

Neutrino Mass Models at the Intensity Frontier

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Where does neutrino mass come from ?

- For charged fermions, they come from the Higgs vev:

$$m_f = h_f v_{wk} \quad v_{wk} = \langle h^0 \rangle$$

★ Discovery of the 125 GeV Higgs h^0 confirms this.

- For **neutrinos**, this formula gives too large a mass !!

- **Enter seesaw paradigm:**

(Minkowski; Gell-Mann, Ramond, Slansky; Yanagida; Glashow; Mohapatra, Senjanovic)

$$m_\nu = \lambda \frac{v_{wk}^2}{M}$$

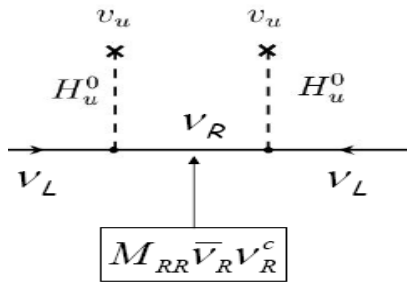
- $\lambda \sim 1$; M big $m_\nu \ll m_f$ **Physics of M ?**

- **Alternative strategies:** Radiative effects (Babu, Zee,...)

Unravelling Seesaw

■ Add New fermions \mathbf{N}_R or new Higgs Δ to SM

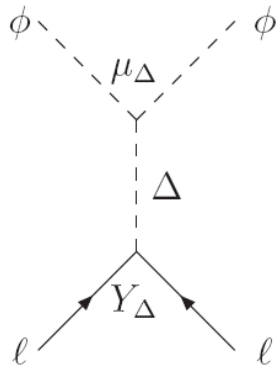
Type I



$$m_\nu \cong -\frac{h_v^2 v_{wk}^2}{M_R}$$

Majorana \mathbf{N}

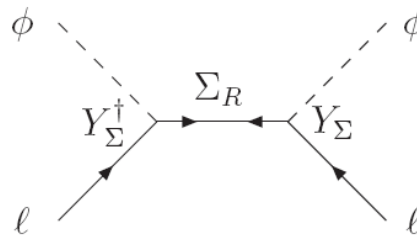
Type II



$$m_\nu = -2Y_\Delta v^2 \frac{\mu_\Delta}{M_\Delta^2}$$

Triplet Higgs $\vec{\Delta}$

Type III



$$m_\nu = -\frac{v^2}{2} Y_\Sigma^T \frac{1}{M_\Sigma} Y_\Sigma$$

Triplet N Maj.

Inverse

$$\begin{pmatrix} 0 & hv_{wk} & 0 \\ hv_{wk} & 0 & M \\ 0 & M & \mu \end{pmatrix}$$

$$m_\nu \cong -m_D^T M^{-1} \mu M^{-1} m_D$$

Dirac \mathbf{N}

Can seesaw scale be TeV ?

How do we probe it ?

- Colliders: key parameter is νN mixing $\varepsilon = \frac{h_\nu v_{wk}}{M_N}$
- Generic TeV models: h_ν small to get small mass hence $\varepsilon \leq 10^{-6}$; N unobservable !!

- **Exceptions:** sym. or Inverse seesaw: $\varepsilon \leq 0.1$

$$h_\nu = \begin{pmatrix} h_{11} & \epsilon_1 & \epsilon_2 \\ h_{21} & \epsilon_3 & \epsilon_4 \\ h_{31} & \epsilon_5 & \epsilon_2 \end{pmatrix}$$

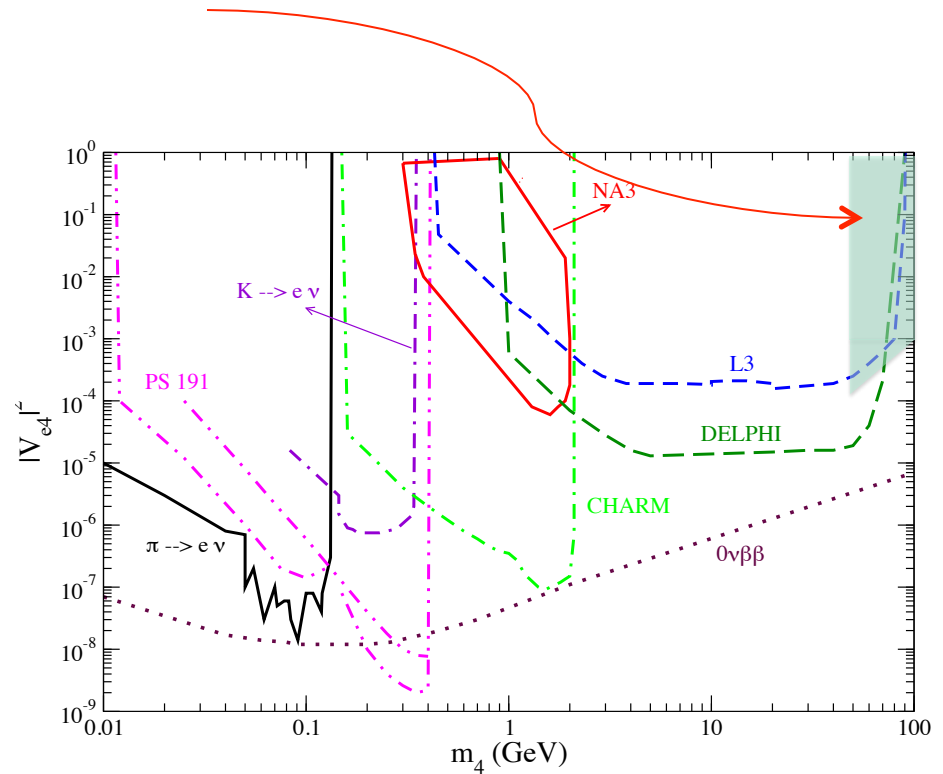
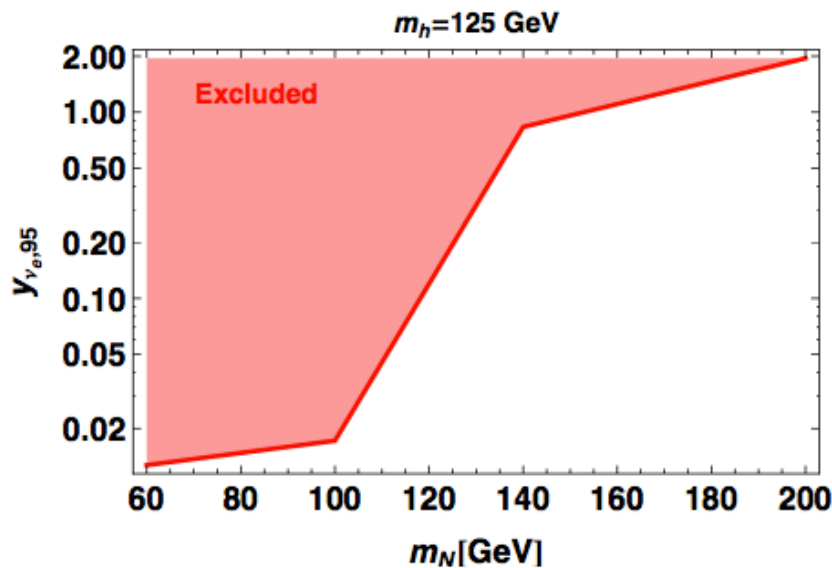
$$M_N = \begin{pmatrix} 0 & M & 0 \\ M & 0 & 0 \\ 0 & 0 & M' \end{pmatrix}$$

$$M_{\nu,N,S} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}$$

$$\mu \ll m_D, M$$

Higgs decay+other constraints

LHC Higgs search: final states $\rightarrow e^+ e^- \cancel{E}_T$ (Dev, Franceschini, RNM'12)



More collider info (Ruiz talk)

(Atre, Han, Pascoli, Zhang)

Lepton Flavor violation and minimal TeV seesaw

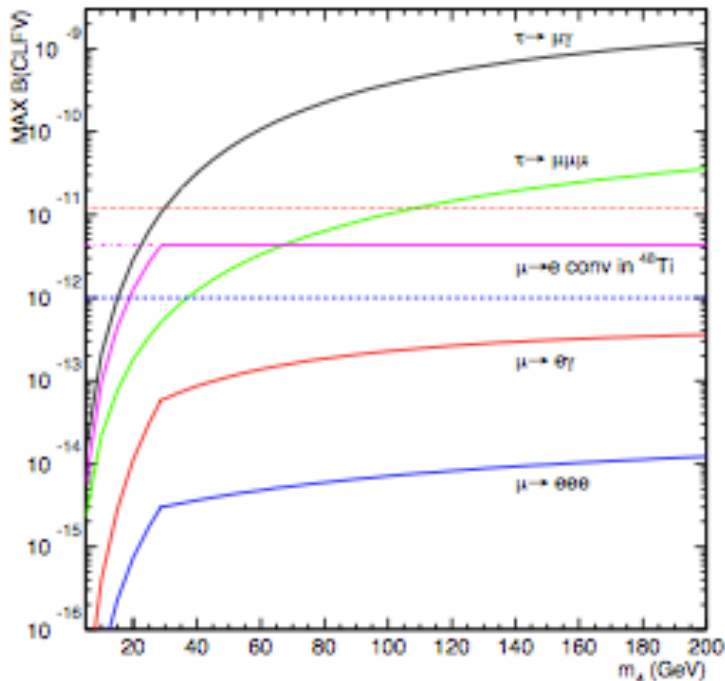
- Processes: (i) $\mu \rightarrow e + \gamma$ $B_{\mu \rightarrow e + \gamma} \leq 5.7 \times 10^{-13}$ MEG
(ii) $\mu \rightarrow 3e$ $B(\mu \rightarrow 3e) \leq 10^{-12}$ Sindrum
(iii) $\mu^- \rightarrow e^- |_{Ti}$ $B(\mu^- \rightarrow e^-) |_{Ti} \leq 4.3 \times 10^{-12}$
- **Generic seesaw** models without SUSY and no new gauge group: **effects are unobservable.**
- However with **symmetries to get small ν mass**, they can be a useful probes of minimal sub-TeV seesaw.

Lepton Flavor Violation with special low scale seesaw

- Majorana N mediated loop graphs: (deg. RH)

- Type I with symmetries: (de Gouvea'07)

Inverse seesaw case:



$$m_N \lesssim 6000 \text{ TeV} \cdot \left(\frac{10^{-18}}{R_{\mu \rightarrow e}^{Ti}} \right)^{\frac{1}{4}},$$

$$m_N \lesssim 1000 \text{ TeV} \cdot \left(\frac{10^{-16}}{R_{\mu \rightarrow e}^{Al}} \right)^{\frac{1}{4}},$$

$$m_N \lesssim 300 \text{ TeV} \cdot \left(\frac{10^{-14}}{Br(\mu \rightarrow e \gamma)} \right)^{\frac{1}{4}},$$

$$m_N \lesssim 1000 \text{ TeV} \cdot \left(\frac{10^{-16}}{Br(\mu \rightarrow eee)} \right)^{\frac{1}{4}}$$

(Gavela, Alonso, Hambye, Dhen'12);

Ilakovic, Pilaftsis, Popov'12

CLFV that directly relates to neutrino Majorana mass

- $\mu \rightarrow e\gamma, \mu \rightarrow 3e, \mu^- \rightarrow e^-$ conserve L and are not true tests of Majorana nu mass.
- However $\mu^- \rightarrow e^+, \mu^- \rightarrow \mu^+$ are $\Delta L \neq 0$

$$B(\mu^- Ti \rightarrow e^+ Ca) \leq 3.6 \times 10^{-11}$$

- Flavor analog of $\beta\beta_{0\nu}$ decay
- Small in minimal type I and inverse seesaw
- Other related processes: $K^+ \rightarrow \pi^- e^+ e^+, \pi^- e^+ \mu^+$

New gauge forces: a natural part of type I, ISS

- **Type I** : why seesaw scale so far below Planck scale:

- **Inverse seesaw case:**

- **Why**

$$\begin{pmatrix} 0 & hv_{wk} & 0 \\ hv_{wk} & 0 & M \\ 0 & M & \mu \end{pmatrix}$$

- **why not**

$$\begin{pmatrix} 0 & hv_{wk} & h'v_{wk} \\ hv_{wk} & M' & M \\ h'v_{wk} & M & \mu \end{pmatrix}$$

- **Local B-L** symmetry or **Left-Right** symmetry guarantees this !!

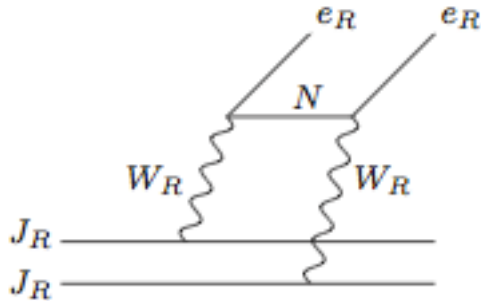
- New affects from $W_{R,N}$ and new seesaw Higgs $\Delta_{L,R}$

- **CMS:** $M_{WR} > 2.9 \text{ TeV}$

TeV W_R manifesting in $\beta\beta_{0\nu}$

$\beta\beta_{0\nu}$ search will have deep impact on left-right seesaw

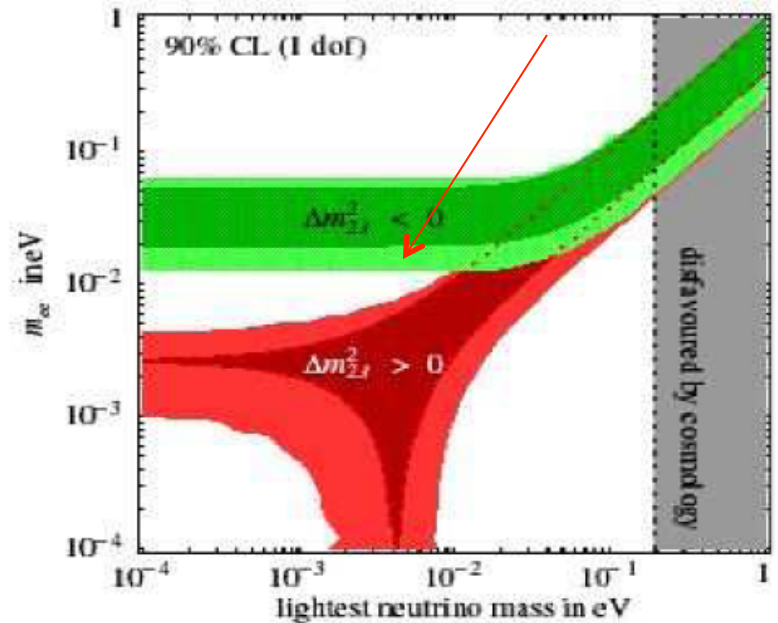
W_R contributes to :



Suppose long baseline $\rightarrow \Delta m_{31}^2 > 0$

and nonzero signal for $\beta\beta_{0\nu}$

\rightarrow could be due to few TeV W_R



$$|(M_N)_{ee}| \gtrsim 10 \text{ GeV} \times \left(\frac{3.5 \text{ TeV}}{M_{W_R}} \right)^4$$

LFV in left-right seesaw

- W_R, N contribution to CLFV for generic seesaw from in LRSM (Riazuddin, Marshak, RNM'81; Cirigliano, Kurylov, Musolf, Vogel'04)

$$B(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left(\frac{m_{W_L}^2}{m_{W_R}^2} \right)^4 \left(\sin\theta' \cos\theta' \frac{m_{N_2}^2 - m_{N_1}^2}{m_{W_L}^2} \right)^2 < 10^{-14}$$

$M_{N_1} \ll M_{N_2} = 400 \text{ GeV}$

- $B(\mu^- \rightarrow e^-) = 10^{-6} \epsilon^2 \sin^2\theta' \cos^2\theta' < 10^{-12}$
($M_2 = 100 \text{ GeV}$)

$$\epsilon = \frac{m_2^2 - m_1^2}{\sin^2\theta_W m_{W_L}^2} \left(\frac{m_{W_L}^2}{m_{W_R}^2} \right)^2 \left(\ln \frac{m_{W_R}^2}{M^2} - 2 \right)$$

→ Can probe W_R and M_N to 10-40 TeV scale !!

New Higgs in LR seesaw and their effects

(i) Extra Higgs doublet: M_H in multi-TeV range.

(ii) Triplet Higgs:

$$\Delta = \begin{pmatrix} \delta^+ / \sqrt{2} & \delta^{++} \\ \delta^0 & -\delta^+ / \sqrt{2} \end{pmatrix}_{L,R}$$

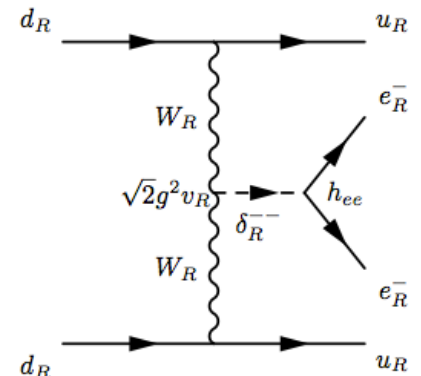
can be light

Spectacular collider signature $\delta^{++} \rightarrow \ell^+ \ell^+$ CMS, ATLAS
 $\sim 200 \text{ GeV}$

δ^{++} in $\beta\beta_{0\nu}$ decay: (RNM, Vergados'81; piccioto, Zahir'82; INemesvek, Nesti, Senjanovic, Tello, Vissani'12; Goswami et al;12; Awasthi, Parida, Patra'12; Barr, Dedeichann'12)

$$\frac{M_N}{M_{\delta^{++}}^2} \leq 10^{-2} \text{ GeV}^{-1}$$

(for $M_{W_R} = 3 \text{ TeV}$)



LR seesaw Higgs and CLFV

(V. Tello, Nemevsek, Nesti, Senjanovic, Vissani'12; Cirigliano, Kurylov, Ramsey-Musolf, Vogel'04)

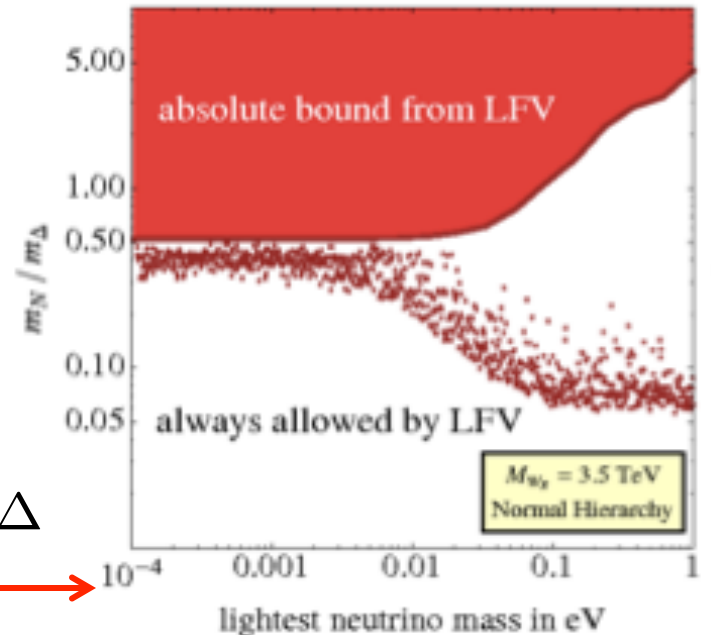
Loops involving δ^{++} and δ^+

$\rightarrow \mu \rightarrow e | Au, \mu \rightarrow e \gamma$

$$B(\mu Au \rightarrow e Au) \simeq 5 \times 10^{-10} \left(\frac{3.5 \text{ TeV}}{M_{WR}} \right)^4 \left| \frac{M_N M_N^*}{m_{\Delta^{++}}^2} \right|_{e\mu}^2$$

Bounds the mass ratio: M_N / M_{Δ}

(Tello,..)



Muonium-anti-muonium osc.

Unique signature

$$G_{M-\bar{M}} \sim \frac{f_{ee} f_{\mu\mu}}{8M_{\Delta^{++}}^2}$$

PSI Limit : $\leq 3G_F 10^{-3}$

BEYOND LEFT-RIGHT : QUARK-LEPTON UNIF.

If Q-L unified at the seesaw scale, a model is

$$SU(2)_L \times SU(2)_R \times SU(4)_c \begin{pmatrix} u & u & u & \nu \\ d & d & d & e \end{pmatrix}_{L,R}$$

→ SU(4) generalization of the seesaw Higgs field Δ_R has partners Δ_{qq} connecting to quarks:

→ leads to neutron-anti-neutron

oscillation: (Mohapatra, Marshak'80)

→ No proton decay.

-Example of nu mass-NNbar connection



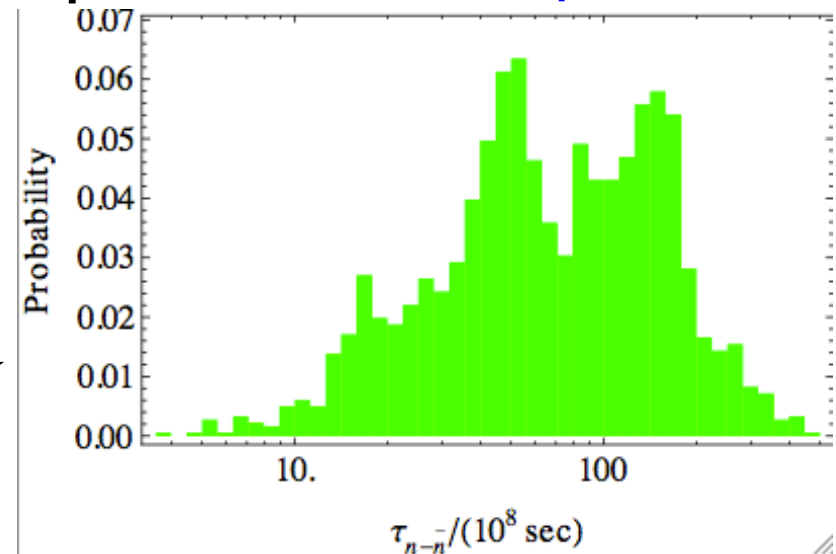
$$\frac{\lambda f^3 v_{BL}}{M_{\Delta}^6}$$

↓

observable for TeV sextets

Baryogenesis constraints

- If $N\bar{N}$ is observable, it will erase all pre-existing baryon asymmetry: need to generate baryons below weak scale:
- Baryogenesis via higher dim operators: **Post-sphaleron baryogenesis**: (Babu, Nasri, RNM'07)
- upper bound on $N\bar{N}$ transition time $< 5 \times 10^{10}$ sec.
(Babu, Dev, Fortes, RNM'arXiv:1303.6918) ★
- Predicts \sim TeV color sextet fields for LHC.



Type II seesaw

- New particles are SM non-singlets:

- **Type II**: $\Delta = \begin{pmatrix} \delta^+/\sqrt{2} & \delta^{++} \\ \delta^0 & -\delta^+/\sqrt{2} \end{pmatrix}$. couples to leptons $f_\nu L L \Delta$

$$m_\nu = f_\nu \frac{\mu_\Delta v_w^2}{M_\Delta^2}$$

- \rightarrow sub-TeV $\vec{\Delta} \rightarrow f_\nu \mu_\Delta \leq 10^{-9}$

- Collider searches directly probe neutrino mass matrix.

- 4-lepton signal $l^+ l^+ l^- l^-$ (Han, Perez, Huang, Li, Wang; Ruiz talk)

Recent interest from Higgs observation

- SM+ 125 GeV Higgs in SM \rightarrow vacuum unstable below Planck scale !
- Presence of the triplet alleviates this problem.
- It also adds new contribution to $\Gamma(h \rightarrow \gamma\gamma)$ and be of help to Higgs that way (unlike minimal type I)
e.g 10% enhancement $\rightarrow M_{\Delta^{++}} \leq 450 \text{ GeV}$ ★
- Current limits: 198 GeV range (CMS)_(mostly $\tau\tau$) ;
265 GeV (ATLAS)_(33% $\mu\mu$)
(Dev, Ghosh, Okada, Saha, arXiv:1301.3453; many earlier papers Melfo et al; Ahreib et al.)

LFV constraints on Type II

$\mu \rightarrow 3e$ Constraints

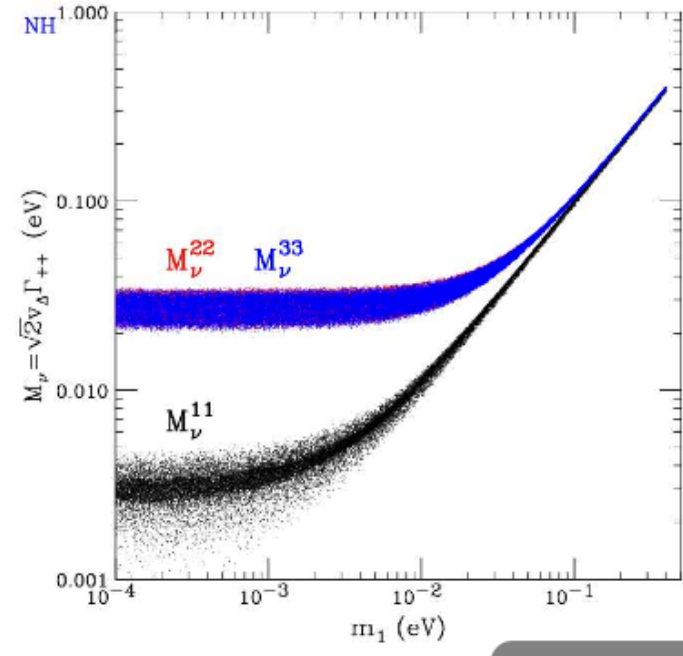
(Han, Perez, Huang, Li, Wang'08)

$$v_{\Delta}^2 > 0.2 \times 10^5 |M_{\nu}^{11} M_{\nu}^{12}| \times \left(\frac{1 \text{ TeV}}{M_{\Delta}} \right)^2$$

v_{Δ}^2 scales like \sqrt{Br}

Muonium-anti-muonium osc: ($M_{\delta} = 450 \text{ GeV}$; $v_{\Delta} = eV$)

$$G_{M-\bar{M}} = 4G_F 10^{-6} \star (\text{unique to type II and LR})$$



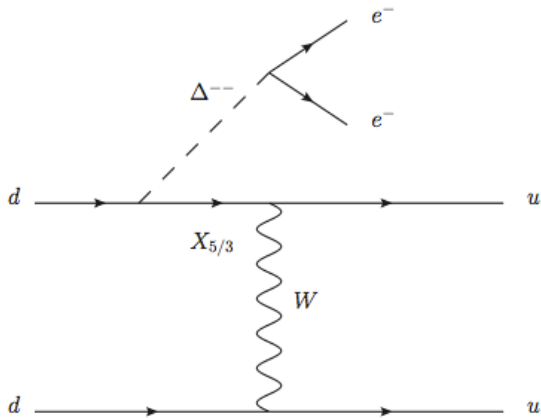
Natural type II and 5/3 charge quarks

- Add vectorlike quark doublet: $Q' = \begin{pmatrix} X_{5/3} \\ t' \end{pmatrix}$

(Franceschini, RNM'13)

- Makes μ_{Δ} naturally small:

- New contributions to $\beta\beta_{0\nu}$



- Limits $f_{Xd} \delta f_{ee} \theta_{Xu} \leq 10^{-4}$

Collider signals:

$X \rightarrow \ell^+ \ell^+ + (b, s, d)$

Current search with

$X \rightarrow t + W^+$

CMS limit: $M_X \geq 645 \text{ GeV}$

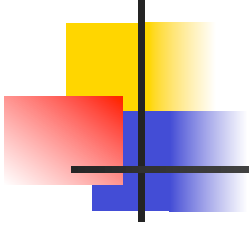
This model: $M_X \geq \text{TeV}$

from searches for Δ^{++}



Conclusion:

- **Seesaw:** Compelling big picture for nu masses;
- Low energy CLFV expts can probe TeV scale left-right seesaw : M_{WR} to 10- 20 TeV; LHC <6 TeV.
- Observation of normal Hierarchy for nu's and $\beta\beta_{0\nu}$ could indicate low scale WR.
- TeV seesaw+ Q-L unification \rightarrow observable $n\bar{n}$ osc.
- $M - \bar{M}$ and collider $\ell^+ \ell^+$ unique to LR and type II



Extra slides

Future Sensitivities

Experiment

No.	Observable	Upper Limit	Future Sensitivity
1.	$B(\mu \rightarrow e\gamma)$	2.4×10^{-12} [1]	$1 - 2 \times 10^{-13}$ [6], 10^{-14} [6]
2.	$B(\mu \rightarrow eee)$	10^{-12} [2]	10^{-16} [8], 10^{-17} [7]
3.	$R_{\mu e}^{\text{Ti}}$	4.3×10^{-12} [3],	$3 - 7 \times 10^{-17}$ [10, 9], 10^{-18} [11, 7]
4.	$R_{\mu e}^{\text{Au}}$	7×10^{-13} [4]	$3 - 7 \times 10^{-17}$ [10, 9], 10^{-18} [11, 7]
5.	$B(\tau \rightarrow e\gamma)$	3.3×10^{-8} [5]	$1 - 2 \times 10^{-9}$ [13, 12]
6.	$B(\tau \rightarrow \mu\gamma)$	4.4×10^{-8} [5]	2×10^{-9} [13, 12]
7.	$B(\tau \rightarrow eee)$	2.7×10^{-8} [5]	2×10^{-10} [13, 12]
8.	$B(\tau \rightarrow e\mu\mu)$	2.7×10^{-8} [5]	10^{-10} [12]
9.	$B(\tau \rightarrow \mu\mu\mu)$	2.1×10^{-8} [5]	2×10^{-10} [13, 12]
10.	$B(\tau \rightarrow \mu ee)$	1.8×10^{-8} [5]	10^{-10} [12]

Table 1: Current upper limits and future sensitivities of CLFV observables under study.

Left-right seesaw at LHC

■ WR and Z' : $u\bar{d} \rightarrow W_R \rightarrow l^+ N$ $u\bar{u} \rightarrow Z' \rightarrow NN$

(Keung, Senjanovic; Han, Perez, Huang, Li, Wang; Del Aguila, Aguilar-Saavedra; de Blas, Azuelos, Nersti, Nemevsek,...)

■ **type I** : W_R production source of new signal:

$$pp \rightarrow l^\pm l^\pm jj + X$$

(ATLAS, CMS bounds)

■ **Inv. Seesaw**

$$\mathcal{E} > 10^{-3}$$

$$N \rightarrow l^- jj, l^- l^+ \nu$$

$$pp \rightarrow lll \nu + X$$

LHC reach < 4 TeV

(Dev, Chen'11)

(Ruiz's talk)

TeV seesaw in Colliders:

New particles and decays

- RH neutrino N : $\left\{ \begin{array}{l} \text{Dirac (Inverse)} \quad N \rightarrow l^- W^+ \rightarrow l^- l^+ \nu \\ \text{Majorana (Type I)} \quad N \rightarrow l^\pm W^\mp \rightarrow l^\pm jj \end{array} \right.$
via $\theta_{\nu N} \equiv \varepsilon$
Higgs decay: $h \rightarrow N \nu$

- Scalar triplet (Type II) $\Delta = \begin{pmatrix} \delta^+/\sqrt{2} & \delta^{++} \\ \delta^0 & -\delta^+/\sqrt{2} \end{pmatrix}$ $\delta^{++} \rightarrow l^+ l^+, W^+ W^+$
 $\delta^+ \rightarrow l^+ \bar{\nu}, W^+ Z$

- Fermion triplet: (Type III) $\Sigma = \begin{pmatrix} \Sigma^0/\sqrt{2} & \Sigma^+ \\ \Sigma^- & -\Sigma^0/\sqrt{2} \end{pmatrix}$ $\Sigma^0 \rightarrow l^+ W^-$
 $\Sigma^+ \rightarrow l^+ Z, \dots$