

[272/158]

# BEACH 2024

XV International Conference on Beauty, Charm, Hyperons in Hadronic Interactions

3-7 June 2024

Courtyard Charleston Historic District  
Charleston, SC



June, 2024

# HEAVY QUARK EXOTICS

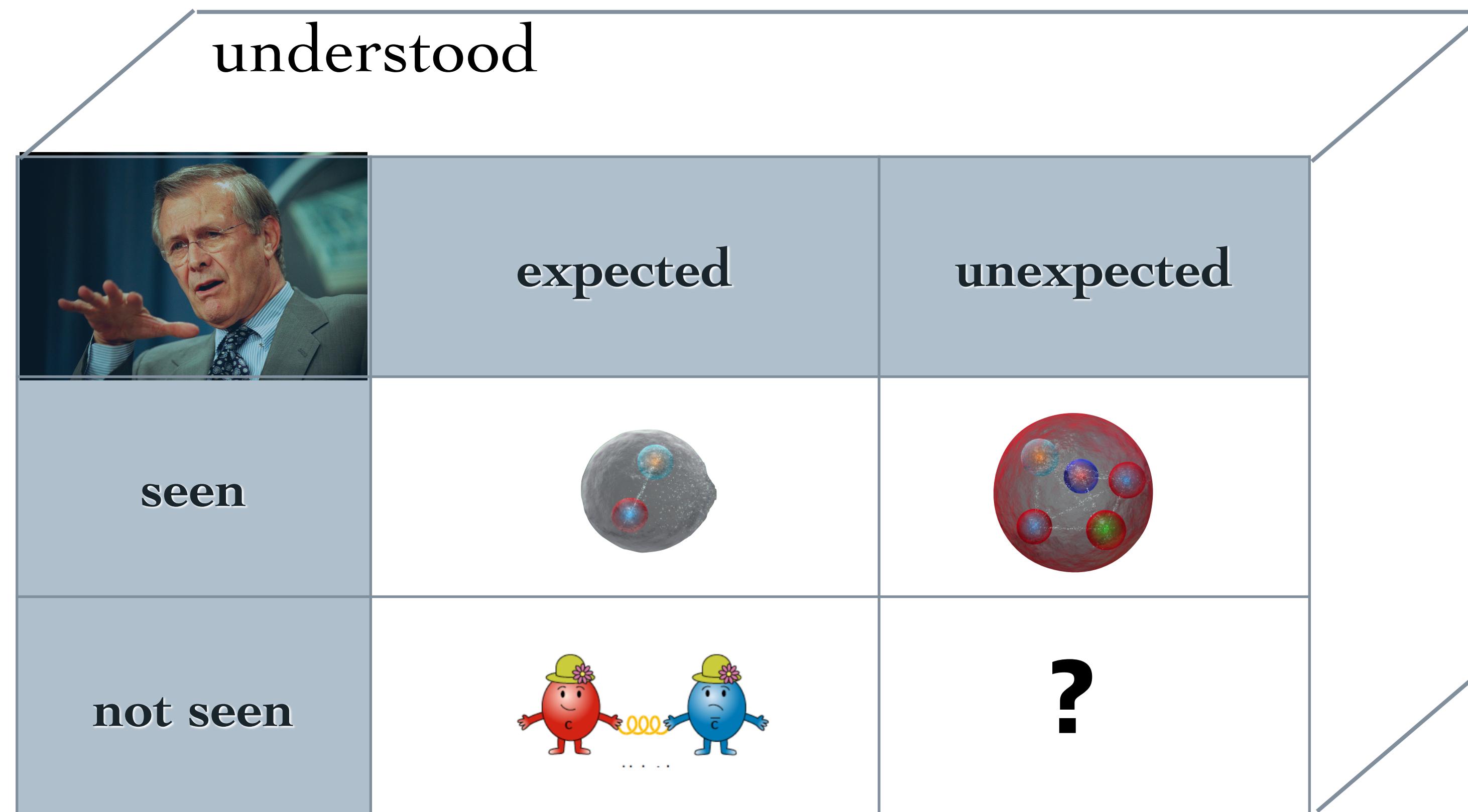
Eric Swanson



# tl;dl

- no shortage of anomalies & multiquark candidates
- definite shortage of hybrid candidates!
- naive analysis can create states 
- many "states" can appear due to production (near) singularities, cusps, interferences 
- much work remains to be done!

# Rumsfeld hadronic matrix



# The QCD Panoply

**Quark propagator:**

$$\text{---} \circ \text{---}^{-1} = \text{---} \text{---}^{-1} + \text{---} \text{---} \text{---} \text{---}$$

**Ghost propagator:**

$$\text{---} \circ \text{---}^{-1} = \text{---} \text{---}^{-1} + \text{---} \text{---} \text{---} \text{---}$$

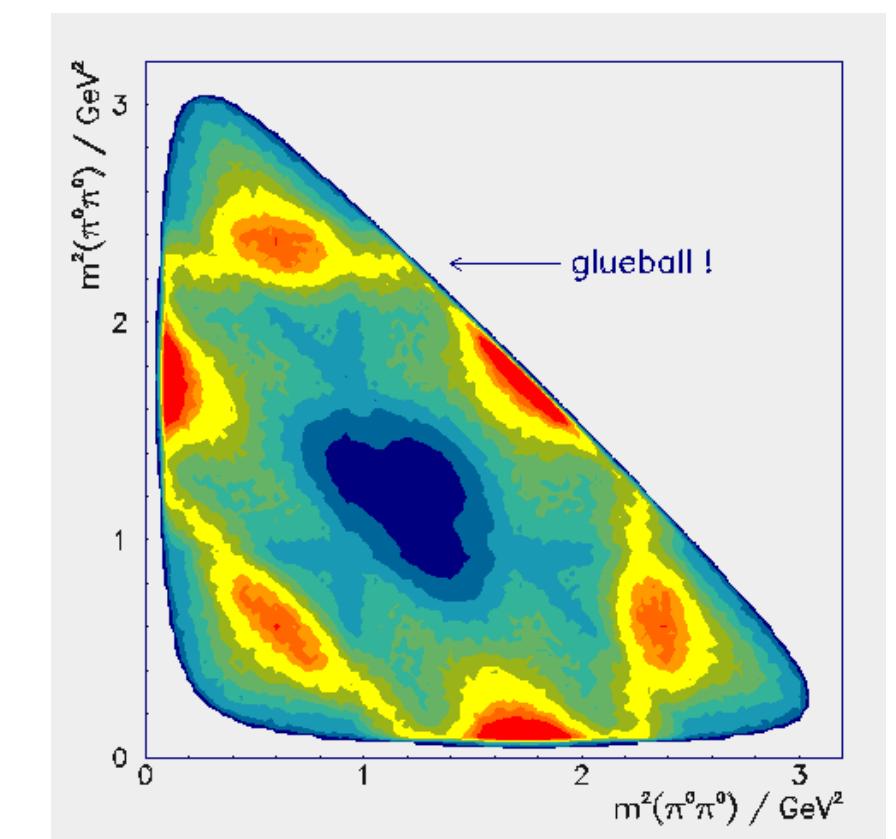
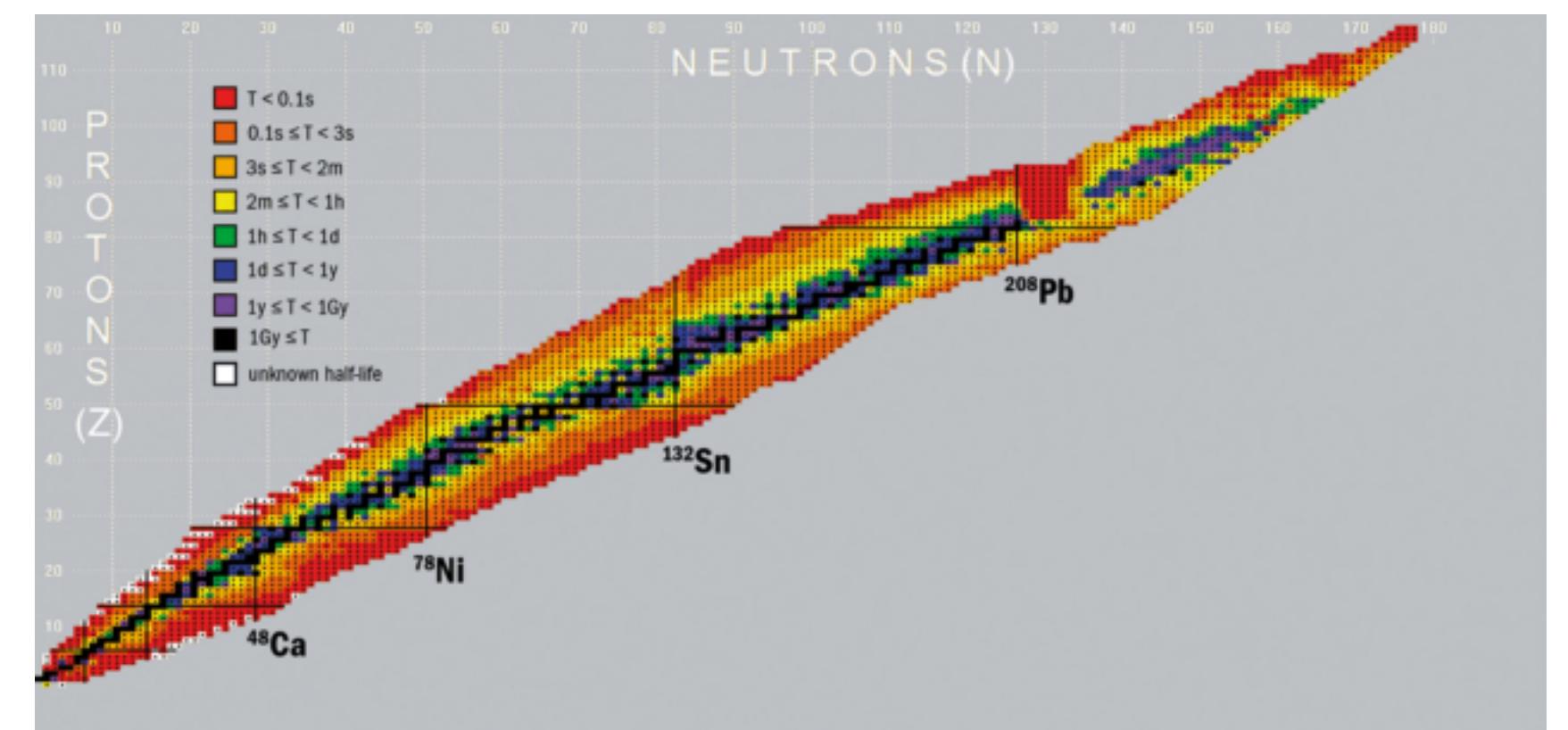
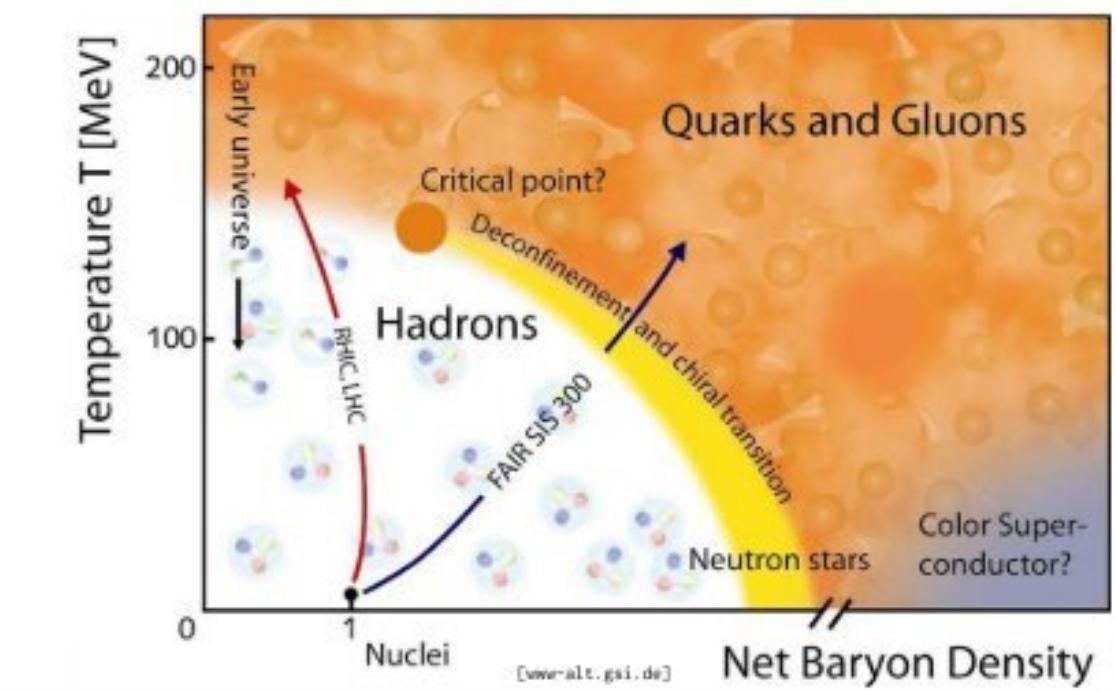
**Ghost-gluon vertex:**

$$\text{---} \text{---} \text{---} \text{---} \text{---} = \text{---} \text{---} \text{---} \text{---} \text{---} + \text{---} \text{---} \text{---} \text{---} \text{---}$$

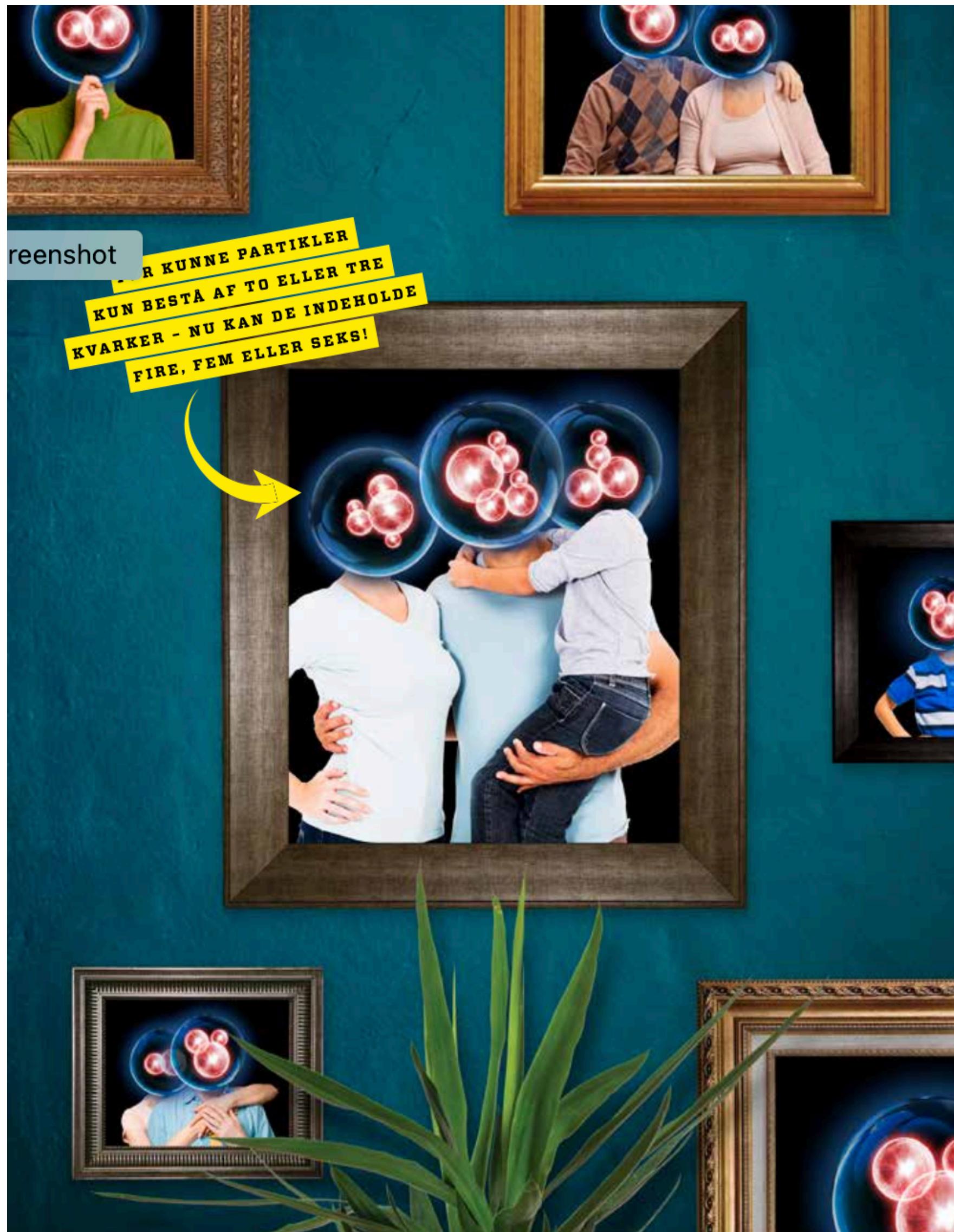
**Quark-gluon vertex:**

$$\text{---} \text{---} \text{---} \text{---} \text{---} = \text{---} \text{---} \text{---} \text{---} \text{---} + \text{---} \text{---} \text{---} \text{---} \text{---}$$

$$+ \text{---} \text{---} \text{---} \text{---} \text{---} + \text{---} \text{---} \text{---} \text{---} \text{---} + \text{---} \text{---} \text{---} \text{---} \text{---}$$

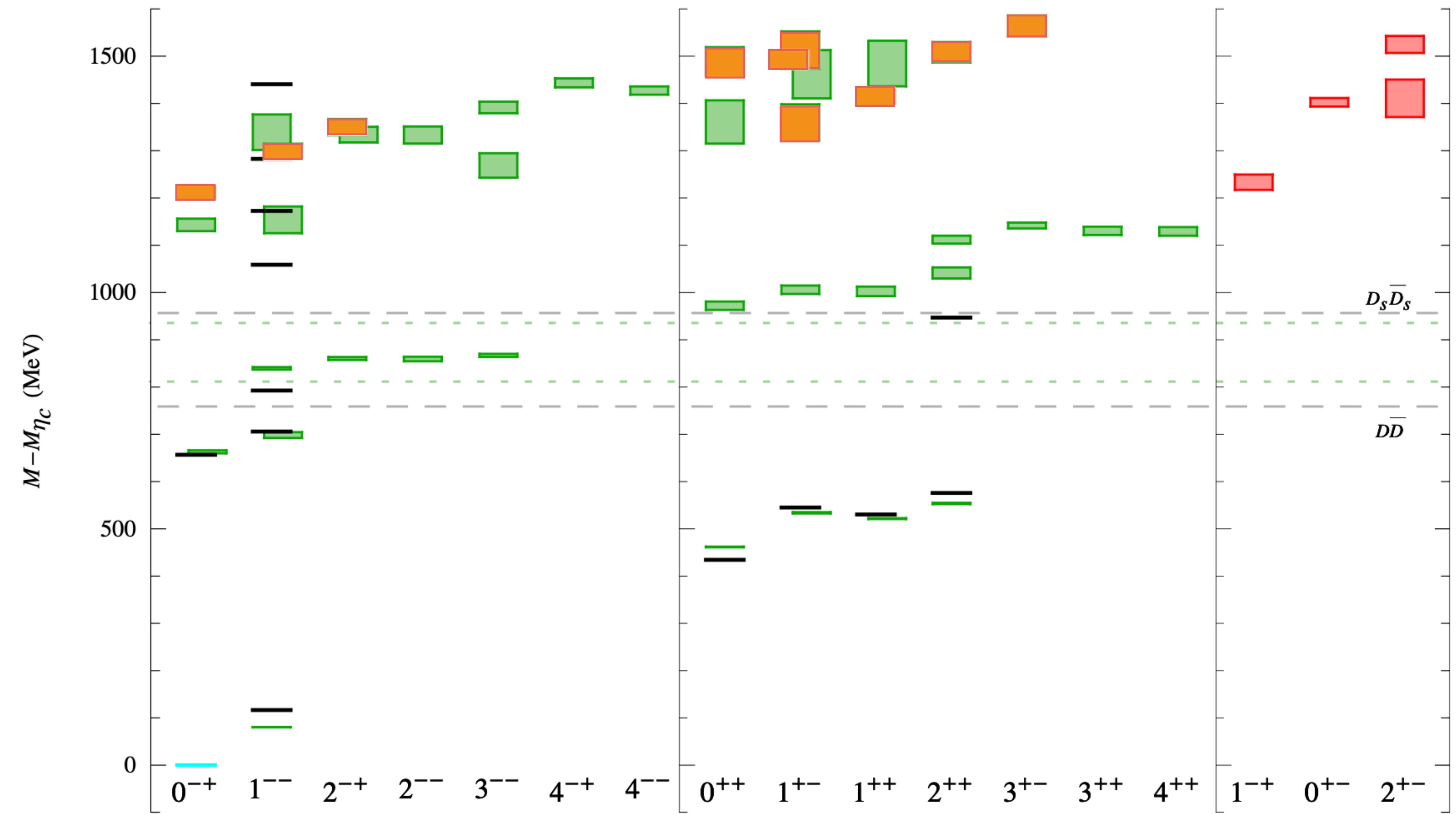


# Multi-quark States



“Vi har nu en model, der på smukke ste vis forklarer data og for første gang indeholder alle de begrænsninger, data giver,” sagde fysikeren Tim Burns fra Swansea University ved offentliggørelsen.

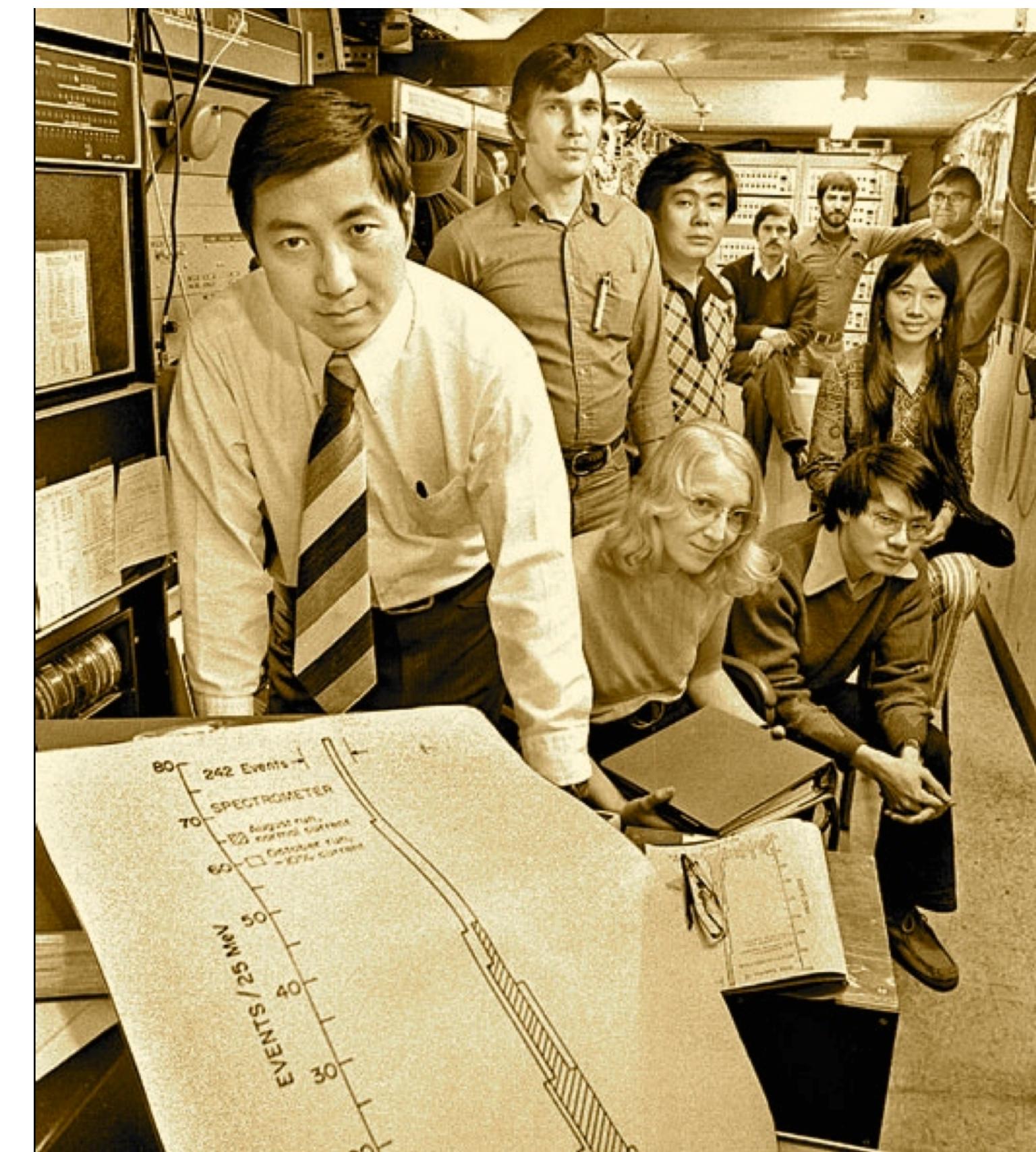
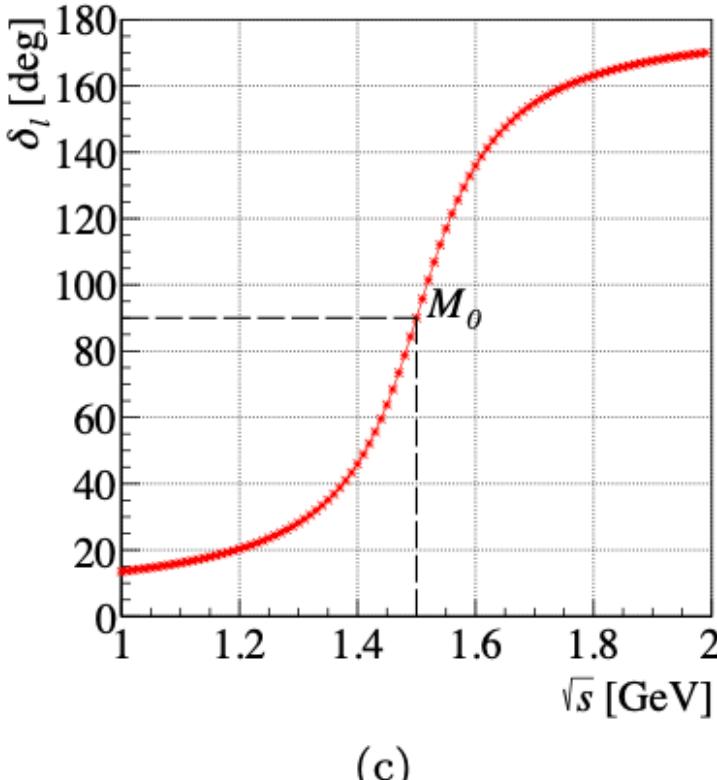
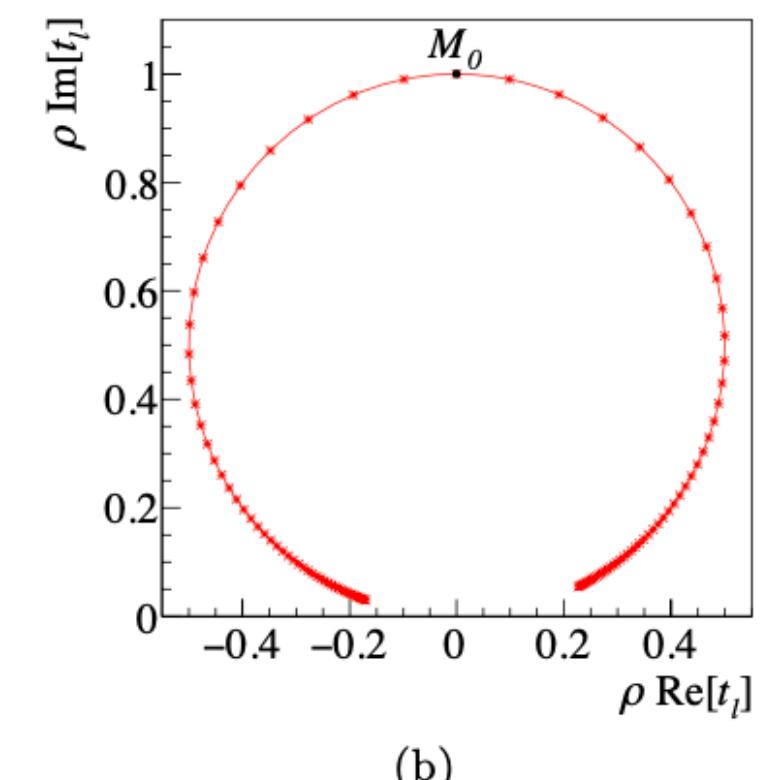
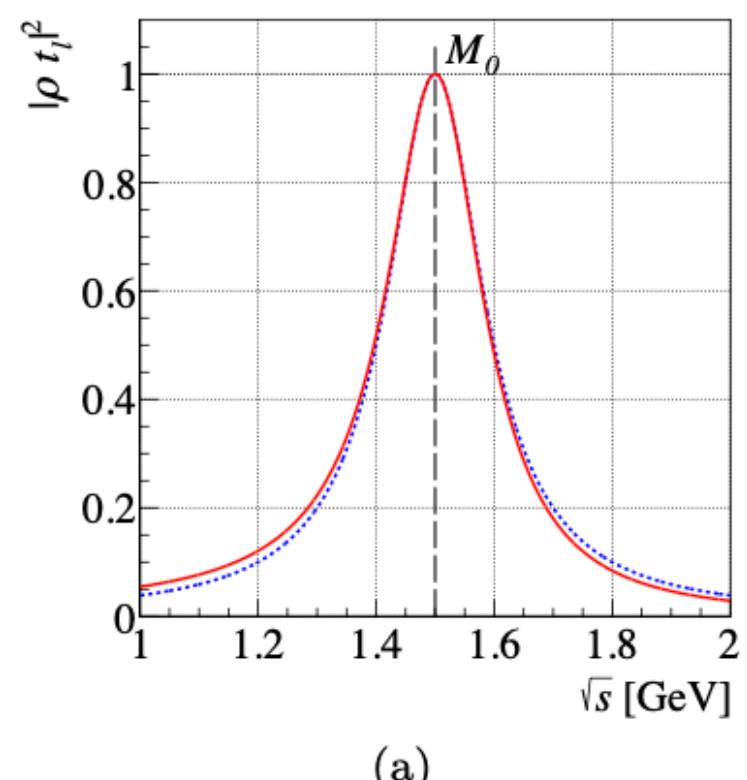
# Gluonic Excitations



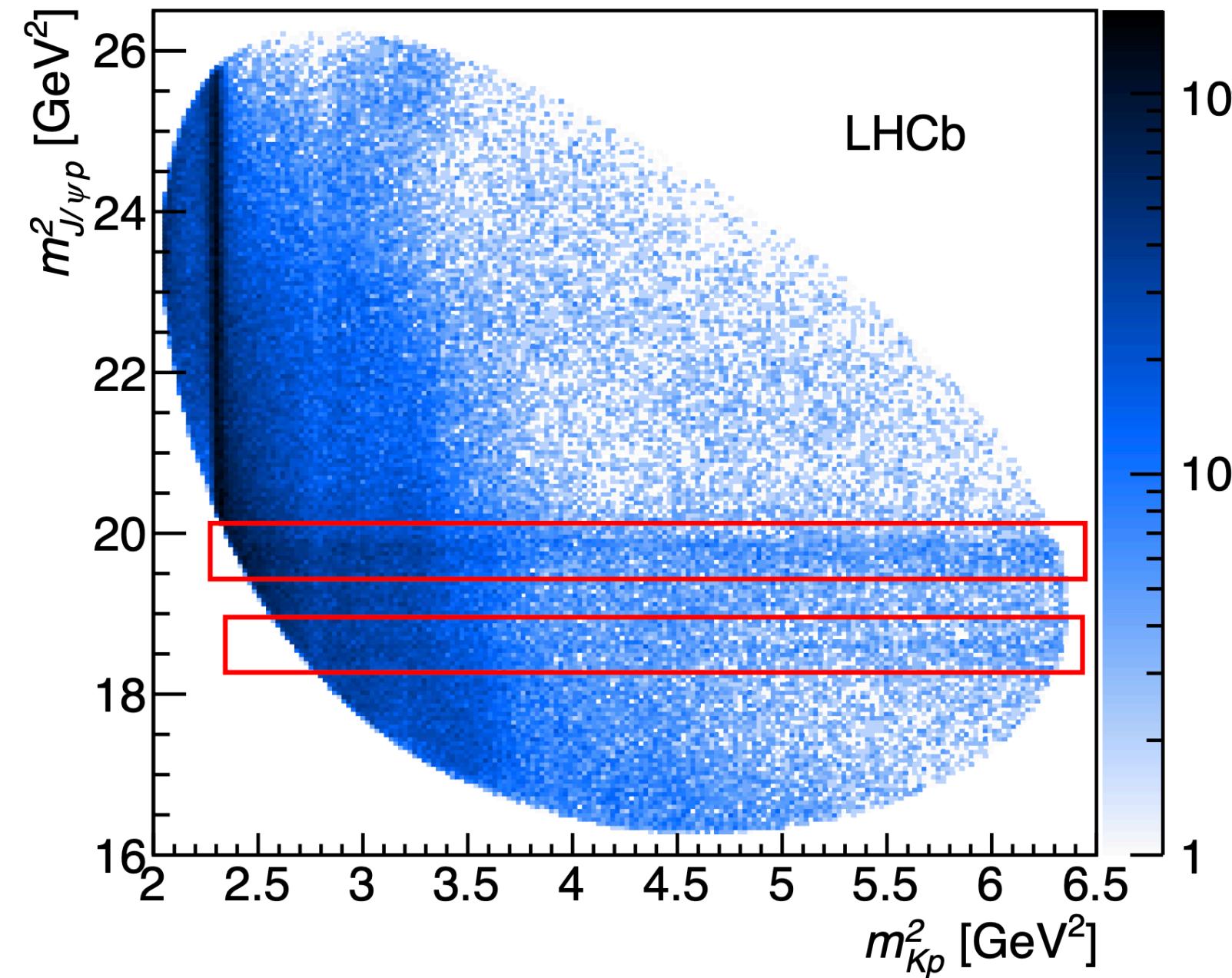
# Comments on "Fitting"

*"Not every bump is a resonance, not every resonance is a bump"* - R. G. Moorhouse (1960s)

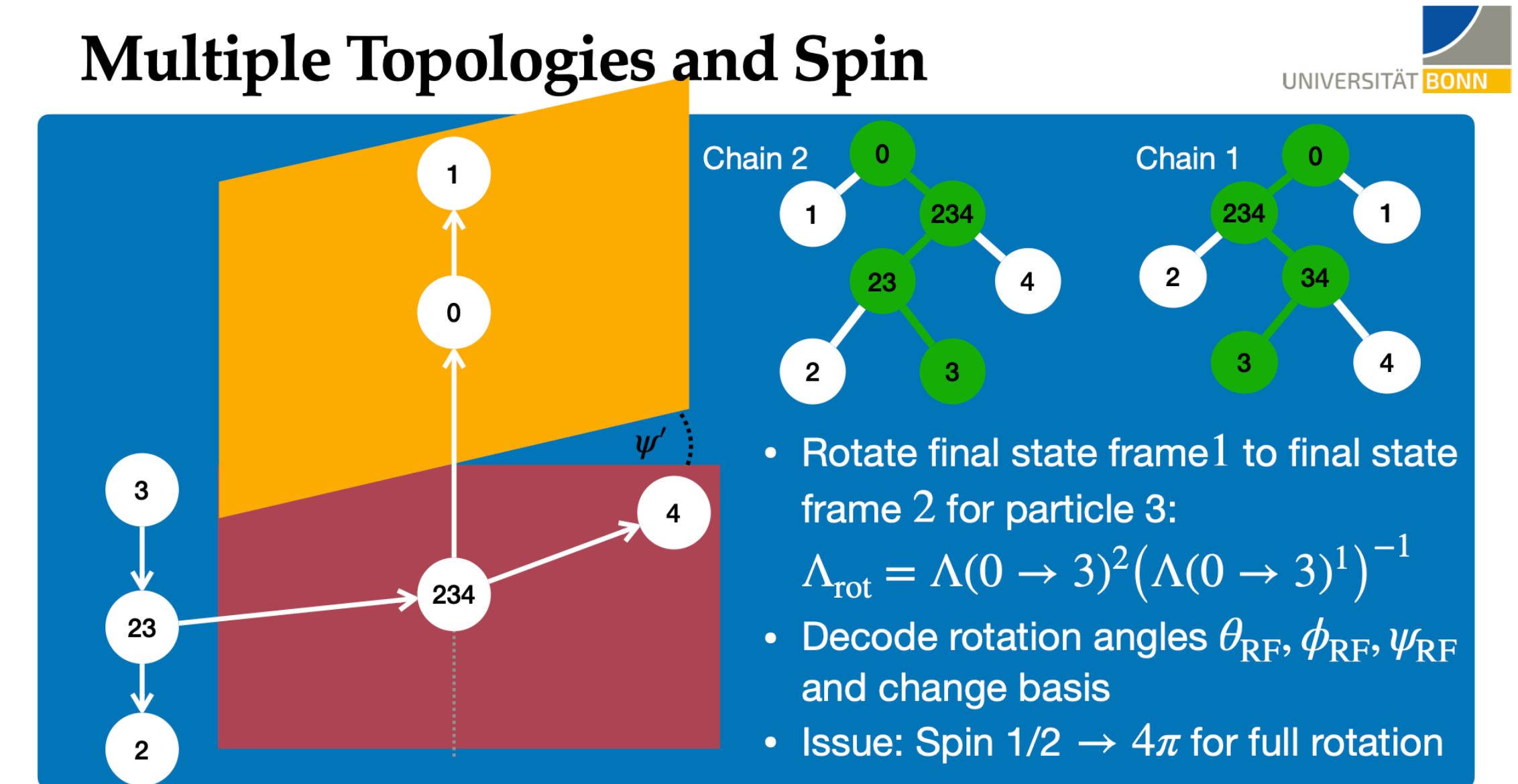
These days are over.



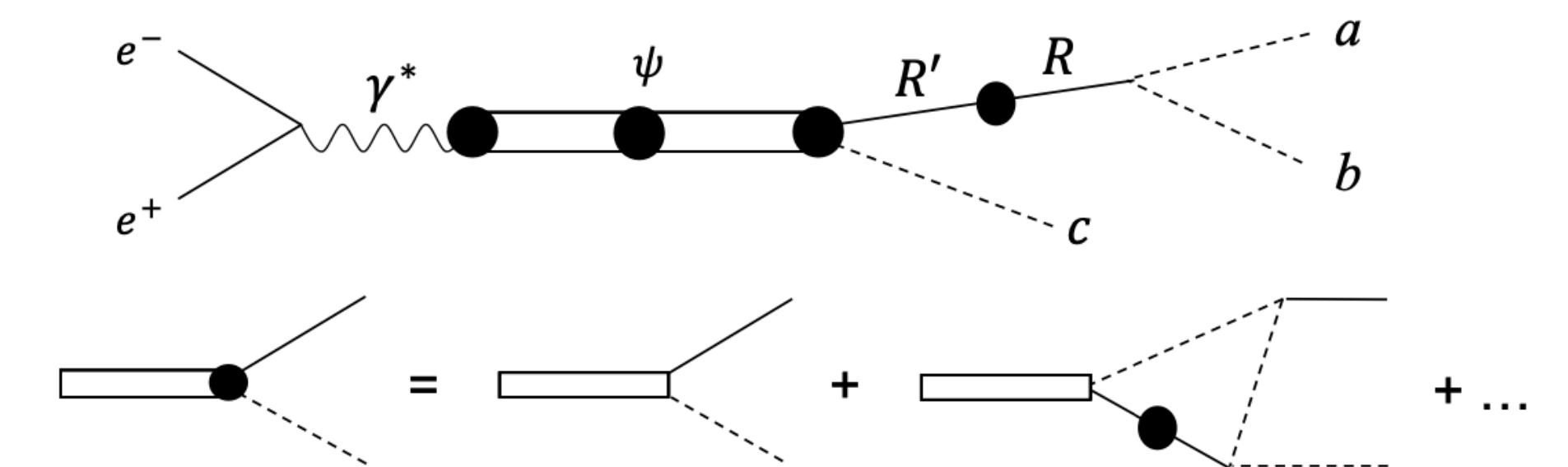
# Present reality.



## Multiple Topologies and Spin

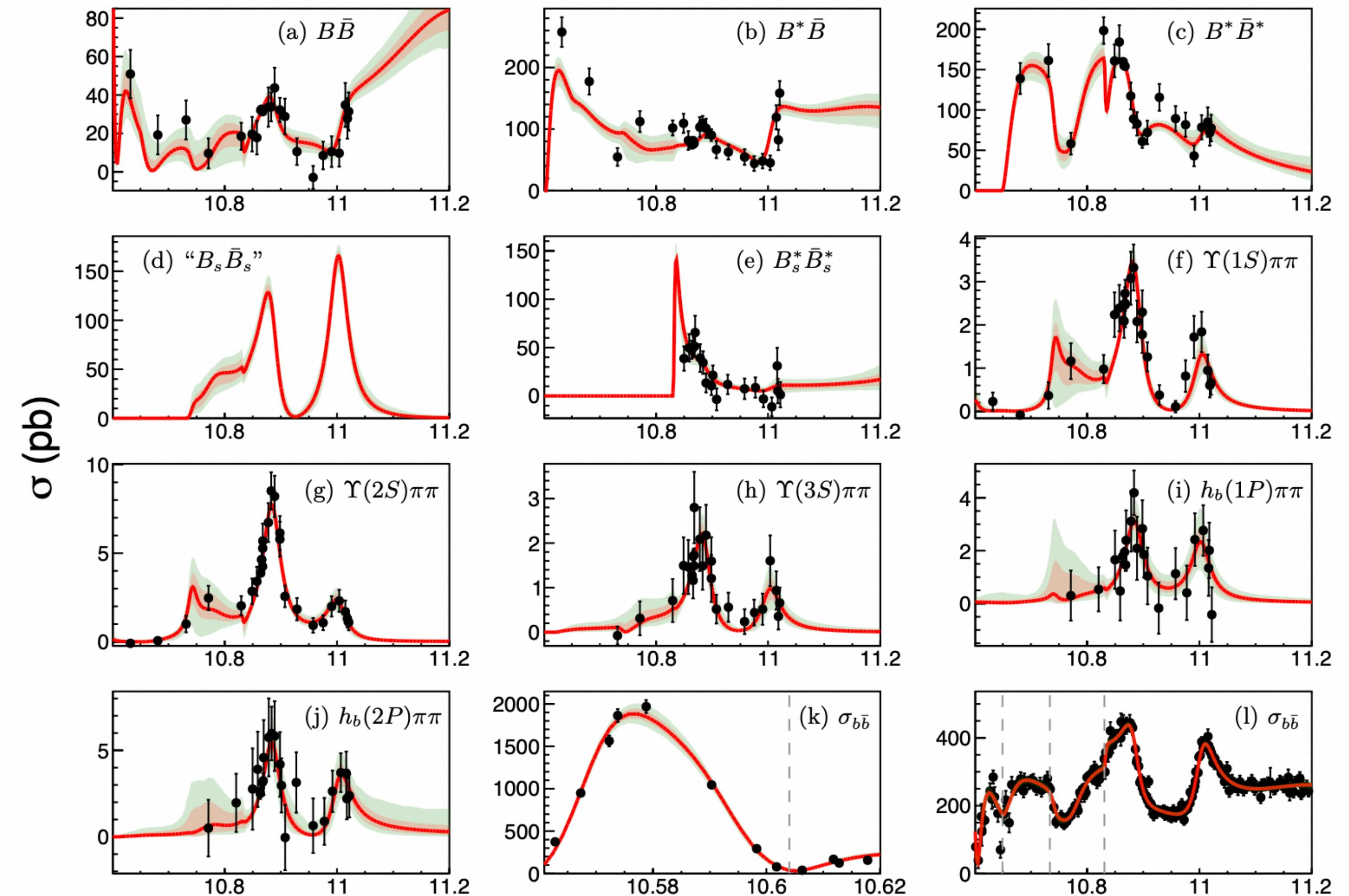
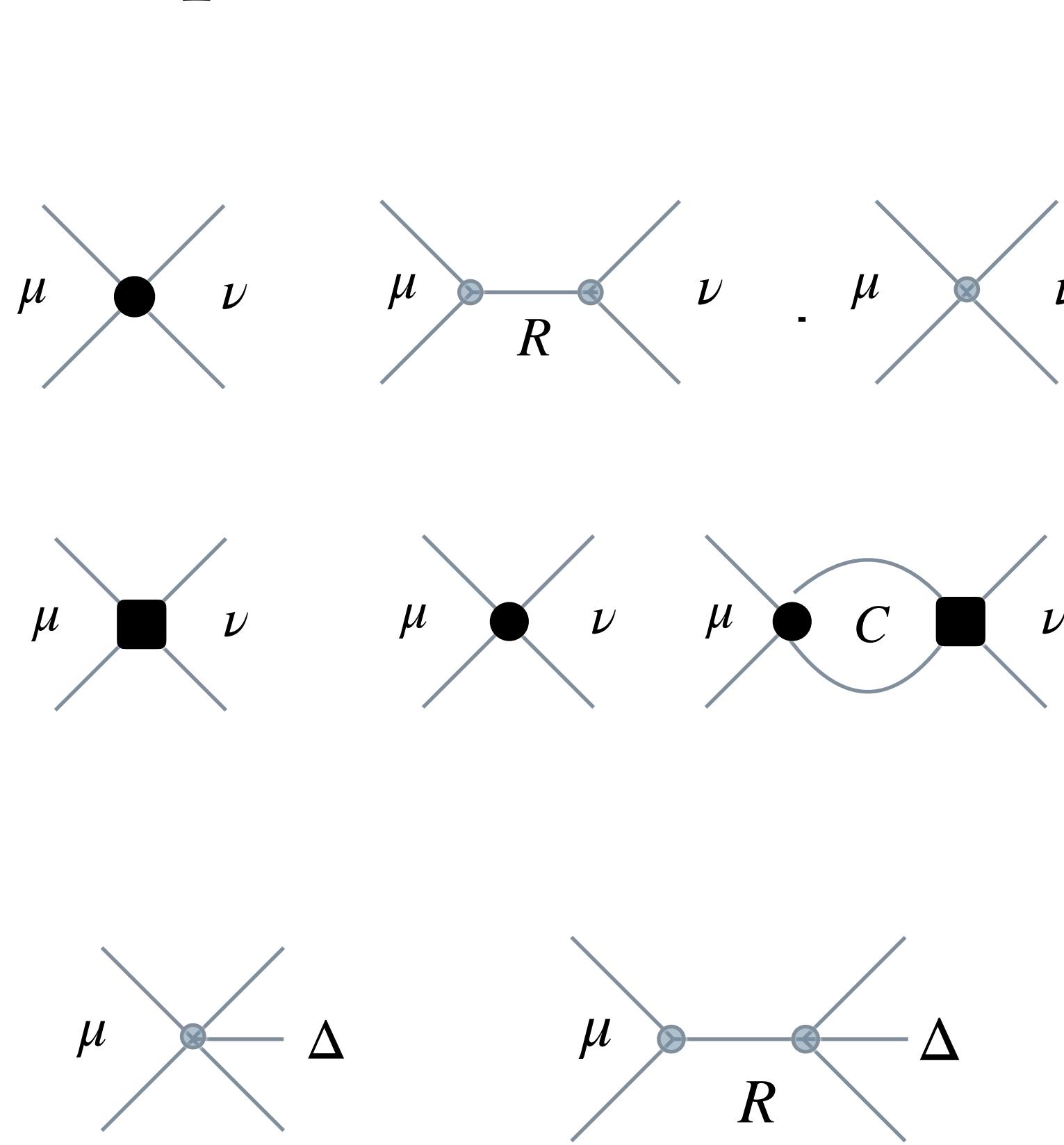


$$I(\Omega, \Phi) = 2\kappa \sum_k \left\{ (1 - P_\gamma) \left| \sum_{\ell,m} [\ell]_{m;k}^{(-)} \text{Re}[Z_\ell^m(\Omega, \Phi)] \right|^2 + (1 - P_\gamma) \left| \sum_{\ell,m} [\ell]_{m;k}^{(+)} \text{Im}[Z_\ell^m(\Omega, \Phi)] \right|^2 + (1 + P_\gamma) \left| \sum_{\ell,m} [\ell]_{m;k}^{(+)} \text{Re}[Z_\ell^m(\Omega, \Phi)] \right|^2 + (1 + P_\gamma) \left| \sum_{\ell,m} [\ell]_{m;k}^{(-)} \text{Im}[Z_\ell^m(\Omega, \Phi)] \right|^2 \right\}$$



# Vector Bottomonium

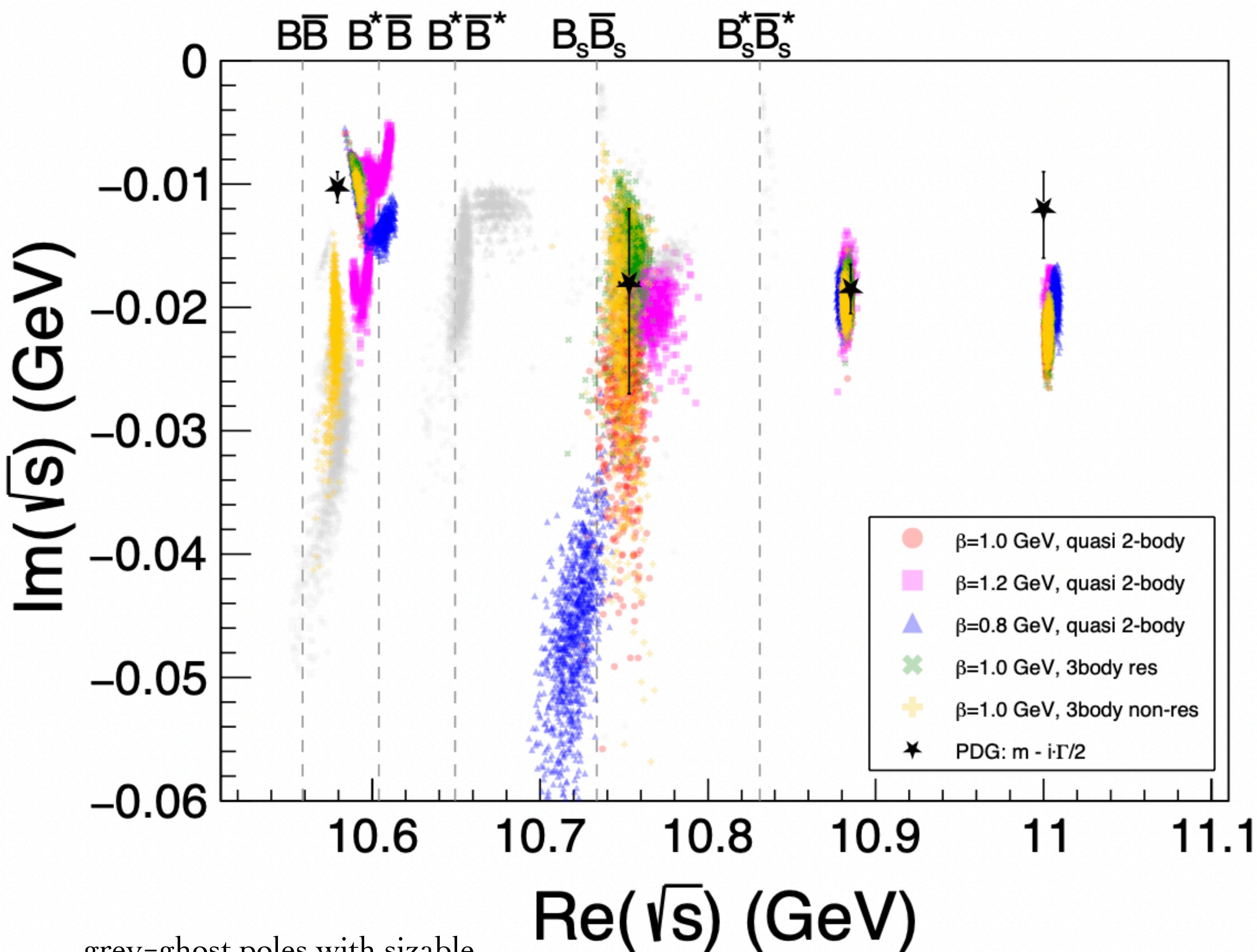
# Coupled channel K-matrix



N. Hüsken, R.E. Mitchell,  
E.S. Swanson, 2204.11915

$\sqrt{s}$  (GeV)  
quasi two-body, beta=1, fit+68% and 90% CL regions

pole positions (+ 1000 bootstrap datasets)

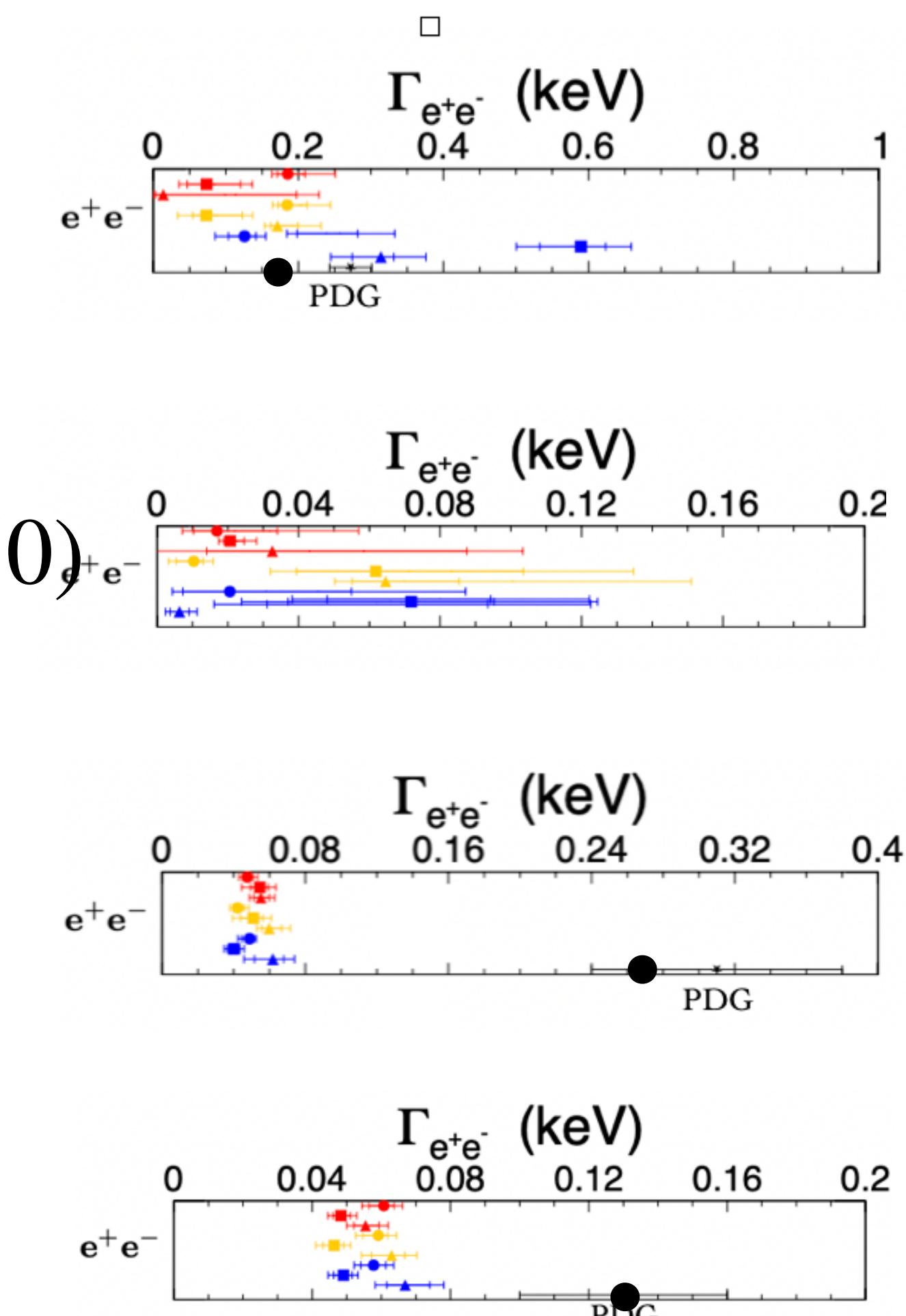


$\Upsilon(4S)$

$\Upsilon(10750)$

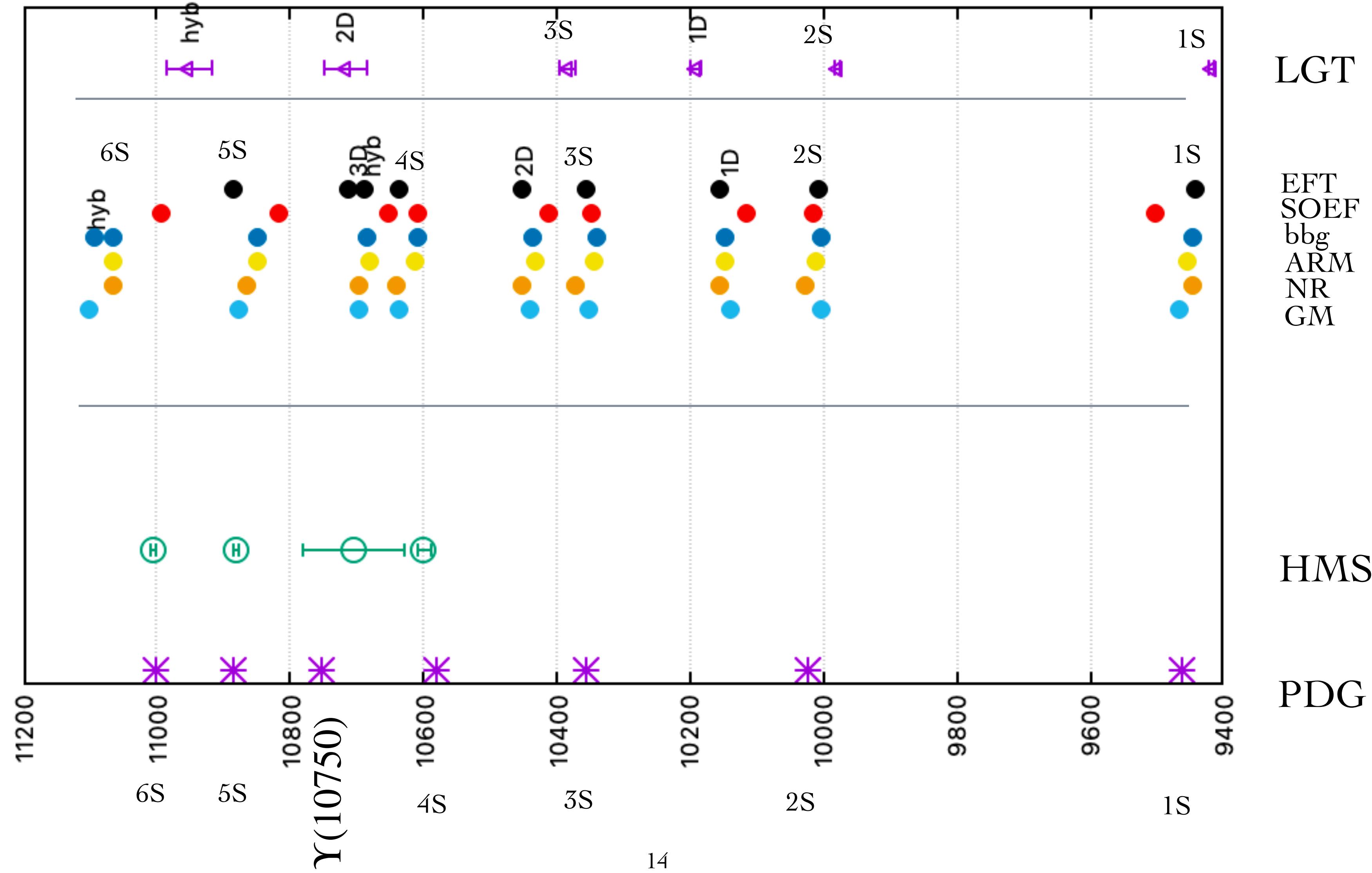
$\Upsilon(5S)$

$\Upsilon(6S)$

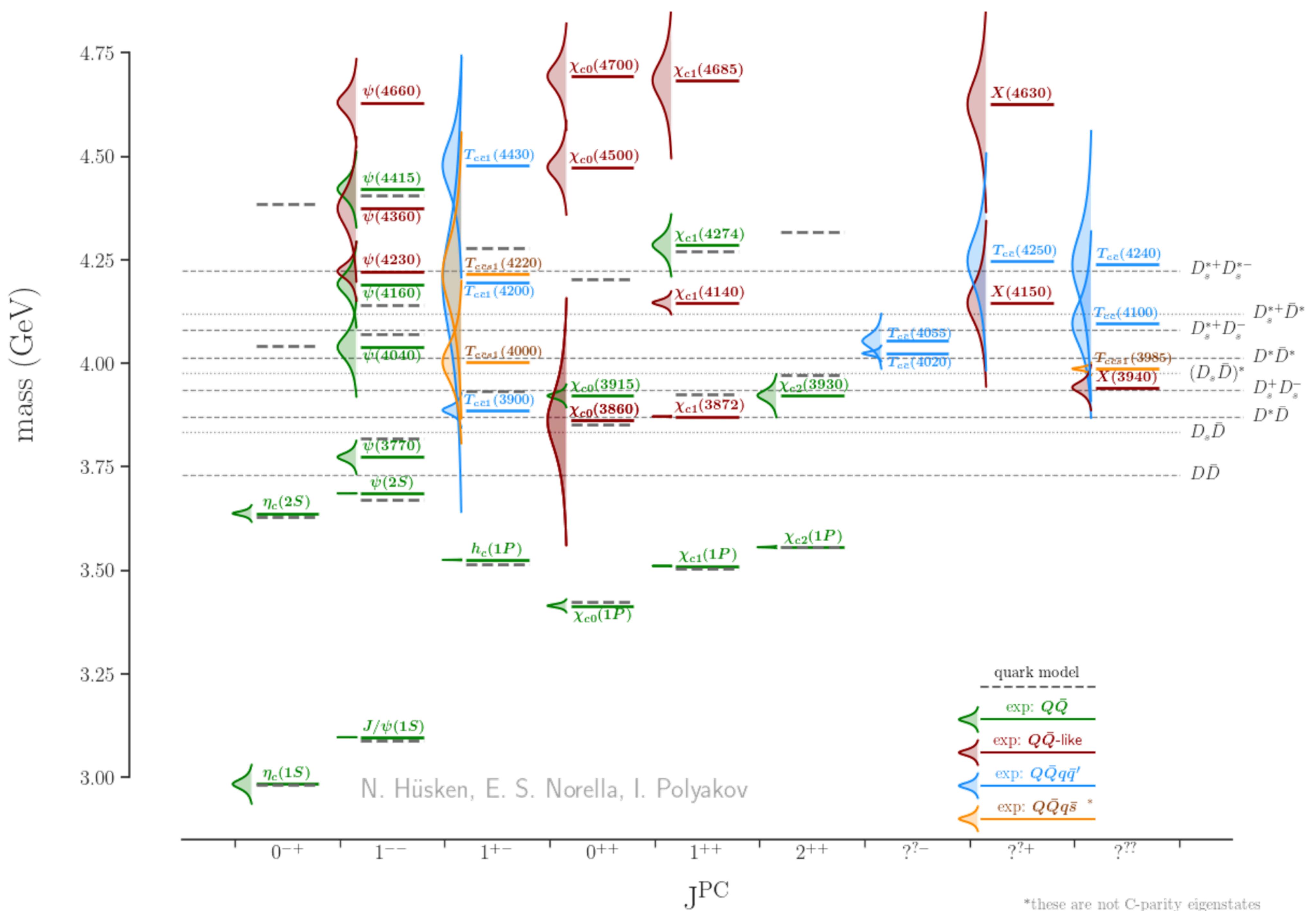


# "masses"

[BW params, poles, quark model eigenvalues, LGT plateaus]



# Charmonia



$\psi(4660)$

$\psi(4415)$

$\psi(4360)$

$\psi(4230)$

$\psi(4160)$

$\psi(4040)$

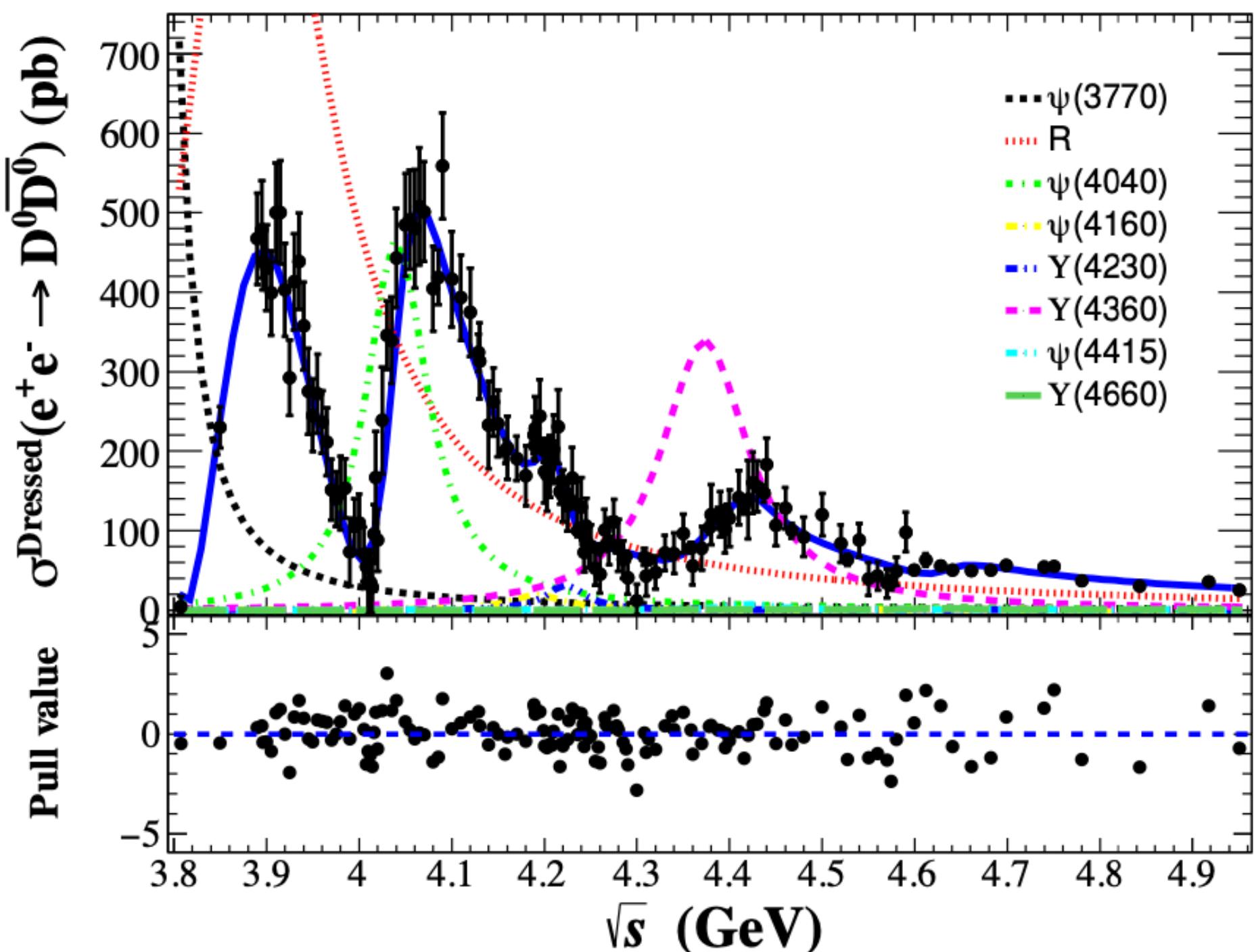
$\psi(3770)$

$\psi(2S)$

$J/\psi(1S)$

# The R(3900) [prev. G(3900)]

$e^+e^- \rightarrow D\bar{D}$



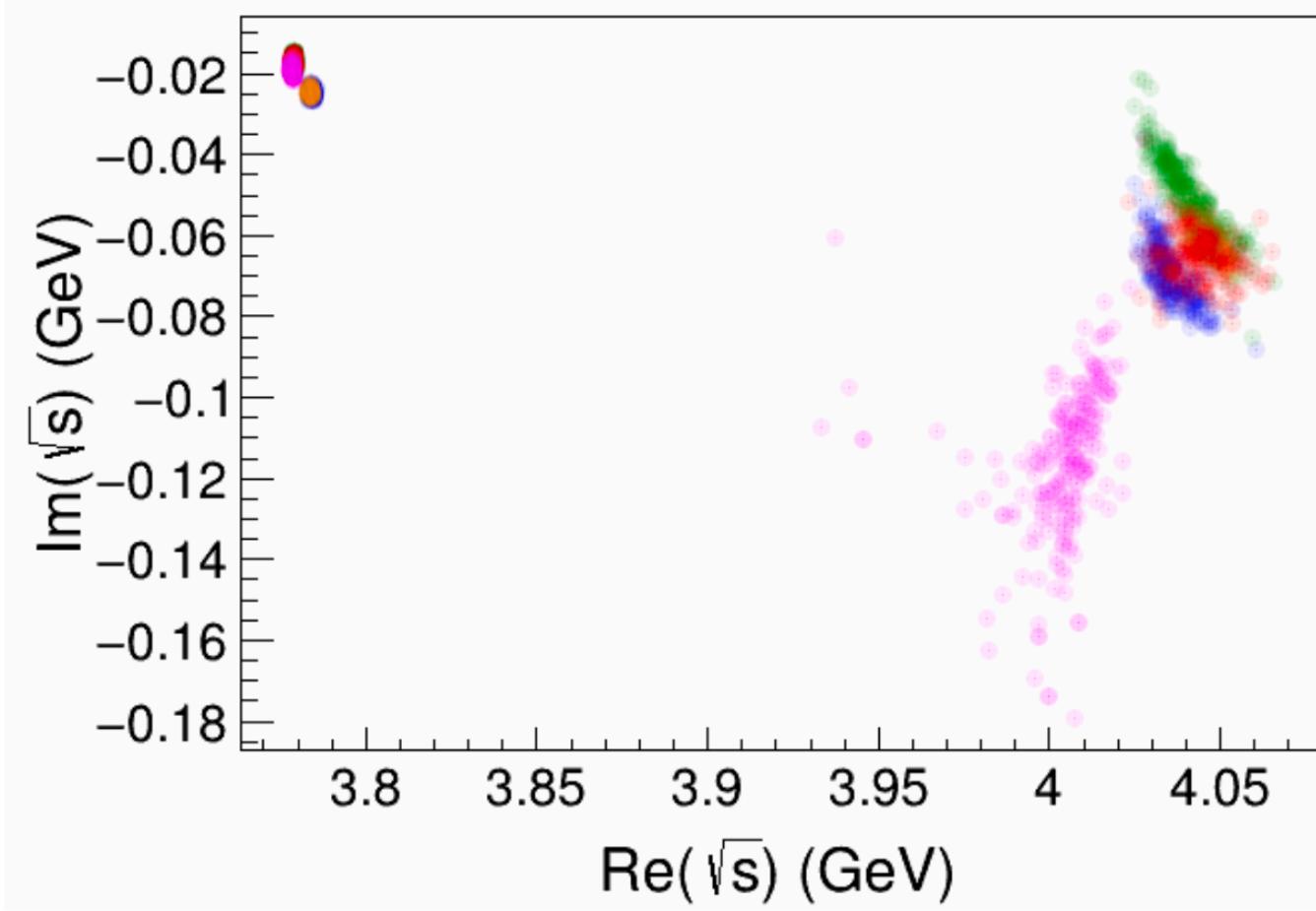
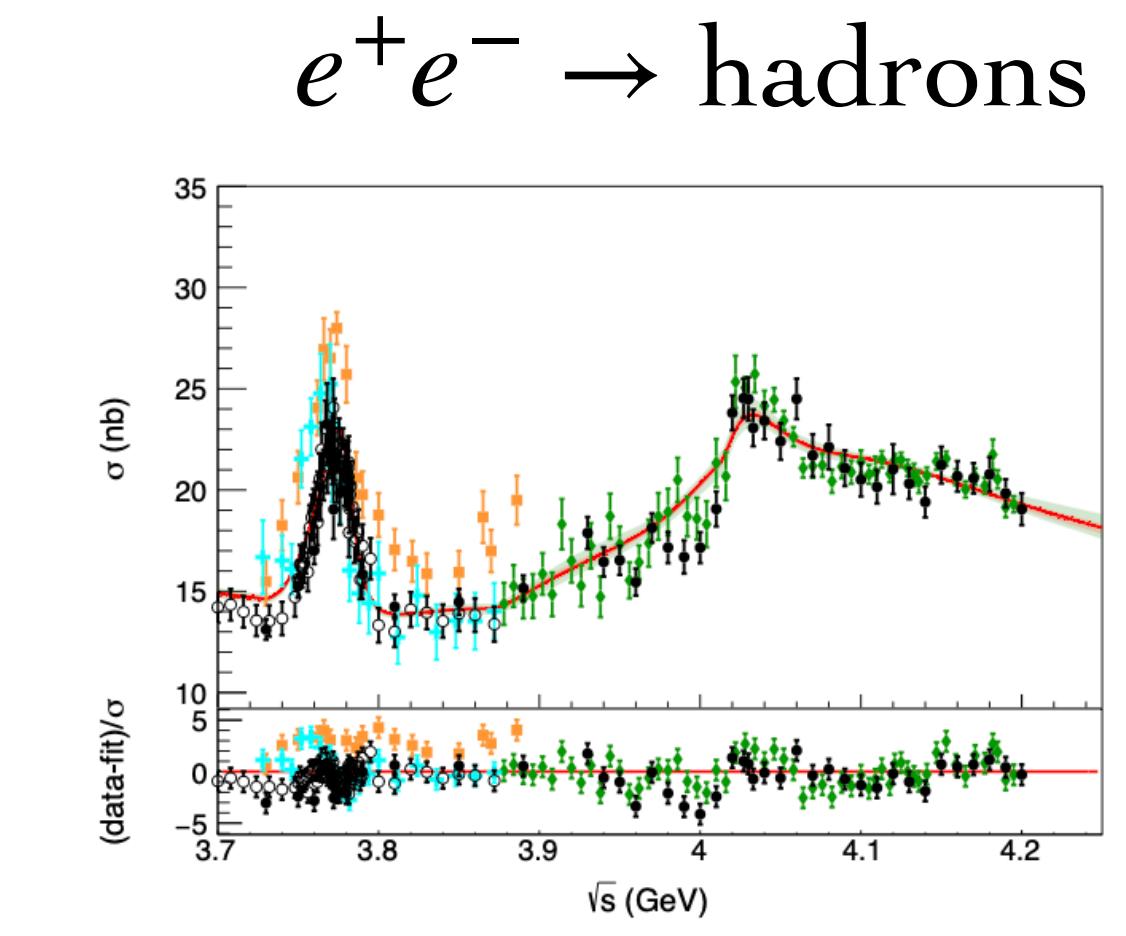
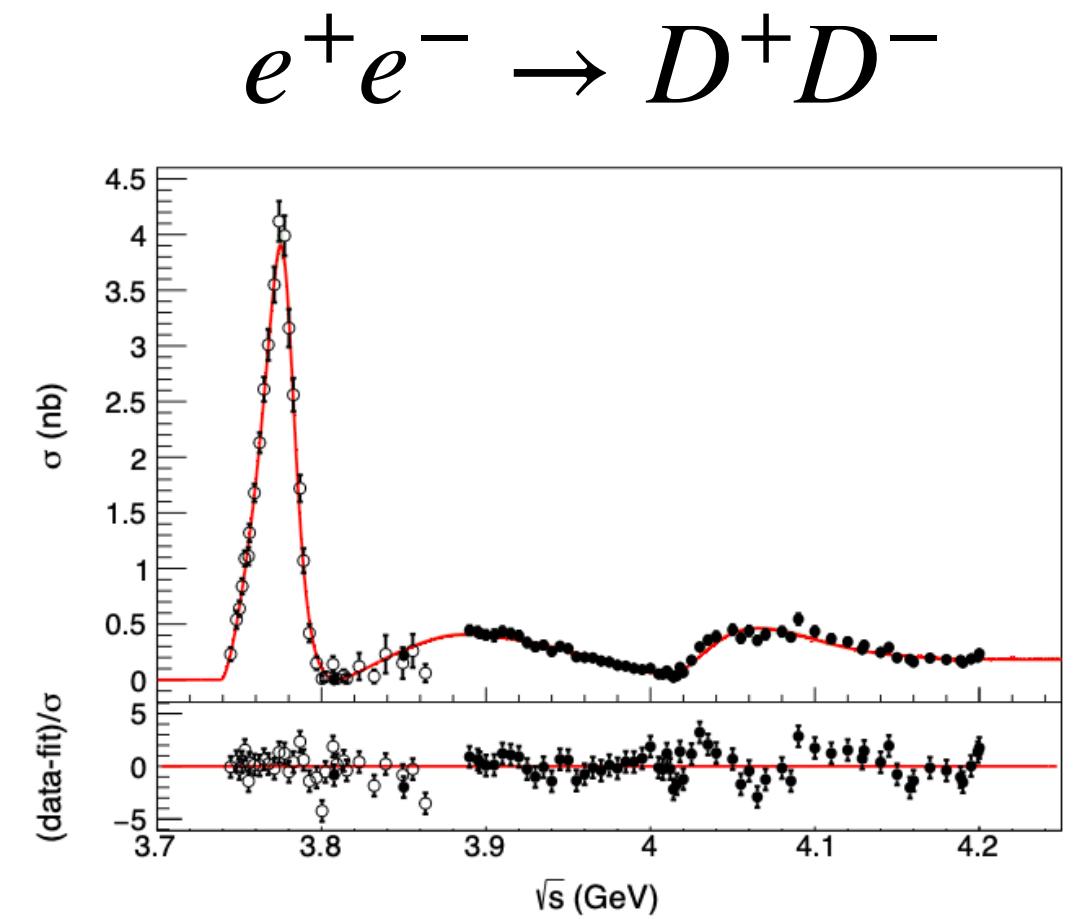
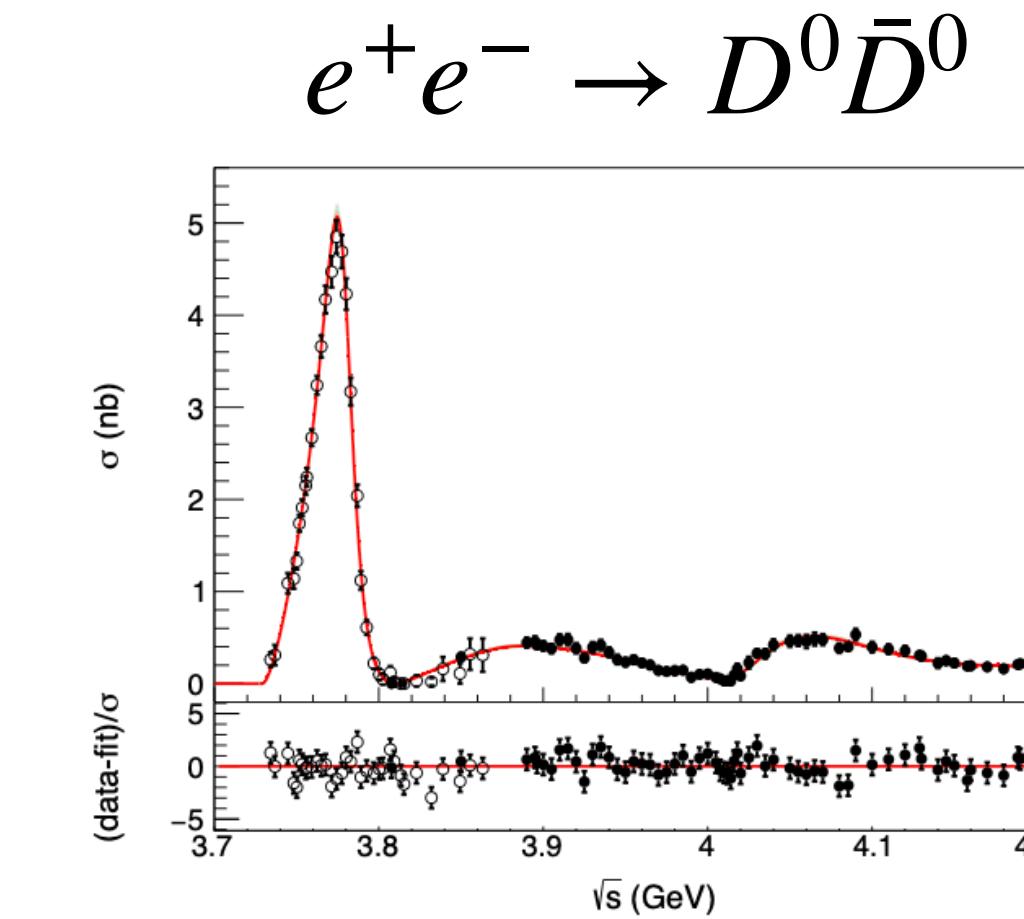
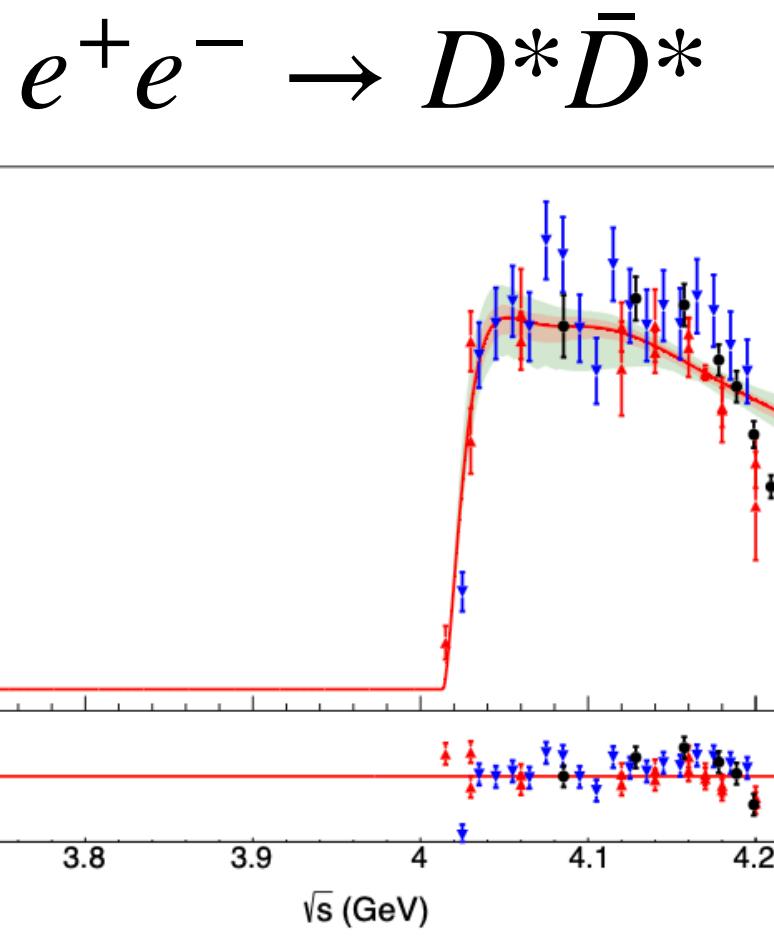
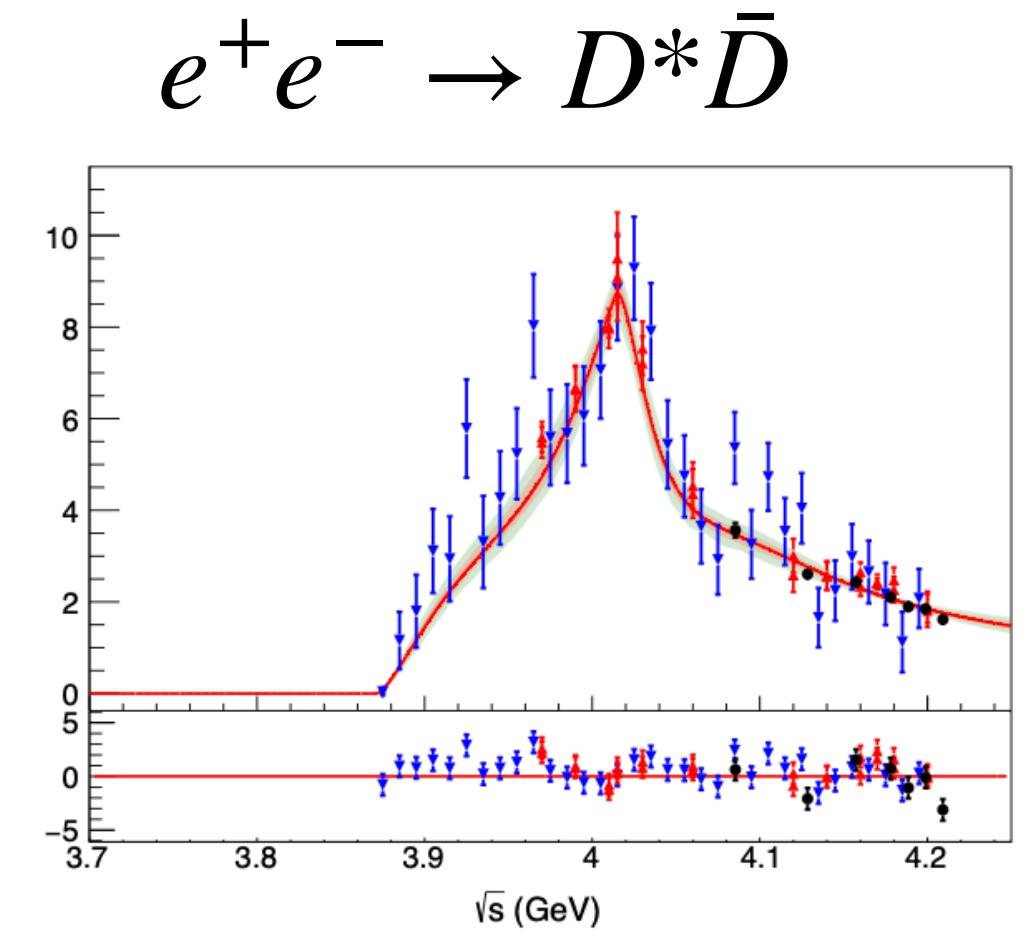
BESIII, 2402.03829

TABLE I. Fit results of the Born cross section, where the first uncertainties are the statistical and the second are systematic and S denotes the significance.

Resonance	$e^+e^- \rightarrow D\bar{D}$							
	$\psi(3770)$	$R$	$\psi(4040)$	$\psi(4160)$	$Y(4230)$	$Y(4360)$	$\psi(4415)$	$Y(4660)$
Mass ( $\text{MeV}/c^2$ )	3773.7 (fixed)	$3872.5 \pm 14.2 \pm 3.0$	4039 (fixed)	4191 (fixed)	4222.5 (fixed)	4374 (fixed)	4421 (fixed)	4630 (fixed)
Width ( $\text{MeV}/c^2$ )	87.6 (fixed)	$179.7 \pm 14.1 \pm 7.0$	80 (fixed)	70 (fixed)	48 (fixed)	118 (fixed)	62 (fixed)	72 (fixed)
$\Gamma_{ee}\mathcal{B}$ (eV)	95-106	202-292	41-44	1-2	1-2	50-144	0-2	0-1
S( $\sigma$ )	10	> 20	13	7	11	11	4	8
$\chi^2/\text{d.o.f}$	346/275							p-value = 0.002

# Analyse coupled channels with K-matrix

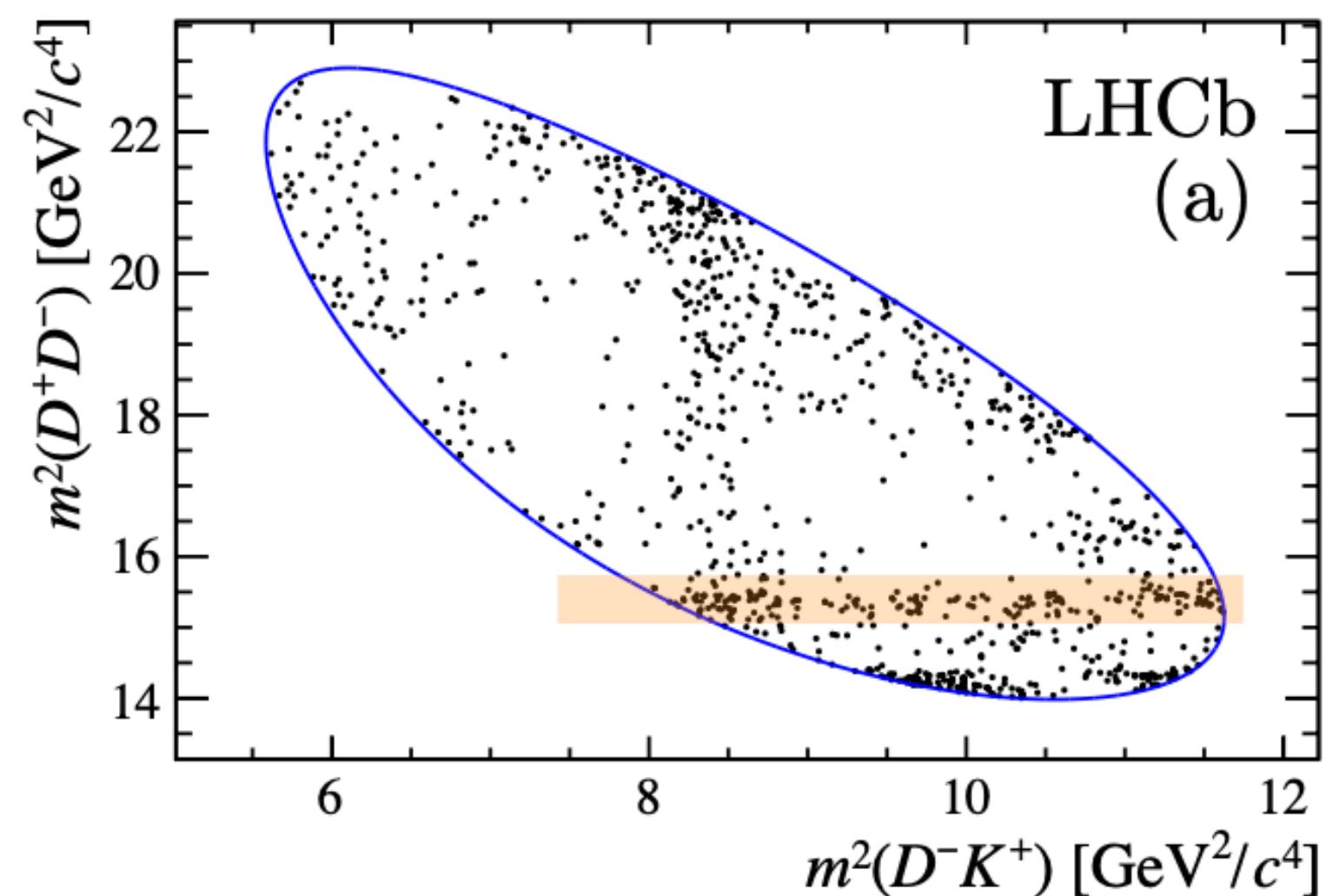
Feature is explained by channel threshold & interference



# Canonical Charmonia

$\chi_{c0}(3930)$  &  $\chi_{c2}(3930)$

## $B^+ \rightarrow D^+ D^- K^+$ Dalitz Plot

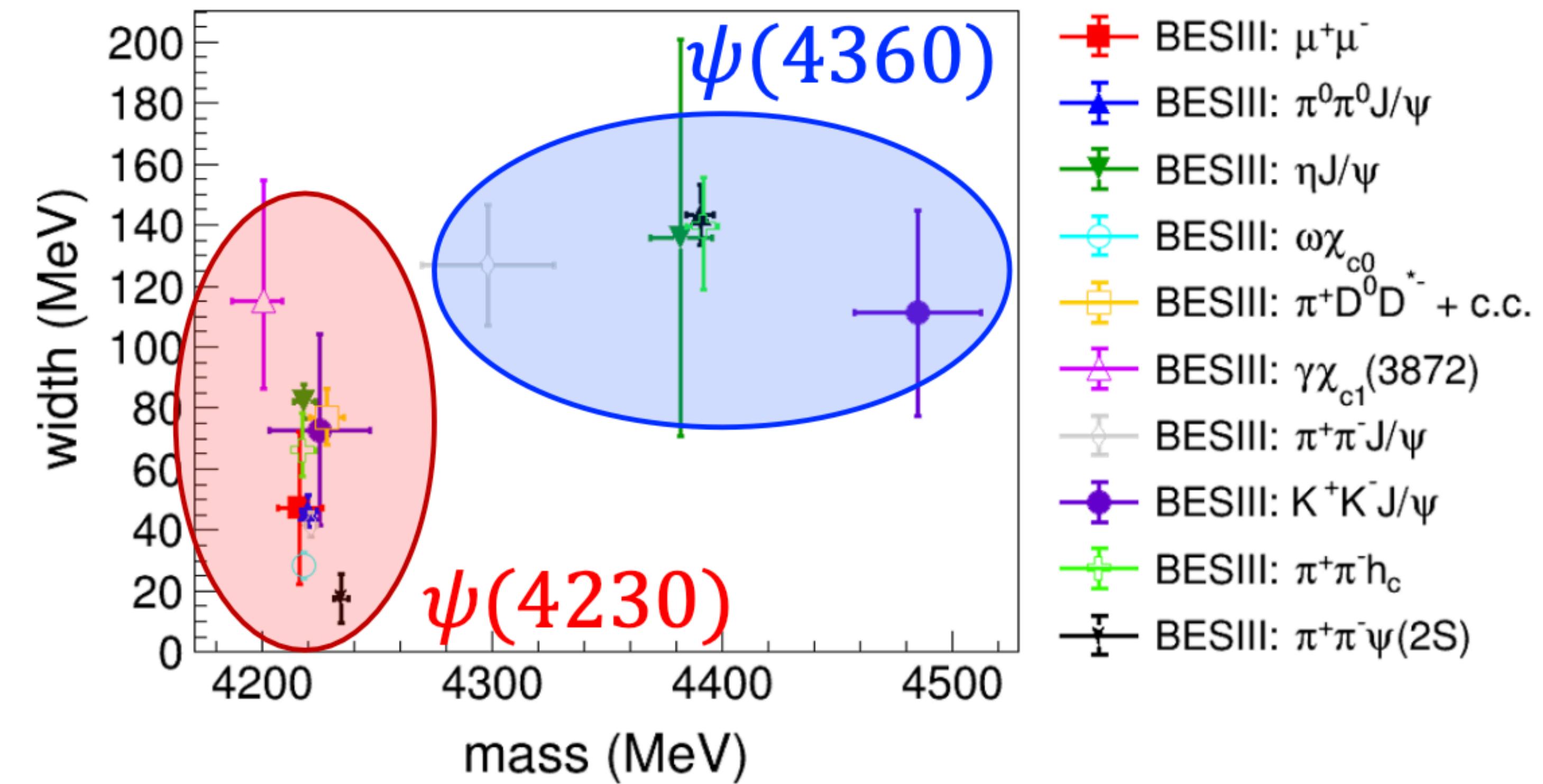
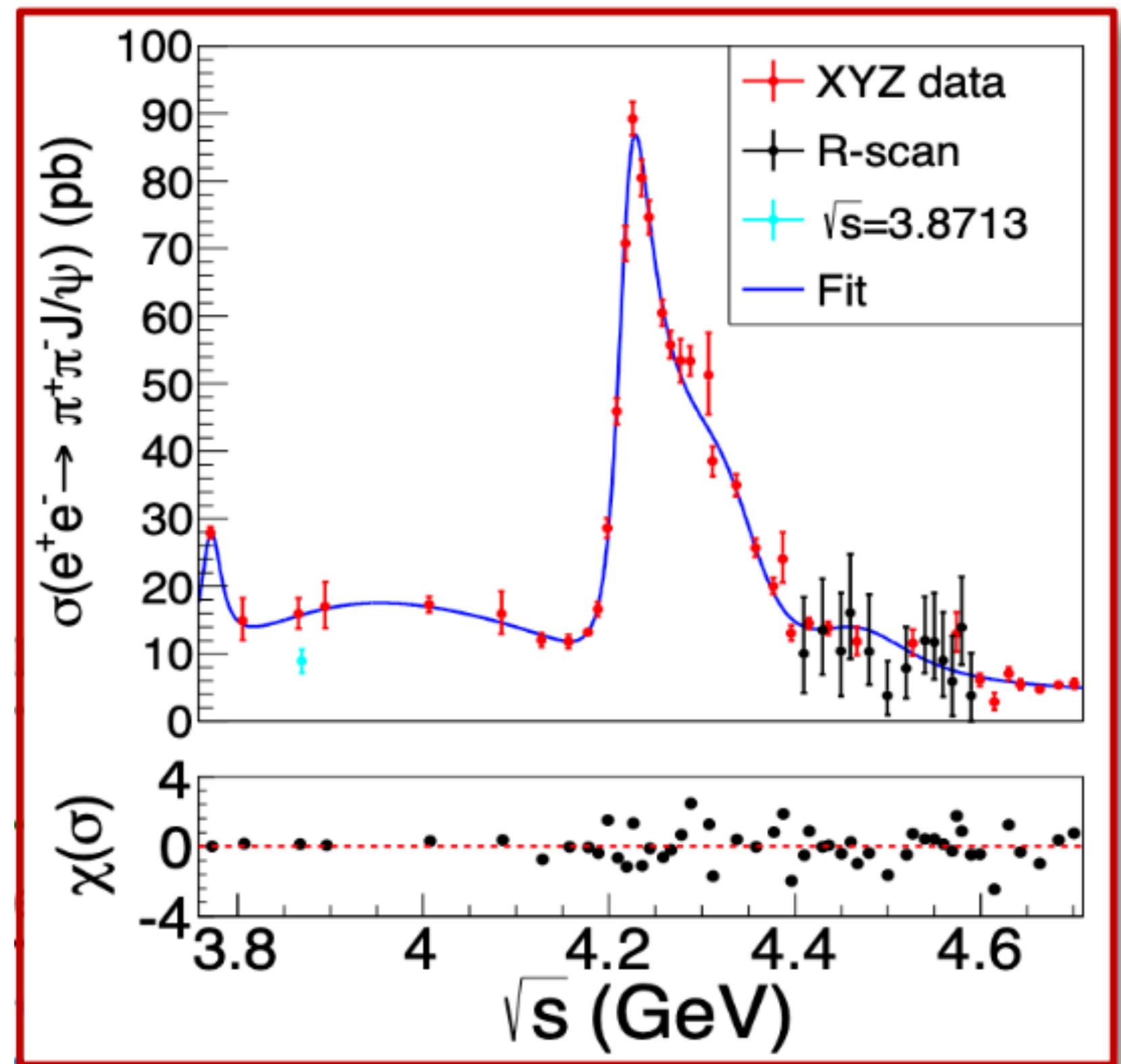


Previously observed  $\chi_c(3930)$   
seen as two states

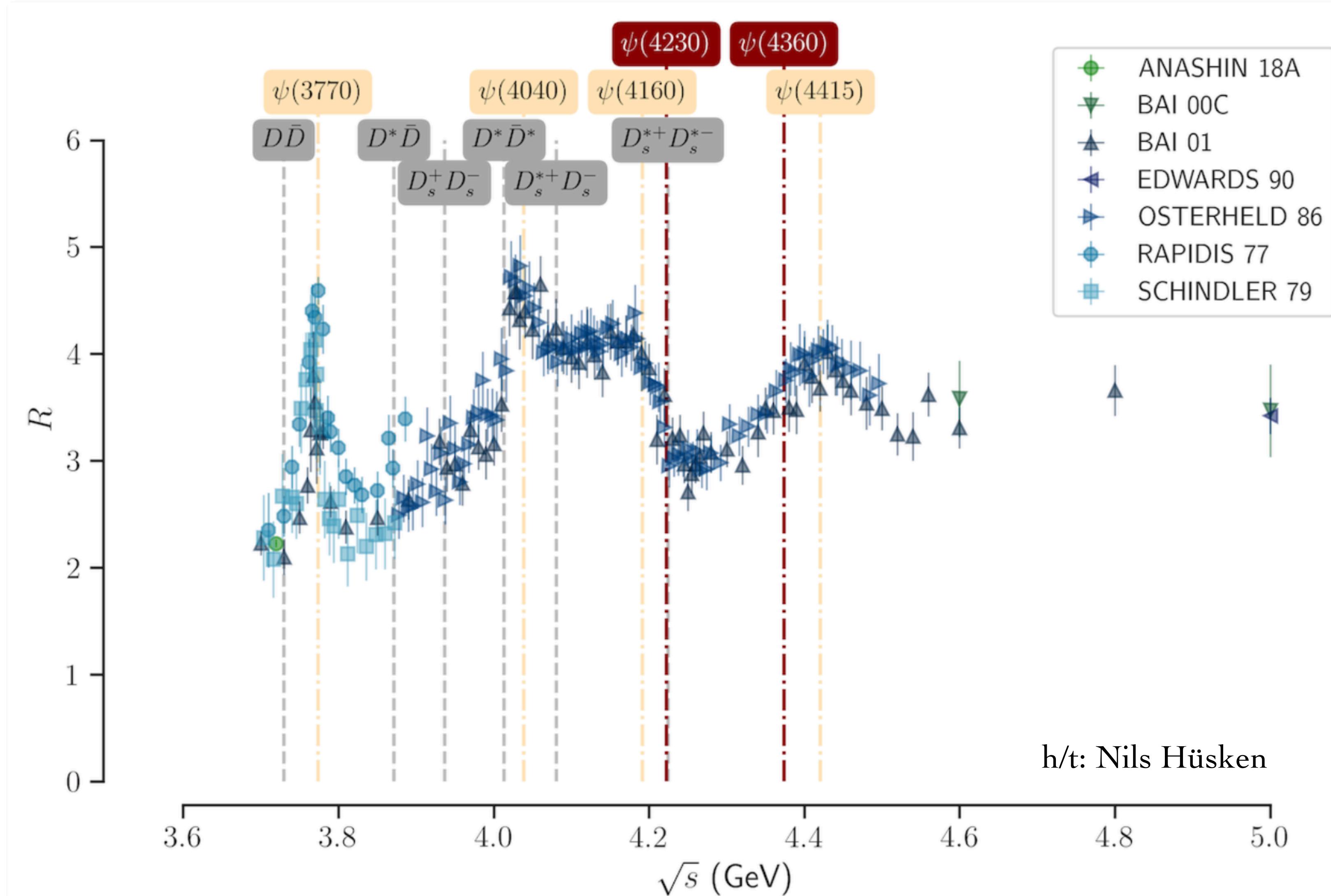
$\chi_{c0}(3930)$

$\chi_{c2}(3930)$

$\psi(4320)$  &  $\psi(4360)$



\* PRD 106 (2022) 7, 072001

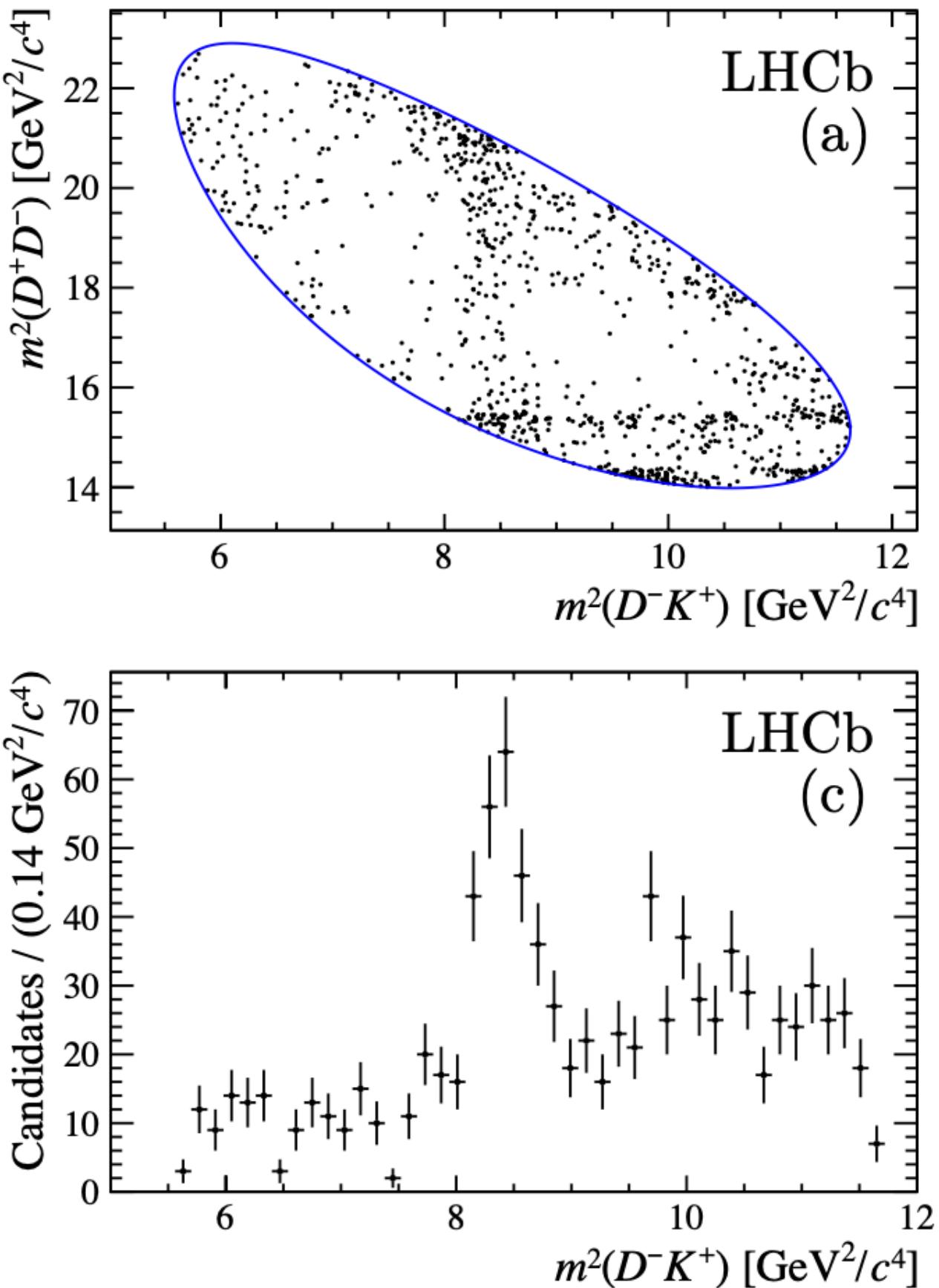


The situation is even worse: we rely on  $R$  for much information! This is not reliable!

# Tetraquarks

X(2900)

$$B^+ \rightarrow D^+ D^- K^+$$

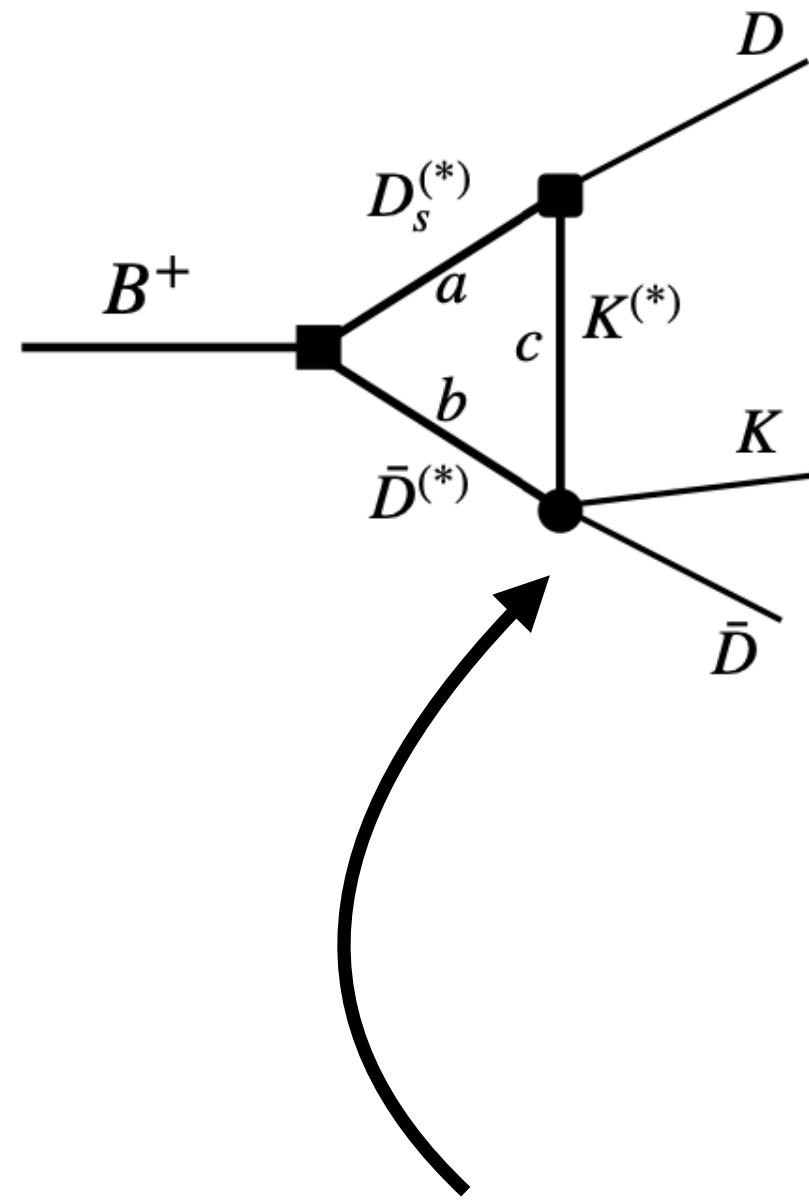


LHCb, arXiv:2009.00026.

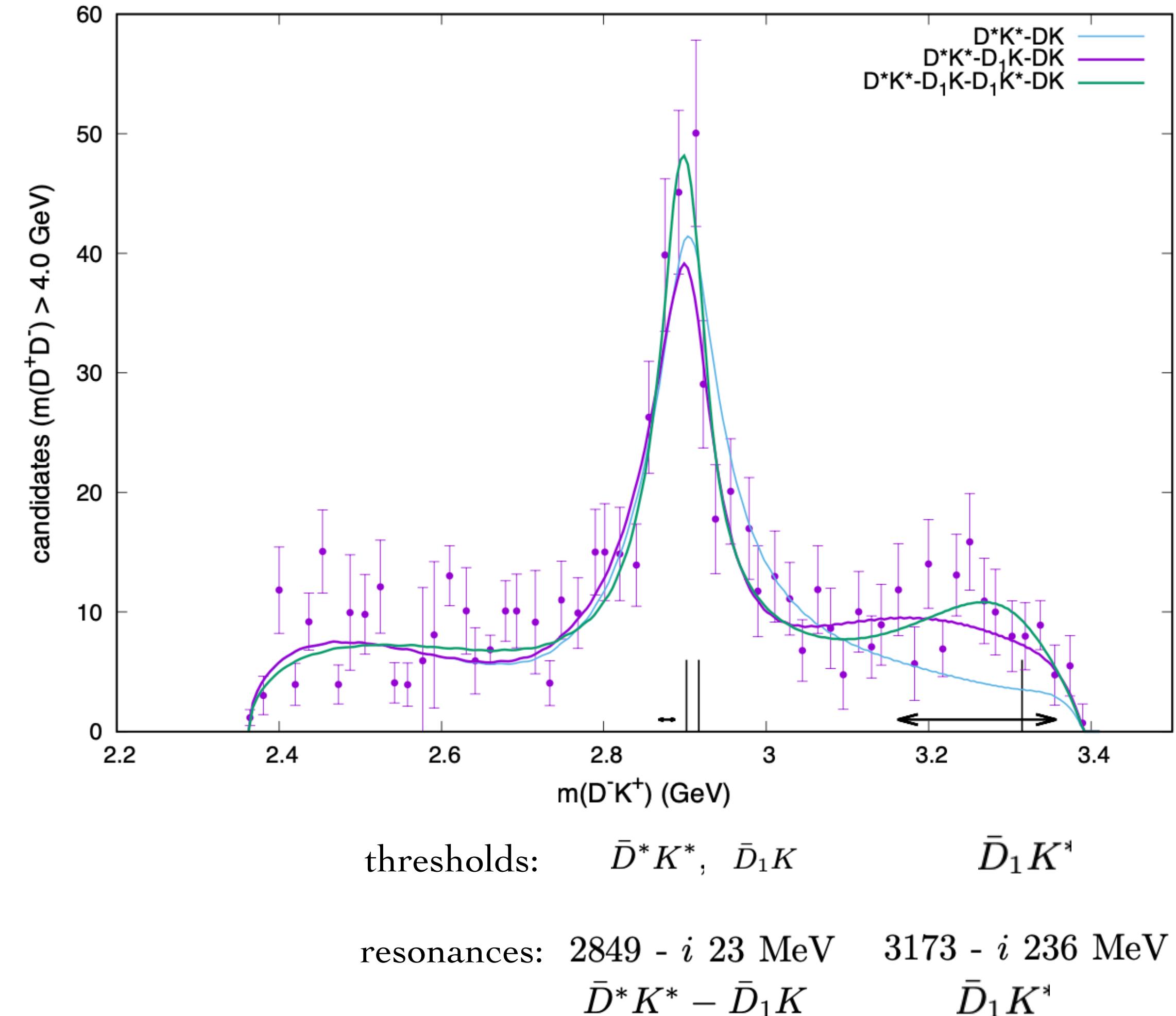
$$X_0 \quad M = 2.866 \pm 0.007 \pm 0.002 \text{ GeV}, \\ \Gamma = 57 \pm 12 \pm 4 \text{ MeV},$$

$$X_1 \quad M = 2.904 \pm 0.005 \pm 0.001 \text{ GeV}, \\ \Gamma = 110 \pm 11 \pm 4 \text{ MeV}.$$

manifestly exotic channel  $ud\bar{s}\bar{c}$



$\lambda(1^-)$	$\bar{D}^*K^* _P$	$\bar{D}_1K _S$	$\bar{D}_1K^* _S$	$\bar{D}K _P$
$D^*K^* _P$	$C_1$	$C_2$	$C_3$	$C_4$
$\bar{D}_1K _S$	0	$C_5$	0	
$\bar{D}_1K^* _S$		$C_6$	0	
$\bar{D}K _P$			0	



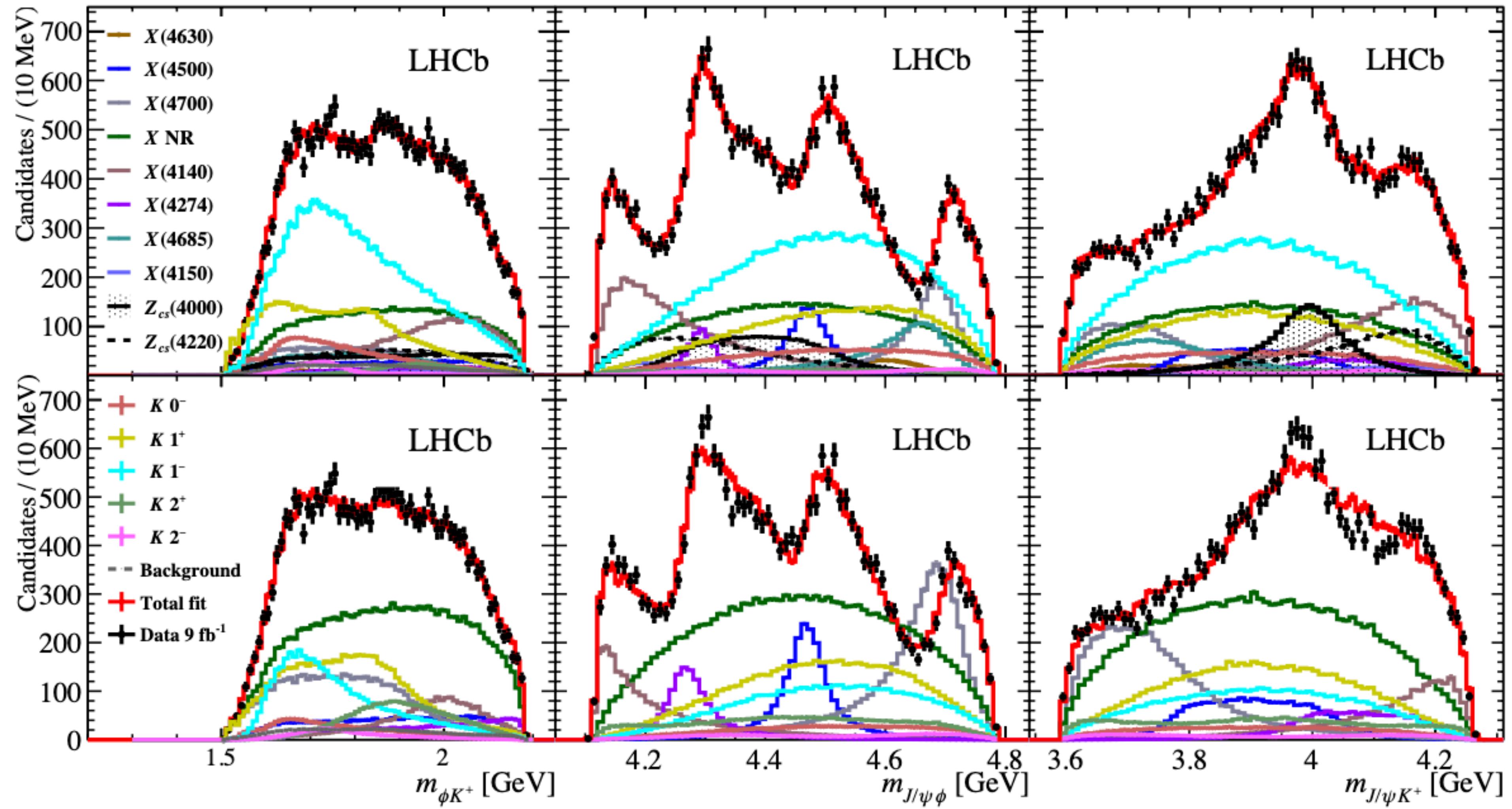
Production matters!

a resonance interpretation is possible,  
but has weak evidence

$Z_{cs}(4000), Z_{cs}(4220), X(4140), X(4150), X(4274)$

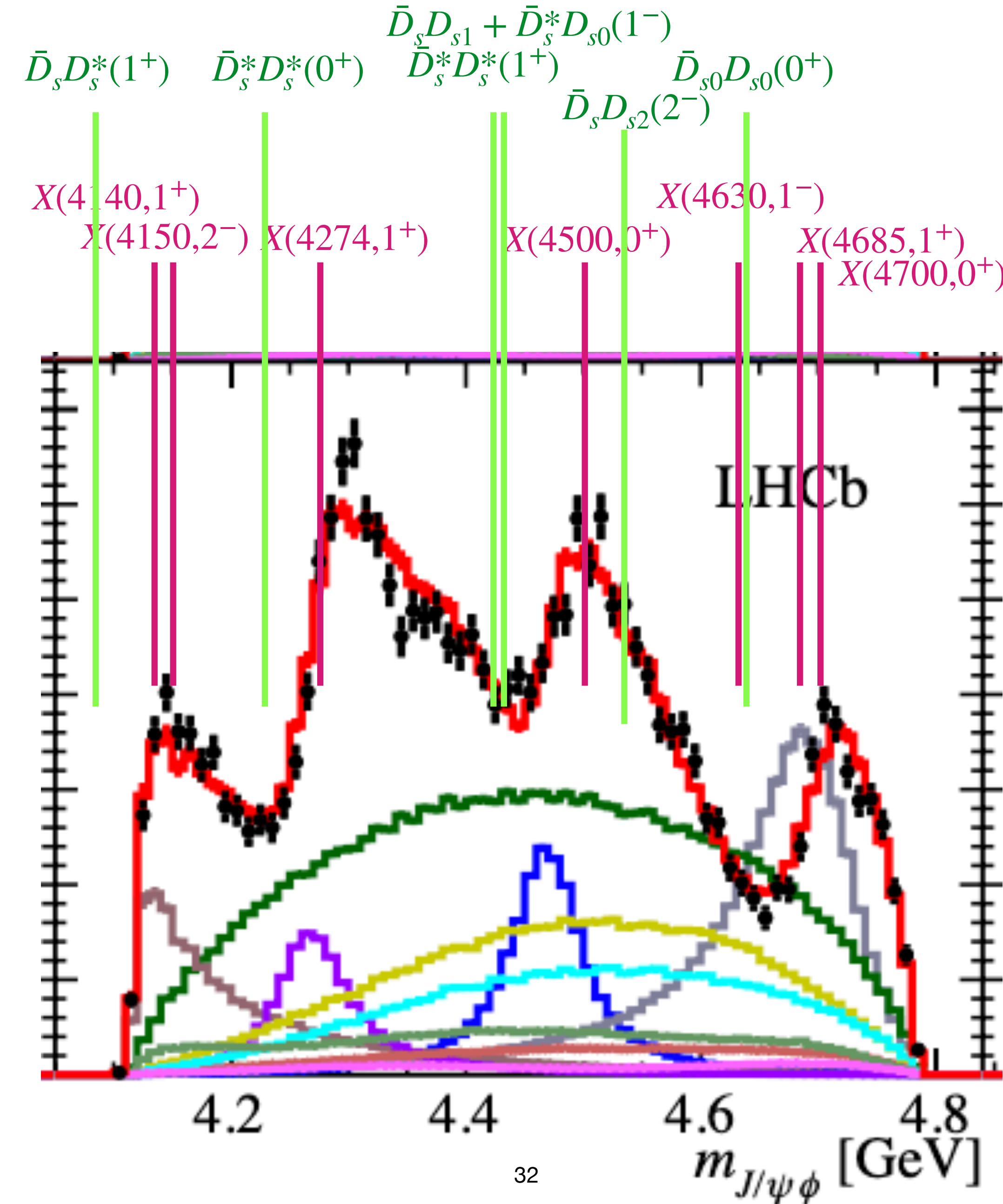
$X(4500), X(4630), X(4685), X(4700)$

$$B^+ \rightarrow J/\psi \phi K^+$$



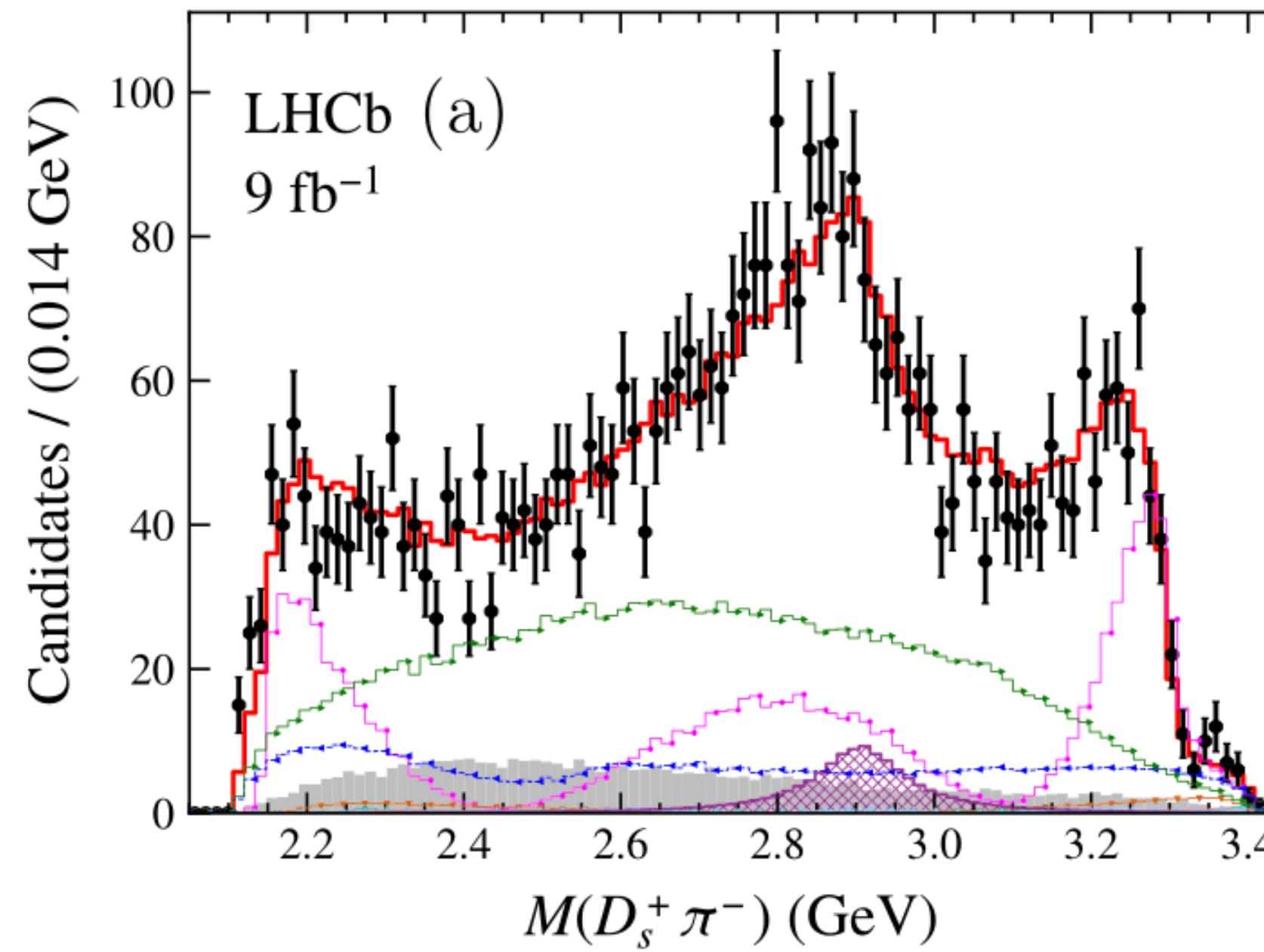
LHCb, 2103.01803

# X Thresholds

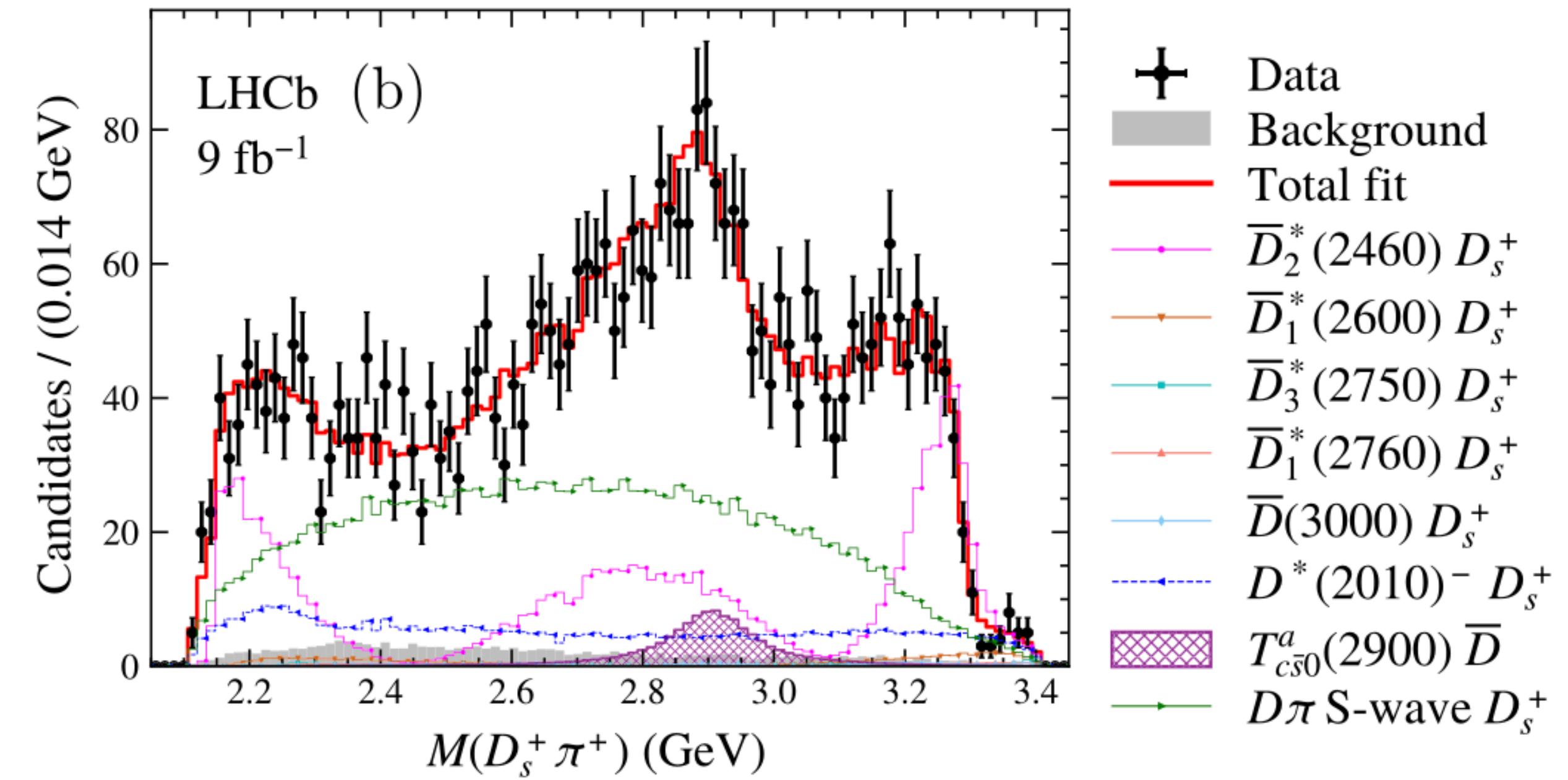


$T_{c\bar{s}0(2908)}$

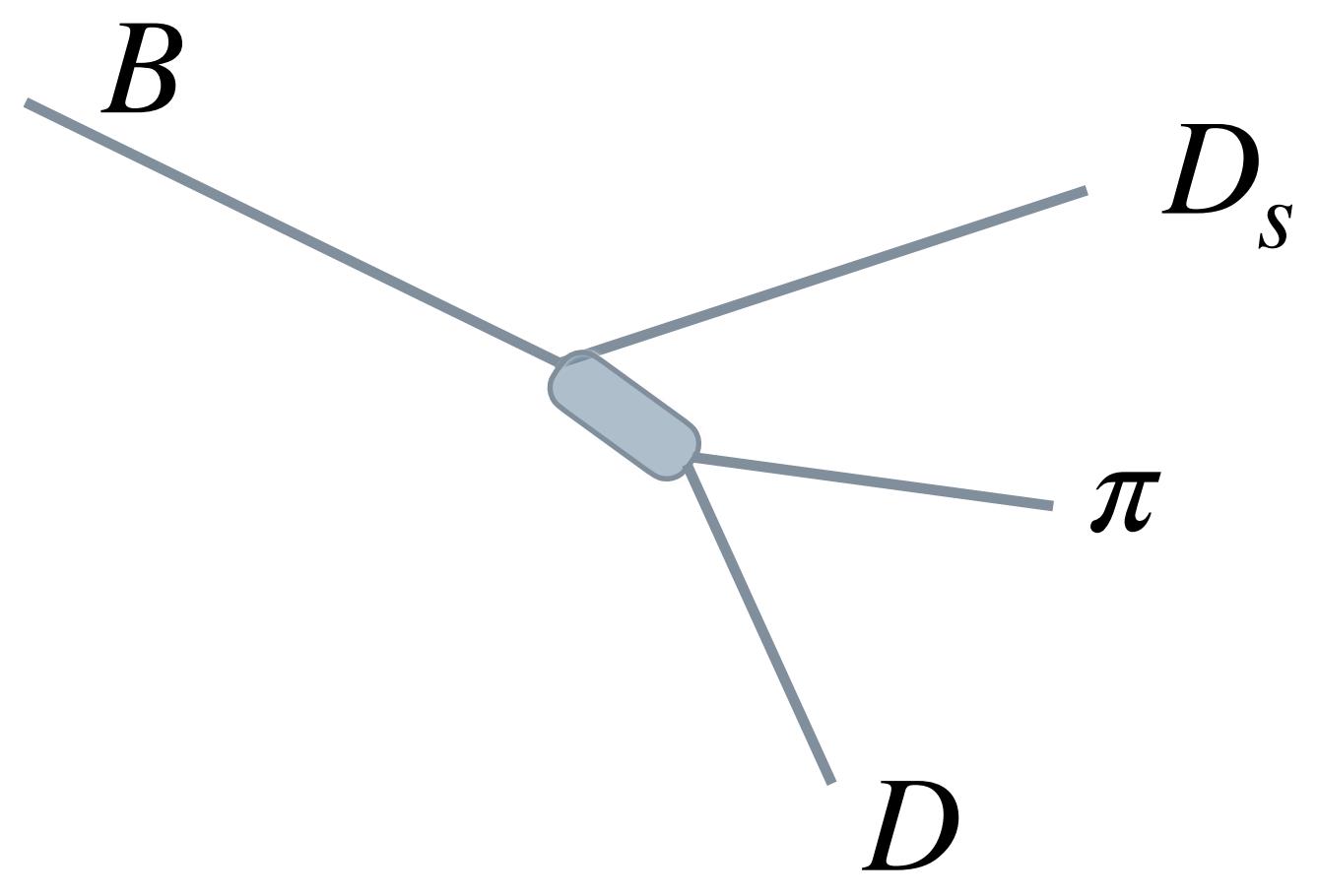
$$B^0 \rightarrow \bar{D}^0 D_s^+ \pi^-$$



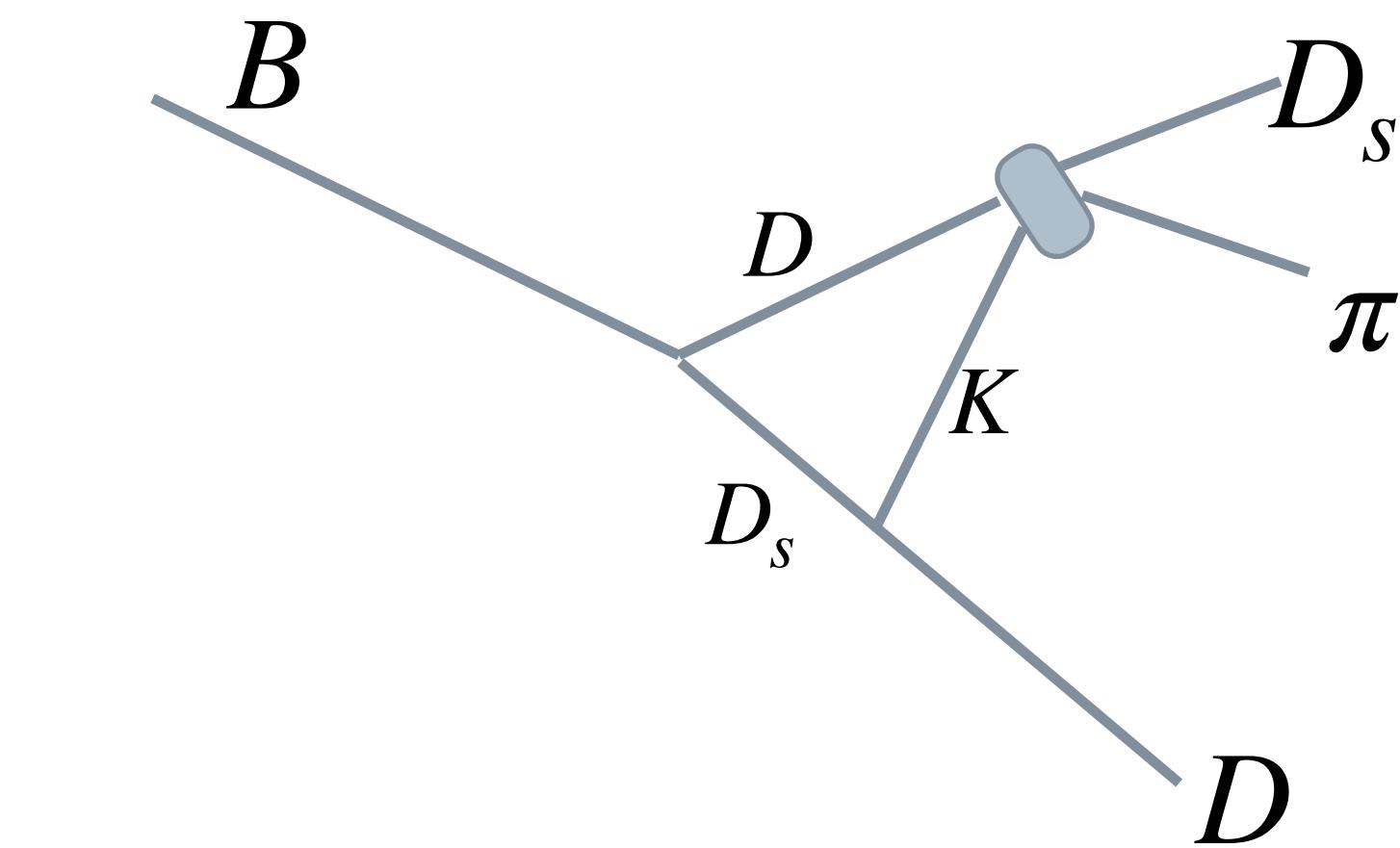
$$B^+ \rightarrow D^- D_s^+ \pi^+$$



BESIII, PRL131, 041902 (2023)

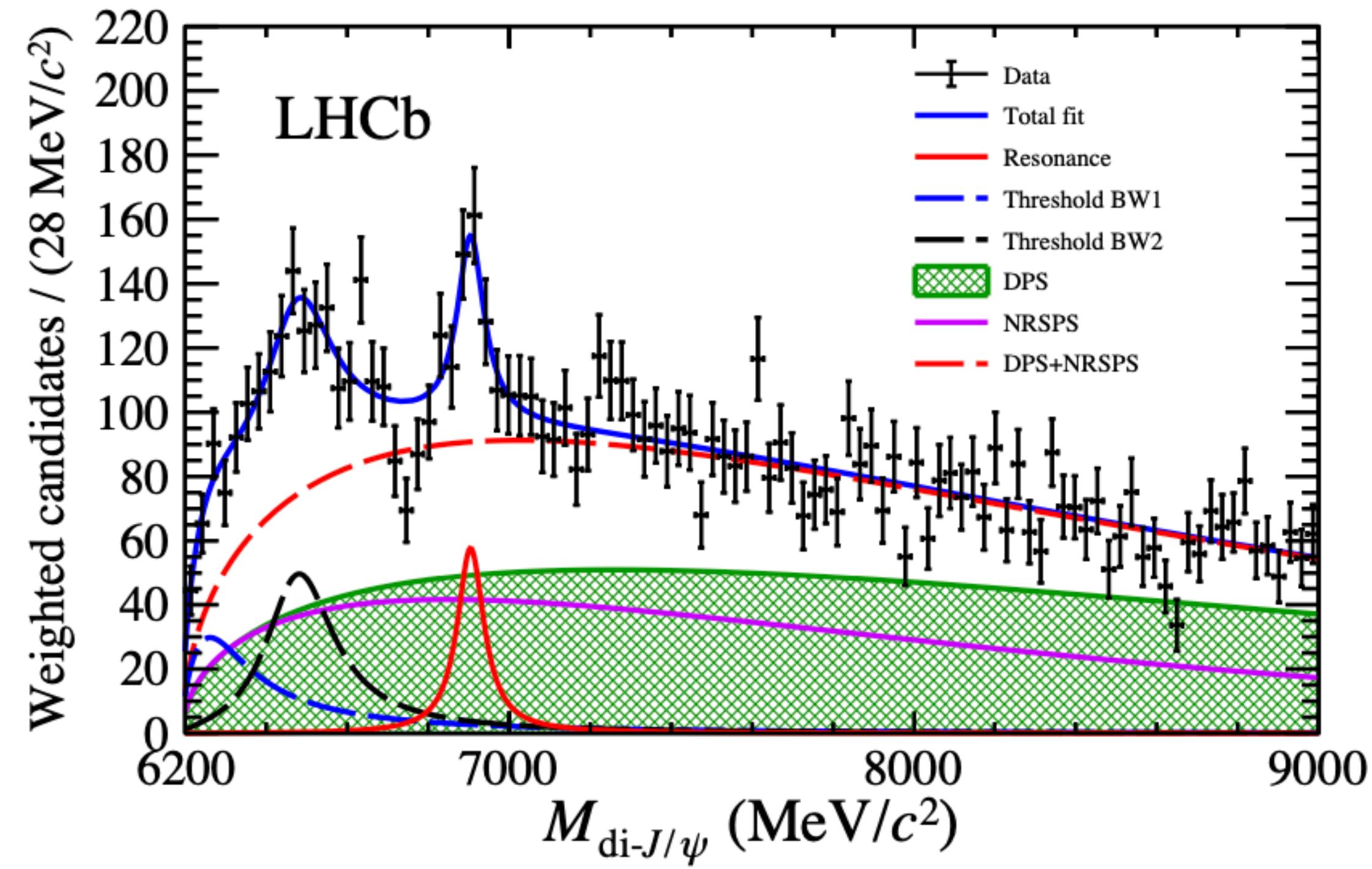


tree order process exists

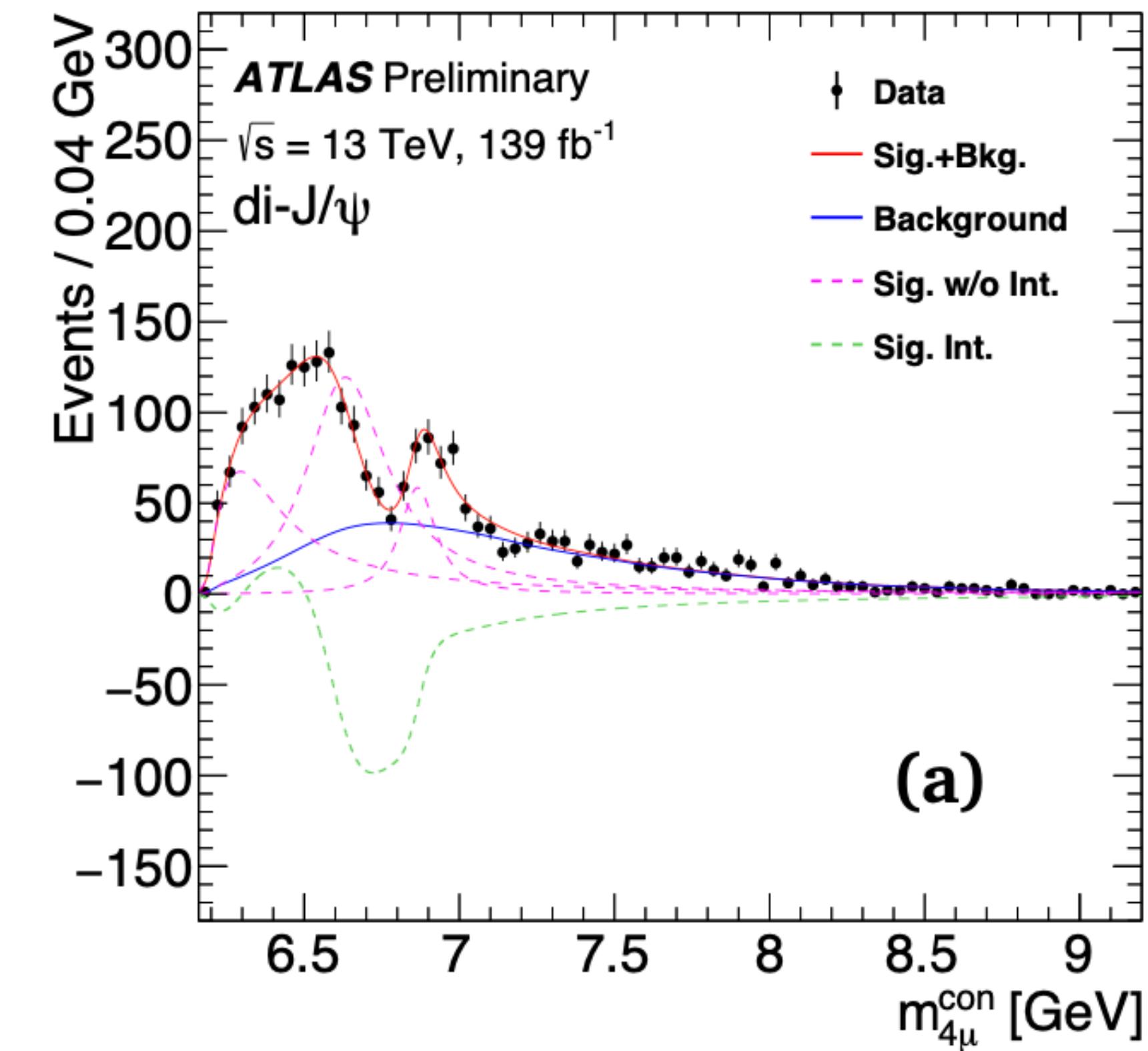


masses don't align

$$T_{\psi\psi}(6200), T_{\psi\psi}(6600), T_{\psi\psi}(6900), T_{\psi\psi}(7200)$$



LHCb, 2006.16957



ATLAS, 2209.12173

# Pentaquarks

$$P_{\psi S}^\Lambda(4338)$$

# Observation of a $J/\psi\Lambda$ resonance in $B^- \rightarrow J/\psi\Lambda\bar{p}$ decays

LHCb-PAPER-2022-031 in preparation

## Discussion on the new $J/\psi\Lambda$ state

### For theoretical interpretation

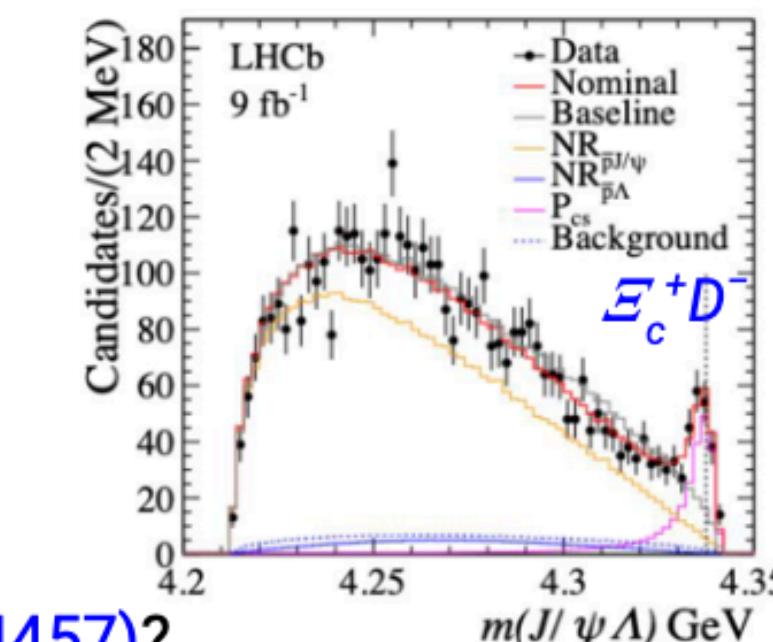
First pentaquark candidate  $P_{\psi s}^{\Lambda}(4338)$   
with strange quark content  $c\bar{c}uds$ ,

$$M_{P_{cs}} = 4338.2 \pm 0.7 \pm 0.4 \text{ MeV}$$

$$\Gamma_{P_{cs}} = 7.0 \pm 1.2 \pm 1.3 \text{ MeV}$$

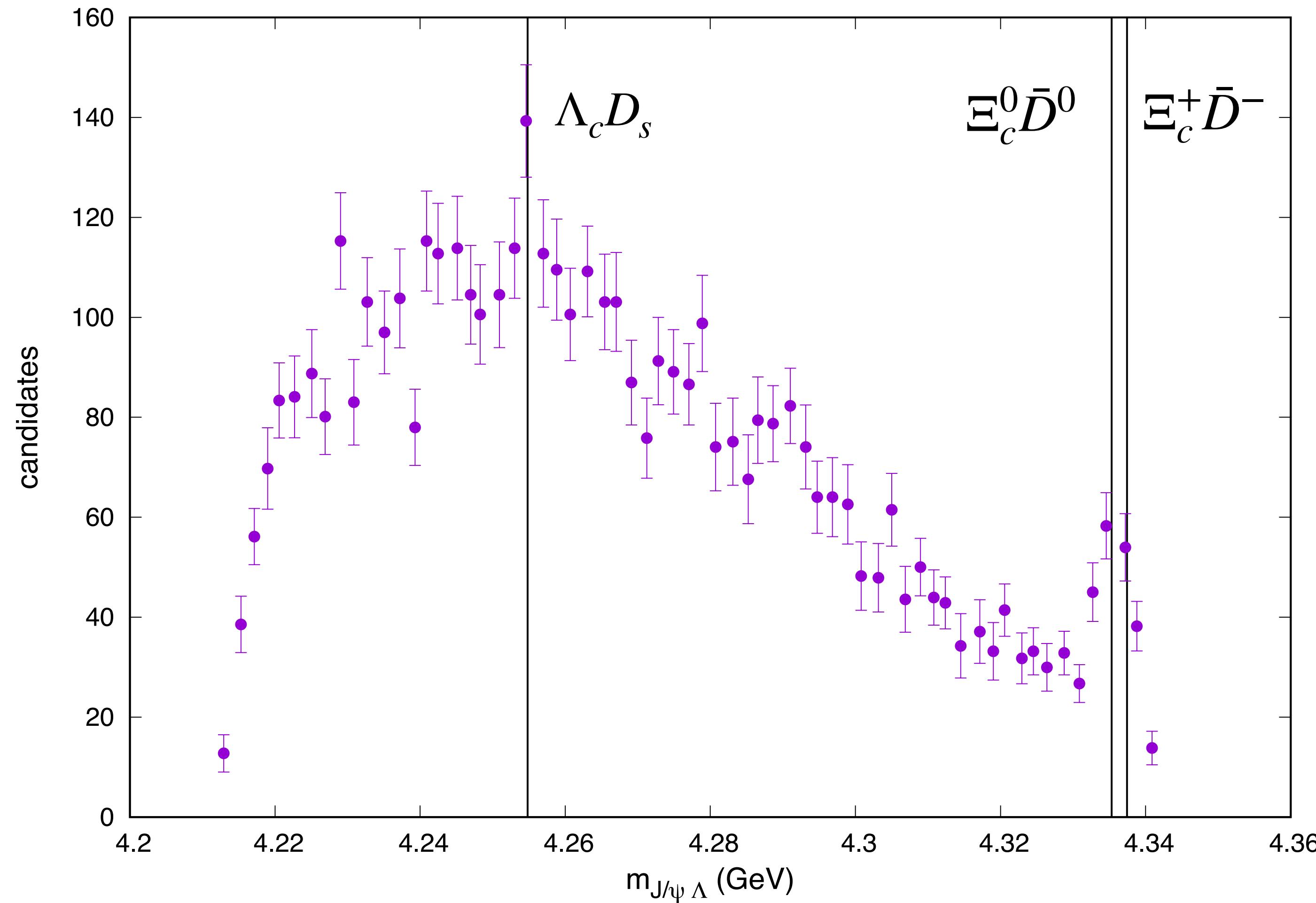
$\Rightarrow$  first pentaquark with spin assigned  $J^P=1/2^-$

- ✓ narrow, close to  $\Xi_c^+ D^-$  threshold and in S-wave
- ✓ pentaquark with strangeness, due to SU(3) symmetry
- ✓ at same mass of  $P_{\psi}^N(4337)$ : analogy to  $P_{\psi s}^{\Lambda}(4459)$  &  $P_{\psi}^N(4457)$ ?



Can fit in SU(3) multiplets or are more likely molecular states?

# Relevant Thresholds



Is a  $\Xi_c D$  bound state plausible?

Heavy quark symmetry implies  $\Xi_c D^*$  partners

$$V(\Xi_c \bar{D}, 1/2^-) = V(\Xi_c \bar{D}^*, 1/2^-) = V(\Xi_c \bar{D}^*, 3/2^-),$$

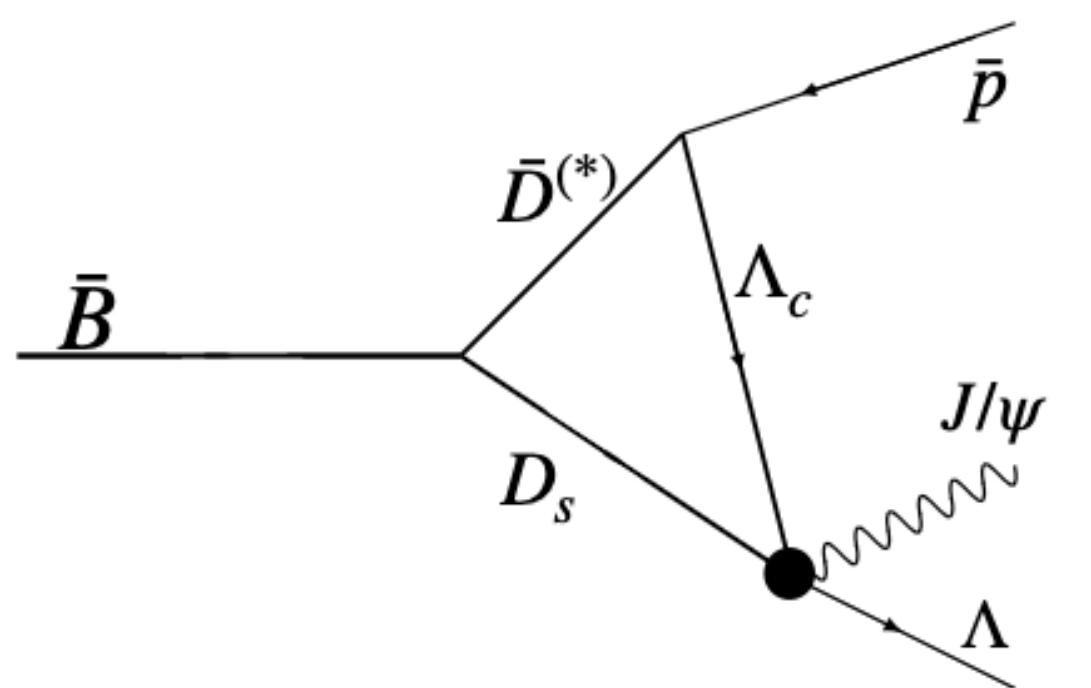
Possible partner state is the  $P_{cs}(4459)$ , but the binding energy is  $\sim 19$  MeV, not  $\sim 0$ .

The  $P_{\psi S}^\Lambda$  is 1-3 MeV *above* threshold.

# Production

the tree-level diagrams for the  $J/\psi \Lambda p^-$  final state are color-suppressed; hence it is natural to assume that the color-favored triangle diagram is a dominant contribution.

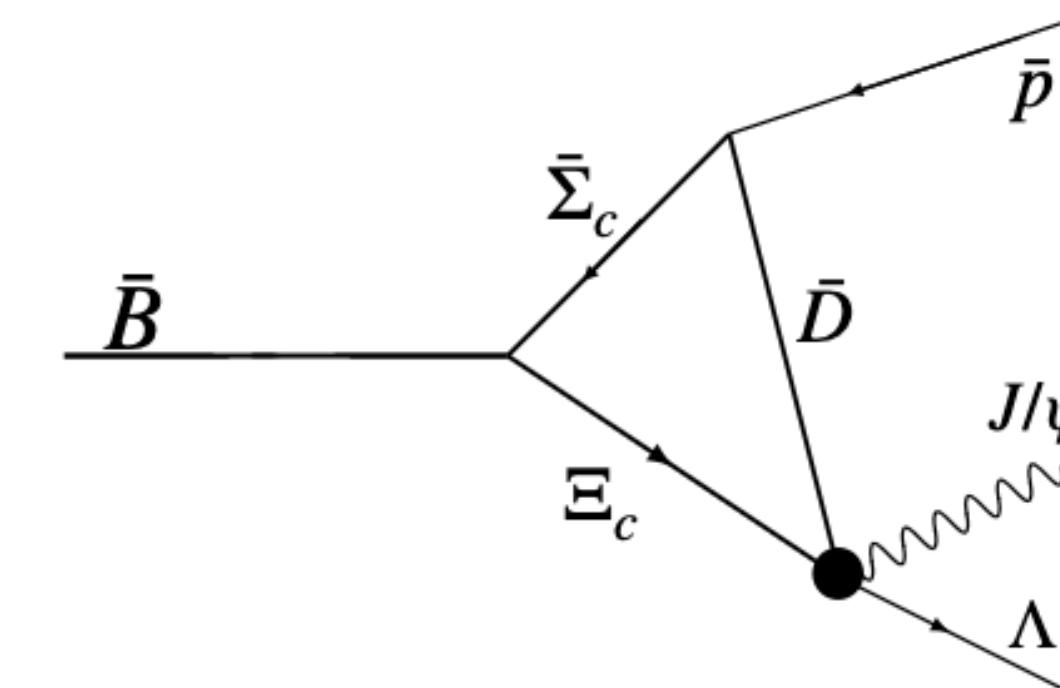
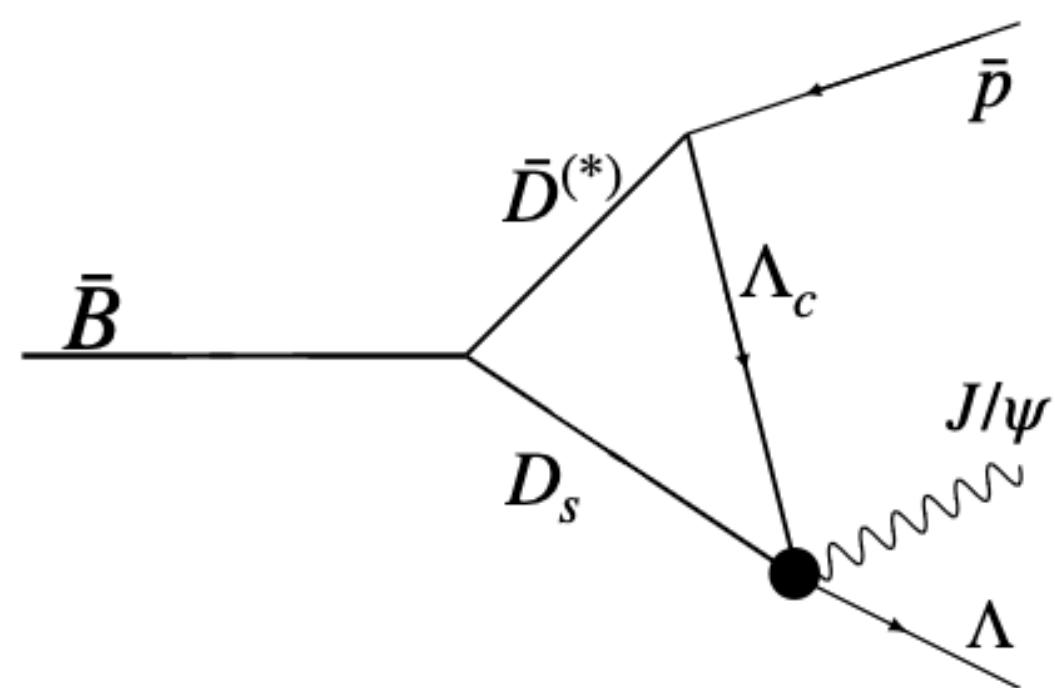
dominant mechanism



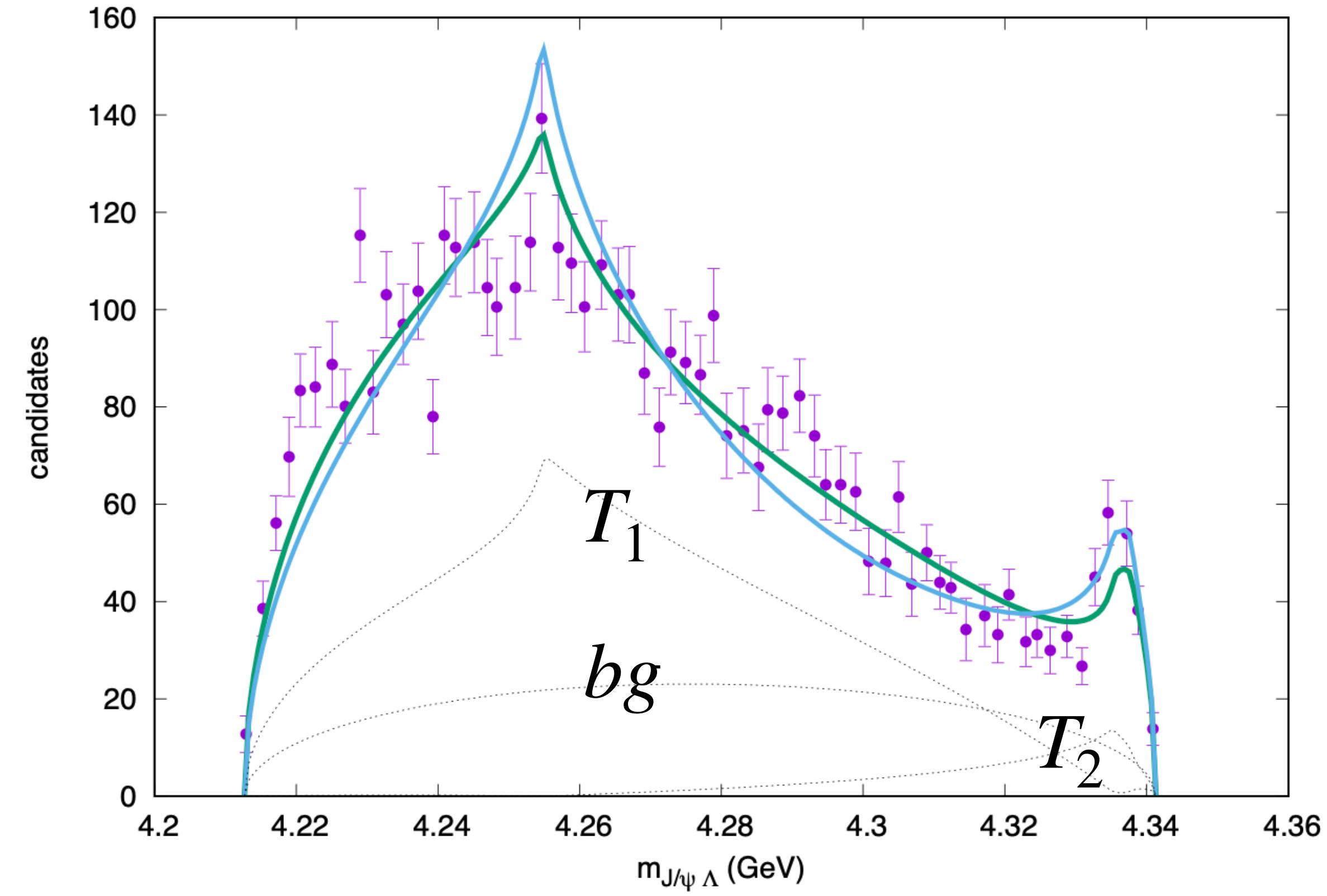
# Production

the tree-level diagrams for the  $J/\psi \Lambda p^-$  final state are color-suppressed; hence it is natural to assume that the color-favored triangle diagram is a dominant contribution.

dominant mechanism



*but this can be comparable if the Landau conditions are  $\sim$  satisfied*



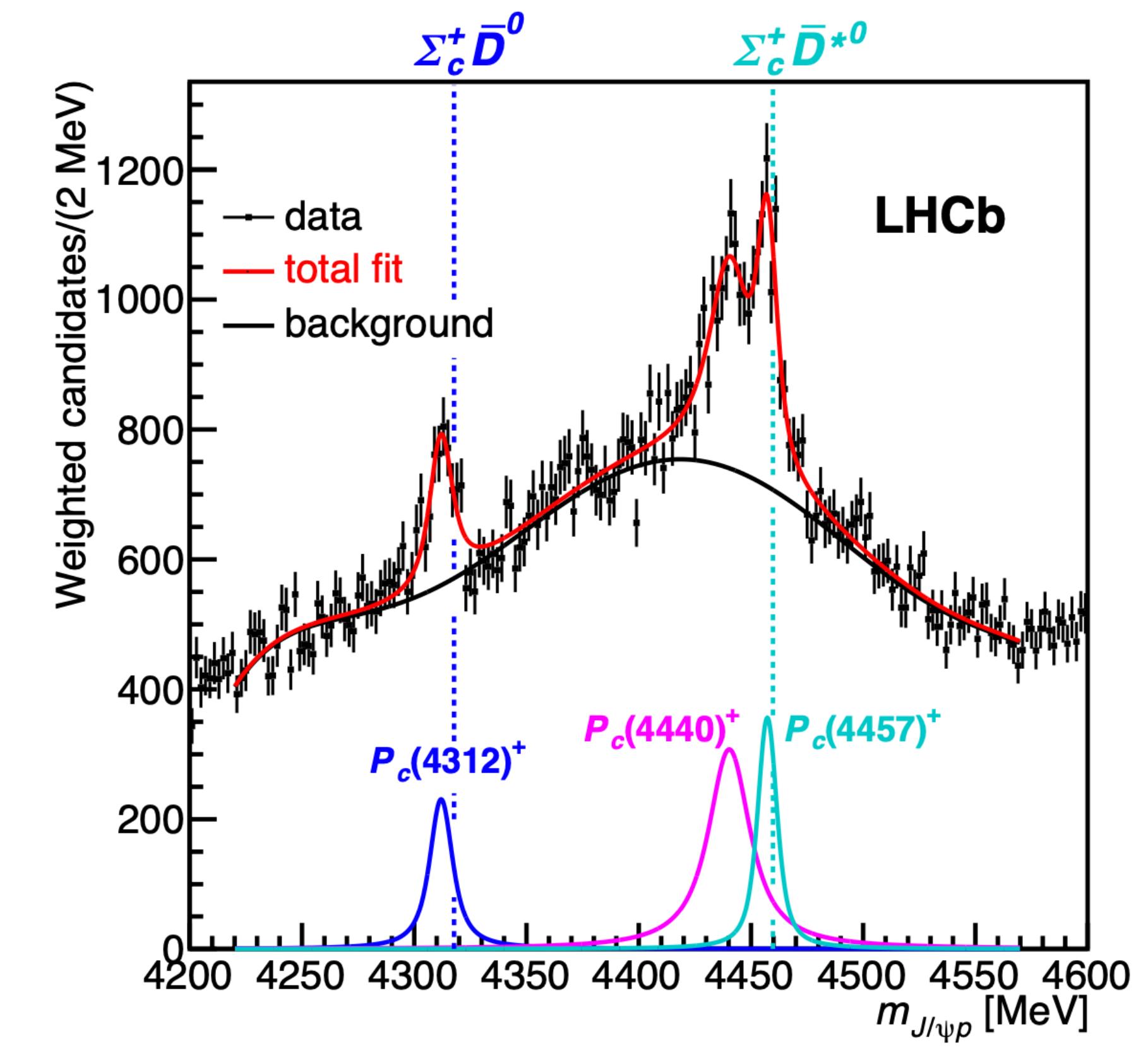
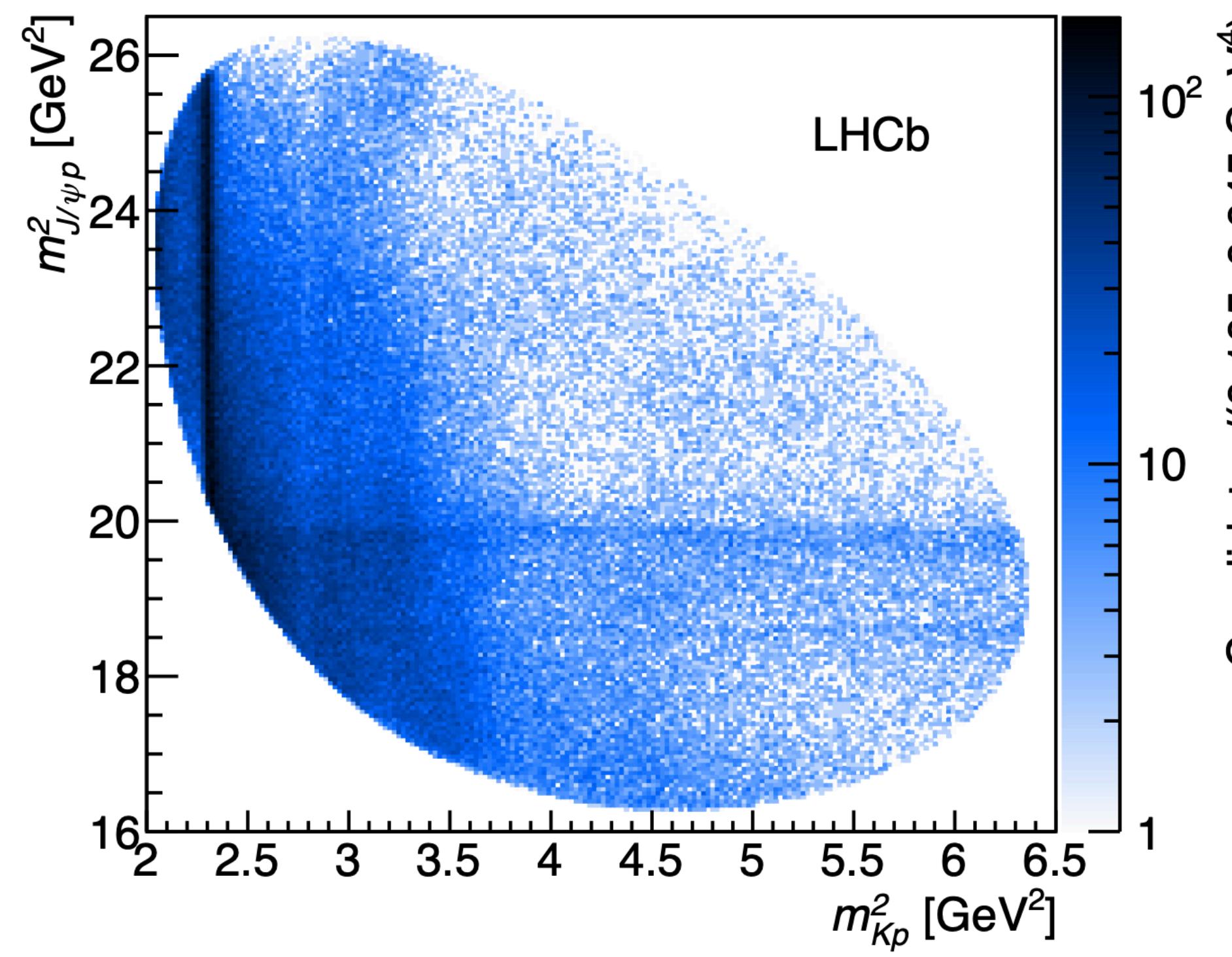
$$\mathcal{A} = b + g_1 T_1 + g_2 \frac{1}{\sqrt{6}} \left[ 2T_2^{(--)} - T_2^{(-)} \right]$$

$\Lambda_c D_s$        $\Xi_c^+ \bar{D}^-$        $\Xi_c^0 \bar{D}^0$

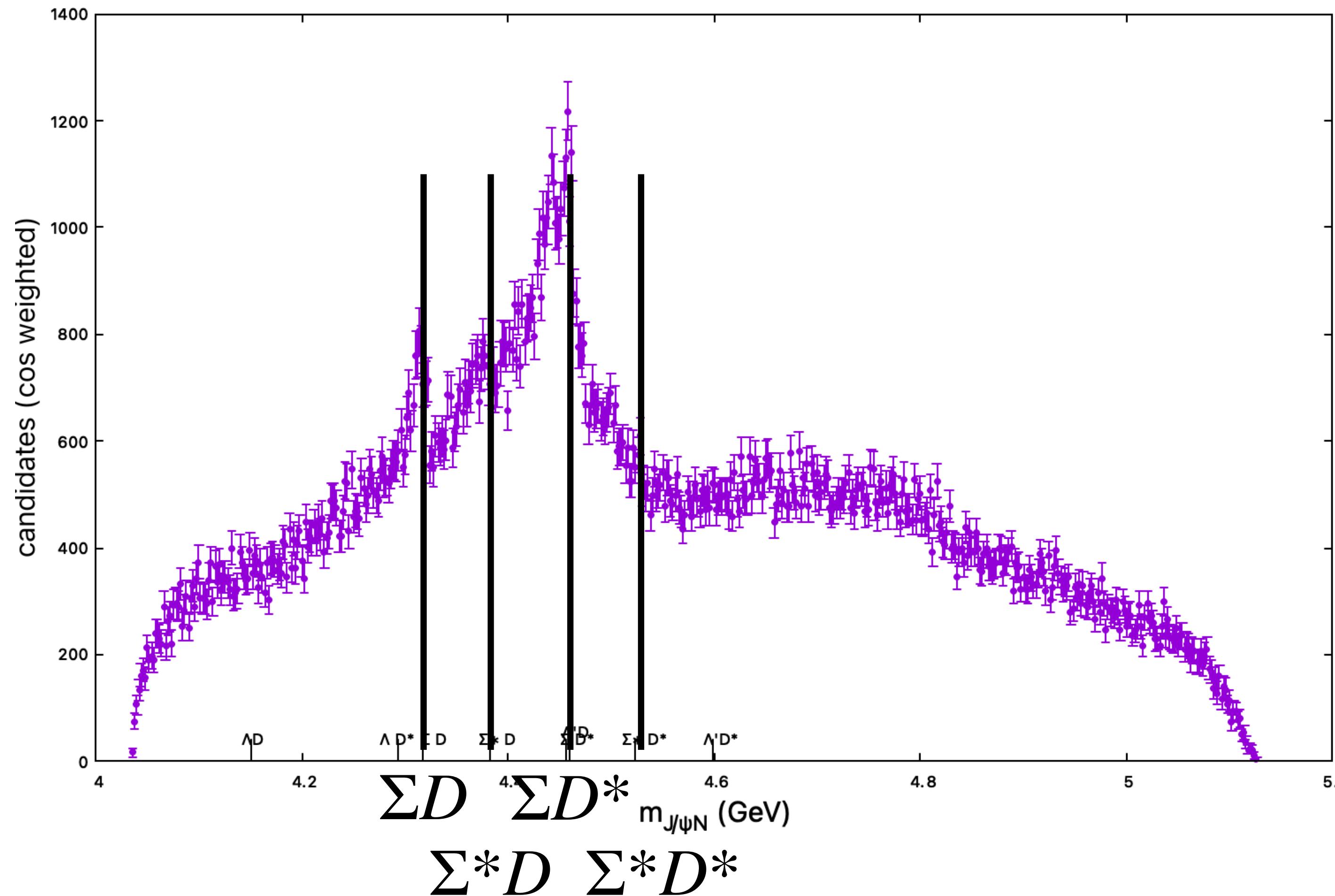
$g_2 \ll g_1 \quad \checkmark$

$P_c(4312)$ ,  $(P_c(4380))$ ,  $P_c(4440)$ ,  $P_c(4457)$

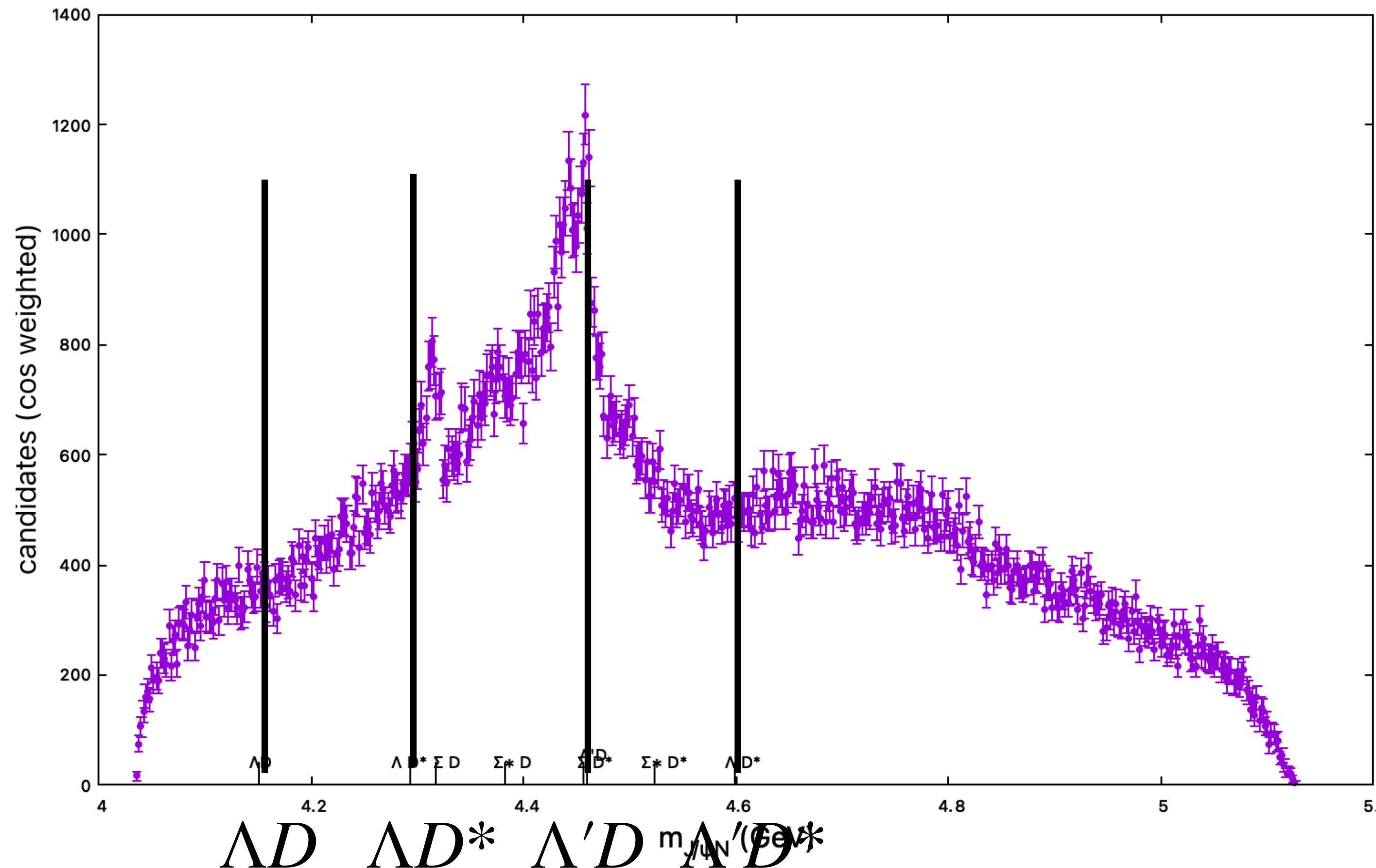
$$\Lambda_b^0 \rightarrow J/\psi p K^-$$



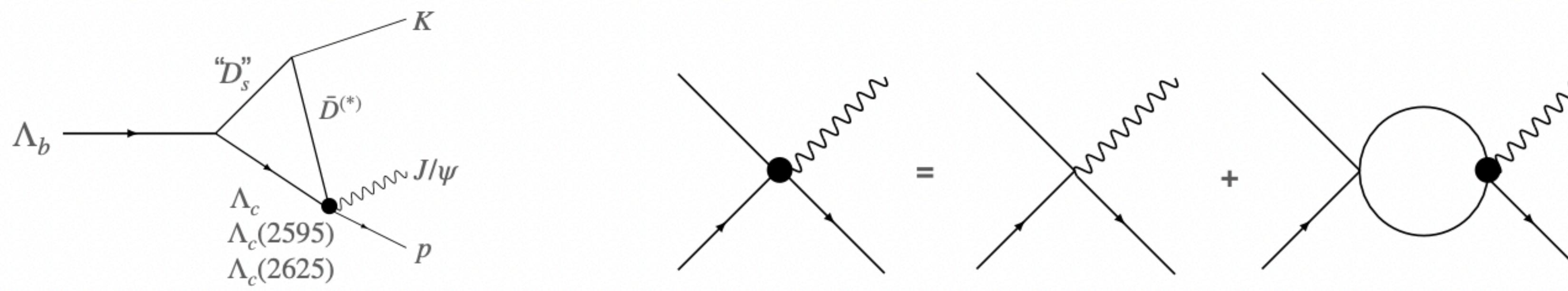
# A Look at the Data (LHCb cos weighted)



# A Look at the Data (LHCb cos weighted)

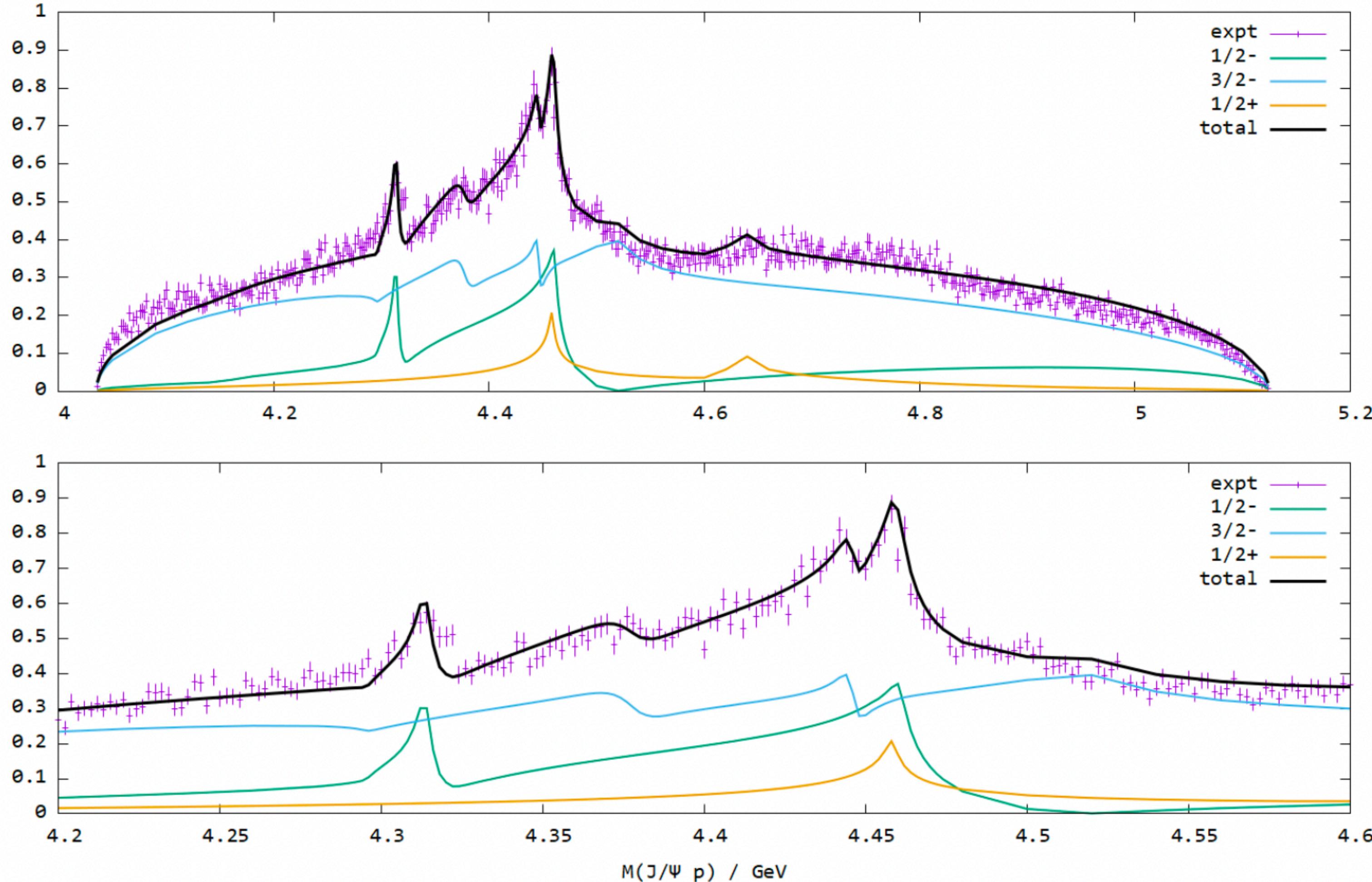


# A Production/ Rescattering Model for Pentaquarks



- bound/resonance states
- threshold cusps
- triangle singularities

# Model Fit

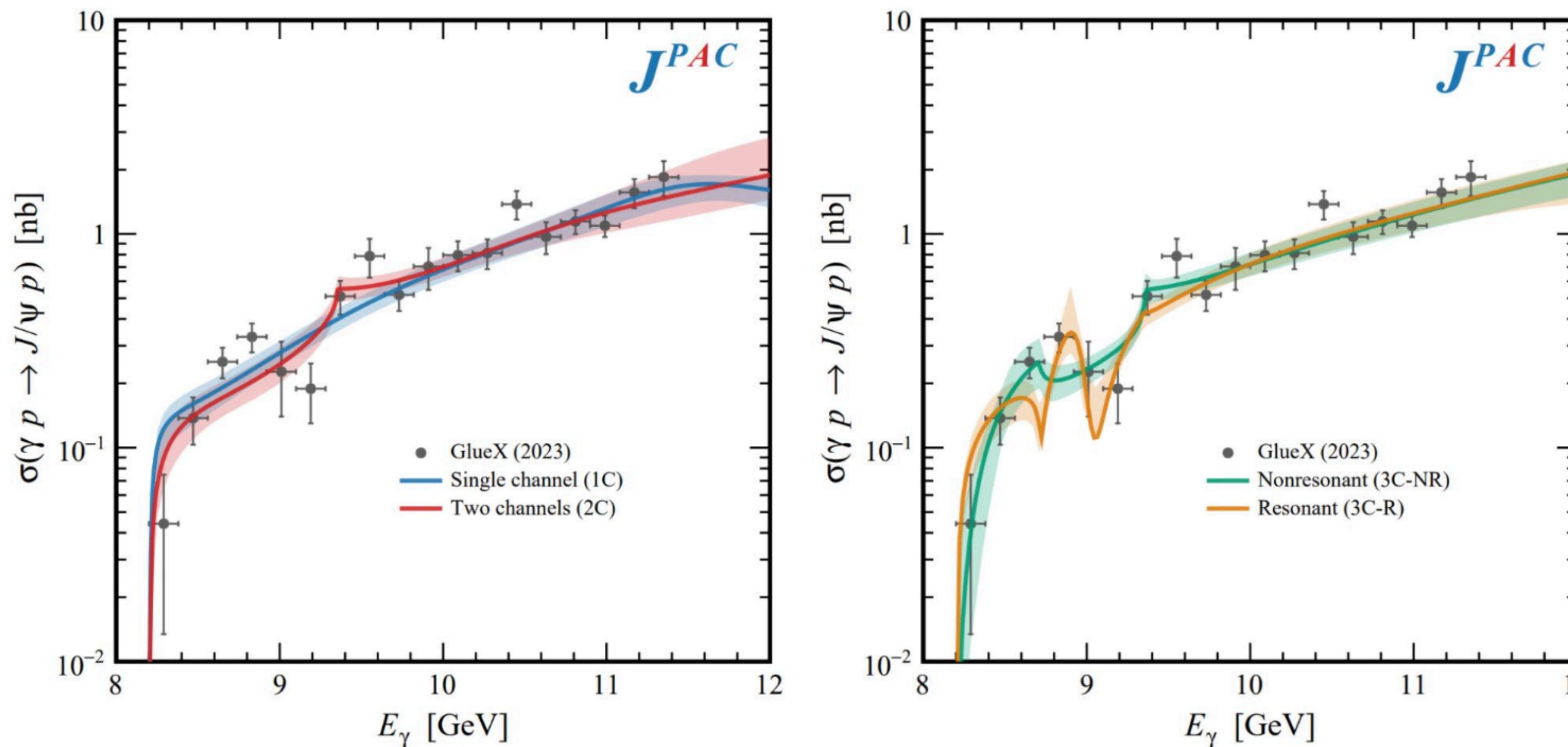


- 4312 ( $\Sigma_c D$ , 1/2-)
- 4380 ( $\Sigma_c^* D$ , 3/2-)
- 4440 ( $\Sigma_c D^*$ , 3/2-)
- 4457 (1/2- $\Sigma_c D^*$  threshold cusp / 1/2+ triangle)
- 4508 ( $\Sigma_c^* D^*$ , 5/2-)

T.J. Burns and E.S. Swanson, 2112.11527, 2207.00511

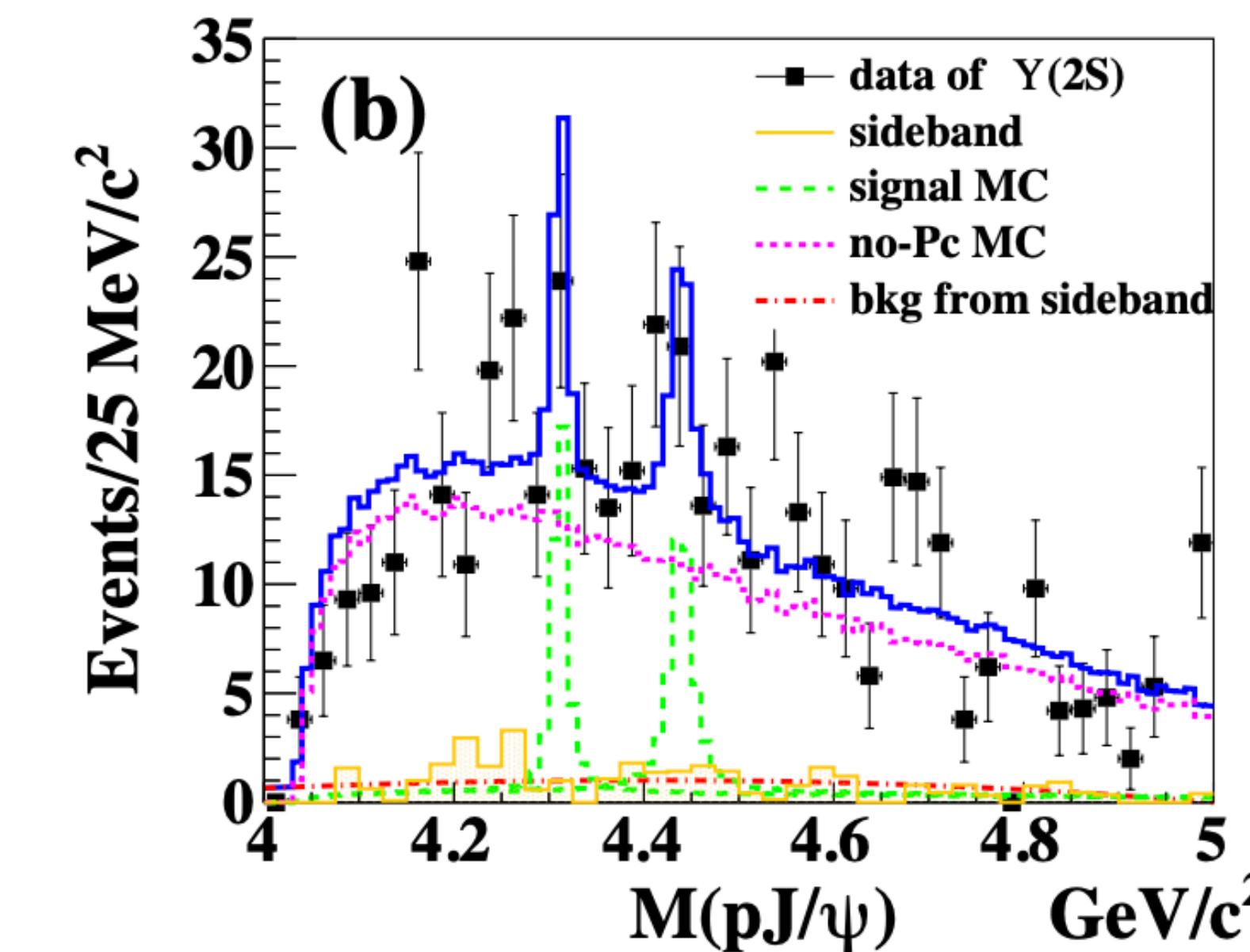
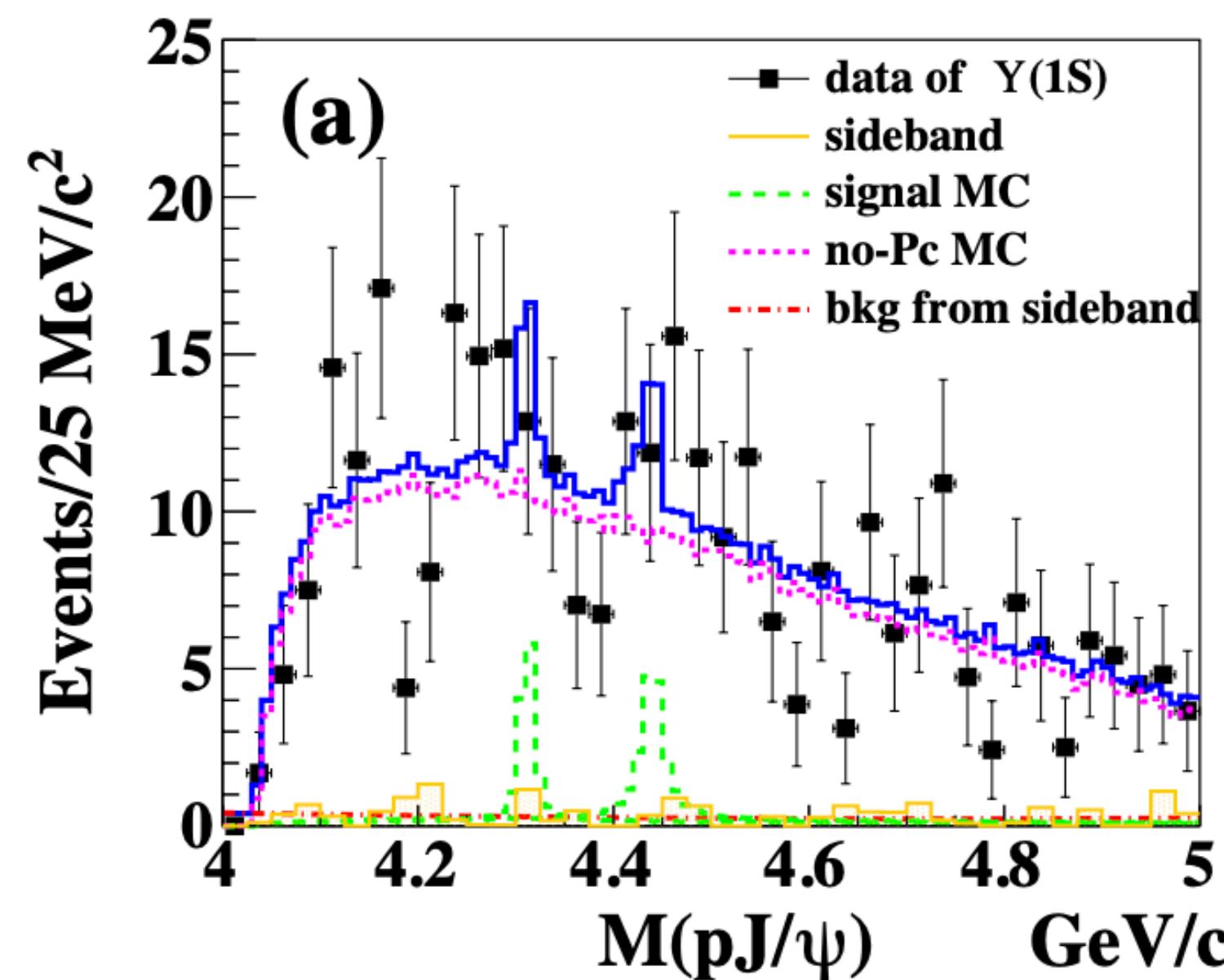
# Non Sighting i

**Four solutions** with different dynamical pictures found to be consistent with full data with similar statistical significance.



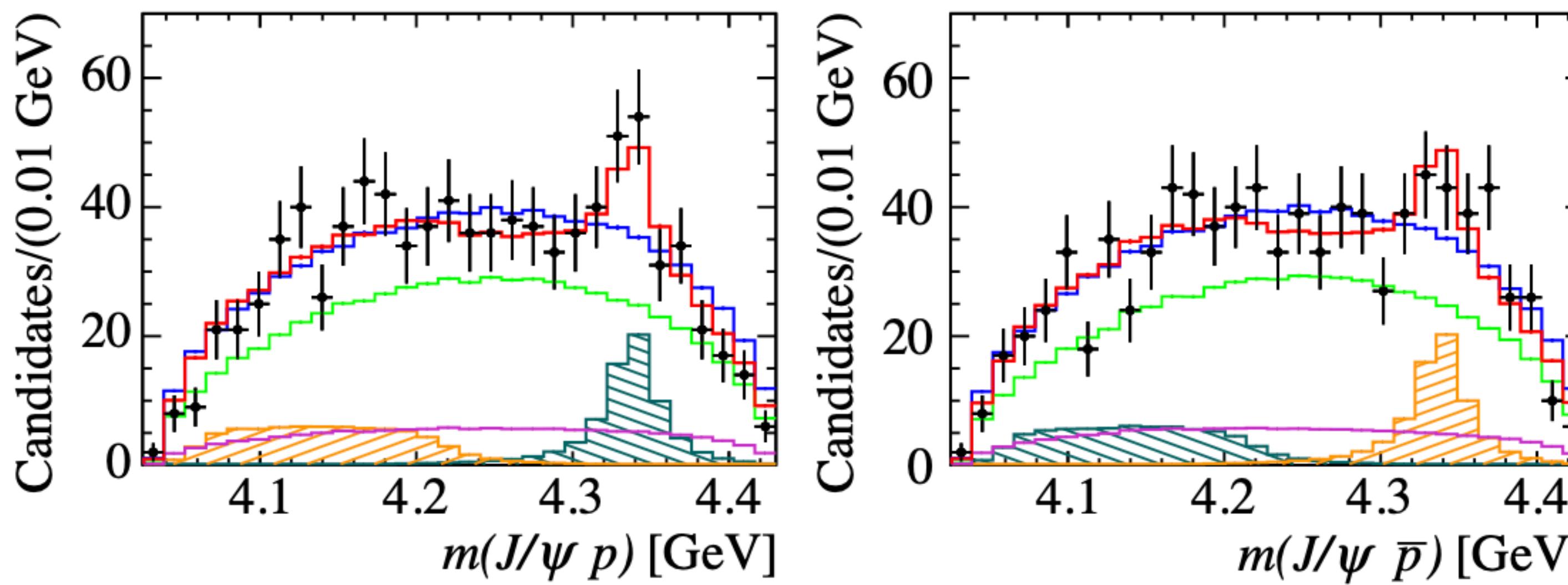
## Non Sighting ii

No evidence for  $P_c(4312)$ ,  $P_c(4440)$ ,  $P_c(4457)$  in  $\Upsilon(1S)$  or  $\Upsilon(2S)$  decays



$P_{c\bar{c}}(4337)$

# $B \rightarrow J/\psi p\bar{p}$



integrated luminosity of  $9 \text{ fb}^{-1}$ . No evidence is seen for either a  $P_c$  state at a mass of 4312 MeV [2] or the glueball state  $f_J(2220)$  predicted in Ref. [11]. Unlike in other  $B$

# Conclusions

tl;dl

- no shortage of anomalies & multiquark candidates
- definite shortage of hybrid candidates!
- naive analysis can create states 
- many "states" can appear due to production (near) singularities, cusps, interferences 
- much work remains to be done!

+ ÆRIC MEC HEHT GEWYRCAN

