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# $\nu$ -Nucleus Scattering Systematics: Interplay of Neutrino Flux, Cross sections and Nuclear Effects

Jorge G. Morfín – Fermilab  
SLAC Neutrino Workshop – March, 2013

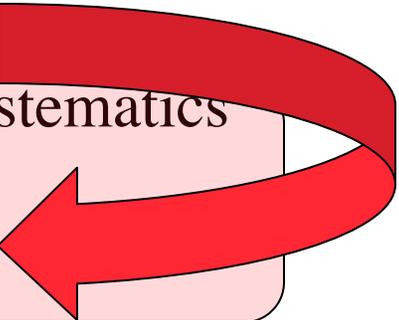
# Neutrino Experimental Systematics

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- ◆ Detector Systematics:
  - ▼ Muon energy scale
  - ▼ Hadron energy scale
  - ▼ Muon tracking – reconstruction
  - ▼ Neutron and proton response
  - ▼ Target mass
  - ▼ Cross-talk
  - ▼ .....
- ◆ Flux Systematics
- ◆ Interaction Model Systematics
  - ▼ Cross section
  - ▼ Nuclear Effects

# Neutrino Experimental Systematics

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    - ▼ .....
  - ◆ **Flux Systematics**
  - ◆ **Interaction Model Systematics**
    - ▼ Cross section
    - ▼ Nuclear Effects
- 
- A thick red ribbon starts from the right side of the 'Flux Systematics' box and loops around to point towards the 'Interaction Model Systematics' box, indicating a relationship or flow between these two categories.

# Neutrino Nucleus Scattering

What do we observe in our detectors?

- ◆ The events we observe in our detectors are convolutions of:

$$Y_{c\text{-like}}(E) \propto \phi(E' \geq E) \otimes \sigma_{c,d,e..}(E' \geq E) \otimes \text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E)$$

- ◆  $Y_{c\text{-like}}(E)$  is the event energy and channel / topology of the event observed in the detector. It is called c-like since it appears to be channel c but may not have been channel c at interaction.
- ◆ That is the topology measured in the detector is what we observe in the detector and not necessarily what was produced at the initial interaction.
- ◆ The energy E is not given by knowing the E of the incoming particle as in charged particle scattering, but is the sum of energies coming out of the nucleus and measured in the detector.

# Neutrino Nucleus Scattering

What do we observe in our detectors?

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- ◆ The events we observe in our detectors are convolutions of:

$$Y_{c\text{-like}}(E) \propto \boxed{\phi(E' \geq E)} \otimes \sigma_{c,d,e..}(E' \geq E) \otimes \text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E)$$

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- ◆  $\phi(E)$  is the energy dependent neutrino flux that enters the detector.
- ◆ With traditional meson-decay-source neutrino beams we can, with considerable effort, estimate the incoming neutrino energy distribution to  $\leq 10\%$  absolute and  $\leq 7\%$  energy bin-to-bin accuracy. **Significant contribution to systematics.**
- ◆ With muon-decay-source neutrino beams (NuSTORM and Neutrino Factory) we could know the **energy dependent absolute flux to order 1%**.

# Neutrino Nucleus Scattering

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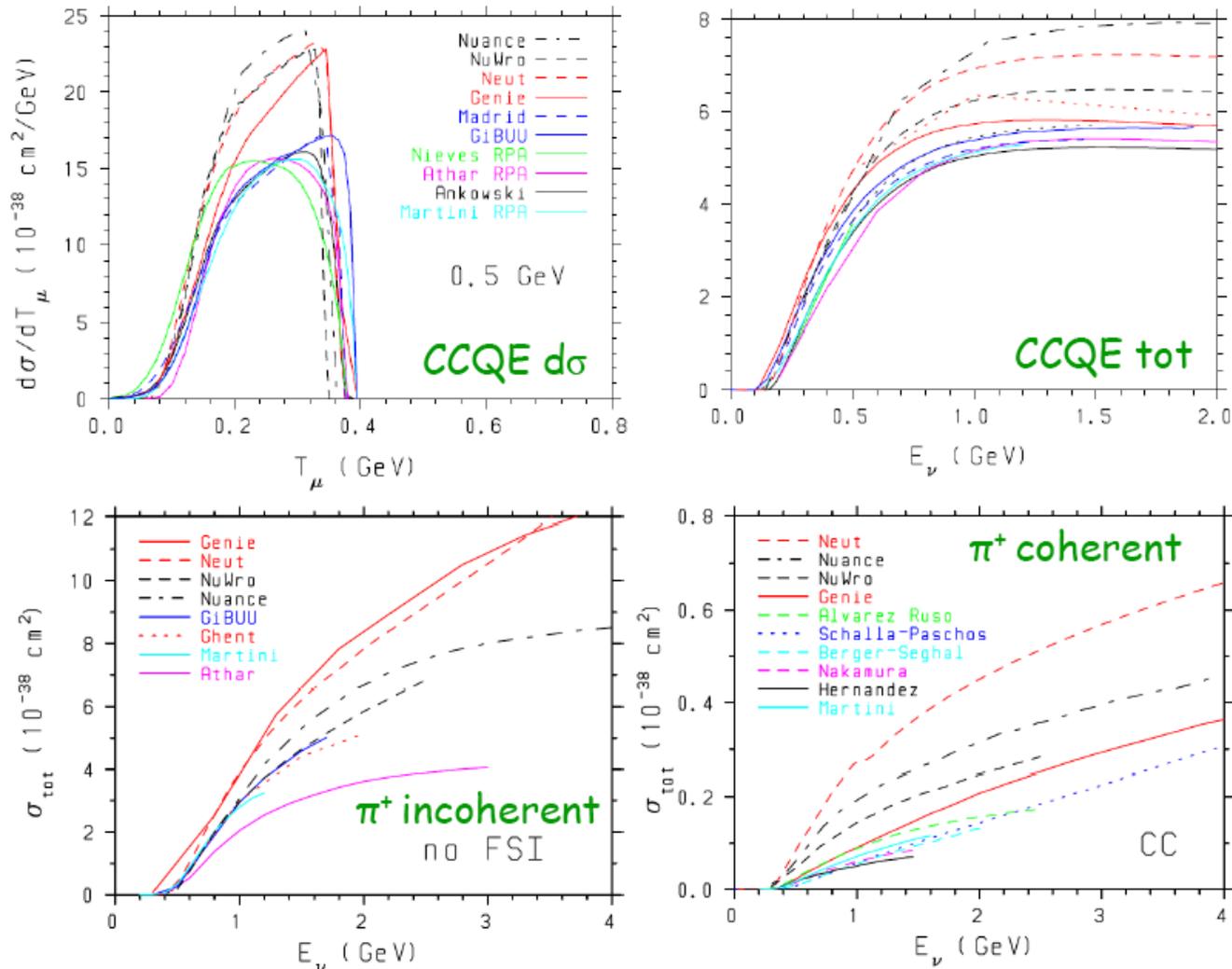
$$Y_{c\text{-like}}(E) \propto \phi(E' \geq E) \otimes \sigma_{c,d,e..}(E' \geq E) \otimes \text{Nuc}_{c,d,e..\rightarrow c}(E' \geq E)$$

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- ◆  $\sigma_{c,d,e..}(E' \geq E)$  is the measured or the Monte Carlo (model) energy dependent neutrino cross section off a **nucleon within a nucleus**.
- ◆ Form factors are modified within a nucleus compared to a nucleon. Analogous to the difference between PDFs and nuclear NPDFs
- ◆ The width of resonances, i.e the  $\Delta$ , changes within a nucleus.
- ◆ **Significant contribution to systematics.**

# Range of Existing Model (MC) Predictions off C

NuInt09 – Steve Dytman



Jorge G. Morfín - Fermilab

# Neutrino Nucleus Scattering

What do we observe in our detectors?

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$$Y_{c\text{-like}}(E) \propto \phi(E' \geq E) \otimes \sigma_{c,d,e..}(E' \geq E) \otimes \text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E)$$

- ◆  **$\text{Nuc}_{c,d,e.. \rightarrow c}(E' \geq E)$  – Nuclear Effects**

- ◆ In contemporary neutrino experiments the interactions do not occur on a free nucleon but rather nucleon(s) within a nucleus and there are many nuclear effects that have to be considered.
- ◆ In general the interaction of a neutrino with energy  $E'$  creating initial channel  $d,e...$  can appear in our detector as energy  $E$  and channel  $c$ .
- ◆ **Nuclear Effects** – a migration matrix that mixes produced/observed channels and energy. **Significant contribution to systematics.**
- ◆ A bit tricky to measure the cross section off a nucleon within a nucleus because of these nuclear effects.

# What are these Nuclear Effects $\text{Nuc}_{c,d,e.. \rightarrow c} (E' \geq E)$ in Neutrino Nucleus Interactions? (Partial List)

- ◆ Target nucleon in motion – classical Fermi gas model or the superior spectral functions (Benhar et al.)
- ◆ Multi-nucleon initial states: Short-range correlations, meson exchange currents.
- ◆ Form factors, structure functions, resonance widths, parton distribution functions and, consequently, cross sections are modified within the nuclear environment. (Butkevich / Kulagin, Tsushima et al., Kovarik et al.)
- ◆ Produced topologies are modified by final-state interactions modifying topologies and possibly reducing **detected** energy.
  - ▼ Convolution of  $\delta\sigma(n\pi)$  (x) formation zone uncertainties (x)  $\pi$ -charge-exchange/absorption probabilities and nuclear density uncertainties.
- ◆ **Systematics associated with each of these effects.**
  - ◆ Monte Carlos – like GENIE – try to include all these effects.  
**GENIE needs improvements! GENIE group needs additional help from the community.**

# Example Model Uncertainties

## Cross Section Model Uncertainties

Uncertainty	1 $\sigma$
$M_A$ (Elastic Scattering)	$\pm 25\%$
$F_A$ (Elastic scattering)	$\pm 30\%$
$M_A$ (CCQE Scattering)	+25% -15%
CCQE Normalization	+20% -15%
CCQE Vector Form factor model	on/off
CC Resonance Normalization	$\pm 20\%$
$M_A$ (Resonance Production)	$\pm 20\%$
$M_V$ (Resonance Production)	$\pm 10\%$
1pi production from $\nu p / \bar{\nu} n$ non-resonant interactions	$\pm 50\%$
1pi production from $\nu n / \bar{\nu} p$ non-resonant interactions	$\pm 50\%$
2pi production from $\nu p / \bar{\nu} n$ non-resonant interactions	$\pm 50\%$
2pi production from $\nu n / \bar{\nu} p$ non-resonant interactions	$\pm 50\%$
Modtly Pauli blocking (CCQE) at low $Q^2$ (change PB momentum threshold)	$\pm 30\%$

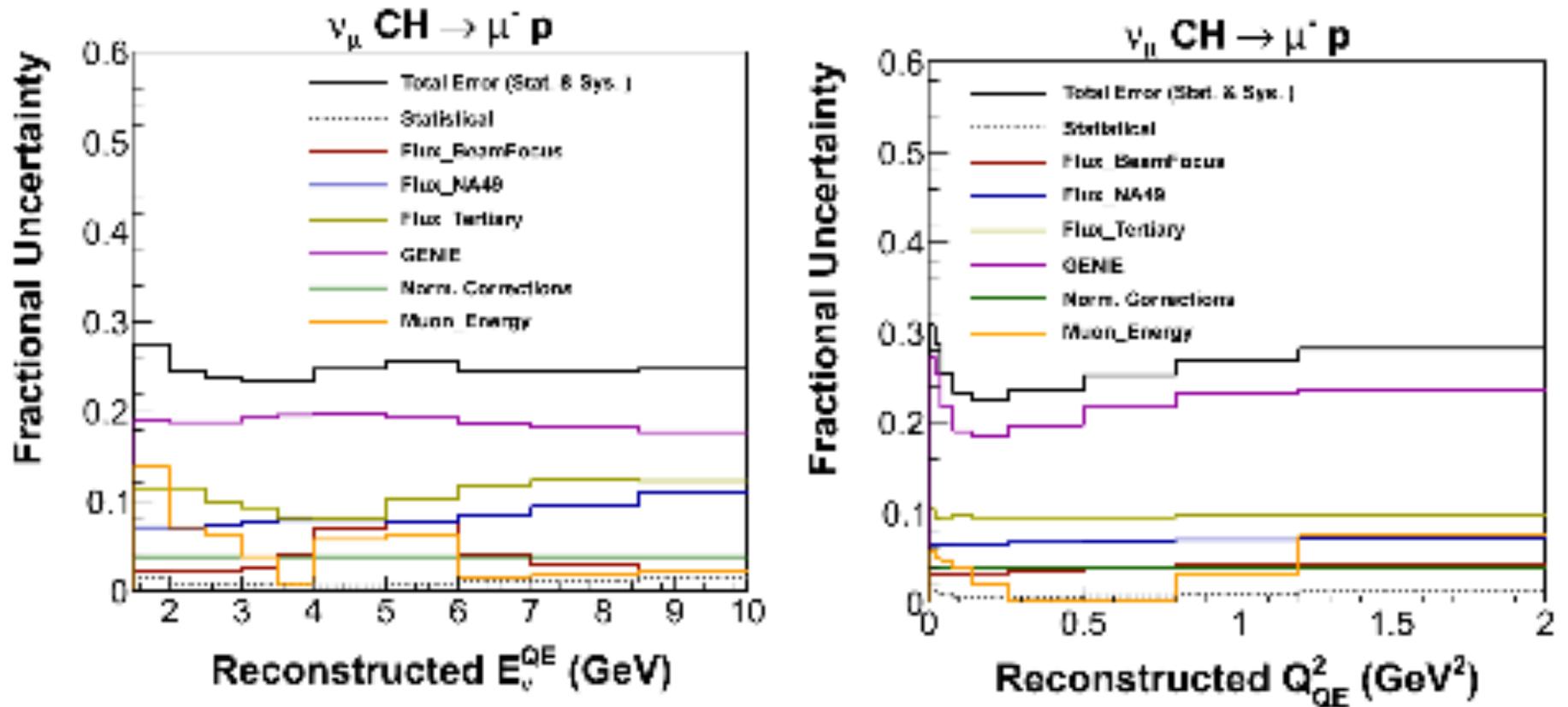
## Intranuclear Rescattering Uncertainties

Uncertainty	1 $\sigma$
Pion mean free path	$\pm 20\%$
Nucleon mean free path	$\pm 20\%$
Pion fates – absorption	$\pm 30\%$
Pion fates – charge exchange	$\pm 50\%$
Pion fates – Elastic	$\pm 10\%$
Pion fates – Inelastic	$\pm 40\%$
Pion fates – pion production	$\pm 20\%$
Nucleon fates – charge exchange	$\pm 50\%$
Nucleon fates – Elastic	$\pm 30\%$
Nucleon fates – Inelastic	$\pm 40\%$
Nucleon fates – absorption	$\pm 20\%$
Nucleon fates – pion production	$\pm 20\%$
AGKY hadronization model – $x_T$ distribution	$\pm 20\%$
Delta decay angular distribution	On/off
Resonance decay branching ratio to photon	$\pm 50\%$

Hugh Gallagher

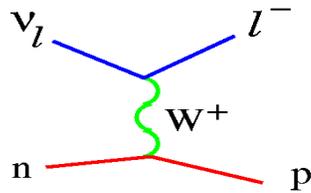
References: (1) [www.genie-mc.org](http://www.genie-mc.org), (2) arXiv:0806.2119, (3) D. Bhattacharya, Ph. D Thesis (U. Pittsburgh) 2009.

# Example: Uncertainty on Exclusive Prediction



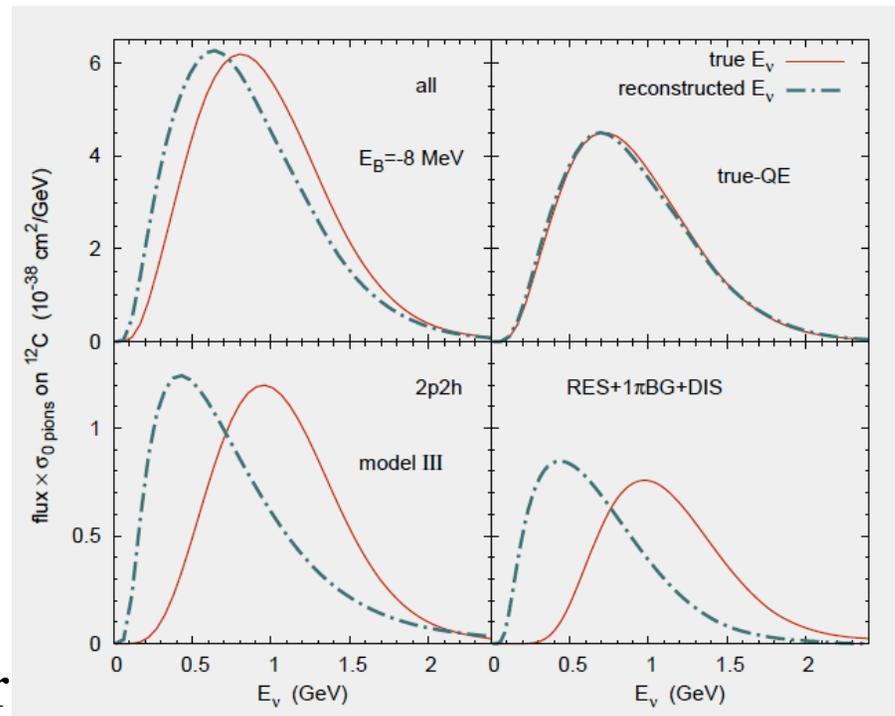
# Nuclear Effects can Change the Energy Reconstruction for “QE” Events

- In pure QE scattering on nucleon at rest, the outgoing lepton can determine the neutrino energy:



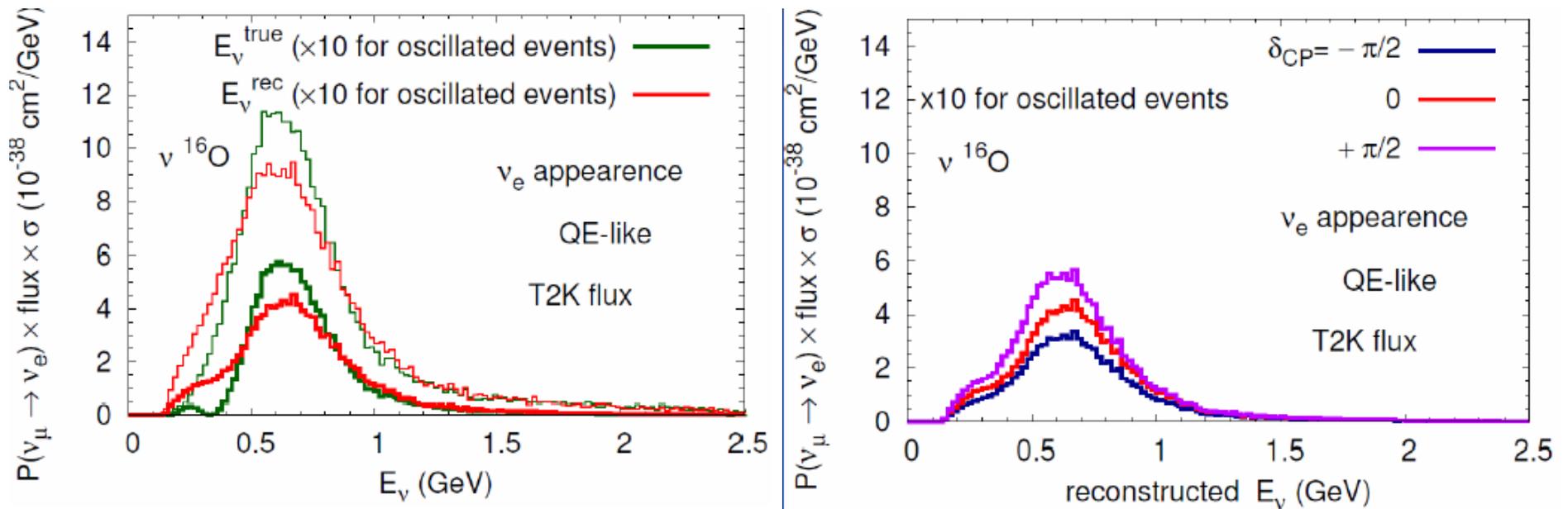
$$E_\nu = \frac{2M_N E_\mu - m_\mu^2}{2(M_N - E_\mu + p_\mu \cos \theta_\mu)}$$

**However,** all neutrino oscillation experiments contain nuclei as targets. Reconstructed energy shifted to lower energies for all processes other than true QE off nucleon at rest



# Nuclear Effects and Oscillation Measurements

Ulrich Mosel using his Giessen Boltzmann-Uehling-Uhlenbeck (GiBUU) Transport Model looking at T2K



# A Nuclear Theorist's View

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From Ulrich Mosel – Nuclear Theorist from University of Giessen, Germany

**.... these neutrino experiments are - from a nuclear physicist's point of view - unique in the sense that their analysis has to rely on nuclear structure and nuclear reaction theory more so than any other nuclear physics experiment that I know of ( the closest is the extraction of properties of the quark-gluon plasma from ultra-relativistic heavy ion collisions)**

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← effective  $\sigma_c^A(E)$

- ◆ Experimentally, the last two terms convoluting the initial nucleon (within a nucleus) cross section and nuclear effects are combined into an effective cross section  $\sigma_c^A(E)$ .
- ◆ Note that the **effective cross section  $\sigma_c^A(E)$  measured depends on the incoming neutrino energy spectrum and the involved nuclear effects that populate the yield  $Y_c^A(E)$ .**
- ◆ This implies that, for example, the effective  $\sigma_{\pi^0}^C(1 \text{ GeV})$  measured in the MiniBooNE Booster beam **will be different** than the same effective  $\sigma_{\pi^0}^C(1 \text{ GeV})$  observed by MINERvA in the higher energy NuMI beam due to, for example, more feed down from multi-pi events via pion absorption in the NuMI beam.

# Significant Implications for Oscillation Experiments

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- ◆ Can not simply plug in effective  $\sigma_{\pi 0}^A$  from experiments in a significantly different beam.
- ◆ In a two-detector oscillation experiment the neutrino flux entering the far detector is altered from the neutrino flux at the near detector due to oscillations.
- ◆ The  $\sigma_c^A(E)$  effective that should be applied to expectations (Monte Carlo) at the far detector is NOT the same as that which we would measure at the near detector.  
**However, the near detector results give us an excellent starting point for calculating the difference.**
- ◆ **The convoluted  $\phi(E' \geq E)$   $\otimes$   $\sigma(E)$   $\otimes$  Nuc( $E' \geq E$ ) systematics need to be correctly incorporated in determining the systematics of oscillation parameter measurements.**

# Summary and Conclusions

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- ◆ Nuclear effects, present in the data of all contemporary neutrino oscillation experiments, **mixes channels and changes energy between produced and final (observed) states.**
- ◆ Nuclear effects couples with the initial cross section and incoming neutrino spectrum such that an observed result for a specific channel from one detector does not transfer to another detector unless they are using the same nucleus AND **same neutrino beam. What is a “standard candle”?**
- ◆ GENIE generator that tries to model these coupled effects **needs additional help.**
- ◆ To untangle these effects experimentally, a significant step forward would be a **high-statistics neutrino-hydrogen /deuterium experiment in a neutrino beam with a flux that we know to  $\approx 1\%$  such as from NuSTORM or NuFact.**

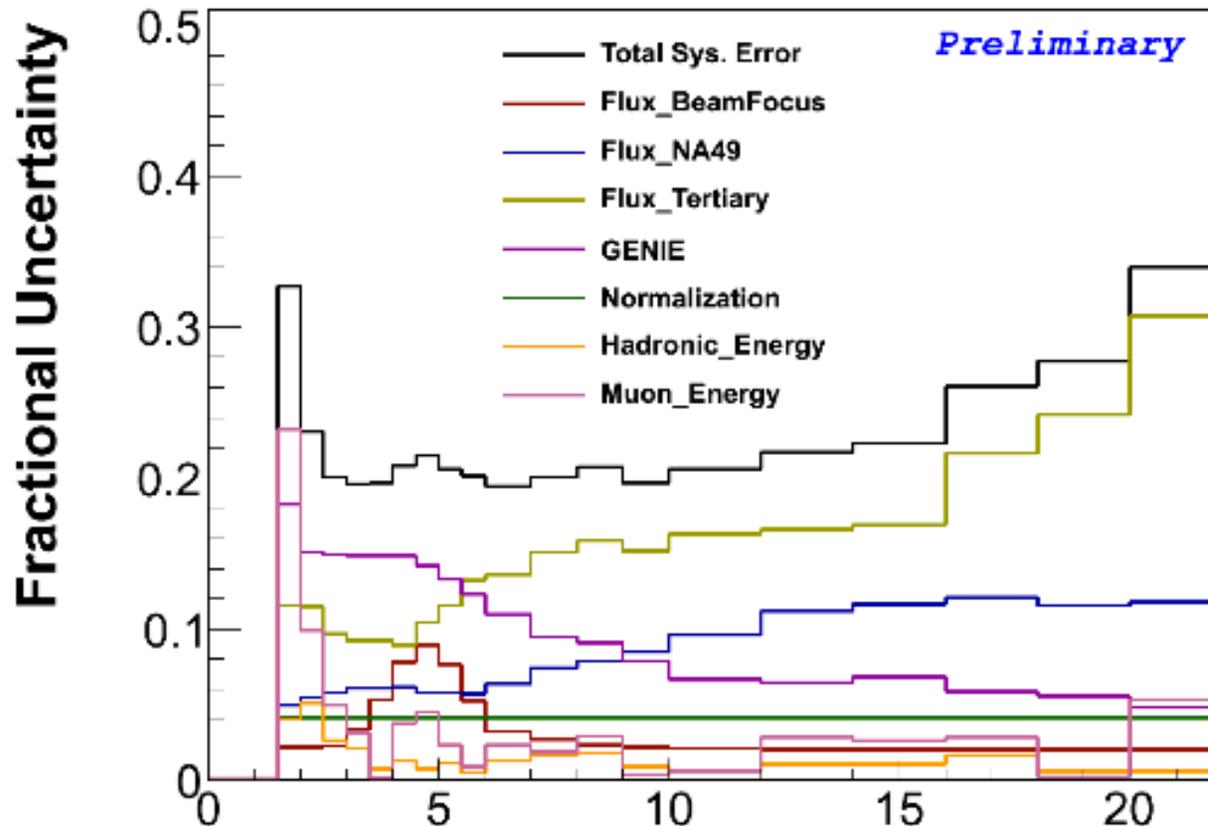
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- ◆ **The U. S. neutrino physics community is in need of a significant increase of neutrino physics phenomenologists. Currently, need to go to Europe where a thriving phenomenologists community exists.**

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# Backup

# Example: Uncertainty on an Inclusive Prediction

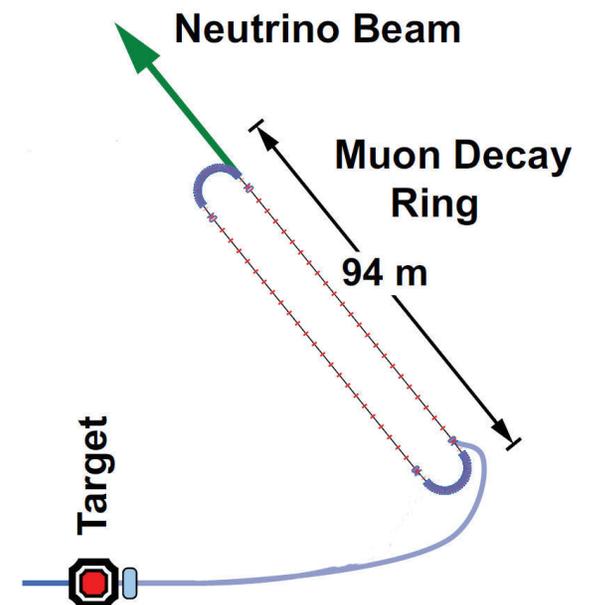
## Uncertainty on the energy spectrum from Fe



# Can we Actually MEASURE these Differences in the 0.5 – 4 GeV region

## $\nu$ STORM Neutrinos from Stored Muons

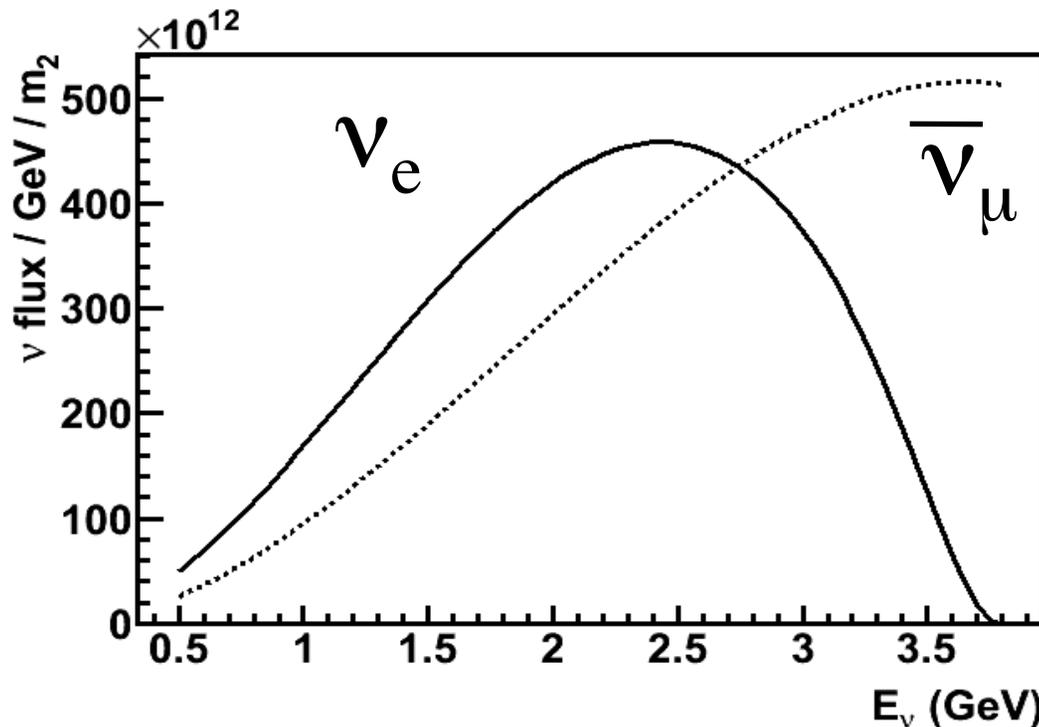
- ◆ High-Precision  $\nu$  interaction physics program.
- ▼ The  $\nu$ STORM beam will provide a very well-known ( $\delta \phi(E) \approx 1\%$ ) beam of  $\nu$  and  $\bar{\nu}$ .
  - ▼  $\nu_e$  and  $\bar{\nu}_e$  cross-section measurements.
  - ▼  $\nu_\mu$  and  $\bar{\nu}_\mu$  cross-section measurements
- ◆ Address the large  $\Delta m^2$  oscillation regime, make major contribution to the study of sterile neutrinos.
  - ▼ Either allow for precision study (in many channels), if they exist in this regime.
  - ▼ Or greatly expand the dis-allowed region.
- ◆ Provide a  $\mu$  decay ring test demonstration and  $\mu$  beam diagnostics test bed.
- ◆ Provide a precisely understood  $\nu$  beam for detector studies.
- ◆ **Change the conception of the neutrino factory.**



# The $\nu$ STORM Neutrino Beam



- ◆ A high-intensity source of  $\nu_e$  events for experiments.



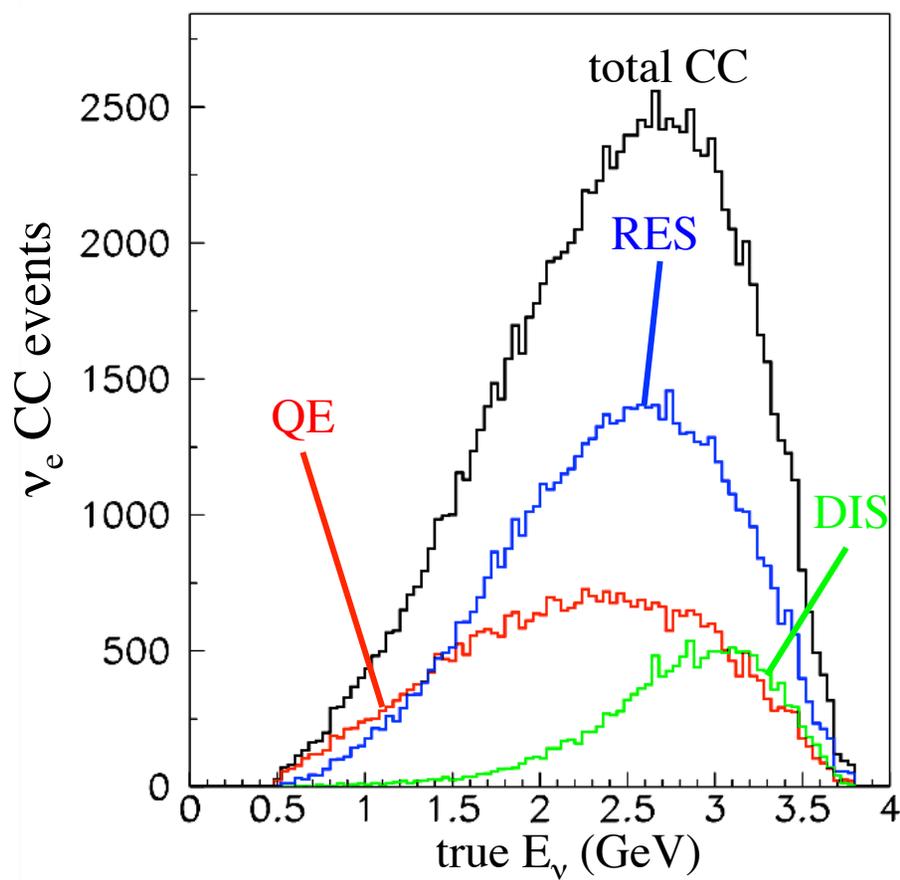
3.8 GeV  $\mu^+$  stored, 150m straight, flux at 100m  
*(thanks to Sam Zeller and Chris Tunnell!)*

$\mu^+$		$\mu^-$	
Channel	$N_{\text{evts}}$	Channel	$N_{\text{evts}}$
$\bar{\nu}_\mu$ NC	844,793	$\bar{\nu}_e$ NC	709,576
$\nu_e$ NC	1,387,698	$\nu_\mu$ NC	1,584,003
$\bar{\nu}_\mu$ CC	2,145,632	$\bar{\nu}_e$ CC	1,784,099
$\nu_e$ CC	3,960,421	$\nu_\mu$ CC	4,626,480

event rates per 1E21 POT -  
 100 tons at 50m

# $\nu_e$ Event Fractions in $\nu$ STORM

- ◆  $\nu_e$  produced by 3.8 GeV  $\mu^+$  beam.



**out of the  
CC modes:**

\* 56%

resonant

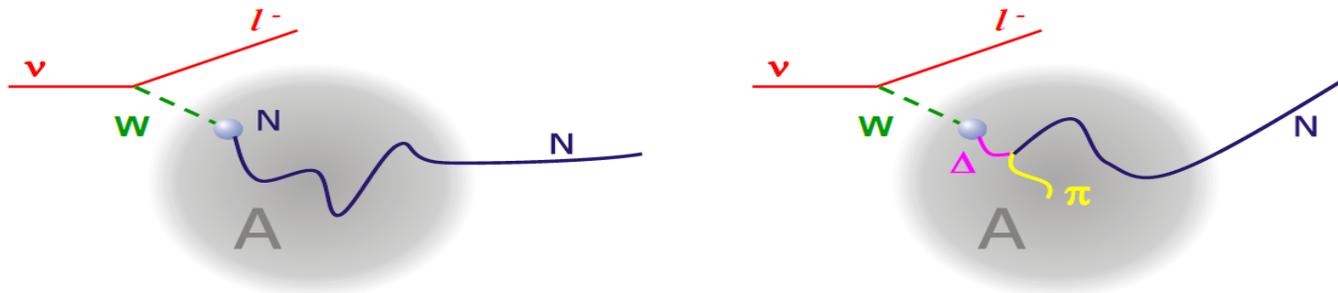
\* 32% QE

\* 12% DIS

- ◆ For  $\bar{\nu}_e$  sample, 52% resonant, 40% QE, 8% DIS)

# Final State Interactions can mimic a QE event

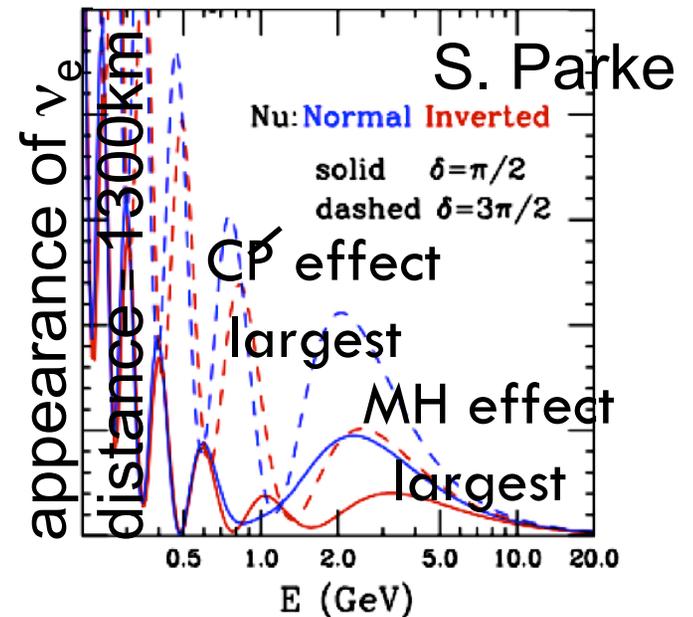
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- ◆ Define a class of events as “**QE-like**” that have the apparent topology but can have been produced as something other than QE.

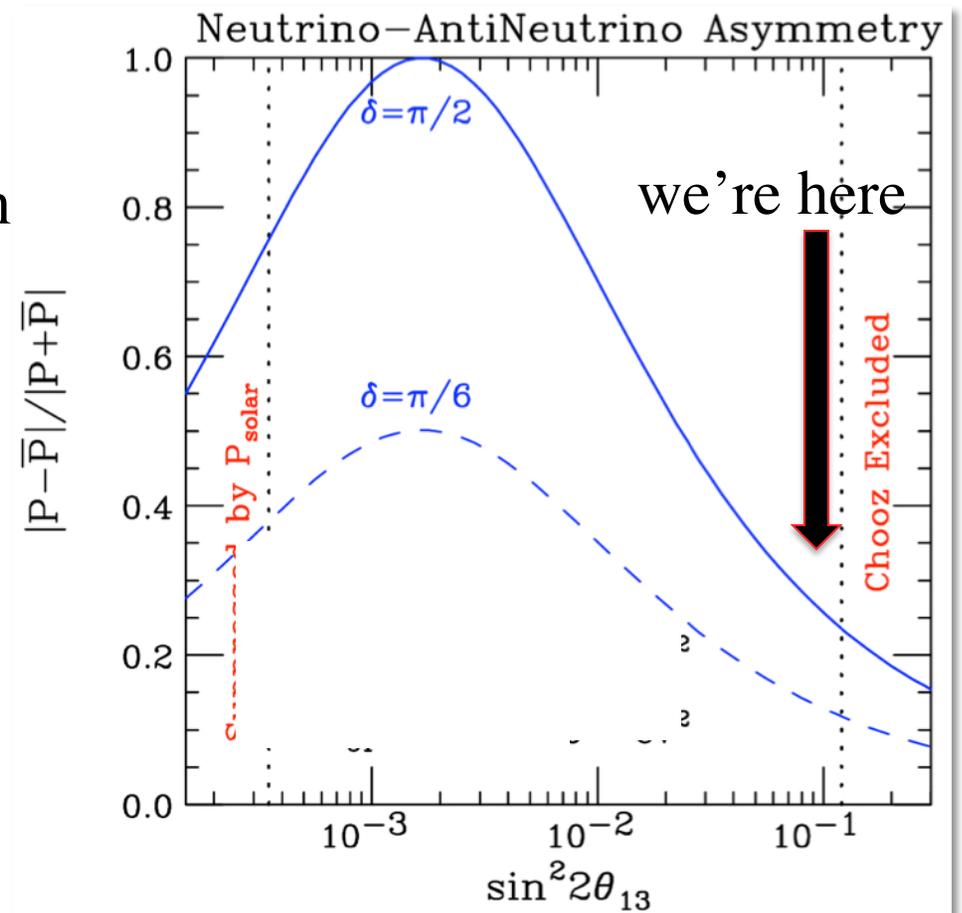
# Why are $\nu_e$ Cross Sections Important?

- ◆  $\nu_e$  A – scattering results are interesting on their own.
- ◆ Recent determination of large  $\theta_{13}$  has opened up possibilities of
  - ▼ Determining  $\nu$  mass ordering.
  - ▼ Searching for CP-violation in the  $\nu$  sector.
- ◆ To be sensitive to these effects, current/near-future long-baseline experiments will be looking for  $\nu_\mu$  to  $\nu_e$  and  $\bar{\nu}_\mu$  to  $\bar{\nu}_e$  oscillations over a range of energies.
- ◆ These will no longer be only “counting” experiments but rather will depend on observing distortions in the far detectors neutrino energy spectrum in **both neutrino and anti-neutrino samples**



# Why are $\nu_e$ and $\bar{\nu}_e$ Cross Sections Important?

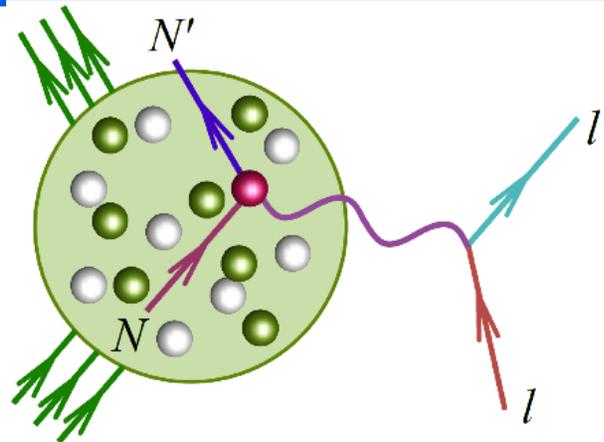
- ◆ Large  $\theta_{13}$  means we could have reasonable statistics.
- ◆ However, as the now-well-known plot at right suggests, the asymmetry between  $\nu$  and  $\bar{\nu}$  will be small and the goal of constraining the range of  $\delta$  will demand minimal systematic errors.
- ◆ One of these systematics will be our knowledge of  $\nu_e$  and  $\bar{\nu}_e$  cross sections in the relevant energy range.



(not including matter effects & backgrounds)  
(S. Parke)

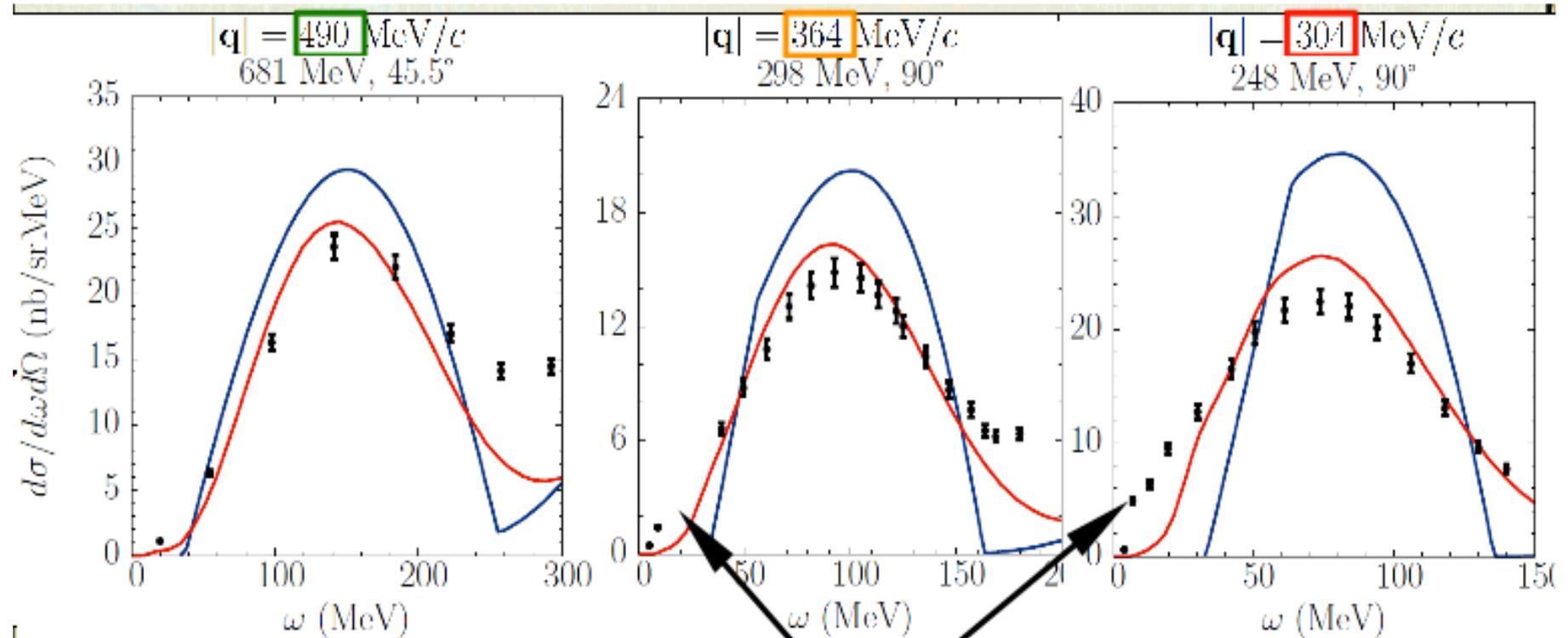


# Target Nucleon in Motion – Classical Fermi Gas Model or the Superior Spectral Functions



- ◆ Impulse Approximation (IA) – nucleus treated as a collection of independent nucleons – no collective excitations
  - ▼ breaks down as  $Q$  decreases with spatial resolution decreasing as  $1/Q$
- ◆ In the IA the nucleus is fully described by its spectral function
  - ▼ The spectral function gives the distribution of momenta and energies of the nucleons inside the nucleus
- ◆ The original model to describe this distribution is the Fermi Gas model

# Spectral Function Approach Superior – Particularly as Q Decreases



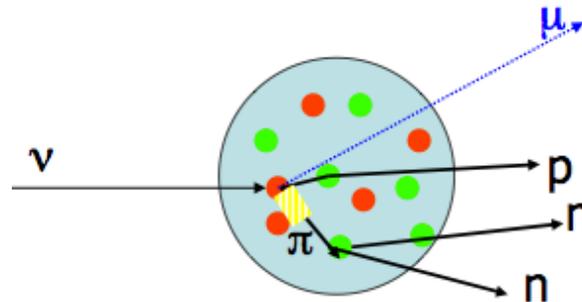
**Spectral function**

**Fermi gas**

When  $|q| \leq 400 \text{ MeV}$  two- and few-nucleon contributions appear

Artur Ankowski  
NuInt09

# Final State Interactions (FSI)

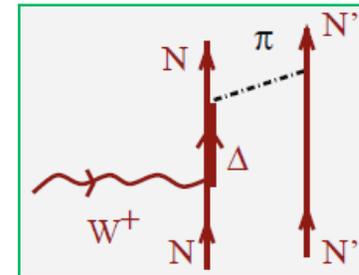
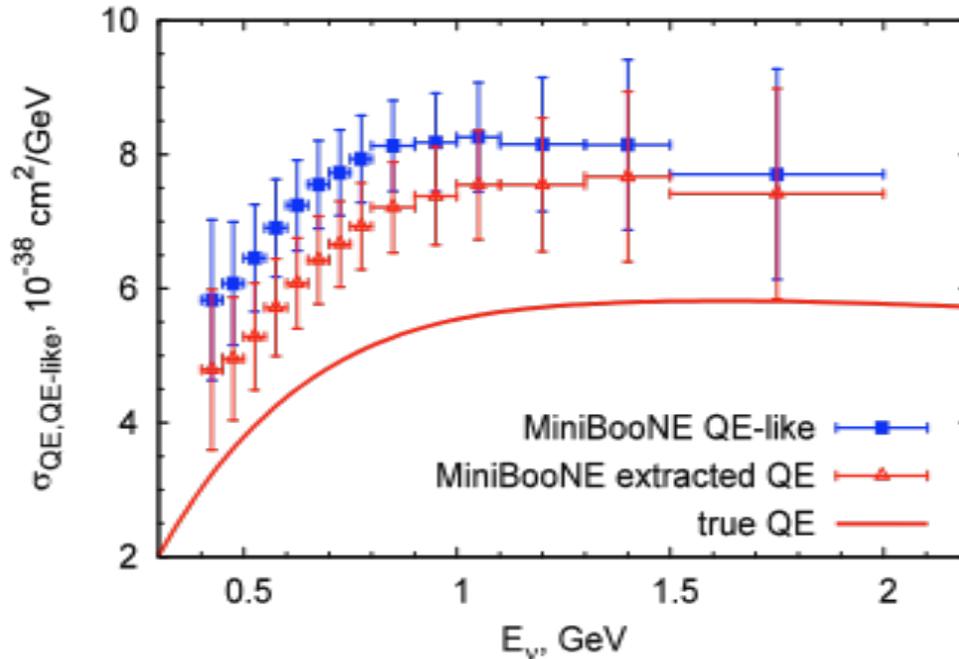


- ◆ Components of the initial hadron shower interact within the nucleus changing the apparent final state configuration and even the detected energy.
- ◆ For example, an initial pion can charge exchange or be absorbed on a pair of nucleons and an initial nucleon can scatter producing a pion

Example numbers	Final $\mu$ $p$	Final $\mu$ $p$ $\pi$
Initial $\mu$ $p$	90%	10%
Initial $\mu$ $p$ $\pi$	25%	75%

# Attempt to Remove Resonance Background

## MiniBooNE Experiment example

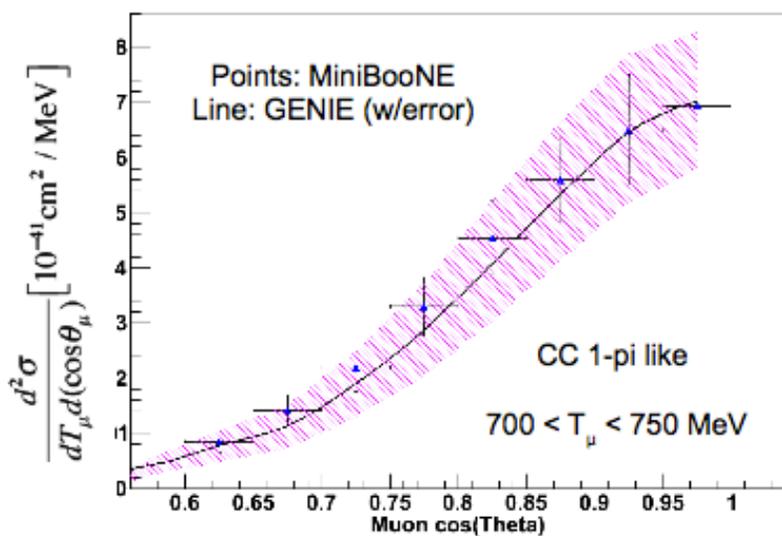


Event generator – a particular model - is used to remove QE-like background (pion absorption) from QE-like Xsect (blue) yielding an extracted QE Xsect (red)  $\rightarrow$  large pion absorption model dependence of QE result.

# Example: Interplay of Cross section and Nuclear Effects

## ► Challenges to QE analyses at MINERvA:

Laura Fields, NuInt12



► Measurements depend heavily on the simulation of backgrounds, obtained from GENIE:

- QEL: BBA05 FF,  $M_A = 0.99$  GeV
- Resonance: Rein-Segal
- Coherent: Rein-Segal
- DIS: GRV94/GRV98 with Bodek-Yang
- DIS & QEL charm (Kovalenko, Sov.J.Nucl.Phys.52:934 (1990))

### Nuclear Model

RFGM with NN correlations

Hadronization Model: AGKY – transitions between KNO-based and JETSET T. Yang, AIP Conf. Proc.967:269-275 (2007)

Formation zone: SKAT  $\mu^2 = 0.08$  GeV<sup>2</sup>

Intranuclear Rescattering: cascade model; INTRANUKE-hA (S. Dytman, AIP Conf Proc, 896, pp. 178-184 (2007)) anchored to  $\pi, p/n$ -Fe data

- ◆ **Improvements to GENIE are severely man-power limited!  
GENIE group needs additional help from the community.**