

# Alternatives to inflation

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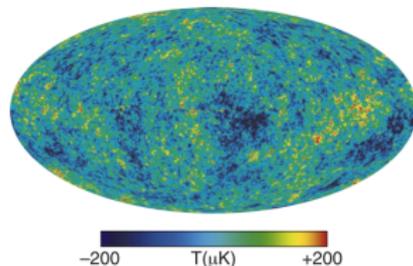
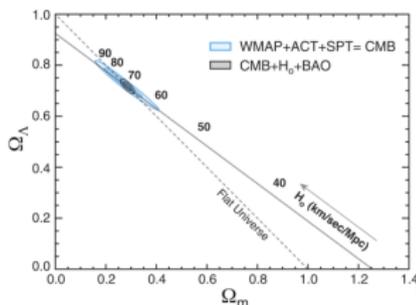
March 6, 2013



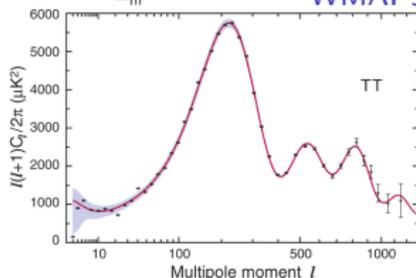
# Cosmological puzzles

On the largest scales, we observe the universe to be

- Flat
- Homogeneous
- Isotropic



WMAP9 1212.5225



Further, we observe a spectrum of perturbations in the CMB which is correlated on super-horizon scales and nearly **scale-invariant** and **gaussian**

# Handles on early universe physics

- Homogeneity and flatness of the background solution
  - ▶ We'll see how this is achieved both in inflation and in alternatives
- Temperature anisotropies  $\rightarrow$  nearly scale-invariant
  - ▶ The field responsible has to be nearly gaussian (not strongly self-interacting)
- Non-gaussianities of perturbations
  - ▶ Typically alternatives involve multiple field  $\rightsquigarrow$  different non-gaussian signatures
- Gravitational waves
  - ▶ Inflation  $\rightsquigarrow$  a scale-invariant spectrum of gravitational waves
  - ▶ Alternatives  $\rightsquigarrow$  no appreciable excitation of gravitational waves

# Flatness and homogeneity

The [Friedmann equation](#) reads:

$$3H^2 M_{\text{Pl}}^2 = \frac{k}{a^2} + \frac{C_{\text{matter}}}{a^3} + \frac{C_{\text{radiation}}}{a^4} + \frac{C_{\text{anisotropy}}}{a^6} + \dots + \frac{C}{a^{3(1+w)}}$$

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- For an expanding universe, curvature ( $\sim 1/a^2$ ) is the most dangerous, but a smooth component with  $w < -1/3$  will win  $\implies$  accelerated expansion: [inflation](#)
- Another logical possibility: if the universe is contracting before the big bang, the most dangerous term is now anisotropy ( $\sim 1/a^6$ ). A component with  $w > 1$  will win out  $\implies$  [slow contraction](#)

[Gratton, Khoury, Steinhardt & Turok astro-ph/0301395](#)

- ▶ Since  $w$  is very large, the background evolves slowly  $\implies$  [negligible gravitational waves](#)

# Null Energy Condition

At some point, all alternatives have to violate the Null Energy Condition

$$T_{\mu\nu} n^\mu n^\nu \geq 0 \xrightarrow{\text{fluid}} \rho + P \geq 0$$

- $M_{\text{Pl}}^2 \dot{H} = -\frac{1}{2}(\rho + P)$ ; To have  $\dot{H} > 0$ , have to violate the NEC
- Whether or not this is possible is an open question — typically theories which violate the NEC exhibit pathologies
- No-go theorem: For  $\mathcal{L} = \mathcal{L}(\phi, \partial\phi)$ , violating the NEC introduces instabilities [Dubovsky, Gregoire, Nicolis, Rattazzi 0512260](#)

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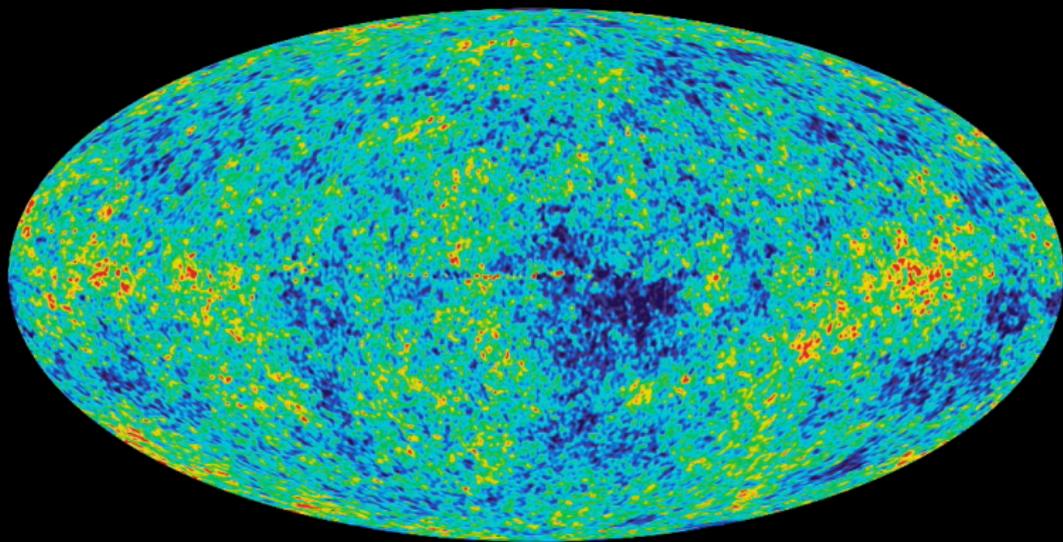
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- No-go theorem: For  $\mathcal{L} = \mathcal{L}(\phi, \partial\phi)$ , violating the NEC introduces instabilities [Dubovsky, Gregoire, Nicolis, Rattazzi 0512260](#)
- Possible way out: consider theories where  $\partial^2\phi$  is important

[Arkani-Hamed, Cheng, Luty, Mukohyama 0312099](#); [Nicolis, Rattazzi, Trincherini 0912.4258](#); [Creminelli, Nicolis, Trincherini 1007.0027](#); [Hinterbichler, AJ, Khoury, Miller 1212.3607](#)

# Anisotropy



NASA/WMAP Science Team

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$$C_\ell^{TT} \sim \int dk k^2 P_\zeta(k) \Delta_{\ell T}^2(k)$$

$$\text{observations} \implies P_\zeta(k) \propto k^3 \langle \zeta_k \zeta_{-k} \rangle \sim k^{2(n_s-1)}$$

$$n_s = 0.967 \pm 0.14 \quad \text{WMAP7}$$

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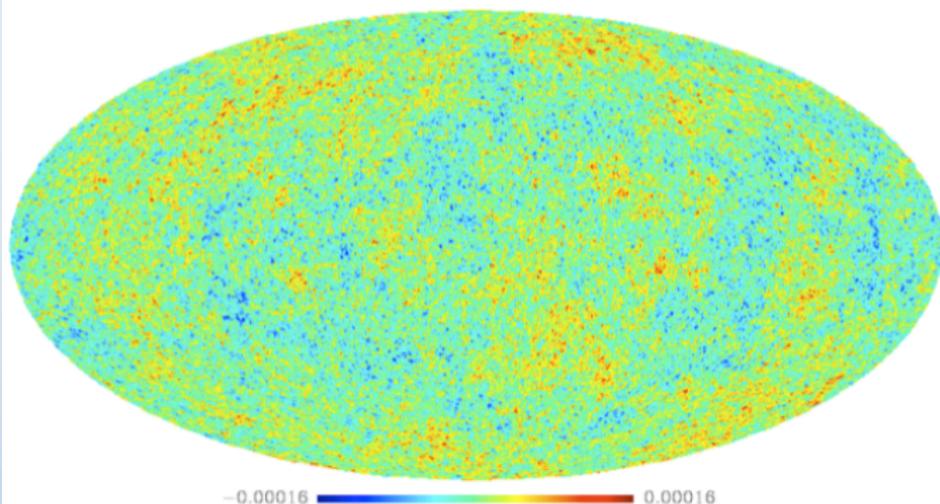
- Approximately **gaussian**
  - ▶ this says roughly that higher-point correlations are small compared to the two-point function

# Non-gaussianities

$$f_{NL} = 0$$

Temperature ( $f_{NL} = 0$ )

$$f_{NL} \equiv -\frac{\langle \frac{\delta T}{T} \frac{\delta T}{T} \frac{\delta T}{T} \rangle}{\langle \frac{\delta T}{T} \frac{\delta T}{T} \rangle^2}$$



Liguori et al. 0708.3786

## • Constraints

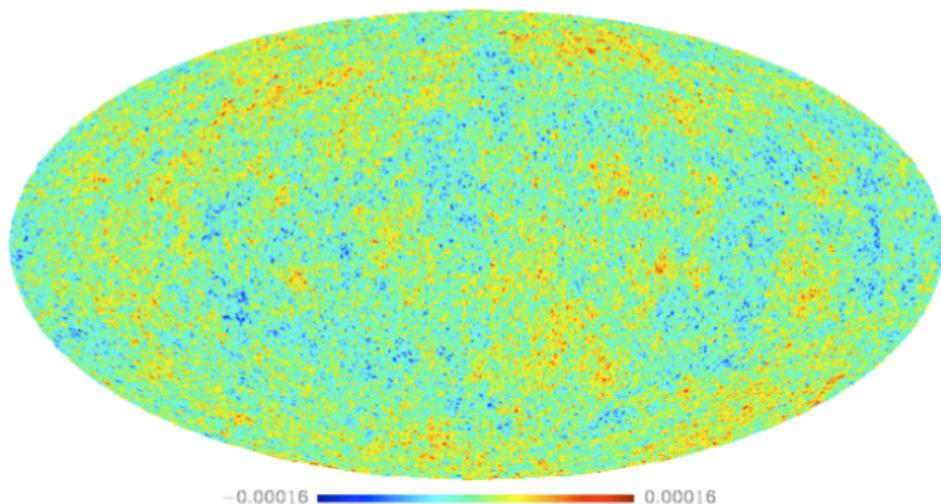
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Liguori et al. (2007)

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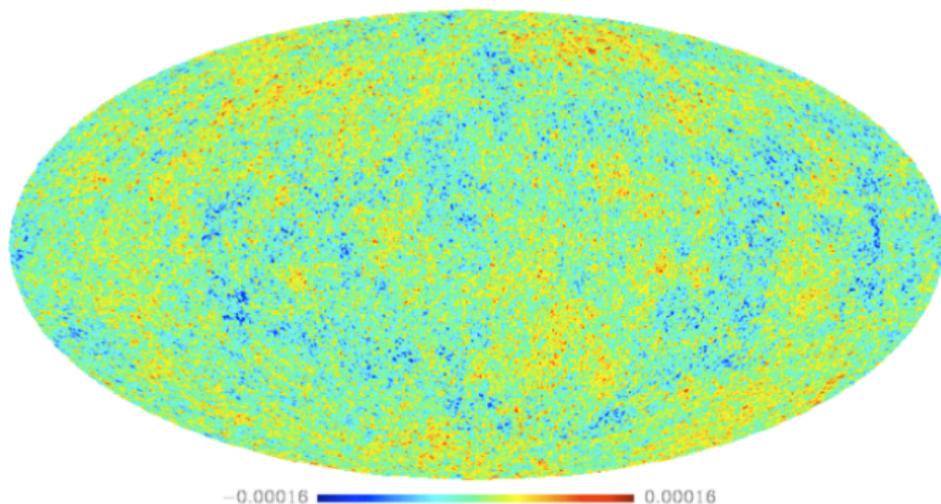
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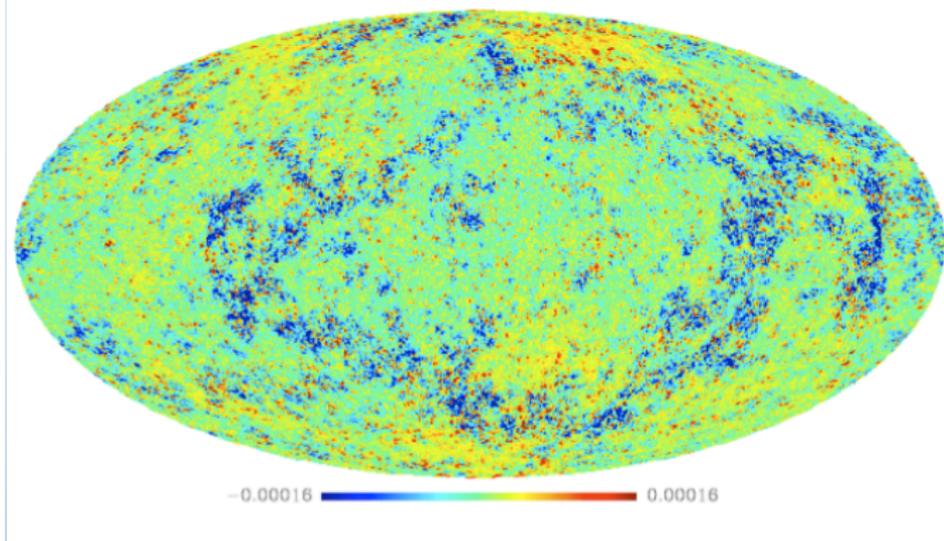
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# Symmetries of inflation

- Inflation is a period of quasi-de Sitter expansion

$$ds^2 \simeq -dt^2 + e^{2Ht} d\vec{x}^2$$

- Inflation ends  $\implies$  there must be a clock telling it when to end! The level sets of this clock provide a preferred foliation of de Sitter space

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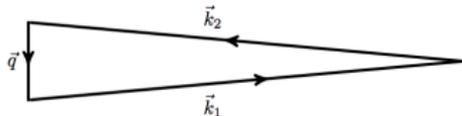
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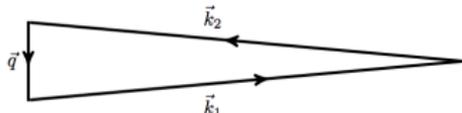
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- Then, the scale-invariant spectrum of  $\zeta$  is a consequence of the diagonal combination of a (broken) coordinate dilation and the shift symmetry of the field
- Spectator fields enjoy the full de Sitter isometries  $\implies$  gravitational waves acquire [scale-invariant](#) spectrum  
[Maldacena, Pimentel 1104.2846;](#)  
[Creminelli 1108.0874](#)

## Consistency relation



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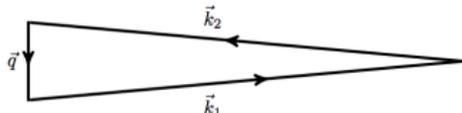


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- We can therefore infer the 3-point function where one of the modes is very soft ( $q \ll k_1, k_2$ ) [Maldacena 0210603](#); [Creminelli & Zaldarriaga 0407059](#)

$$\lim_{q \rightarrow 0} \frac{1}{P_\zeta(q)} \langle \zeta_q \zeta_{k_1} \zeta_{k_2} \rangle' = \left( 3 + \vec{k} \cdot \vec{\partial}_k \right) \langle \zeta_{k_1} \zeta_{-k} \rangle' = (n_s - 1) \langle \zeta_{k_1} \zeta_{-k} \rangle'$$

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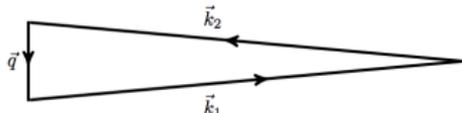
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- Since the 2-point function is very close to scale-invariant, the RHS is *very small* — detection of  $f_{NL}$  in this limit would rule out *all* single-field models
  - ▶ Assumptions: the background is an attractor ( $\zeta \rightarrow \text{const.}$ ); there is a single clock; Bunch–Davies vacuum

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In general, single-field alternatives will have different non-Gaussian signatures from inflationary models [but, their squeezed limit is also constrained by the consistency relation:](#)

# Alternatives?

Khoury & Miller 1012.0846; AJ, Khoury 1107.3550;  
Baumann, Senatore, Zaldarriaga; 1101.3320

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- Adiabatic ekpyrosis/expansion:  $f_{NL} \sim \tau^{-4} \rightsquigarrow$  strong coupling issues  
Khoury, Steinhardt 0910.2230; AJ, Khoury 1104.4347

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[Lehners, McFadden, Turok, Steinhardt 0702153](#);  
[Creminelli, Senatore 0702165](#)

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  - ▶ Conformal mechanism 

## Conformal mechanism — scale invariance from conformal invariance

Inflation is rooted in symmetry ( $so(4, 1)$ ); worth thinking about alternatives also based on symmetries

- **Conformal mechanism:** At early times, the universe is described by a (nearly) CFT on (nearly) flat space
  - ▶ 4 translations
  - ▶ 6 rotations/boosts
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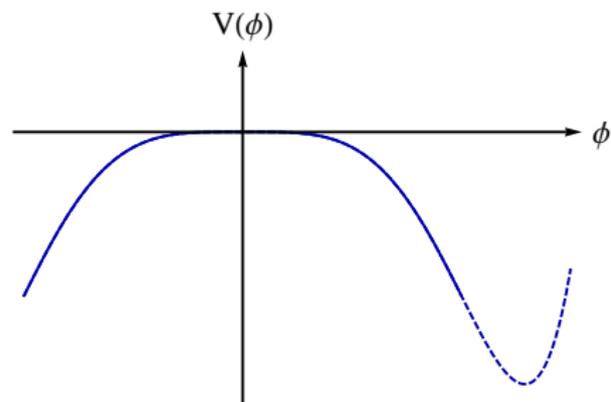
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- Under **general** conditions, scale-invariance for spectator fields follows from symmetry breaking to the isometries of de Sitter
- Universe is driven to be homogeneous and flat ( $|w| \gg 1$ )

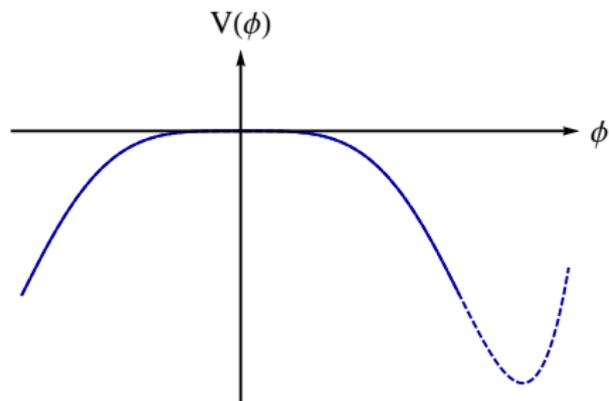
## Negative quartic example — Hinterbichler, Khoury 1106.1428



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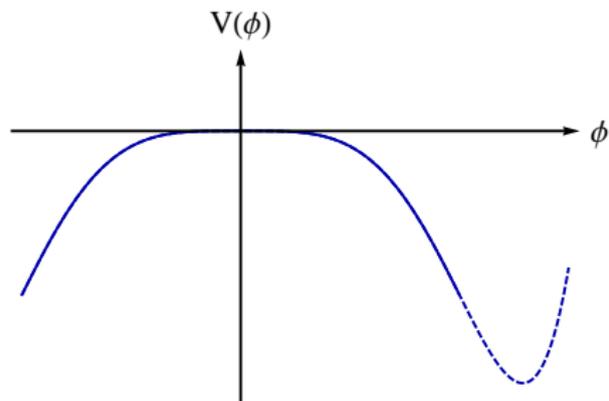
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Consider coupling a massless field  $\chi$  in the CFT

$$\mathcal{L}_\chi = -\frac{1}{2}\phi^2(\partial\chi)^2.$$

This field couples to the **effective** metric  $g_{\mu\nu}^{\text{eff}} = \phi^2\eta_{\mu\nu}$

## Negative quartic model cont.



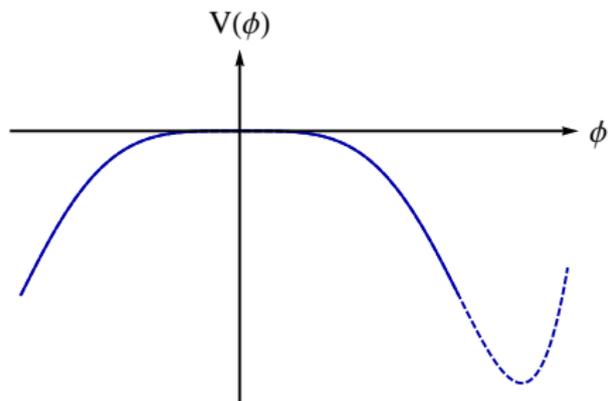
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- If one couples this to gravity, they find that the universe is very slowly **contracting** with equation of state

$$w = \frac{P}{\rho} \sim t^2 M_{\text{Pl}}^2,$$

which is very large; the universe is therefore driven to be homogeneous, flat, isotropic

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- This profile breaks 5 of these symmetries (e.g. time translation symmetry); leaving us with 10
- These can be recombined into the isometries of de Sitter space  $so(4, 1)$

It is therefore not so surprising that certain fields will acquire a scale invariant spectrum

- Recall that  $\chi$  coupled to the *effective* metric  $\bar{\phi}^2 \eta_{\mu\nu} \sim \frac{1}{t^2} \eta_{\mu\nu}$ 
  - ▶ This is the metric of [de Sitter space!](#)

I've showed you a particular realization, but most of the physics follows solely from symmetry breaking pattern

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and for spectator fields

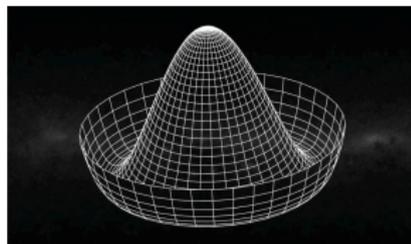
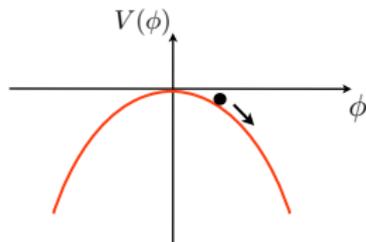
$$\mathcal{L}_\chi = -\frac{M_\chi^2}{2} e^{2\pi} (\partial\chi)^2 + e^{4\pi} V(\chi) + a_1 (\partial\chi)^4 + \dots$$

When  $\chi$  is massless, it acquires a scale-invariant spectrum

# Realizations

There are various realizations of this mechanism

Negative  $\phi^4$ ,  $U(1)$  model



Craps, Hertog, Turok 0712.4180;  
Rubakov 0906.3693;

Hinterbichler, Khoury 1106.1428

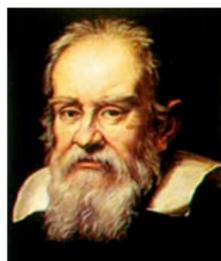
## DBI braneworlds



Hinterbichler, Khoury 1106.1428;

Hinterbichler, AJ, Khoury, Miller 1212.3607

## Galilean Genesis



Creminelli, Nicolis, Trincherini 1007.0027;

Creminelli, Hinterbichler, Khoury, Nicolis, Trincherini 1209.3768

## Distinguishing from inflation? – Creminelli, AJ, Houry & Simonović 1212.3329

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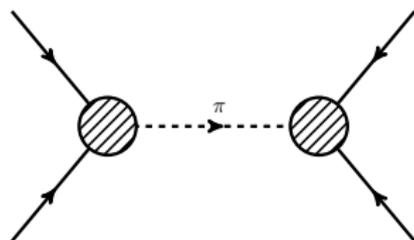
But this also has *additional* symmetries, because it came from an  $so(4, 2)$  invariant action

- These additional symmetries have corresponding Ward identities, which constrain correlation functions in a way different from inflation

$$\lim_{q \rightarrow 0} \frac{1}{P_\pi(q)} \langle \pi_{\vec{q}} \phi_{\vec{k}_1} \dots \phi_{\vec{k}_N} \rangle' = - \left( 1 + \frac{1}{N} q_i \sum_a \partial_{k_{ai}} + \frac{1}{6N} \vec{q}^2 \sum_a \partial_{k_a}^2 \right) \frac{d}{d \log t} \langle \phi_{\vec{k}_1} \dots \phi_{\vec{k}_N} \rangle'$$

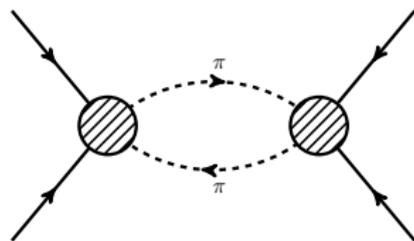
## 4pt function from symmetry - Creminelli, AJ, Khoury & Simonović 1212.3329

There are two distinct contributions to the 4-point function, coming from exchanging either one or two soft goldstone fields. The predicted shapes are model-independent



A Feynman diagram showing two vertices, each represented by a shaded circle. Each vertex has two external lines with arrows pointing away from it. A dashed line labeled  $\pi$  connects the two vertices, representing the exchange of a soft goldstone field.

$$\sim \frac{1}{qk_1^4 k_3^4} \left( 3(\hat{k}_1 \cdot q)^2 - 1 \right) \left( 3(\hat{k}_2 \cdot q)^2 - 1 \right)$$



A Feynman diagram showing two vertices, each represented by a shaded circle. Each vertex has two external lines with arrows pointing away from it. A dashed line labeled  $\pi$  forms a loop between the two vertices, representing a loop-level contribution.

$$\sim \frac{1}{q^3 k_1^3 k_2^3}$$

Notice that the loop's contribution is of  $\tau_{NL}$  form, which is relevant for the stochastic scale-dependent bias or  $\mu$ -distortion

# Summary

- We have several probes of the early universe
  - ▶ Homogeneity, flatness and isotropy  $\rightsquigarrow w < -1/3$  or  $|w| \gg 1$
  - ▶ Scale-invariant & Gaussian perturbations  $\rightsquigarrow$  alternatives with multiple fields
  - ▶ Gravitational waves — inflation predicts them, alternatives do not
- Inflation is a theory deeply rooted in symmetry, therefore alternatives should have similarly deep symmetry principles
- Conformal mechanism is an alternative to inflation based upon breaking  $so(4, 2) \rightarrow so(4, 1)$
- Non-linearly realized conformal symmetry imposes additional constraints on correlation functions relative to inflation