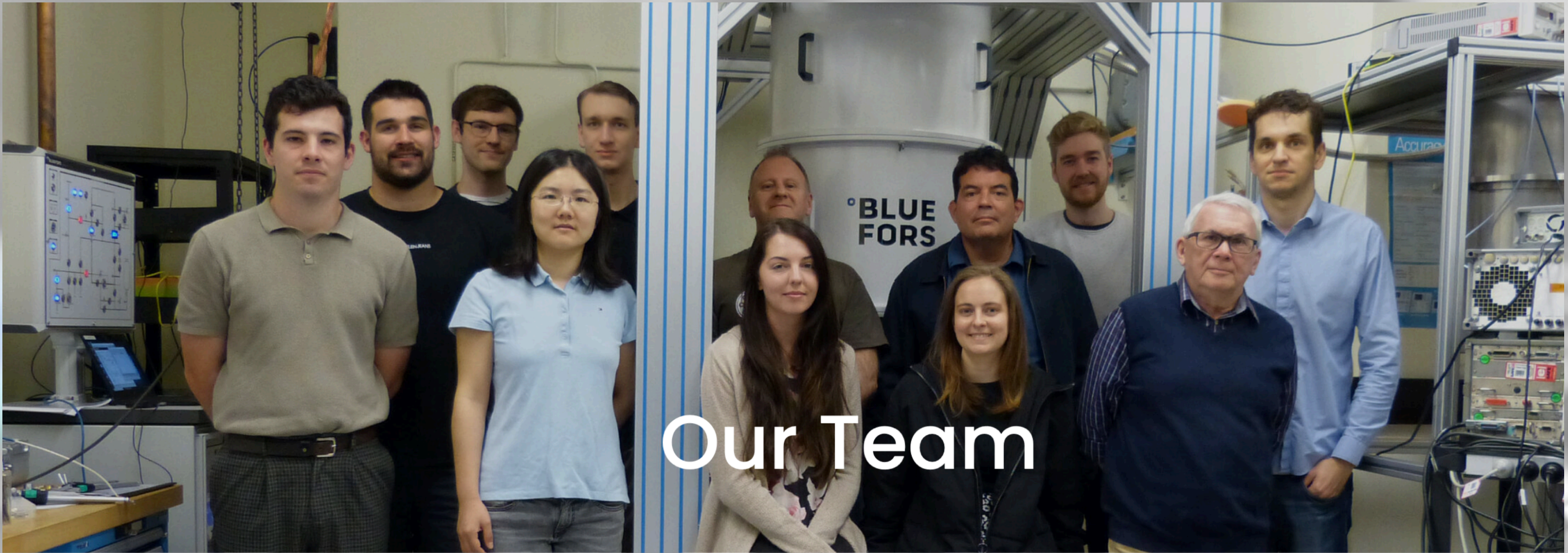


Dark Wave Workshop



Our Team

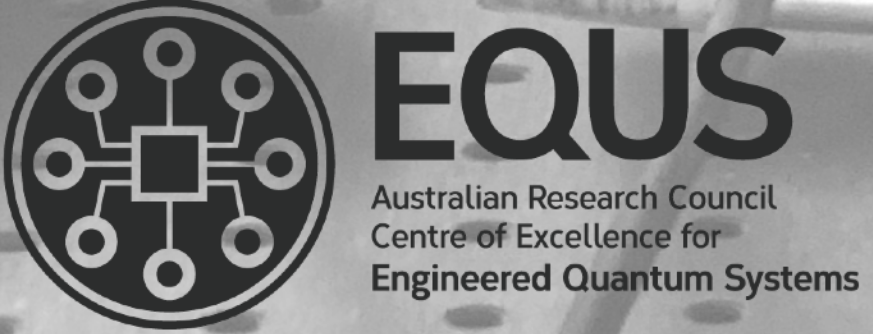
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Graeme Flower
William Campbell

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Aaron Quiskamp
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Steven Samuels
Emma Paterson
Robert Crew

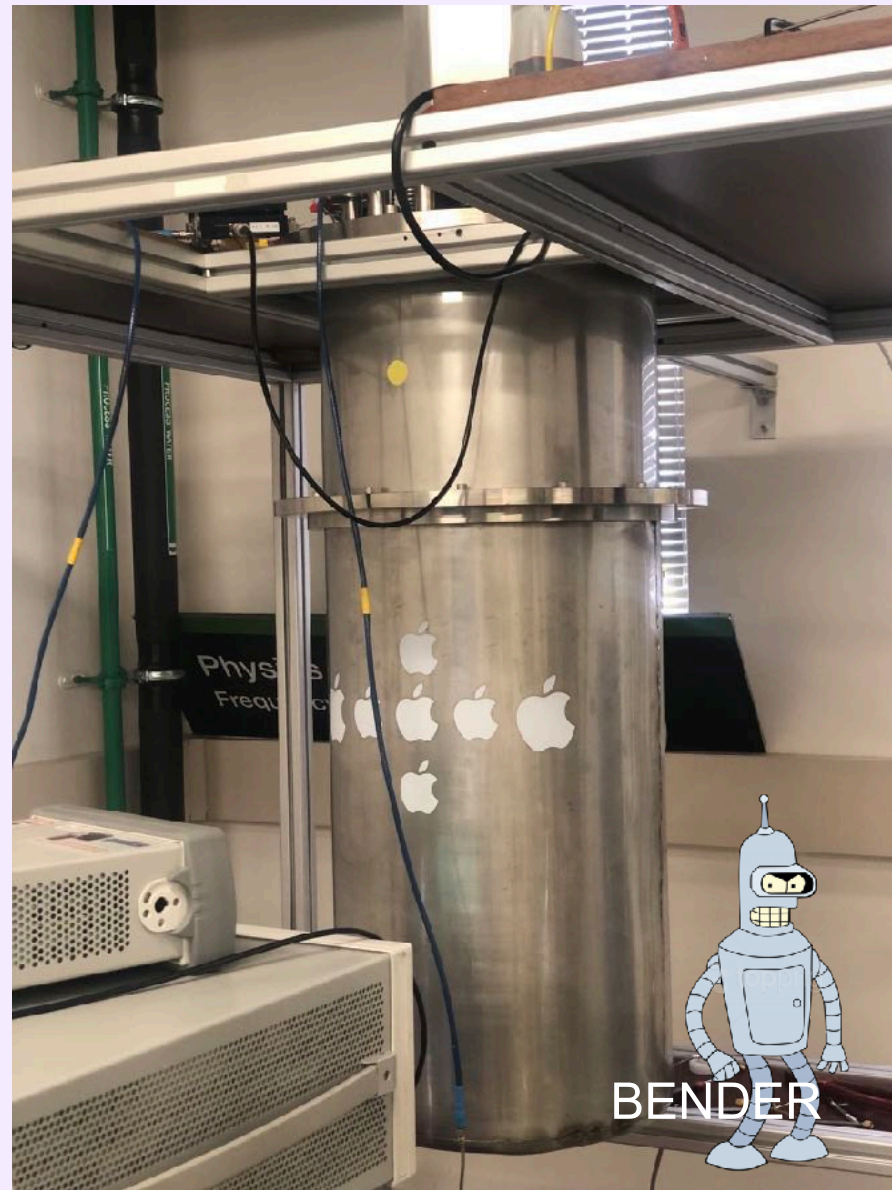
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Michael Hatzon (Hons)
Emily Waterman (Hons)
Ashley Johnson (MSc)

Quantum Technologies and Dark Matter Laboratory QDM-Lab

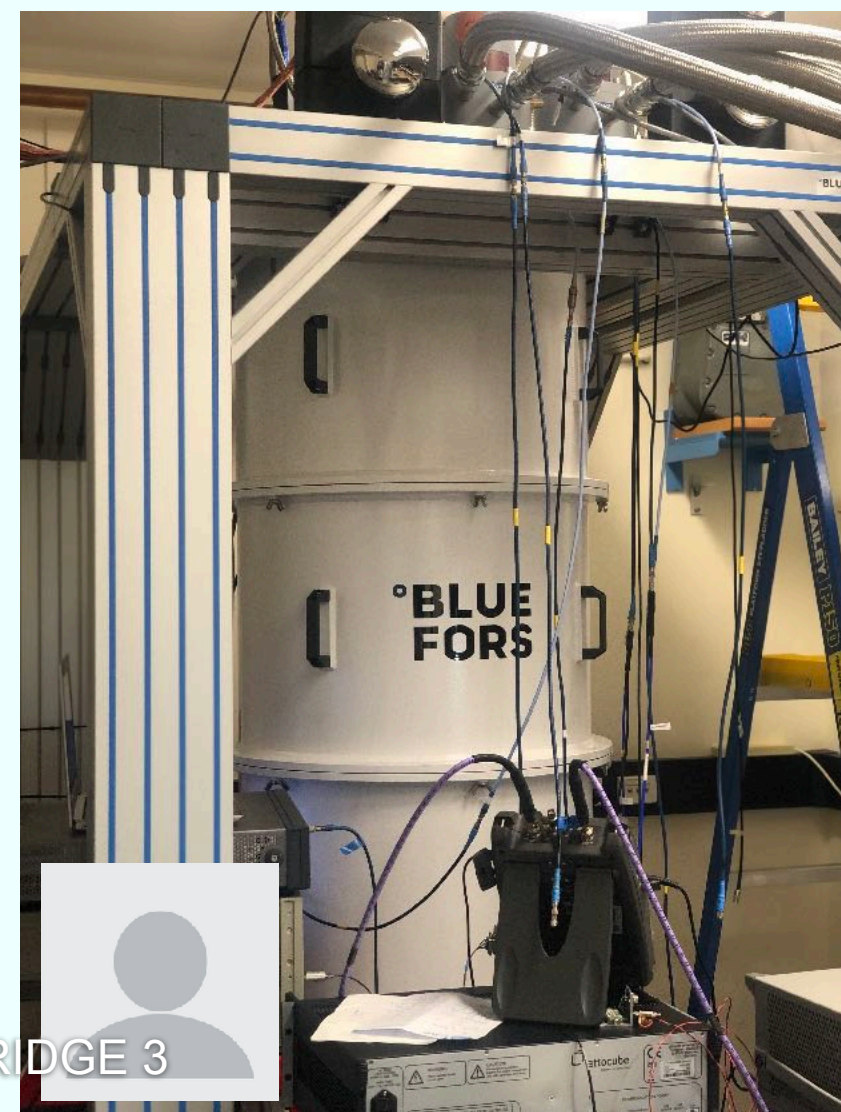
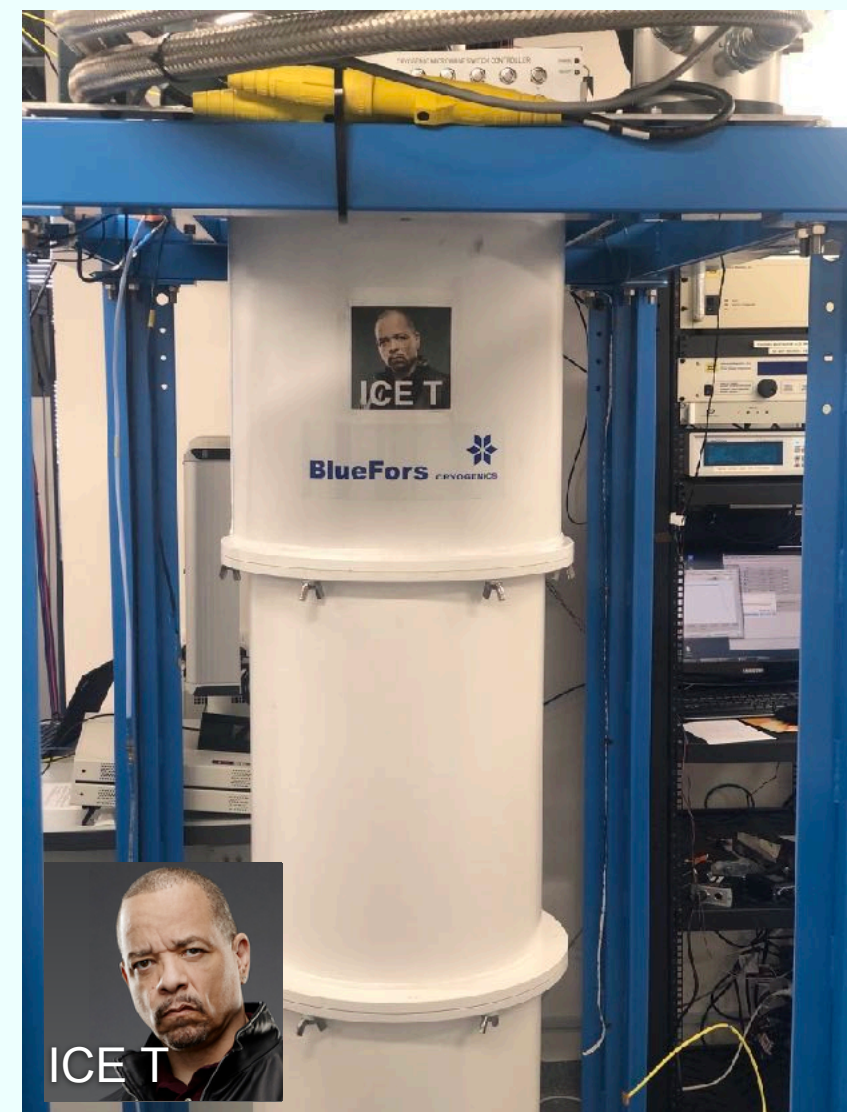


THE UNIVERSITY OF
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AUSTRALIA

4 Kelvin Systems



- Extensive experience with cryogenic systems
- 3, 7 and 12 T superconducting magnets
- Large collection of microwave (and a some optical) diagnostic equipment and hardware
- Expertise with precision frequency metrology



Dilution Systems

STATUS AND PLANS

STATUS AND PLANS

CURRENT AXION DM PROGRAMS

ORGAN

UPLOAD

ADMX

Collaboration

STATUS AND PLANS

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TWISTED ANYON

AXION-MONOPOLE
COUPLINGS

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BULK ACOUSTIC WAVE:
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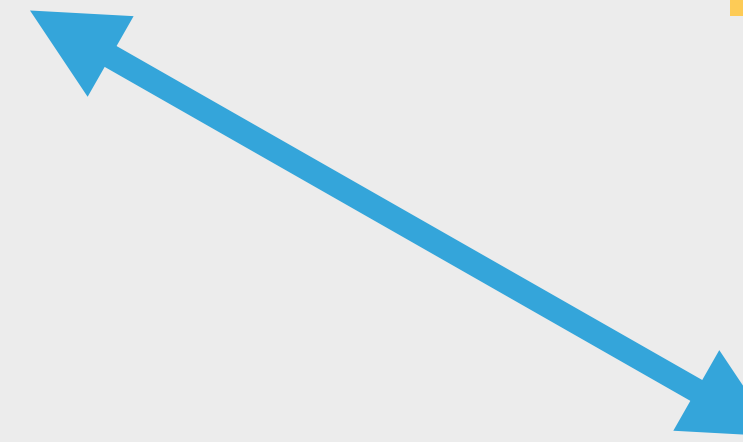
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TECHNIQUES



ORGAN

PHYSICAL REVIEW LETTERS **132**, 031601 (2024)

Exclusion of Axionlike-Particle Cogenesis Dark Matter in a Mass Window above 100 μeV

Aaron Quiskamp^{1,*}, Ben T. McAllister^{1,2,†}, Paul Altin³, Eugene N. Ivanov¹, Maxim Goryachev¹, and Michael E. Tobar^{1,‡}

¹Quantum Technologies and Dark Matter Laboratory, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley, Western Australia 6009, Australia

²ARC Centre of Excellence for Dark Matter Particle Physics, Swinburne University of Technology, John Street, Hawthorn, Victoria 3122, Australia

³ARC Centre of Excellence For Engineered Quantum Systems, The Australian National University, Canberra, Australian Capital Territory 2600, Australia

(Received 3 October 2023; accepted 28 November 2023; published 16 January 2024)

RECENT PUBLICATIONS

RESEARCH ARTICLE

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Limits on Dark Photons, Scalars, and Axion-Electromagnetodynamics with the ORGAN Experiment

Ben T. McAllister,^{*} Aaron Quiskamp, Ciaran A. J. O'Hare, Paul Altin, Eugene N. Ivanov, Maxim Goryachev, and Michael E. Tobar

UPLOAD

PHYSICAL REVIEW D **107**, 112003 (2023)

Searching for low-mass axions using resonant upconversion

Catriona A. Thomson^{1,*}, Maxim Goryachev¹, Ben T. McAllister^{1,2}, Eugene N. Ivanov¹, Paul Altin³, and Michael E. Tobar^{1,‡}

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³ARC Centre of Excellence For Engineered Quantum Systems, The Australian National University, Canberra, Australian Capital Territory 2600 Australia

ANYON

PHYSICAL REVIEW D **108**, 052014 (2023)

Searching for ultralight axions with twisted cavity resonators of anyon rotational symmetry with bulk modes of nonzero helicity

J. F. Bourhill, E. C. I. Paterson¹, M. Goryachev, and M. E. Tobar²

Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia, 35 Stirling Highway, 6009 Crawley, Western Australia

Direct search for dark matter axions excluding ALP cogenesis in the 63- to 67- μeV range with the ORGAN experiment

Aaron Quiskamp^{1,*}, Ben T. McAllister^{1,2,*}, Paul Altin³, Eugene N. Ivanov¹, Maxim Goryachev¹, Michael E. Tobar^{1,*}

Scalar Field Dark Matter

PHYSICAL REVIEW D **106**, 055037 (2022)

Searching for scalar field dark matter using cavity resonators and capacitors

V. V. Flambaum^{1,*}, B. T. McAllister^{2,3,†}, I. B. Samsonov^{1,‡}, and M. E. Tobar^{2,§}

DETECTOR COMPARISON: Defining Instrument Sensitivity independent of signal (Spectral)

symmetry

MDPI

Article

Comparing Instrument Spectral Sensitivity of Dissimilar Electromagnetic Haloscopes to Axion Dark Matter and High Frequency Gravitational Waves

Michael E. Tobar^{*}, Catriona A. Thomson, William M. Campbell, Aaron Quiskamp, Jeremy F. Bourhill, Benjamin T. McAllister, Eugene N. Ivanov and Maxim Goryachev

Axions with Magnetic Charge

PHYSICAL REVIEW D **108**, 035024 (2023)

Searching for GUT-scale QCD axions and monopoles with a high-voltage capacitor

Michael E. Tobar^{1,*}, Anton V. Sokolov², Andreas Ringwald³, and Maxim Goryachev¹

¹Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley, Western Australia 6009, Australia

²Department of Mathematical Sciences, University of Liverpool, Liverpool, L69 7ZL, United Kingdom

³Deutsches Elektronen-Synchrotron DESY, Notkestraße 85, 22607 Hamburg, Germany

PHYSICAL REVIEW D **105**, 045009 (2022)

Poynting vector controversy in axion modified electrodynamics

Michael E. Tobar^{*}, Ben T. McAllister, and Maxim Goryachev

ARC Centre of Excellence for Engineered Quantum Systems and ARC Centre of Excellence for Dark Matter Particle Physics, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley, Western Australia 6009, Australia

(Received 9 September 2021; accepted 28 January 2022; published 15 February 2022)

PHYSICAL REVIEW D **106**, 109903(E) (2022)

Erratum: Poynting vector controversy in axion modified electrodynamics [Phys. Rev. D **105**, 045009 (2022)]

Axion ED Poynting Theorem: Standardised way of Calculating Sensitivity

If Magnetic Charge Can Exist at High Energy

-> Further Modifications to Axion Electrodynamics

-> Can test the existence of Magnetic Charge through Axions

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Generic Axion Maxwell Equations: Path Integral Approach

Anton V. Sokolov , Andreas Ringwald

First published: 11 October 2023 | <https://doi.org/10.1002/andp.202300112>

> hep-ph > arXiv:2205.02605

High Energy Physics – Phenomenology

[Submitted on 5 May 2022]

Electromagnetic Couplings of Axions

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Axion-photon coupling parameter space is expanded from one parameter to three

$$g_{a\gamma\gamma} \rightarrow (g_{a\gamma\gamma}, g_{aEM}, g_{aMM})$$



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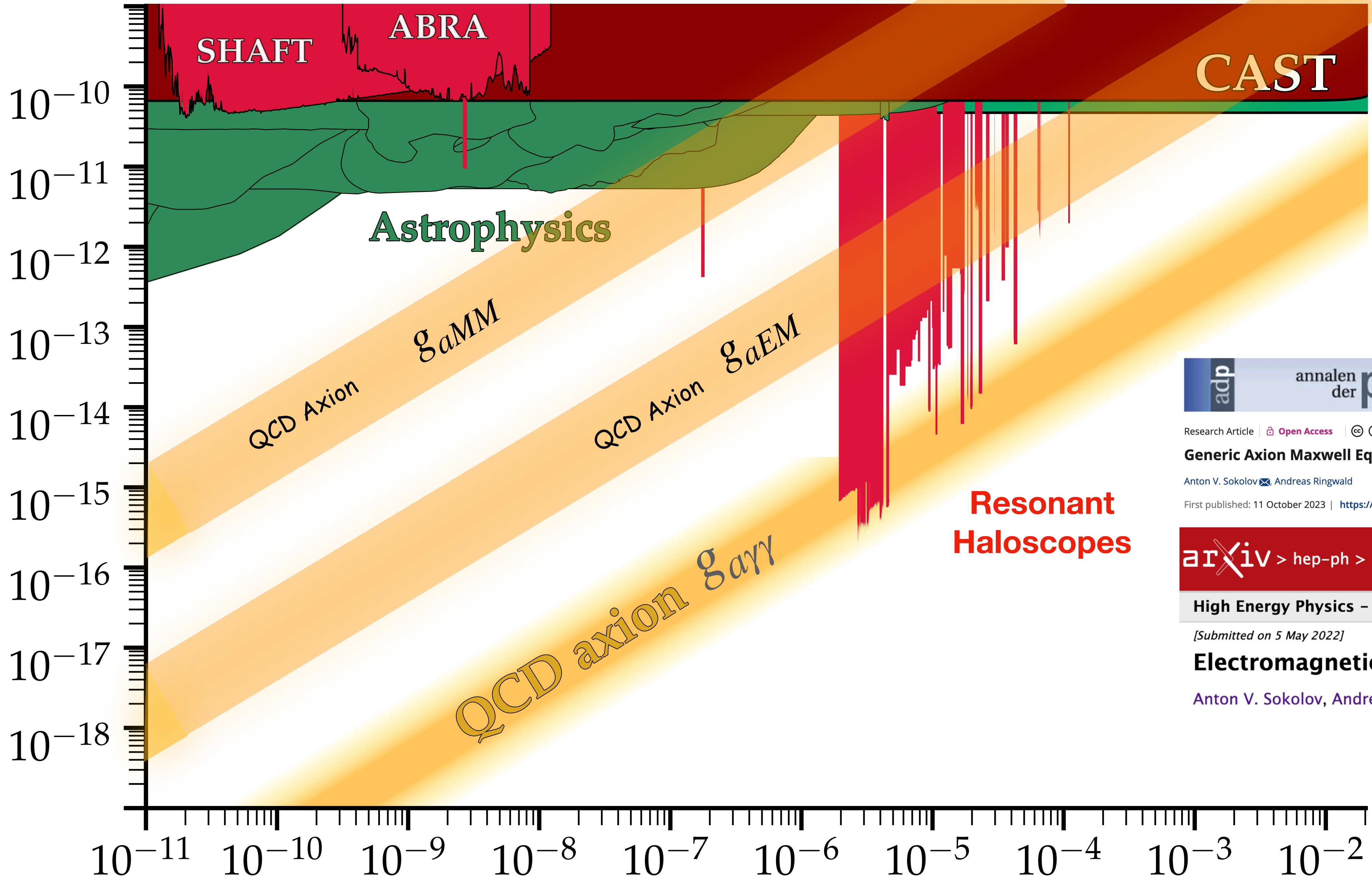
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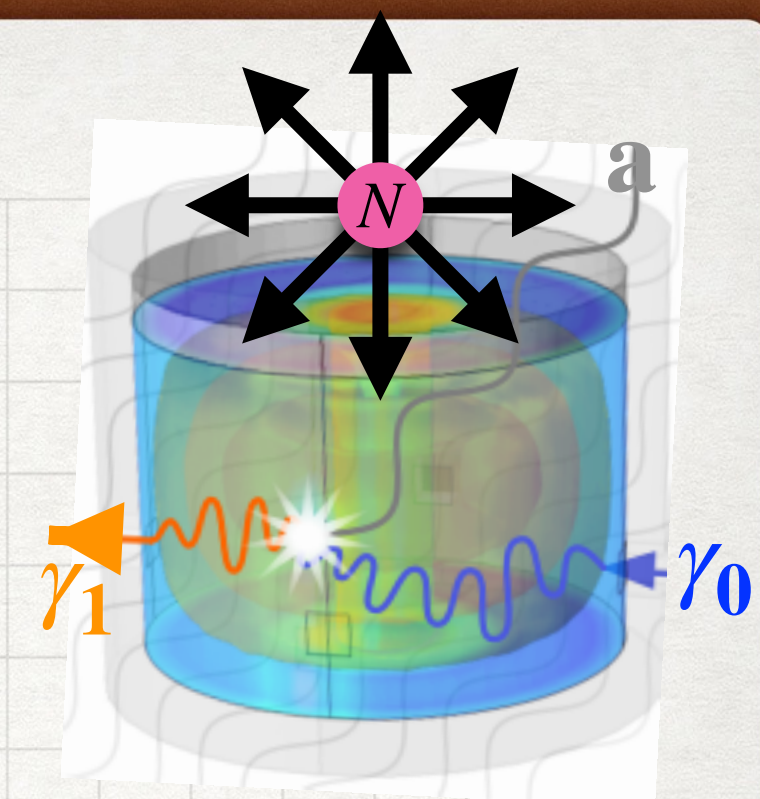
Axion-photon coupling [GeV^{-1}]



Axion mass [eV]

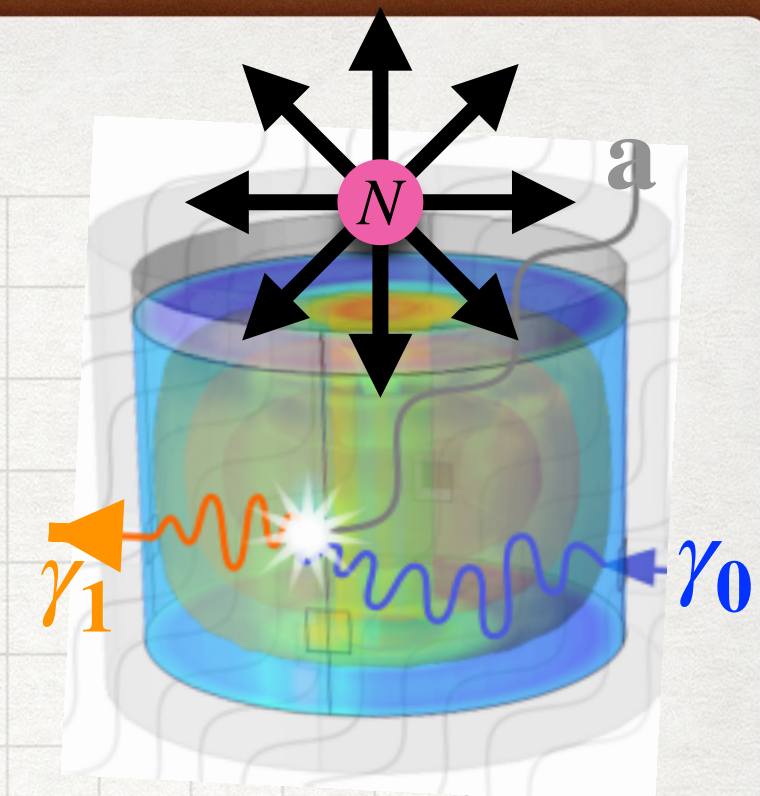
Form Factors for Resonators

- > Static and Time varying Background E + B Fields
- > Calculate from Real Part of Complex Poynting Theorem



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- > Static and Time varying Background E + B Fields
- > Calculate from Real Part of Complex Poynting Theorem



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Sensitivity of Resonant Axion Haloscopes to Quantum Electrodynamics

Michael E. Tobar,* Catriona A. Thomson, Benjamin T. McAllister, Maxim Goryachev,
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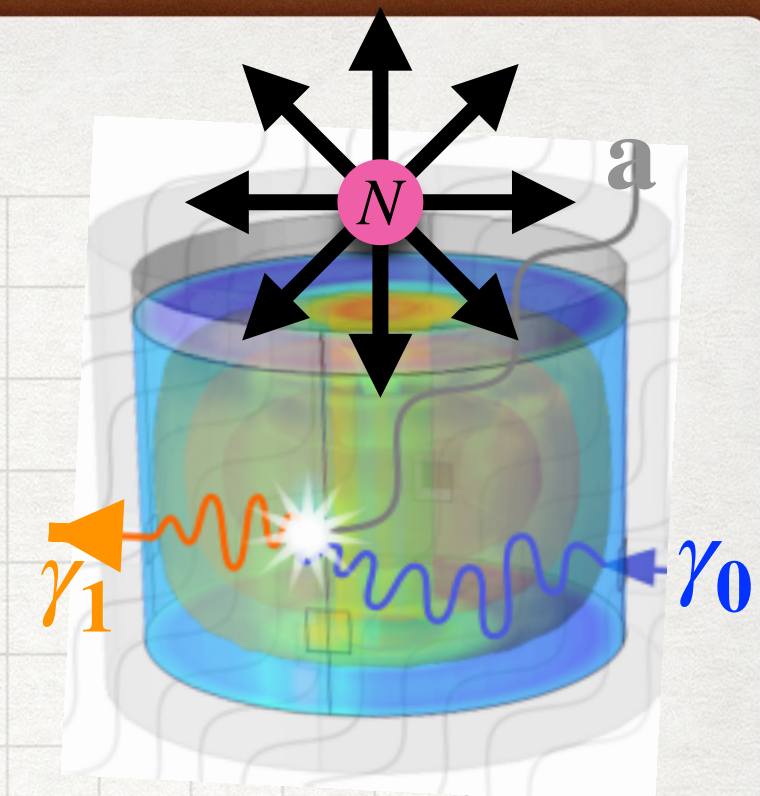
Form Factors

$$C_{1a\gamma\gamma} = \frac{(\int \vec{B}_0 \cdot \text{Re}(\mathbf{E}_1) dV)^2}{B_0^2 V_1 \int \mathbf{E}_1 \cdot \mathbf{E}_1^* dV} \quad C_{1EM} = \frac{(\int \vec{B}_0 \cdot \text{Re}(\mathbf{B}_1) dV)^2}{B_0^2 V_1 \int \mathbf{B}_1 \cdot \mathbf{B}_1^* dV}$$

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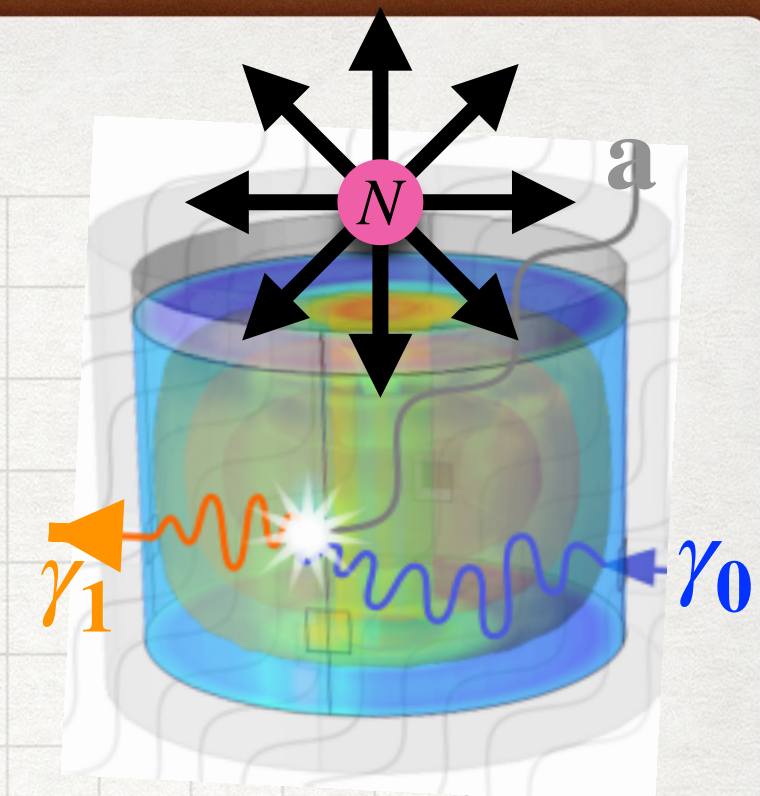
Limits on Dark Photons, Scalars, and Axion-Electromagnetodynamics with the ORGAN Experiment

Ben T. McAllister,* Aaron Quiskamp, Ciaran A. J. O'Hare, Paul Altin, Eugene N. Ivanov, Maxim Goryachev, and Michael E. Tobar

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PHYSICAL REVIEW D **107**, 112003 (2023)

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Searching for low-mass axions using resonant upconversion

Catriona A. Thomson^{1,*}, Maxim Goryachev,¹ Ben T. McAllister,^{1,2} Eugene N. Ivanov,¹ Paul Altin,³ and Michael E. Tobar^{1,†}

¹Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley, Western Australia 6009, Australia

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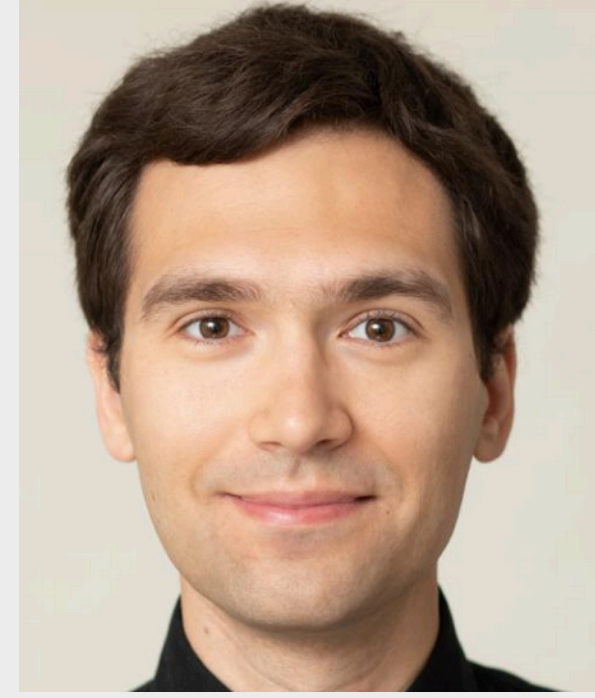
(Received 17 January 2023; accepted 5 May 2023; published 5 June 2023)

$g_{aEM} \rightarrow$ Suppressed

UPLOAD $\rightarrow g_{aMM}$

Reactive Experiment with Static Background Electric and Magnetic Field -> Imaginary Part of Complex Poynting Theorem

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PHYSICAL REVIEW D **108**, 035024 (2023)

arXiv:2306.13320 [hep-ph]

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Michael E. Tobar ^{1,*}, Anton V. Sokolov ², Andreas Ringwald ³ and Maxim Goryachev¹

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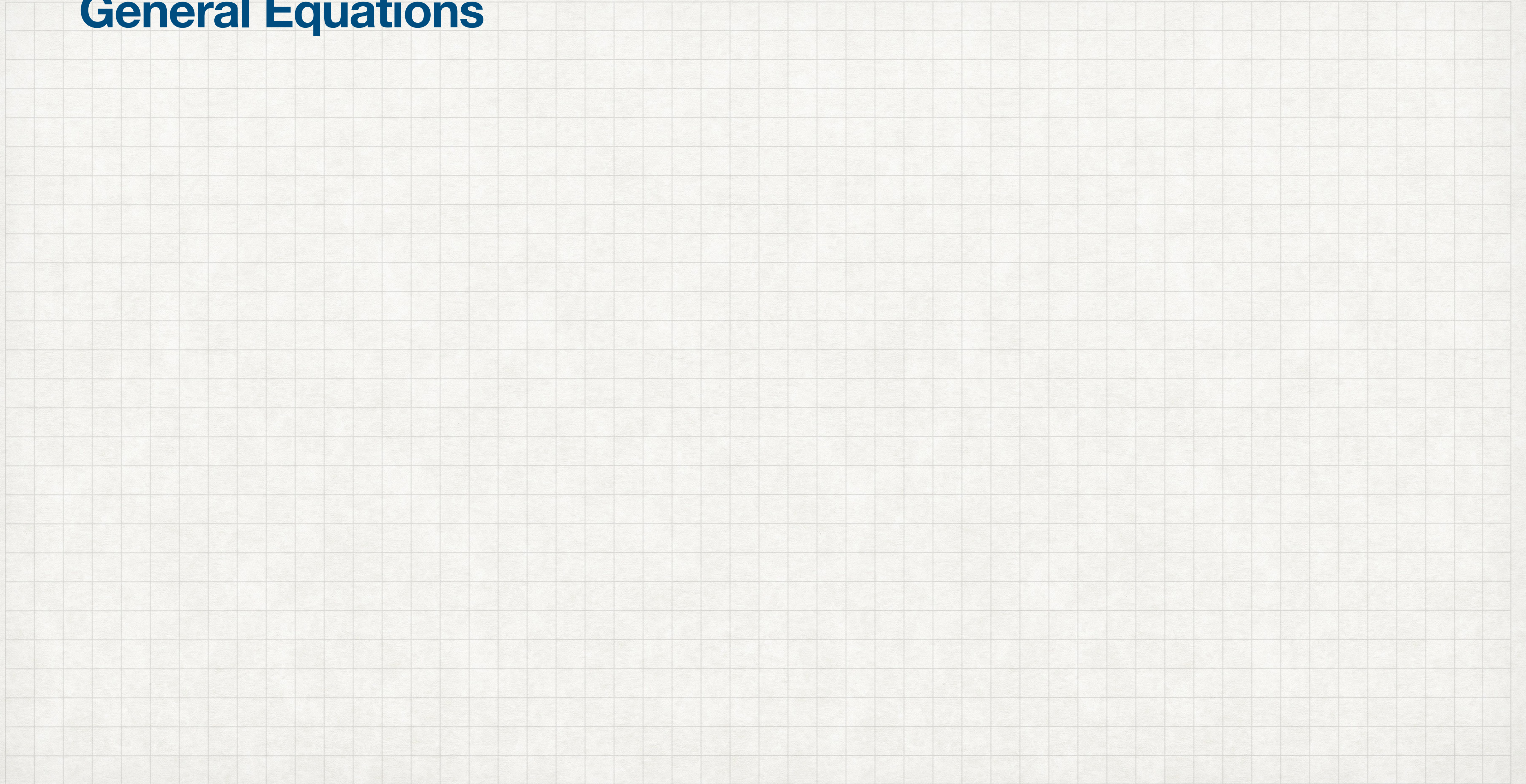
²*Department of Mathematical Sciences, University of Liverpool, Liverpool, L69 7ZL, United Kingdom*

³*Deutsches Elektronen-Synchrotron DESY, Notkestraße 85, 22607 Hamburg, Germany*



(Received 20 June 2023; accepted 2 August 2023; published 17 August 2023)

General Equations



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Background Electric Field $\vec{\nabla} a = 0$

$$\nabla \times \vec{E}_0 = 0 \quad \nabla \cdot \vec{E}_0 = \epsilon_0^{-1} \rho_{e0} \quad \vec{B}_0 = 0$$

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$$\vec{\nabla} \times \vec{E}_1 = -\partial_t \vec{B}_1 - \vec{J}_{ma1}.$$

General Equations

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Doing the Calculation This Way -> Can Hide Surface Effects

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Impressed Charges and Currents Create Fields, and these Surfaces do not go to infinity

$$\nabla a \cdot \vec{E}_0 = \nabla \cdot (a \vec{E}_0) - a(\nabla \cdot \vec{E}_0)$$

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The axion field is strongly repelled by electric charges due to the infinite potential barrier

Willy Fischler and John Preskill. DYON - AXION DYNAMICS. Phys. Lett. B, 125:165–170, 1983

Thus, one has $a=0$ at the locations of the charged particles, so $a(\nabla \cdot \vec{E}_0) = 0$,
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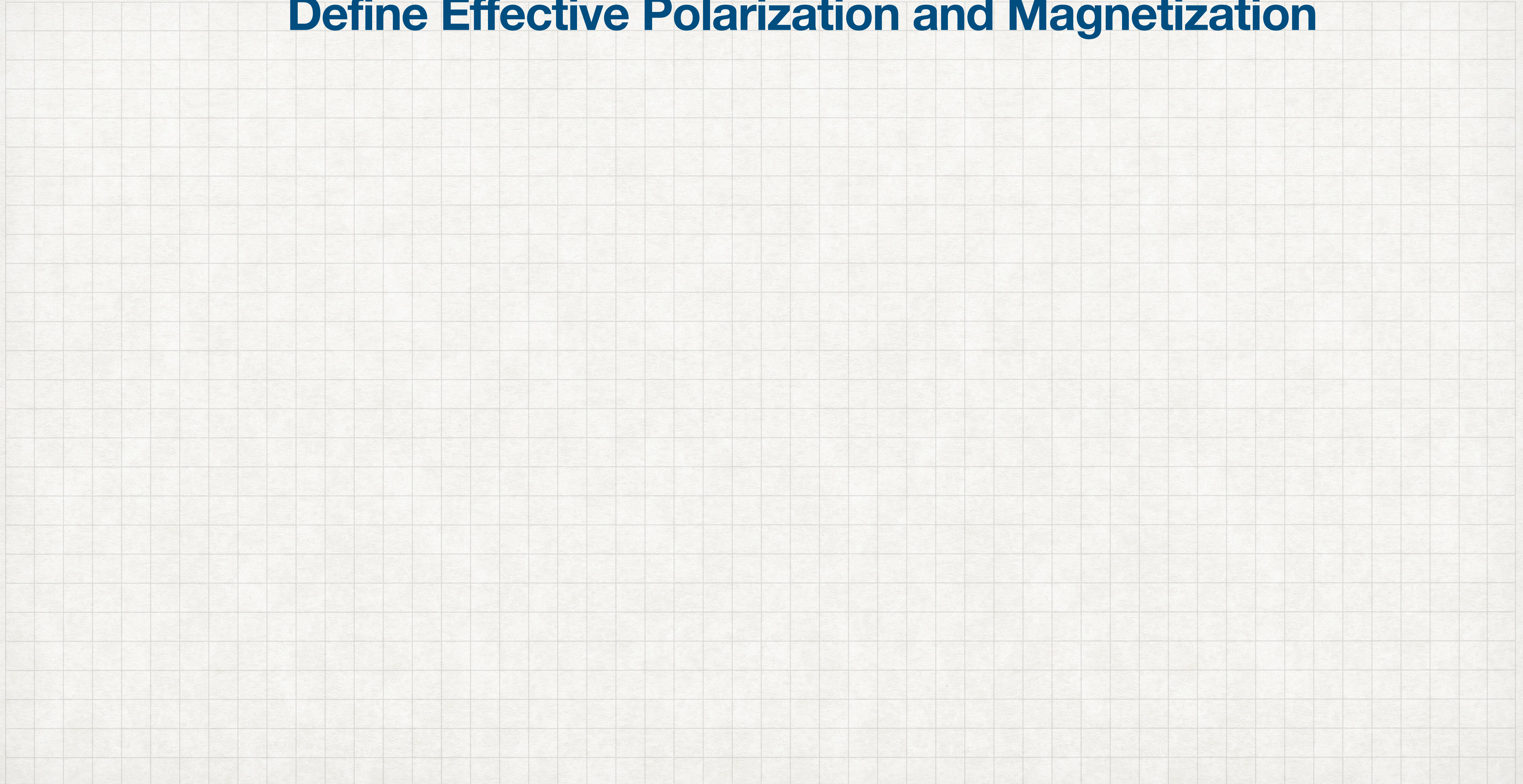
$$\vec{\nabla} \cdot \left(\vec{E}_1 + g_{aEM} a \vec{E}_0 \right) = \epsilon_0^{-1} \rho_{e1},$$

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$$\vec{\nabla} \cdot \left(\vec{B}_1 + \frac{g_{aMM} a \vec{E}_0}{c} \right) = 0,$$

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Define Effective Polarization and Magnetization



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$$\vec{\nabla} \cdot \vec{D}_1 = \rho_{e1}$$

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$$\vec{\nabla} \cdot \vec{H}_1 = 0$$

$$\vec{\nabla} \times \vec{E}_1 = -\mu_0 \partial_t \vec{H}_1$$

AC Capacitor: Apply Poynting Theorem: Sensitive to g_{aEM}

Vector Phasor Amplitudes

$$\oint \text{Im} (\mathbf{S}_1) \cdot \hat{n} ds = \omega_a \int \left(\left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV.$$

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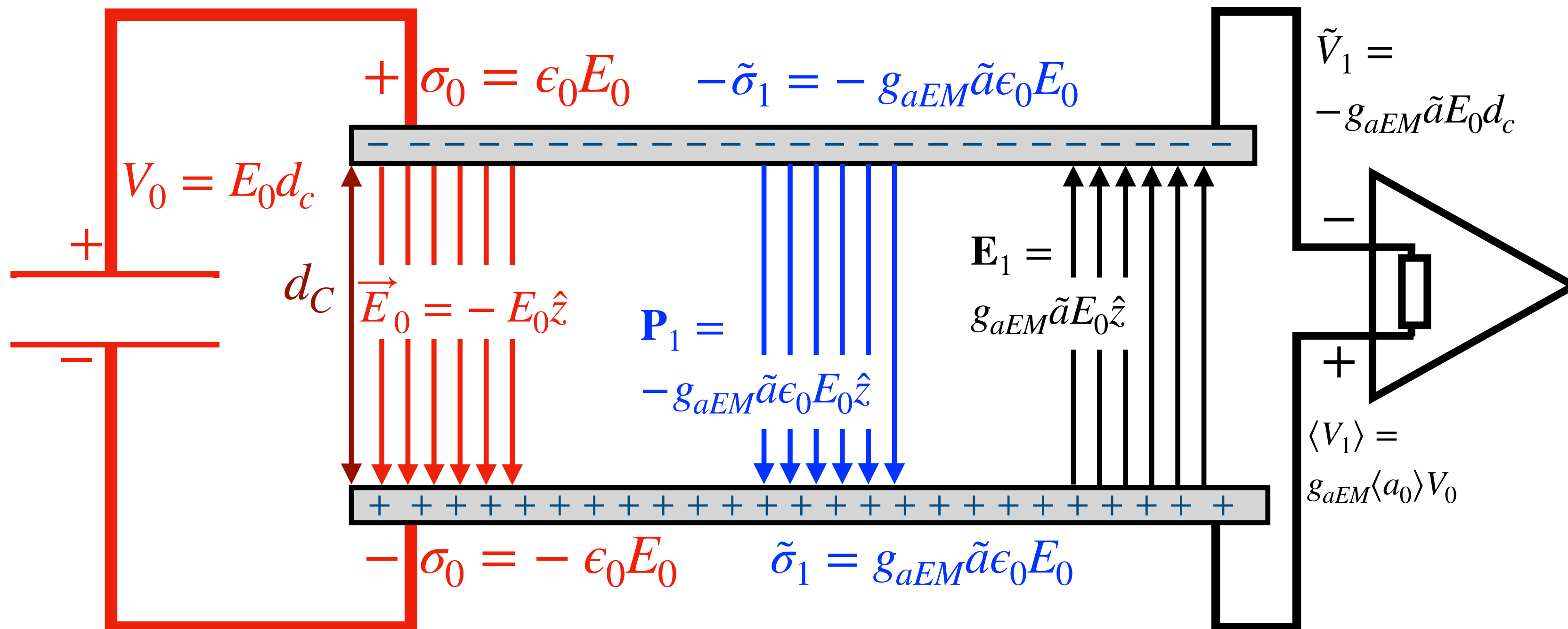
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Axion generated Electric Field



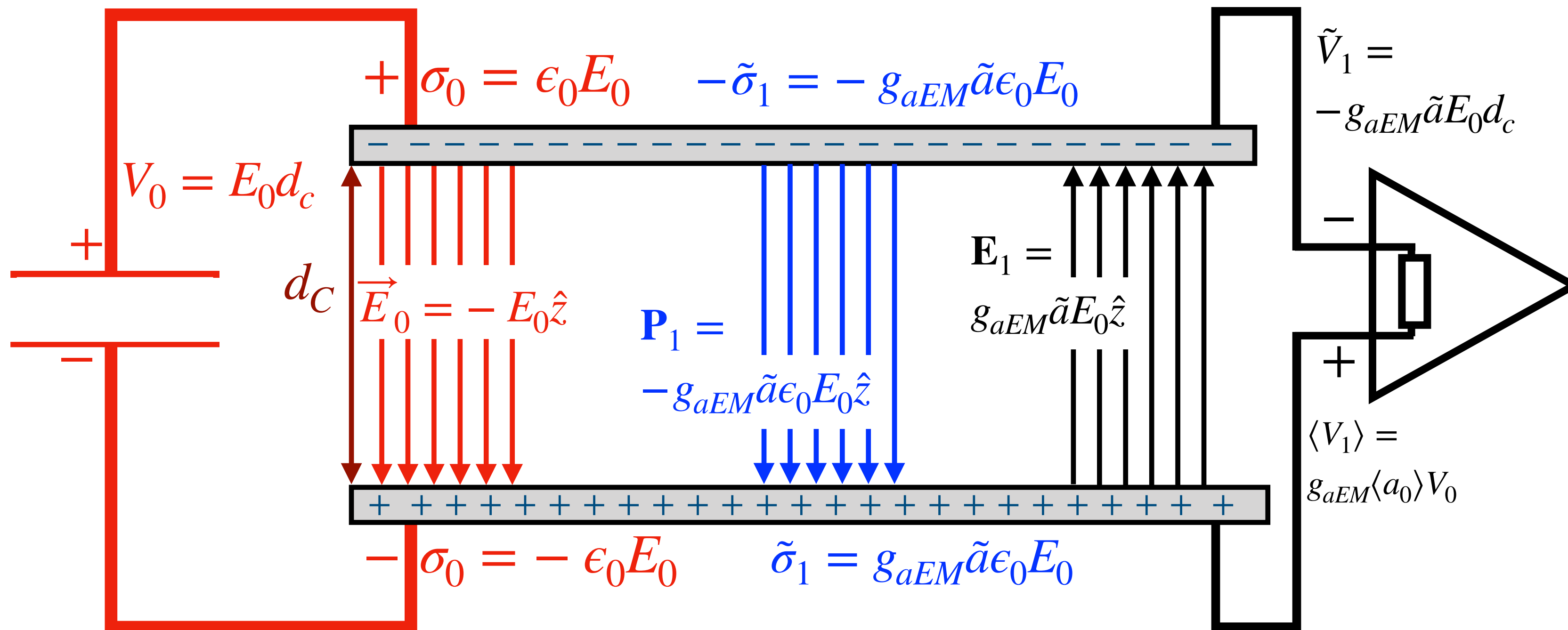
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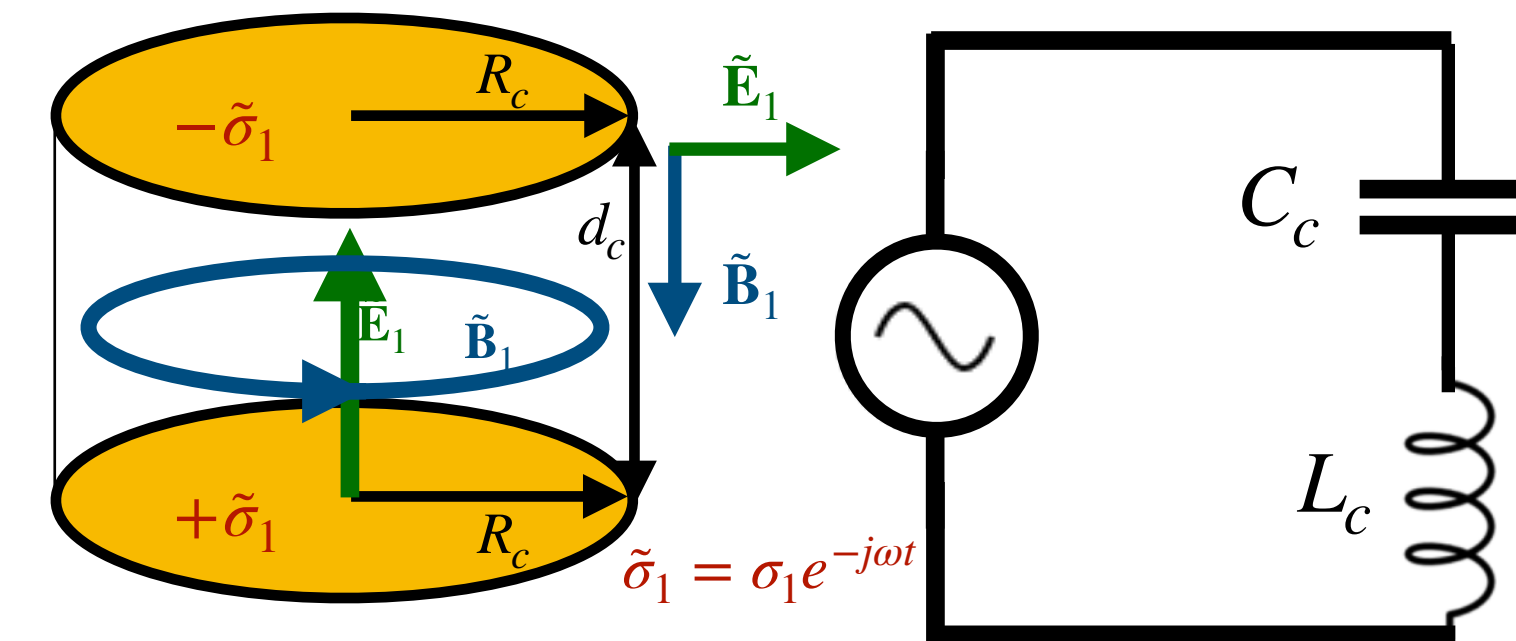
Axion generated Electric Field



Cylindrical // Plate Capacitor

$$\tilde{\mathbf{E}}_1 = \tilde{E}_{01} J_0 \left(\frac{\omega_1 r}{c} \right) e^{-j\omega_1 t \hat{z}}$$

$$\tilde{\mathbf{B}}_1 = -j \frac{\tilde{E}_{01}}{c} J_1 \left(\frac{\omega_1 r}{c} \right) e^{-j\omega_1 t \hat{\phi}} \quad \tilde{E}_{01} = \frac{\tilde{q}_1}{\pi R_c^2 \epsilon_0}$$



SCALAR DARK MATTER: ELECTROMAGNETIC TECHNIQUES

PHYSICAL REVIEW D **106**, 055037 (2022)

Searching for scalar field dark matter using cavity resonators and capacitors

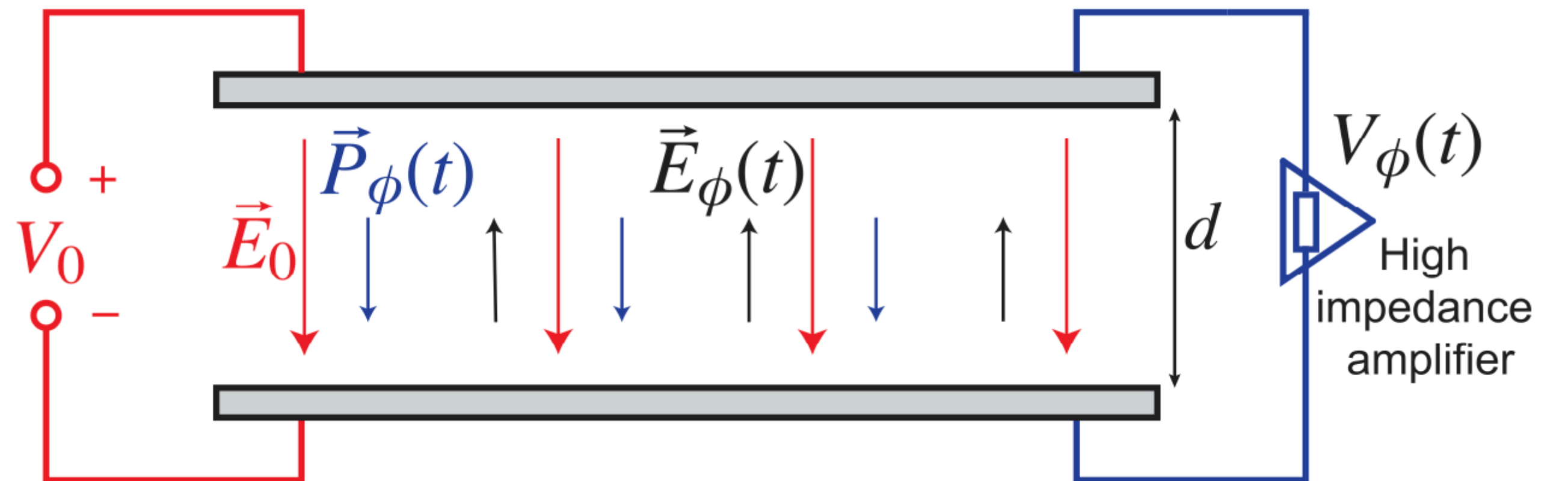
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¹*School of Physics, University of New South Wales, Sydney 2052, Australia*

²*ARC Centre of Excellence For Engineered Quantum Systems and ARC Centre of Excellence For Dark Matter Particle Physics, QDM Laboratory, Department of Physics, University of Western Australia, 35 Stirling Highway, Crawley WA 6009, Australia*

³*ARC Centre of Excellence for Dark Matter Particle Physics, Centre for Astrophysics and Supercomputing, Swinburne University of Technology, John St, Hawthorn VIC 3122, Australia*

$$g_{aEM} \equiv g_{\phi\gamma\gamma}$$



Axion Generated Magnetic Field-> Magnetic Circuit Readout Sensitive to g_{aMM}

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$$U_1 = \frac{\left(\frac{g_{aMM} a_0 \epsilon_0 c}{2} \int \mathbf{B}_1 \cdot \vec{E}_0 dV \right)^2}{\int \left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) dV}$$

Axion Generated Magnetic Field-> Magnetic Circuit Readout Sensitive to g_{aMM}

$$\frac{\oint \text{Im}(\mathbf{S}_1) \cdot \hat{n} ds}{\omega_a} = \int \left(\left(\frac{1}{2\mu_0} \mathbf{B}_1^* \cdot \mathbf{B}_1 - \frac{\epsilon_0}{2} \mathbf{E}_1 \cdot \mathbf{E}_1^* \right) - \frac{g_{aEM} a_0 \epsilon_0}{4} (\mathbf{E}_1 + \mathbf{E}_1^*) \cdot \vec{E}_0 + \frac{g_{aMM} a_0 \epsilon_0 c}{4} (\mathbf{B}_1 + \mathbf{B}_1^*) \cdot \vec{E}_0 \right) dV$$

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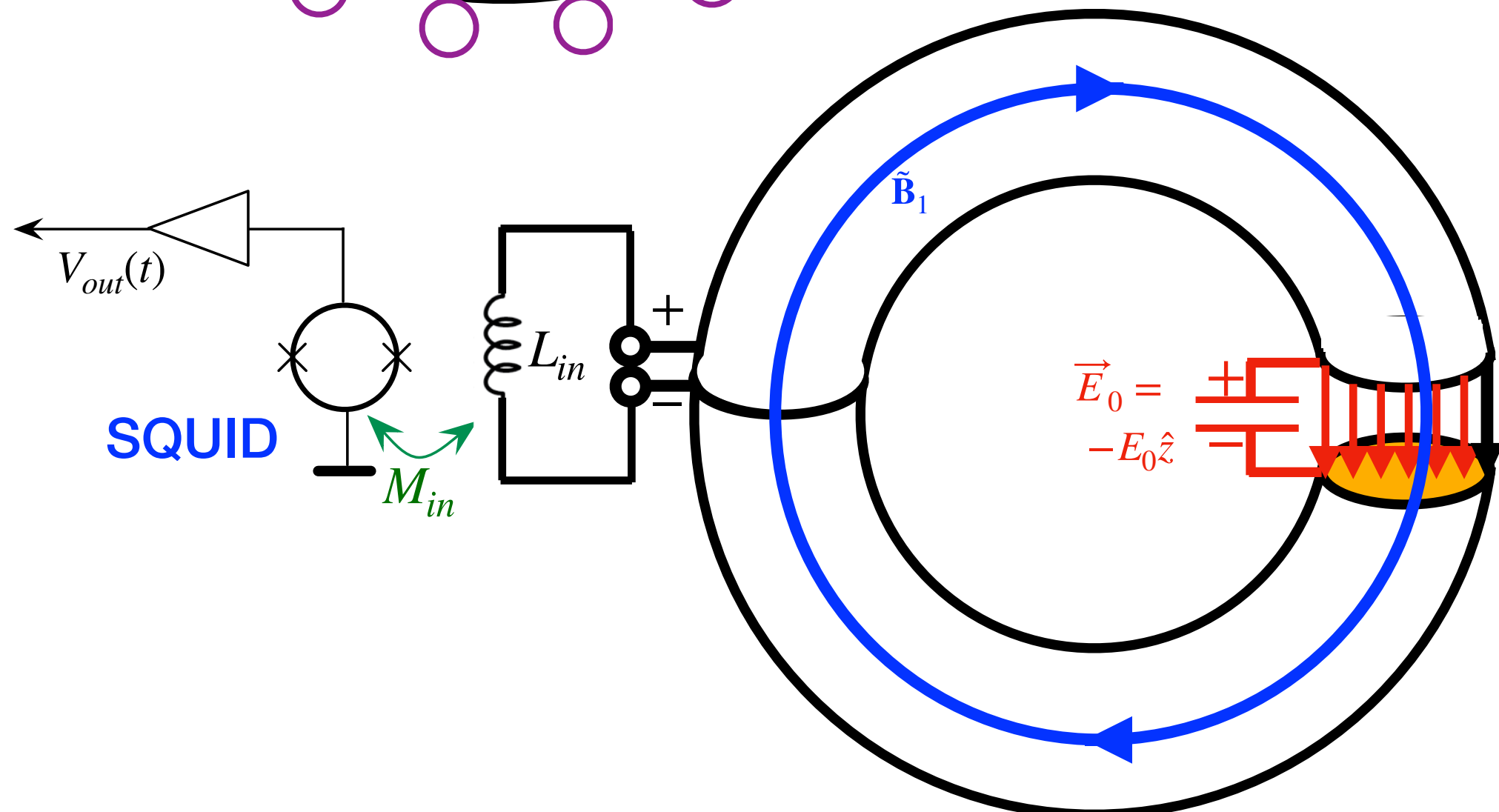
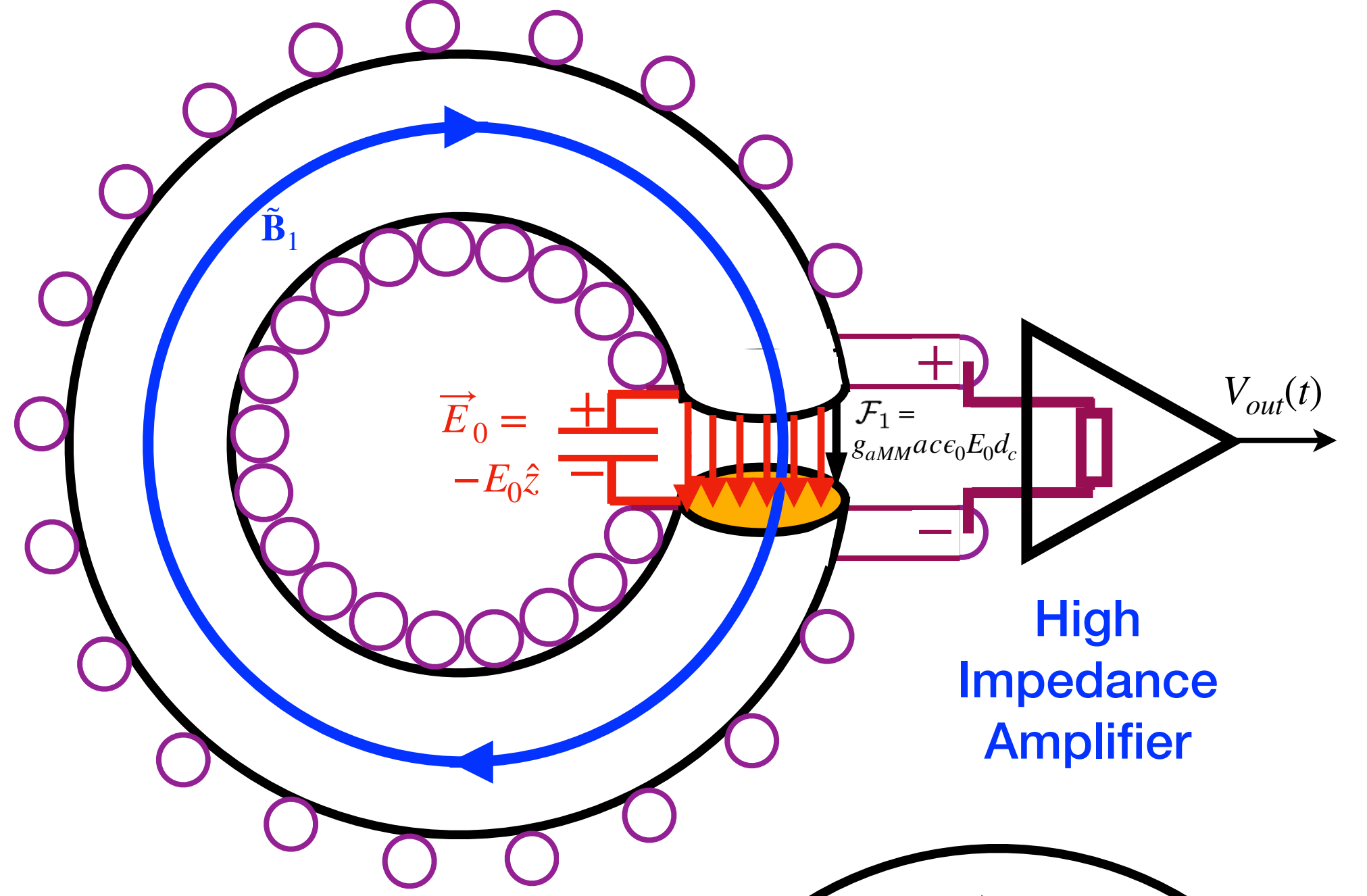
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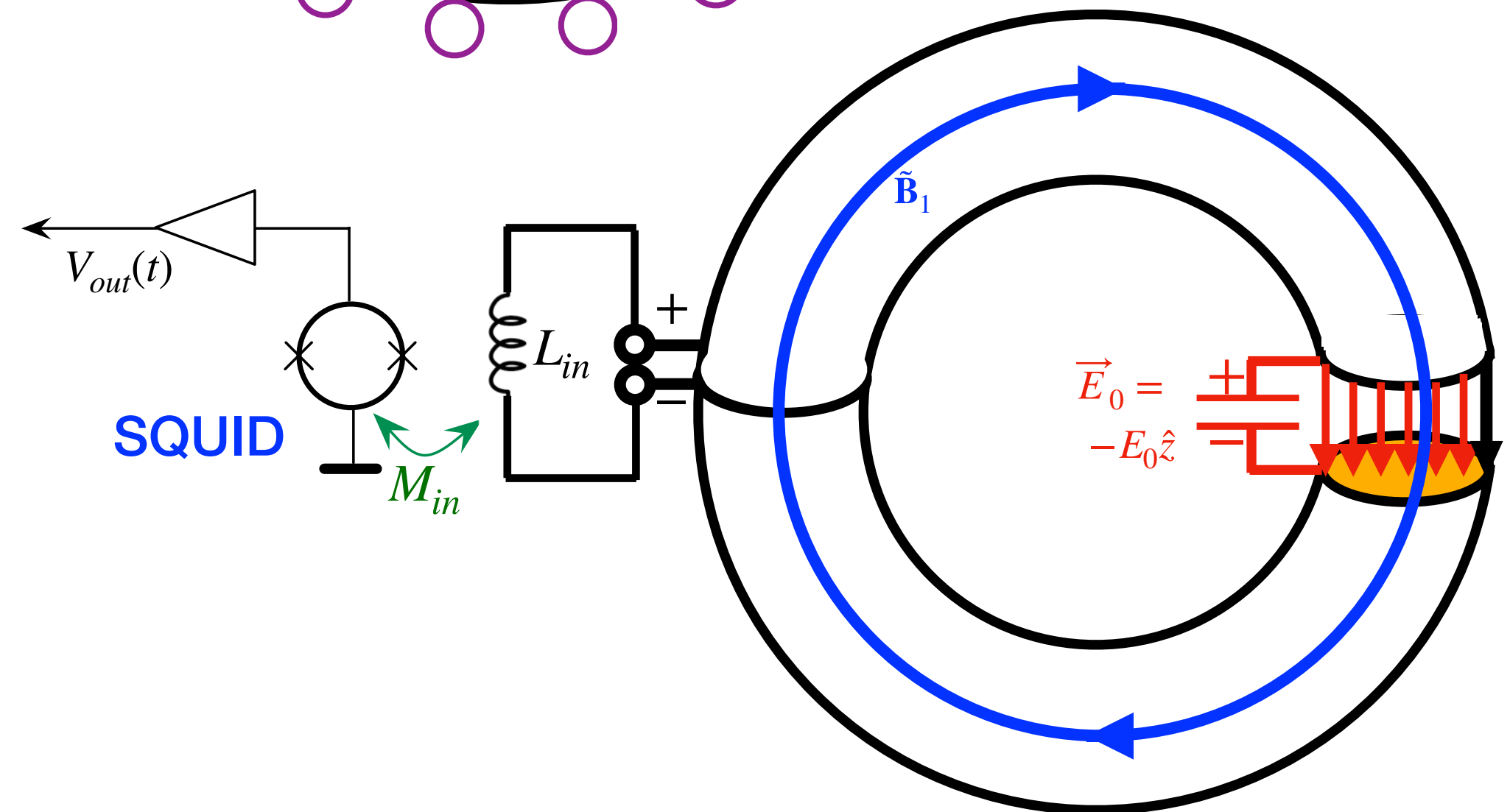
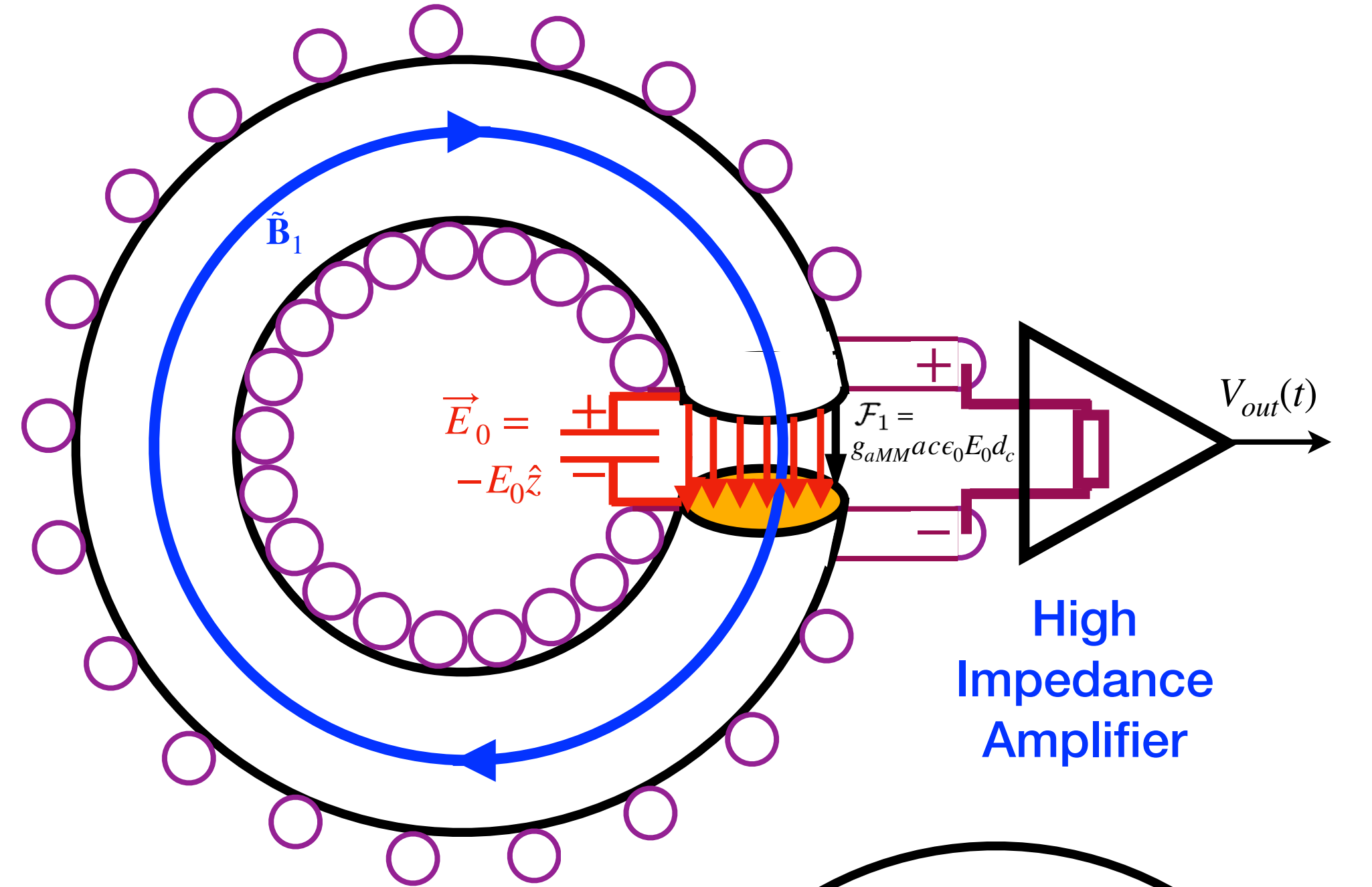
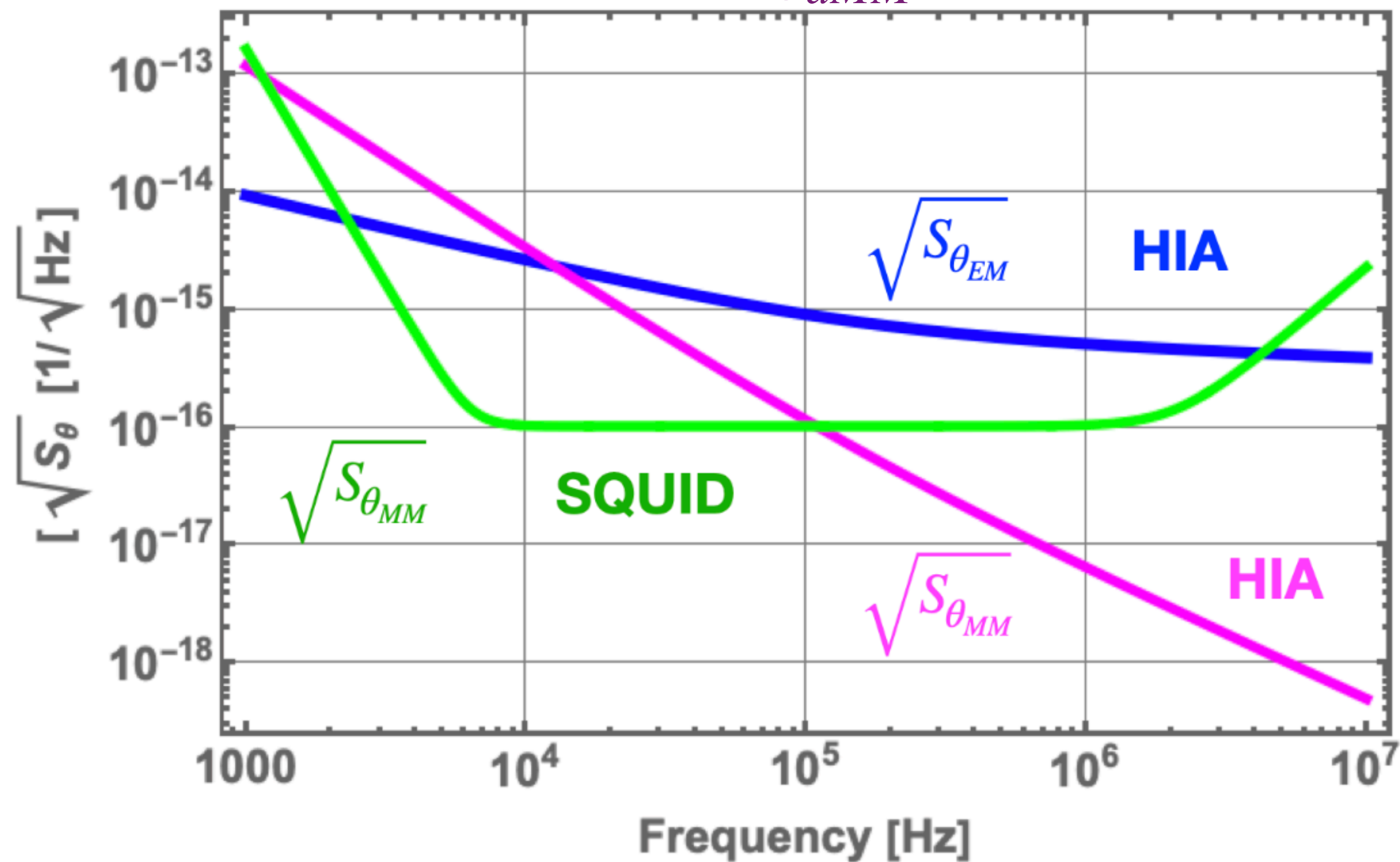
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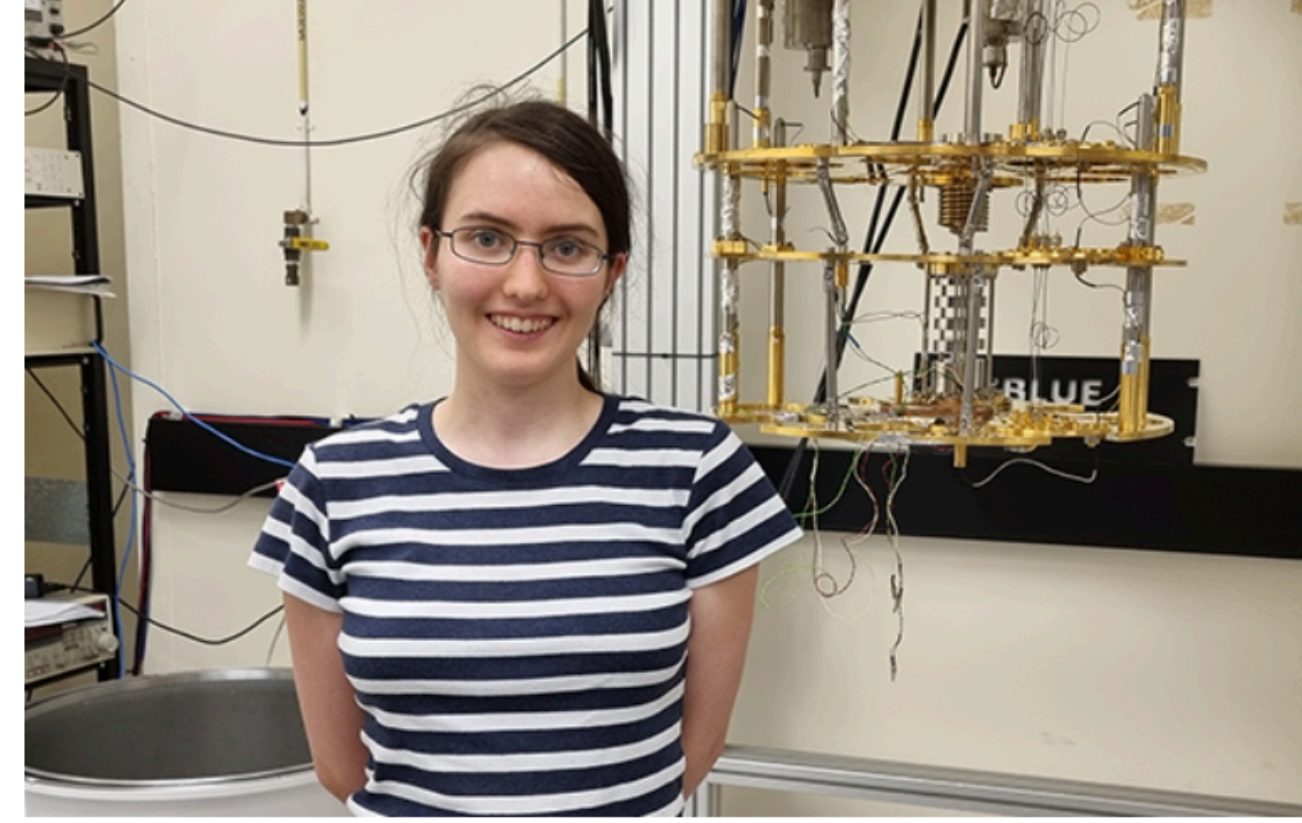
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$$\theta = a g_{aMM}$$



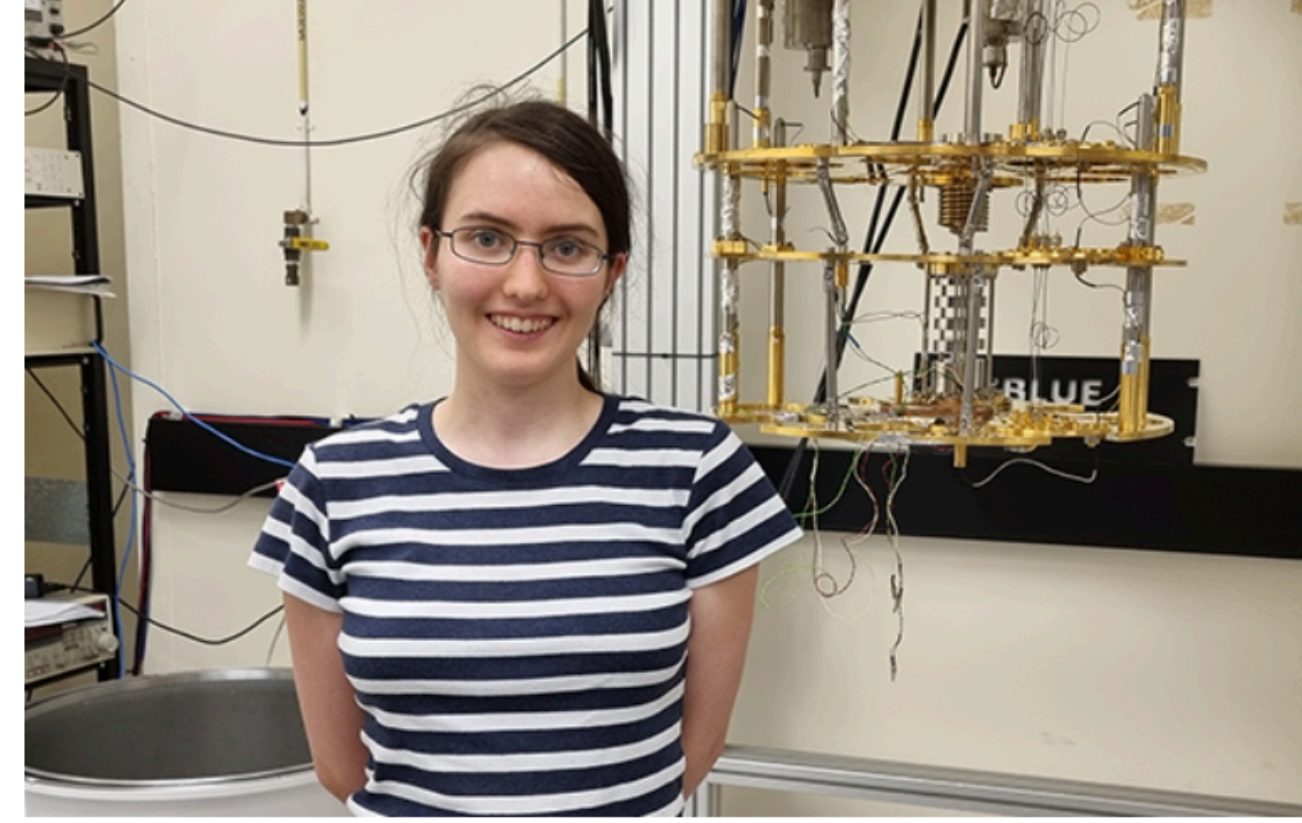
The Axion-MonoPole-Detection (AMPD) Experiment Initial Prototype ~ 4cm Purchased Standard Ferrite Core



Emily Waterman

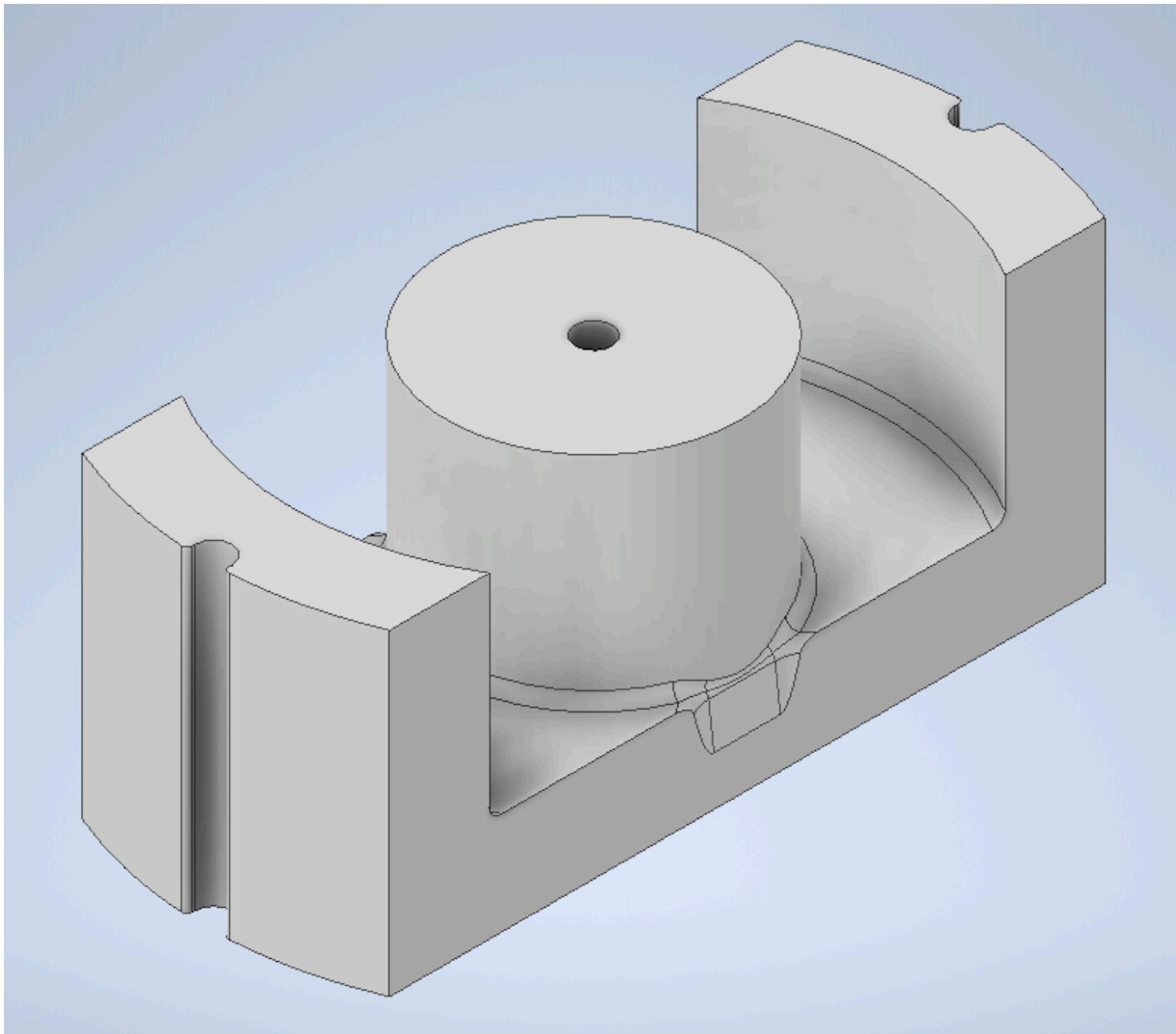
BPhil (Hons) Honours Dissertation

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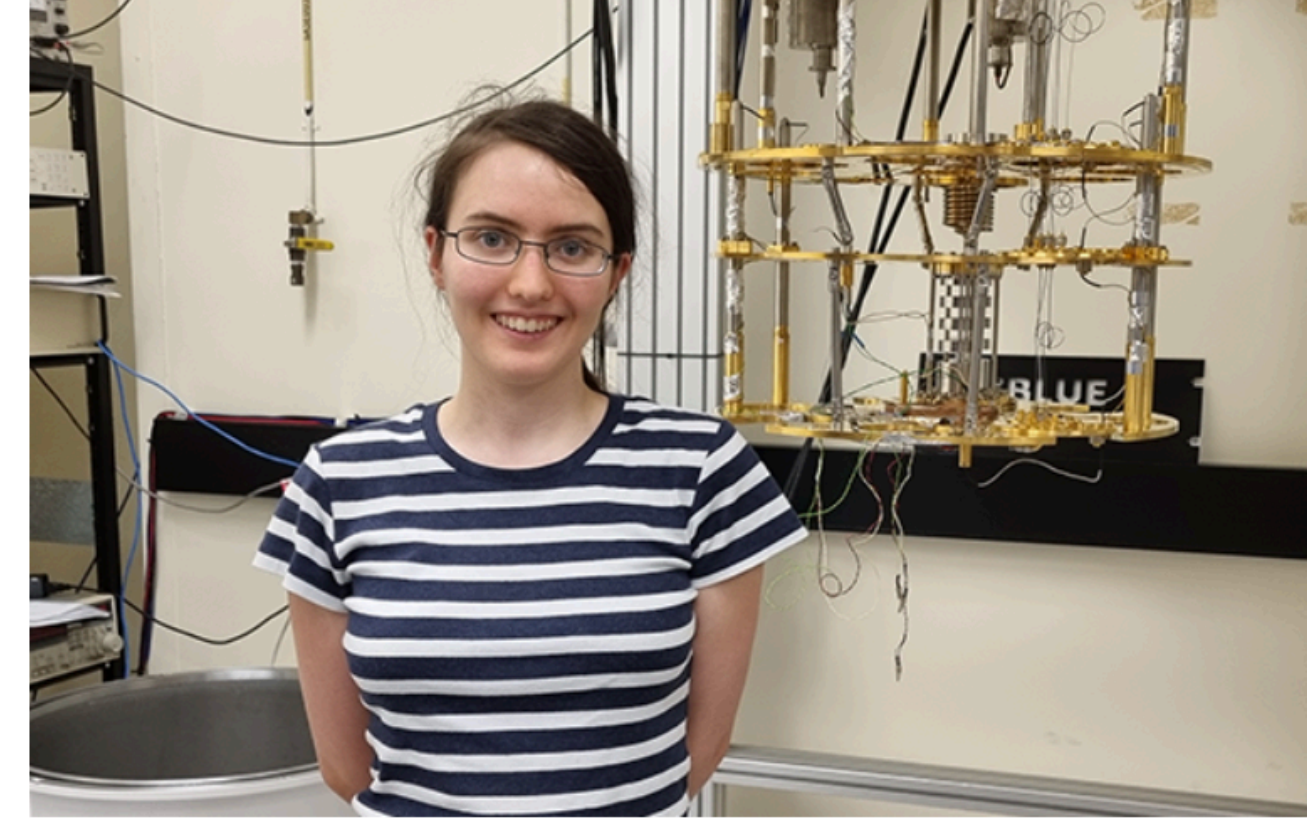
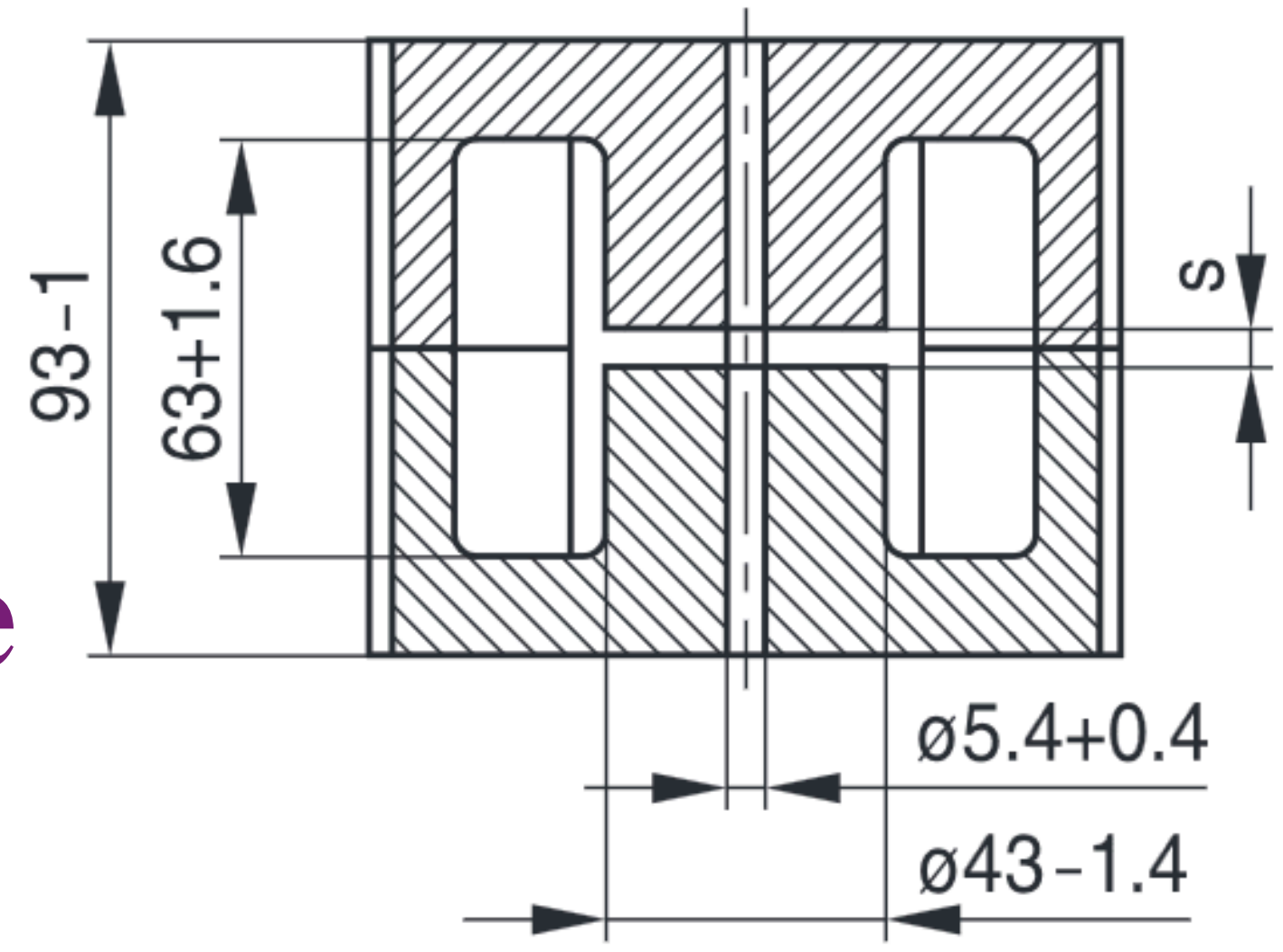


Emily Waterman

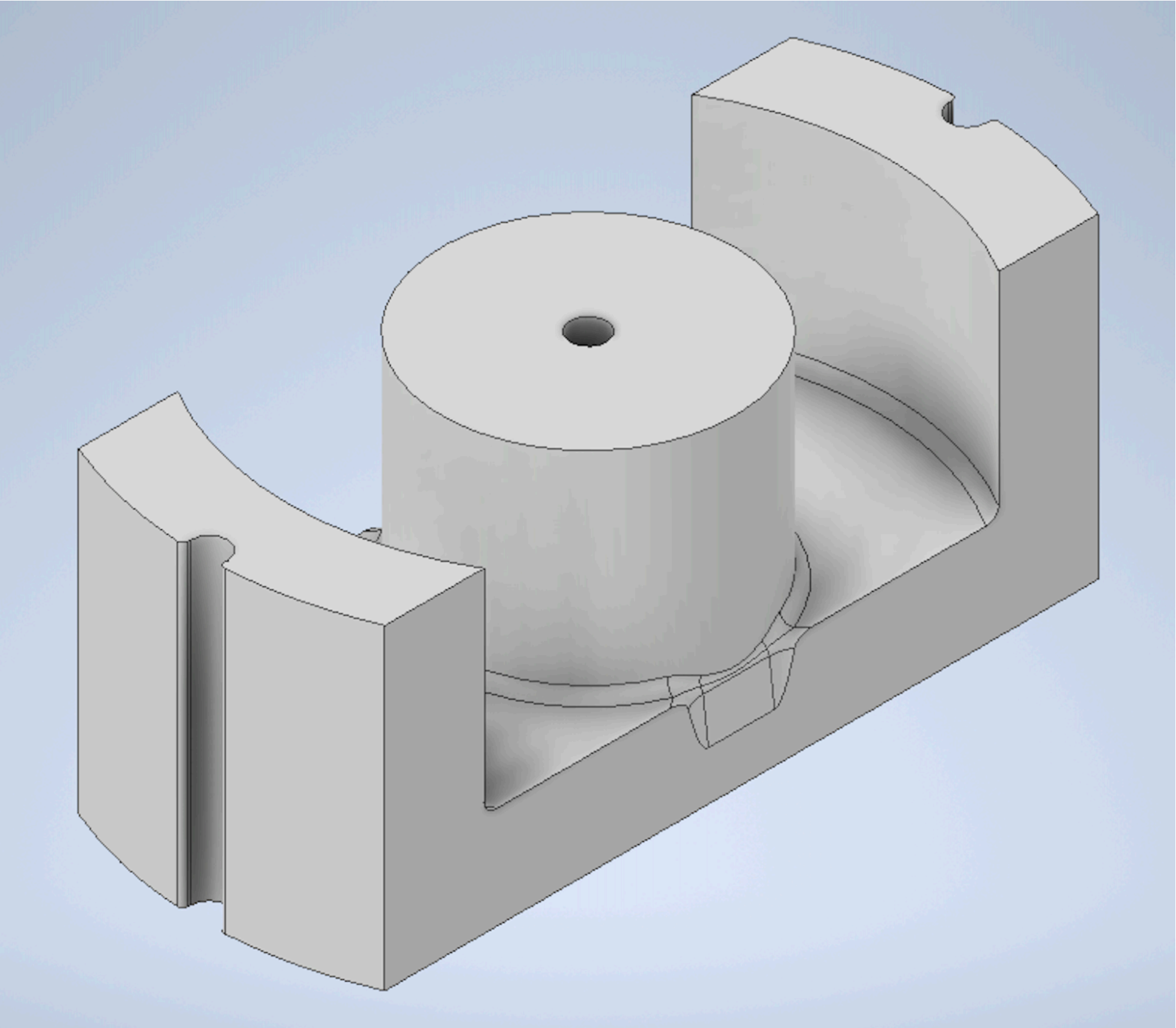
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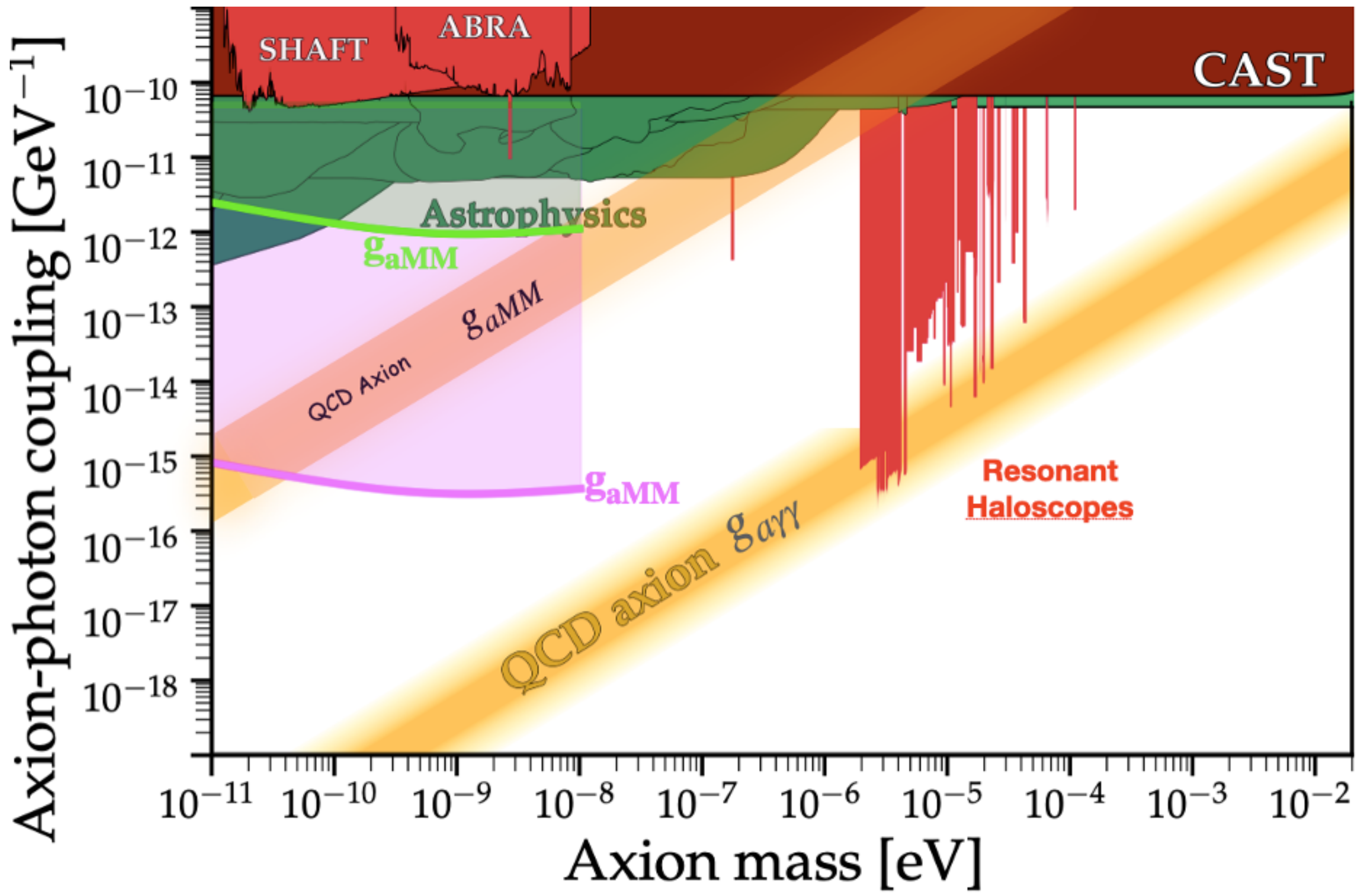


The Axion-MonoPole-Detection (AMPD) Experiment Initial Prototype ~ 4cm Purchased Standard Ferrite Core



Emily Waterman
BPhil (Hons) Honours Dissertation





Twisted “anyon” microwave cavities

Why is it called an “anyon” cavity?

Twisted “anyon” microwave cavities

Why is it called an “anyon” cavity?

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Classical Möbius-Ring Resonators Exhibit Fermion-Boson Rotational Symmetry

Douglas J. Ballon and Henning U. Voss
Phys. Rev. Lett. **101**, 247701 – Published 9 December 2008

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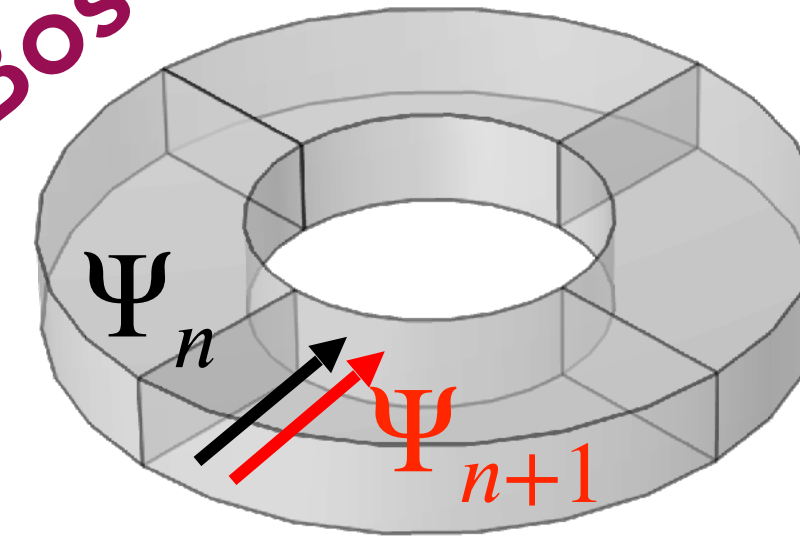
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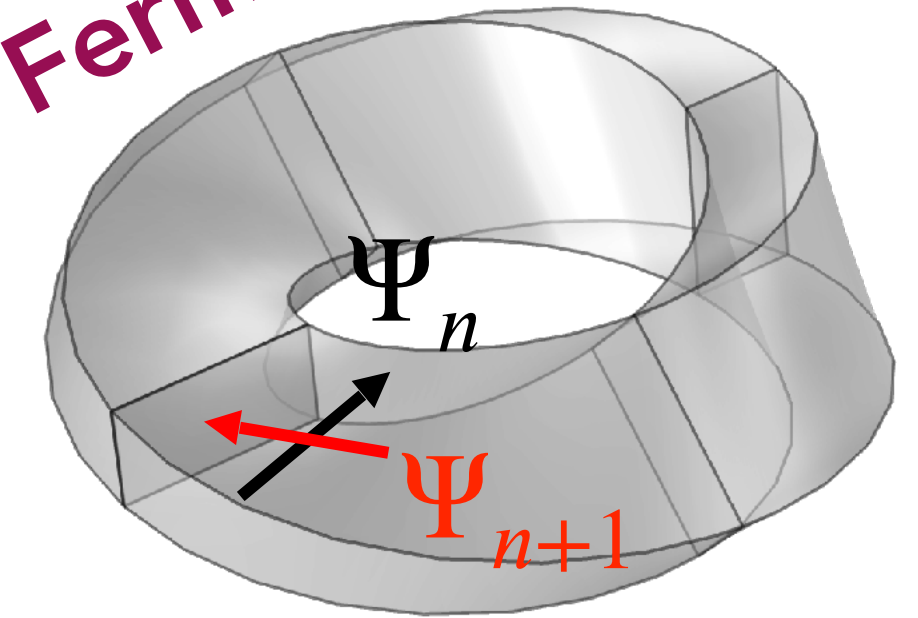
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"Boson"



$$\begin{aligned}\psi_n &= \psi_{n+1} \\ \psi_n &= \psi_{n+N} \\ \theta &= 0\end{aligned}$$

"Fermion"



$$\begin{aligned}\psi_n &= -\psi_{n+1} \\ \psi_n &= \psi_{n+2N} \\ \theta &= \pm \pi\end{aligned}$$

Twisted "anyon" microwave cavities

Why is it called an "anyon" cavity?

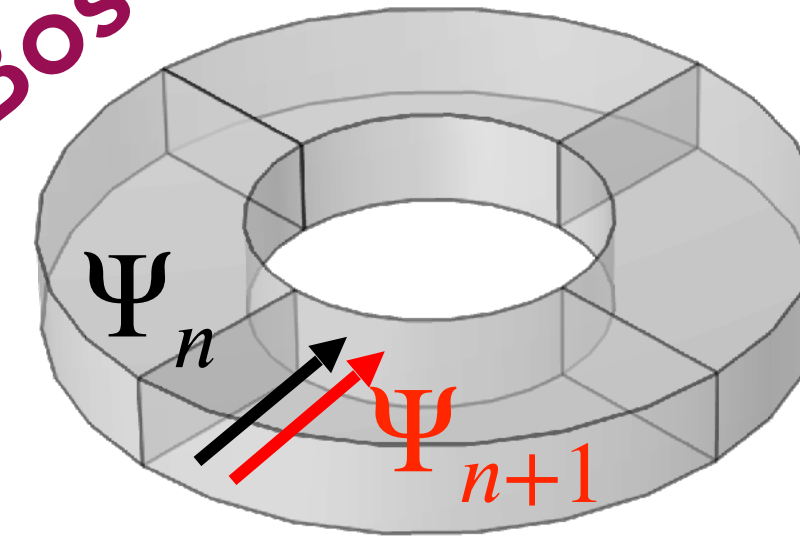
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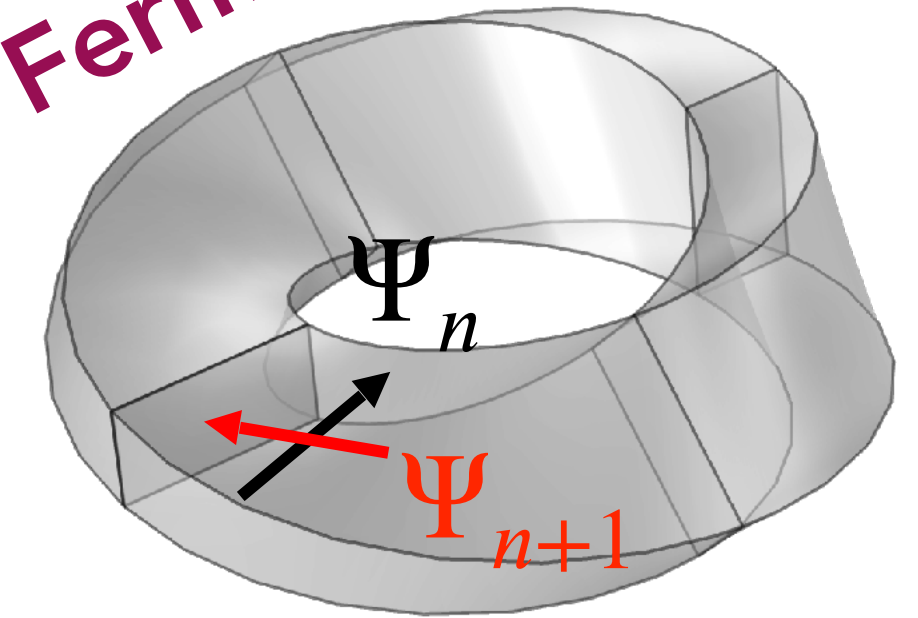
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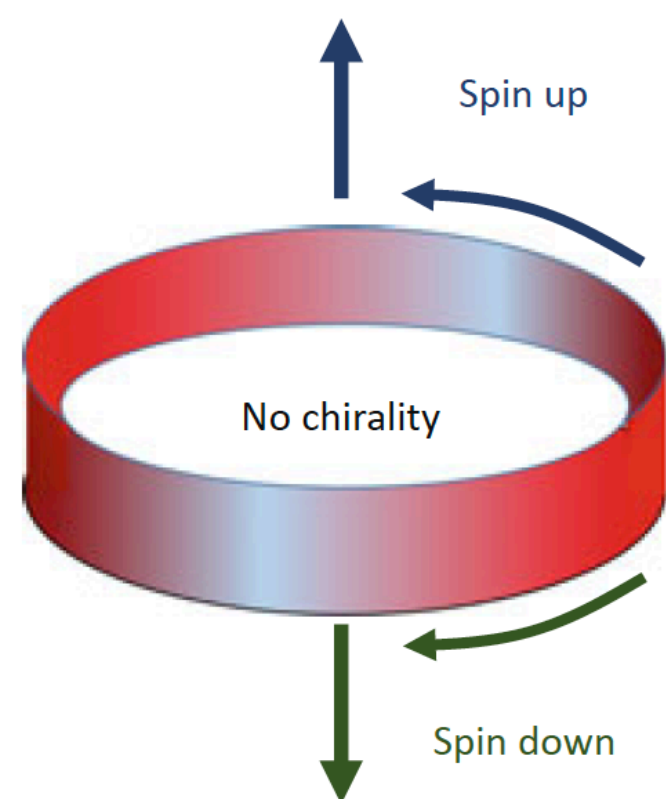
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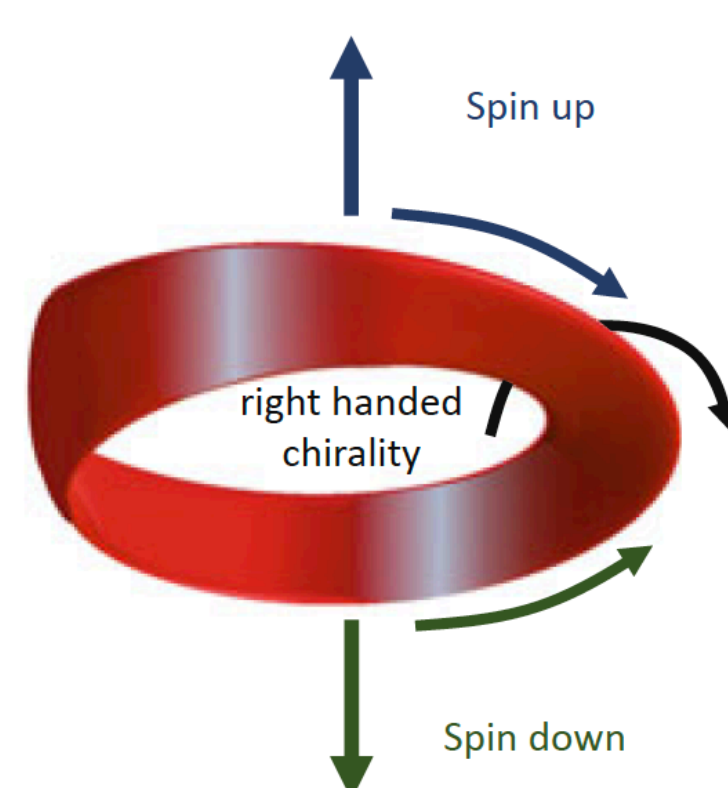
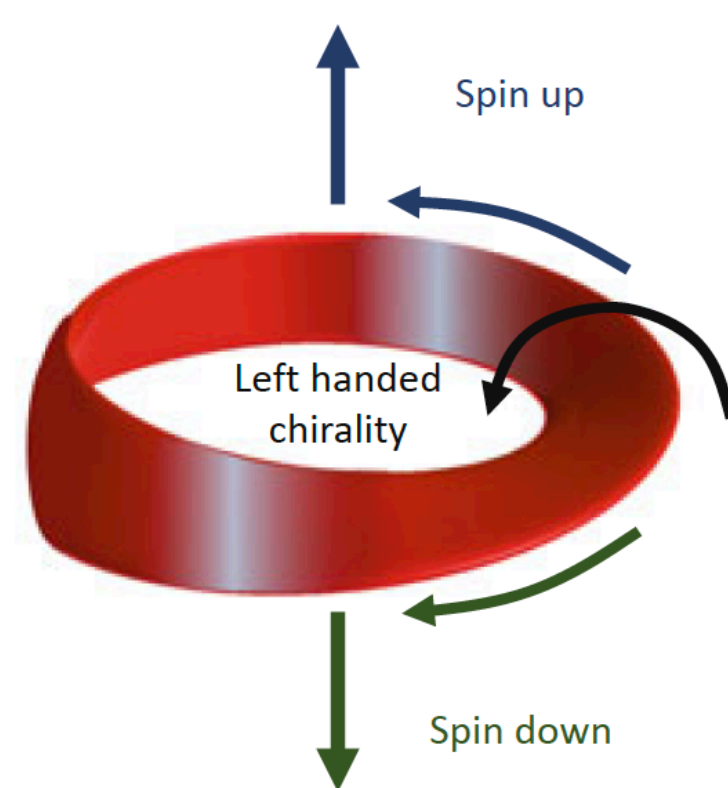
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**Fermions Come in Two Chiralities, Called Left and Right.
Bosons Do Not**

Plain circle



Twisted circle that shows a chirality: a Möbius strip



Twisted "anyon" microwave cavities

Why is it called an "anyon" cavity?

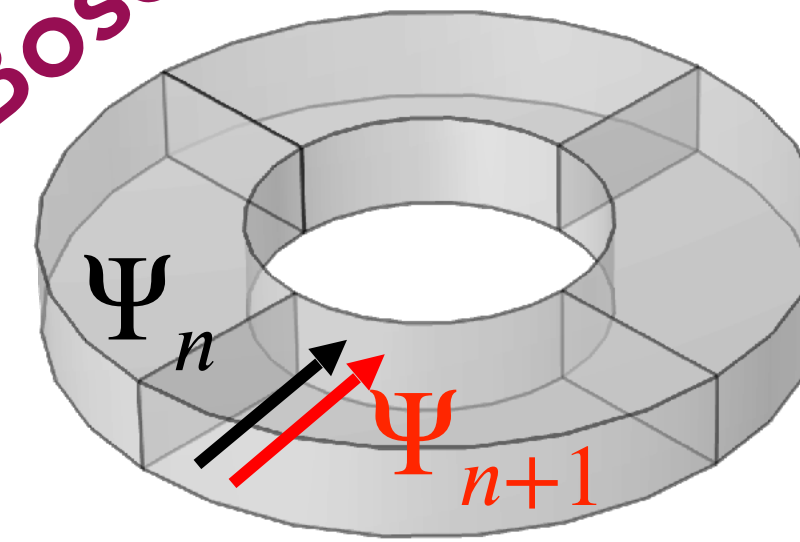
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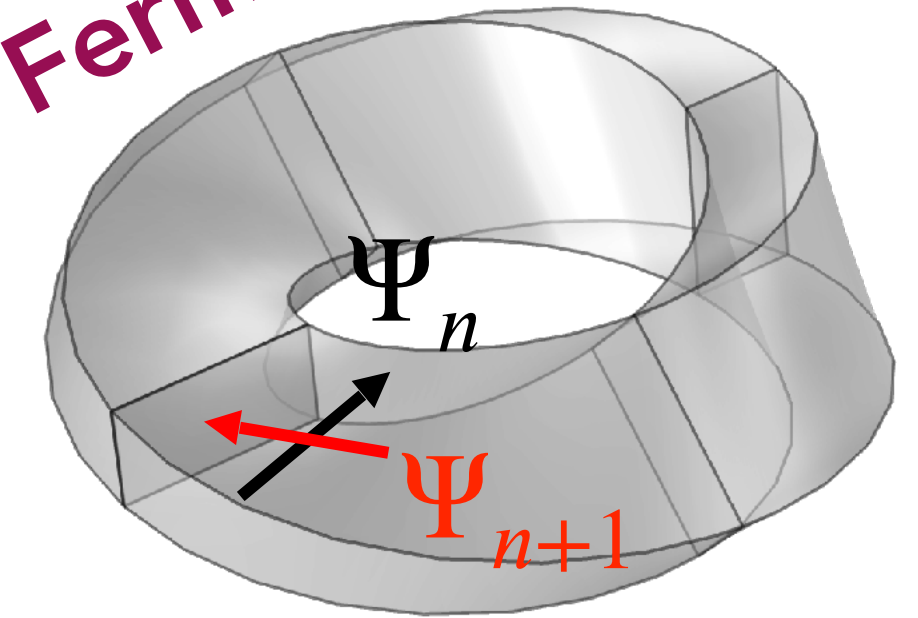
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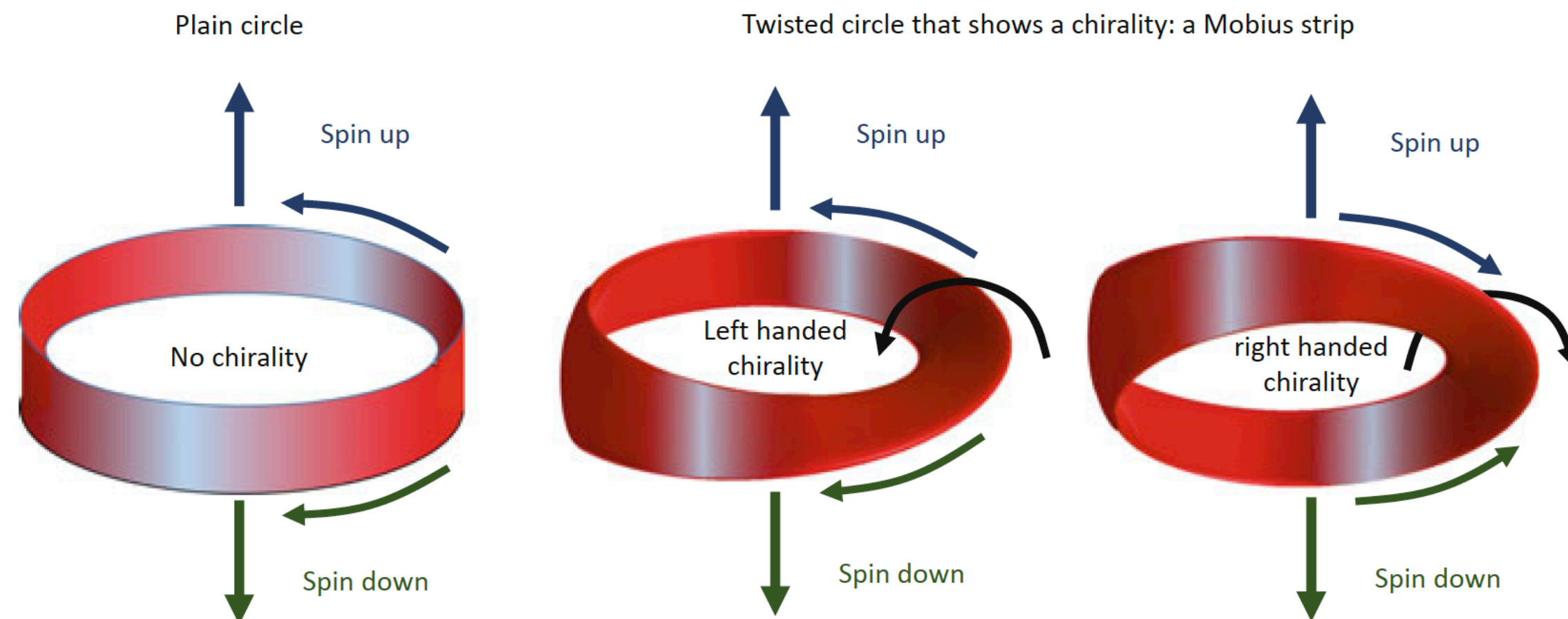
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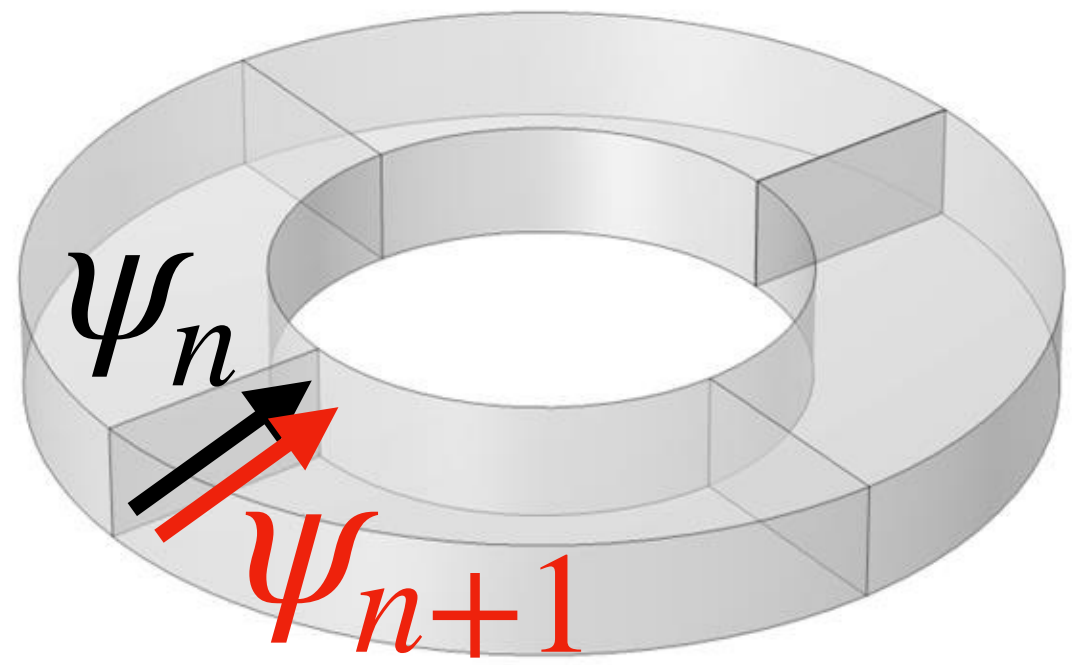
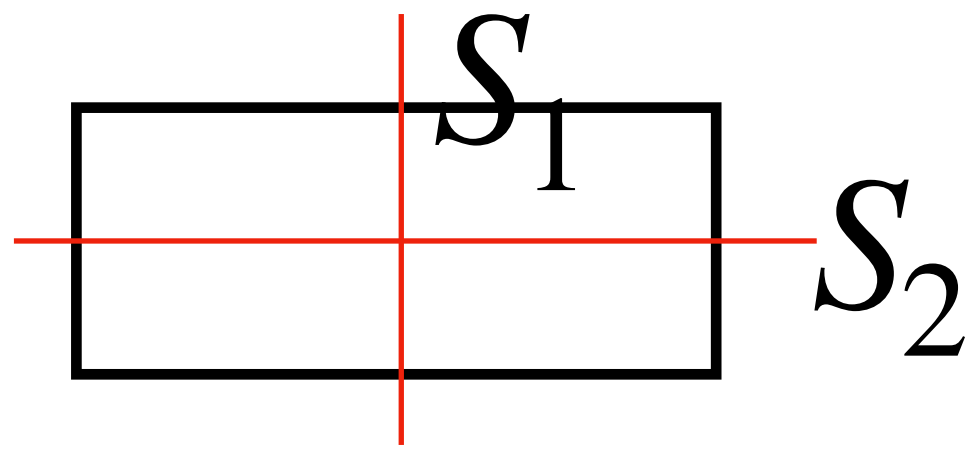
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HOWEVER: For Both Cavities

$$\mathcal{H}_p = \frac{2 \operatorname{Im}[\int \mathbf{B}_p(\vec{r}) \cdot \mathbf{E}_p^*(\vec{r}) d\tau]}{\sqrt{\int \mathbf{E}_p(\vec{r}) \cdot \mathbf{E}_p^*(\vec{r}) d\tau \int \mathbf{B}_p(\vec{r}) \cdot \mathbf{B}_p^*(\vec{r}) d\tau}} \sim 0$$

Torus



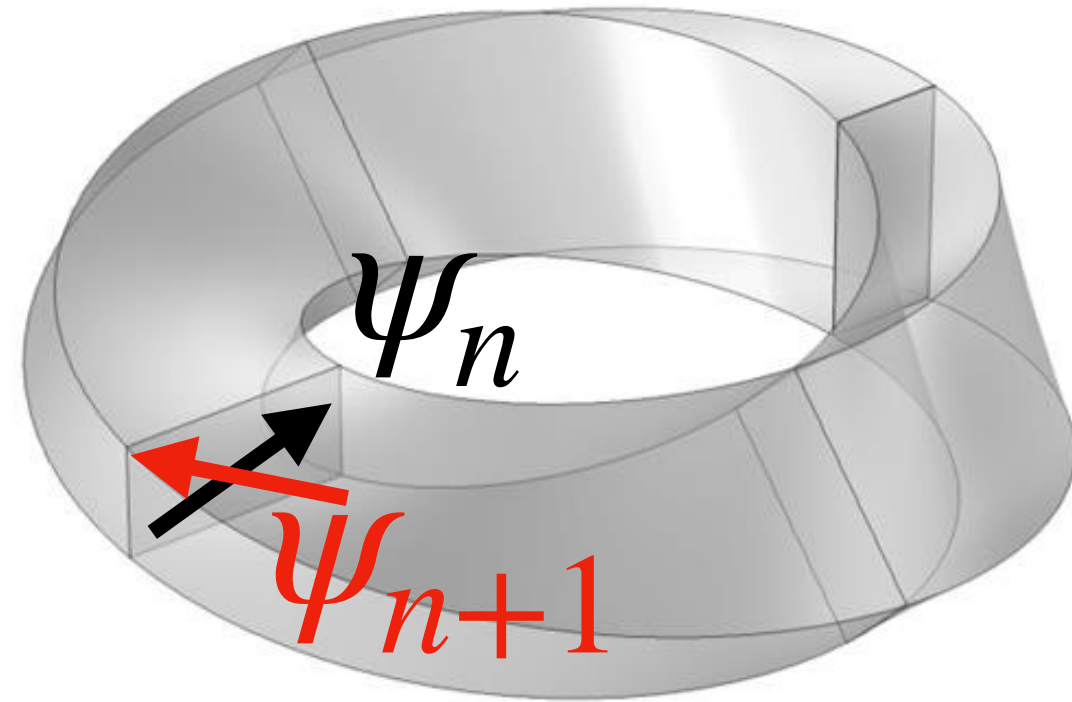
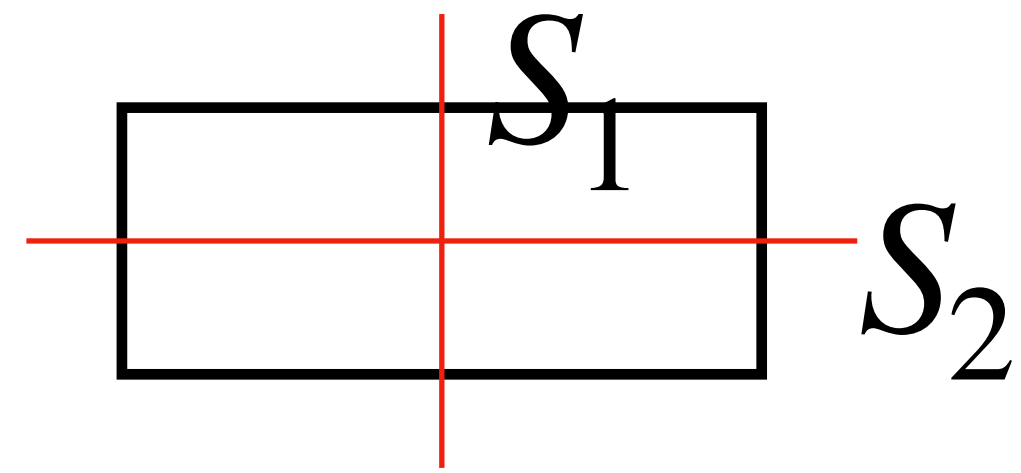
$$\psi_n = \psi_{n+1}$$

$$\psi_n = \psi_{n+N}$$

$$\theta = 0$$

Boson

Möbius



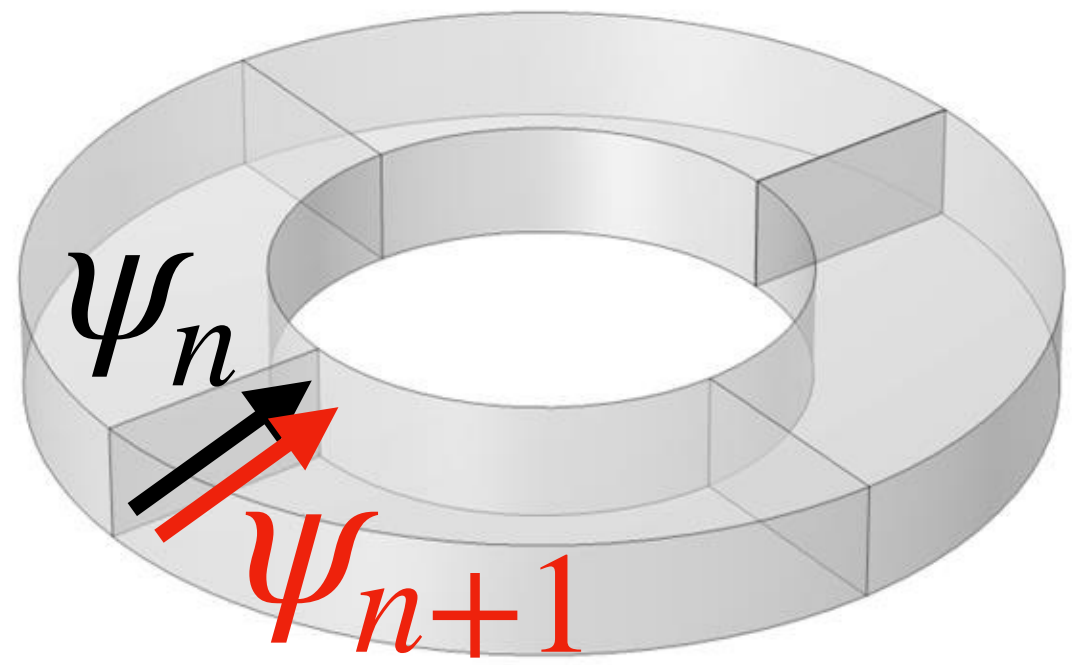
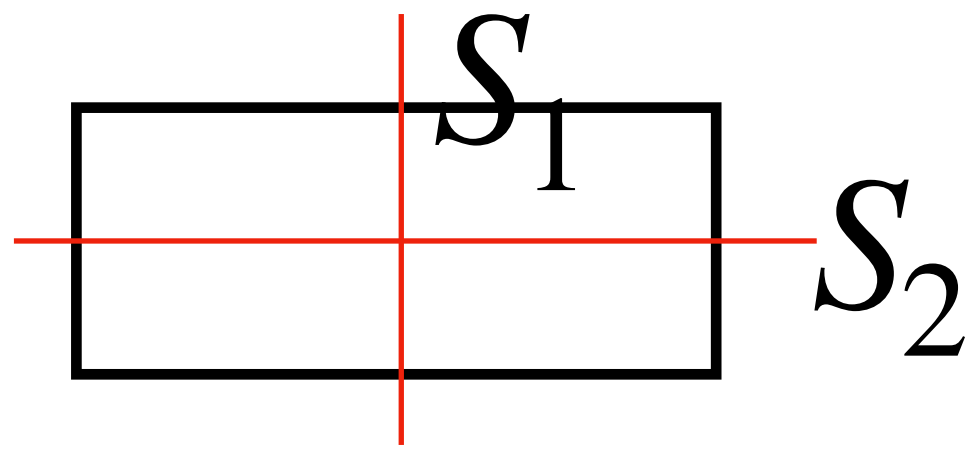
$$\psi_n = -\psi_{n+1}$$

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Fermion

Torus



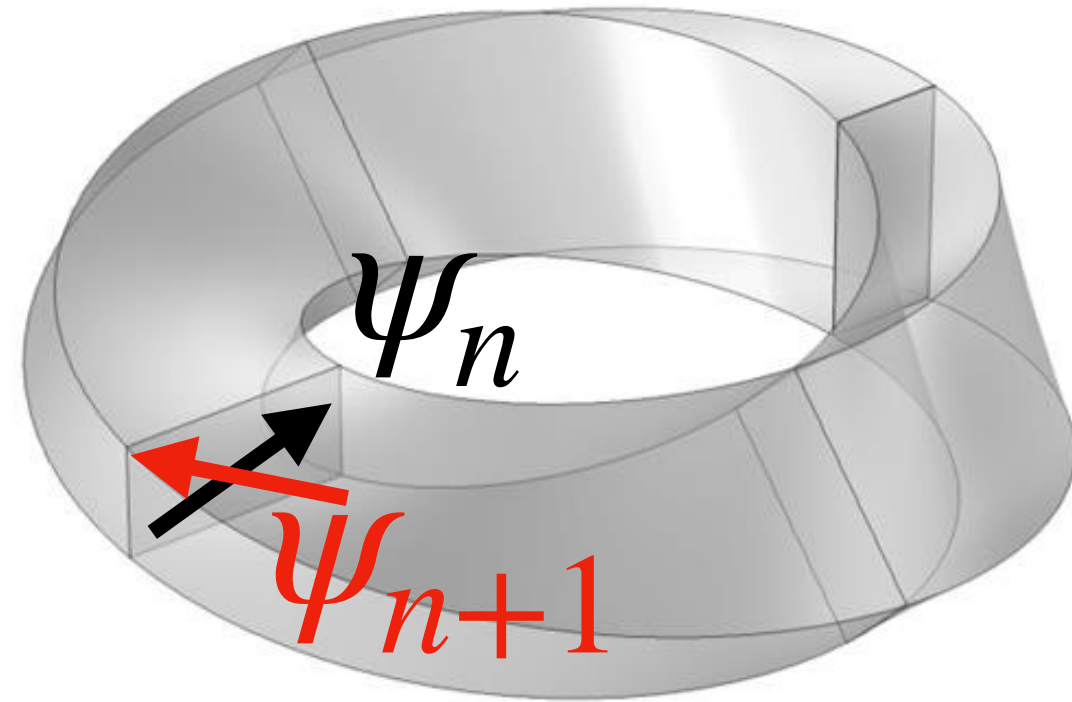
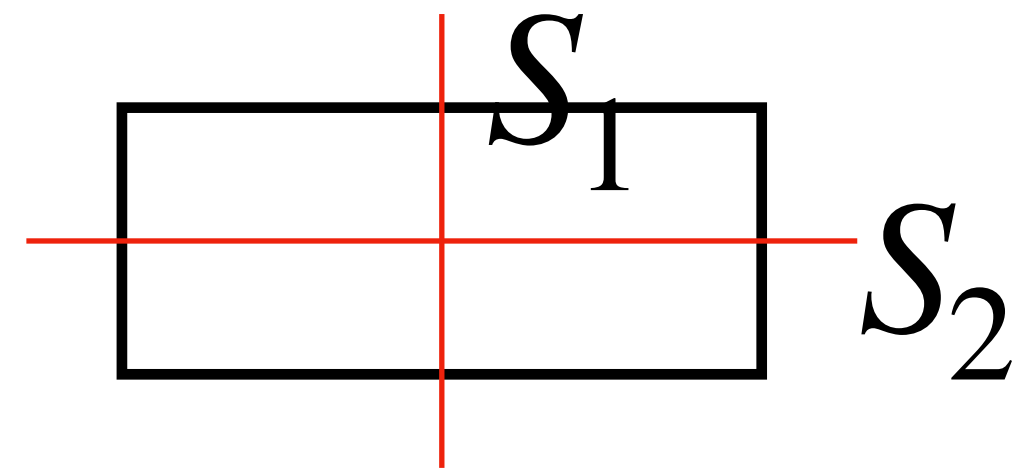
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Boson

Möbius



$$\psi_n = -\psi_{n+1}$$

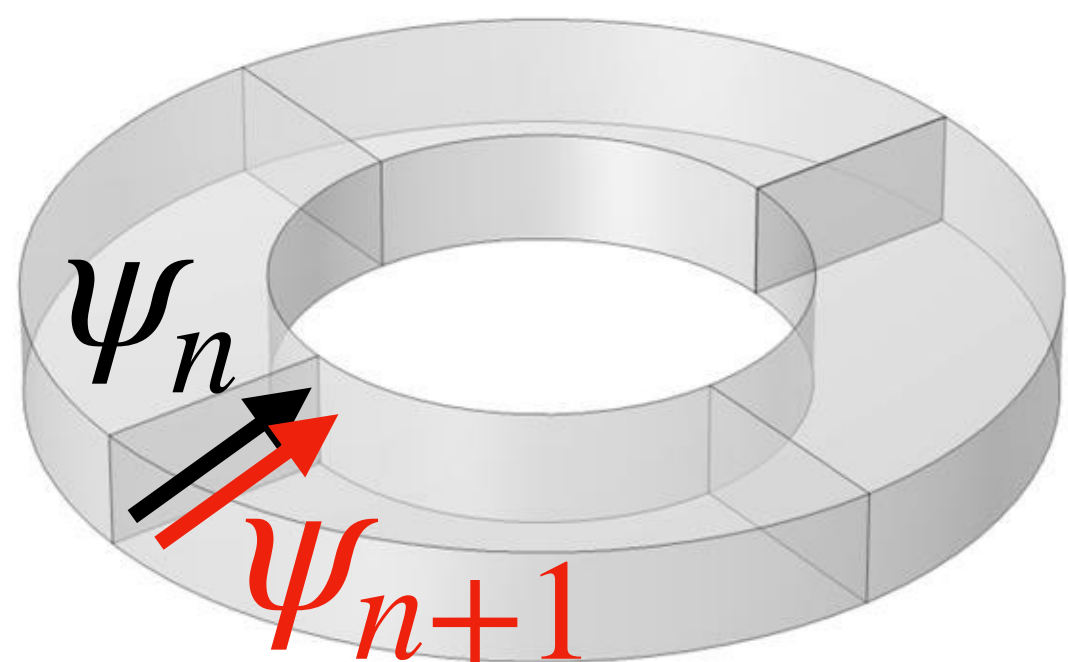
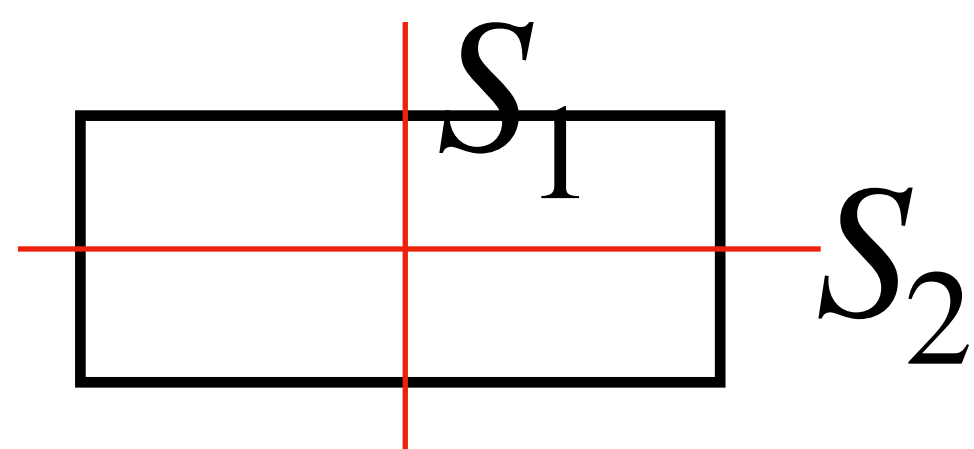
$$\psi_n = \psi_{n+2N}$$

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Fermion

Anyon Cavity

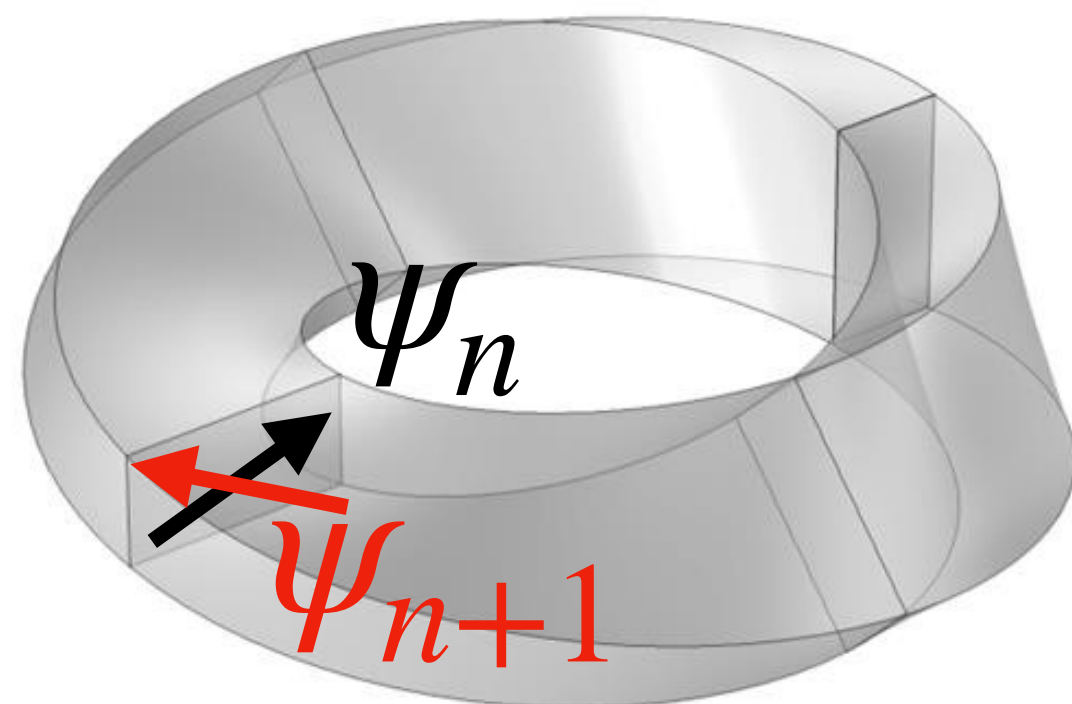
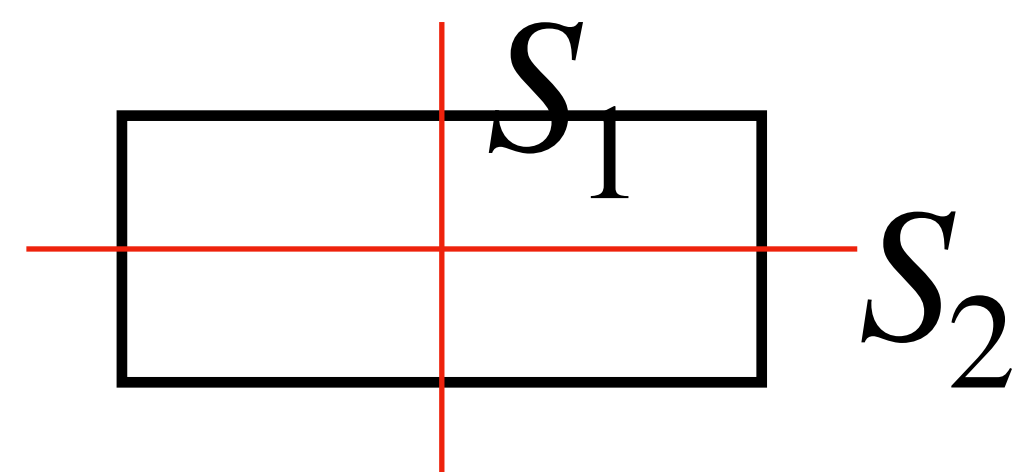
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Boson

Möbius

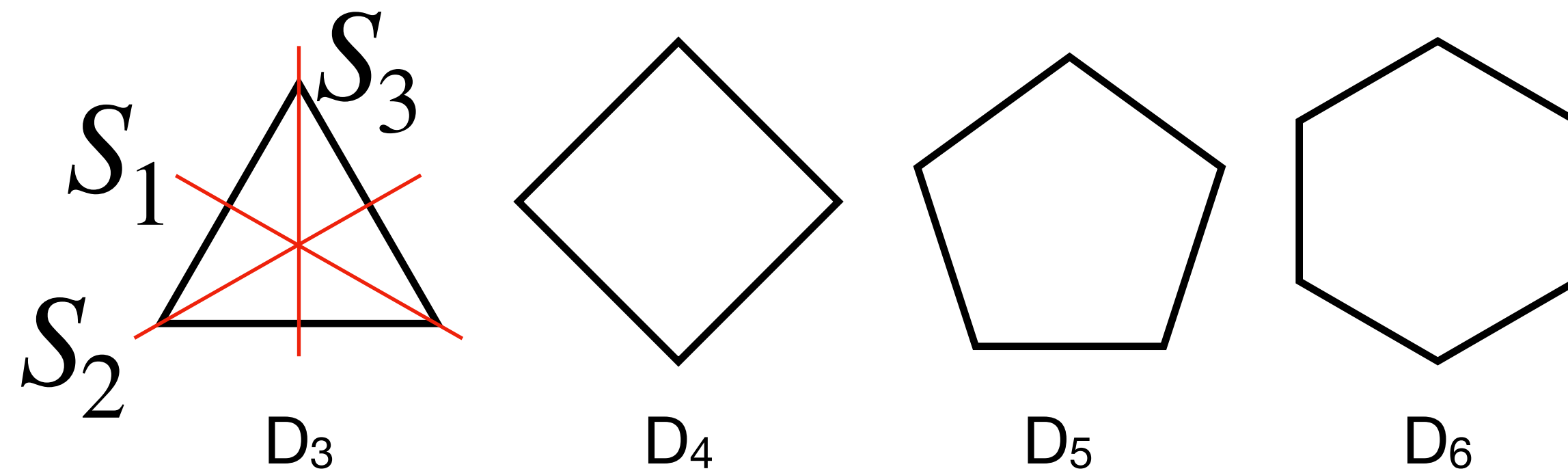


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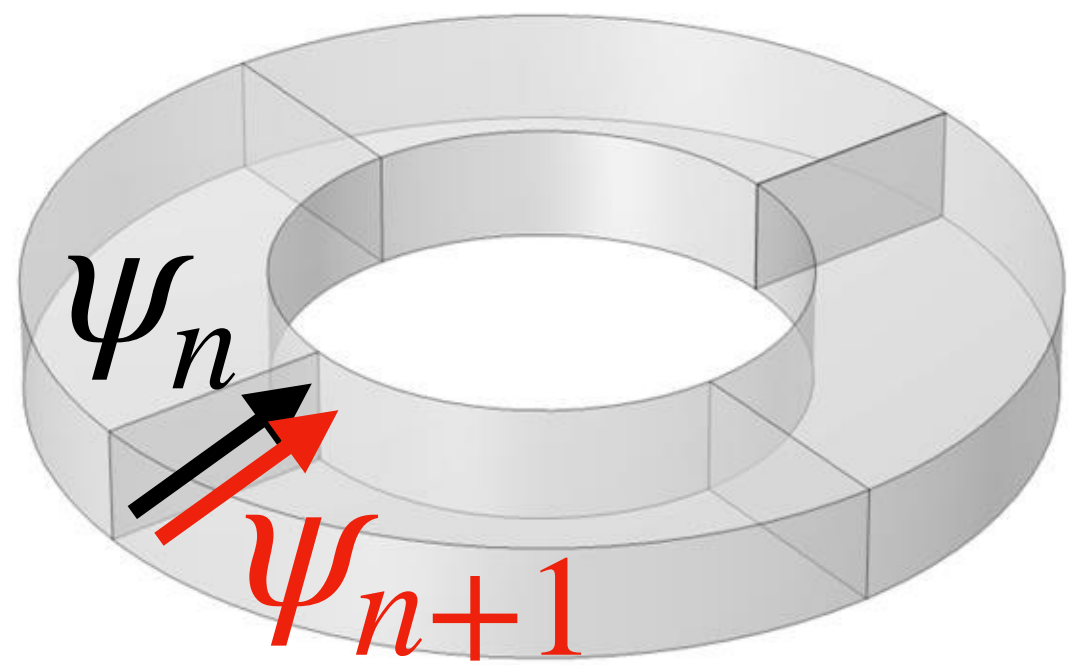
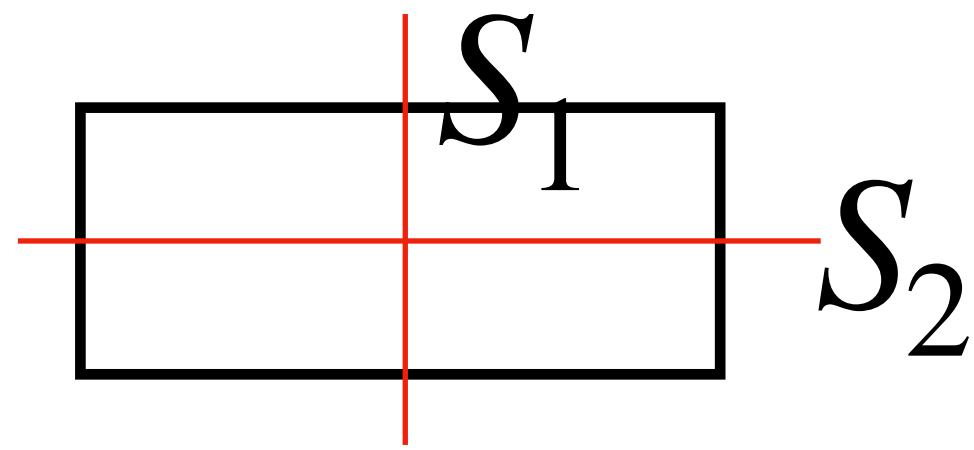
Fermion

Anyon Cavity

Dihedral group of regular convex polygons: D_p



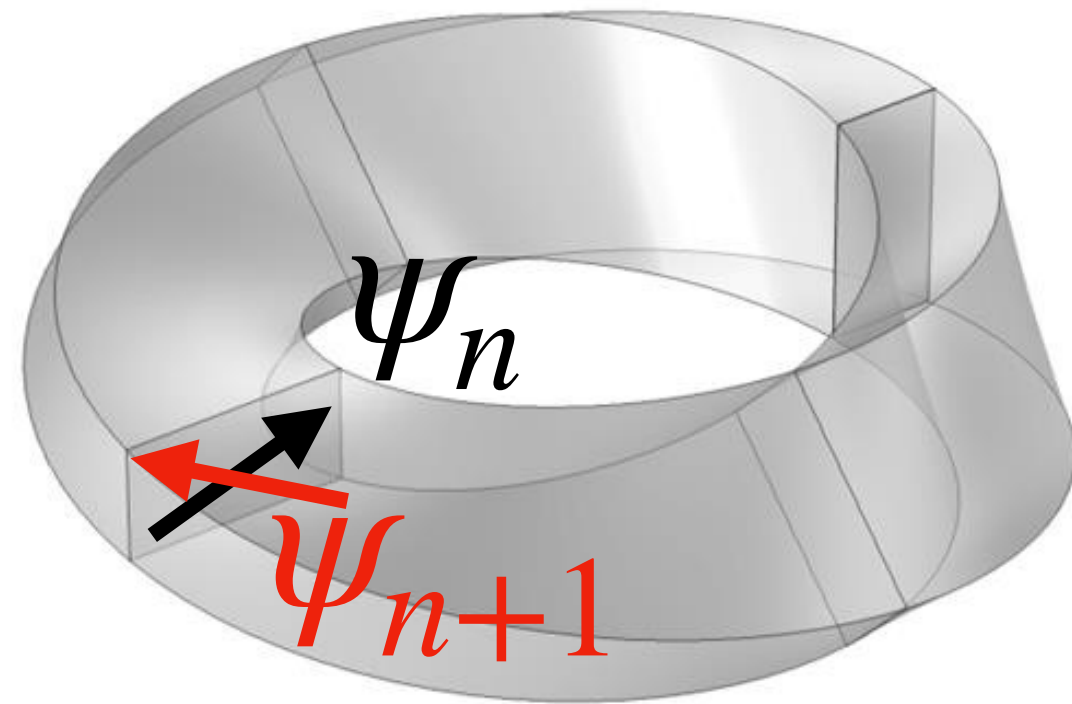
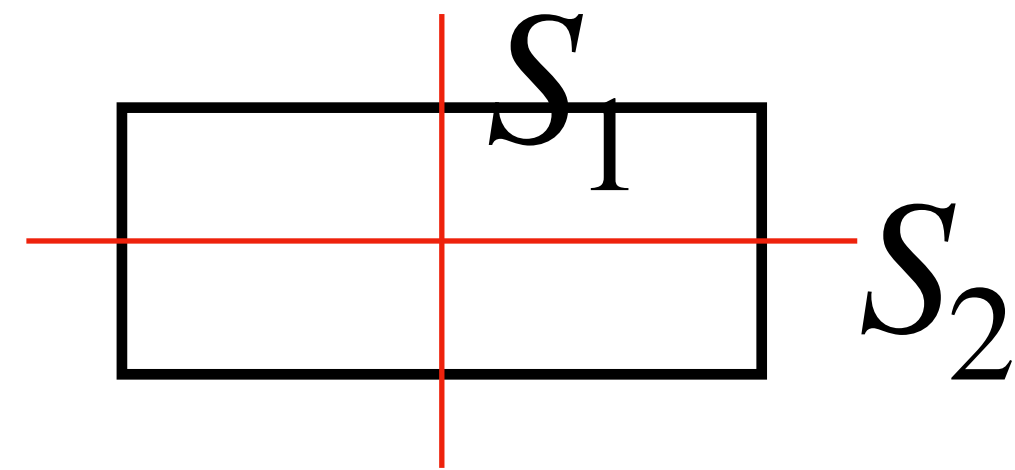
Torus



$$\begin{aligned}\psi_n &= \psi_{n+1} \\ \psi_n &= \psi_{n+N} \\ \theta &= 0\end{aligned}$$

Boson

Möbius

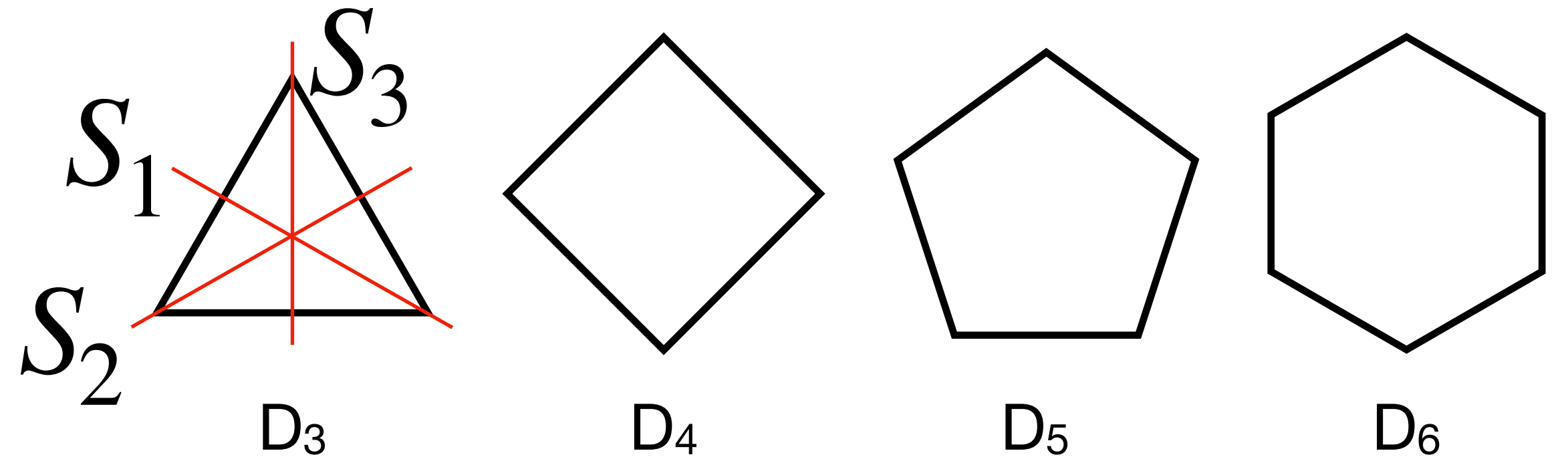


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Fermion

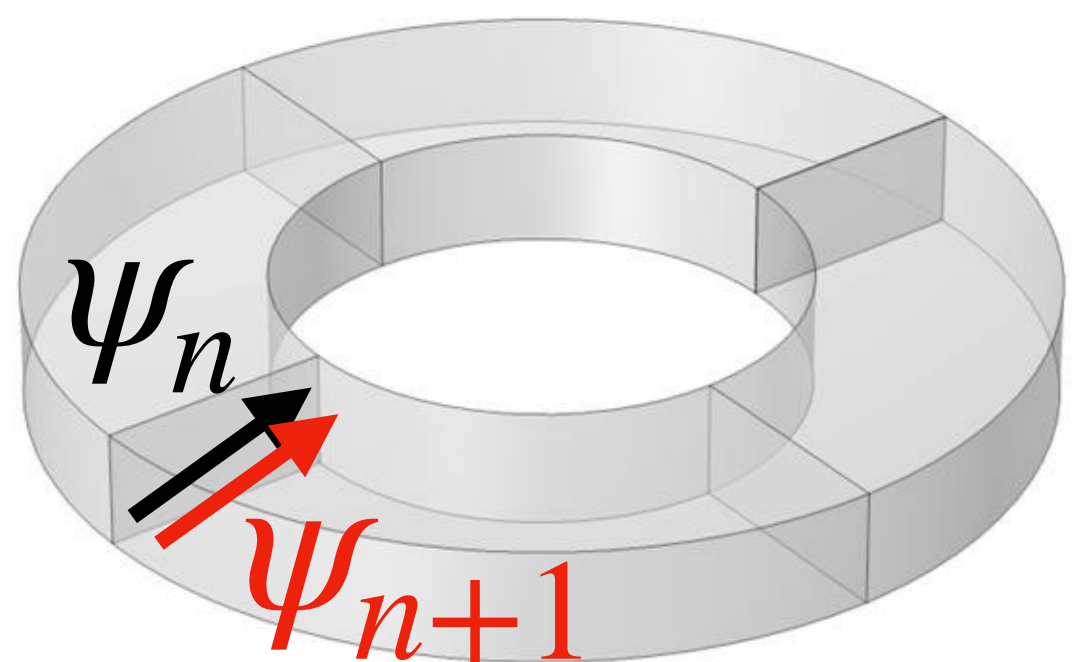
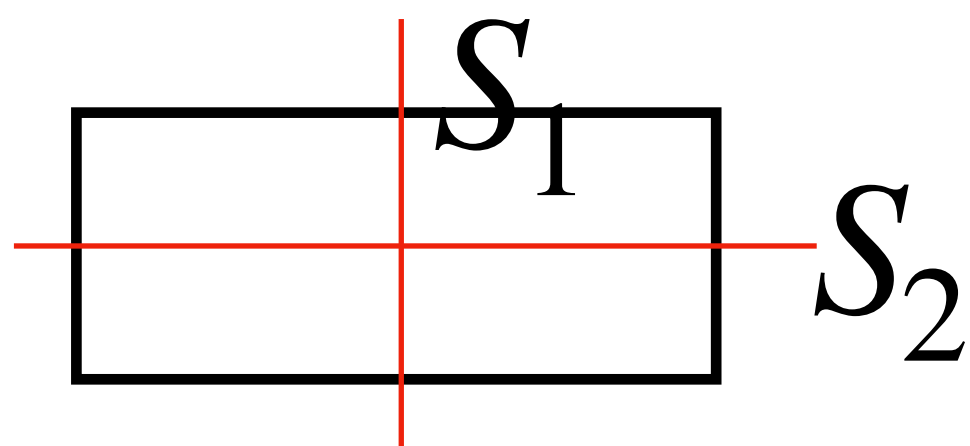
Anyon Cavity

Dihedral group of regular convex polygons: D_p



$2p$ symmetries: p rotational + p reflection
Rotation by $2\pi/p$ preserves the object

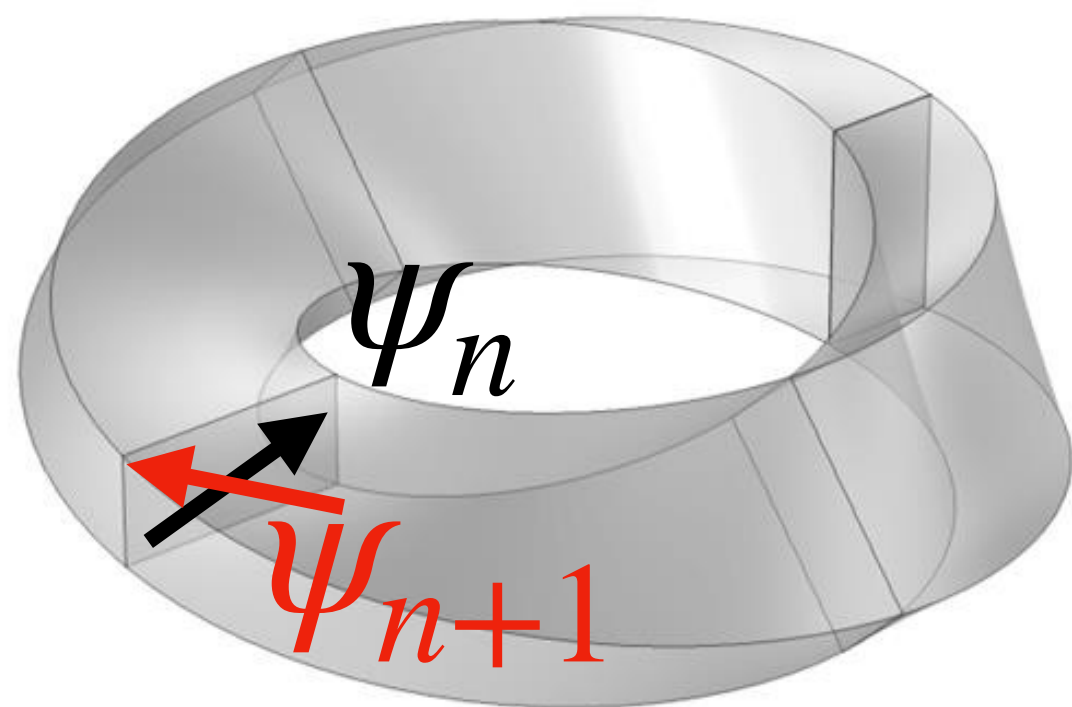
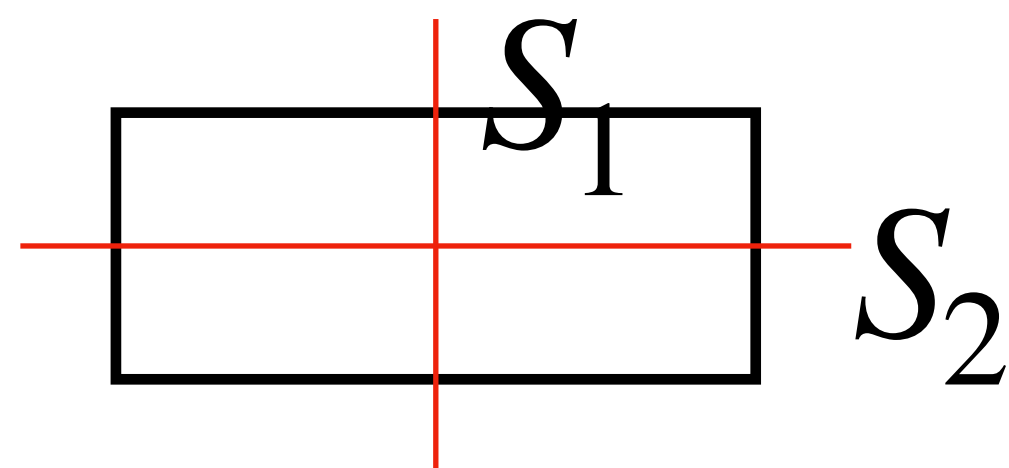
Torus



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Boson

Möbius

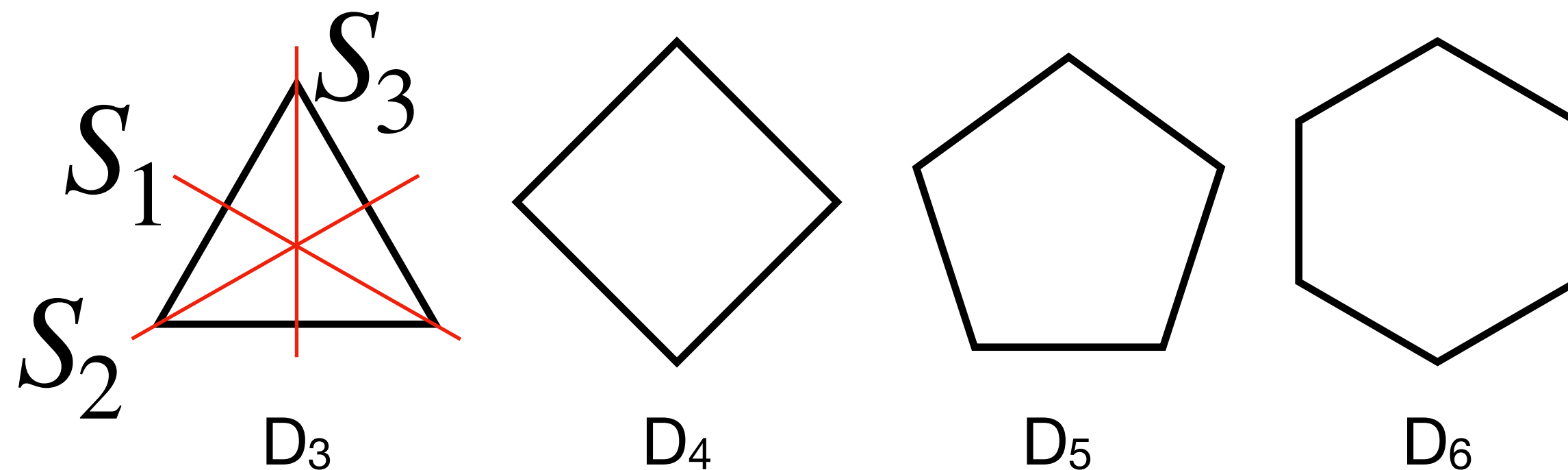


$$\begin{aligned}\psi_n &= -\psi_{n+1} \\ \psi_n &= \psi_{n+2N} \\ \theta &= \pm \pi\end{aligned}$$

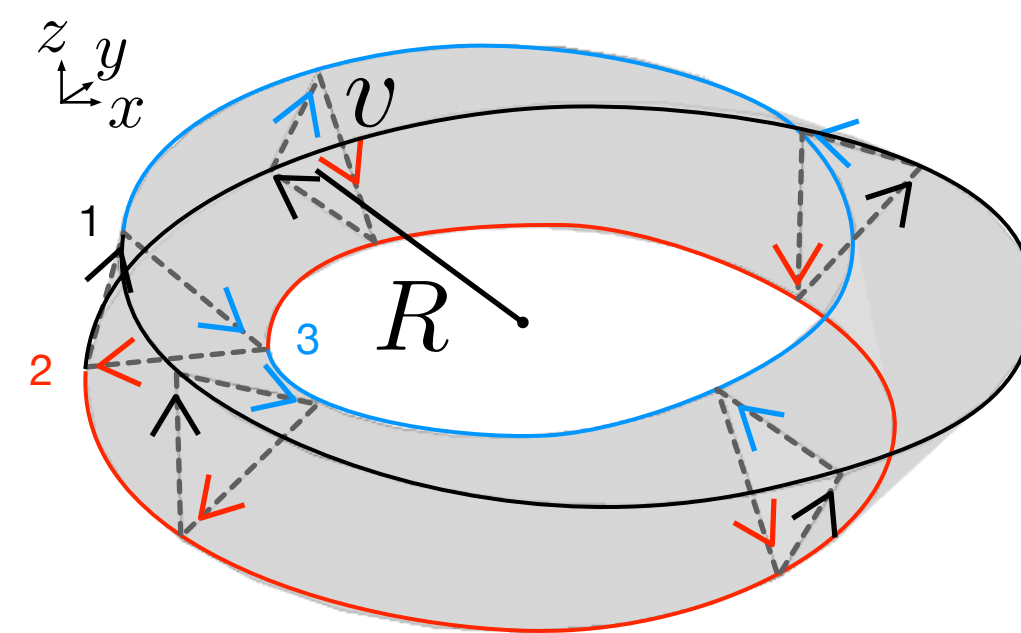
Fermion

Anyon Cavity

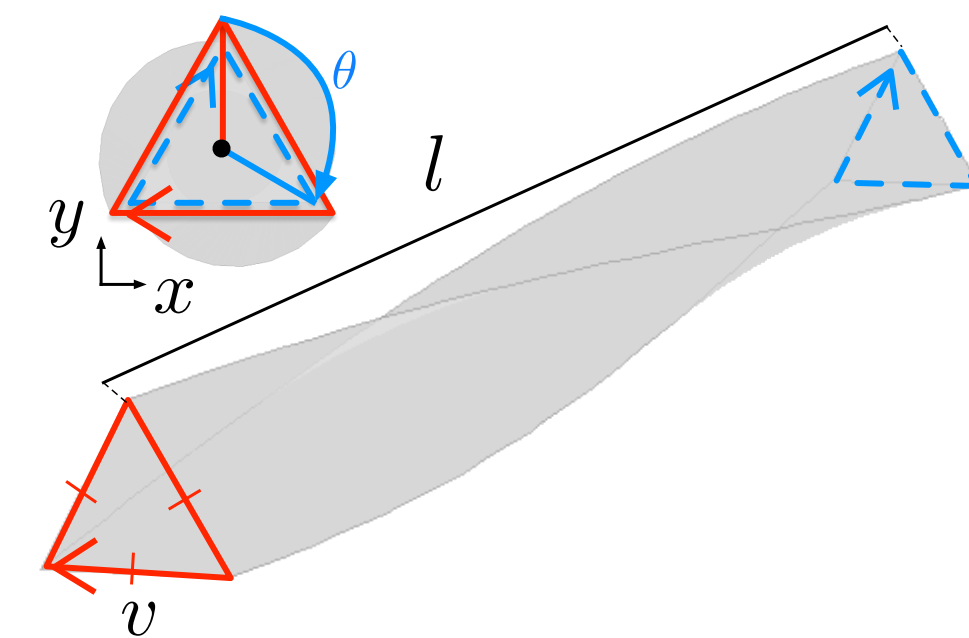
Dihedral group of regular convex polygons: D_p



$2p$ symmetries: p rotational + p reflection
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$$\begin{aligned}\psi_n &= e^{i\theta} \psi_{n+1} \\ \theta &= (2\pi/p)Z \\ Z &\in \pm \mathbb{Z}\end{aligned}$$



$$\begin{aligned}\psi_n &= e^{i\theta} \psi_{n+1} \\ \theta &\in \mathbb{R}\end{aligned}$$

Anyon

Twisted "anyon" microwave cavities

$$\mathcal{H}_p = \frac{2 \operatorname{Im} \left[\int \mathbf{B}_p(\vec{r}) \cdot \mathbf{E}_p^*(\vec{r}) d\tau \right]}{\sqrt{\int \mathbf{E}_p(\vec{r}) \cdot \mathbf{E}_p^*(\vec{r}) d\tau \int \mathbf{B}_p(\vec{r}) \cdot \mathbf{B}_p^*(\vec{r}) d\tau}}$$

PHYSICAL REVIEW D **108**, 052014 (2023)

Searching for ultralight axions with twisted cavity resonators of anyon rotational symmetry with bulk modes of nonzero helicity

J. F. Bourhill, E. C. I. Paterson^{id}, M. Goryachev, and M. E. Tobar^{id}

*Quantum Technologies and Dark Matter Labs, Department of Physics, University of Western Australia,
35 Stirling Highway, 6009 Crawley, Western Australia*

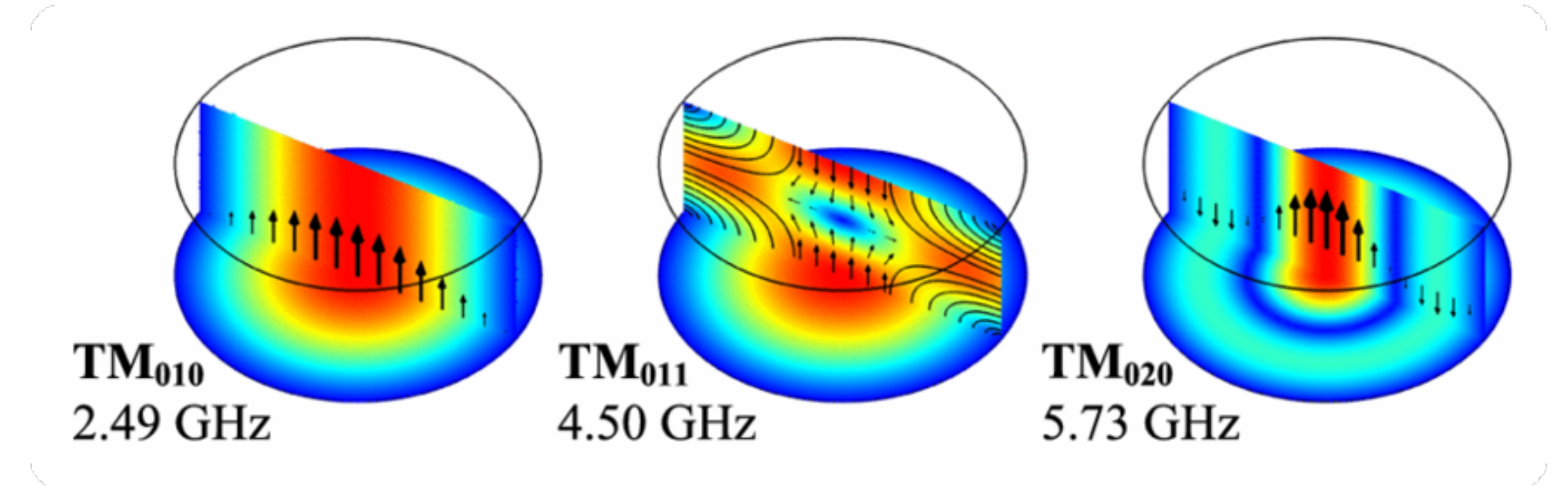
- 3D printed
- Measured mode frequencies to confirm simulation results



Cause of Helicity

Usual Haloscope Modes

$$\mathcal{H} = 0$$



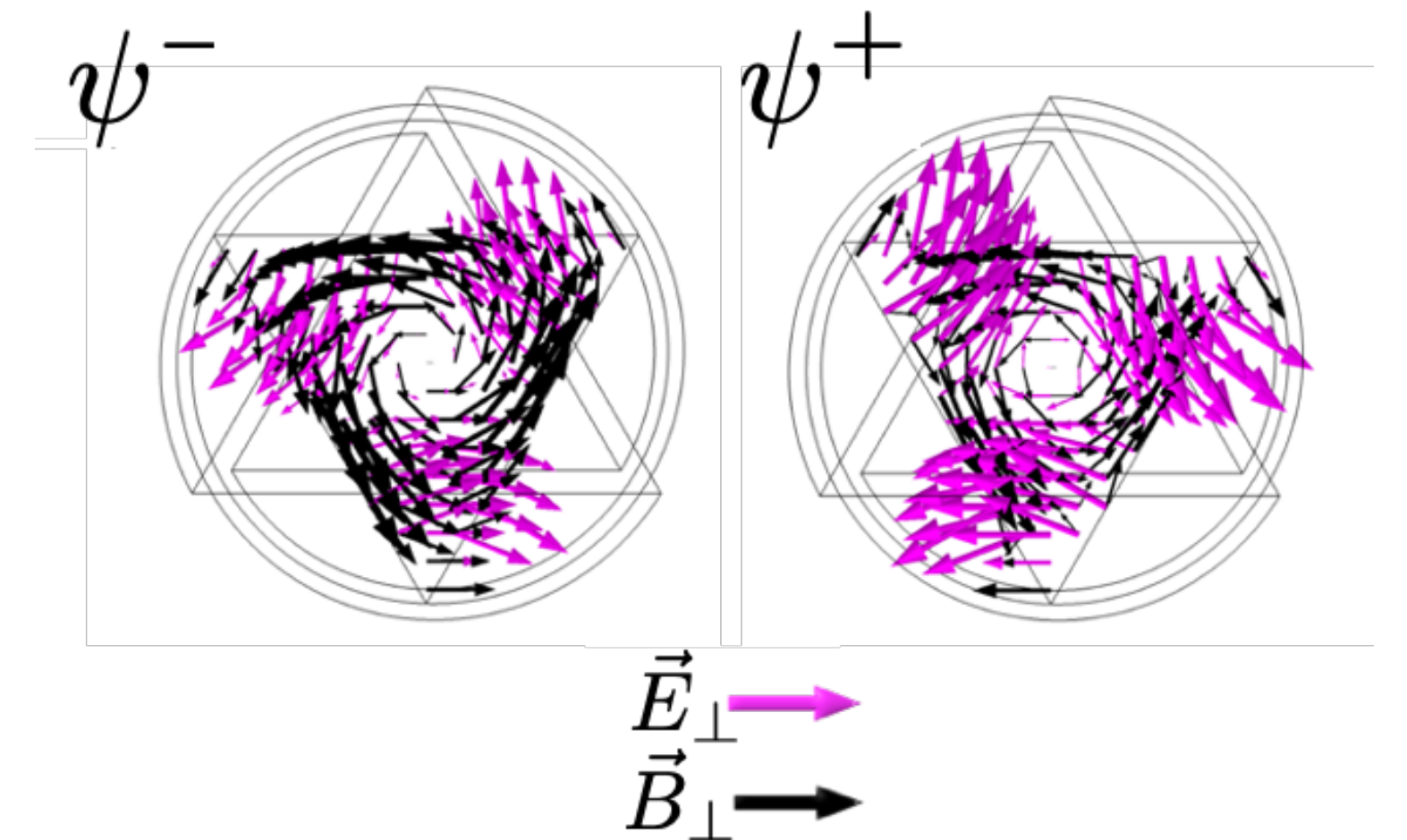
Twisted Anyon Cavity Modes

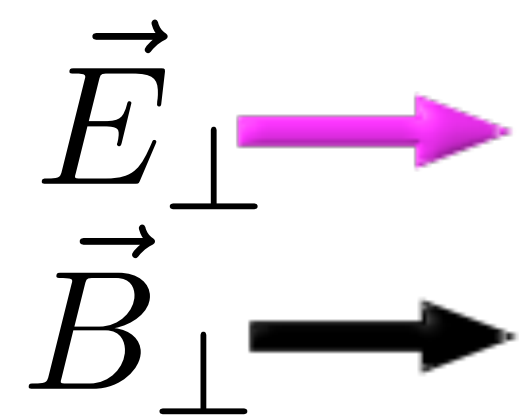
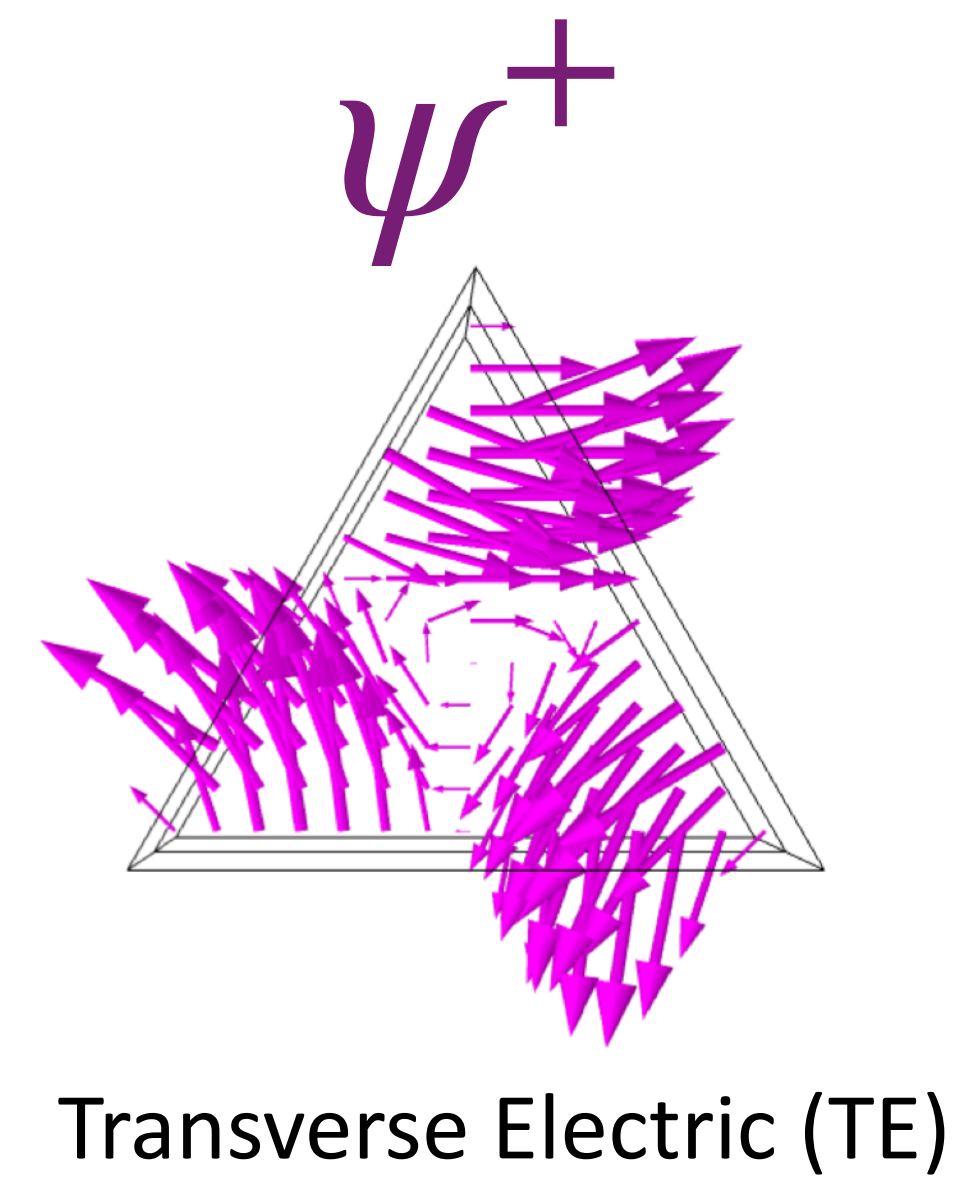
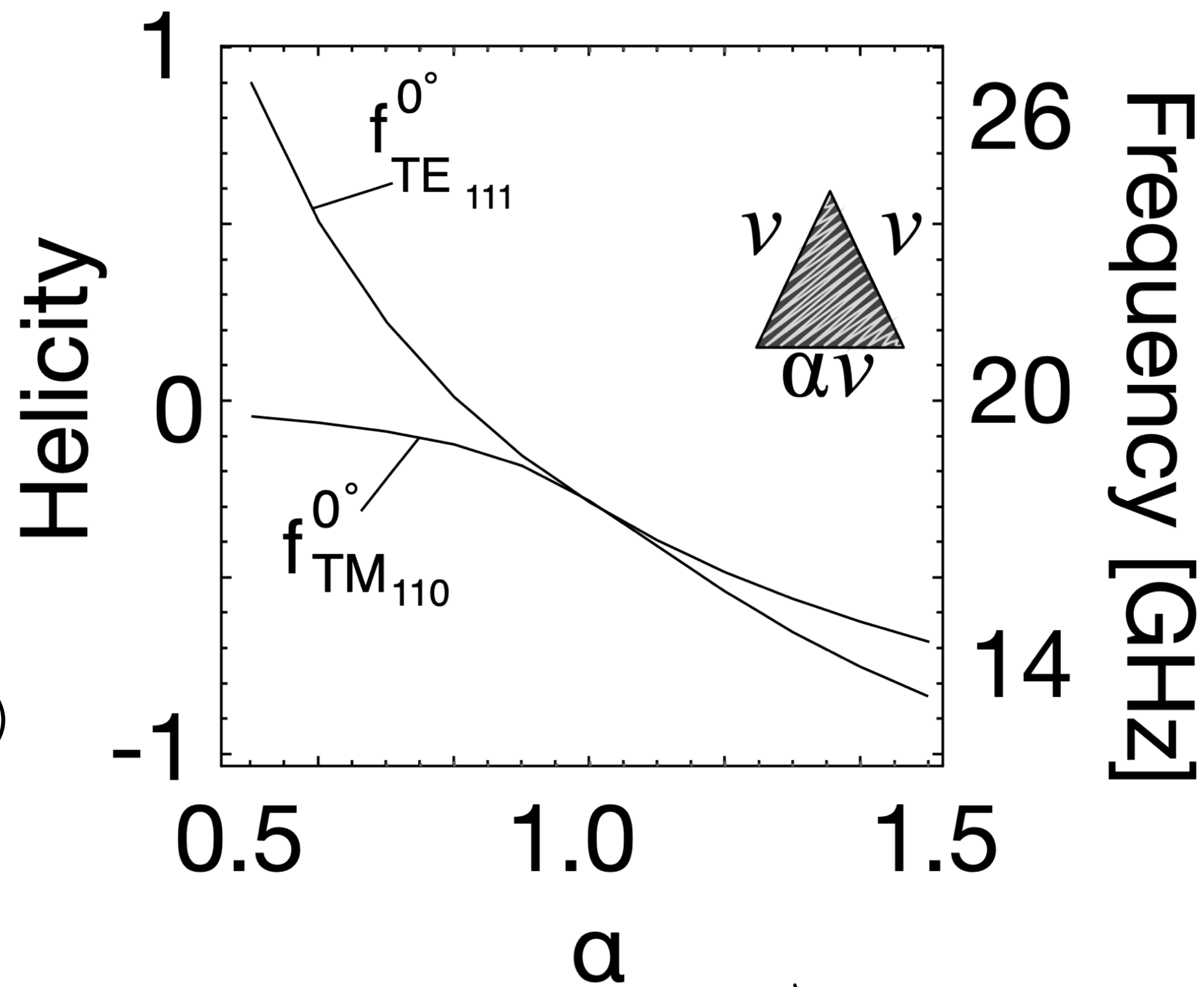
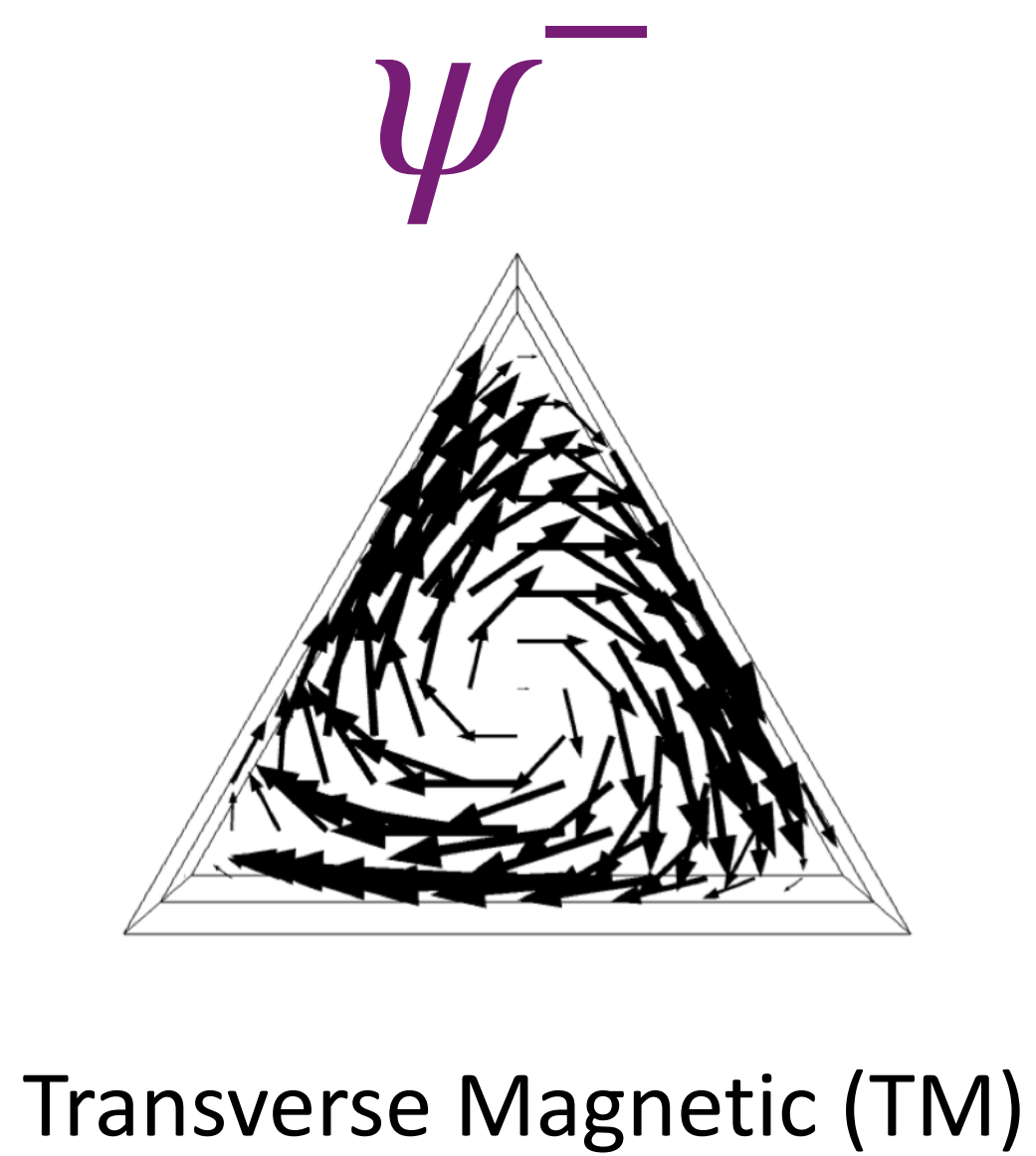
$$\mathcal{H} \neq 0$$

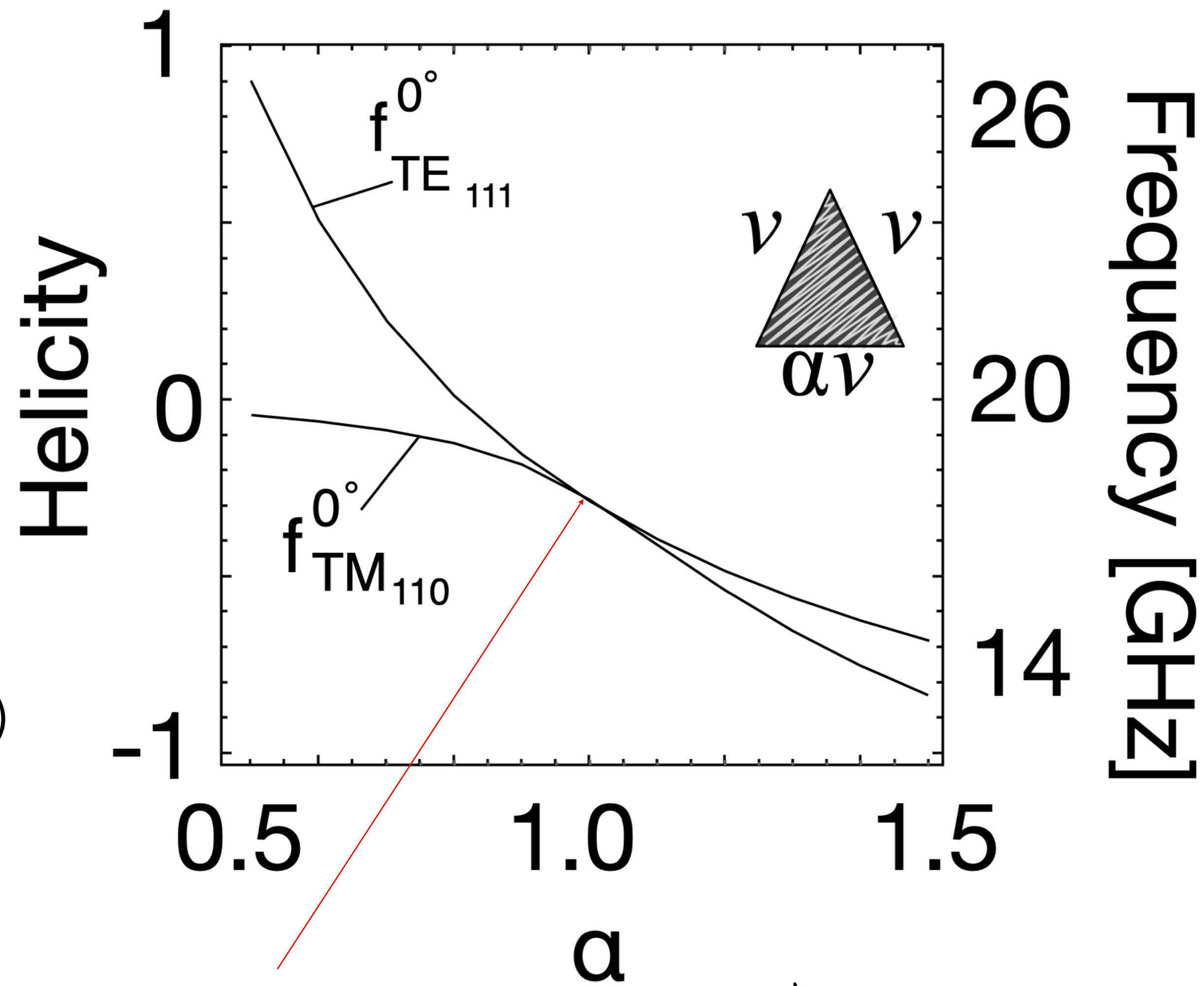
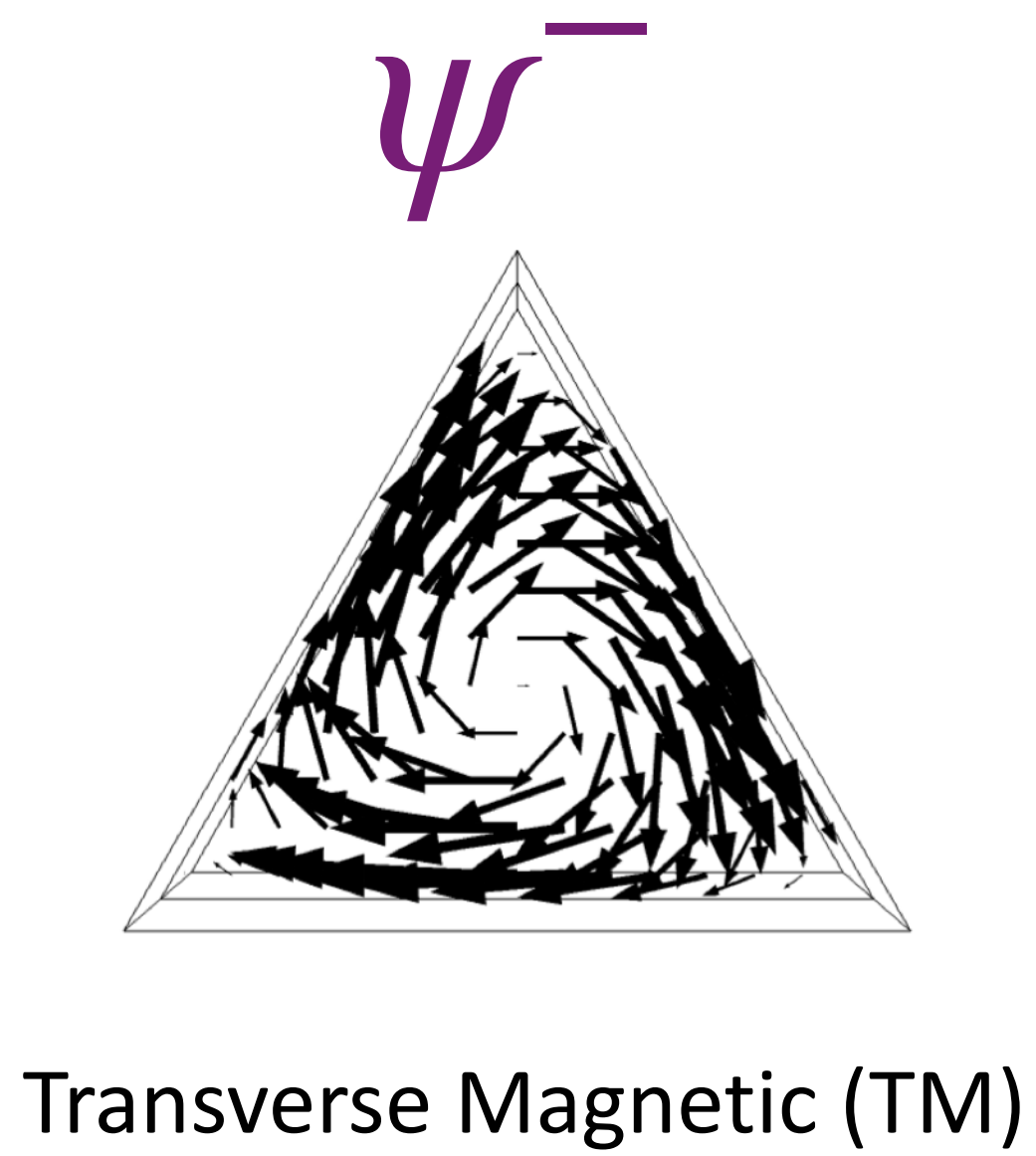
Circularly polarized

Two modes: TE & TM modes

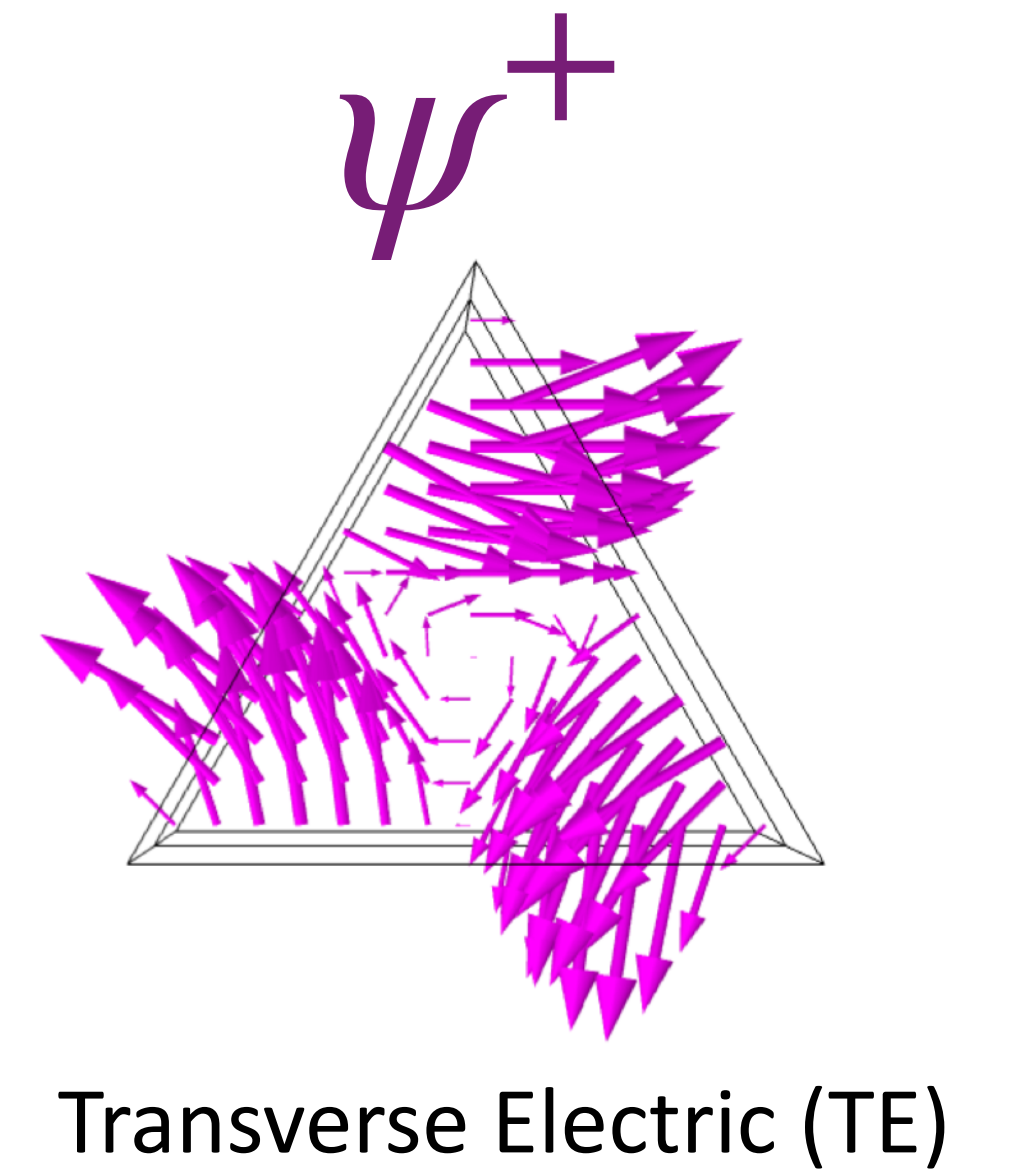
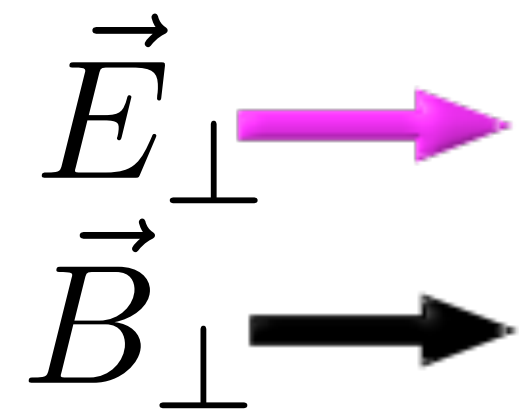
- Non-degenerate
- Magneto-electric coupling

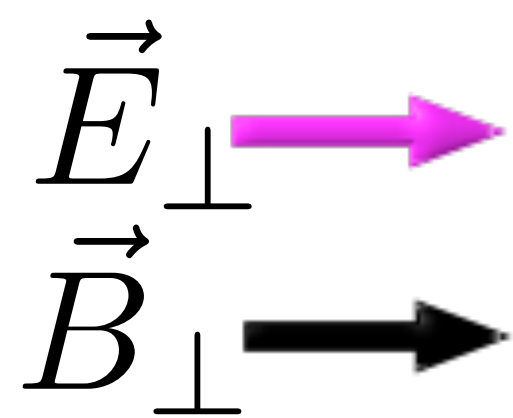
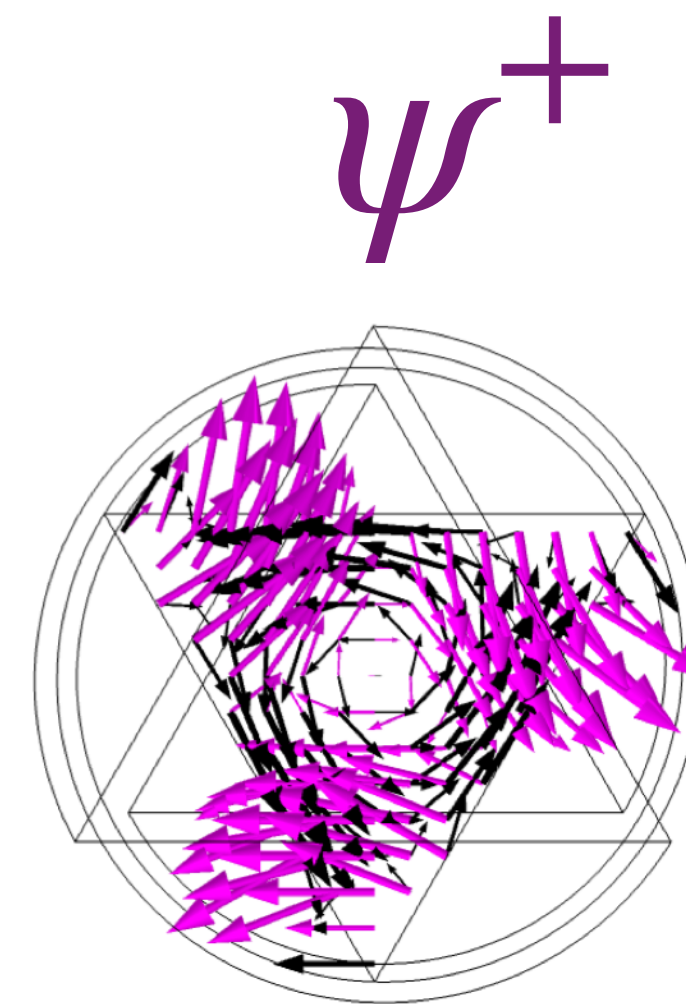
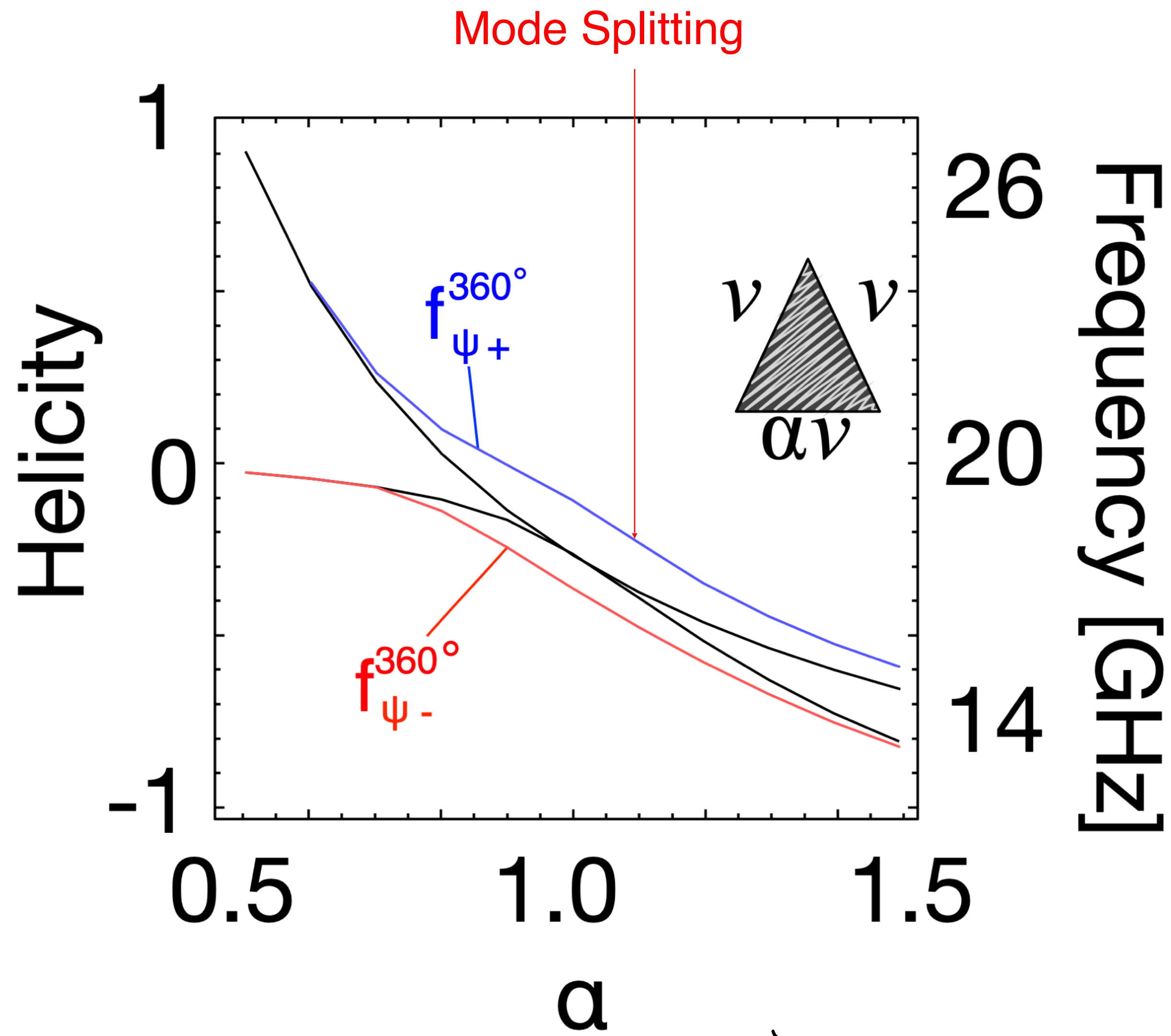
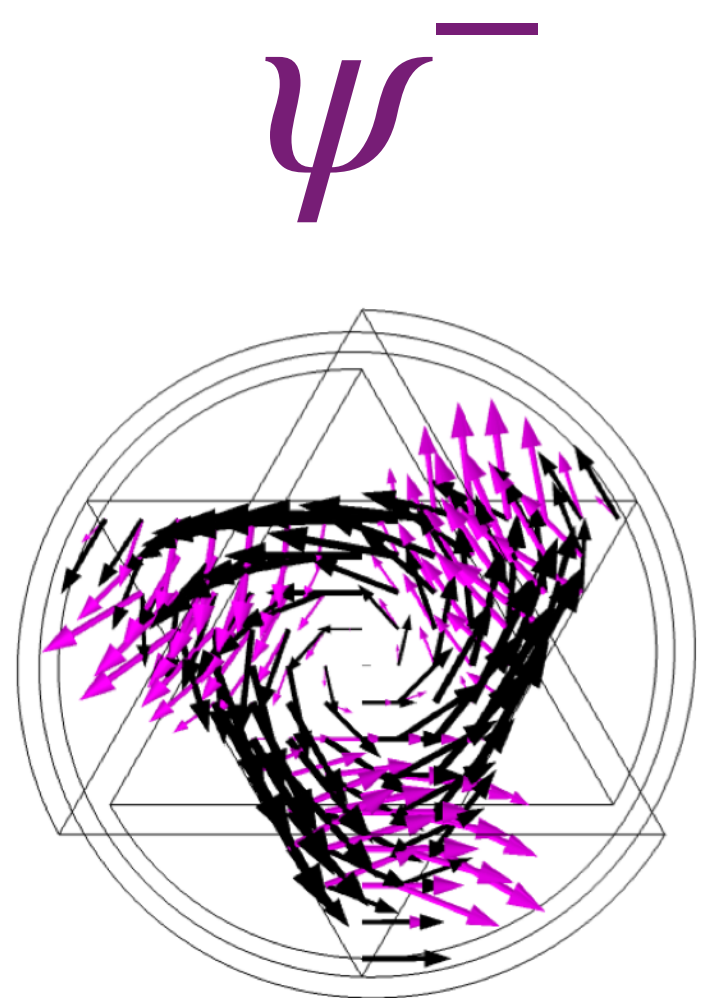


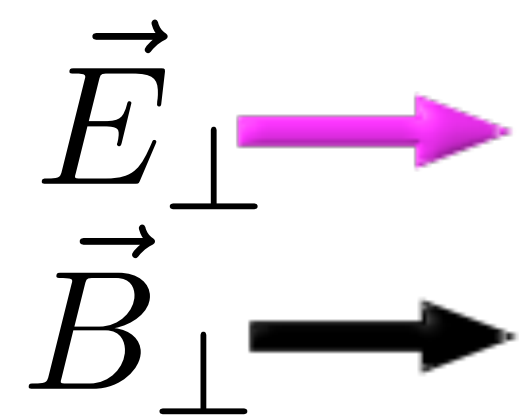
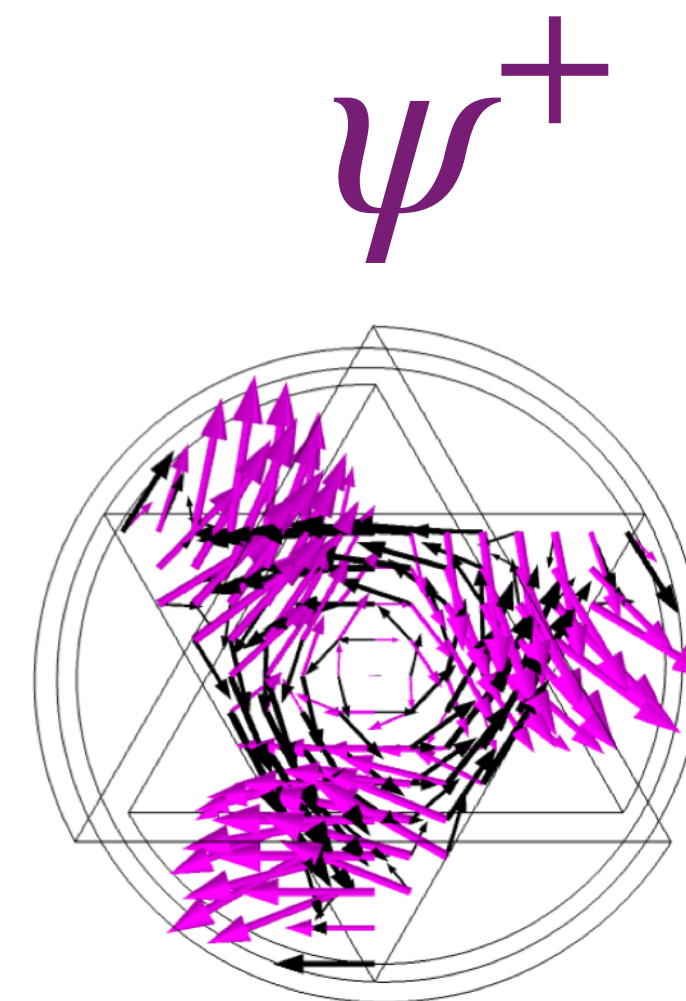
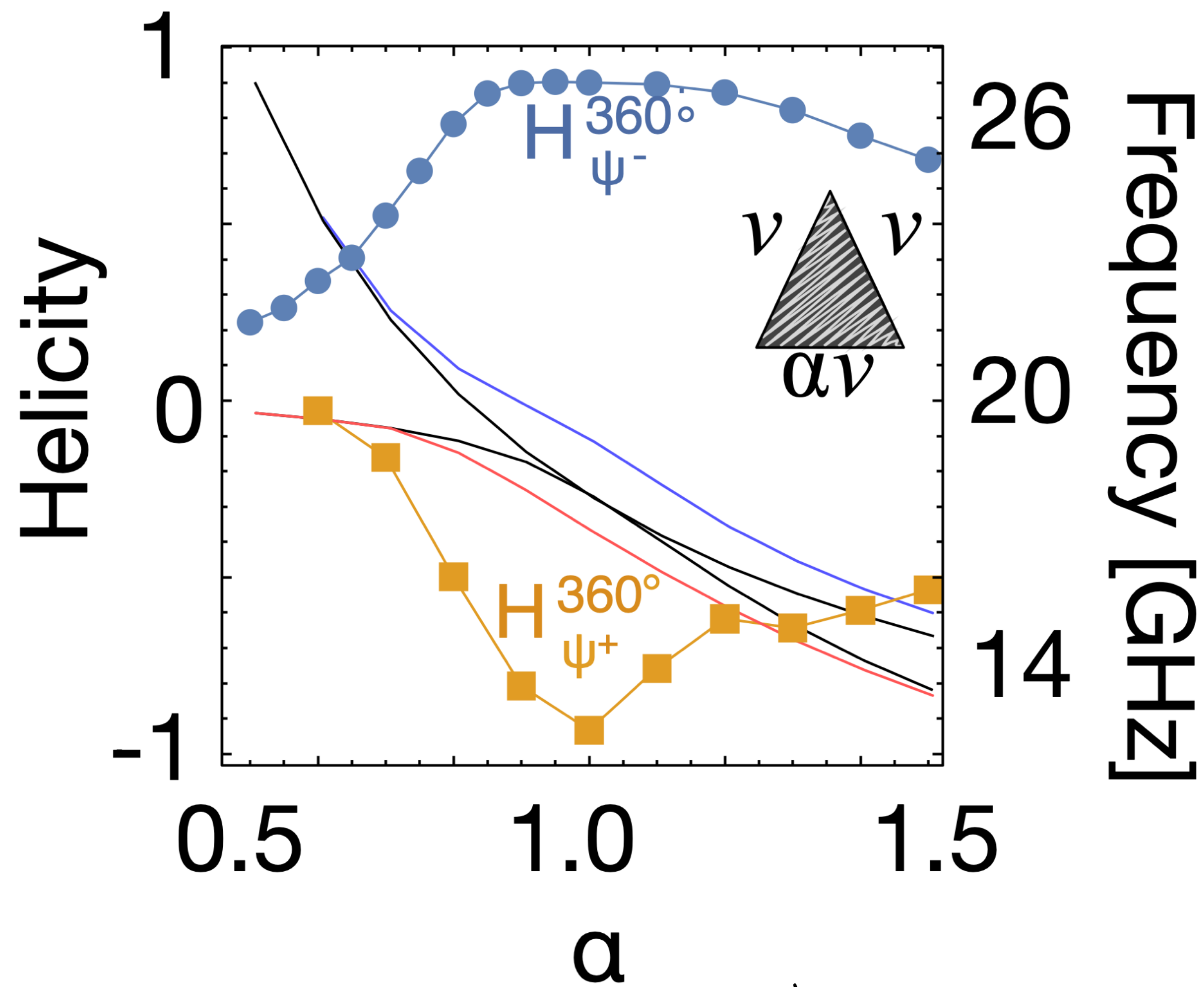
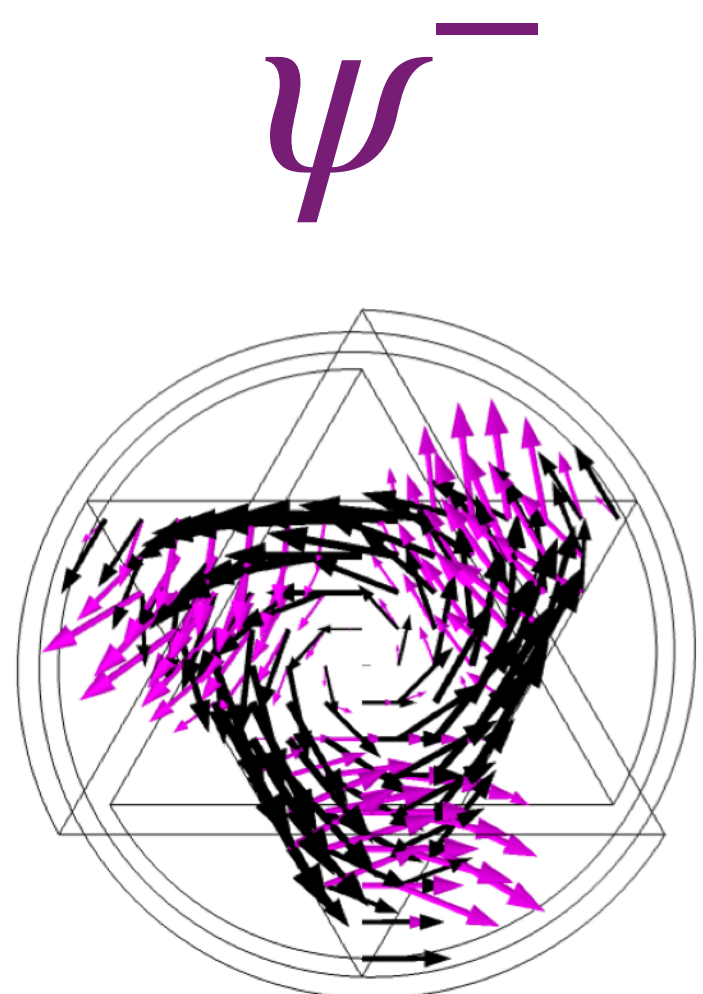




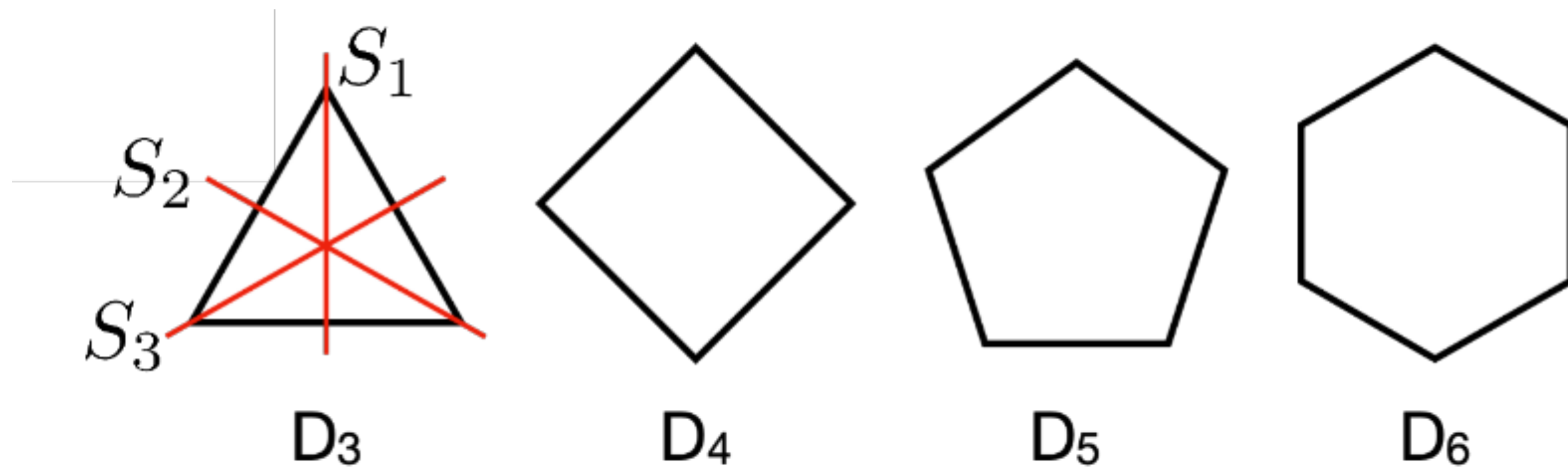
TE & TM modes
degenerate in frequency



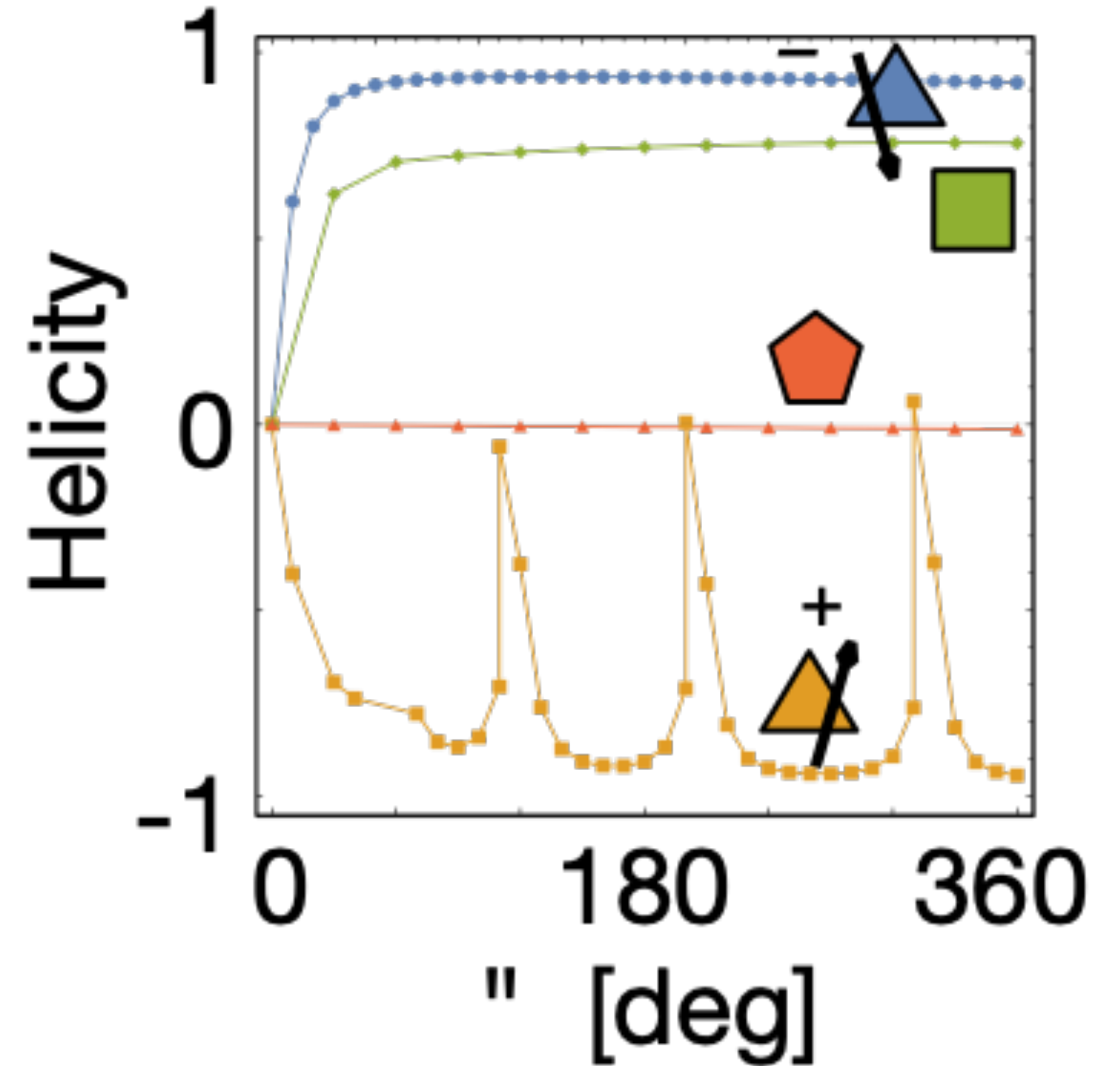


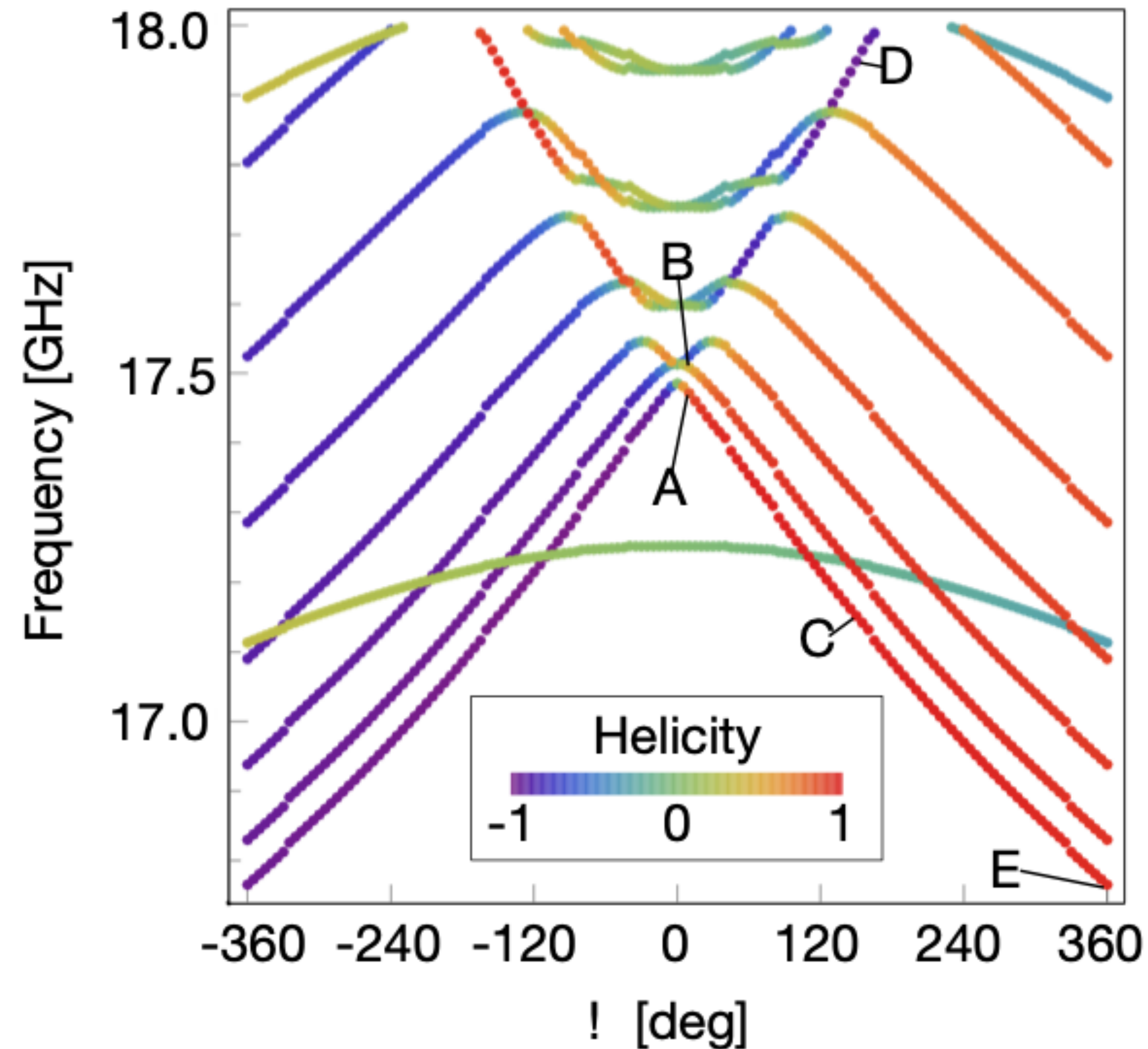


Cross-section



- Triangular cross-section shows greatest helicity (order unity)





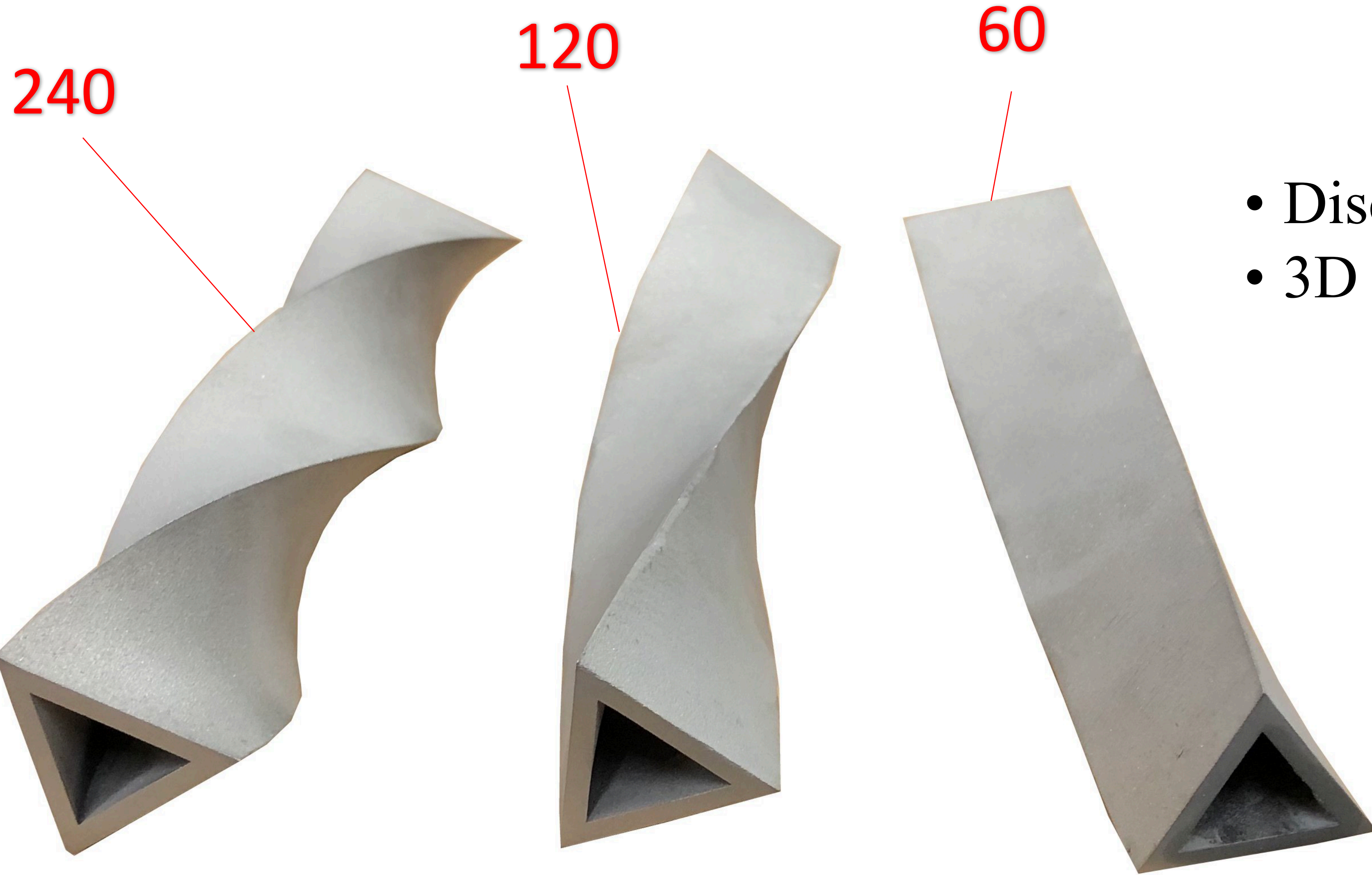
COMSOL

- Helicity is calculated via finite element analysis

$$H_p = \frac{2\text{Im}[\int \mathbf{B}_p(\vec{r}) \cdot \mathbf{E}_p^*(\vec{r}) d\tau]}{\sqrt{\int \mathbf{E}_p(\vec{r}) \cdot \mathbf{E}_p^* d\tau \int \mathbf{B}_p(\vec{r}) \cdot \mathbf{B}_p^*(\vec{r}) d\tau}}$$

- With twist
 - Eigenmodes tune in frequency
 - Helicity increases
- Confirm theoretical predictions

3D Printed Triangular Waveguide Cavities



- Discrete angles
- 3D printed aluminum

Simulation and Experimental Results Agree

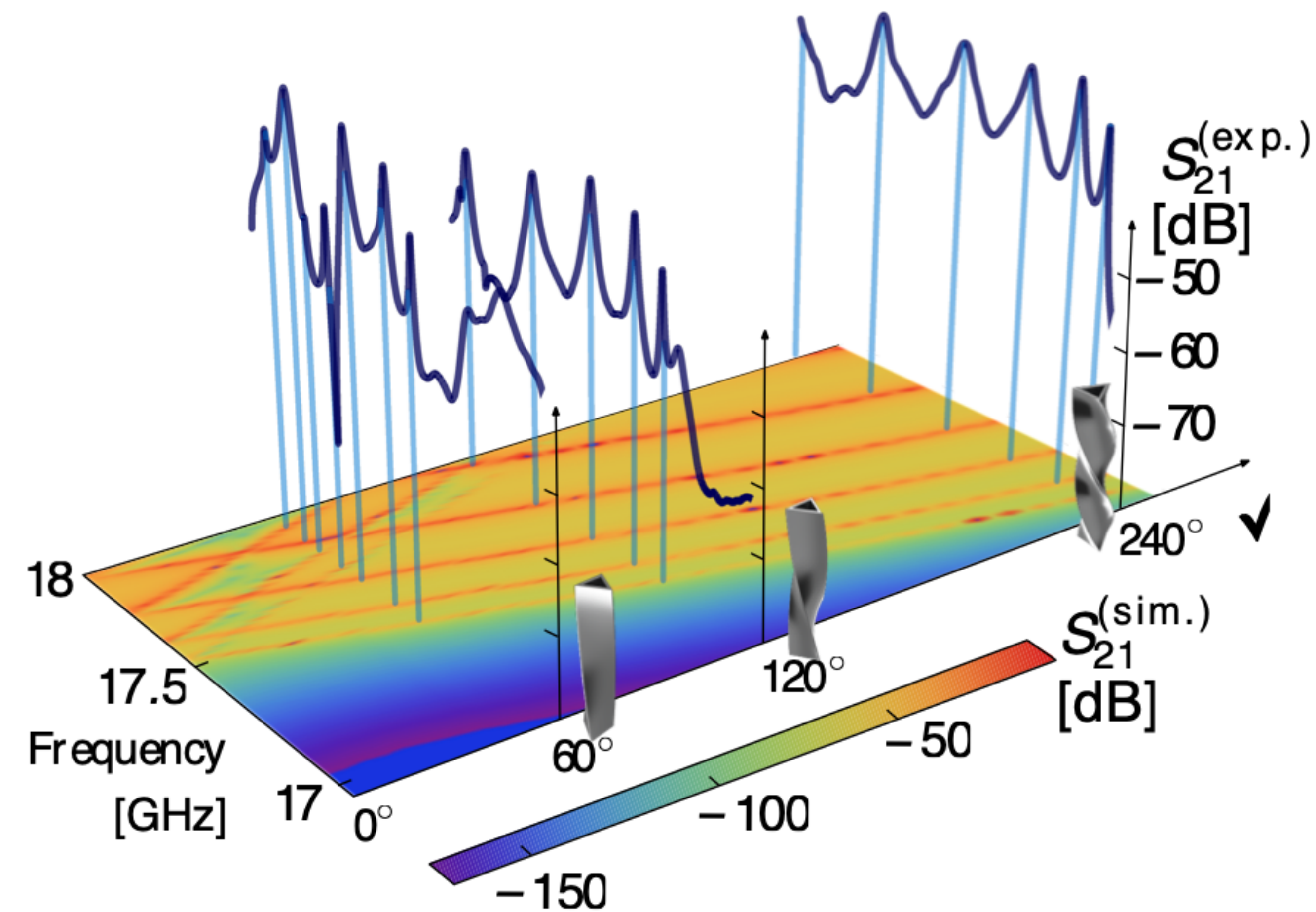
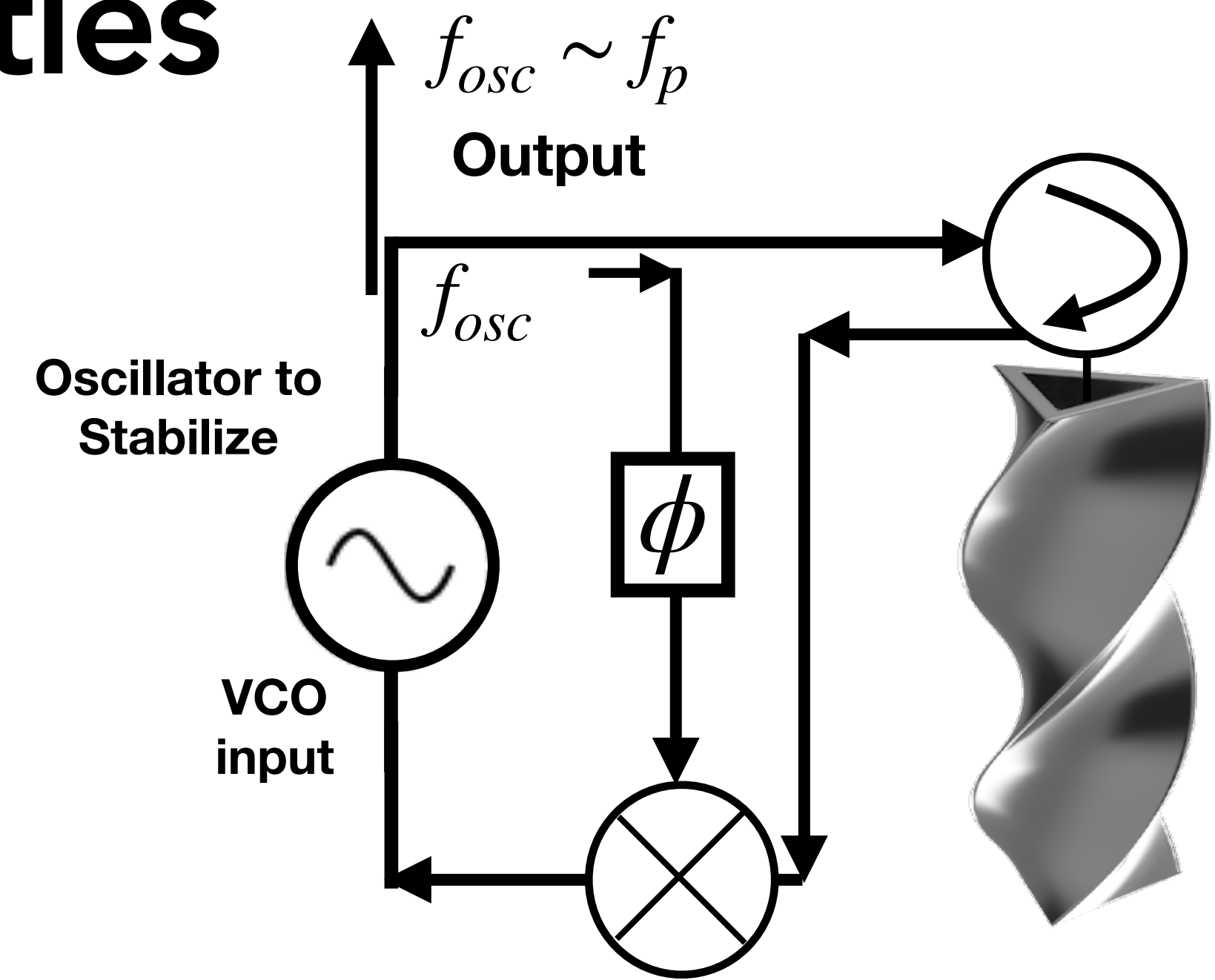
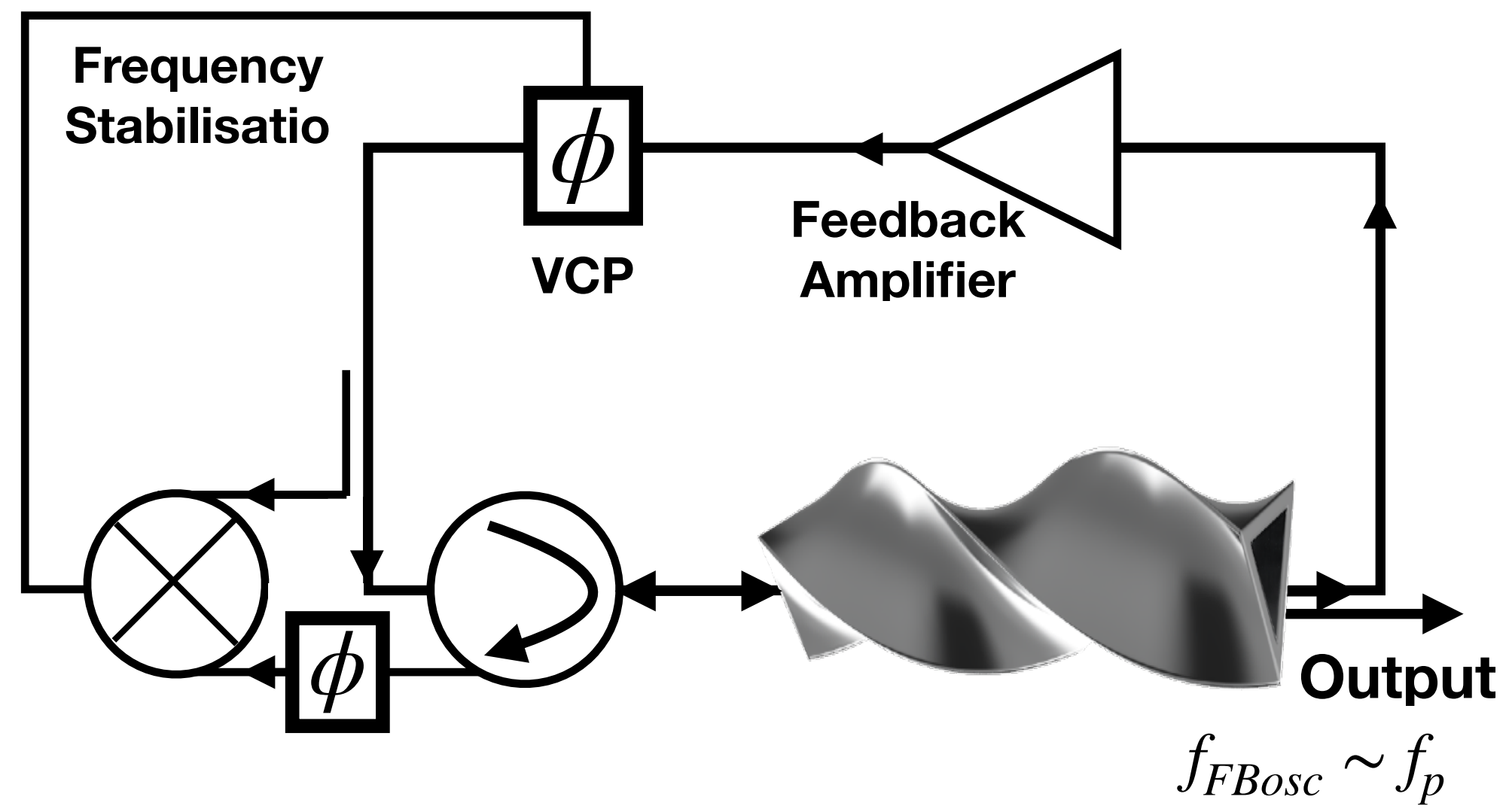


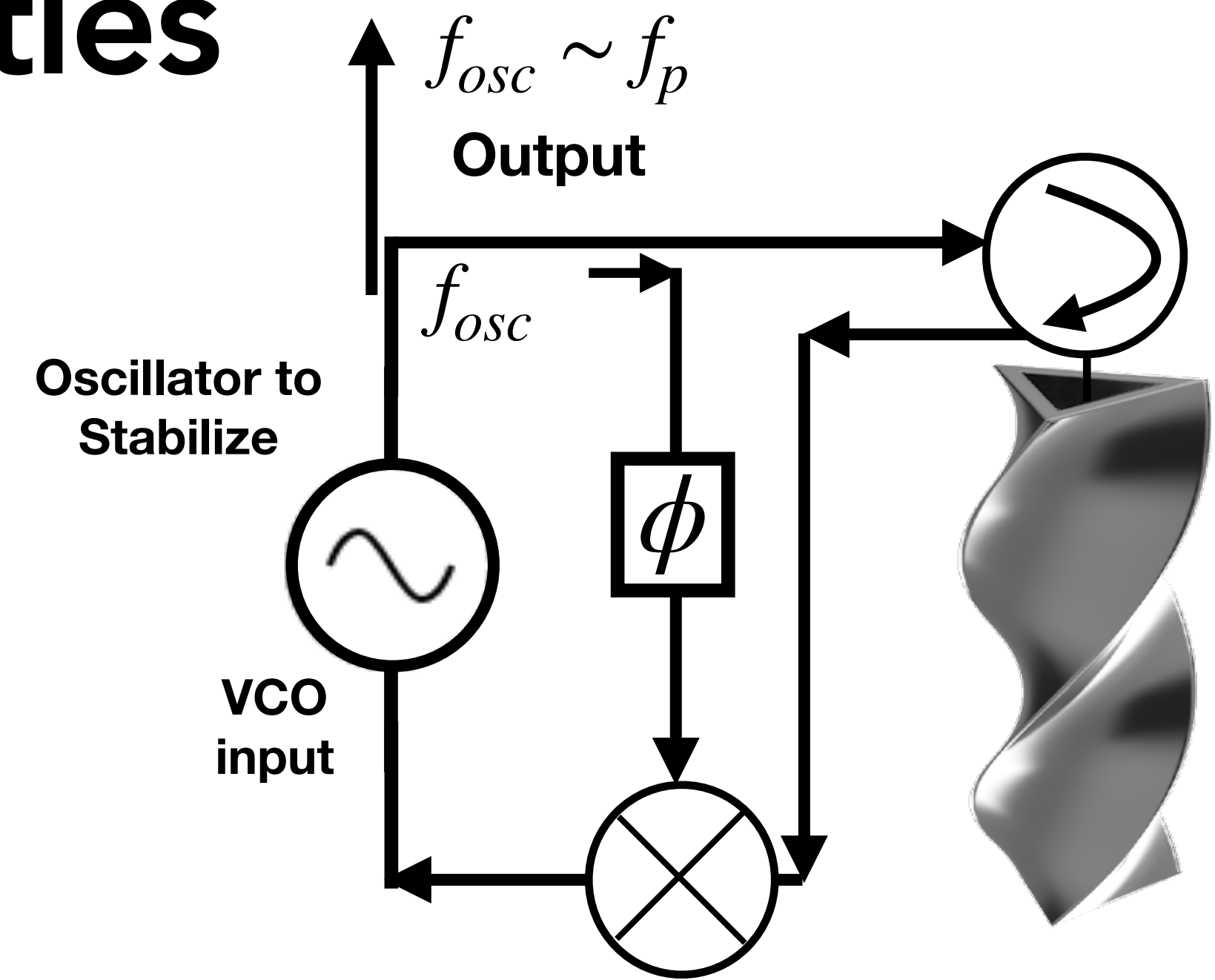
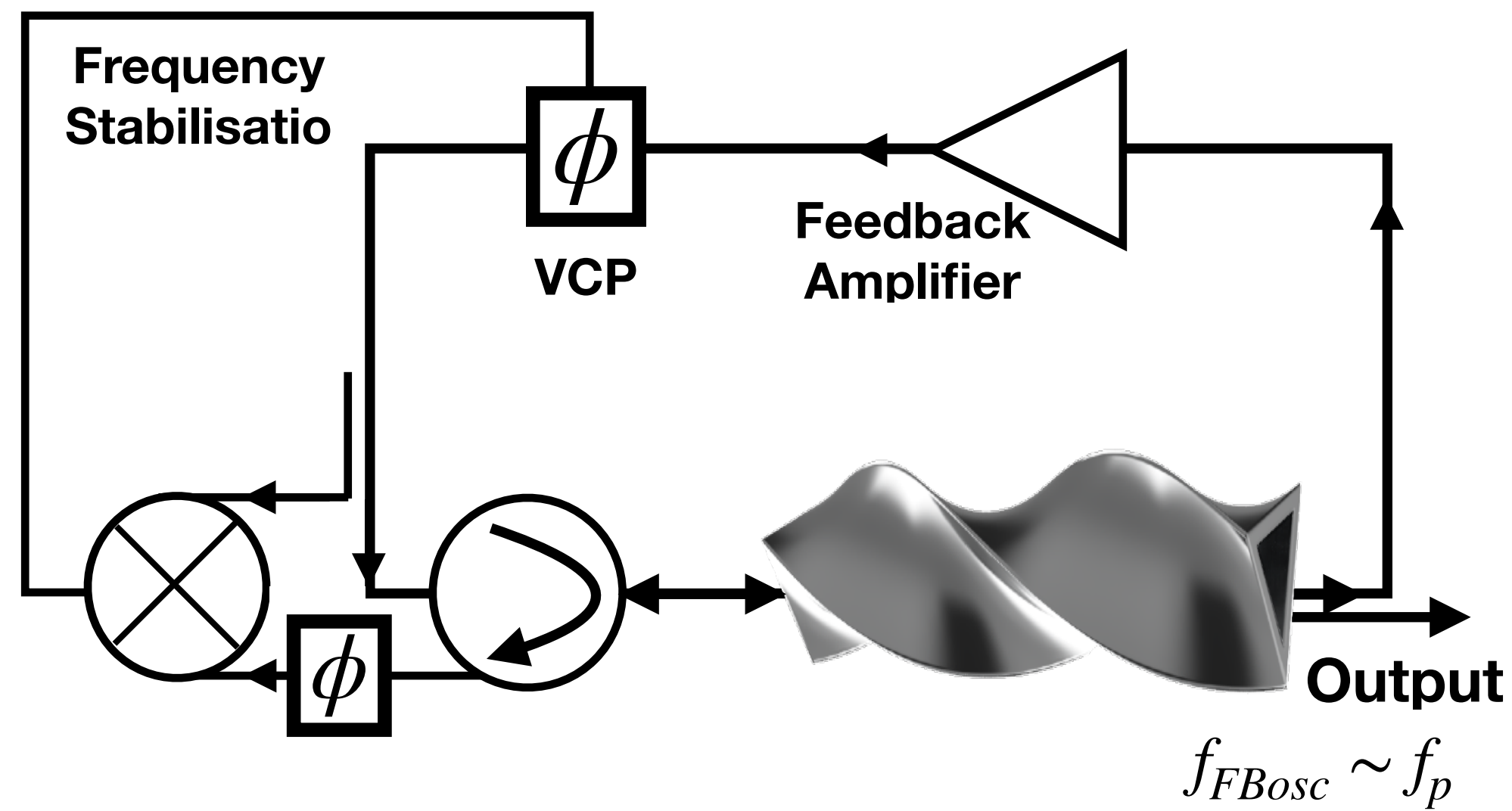
TABLE I. Simulated f_p , G_p and \mathcal{H}_p values for the greatest $|\mathcal{H}_p|$ modes for the linear and ring resonators with $l = 150$ mm, $\nu = 20$ mm, $\alpha = 1$ and $\theta = 120^\circ$.

| Resonator | f_p (GHz) | G_p (Ω) | \mathcal{H}_p |
|-----------|-------------|--------------------|-----------------|
| Linear | 17.044 | 1950 | -0.931 |
| Linear | 17.688 | 1920 | 0.8796 |
| Ring | 17.022 | 6200 | -0.931 |
| Ring | 17.814 | 7290 | 0.954 |

Twisted "anyon" microwave cavities

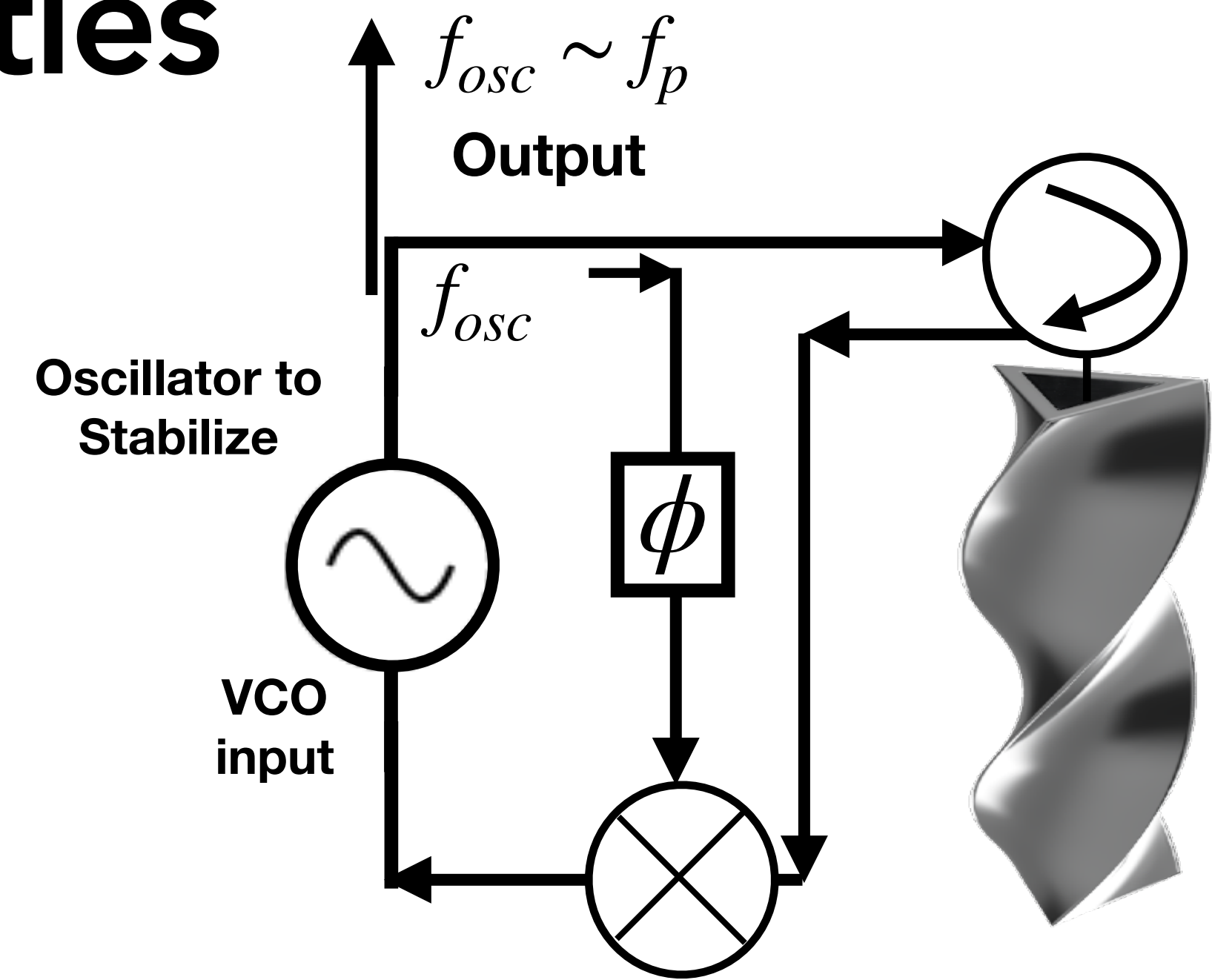
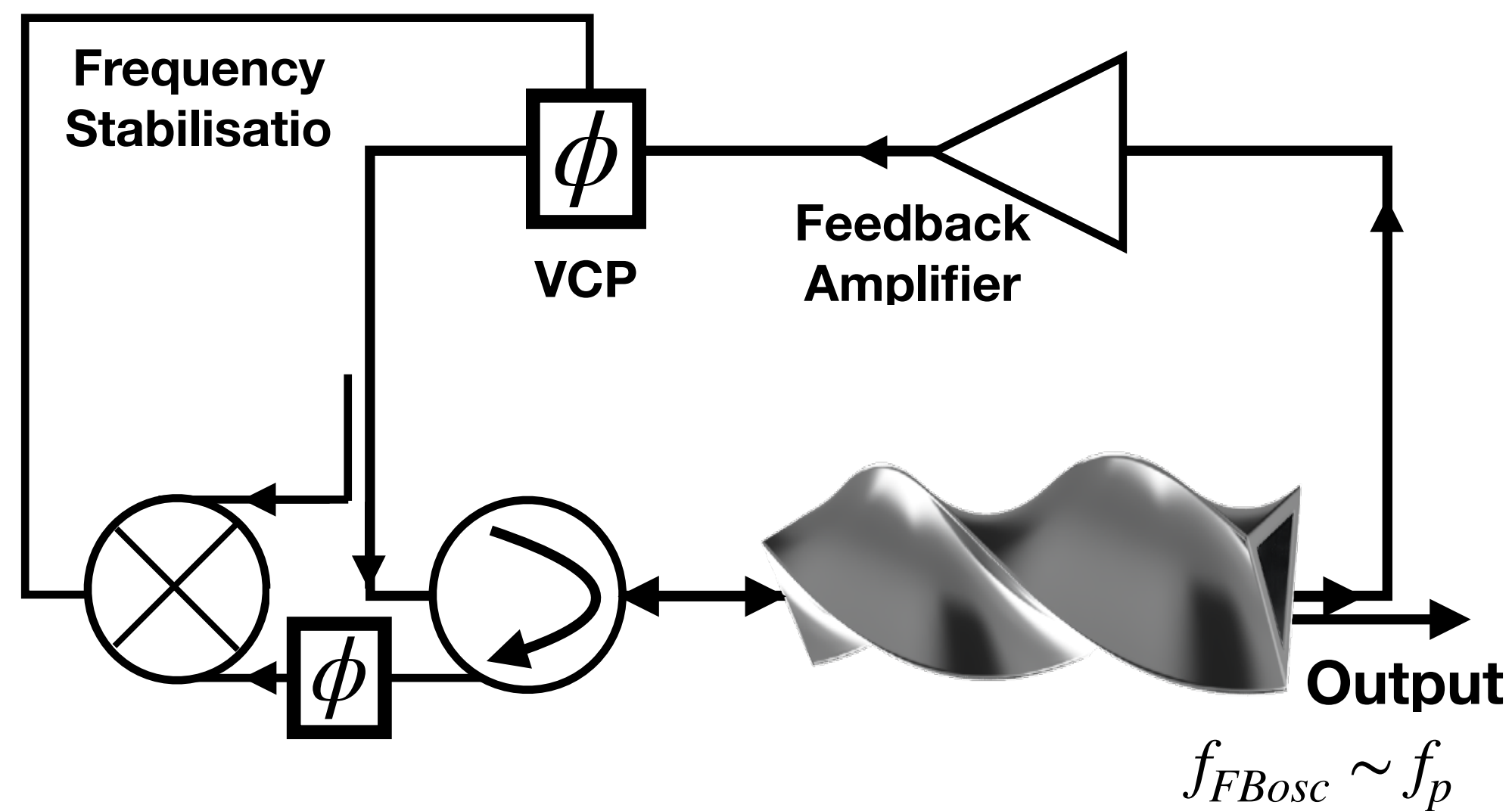


Twisted "anyon" microwave cavities



$$SNR = \frac{g_a \gamma \beta_p |\mathcal{H}_p|}{\sqrt{2}(1 + \beta_p)} \frac{Q_p}{\sqrt{1 + 4Q_p^2 \left(\frac{\omega_a}{\omega_p}\right)^2}} \frac{\left(\frac{10^6 t}{\omega_a}\right)^{\frac{1}{4}} \sqrt{\rho_a c^3}}{\omega_p \sqrt{S_{am}}}$$

Twisted "anyon" microwave cavities



$$SNR = \frac{g_{a\gamma\gamma} \beta_p |\mathcal{H}_p| Q_p \left(\frac{10^6 t}{\omega_a} \right)^{\frac{1}{4}} \sqrt{\rho_a c^3}}{\sqrt{2(1 + \beta_p)} \sqrt{1 + 4Q_p^2 \left(\frac{\omega_a}{\omega_p} \right)^2} \omega_p \sqrt{S_{am}}}$$

Axon Photon Coupling

Microwave Probe Coupling

Helicity

Q factor

Axon Frequency

Measurement time (1 week)

Cold dark matter density ($8 \times 10^{-22} \text{kgm}^{-3}$)

Speed of light ($3 \times 10^8 \text{ms}^{-1}$)

Cavity frequency (1 GHz)

Amplitude noise (-160 dBcHz⁻¹)

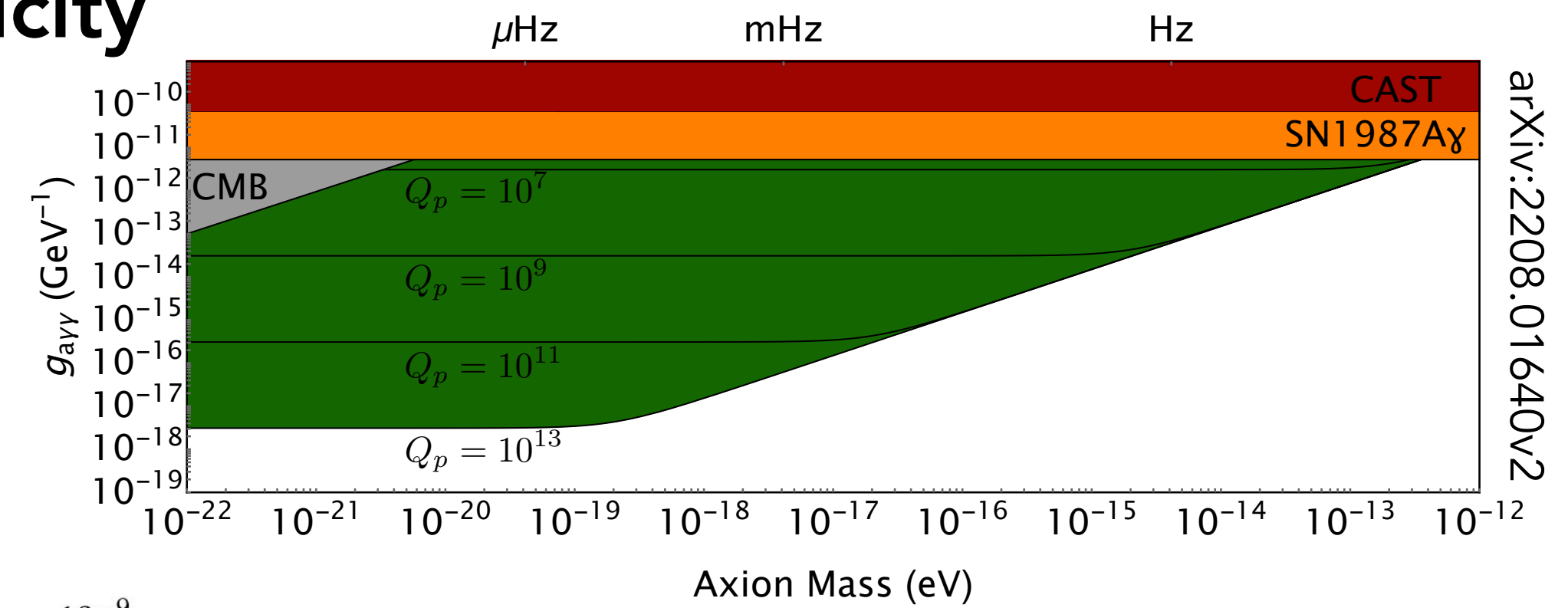
Twisted “anyon” microwave cavities

Dark matter detection in a single mode thanks to helicity

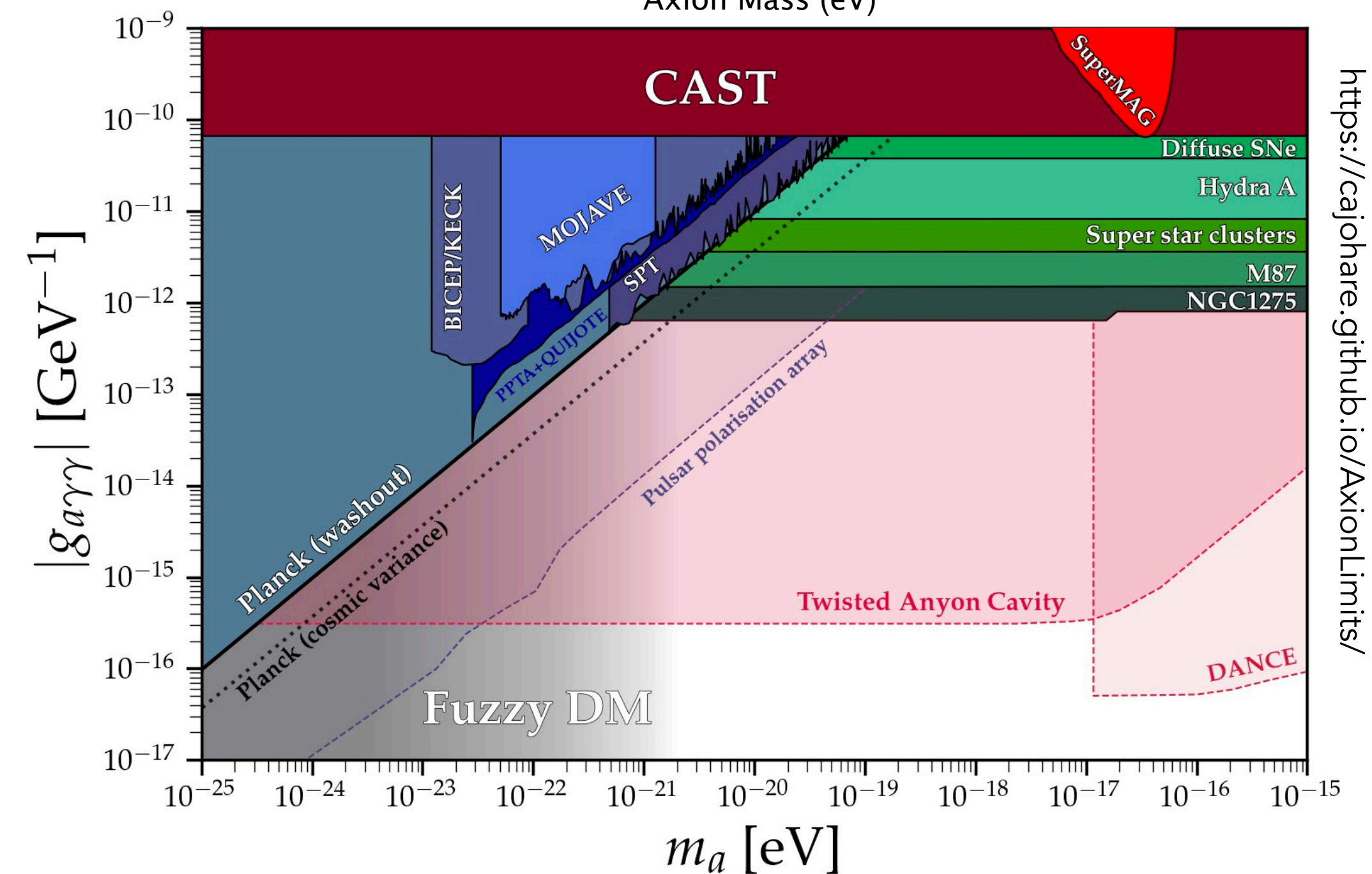
Twisted "anyon" microwave cavities

Dark matter detection in a single mode thanks to helicity

- Accesses an axion mass range very difficult to search



arXiv:2208.01640v2

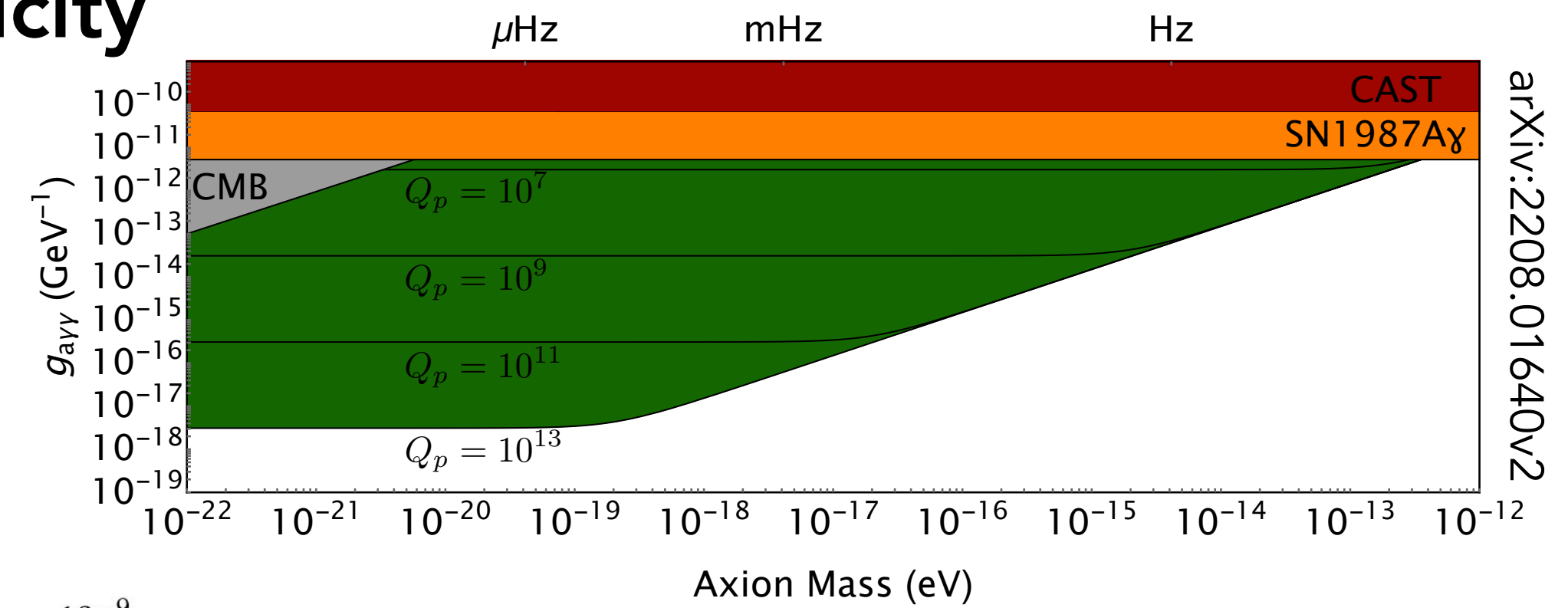


<https://cajohare.github.io/AxionLimits/>

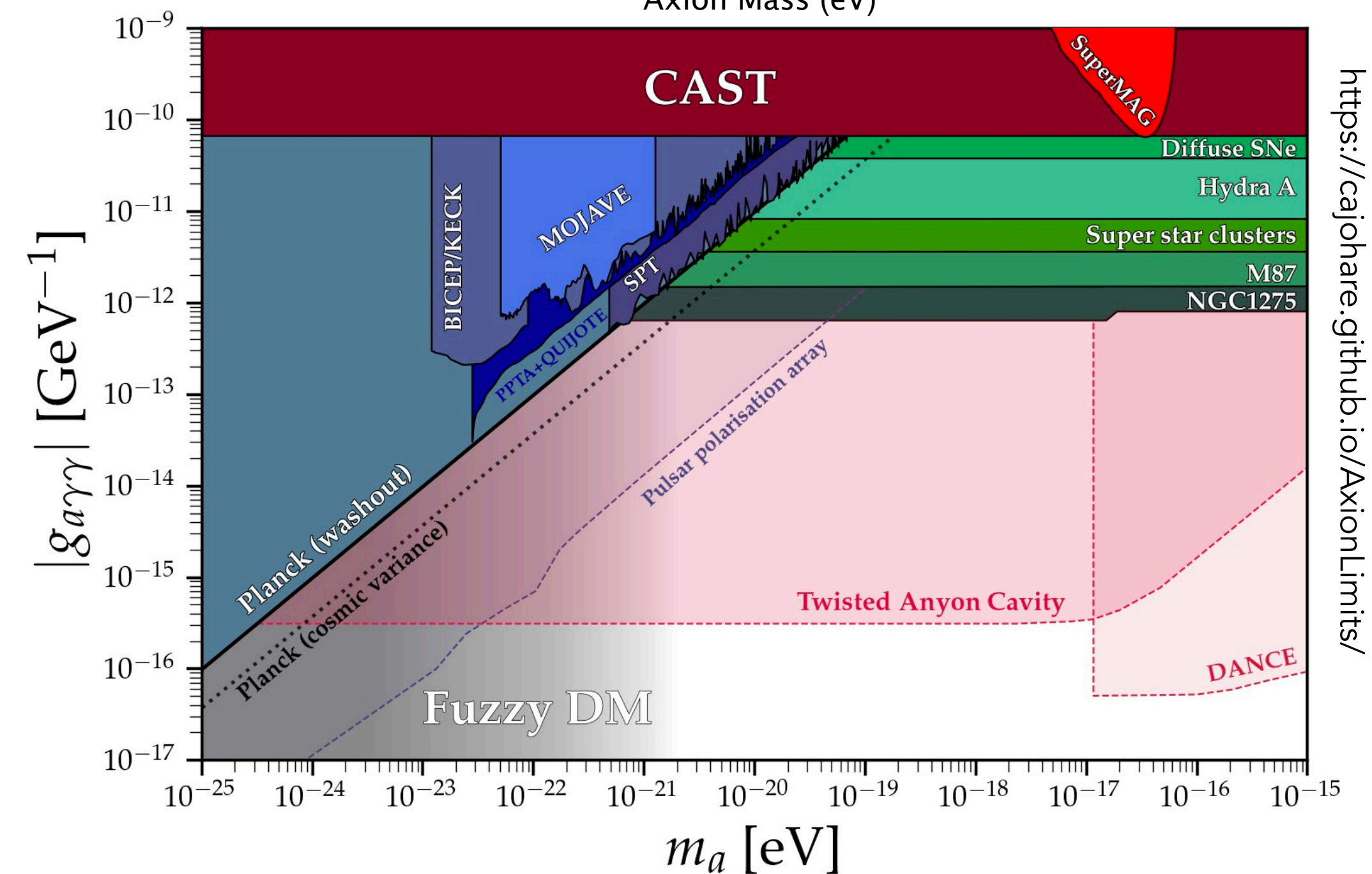
Twisted "anyon" microwave cavities

Dark matter detection in a single mode thanks to helicity

- Accesses an axion mass range very difficult to search
- **No external magnetic field needed**



arXiv:2208.01640v2

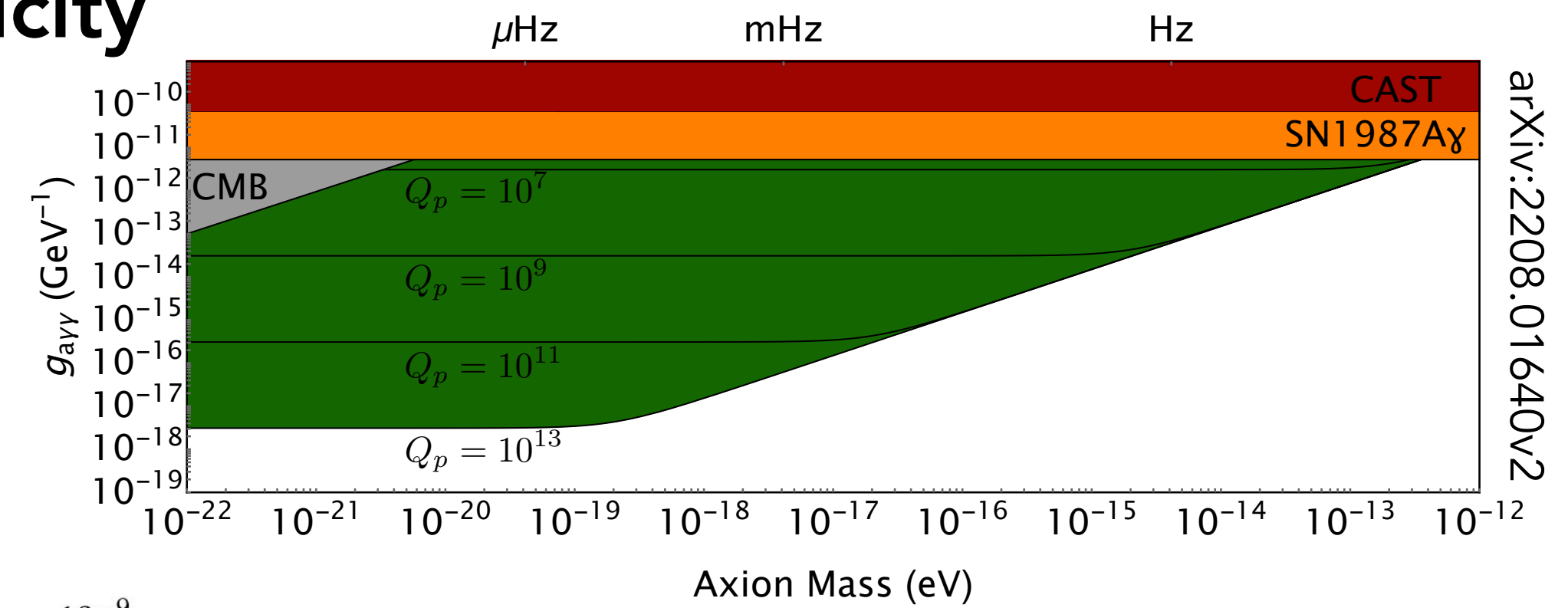


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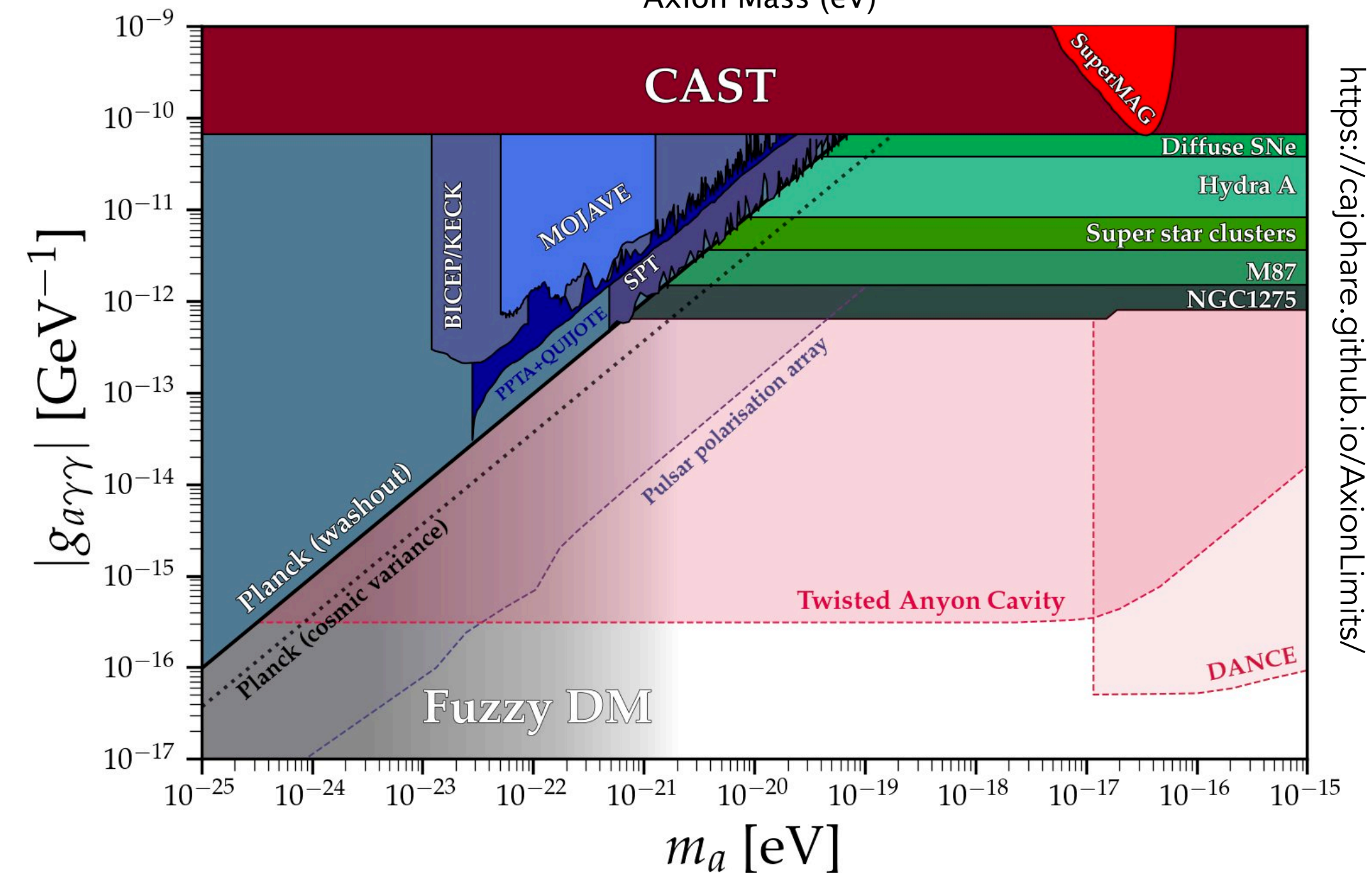
Twisted "anyon" microwave cavities

Dark matter detection in a single mode thanks to helicity

- Accesses an axion mass range very difficult to search
- **No external magnetic field needed**
- Ability to use **superconducting** materials



arXiv:2208.01640v2

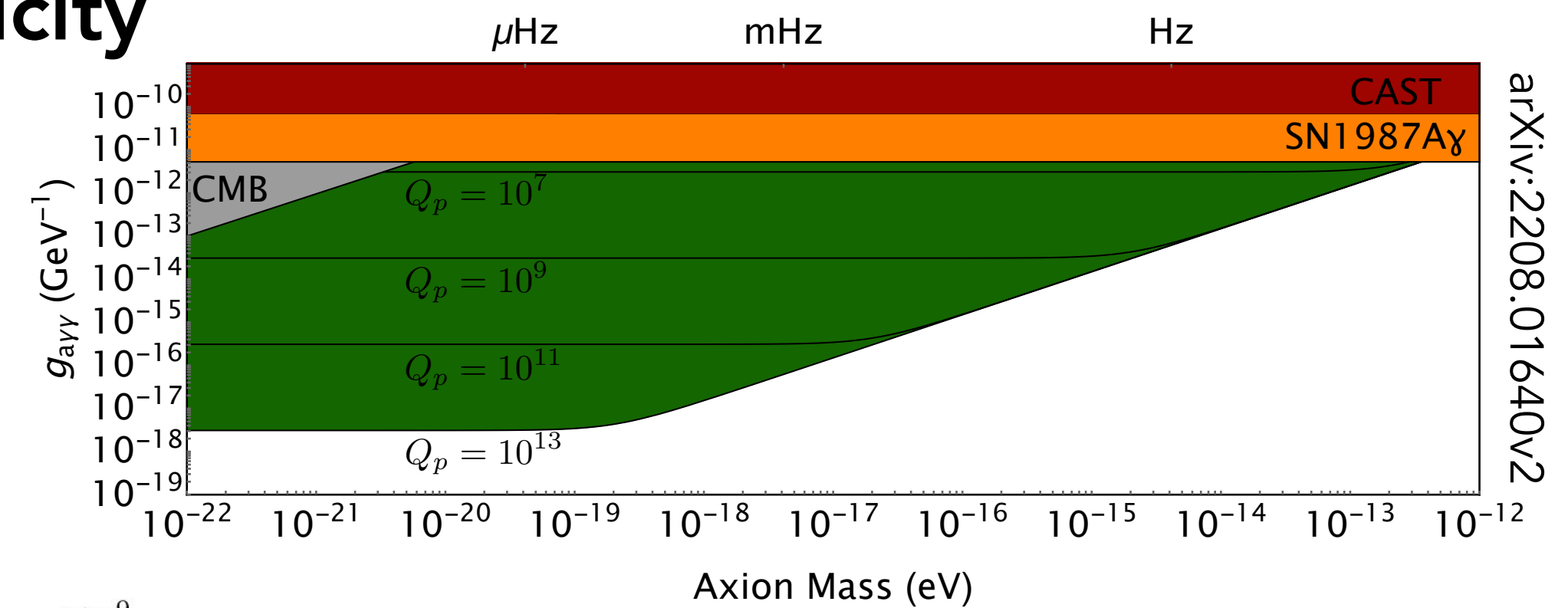


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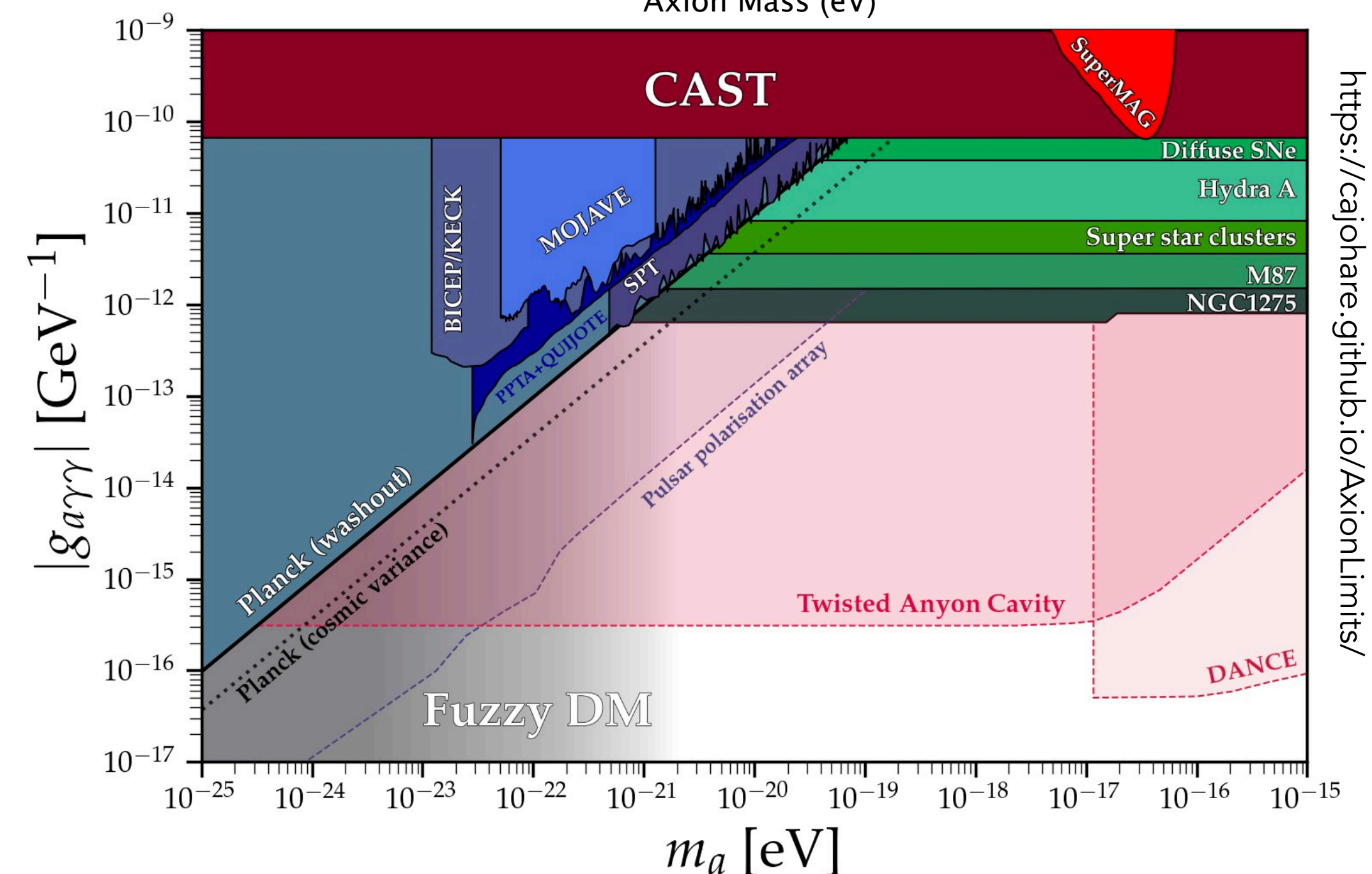
Twisted "anyon" microwave cavities

Dark matter detection in a single mode thanks to helicity

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- Ability to use **superconducting** materials
- Allows high Q-factors and improved sensitivity



arXiv:2208.01640v2

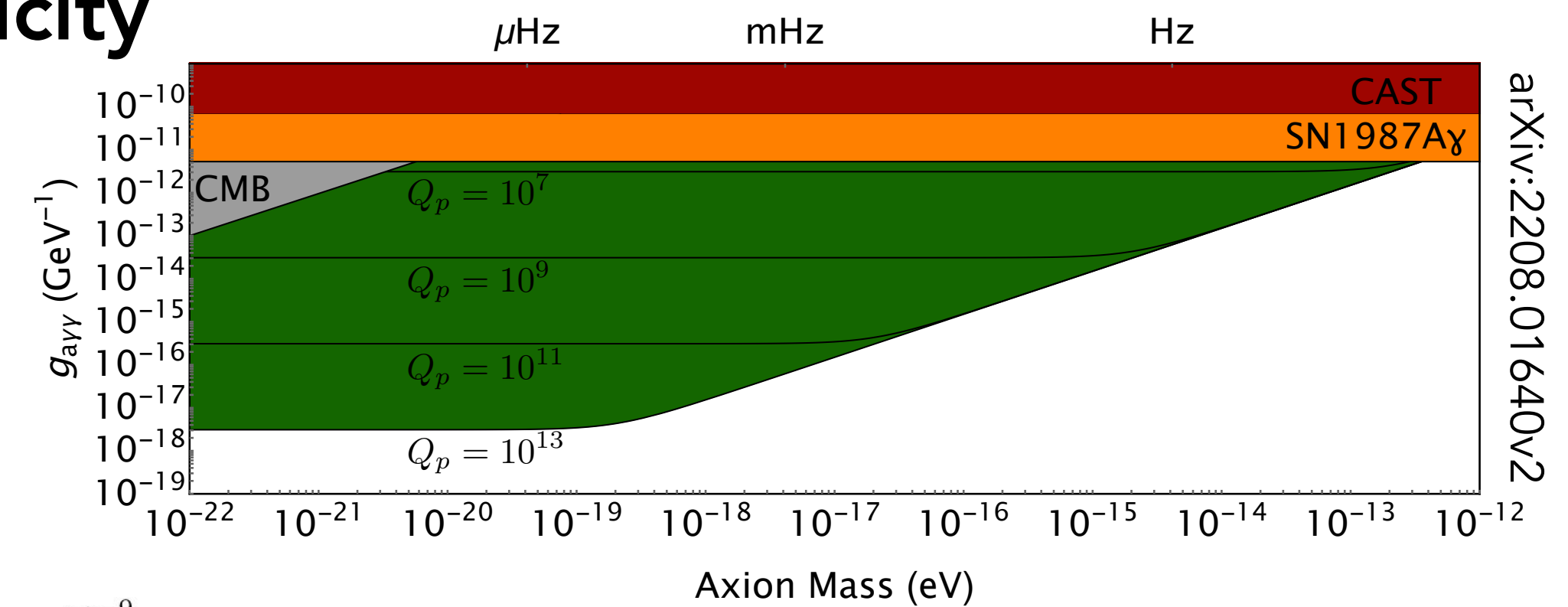


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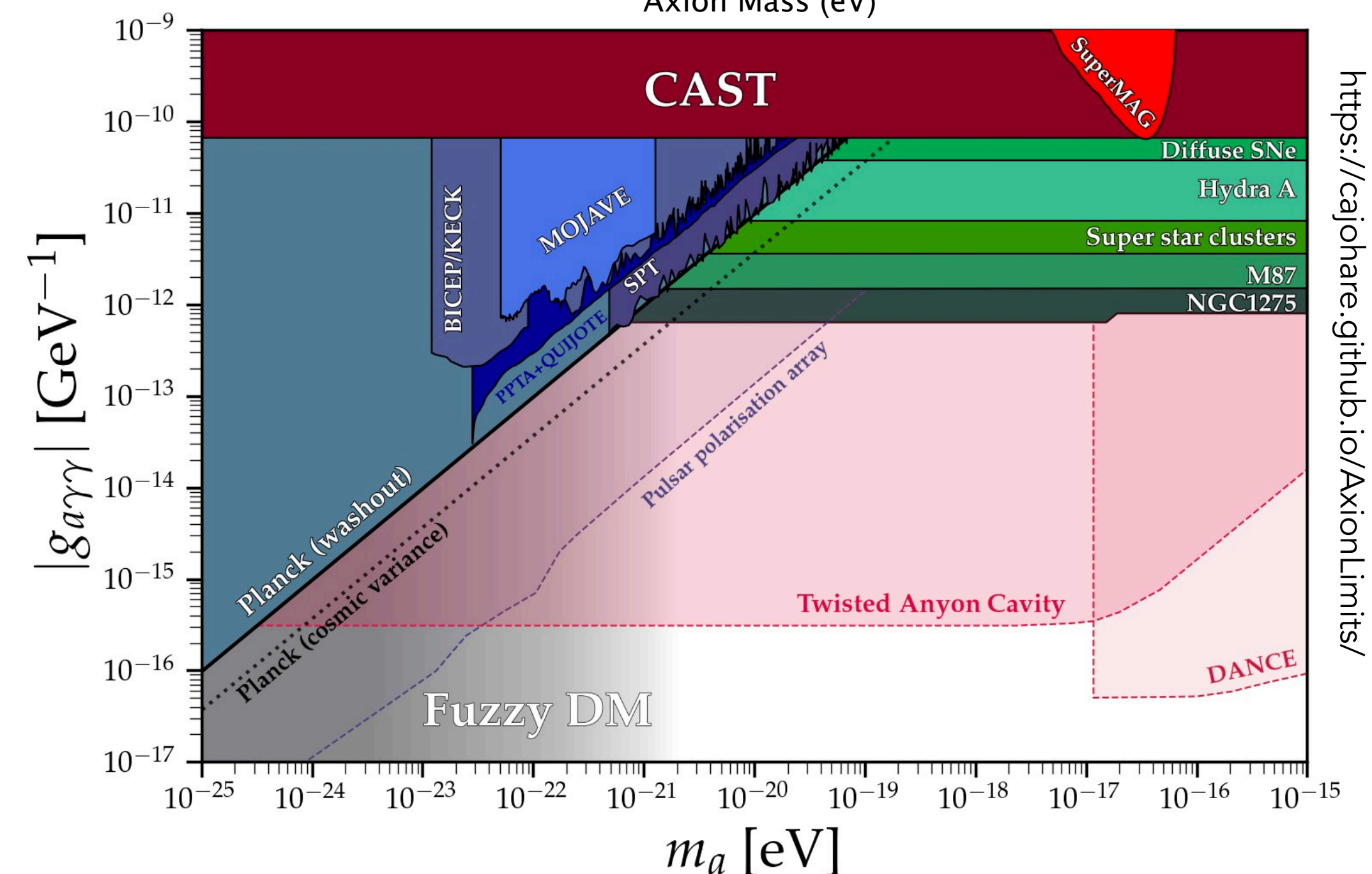
Twisted "anyon" microwave cavities

Dark matter detection in a single mode thanks to helicity

- Accesses an axion mass range very difficult to search
- **No external magnetic field needed**
- Ability to use **superconducting** materials
- Allows high Q-factors and improved sensitivity
- Next: Optimising Q-factors and minimising read-out amplitude modulation noise for a detection run



arXiv:2208.01640v2

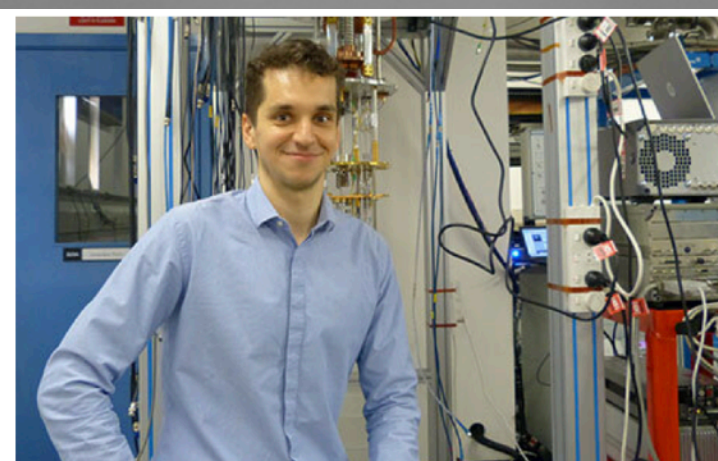


<https://cajohare.github.io/AxionLimits/>

The QDM Team



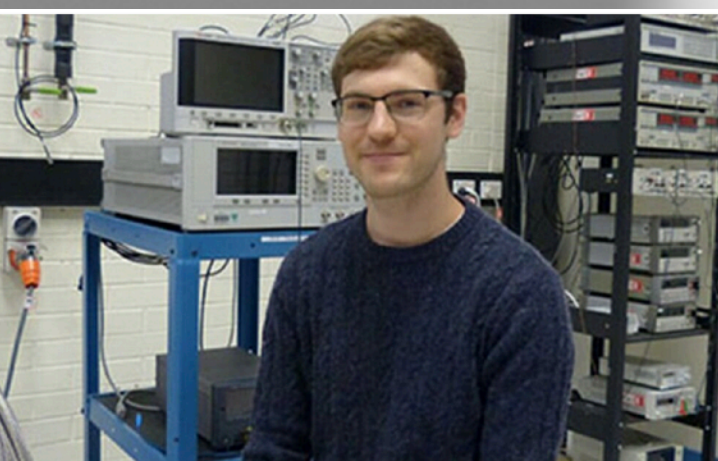
Professor Michael Tobar
Director—QDM Lab, EQUUS Node Director, CDM Node Director



Dr Maxim Goryachev
EQUUS Chief Investigator, CDM Chief Investigator, Lecturer—Research Intensive



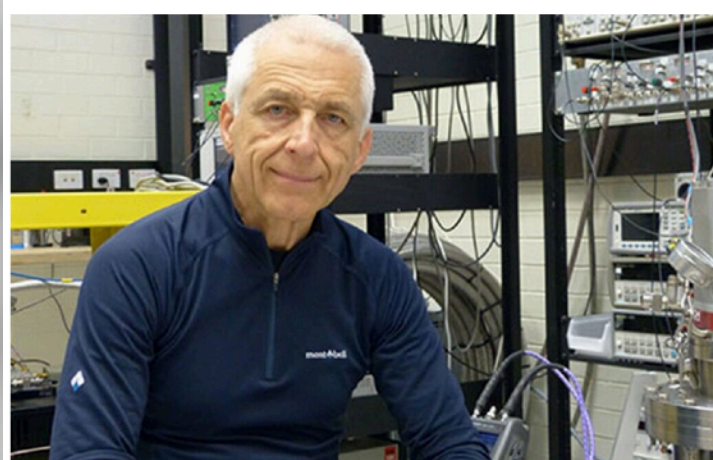
Dr Ben McAllister
Adjunct Research Fellow



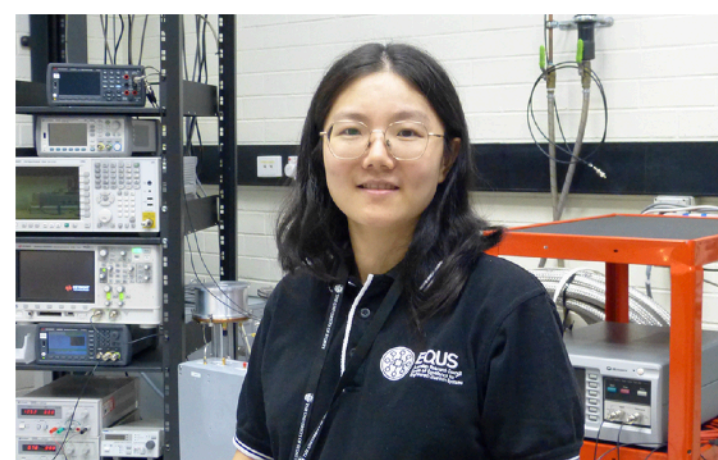
Dr Graeme Flower
Research Associate



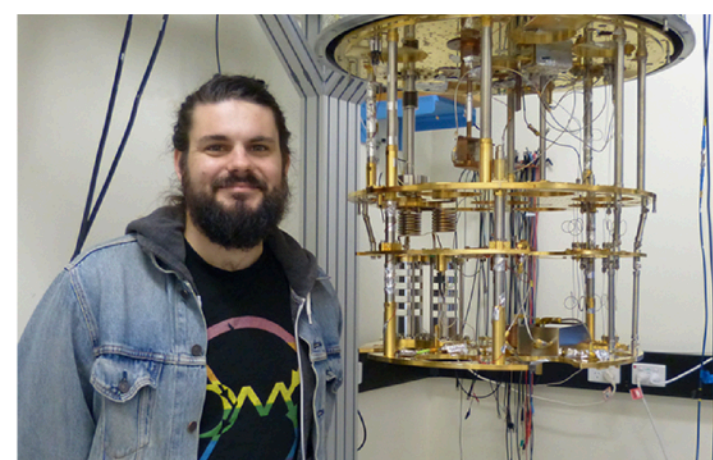
Will Campbell
Research Associate—Clock Flagship



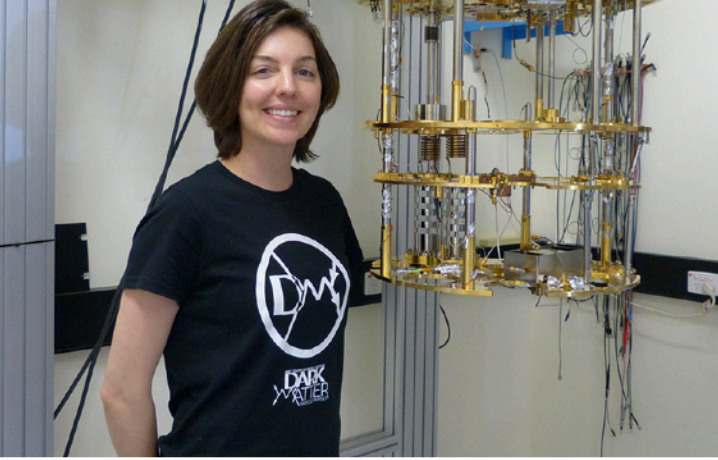
Winthrop Professor Eugene Ivanov
Senior Principle Research Fellow



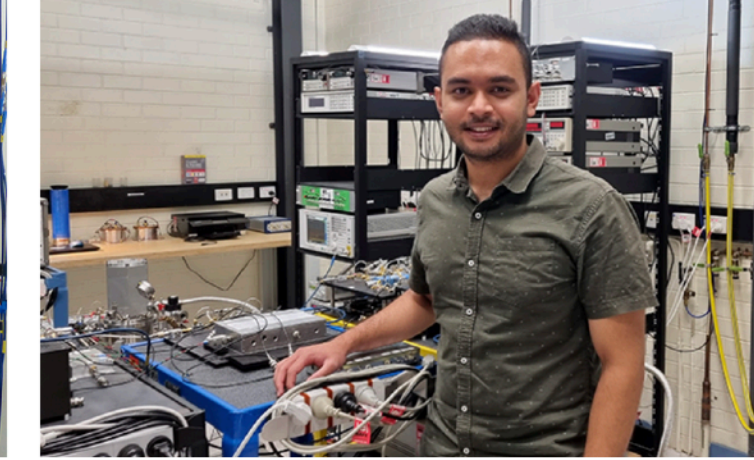
Dr Cindy Zhao
Deborah Jin Fellow—EQUUS



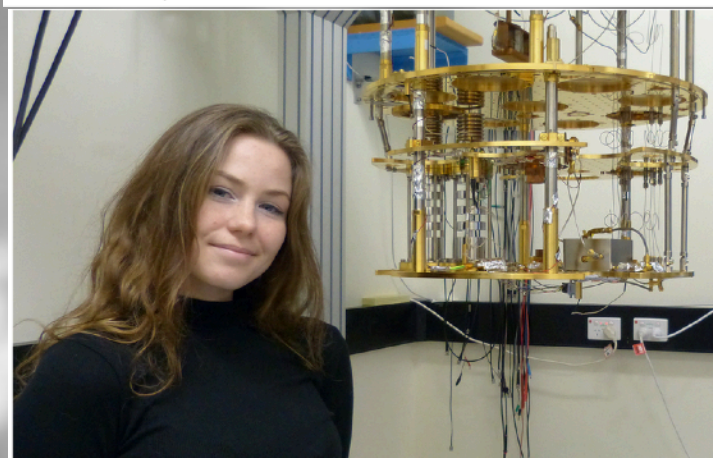
Dr Jeremy Bourhill
Postdoctoral Research Associate



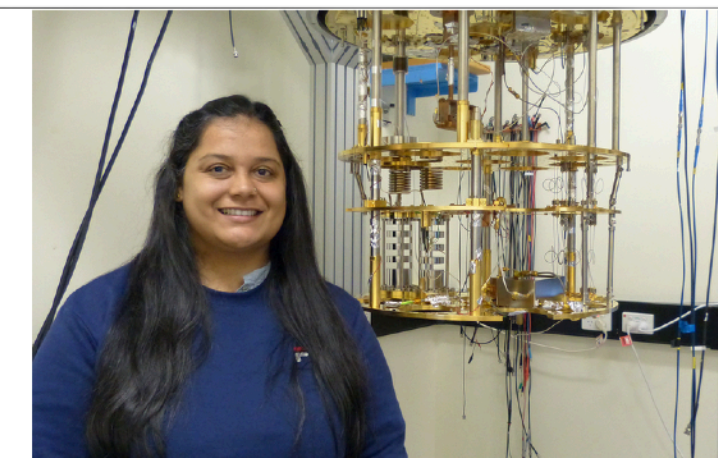
Elrina Hartman
PhD



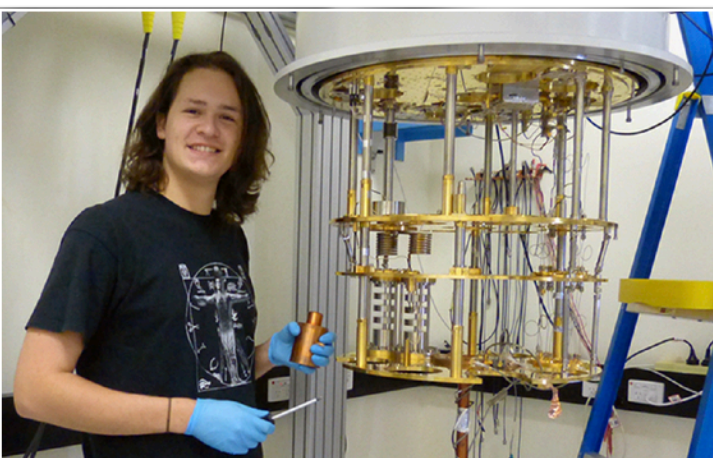
Steven Samuels
PhD



Emma Paterson
PhD



Sonali Parashar
Master of Physics—Coursework and Dissertation



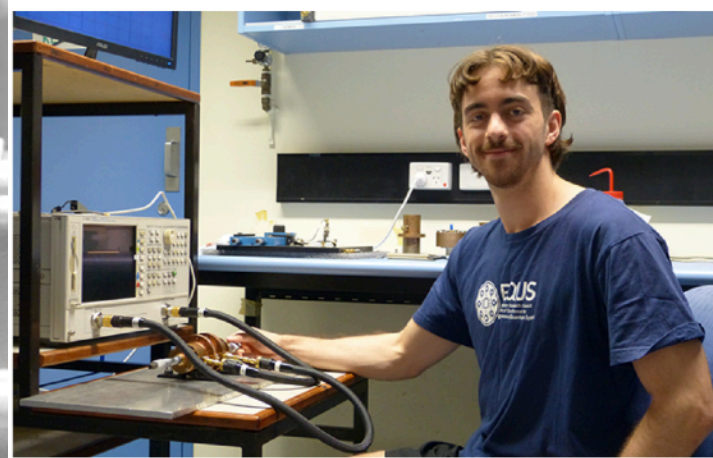
Tim Holt
BSc (Frontier Physics) and Master of Physics



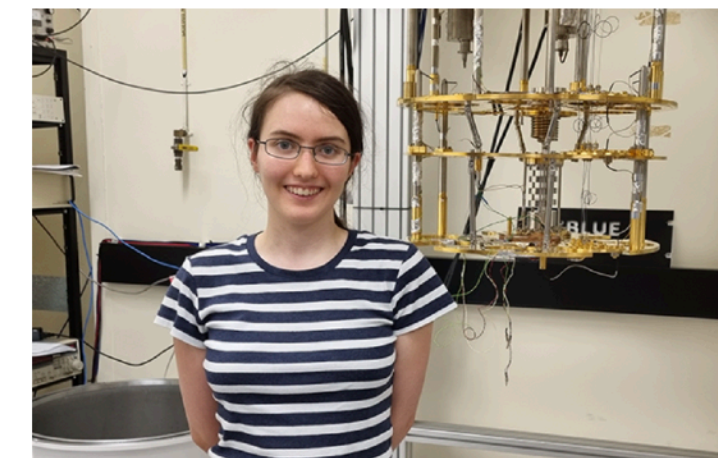
Aaron Quiskamp
PhD



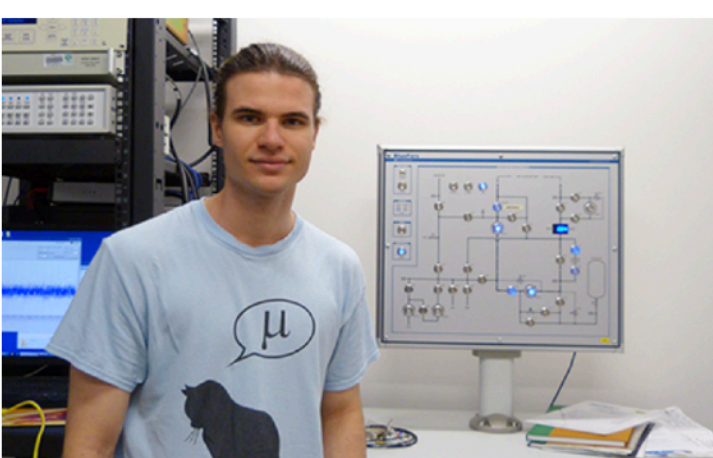
Teehani Ralph
Master of Professional Engineering



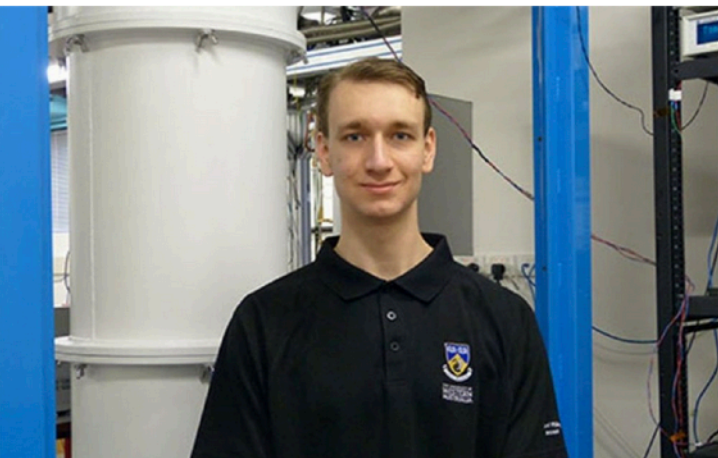
Michael Hatzon
BPhil (Hons) Honours Dissertation



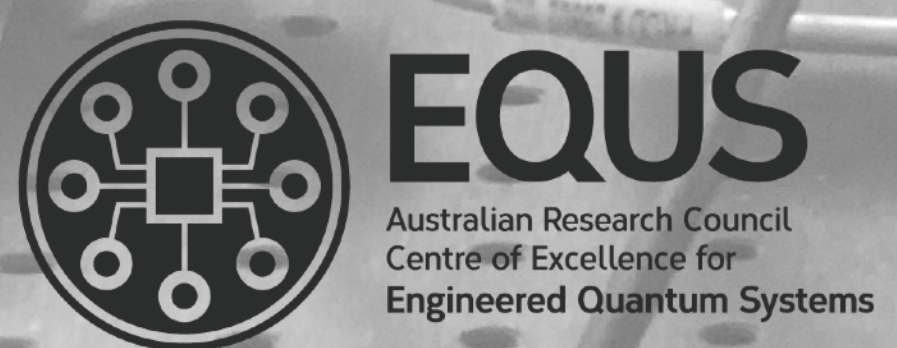
Emily Waterman
BPhil (Hons) Honours Dissertation



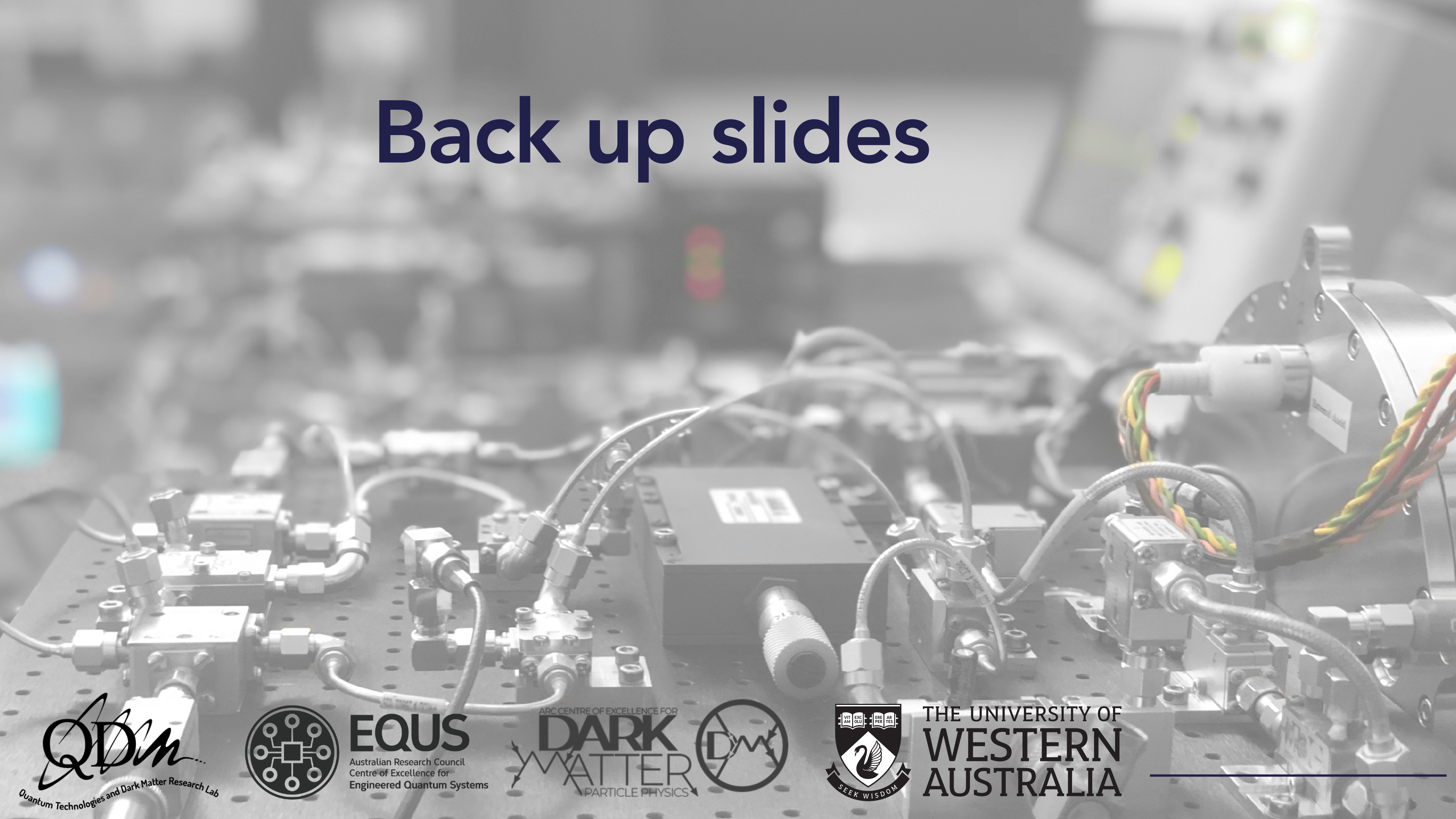
Ashley Johnson
BPhil (Hons) Honours Dissertation



Robert Crew
PhD



Back up slides



EQUS
Australian Research Council
Centre of Excellence for
Engineered Quantum Systems

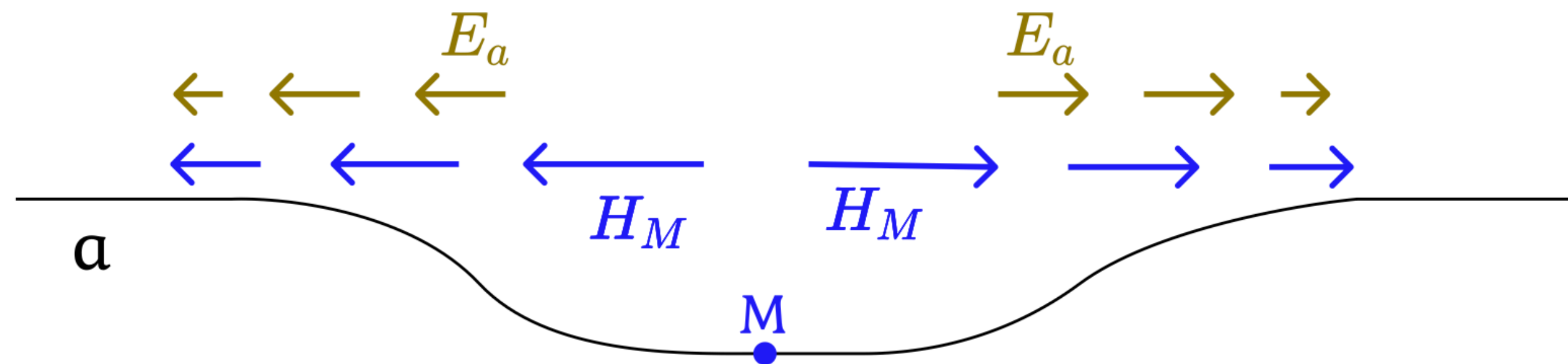


THE UNIVERSITY OF
**WESTERN
AUSTRALIA**

Slide From Anton Sokolov

AXION EFFECTS ON CHARGED PARTICLES

- An analogue of the Witten effect in axion electrodynamics:



$$\nabla \cdot \mathbf{E}_a = g_{a\gamma\gamma} \mathbf{H}_0 \cdot \nabla a$$

↓
fictitious charge density

- Magnetic monopole looks like a dyon
- No new charged particle states are produced: fictitious charge can only be generated at distance scales $r \gtrsim \omega_a^{-1}$, and so it is never point-like in a given axion EFT
- Axion shift symmetry is preserved since dependence only on ∇a