < 30$  MeV



(b)  $30 < E_m < 54$  MeV

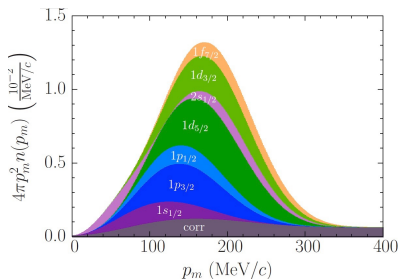


(c)  $54 < E_m < 90$  MeV

- ★ The agreement—within uncertainty—between distributions corresponding to different kinematical settings supports the validity of the DWIA treatment of FSI, and, more generally, of factorisation

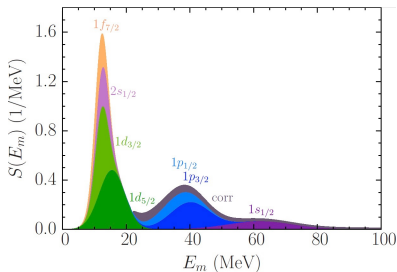
# TITANIUM MISSING MOMENTUM DISTRIBUTIONS

$\alpha$	$N_\alpha$	all priors	w/o $p_m$	w/o corr.
			$S_\alpha$	
$1f_{7/2}$	2	$1.53 \pm 0.25$	$1.55 \pm 0.28$	$1.24 \pm 0.22$
$1d_{3/2}$	4	$2.79 \pm 0.37$	$3.15 \pm 0.54$	$3.21 \pm 0.37$
$2s_{1/2}$	2	$2.00 \pm 0.11$	$1.78 \pm 0.46$	$2.03 \pm 0.11$
$1d_{5/2}$	6	$2.25 \pm 0.16$	$2.34 \pm 0.19$	$3.57 \pm 0.29$
$1p_{1/2}$	2	$2.00 \pm 0.20$	$1.80 \pm 0.27$	$2.09 \pm 0.19$
$1p_{3/2}$	4	$2.90 \pm 0.20$	$2.92 \pm 0.20$	$4.07 \pm 0.15$
$1s_{1/2}$	2	$2.14 \pm 0.10$	$2.56 \pm 0.30$	$2.14 \pm 0.11$
corr.	0	$4.71 \pm 0.31$	$4.21 \pm 0.46$	excluded
$\sum_\alpha S_\alpha$		$20.32 \pm 0.65$	$20.30 \pm 1.03$	$18.33 \pm 0.59$
d.o.f.		121	153	125
$\chi^2/\text{d.o.f.}$		0.95	0.71	1.23



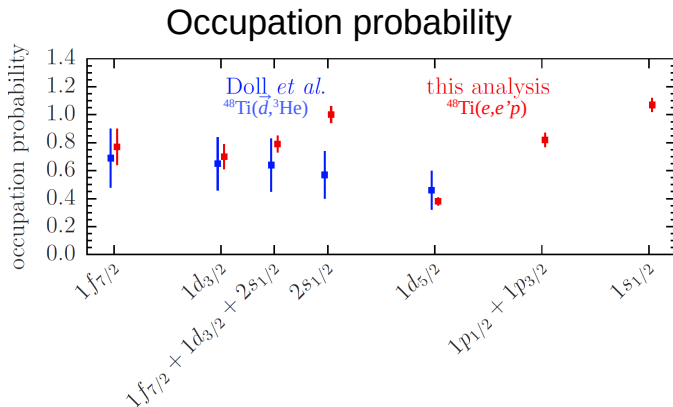
# TITANIUM MISSING ENERGY DISTRIBUTIONS

$\alpha$	$E_\alpha$ (MeV)		$\sigma_\alpha$ (MeV)	
	w/ priors	w/o priors	w/ priors	w/o priors
$1f_{7/2}$	$11.32 \pm 0.10$	$11.31 \pm 0.10$	$8.00 \pm 5.57$	$8.00 \pm 6.50$
$1d_{3/2}$	$12.30 \pm 0.24$	$12.33 \pm 0.24$	$7.00 \pm 0.61$	$7.00 \pm 3.84$
$2s_{1/2}$	$12.77 \pm 0.25$	$12.76 \pm 0.25$	$7.00 \pm 3.76$	$7.00 \pm 3.84$
$1d_{5/2}$	$15.86 \pm 0.20$	$15.91 \pm 0.22$	$2.17 \pm 0.27$	$2.23 \pm 0.29$
$1p_{1/2}$	$33.33 \pm 0.60$	$33.15 \pm 0.65$	$3.17 \pm 0.45$	$3.03 \pm 0.48$
$1p_{3/2}$	$39.69 \pm 0.62$	$39.43 \pm 0.68$	$5.52 \pm 0.70$	$5.59 \pm 0.70$
$1s_{1/2}$	$53.84 \pm 1.86$	$52.00 \pm 3.13$	$11.63 \pm 1.90$	$13.63 \pm 2.59$
corr.	$25.20 \pm 0.02$	$25.00 \pm 0.29$	—	—



## COMPARISON WITH PREVIOUS TITANIUM DATA

- ▶ Nucleon knock-out from Argon has been also studied in the proton pick-up reaction  $^{40}\text{Ar}(^2\text{H}, ^3\text{He})$  using both inpolarised and polarised deuteron beams



- ▶ The results of present analysis turn out to be largely compatible with previous data