

# Constraints on flavor-dependent long-range interactions of high-energy astrophysical neutrinos

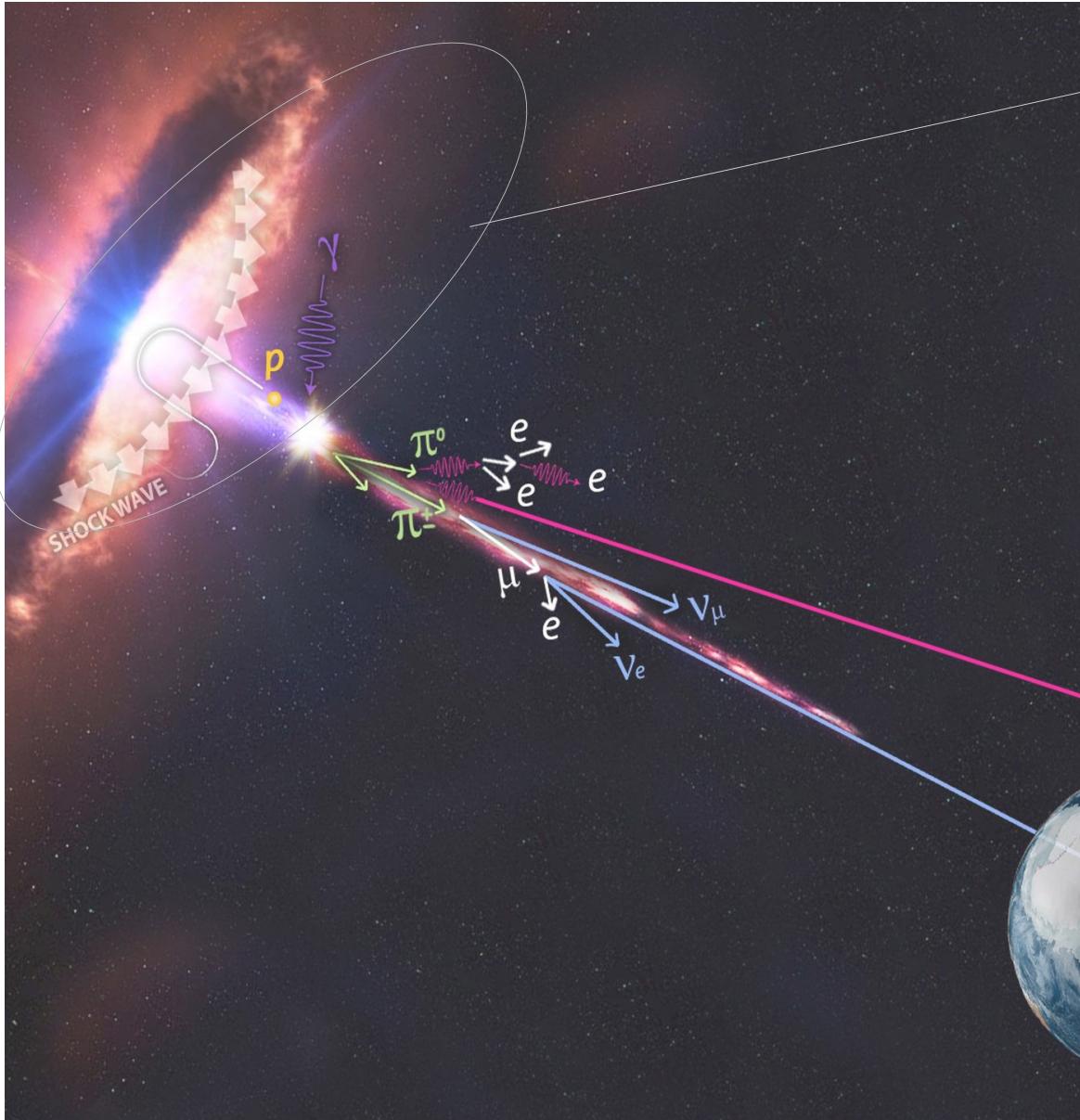
Sudipta Das

Institute of Physics, Bhubaneswar, India



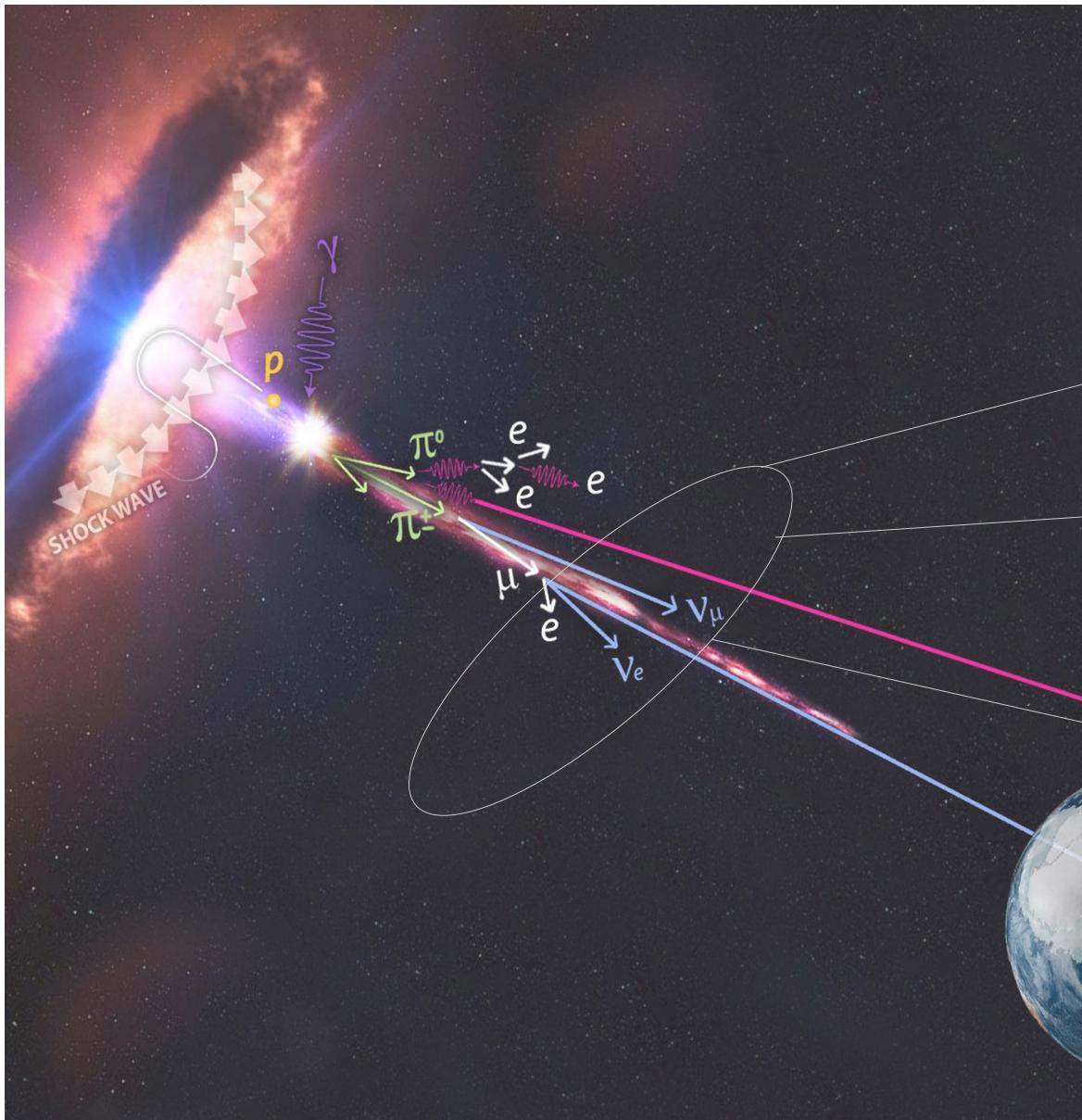
**NuFACT 2024**

# Introduction



AGN, Gamma ray bursts,  
Supernovae, Galaxy clusters...

# Introduction

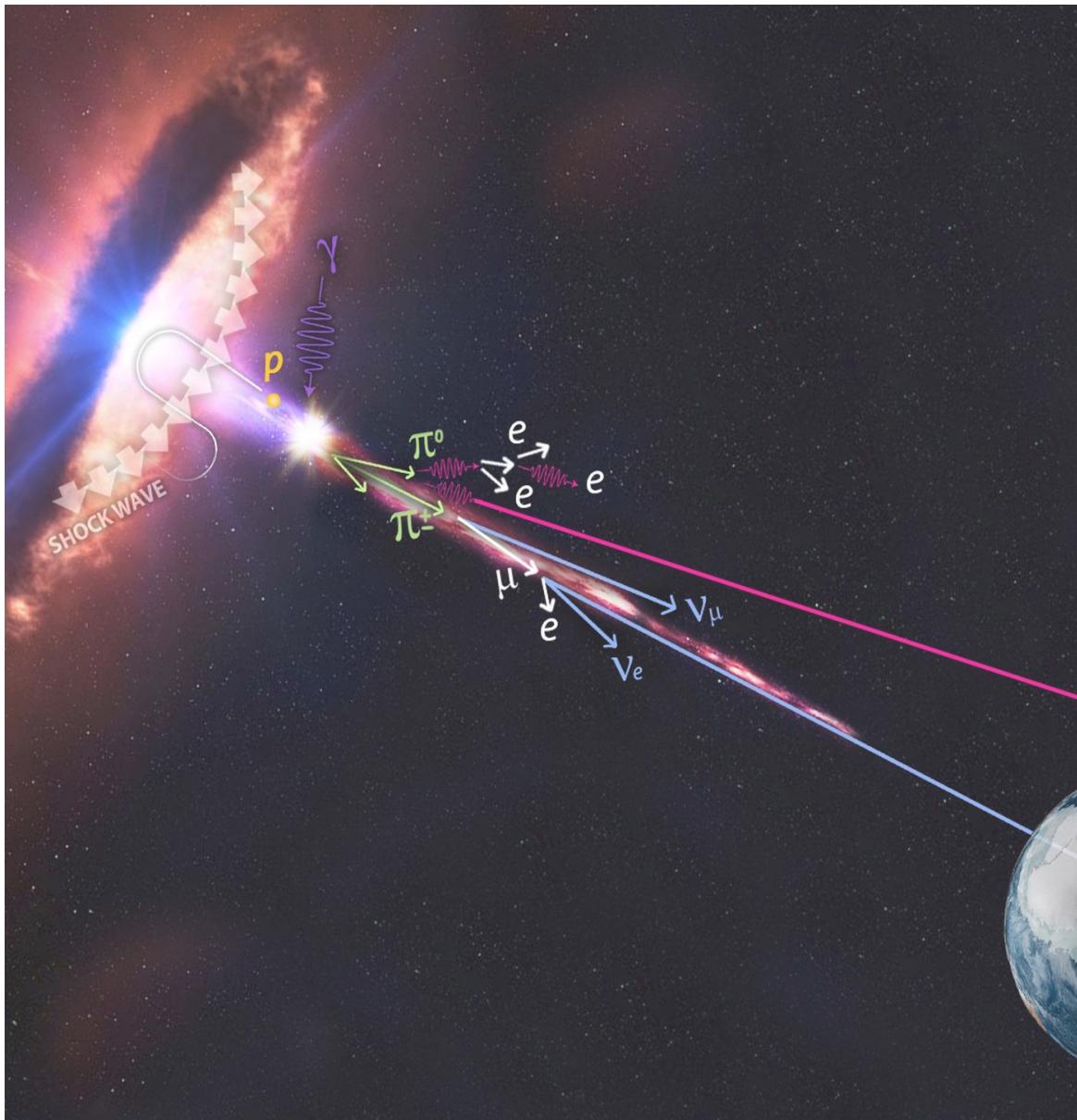


AGN, Gamma ray bursts,  
Supernovae, Galaxy clusters...

- TeV - EeV energy scale
- Highest energy among all sources
- MPC to GPC distances
- Travel longest distances
- Weakly interacting
- Travel almost straight from the source.

Excellent Messenger for various  
Astrophysical activities.

# Introduction



- Neutrino flavor oscillation

$$P_{\alpha\beta} = \left| \sum_{i=1}^3 U_{\alpha i} \exp \left[ -i \frac{\Delta m_{i1}^2 L}{2E} \right] U_{\beta i}^* \right|^2$$

$$\downarrow \quad \Delta m_{ij}^2 L / (2E) \gg 1$$

$$\bar{P}_{\alpha\beta} = \sum_{i=1}^3 |U_{\alpha i}|^2 |U_{\beta i}|^2$$

- Neutrino flavor compositions

$$(f_e : f_\mu : f_\tau)_S = (1 : 2 : 0)$$

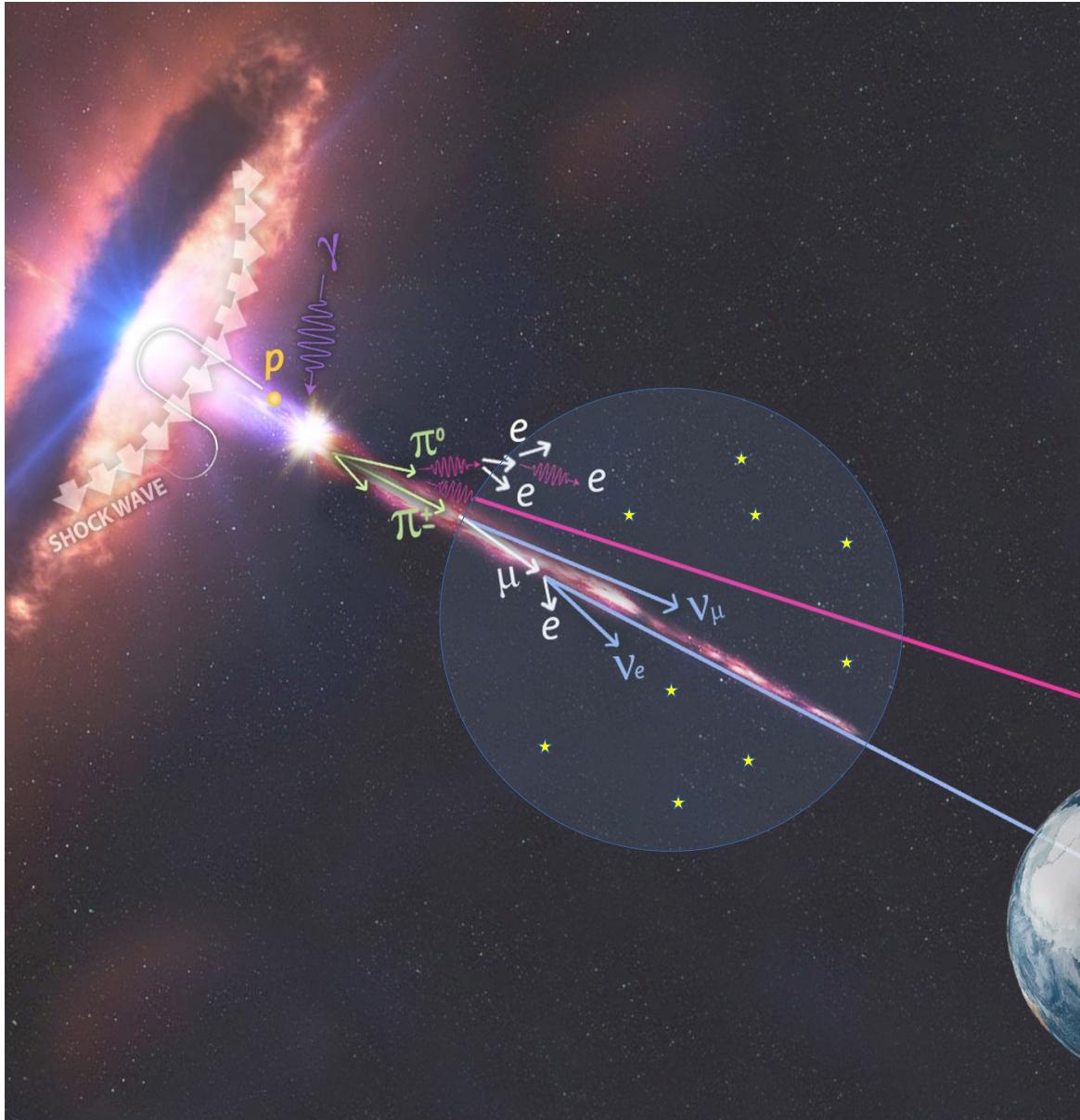
$$\downarrow \quad \bar{P}_{\beta\alpha} f_{\beta,S}$$

$$(f_e : f_\mu : f_\tau)_\oplus \approx (1 : 1 : 1)$$

Assumption:

Neutrino propagating in vacuum

# Introduction



Neutrino interaction with the surrounding matter

- Neutrino flavor oscillation

$$\bar{P}_{\alpha\beta}(U_{\alpha i}) \longrightarrow \bar{P}'_{\alpha\beta}(U_{\alpha i}, V, E_\nu)$$

- Neutrino flavor compositions

$$(f_e : f_\mu : f_\tau)_S = (1 : 2 : 0)$$

$$\downarrow \bar{P}_{\beta\alpha} f_{\beta,S}$$

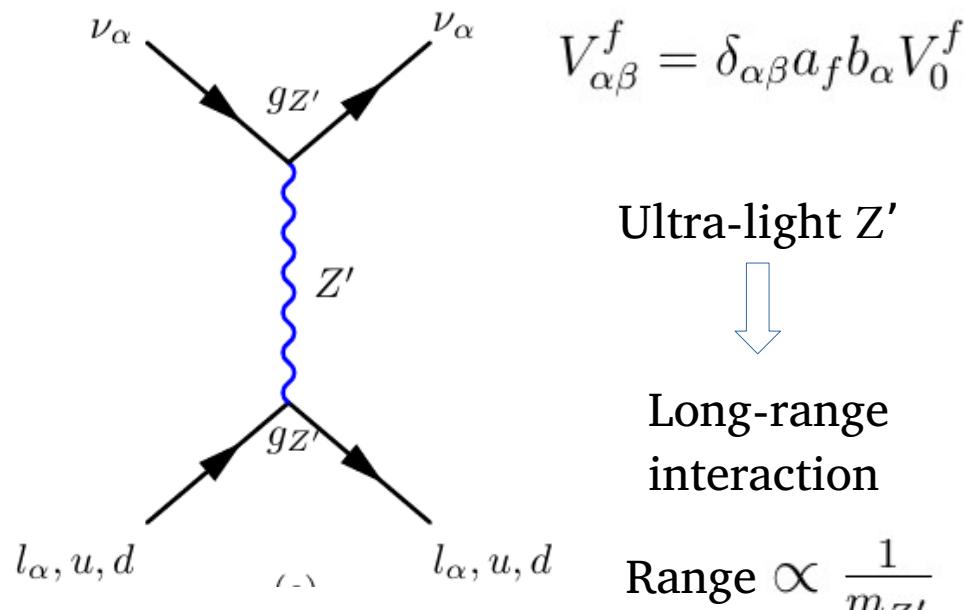
$$(f_e : f_\mu : f_\tau)_\oplus = x : y : z$$

- Deviation from the 1:1:1 may hint toward a new interaction

# Neutrino-matter interaction in Z' models

$$\text{SU}(3)_C \otimes \text{SU}(2)_L \otimes \text{U}(1)_Y \otimes \text{U}(1)'_X$$

$$\begin{aligned} \mathcal{L}_{Z'} = -g_{Z'} & \left( a_u \bar{u} \gamma^\alpha u + a_d \bar{d} \gamma^\alpha d + a_e \bar{e} \gamma^\alpha e \right. \\ & \left. + b_e \bar{\nu}_e \gamma^\alpha P_L \nu_e + b_\mu \bar{\nu}_\mu \gamma^\alpha P_L \nu_\mu + b_\tau \bar{\nu}_\tau \gamma^\alpha P_L \nu_\tau \right) Z'_\alpha \end{aligned}$$



Model (X)	$a_u$	$a_d$	$a_e$	$b_e$	$b_\mu$	$b_\tau$
$B - 3L_e$	$\frac{1}{3}$	$\frac{1}{3}$	-3	-3	0	0
$L - 3L_e$	0	0	-2	-2	1	1
$B - 3L_\mu$	$\frac{1}{3}$	$\frac{1}{3}$	0	0	-3	0
$L - 3L_\mu$	0	0	1	1	-2	1
$B - 3L_\tau$	$\frac{1}{3}$	$\frac{1}{3}$	0	0	0	-3
$L - 3L_\tau$	0	0	1	1	1	-2
$B - \frac{3}{2}(L_\mu + L_\tau)$	$\frac{1}{3}$	$\frac{1}{3}$	0	0	$-\frac{3}{2}$	$-\frac{3}{2}$
$L_e - L_\mu$	0	0	1	1	-1	0
$L_e - L_\tau$	0	0	1	1	0	-1
$L_e - \frac{1}{2}(L_\mu + L_\tau)$	0	0	1	1	$-\frac{1}{2}$	$-\frac{1}{2}$
$B_y + L_\mu + L_\tau$	$\frac{1}{3}$	$\frac{1}{3}$	0	0	1	1
$L_e + 2L_\mu + 2L_\tau$	0	0	1	1	2	2
$B - L_e - 2L_\tau$	0	0	0	0	1	-1

# Classifications of the Models

Flavor-dependent Interaction potential:  $V_{\alpha\alpha}^f \propto \frac{1}{2} a_f b_\alpha V_0^f$

Class - I

$$\begin{pmatrix} \bullet & & \\ & 0 & \\ & & 0 \end{pmatrix}$$

$$B - 3L_e$$

$$L - 3L_e$$

$$B - \frac{3}{2}(L_\mu + L_\tau)$$

$$L_e - \frac{3}{2}(L_\mu + L_\tau)$$

$$L_e + 2(L_\mu + L_\tau)$$

$$B_y + L_\mu + L_\tau$$

Class - II

$$\begin{pmatrix} 0 & & \\ & \bullet & \\ & & 0 \end{pmatrix}$$

$$\underbrace{\qquad}_{B - 3L_\mu}$$

$$\underbrace{\qquad}_{L - 3L_\mu}$$

Class - III

$$\begin{pmatrix} 0 & & \\ & 0 & \\ & & \bullet \end{pmatrix}$$

$$\underbrace{\qquad}_{B - 3L_\tau}$$

$$\underbrace{\qquad}_{L - 3L_\tau}$$

Class - IV

$$\begin{pmatrix} \bullet & & \\ & \bullet & \\ & & 0 \end{pmatrix}$$

$$\underbrace{\qquad}_{L_e - L_\mu}$$

Class - IV

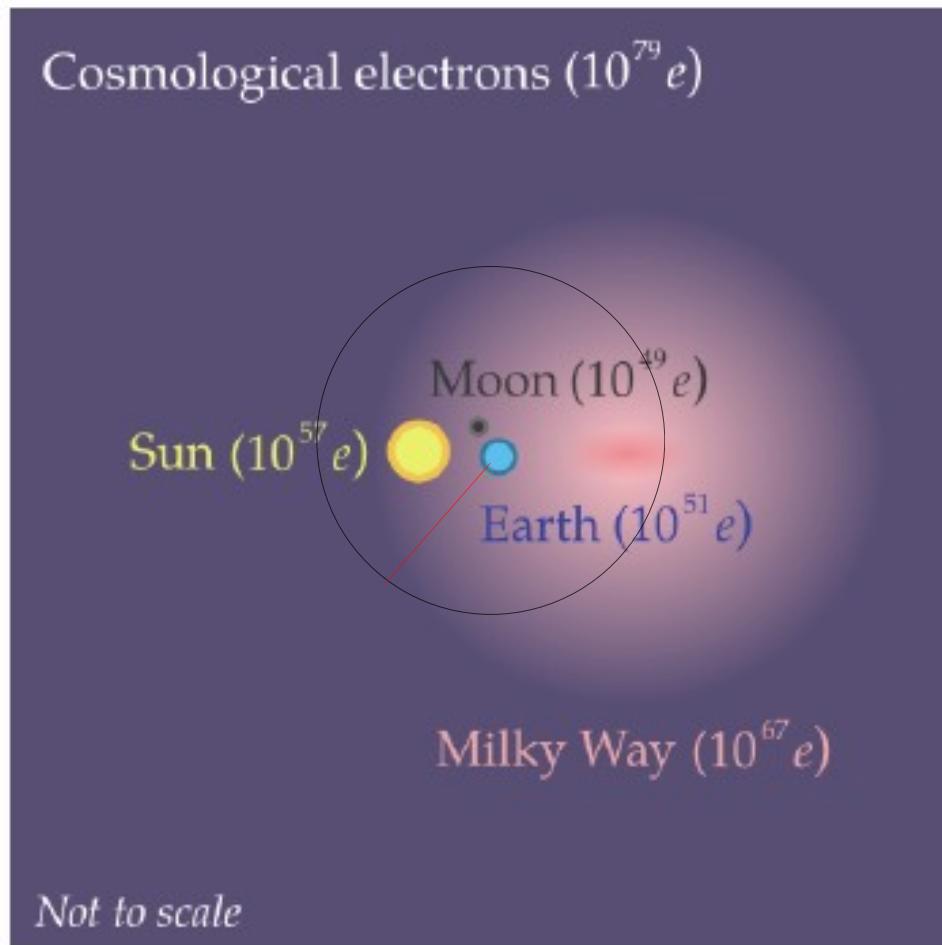
$$\left. \begin{pmatrix} \bullet & & \\ & 0 & \\ & & \bullet \end{pmatrix} \right\} L_e - L_\tau$$

Class - VI

$$\left. \begin{pmatrix} 0 & & \\ & \bullet & \\ & & \bullet \end{pmatrix} \right\} B - L_e - 2L_\tau$$

# Long-range neutrino matter interaction with U(1)' models

Matter particles inside the interaction range will contribute to the potential.



$$\text{Interaction range} \propto \frac{1}{m_{Z'}}$$

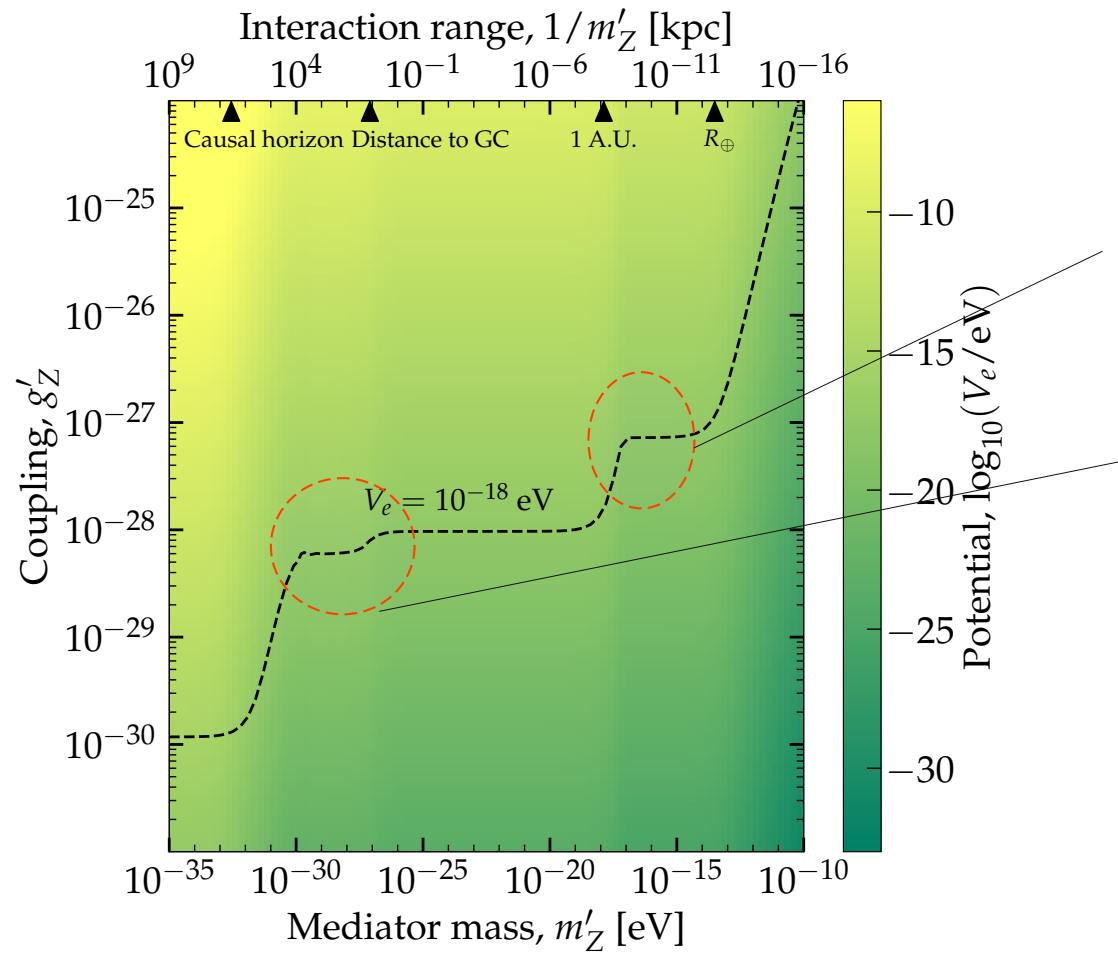
$$V_0^f = g_{Z'}^2 \frac{n_f}{4\pi d} e^{-m_{Z'} d}$$

$$V_f(m_{Z'}, G') = \left( V_f^{\oplus} + V_f^{\mathbb{C}} + V_f^{\odot} + V_f^{\text{MW}} + V_f^{\text{cos}} \right)$$

$$V_{\text{LRI},\alpha} = b_\alpha \sum_{f=e,p,n} a_f V_f(m_{Z'}, G')$$

Bustamante, Agarwalla, PRL, 2019

# Long-range neutrino matter interaction with U(1)' models



Inclusion of electrons in Sun

Electrons from Galactic Centre

# Neutrino flavor composition in the presence of long-range potential

- Neutrino propagation Hamiltonian

$$\mathbf{H} = \mathbf{H}_{\text{vac}} + \mathbf{V}_{\text{mat}} + \mathbf{V}_{\text{LRI}}$$

New potential

$$\mathbf{H}_{\text{vac}} = \frac{1}{2E} \mathbf{U} \text{ diag}(0, \Delta m_{21}^2, \Delta m_{31}^2) \mathbf{U}^\dagger , \quad \mathbf{V}_{\text{mat}} = \text{diag}(V_{\text{CC}}, 0, 0) ,$$

- Neutrino flavor transition probability  $\Delta \tilde{m}_{ij}^2 L / (2E) \gg 1$

$$\bar{P}_{\alpha\beta} = \sum_{i=1}^3 |U_{\alpha i}^m|^2 |U_{\beta i}^m|^2 . \quad U^m \rightarrow U^m(\theta_{23}^m, \theta_{13}^m, \theta_{12}^m, \delta^m) \xrightarrow{\text{Modified Mass-mixing parameters}}$$

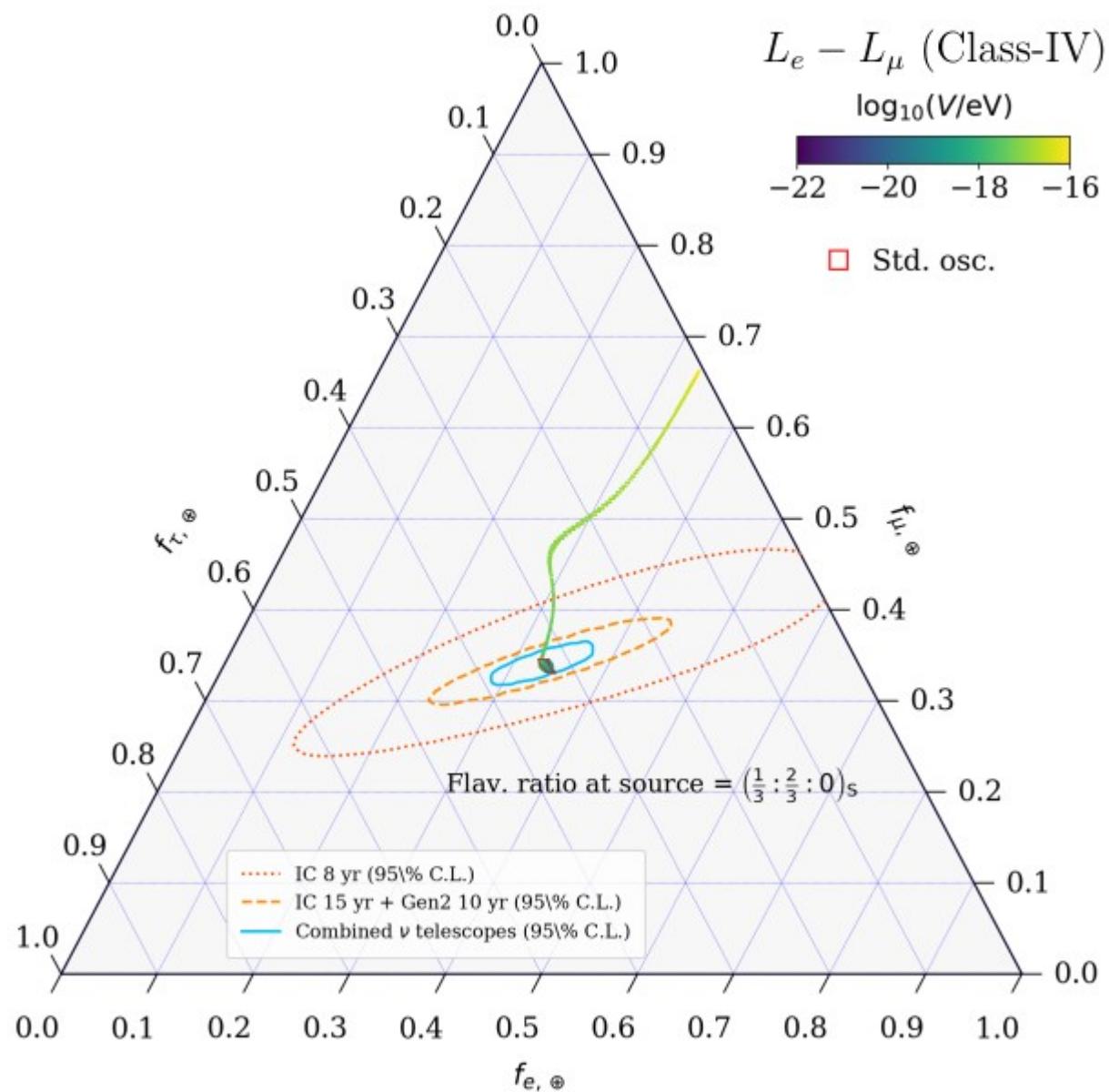
- Neutrino flavor composition at Earth

$$f_{\alpha, \oplus} = \sum_{\beta=e,\mu,\tau} \bar{P}_{\beta\alpha} f_{\beta,S} , \quad \begin{aligned} f_{\alpha, \oplus} &\rightarrow (f_e : f_\mu : f_\tau)_\oplus \\ f_{\alpha, S} &\rightarrow (f_e : f_\mu : f_\tau)_S \end{aligned}$$

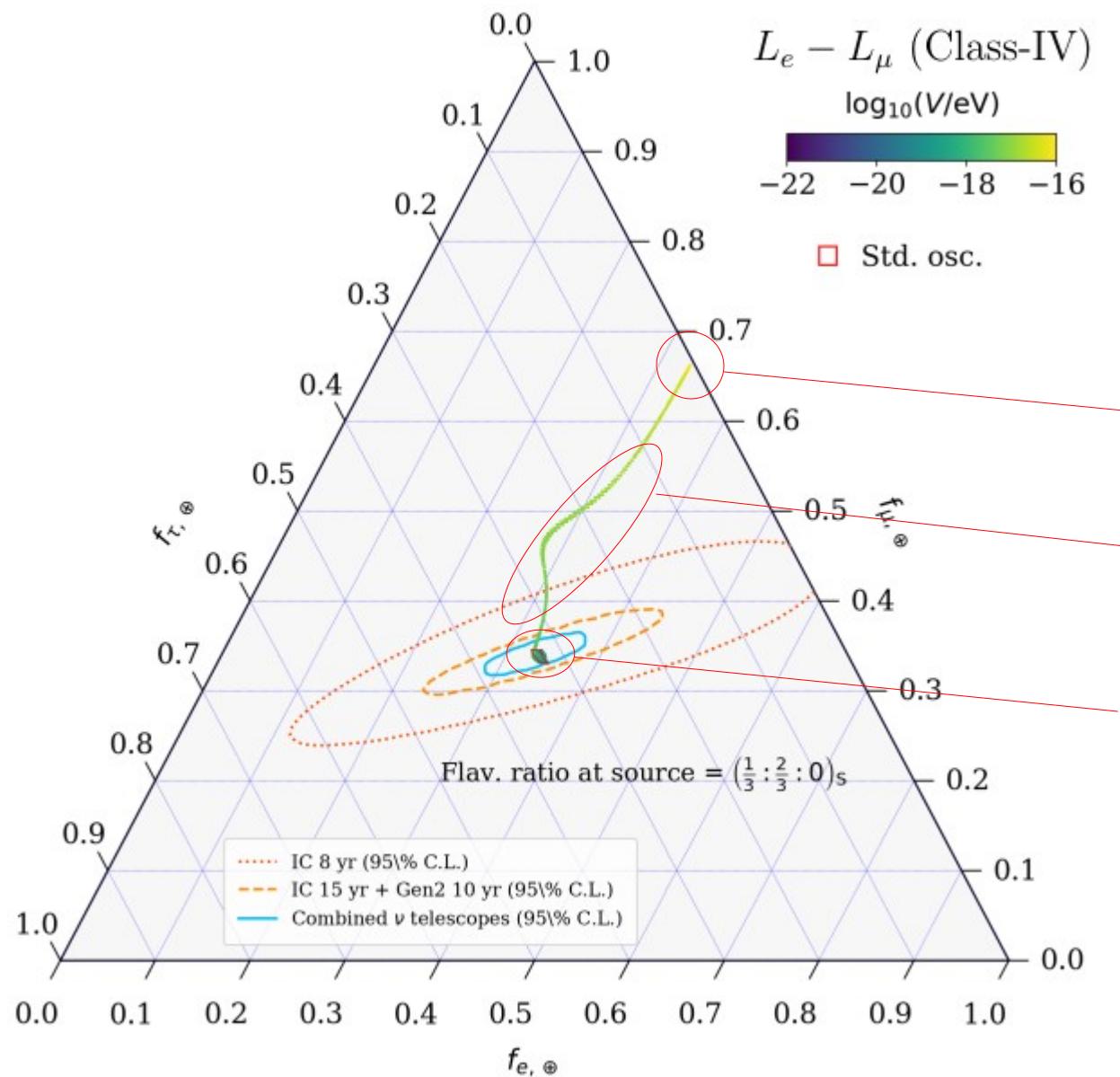
Assumed flavor  
composition  
At source

$$(f_e : f_\mu : f_\tau)_S = (1 : 2 : 0) \left\{ \begin{array}{l} \text{From } pp \text{ or } p\gamma \text{ collision} \\ \pi^+ \rightarrow \mu^+ + \nu_\mu \\ \mu^+ \rightarrow \bar{\nu}_\mu + e^+ + \nu_e \end{array} \right.$$

# Neutrino Flavor composition



# Neutrino Flavor composition

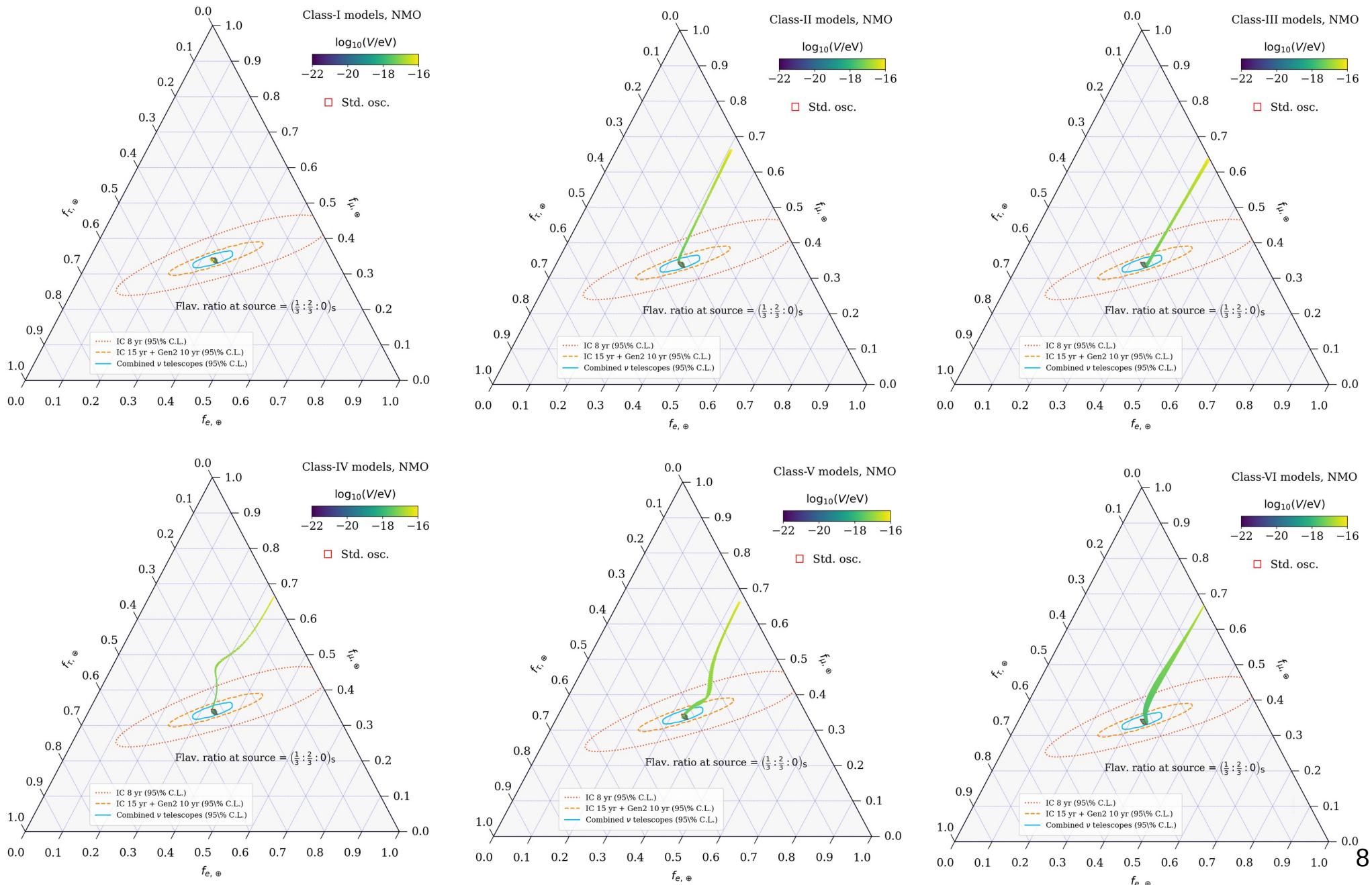


$$V_{\alpha\beta} \gg \Delta m_{ij}^2 / (2E)$$

$$V_{\alpha\beta} \sim \Delta m_{ij}^2 / (2E)$$

$$V_{\alpha\beta} \ll \Delta m_{ij}^2 / (2E)$$

# Neutrino Flavor composition



# Statistical Analysis

- Posterior probability density of the long-range potential :

$$\mathcal{P}(V_{\alpha\beta}) = \int d\vartheta \mathcal{L}(\langle \mathbf{f}_\oplus(V_{\alpha\beta}, \vartheta) \rangle) \pi(\vartheta) \pi(V_{\alpha\beta}).$$

$$\vartheta \equiv (\sin^2 \theta_{12}, \sin^2 \theta_{23}, \sin^2 \theta_{13}, \delta_{CP}) , \quad \langle \mathbf{f}_\oplus \rangle \equiv (\langle f_{e,\oplus} \rangle, \langle f_{\mu,\oplus} \rangle, \langle f_{\tau,\oplus} \rangle)$$

- Estimated and projected neutrino flavor composition from neutrino telescopes

Observation epoch	Neutrino telescopes	Neutrino mixing parameters
2020 (estimated)	IC 8 yr	NuFit 5.1 (2021)
2040 (projected)	IC 15 yr + IC-Gen2 10 yr	NuFit 5.1 + JUNO + DUNE + HK
2040 (projected)	Combined $\nu$ telescopes	NuFit 5.1 + JUNO + DUNE + HK

*Song, Li, Arguelles, Bustamante, Vincent, 2020*

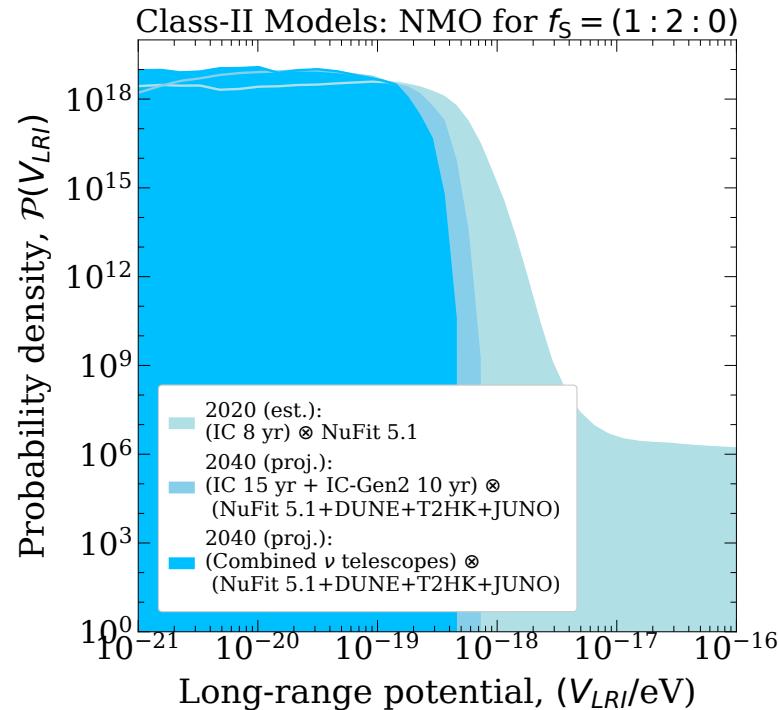
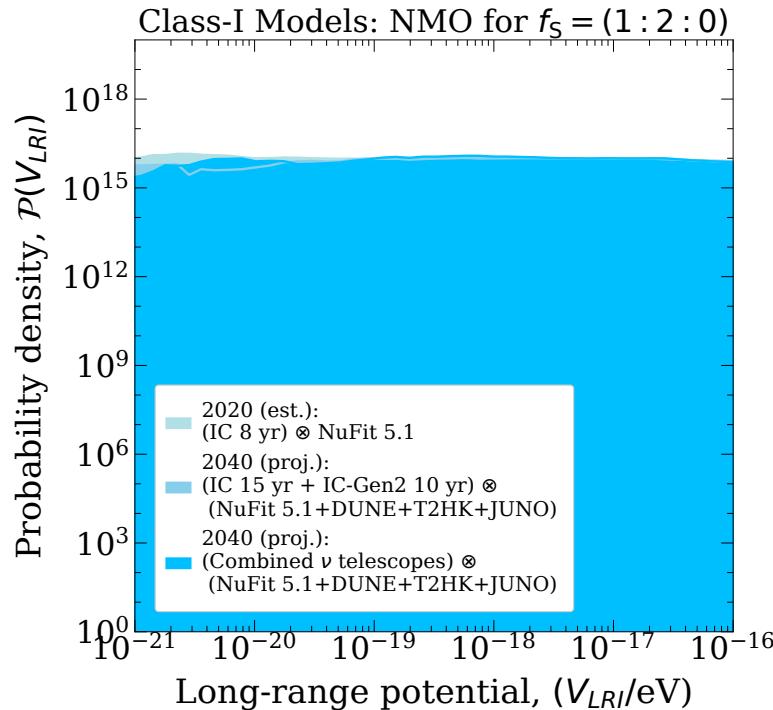
IC 8 yr : estimated through-going + HESE events at IceCube

IC + IC-Gen2 : projected 15 yr IceCube + 10 yr IceCube-Gen2 10 yr

Combined telescopes : projected data from IceCube+Gen2+KM3NeT  
+GVD+P-ONE+TAMBO

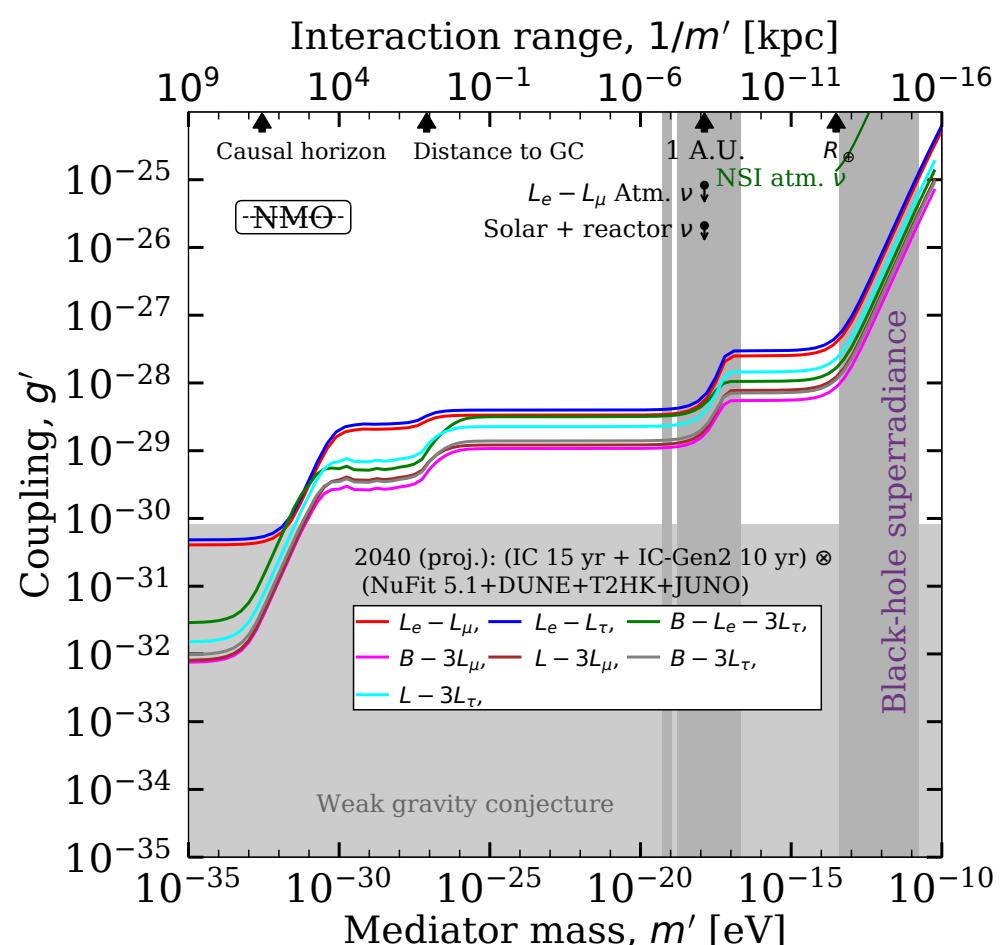
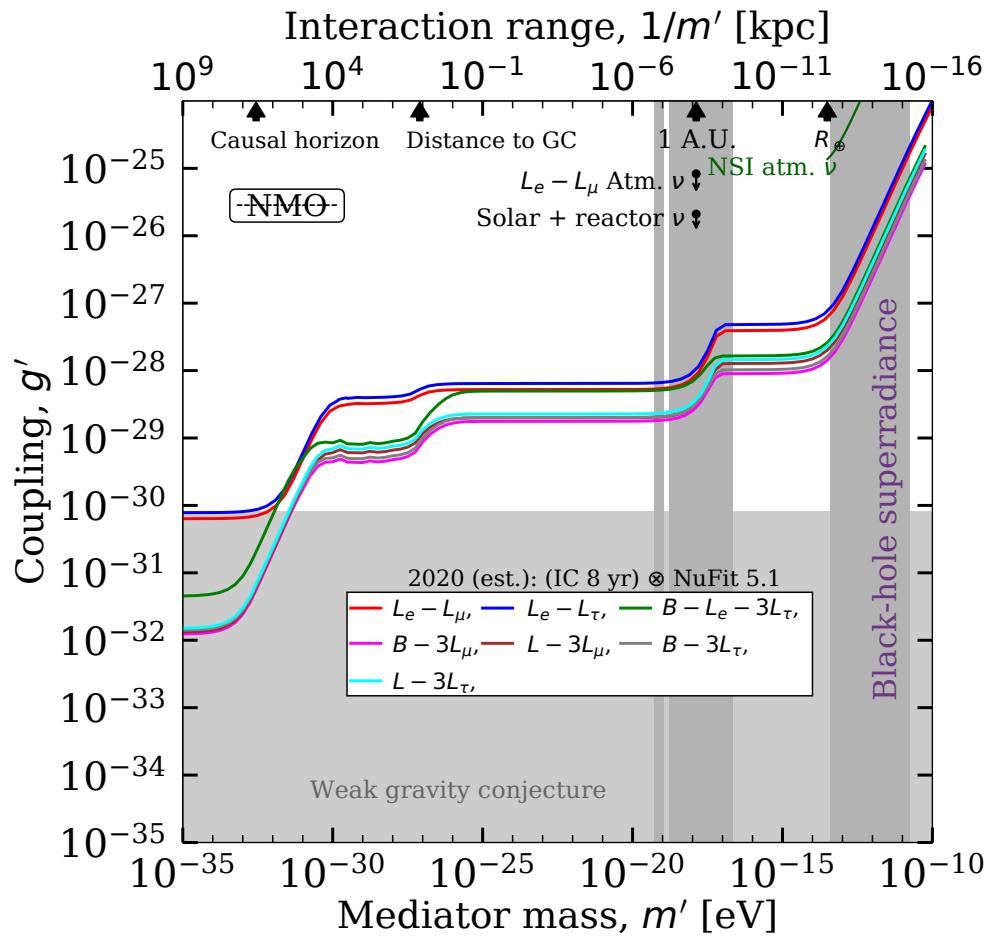
Improvements in  
 $\theta_{12}, \theta_{23}, \delta_{CP}$

# Constraints on long-range potential



Models	Upper limit (95% C.L.) on potential [ $10^{-19}$ eV]		
	IC 8 yr	IC 15 yr + Gen2 10 yr	Combined $\nu$ telescopes
Class - I	—	—	—
Class-II	3.20	1.19	1.04
Class-III	4.16	1.99	1.76
Class-IV	3.11	1.11	1.08
Class-V	4.41	1.69	1.63
Class-VI	1.79	0.731	0.702

# Constraints in coupling-mass plane



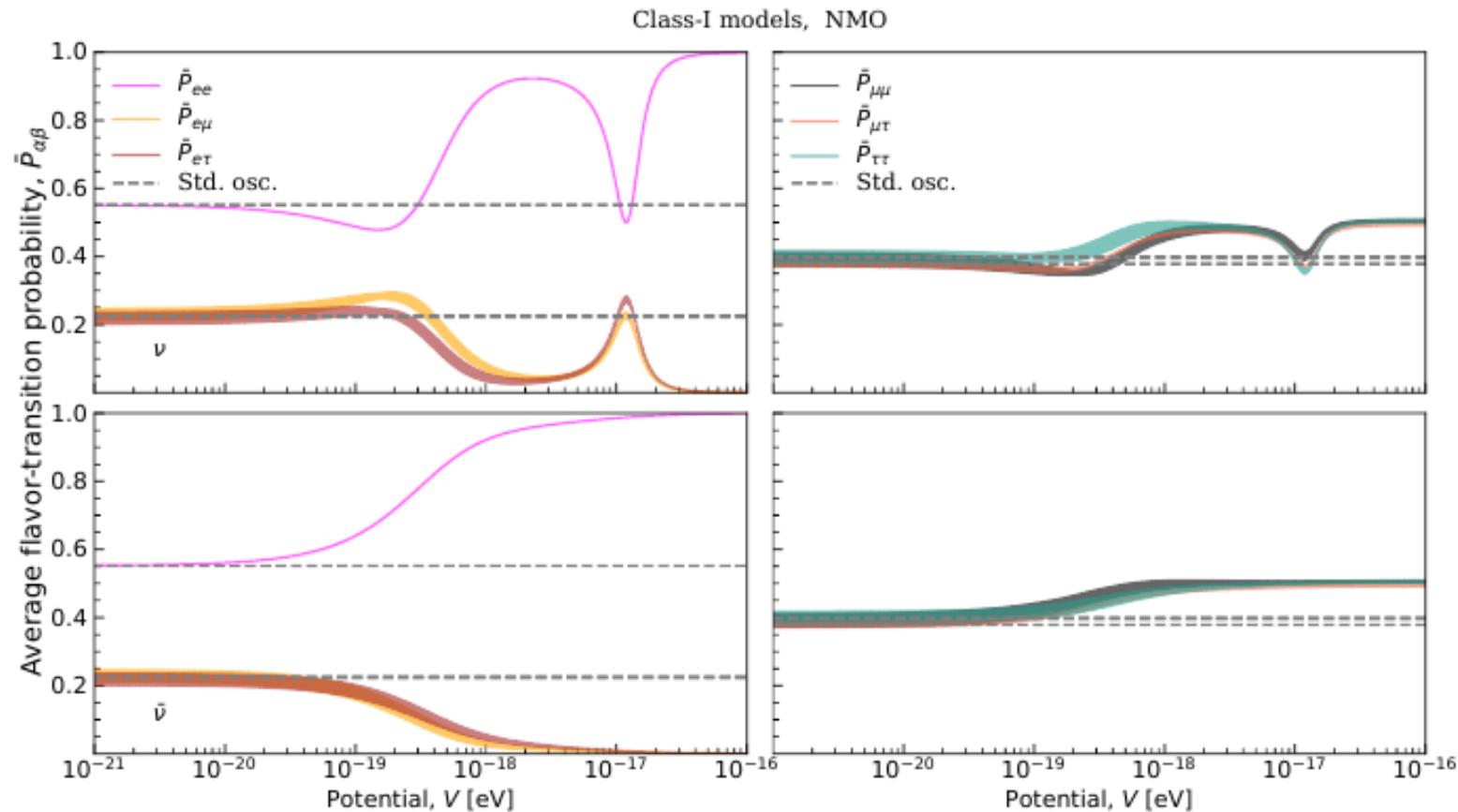
Work under progress...  
Sanjib Kumar Agarwalla, SD, Ashish Narang

# Summary

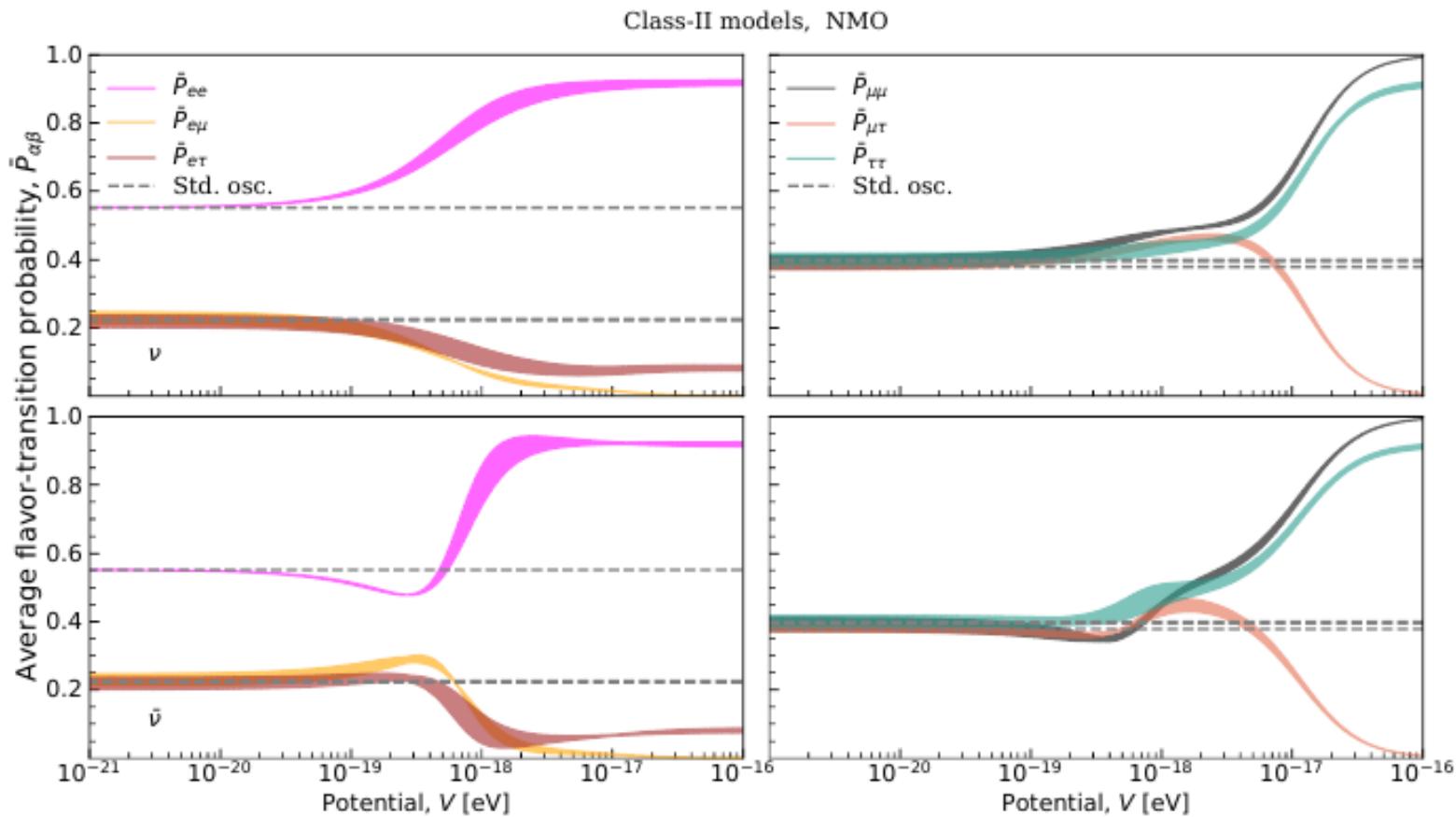
- We probe the possible new neutrino-matter long-range interactions (LRI) induced by anomaly-free  $U(1)'$  models.
- Neutrino flavor composition estimates from IceCube and other neutrino telescopes can constrain certain models.
- We find that using the estimated current flavor sensitivity of IceCube and current mixing parameter uncertainties, high-energy astrophysical neutrinos could tightly constrain long-range interactions, surpassing existing limits.

Thank You

# Back-up slides



# Back-up slides



# Back-up slides

**IceCube 8 yrs estimates (year 2020)** : Estimated sensitivity to flavor composition using HESE+through going events in IceCube.

**IceCube 15yrs + Gen2 10 yrs projections (year 2040)** : 15 years projected sensitivity of IceCube and 10 years projected sensitivity of IceCube-Gen2 using HESE and through going events.

**Projected data from the combined telescopes (year 2040)** : Apart from IceCube-Gen2, the next generation neutrino telescopes used for our analysis are KM3NeT, GVD, P-ONE, and TAMBO.

- 2040 projections for the other neutrino telescopes based on the projections for IceCube-Gen2.

$$\ln \mathcal{L}_{\text{comb.}} = \Xi_S \ln \mathcal{L}_{\text{Gen2-10yr}} + \ln \mathcal{L}_{\text{IC-15 yr}} + \ln \mathcal{L}_{\text{TAMBO}}$$

$$\Xi_S = \frac{\Xi_{\text{Gen2-10yr}} + \Xi_{\text{KM3NeT}} + \Xi_{\text{GVD}} + \Xi_{\text{P-ONE}}}{\Xi_{\text{Gen2-10yr}}}$$

$$-2 \ln \mathcal{L}_{\text{TAMBO}} = \frac{(N_{\nu_\tau} - \bar{N}_{\nu_\tau})^2}{\bar{N}_{\nu_\tau}}$$

$$\Xi_{\text{Gen2-10yr}} = 81.6 \text{ km}^3 \text{ yr}$$

$$\Xi_{\text{KM3NeT}} = 42.1 \text{ km}^3 \text{ yr}$$

$$\Xi_{\text{GVD}} = 24.3 \text{ km}^3 \text{ yr}$$

$$\Xi_{\text{P-ONE}} = 31.6 \text{ km}^3 \text{ yr}$$

# Back-up slides

- **Alternative flavor composition choices** : We use only one canonical choice of the flavor ratio at source,  $(1 : 2 : 0)_S$ . Our methods are general and applicable also for other choices of flavor ratio at the source.
- **Energy dependence of the flavor composition** : Our analysis is based on the estimated flavor composition at Earth, assuming it is energy independent. In principle, it can be energy dependent.
- **Computing neutrino propagation** : We compute the long-range matter potential at the location where the neutrinos are detected, at IceCube. Potential can be calculated for each point of the propagating neutrinos along the trajectory.
- **Flavor-measurement capabilities of upcoming detectors** : Our forecasts for the upcoming neutrino telescopes assume the capabilities to measure the flavor composition will be similar to those of IceCube. This is a necessary assumption, given the absence of their realistic capabilities.