

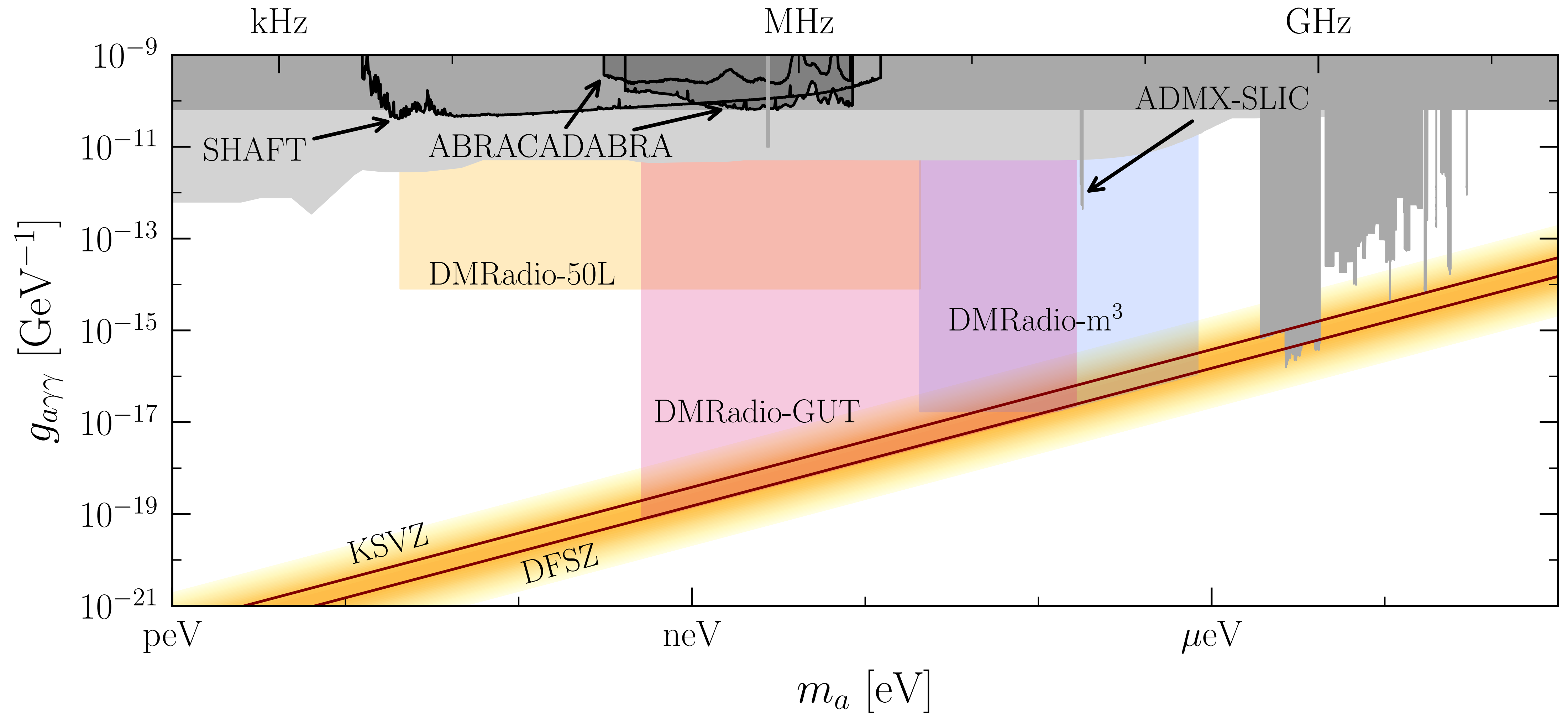
LUMPED ELEMENT AXION DETECTION AT ALL FREQUENCIES

Joshua W. Foster

MIT Center for Theoretical Physics

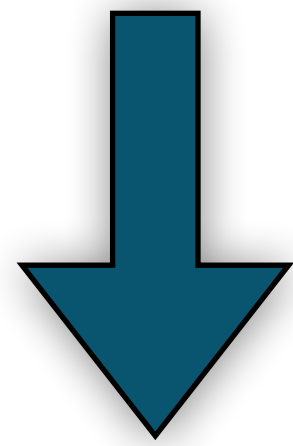
April 16, 2024

THE DMRADIO EXPERIMENTAL PROGRAM



LUMPED ELEMENT AXION DETECTION

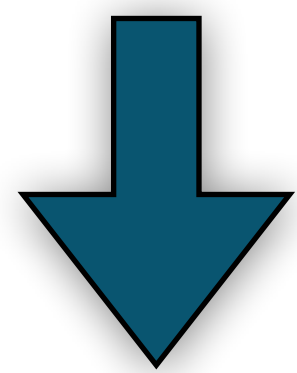
$$\mathcal{L}_{\text{EM}} \supset -\frac{1}{4}FF - \frac{1}{4}g_{a\gamma\gamma}aF\tilde{F}$$



Modified Maxwell's Equations

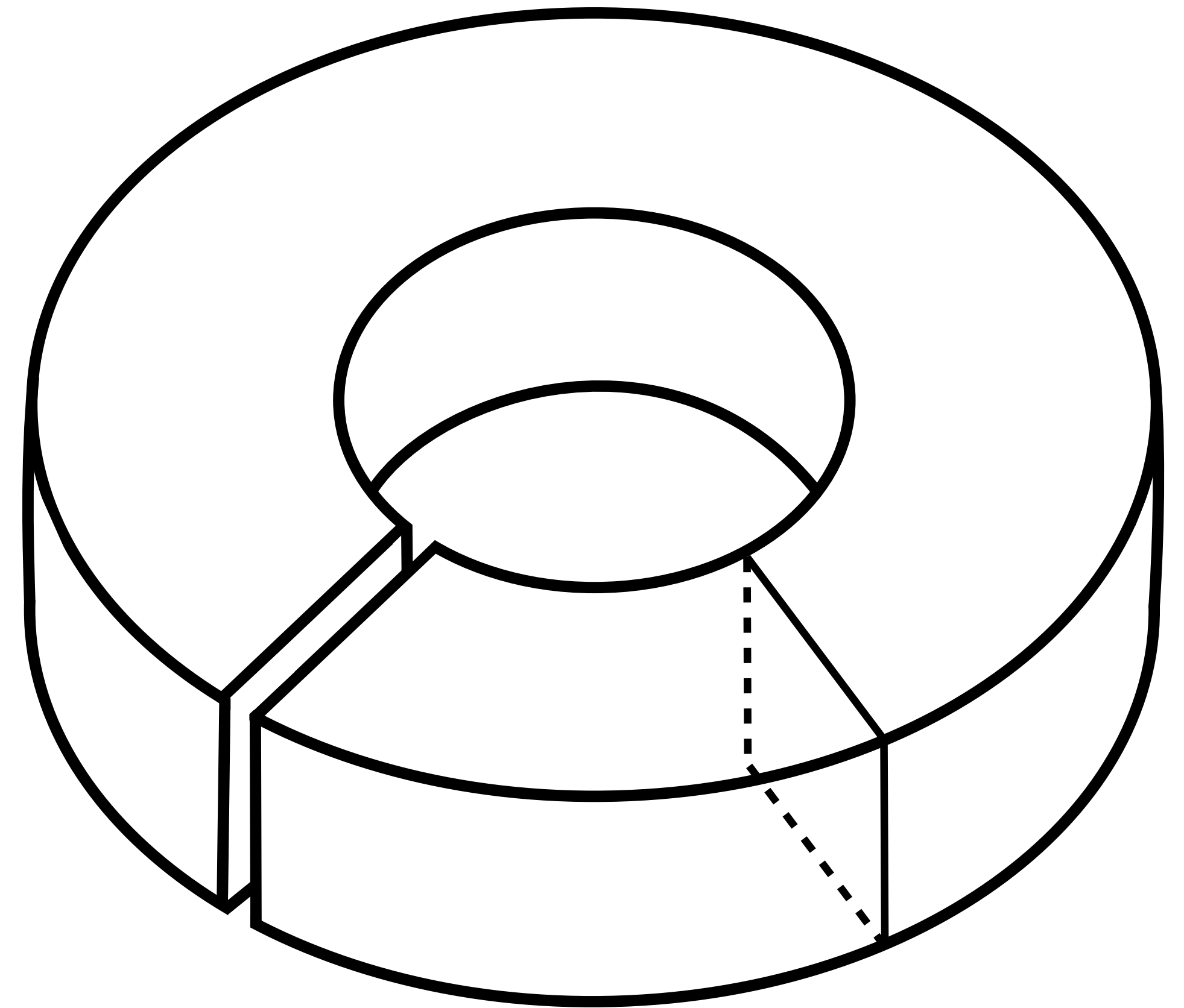
$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \times \mathbf{B} = \dot{\mathbf{E}} + \mathbf{J} - g_{a\gamma\gamma} (\mathbf{E} \times \nabla a - \dot{a}\mathbf{B})$$



Cold DM limit

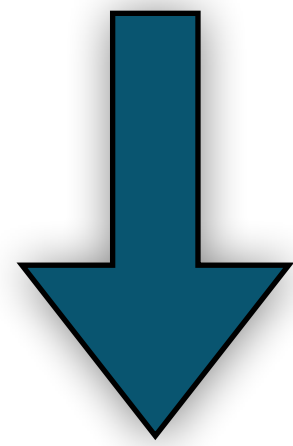
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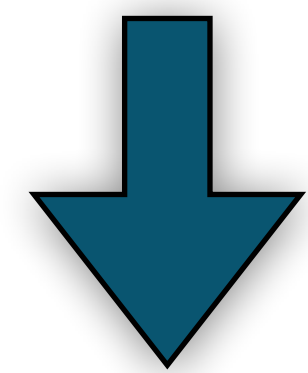
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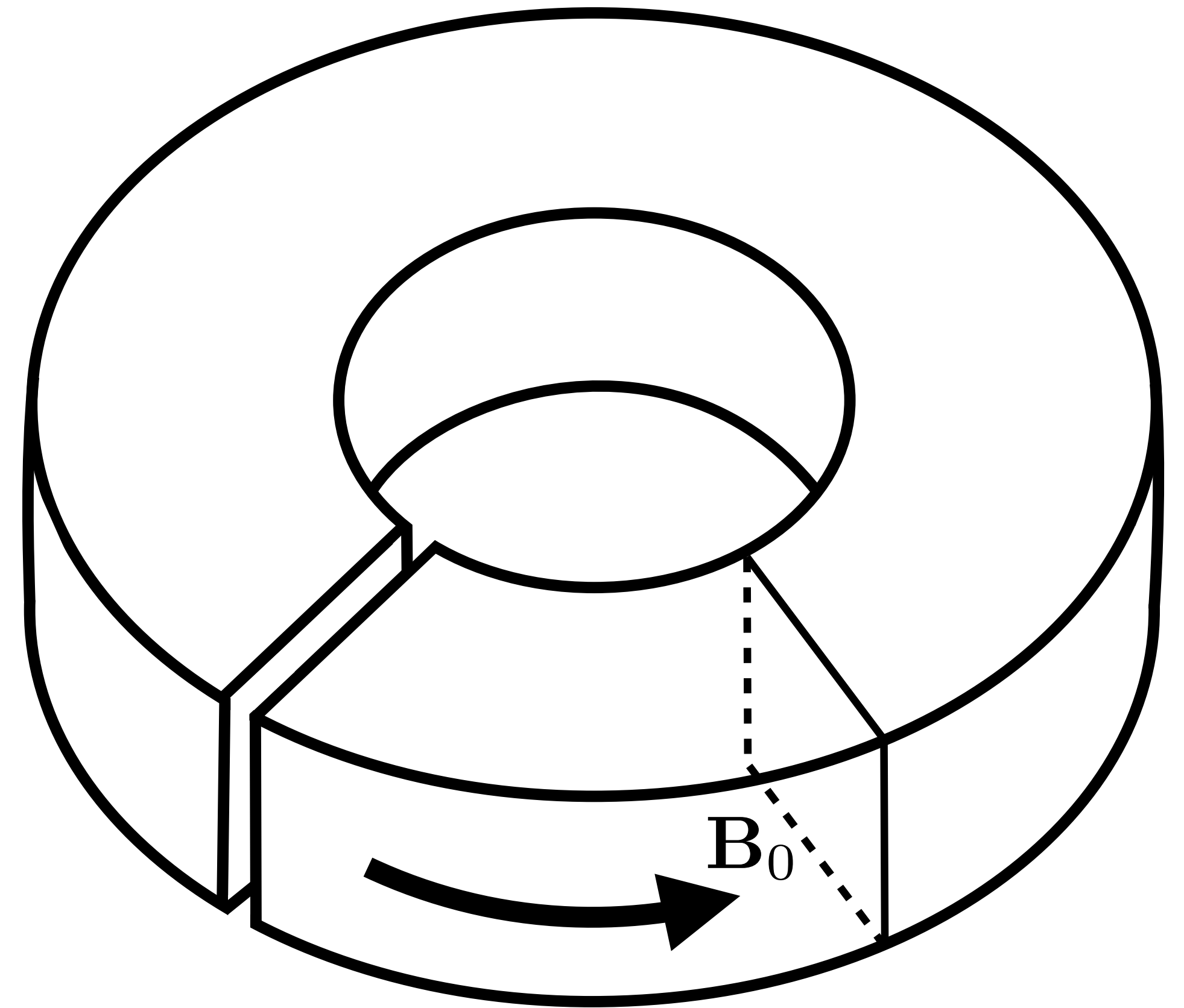
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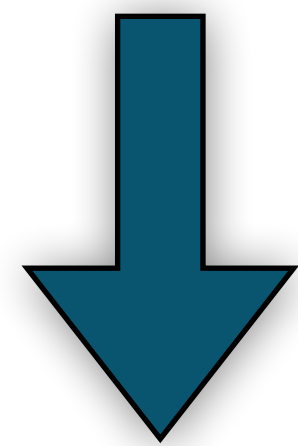
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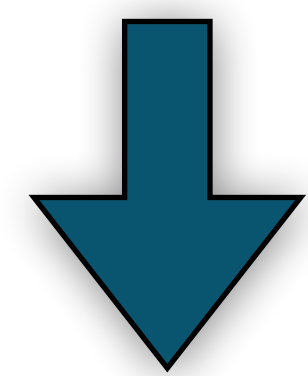
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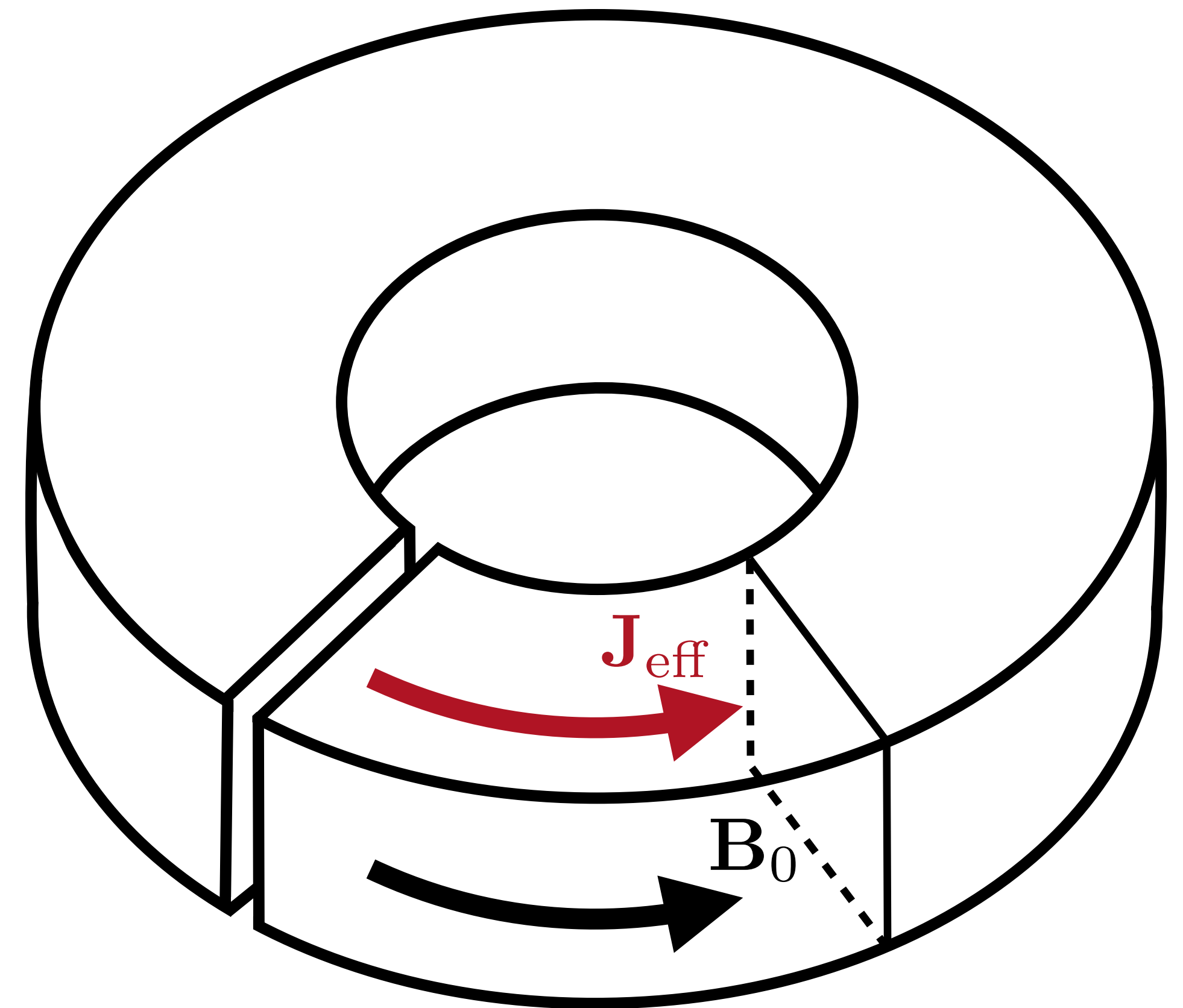
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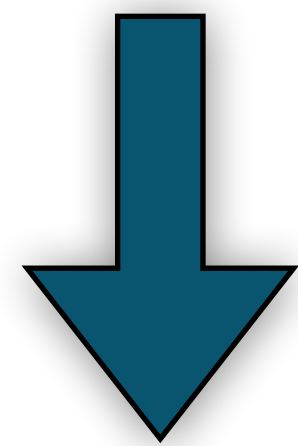
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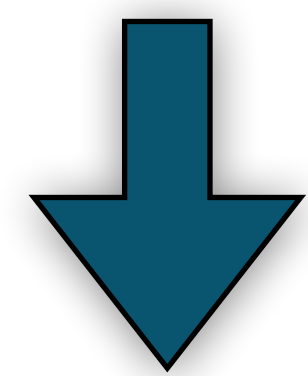
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Modified Maxwell's Equations

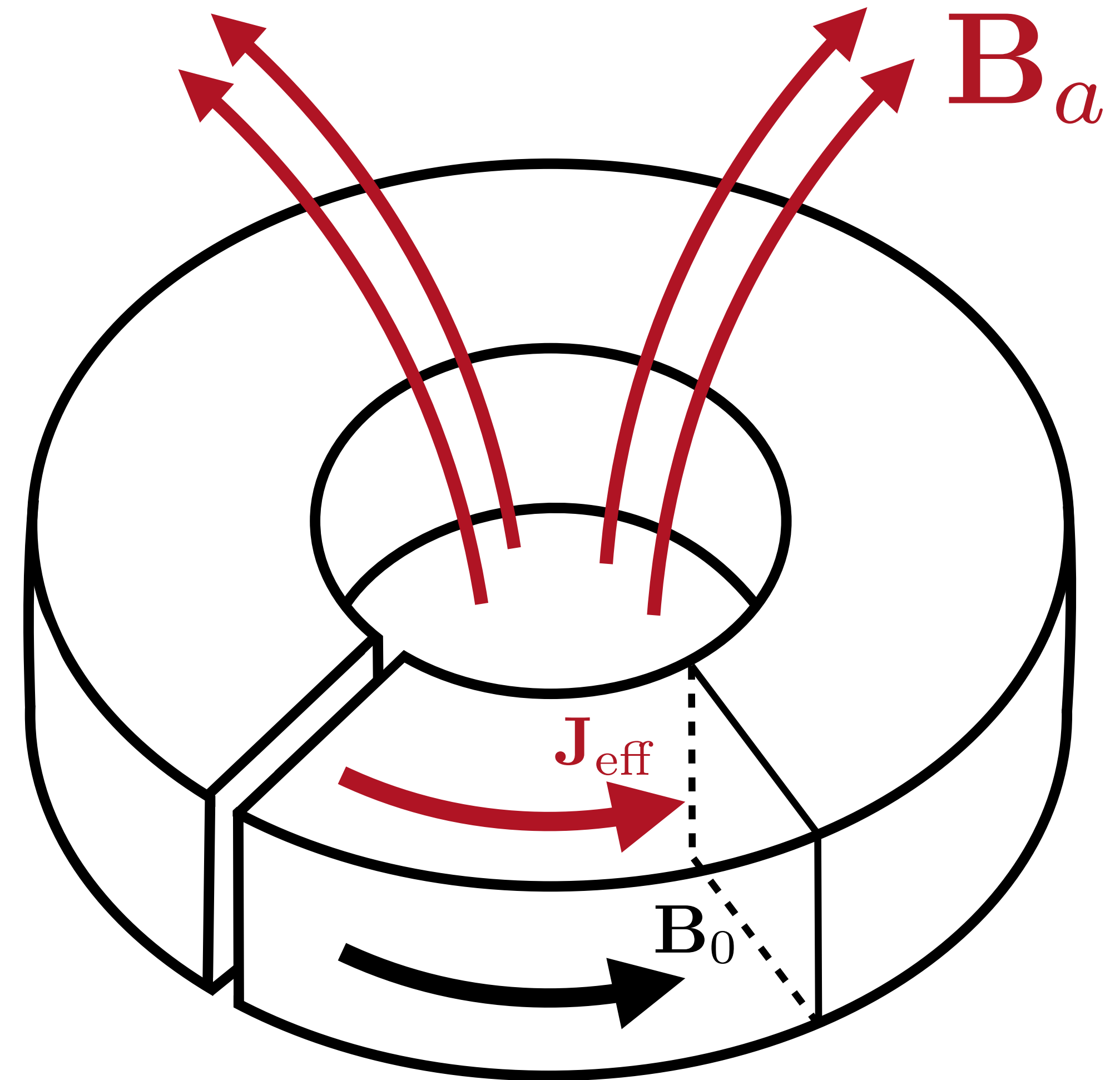
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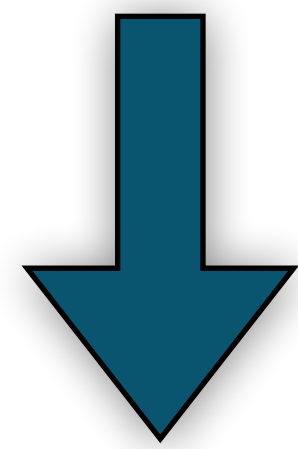
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LUMPED ELEMENT AXION DETECTION

ABRACADABRA

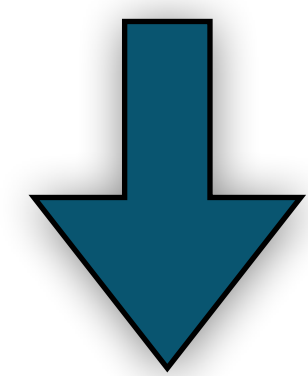
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Modified Maxwell's Equations

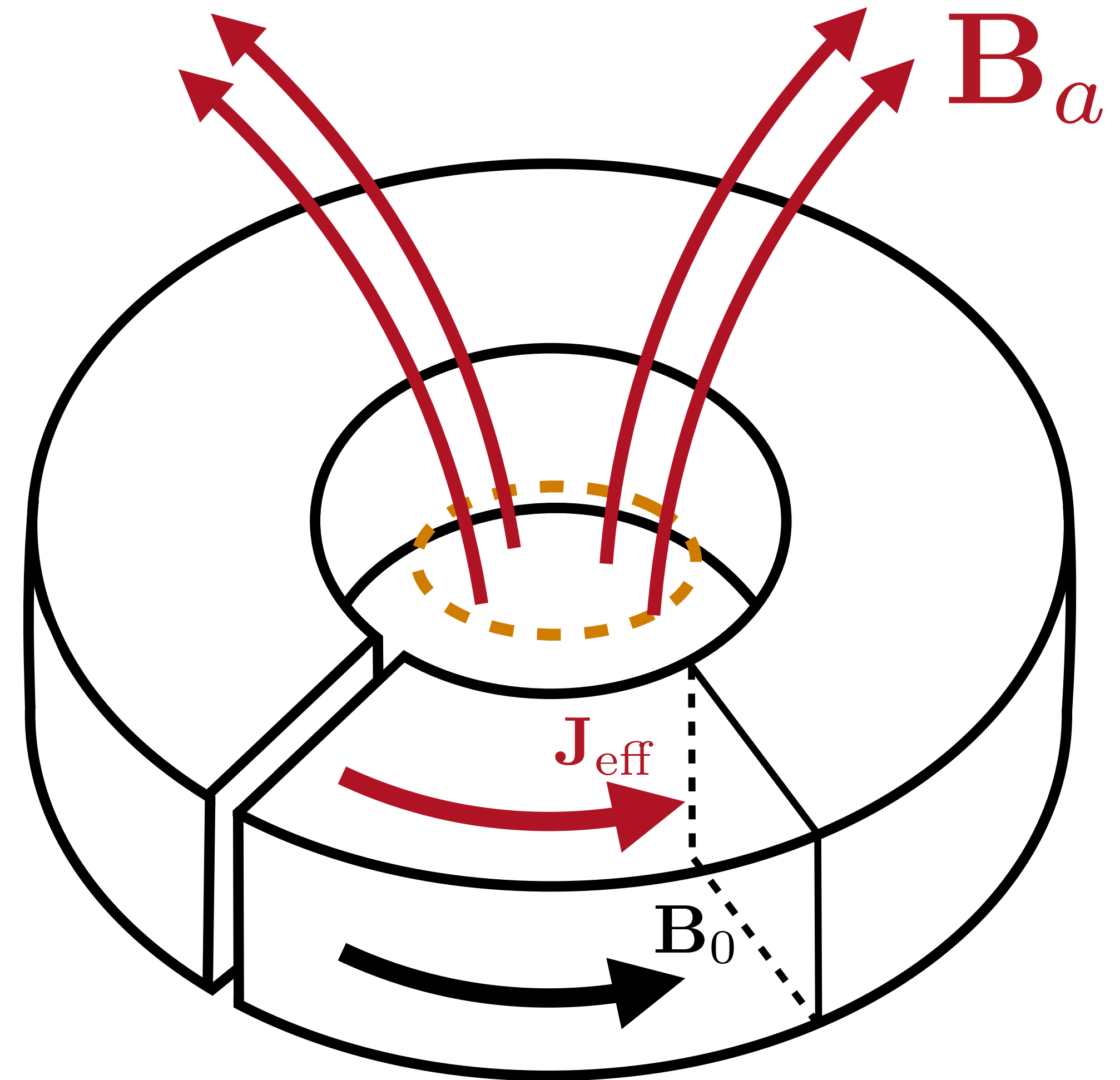
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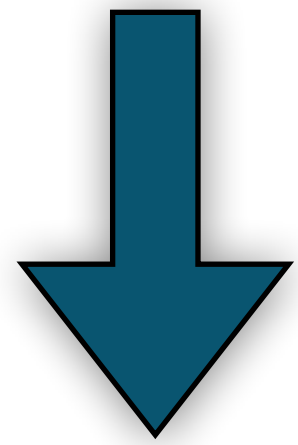
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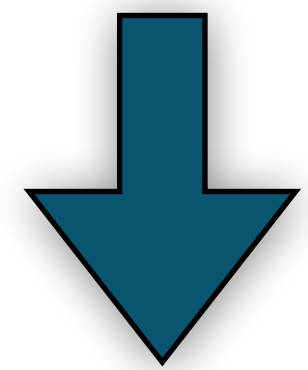
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Modified Maxwell's Equations

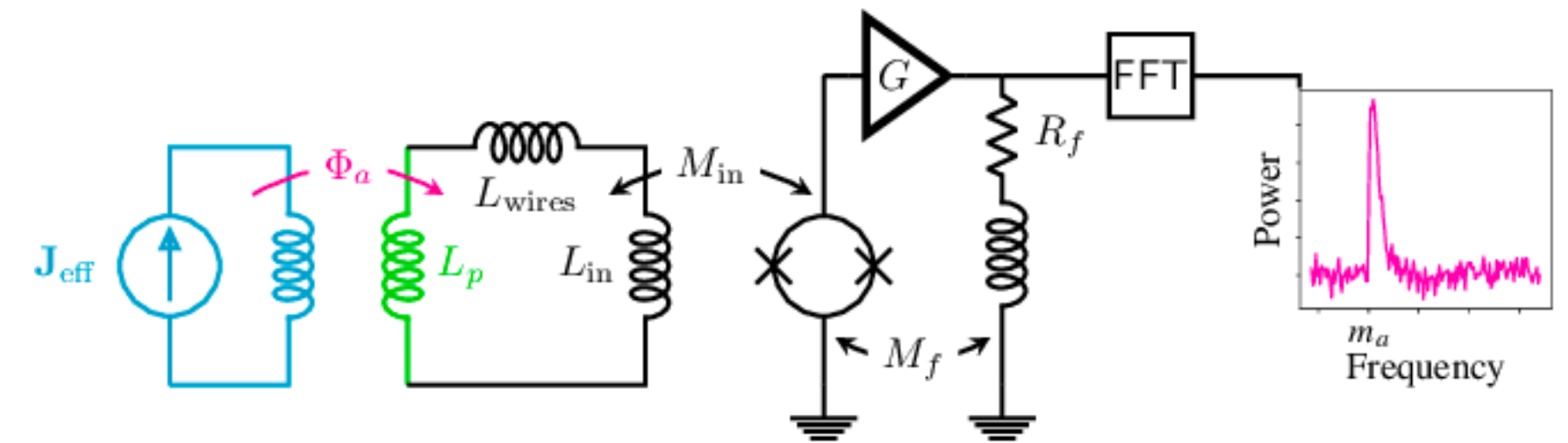
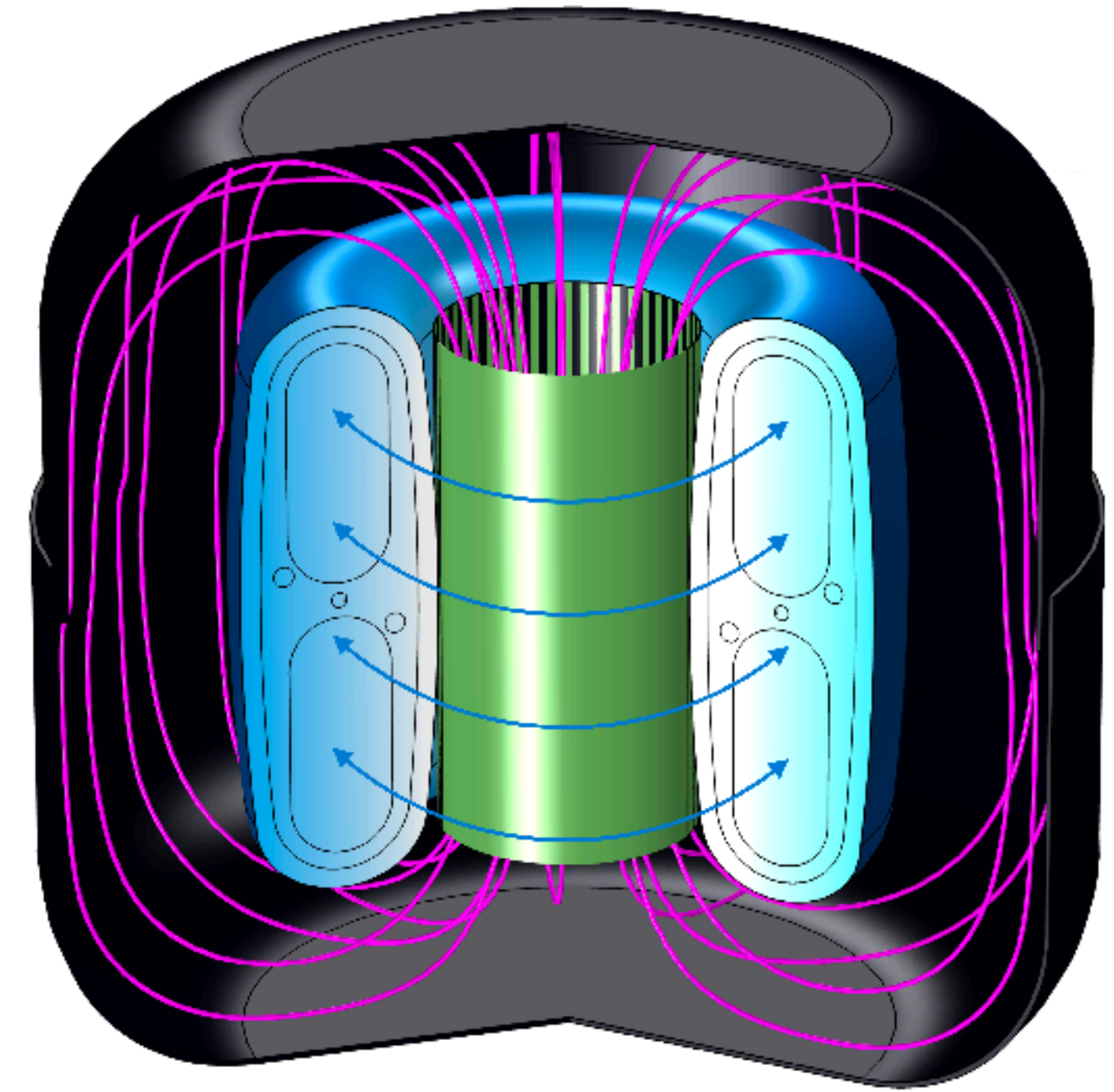
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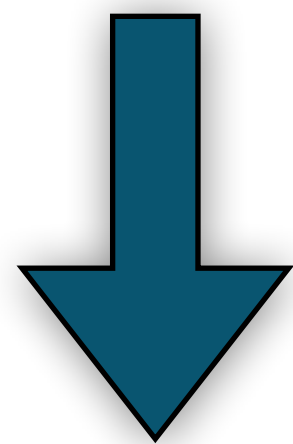
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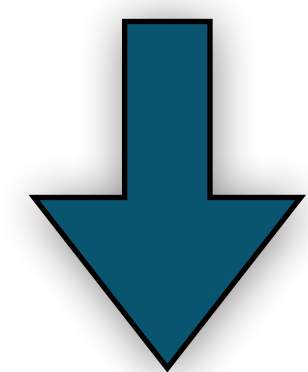
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Modified Maxwell's Equations

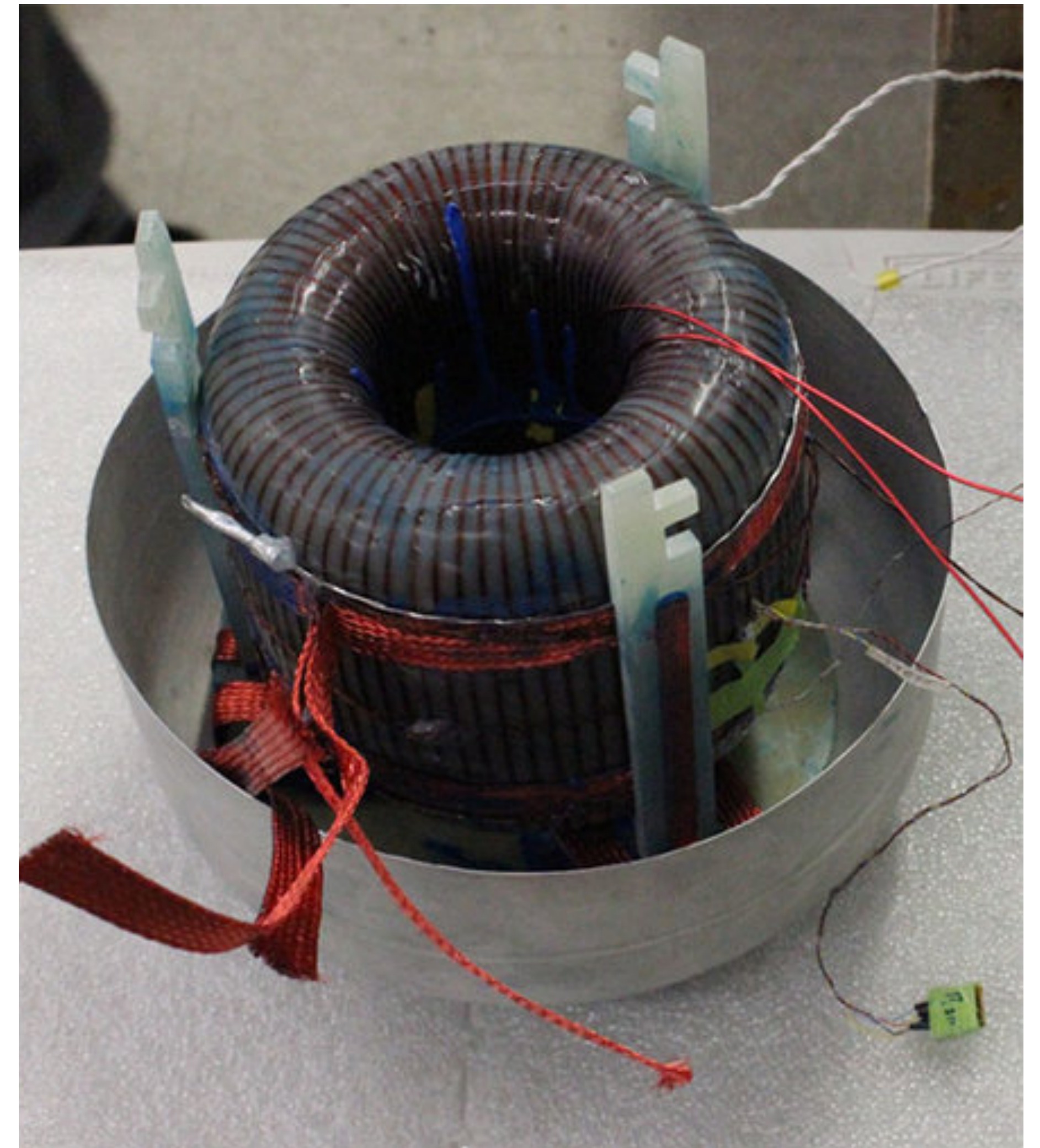
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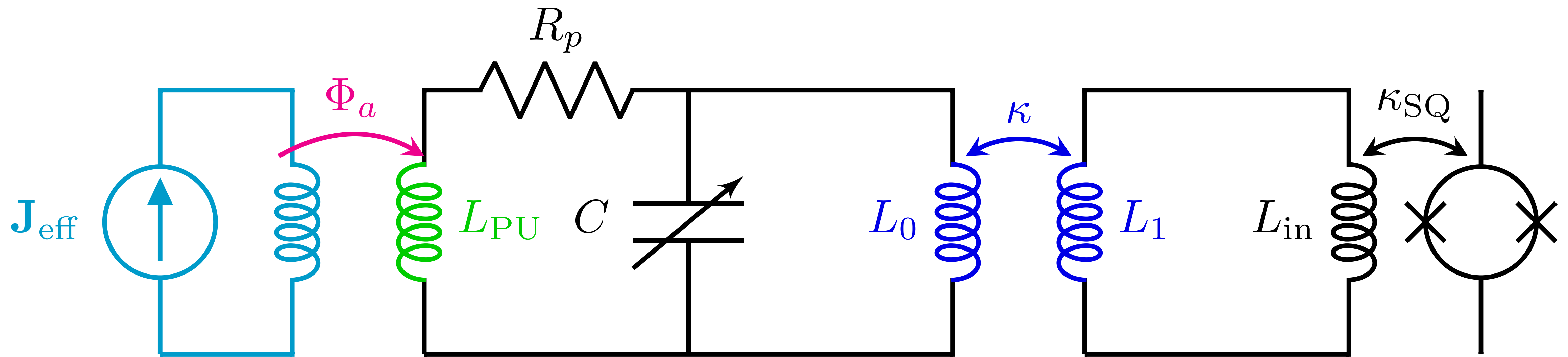


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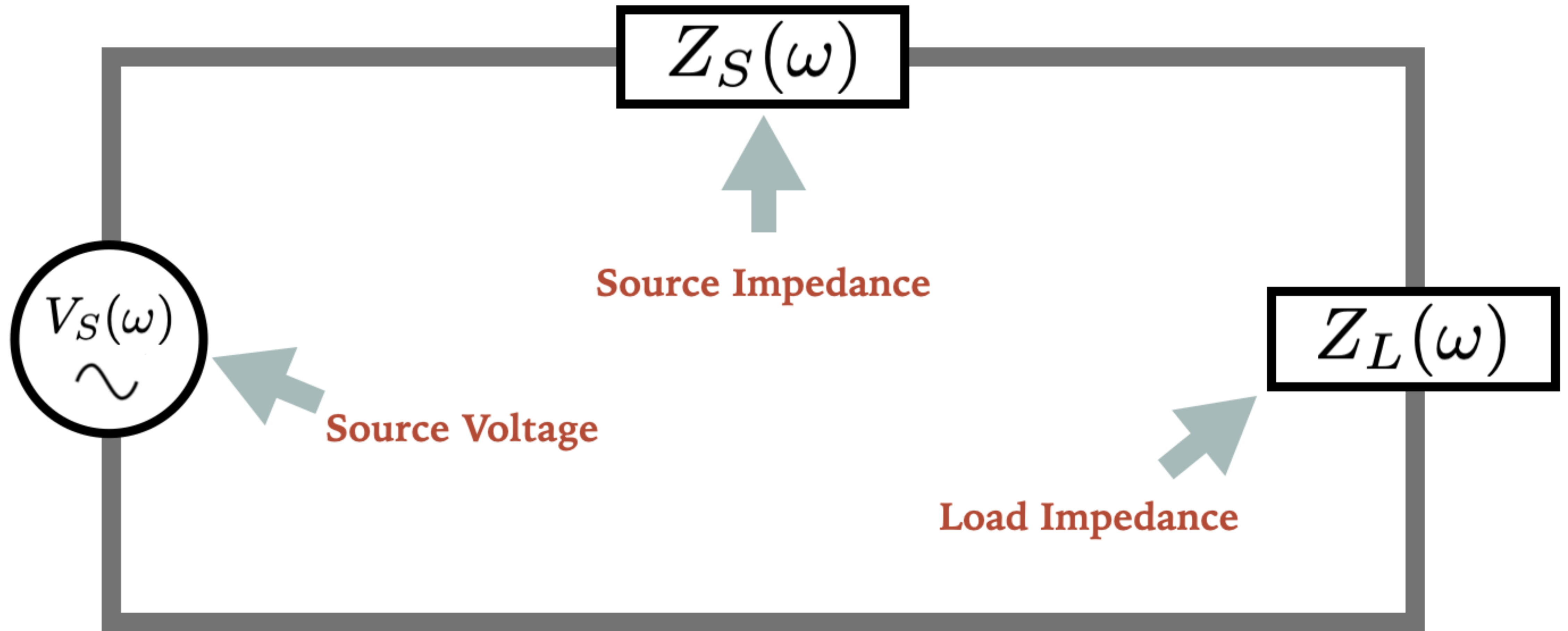
LUMPED ELEMENT EQUIVALENT CIRCUIT AND READOUT CONCEPT



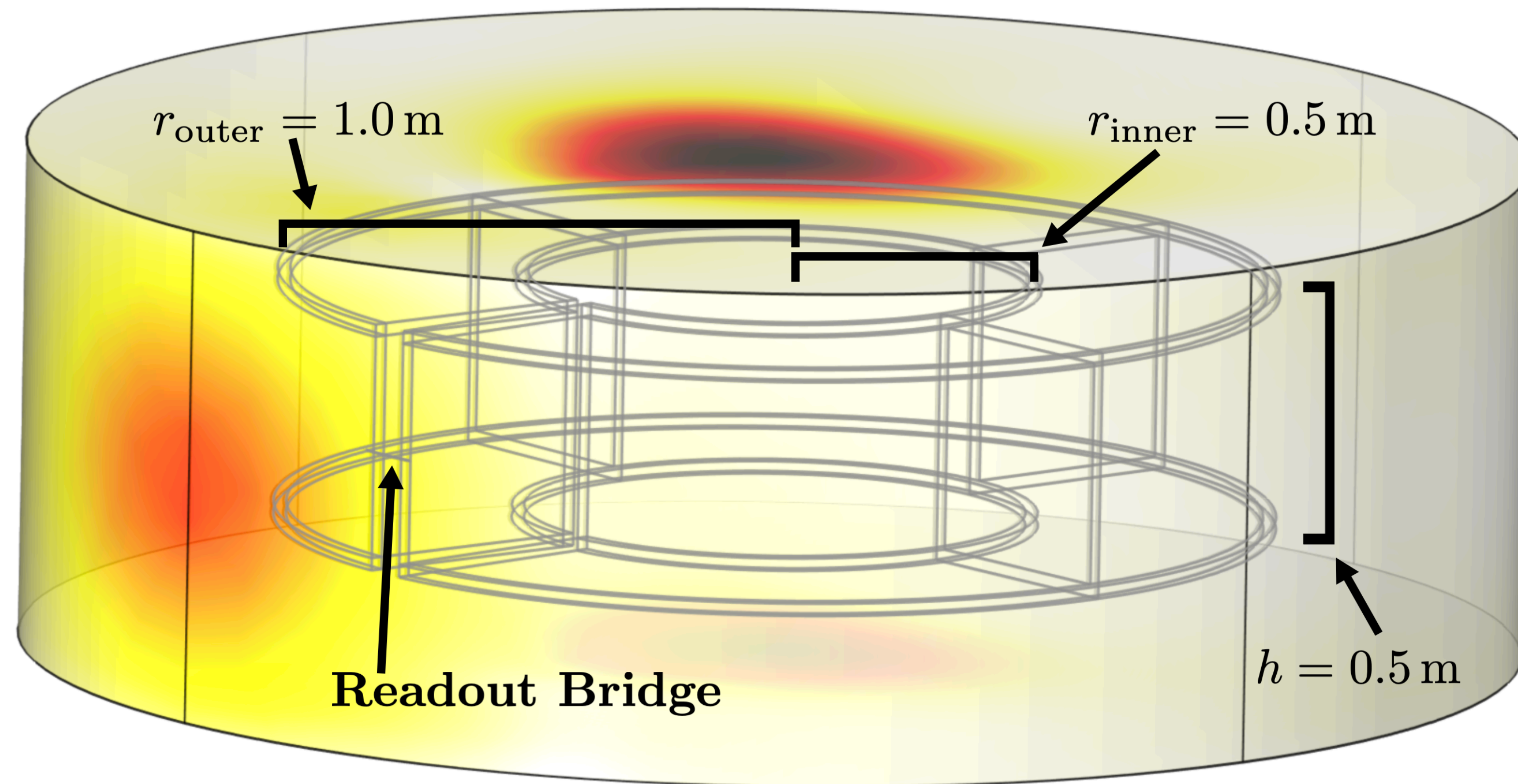
$$I_{\text{sig}}(\omega) = \frac{V_{\text{source}}(\omega)}{Z_{\text{tot}}(\omega)} \propto g_{a\gamma\gamma},$$

$$Z_{\text{tot}} = Z_{R_p} + Z_C + Z_{L_0} + Z_{L_{\text{PU}}}$$

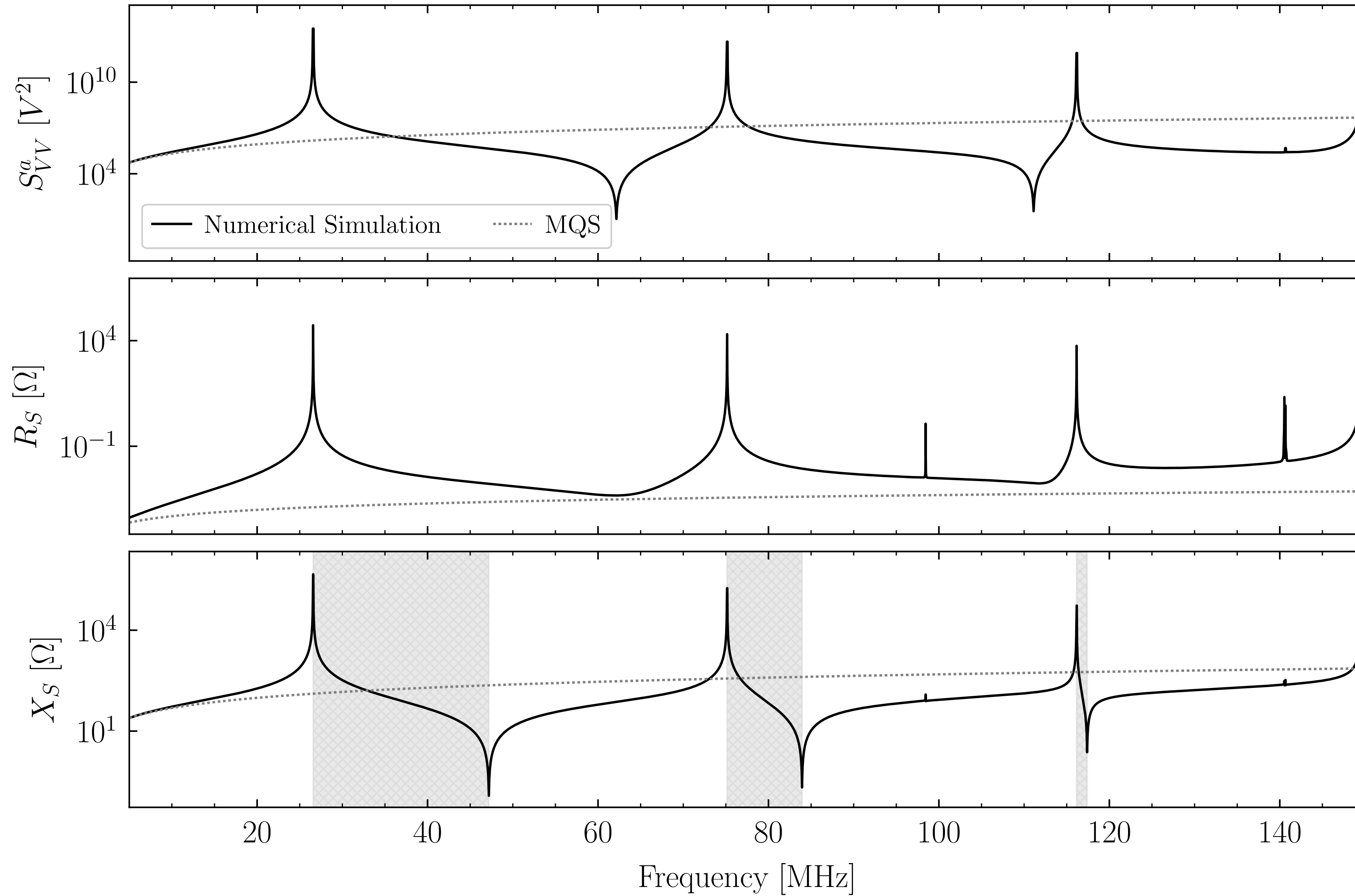
SIMPLIFIED EQUIVALENT CIRCUIT FOR LUMPED ELEMENT DETECTION



NUMERICAL SIMULATIONS OF LUMPED ELEMENT DETECTORS WITH COMSOL



NUMERICAL SIMULATION FOR DETECTOR CHARACTERIZATION



LUMPED ELEMENT EQUIVALENT CIRCUIT AND READOUT CONCEPT

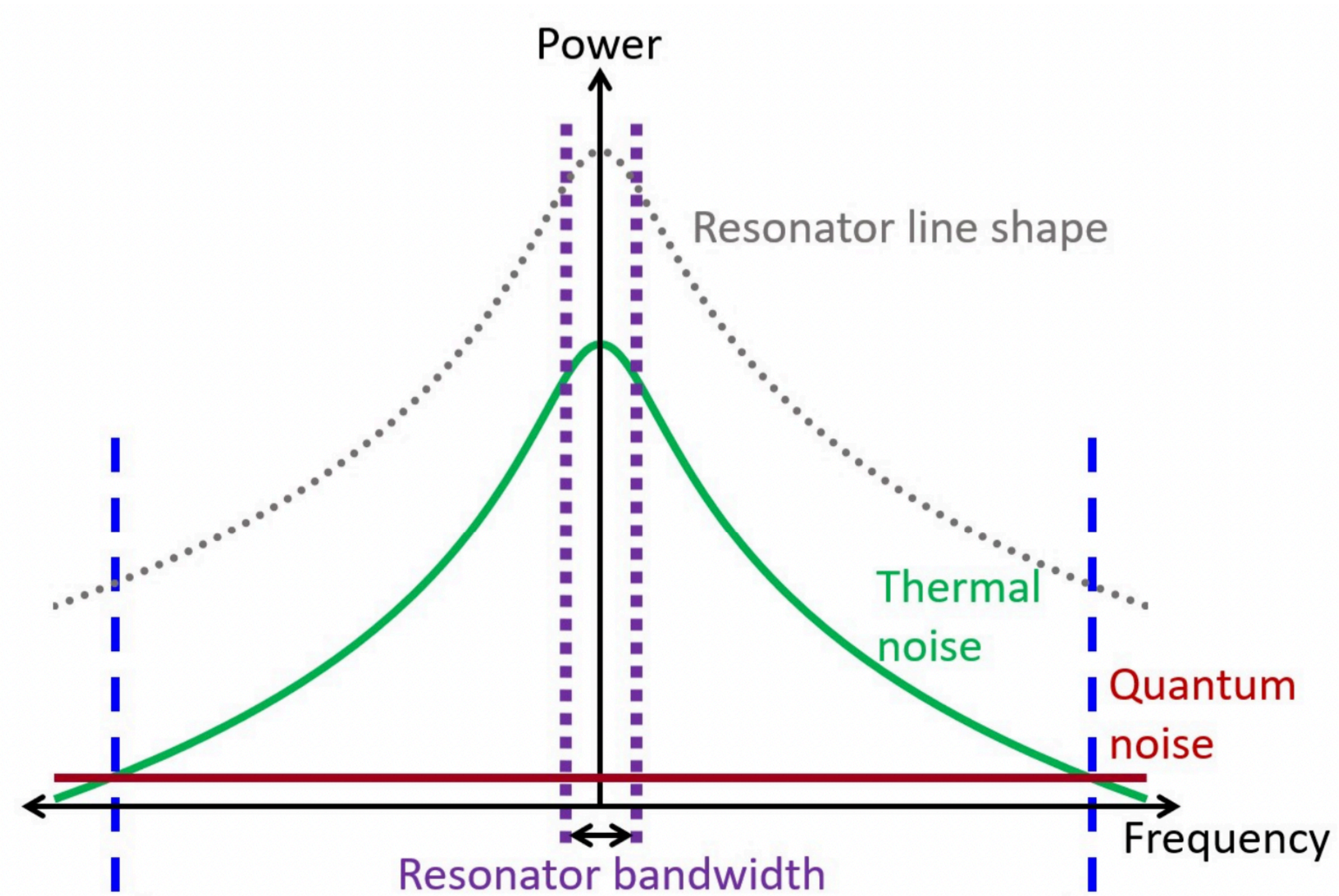
$$I_{\text{sig}}^2(\omega) = \frac{V_S(\omega)^2}{R^2 + X_{\text{tot}}(\omega)^2}$$

Quasistatic Approximation

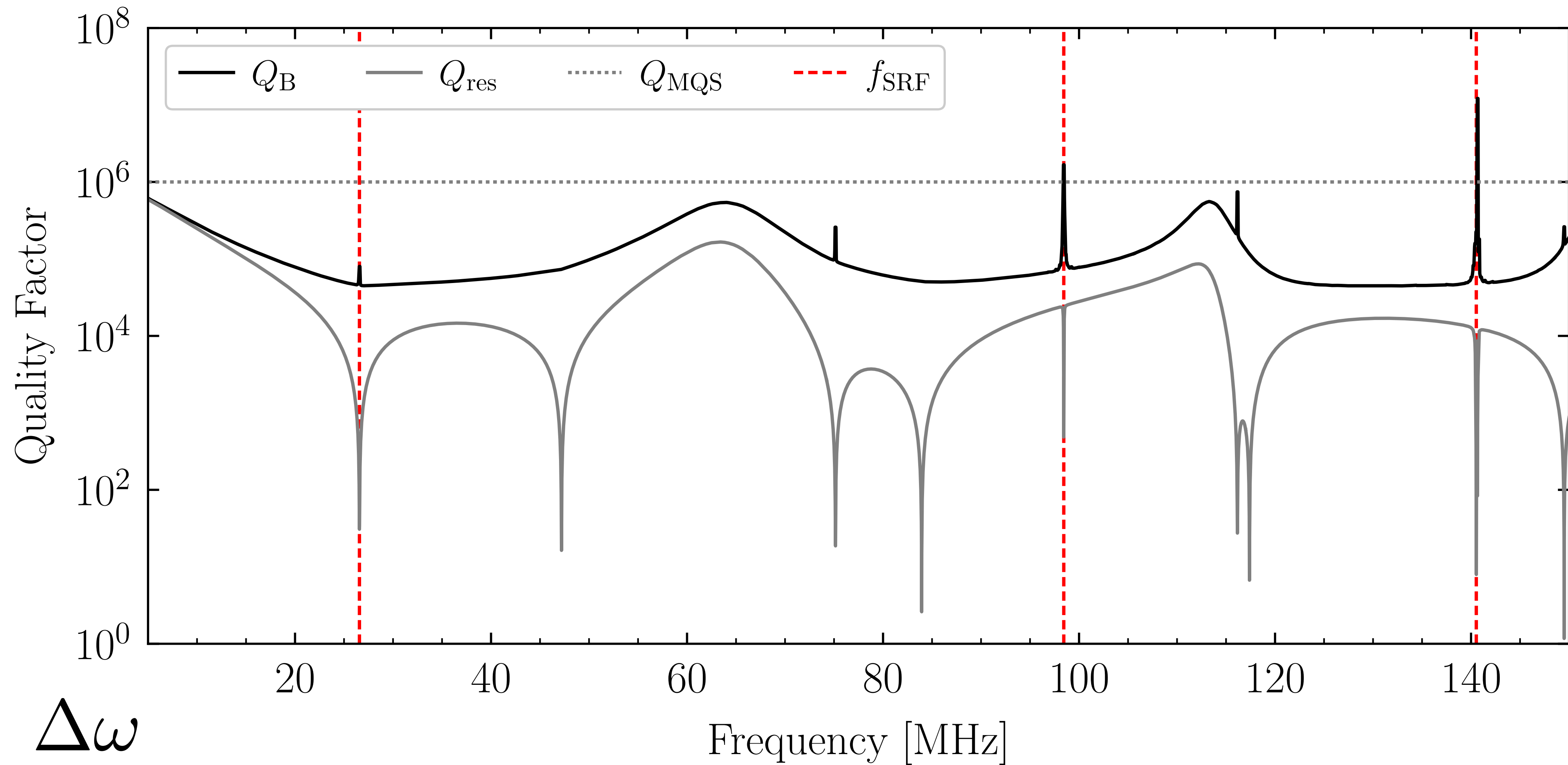
$$X_L(\omega) = \omega L$$

$$X_C(\omega) = -\frac{1}{\omega C}$$

$$I_{\text{sig}}(\omega) \approx \frac{V_S(\omega)^2}{R^2} \left[1 - \frac{L^2}{R^2} (\omega - \omega_r)^2 \right]$$

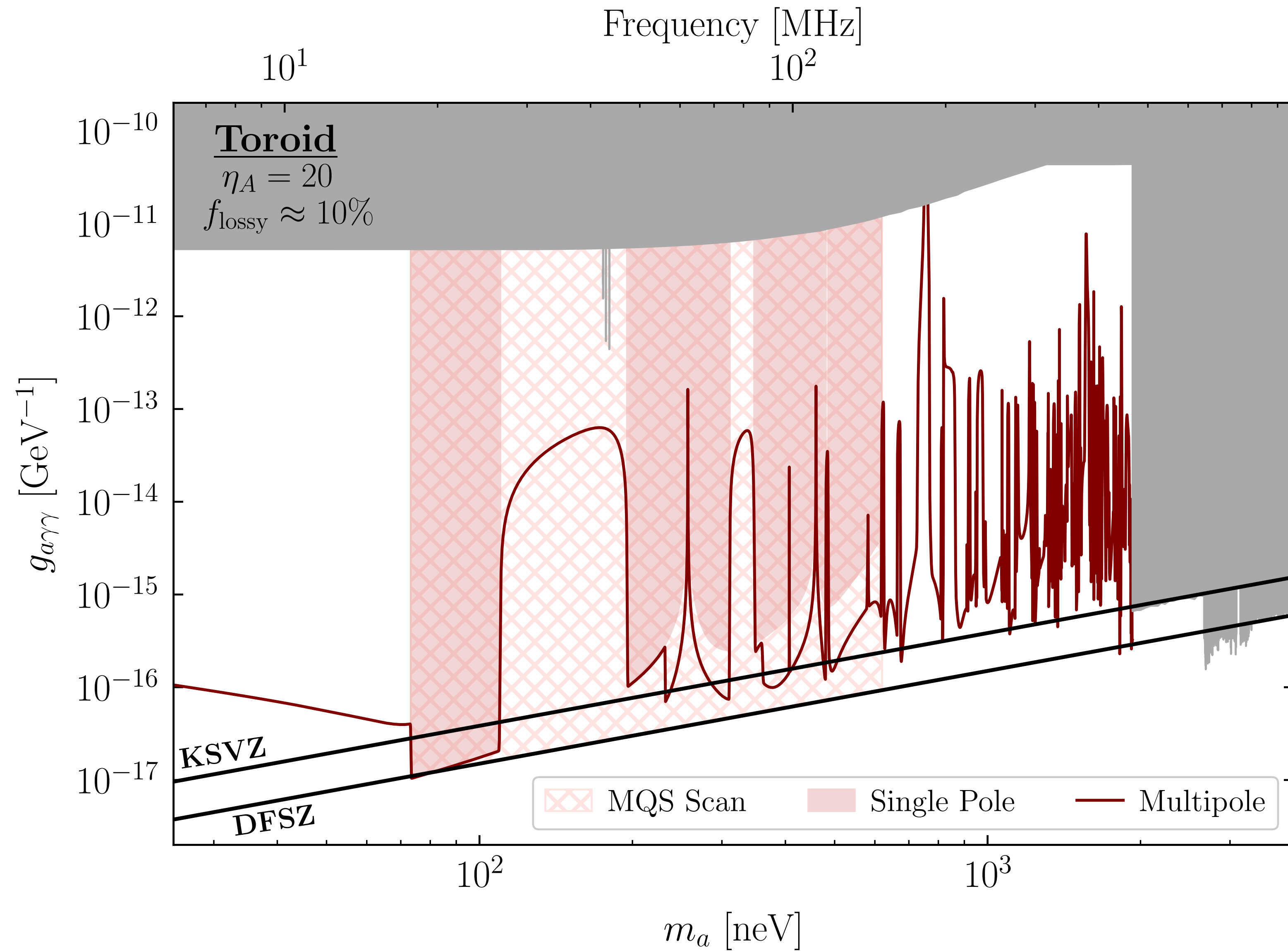


SCANNING SENSITIVITIES FOR LUMPED ELEMENT DETECTION

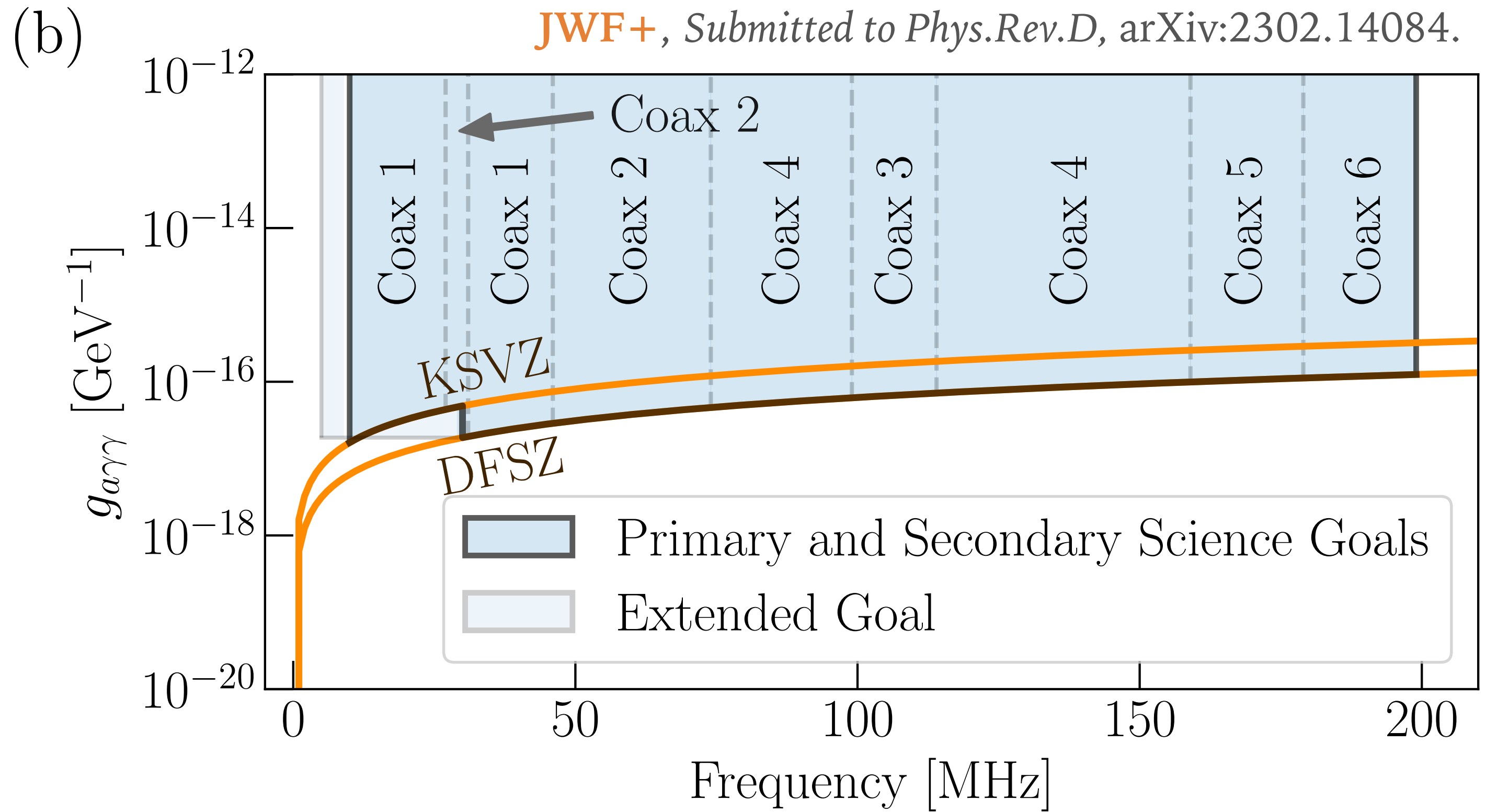
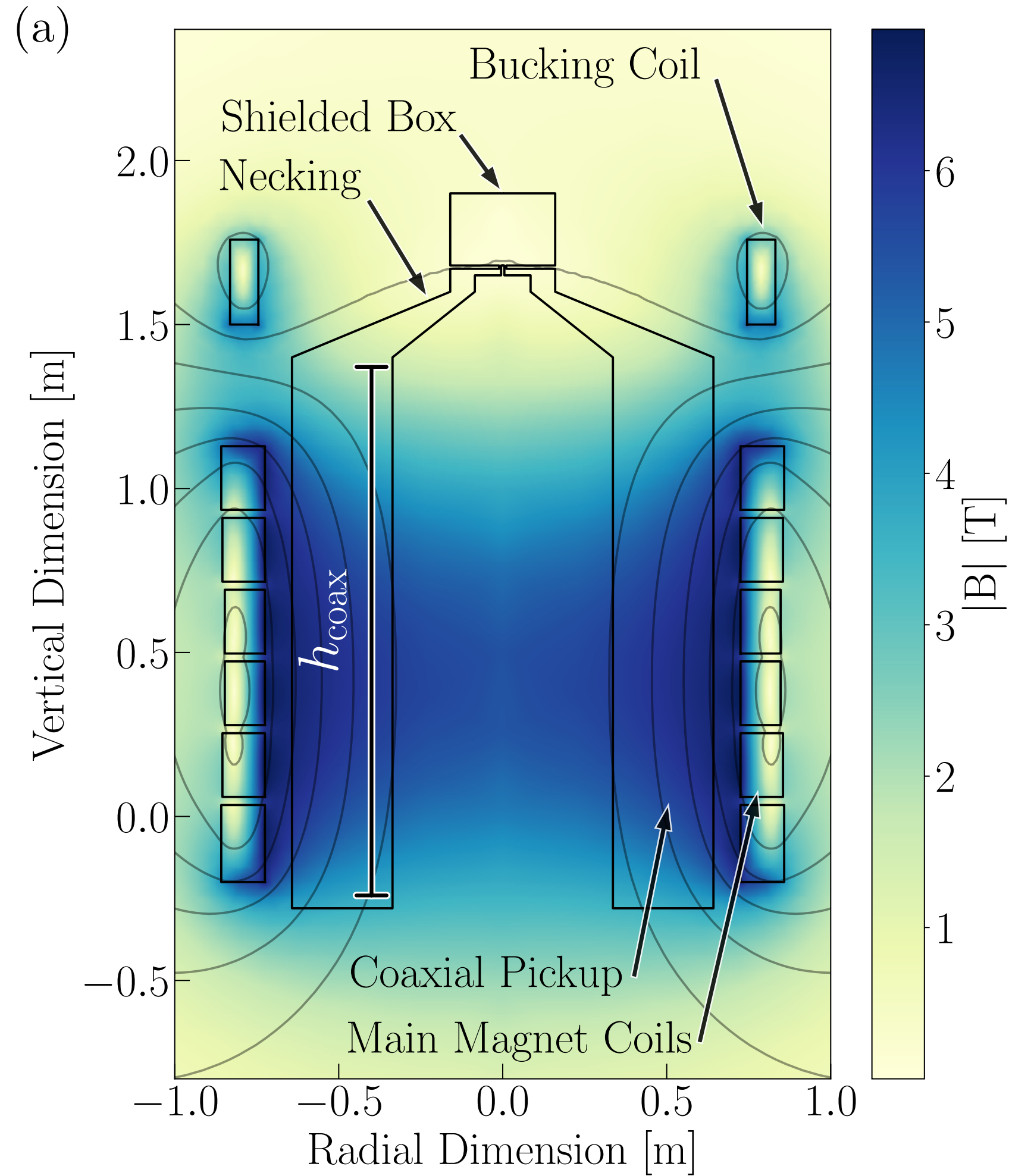


$$Q \approx \frac{\Delta\omega}{\omega_{res}}$$

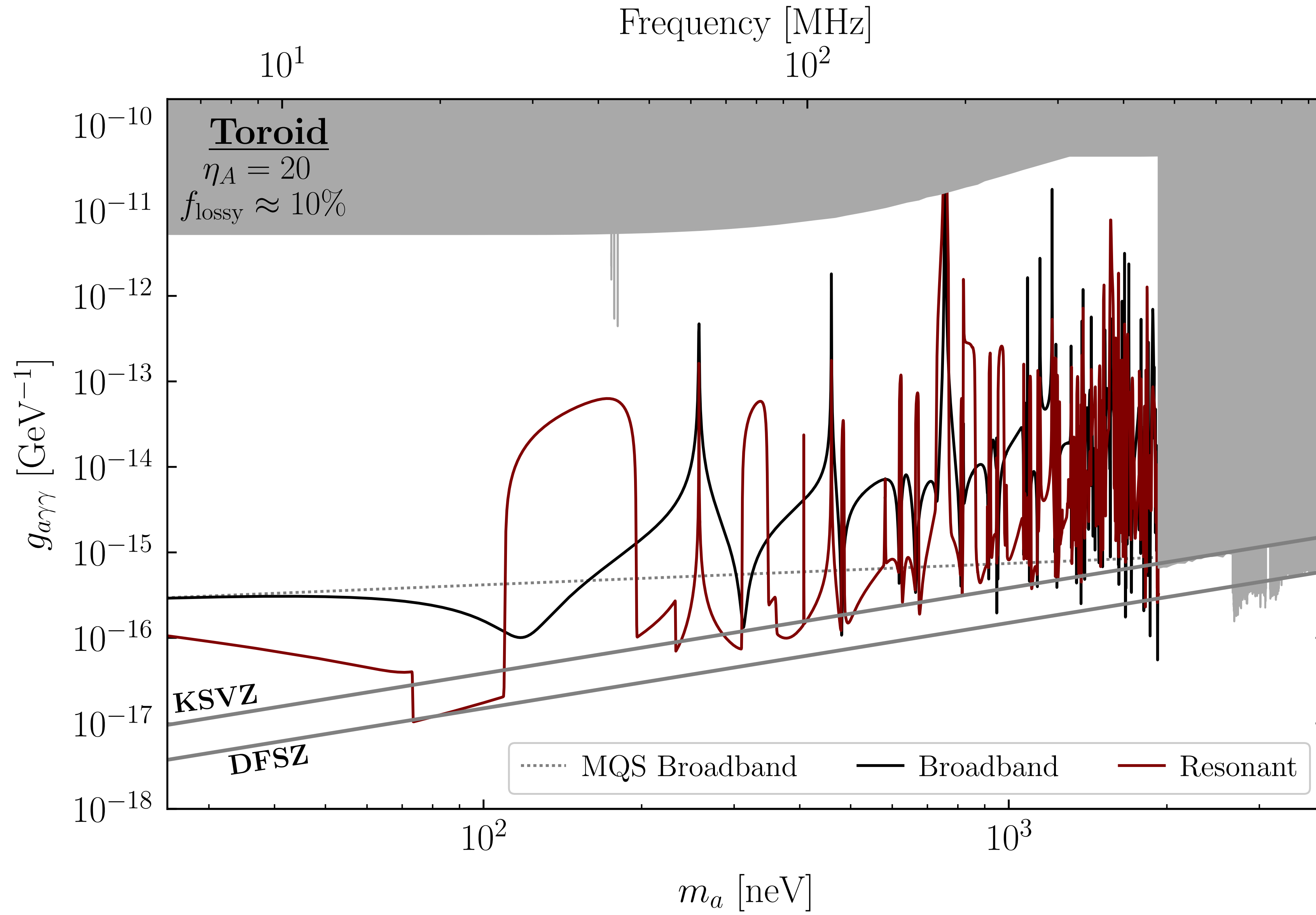
SCANNING SENSITIVITIES FOR LUMPED ELEMENT DETECTION



THE FUTURE OF LUMPED ELEMENT DETECTION



BROADBAND SENSITIVITIES FOR LUMPED ELEMENT DETECTION



BACKUP SLIDES

QUANTUM LIMITED SENSITIVITIES FOR LUMPED ELEMENT DETECTORS

Total Noise PSD

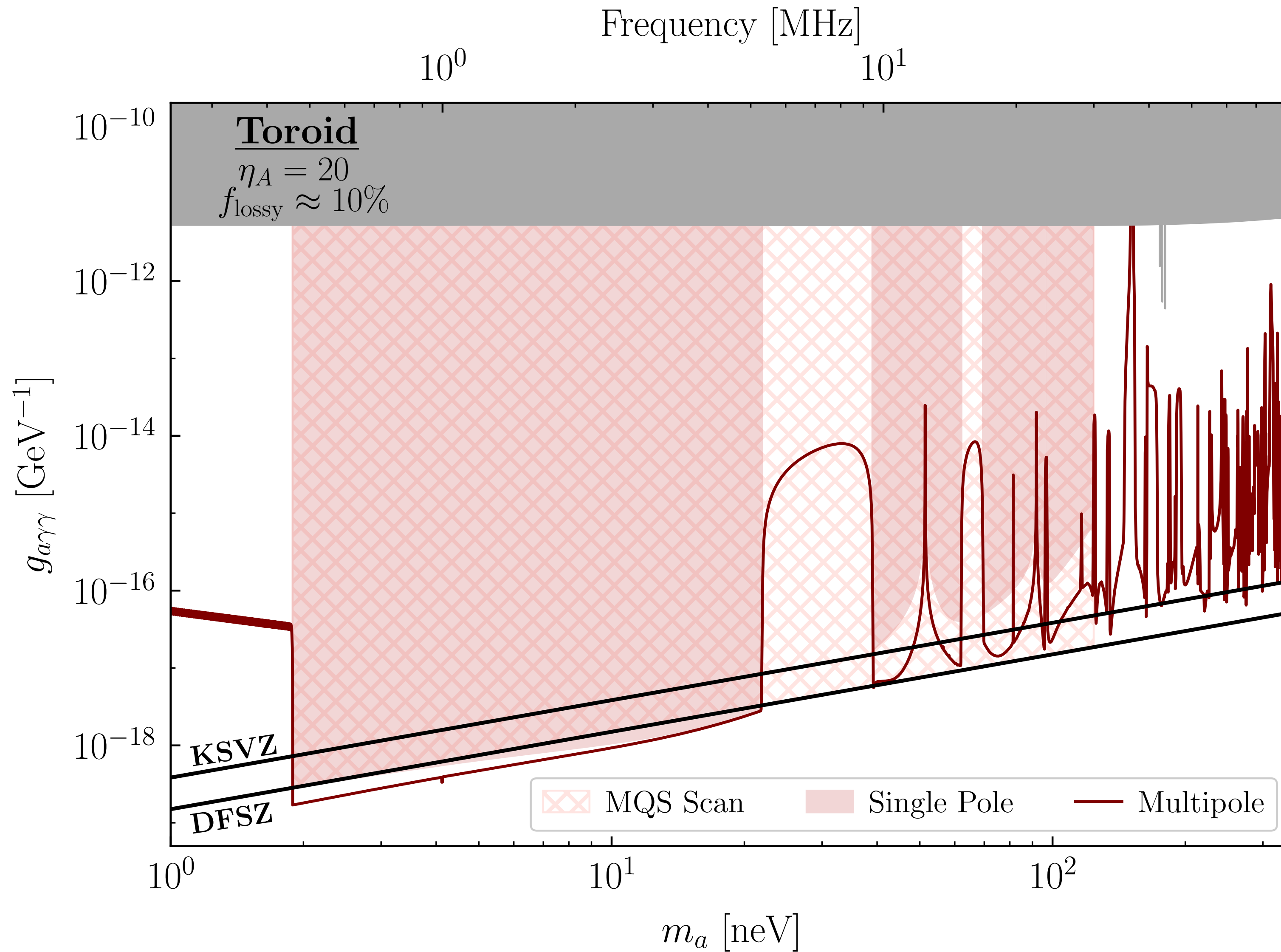
Thermal noise Noise-generating resistance Imprecision Noise

$$S_{II}^{\text{noise}}(\omega) = \frac{2\omega}{\pi} \left[\frac{1}{\exp(\omega/T) - 1} + \frac{1}{2} \right] \frac{R_{\text{th}}}{|Z(\omega)|^2} + \frac{S_{II}^{\text{imp}}}{2\pi} + \frac{S_{VV}^{\text{BA}}}{2\pi|Z(\omega)|^2}$$

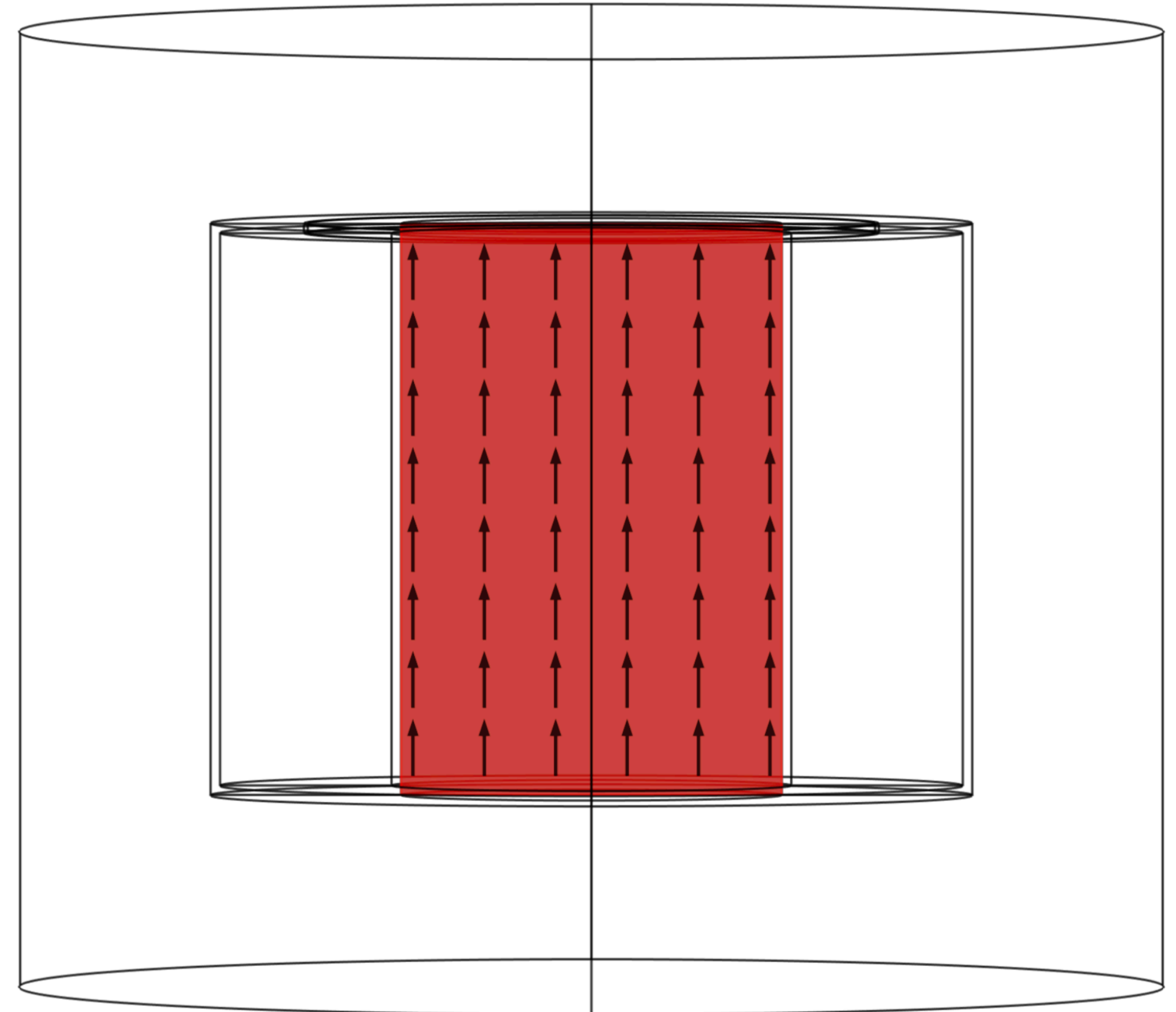
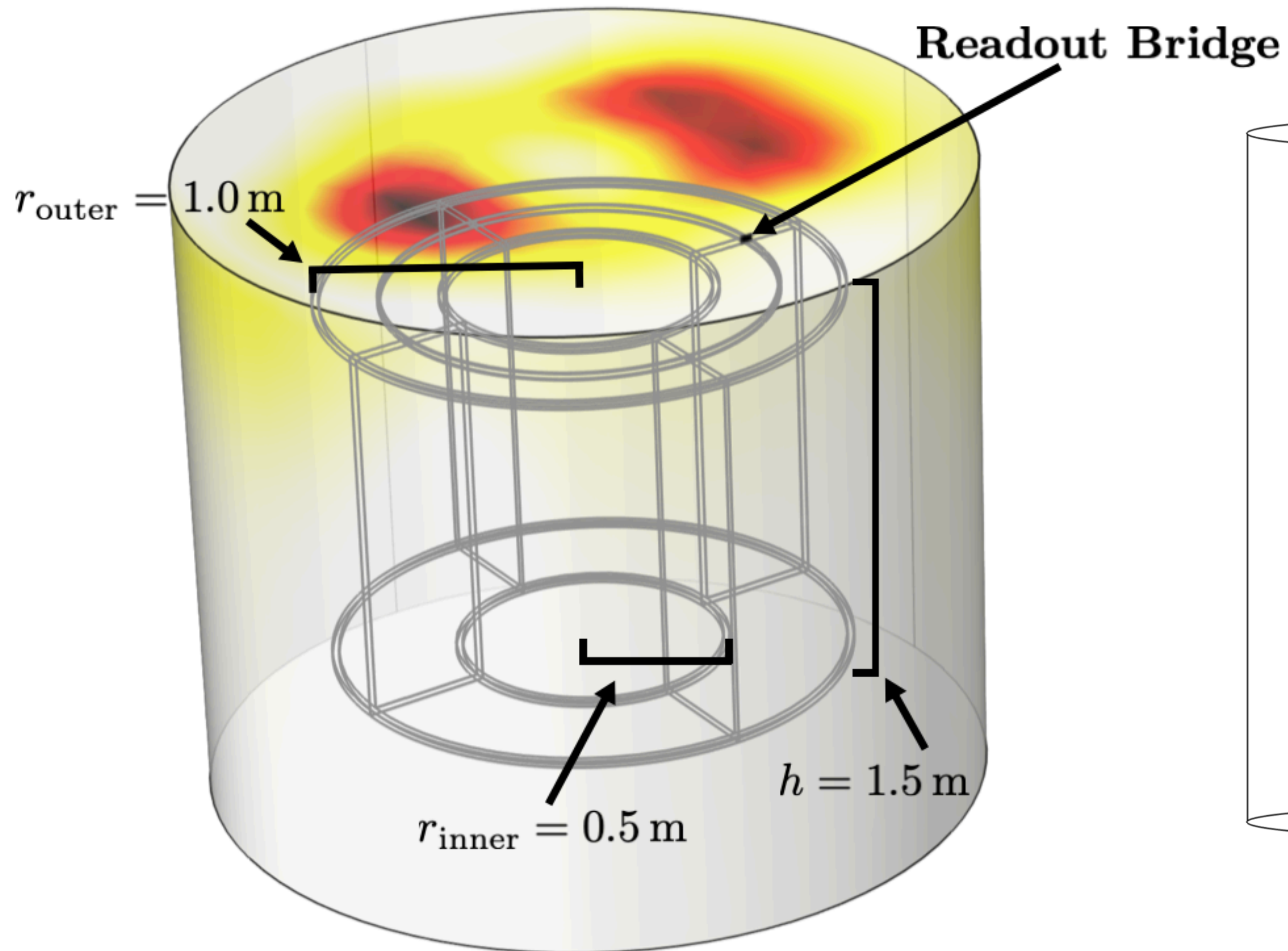
$$\eta_A = \frac{\sqrt{S_{II}^{\text{imp}} S_{II}^{\text{BA}}}}{\omega}$$

Backaction Noise

DMRADIO-GUT SENSITIVITY PROJECTIONS



SENSITIVITY WITH A SOLENOIDAL GEOMETRY



SENSITIVITY WITH A SOLENOIDAL GEOMETRY

