

# Testing Inflation with Large-Scale Structure (LSS)

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# Vanilla\* inflation predicts:

- Flat universe ( $\Omega_K=1$ ) with nearly scale-invariant fluctuation spectrum ( $n_s \approx 1-6\epsilon+2\eta$ )
- Stochastic background of gravity waves
- Nearly gaussian density fluctuations
- Homogeneous and isotropic universe

Any departures (as well as measurements of  $n_s$ )  
shed direct light on inflation

\*Single scalar field, canonical kinetic term, in Bunch-Davies vacuum, always slow-rolls, in Einstein GR

# LSS: an under-utilized probe of the early universe

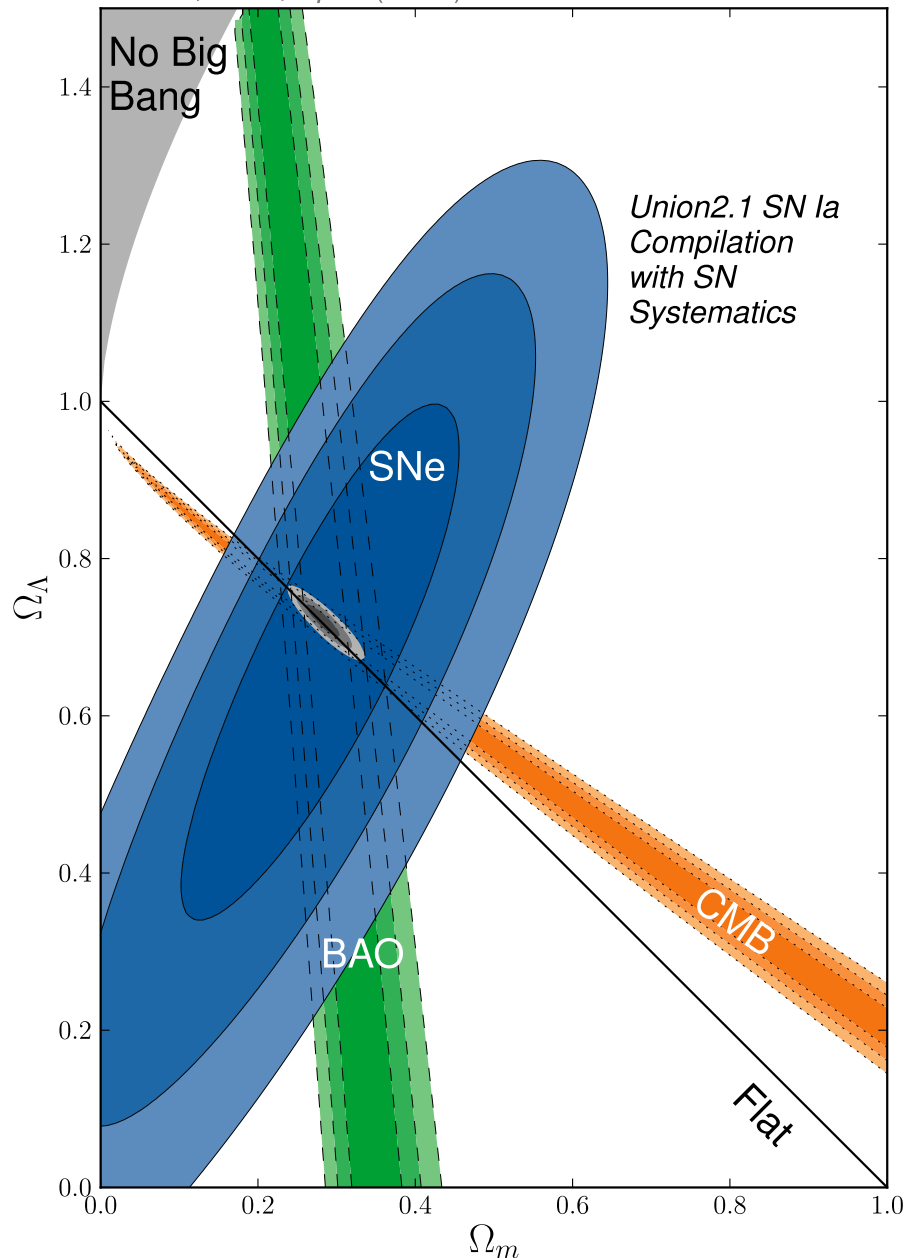
	CMB	LSS
dimension	2D	3D
# modes	$\propto l_{\text{max}}^2$	$\propto k_{\text{max}}^3$
systematics & selection func.	relatively clean	relatively messy
temporal evol.	no	yes
slice vs. color, M, bias...	no	yes

# LSS and inflationary cosmological parameters

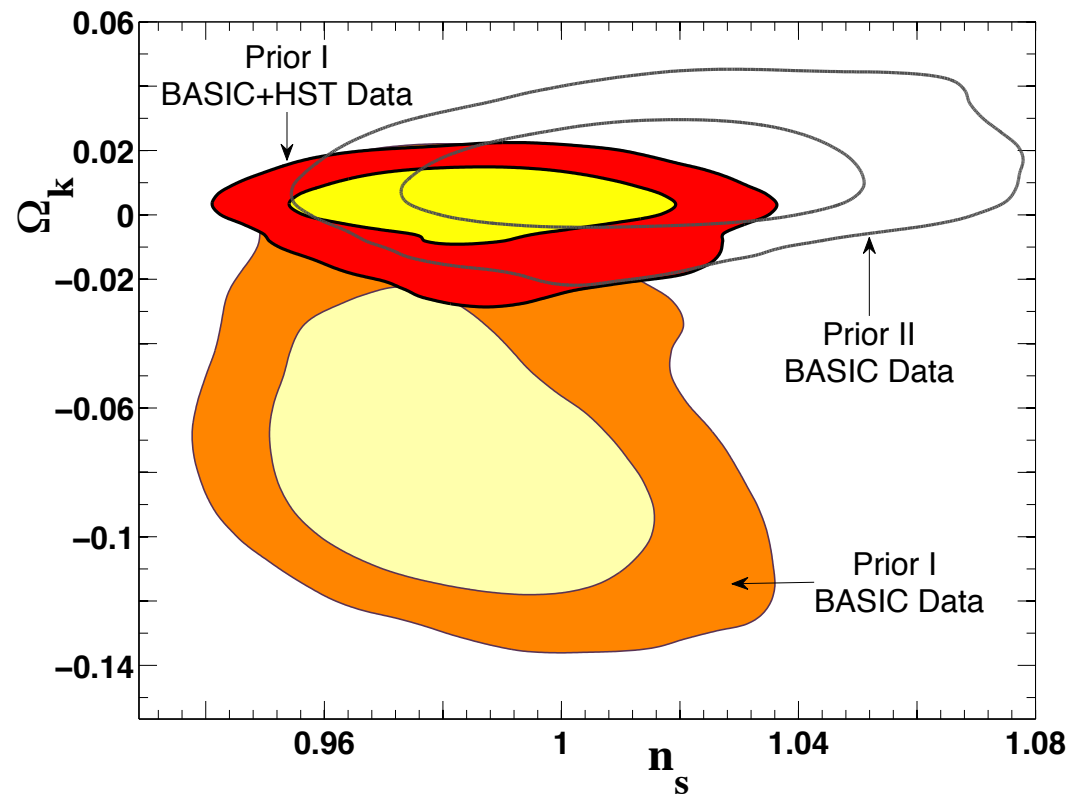
# Spatial Curvature:

## LSS helps break parameter degeneracies

Supernova Cosmology Project  
Suzuki, et al., *Ap.J.* (2011)

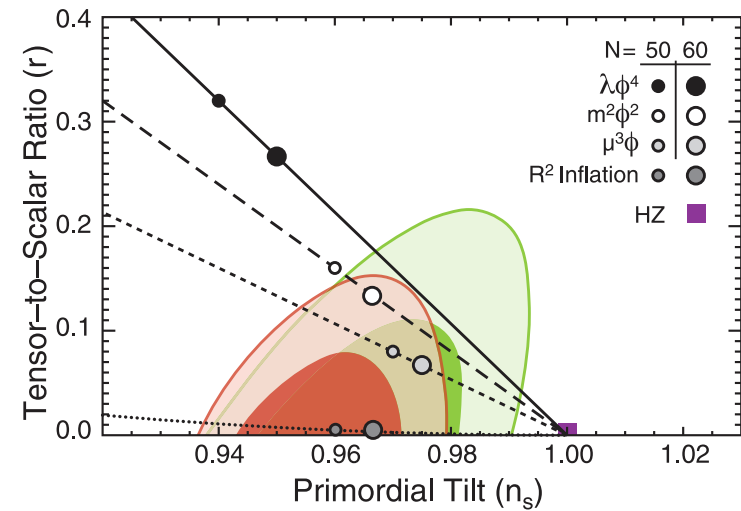
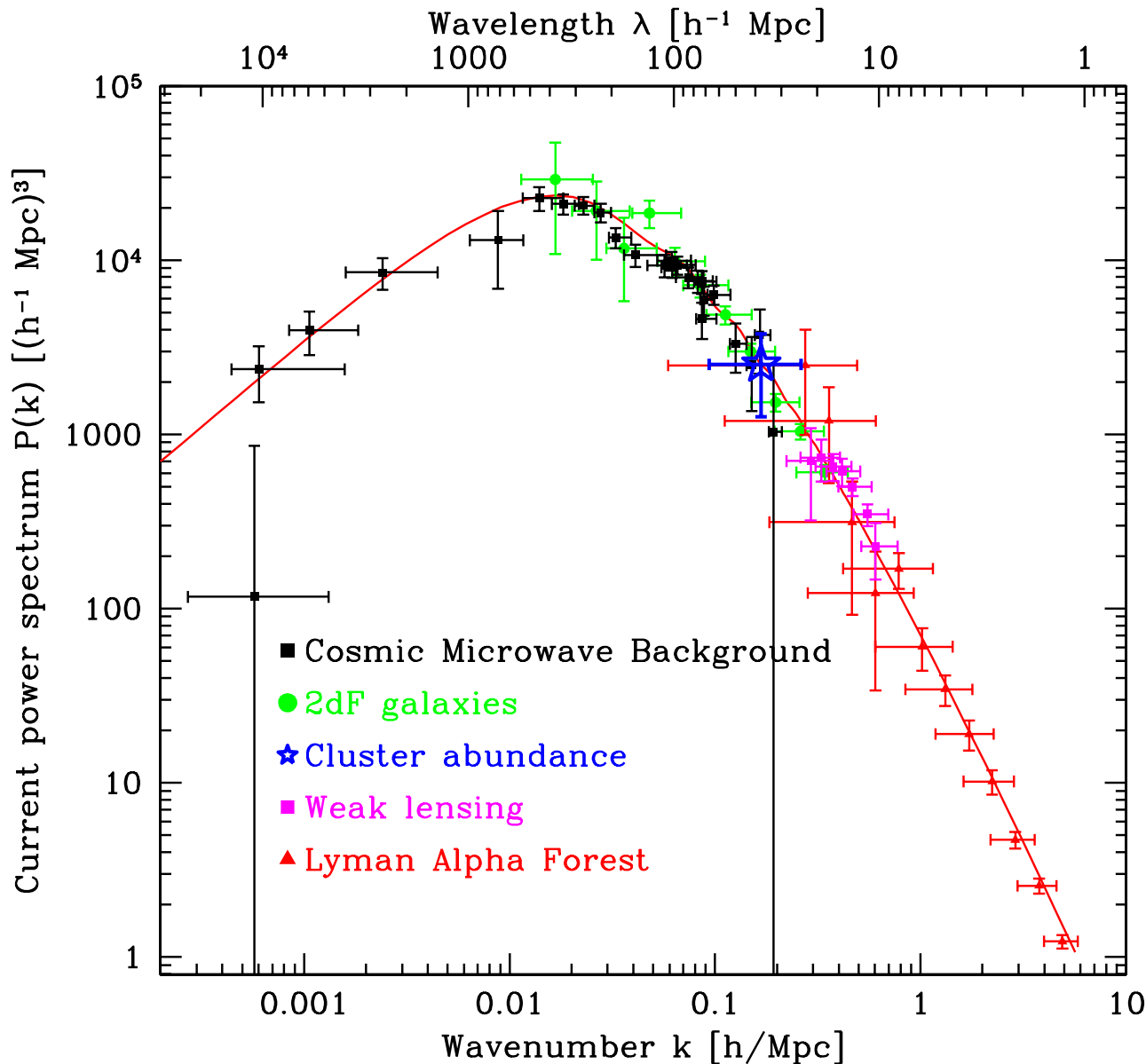


More complicated if  $w \neq -1$ , or if  $w(a)$  allowed, but general picture still holds:



Okouma, Fantaye & Bassett 2012

# Scalar spectral index: LSS extends the lever arm in $k$

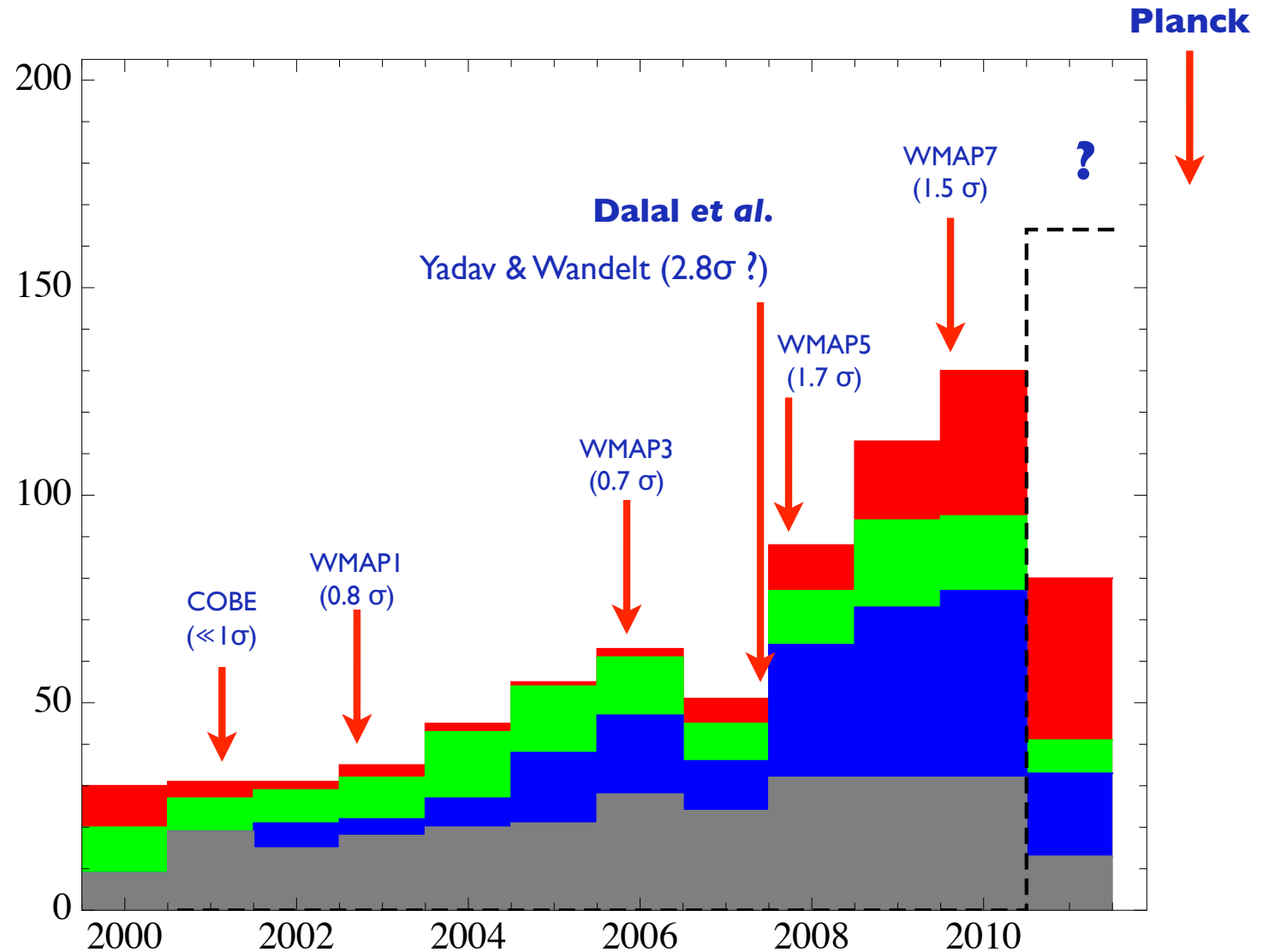
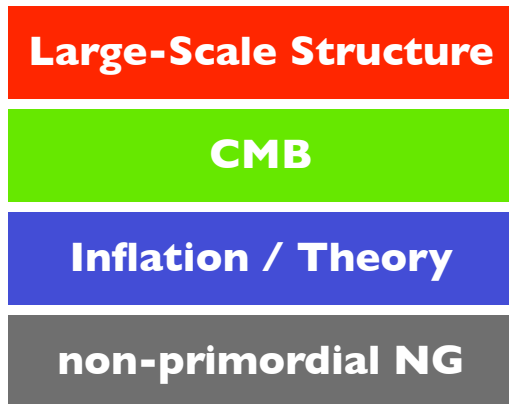


Hinshaw et al (WMAP9) 2013

# LSS and primordial non-Gaussianity

# Non-Gaussianity papers in the past 10 years

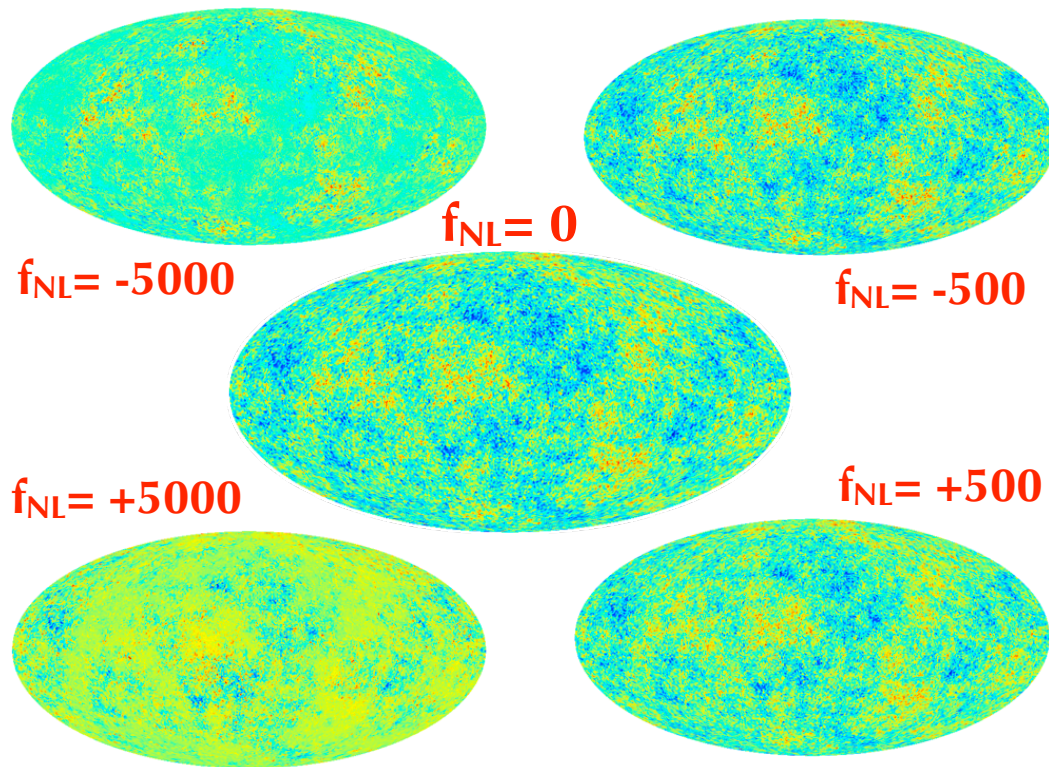
# of articles with  
“Non-Gaussian”  
in the title  
on the ADS data base



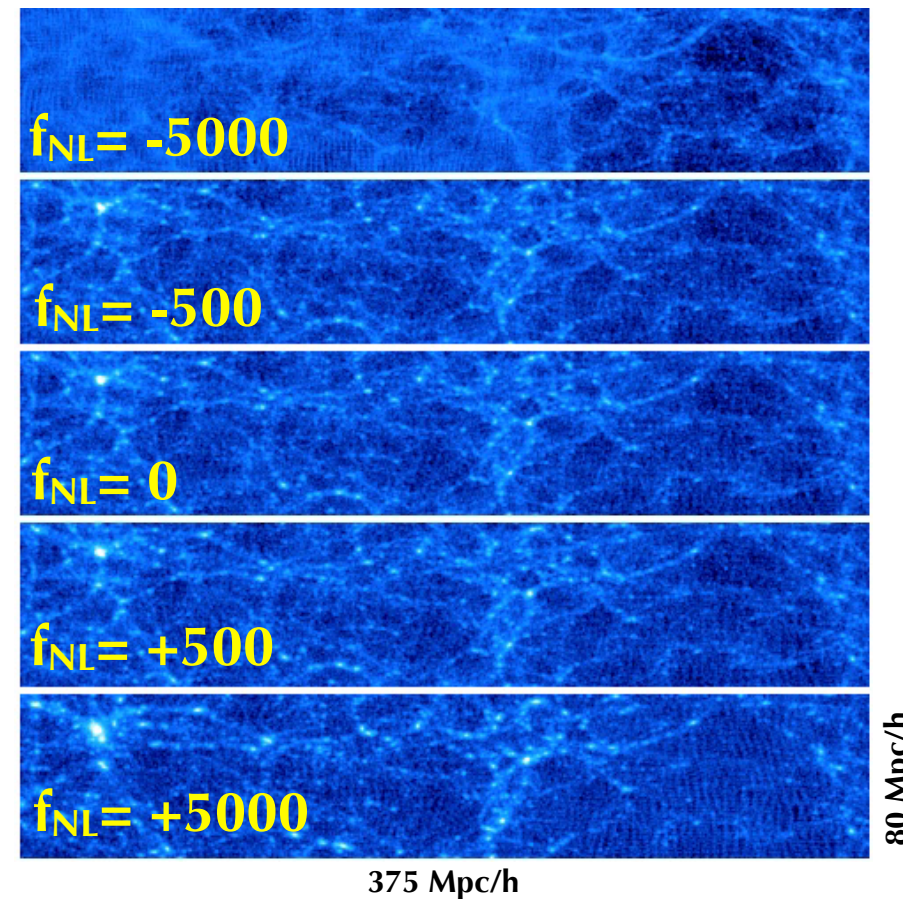


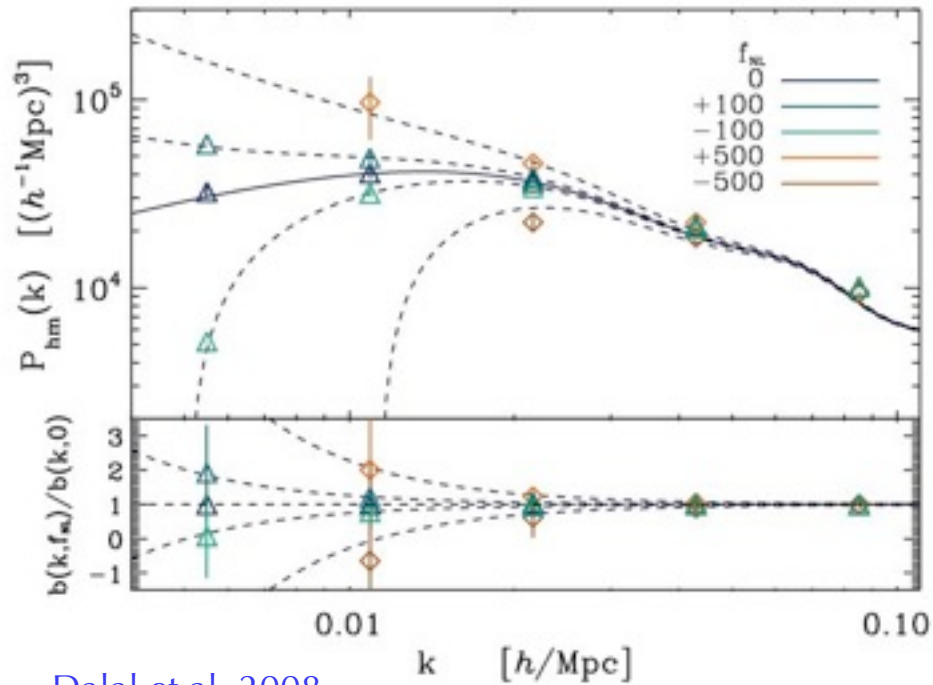
# Effects of primordial non-Gaussianity of local type

CMB: 3-point function  
is non-zero



LSS: over/under accentuation  
of density peaks



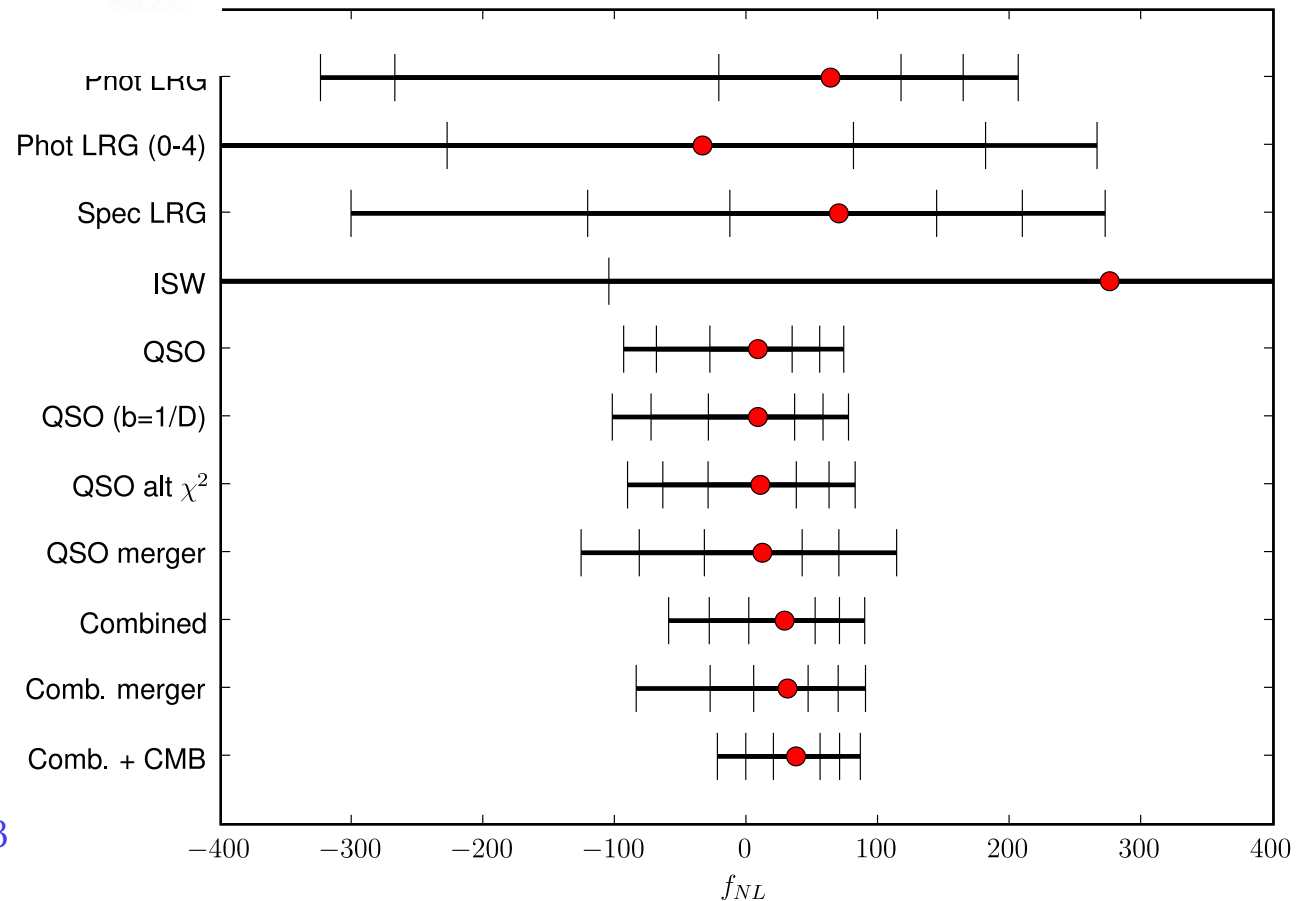


Dalal et al. 2008

$$b(k) = b_{\text{G}} + f_{\text{NL}}(b_{\text{G}} - 1) \delta_c \frac{3 \Omega_M H_0^2}{T(k) D(a)} \frac{1}{k^2}$$

$f_{\text{NL}} = 8 \pm 30$  (68%, QSO)

$f_{\text{NL}} = 23 \pm 23$  (68%, all)

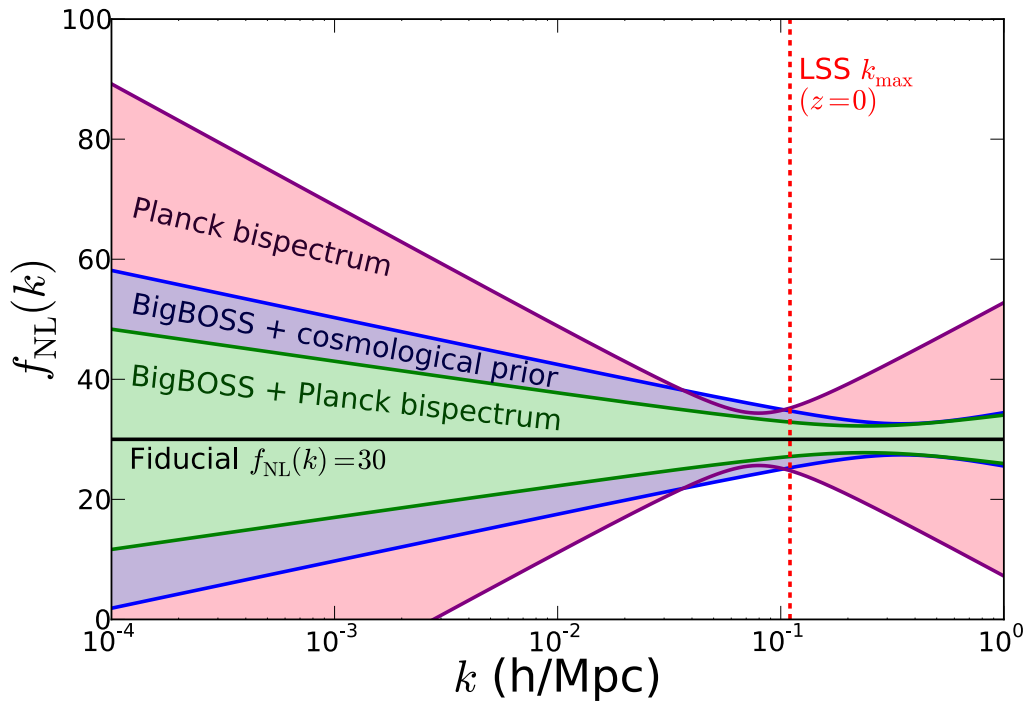


Slosar et al. 2008

# More generic NG: $f_{\text{NL}}(k)$ forecasts

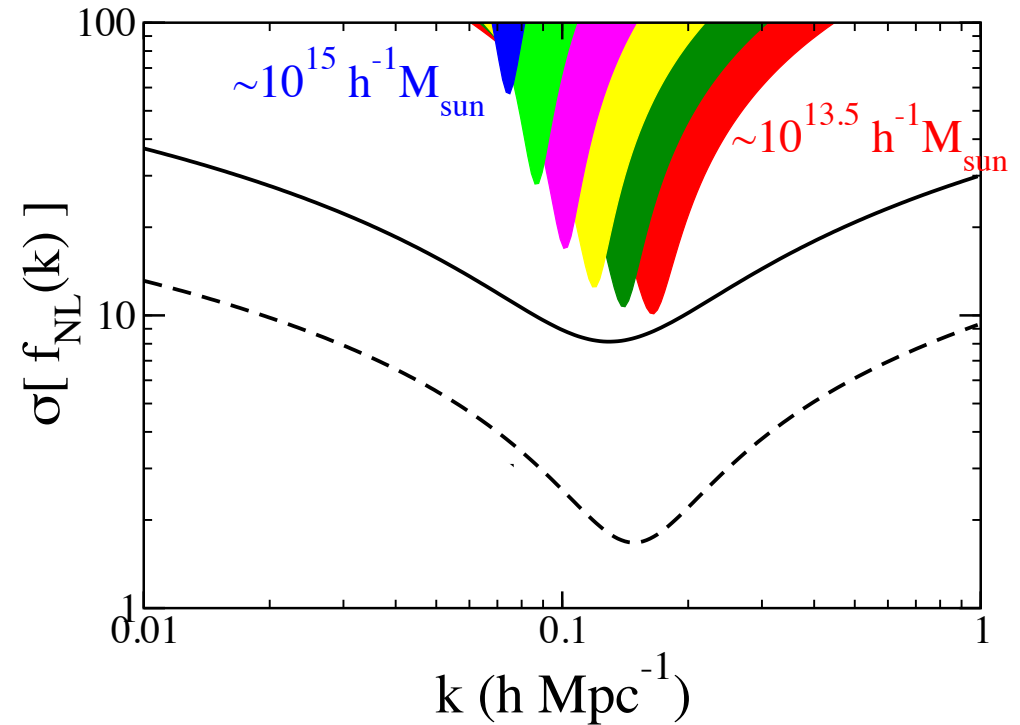
$$f_{\text{NL}}(k) = f_{\text{NL}}^* \left( \frac{k}{k_*} \right)^{n_{f_{\text{NL}}}}$$

CMB and LSS are very complementary



Becker, Huterer & Kadota 2012, Shandera, Dalal & Huterer 2012

Halos of mass  $M$  probe  
NG on scale  $k \sim M^{-1/3}$



In general, LSS can probe:

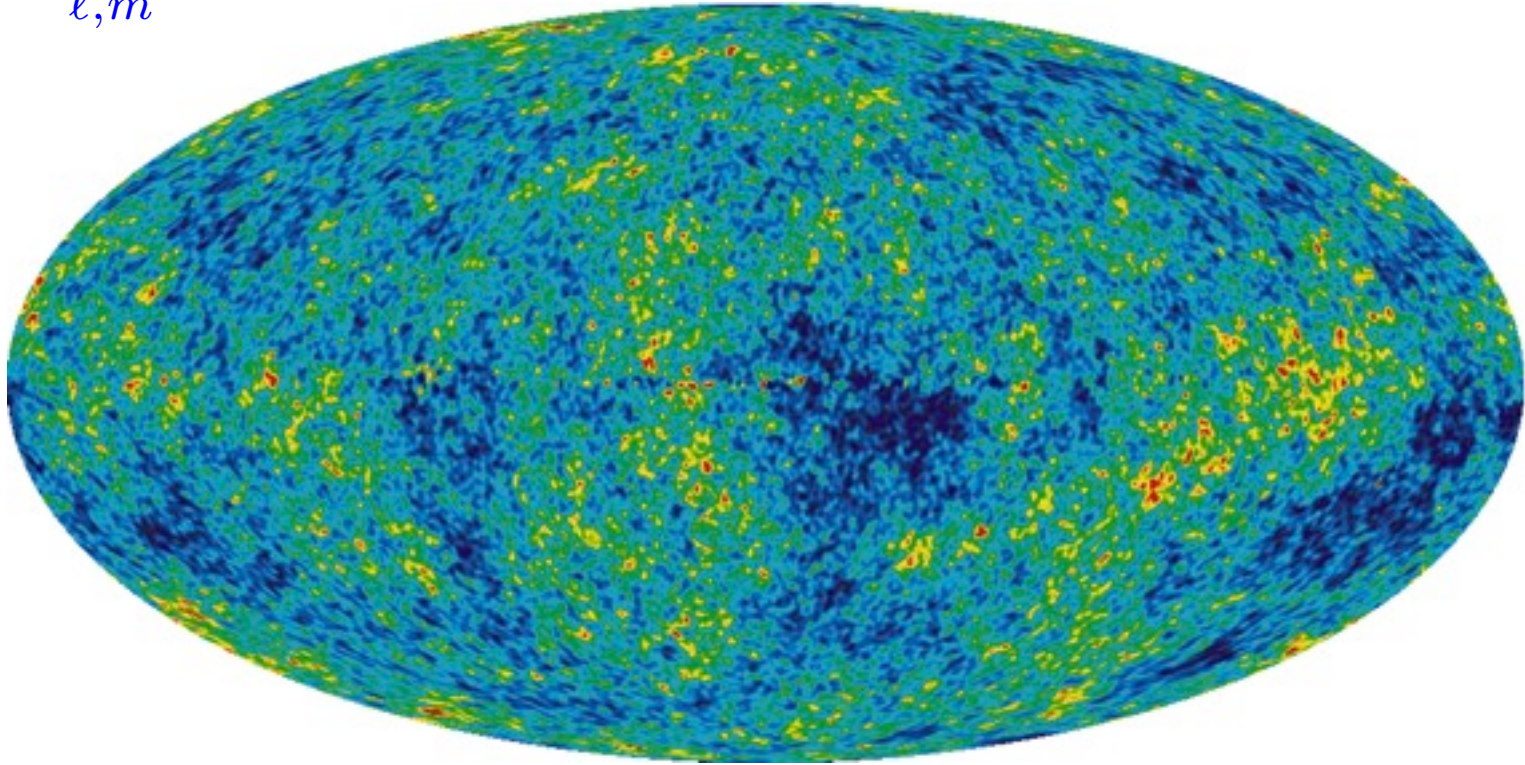
$$\Delta b_{\text{NG}} \propto \begin{cases} k^{-2} \text{ (local)} \\ k^{-1} \text{ (folded)} \\ k^0 \text{ (equilateral)} \\ k^{-\alpha} \text{ (generic); } 0 \leq \alpha \leq 3 \end{cases}$$

LSS and  
statistical isotropy + homogeneity



# Initial conditions in the universe

$$\frac{\delta T}{T}(\theta, \phi) = \sum_{\ell, m} a_{\ell m} Y_{\ell m}(\theta, \phi) \quad \ell \simeq \frac{180^\circ}{\theta}$$



Statistical Isotropy:

$$\langle a_{\ell m} a_{\ell' m'} \rangle \equiv C_{\ell \ell' m m'} = C_\ell \delta_{\ell \ell'} \delta_{m m'}$$

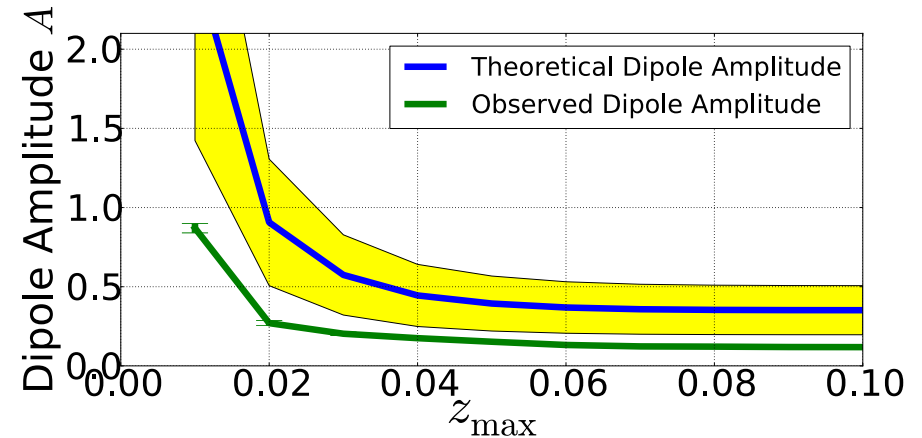
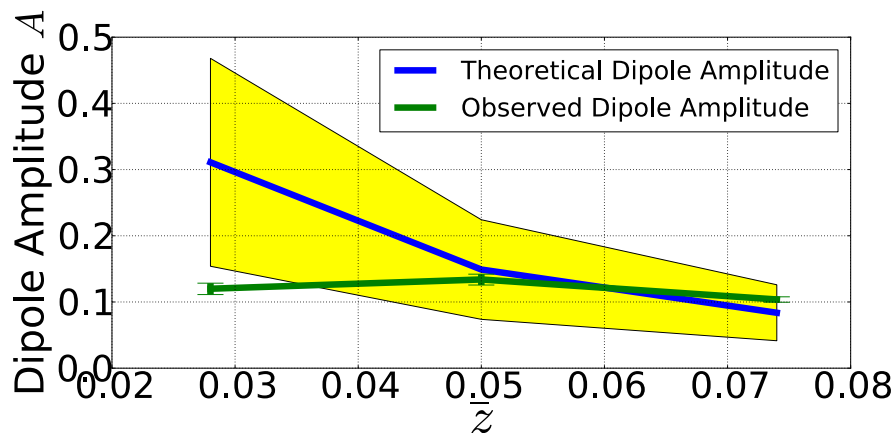
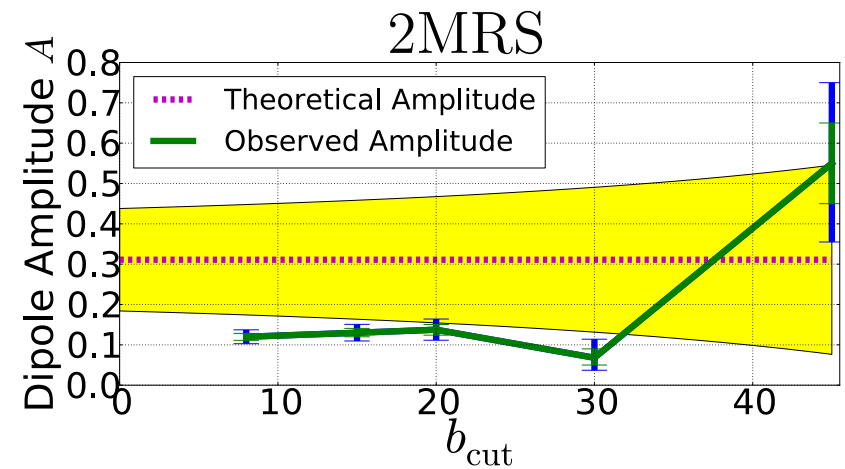
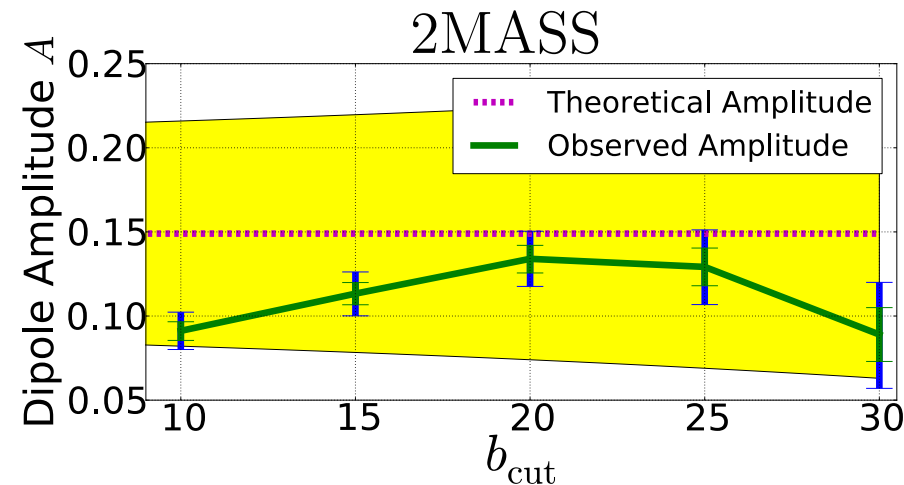
Gaussianity:

$$\langle a_{\ell m} a_{\ell' m'} a_{\ell'' m''} \rangle = 0$$

# Testing homogeneity and statistical isotropy with the LSS

Example I: dipole modulations in number counts:

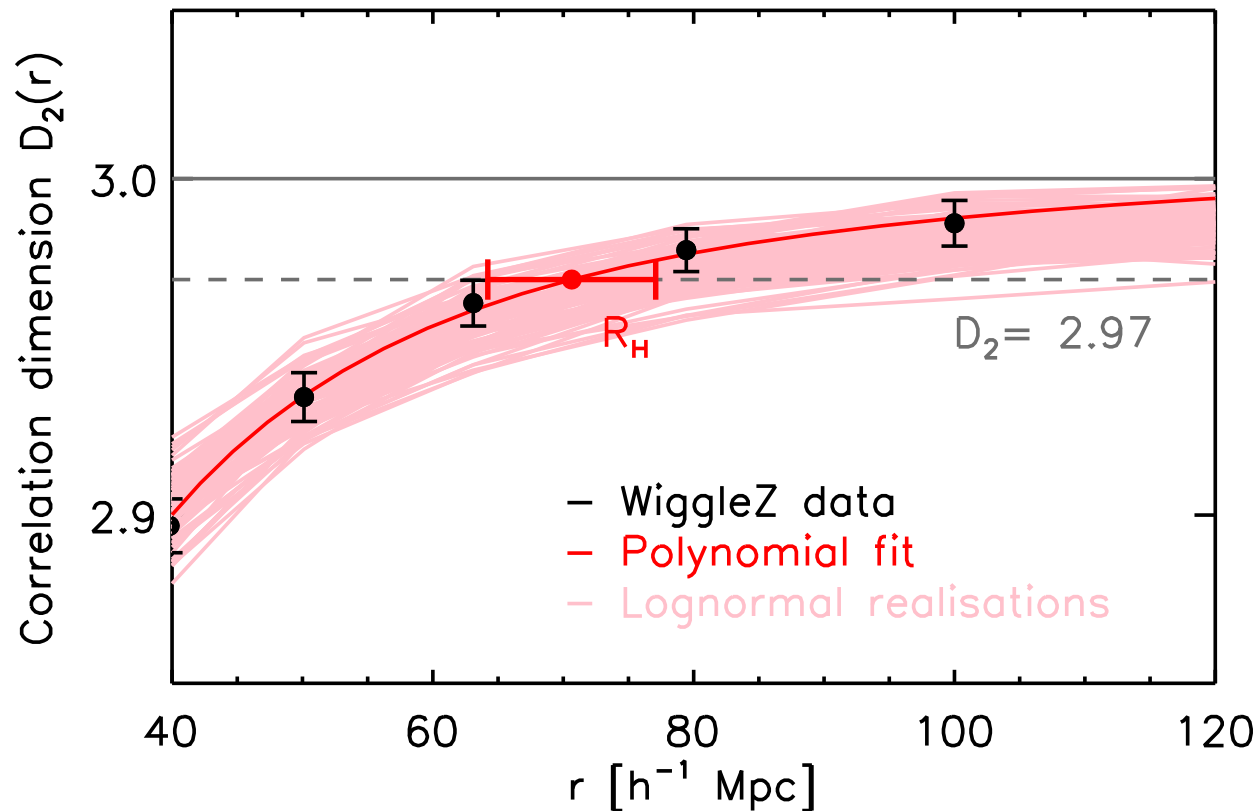
$$N(\hat{\mathbf{n}}) = \bar{N}(\hat{\mathbf{n}}) [1 + A(\hat{\mathbf{d}} \cdot \hat{\mathbf{n}})]$$



# Testing homogeneity and statistical isotropy with the LSS

Example II: testing homogeneity with galaxies:

$$N(< r) \propto r^{D_2}$$

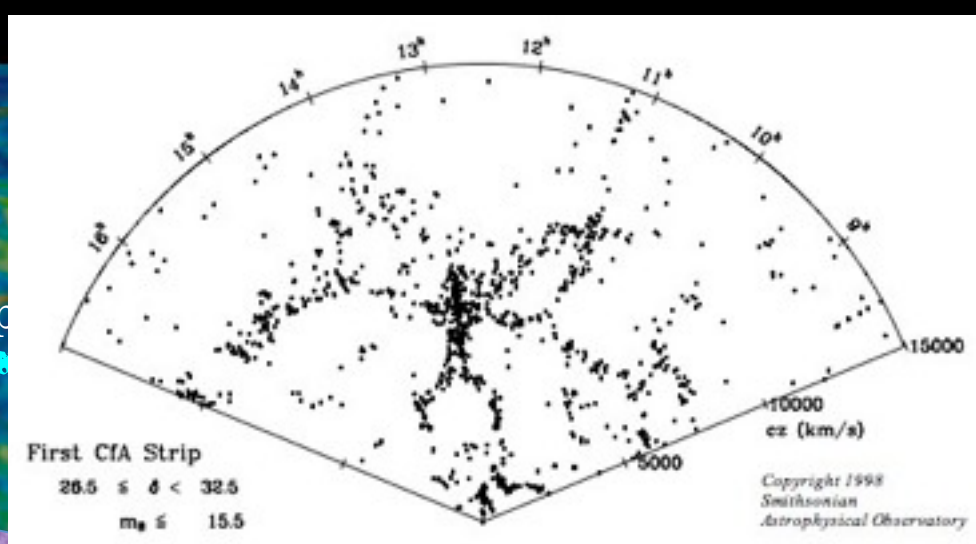




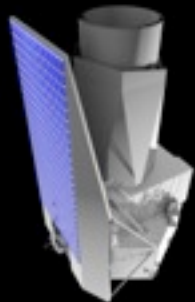
▲ Harvard-Cfa survey (1980s)

Dark Energy  
Survey (2012)

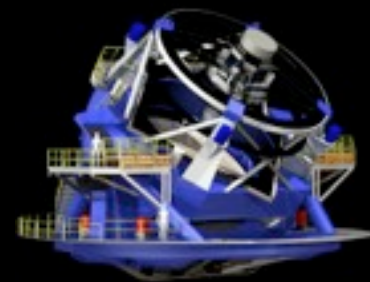
21cm map



Euclid or  
WFIRST  
(~202X)



LSST (~2018)





# Desiderata for future LSS surveys

**Large volume:** at large spatial scales, errors on cosmological parameters go as  $V^{-1/2}$

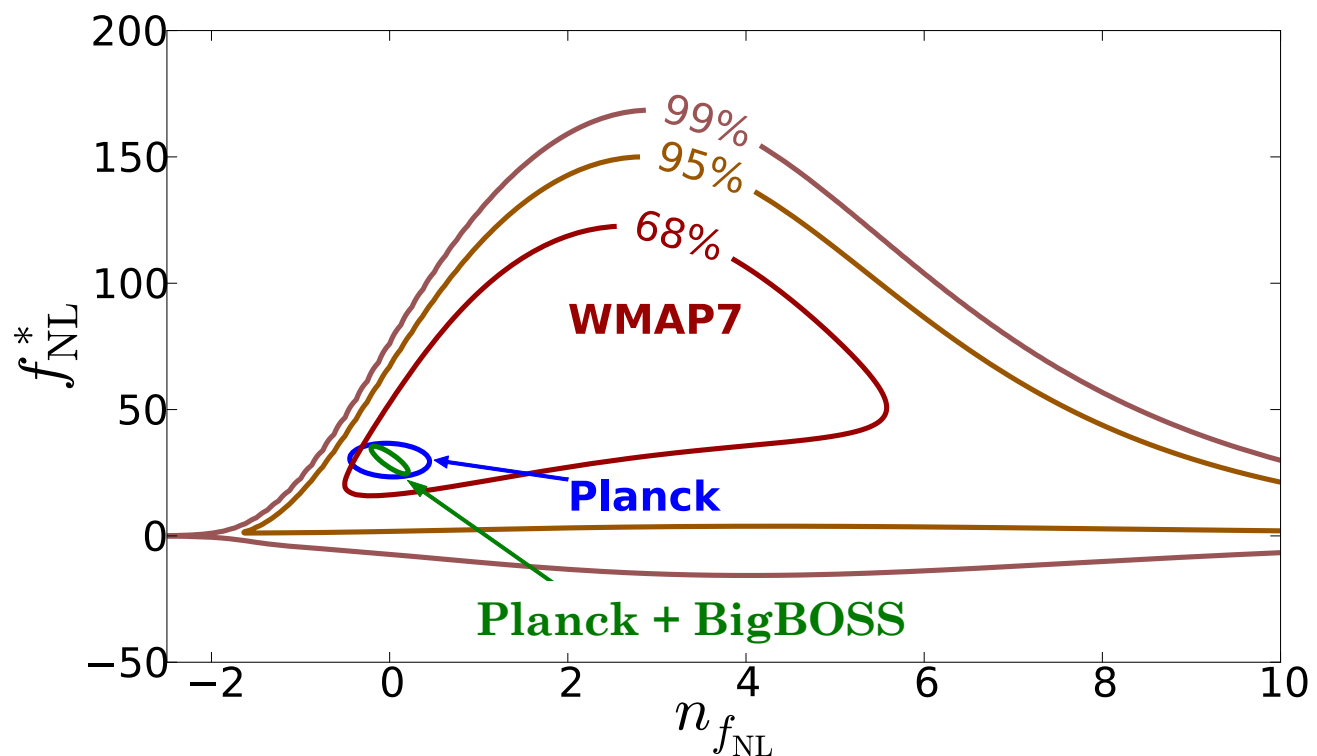
**Redshifts:** enormous amount doable with photometric info alone, but the photo-zs are inherently messy; accurate knowledge of the full  $P(z_s | z_p)$  is required (or: spectra).

**Well-characterized selection:** helps pin down masses of halos, and their other properties such as bias

....

**EXTRA SLIDES**

# Forecasts for $f_{\text{NL}}(k)$ with BigBOSS

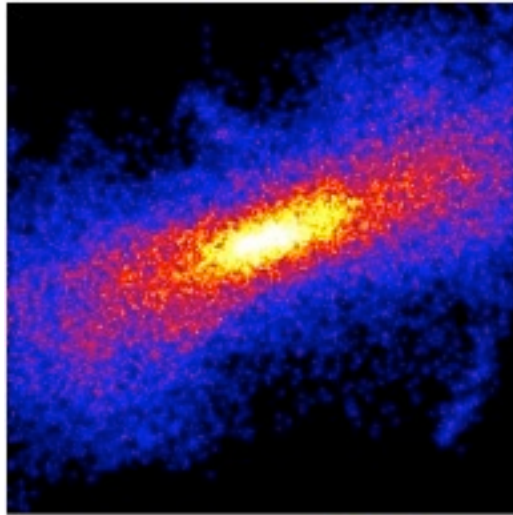


Projected errors  $\sigma(f_{\text{NL}}^*)$  and  $\sigma(n_{f_{\text{NL}}})$ , and the corresponding pivots

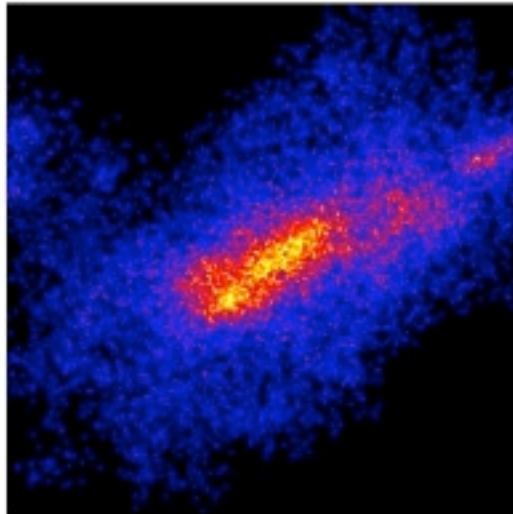
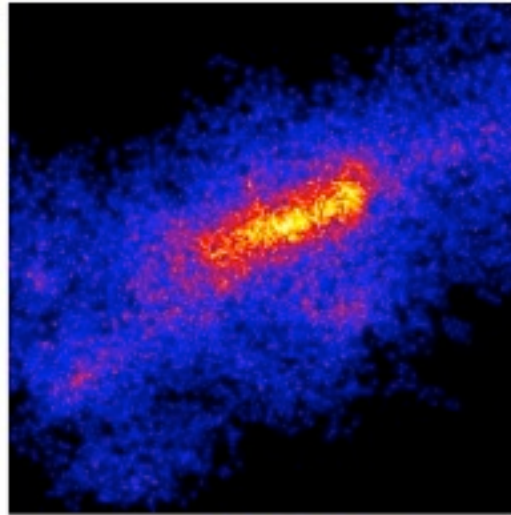
Variable	BigBOSS	BigBOSS+Planck $C_{\ell\text{s}}$	Planck bispec	<b>BigBOSS+all Planck</b>
$\sigma(f_{\text{NL}}^*)$	3.0	2.6	4.4	2.2
$\sigma(n_{f_{\text{NL}}})$	0.12	0.11	0.29	0.078
FoM <sup>(NG)</sup>	2.7	3.4	0.78	5.8
$k_{\text{piv}}$	0.33	0.35	0.080	0.24

# DM halo gets more massive with $f_{\text{NL}} > 0$ (and v.v.)

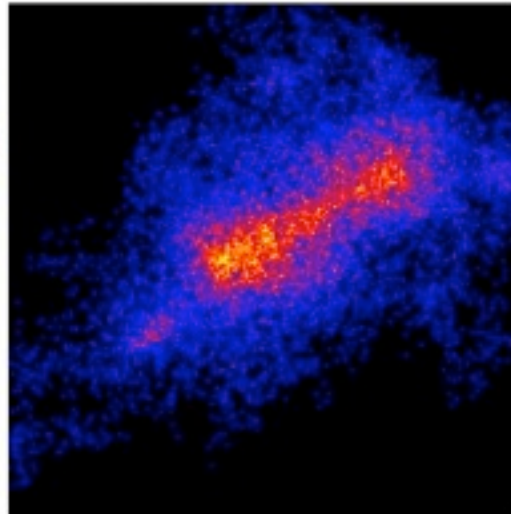
$f_{\text{NL}} = +5000$   
 $M = 1.2 \cdot 10^{16} M_{\odot}$



$f_{\text{NL}} = +500$   
 $M = 5.9 \cdot 10^{15} M_{\odot}$

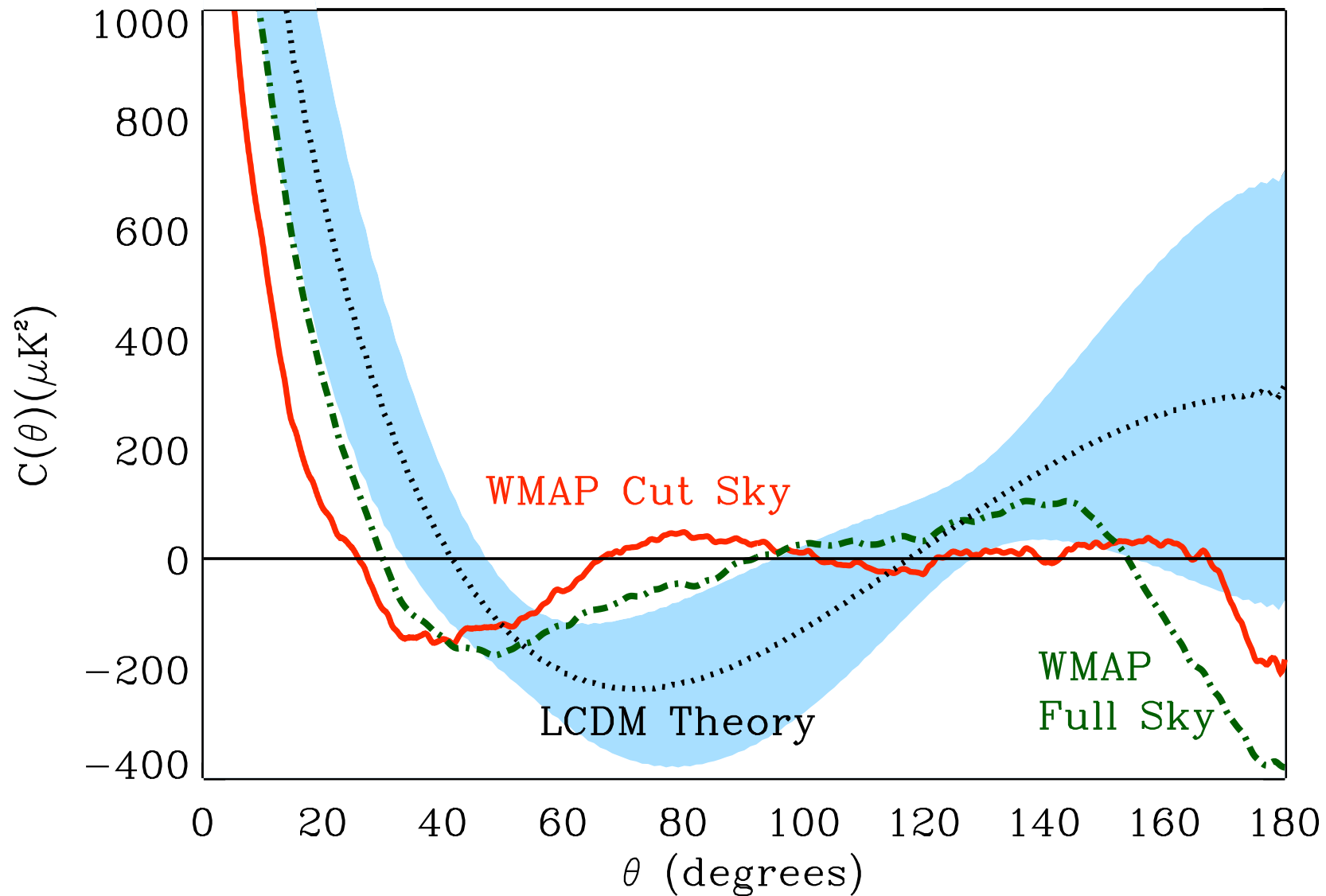


$f_{\text{NL}} = 0$   
 $M = 5.1 \cdot 10^{15} M_{\odot}$



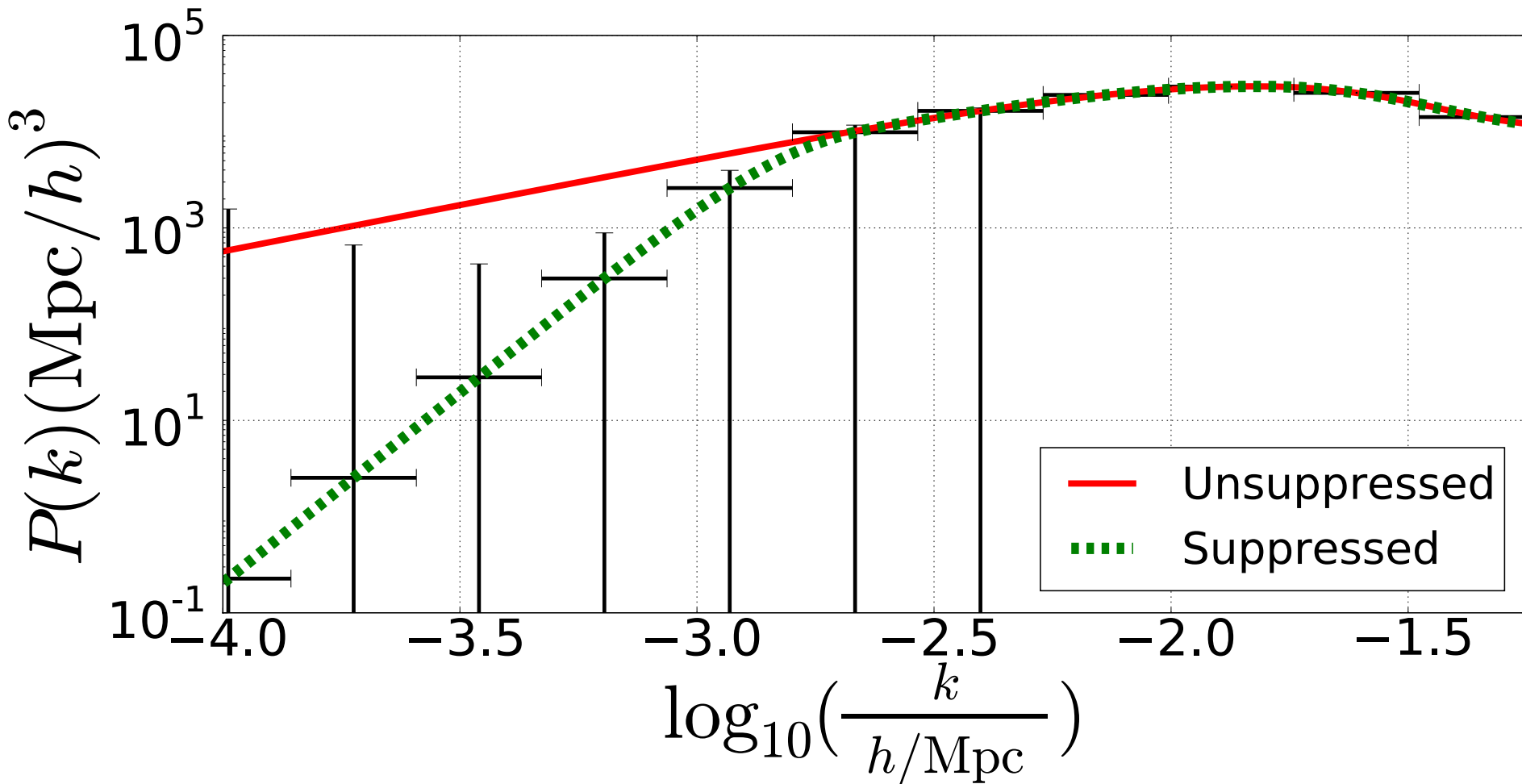
$f_{\text{NL}} = -500$   
 $M = 4.3 \cdot 10^{15} M_{\odot}$

# Missing power above 60°



Hinshaw et al 1996 (COBE);  
Spergel et al 2003 (WMAP)  
Copi et al 2007, 2009; Sarkar et al 2010

Using LSS to test whether  
low  $P(k)$  is the cause of low  $C(\theta)$



Can do this with LSS if you have a HUGE number of  
galaxy redshifts, as assumed in plot above  
(LSST with gazillion redshifts)