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Electronic and Atomistic Modeling of Qubit Materials & Interfaces

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Materials Theory and Design Group
(1) UG – Alex Tai

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(4) PD – Danilo Puggioni, Mike Waters, Alex Georgescu, John Cavin

Numerous Collaborators



Argonne



Local structure ~ geometry of these units



 Crystal structure ~ how one or more of these units tile space to from an extended solid





Local structure ~ geometry of these units



 Crystal structure ~ how one or more of these units tile space to from an extended solid





heterostructures and superlattices

polyhedral-property harm control

y harmonizing contraindicated properties materials informatics corrosion and electrochemistry



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Lecture Outcomes

• Begin to bridge the gap between theory and experiment, fostering a deeper understanding of qubit materials and interfaces and their practical applications

Use systems charts to guide materialproperty correlation studies Create atomistic models of materials and interfaces used for superconducting qubits

Understand principles of electronic and atomistic modeling Analyze and interpret modeling results from electronic and atomistic calculations







Agenda

- SC Qubit Materials and Systems Charts Introduction
- Modeling Materials
 - Model Formulation
 - Electronic Structure Models
 - Atomistic Models
 - From Phenomenological to Microscopic
- Use Cases
 - Nb and its hydrides
 - Nb and its oxides
- Co-Design and Integration with Experimentation Summary

Use systems charts to guide materialproperty correlation studies



SC Qubit Architecture

Primary Materials

- Superconducting Films (Al, Nb, Ta)
- Insulating Substrate (Si, Sapphire)
- Josephson Junction (S-I-S)

Secondary Materials

- Silicon and metal oxides
- Intermetallic phases (Nb-Si)
- Adhered contaminants
- Interstitial contaminants
 - Hydrogen, Oxygen, Carbon, ...



Materials Contributions to Losses (T₁) from CPW Resonators

Two-level systems

- Electric dipoles (charge noise)
- Magnetic moments (flux noise)
- Quasiparticles (broken pairs)

Quasiparticles

- Coupling directly to qubit

Thermal losses

- Dielectric loss at CPW interfaces
- Quasiparticles



M. V. P. Altoé et al., Localization and Mitigation of Loss in Niobium Superconducting Circuits, PRX Quantum 3, (2022).



C. Wang, C. Axline, Y. Y. Gao, T. Brecht, Y. Chu, L. Frunzio, M. H. Devoret, and R. J. Schoelkopf, Surface Participation and Dielectric Loss in Superconducting Qubits, Appl. Phys. Lett. 107, 162601 (2015).



- Processing
- Structure
- Properties
- Performance





- Processing
- Structure
- Properties
- Performance





- **Processing:** The way a material is made (thermal, chemical, physical)
- Structure
- Properties
- Performance







- Processing: The way a material is made (thermal, chemical, physical)
- Structure: The way the material is organized
- Properties
- Performance





Internal structures of materials

The way in which of atoms, molecules, phases, etc. assemble across length scales



Quartz crystal

Grains in a SrTiO₃ ceramic

Nanocrystalline $Mn_{0.5}Zn_{0.5}Fe_2O_4$ particles

Atomic resolution image of BaTiO₃

Structure of a material depends on processing history, not just composition, and often exhibits hierarchical order



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- Processing: The way a material is made (thermal, chemical, physical)
- Structure: The way the material is organized
- **Properties**: The way the material behaves
- Performance



A quantifiable attribute of a material and informs us about how we expect a material to respond (displace) to a stimulus (force)

- Mechanical stiffness, piezoelectricity
- Electrical electrical conductivity
- Optical transparency, emission
- Magnetic ferromagnetic, diamagnetic
- Chemical corrosion resistance
- Thermal heat capacity, conductivity

- Processing: The way a material is made (thermal, chemical, physical)
- Structure: The way the material is organized
- Properties: The way the material behaves
- Performance: How well a material does what it is intended to do



MSE Tools of the Trade

- Theory
- Characterization
- Computation/Modeling
- Data Science/AI



Apply systems approach to simplify complexity

• System engineering developed by G.M. Jenkins (1970s)

Nature of systems

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- Complex grouping of components
- Divisible into subsystems (flow-block diagrams)
- Subsystems interactive: output of 1 is input of 2
- System is a part of hierarchy of systems (strong influence of higher levels)
- System has **objective(s)** influenced by the wider system; overall objective is compromise between conflicting objectives
- System must be **designed** to function at maximum efficiency
- Apply systems approach to materials, integrating processing, structure, property, and performance (G.B. Olson)
 - <u>Science 277,1237-1242 (1997)</u>



Figure 4.1 Simplified flow-block diagram of an acrolein plant as an example of a simple system with interacting subsystems.



Using materials science paradigm – Systems Design Charts

- Consider the material, interface(s), or device(s) as a system
- Identify connections between processing-structure-properties-performance
 - Understanding the strength of connections requires domain expertise





Using materials science paradigm – Systems Design Charts

- Consider the material, interface(s), or device(s) as a system
- Identify connections between processing-structure-properties-performance
 - Understanding the strength of connections requires domain expertise



- Guidelines
 - Processing is sequential (use arrows to show direction)
 - Structures can interact with one-way arrows
 - "Links" represent the reciprocal interactions
 - Properties are quantitative / measurable
 - Performance is what an end-user may request for a component or application



Using materials science paradigm – Systems Design Charts

- Consider the material, interface(s), or device(s) as a system
- Identify connections between processing-structure-properties-performance
 - Understanding the strength of connections requires domain expertise



- Systems design chart for chocolate cake
 - Processing?
 - Structures?
 - Properties?
 - Performance?





Simplified Systems Design Chart for Cake





System Design Charts Get Complex! – C64 Gear Steel





Pub. No.: US 2009/0199930 A1 Pub. Date: Aug. 13, 2009



Superconducting Qubits as a Complex System



More recommendations for system design charts

- Be as specific as possible
- Charts can and should evolve as we understand more about the system
- Subsystems are usually your focus, but also consider the whole system first
- Consider what models, tools, experiments the links represent





2 anaco : tougimooo

Volume Defects

- Hydrides
- Surface Oxides
- Interfacial Phases

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MATERIALS & SYSTEMS CENTER









MATERIALS & SYSTEMS CENTER

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Create atomistic models of materials and interfaces used for superconducting qubits

Understand principles of electronic and atomistic modeling



Theory, modeling, and simulation

- Theory
 - Attempt to find a fundamental description of a physical process
 - Coherent group of general propositions used as principles of explanation for a class of phenomena
- Model
 - An idealization of real behavior
 - Approximate description based on empirical and/or physical reasoning
 - Distinction from theory: Model attempts to create idealization of real behavior to a given accuracy, not a fundamental description that is strictly true

models describes a part of a real system by using a similar but simpler structure; they providing a starting point for theory



Model representation

- Models always have an external representation of some kind
 - Representation is approximate
 - Each representation is useful for some purposes

Electronic Structure Model



FIG. 4. Calculated spin-polarized electronic band structure in smaller energy range around the Fermi level showing the isolated two-band Cu-d manifold. The Fermi level is set to 0 eV and is marked by the dashed line.

Atomic Structure Model



Equation Models

Classification Models



Theory, modeling, and simulation

Simulation

- Study of the dynamical response of a system
- Subjecting models to inputs and constraints that simulate real events
- Does not mimic reality, but mimics a model of reality
- Accuracy depends on many factors
 - Numerical methods and their accuracy
 - Inadequacies of the model (assumptions, principles) upon which simulation is based



Interstitial Oxygen Diffusion in Nb



- Successful materials modeling relies on
 - Adequate familiarity with the underlying mathematics and numerical analysis principles
 - Solid understanding of the materials physics or chemistry of the problem to be solved

Theory, modeling, and simulation

Simulation

- Study of the dynamical response of a system
- Subjecting models to inputs and constraints that simulate real events
- Does not mimic reality, but mimics a model of reality
- Accuracy depends on many factors
 - Numerical methods and their accuracy
 - Inadequacies of the model (assumptions, principles) upon which simulation is based
- Cannot separate simulations from the underlying models!



Building physical and testable models

- Simulations are not reality, they represent a model of reality
- Cost/benefit analysis
 - Just because you can calculate something, it does not mean it's always the best approach
 - It is sometimes simpler and better to do a measurement
- Garbage In = Garbage out (GIGO)



– Pablo Picasso


Length scales and methods



machine learning and artificial intelligence



Types of methods

Electronic structure

Calculate where the electrons are in materials

total energy

- Relies on quantum mechanics, wave functions and methods to solve Schrodinger equations

Atomistic

- Follow individual atoms in materials
 - Molecular statics ۰
 - Quasi-harmonic theory ۰
 - Molecular dynamics •
 - (Kinetic) Monte Carlo ۰



Types of methods

Mesoscale

- Track other entities (grains size, magnetization,...)
 - Cellular automata (CA)
 - Monte Carlo
 - Phase fields
- Continuum modeling
 - General differential equation solving
 - Numerical methods of ODEs/PDEs
 - Thermal transport
- Data-driven methods
 - Unsupervised learning
 - Supervised learning
 - Neural networks
 - Symbolic regression

Metropolis Monte Carlo – generates configurations according to the desired statistical mechanics distribution

- There is no time, the method cannot be used to study evolution of the system
- Equilibrium properties can be studied

Kinetic Monte Carlo (KMC) - can address kinetics of a system

 Use transition rates that depend on the energy barrier between the states, with time increments formulated so that they relate to the microscopic kinetics of the system



Methodology: Density Function Theory (DFT) Simulations



• Solve a set of Schrodinger-like equations for the electronic states to obtain the ground state density (and properties) of a material



DFT approach (band theory)



 The ground-state density of electrons interacting with each other can be calculated as the ground-state density of an auxiliary system of non-interacting electrons (Kohn & Sham, 1965)



Popularity of DFT for materials modeling

- Transferability method applies to many material classes
- Simplicity direct link between elementary QM (independent particles) and materials physics and chemistry
- Reliability
 - Accuracies can be as good as a few percent
 - Approximations (uncontrolled but often very good)
- Software sharing
 - Efficient numerical methods to perform the minimization
- Reasonable starting point for higher level methods



Methodology: Density Function Theory (DFT) Simulations



Workflow of DFT simulations





What we can calculate with DFT (accessible properties)

- Total energy in the ground state
 - Cohesive energies
 - Relative stability of different phases/structures
 - Heats of formation
 - Surface and interface energies
 - Adsorption energies, diffusion barriers, etc.
- Structural Optimization
 - Cell shape and size
 - Atomic positions
- Electronic properties
 - Electron density plots
 - Atomic charges and magnetic moments
- ¹⁴ Kohn-Sham band structure/ eigenvalues (not real-world structure, but often compared)

Material	Expt	Theory	Delta	lype	
LaBi	6.57	6.648	1.2%	alloy	
CaF_2	5.4626	5.496	0.6%	halide	
Ag	4.086	4.112	0.6%	metal	
V	3.028	3.019	-0.3%	metal	
ZrN	4.62	4.634	0.3%	misc	
NbO	4.2103	4.2344	0.6%	oxide	
GaAs	5.653	5.663	0.2%	semiconductor	
$CoSi_2$	5.36	5.3	-1.1%	silicide	

Accuracy: 1-2% for a weakly correlated material Except for E_{coh} and band gaps

What we can calculate (energy derivatives)

- First-order
 - Atomic forces, stress tensor
 - Macroscopic polarization (Berry Phase approach)
 - Magnetoelectric coupling (recent development)
- Second-order
 - Optical and static dielectric tensor
 - Elastic constants and piezoelectric tensor
 - Born effective charges and IR intensities
 - Phonon dispersion plots
- Third-order
 - Non-linear optical susceptibilities
 - Raman intensities

Accuracy: 5-10% Except for high-frequency dielectric constant



Building models

- Standard steps which are often not explicitly recognized
- · Approach is often used even implicitly

DISCLAIMER: Inaccurate answers from numerical methods do not necessarily imply errors in the model

and

Accurate numerical solutions do not imply a correct model

- Models should be no more complicated than necessary
- "Everything should be made as simple as possible, but no simpler."



Steps in physical model formulation

- Step 1 : Identifying the problem
- Step 2 : Identifying the desired inputs and outputs
- Step 3 : Identifying the physical mechanisms
- Step 4 : Targeting the precision
- Step 5 : Constructing the model
- Step 6 : Dimensional analysis
- Step 7 : Computer implementation
- Step 8 : Interrogating the model
- Step 9 : Displaying the results
- ⁴⁷ Step 10: Validate



M.F. Ashby Mat Sci Tech 8, 102 (1992)

Step 1: Identifying the problem

- Pertinent length scales and materials structure
- E-M Fields



• Localized materials defects

10⁻¹⁰ m > 10⁻⁸ m

Extend materials defects





- Hydrogen interstitials
- Role of oxygen vacancies
- Processing RRR
- Quasiparticles

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Step 2: Identifying desired inputs and outputs

- What are the essential ingredients of the model?
 - Composition, structure, boundary conditions, temperature, time, etc.
- What are the less important quantities that could be added later?
 - Start simple and then add complexity
- Remember that the output...
 - Is only as good as the input
 - Could be used as input for a higher-level model



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 - Nb and its oxides
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Analyze and interpret modeling results from electronic and atomistic calculations



Nb and its hydrides (NbH_x)

- Recent discovery hydrides in Nb films on Silicon processed by Rigetti
 - 3 types of Nb hydrides with varying atomic structures, crystalline orientation, and morphology
 - Small irregularly shaped (~5 nm) to large distinctly shaped (~100 nm)

	Help
Quantum Physics	
Submitted on 23 Aug 2021]	
Discovery of Nb hydride precipitates in superconducting qubits	
laeyel Lee, Zuhawn Sung, Akshay A. Murthy, Matt Reagor, Anna Grassellino, Alexander Romanenko	
We report the first evidence of the formation of niobium hydrides within niobium films on silicon substrates in superconducting qubits Rigetti Computing. We combine complementary techniques including room and cryogenic temperature atomic scale high-resolution transmission electron microscopy (HR-TEM and STEM), atomic force microscopy (AFM), and the time-of-flight secondary ion mass (TOF-SIMS) to reveal the existence of the niobium hydride precipitates directly in the Rigetti chip areas. Electron diffraction and high transmission electron microscopy (HR-TEM) analyses are performed at room and cryogenic temperatures (~106 K) on superconduct niobium film areas, and reveal the formation of three types of Nb hydride domains with different crystalline orientations and atomics There is also variation in their size and morphology from small (~5 nm) irregular shape domains within the Nb grains to large (~10-1 grains fully converted to niobium hydride. As niobium hydrides are non-superconducting and can easily change in size and location cooldowns to cryogenic temperatures, our findings highlight a new previously unknown source of decoherence in superconducting contributing to both quasiparticle and two-level system (TLS) losses, and offering a potential explanation for qubit performance char cooldowns. A pathway to mitigate the formation of the Nb hydrides for superconducting qubit applications is also discussed.	and scannin spectroscop -resolution tring qubit tructures. 00 nm) Nb upon differe jubits, iges upon

1111ps.//arxiv.019/abs/2100.10000

- Hydrides lead to loss of performance in SRF Cavities (Alex's lecture): Q disease Supercond. Sci. Technol. 26 035003 (2013)
- Hydrides are metallic and non-superconducting
 - Small hydrides, proximity-induced superconductivity
 - Large hydrides, regular metal conductivity
- Additional QPs due to proximity breakdown under high fields (H>Hb)



Steps in physical model formulation

- Step 1 : Identifying the problem
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- Step 9 : Displaying the results



Steps in physical model formulation

- Step 1 : Identifying the problem
- Step 2 : Identifying the desired inputs and outputs
- Step 3 : Identifying the physical mechanisms
- 1. Which are the relevant hydride phases?
- 2. Are bulk or interface structure/properties important?
- 3. What are the electronic/magnetic properties of the Nb/NbH grain boundaries?
 - Input structure
 - Output electronic properties
- 4. Can we understand and predict hydride nucleation and growth?
 - Input structure
 - Output elastic stiffness tensors



Building atomistic model – a short diversion

• BCC crystal has 12 tetrahedral sites and 6 octahedral sites



Structures and densities can be visualized in VESTA

• Structure can be rendered in 3D using minimal information (atomic species and their occupied Wyckoff sites) and a structure visualization program like VESTA





Choose the VESTA version for your OS and follow the install directions or extract the files

You can use this (or equivalent software) for constructing input structures and analyzing crystal structures



http://jp-minerals.org/vesta/en

VESTA demo (later for homework)

- Opening files
- Drawing bonds
- Measuring angles and distances
- Applying periodic boundary conditions
- Creating supercells



Face Centered Cubic (FCC) structure

• Atoms touch each other along the face diagonals



Example: Al, Cu, Au, Pb, Ni, Pt, Ag

Coordination # = 12 Cubic-close packing forms an **antiprism**





Octahedral and tetrahedral voids in cubic close-packed structures

• Full list of site positions



Atom	x	y	z
Anion	0	0	0
	1/2	1/2	0
	1/2	0	1/2
	0	1/2	1/2
hole	1/2	1/2	1/2
	1/2	0	0
	0	1/2	0
	0	0	1/2





AB crystal structures

- NaCl structure
 - Equal number of cations and anions
 - CCP array of Cl⁻ anions
 - Na⁺ cations fill 100% of octahedral voids filled
 - Tetrahedral interstices remain empty
- Alternative description
 - Can be considered as two interpenetrating FCC lattices (one cation FCC lattice and one anion FCC lattice)
- Examples
 - Alkali metal hydrides
 - Alkali halides except for CsX (X=Cl, Br, I)
 - Alkaline earth oxides, sulfides, selenides, and tellurides Mg-Ba except MgTe
 - Carbides and nitrides MC and MN and some phosphides
 - ⁶ Many alloy phases



NaCl				
SG = Fm	$a\bar{3}m$ (N	No. 225	(5), a =	5.63 Å
Atom	x	y	z	:
Na	0	0	0	
Cl	1/2	1/2	1/2	





Build atomistic model

- BCC crystal has 12 tetrahedral sites and 6 octahedral sites
- Hydrogen can occupy any of the 12 tetrahedral sites, and its concentration governs which Nb hydrides can form in the Nb matrix







- Hydride-induced decoherence in Nb superconducting planar resonators and superconducting qubits
- Various hydride structures
 - Bulk (single phase)
 - Interfaces (two-phase)

Electronic structure



Microwave dissipation emerges due to Nb hydrides being poor or non-superconductors

Quality factor Q_0 of SRF cavities is determined by the surface resistance via the formula:

$$Q_0 = \frac{\omega U}{P_{\text{diss}}} = \frac{\omega \mu_0 \int_V H^2 \mathrm{d}V}{\int_A R_{\text{s}}(H) H^2 \mathrm{d}A} \tag{1}$$

where ω is the angular frequency, U is stored energy calculated from the integral of the field over cavity volume, and $P_{\rm diss}$ is the power dissipated in cavity walls calculated as an integral of surface resistance over cavity walls. Extremely low surface resistance in superconducting state and hence very high quality factors $Q_0 > 10^{11}$ are achievable in such structures.



Electronic density of states of bulk NbH_x



- $Nb_4H_3(\epsilon)$ is the low temperature stable hydride phase
- Metallic character persists with increasing hydrogen content but poor SCs
- Superconducting character lost with increasing content
- Hydrides are nonmagnetic



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Nb hydride precipitates in superconducting qubits

- Nb hydrides analyzed in detail using HR-TEM
- Nb hydrides in Nb grains within the superconducting coplanar resonators
- Hydride volume fraction is estimated to be 0.1~1%



(100) plane of ϵ -NbH_x is parallel to the (110) Nb in the film



- Hydride-induced decoherence in Nb superconducting planar resonators and superconducting qubits
- Various hydride structures
 - Bulk (single phase)
 - Interfaces (two-phase)

Identify the problem Identify the **ITERATE** Target the precision Construct the model Dimensional analysis Develop or find compute code Use the results / validate

- Nucleation and growth
- Balancing interfacial energies



Elastic moduli

Are the interfaces coherent?



A <u>coherent interface</u> with slight mismatch leads to <u>coherency strains</u> (or lattice distortions) in the adjoining lattices. A <u>semicoherent interface</u>. The misfit parallel to the interface is accommodated by a series of edge dislocations.



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Are the interfaces coherent?



The transition occurs at critical a particle size $R_c\sim {3\Delta\sigma\over 4\mu\epsilon^2}$ For Nb hydrides $R_c\sim 2$ nm

Porter and Easterling and Courtesy Peter Voorhees

How a coherent precipitate becomes incoherent?



- MD simulation shows a TiC precipitate (20% lattice misfit)
- The precipitate is completely encased in dislocations



Hydride Mitigation Strategies

- Post-annealing of Nb films above 600 °C to degas H
 - Supercond. Sci. Technol. 30(9) 094004 (2017)
- Challenge Nb silicides can form at Nb/Si interfaces

PHYSICAL REVIEW MATERIALS 6, 064402 (2022)

Stability, metallicity, and magnetism in niobium silicide nanofilms

Xuezeng Lu,¹ Dominic P. Goronzy⁰,^{1,2} Carlos G. Torres-Castanedo,¹ Paul Masih Das,¹ Maryam Kazemzadeh-Atoufi⁰,¹ Anthony McFadden⁰,³ Corey Rae H. McRae⁰,^{4,5} Peter W. Voorhees,¹ Vinayak P. Dravid⁰,^{1,6} Michael J. Bedzyk⁰,^{1,7,8} Mark C. Hersam,^{1,9,10} and James M. Rondinelli⁰,^{1,*}

- Use nitrogen during processing to control nucleation
 - Supercond. Sci. Technol. 31(11) 115007 (2018)
- Modify grain boundary structure (size, texture, etc.) to nucleation

- J. Appl. Phys. 121(19) 193903 (2017)

Suppression of Hydrides with Nitrogen

- DFT calculations identify why there are low hydride concentrations observed near nitrogen treated niobium surfaces
 - Hydrogen binding is suppressed (short-range effect limited ~2.5 Å away)
 - Hydrogen disrupts covalent bonding between Nb-H
 - Nitrogen increases the energy barrier for hydrogen diffusion





Papers for More Information

- Suppression of hydride precipitates in niobium superconducting radio-frequency cavities
 - Supercond. Sci. Technol. 26 105003 (2013)
 - https://doi.org/10.1088/0953-2048/26/10/105003
- Revealing the role of nitrogen on hydride nucleation and stability in pure niobium using first-principles calculations
 - Supercond. Sci. Technol. 31 115007 (2018)
 - <u>https://doi.org/10.1088/1361-6668/aae147</u>
- Suppression of nano-hydride growth on Nb(100) due to nitrogen doping
 - J. Chem. Phys. 152, 214703 (2020)
 - <u>https://doi.org/10.1063/5.0007042</u>


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Magnetic Impurities as Loss Source in amorphous Nb_2O_{5-x}

- Reduced Nb pentoxides exhibit temperature dependent paramagnetism
 - Magnetic susceptibility increases with decreasing oxygen content
- Magnetic moments provide several channels for qubit decoherence:
 - Increased quasiparticle losses through Shiba mechanism*
 - Bloch relaxation of moments
 - Magnetic flux noise



FIG. 13. Magnetic susceptibilities of $Nb_{25}O_{62},\ Nb_{47}O_{116},\ Nb_{22}O_{54},\ Nb_{12}O_{29},\ and\ Ti_{0.3}Nb_{11.5}O_{29}$ plotted per mole $(Nb,Ti)O_x.$

DOI: 10.1103/PhysRevB.44.6973



DOI: 10.1103/PRXQuantum.3.020312



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- Various NbO_x structures
 - Bulk Crystalline
 - Bulk Amorphous





Parameters Magnetic impurity density: au_s^{-1} Dissipation: $Q_2(\omega, k)$ Superconducting gap: $|\Delta|$

superconducting host

Energy scale $\gamma \approx 0$ Weak exchange $\gamma \approx 1$ Strong exchange

Courtesy S. Griffin (Molecular Foundry)



Nb Oxide Crystal Structures



NbO Pm3m	NbO ₂ Rutile, P4 ₂ /mnm	NbO ₂ I4 ₁ /a	N-Nb ₂ O ₅ C2/m	B-Nb ₂ O ₅ C2/c	M-Nb ₂ O ₅ I4/mmm	Nb ₂ O ₅ Amorphous
4d ³	4d ¹	4d ¹	4d ⁰	4d ⁰	4d ⁰	4d ⁰
Planar	Octahedral	Octahedral	Octahedral+ Tetrahedral	Octahedral	Octahedral+ Tetrahedral	4-, 5- and 6- coordinated
Paramagnetic	Paramagnetic	Paramagnetic	Diamagnetic	Diamagnetic	Diamagnetic	Diamagnetic

FIG. 1. Crystal structures of the Nb oxides considered in this work with their nominal valence configuration on the Nb atoms, the Nb coordination environment(s) and the resulting magnetic order in the stoichiometric case.

Sheridan, E., Harrelson, T. F., Sivonxay, E., Persson, K. A., Altoé, M. V. P., Siddiqi, I., Ogletree, D. F., Santiago, D. I., & Griffin, S. M. (2021). *Microscopic Theory of Magnetic Disorder-Induced Decoherence in Superconducting Nb Films*. <u>https://arxiv.org/abs/2111.11684</u>



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Electronic structure of NbO₂

Niobium

ΝΙΟΒΙϤΙΤΙ					low-spin filling		
Charge lo		Ionic Ra	dius (Å)				
3+		0.72			_t	_	
4+		0.68			<u>3d</u>	/	
5+		0.64			er IIII	(`````	
	Periodic T	Table	5 26 77 28 29 29 Мп Бее Со Міа Сі 5 44 60 48 ТС Ruu Rh Pd A 7 7 78 29 77 78 7 77 78 29 77 78 7 8 77 78 29 79 79 7 8 77 78 29 79 79 7 8 77 78 29 79 79 7 8 79 79 79 79 79 79 79 79 79 7 8 79 79 79 79 79 79 79 79 79 79 79 79 79	S and a second s	C N COUPER TRANS (free at a couper transformed at a c	1 = om) He No Arr Arr COOR Kr Re Re Re Re Re Re Re Re Re Re	
78	Francum Radium Actini	Rutherfa. Duthium Seatorg.	Perform Factor Methods Dermits Revenuence Pm Sm Eu Gd Th Samanum Lange Gaddini. Totak Physical Sector Se	66 67 6 Dysprosi Hadmium 98 99 CCf Es	nervium Mazzuvi Liverma Tenness og Erium Thulum Yterbum Latelium Fm Md No Lr		



octahedral coordination

~

Electronic structure of NbO₂





Electronic structure of NbO₂





Paramagnetism in Reduced Nb Pentoxides (oxygen vacancies)





Electronic Structure Origin

- Nb₁₂O₂₉ exhibits two forms with different symmetries, monoclinic (m) and orthorhombic (o)
- M-Nb₁₂O₂₉ is an unusual metallic antiferromagnetic below 12 K
- Stoner-like instability but with delocalized moments across multiple Nb sites



Fang, C. M., van Huis, M. A., Xu, Q., Cava, R. J., & Zandbergen, H. W. (2015). Unexpected origin of magnetism in monoclinic Nb₁₂O₂₉ from first-principles calculations. *Journal of Materials Chemistry C*, *3*(3), 651–657 (2015)

Modeling Nonstoichiometric Crystalline Nb_2O_{5-x} with Oxygen Defects

Oxygen vacancies

- Donates two electrons (n-type)
- Occupy conduction band (donor states)

Oxygen interstitials

- Donates two holes (p-type)
- Occupy valence band (acceptor states)





NbO ($Pm\bar{3}m$) Stabilized by π -type interaction between Nb 4d and O 2p orbitals



Modeling Nonstoichiometric Crystalline Nb₂O_{5-x} with Oxygen Defects

Rigid band model

- Pros: Simple, fast, and qualitatively correct
- Cons: Cannot account for localized defect states, structural rearrangements, polarons, etc.
- Explicit oxygen vacancies
- Pros: Explicit representation of environment around defects
- Cons: Dilute defects require large simulation cells



Sheridan, E., Harrelson, T. F., Sivonxay, E., Persson, K. A., Altoé, M. V. P., Siddiqi, I., Ogletree, D. F.,

- Santiago, D. I., & Griffin, S. M. (2021). *Microscopic Theory of Magnetic Disorder-Induced*
 - Decoherence in Superconducting Nb Films. <u>https://arxiv.org/abs/2111.11684</u>

Proposed Link: Magnetic induced Losses

- Dilute magnetic moment in superconductors can lead to 'impurity' band development in SC density of states
 - SCs have gap at the Fermi level
 - Cooper pair states below fermi level
 - Broken cooper pairs (e-) above fermi level
 - Scattering of e- leads to resistive losses
 - For large gap, thermal occupation of states above fermi level is small
 - With impurity band, these states can be more easily thermally occupied



FIG. 4. (a) The normalised superconducting density of states for a Nb film with magnetic impurities in the strong (red) [$\gamma = 0.9, \tau_s^{-1} = 0.05$] and weak (teal) [$\gamma = 0.1, \tau_s^{-1} = 0.1$] coupling limits in the vicinity of the Fermi level. (b) The real part of the current dissipation function in the corresponding limits, where the inset shows the region near the Fermi level which participates in the dissipation. For strong coupling, the decoherence is associated to *d*-channel losses, while for weak coupling it is compatible with *p*-channel losses.

Sheridan, E., Harrelson, T. F., Sivonxay, E., Persson, K. A., Altoé, M. V. P., Siddiqi, I., Ogletree, D. F., Santiago, D. I., & Griffin, S. M. (2021). *Microscopic Theory of Magnetic Disorder-Induced Decoherence in Superconducting Nb Films*. https://arxiv.org/abs/2111.11684

Proposed Link: Magnetic induced Losses

- Dilute magnetic moment in superconductors can lead to 'impurity' band development in SC density of states
- Add microscopics to phenomenological theory

Key parameters:
J: magnetic coupling strength (from DFT)
Ts: Scattering time (measured, approximated DFT)
Δ: Energy gap (measured, DFT)

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Current Dissipation Function



FIG. 4. (a) The normalised superconducting density of states for a Nb film with magnetic impurities in the strong (red) $[\gamma = 0.9, \tau_s^{-1} = 0.05]$ and weak (teal) $[\gamma = 0.1, \tau_s^{-1} = 0.1]$ coupling limits in the vicinity of the Fermi level. (b) The real part of the current dissipation function in the corresponding limits, where the inset shows the region near the Fermi level which participates in the dissipation. For strong coupling, the decoherence is associated to *d*-channel losses, while for weak coupling it is compatible with *p*-channel losses.

Sheridan, E., Harrelson, T. F., Sivonxay, E., Persson, K. A., Altoé, M. V. P., Siddiqi, I., Ogletree, D. F., Santiago, D. I., & Griffin, S. M. (2021). *Microscopic Theory of Magnetic Disorder-Induced Decoherence in Superconducting Nb Films*. https://arxiv.org/abs/2111.11684

- Various NbO_x structures
 - Bulk Crystalline
 - Bulk Amorphous







Simulating Amorphous Nb_2O_5 with DFT

• Combine simulated-annealing process with ab initio molecular dynamics (AIMD)



<u>Steps:</u>

- 1. Increase T to >3000K with expanded cell (15% expansion) (NVE)
- 2. Decrease temperature to 500 K (NVE)
- 3. AIMD at 500 K for 1-2ps (NVT)

Validation of Model

- Why should we trust simulations?
 - Elucidating the local atomic and electronic structure of amorphous oxidized superconducting niobium films. <u>Applied Physics Letters, 119(24), 244004 (2021)</u>
- Good match between simulated and experimental amorphous XAS absorption spectra



FIG. 3. (a) Calculated XAS spectra for crystalline NbO, NbO₂, and Nb₂O₅ (averaged over all three calculated phases) and XAS measurements of the O K edge of sample 1. (b) Calculated XAS spectra for crystalline Nb₂O₅ in the M-, B-, and B-phases, a representative *ab initio* generated amorphous structure, and XAS measurements of sample 1. Experimental data are normalized by rigidly shifting the spectrum to the relative scale, removing the background signal, and normalizing the heights to be comparable to our XAS calculations.



Implications of Magnetic-Induced Losses

- d-band moments (on Nb atoms from oxygen vacancies) lead to impurity band states in the SC DOS
 - There thermal occupation leads to additional dissipation channels (YSR dissipation)
- p-band moments (on O atoms from oxygen interstitials) do not lead to impurity band states
- Mitigation strategies

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- Need to fill oxygen vacancies (annealing, surface passivation, etc.)
- Remove native oxides completely

Sheridan, E., Harrelson, T. F., Sivonxay, E., Persson, K. A., Altoé, M. V. P., Siddiqi, I., Ogletree, D. F., Santiago, D. I., & Griffin, S. M. (2021). *Microscopic Theory of Magnetic Disorder-Induced Decoherence in Superconducting Nb Films*. https://arxiv.org/abs/2111.11684



Papers for More Information

Sheridan Nb_2O_5 magnetism and structure

- Sheridan, E., Harrelson, T. F., Sivonxay, E., Persson, K. A., Altoé, M. V. P., Siddiqi, I., Ogletree, D. F., Santiago, D. I., & Griffin, S. M. (2021). *Microscopic Theory of Magnetic Disorder-Induced Decoherence in Superconducting Nb Films*. <u>https://arxiv.org/abs/2111.11684</u>
- Elucidating the local atomic and electronic structure of amorphous oxidized superconducting niobium films. <u>Applied</u> <u>Physics Letters</u>, <u>119(24)</u>, 244004 (2021)

Nb₂O₅ Crystalline paramagnetism and electronic structure origin of moments

- Electrical and magnetic properties of Nb₂O_{5-δ} crystallographic shear structures. <u>Physical Review B</u>, 44(13), 6973– 6981 (1991)
- Fang, C. M., van Huis, M. A., Xu, Q., Cava, R. J., & Zandbergen, H. W. (2015). Unexpected origin of magnetism in monoclinic Nb₁₂O₂₉ from first-principles calculations. *Journal of Materials Chemistry C*, 3(3), 651–657 (2015)

Nb₂O₅ structure in resonators

- Localization and Mitigation of Loss in Niobium Superconducting Circuits, <u>PRX Quantum 3, 020312 (2022)</u>
 Lambda Ta₂O₅
- Hidden Structural Order in Orthorhombic Ta₂O₅, <u>Phys. Rev. Lett. 110, 235502 (2013)</u>

Stephenson Roth Phase

• Structural systematics in the binary system Ta2O₅-WO₃, <u>Acta Cryst. B27, 1037-1044 (1971)</u>



Agenda

- SC Qubit Materials and Systems Charts Introduction
- Modeling Materials
 - Model Formulation
 - Electronic Structure Models
 - Atomistic Models
 - From Phenomenological to Microscopic
- Use Cases
 - Nb and its hydrides
 - Nb and its oxides
- Co-Design and Integration with Experimentation Summary



Integrated theoretical, computational & experimental approaches

Advance novel experimental methods guided by systems design charts

PROCESSING

STRUCTURE

PROPERTIES

PERFORMANCE

ARCHITECTURE

- Fuse simulations at multiple length scales with phenomenological models
- Computationally assess mitigation strategies for identified decoherence mechanisms and ensure industry compatible
- Streamline data acquisition and analysis for rapid model assessments







Thank you!

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MATERIALS THEORY AND DESIGN GROUP

