

Experimental Measurements of the Muon $g-2$ & Searches for Charged Lepton Flavor Violation using Muons

Sophie Charlotte Middleton(Caltech)

25th International Workshop on Neutrinos from Accelerators (NuFact)

19th Sept. 2024

Argonne National Laboratory

Caltech



Muons as probes for New Physics

How can muons help us explore New Physics?

Muons as Probes of New Physics

Muon $g-2$

Muon CLFV Searches: Motivations

Muon CLFV Searches: Design, Status

What happens next?



Muons as probes for New Physics

How can muons help us explore New Physics?

Muons as Probes of New Physics

Muon $g-2$

Muon CLFV Searches: Motivations

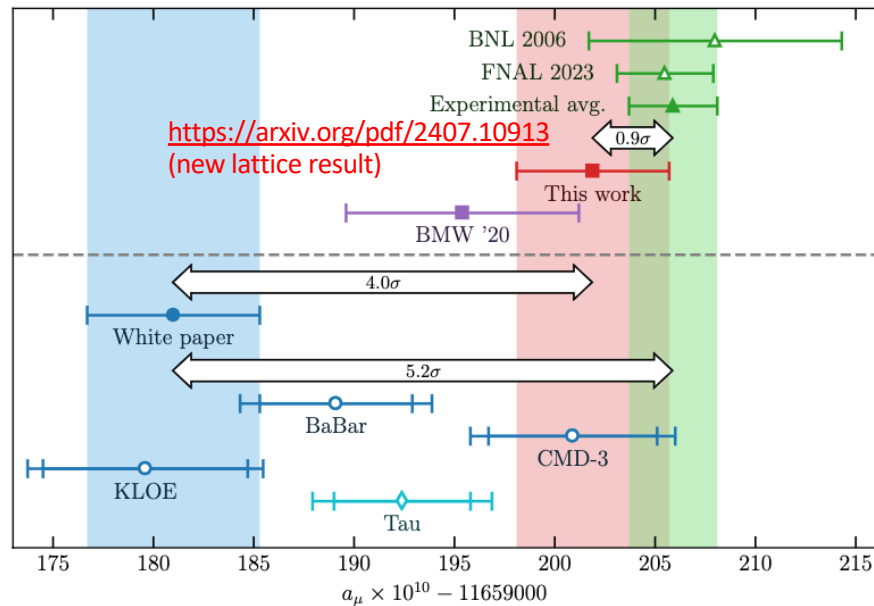
Muon CLFV Searches: Design, Status

What happens next?

Muons as Probes for New Physics

- Muons have been an invaluable probe of the Standard Model.
- Precision muon searches and searches for muon/electron flavor transitions are indirect probes of new physics:

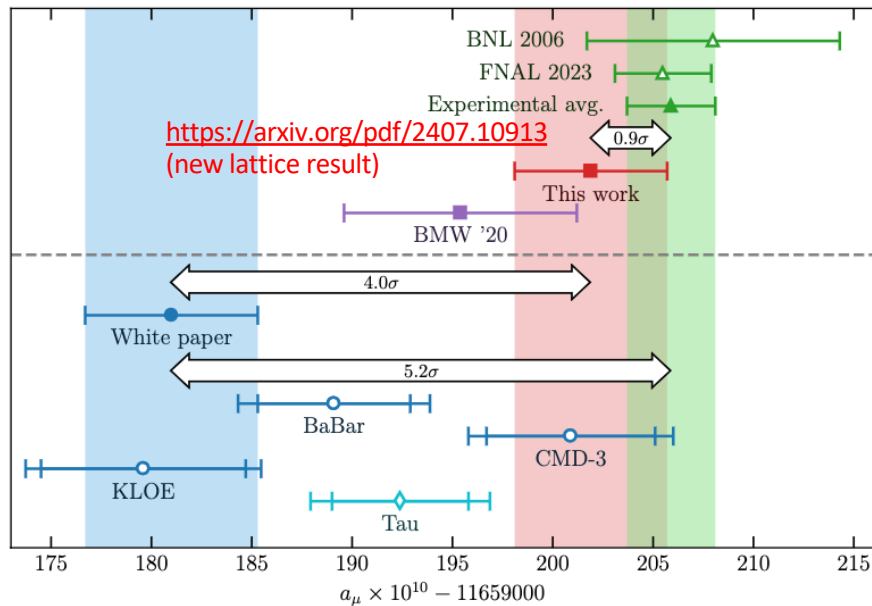
Muon $g-2$ anomaly



Muons as Probes for New Physics

- Muons have been an invaluable probe of the Standard Model.
- Precision muon searches and searches for muon/electron flavor transitions are indirect probes of new physics:

Muon $g-2$ anomaly



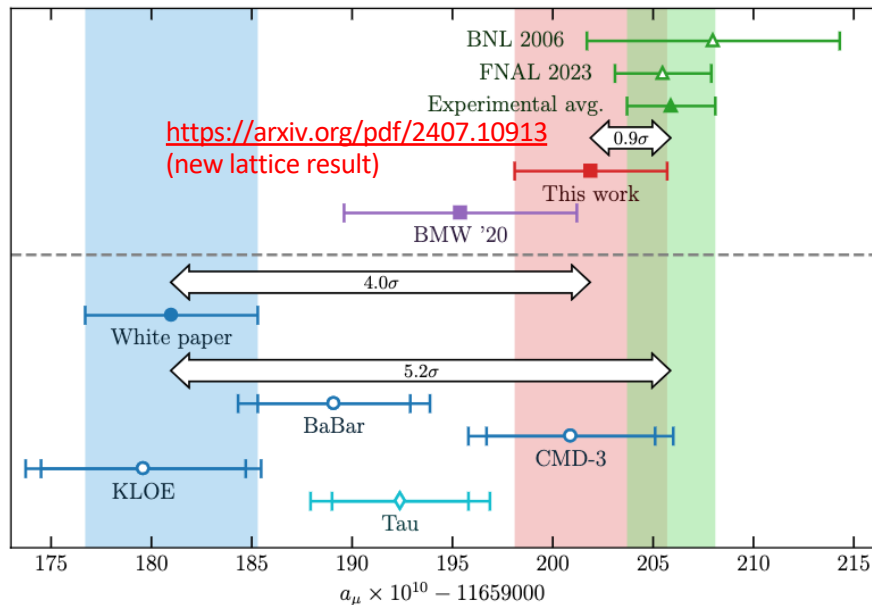
In general:

- Do not decay hadronically \rightarrow clean, well-understood backgrounds.
 - Lifetime $\sim 2.2 \mu\text{s}$ \rightarrow can be stored efficiently before decay, decay easy to measure.
- Plus:
- Mass scaling could mean 10^4 enhancement in coupling to BSM over electrons.

Muons as Probes for New Physics

- Muons have been an invaluable probe of the Standard Model.
- Precision muon searches and searches for muon/electron flavor transitions are indirect probes of new physics:

Muon $g-2$ anomaly



In general:

- Do not decay hadronically \rightarrow clean, well-understood backgrounds.
- Lifetime $\sim 2.2 \mu\text{s}$ \rightarrow can be stored efficiently before decay, decay easy to measure.

Plus:

- Mass scaling could mean 10^4 enhancement in coupling to BSM over electrons.

Can create high-intensity, clean, background-free, experimental environment to probe new physics.

Many experimental searches looking for new physics in the muon sector or ways to elucidate the apparent $g-2$ discrepancy will come online this decade.....

.... the 2020's are proving to be a very exciting time for muon physics!

Muon $g-2$

Is the $g-2$ measurement an indication of new physics?

Muons as Probes of New Physics

Muon $g-2$

Muon CLFV Searches: Motivations

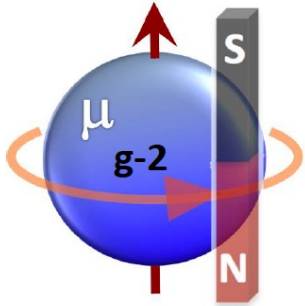
Muon CLFV Searches: Design, Status

What happens next?

Muon g-2

corrections to g called the anomalous magnetic moment:

Magnetic moment and spin

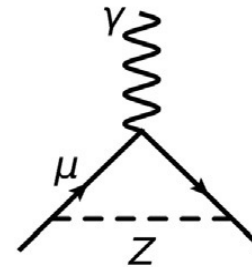


$$\vec{\mu} = g \frac{e}{2m} \vec{S}$$

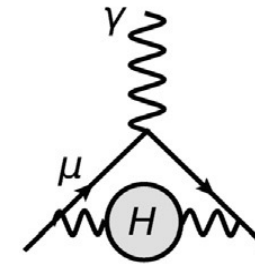
$$a_\mu = \frac{g-2}{2}, g = 2 \text{ at tree level}$$



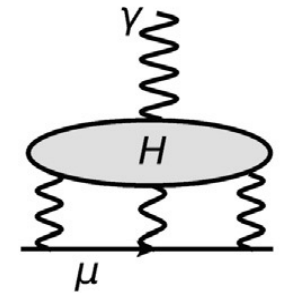
QED



Electroweak



Hadronic
Vacuum
Polarization



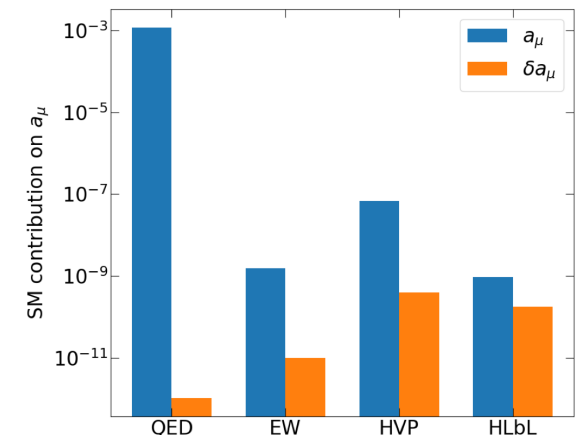
Hadronic
Light-by-light

- Relativistic quantum field theory leads to small radiative corrections.
- g-2 can be measured and calculated to high-precision (sub-ppm).
- It has become a powerful discriminant for BSM physics.

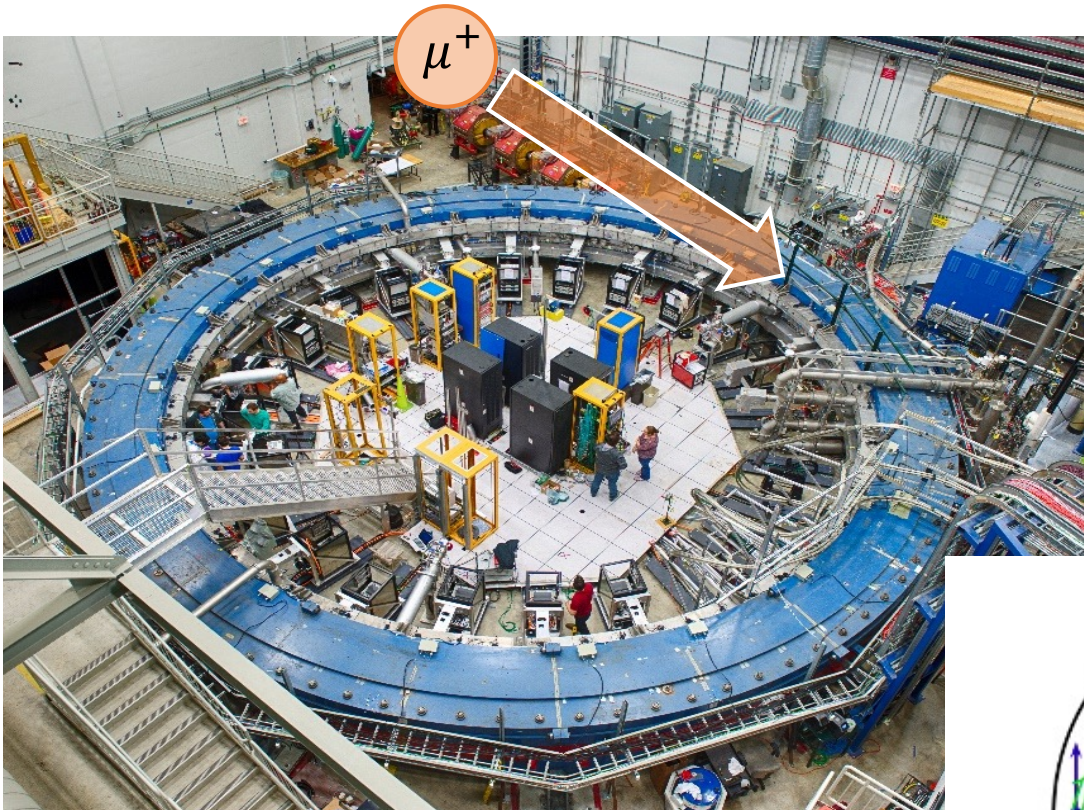
$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{HVP, LO}} + a_\mu^{\text{HVP, NLO}} + a_\mu^{\text{HVP, NNLO}} + a_\mu^{\text{HLbL}} + a_\mu^{\text{HLbL, NLO}}$$

$$= 116\,591\,810(43) \times 10^{-11}.$$

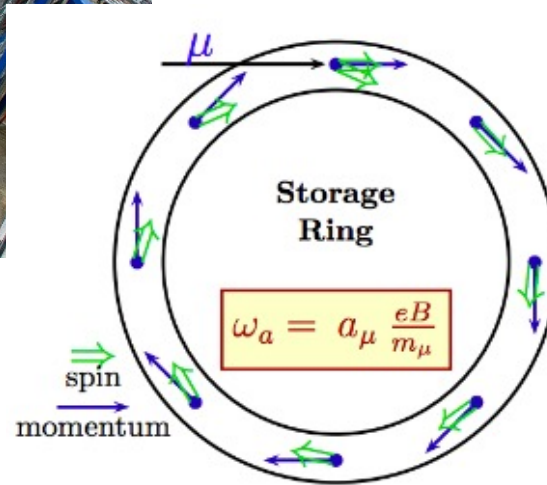
Theory Initiative White Paper
T. Aoyama et al. Phys. Rept. **887** (2020)



Muon g-2 Experiment at FNAL



- Muons are stored in the storage ring (~15 m diameter) under a 1.5 T homogeneous magnetic field.
- Muon spins precess at a rate: ω_a with respect to momentum.



Measure the difference in frequency

Measure the magnetic field of the storage ring

$$\omega_a = \omega_s - \omega_c = a_\mu \frac{eB}{m_\mu}$$

Obtain g-2

$$p_{\text{magic}} \simeq 3.09 \text{ GeV}/c$$

ω_s = spin precession frequency;
 ω_c = cyclotron frequency.

Status of Experiment

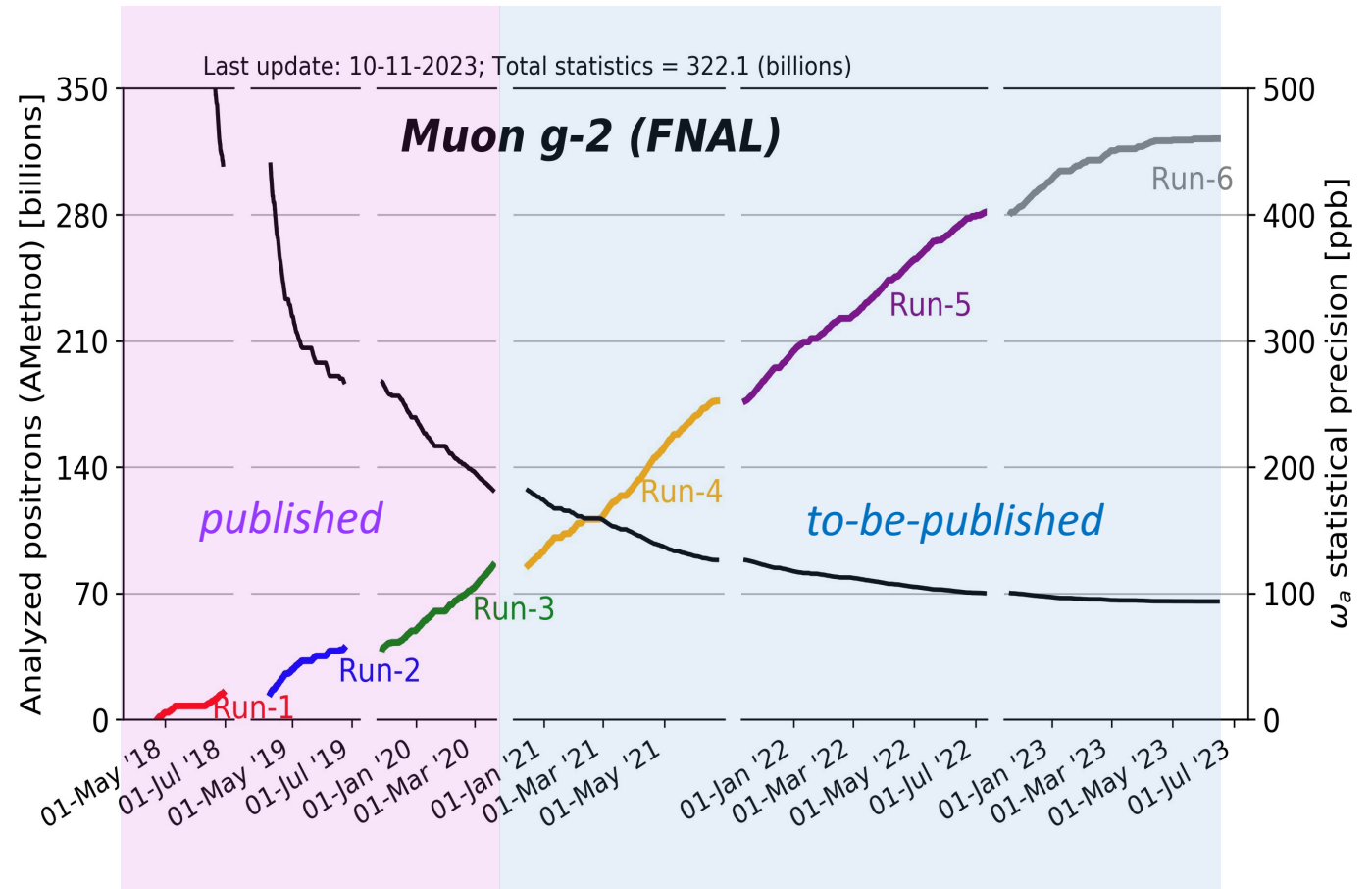
Apr 2021: **Run-1** Result (2018 data):

PRL 126, 141801 (2021)

Aug 2023: **Run-2/3** Result (2019-20 data):

PRL 131, 161802 (2023)

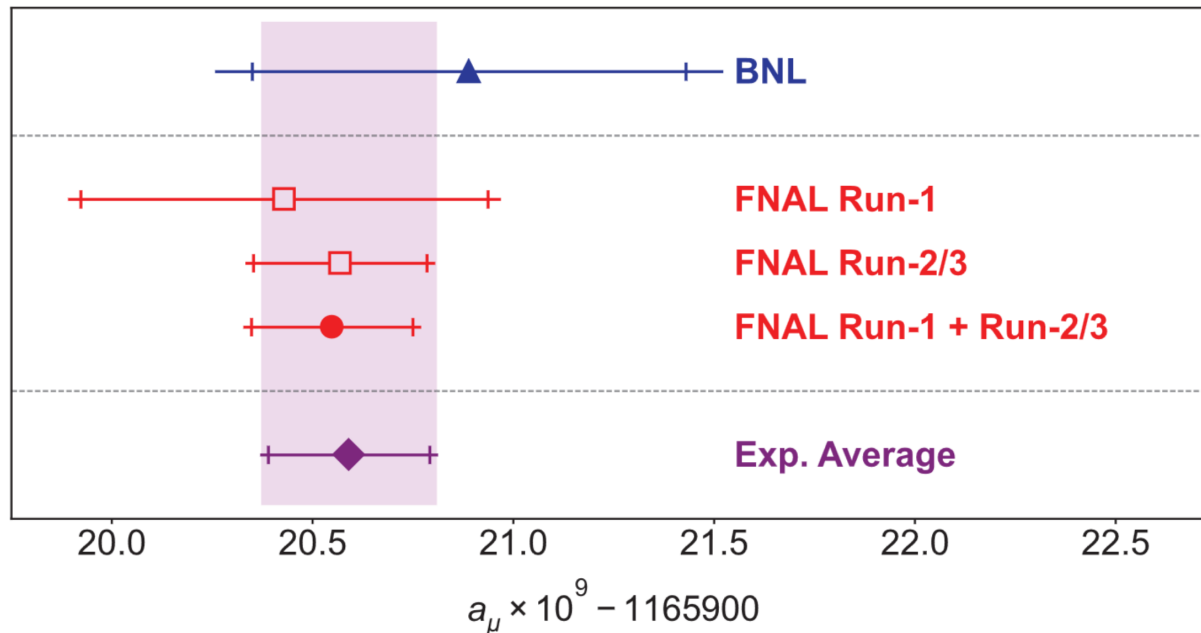
Expected ~ 2025: **Run-4/5/6** Result (2021-23 data)



First (2021) and Second (2023) Results

PRL 126, 141801 (2021)
PRL 131, 161802 (2023)

- Run-1 result (2018 data) and Run-2/3 result (2019/2020 data) were consistent.
- **Both renewed the most precise measurement of muon magnetic anomaly.**



$$a_\mu(\text{Exp}) = 0.00116592059(22) \text{ [190 ppb]}$$

See Talk by O. Kim

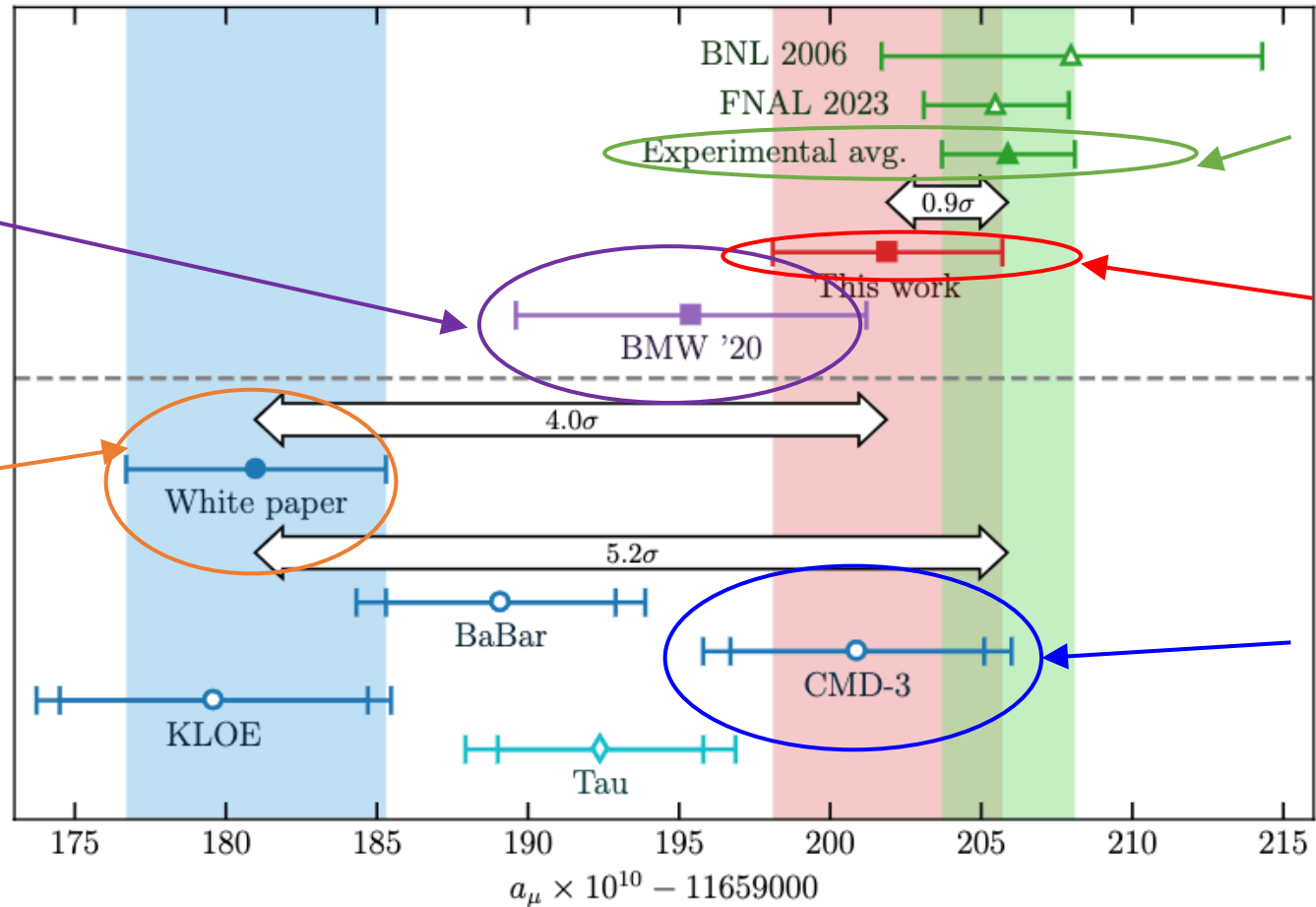
Experiment vs. Theory (SM)

Theory predictions from different approaches (for a_μ (HVP), hadronic vacuum polarization) **don't agree!**

Ab-initio lattice QCD calculation favors the measured value much better than the dispersive method.

Muon $g - 2$ Theory Initiative compiled the SM estimation primarily using the dispersive method for the hadronic vacuum polarization (HVP).

It uses 20+ years of e^+e^- data (contribution dominated by $e^+e^- \rightarrow \pi^+\pi^-$) from various collaborations (BaBar, KLOE, SND, BESIII, etc.)



> 5σ significance by comparing the experiment average and 2020 WP, but several other results sit closer.

New result <https://arxiv.org/pdf/2407.10913> (2024)

New dispersive approach result from CMD-3 has a strong tension with the other dispersive method results (even with the previous themselves: CMD-2).

See g-2 theory talk for more discussion!

Experiment vs. Theory (SM)

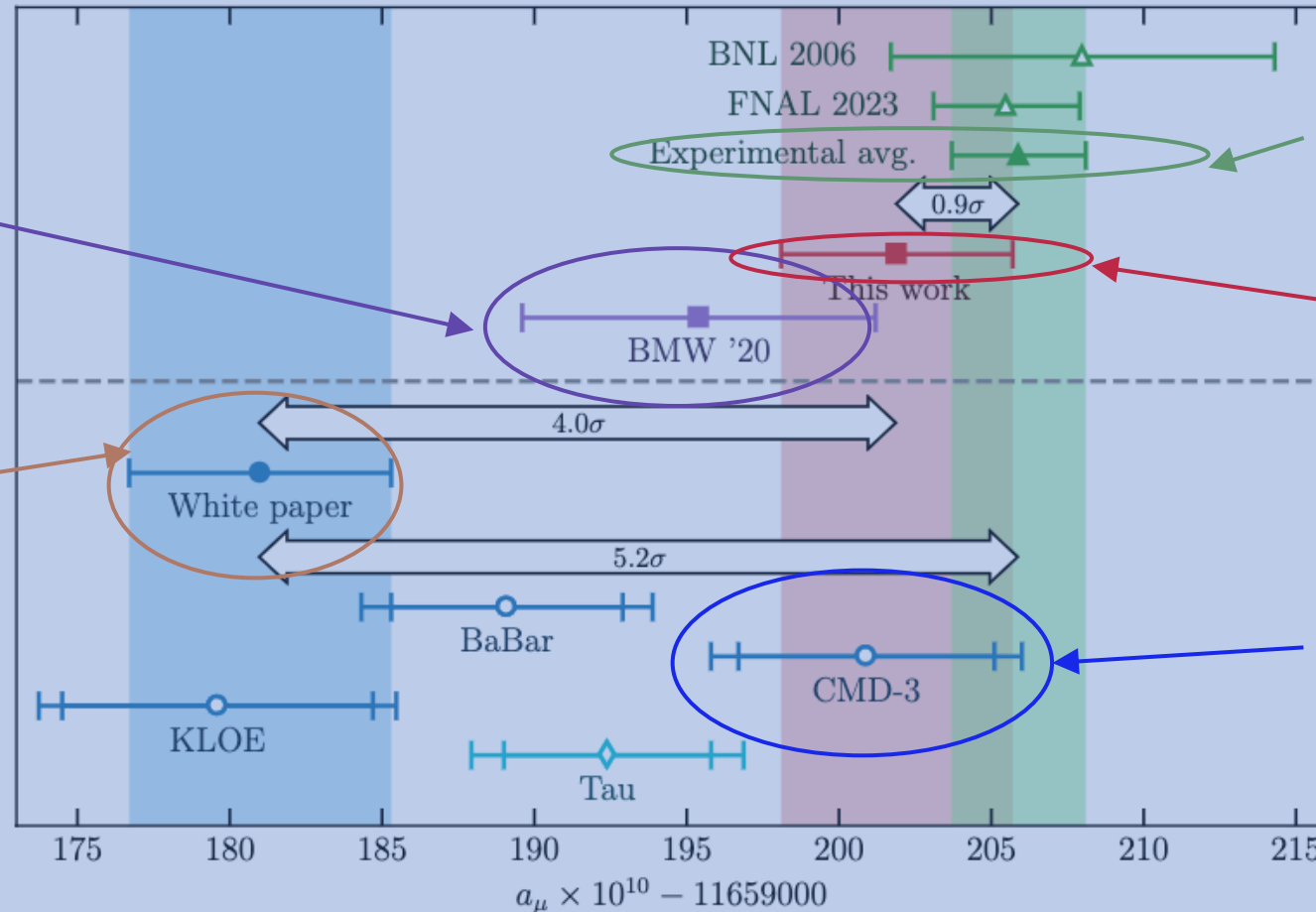
Several on going efforts: <https://muon-gm2-theory.illinois.edu/>

Theory predictions from different approaches (for a_μ (HVP), hadronic vacuum polarization) **don't agree!**

Ab-initio lattice QCD calculation favors the measured value much better than the dispersive method.

Muon $g - 2$ Theory Initiative compiled the SM estimation primarily using the dispersive method for the hadronic vacuum polarization (HVP).

It uses 20+ years of e^+e^- data (contribution dominated by $e^+e^- \rightarrow \pi^+\pi^-$) from various collaborations (BaBar, KLOE, SND, BESIII, etc.)



> 5σ significance by comparing the experiment average and 2020 WP, but several other results sit closer.

New result <https://arxiv.org/pdf/2407.10913> (2024)

New dispersive approach result from CMD-3 has a strong tension with the other dispersive method results (even with the previous themselves: CMD-2).

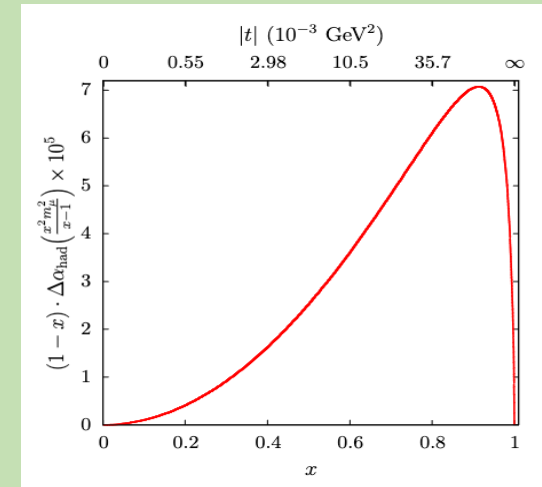
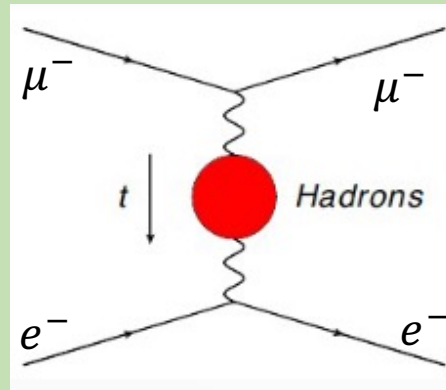
See $g-2$ theory talk for more discussion!

What's next?: MuonE Experiment

- **MuonE @ CERN (Eur. Phys. J. C (2017) 77:139)**: will make independent determination of hadronic leading order contribution to a_μ .
- Measure the hadronic contribution using space-like elastic scattering of 150GeV μ beam on atomic electrons.

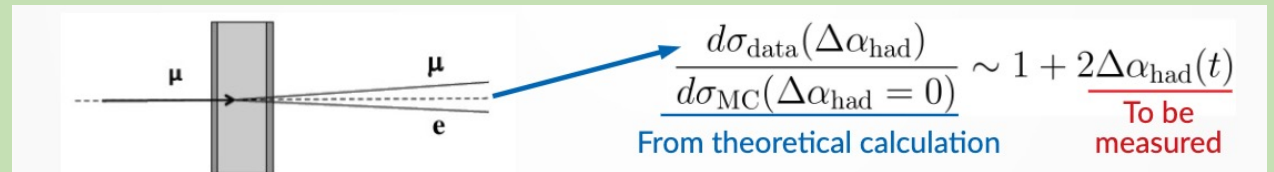
$$a_\mu^{\text{HLO}} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{\text{had}}[t(x)]$$

$$t(x) = \frac{x^2 m_\mu^2}{x-1} < 0$$



Based on the measurement of $\Delta\alpha_{\text{had}}(t)$: hadronic contribution to the running of the QED coupling constant $\alpha(t)$.

Extract $\Delta\alpha_{\text{had}}(t)$ from shape of differential cross-section.

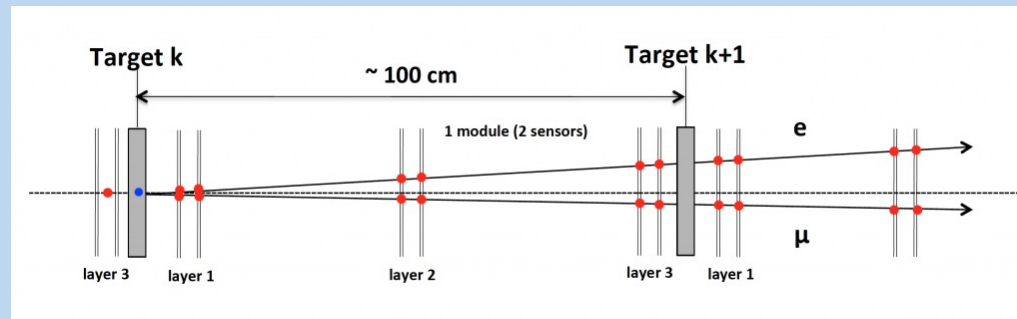
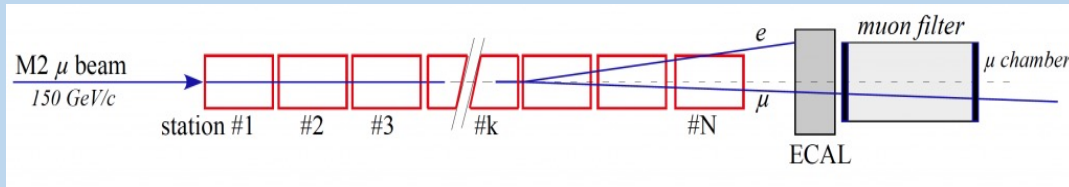


What's next?: MuonE Experiment

- **MuonE @ CERN (Eur. Phys. J. C (2017) 77:139):** will make independent determination of hadronic leading order contribution to a_μ .
- Measure the hadronic contribution using elastic scattering $\mu - e$ with 150GeV Muon beam.

40 identical stations made of thin Be target interspersed Si trackers.

Calorimeter helps with final PID.



Test beam: 2023, pic from CERN Courier



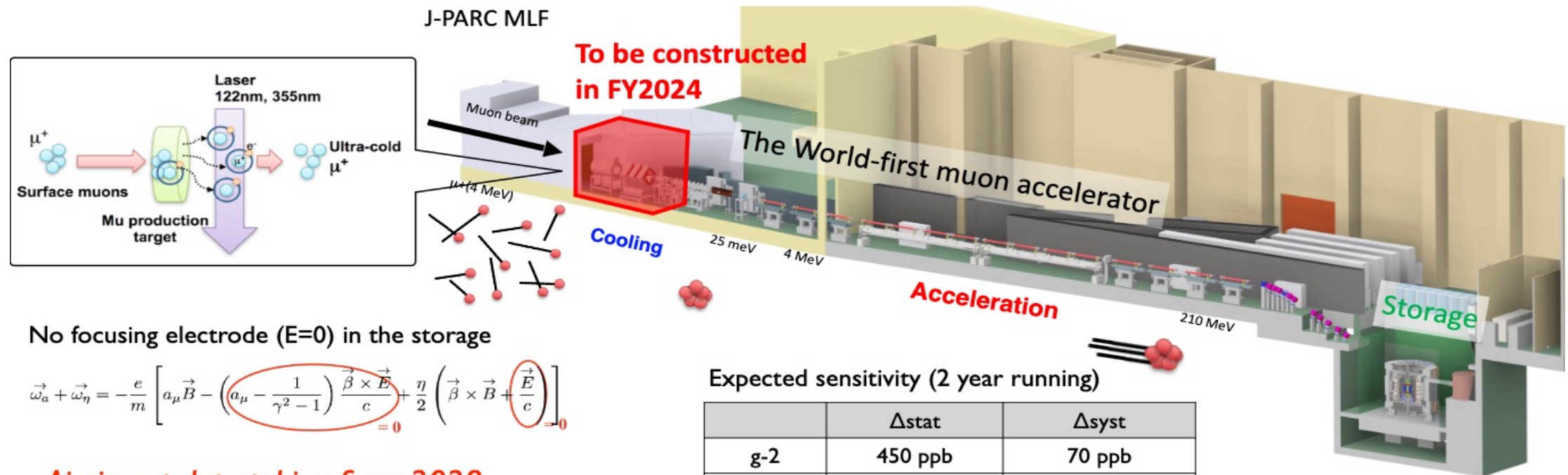
Goal: 3.5×10^{12} elastic scattering events with an electron energy larger than 1 GeV, in 3 years. Aim to achieve a stat error of 0.3% and 10 ppm sys. error. comparable with the results from the time-like dispersive approach and the lattice simulations.

What's next?: Alternative g-2 measurement

Alongside further results from Fermilab there are complementary experimental efforts:

See Talk by K. Suzuki

- **J-PARC g-2 experiment:** provide complementary approach to measure a at the J-PARC facility
 - low emittance muon beam by cooling and re-acceleration:
 - no strong focusing & good injection efficiency (x10)
 - much more compact storage magnet



Aiming at data taking from 2028.

V
Al

measurement

mental efforts:
a at the J-PARC facility

Progress

INTERACTIONS.ORG
PARTICLE PHYSICS NEWS AND RESOURCES

Home About News Physics Hubs Fighting COVID-19 Higgs10 Dark Matter Day [Subscribe to Newsletter](#)

A communication resource from the world's particle physics laboratories.

World's first cooling and acceleration of muon

A muon is an elementary particle like an electron. Muons were first discovered in 1936 as cosmic rays falling from the sky. Natural muons originated from cosmic rays have been used to see through the interior of large and/or thick objects, such as pyramids. Presently, muons can be produced in much higher intensity using accelerators for the use of various research and applications.

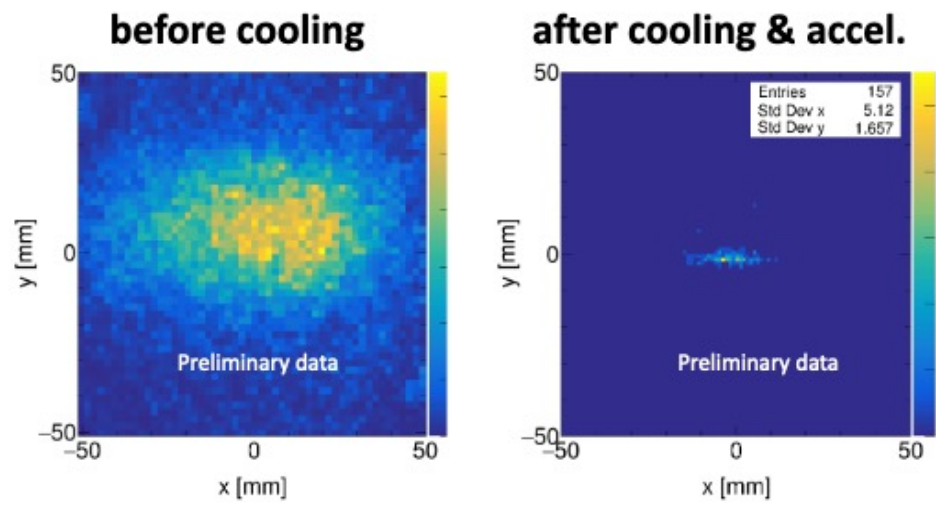
[Read More](#)

<https://www.interactions.org>



World first The experimental set up for muon cooling and acceleration at J-PARC. A beam of antimatter muons enters the apparatus from the right. Credit: J-PARC

Beam profiles



target

Cooling

25 meV 4 MeV

No focusing electrode ($E=0$) in the storage

$$\vec{\omega}_a + \vec{\omega}_\eta = -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} + \frac{\eta}{2} \left(\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} \right) \right]$$

Expected sensitivity

	Δ	
g-2	450 ppb	70 ppb
EDM	$1.5 \times 10^{-21} e \cdot \text{cm}$	$0.4 \times 10^{-21} e \cdot \text{cm}$

Aiming at data taking from 2028.

Muons CLFV Searches: Motivations

Why search for CLFV in the muon sector?

Muons as Probes of New Physics

Muon $g-2$

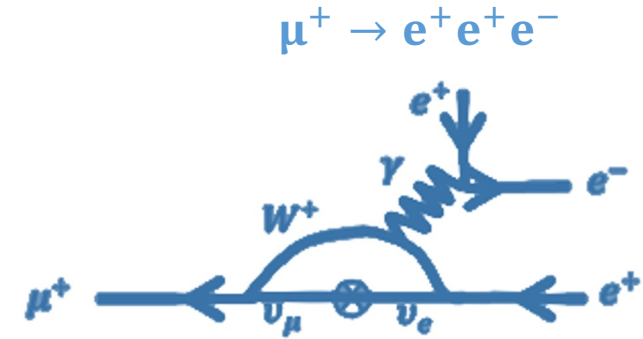
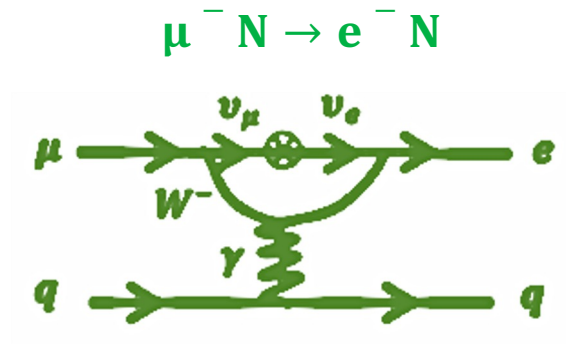
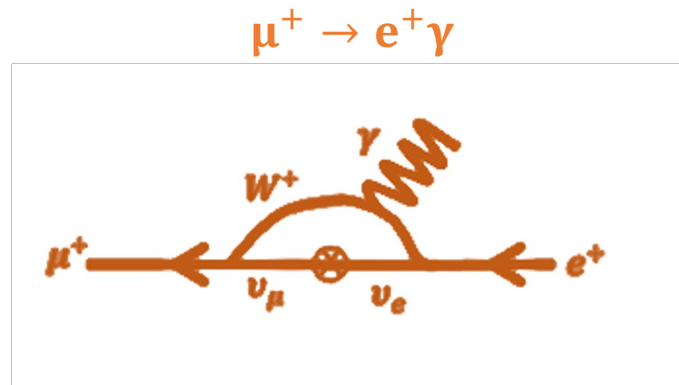
Muon CLFV Searches: Motivations

Muon CLFV Searches: Design, Status

What happens next?

Charged Lepton Flavor Violation (CLFV)

- Adding neutral lepton flavor violation to the Standard Model, introduces CLFV at loop level, mediated by W bosons:



No outgoing neutrinos!

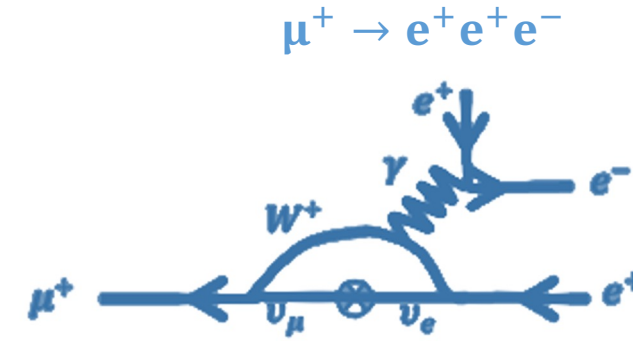
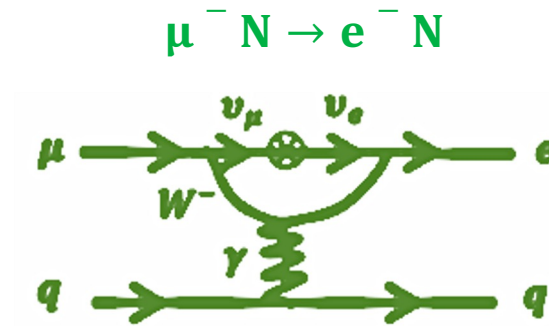
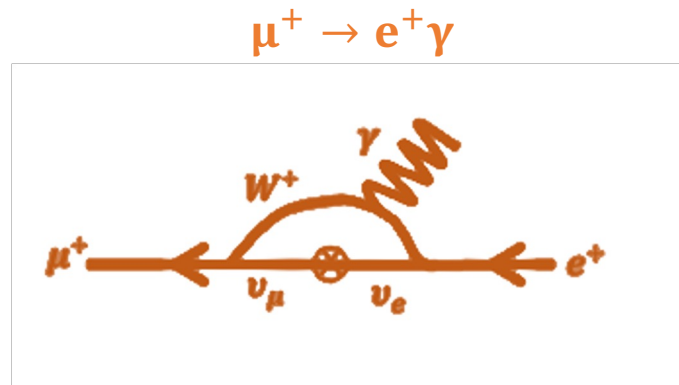
- Rates heavily suppressed by GIM suppression and are far below any conceivable experiment could measure:

$$B(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left(\frac{1}{4}\right) \sin^2 2\theta_{13} \sin^2 \theta_{23} \left| \frac{\Delta m_{13}^2}{M_W^2} \right|^2$$

$$B(\mu \rightarrow e\gamma) \sim \mathcal{O}(10^{-54})$$

Charged Lepton Flavor Violation (CLFV)

- Adding neutral lepton flavor violation to the Standard Model, introduces CLFV at loop level, mediated by W bosons:



No outgoing neutrinos!

- Rates heavily suppressed by GIM suppression and are far below any conceivable experiment could measure:

$$B(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left(\frac{1}{4}\right) \sin^2 2\theta_{13} \sin^2 \theta_{23} \left| \frac{\Delta m_{13}^2}{M_W^2} \right|^2$$

$$B(\mu \rightarrow e\gamma) \sim \mathcal{O}(10^{-54})$$

- ...but many Beyond Standard Model (BSM) theories (e.g. SO(10) SUSY, scalar leptoquarks, seesaw models) predict enhanced rates of CLFV just below current limits $\mathcal{O}(10^{-13})$.

Muon CLFV is an indirect search for New Physics and offers a deep probe of well-motivated BSM theories.

Current Experimental Searches for CLFV

- There is a global program of experiments currently coming online and which seek to observe several types of muon CLFV:

Mode	Current Upper Limit (at 90% CL)	Projected Limit (at 90% CL)	Upcoming Experiment/s
$\mu^+ \rightarrow e^+ \gamma$	3.1×10^{-13}	4×10^{-14}	MEG II
$\mu^+ \rightarrow e^+ e^+ e^-$	1.0×10^{-12}	5×10^{-15} 10^{-16}	Mu3e Phase-I Mu3e Phase-II
$\mu^- N \rightarrow e^- N$	7×10^{-13} (SINDRUM-II, 2006)	8×10^{-15} 6×10^{-16} 8×10^{-17} (Mu2e)	COMET Phase-I Mu2e Run-I Mu2e Run-II/ COMET Phase-II

Tight limits already due to nature of the muon allowing for intense muon beam and reducible, well understood backgrounds

Effective Physics Reach

- Can think of indirect searches in terms of Effective Field Theories;
- 90+ operators describe these processes;
- *Eur.Phys.J.C 82 (2022) 9, 836* reduced to 6 terms for $\mu^+ \rightarrow e^+ \gamma$, $\mu^+ \rightarrow e^+ e^+ e^-$, and spin-independent $\mu^- \text{N} \rightarrow e^- \text{N}$;
- These represent different types of physics contributing to the three channels:

$$\delta\mathcal{L} = \frac{1}{\Lambda_{LFV}^2} \left[C_D (\bar{e} \sigma^{\alpha\beta} P_R \mu) F_{\alpha\beta} + C_S (\bar{e} P_R \mu) (\bar{e} P_R e) + C_{VR} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_R e) \right. \\ \left. + C_{VL} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_L e) + C_{A\text{light}} \mathcal{O}_{A\text{light}} + C_{A\text{heavy}\perp} \mathcal{O}_{A\text{heavy}\perp} \right]$$

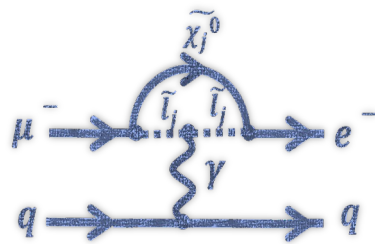
Λ = Effective Mass Reach, \mathbf{D} = dipole, \mathbf{V} = vector, \mathbf{S} = scalar

Effective Physics Reach

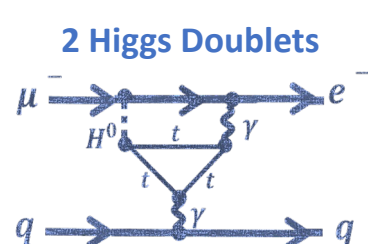
Dipole Term:

Mediating $\mu^+ \rightarrow e^+ \gamma$
 Contributing to $\mu^+ \rightarrow e^+ e^+ e^-$ and
 $\mu^- N \rightarrow e^- N$ at loop level

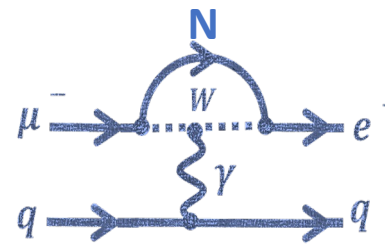
$$\delta\mathcal{L} = \frac{1}{\Lambda_{LFV}^2} \left[C_D (\bar{e} \sigma^{\alpha\beta} P_R \mu) F_{\alpha\beta} + C_S (\bar{e} P_R \mu) (\bar{e} P_R e) + C_{VR} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_R e) \right. \\ \left. + C_{VL} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_L e) + C_{A\text{light}} \mathcal{O}_{A\text{light}} + C_{A\text{heavy}\perp} \mathcal{O}_{A\text{heavy}\perp} \right]$$



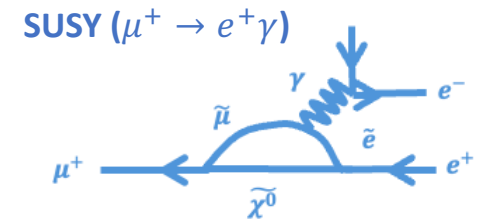
SO(10) SUSY
 Rate $\sim 10^{-15}$



$g(H_{\mu e}) \sim 10^{-4} g(H_{\mu\mu})$



$|U_{\mu N} U_{e N}|^2 \sim 8 \times 10^{-13}$



Eur.Phys.J.C 82 (2022) 9, 836
 Davidson & Echenard

Effective Physics Reach

“Contact”
Scalar
 $\mu^+ \rightarrow e^- e^+ e^+$

Leptonic “Contact” term
i.e. 4 Fermion Term
 $\mu^+ \rightarrow e^- e^+ e^+$ at leading order.
Heavily suppressed in $\mu^+ \rightarrow e^+ \gamma$

$$\delta\mathcal{L} = \frac{1}{\Lambda_{LFV}^2} \left[C_D (\bar{e} \sigma^{\alpha\beta} P_R \mu) F_{\alpha\beta} + C_S (\bar{e} P_R \mu) (\bar{e} P_R e) + C_{VR} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_R e) \right. \\ \left. + C_{VL} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_L e) + C_{A\text{light}} \mathcal{O}_{A\text{light}} + C_{A\text{heavy}\perp} \mathcal{O}_{A\text{heavy}\perp} \right]$$



“Contact”
Vector
 $\mu^+ \rightarrow e^- e^+ e^+$

Effective Physics Reach

quark “Contact” term

i.e. 4 Fermion Term

$\mu^- N \rightarrow e^- N$ at leading order.

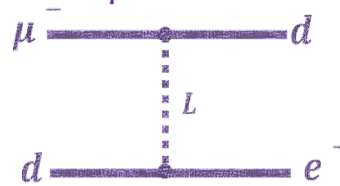
Heavily suppressed in $\mu^+ \rightarrow e^+ \gamma$

Au and Al are prototypical “heavy” and “light” targets

$$\delta\mathcal{L} = \frac{1}{\Lambda_{LFV}^2} \left[C_D (\bar{e} \sigma^{\alpha\beta} P_R \mu) F_{\alpha\beta} + C_S (\bar{e} P_R \mu) (\bar{e} P_R e) + C_{VR} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_R e) \right. \\ \left. + C_{VL} (\bar{e} \gamma^\alpha P_L \mu) (\bar{e} \gamma_\alpha P_L e) + C_{A\text{light}} \mathcal{O}_{A\text{light}} + C_{A\text{heavy}\perp} \mathcal{O}_{A\text{heavy}\perp} \right]$$

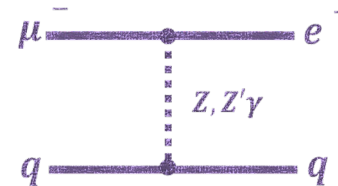
Leptoquarks

$$M_{LQ} = 3000 (\lambda_{\mu d} \lambda_{ed})^{\frac{1}{2}} \text{TeV}/c^2$$



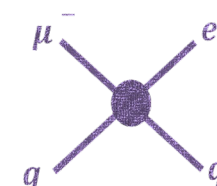
New Bosons

$$M_{Z'} = 3000 \text{TeV}/c^2$$



Compositeness

$$\Lambda_c \sim 3000 \text{TeV}$$

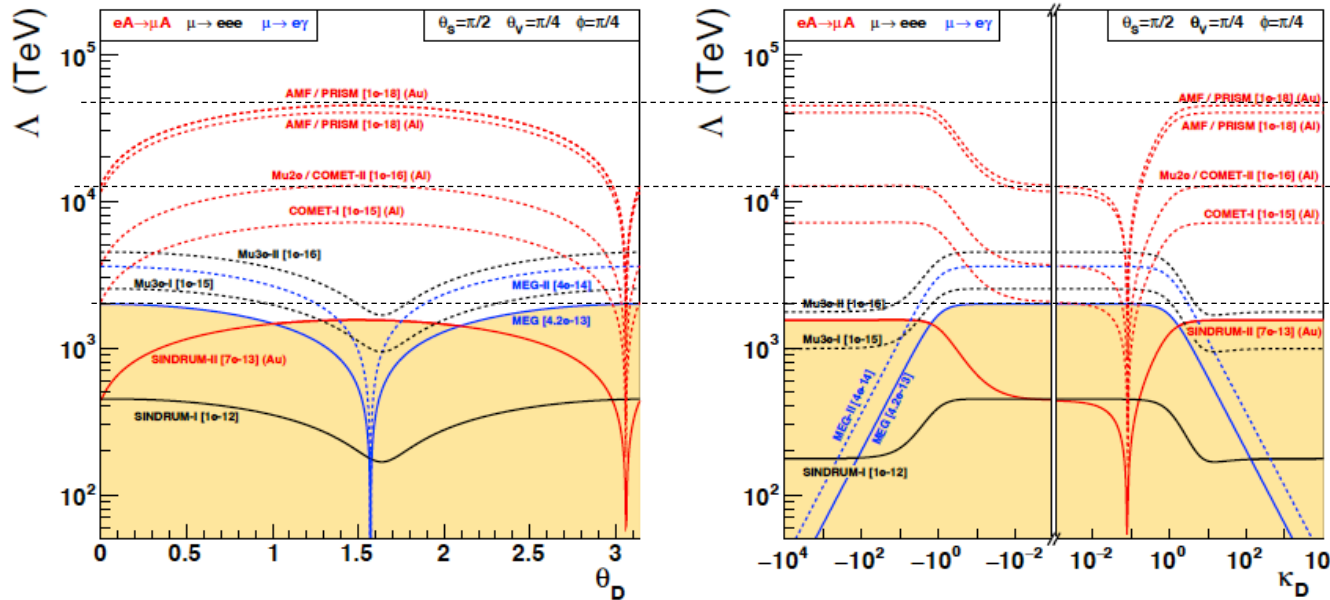


Eur.Phys.J.C 82 (2022) 9, 836

Davidson & Echenard

Effective Physics Reach

Current physics reach at $O(10^3)$ TeV, Projections of upto $O(10^4)$ TeV in next generation.



High magnitude κ_D = contact-like, closer to zero is dipole-like

Λ = effective mass reach

$\vec{C} \cdot \vec{e}_D$	$ \vec{e}_D \cos \theta_D$
$\vec{C} \cdot \vec{e}_S$	$ \vec{e}_S \sin \theta_D \cos \theta_S$
$\vec{C} \cdot \vec{e}_{VL}$	$ \vec{e}'_{VL} \sin \theta_D \sin \theta_S \cos \theta_V$
$\vec{C} \cdot \vec{e}_{VR}$	$ \vec{e}'_{VR} \sin \theta_D \sin \theta_S \cos \theta_V$
$\vec{C} \cdot \vec{e}_{Align}$	$ \vec{e}_{Align} \sin \theta_D \sin \theta_S \sin \theta_V \sin \phi$
$\vec{C} \cdot \vec{e}_{Aheavy\perp}$	$ \vec{e}_{Aheavy\perp} \sin \theta_D \sin \theta_S \sin \theta_V \cos \phi$

Parameterize coefficient space with spherical coordinates *lets you express constraints on all three processes simultaneously.*

$$\kappa_D = \cotan(\theta_D - \pi/2)$$

where angle θ_D , parametrizes relative magnitude of dipole and four-fermion coefficients.

Eur.Phys.J.C 82 (2022) 9, 836 Davidson & Echenard

Note: plots are a slice in multi-dimensional space, several other plots shown in paper for different slices

Complementarity amongst channels

- All three channels are sensitive to many New Physics models → discovery sensitivity across the board.
- Relative Rates however will be model dependent and can be used to elucidate the underlying physics.

Mode	$\mu^+ \rightarrow e^+ e^+ e^-$	$\mu^- N \rightarrow e^- N$	$\frac{BR(\mu^+ \rightarrow e^+ e^+ e^-)}{BR(\mu^+ \rightarrow e^+ \gamma)}$	$\frac{BR(\mu^- N \rightarrow e^- N)}{BR(\mu^+ \rightarrow e^+ \gamma)}$
MSSM	Loop	Loop	$\sim 6 \times 10^{-3}$	$10^{-3} - 10^{-2}$
Type I Seesaw	Loop	Loop	$3 \times 10^{-3} - 0.3$	0.1-10
Type II Seesaw	Tree	Loop	$(0.1 - 3) \times 10^3$	10^{-2}
Type III Seesaw	Tree	Tree	$\sim 10^3$	10^3
LFV Higgs	Loop	Loop	10^{-2}	0.1
Composite Higgs	Loop	Loop	0.05-0.5	2-20

Complementarity amongst channels

- All three channels are sensitive to many New Physics models → discovery sensitivity across the board.
- Relative Rates however will be model dependent and can be used to elucidate the underlying physics.

Mode	$\mu^+ \rightarrow e^+ e^+ e^-$	$\mu^- N \rightarrow e^- N$	$\frac{BR(\mu^+ \rightarrow e^+ e^+ e^-)}{BR(\mu^+ \rightarrow e^+ \gamma)}$	$\frac{BR(\mu^- N \rightarrow e^- N)}{BR(\mu^+ \rightarrow e^+ \gamma)}$
MSSM	Loop	Loop	$\sim 6 \times 10^{-3}$	$10^{-3} - 10^{-2}$
Type I Seesaw	Loop	Loop	$3 \times 10^{-3} - 0.3$	0.1-10
Type II Seesaw	Tree	Loop	$(0.1 - 3) \times 10^3$	10^{-2}
Type III Seesaw	Tree	Tree	$\sim 10^3$	10^3
LFV Higgs	Loop	Loop	10^{-2}	0.1
Composite Higgs	Loop	Loop	0.05-0.5	2-20



CLFV: Experimental Design

Current experiments, design and status updates.

Muons as Probes of New Physics

Muon $g-2$

Muon CLFV Searches: Motivations

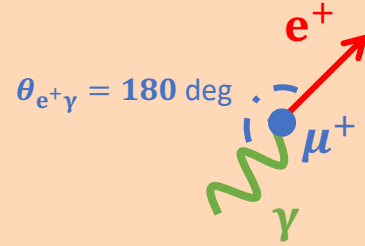
Muon CLFV Searches: Design, Status

What happens next?

$\mu^+ \rightarrow e^+ \gamma$: Physics

Signal:

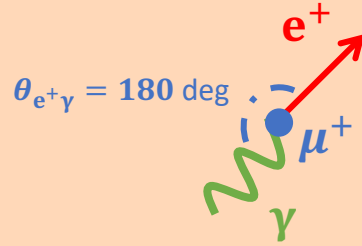
- Two body decay:
 - $e^+ \gamma$ coincidence in time;
 - $E_{e^+} = E_\gamma$ 52.8 MeV;
 - $\theta_{e^+ \gamma} = 180$ deg. i.e. back-to-back.



$\mu^+ \rightarrow e^+ \gamma$: Physics

Signal:

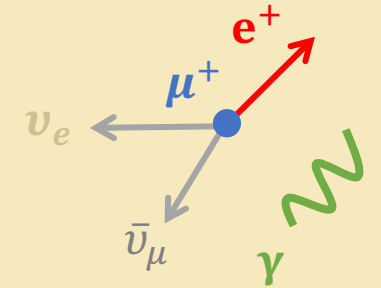
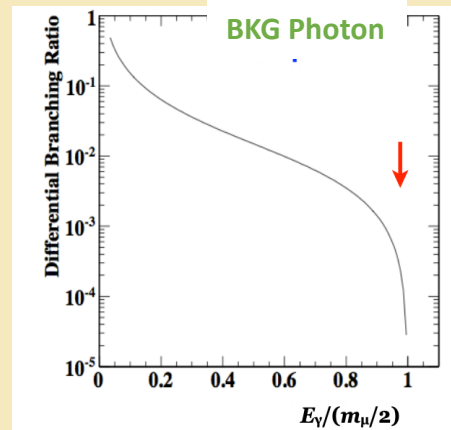
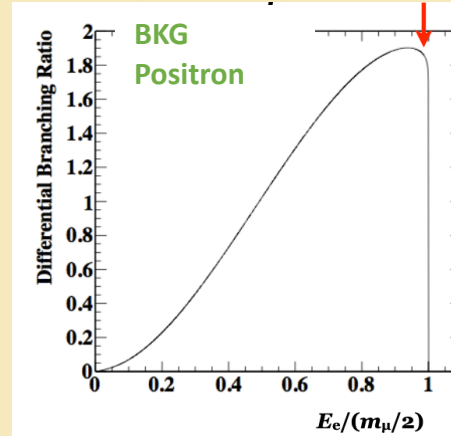
- Two body decay:
 - $e^+ \gamma$ coincidence in time;
 - $E_{e^+} = E_\gamma = 52.8 \text{ MeV}$;
 - $\theta_{e^+ \gamma} = 180 \text{ deg}$. i.e. back-to-back.



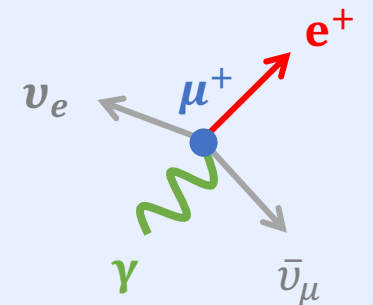
Backgrounds:

- Dominant background from **accidentals**:

W. Otani (ICHEP 2024)



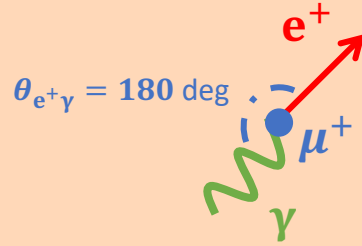
Also, **rare physics background**:



$\mu^+ \rightarrow e^+ \gamma$: Physics

Signal:

- Two body decay:
 - $e^+ \gamma$ coincidence in time;
 - $E_{e^+} = E_\gamma = 52.8 \text{ MeV}$;
 - $\theta_{e^+ \gamma} = 180 \text{ deg.}$ i.e. back-to-back.



Strategy:

- Measure $E_\gamma, p_{e^+}, \theta_{\gamma e^+}, t_{e^+}$ with the best possible resolutions.

Signal

$$N_{\text{sig}} = R_\mu \times T \times \Omega \times \mathcal{B} \times \epsilon_\gamma \times \epsilon_e \times \epsilon_{\text{sel}}$$

Beam intensity Acceptance Branching ratio Efficiencies

Background

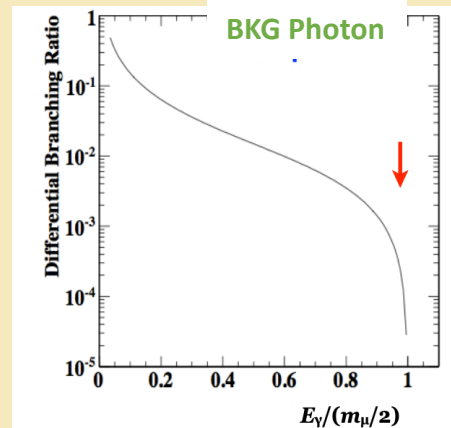
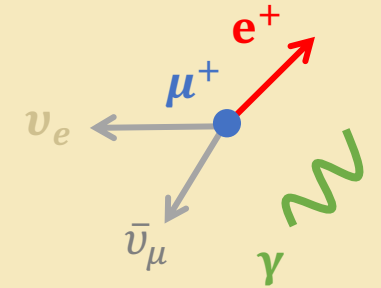
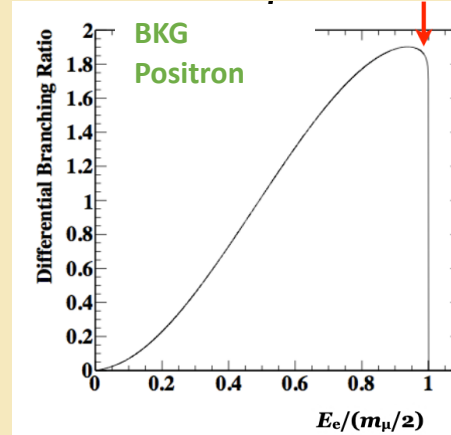
$$N_{\text{acc}} \propto R_\mu^2 \times \Delta E_\gamma^2 \times \Delta E_e \times \Delta \Theta_{e\gamma}^2 \times \Delta t_{e\gamma} \times T$$

E_γ resolution E_e resolution Angular resolution Time resolution

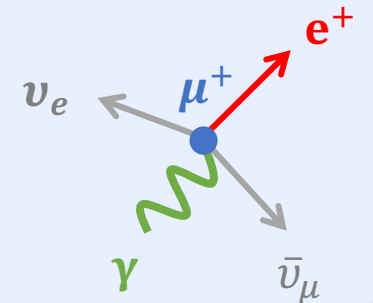
Backgrounds:

- Dominant background from **accidentals**:

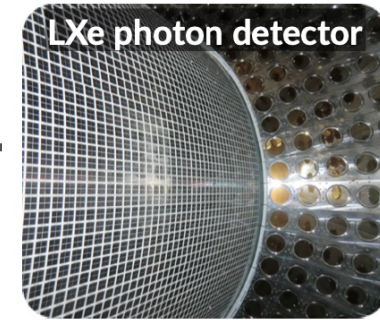
W. Otani (ICHEP 2024)



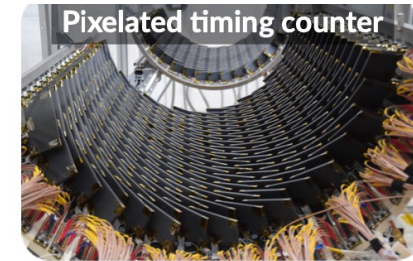
Also, **rare physics background**:



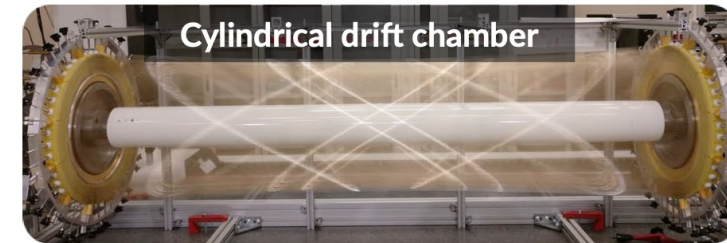
$\mu^+ \rightarrow e^+ \gamma$: MEG-II Design



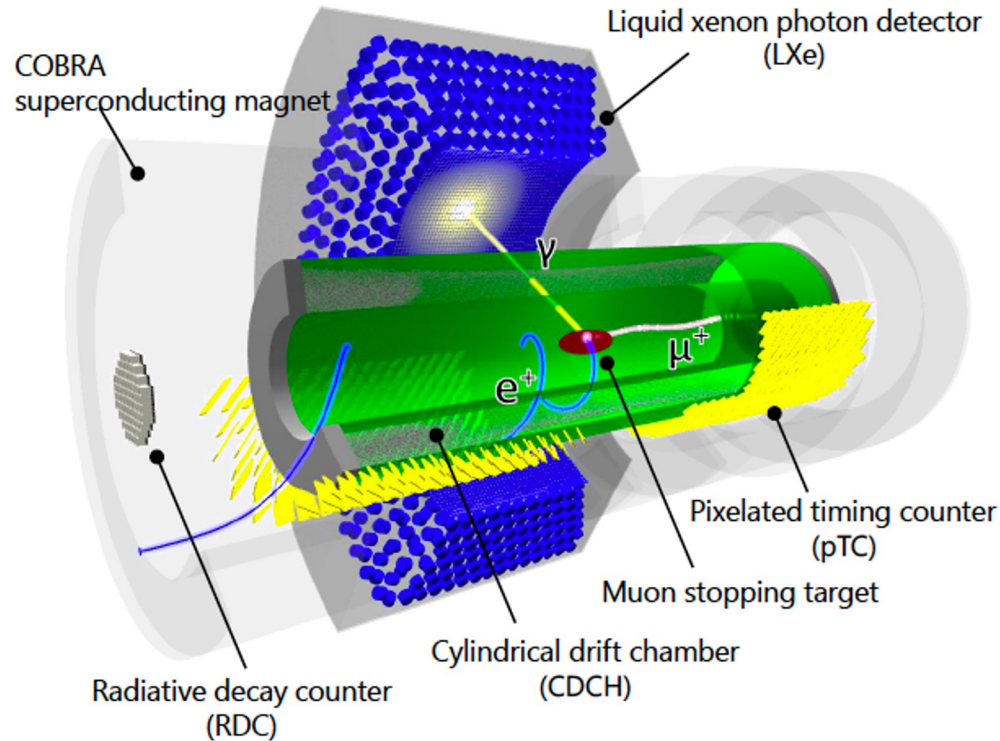
- 900L of LXe
- Highly granular scintillation readout with 4092 SiPM and 668 PMT



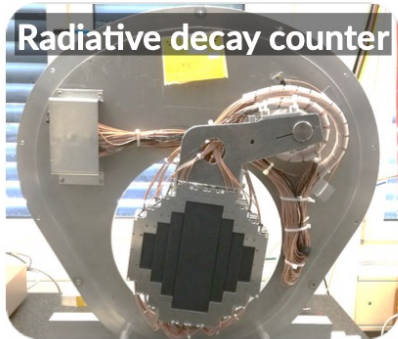
- 512 plastic scintillator plates
- 40 ps time resolution average



- Low mass design with single gas volume
- Drift cells with stereo wires



PSI proton cyclotron (2.3mA, 1.4MW)
World's most intense DC muon beam



- BKG photon suppression by identifying associated low mom. positron.

Design:

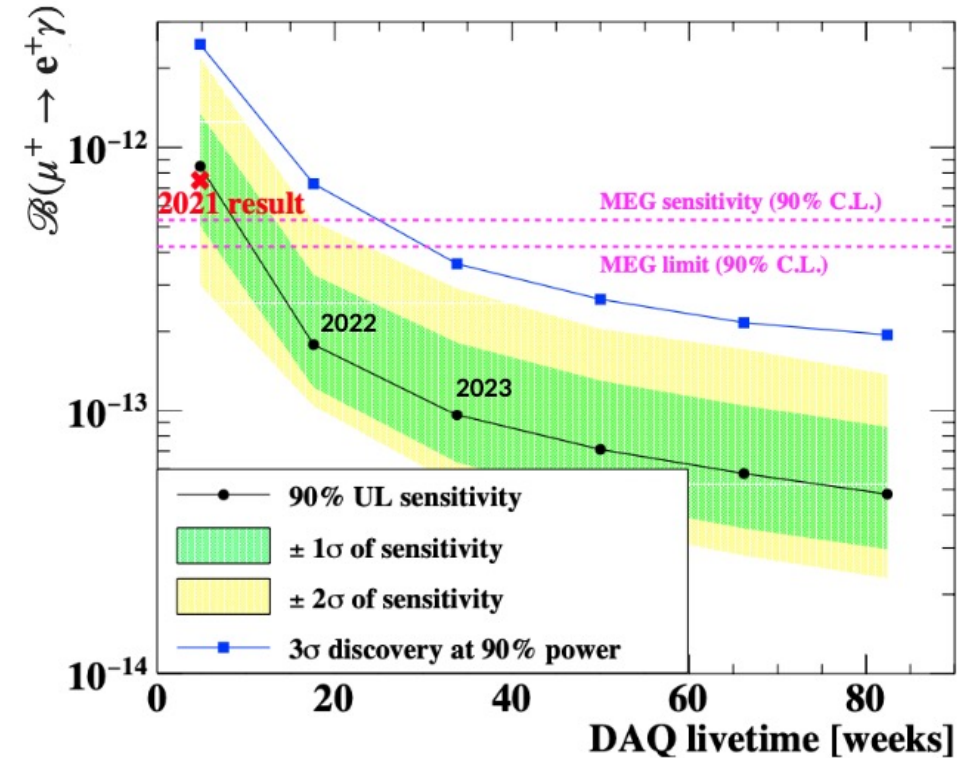
- Based at PSI, muon stopping rate of $10^7 \mu^+ / s$, $p = 28 \text{ MeV}/c$.
- μ^+ stopped on thin plastic target - decay at rest to exploit the two-body kinematics.
- Accurate reconstruction of photon and positron energy and time:
 - **Magnetic spectrometer and low mass drift chamber** to track the candidate positron.
 - **LXe photon detector** measures the timing, energy and position of the photon.

$\mu^+ \rightarrow e^+ \gamma$: Status

Eur.Phys.J.C 84 (2024) 3, 216

Status:

- MEG-II has been taking physics data since 2021.
- Results from the first physics run show:
 - No excess over background-only hypothesis:
 - Upper limit $\mathbf{B(\mu^+ \rightarrow e^+ \gamma) < 7.5 \times 10^{-13}}$ (90% C.L.)
 - Combined with MEG: $\mathbf{B(\mu^+ \rightarrow e^+ \gamma) < 3.1 \times 10^{-13}}$ (90% C.L.)
- x10 more data already taken: new results coming soon!
- Physics run will continue until PSI shutdown in 2027.
 - Goal to reach 6×10^{-14} (x10 on MEG) and potential discovery.

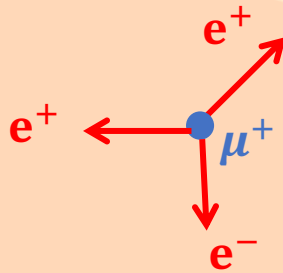


See Talk by M. De Gerone

$\mu^+ \rightarrow e^+ e^+ e^-$: Physics

Signal:

- **Three body decay:**
 - Common vertex
 - Coplanar
 - $\sum p_i = 0, \sum E_i = m_\mu, \Delta t_{eee} = 0$

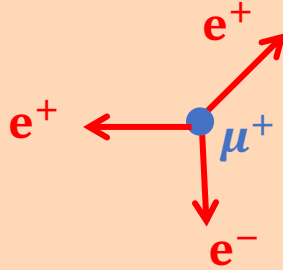


$\mu^+ \rightarrow e^+ e^+ e^-$: Physics

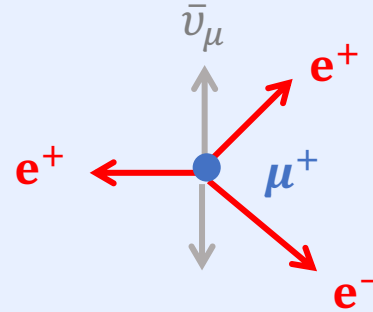
Signal:

Three body decay:

- Common vertex
- Coplanar
- $\sum p_i = 0, \sum E_i = m_\mu, \Delta t_{eee} = 0$



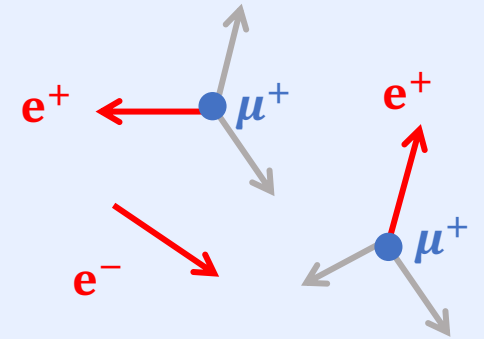
Backgrounds:



Internal conversions:

- Common vertex
- $\sum p_i \neq 0,$
- $\sum E_i < m_\mu,$
- $\Delta t_{eee} = 0$

Combinational:



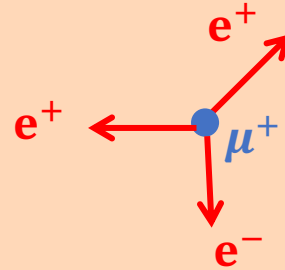
- No common vertex
- $\sum p_i \neq 0,$
- $\sum E_i \neq m_\mu,$
- $\Delta t_{eee} \neq 0$

$\mu^+ \rightarrow e^+ e^+ e^-$: Physics

Signal:

Three body decay:

- Common vertex
- Coplanar
- $\sum p_i = 0, \sum E_i = m_\mu, \Delta t_{eee} = 0$

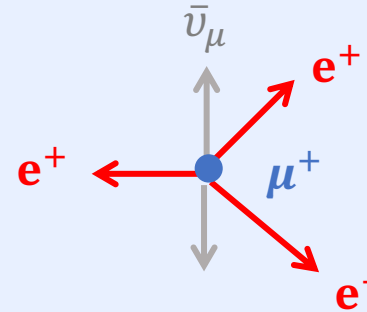


Strategy:

Need to establish that three charged tracks (total +) emanate from the same location and coincide in time, this requires:

- Precise time resolution;
- Excellent position and momentum resolution.

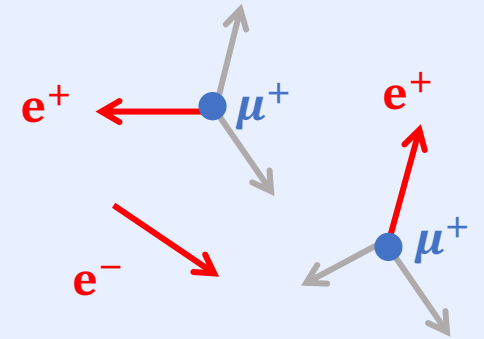
Backgrounds:



Internal conversions:

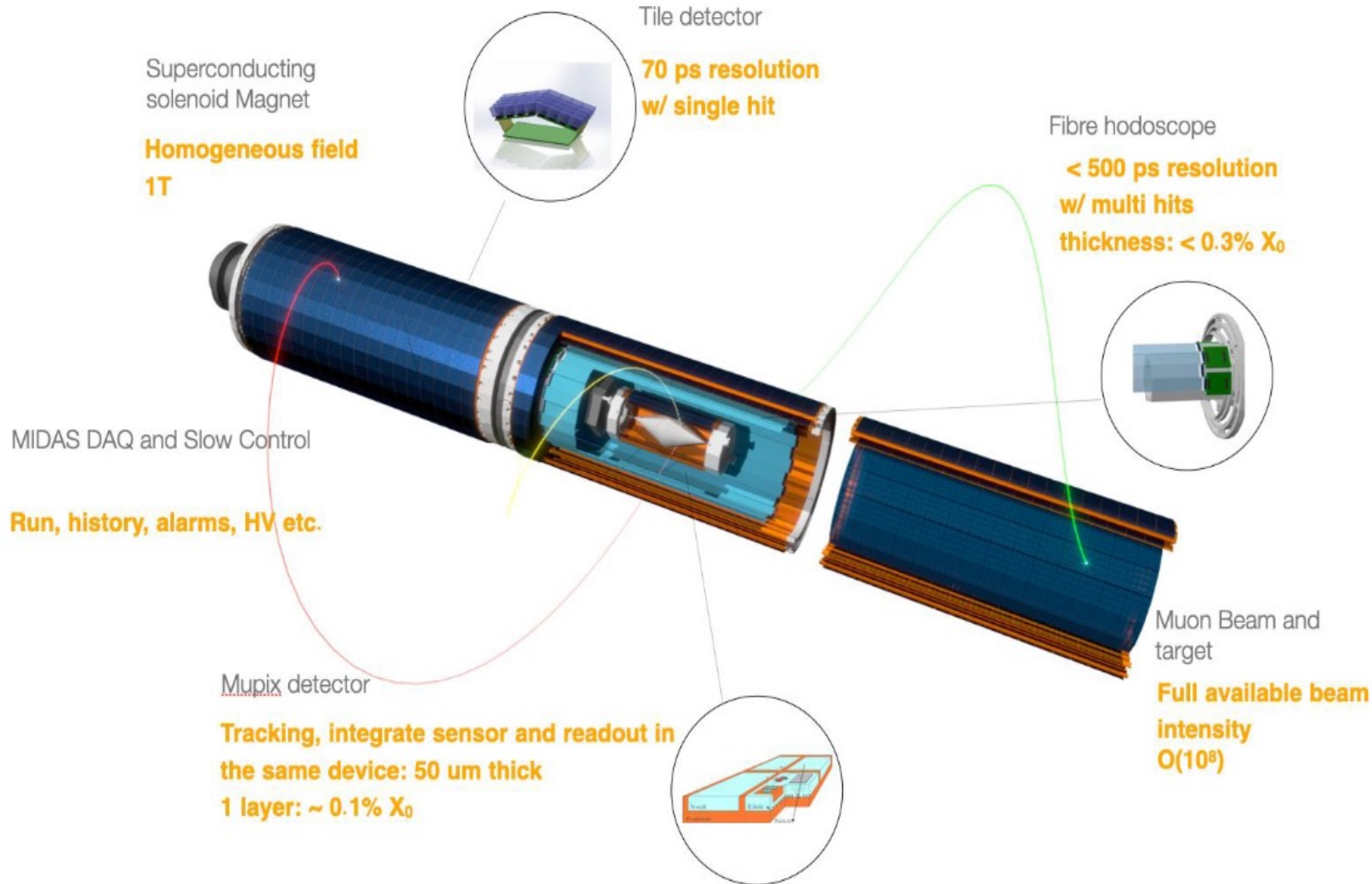
- Common vertex
- $\sum p_i \neq 0,$
- $\sum E_i < m_\mu,$
- $\Delta t_{eee} = 0$

Combinational:



- No common vertex
- $\sum p_i \neq 0,$
- $\sum E_i \neq m_\mu,$
- $\Delta t_{eee} \neq 0$

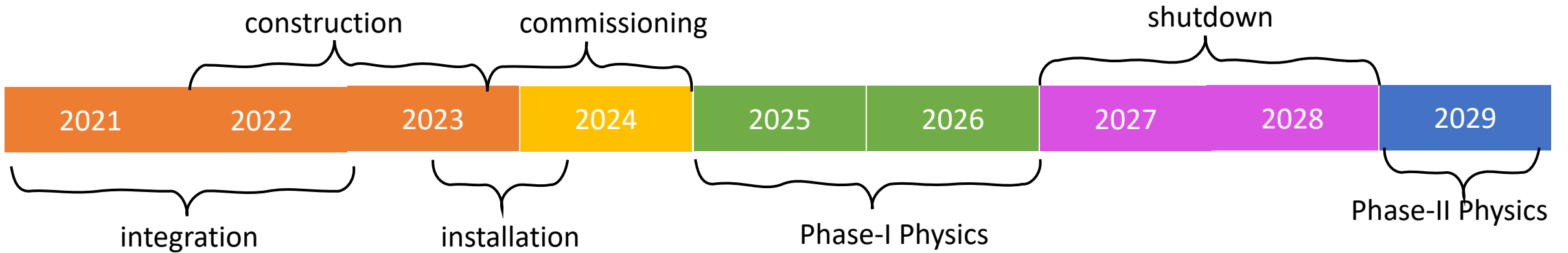
$\mu^+ \rightarrow e^+ e^+ e^-$: Mu3e Design



Design:

- High tracker occupancy requires excellent timing and position resolution to select hits belonging to the same track: thin, fast, high-resolution detectors:
 - 175 HV-MAPS channels
 - ~ 3000 SciFi and $\sim 7K$ Tile TOF channels.
- Method of recurling tracks allows good momentum resolution.
- Superconducting magnet (not shown).

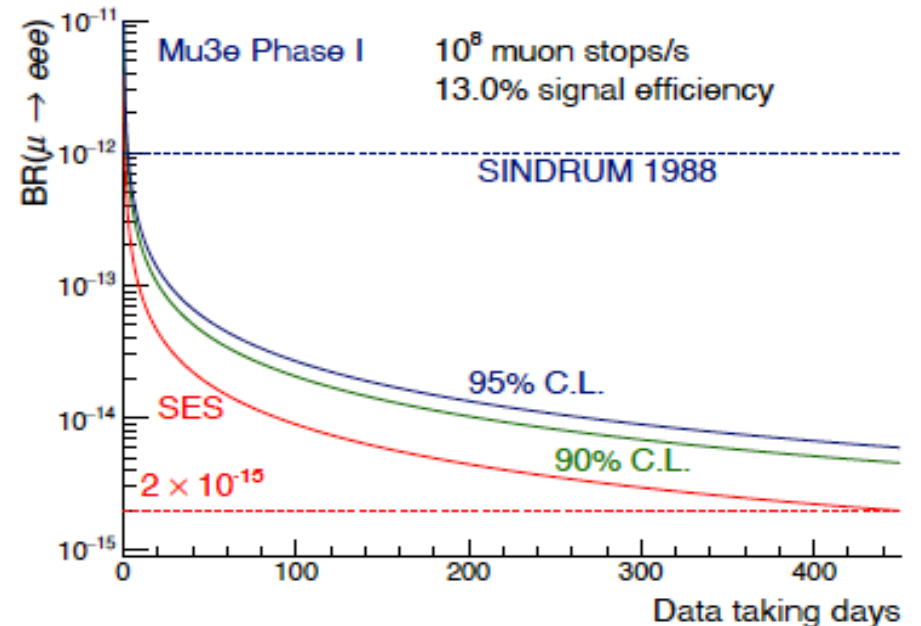
$\mu^+ \rightarrow e^+ e^+ e^-$: Mu3e Status



Status:

- Based at PSI, expect data-taking by 2025-26.
- Two Phased implementation:
 - **Phase-I** – Sensitivity 10^{-15} ;
 - **Phase-II** – Sensitivity 10^{-16} (requires beam upgrade).

See Talk by R. Amarinei



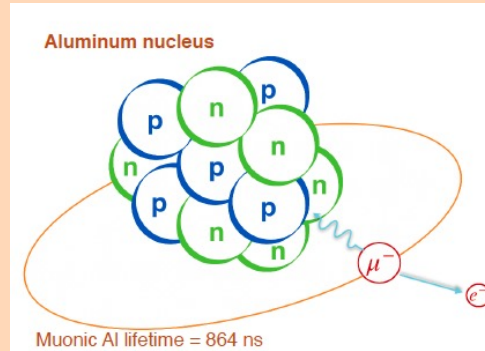
$N\mu^- \rightarrow Ne^-$: Physics

Signal:

- Monoenergetic electron (1st order)

$$E_e = m_\mu - E_{recoil} - E_{1SB.E}, \text{ e.g For Al: } E_e = 104.97 \text{ MeV}$$

- Coherent = nucleus stays intact.
- Will be smeared by scattering and energy losses



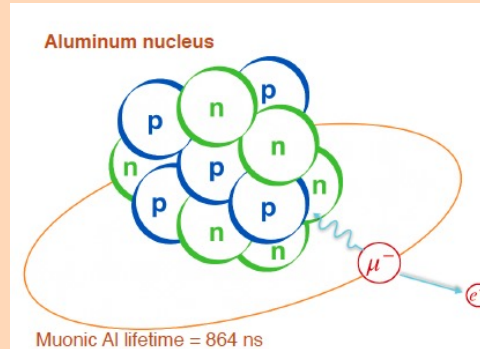
$N\mu^- \rightarrow Ne^-$: Physics

Signal:

- Monoenergetic electron (1st order)

$$E_e = m_\mu - E_{recoil} - E_{1SB.E}, \text{ e.g For Al: } E_e = 104.97 \text{ MeV}$$

- Coherent = nucleus stays intact.
- Will be smeared by scattering and energy losses



Backgrounds:

Decay in Orbit:

- 39 % of stopped muons decay :



Radiative Pion Capture:

- Pions captured into Al nucleus, undergo a radiative process (internal or external), results in: $\gamma \rightarrow e^+e^-$
- Electrons have energy up to \sim pion mass.

Cosmic Induced:

- Cosmic muons or secondary particles can be confused for signal is appear to emanate from target.

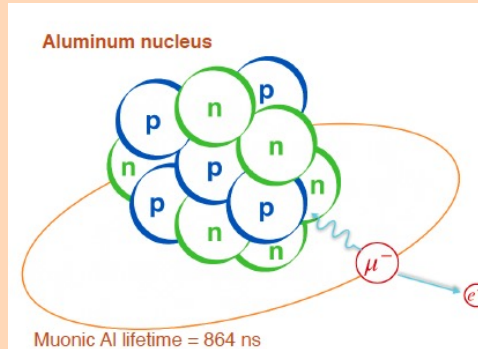
$N\mu^- \rightarrow Ne^-$: Physics

Signal:

- Monoenergetic electron (1st order)

$$E_e = m_\mu - E_{recoil} - E_{1SB.E}, \text{ e.g For Al: } E_e = 104.97 \text{ MeV}$$

- Coherent = nucleus stays intact.
- Will be smeared by scattering and energy losses



Strategy:

Stop 10^{18} muons with $\ll 1$ background in signal region:

- Intense muon beam;
- Efficient transportation and collection of muons;
- Pulsed beam to eliminate pions;
- Precise momentum resolution to remove decay backgrounds.

Backgrounds:

Decay in Orbit:

- 39 % of stopped muons decay :



Radiative Pion Capture:

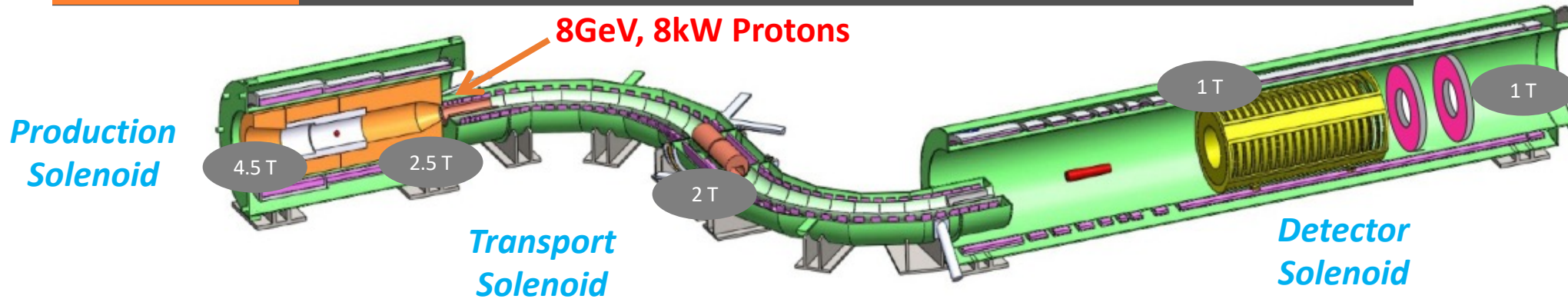
- Pions captured into Al nucleus, undergo a radiative process (internal or external), results in: $\gamma \rightarrow e^+e^-$
- Electrons have energy up to \sim pion mass.

Cosmic Induced:

- Cosmic muons or secondary particles can be confused for signal is appear to emanate from target.

$N\mu^- \rightarrow Ne^-$: Mu2e Design

*Intense muon beam;
Efficient transportation and collection;*



Production Solenoid:

- Pulsed 8 GeV Protons enter, hit Production Target. π produced, decay to μ .
- Graded magnetic field reflects muons to transport solenoid.

Transport Solenoid:

- "S" shape removes line of sight backgrounds.
- Collimators select low momentum, negative muons.

Detector Solenoid:

- Thin aluminum foil target captures the muons.
- Possible signal electrons are detected by a tracker and a calorimeter.
- Cosmic ray veto covers the whole detector solenoid and half the transport solenoid.

See Talk by A. Gapanenko

$N\mu^- \rightarrow Ne^-$: Mu2e Projections

2027 Run-I:

- 1×10^{-15} 5σ discovery,
- Single-Event-Sensitivity = 2×10^{-16}
- U.L : 6×10^{-16} (90% C.L.)
 - **1000 x current limit.**
 - **Universe 2023, 9, 54** shows simulated analysis for Run-I.

Total (Run-I + Run-II) end-goal:

- 2×10^{-16} 5σ discovery,
- Single-Event-Sensitivity = 3×10^{-17}
- U.L : 8×10^{-17} (90% C.L.)
 - **10000 x current limit.**

Need to stop $O(10^{18})$ muons and have $\ll 1$ background event over entire lifetime of the experiment to achieve these numbers!

$N\mu^- \rightarrow Ne^-$: (Mu2e) Backgrounds

Beam delivery and detector systems optimized for high intensity, pure muon beam – must be “background free”:

Type	Source	Mitigation	Yield (for Run-I only)*
Intrinsic	Decay in Orbit (DIO)	Tracker Design/Resolution	0.038 ± 0.002 (stat) $^{+0.025}_{-0.015}$ (sys)
Beam Backgrounds	Pion Capture	Beam Structure/Extinction	(in time) 0.010 ± 0.002 (stat) $^{+0.001}_{-0.003}$ (sys) (out time) (1.2 ± 0.001 (stat) $^{+0.1}_{-0.3}$ (sys)) $\times 10^{-3}$
Cosmic Induced	Cosmic Rays	Active Veto System	0.046 ± 0.010 (stat) ± 0.009 (sys)

* assumes signal region of $103.6 < p < 104.9$ MeV/c and $640 < t < 1650$ ns

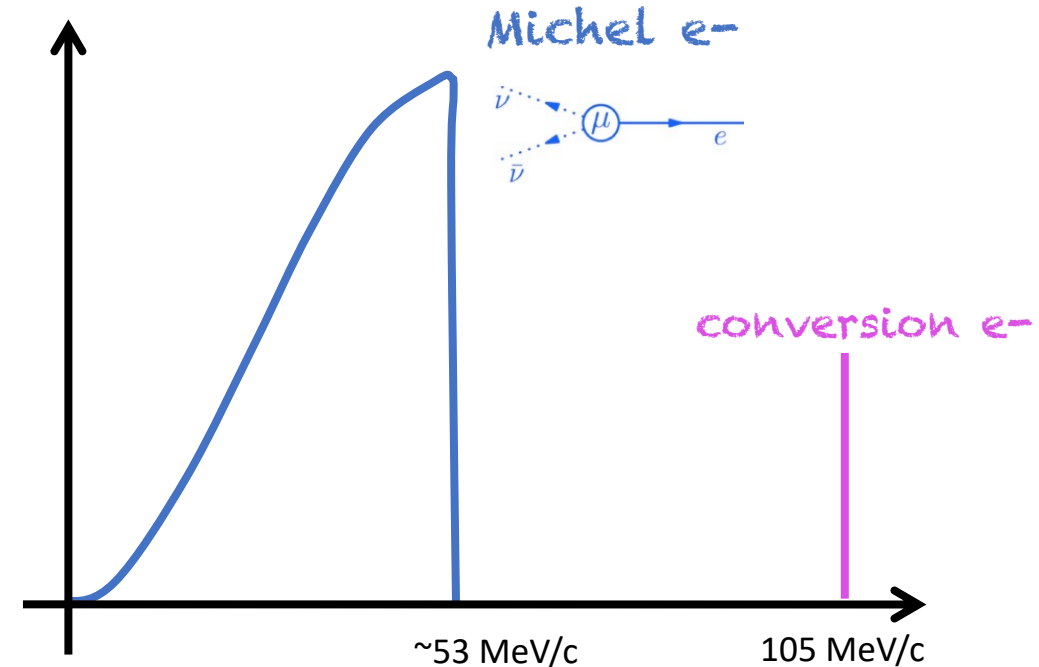
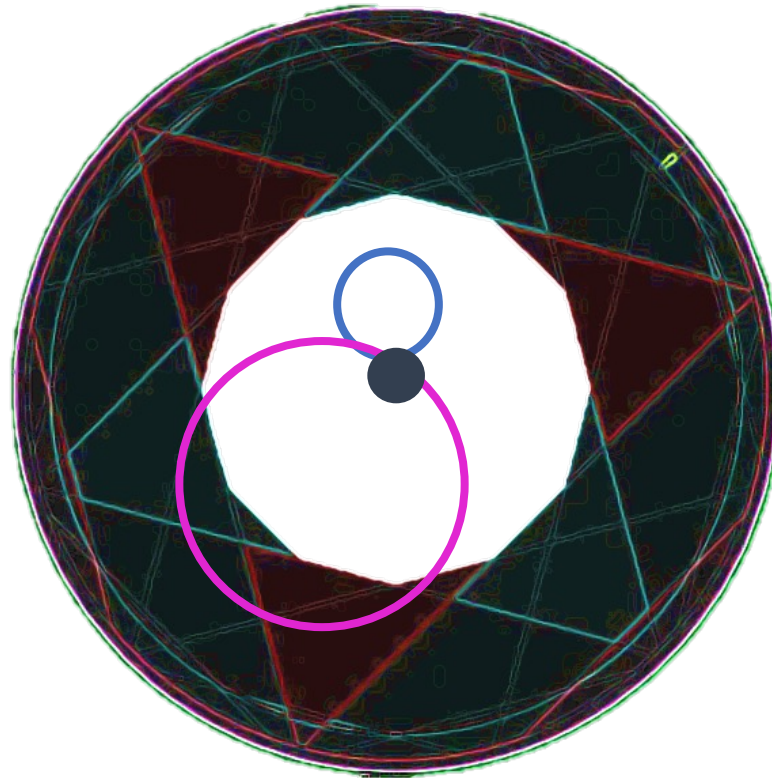
Run-I Sensitivity of Mu2e:
Universe 2023, 9, 54.

(Mu2e) Decay in Orbit (DIO) Backgrounds

- Annular tracker: Removes most of DIO (all Michel peak electrons), analyze 10^5 instead of 10^{18} muons.

$$R = \frac{p_{\perp}}{qB} = 35\text{cm}$$

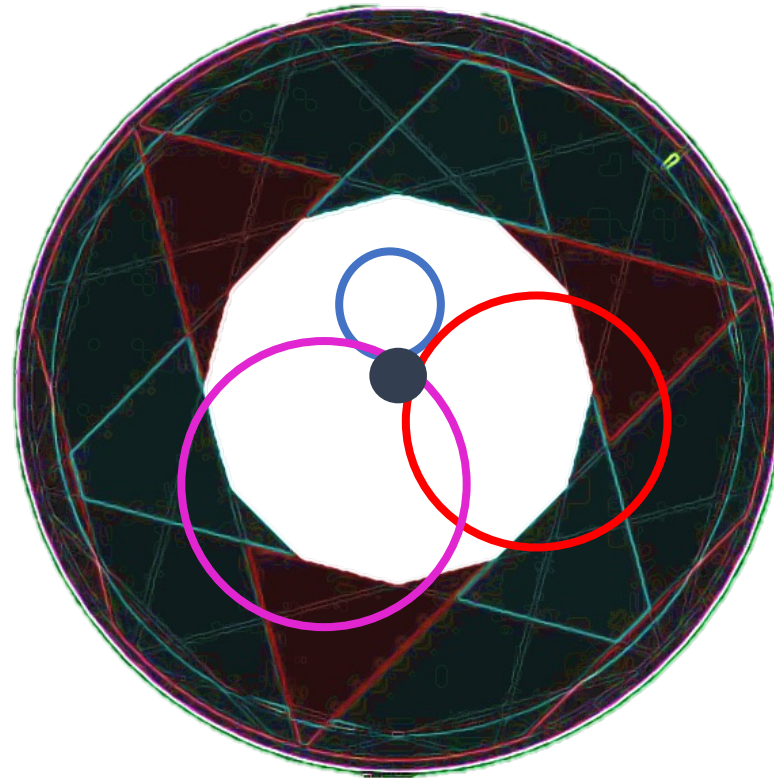
- Michel Electron ($< 52\text{MeV}/c$)
- Signal ($105\text{MeV}/c$)



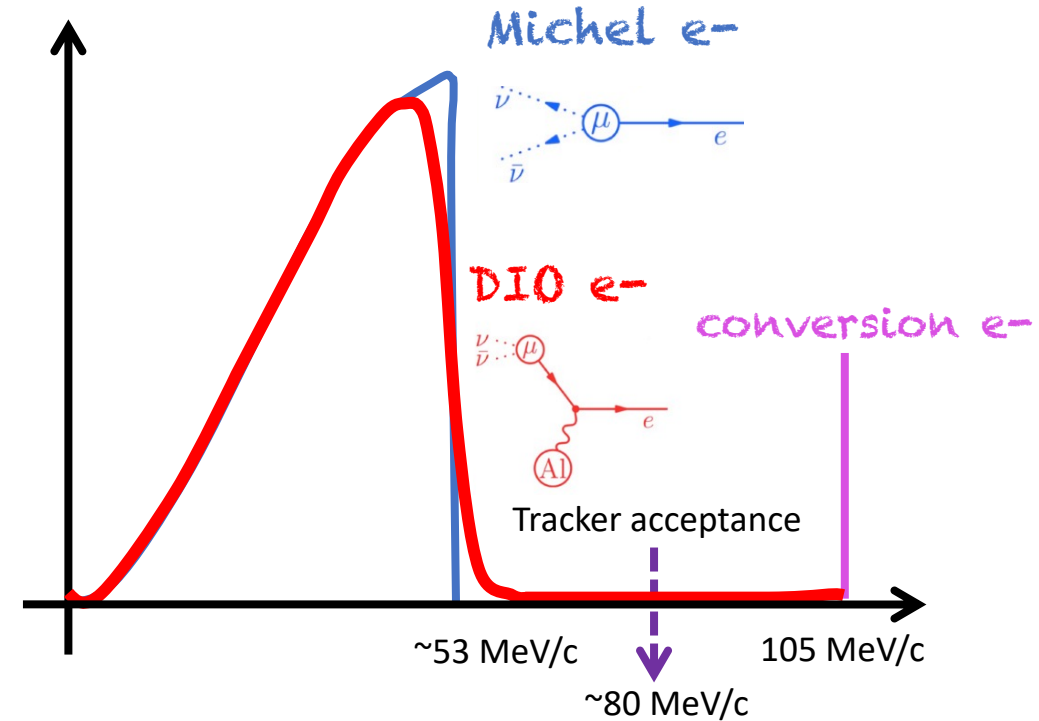
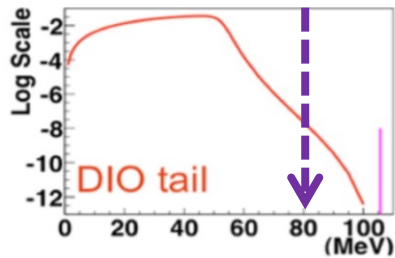
(Mu2e) Decay in Orbit (DIO) Backgrounds

- Annular tracker: Removes most of DIO (all Michel peak electrons), analyze 10^5 instead of 10^{18} muons.
- However, when decay happens in orbit, exchange of momentum produces recoil tail close to signal region (105 MeV/c).
- To remove remaining backgrounds necessitates < 200 keV/c momentum resolution.

$$R = \frac{p_{\perp}}{qB} = 35\text{cm}$$



- Michel Electron ($< 52\text{MeV}/c$)
- Signal ($105\text{MeV}/c$)
- Problematic Tail ($>100\text{MeV}/c$)



(Mu2e) Straw Tracker: achieving resolution

- Need a high-resolution (< 200 keV/c) momentum measurement to distinguish tail DIO from signal:
 - Minimize energy loss by operating in vacuum and using low mass straws of $15 \mu\text{m}$ thickness filled with 80:20 Ar:CO₂ ;
 - Include extra hit position information with high-angle stereo overlaps and readout on both ends of straw.



96 Straws



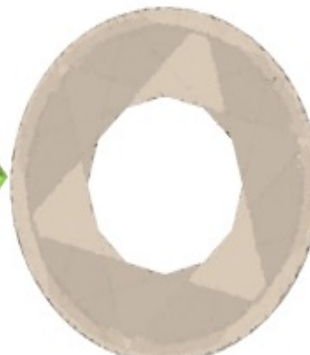
6 Panels



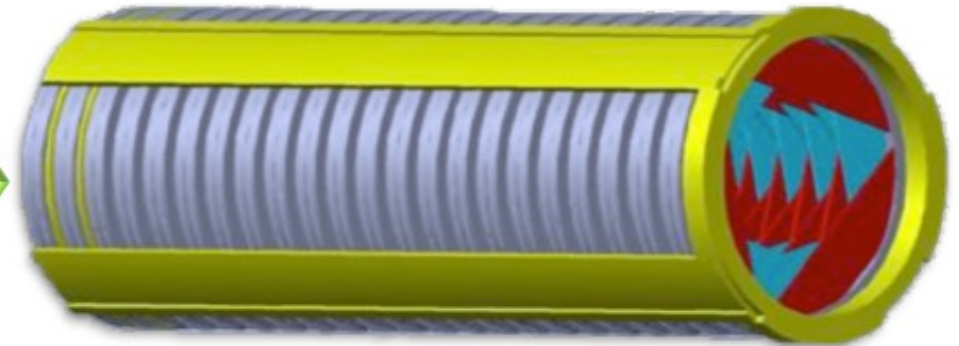
2 Plane



1 Station



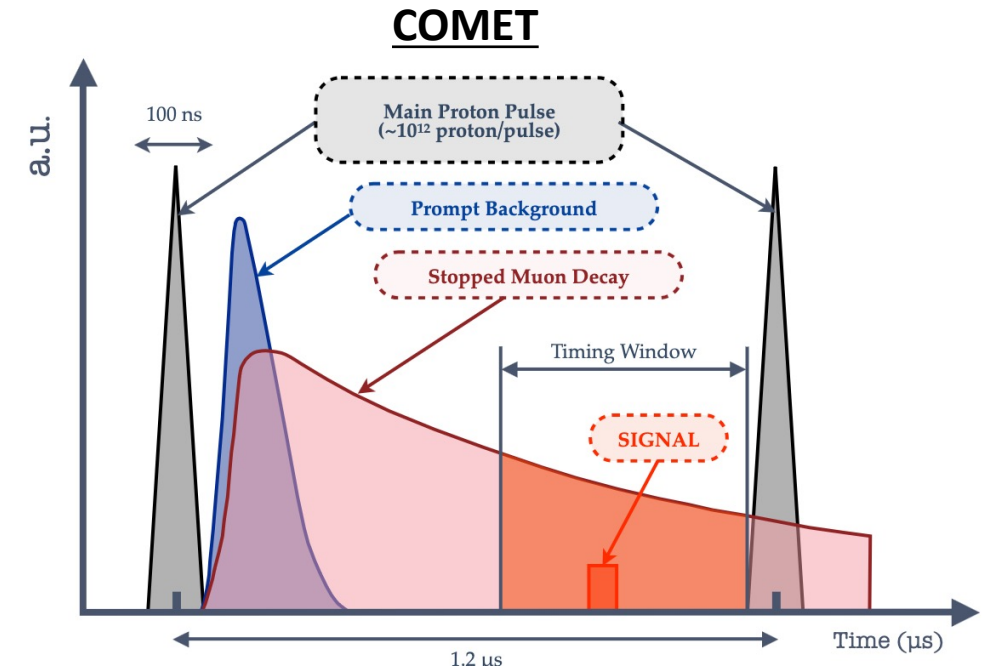
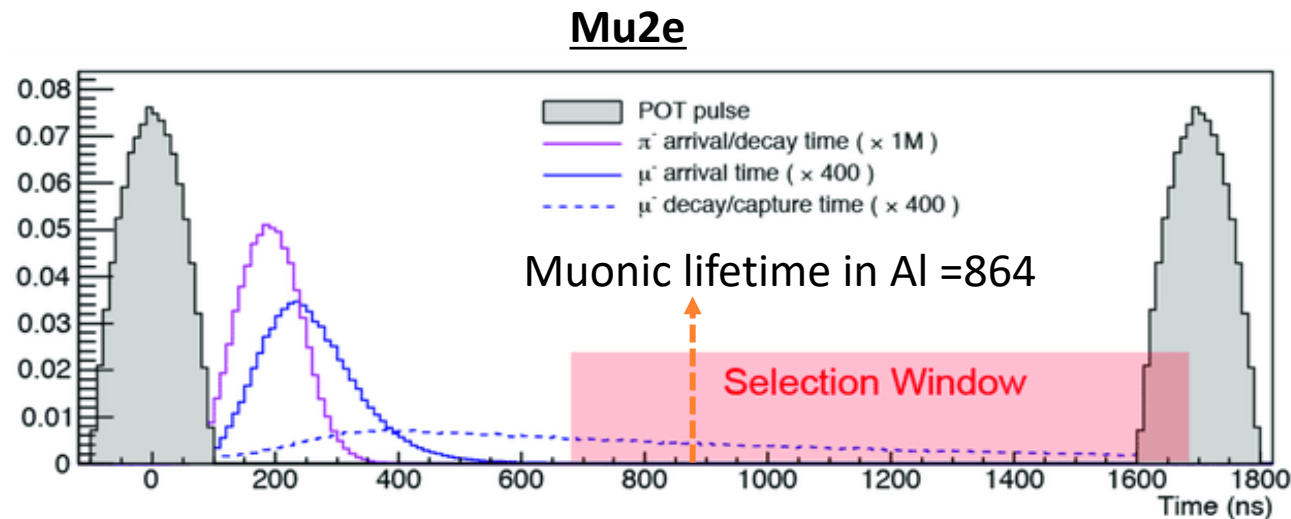
18 Station = 1 Tracker



Radiative Pion Capture Backgrounds

- Use timing information!
- Pion lifetime 26 ns at rest. Pulsed proton beam (250 ns wide, pulses 1695 ns apart) → wait out pion decay.
- In addition, upstream extinction removes out-of-time protons.

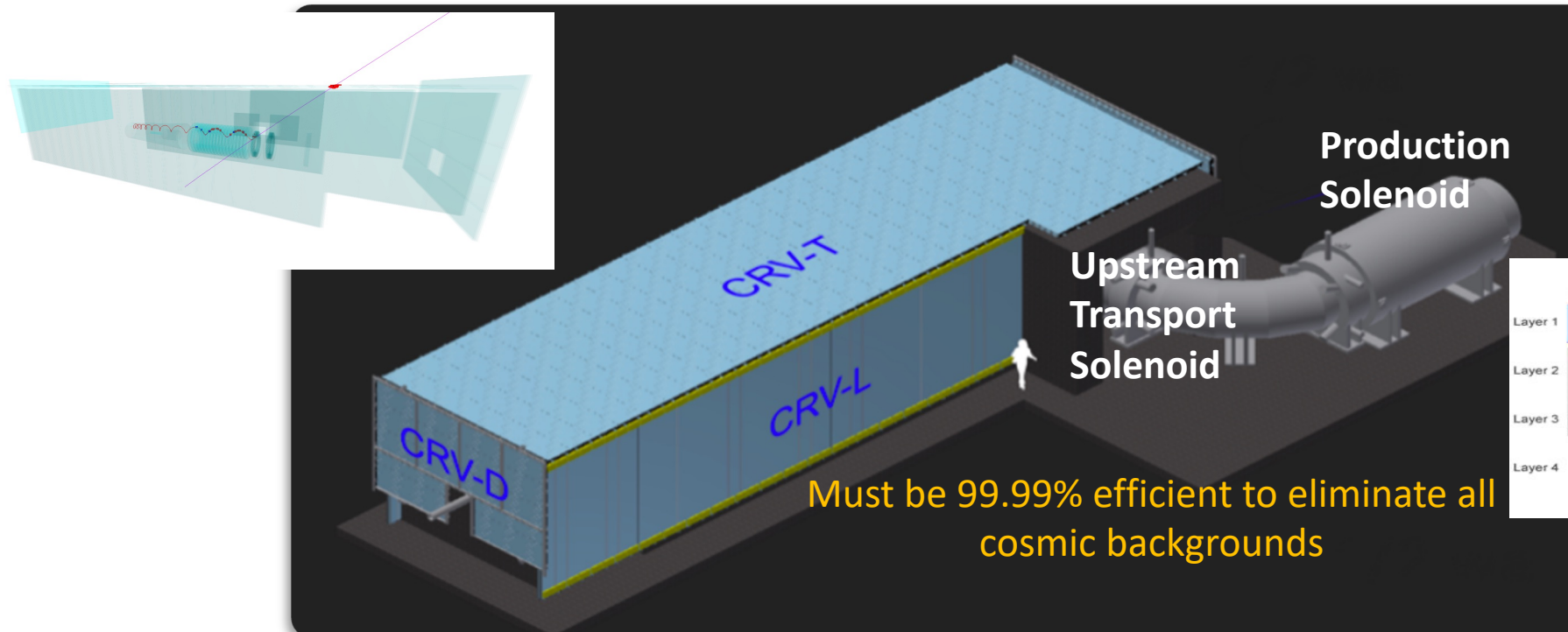
Delayed live-gate helps remove pion and beam backgrounds.



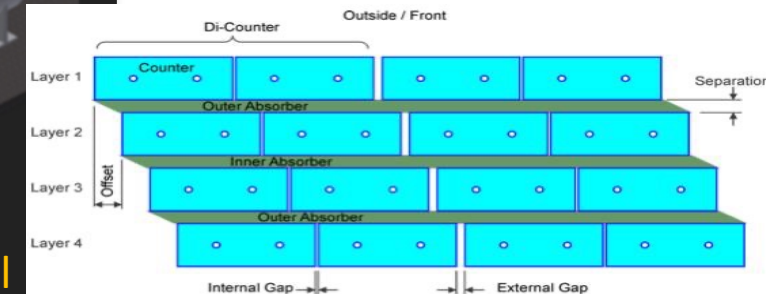
Cosmic Induced Backgrounds

- Cosmic-ray muons can initiate 105 MeV particles that appear to emanate from the stopping target.
- Remove using active veto (CRV) + overburden and shielding concrete surrounding the Detector Solenoid.

Active Cosmic Ray Veto system is key to eliminating cosmic induced backgrounds.



Mu2e (COMET has similar)



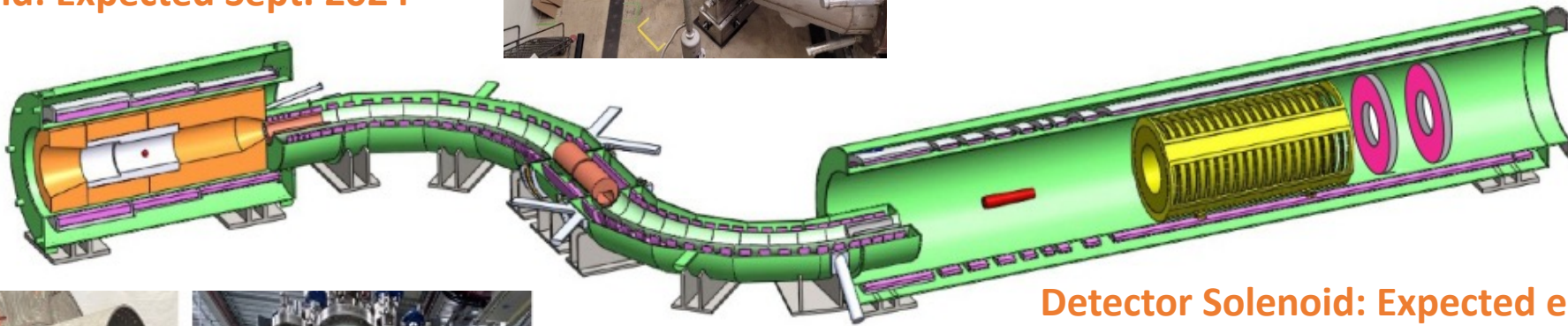
$N\mu^- \rightarrow Ne^-$: Mu2e Status (solenoids)

See Talk by A. Gapanenko



Transport Solenoid: Installed in Mu2e Hall in 2024

Production Solenoid: Expected Sept. 2024



Detector Solenoid: Expected early 2025



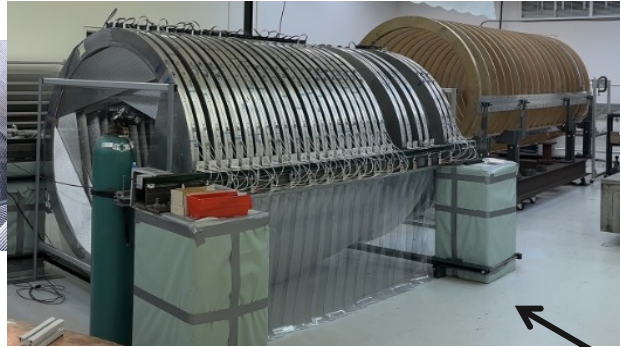
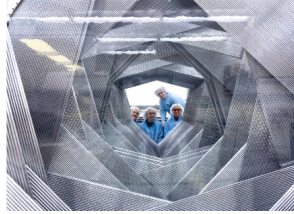
$N\mu^- \rightarrow Ne^-$: Mu2e Status

See Talk by A. Gapanenko

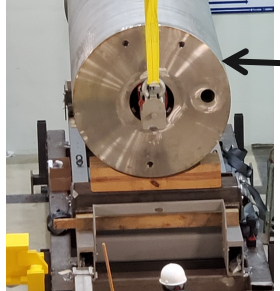
Heat Shield @ FNAL



Tracker being assembled @ FNAL



CRV: modules fabricated, testing with cosmics @ FNAL

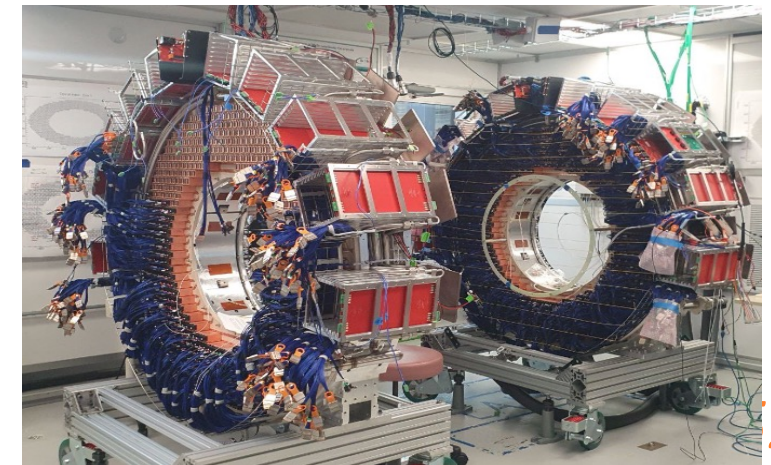
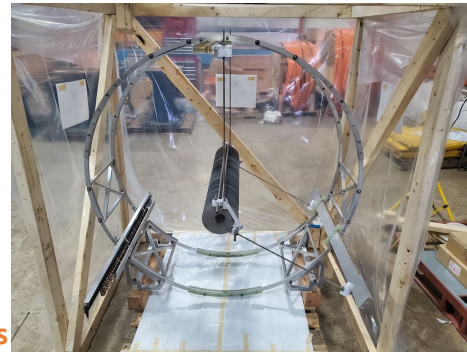


Calorimeter assembled @ FNAL

Stopping Target constructed, now at FNAL



Production Target @ FNAL



Muons as Probes of New Physics

Muon $g-2$

Muon CLFV Searches: Motivations

Muon CLFV Searches: Design, Status

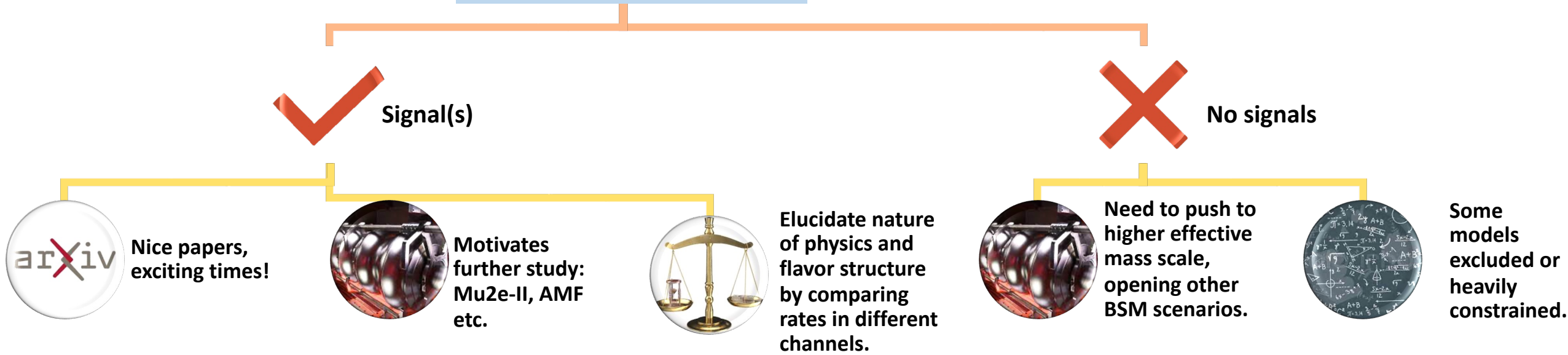
What happens next?

What happens next?

How do we understand a signal?

Possibilities

Outcomes of current era of CLFV searches



What's next??? – In either scenario additional searches are motivated. This motivates: Mu2e-II, AMF or PRISM/PRIME.

Next Generation Searches

Proposed multi-decade muon CLFV at Fermilab which would utilize PIP-II and ACE 2GeV ring:

Mu2e-II [see: [arXiv: 2203.07569 \[hep-ex\]](#)] (mid-2030s):

- **Similar design to Mu2e, reuses much of the hardware but requires new production target and detector systems.**
- Uses pulsed beam as necessary to remove pion backgrounds.
- Lots of R&D on-going including 2 LDRD proposals: tracker and production target.

PRISM/PRIME:

- PRISM uses an FFA to provide monoenergetic muon beam. PRIME is a conversion search.

The Advanced Muon Facility (AMF) [see: [arXiv: 2203.08278 \[hep-ex\]](#)] (mid 2040s):

- **A multi purpose muon facility which would search for all three muon CLFV channels at Fermilab.**
- Would utilize a fixed field alternating (FFA) gradient synchrotron which would provide:
 - **Monoenergetic beam of central momentum 20-40 MeV/c:** thin target, minimizing material effects, retaining momentum resolution.
 - **Pure muon beam:** don't need the pulsed beam and delayed signal window.
 - Can utilize a high Z material to elucidate physics if signal at Mu2e/COMET or Mu2e-II. *See talk by L. Borrel*
 - Has smaller decay branching fraction. *See my talk on AMF*
- R&D required and lots of opportunities to get involved.

Summary

Muon $g-2$:

- Discrepancy with SM theory predictions, experiments are making more precise determination, and theorists and experimentalists are working to resolve the theoretical discrepancies between measurement and each other.

Muon CLFV:

- Muon CLFV channels offer deep indirect probes into BSM and part of an active global CLFV program.
- These experiments have discovery potential over a wide range of well motivated BSM models.
- Three muon CLFV channels form part of a global search for CLFV which will take place this decade.
- Looking further ahead Mu2e-II, PRISM/PRIME and AMF would help elucidate any signal and push to higher mass scales (if no signal).

Thank you for listening!

Any Questions?

Back up

Extra things which did not fit

Muons as Probes of New Physics

Muon $g-2$

Muon CLFV Searches: Motivations

Muon CLFV Searches: Design, Status

What happens next?

Measurement Quantity Anatomy (g-2 FNAL)

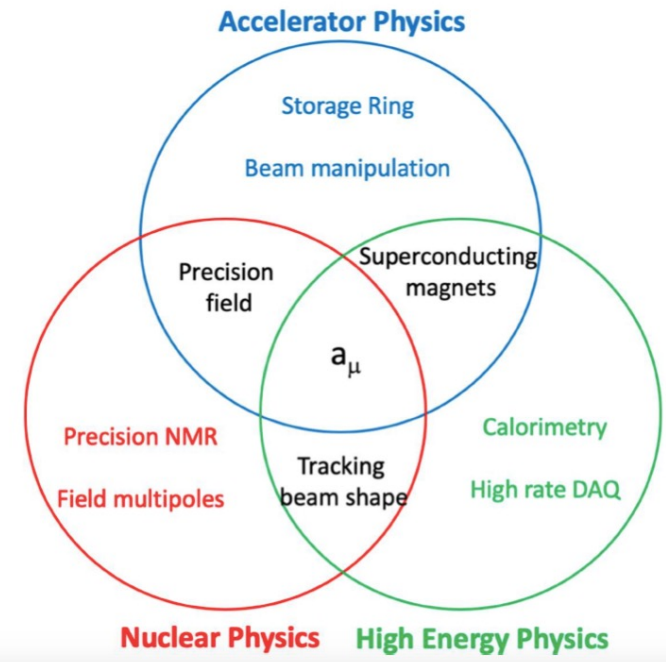
$$\omega_a = a_\mu \frac{qB}{m} \Rightarrow a_\mu = \frac{\omega_a}{\tilde{\omega}'_p(T_r)} \underbrace{\frac{\mu'_p(T_r)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}}_{\text{Known to 24 ppb}}$$

What we measure.

Category	TDR Target Uncertainty [ppb]
Statistical (ω_a)	100
Systematic (ω_a)	70
Systematic ($\tilde{\omega}'_p$)	70
Total	140

$$\mathcal{R}'_\mu = \frac{\omega_a}{\tilde{\omega}'_p(T_r)} = \frac{f_{\text{clock}} \omega_a^m (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \langle \omega_p(x, y, \phi) \times M(x, y, \phi) \rangle (1 + B_k + B_q)}$$

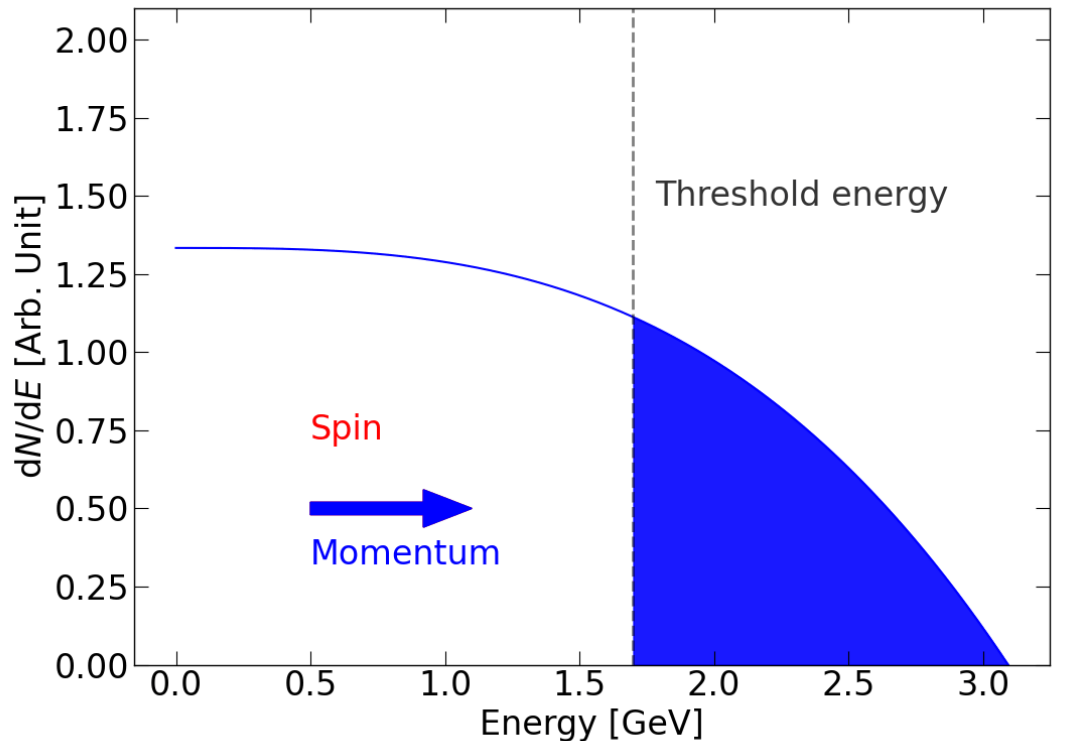
Unblinding conversion factor (points to f_{clock})
 Omega-a Team Measured $g - 2$ frequency (points to ω_a^m)
 Beam Dynamics Team Beam dynamics corrections (points to $1 + C_e + C_p + C_{ml} + C_{pa}$)
 Field Team NMR probe calibration factor (points to f_{calib})
 Magnetic field weighted over the muon distribution (points to $\langle \omega_p(x, y, \phi) \times M(x, y, \phi) \rangle$)
 Corrections from the transient magnetic field (points to $1 + B_k + B_q$)



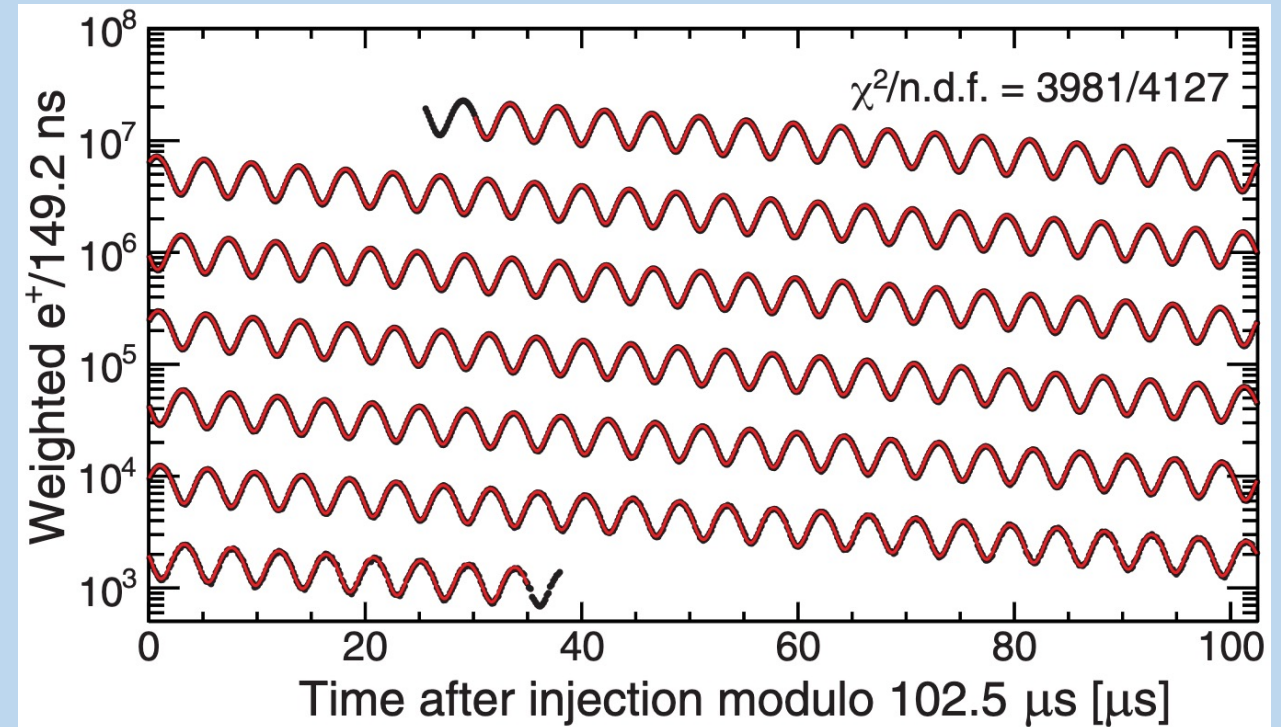
Muon g-2 Experiment at FNAL



μ^+



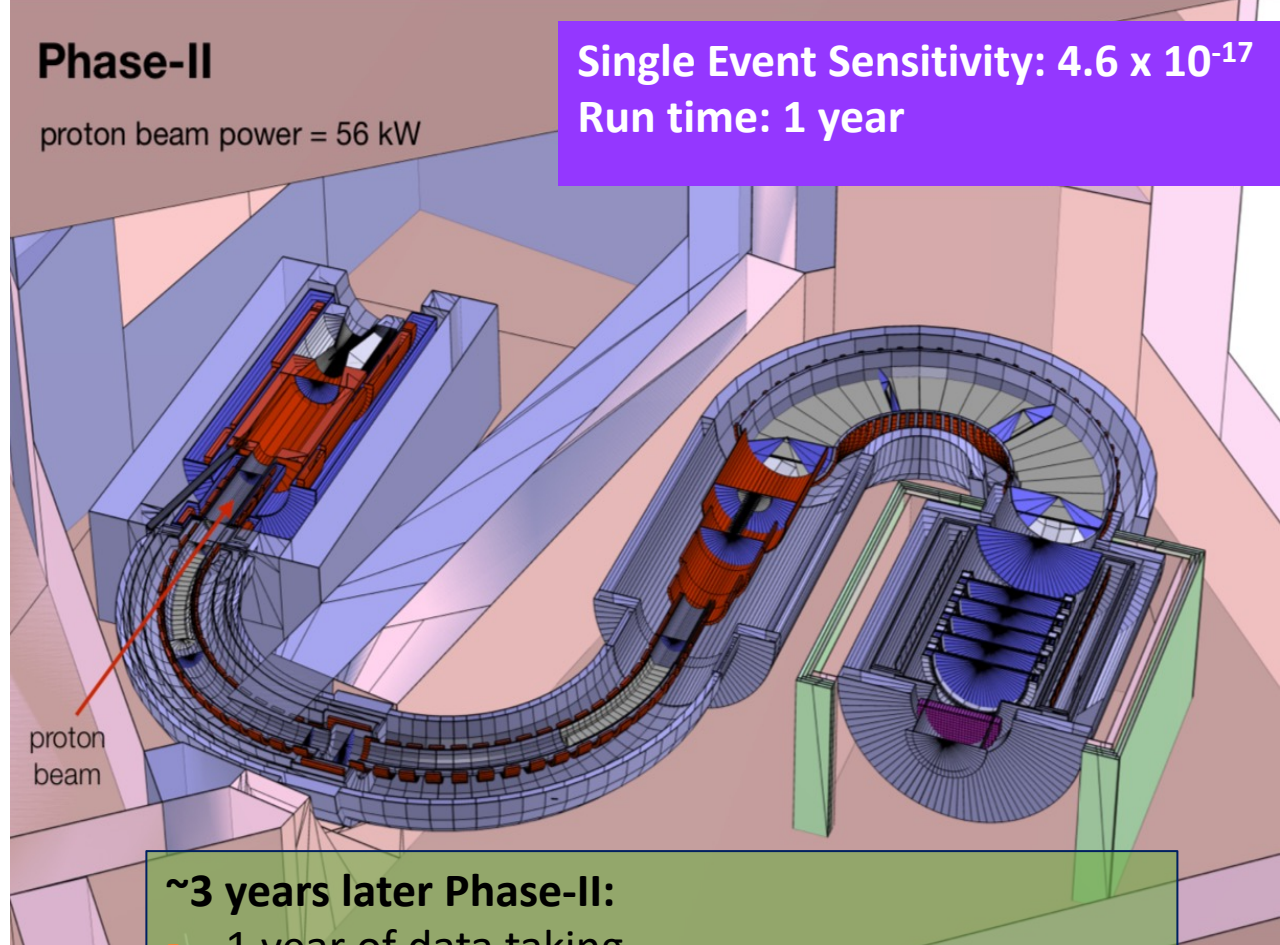
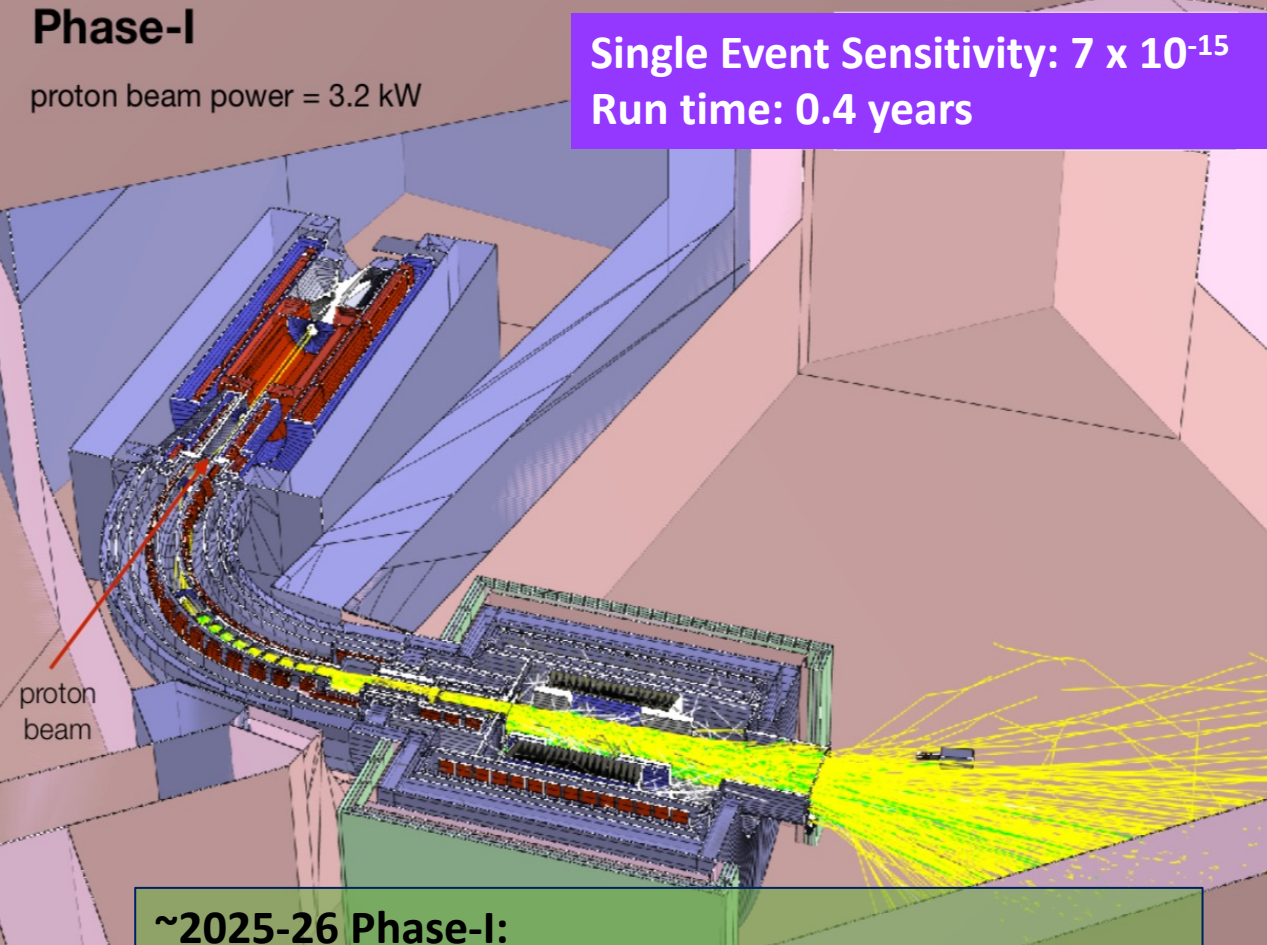
- Resulting "Wiggle plot"



- Fit the wiggle plot to extract ω_a (simplified function).

$$N(t) = N_0 e^{-t/\tau} [1 + A \cos(\omega_a t - \phi)]$$

$N\mu^- \rightarrow Ne^-$: COMET Design



~2025-26 Phase-I:

- 3 months of data provides sensitivity of 7×10^{-15}

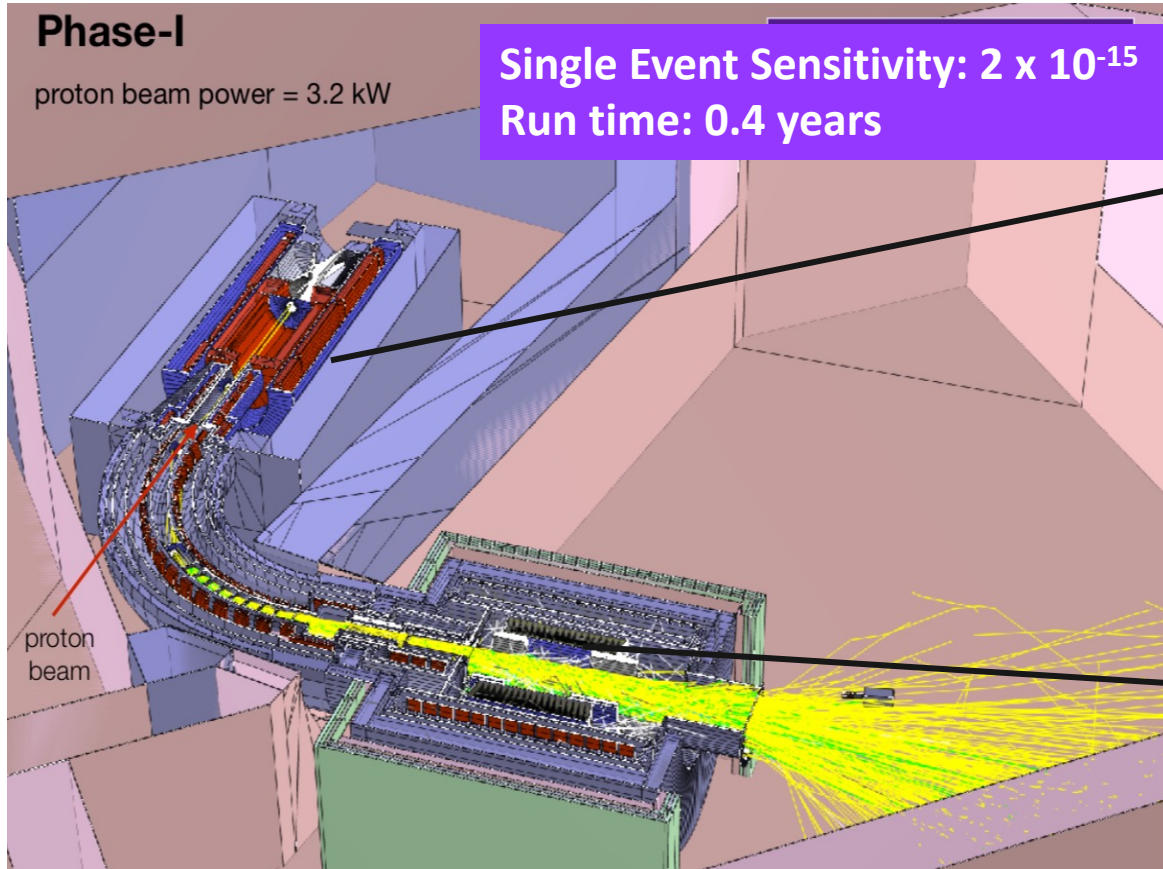
~3 years later Phase-II:

- 1 year of data taking
- Single-Event-Sensitivity = 4.6×10^{-17}

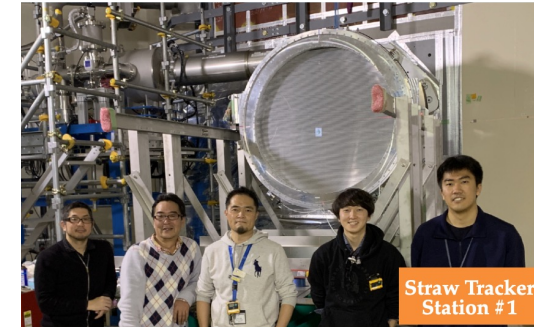
$N\mu^- \rightarrow Ne^-$: COMET Status



Pion Capture Solenoid complete, delivered to JPARC soon



StrECAL (for beam measurement) – to be completed in 2025



Straw Tracker Station #1

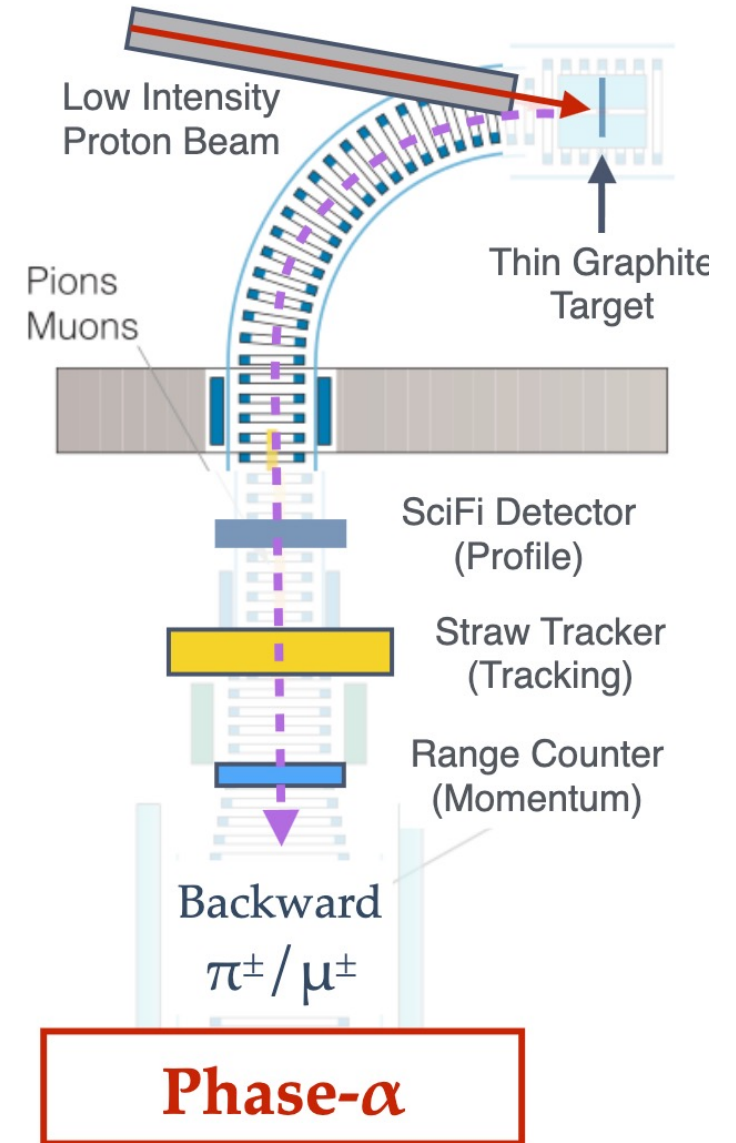
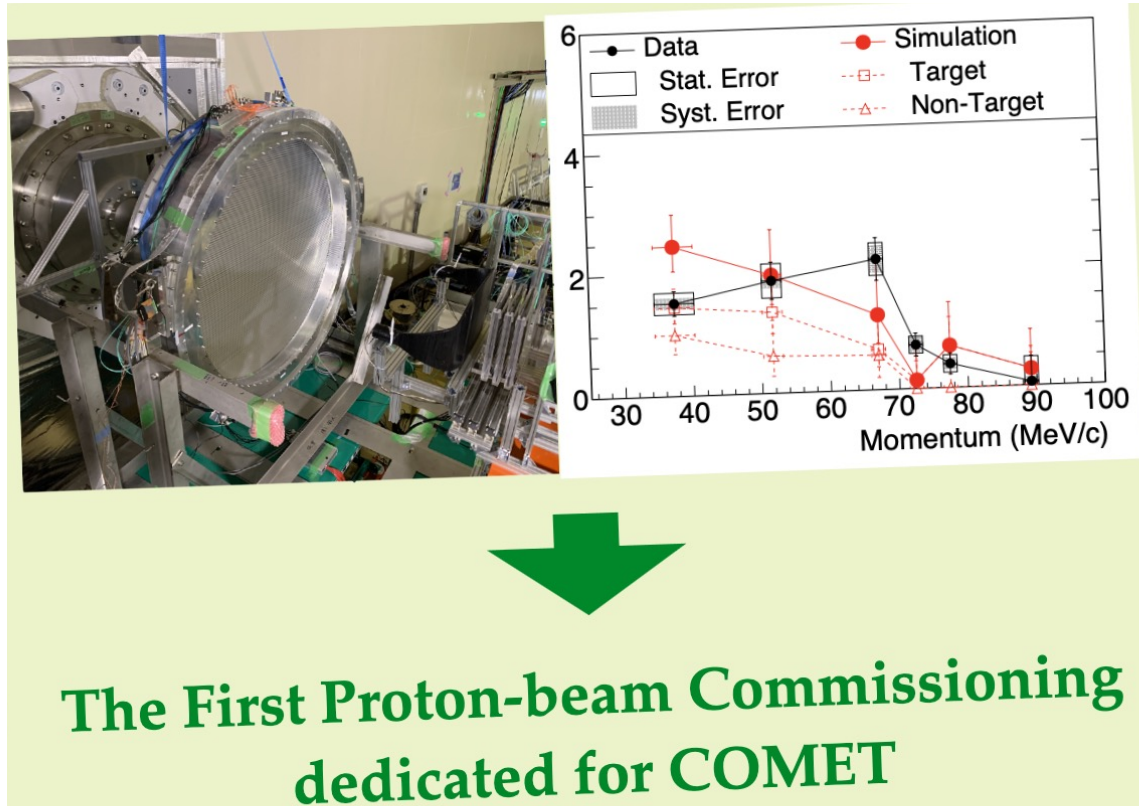
CyDet completed, commissioning with cosmics underway.



Completed CDC

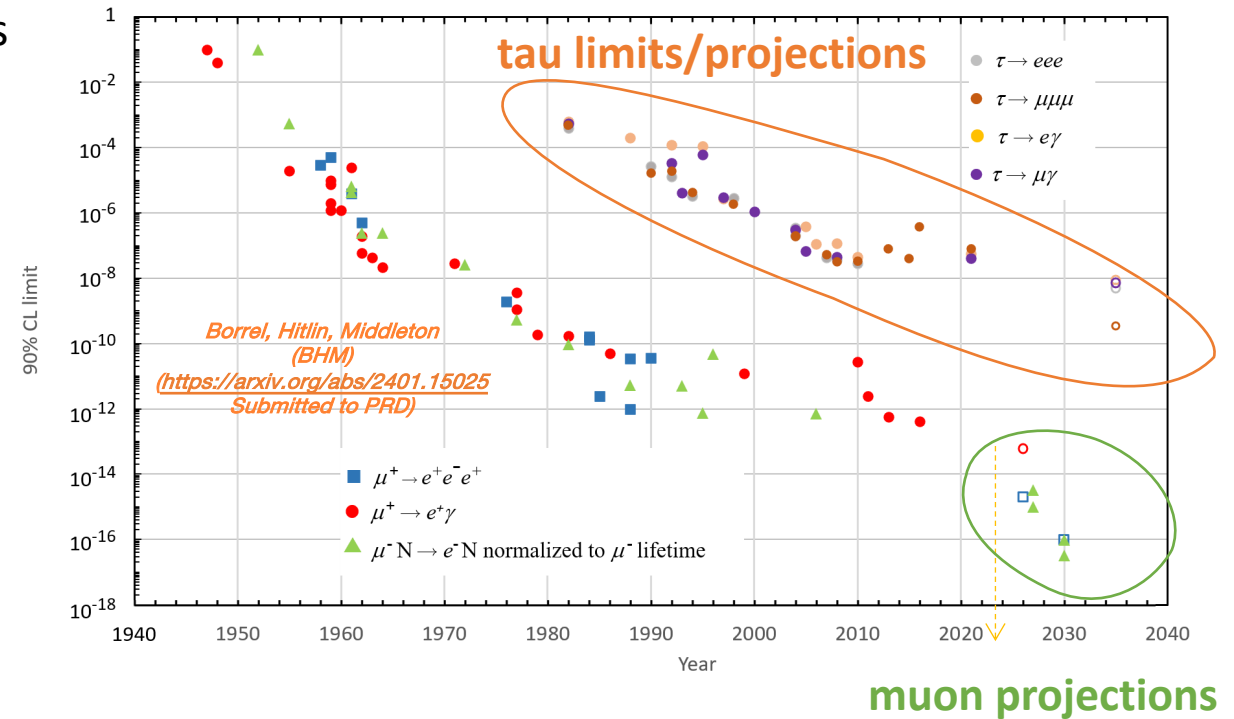
$N\mu^- \rightarrow Ne^-$: COMET Phase α

- Dedicated primary proton beam-line completed in 2022
- Low intensity proton (Phase-I x0.1) was delivered and commissioned in 2023 with muon transport solenoid but no pion capture solenoid.



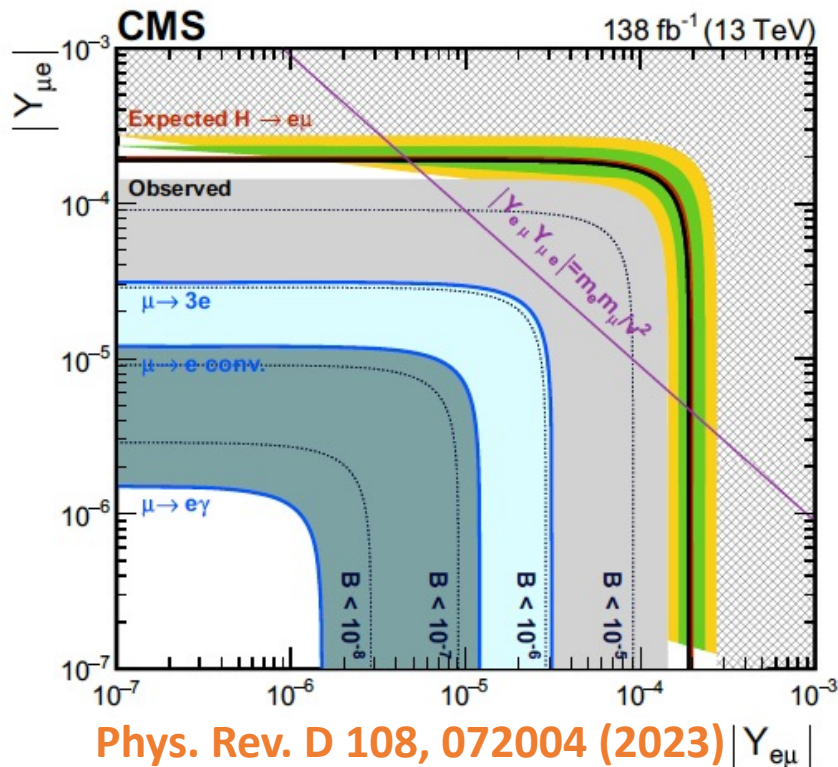
Complementarity with collider searches for CLFV

- Less stringent limits in 3rd generation, but here BSM effects may be higher.
- τ LFV searches at Belle II will be extremely clean, with very little background (if any), thanks to pair production and double-tag analysis technique.
- **To determine type of mediator:**
 - Compare muon channels to each other.
- **To determine the source of flavor violation:**
 - Compare muon rates to tau rates.



Complementarity with collider searches for LFV

$$\Gamma(H \rightarrow e\mu) = \frac{m_H}{8\pi} (|Y_{e\mu}|^2 + |Y_{\mu e}|^2).$$



- Higgs LFV decays arise in many frameworks of New Physics at the electroweak scale such as **two Higgs doublet models, extra dimensions, or models of compositeness.**
- The $\mu \rightarrow e\gamma$ and $\mu \rightarrow 3e$ channels provide constraints but conversion searches such as Mu2e provide tightest projected constraints
- Current $\mu \rightarrow e$ conversion implies:

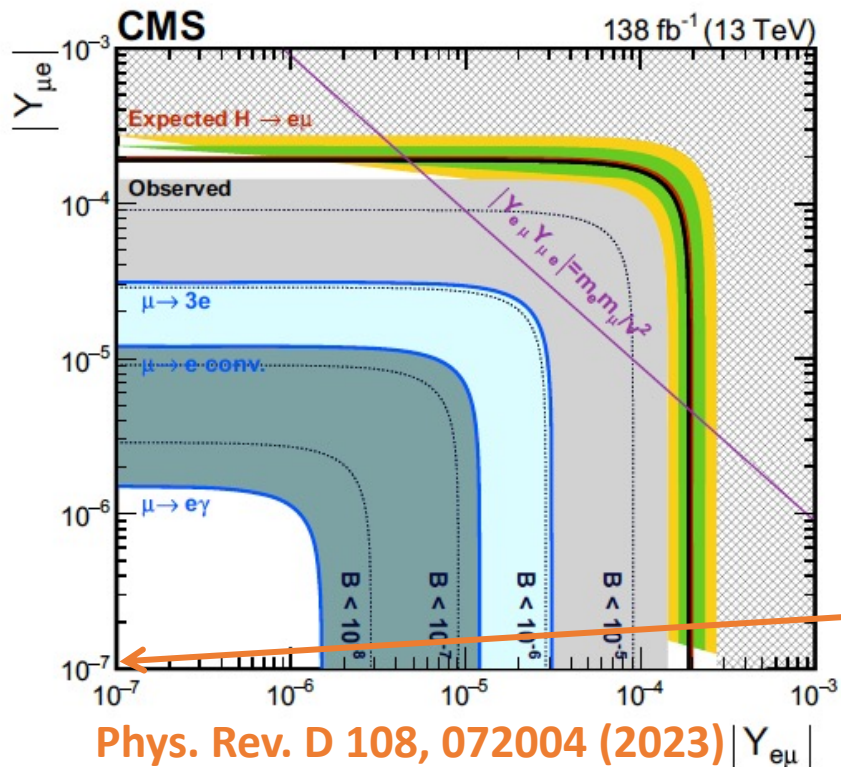
$$\sqrt{|Y_{\mu e}|^2 + |Y_{e\mu}|^2} < 4.6 \times 10^{-5}$$

- Mu2e is expected to be sensitive to:

$$\sqrt{|Y_{\mu e}|^2 + |Y_{e\mu}|^2} \sim \mathcal{O}(10^{-7})$$

where $|Y_{\mu e}|$ and $|Y_{e\mu}|$ are off-diagonal flavor-violating Yukawa couplings for a 125 GeV Higgs boson i.e. $H \rightarrow \mu e$.

Complementarity with collider searches for LFV



- Higgs LFV decays arise in many frameworks of New Physics at the electroweak scale such as **two Higgs doublet models, extra dimensions, or models of compositeness.**
- The $\mu \rightarrow e\gamma$ and $\mu \rightarrow 3e$ channels provide constraints but conversion searches such as Mu2e provide tightest projected constraints
- Current $\mu \rightarrow e$ conversion implies:

$$\sqrt{|Y_{\mu e}|^2 + |Y_{e\mu}|^2} < 4.6 \times 10^{-5}$$

- Mu2e is expected to be sensitive to:

$$\sqrt{|Y_{\mu e}|^2 + |Y_{e\mu}|^2} \sim \mathcal{O}(10^{-7})$$

where $|Y_{\mu e}|$ and $|Y_{e\mu}|$ are flavor-violating Yukawa couplings for a 125 GeV Higgs boson i.e. $h \rightarrow \mu e$.