

Exploring constraints on the core radius and density jumps inside Earth using atmospheric neutrino oscillations

Based on [arXiv:2405.04986](https://arxiv.org/abs/2405.04986)

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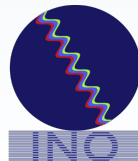
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NuFact 2024 - The 25th International Workshop on Neutrinos from Accelerators

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Collaborators: Anil Kumar, Sanjib Kumar Agarwalla, Amol Dighe

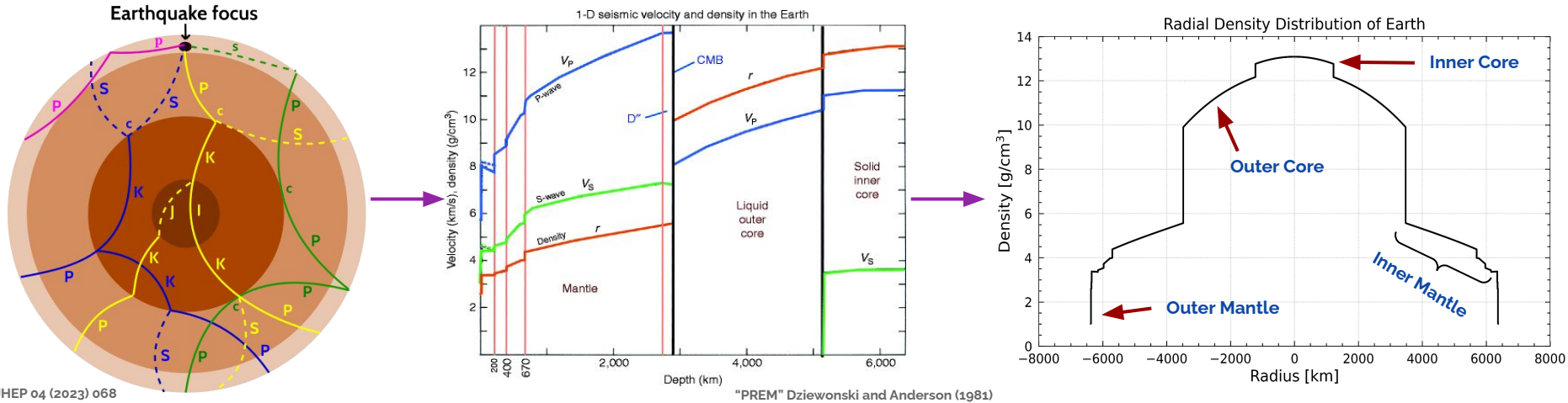


Outline

- Information About Earth's interior
- Atmospheric Neutrinos
- Earth's Matter Effects: Key to Probe Internal Structure of Earth
- Neutrinos for constraining the correlated density jumps and location of core-mantle boundary
 - ICAL@INO
 - Sensitivity Results

The Interior of Earth

- Information about the interior of Earth is obtained from indirect probes used in traditional **seismic** and **gravitational** studies → **Preliminary Reference Earth Model (PREM)**

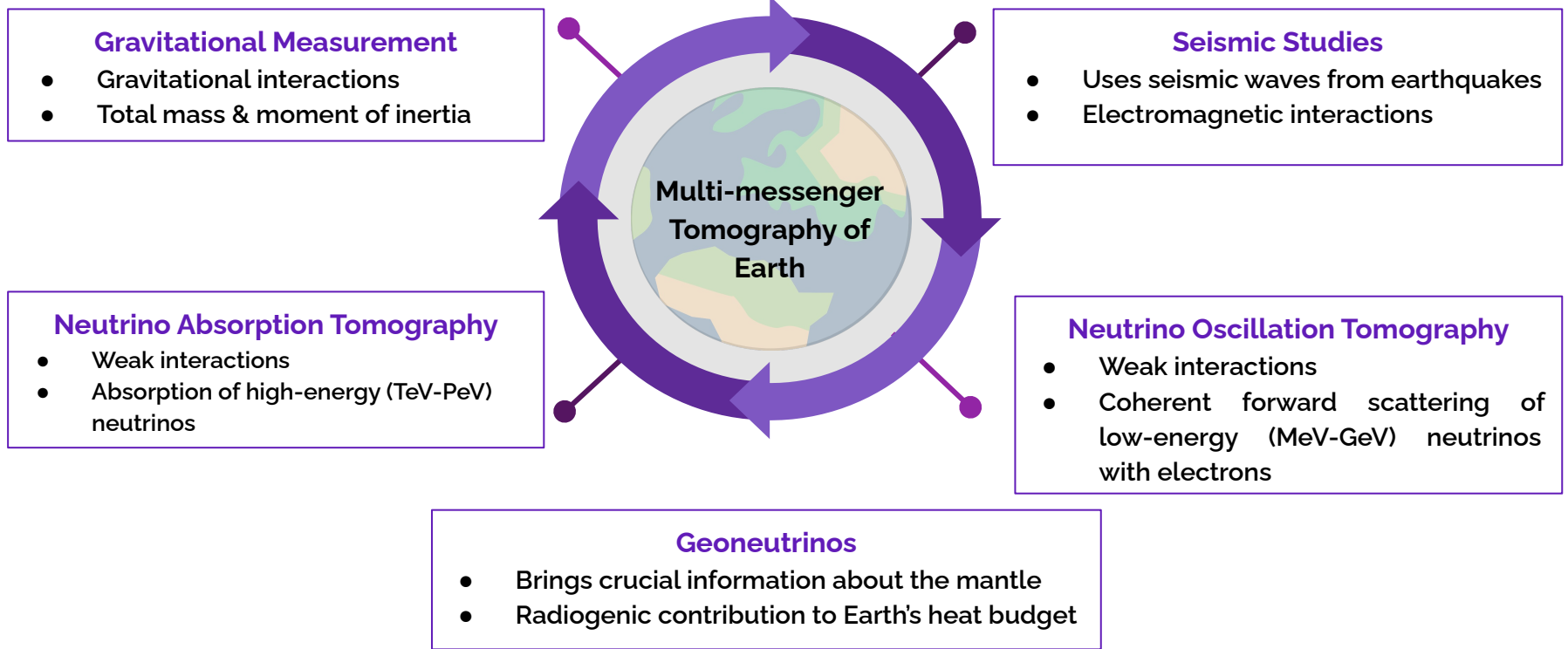


JHEP 04 (2023) 068

- Broadly classified: two concentric shell - the outer one is mantle, and the inner one with a much higher density is core
- Mantle consists of hot rocks of silicate and core is composed of metals like iron and nickel
- Outer core is expected be liquid (absence of S-waves and decrease in the velocity of P-waves)
- Core-Mantle Boundary (CMB): the largest compositional discontinuity within the Earth at a depth of 2891 km**
- The large density contrast across the CMB**

Multi-messenger Tomography of Earth

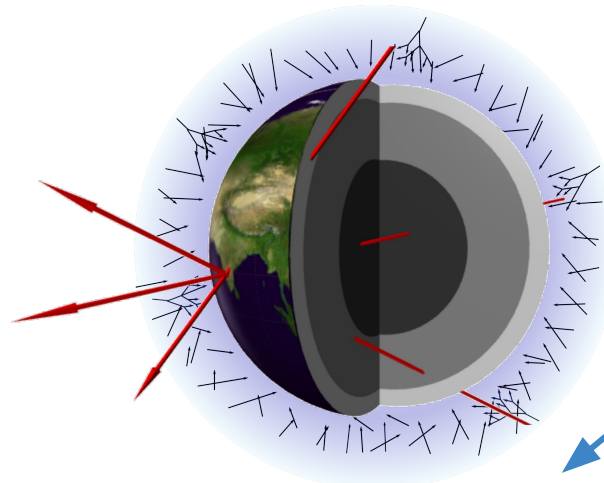
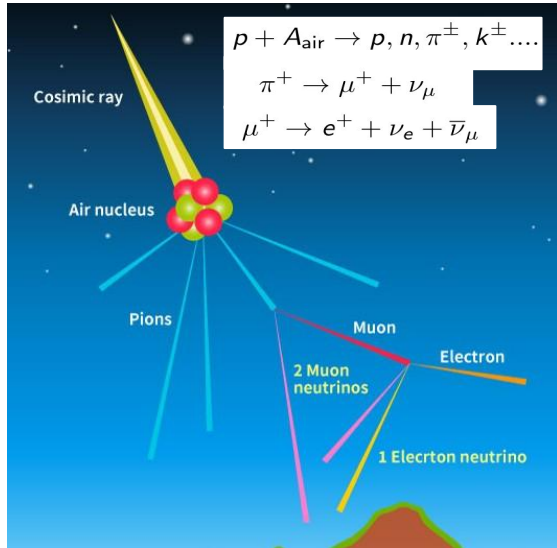
Neutrinos can penetrate deep inside Earth and may shed light on internal structure and composition



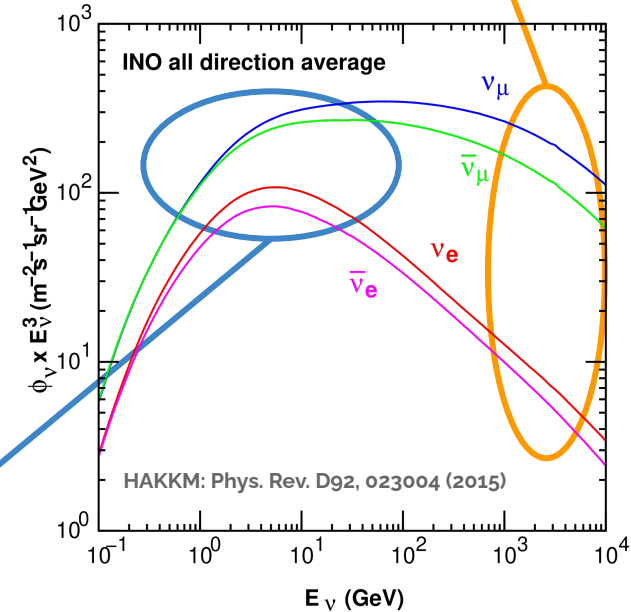
Present study is based on neutrino oscillation tomography

Atmospheric Neutrinos

- Atmospheric neutrinos are the ideally suited source of neutrinos to probe the internal structure of Earth



At high (TeV-PeV) energies: Neutrino absorption tomography

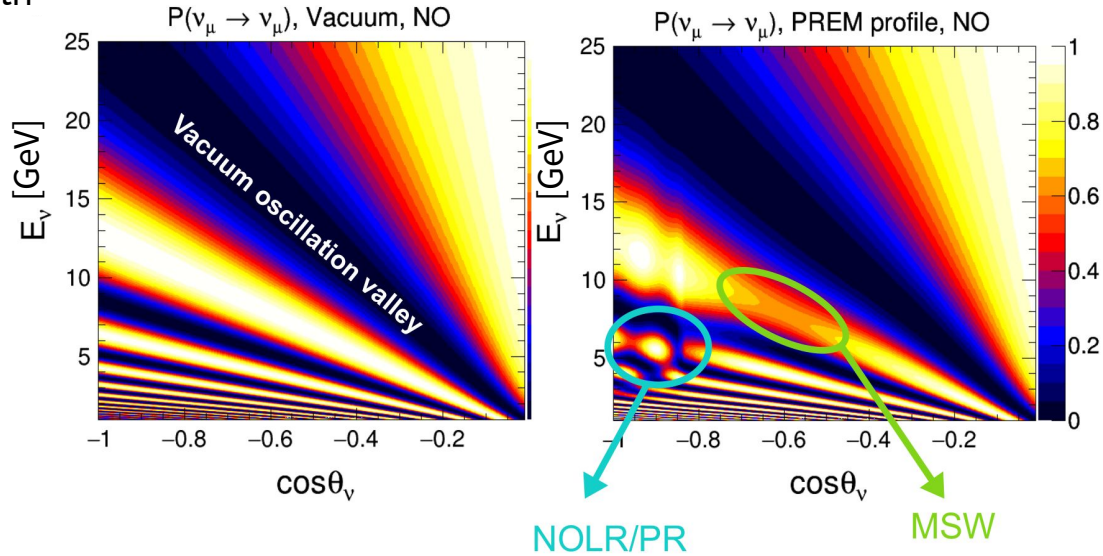
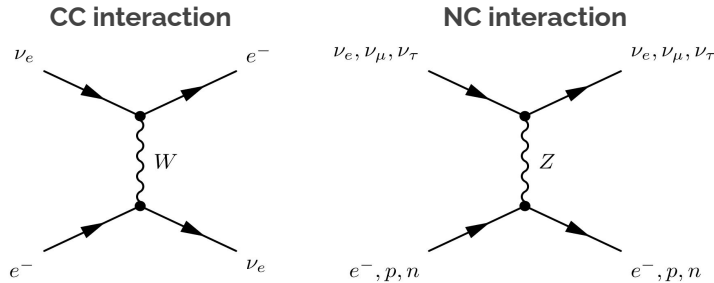


- Baseline:** ~20 km to 12760 km

- Wide energy range:** few MeV to more than TeV

Earth's Matter Effect in Neutrino Oscillations

- Neutrinos feel a charged-current potential V_{CC} during coherent forward scattering with ambient electrons inside Earth



$$V_{CC} = \pm\sqrt{2}G_F N_e$$

$$\approx \pm 7.6 \times Y_e \times 10^{-14} \left[\frac{\rho}{\text{g/cm}^3} \right] \text{ eV}$$

Mikheyev–Smirnov–Wolfenstein (MSW) resonance

([L. Wolfenstein, PRD 17 \(1978\) 2369](#)): $6 \text{ GeV} < E_\nu < 10 \text{ GeV}$

Neutrino oscillation length resonance (NOLR) ([Petcov, PLB 434](#)

[\(1998\) 321](#))/**parametric resonance resonance (PR)** ([Akhmedov,](#)

[NPB 538 \(1999\) 25](#)): $2 \text{ GeV} < E_\nu < 6 \text{ GeV}$

Earth's Matter Effects: key to Probe Internal Structure of Earth

- Earth's matter effect driven neutrino oscillation measurements provide a complementary and independent information about internal structure of Earth

$$V_{CC} = \pm\sqrt{2}G_F N_e \approx \pm 7.6 \times (Y_e) \times 10^{-14} \left[\frac{\rho}{\text{g/cm}^3} \right] \text{ eV}$$

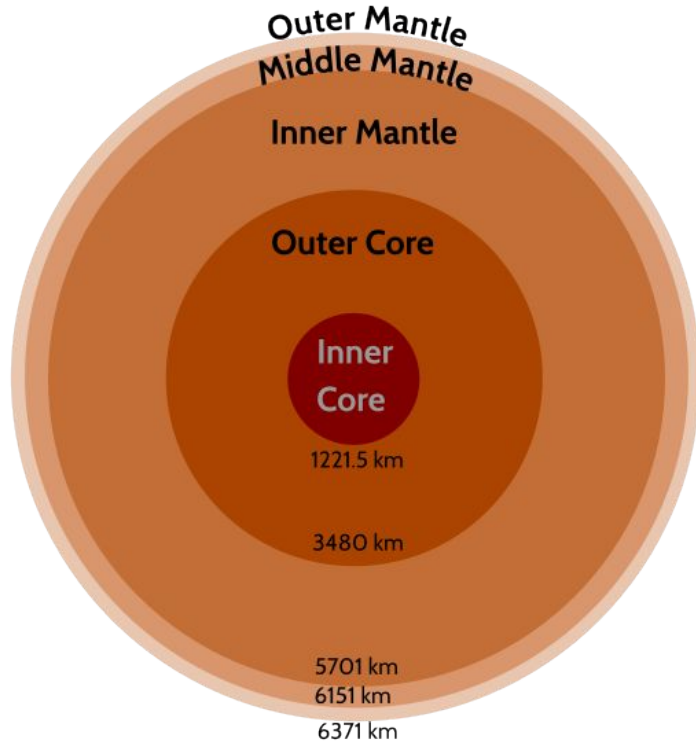
- ρ : matter density \longrightarrow **Density of each layer inside Earth**
- $Y_e = N_e / (N_p + N_n)$: relative electron number density \longrightarrow **Chemical composition of Earth**

- Recent sensitivity studies using atmospheric neutrino oscillations to probe the internal structure of Earth



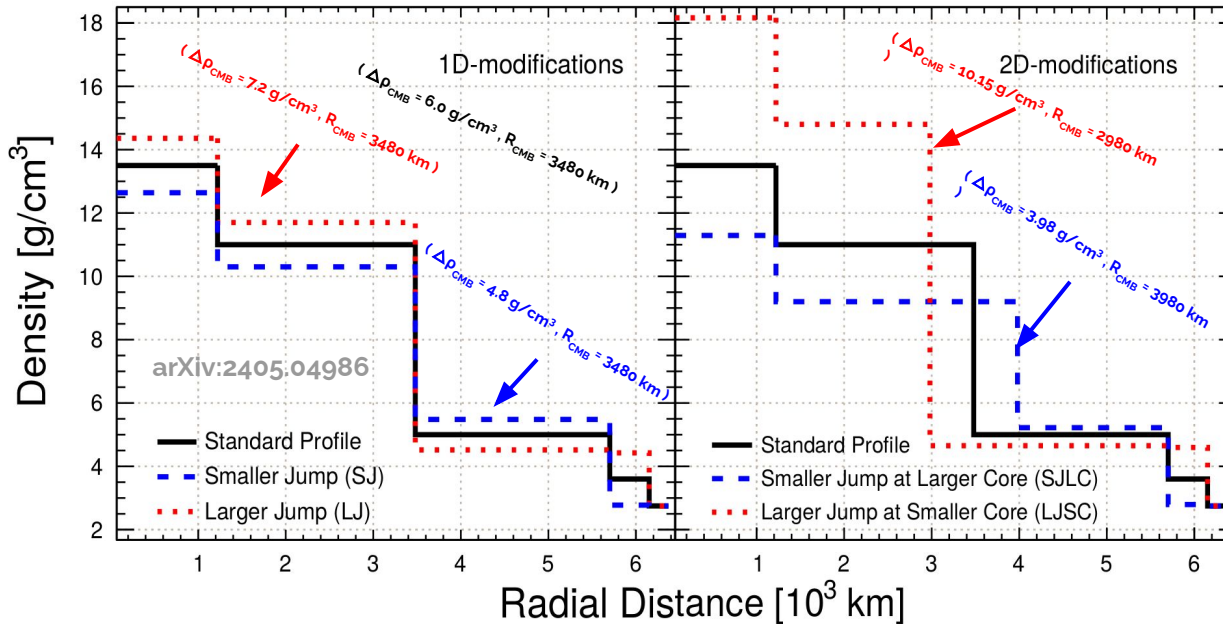
- **Presence of Earth's core:** [JHEP 08 \(2021\) 139](#) (ICAL)
- **Location of core-mantle boundary:** [PRD 104 \(2021\) 11, 113007](#) (DUNE), [JHEP 04 \(2023\) 068](#) (ICAL)
- **Density distribution:** [Nucl.Phys.B 908 \(2016\) 250-267](#) (PINGU & ORCA), [JHEP 05 \(2022\) 187](#) (DUNE), [Eur.Phys.J.C 82 \(2022\) 5, 461](#) (ORCA)
- **Chemical composition:** [Sci.Rep. 5 \(2015\) 15225](#), [Eur.Phys.J.C 82 \(2022\) 7, 614](#) (ORCA), [Front.Earth Sci. 11 \(2023\) 1008396](#)

Toy Density Model of Earth



- Consider a five-layered density profile of Earth, guided by the PREM profile
- **Five layers:**
 - Inner Core (IC),
 - Outer Core (OC),
 - Inner Mantle (IM),
 - Middle Mantle (MM),
 - Outer Mantle (OM)
- **Four significant density jumps:**
 - IC-OC ($\Delta\rho_{IC-OC}$)
 - CMB ($\Delta\rho_{CMB}$)
 - IM-MM ($\Delta\rho_{IM-MM}$)
 - MM-OM ($\Delta\rho_{MM-OM}$)

Toy Density Models of Earth with Modifying Density Jumps & R_{CMB}



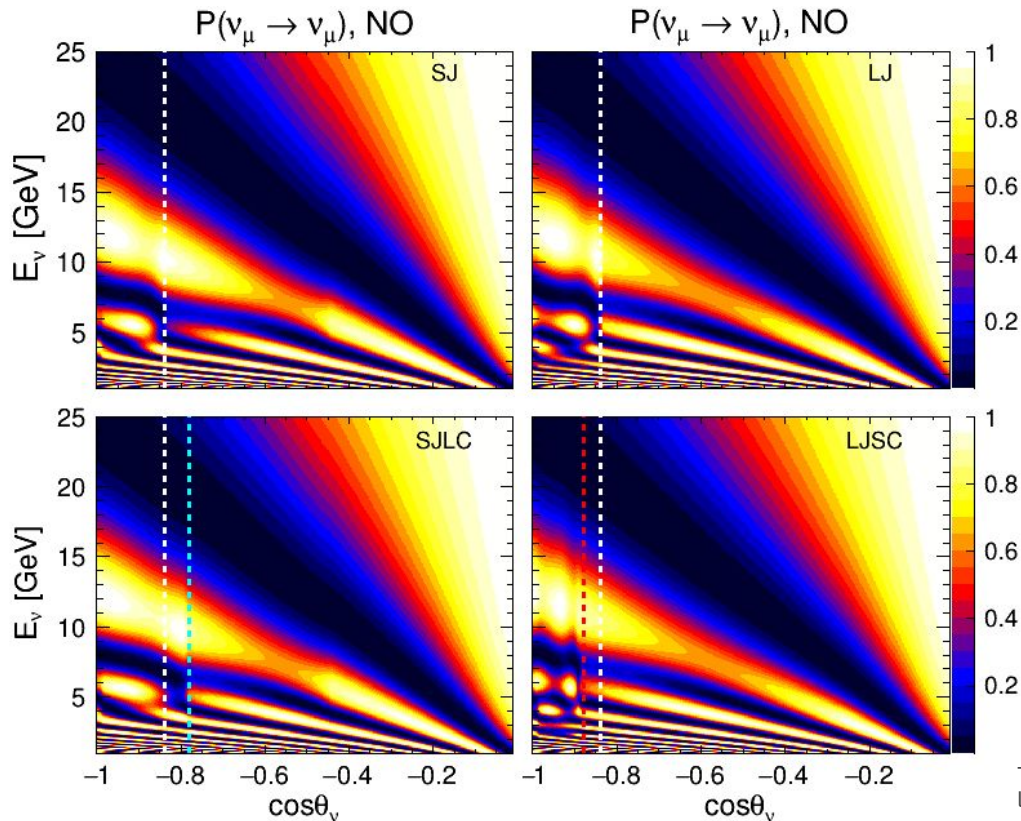
Constraints:

- Mass and Moment of inertia of Earth are fixed
- Density of outer mantle is fixed
- Density ratio between inner core and outer core ($\rho_{\text{IC}} / \rho_{\text{OC}}$) is fixed
- Hydrodynamic condition ($\rho_{\text{inner layer}} > \rho_{\text{outer layer}}$) is satisfied

1D-modifications: R_{CMB} is fixed at 3480 km and only $\Delta\rho_{\text{CMB}}$ is varied

2D-modifications: R_{CMB} is varied simultaneously with $\Delta\rho_{\text{CMB}}$

Effect of Density Jump ($\Delta\rho_{\text{CMB}}$) & R_{CMB} Variation on Oscillograms



Observations:

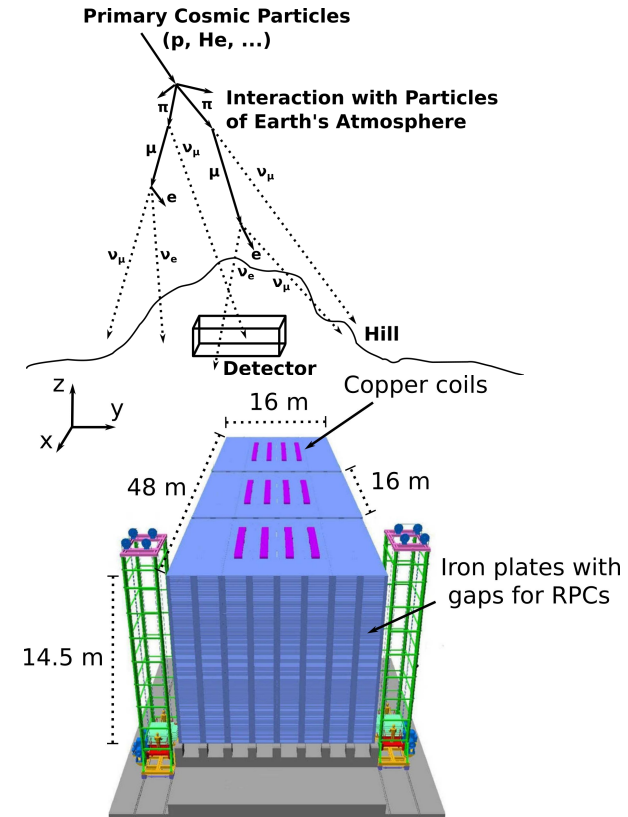
- **For SJ:**
 - NOLR/PR shift to left
 - MSW resonance region shrinks
- **For LJ:**
 - NOLR/PR shift to right
 - MSW resonance region stretches
- **For LJSC:**
 - NOLR/PR shifts to right and patterns shrink
 - MSW resonance region stretch
- **For SJLC:**
 - NOLR/PR shifts to left and patterns become wider
 - MSW resonance region shrink

The white, red, and cyan vertical dotted lines represent the standard, smaller, and larger R_{CMB} values, respectively.

Opposite modification in MSW and NOLR/PR region for SJ and LJ, and LJSC and SJLC scenarios

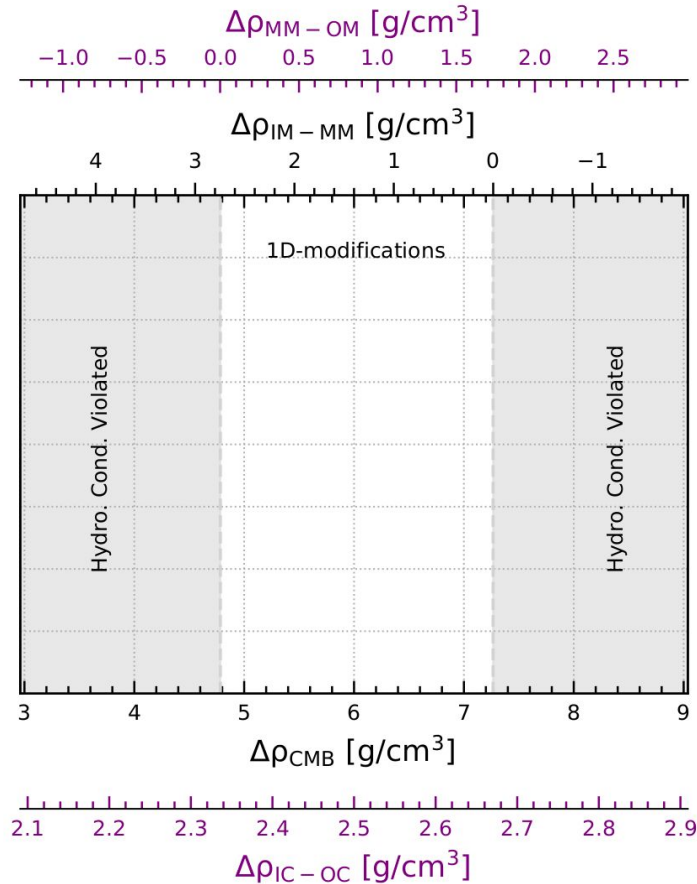
Iron Calorimeter Detector (ICAL) at INO

- **ICAL@INO:** 50 kton magnetized iron calorimeter detector at the proposed India-based Neutrino Observatory (INO)
- **Location:** Bodi West Hills, Theni District, Tamil Nadu, India
- **Aim:** To determine neutrino mass ordering and precision measurement of atmospheric neutrino oscillation parameters
- **Source:** Atmospheric neutrinos and antineutrinos in the multi-GeV range of energies over a wide range of baselines
- **Uniqueness:** Charge identification capability helps to distinguish μ^- and μ^+ and hence, ν_μ and $\bar{\nu}_\mu$
- **Muon energy range:** 1 – 25 GeV
- **Muon energy resolution:** ~ 10%
- **Baselines:** 15 – 12000 km
- **Muon zenith angle resolution:** ~ 1°



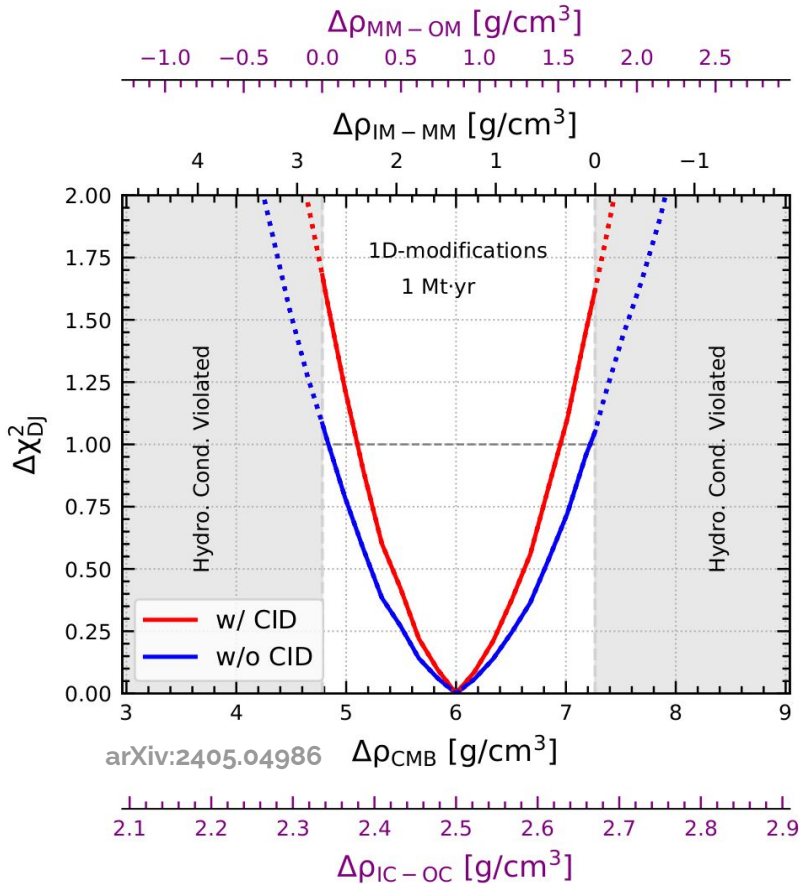
Pramana 88 (2017) 5, 79, arXiv:1505.07380

Sensitivity for Constraining Correlated Density Jumps at Standard R_{CMB}



- The gray area: unphysical region where the hydrostatic equilibrium condition is violated
- White region: allowed by the gravitational measurements and hydrostatic equilibrium condition

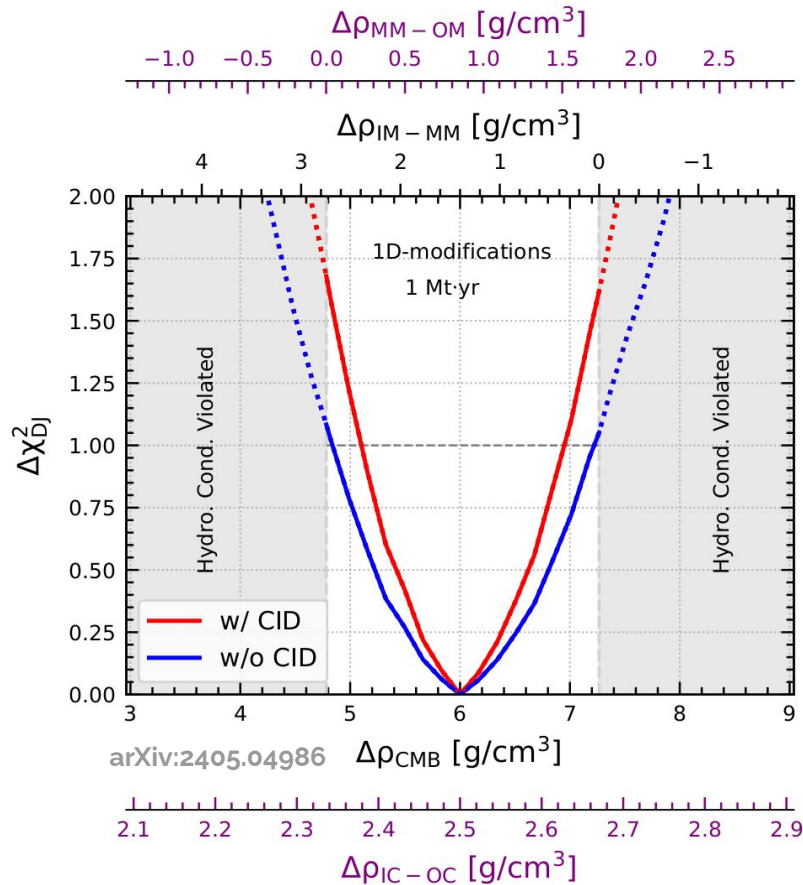
Sensitivity for Constraining Correlated Density Jumps at Standard R_{CMB}



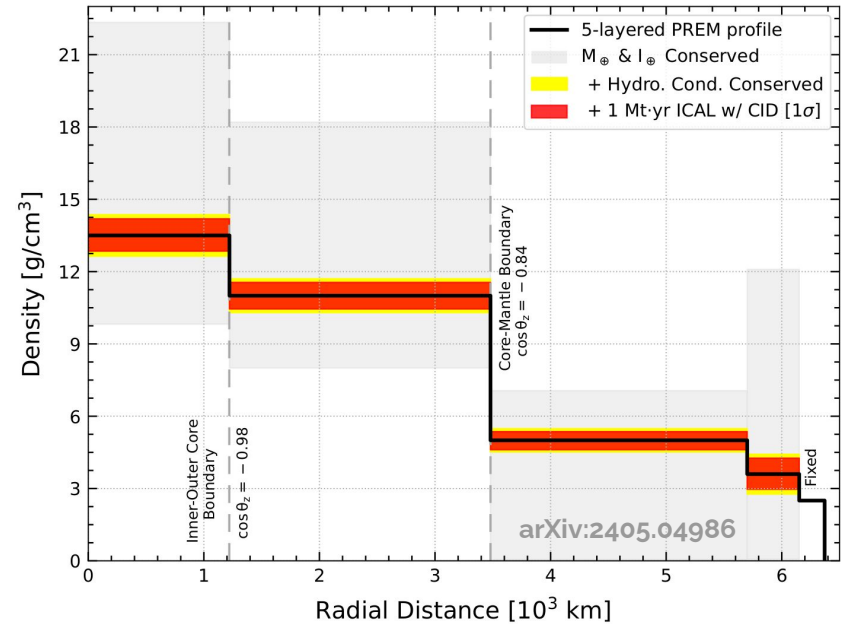
$$\Delta\chi^2_{\text{ID-DJ}} = \chi^2(\text{modified } \Delta\rho) - \chi^2(\text{standard } \Delta\rho)$$

- The gray area: unphysical region where the hydrostatic equilibrium condition is violated
- White region: allowed by the gravitational measurements and hydrostatic equilibrium condition
- **Added neutrino oscillation data on these external constraints**
 - Further constrain the allowed region
- Neutrino data at ICAL would be able to measure $\Delta\rho_{\text{CMB}}$ as [5.1, 7.0] g/cm^3 at 1σ with a relative precision of about 15%
- In the absence of CID, the sensitivity deteriorate to [4.8, 7.2] g/cm^3 at 1σ with a relative precision of about 20%

Sensitivity for Constraining Correlated Density Jumps at Standard R_{CMB}

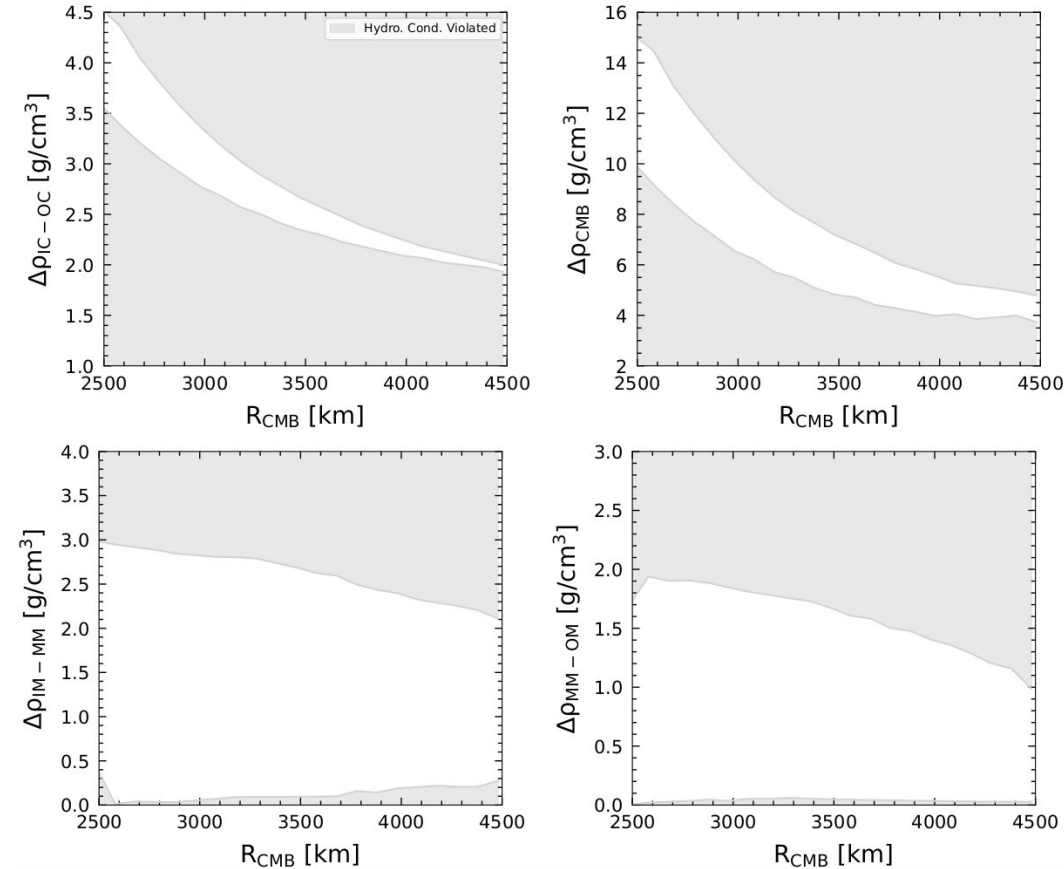


$$\Delta\chi^2_{\text{ID-DJ}} = \chi^2(\text{modified } \Delta\rho) - \chi^2(\text{standard } \Delta\rho)$$



- Neutrino data improve the constraints on the densities of layers of Earth placed by Earth's mass and moment of inertia

Sensitivity for Constraining Correlated Density Jumps and Location of R_{CMB}

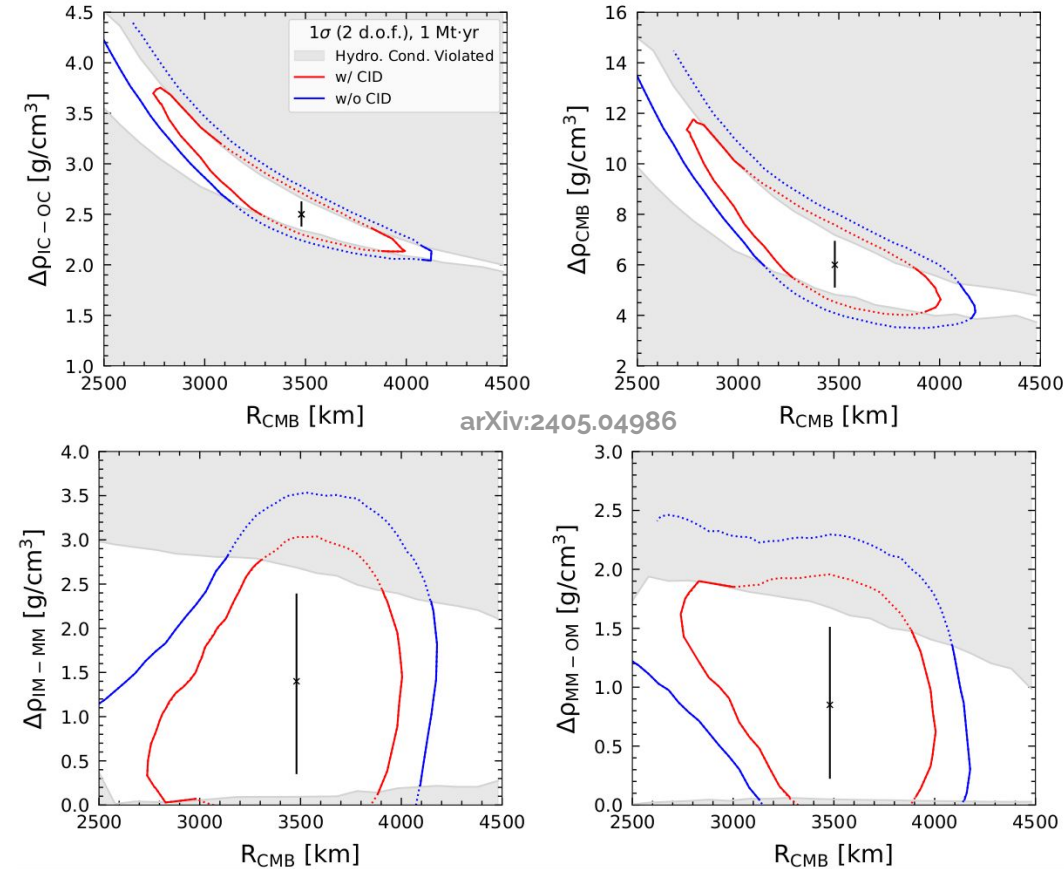


- The gray area: unphysical region where the hydrostatic equilibrium condition is violated
- White region: allowed by the gravitational measurements and hydrostatic equilibrium condition

Sensitivity for Constraining Correlated Density Jumps and Location of R_{CMB}

$$\Delta\chi_{\text{DJ-CMB}}^2 = \chi^2(\text{modified } \Delta\rho \text{ \& } R_{\text{CMB}}) - \chi^2(\text{standard } \Delta\rho \text{ \& } R_{\text{CMB}})$$

- The gray area: unphysical region where the hydrostatic equilibrium condition is violated
- White region: allowed by the gravitational measurements and hydrostatic equilibrium condition
- **Neutrino oscillation data can help us to further constrain the allowed region**
- **An example of the complementarity to the existing measurements**



Summary

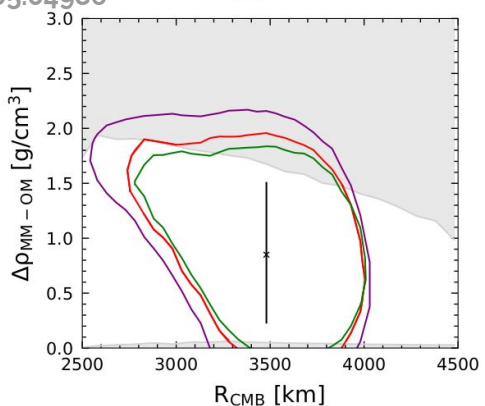
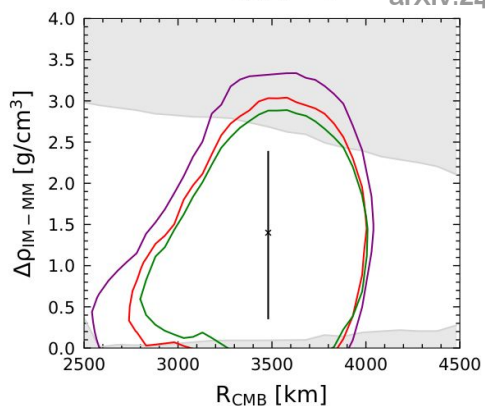
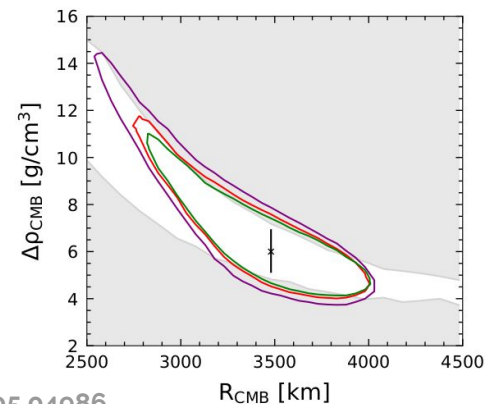
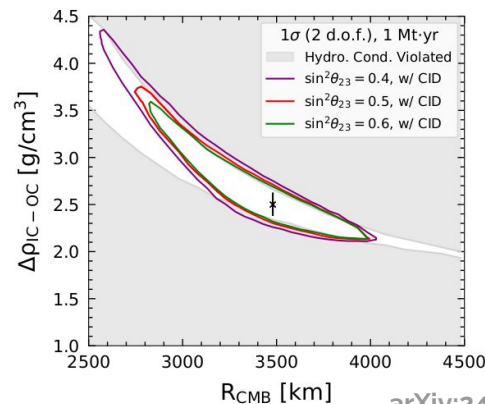
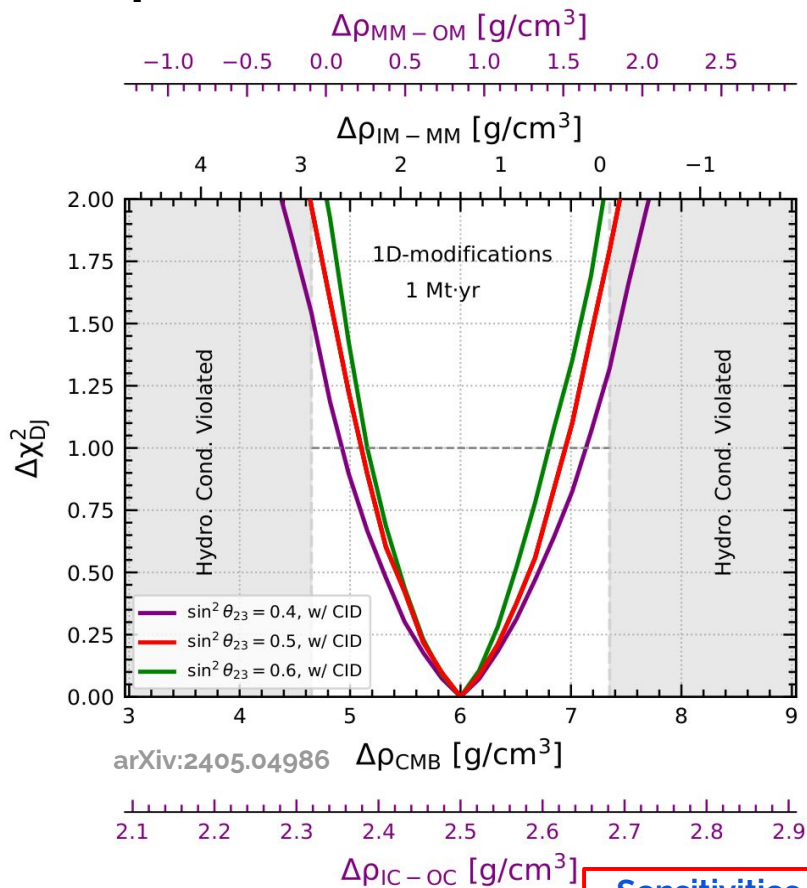
- In combination with gravitational and seismic studies, neutrino oscillations and absorption based measurements would pave the way for **“Multi-Messenger Tomography of Earth”**
- Atmospheric neutrinos have energies in the multi-GeV range where the Earth matter effects are significant, hence they would serve as probes of the internal structure of Earth
- Neutrino data improve the constraints on the densities of Earth's layers placed by Earth's mass and moment of inertia
- ICAL detector with 1 Mt·yr exposure would be able to measure the density jump at CMB ($\Delta\rho_{\text{CMB}}$) at the standard $R_{\text{CMB}} = 3480$ km with a relative precision of about **15%** at the 1σ C.L
- ICAL would be able to further constrain the allowed region by existing measurements

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(DST/INSPIRE Fellowship/2019/IF190755)

Thank you!

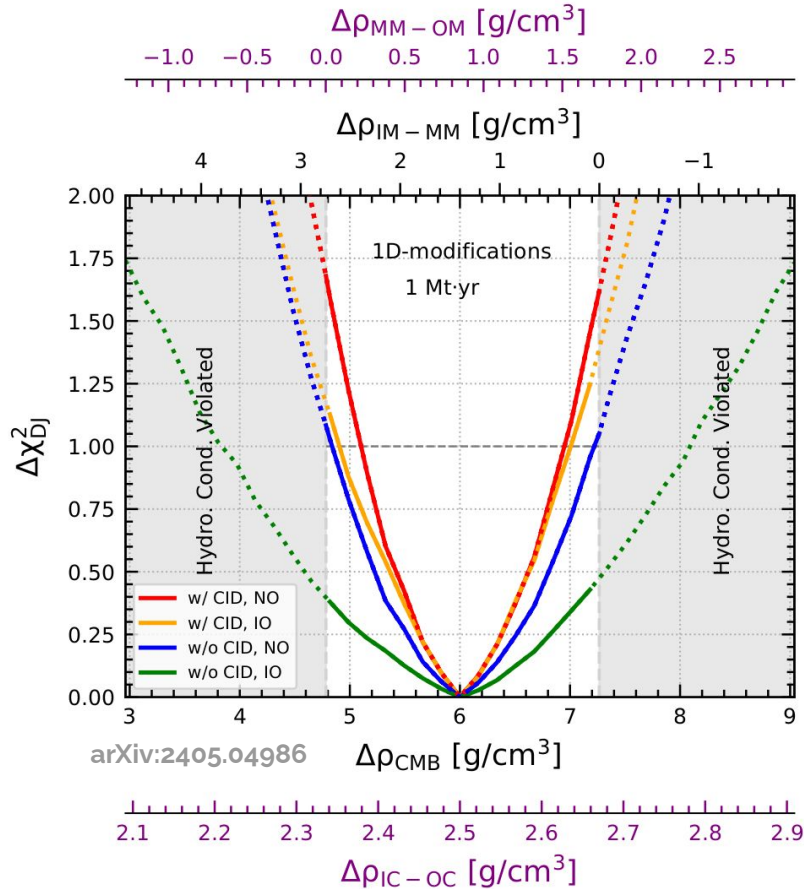
Backup

Impact of Different True Choices of $\sin^2\theta_{23}$ on Sensitivity



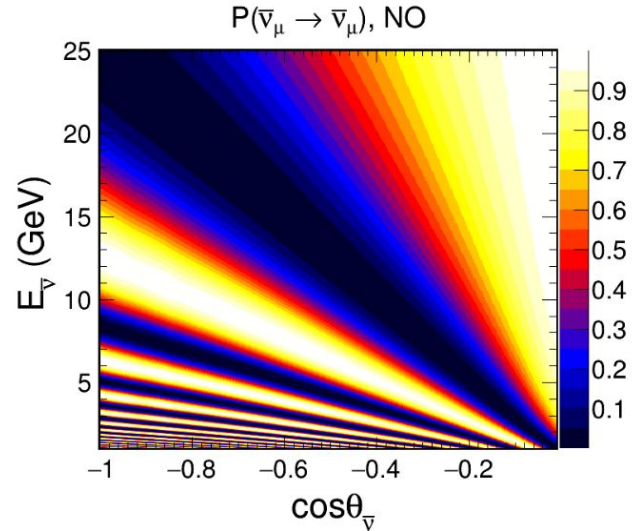
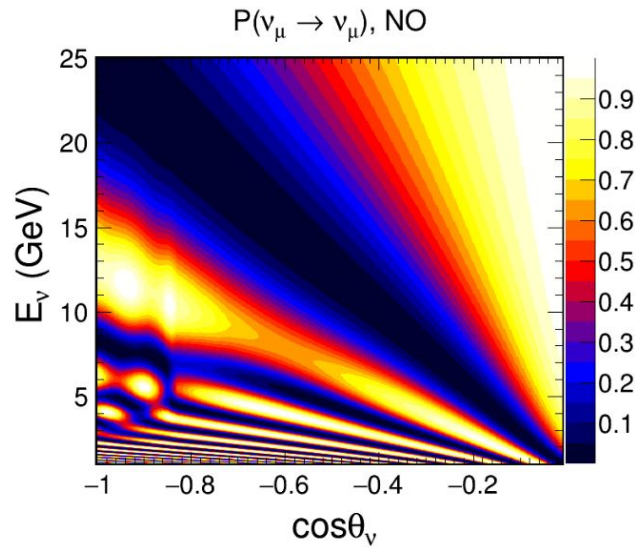
Sensitivities are larger (smaller) for higher (lower) octant

Impact of Inverted Mass Ordering on Sensitivity



- The orange (green) curve corresponds to the expected sensitivity for the IO scenario with (without) the CID capability of the ICAL detector
- Density constraints for IO are similar to NO 1 σ with CID capability of ICAL
- No constraints without CID capability of ICAL

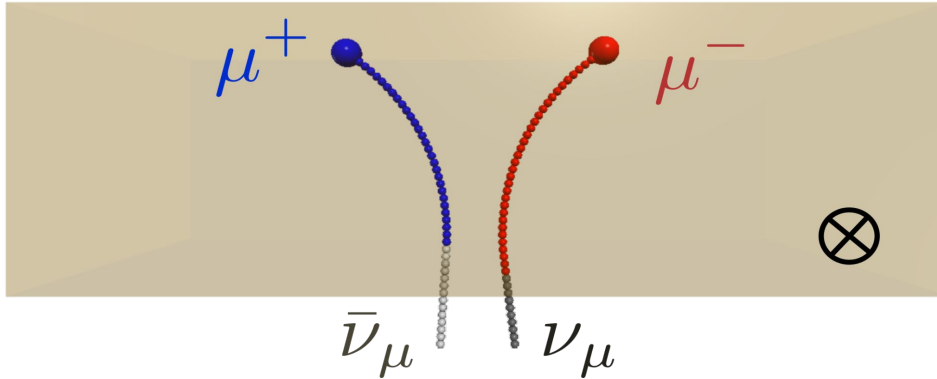
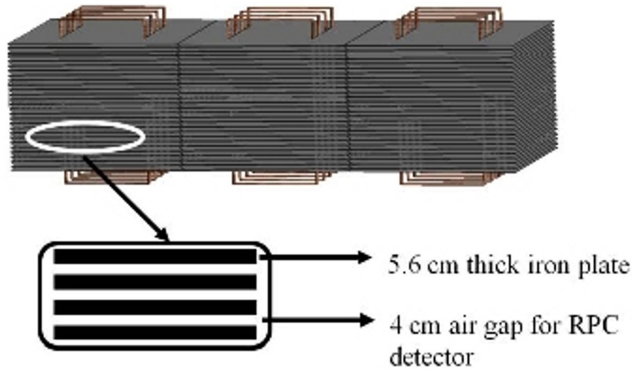
Oscillations in Neutrinos and Antineutrinos



- For **NO**, matter effects occur mainly in **neutrino** channel
- But for **IO**, matter effects occur mainly in **antineutrino** channel

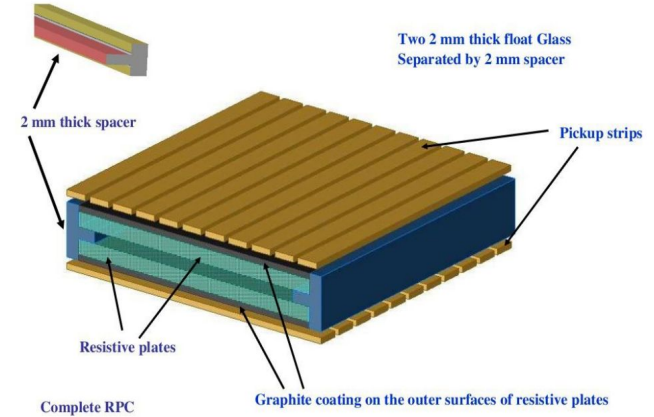
It is important to detect neutrinos and antineutrinos separately to preserve the matter effects

Design of ICAL Detector



Pramana 88 (2017) 5, 79, arXiv:1505.07380

Resistive plate chamber (RPC) (active element)
sandwiched between iron plates (passive element)



- μ^- and μ^+ bend in the opposite direction in the presence of magnetic field
- Therefore, neutrinos and antineutrinos can be detected separately

Statistical Analysis

In this analysis, the χ^2 statistics is expected to give median sensitivity of the experiment in the frequentist approach.

$$\chi_-^2 = \min_{\xi_l} \sum_{i=1}^{N_{E'}^{\text{rec}}_{\text{had}}} \sum_{j=1}^{N_{E\mu}^{\text{rec}}} \sum_{k=1}^{N_{\cos\theta\mu}^{\text{rec}}} \left[2(N_{ijk}^{\text{theory}} - N_{ijk}^{\text{data}}) - 2N_{ijk}^{\text{data}} \ln \left(\frac{N_{ijk}^{\text{theory}}}{N_{ijk}^{\text{data}}} \right) \right] + \sum_{l=1}^5 \xi_l^2$$

where,

$$N_{ijk}^{\text{theory}} = N_{ijk}^0 \left(1 + \sum_{l=1}^5 \pi_{ijk}^l \xi_l \right)$$


Similarly, χ_+^2 is defined for μ^+

$$\chi_{\text{ICAL}}^2 = \chi_-^2 + \chi_+^2$$

Five-layered profile

- Five layers: Inner Core (IC), Outer Core (OC), Inner Mantle (IM), Middle Mantle (MM), Outer mantle (OM)

Layers	Radius (km)	Depth (km)	Density (g/cm ³)
Inner Core	0 - 1221.5	5149.5 - 6371	13.5
Outer Core	1221.5 - 3480	2891 - 5149.5	11.0
Inner Mantle	3480 - 5701	670 - 2891	5.0
Middle Mantle	5701 - 6151	220 - 670	3.6
Outer Mantle	6151 - 6371	0 - 220	2.75



- M_E (PREM) = 5.9723×10^{24} kg

- MI_E (PREM) = 8.01724×10^{37} kg m²

- M_E (Grav.) = 5.9722×10^{24} kg

- MI_E (Grav.) = 8.01736×10^{37} kg m²

The Interior of Earth

Properties	Value (\pm)	Units
Earth's Mass	$(5.9722 \pm 0.006) \times 10^{24}$	kg
Mean moment of inertia	$(8.01736 \pm 0.00097) \times 10^{37}$	kg m ²
Earth's mean radius	6371.23 (0.01)	km
Core-mantle boundary	3483 \pm 5	km
Inner-outer core boundary	1220 \pm 10	km

- W.F. McDonough, Elsevier (2003), p. 547
- W. Chen et. al. Journal of Geodesy 89,179–188 (2015)
- B. Luzum et.al. Celestial Mechanics and Dynamical Astronomy 110, 293–304 (2011)