

# Hydrogen single pion data in $\Delta$ region



UNIVERSAL NEUTRINO GENERATOR  
& GLOBAL FIT

VS.



Who will win?

Update for DUNE, MINERvA January 2024<sup>1</sup>

# GENIE vs BEBC H single pion data, who will win?

The GENIE model for resonances, especially form factors has become untethered from H and D data and what it does is not really documented

The BEBC Q2 data on hydrogen at  $10 < E_\nu < 200$  GeV is a powerful dataset with  $\sim 7\%$  systematic uncertainty

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$1\pi$  anchors resonance rate and pion multiplicity ND constraints

The combination implies uncertainty in the energy dependence that we should be applying to DUNE and within nusystematics

# Technical notes available (skip this slide)

Many components to this nearly complete work

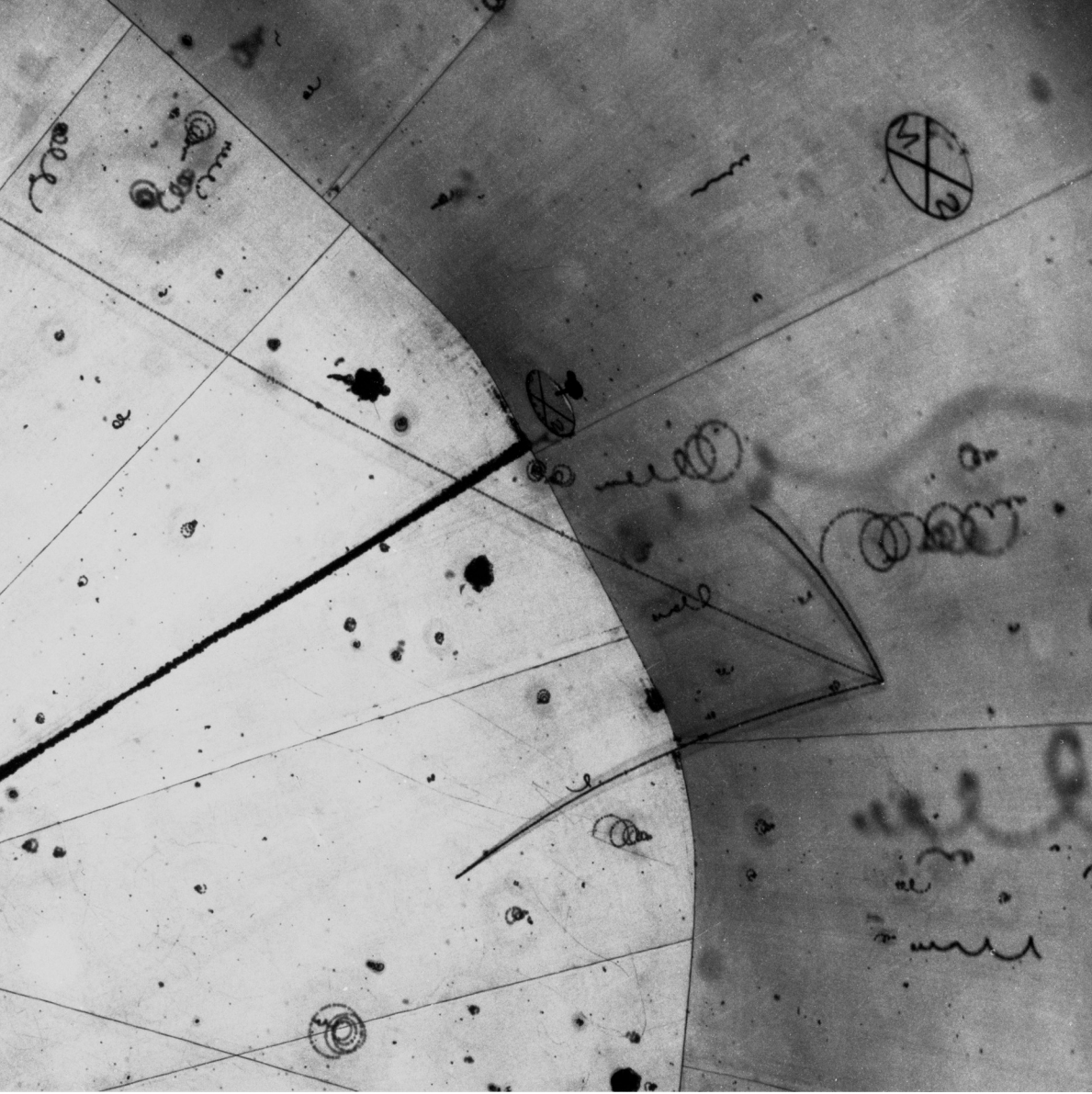
Main tech note in MINERvA docdb:32216

Side note on Diffractive process MINERvA docdb:32152

Side note on SIS region MINERvA docdb:32234

Studies by Bode Applegate and Ben Utt: 30791, 32249

Energy dependence MS theses by  
Ishmam Mahbub and Asit Srivastava



## Three prong event on H

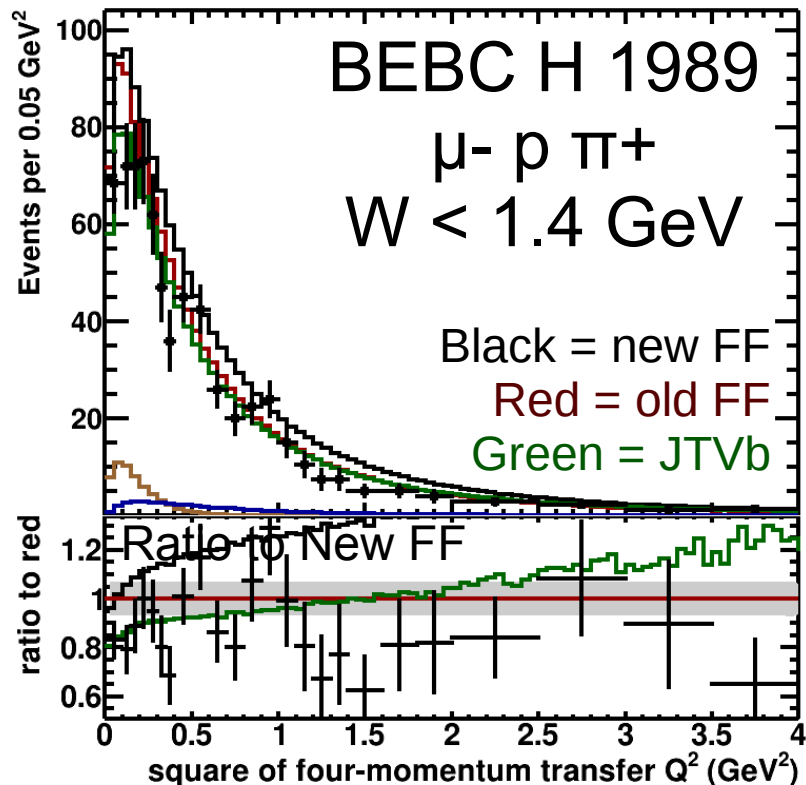
This one from ANL 1970  
Featured in Physics Today  
Today's analysis BEBC 1980s

$\nu\mu + p \rightarrow \mu^- p \pi^+$   
has ++ hadron state

$\text{anti-}\nu\mu + p \rightarrow \mu^+ p \pi^-$   
has neutral hadron state

No missing P, no neutrons  
No FSI, no backgrounds  
95% scanning efficiency<sup>5</sup>

# Before going into the details, this is one end result



1056 events on H from Jones:1989  
reevaluated normalization on  $\sigma$   
Transfer norm to  $Q^2$  event rate  
add estimated  $Q^2$  smearing effects

GENIE 3.4.0 with several configs  
no nuclear effects for hydrogen  
no neutrons in the final state  
diffractive and DIS components

Cross section at 30 GeV is all from  
The  $W_2$  structure function  
Practically constant with  $E_\nu$

GT Jones WA21 ZPhysC 43 (1989) p.527  
Rebinned for resolution, statistics

# Need the best BEBC data $\sigma_H$ for one $\pi^+$ $W < 1.4$

Two papers, two normalizations presented, effectively two fluxes

Allen:1986 takes the flux from beam monitors in wide band beam  
9% uncertain on integrated flux plus acceptance errors

Jones:1989 7% bootstraps the integrated flux using inclusive  
narrow band beam  $\sigma_{Ne}/E$  and measured  $\sigma_H/\sigma_{Ne}$  in WBB

I updated  $\sigma_{Ne}/E$  to use Seligman's "world average"  $\sigma_{Isoscalar}/E$   
They seem independent & consistent, so averaged the two results.

Final  $\sigma_H$  (one  $\pi^+$   $W < 1.4$ ) =  $57.2 \pm 1.8$  stat  $\pm 3.9$  syst  $\times 10^{-40}$  cm<sup>2</sup>

# Transfer the normalization from $\sigma$ to Q2 event rate

Final  $\sigma_H$  (one pi  $W < 1.4$ ) =  $57.2 \pm 1.8$  stat  $\pm 3.9$  syst  $\times 10^{-40}$  cm<sup>2</sup>

GENIE has a value for this for every model configuration  
Energy dependence is so mild, flux weighted average is precise  
For example, **old form factors give  $66.5 \times 10^{-40}$  cm<sup>2</sup>**

Since the Q2 event rate are the same events  
(and acceptance effects are approximately flat)

so ok to scale GENIE to the integrated Q2 data so that  
The ratio (1.16 in this case) between GENIE and data is preserved

(Scale can be reused for other  $W$  regions, I think, not sure) <sup>8</sup>

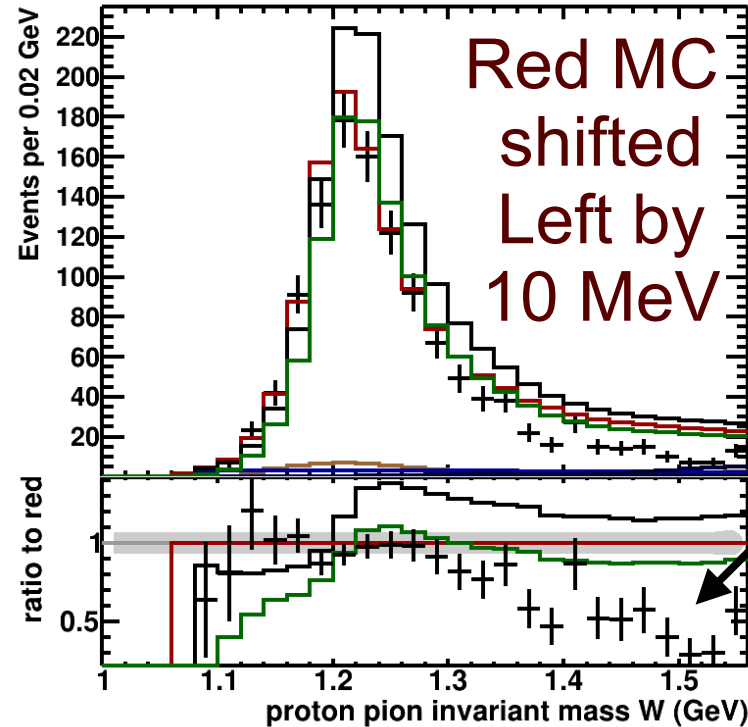
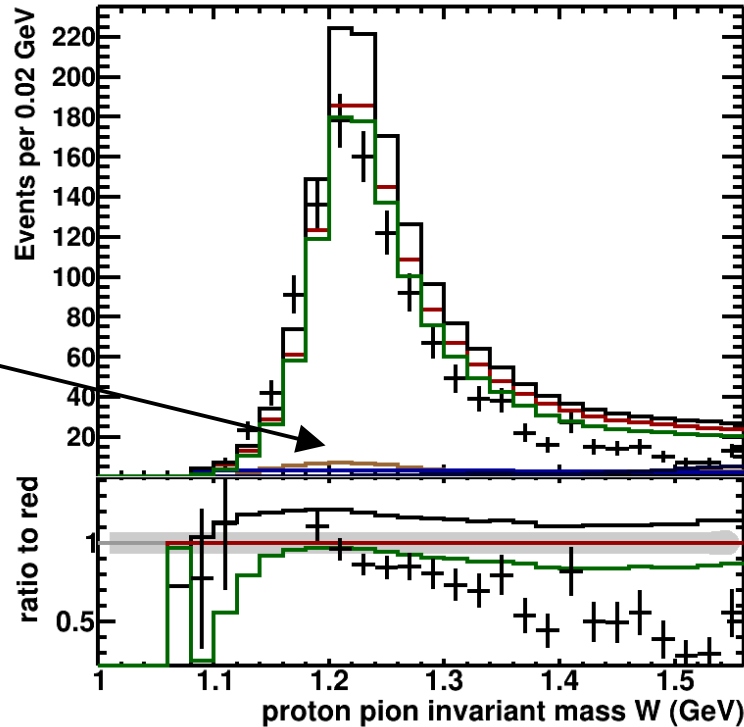


# Check the uncertainty on the $W(p\pi)$ cut

For deuterium, nuclear effects might make this a tricky cut  
Hydrogen is ok except data peaks at 1220 not 1232 MeV

Jones  
WA21  
1989

DIS  
DFR  
non $\Delta$   
too  
small  
to see

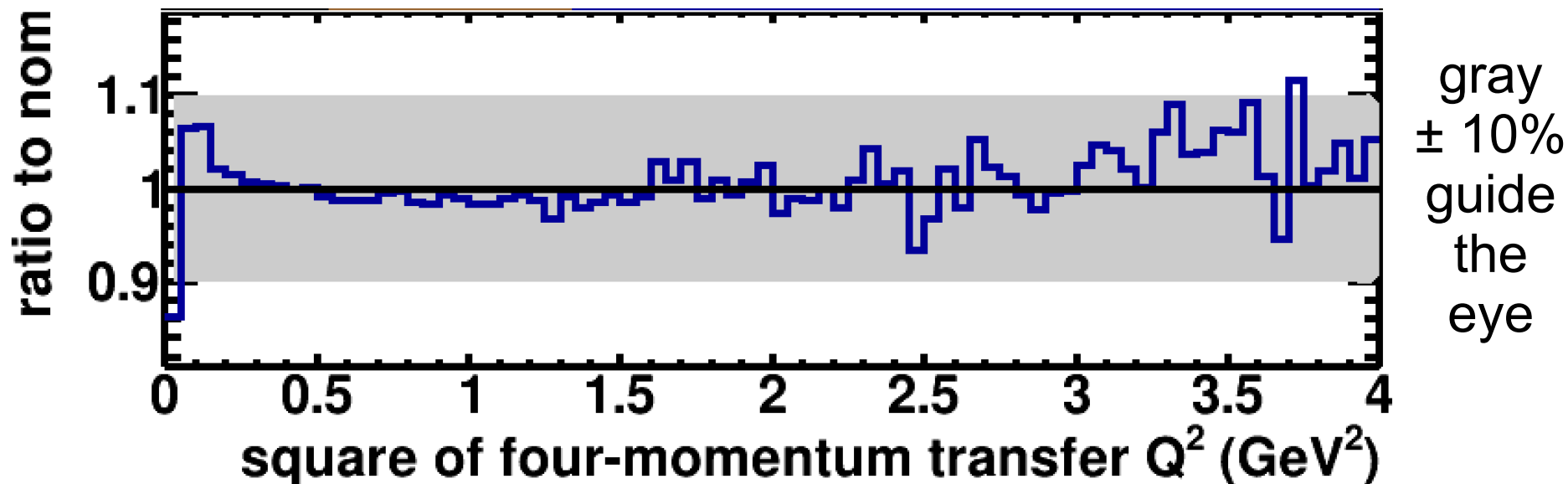


$\Delta^{++}$   
tail  
MC  
too  
high

Real or 3% bias in proton pion momenta ? Only 1% on selection<sup>9</sup>

# Check smearing effects and choose binning

For the fully **inclusive** process (for  $\sigma/E$ ) the resolution on  $Q^2$  in Jones:1987 to be 20% at high  $Q^2$  and 0.02 GeV at low  $Q^2$



It narrows the peak? The three-prong sample should be better!  
Hint that Emu resolution becomes  $dQ^2/Q^2 \sim 10\%$  at high  $Q^2$   
Using this “worst case” and forward fold !

# Other systematics via GENIE sample (can skip slide)

A 0.5% magnetic field bias has negligible effect.

If a large = 3% Ehad bias solves W bias  
implies some additional Q2 bias, not evaluated

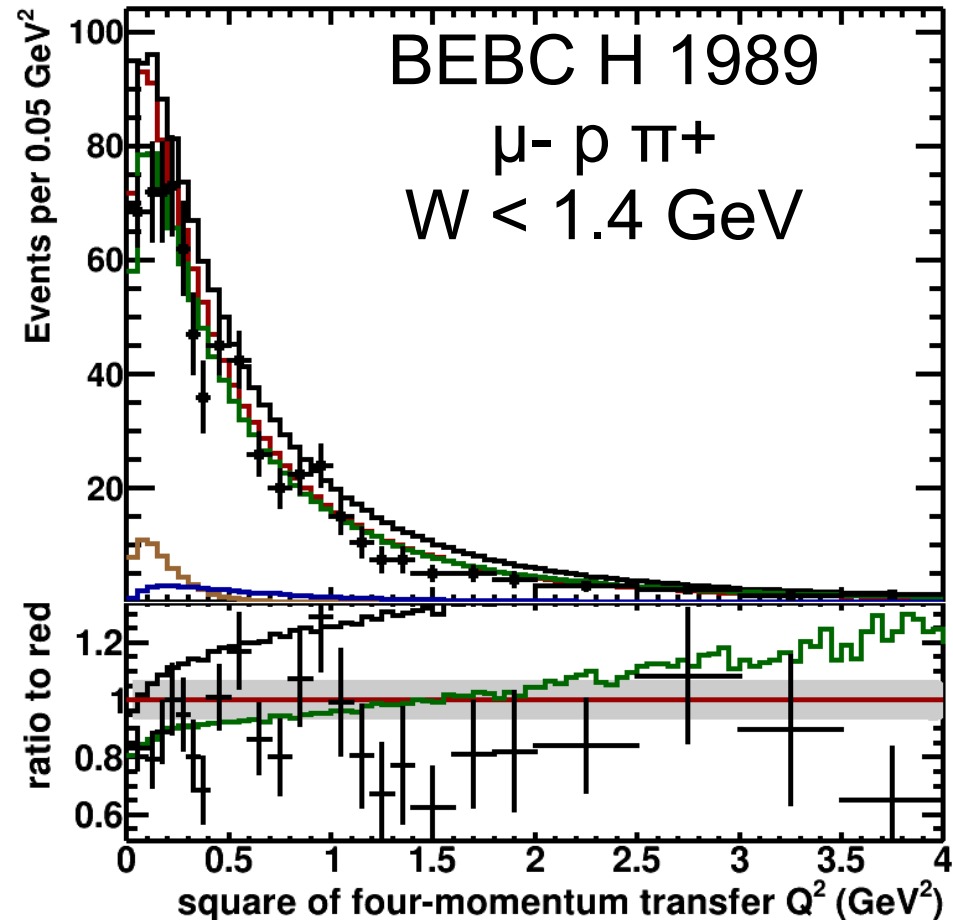
Flux shape has negligible effect  
Tried NuMI/MINERvA-like distortions at peak and in tail

Didn't try hard to reconstruct resolution from Ehad and Emu  
Except that Q2 resolution  $\approx 2 \times$  Emu resolution

Did not try to reproduce the 3C (missing momentum) constraints  
important for neutron final states in D, not for H

Did not try unseen inner Bremsstrahlung or radiative photon

# Here is that first plot again and model descriptions



Note: low  $Q^2$  rolloff feature

Black line is G18 out of the box  
New form factors no tuning MA  
Its way off, above all but one bin

Red is old form factors ~ GENIE v2  
MA was tuned to BEBC, ANL, BNL

Green is Tena Vidal 02\_11b tune  
as in AR23\_20i. Start from Black...  
Scale down resonances 0.84  
Small change in MARES, MAQE  
Almost eliminate DIS  $1\pi$  for  $W < 2$   
No modification of diffractive<sup>12</sup>

The red line is an ok fit, green on the other side of ok

Black new FF is G18 out of the box

Red is old FF, GENIE v2

Green is JTVb tune like AR23\_20i

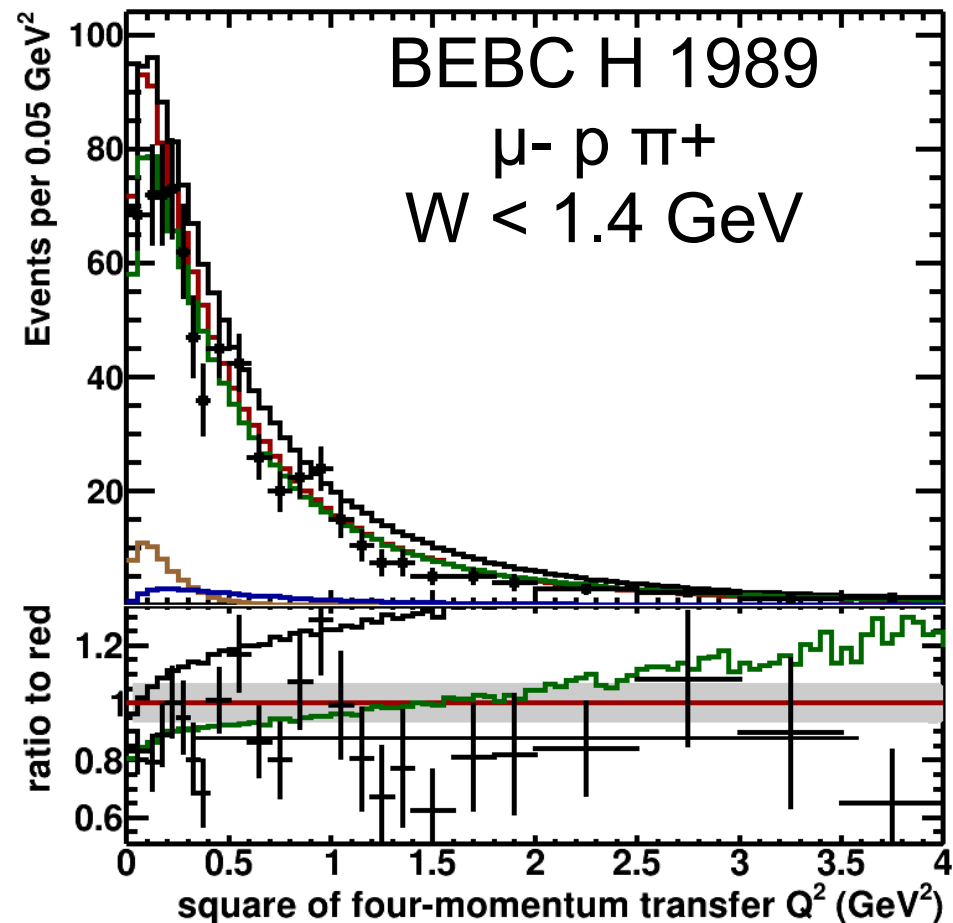
Lower, black horizontal line in ratio is fitting the residual data/MC

Constant 0.88 is an ok fit

Pvalue  $\sim 0.05$  including flux error

Slope+Intercept fit is NOT better

Meh P-value mostly the jumpy data



JTVb is worse  $\chi^2$  by 2 units<sup>13</sup>

# Who needs a new, best tune? Want best uncertainties

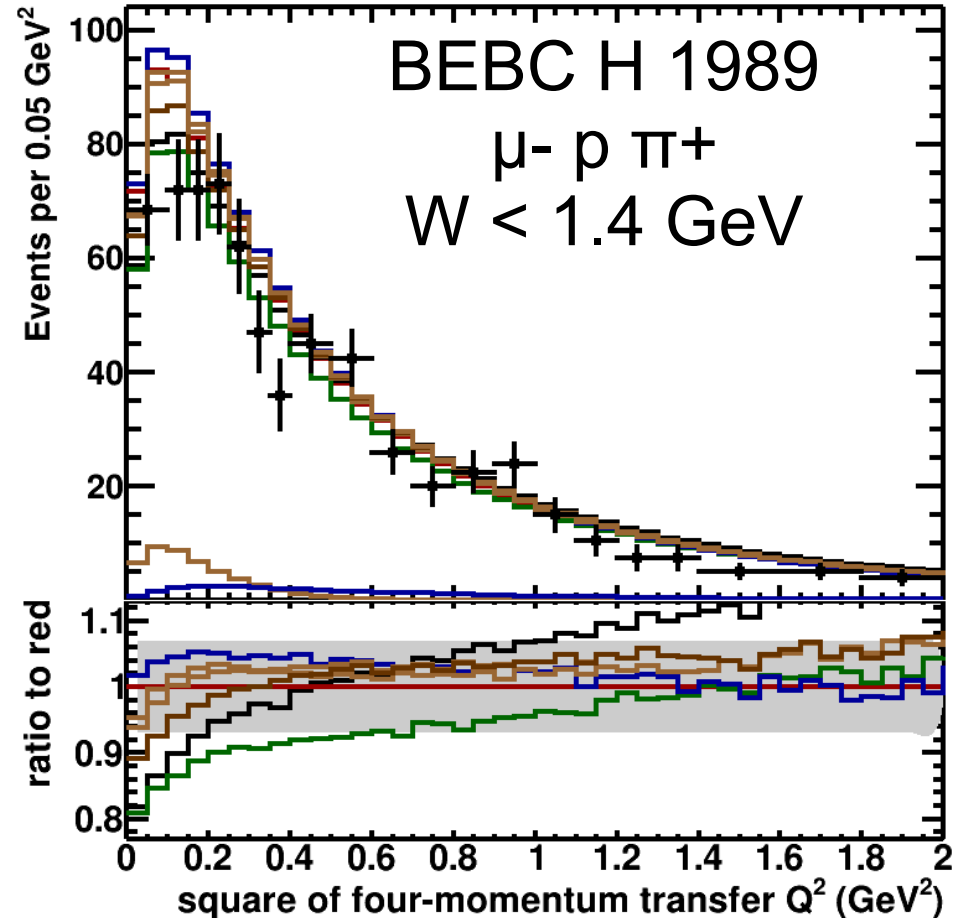
Taking an unexpected point of view in the next few slides.  
I want to **tune to the red model** (old FF, tuned GENIE2-like)  
in the range  $0.3 < Q^2 < 1.5 \text{ GeV}^2$   
as if the GENIE2 model is Nature, mock data.

What are all the ways to modify GENIE3 to look like Nature  
and how does it compare to what the red model really does?

Don't have fitting apparatus yet, doing it by hand this time

Data is plausibly described, learned  $Q^2 < 0.3$  is weird  
want creativity with model before more work with data

# Zoom in & plot other pseudo-tunes of the black model



Red is old form factors  
“tune” is roughly to red (not data)  
So I didn't plot data in ratio here

Black line is base scaled 0.85  
Green is Tena Vidal 02\_11b

Lt browns:  $MA=1.0$  or  $MV=0.7733$   
Dk brown:  $MA=1.0$  & half diffractive

Blue: QE Zexpansion axial FF

Most line up in middle, all diverge for  $Q^2 < 0.3 \text{ GeV}^2$

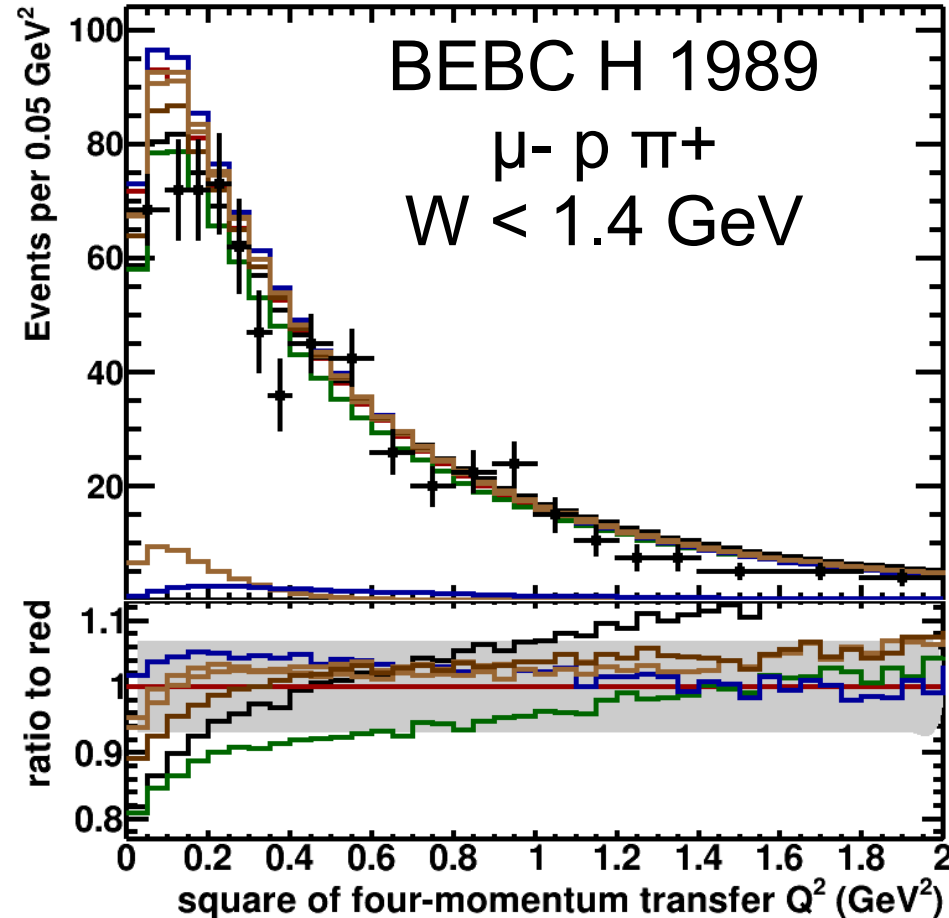
# Take-home message we already probably knew

If Red was Nature

Multiple parameter combinations  
Will successfully describe nature.

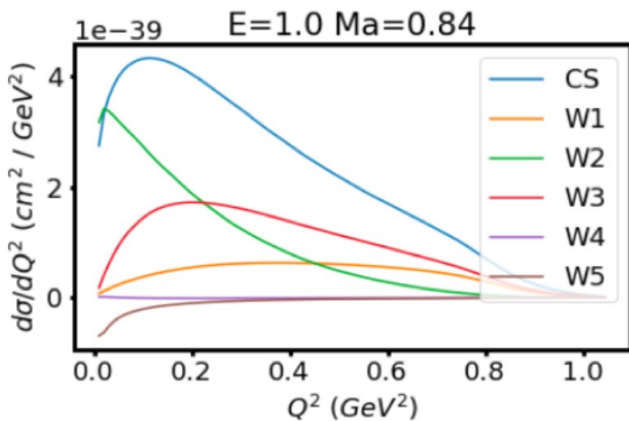
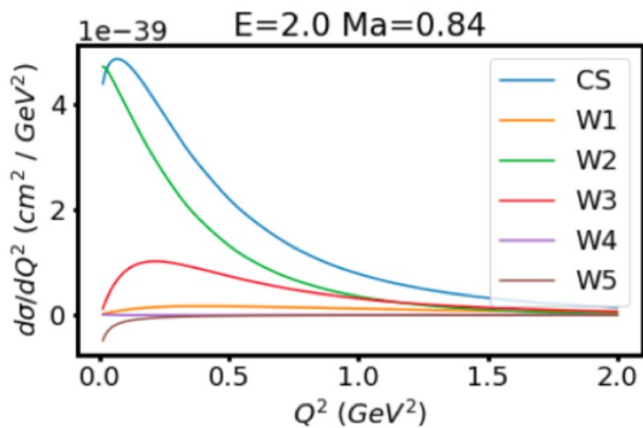
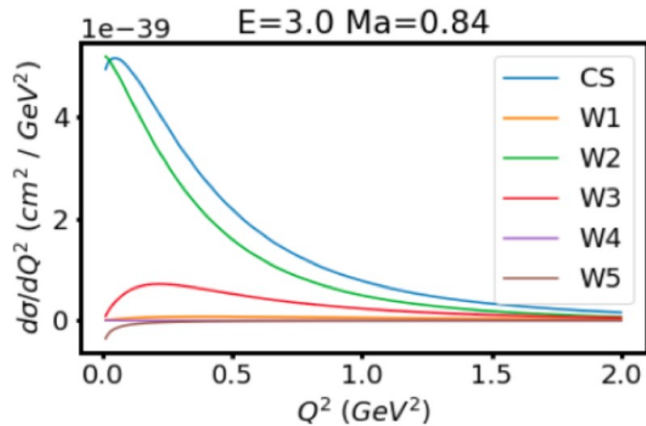
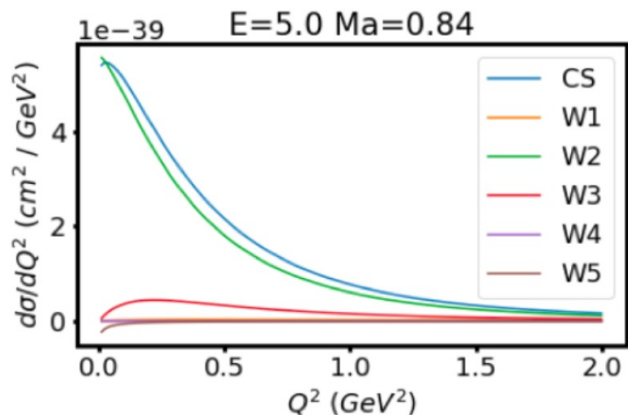
These data constrain them  
just b.o.e'd these numbers so far  
MA  $0.99 \pm 0.05$ ish, MV  $0.76 \pm 0.04$   
Zexp + Diffractive + DIS scale.  
want some kind of covariance

Nusystematics needs parameters  
and some version of the covariance  
probably simplified. Ugh.





# Constraining the W2 structure function to 7% syst



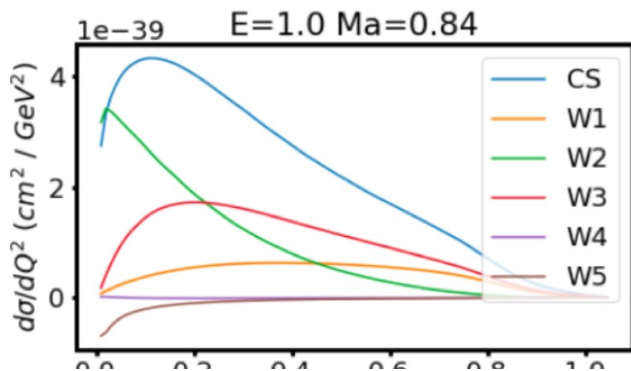
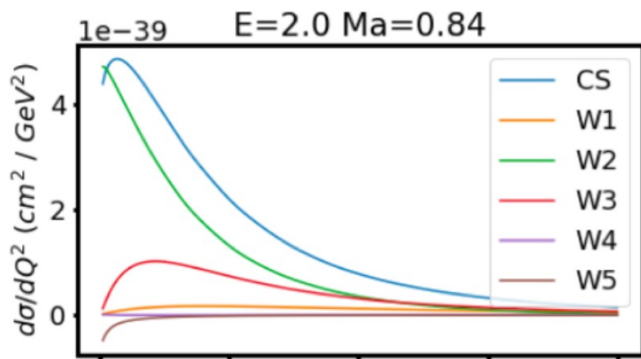
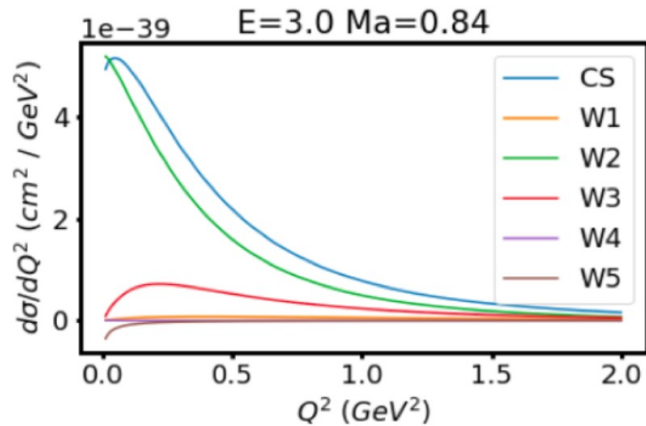
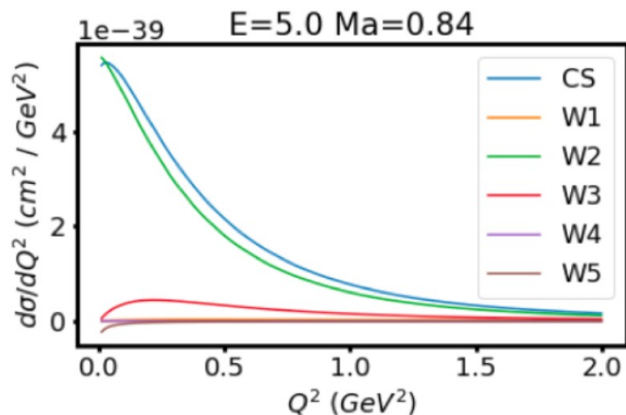
Structure functions  
get multiplied by  
factors of  
 $1/E^2$  and  $1/E$  and  $1$

Form factors are  
inside structure fun

Kinematic boundary  
High  $Q^2$  reach  
Decreases at low  $E$

Ishmam Mahbub MS thesis Duluth 2021  
Delta model by Lalakulich and Paschos 2005

# Goal is to go beyond form factors as only uncertainty



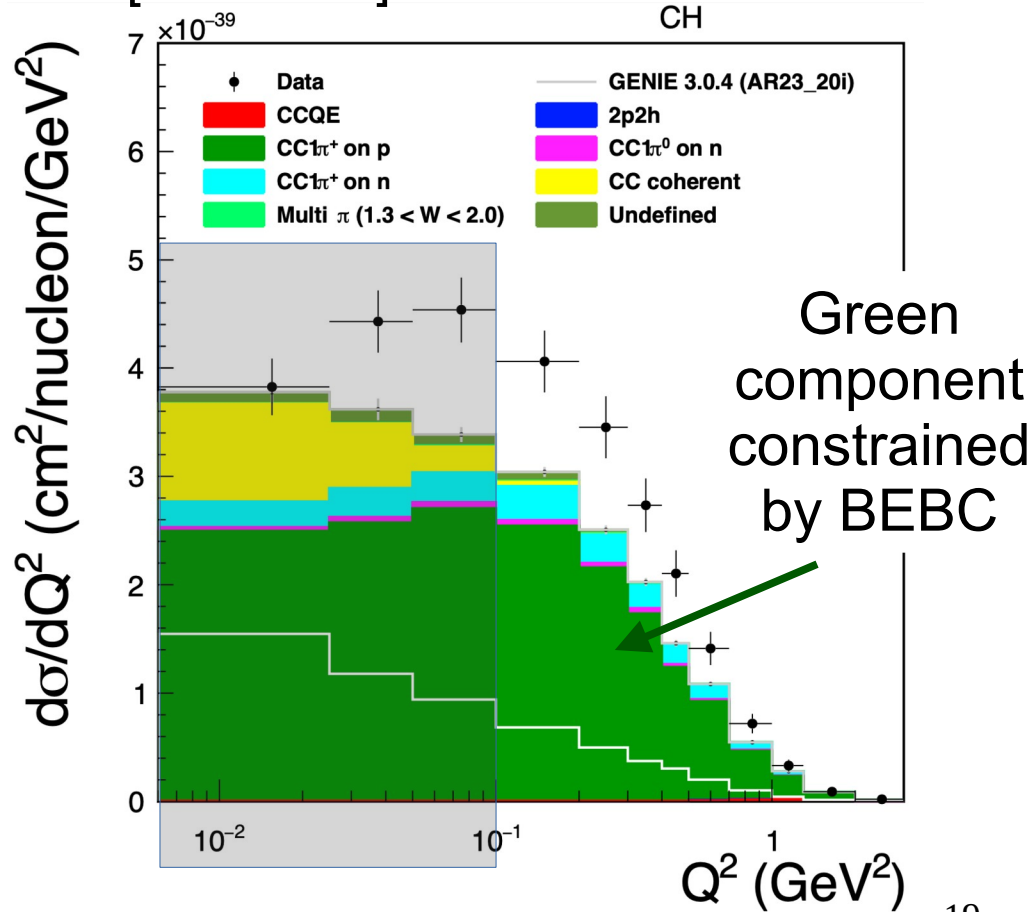
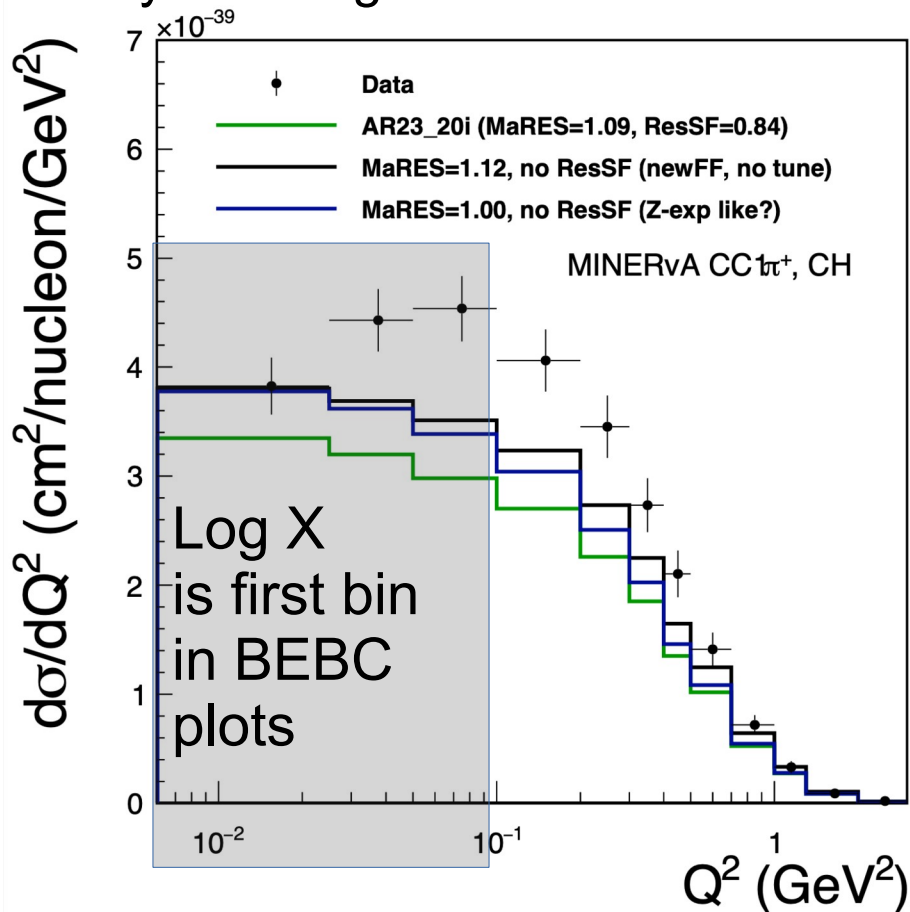
Even the W2 structure function all that remains at high energy on its own is complicated This is simplified form factor  $C5V=0$  but really its not

$$\frac{V_2}{3} = (C_3^V)^2 \frac{2}{3M_R^2} Q^2 [q \cdot p + m_N^2 + M_R^2] + \frac{(C_4^V)^2}{m_N^2} \frac{2}{3} Q^2 [q \cdot p + m_N^2 - m_N M_R] + \frac{C_3^V C_4^V}{m_N} \frac{2}{3M_R} Q^2 [q \cdot p + (M_R - m_N)^2] + \frac{2}{3} \left[ (C_5^A)^2 \frac{m_N^2}{M_R^2} + \frac{(C_4^A)^2}{m_N^2} Q^2 \right] [q \cdot p + m_N^2 + m_N M_R]$$

Delta model by Lalakulich and Paschos 2005 (A2)

# Compare to related configurations on CH & MINERvA

Plots by Jaesung Kim Data from Bercellie et al. [MINERvA] 2023:  $35 < KE_{\pi} < 350$  MeV



MidQ2 models 20-30% low vs MINERvA CH, <10% high vs BEBC H <sup>19</sup>

# Pause before going on. What parameters?

Can use MA, MV, scale Diffractive, scale DIS, scale RES

Old vs. new FF expressions. What about  $W = 1220$  ?

Unless MV really is pinned by electron data, no independent MA.

Data is so jumpy (for unknown reasons, fluctuations we guess)

Dubious we would get a serious constraint anyway.

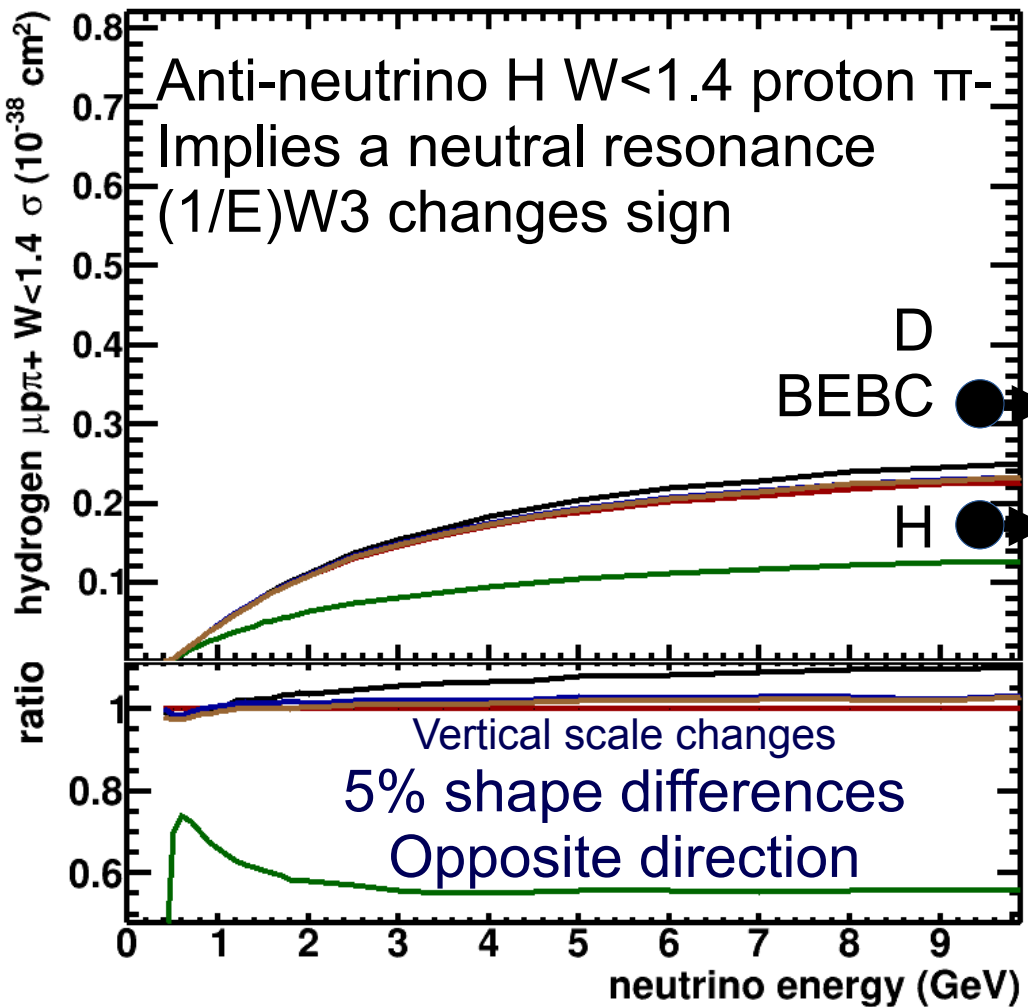
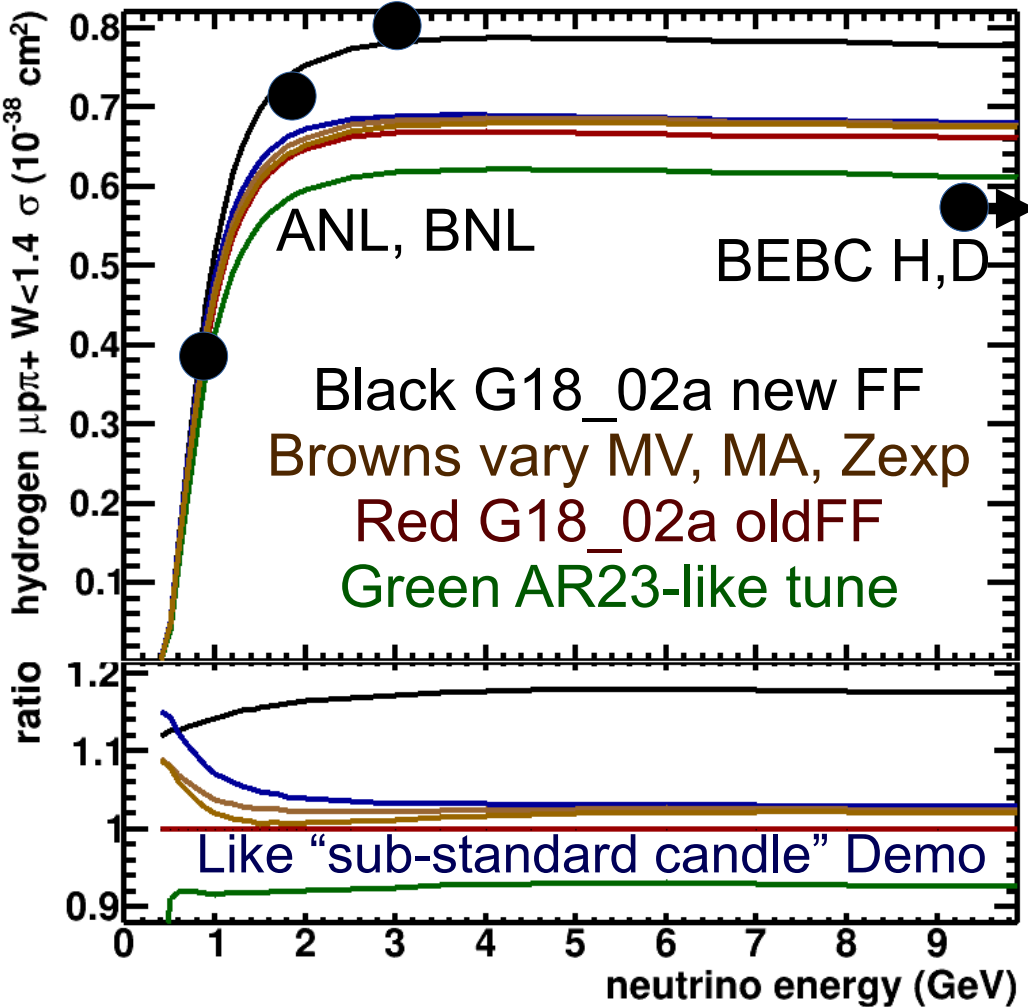
Demo using Z expansion for axial form factor for blue line.

Wondering if further hack lets me use Abi's uncertainties

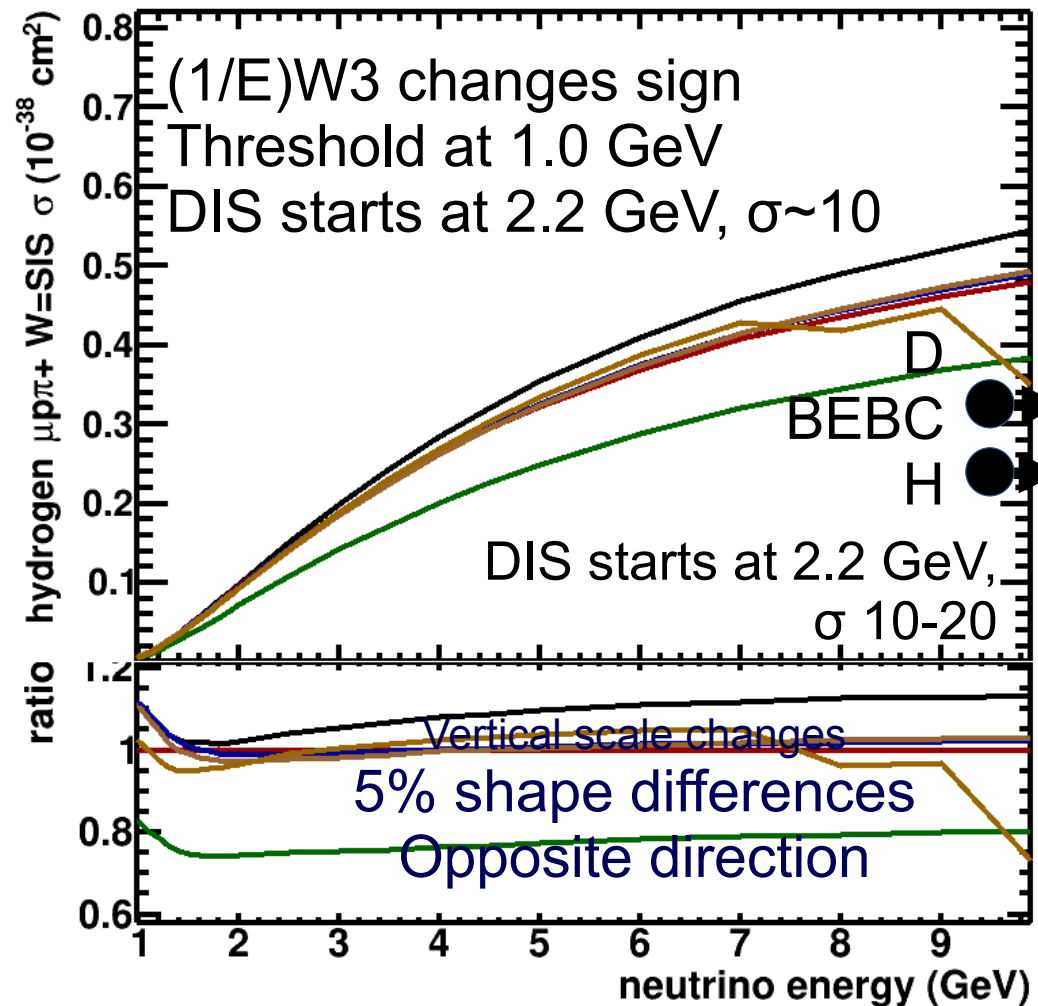
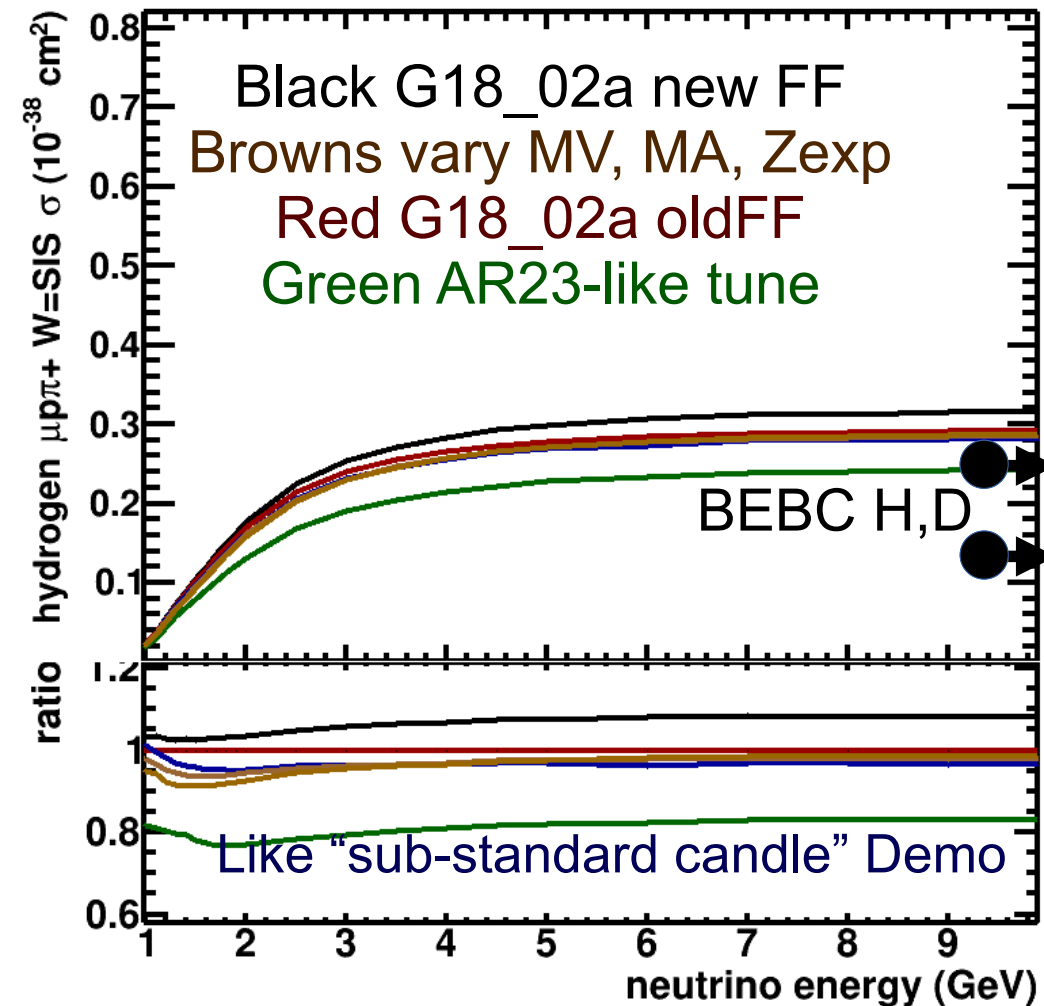
To give more freedoms to the fit compared to just MA?

Difficult design situation. Does 30 GeV data affect DUNE? 20

# Projected onto oscillation region, 10% effects



# 1.4 < W < 2.0 SIS 1π+ region energy dependence



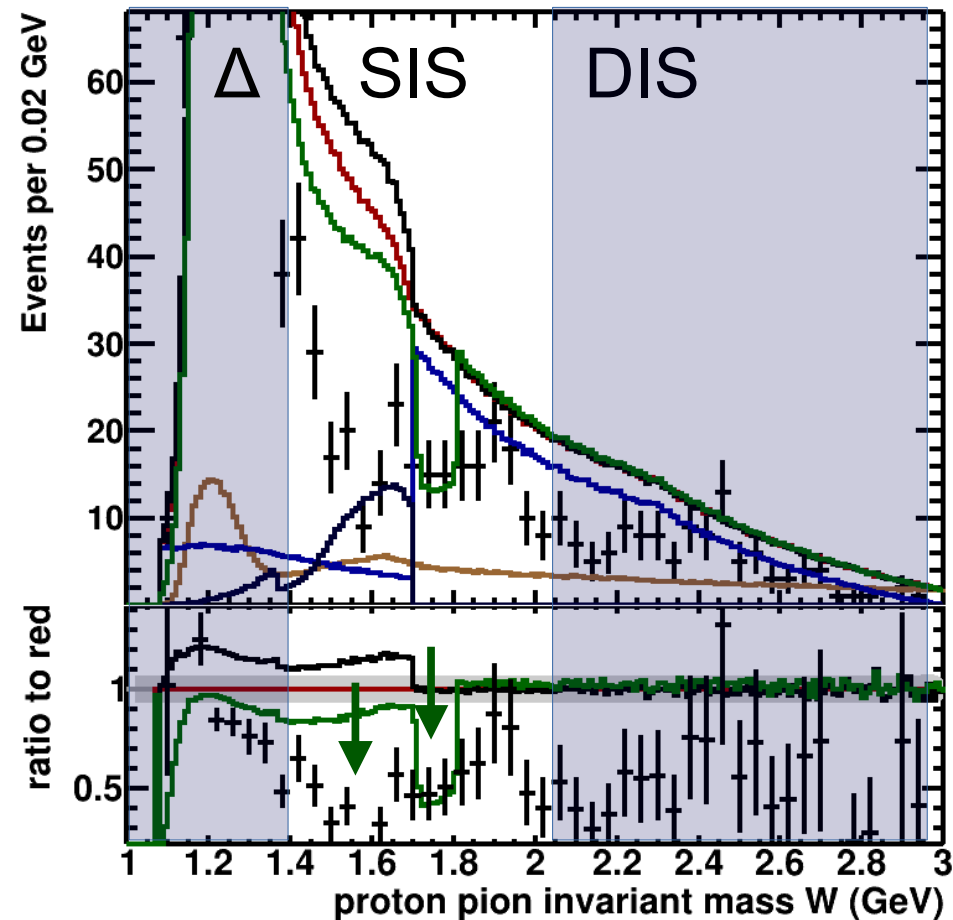
# What about higher W but still single $\pi^+$ sample?

Focus on the near  $\Delta$  region today  
 $1.3 < W < 1.5$  or so  
suppressed vertical axis

This  $p \pi^+$  channel has a  
resonance desert  
only the tail of the  $\Delta$  contributes

GENIE rate is off by x2  
 $\Delta$  tail is too high, too long

More to see here  
Save for future SIS DIS talk <sup>23</sup>



Adequate. By design! <sup>TM</sup>

# Conclusions

BEBC H data has 7% systematics  
Published a lot of basic distributions

Tuned versions of GENIEs can describe Q2 data  
For  $W < 1.4$  by construction

They give 5 to 10% different predictions in 1-2 GeV region

## Next goals

Some lightweight fitting that gives parameter ranges  
and a covariance we can use in nusystematics



## Upcoming tasks

Jarek Nowak and I are trying to describe (for a paper) How the new form factors relate to the non-Rein Sehgal framework and to electron scattering data.

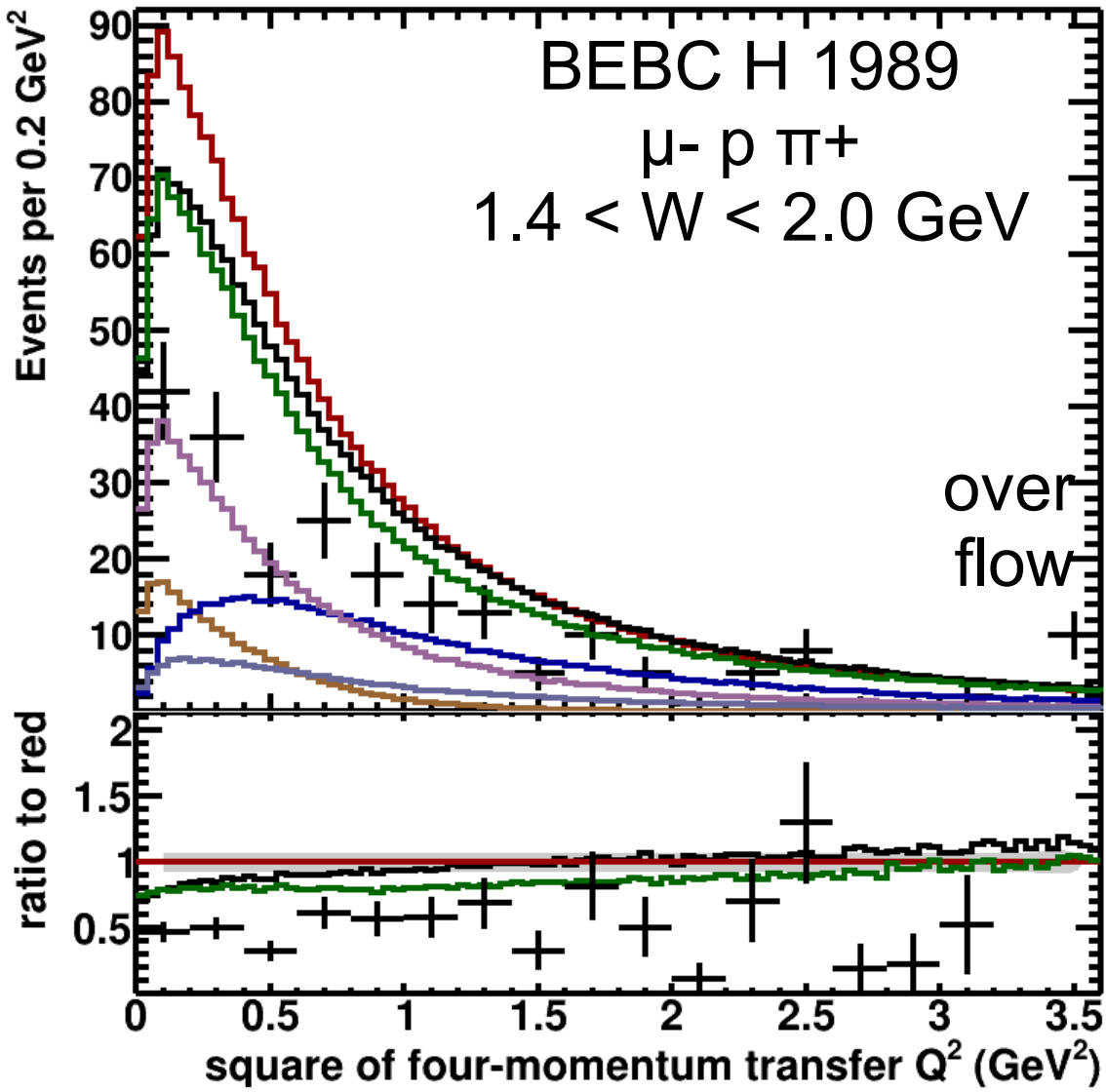
Some of the material here goes in that paper as illustration

Finish something that looks like a fit + covariance for NIUWG

Want to try again the results on deuterium  
ANL, BNL, FNAL, and the other BEBC WA25 papers

Pretty easy (lack of mental strain) to add the anti-neutrino  $Q_2$   
except the anti-nu flux choices have 2-sigma tension

# Backups and old material



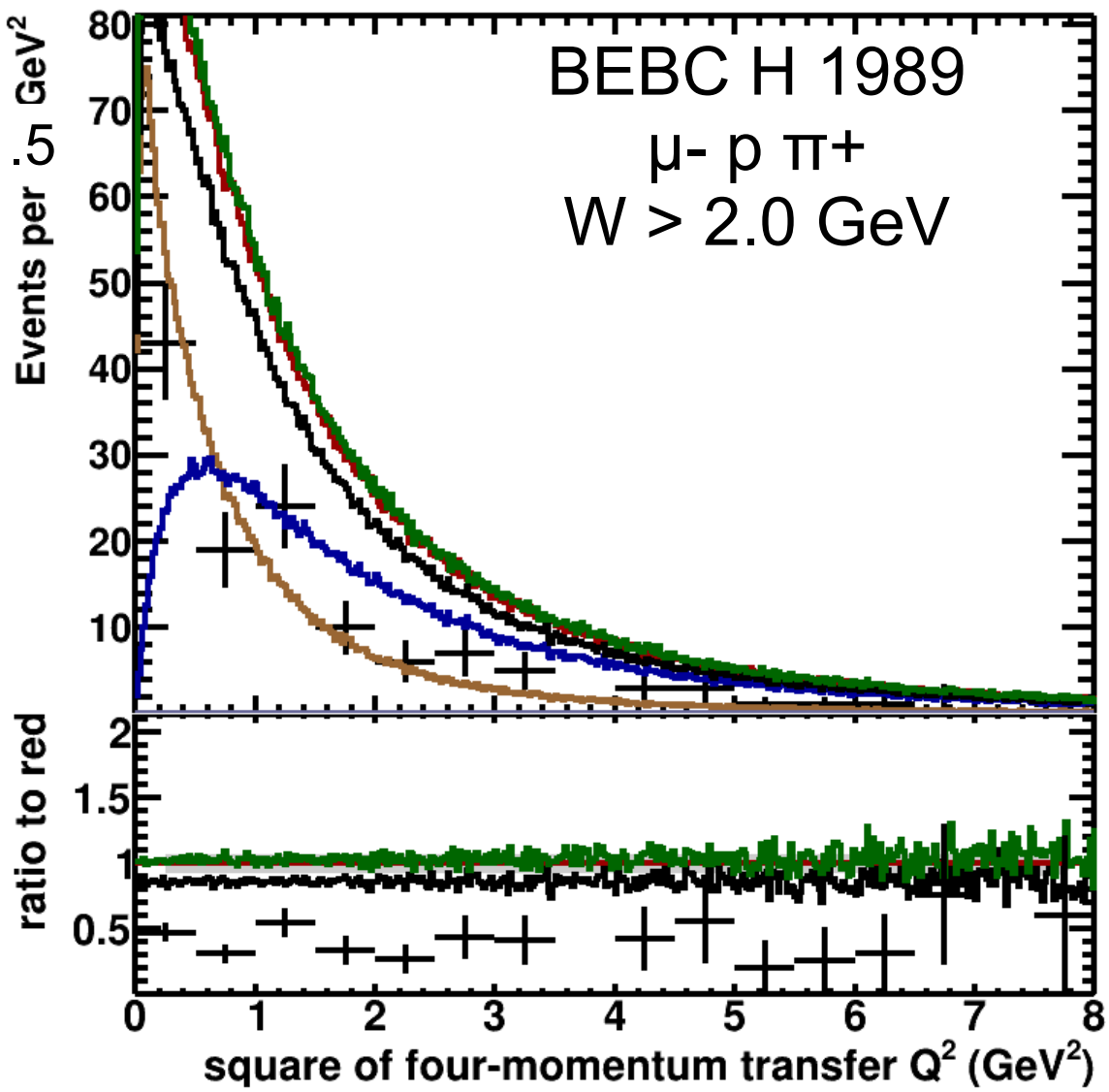
# Q2 distribution in SIS

## $1.4 < W < 2.0$ one $\pi^+$

Data bins combined 2x

- Components include
- Top to bottom
  - Purple = Delta
  - Blue = DIS
  - Brown = diffractive
  - gray/blue = higher res

Normalization is close  
 But worried ~20%



## Q2 distribution in DIS

$W > 2.0 \text{ one } \pi^+$

Only components

Brown = diffractive

Blue = DIS

Normalization seems ok

Need to check

Cant see  $\sim 10\%$  norm error

These data are the one  
 the Rein diffractive paper  
 a kind of PCAC test

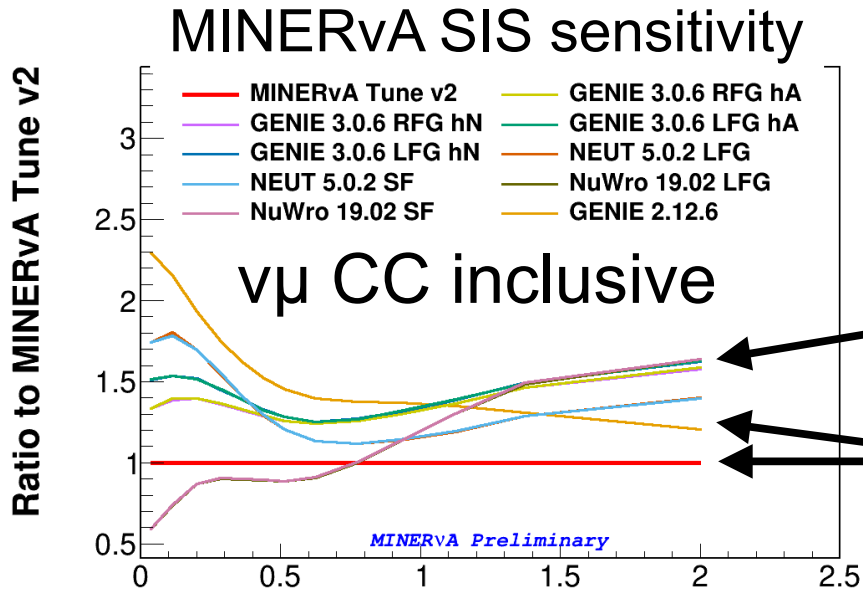
# Same high W information in table form: skip this

	1.4 < W < 2.0 neutrino	W > 2.0	1.4 < W < 2.0 anti-neutrino	W > 2.0
<b>Data average</b>	14.6 ± 1.5	9.8 ± 1.5	24.1 ± 2.9	15.5 ± 2.6
<b>Data Allen:1986</b>	14.0 ± 1.4	9.4 ± 1.4	18.7 ± 2.2	12 ± 2
<b>MC oldFF</b>	29.9	16.9	62.5	33.1
<b>DIS</b>	10.7	9.5	33.6	25.8
<b>Diffraction</b>	3.5	7.4	3.5	7.4
<b>MC JTVb</b>	25.0	17.1	51.5	33.8
<b>DIS</b>	5.5	9.8	15.1	26.6
<b>Diffraction</b>	3.5	7.3	3.5	7.2

Higher W problems for anti-neutrino  $\mu p \pi^-$  too. Future task. <sup>29</sup>

# Diffractive and SIS comments

GENIE models old Form Factors (red) and JTVb (green) 2x high  
 Diffractive alone at  $W > 2.0$  is almost data, before adding DIS  
 Though Rein paper sorta-hinted model was  $\sim 3x$  too high  
 Only data on diffractive until another experiment with a lot of H



Slope in Q2 with new form factors  
 Is more dramatic at higher  $W$   
 Causes this divergence in predictions  
 Offset from Wilkinson & Rodrigues

Genie3

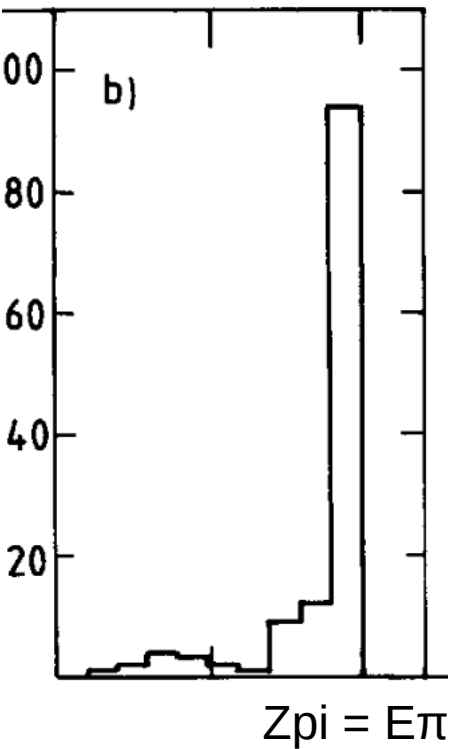
Genie2

Lots of structure here!  
 MINERvA SIS results  
 expected at NuInt24

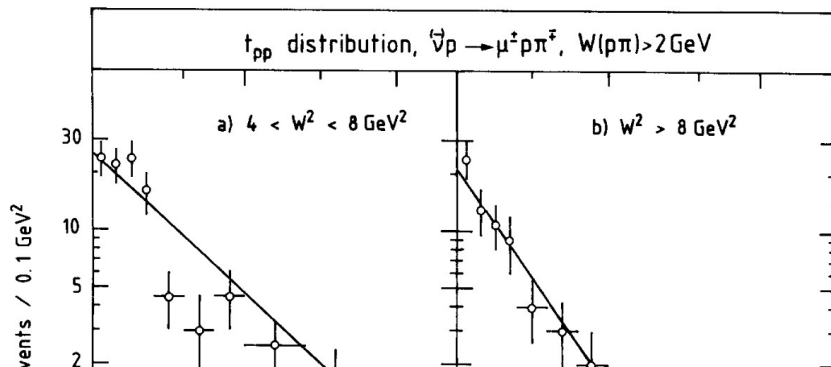
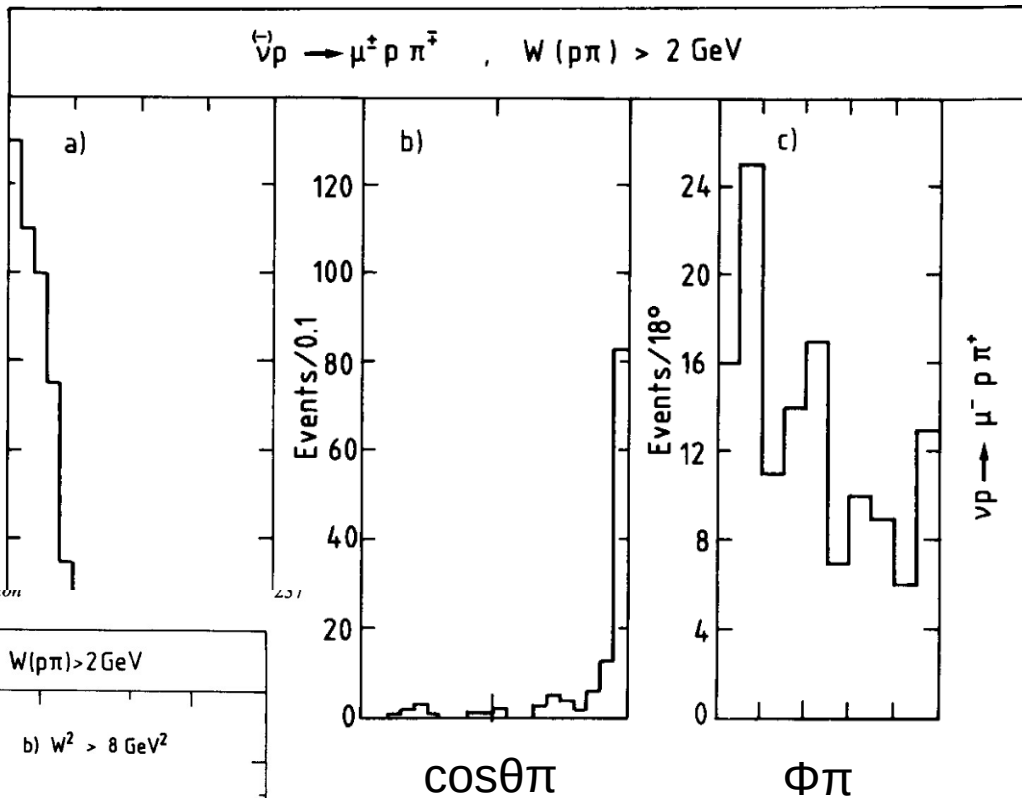
Muon  $p_T$  trends = similar to Q2

# Allen:1986 has four more $W > 2$ distributions

$z_\pi$  -distribution

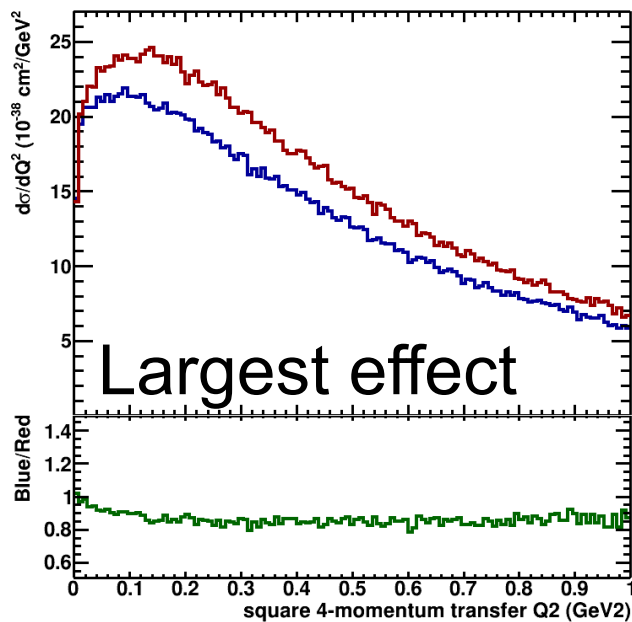


$\nu_p \rightarrow \mu^- \rho \pi^+$

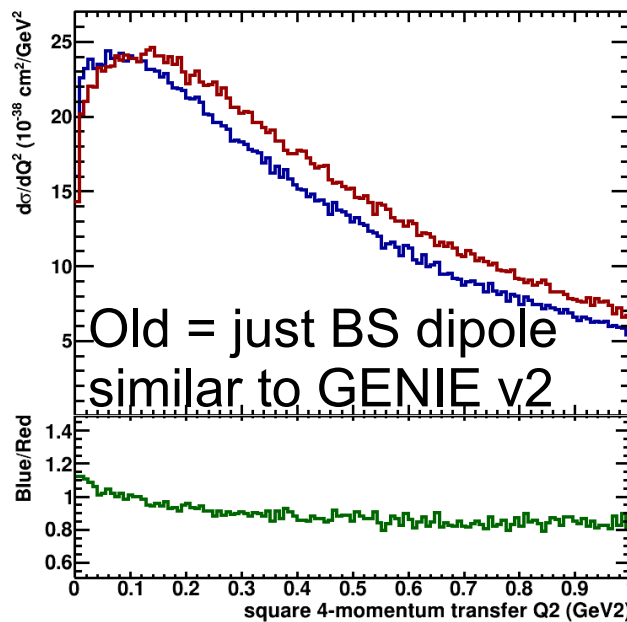


# Separate the vector and axial form factor effects

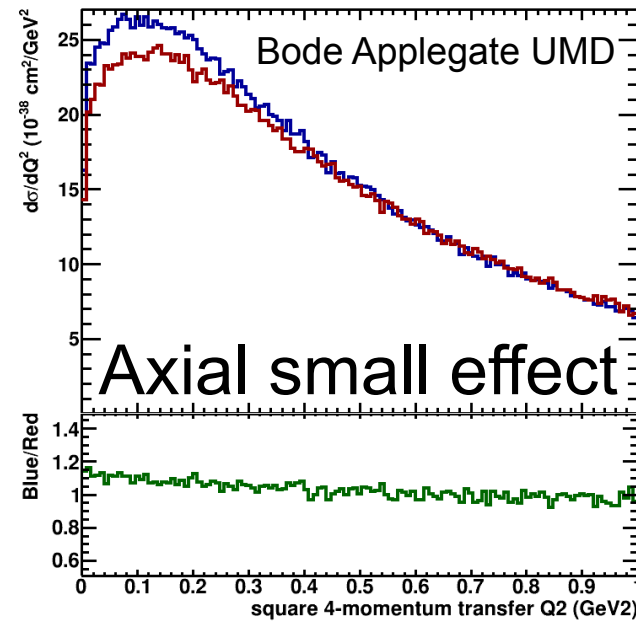
Red: default GENIE3 newFF Argon  $\Delta^{++}$  3 GeV no FS selection



Old Vector FF  
But same MV



Old Axial & Vector  
but same MA, MV

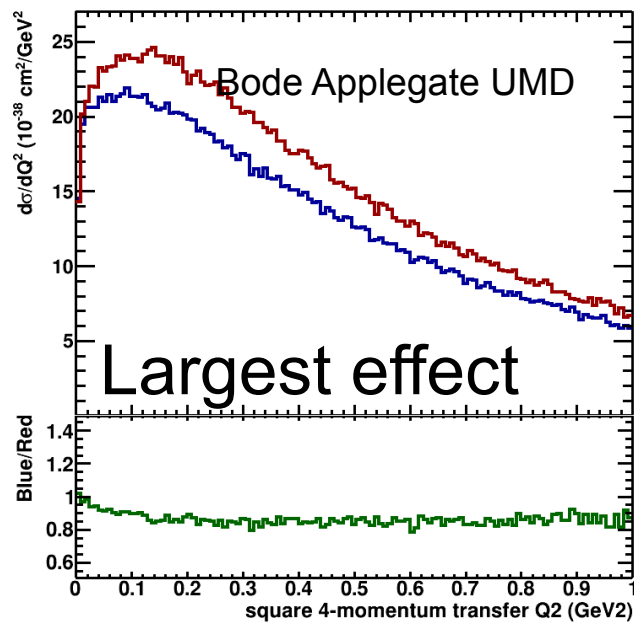


Old Axial FF  
But same MA

Both V & A contribute to a low- $Q^2$  rolloff vs. GENIE2



# But the MA was tuned to data with old Vector FF



Old Vector FF  
But same MV  
MA needs to go down

New VectorFF from Lalakulich  
Obtained from LT analysis near Delta peak  
Old axial MA tuned by Kuzmin and others.

New FF are too high because MA needs to be retuned to data, or something.

Options: Graczyk and Sobczyk did it  
Julia Tena Vidal and GENIE sorta did it  
changed 15% normalization and 3% MA

Use the QE Zexpansion Meyer et al.<sup>33</sup>

# What do we know about the Rein diffractive model?

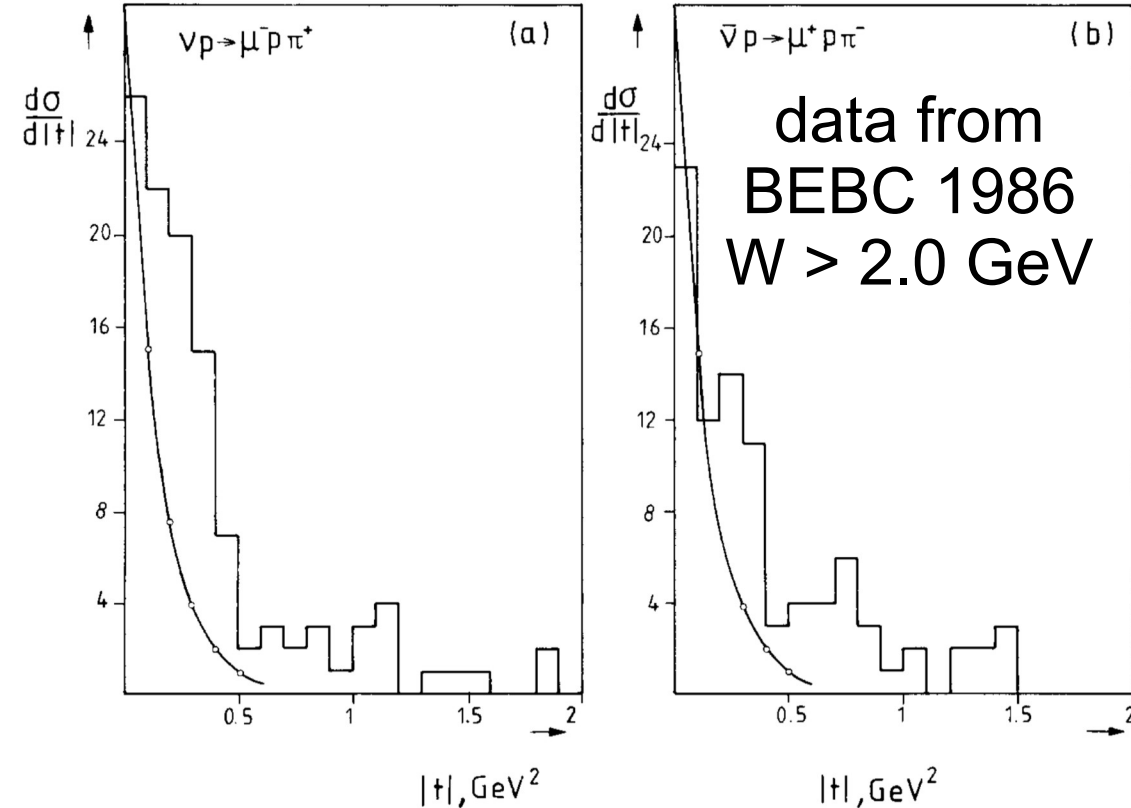


Fig. 7.  $t$ -distributions compared with data (from ref. [8]) (a) for neutrino reaction (b) for antineutrino reaction;  $W > 2 \text{ GeV}$ ,  $b = 7 \text{ GeV}^{-2}$ ,  $m_A = 1.1 \text{ GeV}/c^2$ .

Complicated what Rein did  
And what GENIE did.

Rein's model (and GENIE)  
Integrates to this distribution  
And  $9.4 \pm 1.4 \cdot 10^{-40} \text{ cm}^2$

This distribution is  
Arbitrary normalized

Now I can make the real  
comparison with GENIE

Model D. Rein Nucl.Phys.B 278 (1986) p.61  
Data P. Allen Nucl.Phys.B 264 (1986) p.221

# Vector form factors

Still trying to isolate what Lalakulich form factors are like  
she extracted them from  $(e, e')$  data in the Delta region  
working with Jarek Nowak on that

They should not necessarily look like the QE form factors

Lalakulich got them from data, but how do they compare  
to more recent work on QE vector form factors ?

Do they look like the QE form factors ? Not sure yet.  
(Should they?)

# ANL and BNL plots

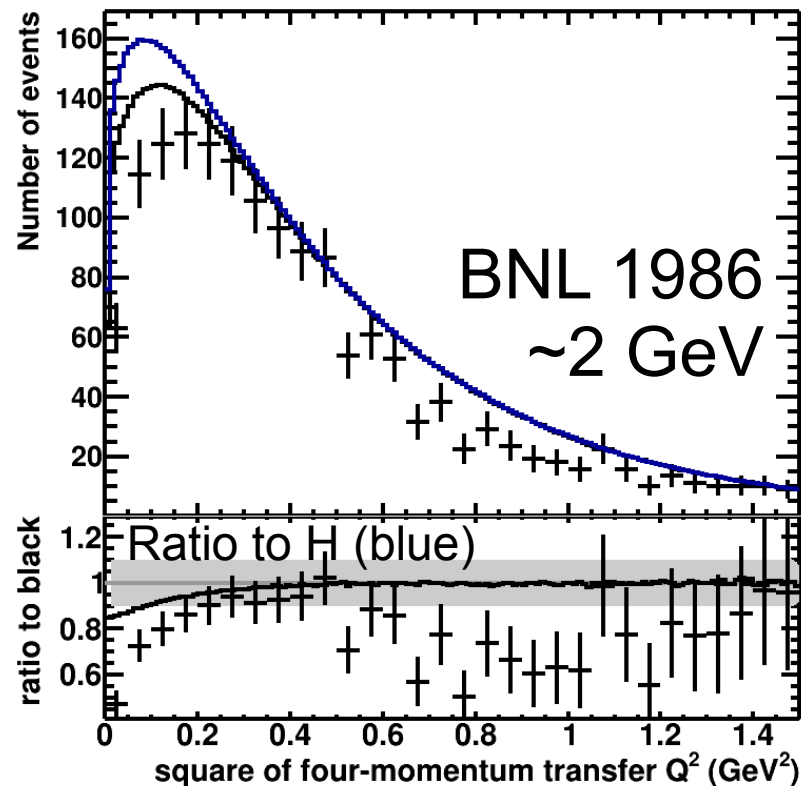
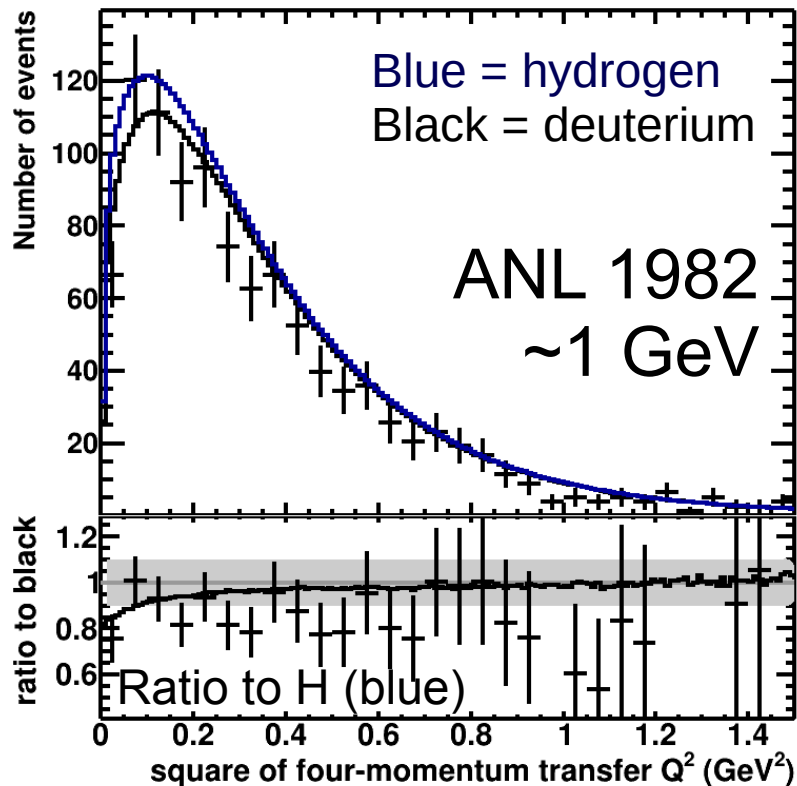
These were done before working on BEBC  
They are still approximately correct

But many adjustments to backport from BEBC experience

Could be surprises.

And there is a spline problem that comes from a surprise  
GENIE build feature that requires developers to make clean  
was few % and fixed already for BEBC

# G18\_02a (RFG+hA) with new (default) form factors

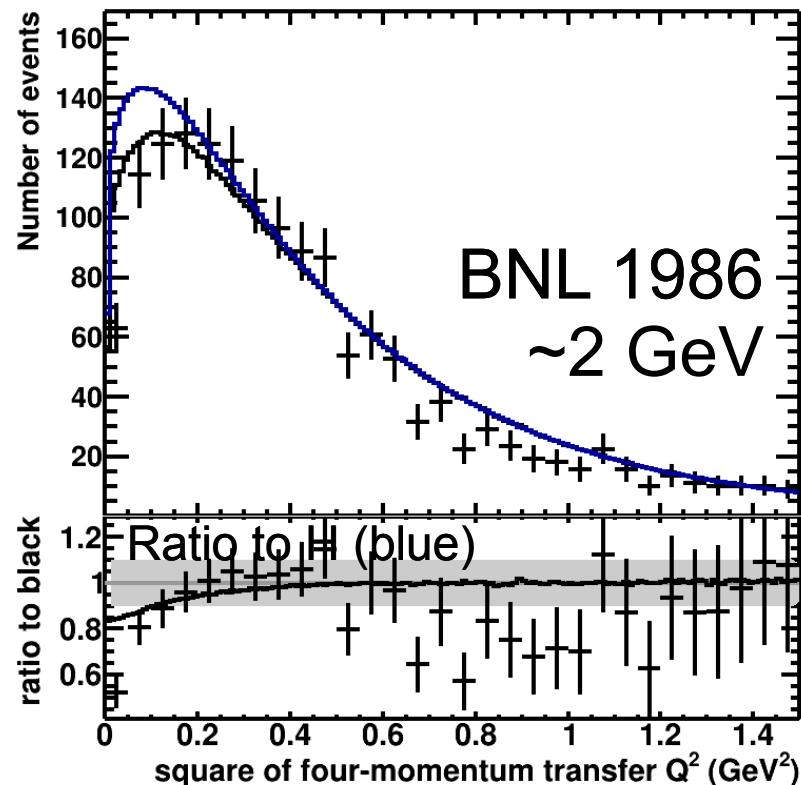
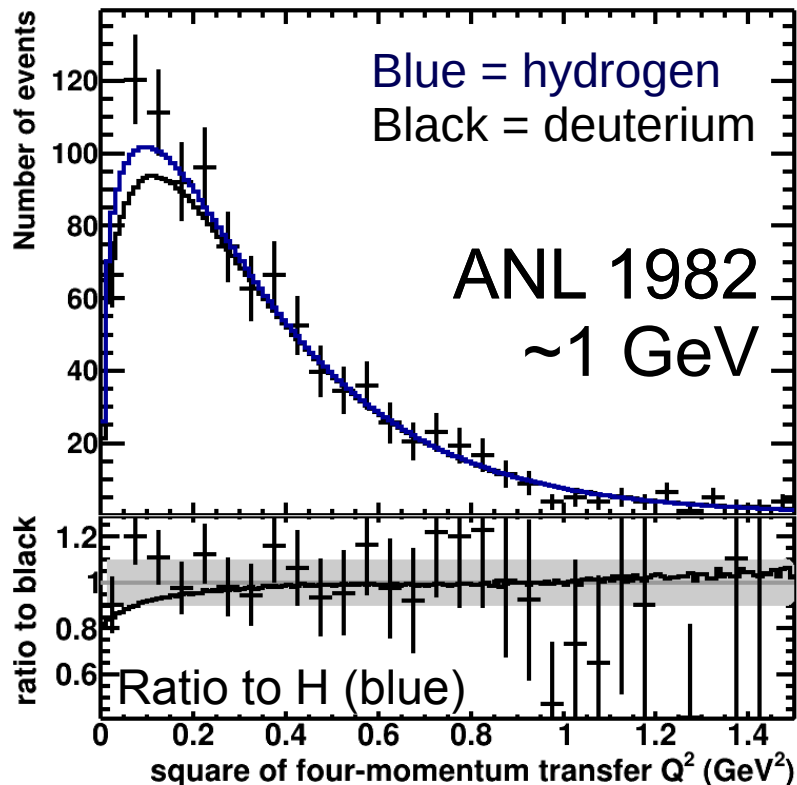


Showed this last time. Similar discrepancy to BEBC despite energy.

Hay! Blue has Diffractive but Black does NOT have coherent. Should it?

Naive test, true  $W(p\bar{d} \pi) > 2.0$ . Need to test assuming reco proton

# G18\_02a (RFG+hA) with old Rein Sehgal Form Factors



This prediction is a lot lower. Hard to tell by eye, but the shape is different.  
MA=1.12 fit this model to these data, before the Callum+Phil modification.  
and according to people not literally using GENIE (Naumov et al.)

$$\begin{aligned}
\frac{\bar{L}_{\mu\nu}\bar{W}^{\mu\nu}}{E_\nu^2} &= \frac{1}{E_\nu^2} \left[ W_1 (Q^2 + m_l^2) - \frac{W_2}{2} (m_l^2 + Q^2) \mp \frac{q_0 W_3}{2M} (m_l^2 + Q^2) \right. \\
&\quad \left. + \frac{W_4}{M^2} \left( \frac{Q^2 m_l^2 + m_l^4}{2} \right) \right] + \frac{1}{E_\nu} \left[ -2q_0 W_2 \pm \frac{W_3 Q^2}{M} - \frac{W_5 m_l^2}{M} \right] + 2W_2
\end{aligned}$$

Are deuterons (from the coherent/diffractive process)  
Reco'd as protons ?

Fermi motion and removal energy effects

Some spectator neutrons have enough momentum to  
Fail the 3C requirement.

There is some FSI, GENIE predicts some, its uncertain

Shape of flux will show up, but will still be small

Many structure function terms contribute, not just  $W_2$