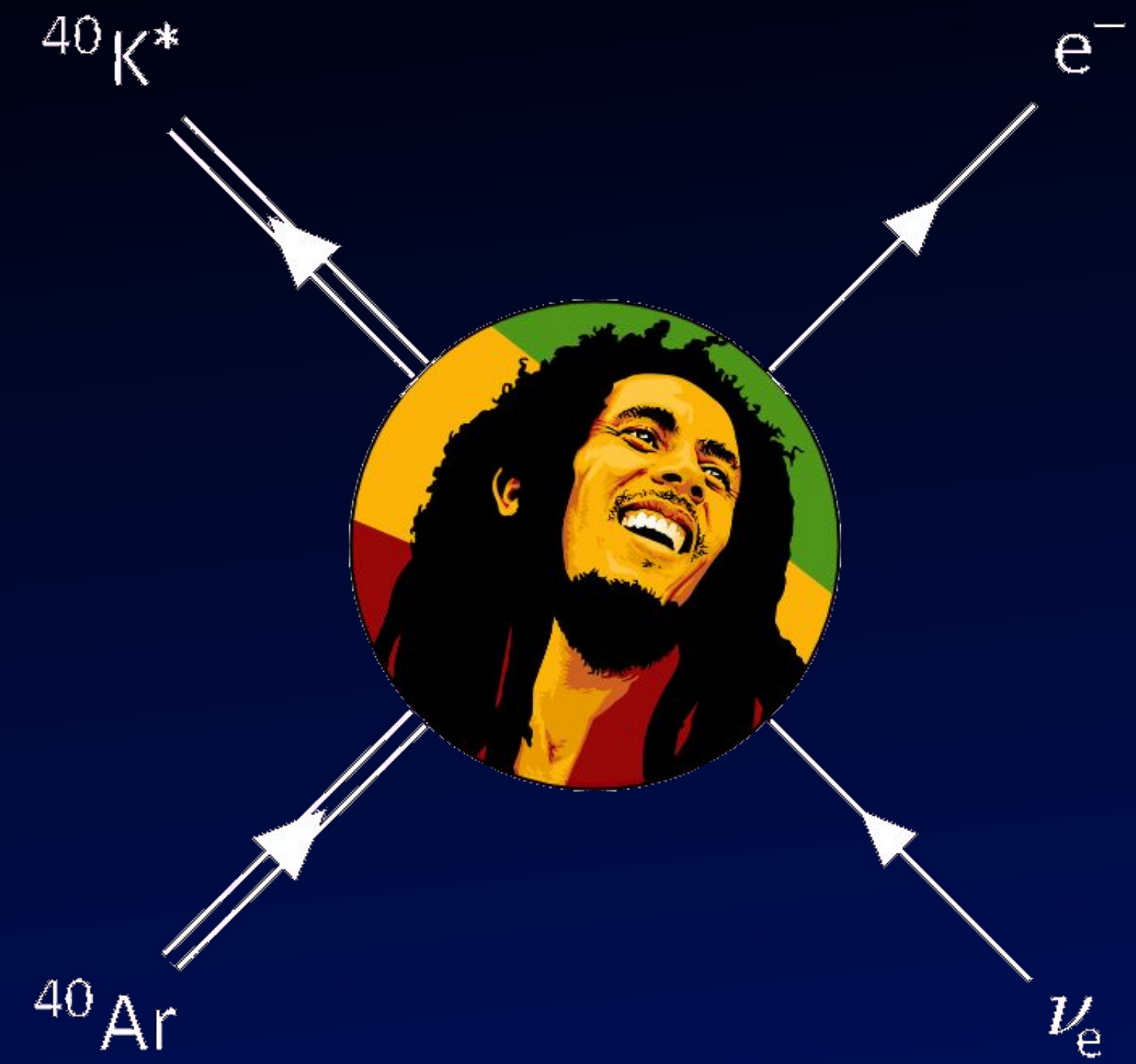


**Fermilab**



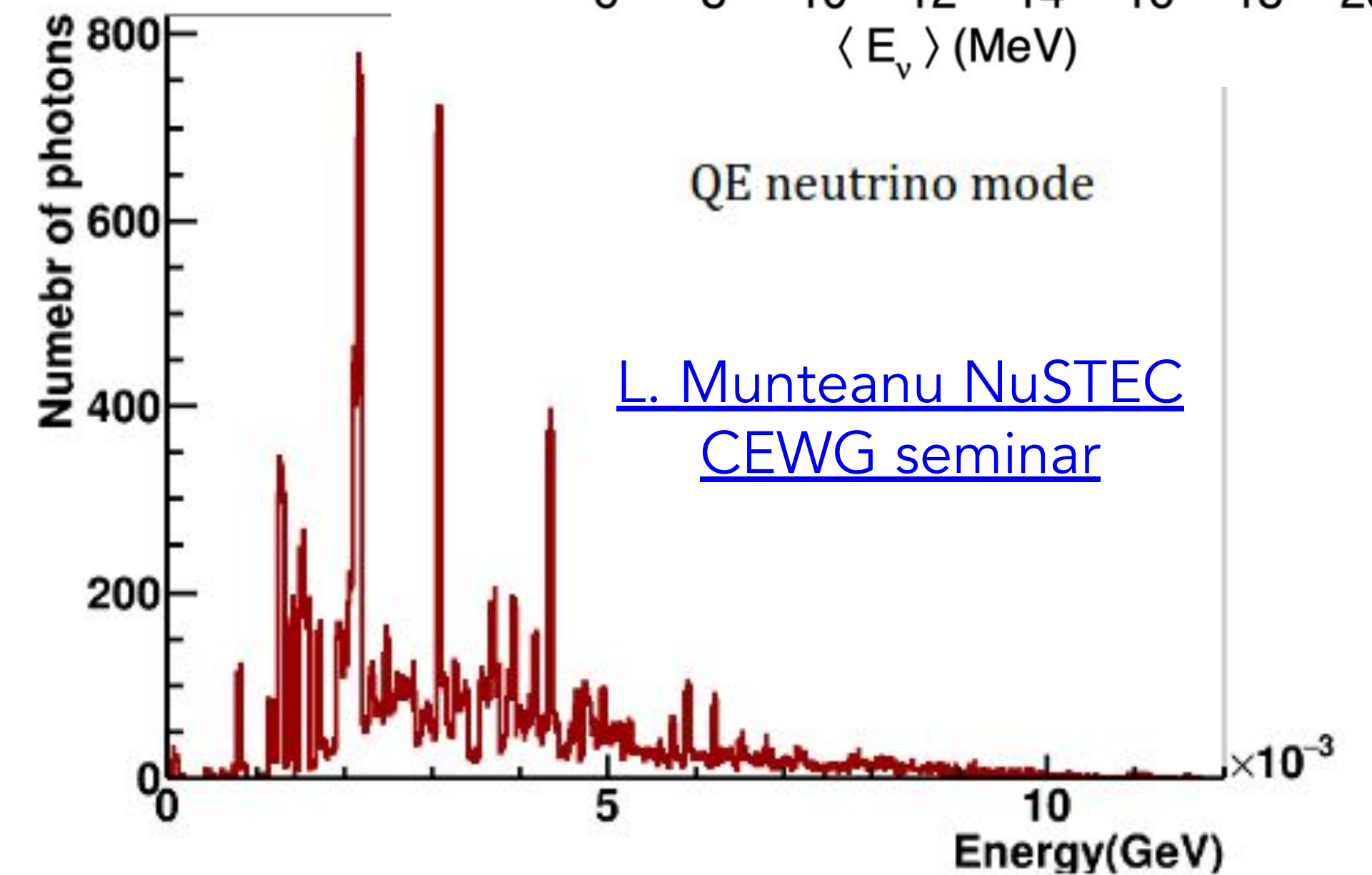
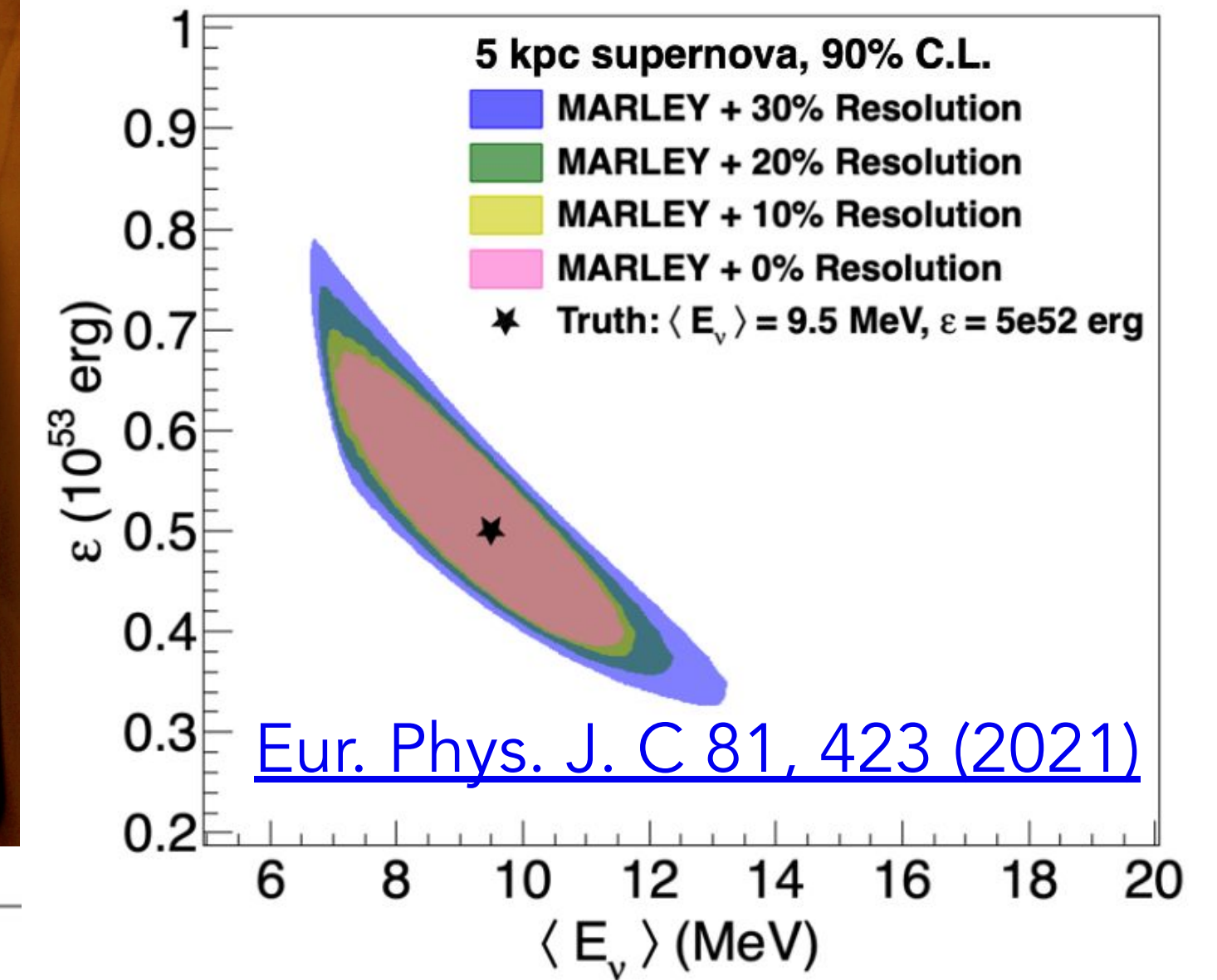
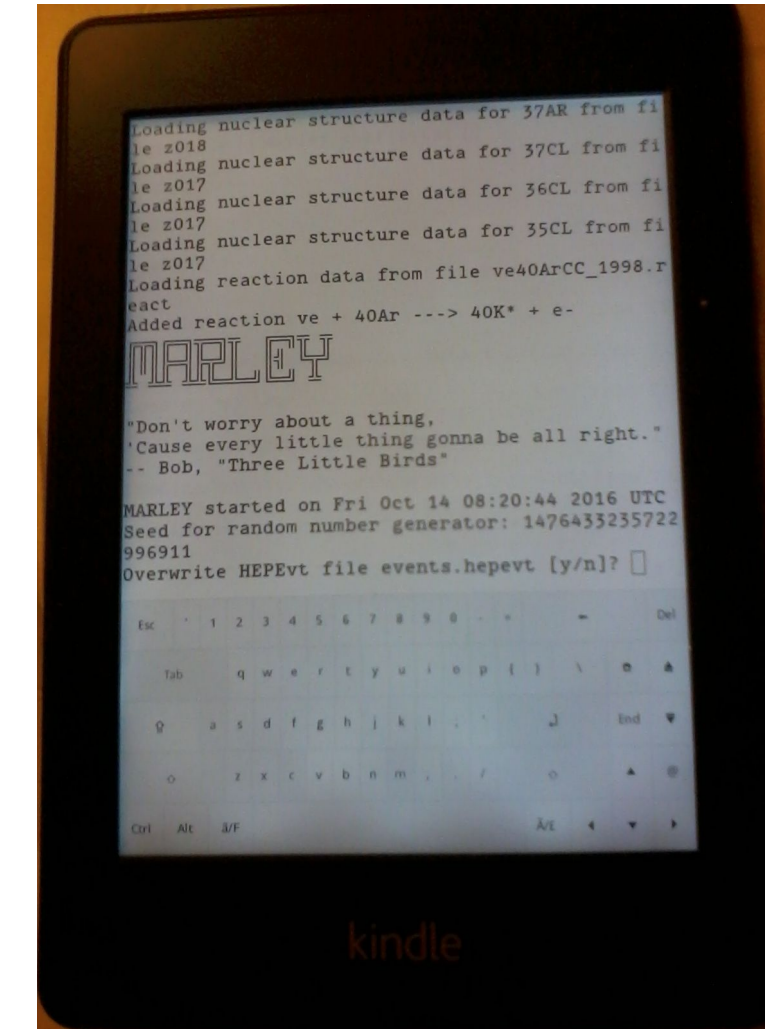
# Physics modeling improvements in the MARLEY neutrino event generator

Steven Gardiner, Pablo Barham Alzás, Luca Abu El-Haj

25th International Workshop on Neutrinos from Accelerators (NuFact 2024)  
Argonne National Laboratory, 17 September 2024

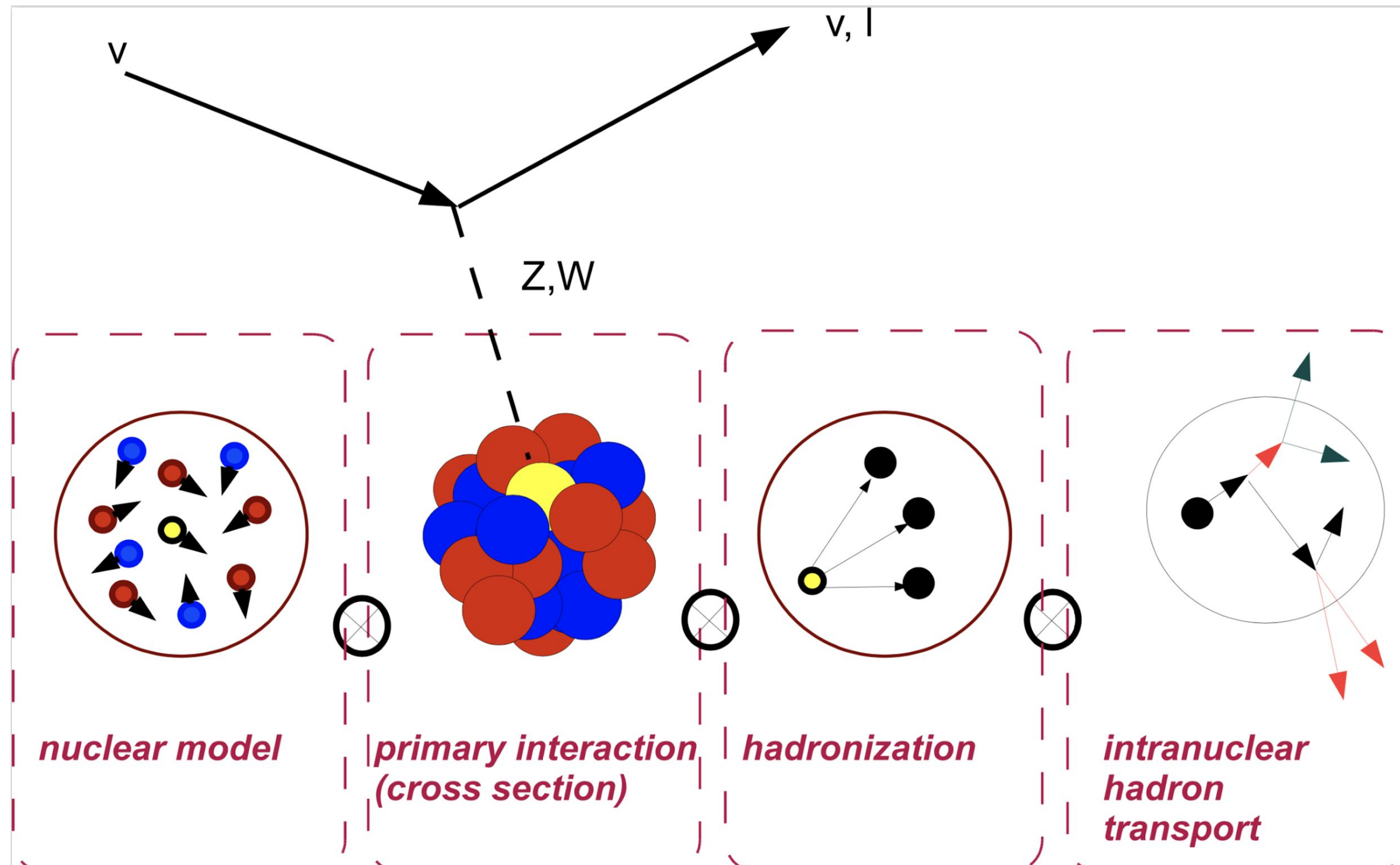
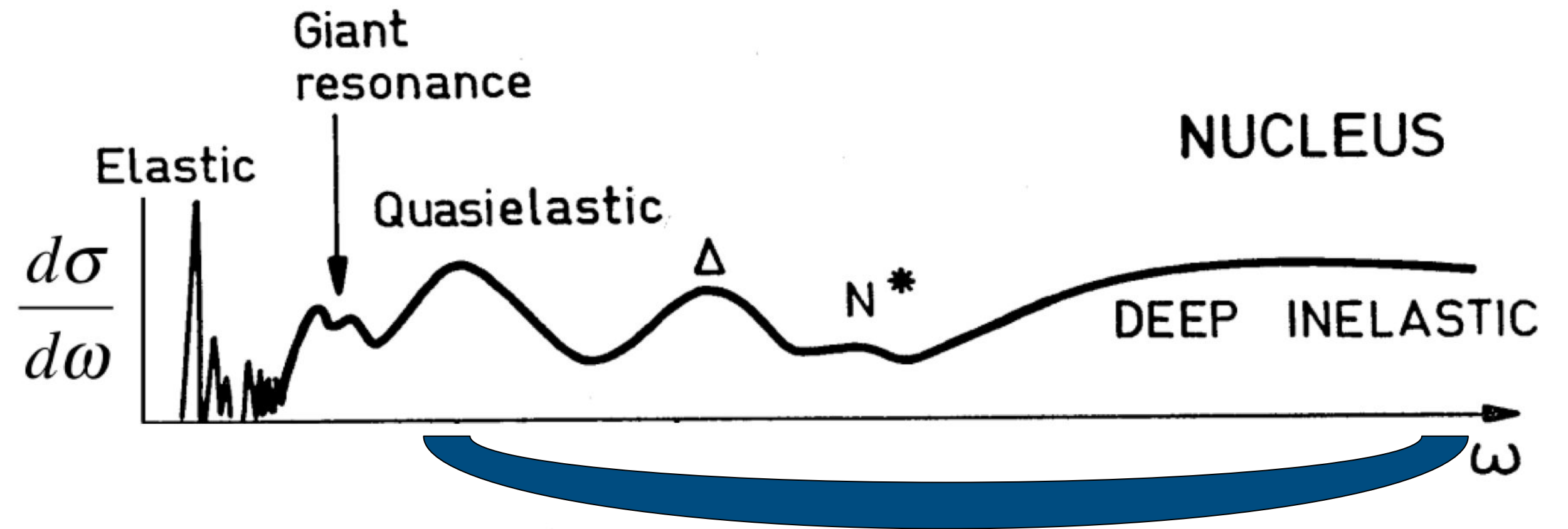
# Model of Argon Reaction Low Energy Yields (MARLEY)

- Event generator for **MeV-scale** neutrino interactions
  - DUNE sensitivity to **supernova + solar neutrinos**
  - COHERENT backgrounds to CEvNS and efficiencies for inelastic cross sections
  - DUNE+SBN **de-excitation  $\gamma$ -rays** in new GENIE model set ("AR23\_20i\_00\_000")
- Current release is **version 1.2.1** ([marleygen.org](http://marleygen.org))
  - Interaction model:  
[Phys. Rev. C 103, 044604 \(2021\)](https://arxiv.org/abs/2104.04460)
  - C++14 implementation:  
[Comput. Phys. Commun. 269, 108123 \(2021\)](https://arxiv.org/abs/2104.10812)



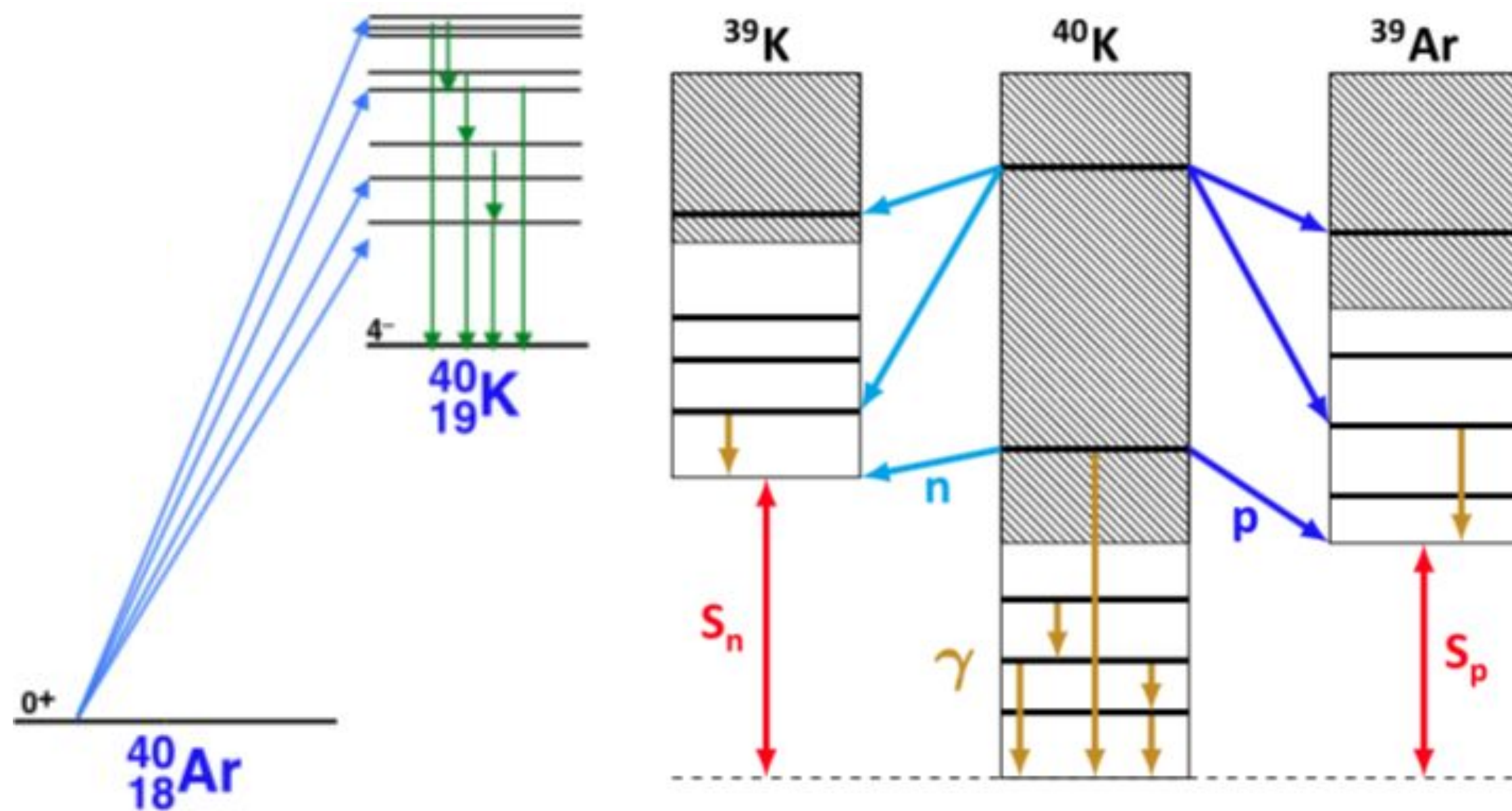
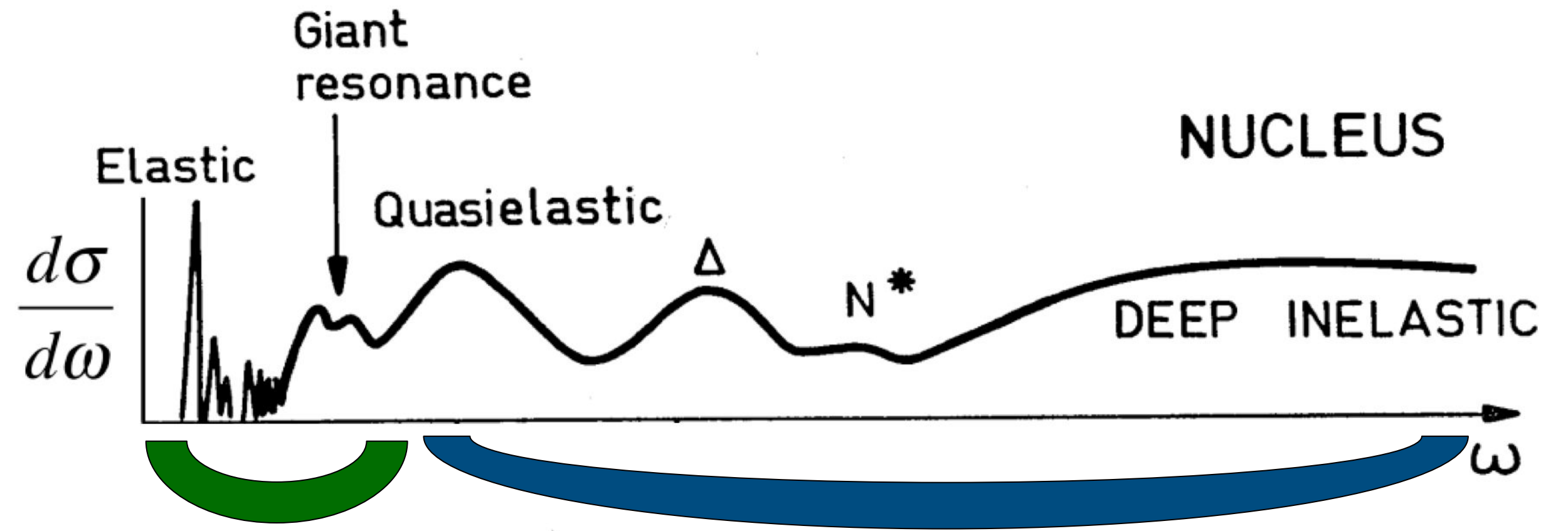
# Typical generator approach for the GeV scale

- Much attention given the needs of accelerator-based oscillation experiments
- **Direct nucleon knockout** with adjustments for nuclear effects (Fermi motion, FSI, etc.)



# MARLEY's treatment is designed for a different regime

- Complements without competing
- Standard **two-step approach**  $\lesssim 100$  MeV
  - Induced transitions to nuclear excited states
  - Emission of de-excitation products

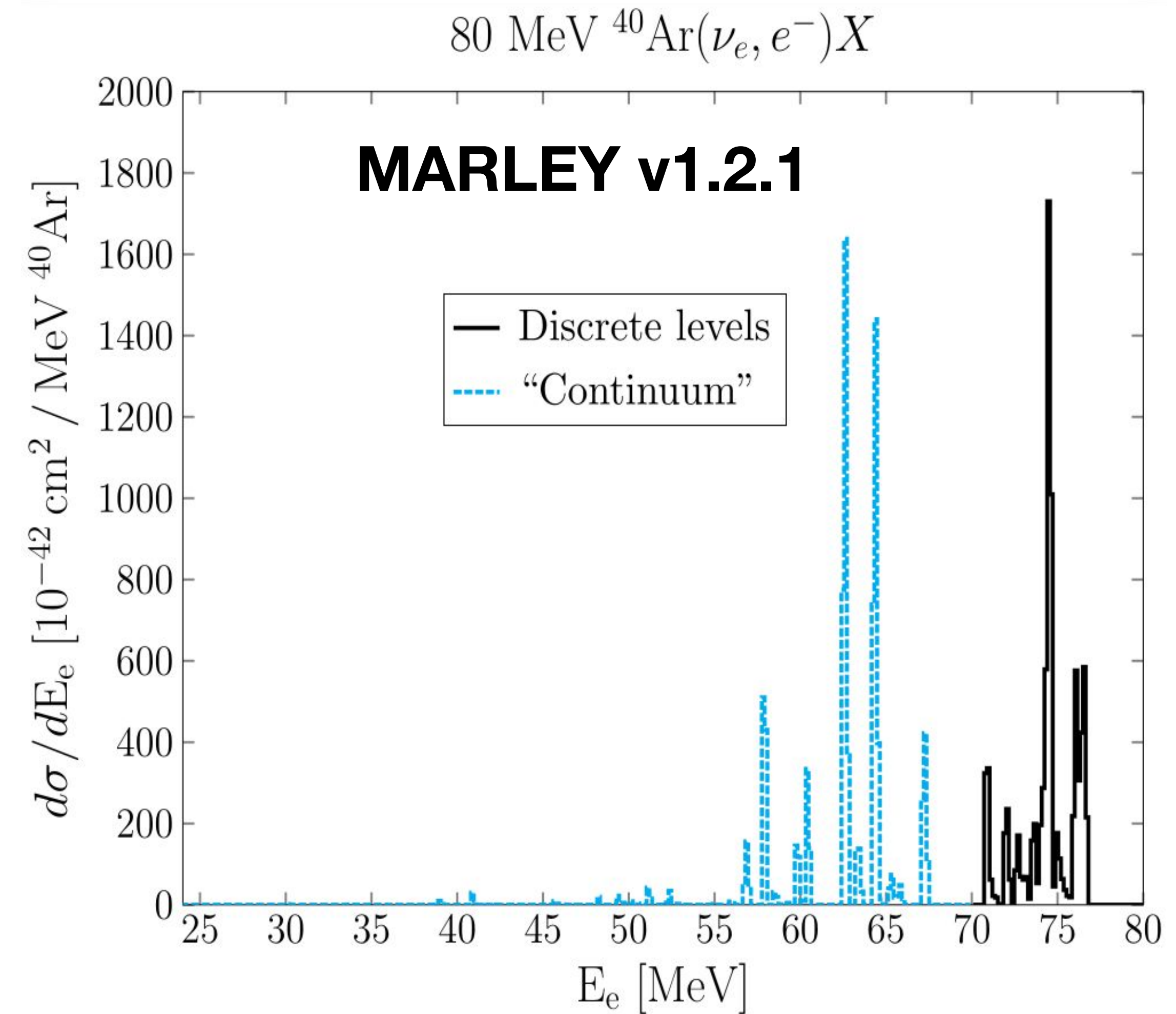


A collage of logos and images related to neutrino physics:
 

- Portrait:** A circular portrait of a man with a beard and dreadlocks.
- NuWro:** Logo for the Neutrino World, featuring a stylized 'W' and the text 'Wrocław Neutrino Event Generator'.
- Genie:** Logo for the Universal Neutrino Generator, featuring a stylized yellow figure.
- GiBUU:** Logo for the GiBUU nuclear model, featuring a cluster of red and blue spheres and a cartoon green lizard.
- Other:** A small logo with a stylized 'v' and the text 'UNIVERSAL NEUTRINO GENERATOR L FIT'.

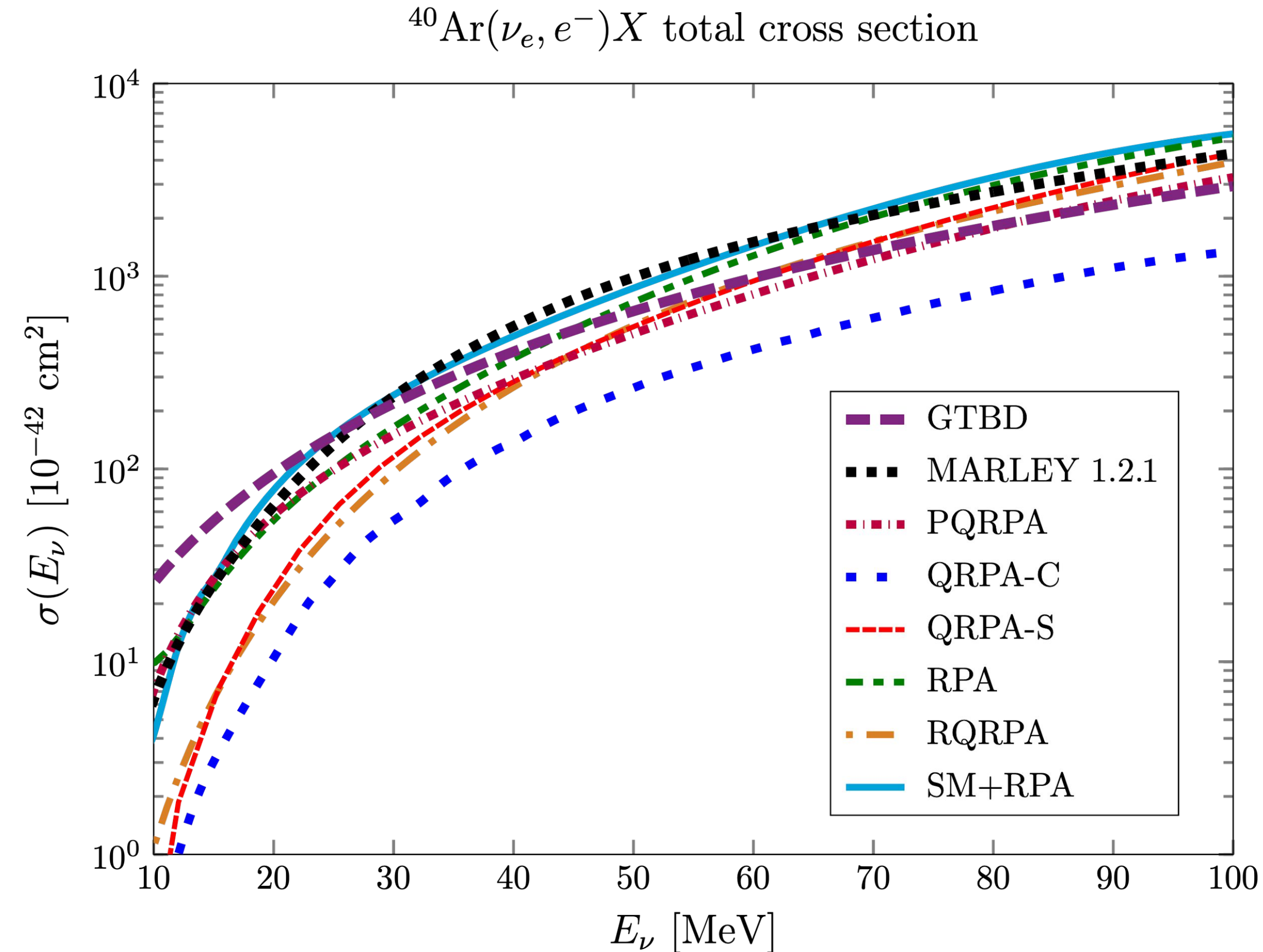
# Physics limitations of MARLEY v1.2.1

- High-lying nuclear energy levels form a **continuum**
  - Existing cross-section model **pretends they are discrete**
- "Allowed approximation" evaluates matrix elements at zero momentum transfer
  - Forbidden contributions neglected
  - Allowed cross section overestimated due to missing  $q$  dependence
- No tools for uncertainty quantification
  - Capability needed for future analyses



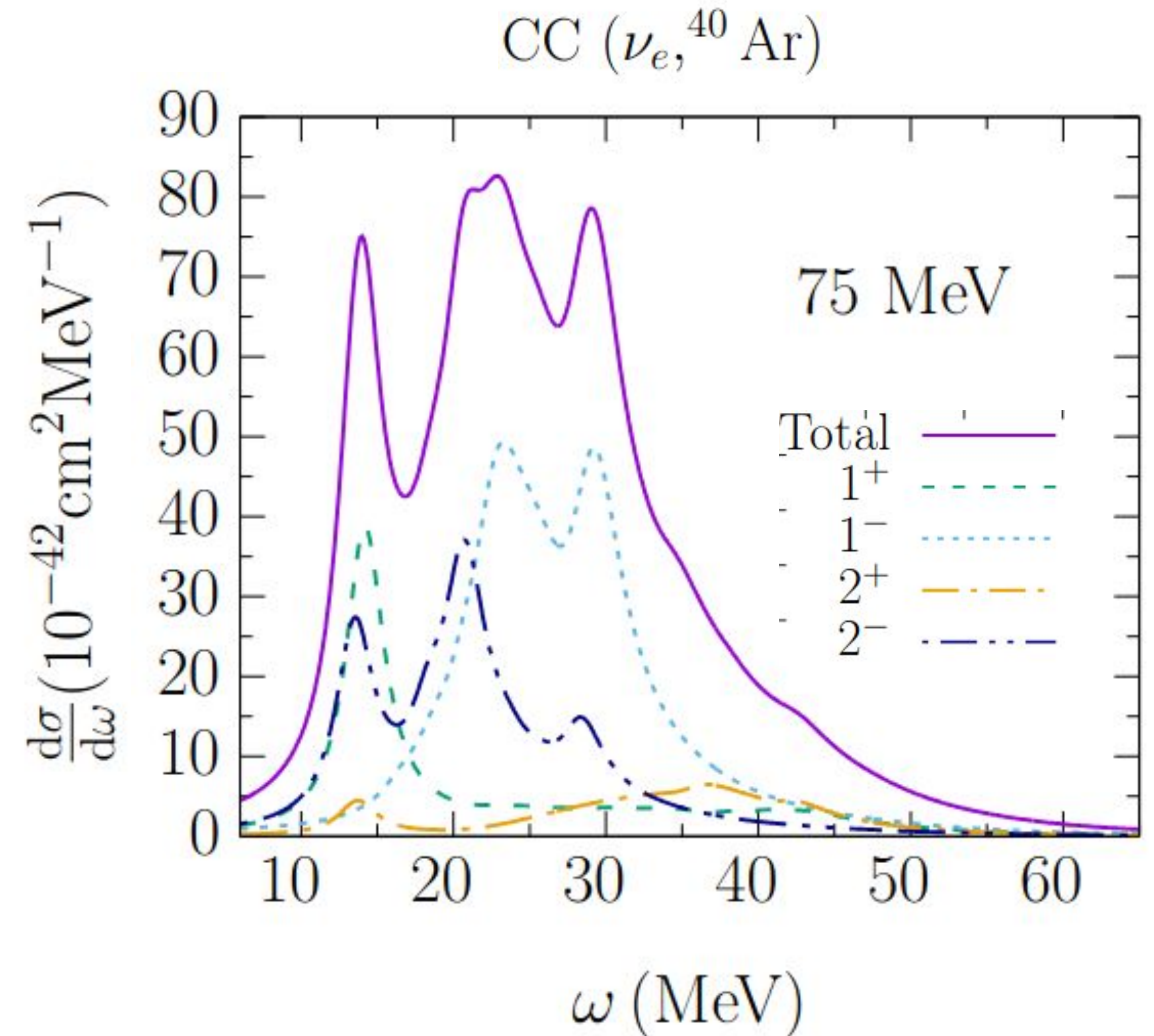
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# A real continuum for MARLEY: The HF-CRPA model

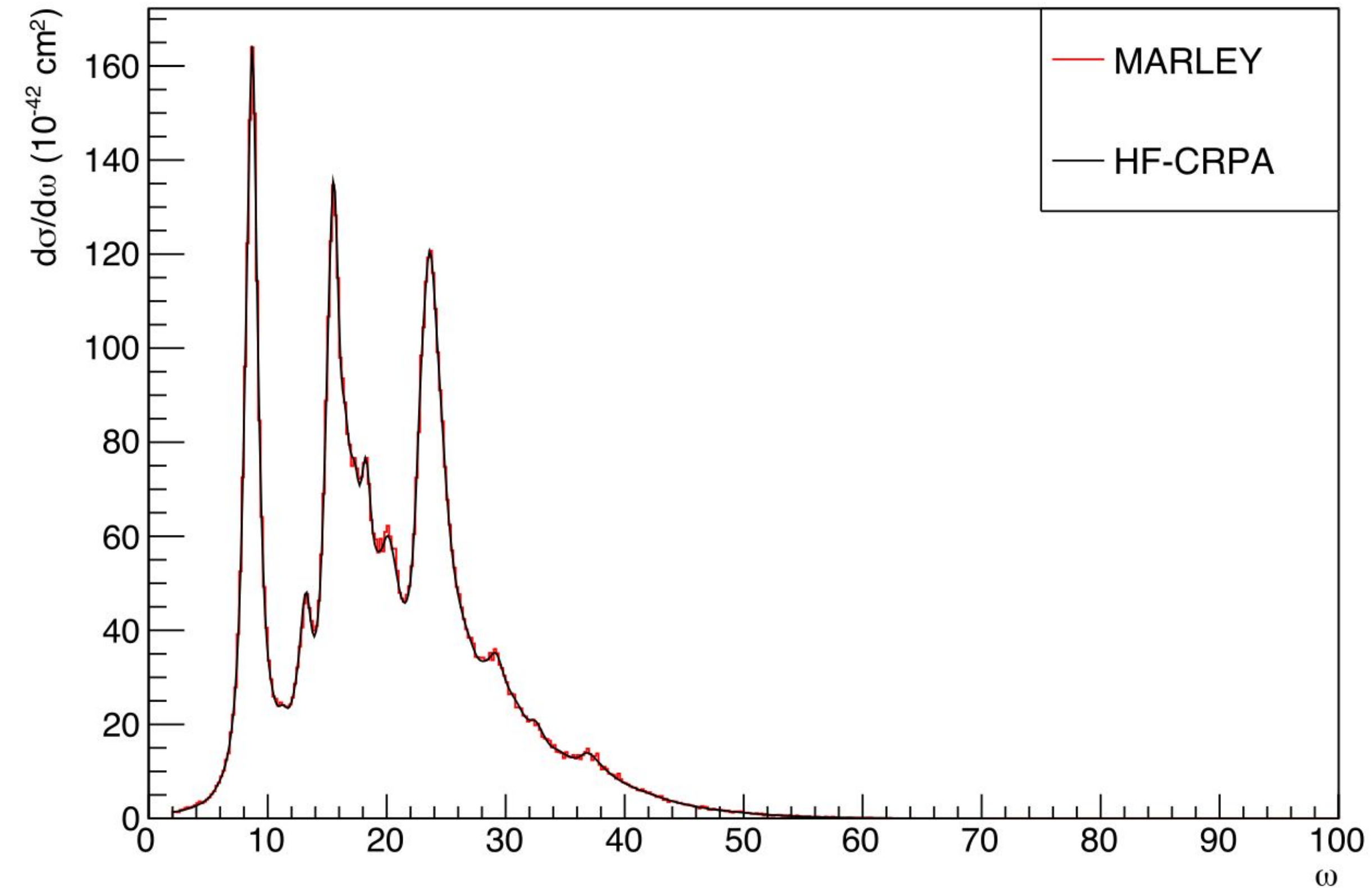
- Low-energy cross sections above the nucleon knockout threshold ( $\sim 8$  MeV)
  - See WG2 talk by Vishvas on Thursday afternoon
  - Developed by University of Ghent group: [Phys. Rev. C 100, 055503 \(2019\)](#)
- **Forbidden transitions** become important at several tens of MeV
  - Curves other than "1+" shown in the plot
- Implemented in MARLEY using tabulated nuclear responses
  - **Many thanks to Natalie Jachowicz, Alexis Nikolakopoulos, and Vishvas Pandey!**



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$${}^{40}\text{Ar}(\nu_e, e^-)X$$





# Discrete transitions in MARLEY v1.2.1: Allowed approximation

Differential cross section can be written in the form  $\frac{d\sigma}{d\cos\theta_\ell} = \frac{G_F^2 |V_{ud}|^2}{2\pi} F_C \left[ \frac{E_i E_f}{s} \right] E_\ell |\mathbf{k}'| \cdot \mathbf{v}_{\mu\nu} R^{\mu\nu}$

AA evaluates the nucleon current under two limits:

Long-wavelength limit:  $q \rightarrow 0$

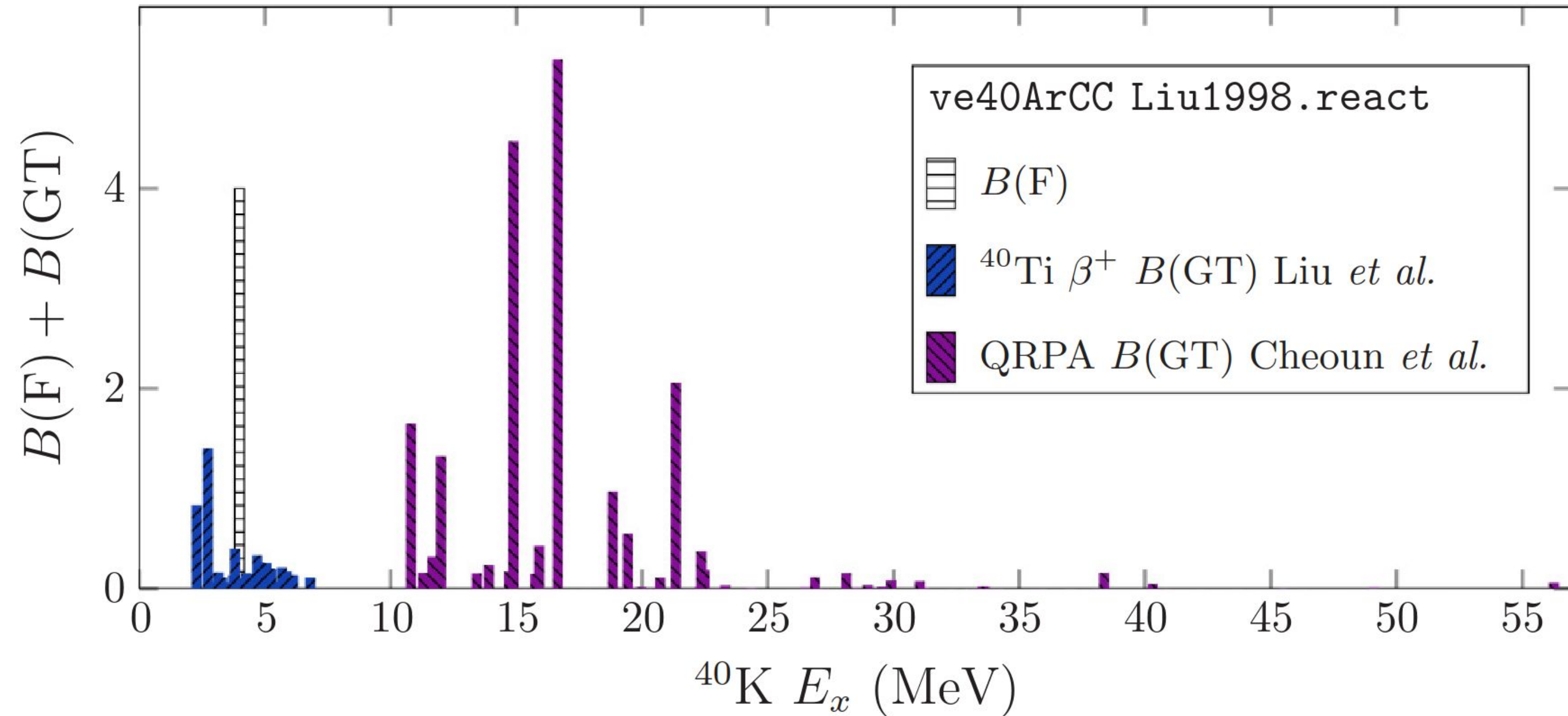
$$j^t = g_V t_\mp$$

$$j^a = -\sigma^a g_A t_\mp$$

Slow nucleon limit:  $\frac{|\mathbf{p}_{N_i}|}{m_N} \rightarrow 0$

Tensor contraction evaluated using Fermi and Gamow-Teller strengths, from data where available

$$\mathbf{v}_{\mu\nu} R^{\mu\nu} = \left(1 + \beta_\ell \cos\theta_\ell\right) B(F) + \left(1 - \frac{1}{3} \beta_\ell \cos\theta_\ell\right) B(GT)$$



[Phys. Rev. C 103, 044604 \(2021\)](#)

# Improved discrete treatment

- Dependence on momentum transfer  $\kappa = |\mathbf{q}|$  needed for compatibility with HF-CRPA
  - Current operators now evaluated to order  $1/m_N$
- Data-driven approach retained
  - "Old MARLEY" preserved in AA limits
  - Input B(F) and B(GT) scaled by relevant form factors dependent on  $Q^2$
- $j_0$  dependence is roughly approximated in nuclear matrix element:

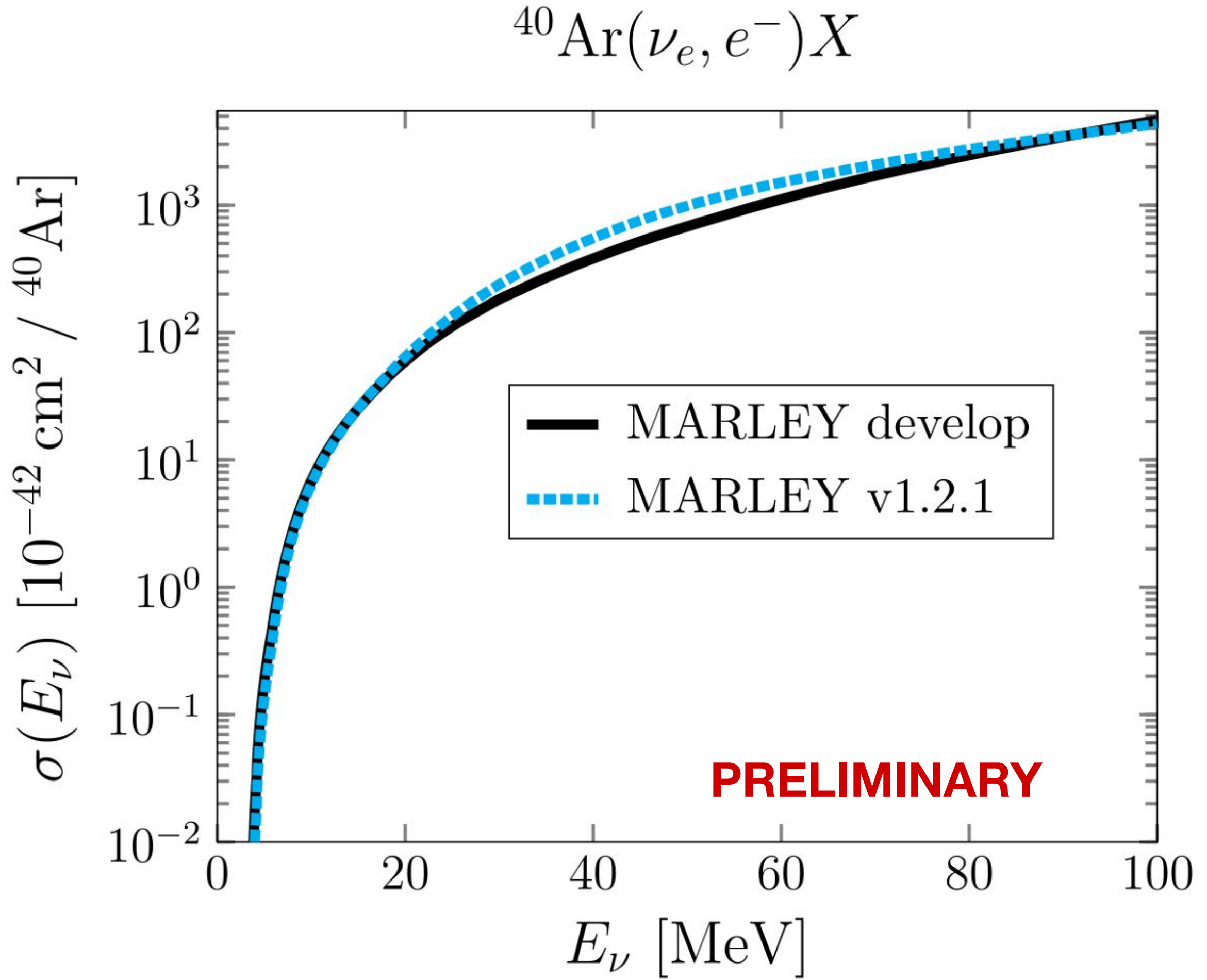
$$\left\langle J_f \left| \left| \sum_{k=1}^A j_0(\kappa r_k) t_-(k) \right| \right| J_i \right\rangle \simeq \left( \frac{1}{N} \sum_{k \in \text{neutrons}} j_0(\kappa r_k) \right) \left\langle J_f \left| \left| \sum_{k=1}^A t_-(k) \right| \right| J_i \right\rangle$$

$$\begin{aligned} v_{\mu\nu} R^{\mu\nu} = & F_1^2 \mathcal{B}_F \left[ v_{CC} + \frac{\kappa}{m_N} v_{CL} + \frac{\kappa^2}{4 m_N^2} v_{LL} \right] \\ & + F_A^2 \mathcal{B}_{GT} \left[ \frac{\kappa^2}{12 m_N^2} (1 - 2\omega F_{PA} + \omega^2 F_{PA}^2) v_{CC} \right. \\ & + \frac{\kappa}{3m_N} \left( 1 - \left[ \omega + \frac{\kappa^2}{2m_N} \right] F_{PA} + \frac{\omega \kappa^2}{2m_N} F_{PA}^2 \right) v_{CL} \\ & + \left( \frac{1}{3} - \frac{\kappa^2}{3m_N} F_{PA} + \frac{\kappa^4}{12 m_N^2} F_{PA}^2 \right) v_{LL} \\ & \left. + \left( \frac{2}{3} + \frac{\kappa^2}{6 m_N^2} F_{12A}^2 \right) v_T - h \frac{2\kappa}{3m_N} F_{12A} v_{T'} \right] \end{aligned}$$

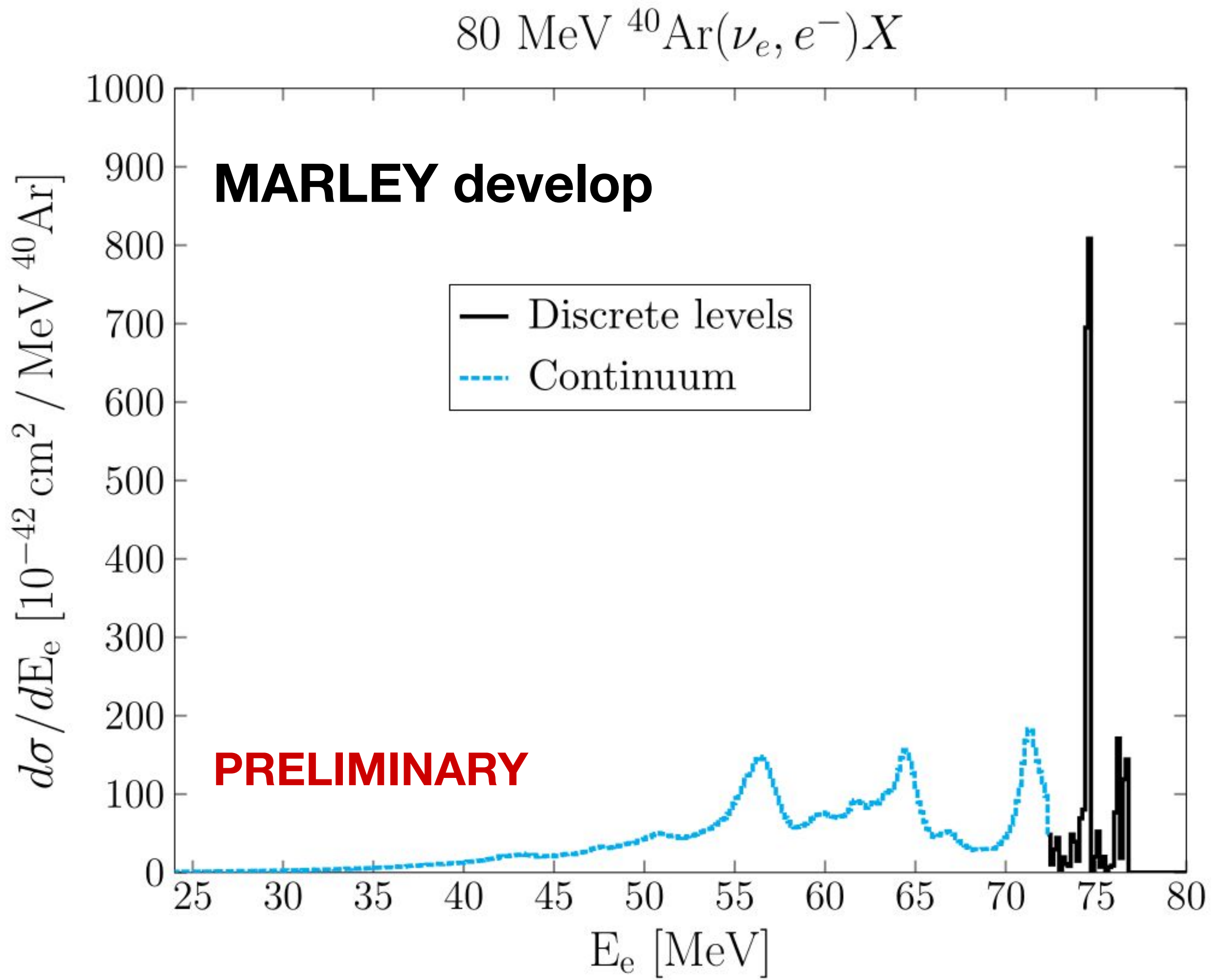
$v$  factors are dimensionless functions of lepton kinematics

$F_{PA}$  and  $F_{12A}$  are expressions involving multiple nucleon form factors

# Inclusive cross-section results

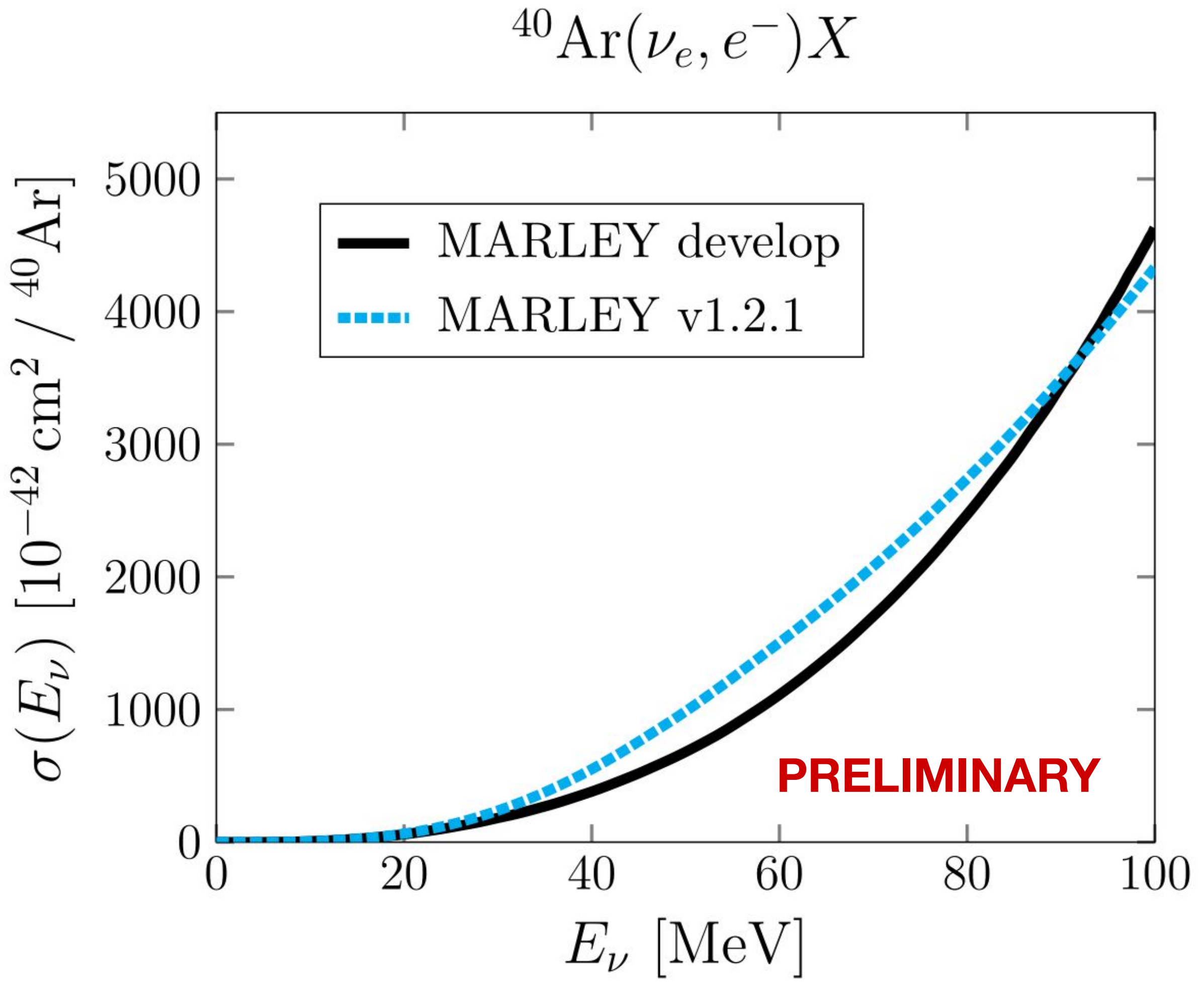


Reduction in  $\sigma(E_\nu)$  seen at a few tens of MeV

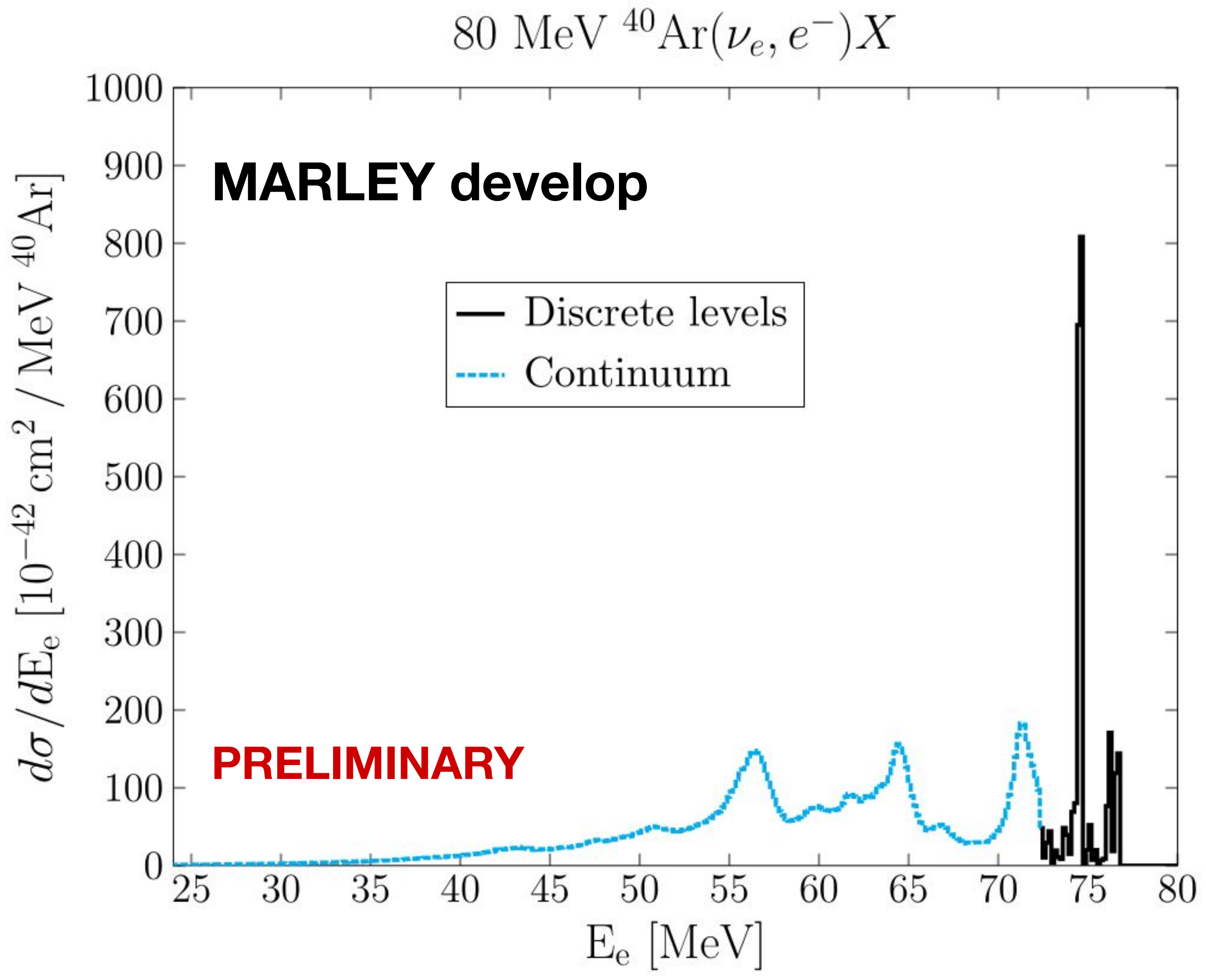


Continuum contributions now behave as expected

# Inclusive cross-section results



Reduction in  $\sigma(E_\nu)$  seen at a few tens of MeV

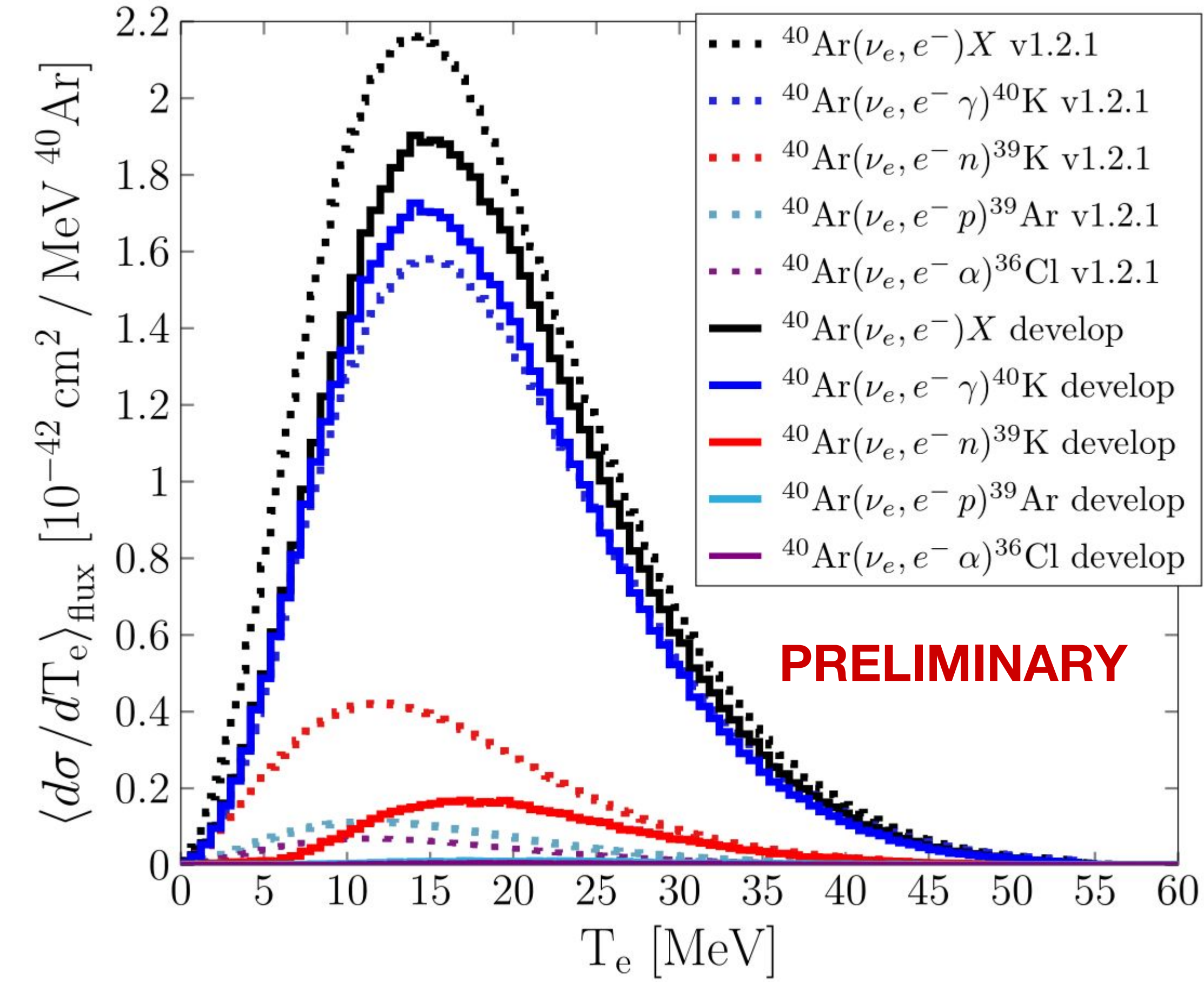


Continuum contributions now behave as expected

# Exclusive predictions

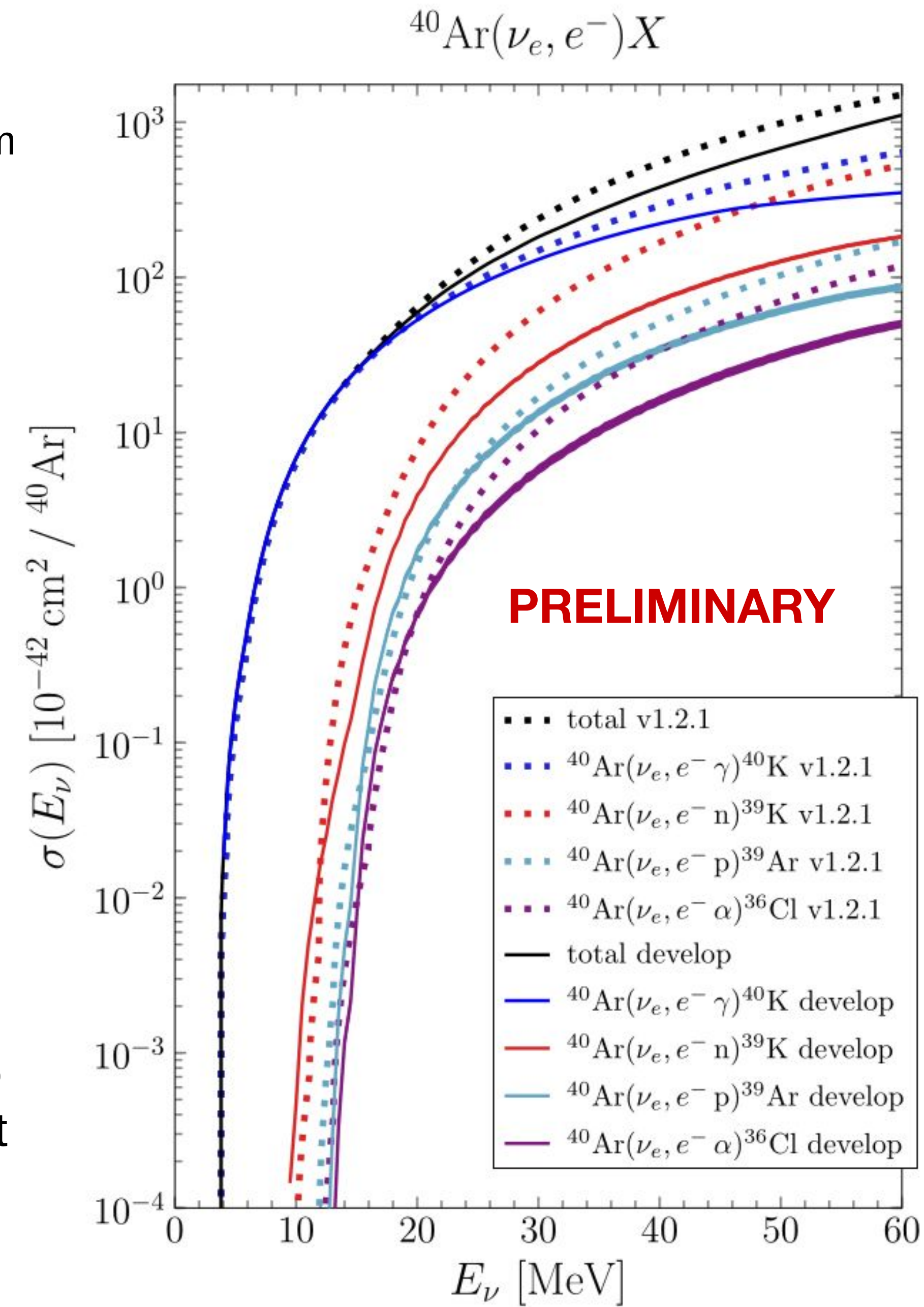
$\text{SN}_T \text{ } ^{40}\text{Ar}(\nu_e, e^-)$

$\text{SN}_T =$  Time-integrated supernova  $\nu_e$  spectrum  
from [Phys. Rev. D 97, 023019 \(2018\)](#)



Neutron emission reduced in new calculation  
= less missing energy for DUNE

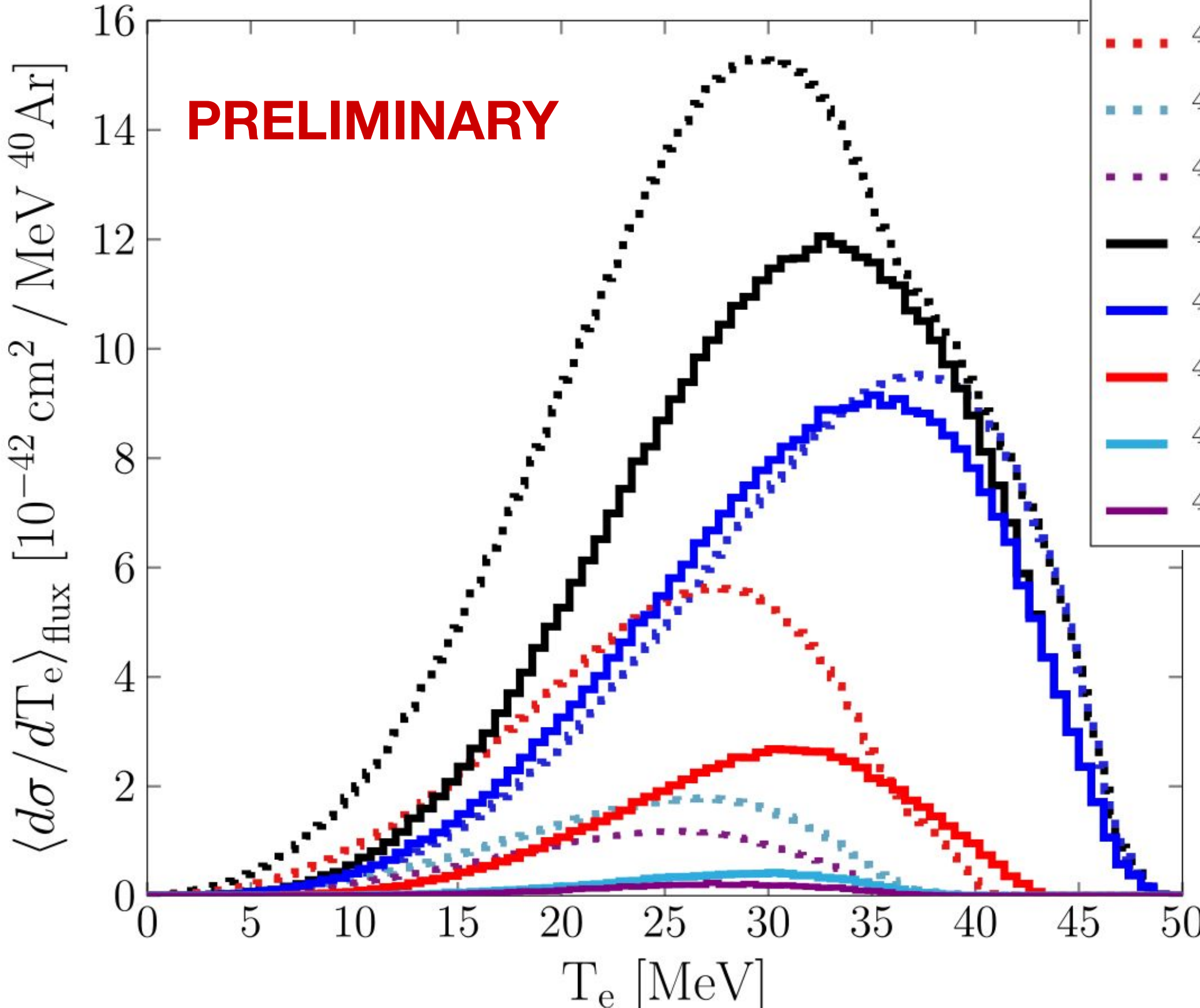
Inclusive cross section  
folded with high-stats  
MC branching ratios to  
produce right-hand plot



# Exclusive predictions

$\mu\text{DAR} = \mu^+$  decay-at-rest spectrum

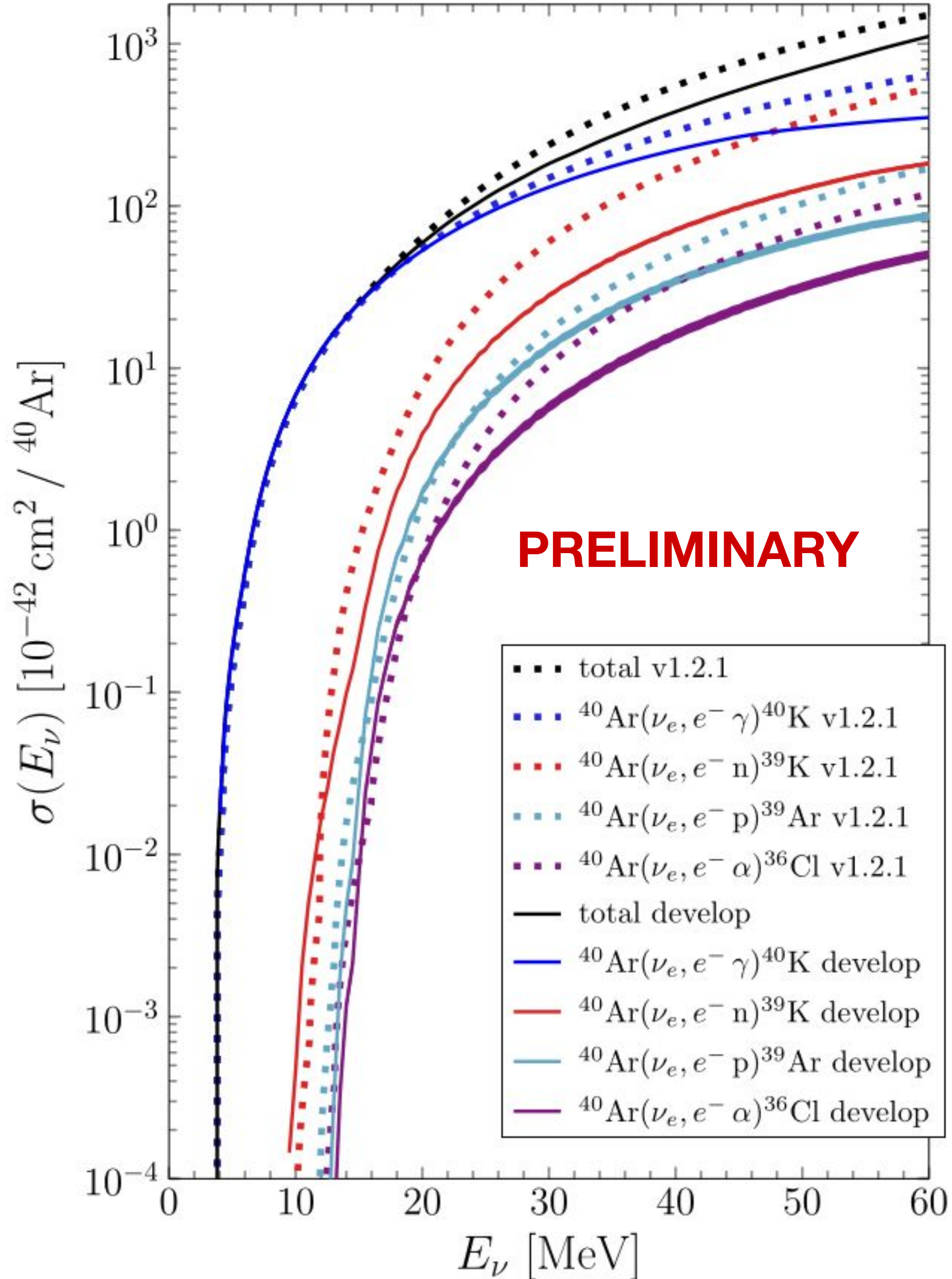
$\mu\text{DAR } ^{40}\text{Ar}(\nu_e, e^-)$



Inclusive cross section  
folded with high-stats  
MC branching ratios to  
produce right-hand plot

Still almost entirely **1n** and **y-only** final states  
in new calculation

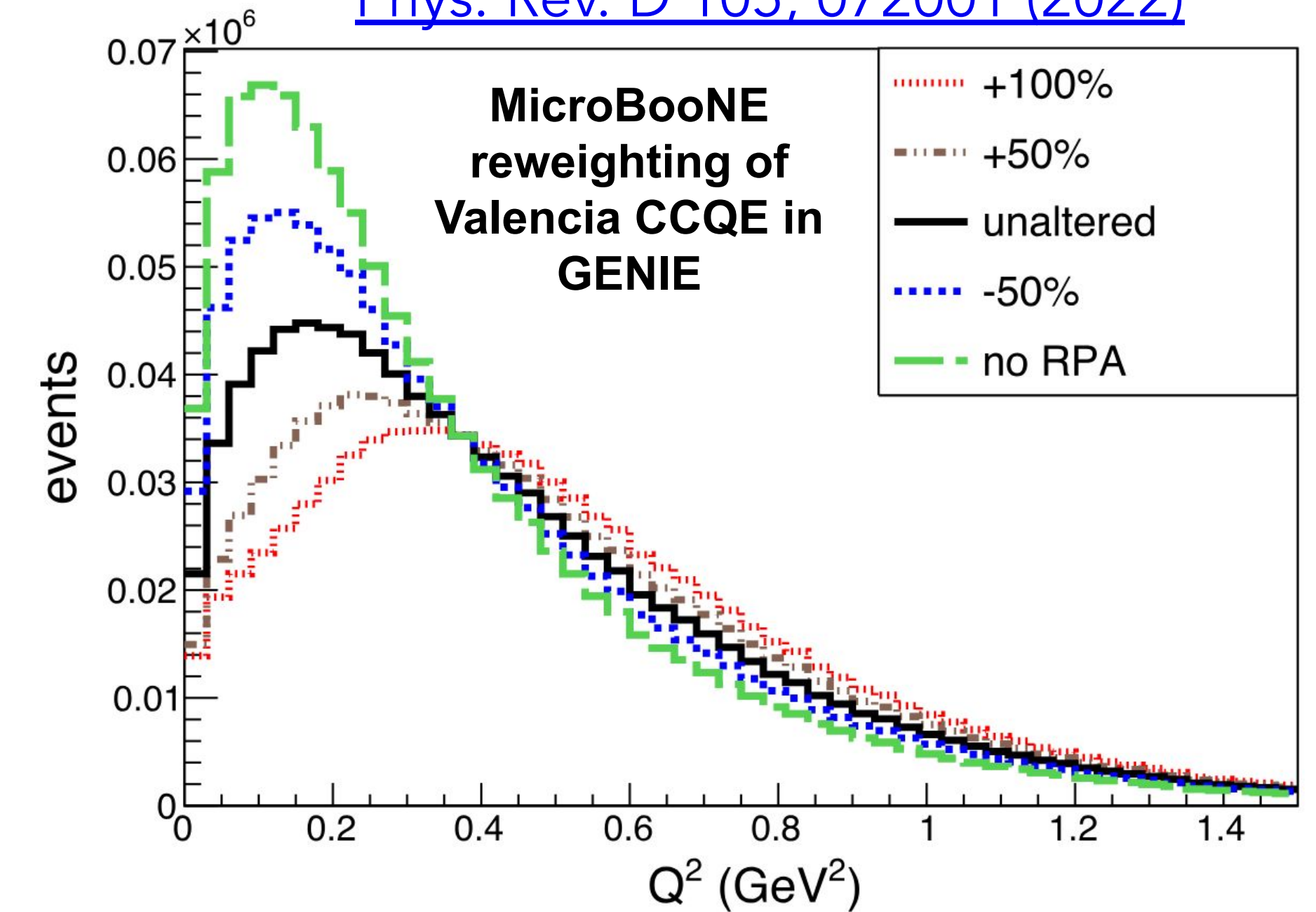
$^{40}\text{Ar}(\nu_e, e^-)X$



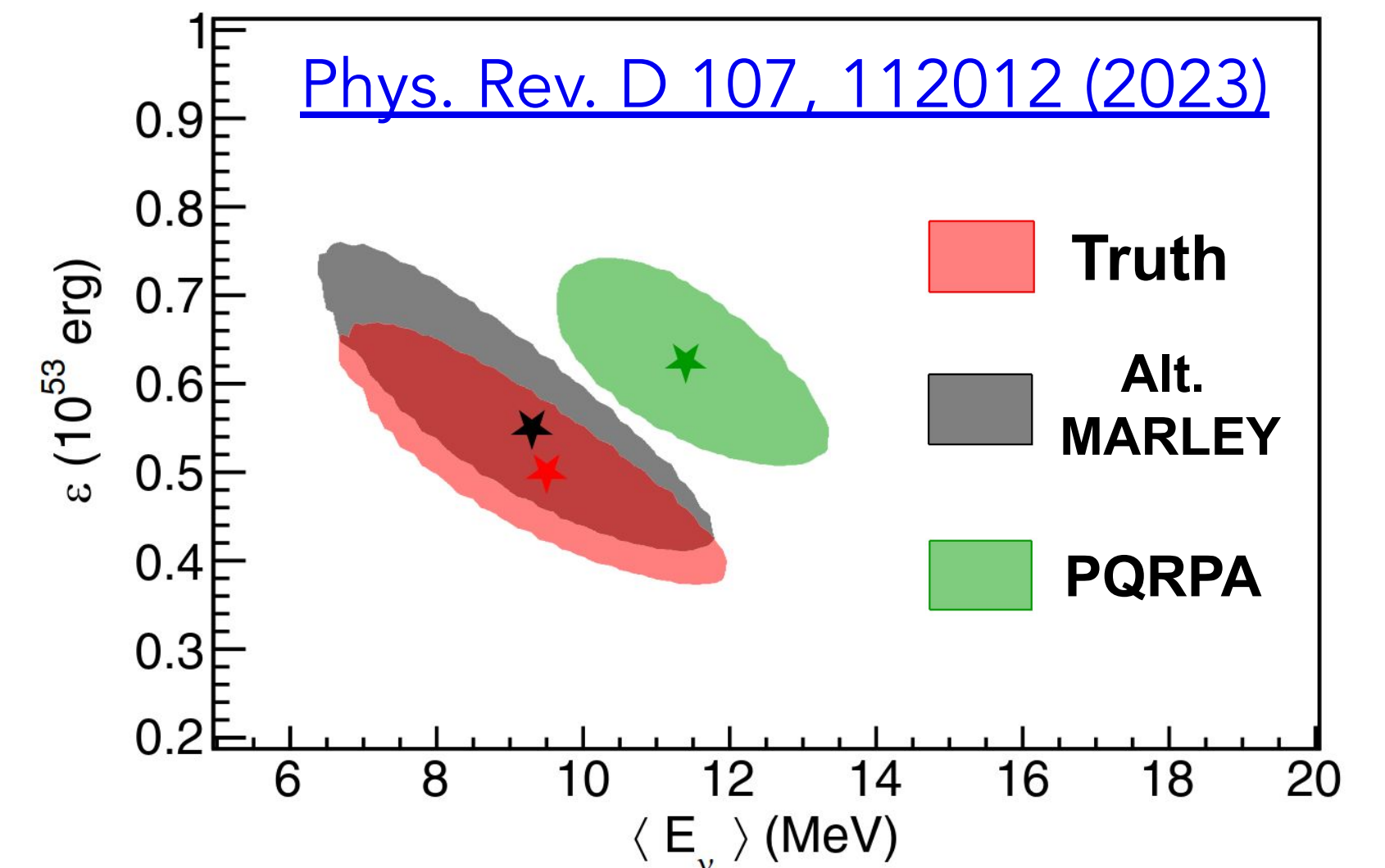
# Reweighting for uncertainty quantification

- Standard "tool of the trade" at GeV energies
  - Weights assigned according to likelihood ratio between alternate and nominal physics models
- **Systematics** in future MARLEY-based analyses
  - Efficiency / purity / energy resolution for supernova  $\nu_e$  detection in DUNE
  - Neutrino backgrounds for MeV-scale exotic physics searches
- Some **exploration of uncertainties** already
  - No technical infrastructure in MARLEY v1.2.1
  - $\sigma(E_\nu)$  uncertainty not rigorously quantified yet

[Phys. Rev. D 105, 072001 \(2022\)](#)



[Phys. Rev. D 107, 112012 \(2023\)](#)



# MARLEY nuclear de-excitation model

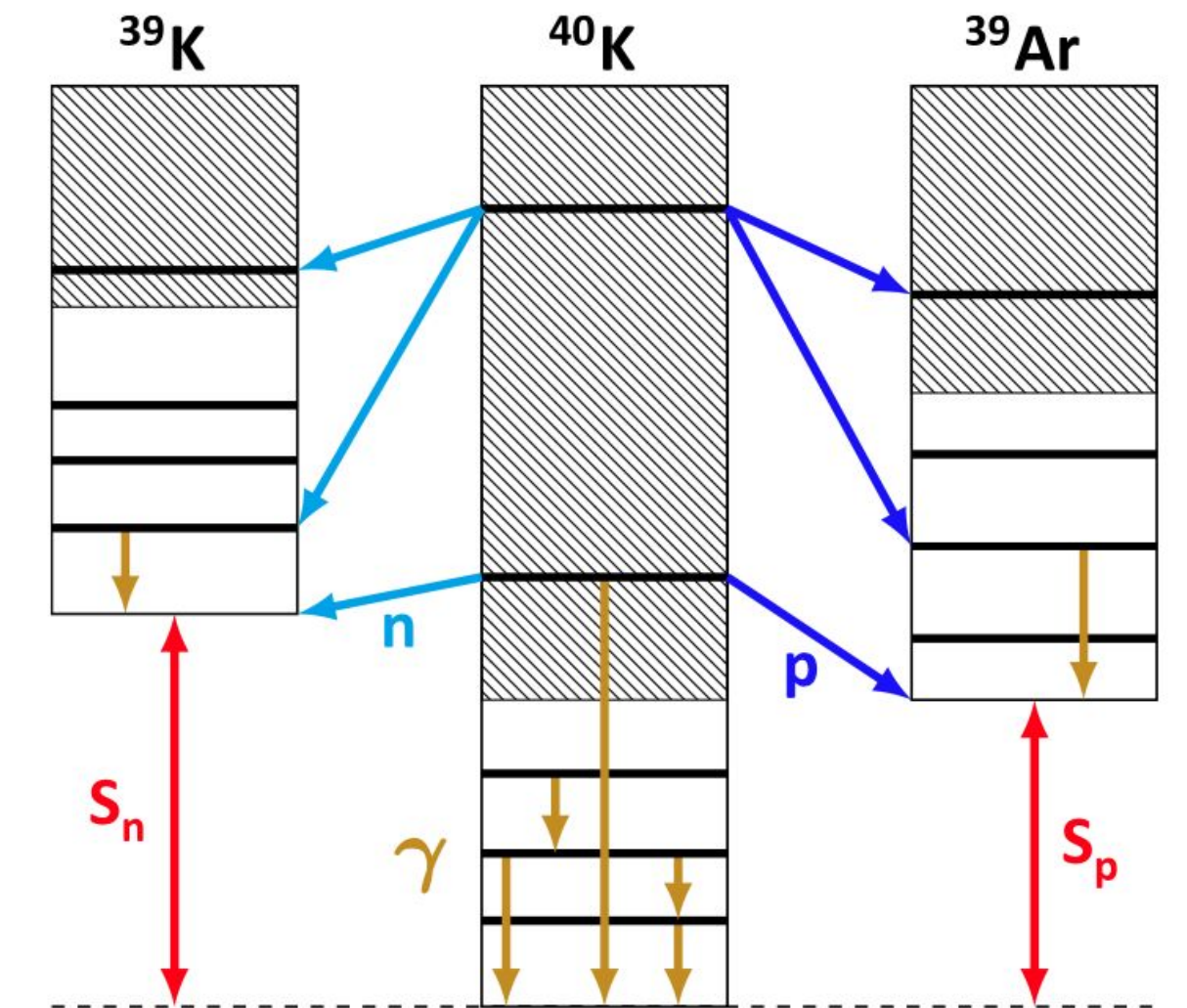
Hauser-Feshbach formalism for computing differential decay widths:

Differential decay width  
for emission of a  
nuclear fragment  $\alpha$   
( $A \leq 4$  considered)

$$\frac{d\Gamma_{\alpha}}{dE'_x} = \frac{1}{2\pi\rho_i(E_x, J, \Pi)} \sum_{\ell=0}^{\ell_{\max}} \sum_{j=|\ell-s|}^{\ell+s} \sum_{J'=|J-j|}^{J+j} T_{\ell j}(\varepsilon) \rho_f(E'_x, J', \Pi')$$

Differential decay width  
for emission of a  
 $\gamma$ -ray

$$\frac{d\Gamma_{\gamma}}{dE'_x} = \frac{1}{2\pi\rho_i(E_x, J, \Pi)} \sum_{\lambda=1}^{\lambda_{\max}} \sum_{J'=|J-\lambda|}^{J+\lambda} \sum_{\Pi' \in \{-1, 1\}} T_{X\lambda}(E_{\gamma}) \rho_f(E'_x, J', \Pi')$$



Phenomenological ingredients based on global fits to nuclear reaction data

**Level density model:** Back-shifted Fermi gas

[Nucl. Data Sheets 110, 3107–3214 \(2009\)](#)

**Nuclear optical model potential:** Koning & Delaroche,

[Nucl. Phys. A 713, 231–310 \(2003\)](#)

**Gamma-ray strength function model:** Standard Lorentzian

[Nucl. Data Sheets 110, 3107–3214 \(2009\)](#)

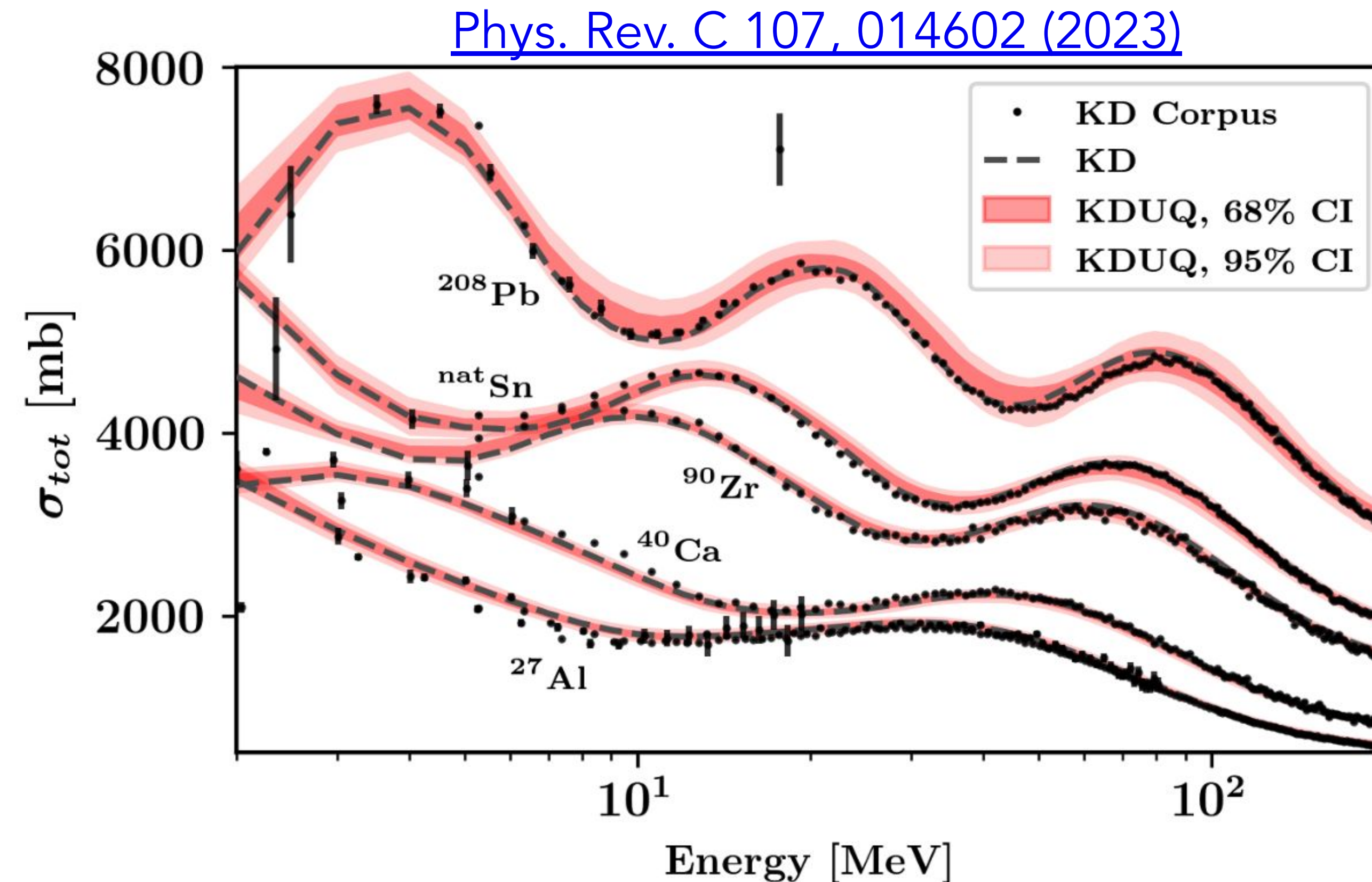
Supplemented with tabulated discrete levels and  $\gamma$ -rays for bound states (taken from TALYS 1.6).

Transitions from continuum to all accessible levels are explicitly treated.



# Optical model potential uncertainties

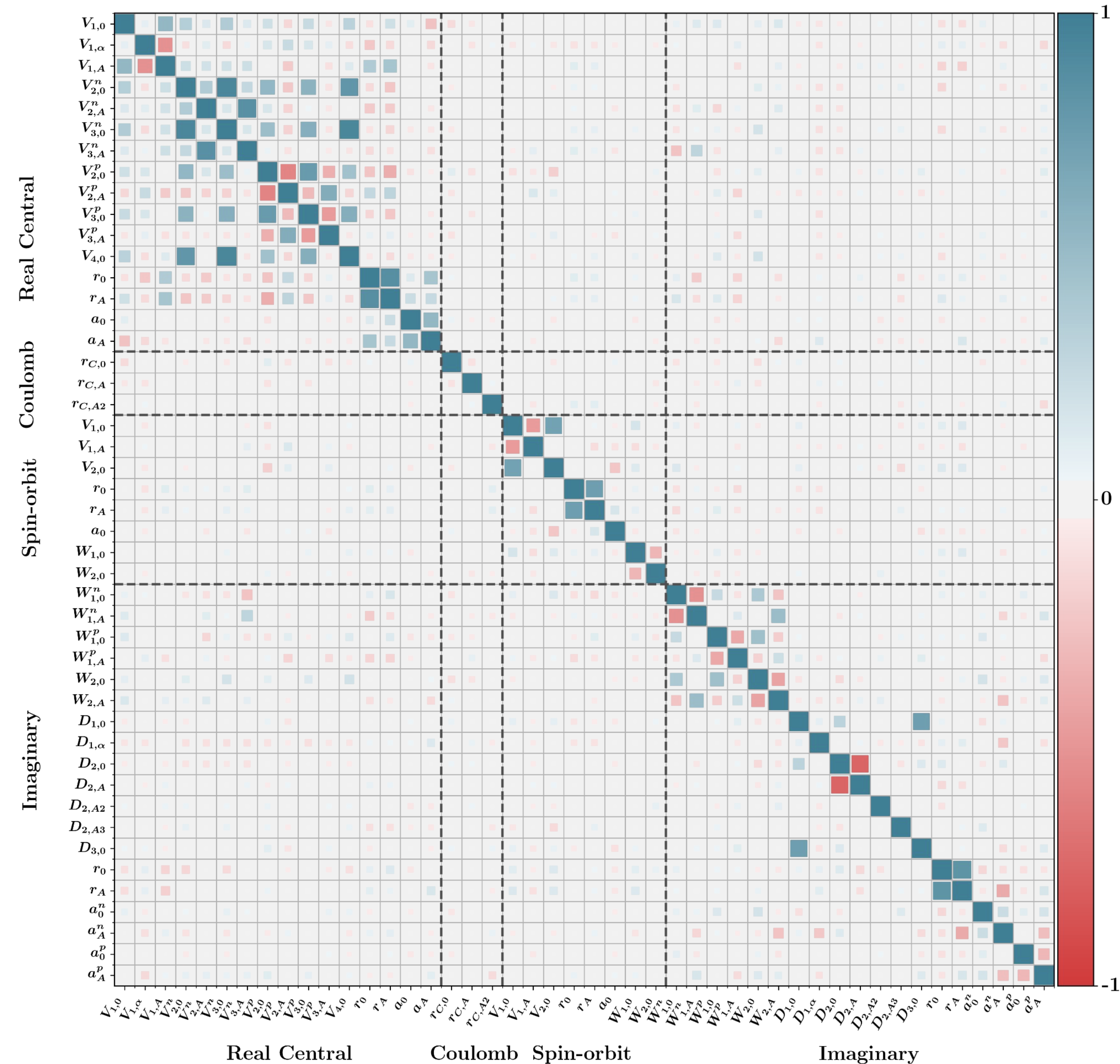
- Original KD fit did not report these
- Revisited by Pruitt *et al.* (LLNL) in 2023
  - Motivated by applications to FRIB, etc.
  - KDUQ optical potential includes covariances between all 46 empirical parameters
- How do these impact calculations of exclusive O(10 MeV) neutrino cross sections?
  - Expected to be sub-leading at present
  - Well-justified by data, related uncertainties (level densities, etc.) under development
  - Starting point for MARLEY uncertainty toolkit



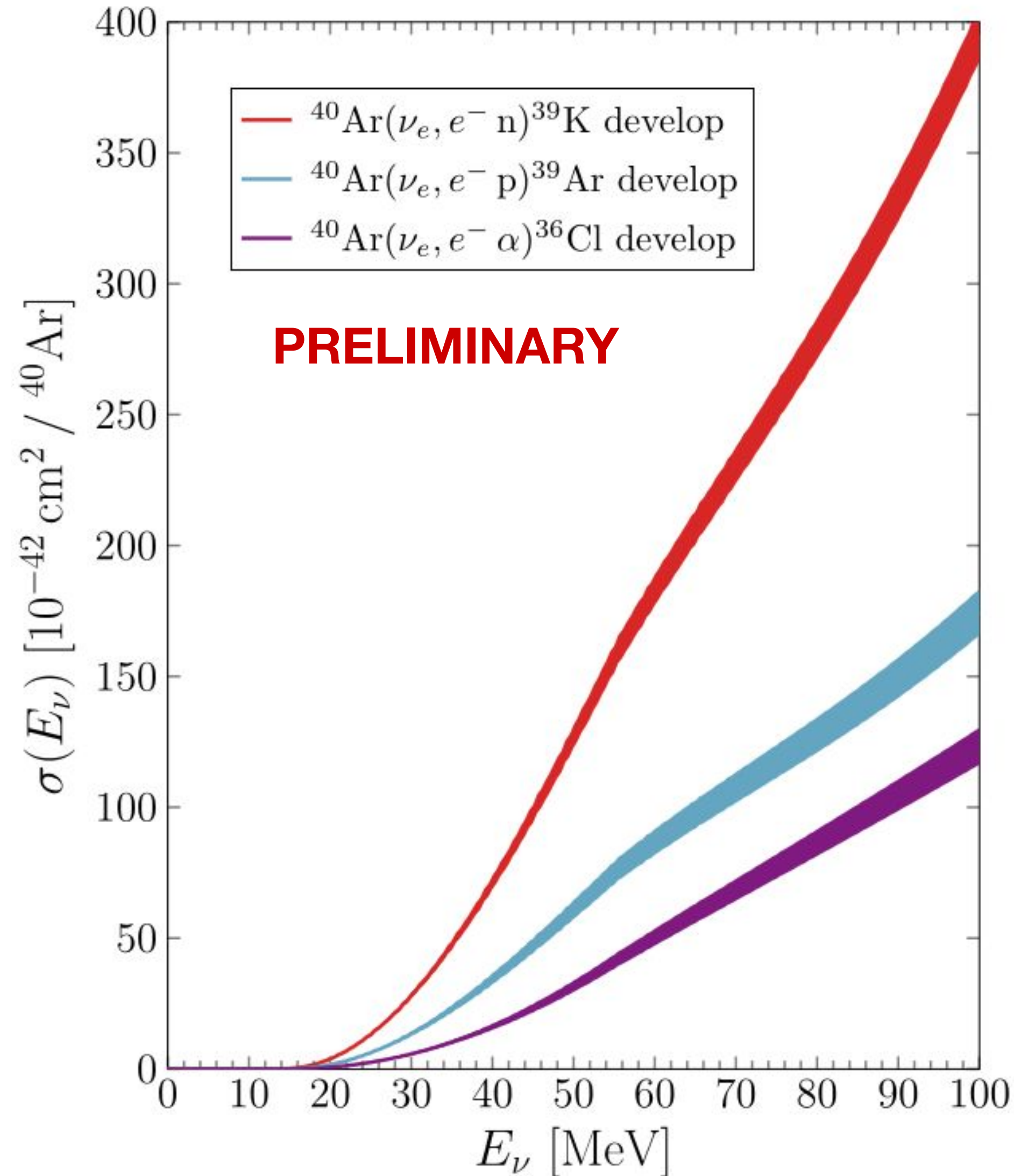
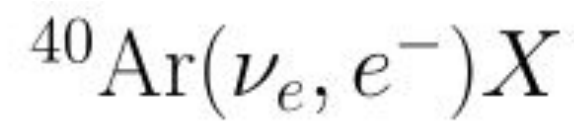
# Optical model potential uncertainties

[Phys. Rev. C 107, 014602 \(2023\)](#)

- Original KD fit did not report these
  - Motivated by applications to FRIB, etc.
- Revisited by Pruitt *et al.* (LLNL) in 2023
  - KDUQ optical potential includes **correlations** between all 46 empirical parameters
- How do these impact calculations of exclusive O(10 MeV) neutrino cross sections?
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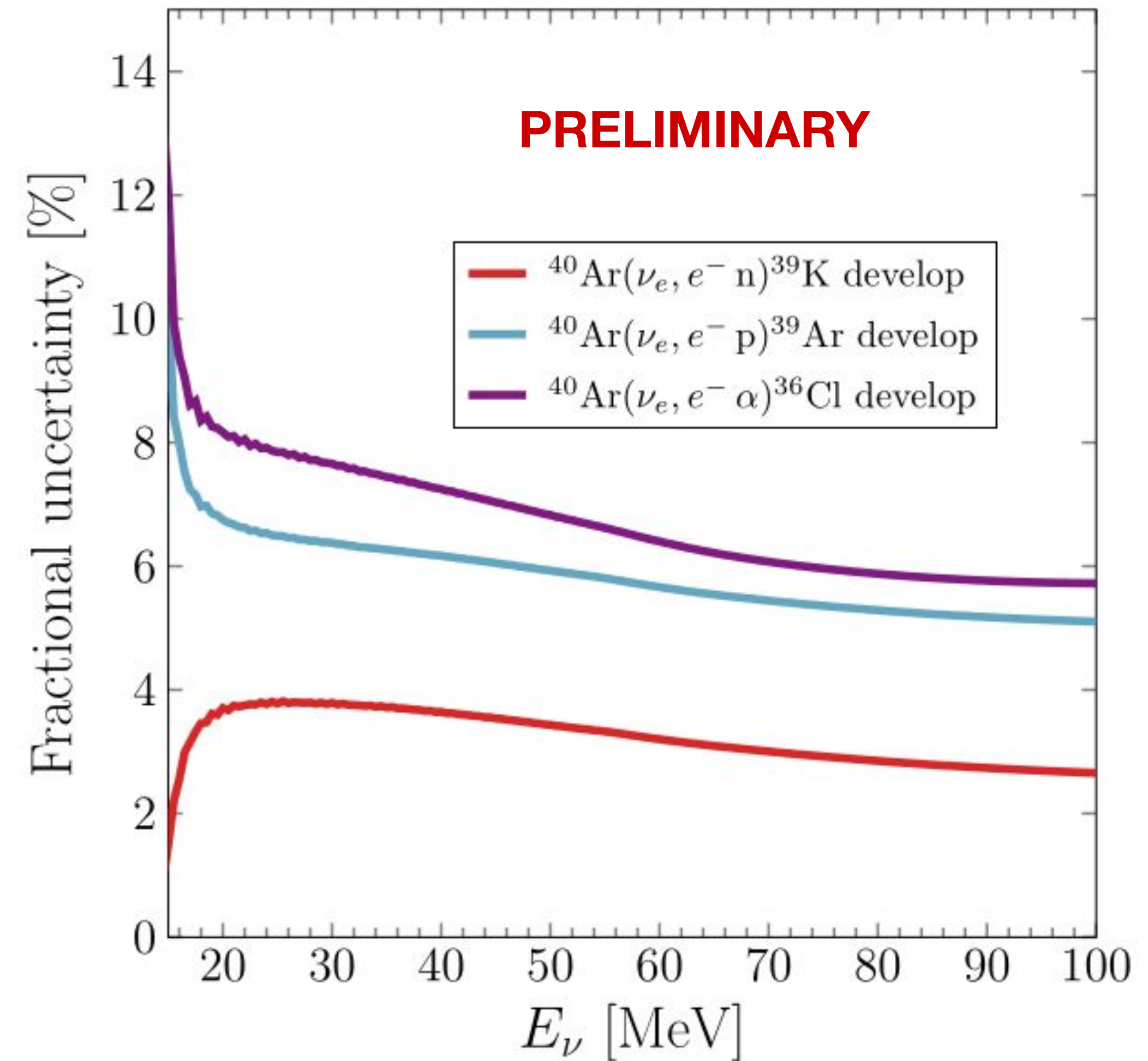
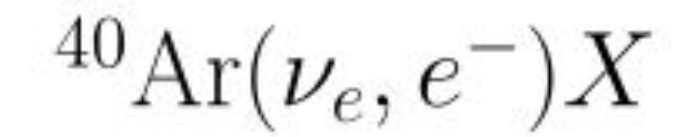


# Optical model potential uncertainties



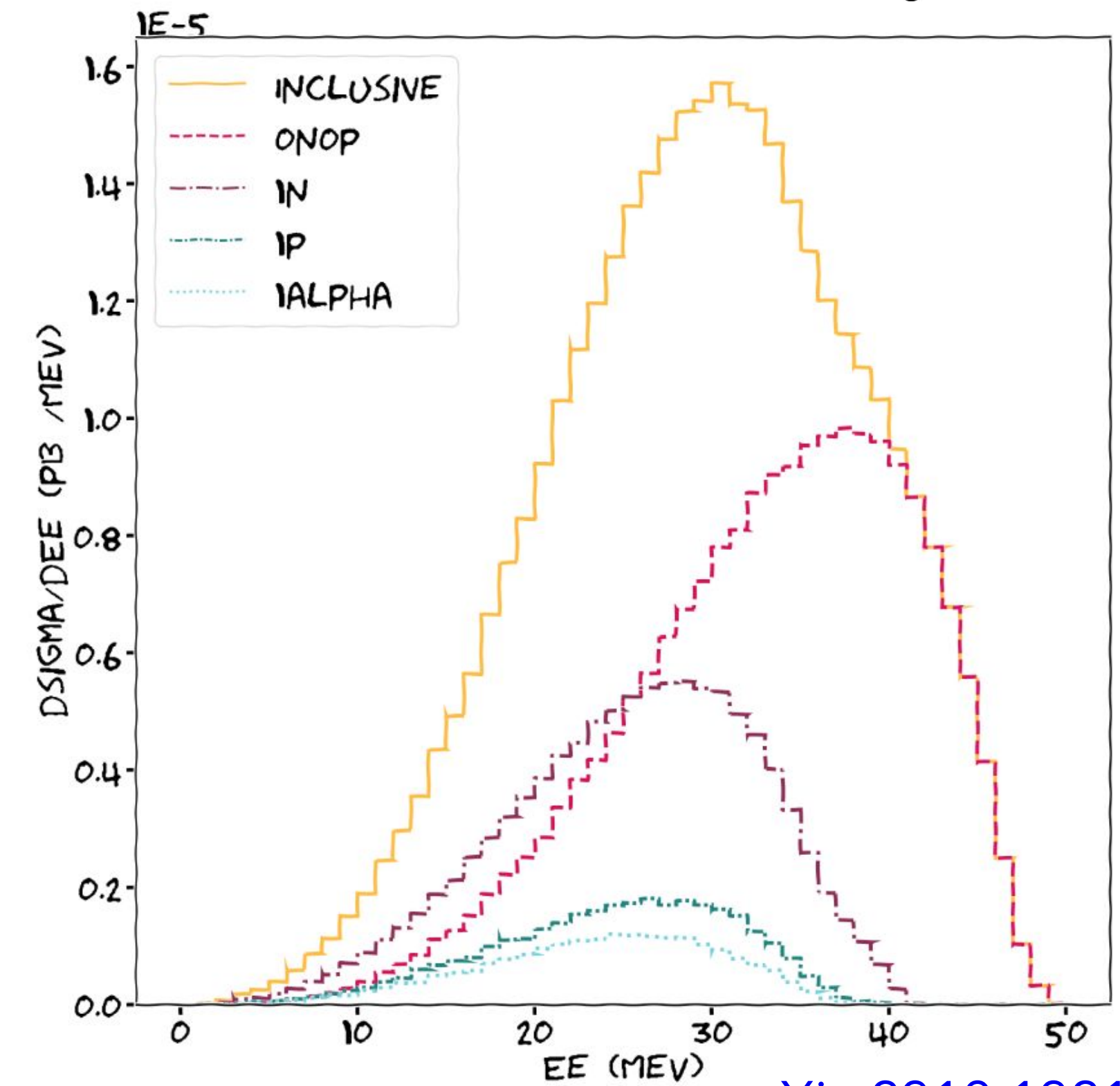
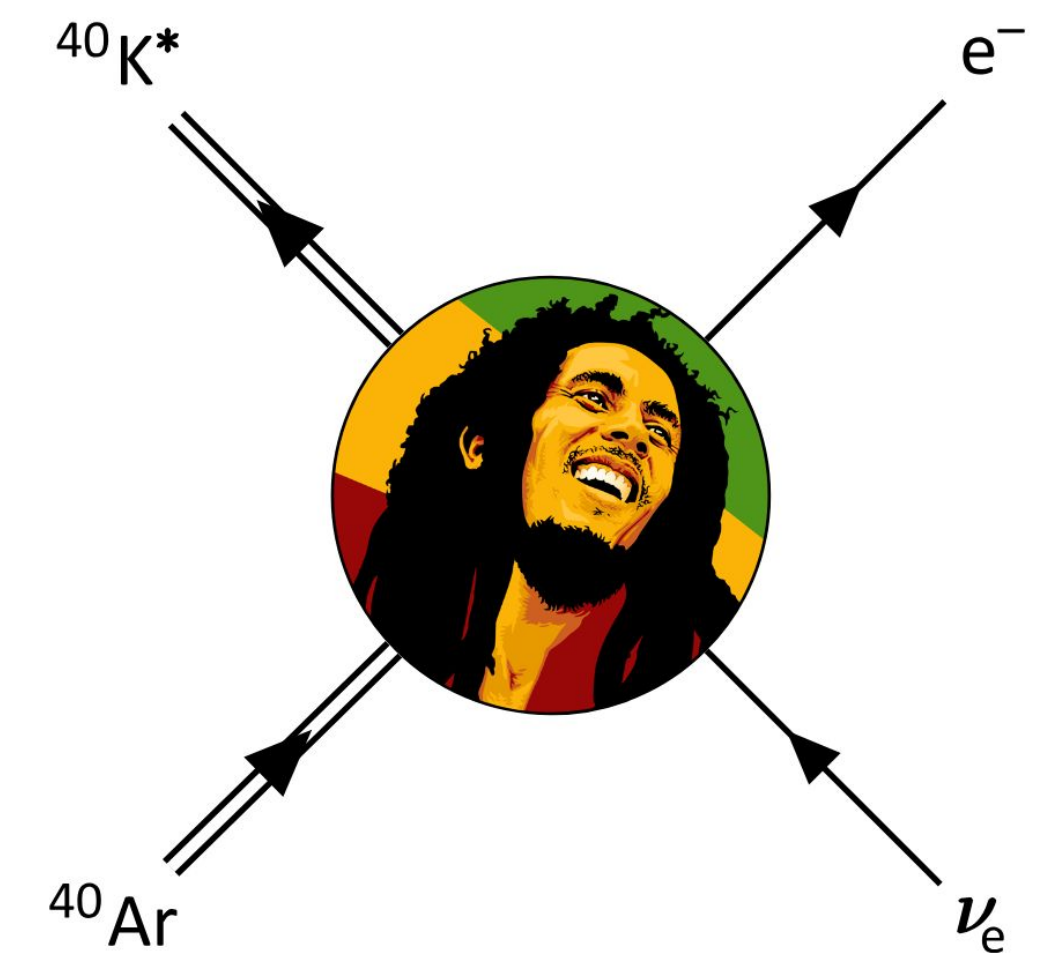
$\gamma$ -only cross section dominated by discrete levels. OMP uncertainty nonzero but tiny!

$1\alpha$  has modestly higher fractional uncertainty  $\rightarrow$  sensitive to both p and n OMP parameters



# Towards MARLEY v2.0.0

- Many technical enhancements in addition to physics topics addressed in this talk
- **NuHepMC**: Universal neutrino generator event format
  - Adopted internally and in MARLEY output
  - Directly enables reweighting, other new features
  - Automated, generator-agnostic **analysis of results**
  - Could enable interoperability (e.g., delegate de-excitations to MARLEY)
- **mardecay**: Standalone simulation of de-excitation step only
- **marweight**: Apply new weights to existing MC sample
- Speedup of optical model calculations (~30x!)
- **New major release (v2)** anticipated in the coming months
  - Development team remains small ( $\ll 1$  FTE)
  - New collaborators are always welcome! ([gardiner@fnal.gov](mailto:gardiner@fnal.gov))



[arXiv:2310.13211](https://arxiv.org/abs/2310.13211)

# Backup