

# Beam Dynamics with Space Charge in ImpactX: Code Design and IOTA Applications

Chad Mitchell, Lawrence Berkeley National Laboratory  
(on behalf of the BLAST team & collaborators)



IOTA/FAST Collaboration Meeting  
Fermilab, March 12-14, 2024

# Acknowledgments

Thanks to the workshop organizers.

\*Special thanks to Axel Huebl and Jean-Luc Vay for providing slides re-used here.

Funding acknowledgments:

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# Overview

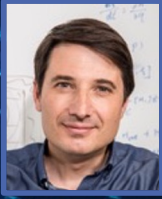
- BLAST toolkit and ImpactX development
- Benchmarking and space charge validation
- Toward applications to IOTA

- Beam Plasma & Accelerator Modeling Toolkit (BLAST)

# Multidisciplinary, Multi-Institutional Contributor Team



Jean-Luc Vay  
(ECP PI)



Arianna Formenti



Marco Garten



Axel Huebl  
(LDRD PI)



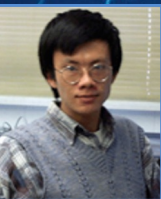
Rémi Lehe



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Ji Qiang



Ryan Sandberg



Olga Shapoval



Edoardo Zoni



Ann Almgren  
(ECP coPI)



John Bell



Kevin Gott



Junmin Gu



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Prabhat Kumar



Andrew Myers



Weiqun Zhang



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Henri Vincenti



Luca Fedeli



Antonin Sainte-Marie



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Marc Hogan  
(ECP coPI)



Lixin Ge



Cho Ng



(France)

Lorenzo Giacomel



(Germany)



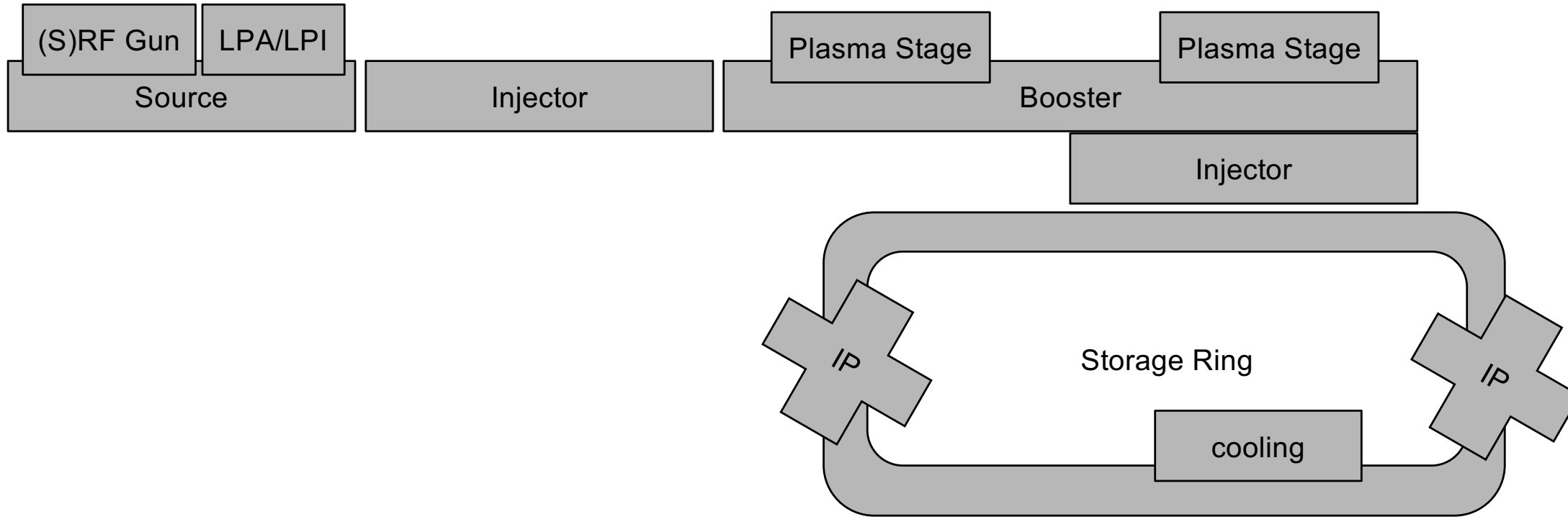
(Switzerland)

...& private sector



# BLAST: integrated beam physics across accelerator subsystems

Imagine a future, **hybrid particle accelerator**, e.g., with conventional and plasma elements.

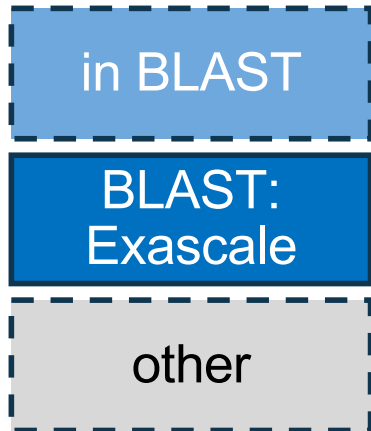


or injection into an FEL linac



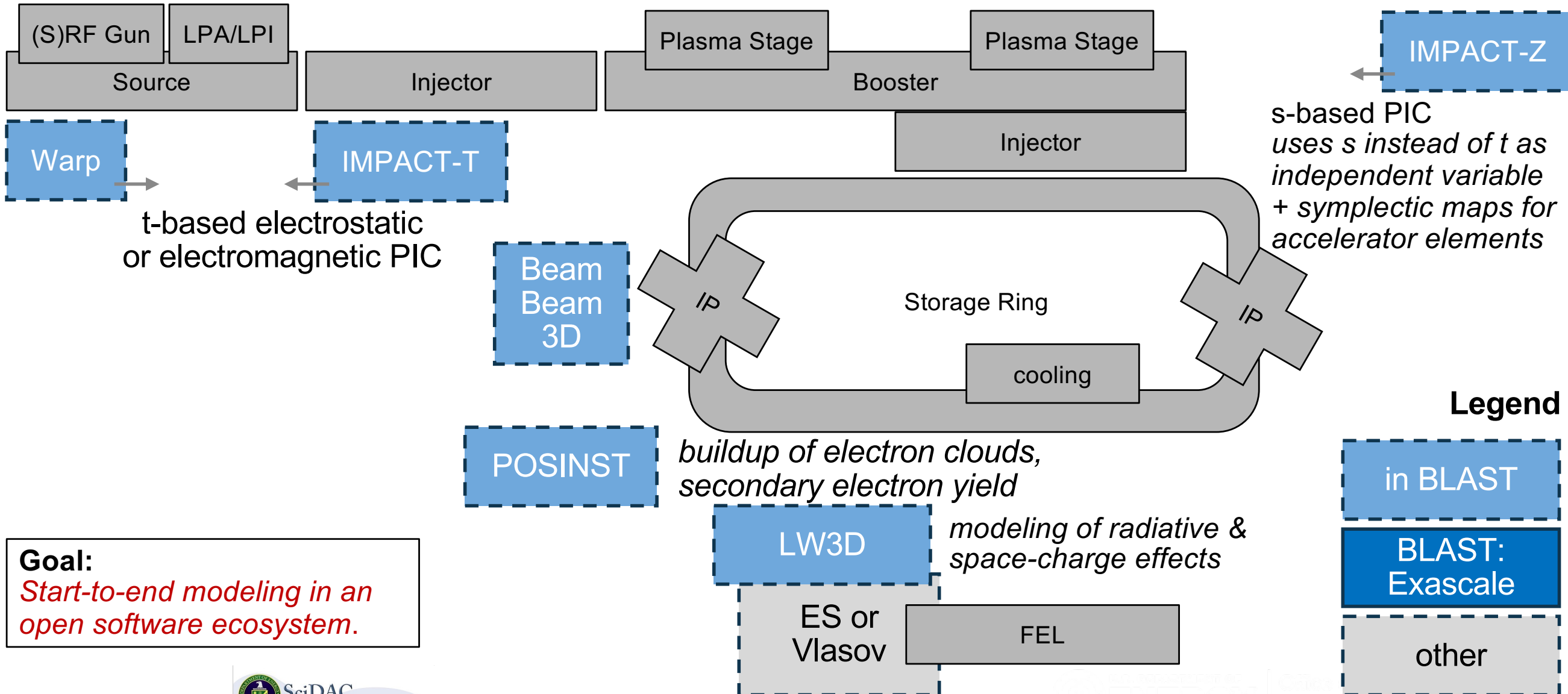
**Goal:**  
*Start-to-end modeling in an open software ecosystem.*

## Legend



# BLAST: integrated beam physics across accelerator subsystems

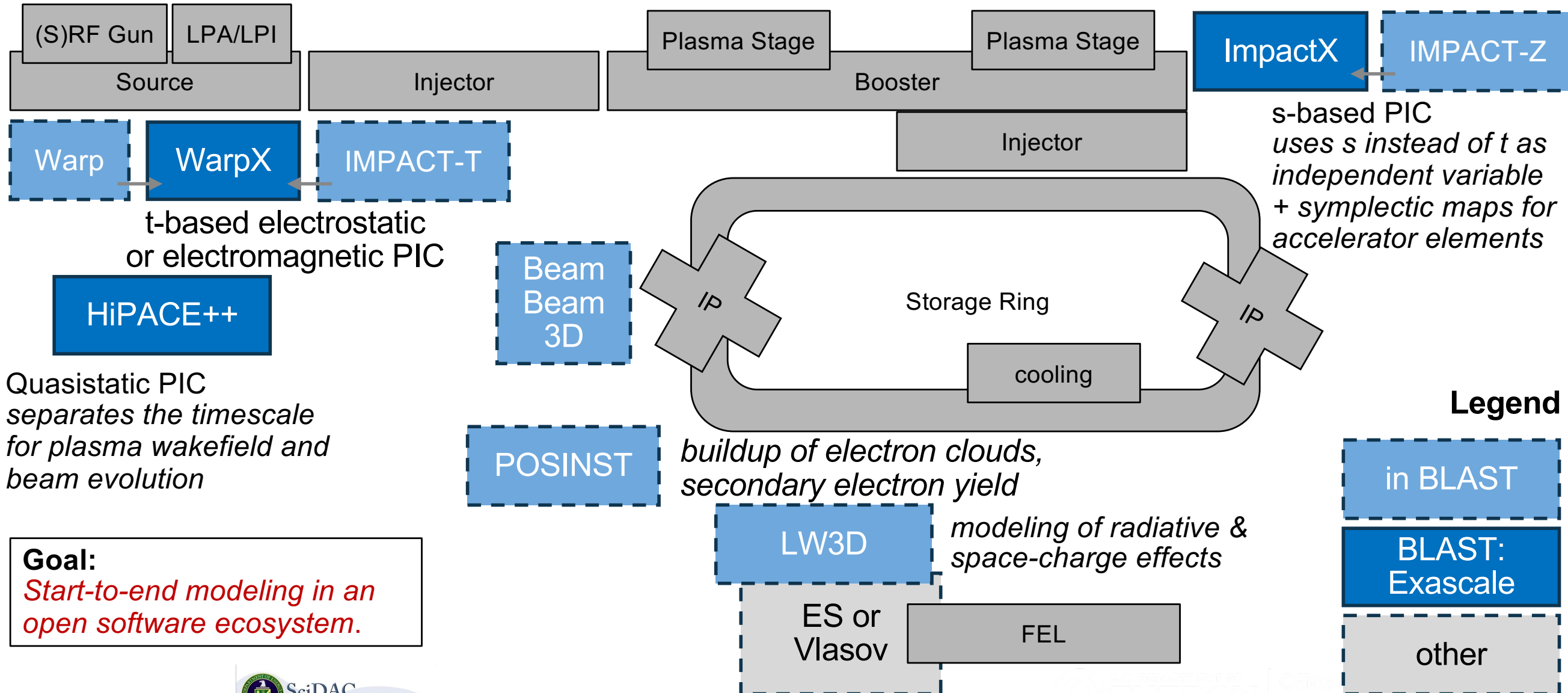
Imagine a future, **hybrid particle accelerator**, e.g., with conventional and plasma elements.



**Goal:**  
*Start-to-end modeling in an open software ecosystem.*

# BLAST: integrated beam physics across accelerator subsystems

Imagine a future, **hybrid particle accelerator**, e.g., with conventional and plasma elements.



Quasistatic PIC separates the timescale for plasma wakefield and beam evolution

**Goal:**  
Start-to-end modeling in an open software ecosystem.

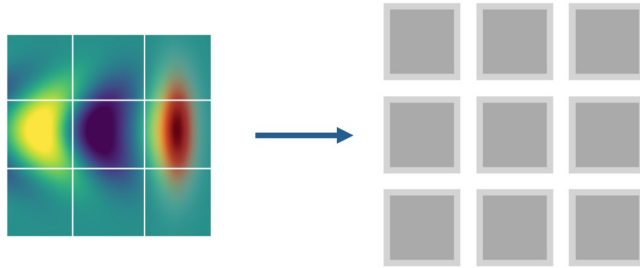


# Modernizing BLAST through an Exascale Programming Model

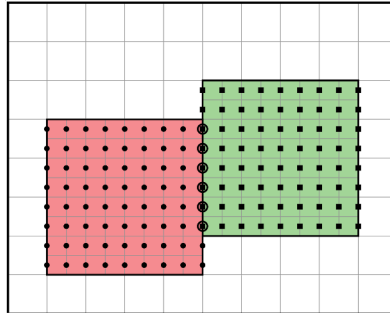
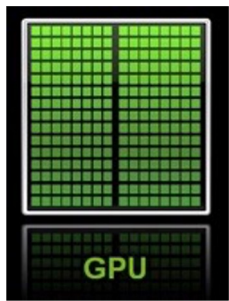
## AMReX library



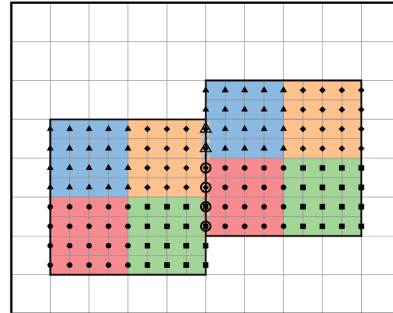
- Domain decomposition & MPI communications: MR & load balance



- Performance-Portability Layer: GPU/CPU/KNL



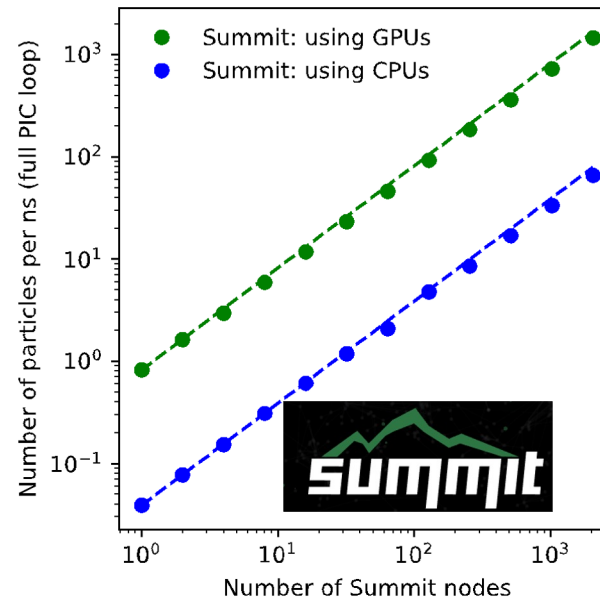
without tiling



with tiling



Data Structures



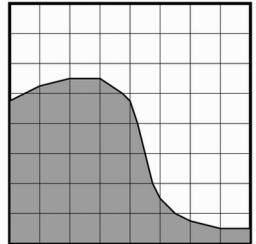
A100 gives additional ~< 2x

- Write the code once, specialize at *compile-time*

ParallelFor (/Scan/Reduce)

```

amrex::ParallelFor( n_particles,
    [=] AMREX_GPU_DEVICE (long i) {
        UpdatePosition( x[i], y[i], z[i],
            ux[i], uy[i], uz[i], dt );
    });
    
```

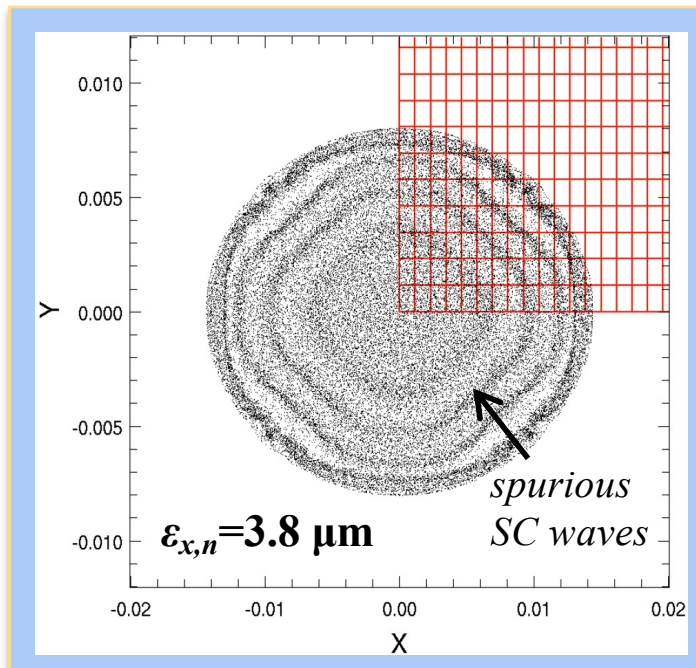
- Parallel linear solvers (e.g. multi-grid Poisson solvers)
- Embedded boundaries 
- Runtime parser for user-provided math expressions (incl. GPU)

# Space charge capabilities supported by BLAST codes using the AMReX software framework

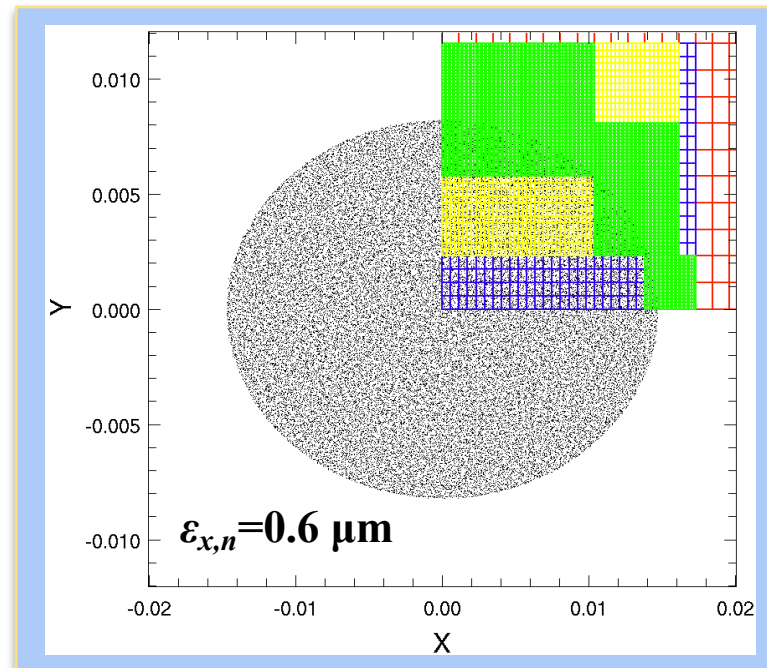
- Higher-order interpolation schemes for charge deposition to aid in noise suppression
- Parallel iterative Multi-Level Multi-Grid Poisson solver for performance scalability
- Adaptive Mesh Refinement (AMR) for resolving density gradients, beam edge and halo

**Example: Using AMR can reduce computation time**

*No AMR*



*With AMR*



Example: initially KV beam  
( $\epsilon_{xn} = 0.5 \mu\text{m}$ )  
in a FODO lattice<sup>1</sup>

Simulation time:

**low resolution with AMR: 10.5 s**  
**high resolution with no AMR: 30 s**

<sup>1</sup>J.-L. Vay, in WARP

# Transitioning BLAST to an integrated ecosystem

User Interfaces

Python Bindings & Particle-In-Cell Modeling Interface (PICMI)

Apps

WarpX

HiPACE++

ImpactX

...

Libraries

pyAMReX

**ABLASTR**

common PIC components

**PICSAR**

QED modules

Computer Science

**AMReX**

Containers, Communication,  
Portability, Utilities

**openPMD** I/O,  
streaming, in situ:  
ADIOS/HDF5

**Math**

LinAlg., FFT

Vendor

MPI multi-node comm.

CUDA, OpenMP, DPC++, HIP



Desktop  
to  
HPC

# ImpactX: GPU-, AMR- & AI/ML-Accelerated Beam Dynamics

## Physical Model based on IMPACT-Z

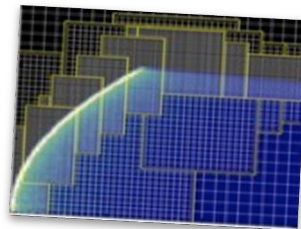
- s-based tracking with symplectic maps
- detailed RF cavity models and standard magnetic elements (w/soft-edge models)
- exact nonlinear maps for sbends, drifts
- support for transverse machine errors
- apertures and lost particle diagnostics

## Space Charge Model

- 3D electrostatic in the bunch rest frame
- Multi-Level, Multi-Grid Poisson solver based on AMReX

## Triple Acceleration Approach

- GPU support
- Adaptive Mesh Refinement
- AI/ML & Data Driven Models



## User-Friendly

- single-source C++, full Python control
- fully tested
- fully documented

 **Same Script**  
CPU/GPU & MPI

## Multi-Node parallelization

- MPI: domain decomposition
- dynamic load balancing (in dev.)



## On-Node Parallelization

- GPU: CUDA, HIP and SYCL
- CPU: OpenMP



## Scalable, Parallel I/O

- openPMD
- in situ analysis

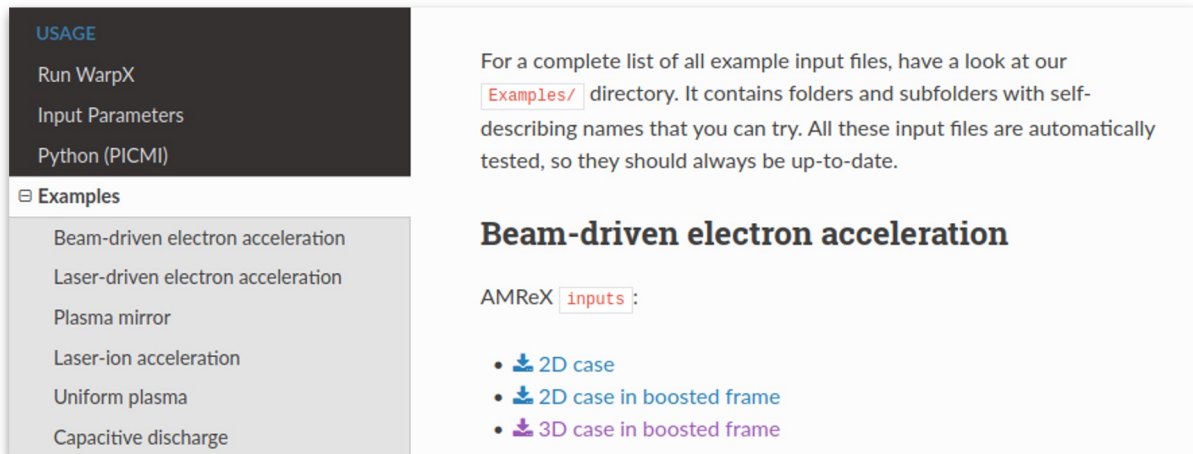


[github.com/ECP-WarpX/impactx](https://github.com/ECP-WarpX/impactx)

- Benchmarking and space charge validation

# Fully open development and continuous benchmarking

Online Documentation:  
[warpX|hipace|impactx.readthedocs.io](http://warpX|hipace|impactx.readthedocs.io)



USAGE

- Run WarpX
- Input Parameters
- Python (PICMI)

Examples

- Beam-driven electron acceleration
- Laser-driven electron acceleration
- Plasma mirror
- Laser-ion acceleration
- Uniform plasma
- Capacitive discharge

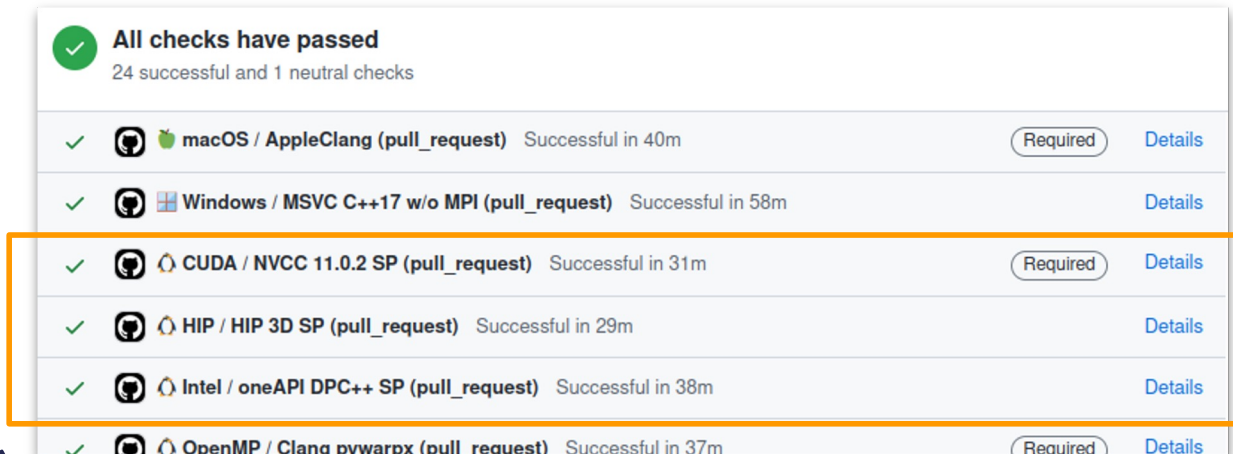
For a complete list of all example input files, have a look at our [Examples/](#) directory. It contains folders and subfolders with self-describing names that you can try. All these input files are automatically tested, so they should always be up-to-date.

### Beam-driven electron acceleration

AMReX `inputs`:

- [2D case](#)
- [2D case in boosted frame](#)
- [3D case in boosted frame](#)

Open-Source Development & Benchmarks:  
[github.com/ECP-WarpX](https://github.com/ECP-WarpX)



All checks have passed  
24 successful and 1 neutral checks

✓	macOS / AppleClang (pull_request)	Successful in 40m	Required	Details
✓	Windows / MSVC C++17 w/o MPI (pull_request)	Successful in 58m		Details
✓	CUDA / NVCC 11.0.2 SP (pull_request)	Successful in 31m	Required	Details
✓	HIP / HIP 3D SP (pull_request)	Successful in 29m		Details
✓	Intel / oneAPI DPC++ SP (pull_request)	Successful in 38m		Details
✓	OpenMP / Clang pywarpX (pull_request)	Successful in 37m	Required	Details



**230 physics benchmarks** run on every code change of WarpX  
**34 physics benchmarks + 106 tests** for ImpactX

Rapid and easy installation on any platform:



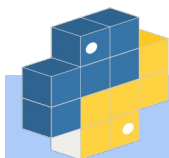
`conda create -n impactx`  
`-c conda-forge impactx`



`spack install warpX`  
`spack install py-warpX`



`cmake -S . -B build`  
`cmake --build build --target install`



`python3 -m pip install .`



`brew tap ecp-warpX/warpX`  
`brew install warpX`



`module load warpX`  
`module load py-warpX`

# ImpactX: Physics Benchmark Examples

**INSTALLATION**

- Users
- Developers
- HPC

**USAGE**

- Run ImpactX
- Parameters: Python
- Parameters: Inputs File

**Examples**

- FODO Cell
- Chicane
- Constant Focusing Channel
- Constant Focusing Channel with Space Charge
- Expanding Beam in Free Space
- Kurth Distribution in a Periodic Focusing Channel
- Kurth Distribution in a Periodic Focusing Channel with Space Charge
- Acceleration by RF Cavities
- FODO Cell with RF
- FODO Cell, Chromatic
- Chain of thin multipoles
- A nonlinear focusing channel based on the IOTA nonlinear lens
- The "bare" linear lattice of the Fermilab IOTA storage ring

Home / Examples [Edit on GitHub](#)

## Examples

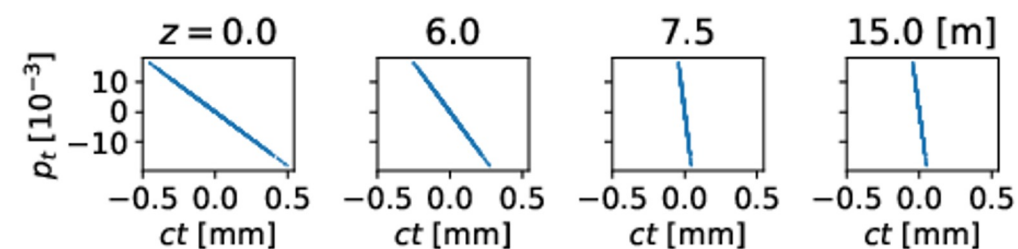
This section allows you to **download input files** that correspond to different physical situations or test different code features.

- FODO Cell
- Chicane
- Constant Focusing Channel
- Constant Focusing Channel with Space Charge
- Expanding Beam in Free Space
- Kurth Distribution in a Periodic Focusing Channel
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- FODO Cell, Chromatic
- Chain of thin multipoles
- A nonlinear focusing channel based on the IOTA nonlinear lens
- The "bare" linear lattice of the Fermilab IOTA storage ring
- Solenoid channel
- Drift using a Pole-Face Rotation
- Soft-edge solenoid
- Soft-Edge Quadrupole
- Positron Channel
- Cyclotron
- Combined Function Bend
- Ballistic Compression Using a Short RF Element
- Test of a Transverse Kicker

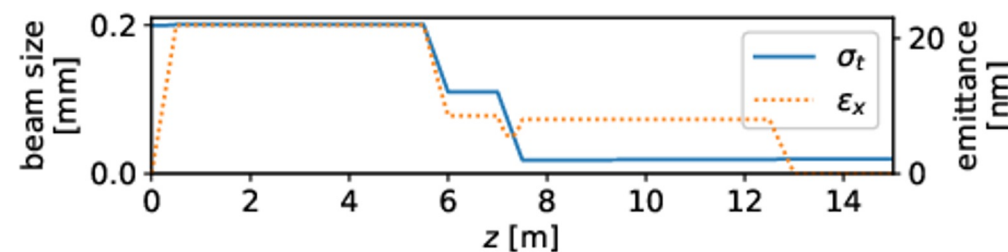
*currently 34*

## Berlin-Zeuthen Chicane

- rms-matched 5 GeV electron beam with initial normalized transverse rms emittance of  $1 \mu\text{m}$
- LCLS (@5GeV) & TESLA XFEL (@500MeV)-like



- longitudinal phase space: 10x compression
- emittance coupling: recovered at exit



[github.com/ECP-WarpX/impactx](https://github.com/ECP-WarpX/impactx)



# ImpactX 3D Space Charge Validation: E field in a 3D Gaussian bunch

- Electric field in a 1 nC Gaussian bunch at rest for several values of aspect ratio (1M particles)\*:

$$r = \sigma_z / \sigma_{\perp}, \quad \sigma_x = \sigma_y = \sigma_{\perp} = 1 \text{ mm}$$

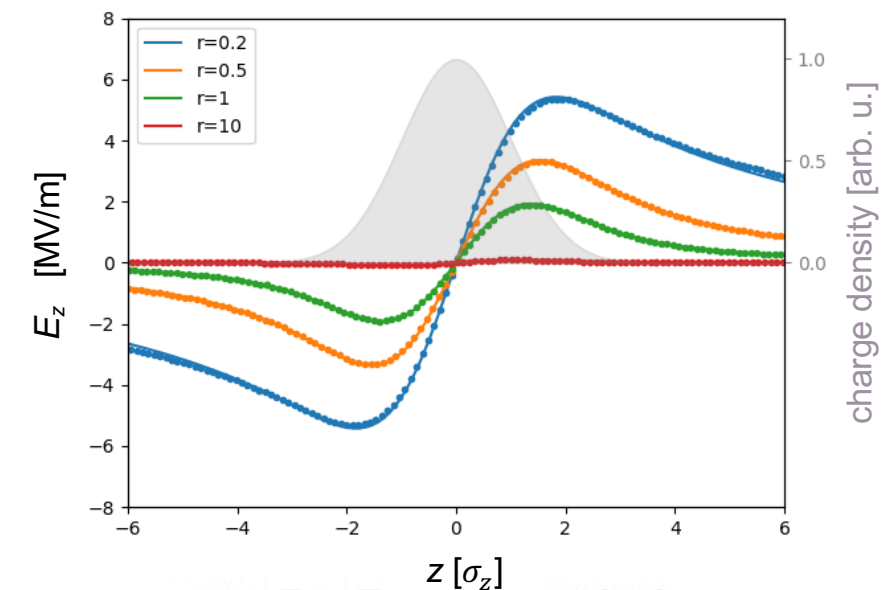
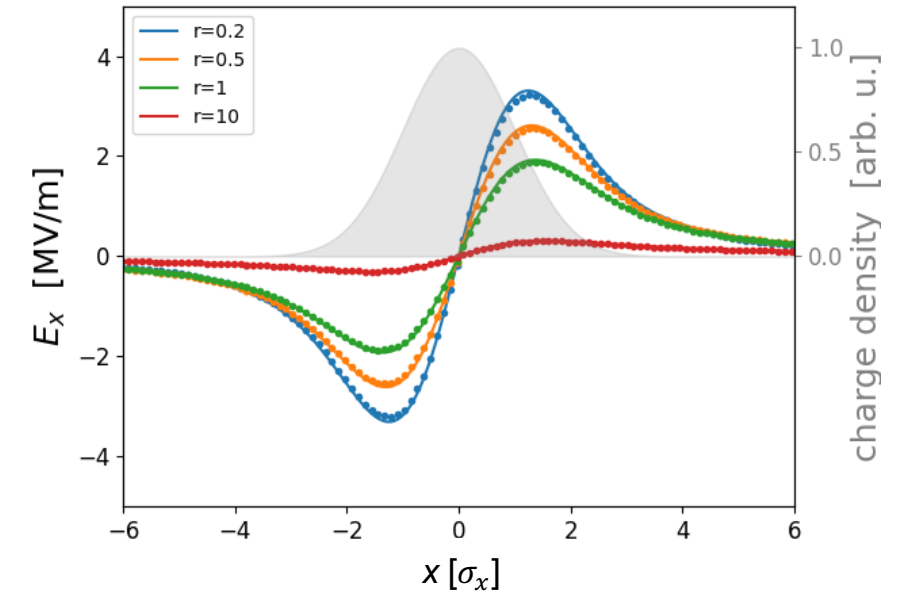
- Points – output from ImpactX. Lines – exact result.

$$\vec{E} = -\nabla\phi \quad \text{where:}$$

$$\phi = \frac{Q}{4\pi\epsilon_0} \sqrt{\frac{2}{\pi}} \int_0^{\infty} \frac{e^{\frac{-\lambda^2 x^2}{2(\lambda^2 \sigma_x^2 + 1)}} e^{\frac{-\lambda^2 y^2}{2(\lambda^2 \sigma_y^2 + 1)}} e^{\frac{-\lambda^2 z^2}{2(\lambda^2 \sigma_z^2 + 1)}}}{\sqrt{(\lambda^2 \sigma_x^2 + 1)(\lambda^2 \sigma_y^2 + 1)(\lambda^2 \sigma_z^2 + 1)}} d\lambda$$

- Convergence becomes more challenging for large aspect ratio → need Integrated Green Function (IGF) approach.

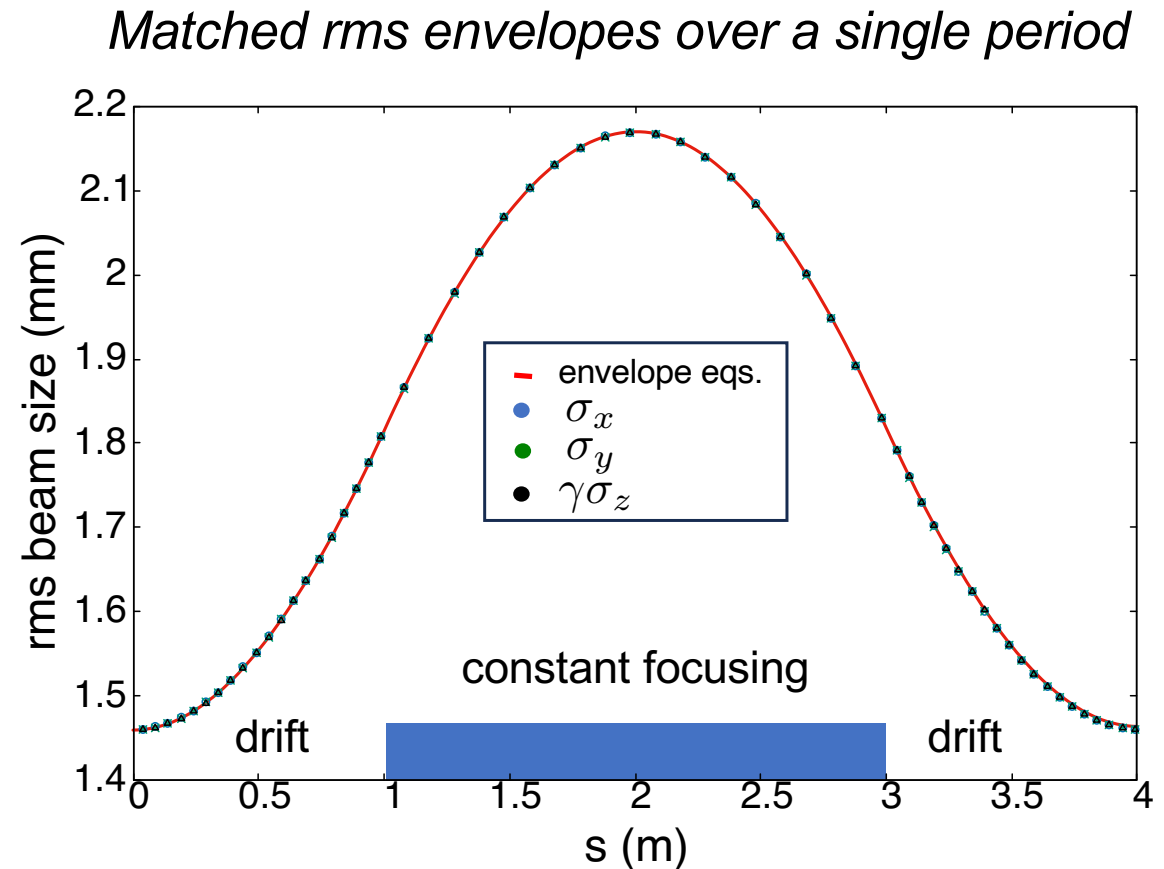
\*C. Mayes et al, IPAC2018, THPAK085 (2018)  
C. Mitchell et al, HB2023, THBP44 (2023)





# ImpactX 3D Space Charge Validation: Kurth beam in periodic focusing

- Analogous to a K-V beam in a FODO channel, but appropriate for 3D bunched beams.
- Space charge forces are linear: fully described by 3D envelope equations
- 10 nC proton bunch @ 2 GeV
- unnormalized emittance  $\epsilon_d = 1 \mu\text{m}$  (all planes)
- Phase advance  $121^\circ \rightarrow 74^\circ$

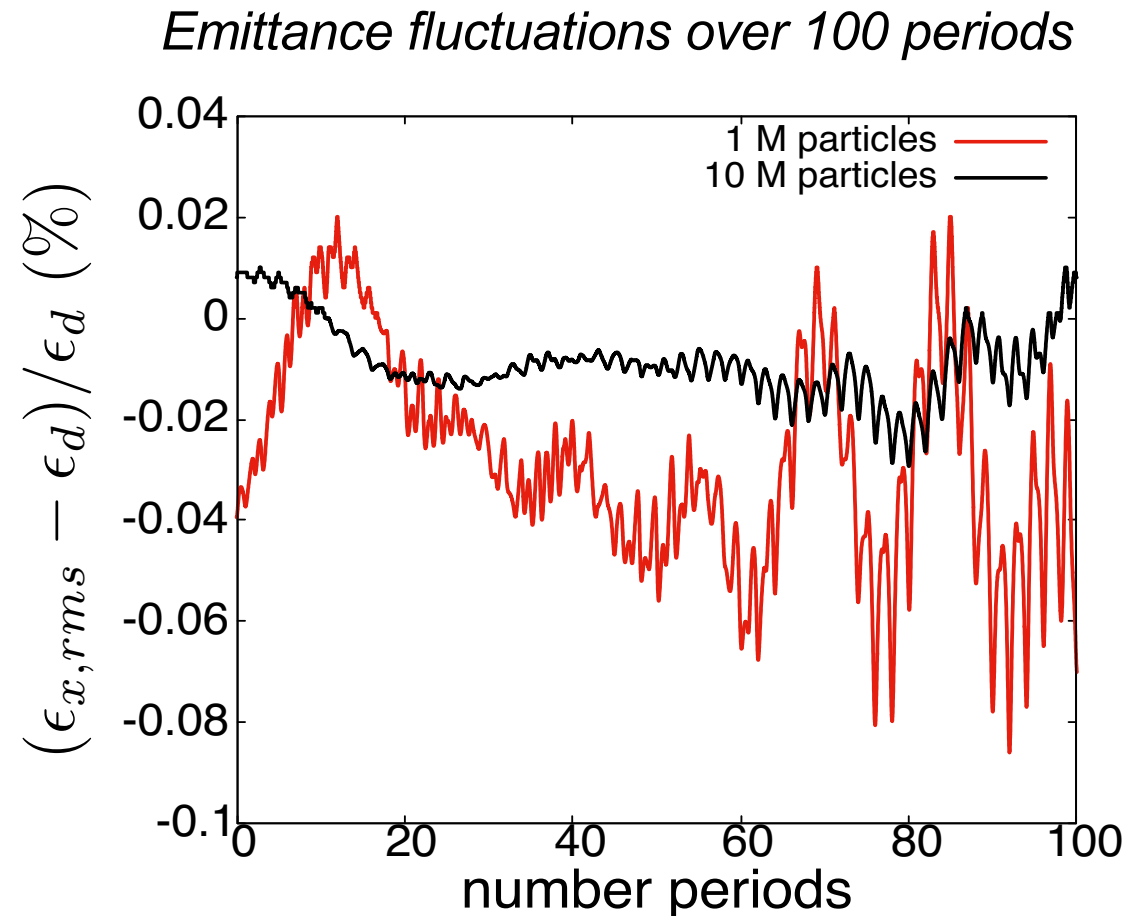


R. Kurth, Quart. Appl. Math. 36, pp. 325-329 (1978), C. Mitchell et al, IPAC2021, pp. 3213-3216 (2021).

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- Phase advance  $121^\circ \rightarrow 74^\circ$

1 M particles, [72,72,72] grid  
10 M particles, [128,128,128] grid



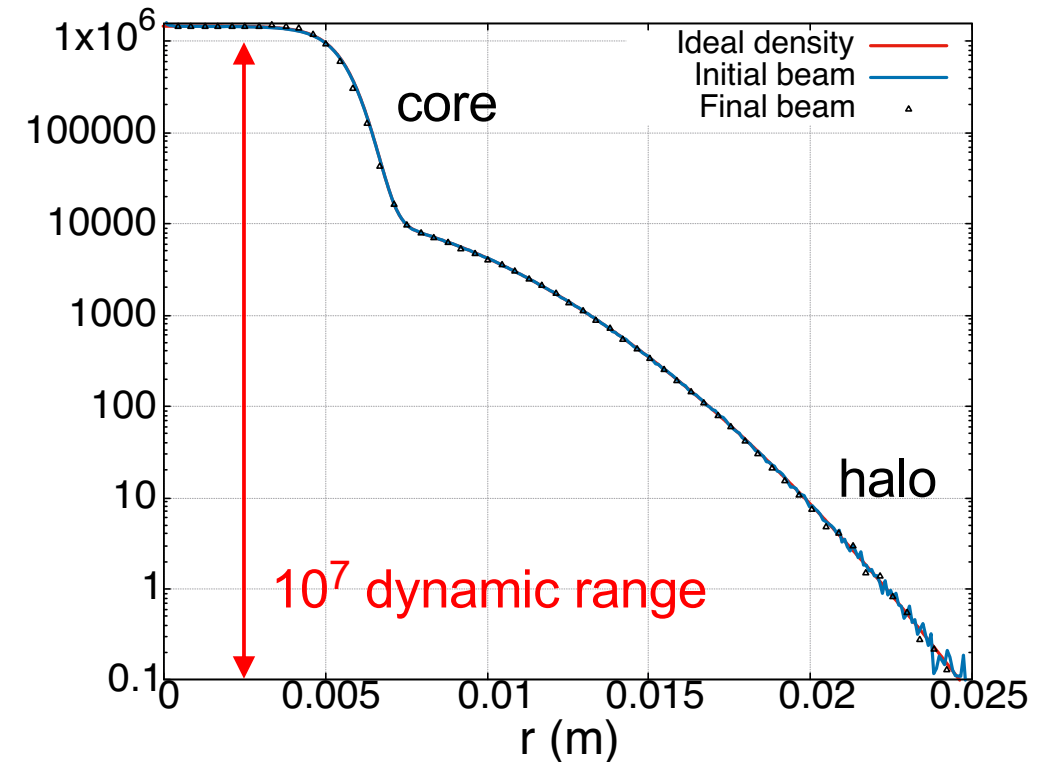
R. Kurth, Quart. Appl. Math. 36, pp. 325-329 (1978), C. Mitchell et al, IPAC2021, pp. 3213-3216 (2021).

# ImpactX 3D Space Charge Validation: bithermal beam in a CF channel

- Self-consistent model of a 3D bunch with a stationary core-halo distribution\*.  
$$f = c_1 \exp(H/kT_1) + c_2 \exp(H/kT_2)$$
- Bunch is radially symmetric in the beam rest frame.
- A system of ODEs is solved for the space charge potential and radial density in equilibrium.
- 10 nC proton bunch @ 0.1 MeV
- $kT_1 = 36 \times 10^{-6}$ ,  $kT_2 = 900 \times 10^{-6}$
- 95% of charge in core, 5% of charge in halo
- Beam is stationary over 10 focusing periods.

\*R. Ryne et al, EPAC2004, WEPLT047 (2004)  
C. Mitchell et al, HB2023, THBP44 (2023)

*Spatial beam density as a function of radius*



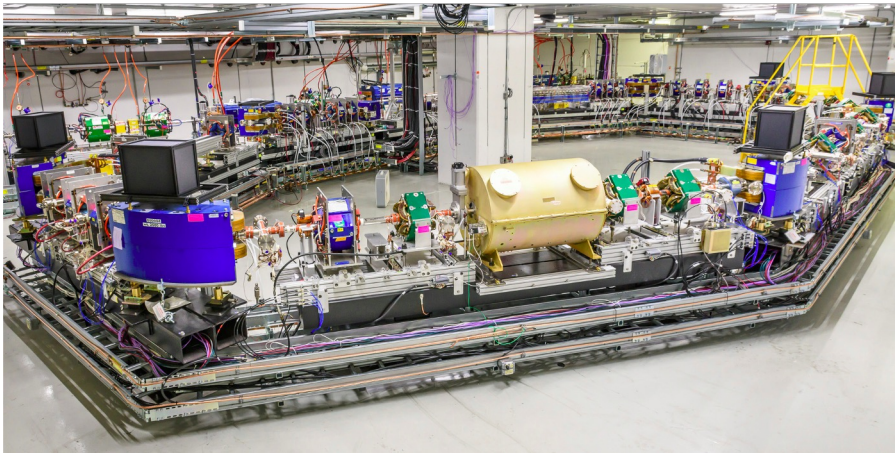
10 M particles, [128,128,128] grid

**Zenodo: [doi.org/10.5281/zenodo.8395849](https://doi.org/10.5281/zenodo.8395849)**

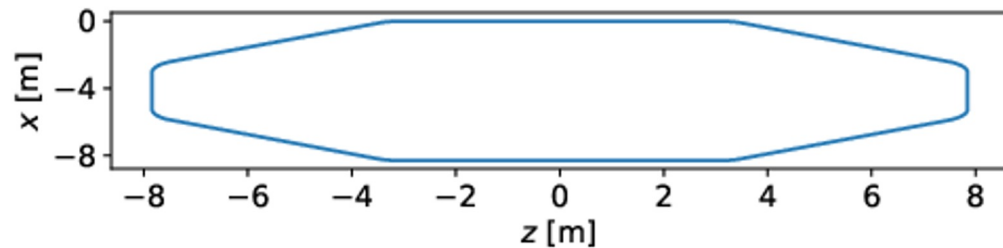
- Toward ImpactX applications to IOTA

# IOTA (v. 8.4) Bare Lattice Benchmark, 2.5 MeV protons

Bare (linear) lattice of the Fermilab IOTA storage ring; an rms-matched proton beam with an un-normalized emittance of  $4.5 \mu\text{m}$  propagates over a single turn

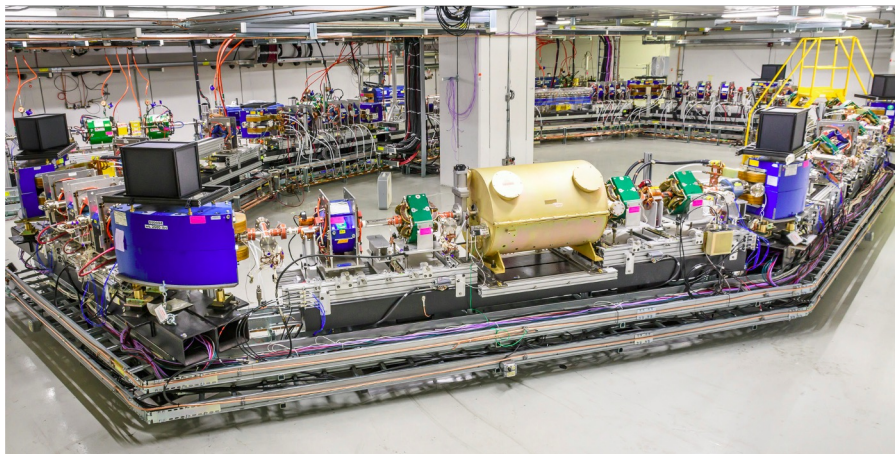


Reference Orbit

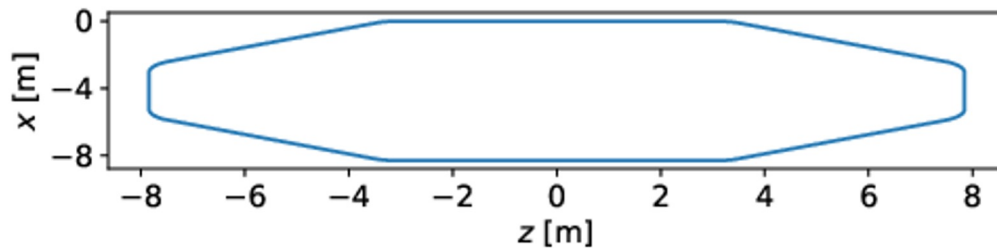


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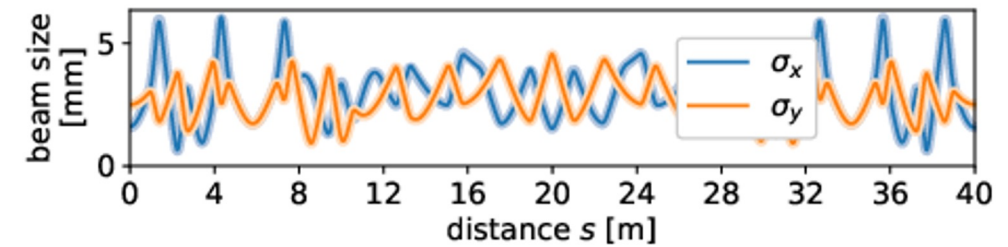
Reference Orbit



## Second Moments / Linear Optics

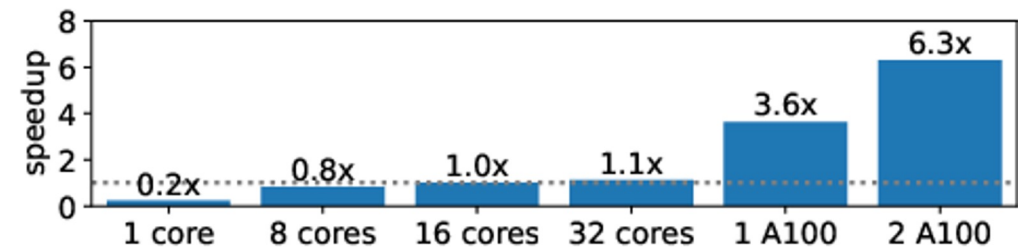
- check emittance preservation
- check rms beam envelopes:

IMPACT-Z vs ImpactX



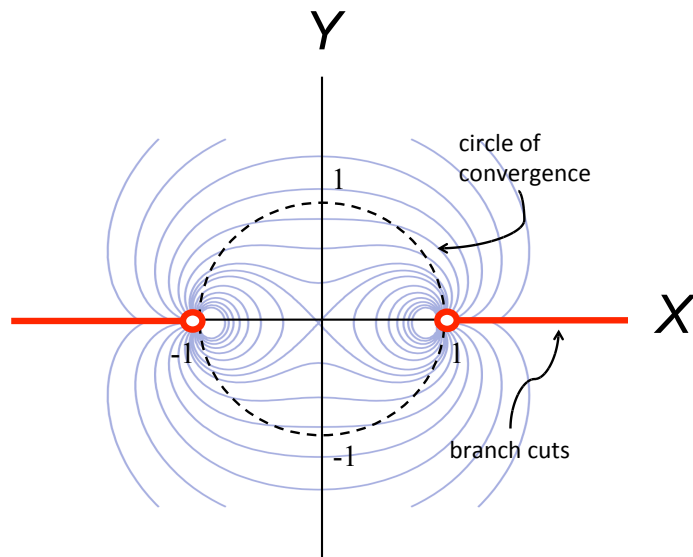
## Preliminary Performance

- on Perlmutter (NERSC) CPU / GPU
- order-of-magnitude perf.  w/o dyn. LB (yet)



# Modeling of IOTA nonlinear integrable optics

## Magnetic field lines in the NLI (transverse plane)



Coordinates normalized  
by  $c\sqrt{\beta_x} = c\sqrt{\beta_y}$ ,  
 $c = 0.01 \text{ m}^{1/2}$

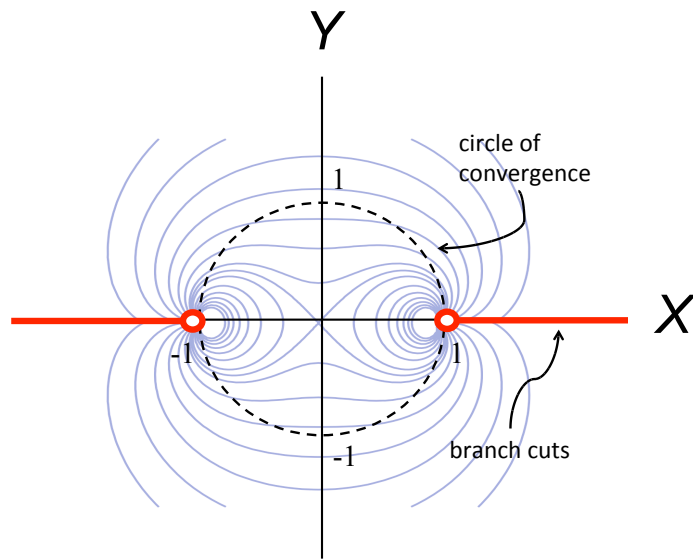
- ImpactX contains a model of the IOTA nonlinear magnetic element\*

V. Danilov and S. Nagaitsev, PRAB 13, 084002 (2010)

C. Mitchell *et al*, PRAB 23, 064002 (2020), & arXiv.1908.0036 (2019)

# Modeling of IOTA nonlinear integrable optics

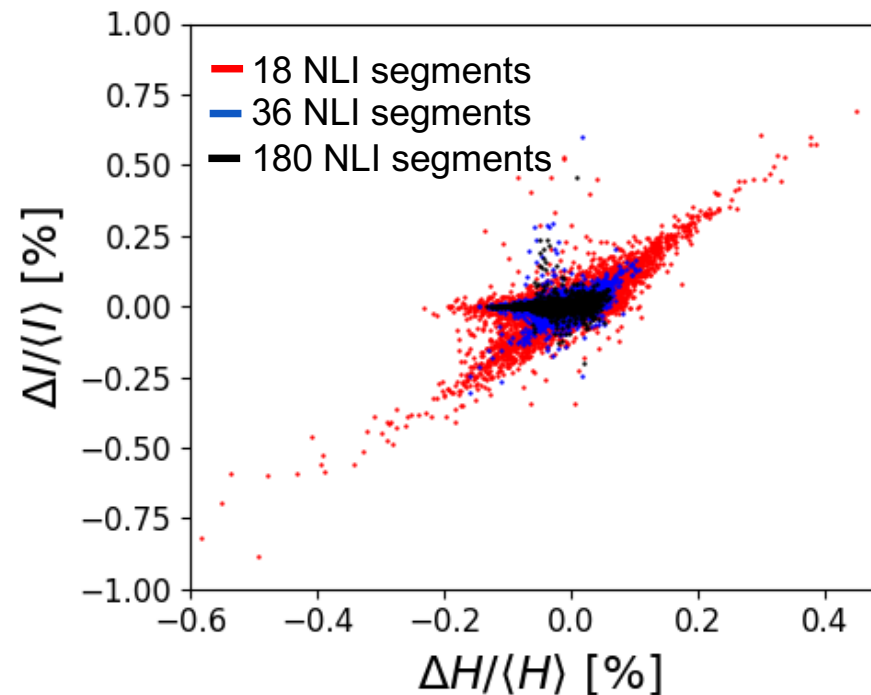
## Magnetic field lines in the NLI (transverse plane)



Coordinates normalized  
by  $c\sqrt{\beta_x} = c\sqrt{\beta_y}$ ,  
 $c = 0.01 \text{ m}^{1/2}$

## Preservation of nonlinear invariants

change in  $(H,I)$  after 100 turns



Increasing the number of NLI segments  
results in improved preservation of  $(H,I)$ .

- ImpactX contains a model of the IOTA nonlinear magnetic element\*
- Example shown for a 2.5 MeV p beam initially matched to the bare lattice linear optics with  $\epsilon_{x,y} = 3 \mu\text{m}$

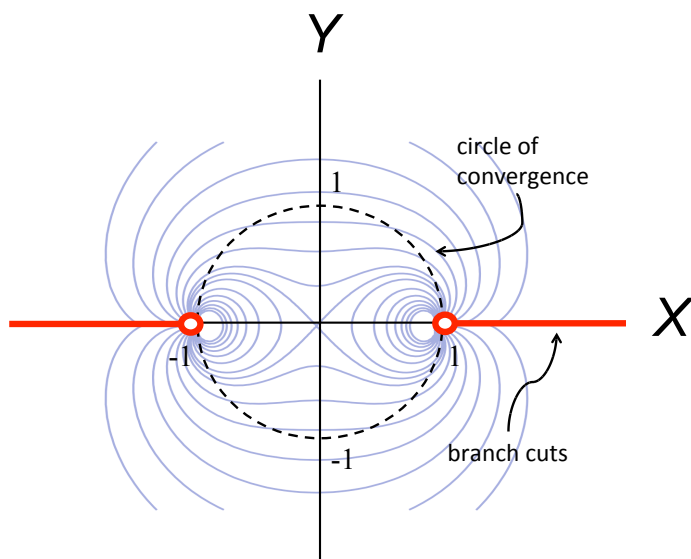
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# Modeling of IOTA nonlinear integrable optics

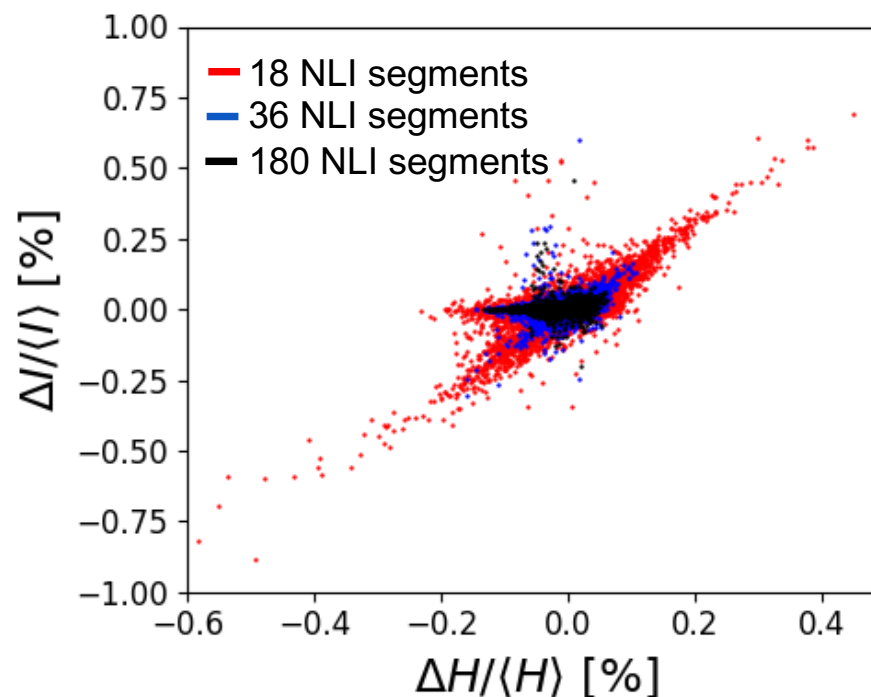
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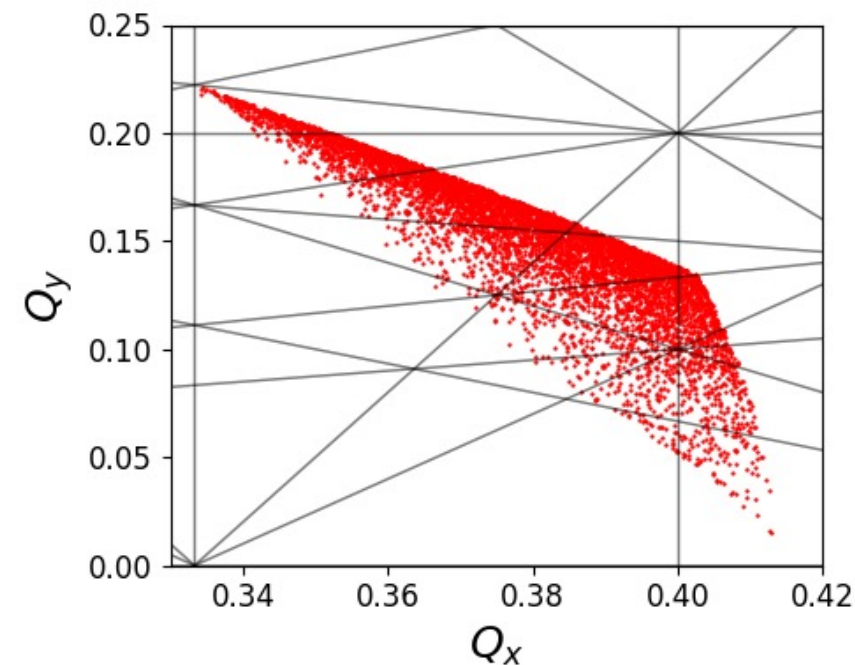
change in  $(H,I)$  after 100 turns



Increasing the number of NLI segments  
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## Fractional tune footprint

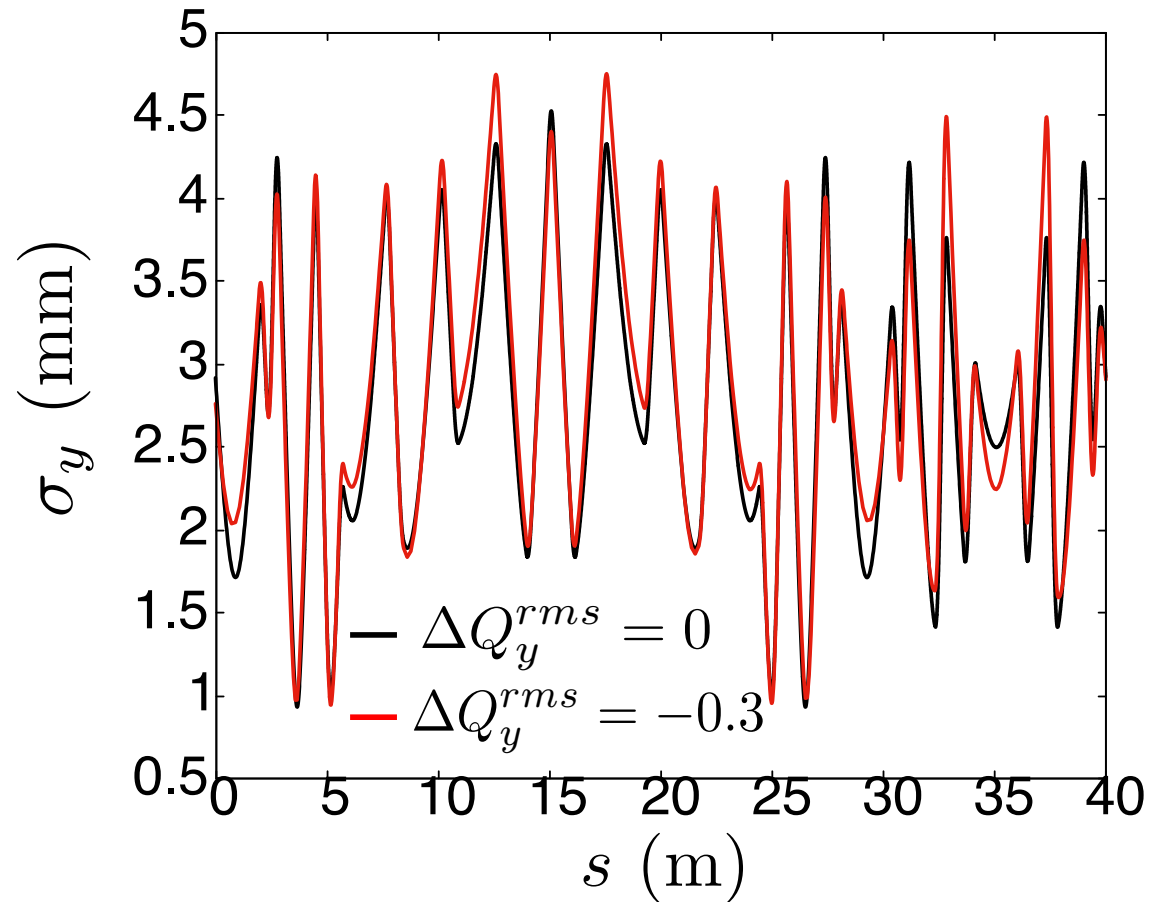
resonance lines through order 5



Nonlinear tune spread from TBT data.  
Cf. bare linear lattice:  $(Q_x, Q_y) = (0.3, 0.3)$

# Examples of IOTA space charge modeling in ImpactX\*

RMS matching w/ space charge (via Python interface)

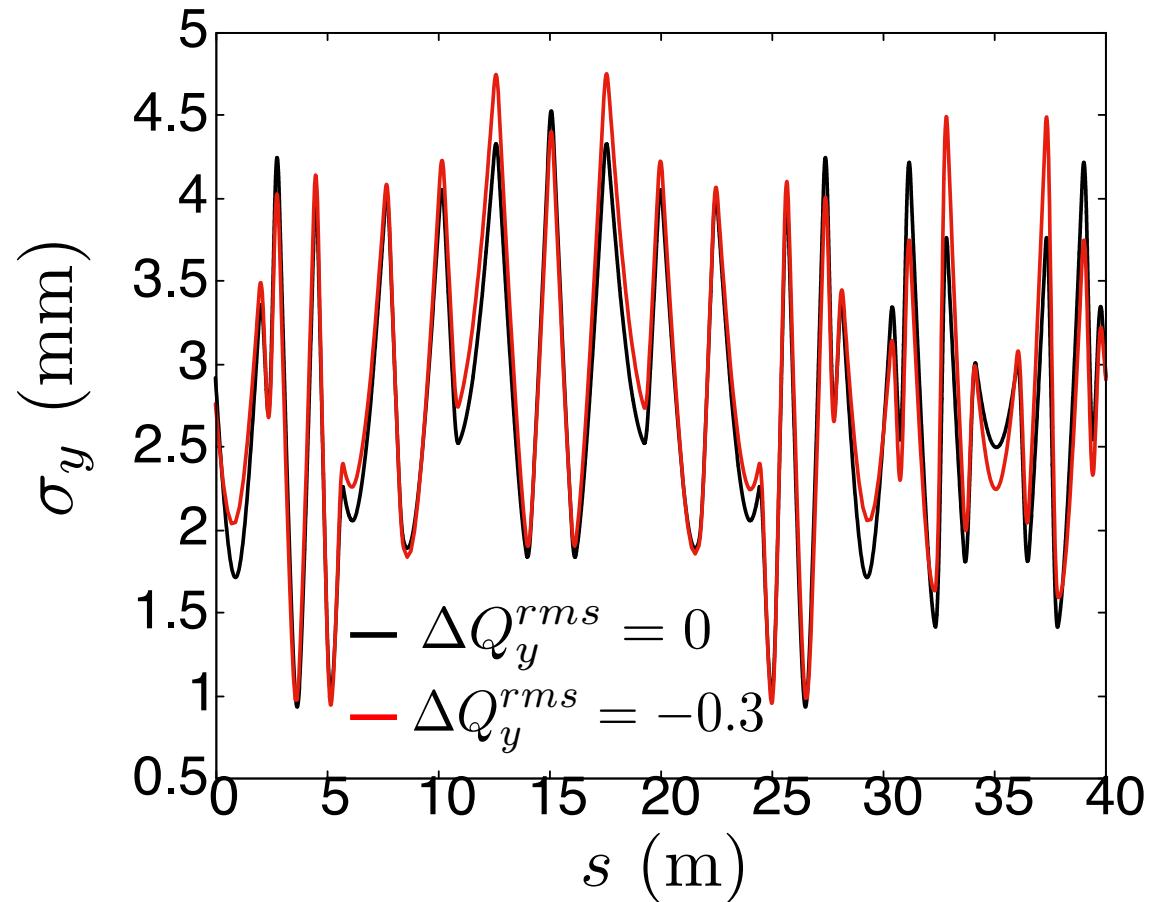


- Using the Python interface, the user can couple ImpactX space charge runs with optimization.
- Vertical beam envelope for a beam matched to the bare linear lattice at nominal emittance with space charge tune depression -0.3.

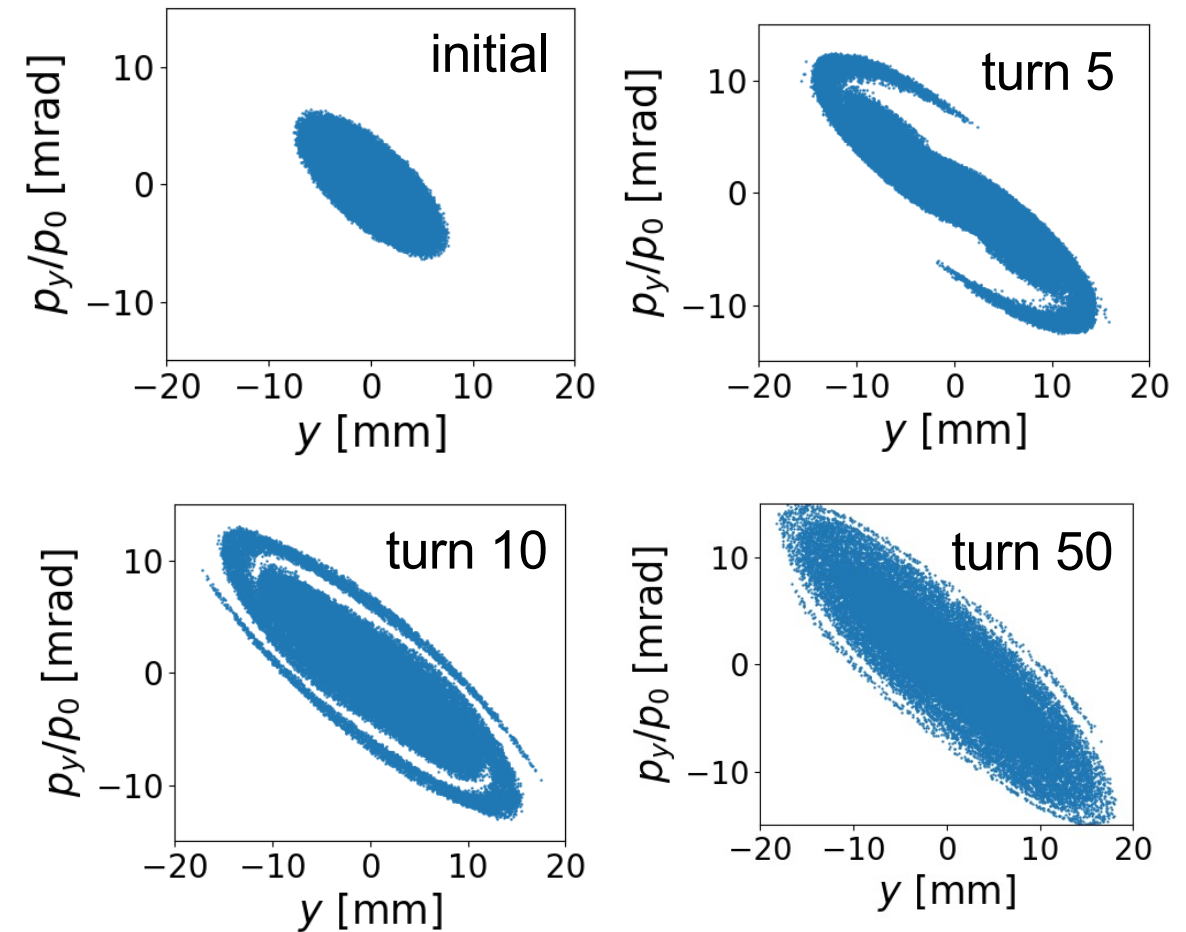
\*Using a bunched beam with  $E_z^{SC} = 0$  to avoid debunching.

# Examples of IOTA space charge modeling in ImpactX\*

RMS matching w/ space charge (via Python interface)




Vertical phase space in the presence of space charge & nonlinear optics



\*Using a bunched beam with  $E_z^{SC} = 0$  to avoid debunching.

For an initial SC tune shift  $\Delta Q_y^{rms} = -0.3$

# Conclusions

- A community approach to code development (eg, based on shared standards, common code interfaces, and shared benchmarks) is needed to address the challenges of high-intensity and high brightness beam modeling.
- BLAST is an open interoperable ecosystem of PIC codes for particle accelerator modeling
  - WarpX – for relativistic t-based laser-plasma and beam modeling
  - ImpactX – for s-based beam dynamics modeling in linacs and rings, ...
- Runs on any platform: Linux, macOS, Windows
- Open public development, automated testing, review & documentation  **GitHub**
- Future plans for ImpactX development include:
  - Implementation of 2D and/or 2.5D space charge models for long and unbunched beams
  - Addition of 1D resistive wall + CSR wakefield models (already in IMPACT-Z)
- *Comments welcome on additional capabilities relevant to FAST/IOTA modeling.*

**Thank you for your attention!**

**Questions?**

**Contact: [ChadMitchell@lbl.gov](mailto:ChadMitchell@lbl.gov)**

- Backup Slides

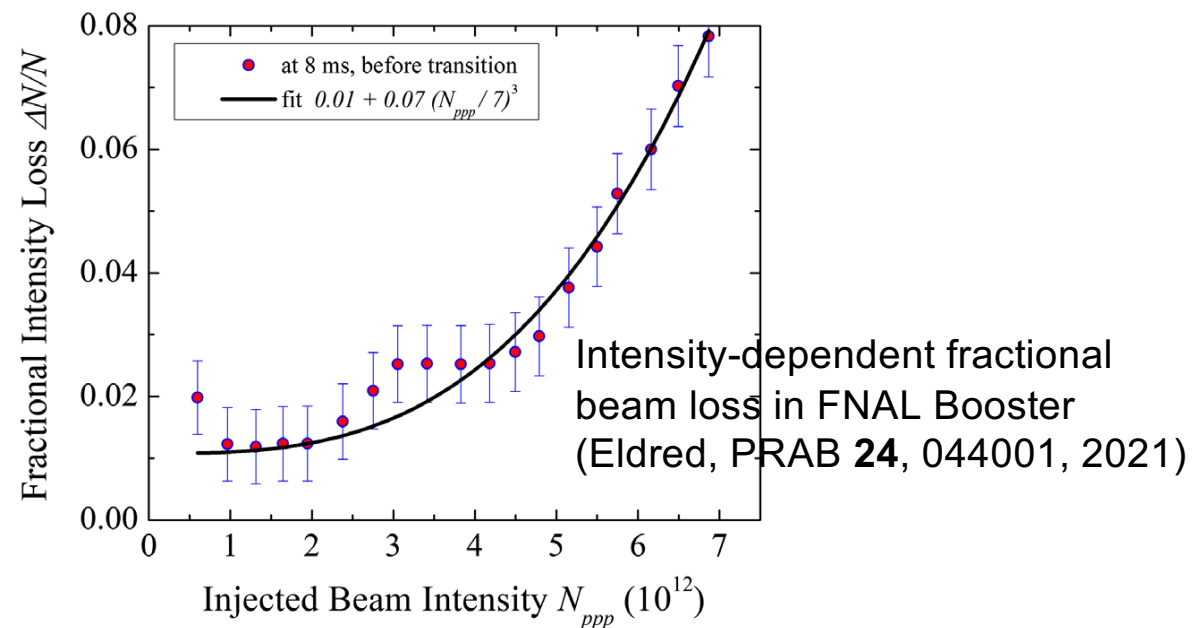
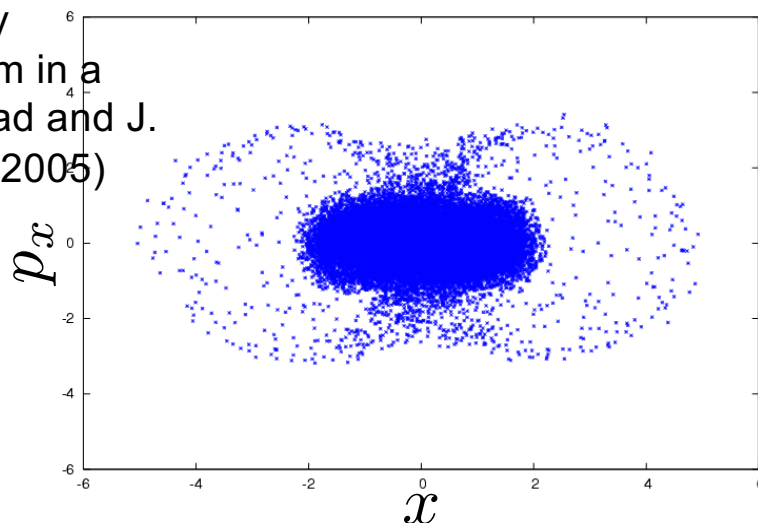
# Space charge modeling at high fidelity: a community effort

PIC modeling with high spatial resolution and good particle statistics is needed to:

- predict low-density beam halo formation
- understand intensity-dependent beam loss
- understand space charge induced emittance growth
- model and mitigate certain collective instabilities

Beam halo generated by mismatched proton beam in a linear channel (K. Sonnad and J. Cary, PRAB **8**, 064202, 2005)

Dynamic range can be  $\gg 10^6$

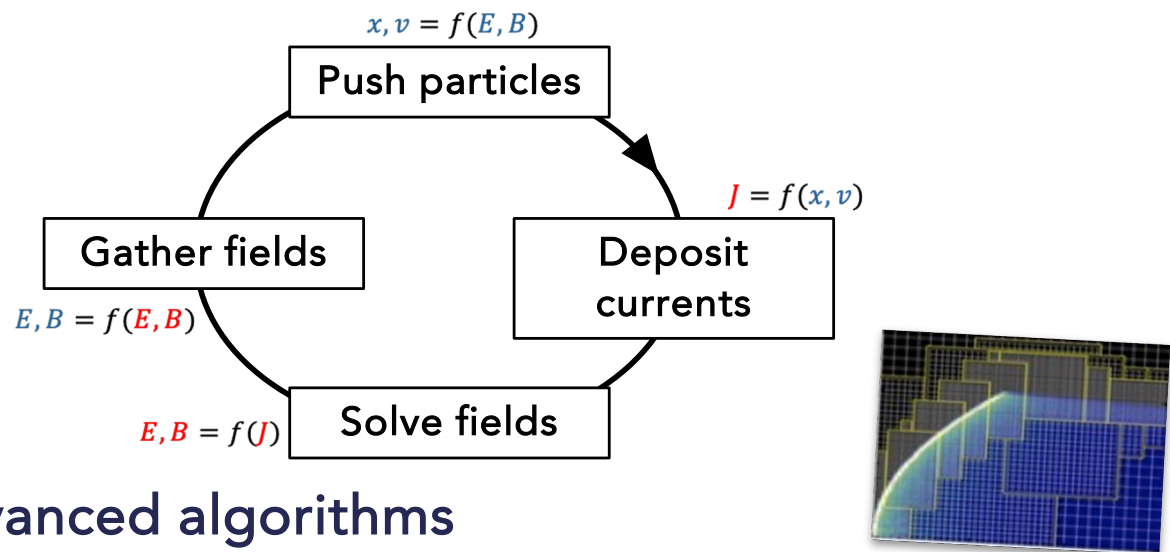


For large turn numbers in rings, PIC is subject to numerical artifacts (noise) and long computing times  $\rightarrow$  fast tools exploiting GPU architectures + integrated workflows + AI/ML

# WarpX is a GPU-Accelerated PIC Code for Exascale

## Available Particle-in-Cell Loops

- electrostatic & electromagnetic (fully kinetic)



## Advanced algorithms

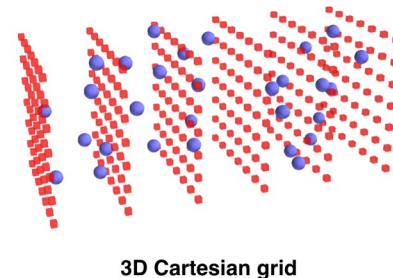
boosted frame, spectral solvers, Galilean frame, embedded boundaries + CAD, MR, ...

## Multi-Physics Modules

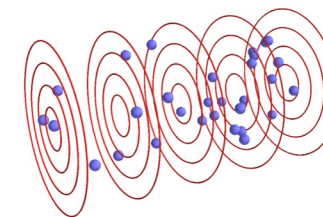
field ionization of atomic levels, Coulomb collisions, QED processes (e.g. pair creation), macroscopic materials

## Geometries

- 1D3V, 2D3V, 3D3V and RZ (quasi-cylindrical)



3D Cartesian grid



Cylindrical grid (schematic)

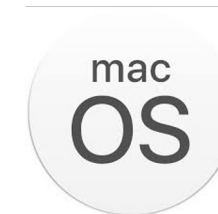
## Multi-Node parallelization

- MPI: 3D domain decomposition
- dynamic load balancing



## On-Node Parallelization

- GPU: CUDA, HIP and SYCL
- CPU: OpenMP



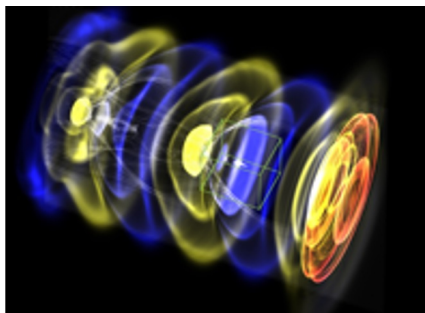
## Scalable, Standardized I/O

- PICMI Python interface
- openPMD (HDF5 or ADIOS)
- in situ diagnostics



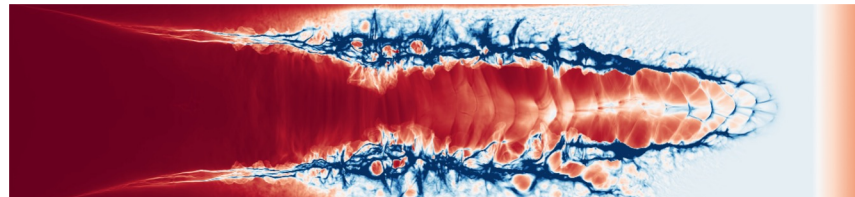


# WarpX supports a growing number of applications

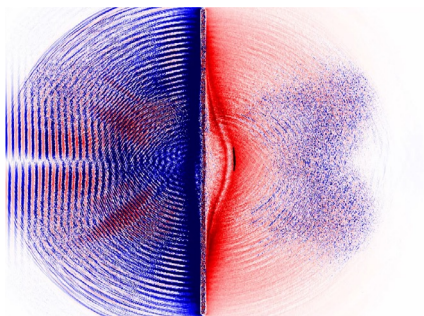
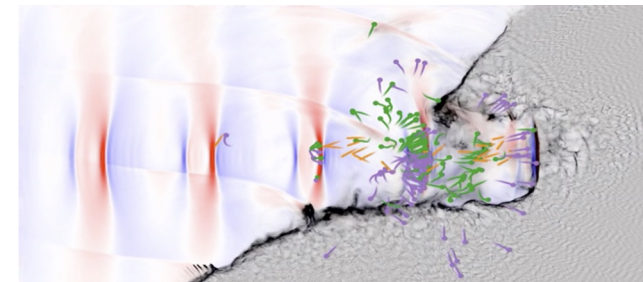


Plasma accelerators (LBNL, DESY, SLAC)

Laser-ion acceleration - advanced mechanisms (LBNL)

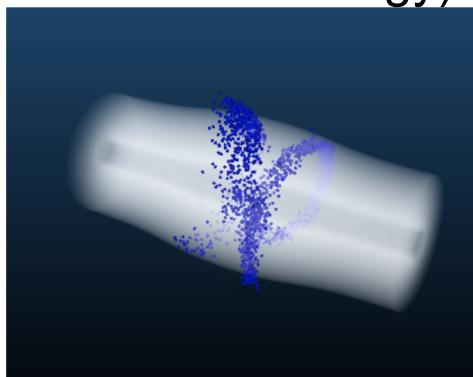


Plasma mirrors and high-field physics + QED (CEA Saclay/LBNL)

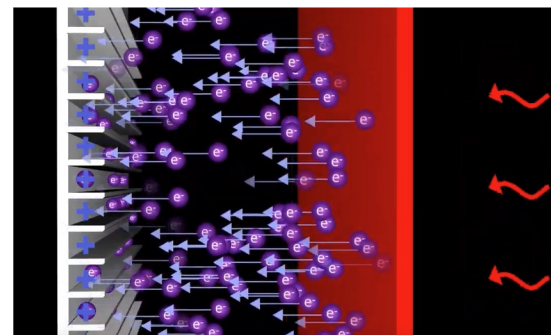


Laser-ion acceleration - laser pulse shaping (LLNL)

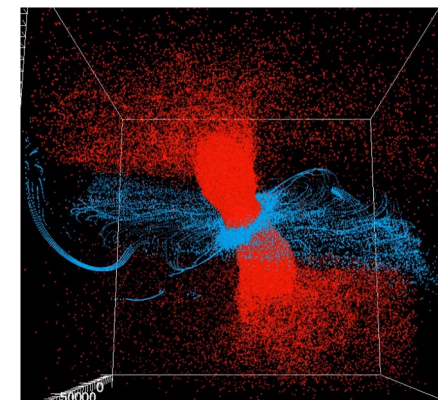
Plasma confinement, fusion devices (Zap Energy, Avalanche Energy)



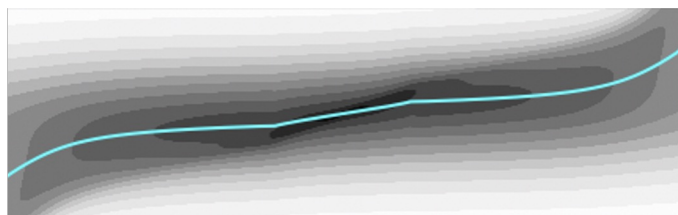
Thermionic converter (Modern Electron)



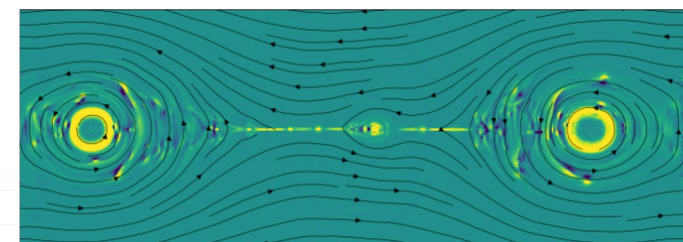
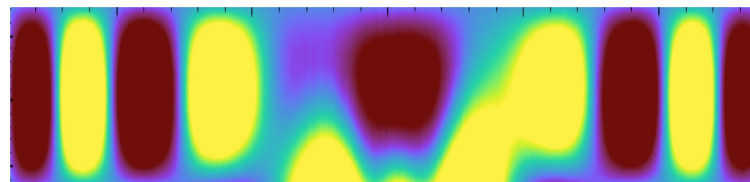
Pulsars, magnetic reconnection (LBNL)



Magnetic fusion sheaths (LLNL)



Microelectronics (LBNL) - ARTEMIS



# openPMD: Open Standard for Particle-Mesh Data



- **markup** / schema for arbitrary hierarchical data formats
- truly, scientifically **self-describing**
- basis for **open data workflows**

**openPMD standard** (1.0.0, 1.0.1, 1.1.0)

*the underlying file markup and definition*

A Huebl et al., DOI:10.5281/zenodo.33624

**base** *general description*

**standard extensions** *domain specific*

wavefronts, particle species, particle beams, weighted particles, PIC, MD, mesh-refinement, CCD images, ...



**openPMD-viewer**

*quick visualization*

explore, e.g., in Jupyter

**openPMD-api**

*reference library*

file-format agnostics API

**openPMD-updater**

*auto-update to new standard, verify*

**openPMD-validator**



# IMPACT: Multi-Physics High-Intensity and High Brightness Beam Dynamics Code Suite

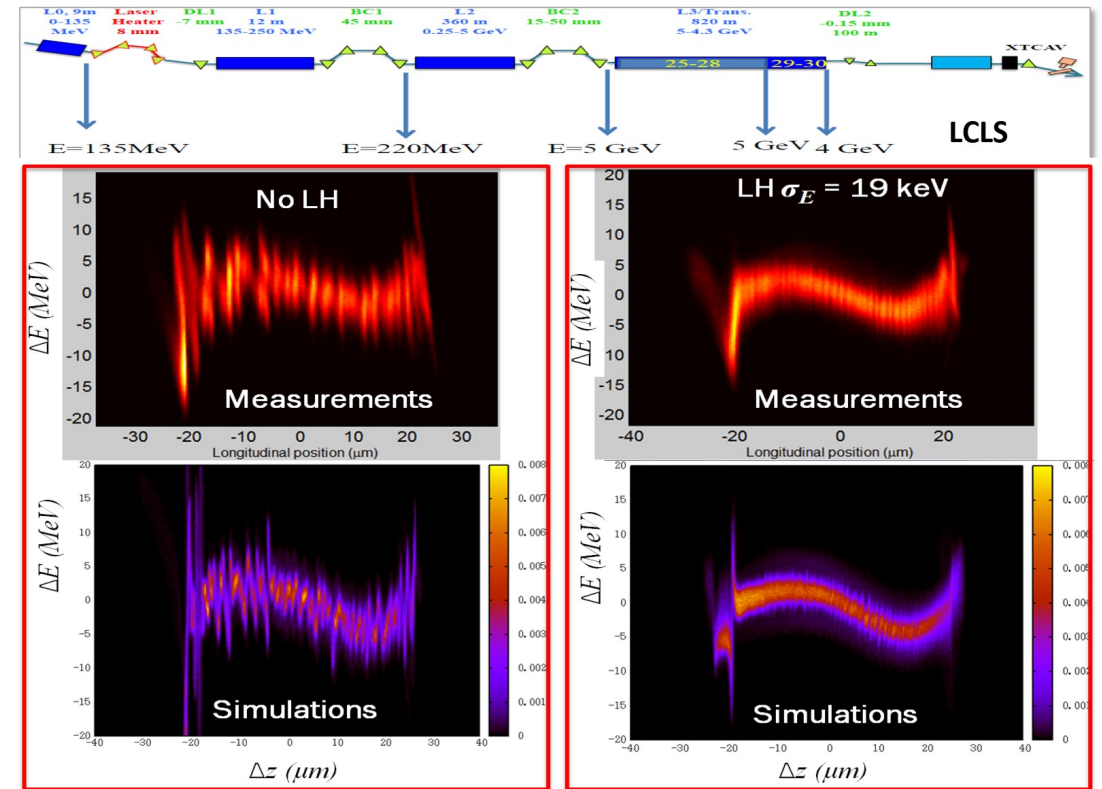
## Key features include:

- time-dependent and position dependent PICs
- serial and massive parallelization
- detailed 3D RF accelerating and focusing model
- standard elements: dipole, solenoid, multipole, etc.
- multiple charge states, multiple bunches
- 3D space charge effects
- structure and resistive wall wakefields
- coherent synchrotron radiation (CSR)
- incoherent synchrotron radiation (ISR)
- photo-electron emission
- machine errors and steering

## The IMPACT code suite is used by > 40 institutes worldwide

- successfully applied to both electron & proton machines:
  - CERN PS2 ring, SNS linac, ...
  - LCLS-II linac
- unprecedented resolution:  $\sim 2B$  macroparticles

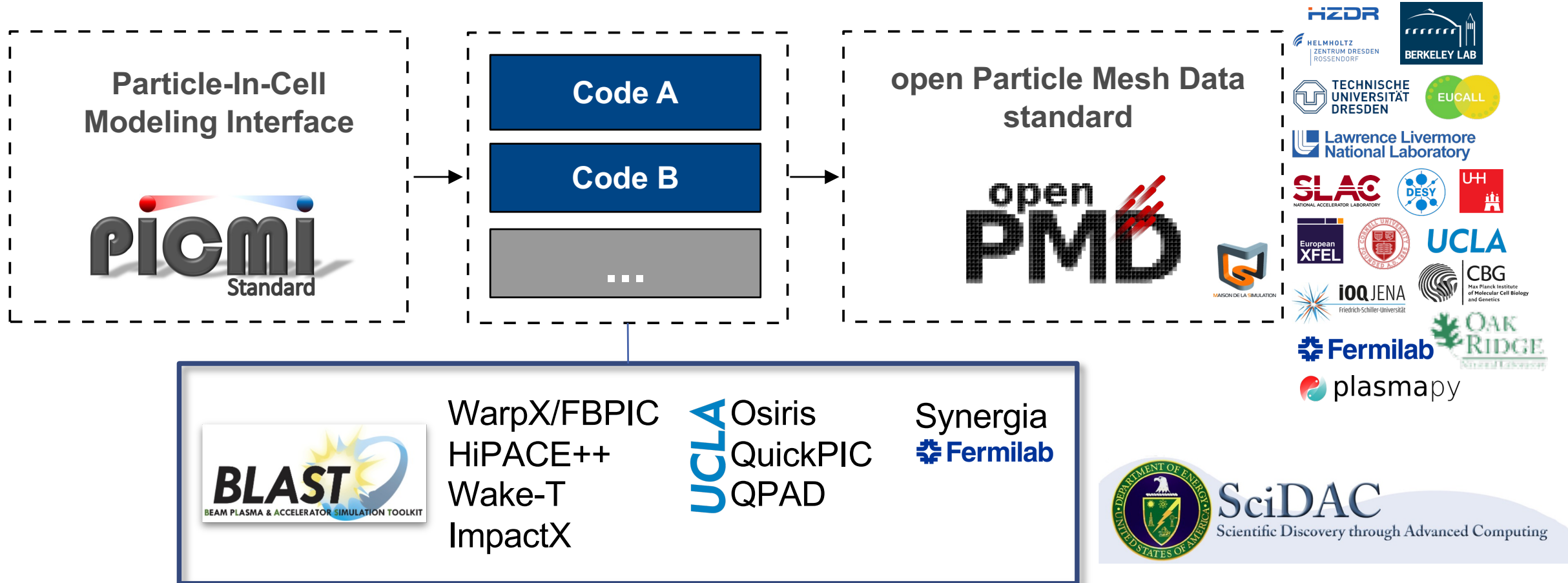
## Start-to-end simulation of the Linac Coherent Light Source



J. Qiang et al., Phys. Rev. Accel. Beams 20, 054402 (2017).

# Integration with standardized I/Os toward a Community Accelerator Simulations Ecosystem (CASE)

CASE



- Collaborative multi-institutional effort supported by SciDAC-5 for HEP applications
- openPMD standard is already fairly mature and widely adopted
- PICMI is more recent and also more challenging: redesign is planned for FY24
- Discussions underway/welcome regarding an accelerator lattice standard (AMI)