

# Implementation of new beam focusing systematics within the PRISM Analysis

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*on behalf of DUNE – PRISM working group*

DUNE Collaboration Meeting

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# Incorporation of beam focusing uncertainties (v3r5p9 release of G4LBNE) within PRISM Analysis

- Focusing uncertainties:
  - the position, geometry, and composition of the beamline components (horns, target, decay pipe, etc)
  - the current or water layer in each horn
  - the geometry of the incident proton beam
- Previous flux focusing systematics (Nov 17) are incomplete and include only 2 horns
- New (not present in the previous releases) uncertainties:
  - tilt of target, horns, decay pipe
  - horns' inner conductor deformations
  - major updates to the decay pipe geometry and positioning

Parameter	1 $\sigma$ Shift	Notes
Proton Beam Transverse X Proton Beam Transverse Y Proton Beam Angle X	0.5 mm 0.5 mm $\delta\theta = 70 \mu\text{rad}$ $\Phi = 0, \pi$	Interaction Position. Updated to 0.5 mm from 4.5 mm in TDR Proton Beam Angle on target Target Interaction Point fixed to center of target
Proton Beam Angle Y Proton Beam Radius	$\delta\theta = 70 \mu\text{rad}$ $\Phi = \pm\pi/2$ 10% (0.27 mm)	Updated from 1% in the TDR. Change X&Y sigmoid simultaneously
Target Density Upstream Target Degredation	2% (0.0356 g/cm <sup>3</sup> ) 5 mm loss	Approximate target degradation Assume complete loss of target on upstream end; basically a shorter target (by dz) shifted downstream by the loss dz
Target Displace Transverse X Target Displace Transverse Y Target Tilt Transverse X Target Tilt Transverse Y Target Length Horn Currents	0.5 mm 0.5 mm 0.5 mm 0.5 mm 1.5 mm (0.01%) 1% (3 kA)	Arbitrarily assumed tolerance Simultaneously change to all 3 Horns; nominal = 300 kA
Horn Water Layer Thickness	0.5 mm	Simultaneous change to all 3 Horns; nominal = 1 mm. Cannot go below 0
Horn A Displace Transverse X Horn A Displace Transverse Y Horn A Displace Longitudinal Z Horn A Tilt Transverse X Horn A Tilt Transverse Y Horn A Eccentricity X Induced B Field	0.5 mm 0.5 mm 2.0 mm 0.5 mm 0.5 mm 0.035 mm	Upstream and downstream ends shifted in opposite directions by tolerance value Horn A Inner conductor eccentricity: Eccentric (off axis) deformation of inner conductor; induced dipole field in y in field-free region. NuMI Horn 1 tolerance assumed
Horn A Ellipticity X Induced B Field	0.120mm	Elliptical deformation of inner conductor; induced quadrupole field in x-y in field-free region; NuMI Horn1 tolerance assumed
Horn B Displace Transverse X Horn B Displace Transverse Y Horn B Displace Longitudinal Z Horn B Tilt Transverse X Horn B Tilt Transverse Y Horn B Ellipticity X Induced B Field	0.5 mm 0.5 mm 3.0 mm 0.5 mm 0.5 mm 0.180 mm	Upstream and downstream ends shifted in opposite directions by tolerance value NuMI Horn 2 tolerance assumed
Horn C Displace Transverse X Horn C Displace Transverse Y Horn C Displace Longitudinal Z Horn C Tilt Transverse X Horn C Tilt Transverse Y Horn C Eccentricity X Induced B Field Horn C Ellipticity X Induced B Field	0.5 mm 0.5 mm 3.0 mm 0.5 mm 0.5 mm 0.07 mm 0.180 mm	NuMI horn 2 tolerance assumed NuMI horn 2 tolerance assumed
Decay Pipe Radius Decay Pipe Length	2.0 cm 2.5 cm	Changed from 10 cm; nominal = 2 m Same as elongating, since the distance between decay pipe upstream is fixed
Decay Pipe Displace Transverse X Decay Pipe Displace Transverse Y Decay Pipe Tilt X _ DSOA Decay Pipe Tilt Y _ DSOA Decay Pipe Elliptical Cross section X (A) Decay Pipe Elliptical Cross section Y (B)	2.5 cm 2.5 cm 2.5 cm 2.5 cm 2.5 cm 2.5 cm	Downstream (DS) end fixed to remain on axis  Ellipse with A (X-axis) or B (y-axis) varied by tolerance, while other dimension fixed to nominal radius
Decay Pipe Geo B Field	1	Scale-factor value to 1 is 1 $\sigma$ tolerance. Mapped from NuMI decay pipe geo B-field measurements
Decay Pipe Segmented Bowing X Decay Pipe Segmented Bowing X	2.5 cm 2.5 cm	Decay Pipe segmented in 3 equal pieces; central piece transverse shifted by tolerance

# Incorporation of beam focusing uncertainties (v3r5p9 release of G4LBNE) within PRISM Analysis

- Use flux systematics provided by P. Weatherly (/pnfs/dune/persistent/users/pweather/fluxfiles/g4lbne/v3r5p9/QGSP\_BERT/)
  - nominal: OfficialEngDesignSept2021/neutrino/flux
  - shift: OEDS21\_HornADisplaceTransverseX\_pos\_1\_sigma/neutrino/flux

## • ND files – Flux vs Off Axis vs Neutrino Energy

Rebin for PRISM Analysis needs  
(diff E binning for diff OA bins)

**Apply the systematics to ND data**  
– Check how the **fractional shift**  
( $1\sigma$  Shift– Nominal) /Nominal looks in **ND data**  
as a function of **Off-axis position vs True  $E_\nu$**

Linearly combine nominal  
ND data and  $n\sigma$  shifted ND data

**Fractional shift** (Lin. Comb.  $1\sigma$  Shifted ND data – Lin. Comb Nominal ND data) / Nominal  
**of PRISM Prediction vs energy**

## • FD files – Flux vs Neutrino energy

Rebin in E for PRISM Analysis needs

**Apply the systematics to FD data**  
– Check how the **fractional shift**  
( $1\sigma$  Shift– Nominal) /Nominal looks in  
**FD data vs energy**

### 1. Compare **FD Fractional** and **PRISM Fractional**:

if different → flux parameter expected to have high impact on the PRISM sensitivity  
(IMPORTANT parameter)

# Incorporation of beam focusing uncertainties (v3r5p9 release of G4LBNE) within PRISM Analysis

- Use flux systematics provided by P. Weatherly (/pnfs/dune/persistent/users/pweather/fluxfiles/g4lbne/v3r5p9/QGSP\_BERT/)
  - nominal: OfficialEngDesignSept2021/neutrino/flux
  - shift: OEDS21\_HornADisplaceTransverseX\_pos\_1\_sigma/neutrino/flux

## • ND files – Flux vs Off Axis vs Neutrino Energy

Rebin for PRISM Analysis needs  
(diff E binning for diff OA bins)

### Apply the systematics to ND data

- Check how the **fractional shift** ( $1\sigma$  Shift– Nominal) /Nominal looks in **ND data** as a function of **Off-axis position vs True  $E_\nu$**

Linearly combine nominal  
ND data and  $n\sigma$  shifted ND data

**PRISM linear combination (@ $n\sigma$ ) energy**

## • FD files – Flux vs Neutrino energy

Rebin in E for PRISM Analysis needs

### Apply the systematics to FD data

- Check how the **fractional shift** ( $1\sigma$  Shift– Nominal) /Nominal looks in **FD data vs energy**

2. **Apply corresponding systematics** (each parameter at a time) to the PRISM Analysis and evaluate the **oscillation parameter sensitivity**

# New Flux Systematics – September 2021

September 2021: 45 flux parameters (beam systs)

→ Investigate the effect each individual parameter has on the PRISM oscillation analysis

**10 IMPORTANT** (influence the sensitivity significantly)

**8 SEMI** (influence the oscillation fit much less)

**27 NEGLIGIBLE** (negligible effect on the oscillation fit)

- Analysis variable **is reconstructed neutrino energy**: EnuReco

→ all of the presented results are obtained by using EnuReco unless stated otherwise

## September 2021 flux focusing parameters

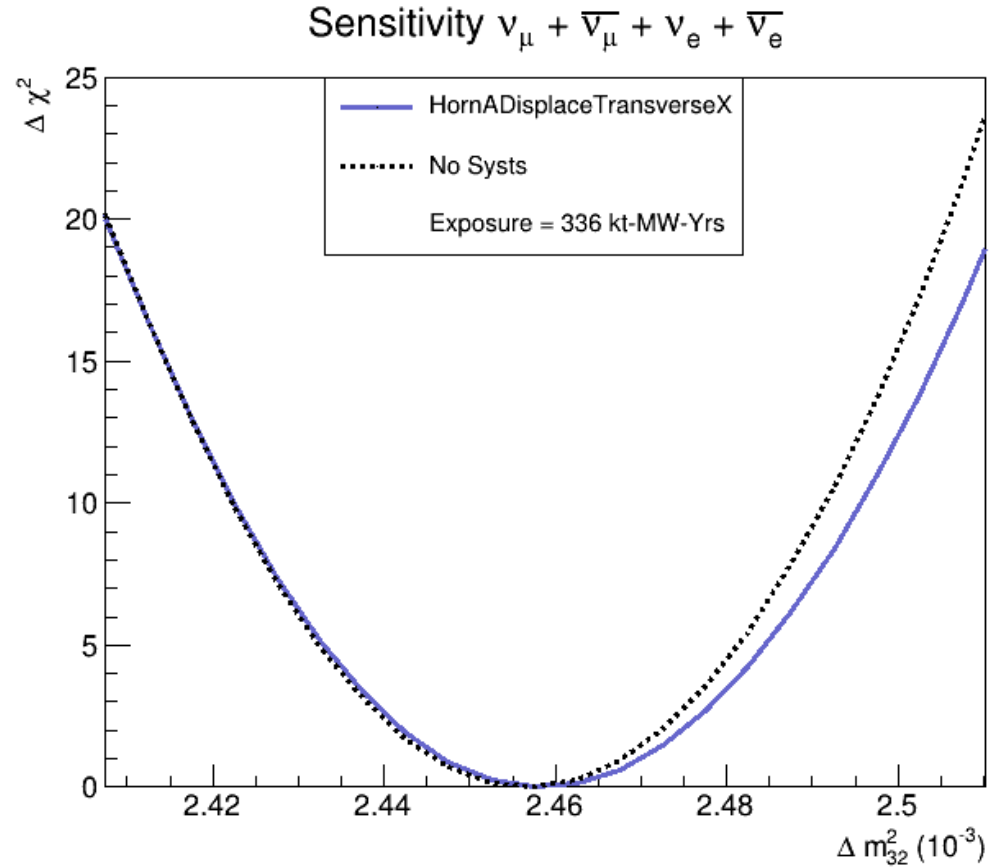
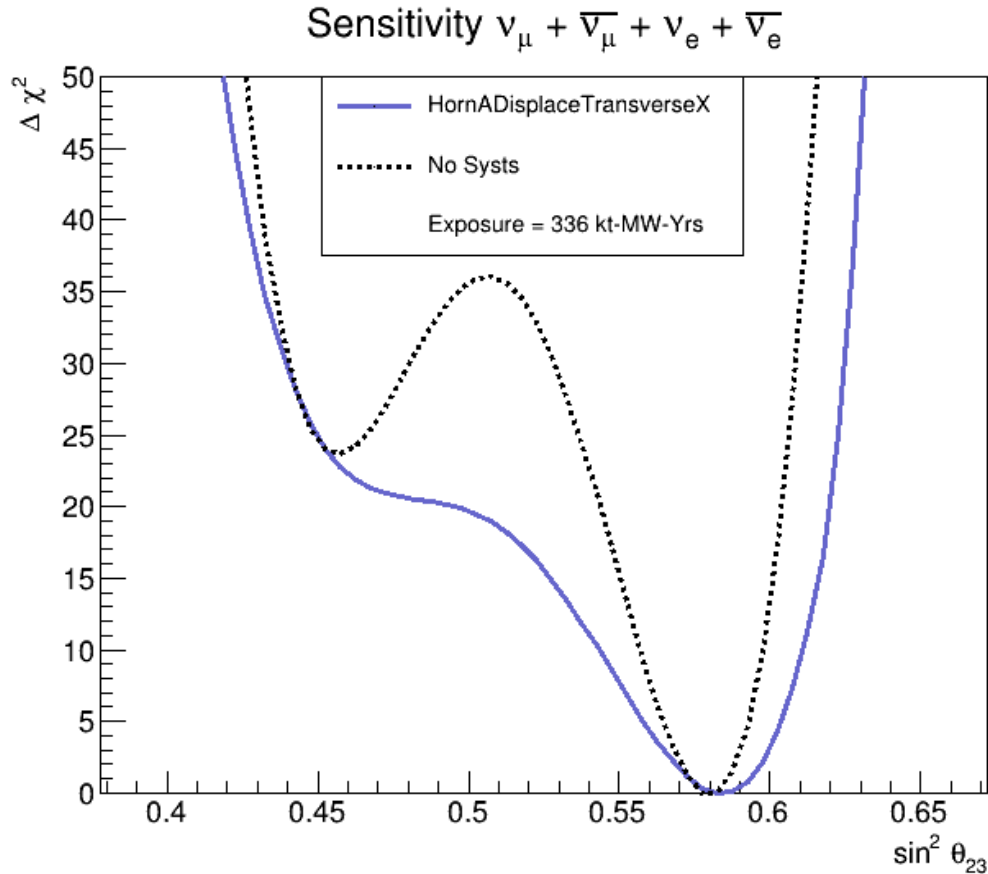
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" HornBDisplaceTransverseX "	" HornBTiltTransverseX "
" HornCDisplaceTransverseX "	" HornBTiltTransverseY "
" HornADisplaceTransverseY "	" HornCDisplaceLongitudinalZ "
" HornBDisplaceTransverseY "	" HornCEccentricityXInducedBField "
" HornCDisplaceTransverseY "	" HornCEllipticityXInducedBField "
" DecayPipe3SegmentBowlingX "	" HornCTiltTransverseX "
" DecayPipe3SegmentBowlingY "	" HornCTiltTransverseY "
" DecayPipeDisplaceTransverseX "	" HornCurrent "
" DecayPipeDisplaceTransverseY "	" HornWaterLayerThickness "
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" DecayPipeEllipticalCrossSectionYB "	" ProtonBeamAngleY "
" DecayPipeGeoBField "	" ProtonBeamRadius "
" DecayPipeLength "	" ProtonBeamTransverseX "
" DecayPipeRadius "	" ProtonBeamTransverseY "
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" DecayPipeTiltY_DSOA "	" TargetDisplaceTransverseX "
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" HornAEllipticityXInducedBField "	" TargetTiltTransverseX "
" HornATiltTransverseX "	" TargetTiltTransverseY "
" HornATiltTransverseY "	" TargetUpstreamDegredation "
" HornBDisplaceLongitudinalZ "	

\* temporary classification (some of important parameters might be considered semi in the end)

# Horn A Displace Transverse X

**IMPORTANT**

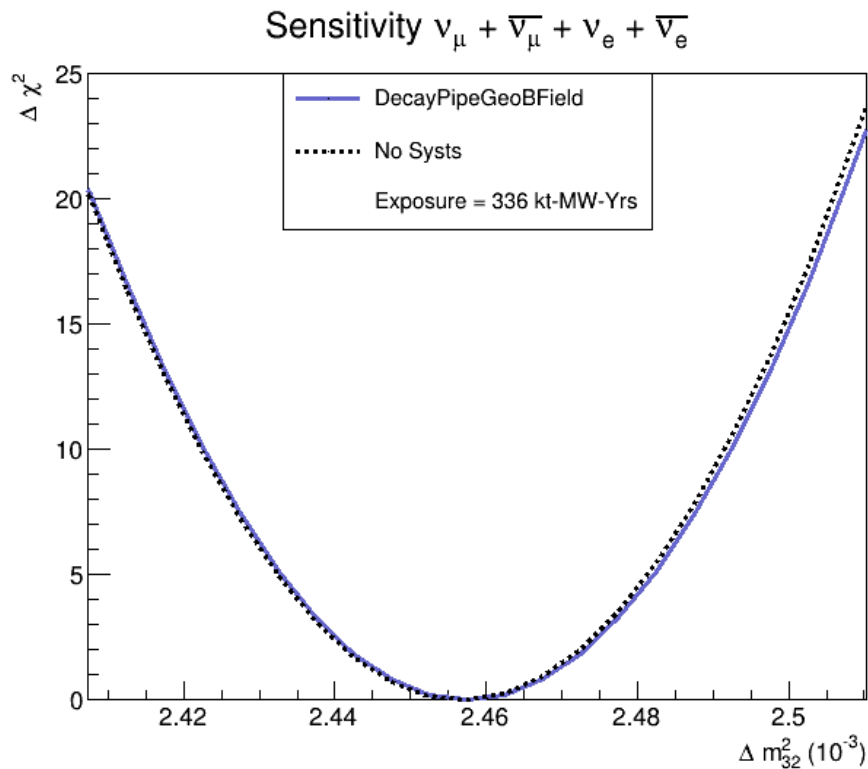
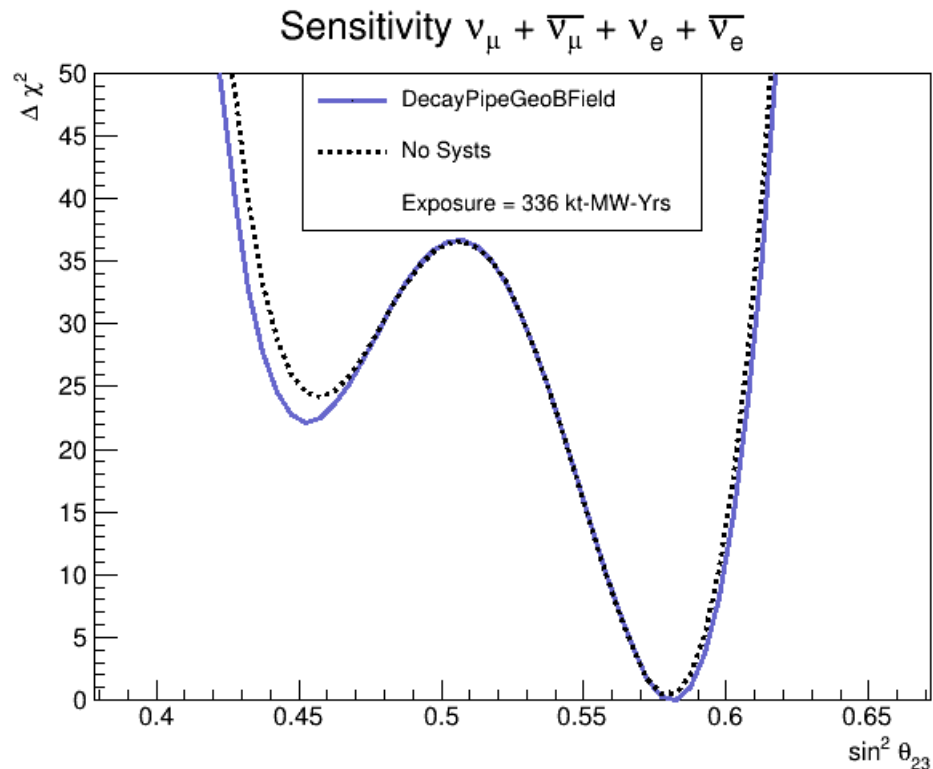
-  $1\sigma$  shift = 0.5 mm



# Decay Pipe Geo BField

SEMI

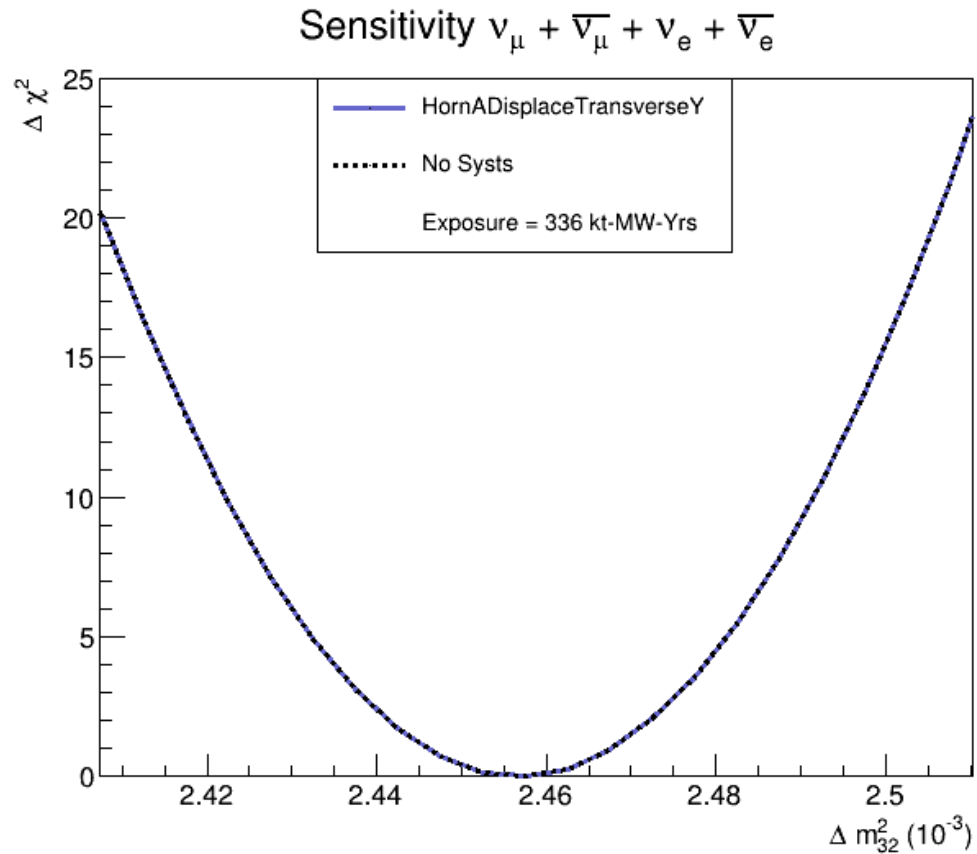
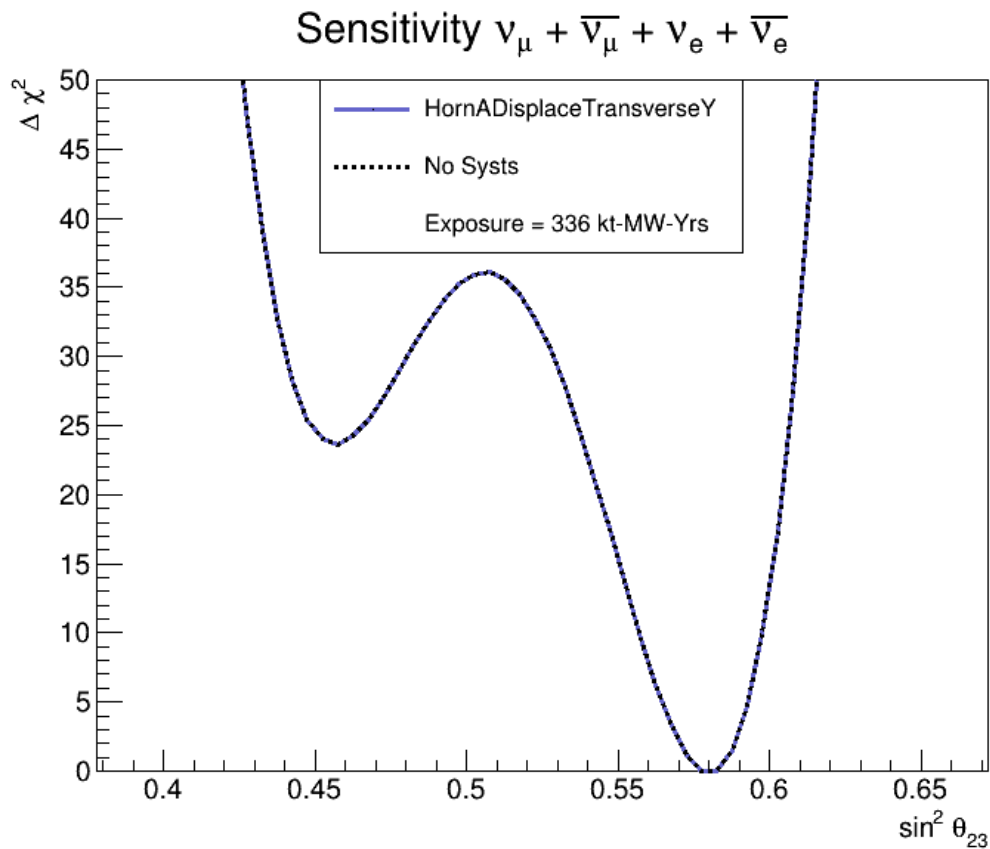
-  $1\sigma$  shift = 1: scale factor value of 1 is  $1\sigma$  tolerance  
(mapped from NuMI Decay Pipe Geo Bfield measurements)



# Horn A Displace Transverse Y

NEGLIGIBLE

-  $1\sigma$  shift = 0.5 mm





# New Flux Systematics (Sept 21) – Important parameters

**10 IMPORTANT** parameters: influence the sensitivity significantly

- HornADisplaceTransverseX → 1  $\sigma$  shift = 0.5 mm
- HornBDisplaceTransverseX → 1  $\sigma$  shift = 0.5 mm
- HornCDisplaceTransverseX → 1  $\sigma$  shift = 0.5 mm
- HornAEccentricityXInducedBField → 1  $\sigma$  shift = 0.035 mm
- HornATiltTransverseX → 1  $\sigma$  shift = 0.5mm
- HornCEccentricityXInducedBField → 1  $\sigma$  shift = 0.07 mm
- HornCurrent → 1  $\sigma$  shift = 3 kA (1%)
- HornWaterLayerThickness → 1  $\sigma$  shift = 0.5 mm
- ProtonBeamTransverseX → 1  $\sigma$  shift = 0.5 mm
- TargetUpstreamDegredation → 1  $\sigma$  shift = 5 mm

- New uncertainties (not present in TDR): Horn C Displace Transverse, Eccentricity X (both A and C), Horn Tilt (horn A), target upstream degradation

# New Flux Systematics (Sept 21) – Important parameters

**10 IMPORTANT** parameters: influence the sensitivity significantly

- HornADisplaceTransverseX → 1  $\sigma$  shift = 0.5 mm
- HornBDisplaceTransverseX → 1  $\sigma$  shift = 0.5 mm
- HornCDisplaceTransverseX → 1  $\sigma$  shift = 0.5 mm
- **HornAEccentricityXInducedBField** → 1  $\sigma$  shift = **0.035 mm**
- HornATiltTransverseX → 1  $\sigma$  shift = 0.5mm
- **HornCEccentricityXInducedBField** → 1  $\sigma$  shift = **0.07 mm**
- HornCurrent → 1  $\sigma$  shift = 3 kA (1%)
- HornWaterLayerThickness → 1  $\sigma$  shift = 0.5 mm
- ProtonBeamTransverseX → 1  $\sigma$  shift = 0.5 mm
- **TargetUpstreamDegredation** → 1  $\sigma$  shift = **5 mm**



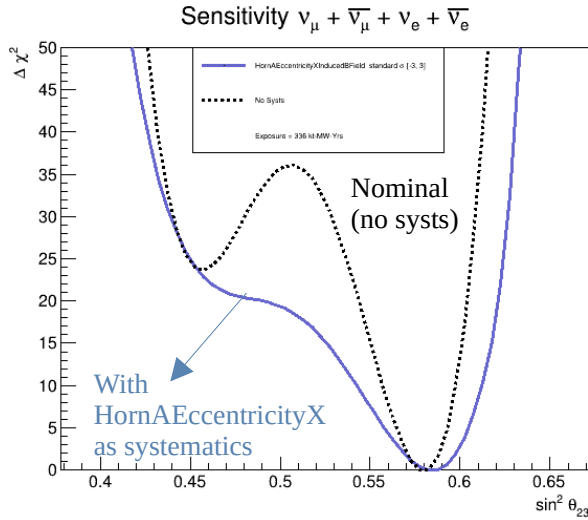
**Need further discussion**

- New uncertainties (not present in TDR): Horn C Displace Transverse, Eccentricity X (both A and C), Horn Tilt (horn A), target upstream degradation

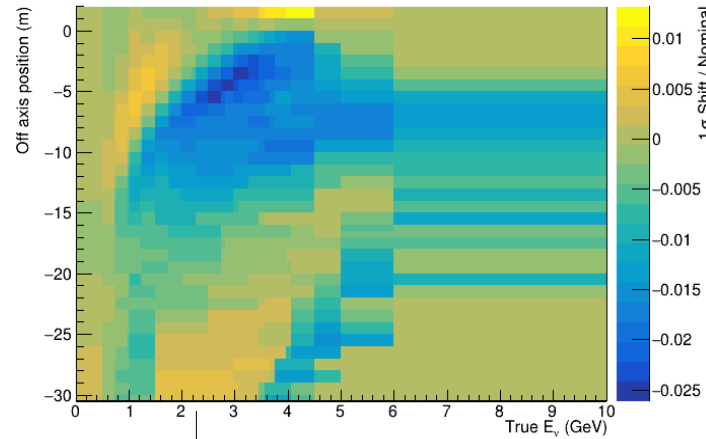
# Horn A Eccentricity X Induced Bfield

IMPORTANT

-  $1\sigma$  shift = **0.035 mm**: NuMi Horn 1 tolerance assumed  
(off axis deformation of inner conductor) → **significant influence on the sensitivity**

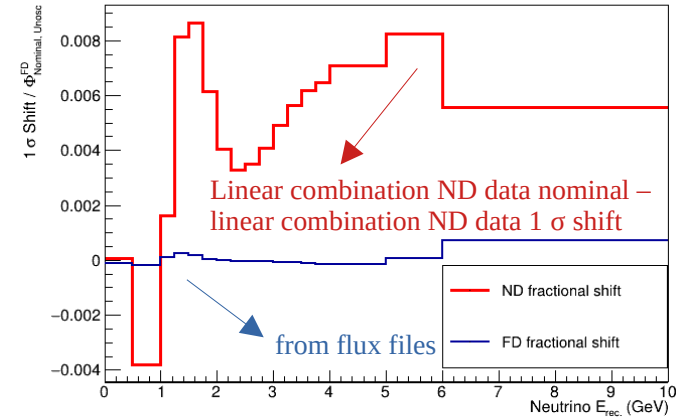


Fractional shift effect (+1 $\sigma$ ) on the ND vs OA vs True  $E_\nu$



Obtained from  
existent flux files

Fractional shift effect on linear combination vs FD



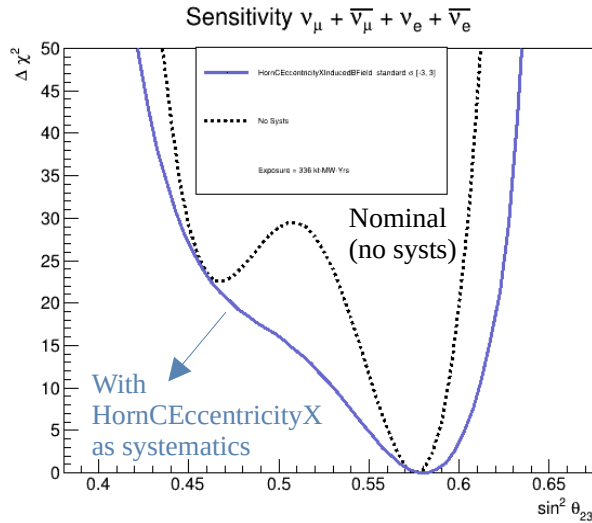
- Very low uncertainties for on-axis data → uncertainties start to become significant for data at several off-axis positions; maximum shift around 5m off-axis and neutrino energies  $\sim 3\text{GeV}$

→ Does it make sense that a **tolerance of 35  $\mu\text{m}$**  in the off axis deformation of the inner conductor results in **uncertainties up to 2.5%** in the ND fluxes? - if it does.. can we do better than **35  $\mu\text{m}$**  ?

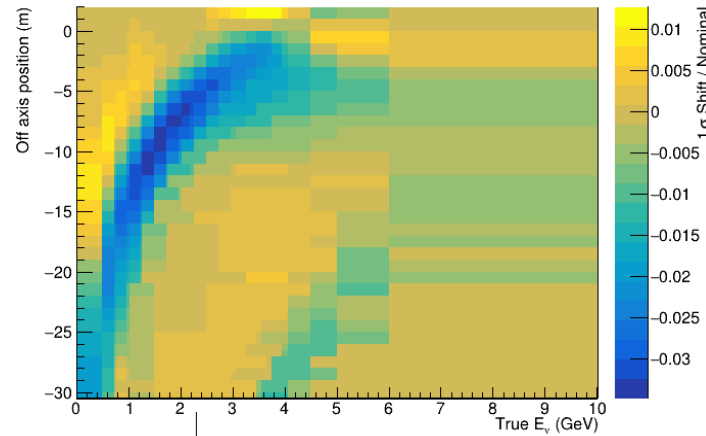
# Horn C Eccentricity X Induced Bfield

IMPORTANT

-  $1\sigma$  shift = **0.07 mm**: NuMi Horn 2 tolerance assumed  
(off axis deformation of inner conductor) → **significant influence on the sensitivity**

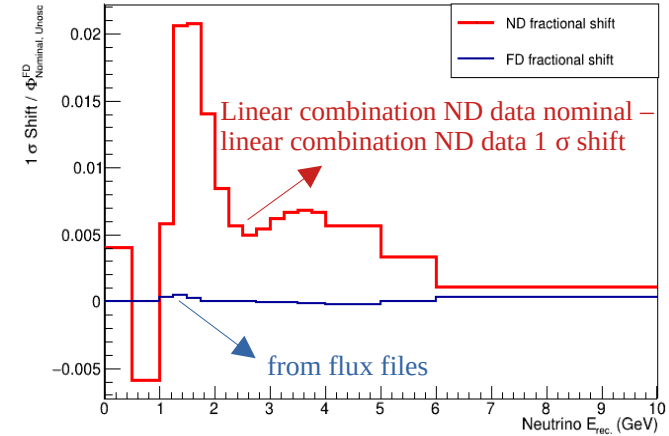


Fractional shift effect (+1 $\sigma$ ) on the ND vs OA vs True  $E_\nu$



Obtained from  
existent flux files

Fractional shift effect on linear combination vs FD



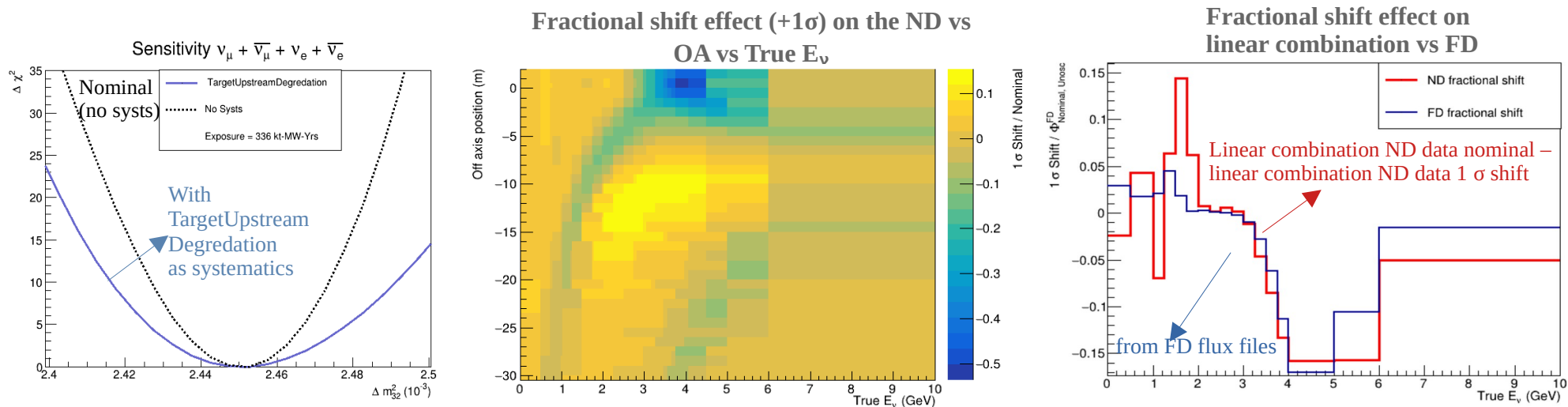
- Very low uncertainties for on-axis data → uncertainties start to become significant for data at several off-axis positions; maximum shift around 10m off-axis and neutrino energies  $\sim 1.5$  GeV
  - high uncertainties 3 % (compared to HornAEccentricity X) for all off-axis positions

→ Does it make sense that a **tolerance of 70  $\mu\text{m}$**  in the off axis deformation of the inner conductor results in **uncertainties up to 3.5%** in the ND fluxes? - if it does.. can we do better than **70  $\mu\text{m}$**  ?

# Target Upstream Degredation

IMPORTANT

- **1 $\sigma$  shift = 5 mm loss**: assume complete loss of target on upstream end  
(a shorter target by  $dz$  shifted downstream by the loss  $dz$ )  $\rightarrow$  **significant influence on the sensitivity**



- Very high uncertainties for ND **on-axis** data (up to **50% at  $E_\nu \sim 4$  GeV**) + off-axis uncertainties also high:  $\sim 15\%$
- High uncertainties (up to 15%) for FD as well

**$\rightarrow$  Do we expect 50% uncertainties from a 5 mm target loss? Why so high uncertainties for this parameter?**

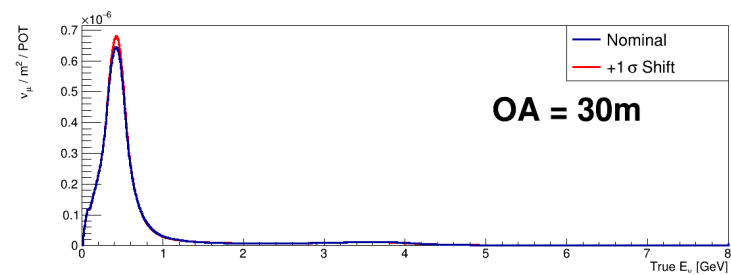
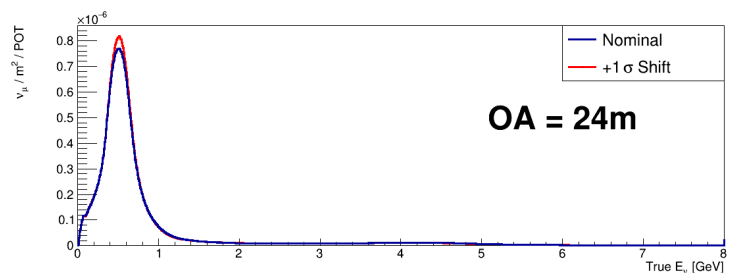
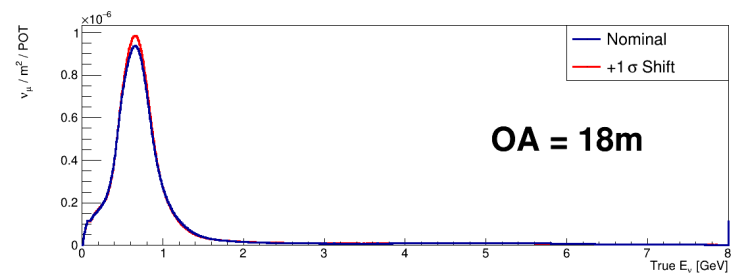
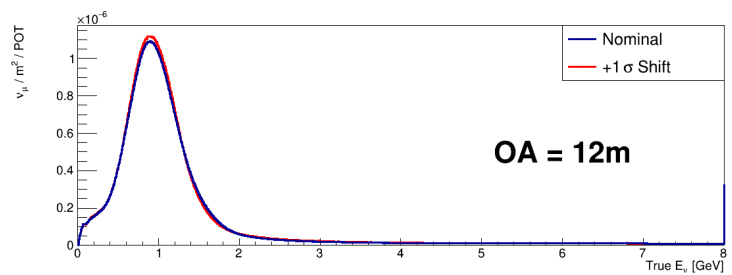
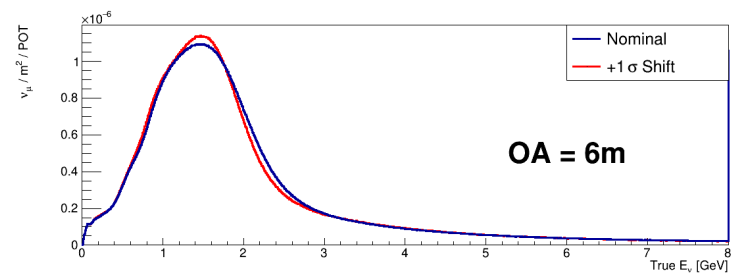
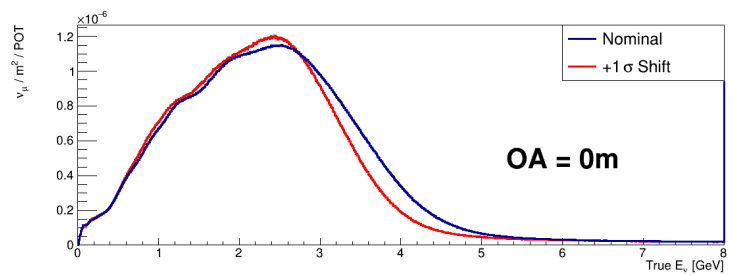
- is a tolerance of 5 mm feasible? Could we do better?

# Target Upstream Degredation

**IMPORTANT**

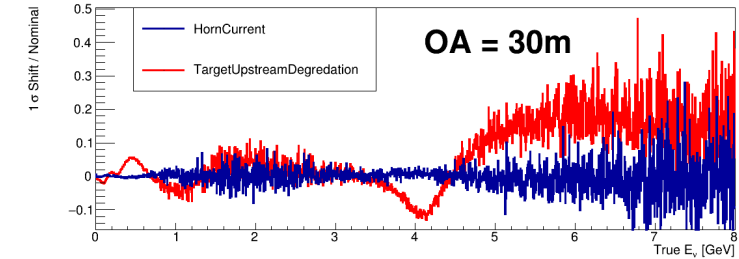
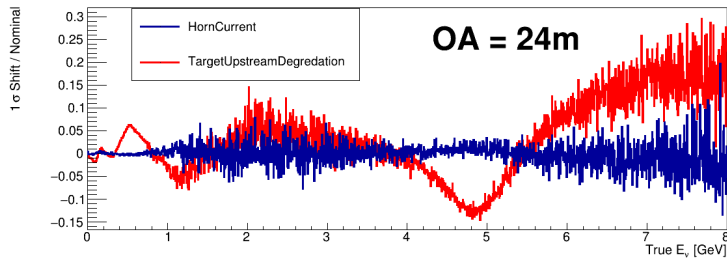
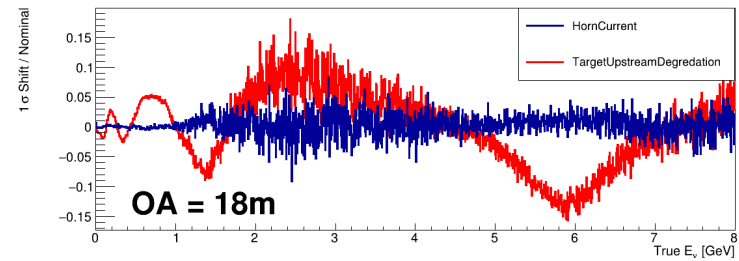
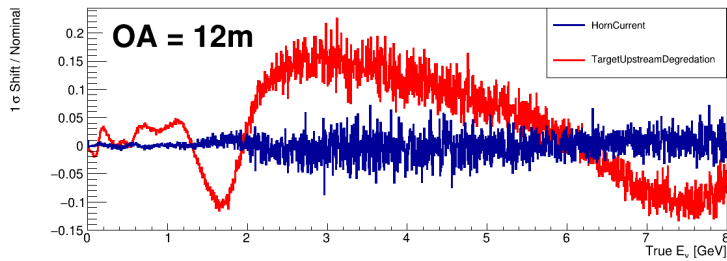
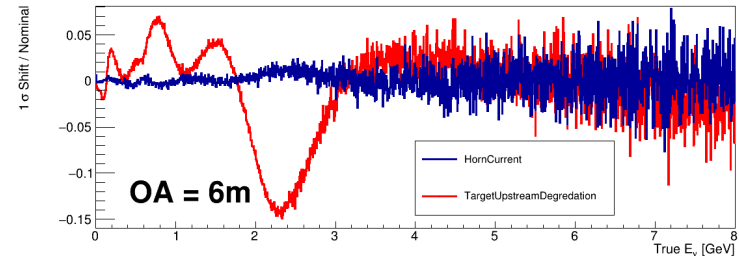
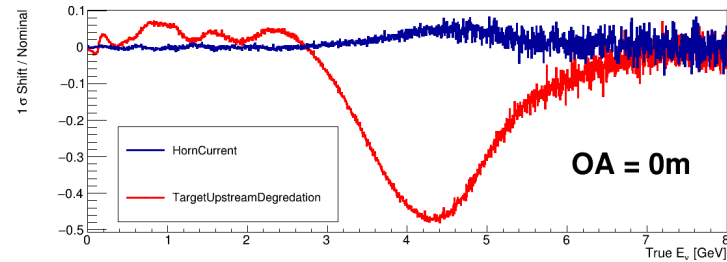
-  $1\sigma$  shift = 5 mm loss: assume complete loss of target on upstream end

→ cross check with fluxes from the provided root files: visible difference in the shifted flux



# Target Upstream Degredation vs HornCurrent

→ fractional error obtained from the flux files (original energy binning)



High fractional uncertainties (up to 50%) for **TargetUpstreamDegredation** parameter are coming from the original root files (not a re-binning issue)

## Open questions:

- **Horn Eccentricity X Induced Bfield** (off axis deformation of inner conductor)
  - why so high uncertainty values ( 1 sigma shift = 0.035 mm resp. 0.07 mm) up to 3%?
- **Target Upstream Degredation** (5 mm loss at 1  $\sigma$ )
  - why are the uncertainties so high? (up to 50% for on-axis at  $E \approx 4\text{GeV}$ )
- **Decay Pipe Geomagnetic field** (1  $\sigma$  shift = 1: nominal – 0 no Earth magnetic field, 1 – NuMi value)
  - what is the assumption for the uncertainty calculation?
  - relatively high values for the uncertainties: 1.5%
- **Could we cross check (i.e reproduce the \*worrying\* systematics..?)**
  - do we have access to Pierce's code?
  - do we have anyone (manpower..) who could help with this.. → how difficult would it be?



# Slide dedicated to path of files and histograms used from Pierce's files

- ND files:

- **nominal**: /pnfs/dune/persistent/users/pweather/fluxfiles/g4lbne/v3r5p9/QGSP\_BERT/OfficialEngDesignSept2021/**neutrino**/flux/histos\_g4lbne\_v3r5p9\_QGSP\_BERT\_OfficialEngDesignSept2021\_neutrino\_LAr\_center.root

- Nominal Flux histogram: **Unosc\_numu\_flux\_DUNEPRISM\_LAr\_center** – TH2D histogram neutrino flux vs energy vs off-axis positions (neutrino energy on x-axis, off-axis position on y-axis and neutrino fluxes on z-axis)

- Energy binning: E [0, 8GeV] – 0.005 GeV bin width  
E (8, 114 GeV) – 0.25 GeV bin width
      - OA binning: OA [-4.0, 36.925 m] – 0.05 m bin width

- **shift**: /pnfs/dune/persistent/users/pweather/fluxfiles/g4lbne/v3r5p9/QGSP\_BERT/OEDS21\_**HornADisplaceTransverseX\_pos\_1\_sigma**/**neutrino**/flux/histos\_g4lbne\_v3r5p9\_QGSP\_BERT\_OEDS21\_HornADisplaceTransverseX\_pos\_1\_sigma\_neutrino\_LAr\_center.root

- Shifted flux histogram: **Unosc\_numu\_flux\_DUNEPRISM\_LAr\_center** – TH2D histogram neutrino flux vs energy vs off-axis positions (neutrino energy on x-axis, off-axis position on y-axis and neutrino fluxes on z-axis)

- Energy binning: E [0, 8GeV] – 0.005 GeV bin width  
E (8, 114 GeV) – 0.25 GeV bin width
      - OA binning: OA [-4.0, 36.925 m] – 0.05 m bin width

- FD files:

- **nominal**: /pnfs/dune/persistent/users/pweather/fluxfiles/g4lbne/v3r5p9/QGSP\_BERT/OfficialEngDesignSept2021/**neutrino**/flux/histos\_g4lbne\_v3r5p9\_QGSP\_BERT\_OfficialEngDesignSept2021\_neutrino\_finemc.root

- Nominal flux histogram: **Unosc\_flux\_numu\_finemc\_DUNEFD** – TH1D hisotgram neutrino flux vs energy

- Energy binning: E [0, 8GeV] – 0.005 GeV bin width  
E (8, 114 GeV) – 0.25 GeV bin width

- **shift**: /pnfs/dune/persistent/users/pweather/fluxfiles/g4lbne/v3r5p9/QGSP\_BERT/OEDS21\_**HornADisplaceTransverseX\_pos\_1\_sigma**/**neutrino**/flux/histos\_g4lbne\_v3r5p9\_QGSP\_BERT\_OEDS21\_HornADisplaceTransverseX\_pos\_1\_sigma\_neutrino\_finemc.root

- Shifted flux histogram: **Unosc\_flux\_numu\_finemc\_DUNEFD** – TH1D hisotgram neutrino flux vs energy

- Energy binning: E [0, 8GeV] – 0.005 GeV bin width  
E (8, 114 GeV) – 0.25 GeV bin width

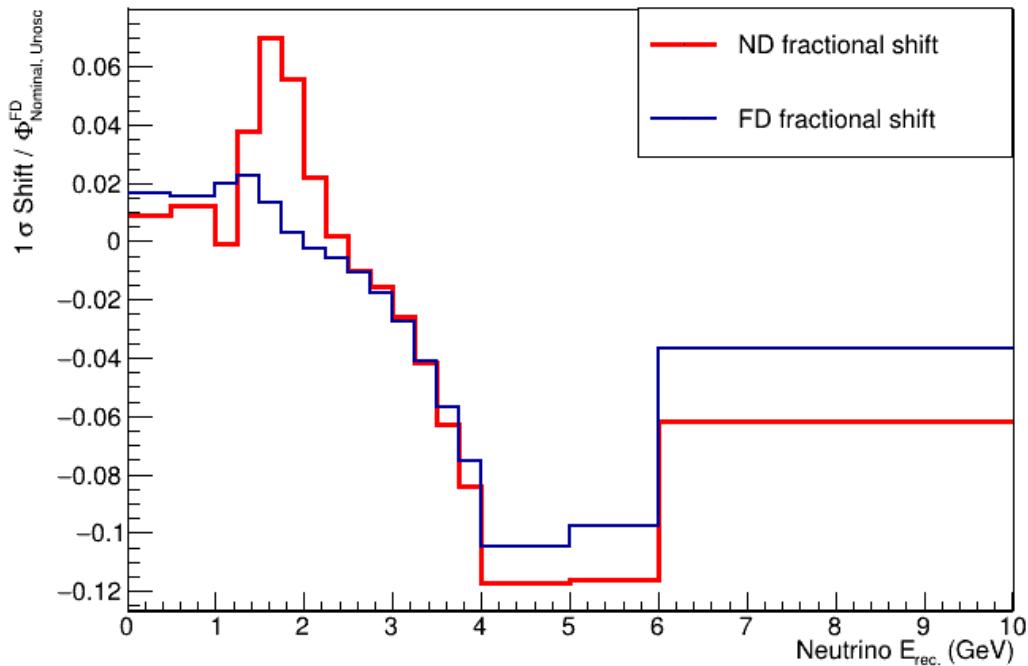
# BACKUP

# Target Upstream Degredation

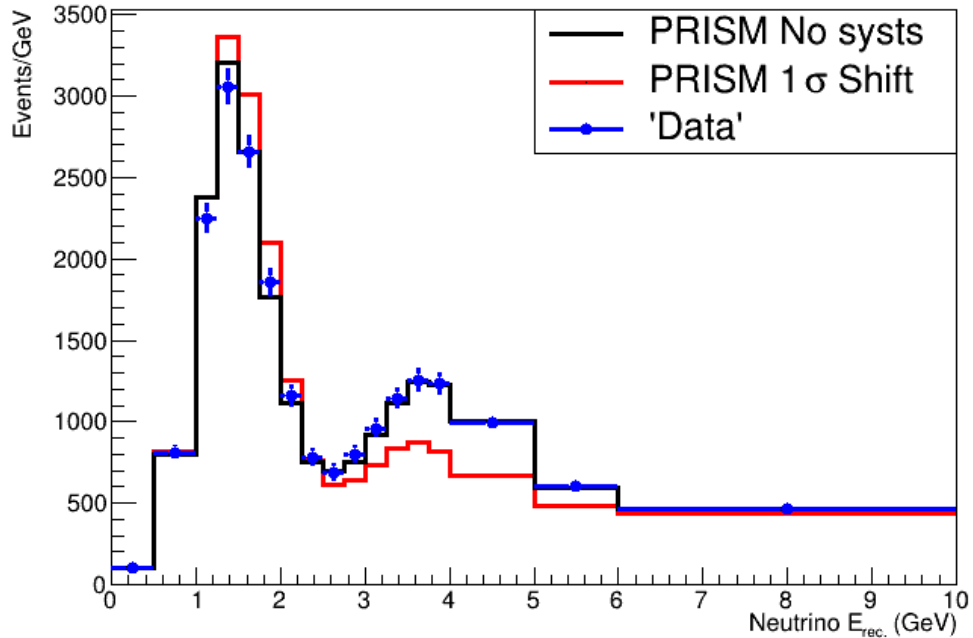
**IMPORTANT**

-  $1\sigma$  shift = 5 mm loss: assume complete loss of target on upstream end (a shorter target by  $dz$  shifted downstream by the loss  $dz$ )

Fractional shift TargetUpstreamDegredation+  $1\sigma$



TargetUpstreamDegredation

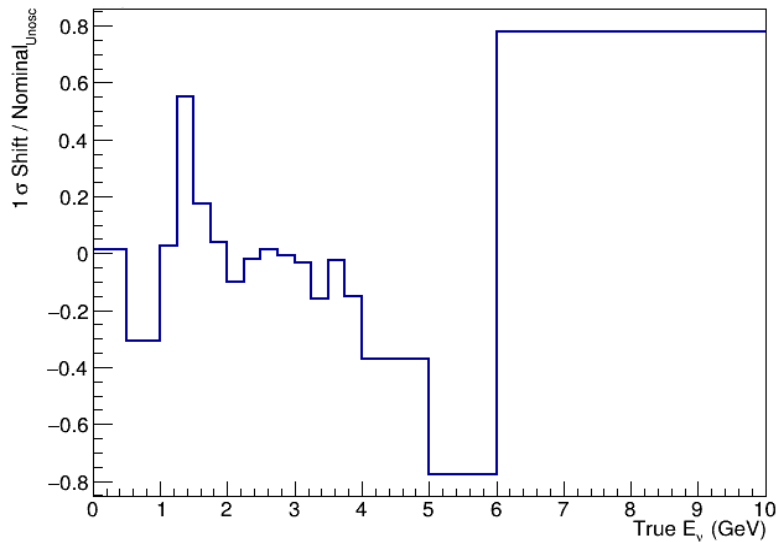


## Horn A Eccentricity X Induced Bfield

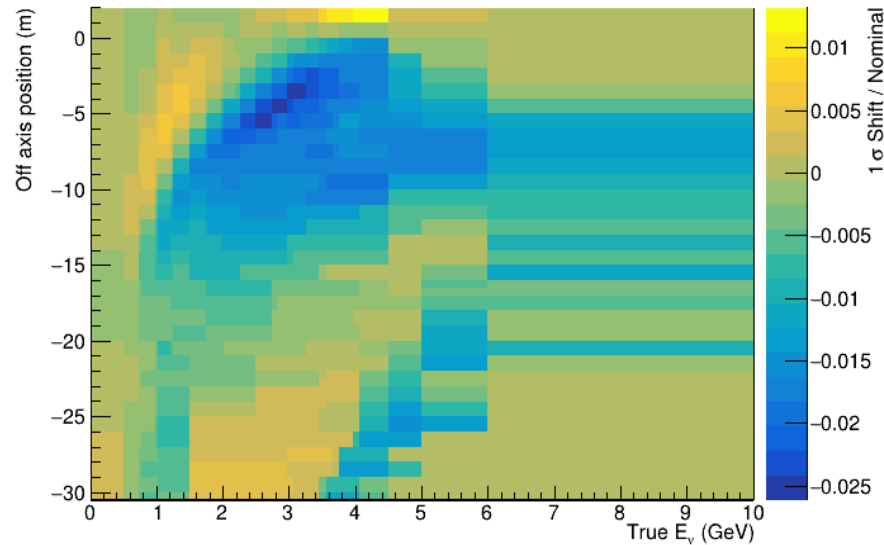
**IMPORTANT**

-  $1\sigma$  shift = 0.035 mm: NuMi Horn 1 tolerance assumed  
(off axis deformation of inner conductor)

Fractional shift effect ( $+1\sigma$ ) on the FD



Fractional shift effect ( $+1\sigma$ ) on the ND

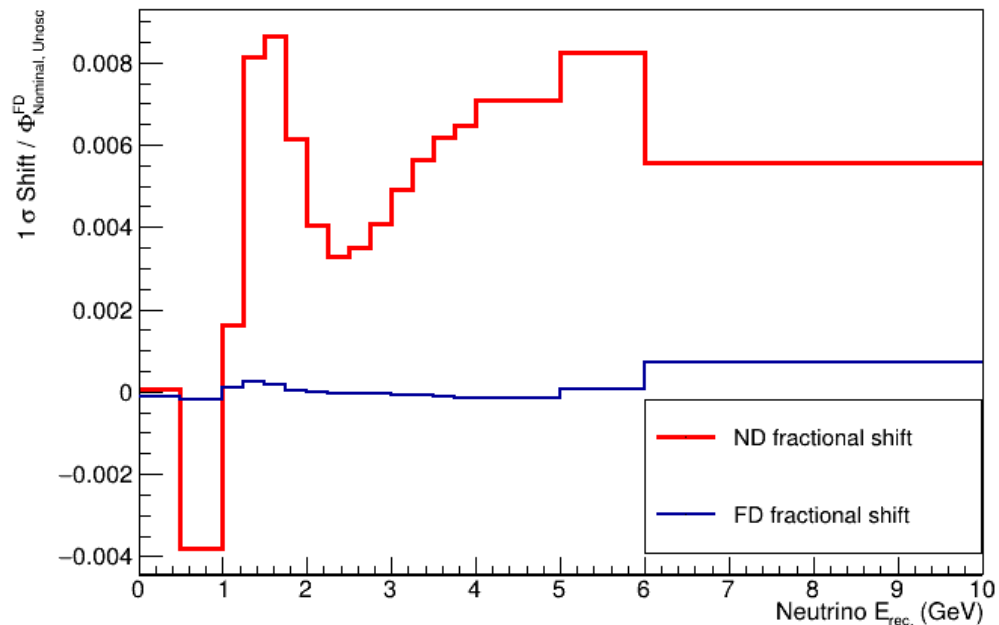


## Horn A Eccentricity X Induced Bfield

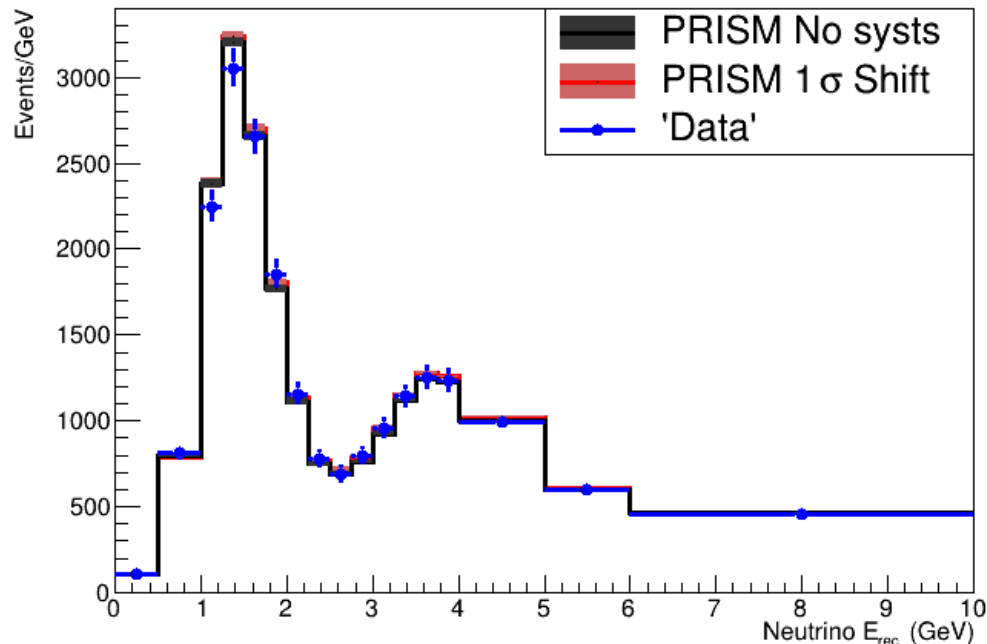
**IMPORTANT**

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(off axis deformation of inner conductor)

Fractional shift HornAEccentricityXInducedBField+  $1\sigma$



HornAEccentricityXInducedBField

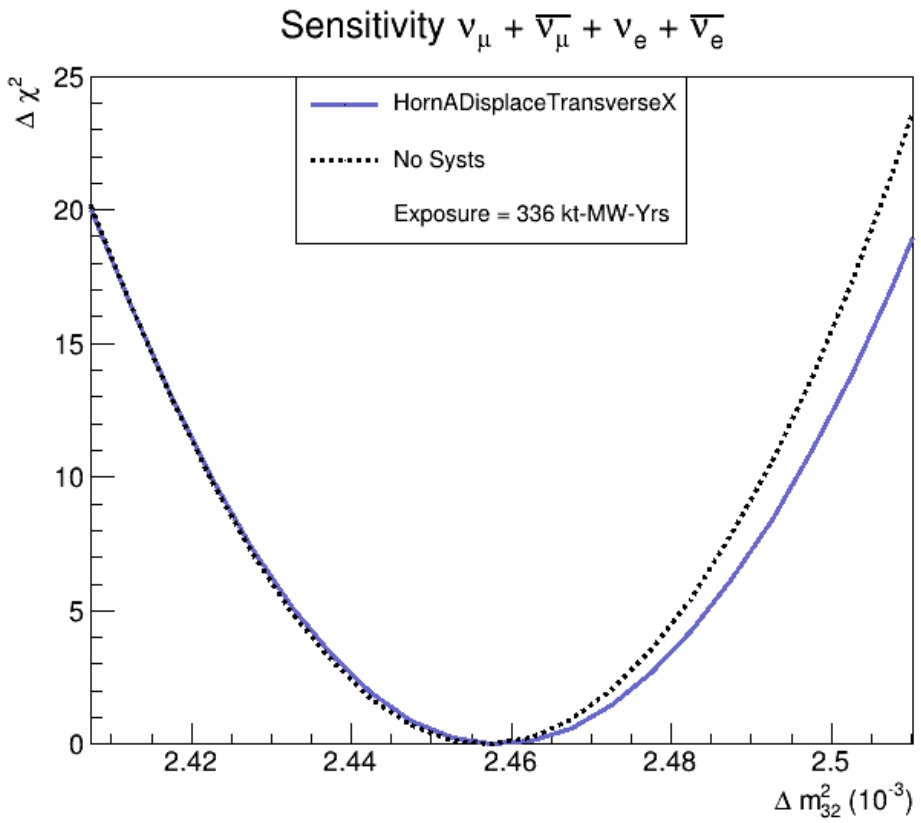
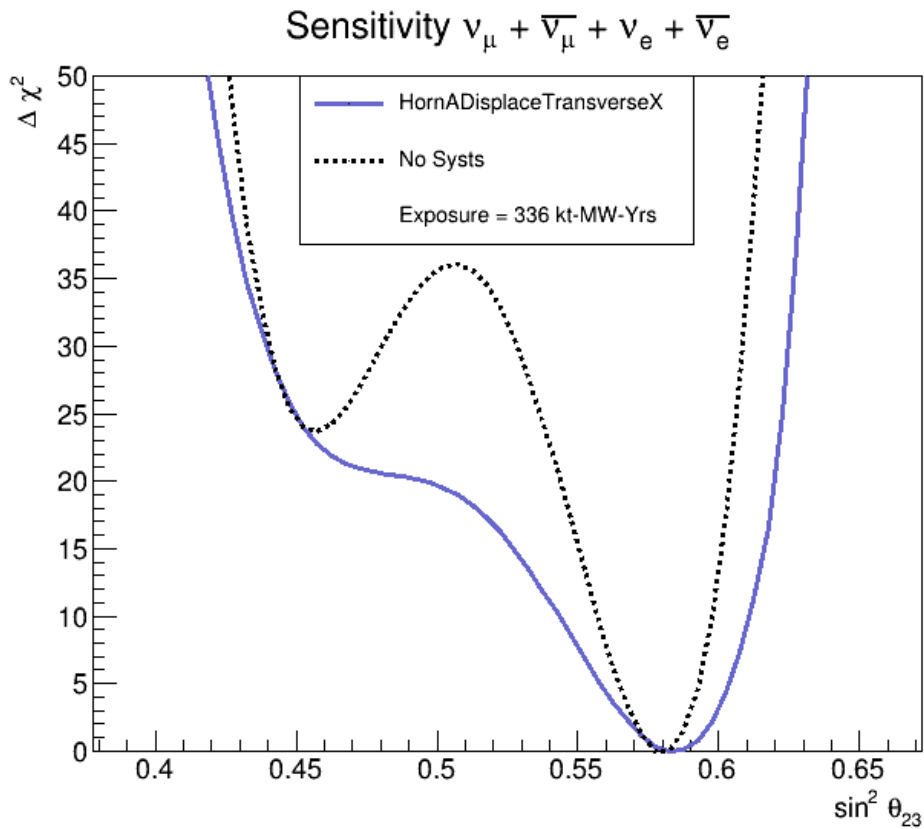


- PRISM linear combination (ND) fractional shift is much higher than the oscillated FD one + different energy dependence between ND and FD  $\rightarrow$  high impact on the oscillation parameters sensitivity

# Horn A Displace Transverse X

IMPORTANT

-  $1\sigma$  shift = 0.5 mm



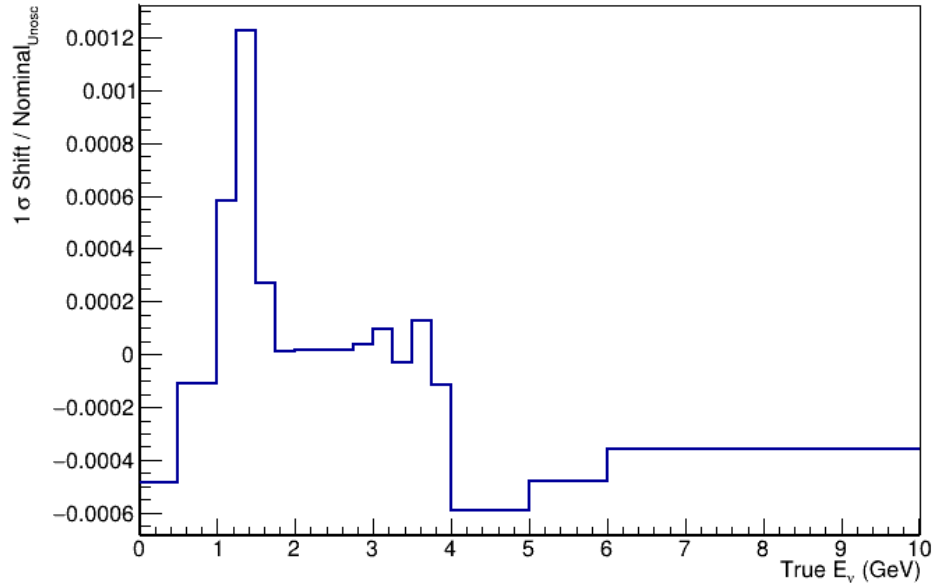
- Significant sensitivity reduction → where does this comes from?

# Horn A Displace Transverse X

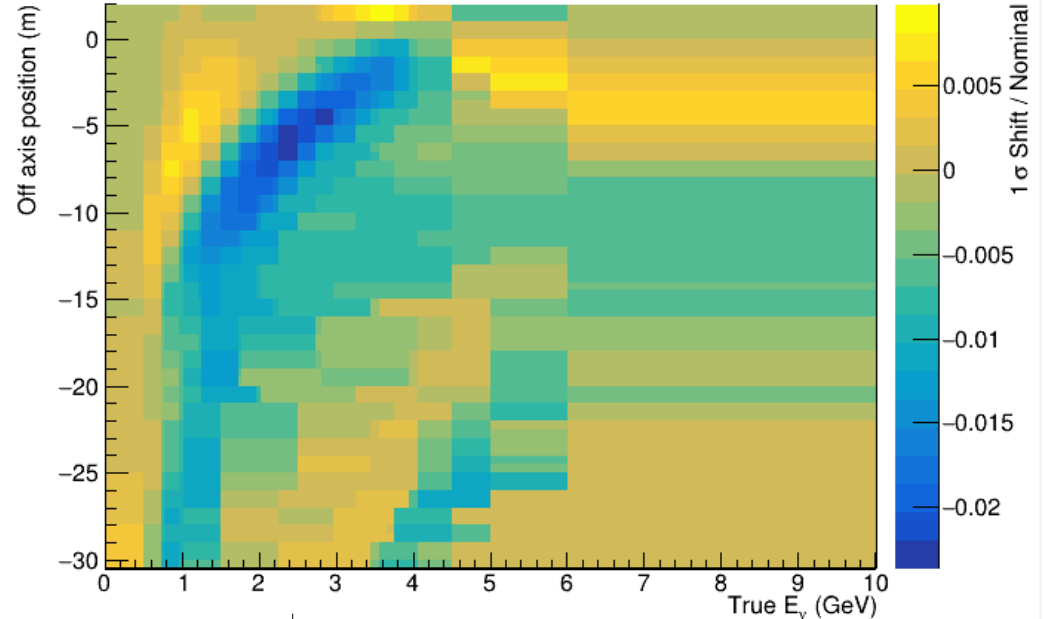
IMPORTANT

- $1\sigma$  shift = 0.5 mm
- look at both FD and ND fractional ratios versus energy when the the flux parameter of interest is shifted by  $1\sigma$

Fractional shift effect ( $+1\sigma$ ) on the FD



Fractional shift effect ( $+1\sigma$ ) on the ND



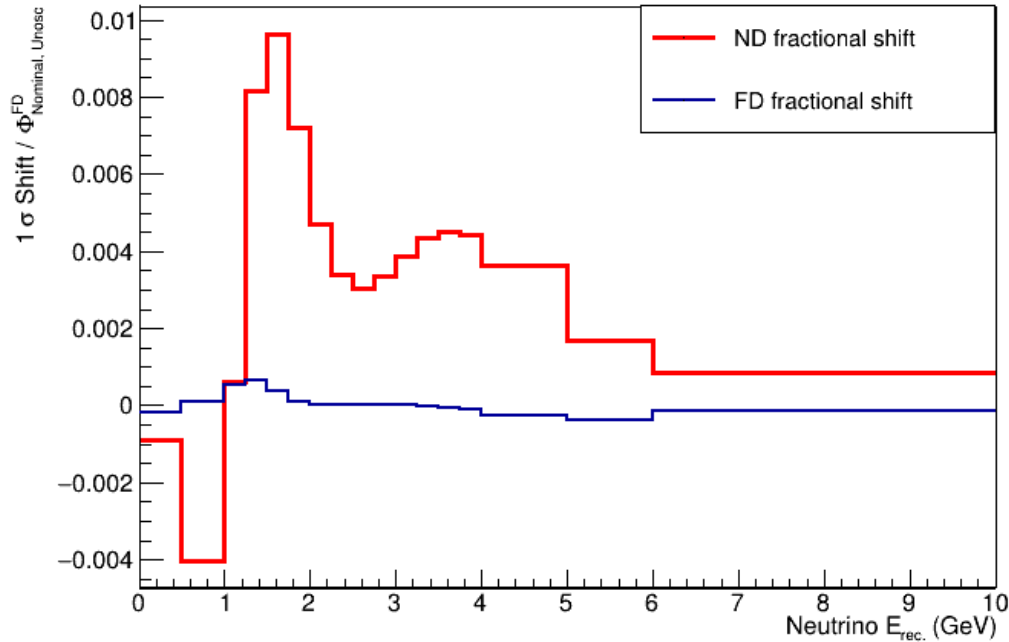
Linearly combine to get the PRISM fractional uncertainty

# Horn A Displace Transverse X

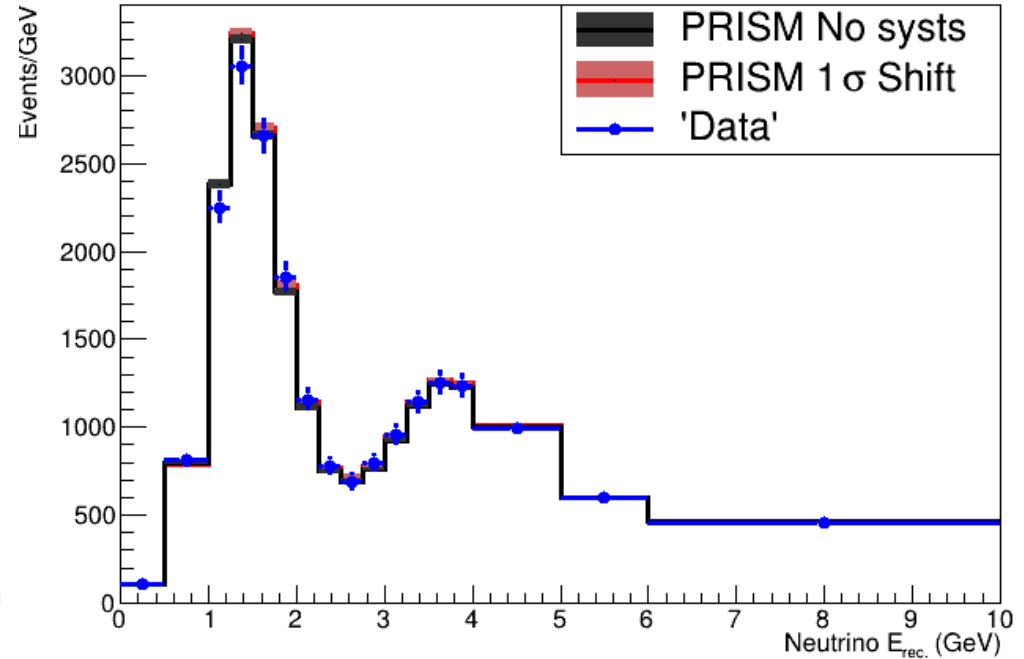
IMPORTANT

-  $1\sigma$  shift = 0.5 mm

Fractional shift HornADisplaceTransverseX+  $1\sigma$



HornADisplaceTransverseX

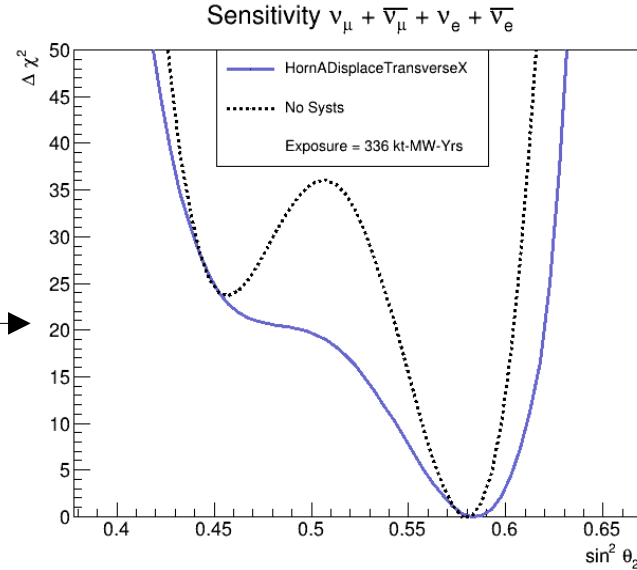
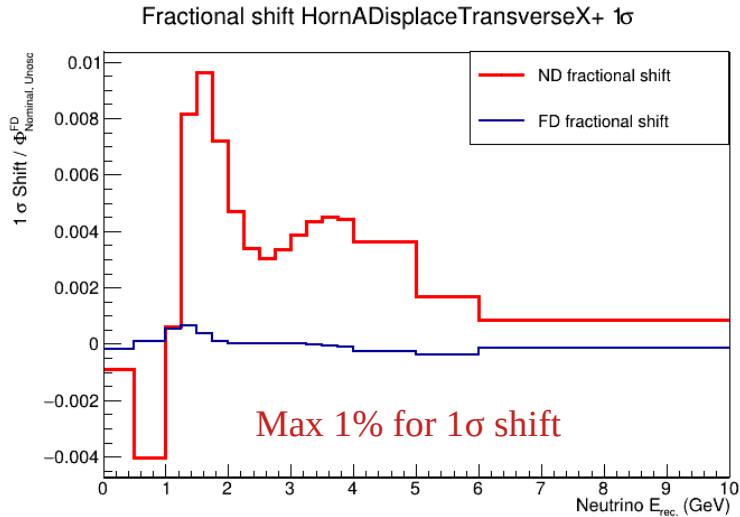


- PRISM linear combination (ND) fractional shift is much higher than the oscillated FD one + different energy dependence between ND and FD  $\rightarrow$  high impact on the oscillation parameters sensitivity



# Horn A Displace Transverse X

IMPORTANT

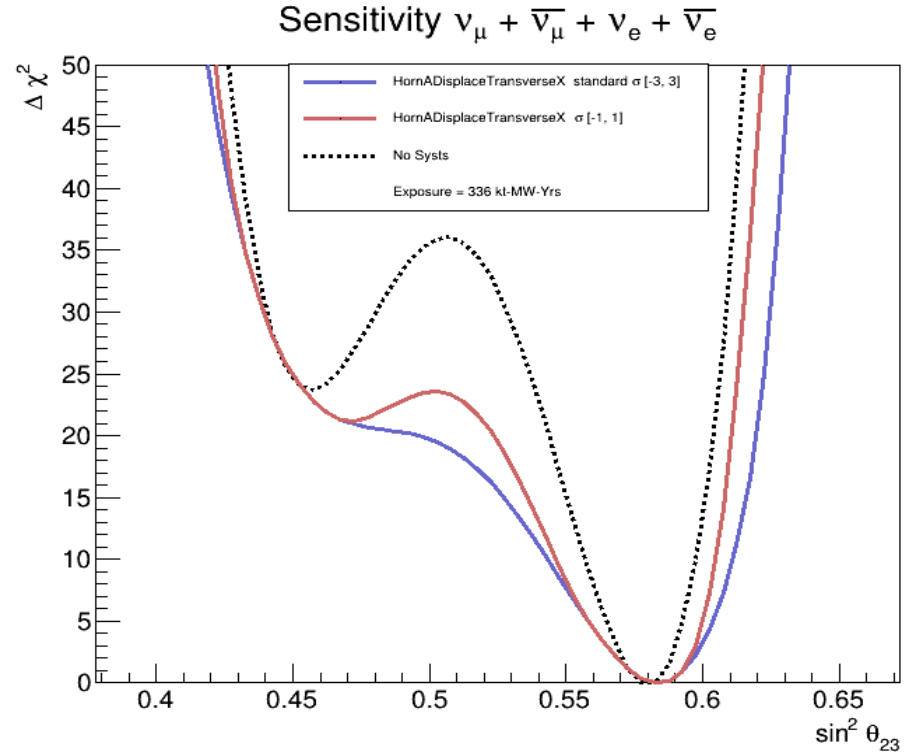
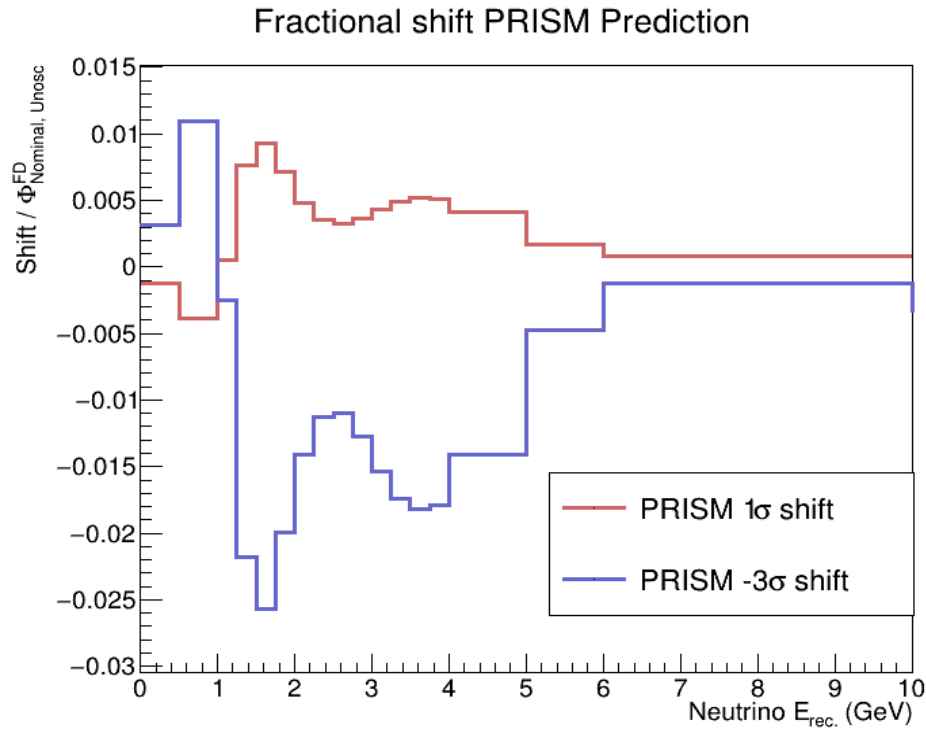


**Why such a big sensitivity reduction?**

- Systematics allowed to vary in a +/- 3  $\sigma$  range
- $\chi^2$  calculation is using Asimov data (PRISM Pred – Asimov data) → nominal PRISM prediction for different scan parameters has a poor agreement with the Asimov data → for certain parameters a maximum systematics shift (+/- 3  $\sigma$ ) results in a better match
- Limit maximum systematics shift to +/- 1  $\sigma$  and re-evaluate the PRISM sensitivity

# Horn A Displace Transverse X

IMPORTANT



- Better sensitivity with a maximum  $\pm 1 \sigma$  ( $< 1\%$ ) systematics shift
  - highest sensitivity reduction correspond to  $\pm 3 \sigma$  shift ( $< 3\%$ )

# Updates to the Decay Pipe

## Geometry and positioning

### - before (1 parameter):

- vary radius by large tolerance (10 cm)  
→ dominant uncertainty in the region of interest ( $E < 4.5$  GeV)

### - now: (11 parameters)

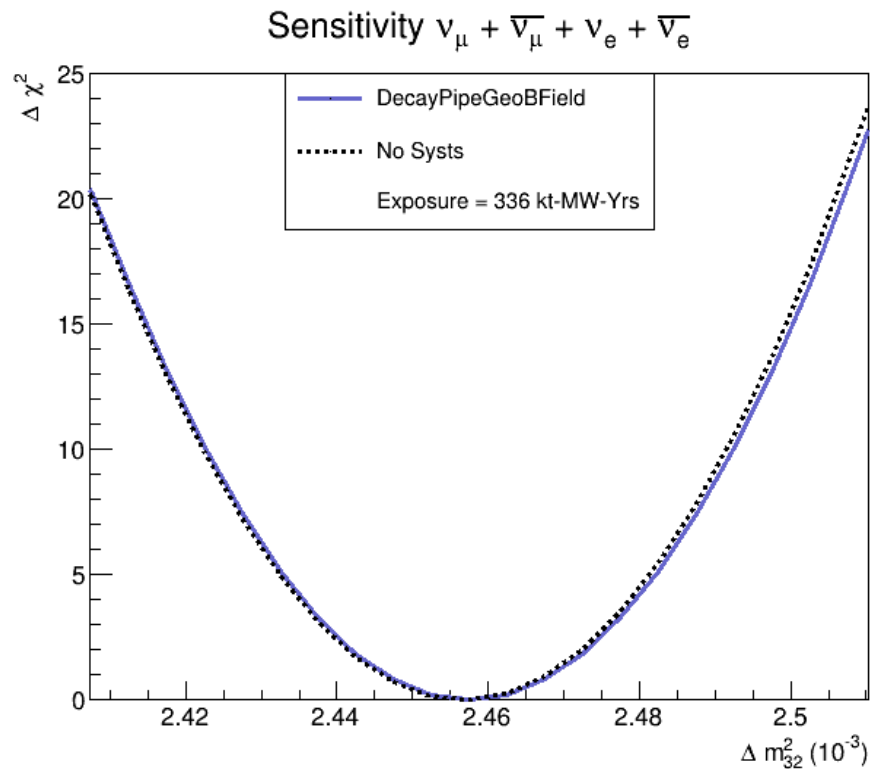
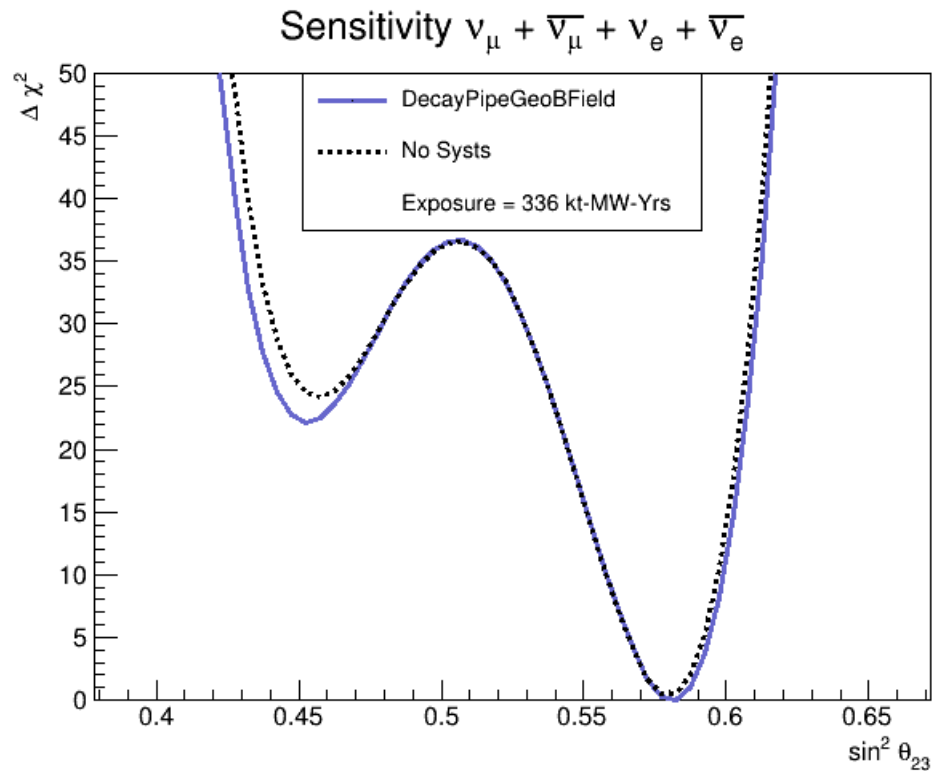
- tolerance of 2 cm in the decay pipe radius
- length of the pipe expected to change  $1\sigma = 2.5$  cm @ 1.2 MW
- **transverse offset** of the decay pipe in X, Y by 2.5 cm
- transverse tilt of the upstream end of decay pipe by 2.5 cm
- **elliptical cross section** of the decay pipe: expectation the decay pipe will come out of round as it settles (2.5 cm tolerance in both X(A) and Y(B) )
- possibility the pipe can be bowed along the beamline
- uncertainty due to the effect of the Earth's geomagnetic field: geomagnetic field measured in NuMI decay pipe was mapped into DUNE decay pipe, and a scale factor of 1 is used to tune the strength of the B-field vector. (0 – nominal, 1-NuMI)

Parameter	1 $\sigma$ Shift	Notes
Decay Pipe Radius	2.0 cm	Changed from 10 cm; nominal = 2 m
Decay Pipe Length	2.5 cm	Same as elongating, since the distance between decay pipe upstream is fixed
Decay Pipe Displace Transverse X	2.5 cm	
Decay Pipe Displace Transverse Y	2.5 cm	
Decay Pipe Tilt X _ DSOA	2.5 cm	Downstream (DS) end fixed to remain on axis
Decay Pipe Tilt Y _ DSOA	2.5 cm	
Decay Pipe Elliptical Cross section X (A)	2.5 cm	Ellipse with A (X-axis) or B (y-axis) varied by tolerance, while other dimension fixed to nominal radius
Decay Pipe Elliptical Cross section Y (B)	2.5 cm	
Decay Pipe Geo B Field	1	Scale-factor value to 1 is $1\sigma$ tolerance. Mapped from NuMI decay pipe geo B-field measurements
Decay Pipe Segmented Bowing X	2.5 cm	Decay Pipe segmented in 3 equal pieces; central piece transverse shifted by tolerance
Decay Pipe Segmented Bowing Y	2.5 cm	

## Decay Pipe Geo BField

SEMI

-  $1\sigma$  shift = 1: scale factor value of 1 is  $1\sigma$  tolerance  
(mapped from NuMI Decay Pipe Geo Bfield measurements)

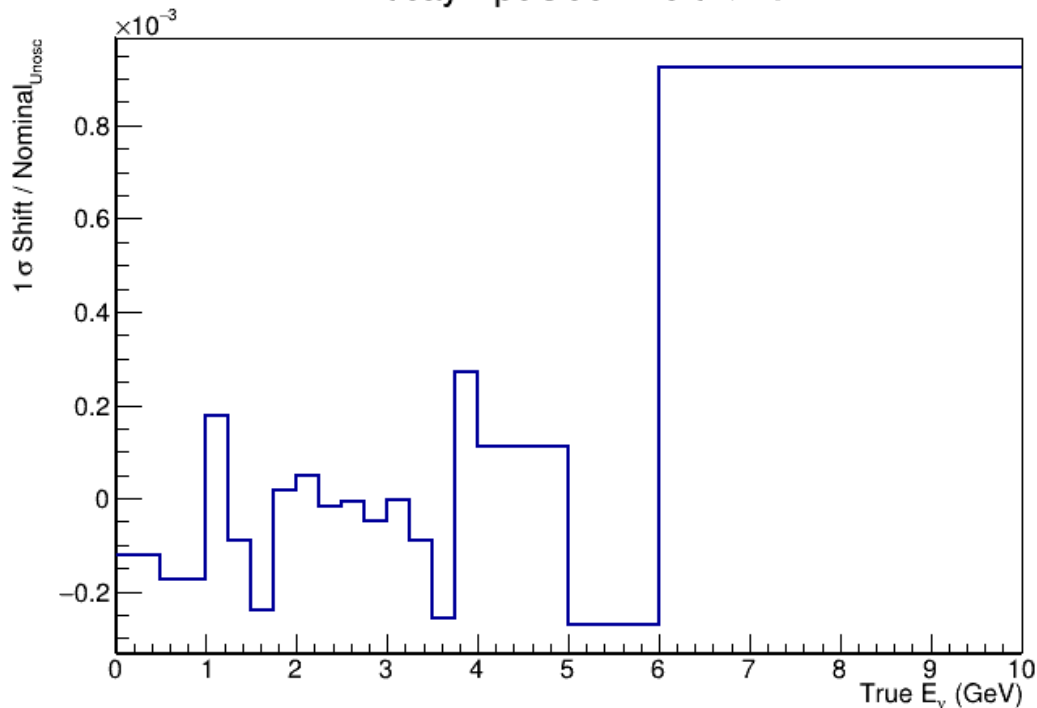


## Decay Pipe Geo BField

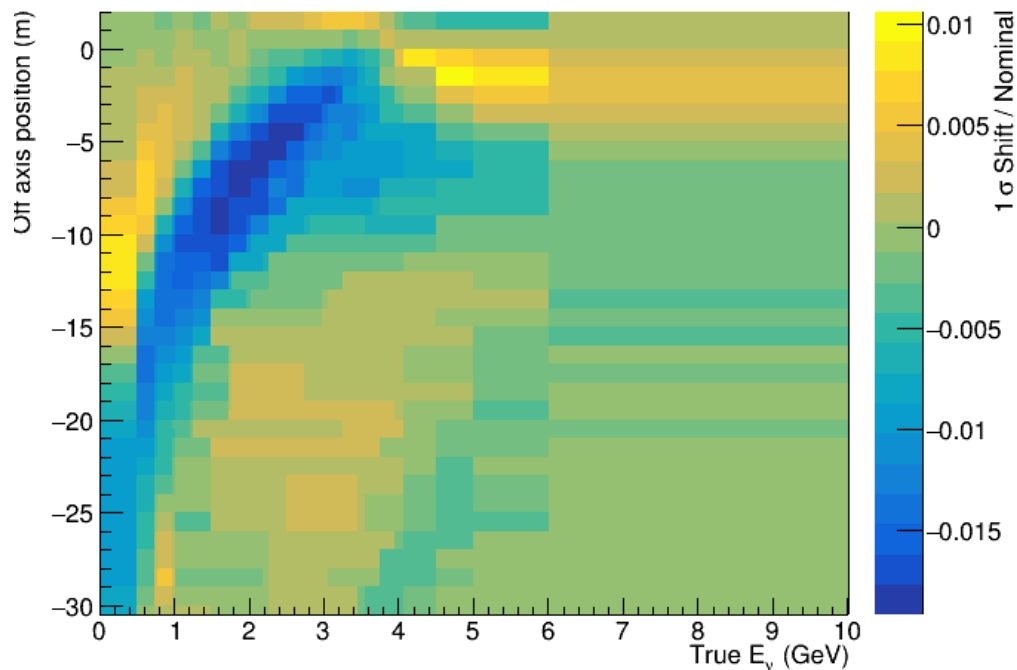
SEMI

-  $1\sigma$  shift = 1: scale factor value of 1 is  $1\sigma$  tolerance  
(mapped from NuMI Decay Pipe Geo Bfield measurements)

FD DecayPipeGeoBField +  $1\sigma$



ND DecayPipeGeoBField +  $1\sigma$

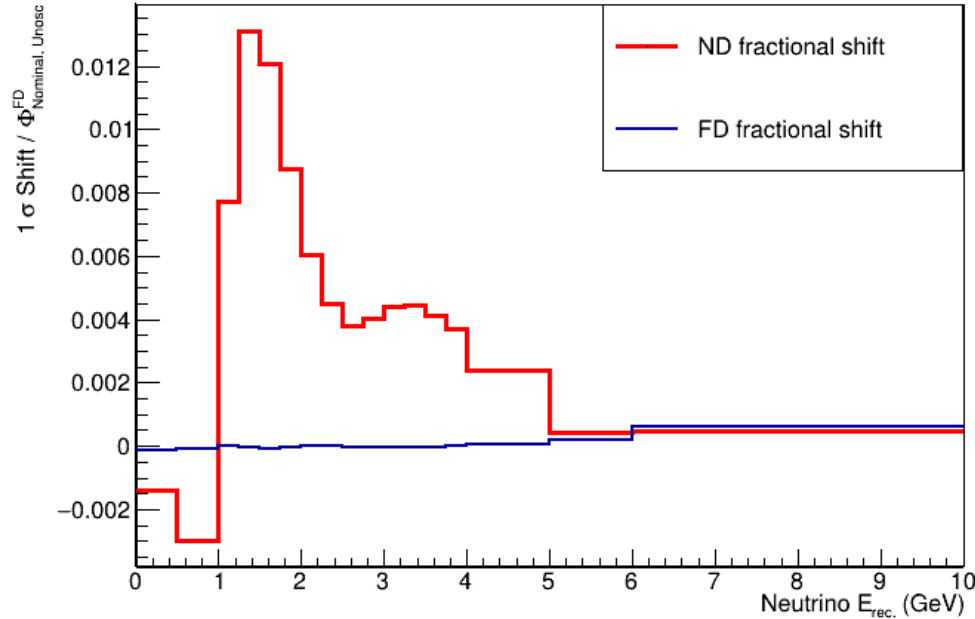


# Decay Pipe Geo Bfield

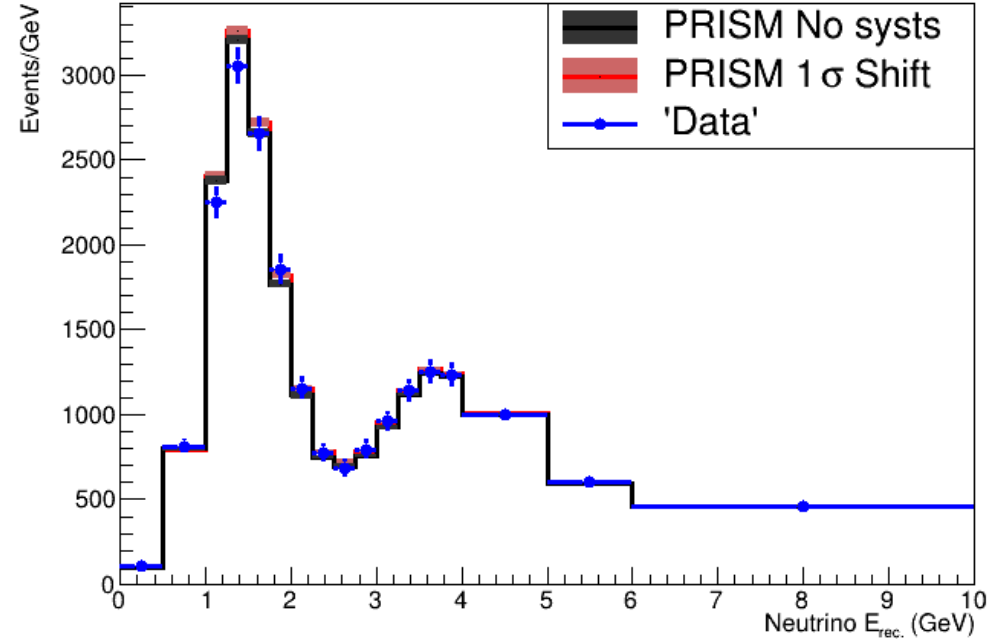
SEMI

-  $1\sigma$  shift = 1: scale factor value of 1 is  $1\sigma$  tolerance  
(mapped from NuMI Decay Pipe Geo Bfield measurements)

Fractional shift DecayPipeGeoBfield+  $1\sigma$



DecayPipeGeoBfield



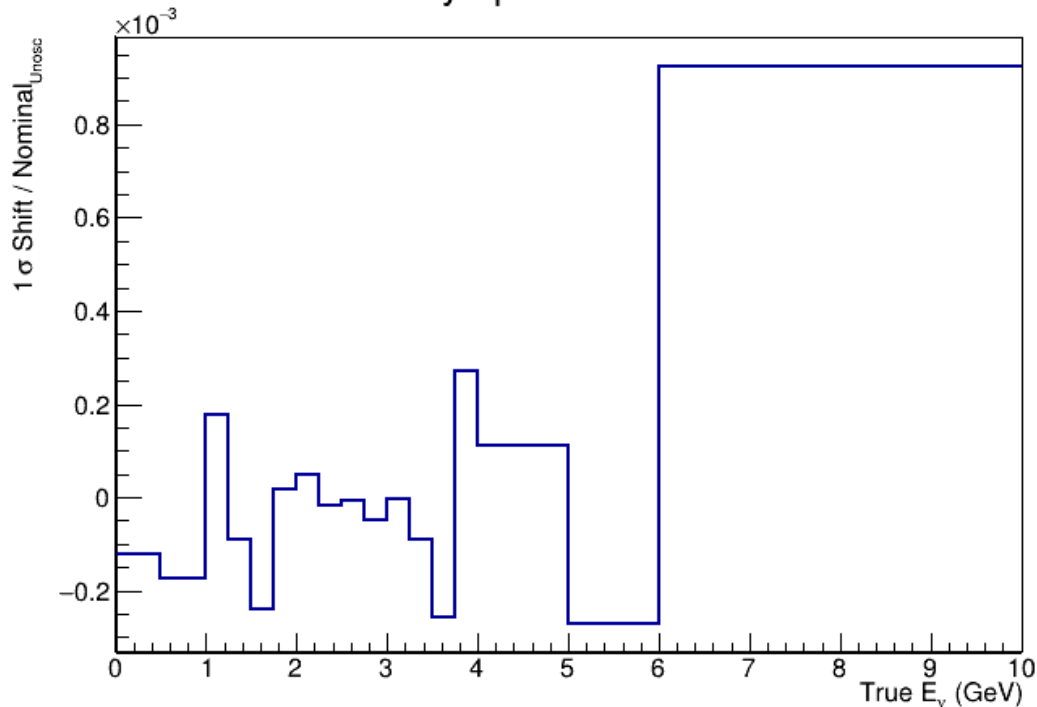
- high uncertainty values for this parameter, BUT partially canceled out by the antineutrino channel (not a significant influence on the oscillation parameter sensitivity)

# BACKUP: Decay Pipe Geo Bfield: neutrino channel $\nu_\mu \rightarrow \nu_\mu$

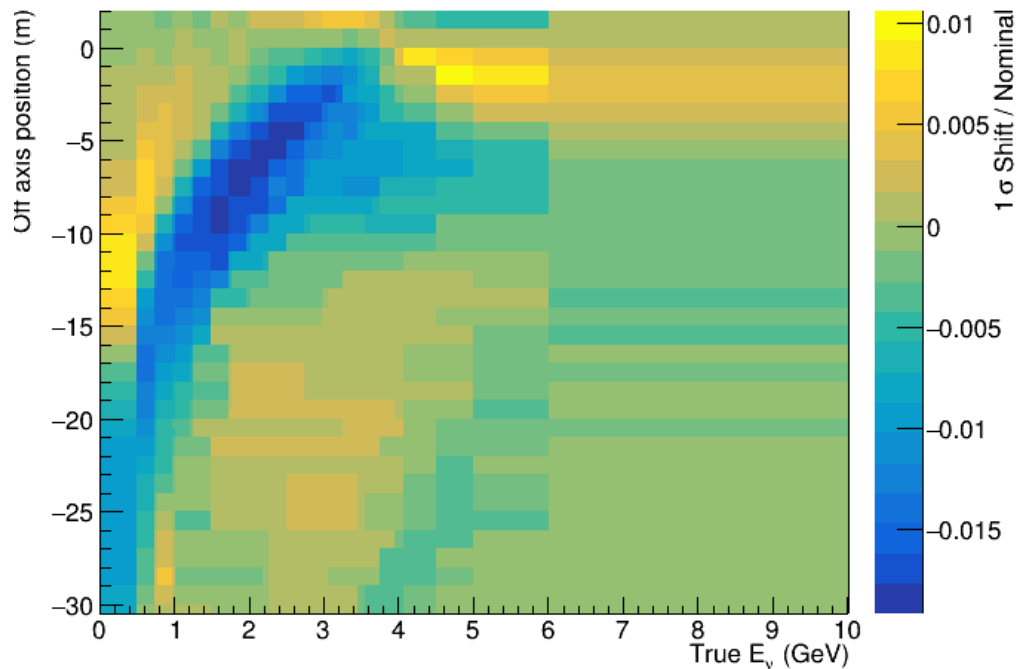
SEMI

-  $1\sigma$  shift = 1: scale factor value of 1 is  $1\sigma$  tolerance  
(mapped from NuMI Decay Pipe Geo Bfield measurements)

FD DecayPipeGeoBField +  $1\sigma$



ND DecayPipeGeoBField +  $1\sigma$

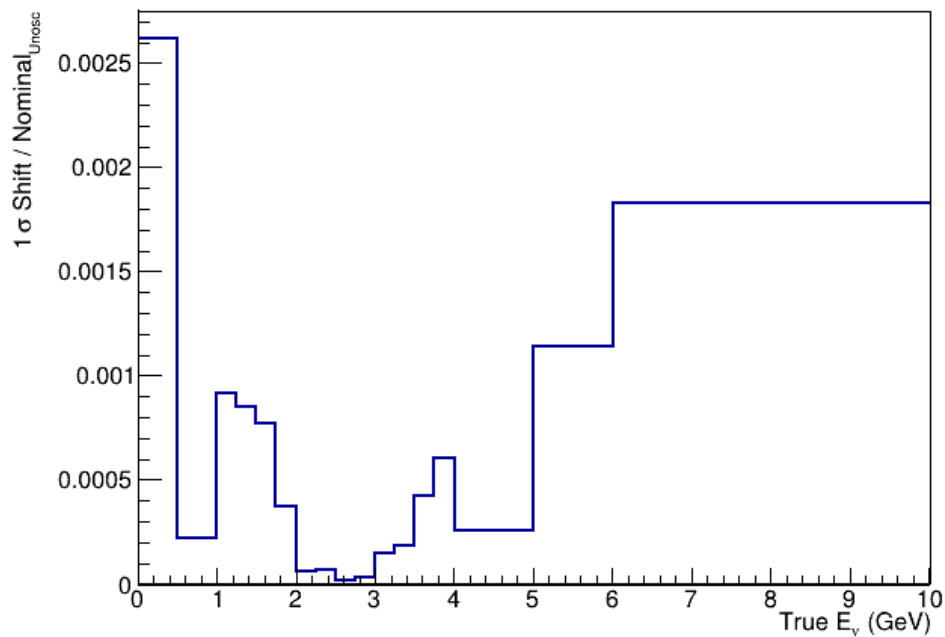


# BACKUP

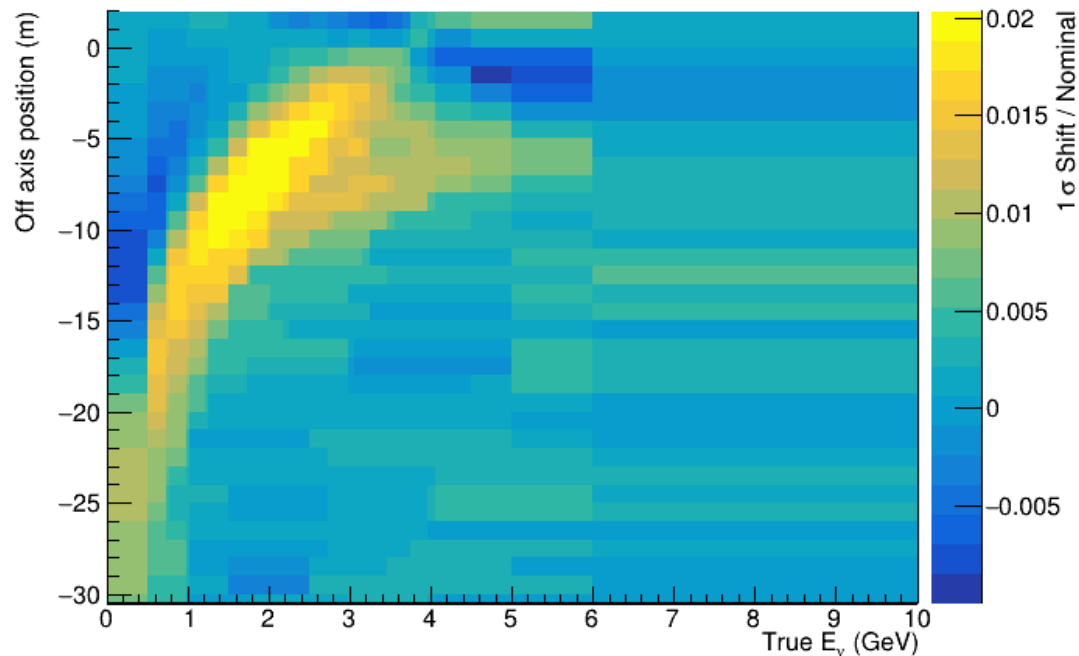
## Decay Pipe Geo BField: antineutrino channel $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$

SEMI

FDDecayPipeGeoBField+ 1 $\sigma$



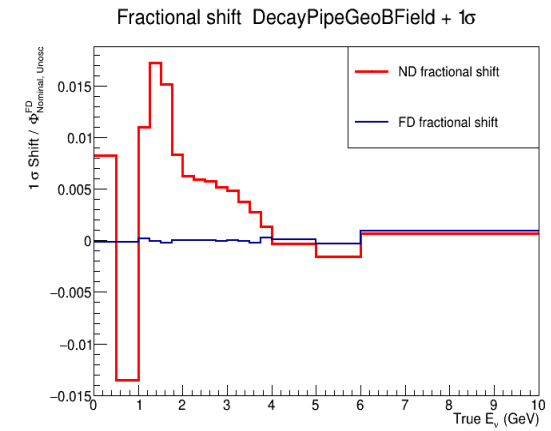
NDDecayPipeGeoBField+ 1 $\sigma$



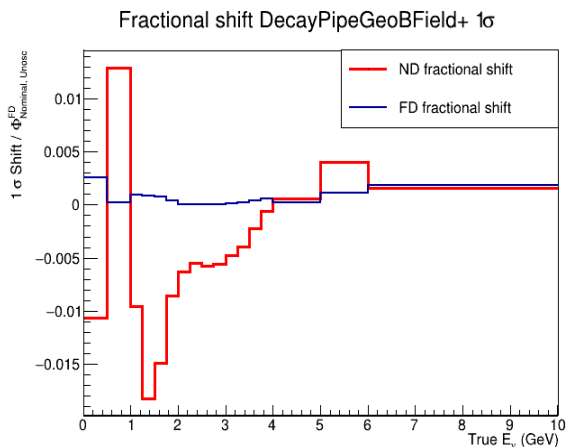
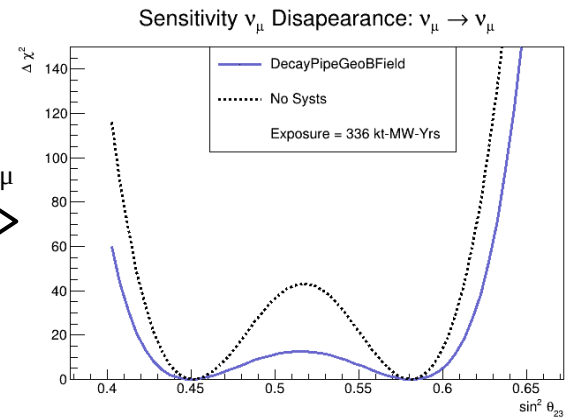


# BACKUP: Decay Pipe Geo BField

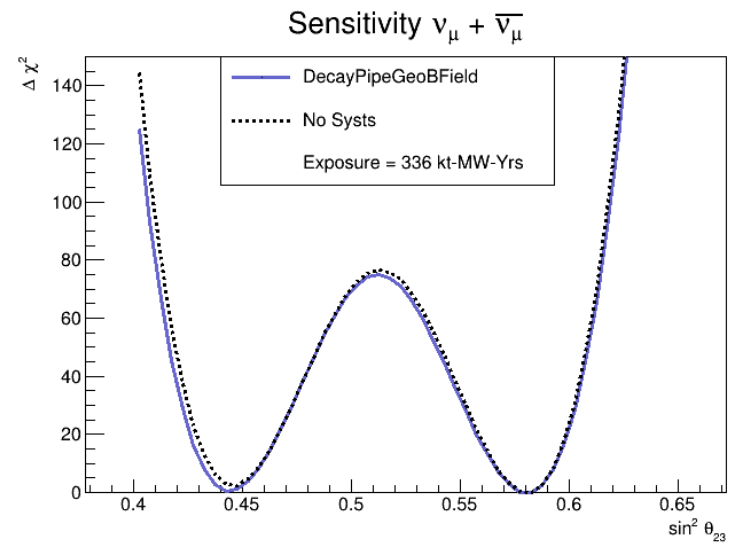
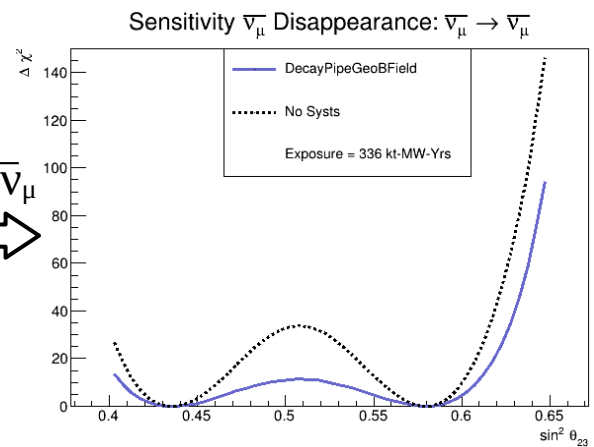
SEMI



$\nu_\mu \rightarrow \nu_\mu$



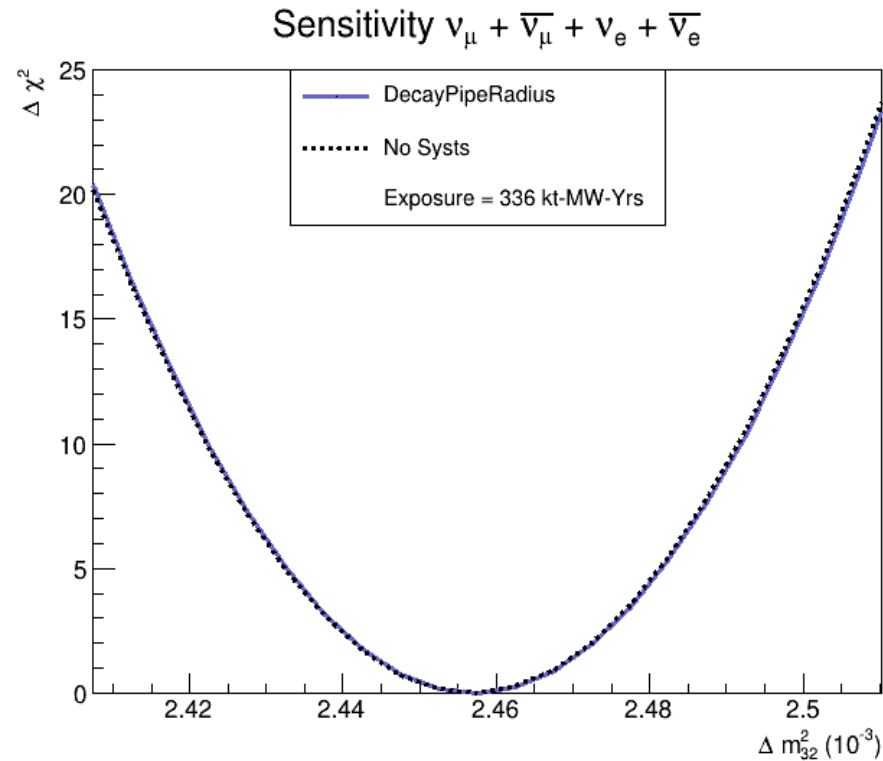
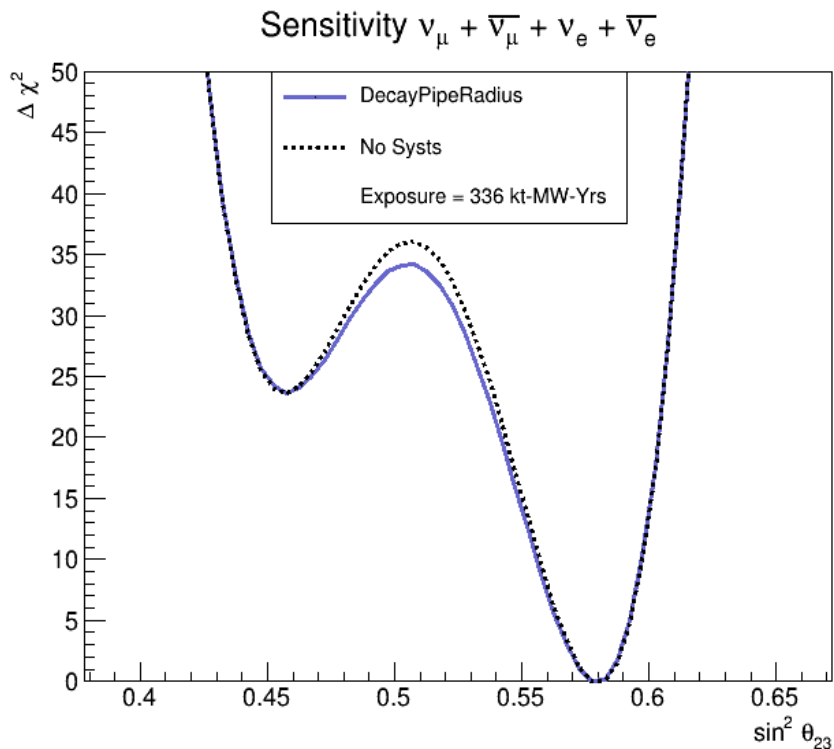
$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$



## Decay Pipe Radius

SEMI

-  $1\sigma$  shift = 2cm: changed from 10 cm (nominal = 2m)



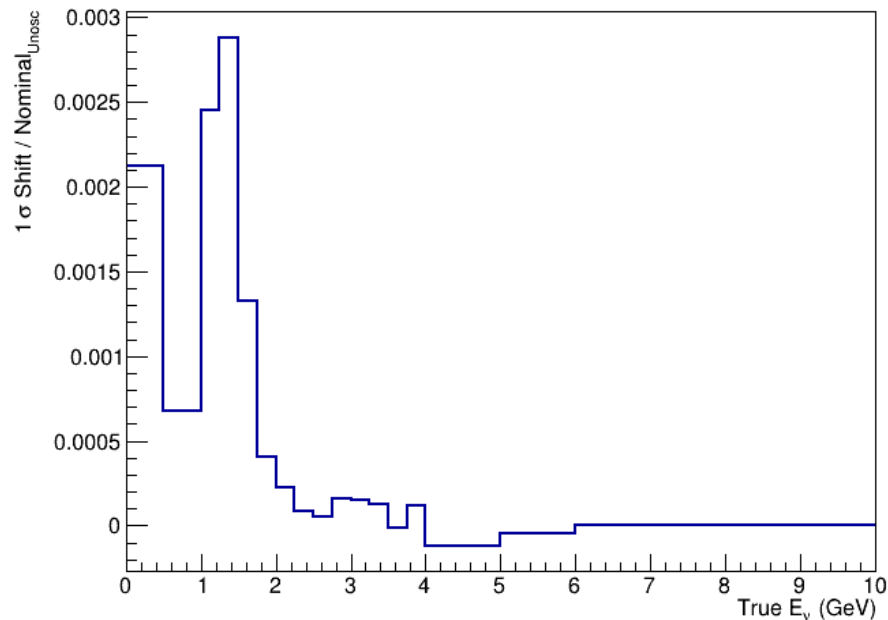
Used to be **IMPORTANT** in the old (Nov17) systematics!

## Decay Pipe Radius

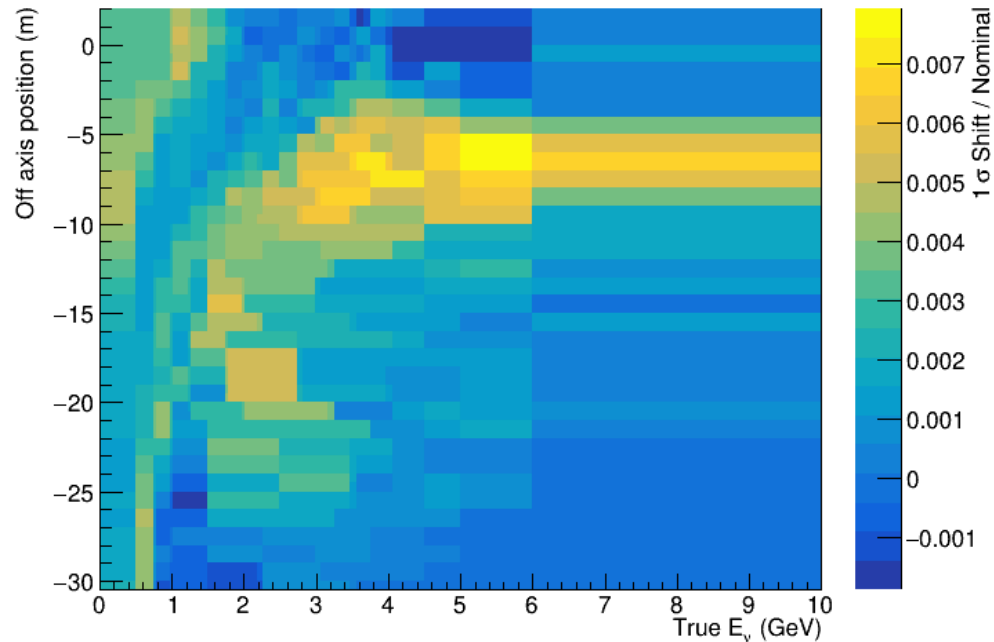
SEMI

-  $1\sigma$  shift = 2cm: changed from 10 cm (nominal = 2m)

FD DecayPipeRadius +  $1\sigma$



ND DecayPipeRadius +  $1\sigma$



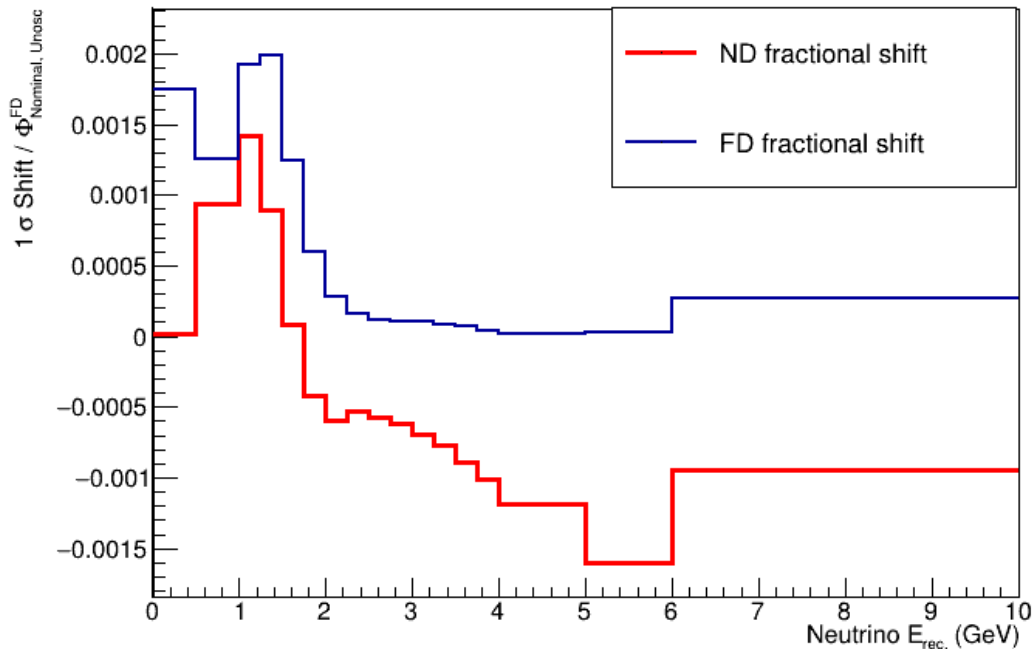
- Comparable ND and FD uncertainties: max. of 0.8%

# Decay Pipe Radius

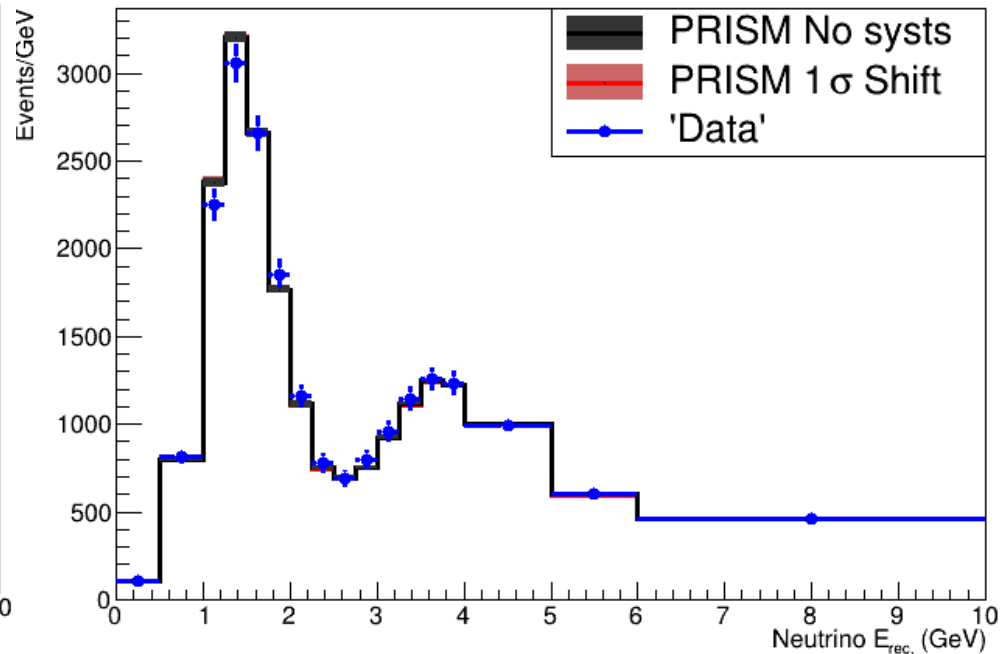
SEMI

-  $1\sigma$  shift = 2cm: changed from 10 cm (nominal = 2m)

Fractional shift DecayPipeRadius+  $1\sigma$



DecayPipeRadius

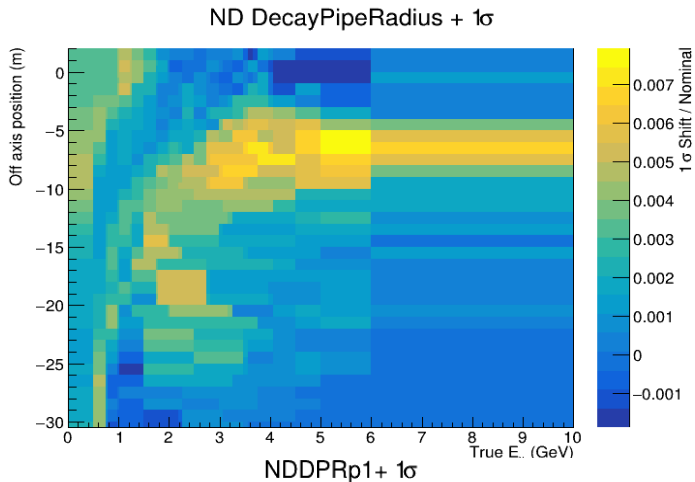


- Maximum difference between PRISM prediction (ND) and FD of  $\approx 0.15\%$

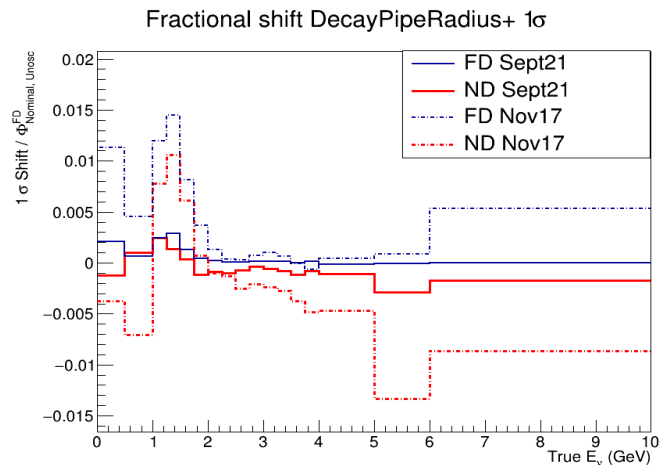
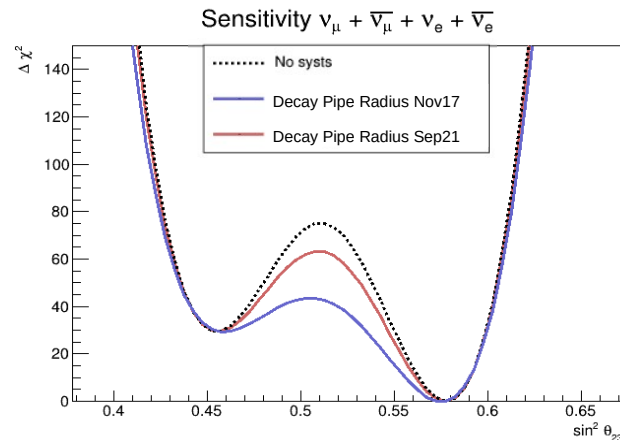
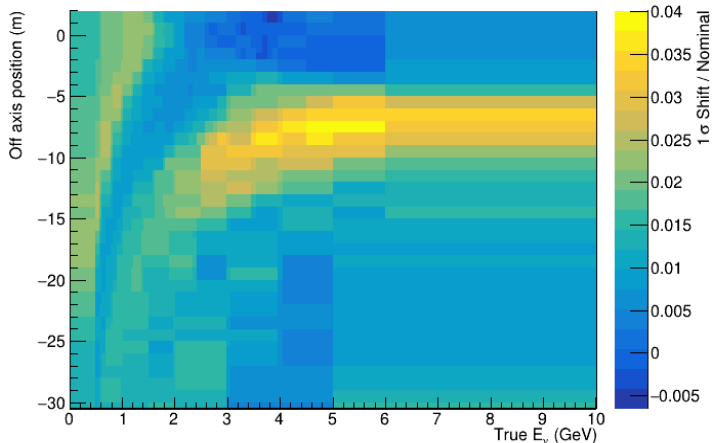
# Decay Pipe Radius → Comparison to Nov17 systematics

SEMI

Sept 21:  
 $1\sigma = 2\text{ cm}$

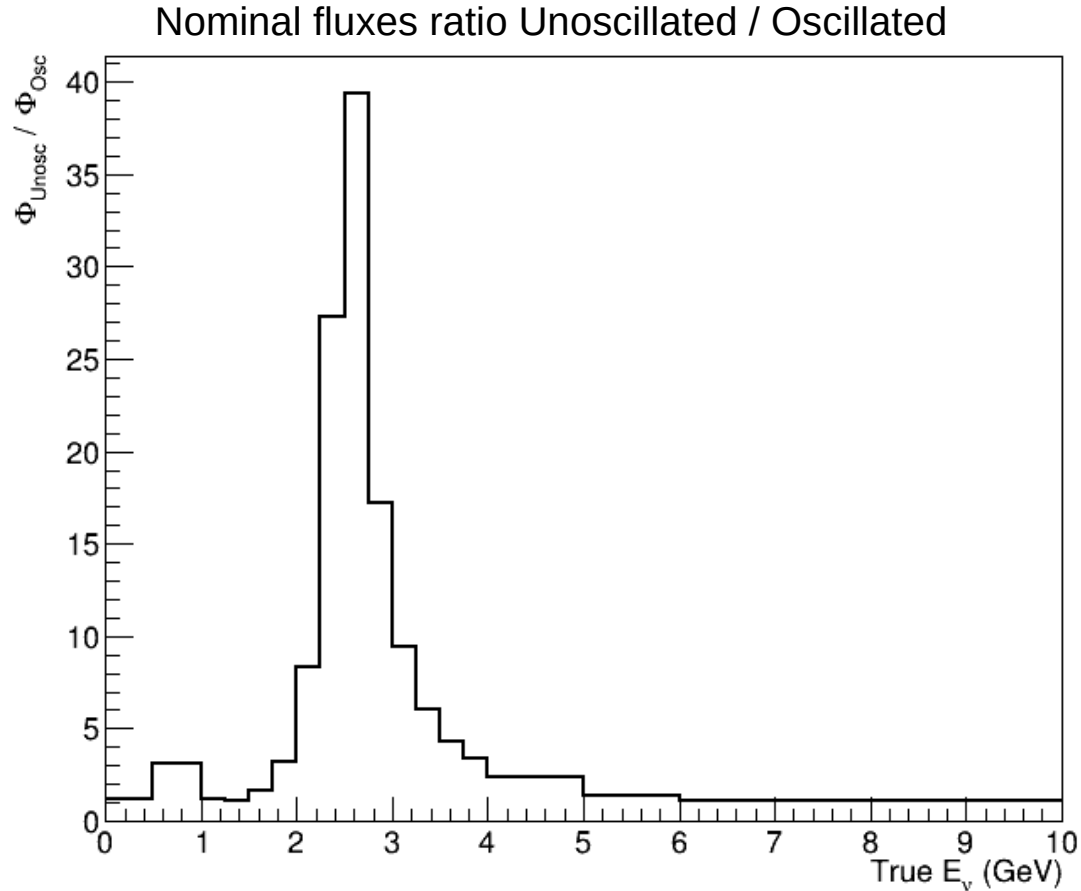


Nov 17:  
 $1\sigma = 10\text{ cm}$



Much smaller uncertainties with the new (Sep 21) systematics → increased sensitivity

# Flux normalization: Unoscillated versus Oscillated



→ if the oscillated flux is chosen as the normalization factor:

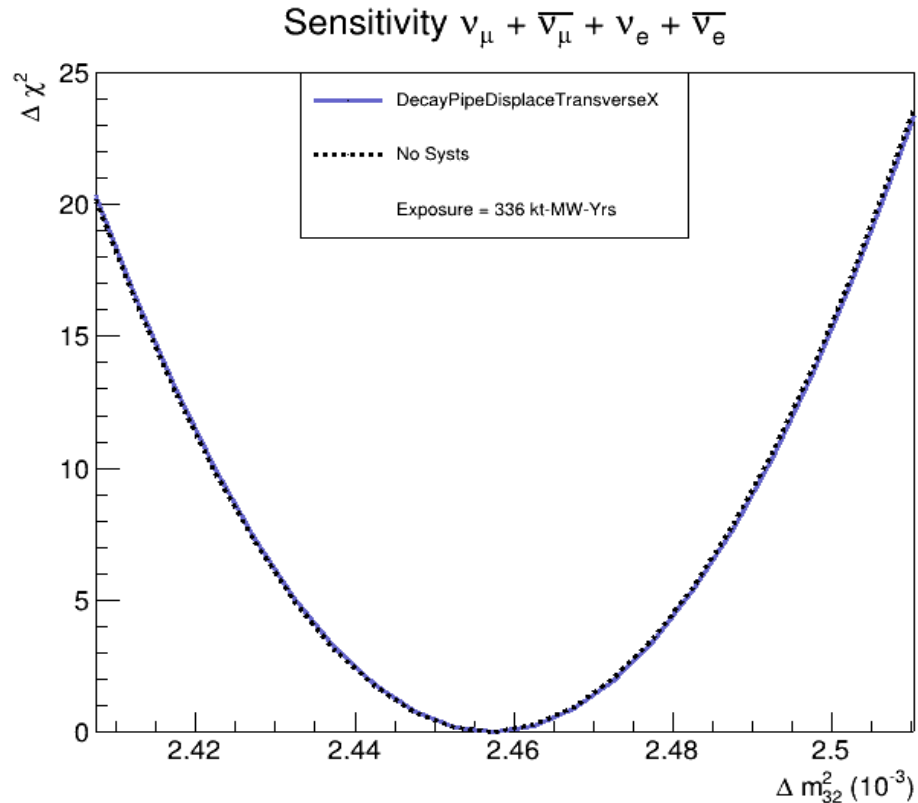
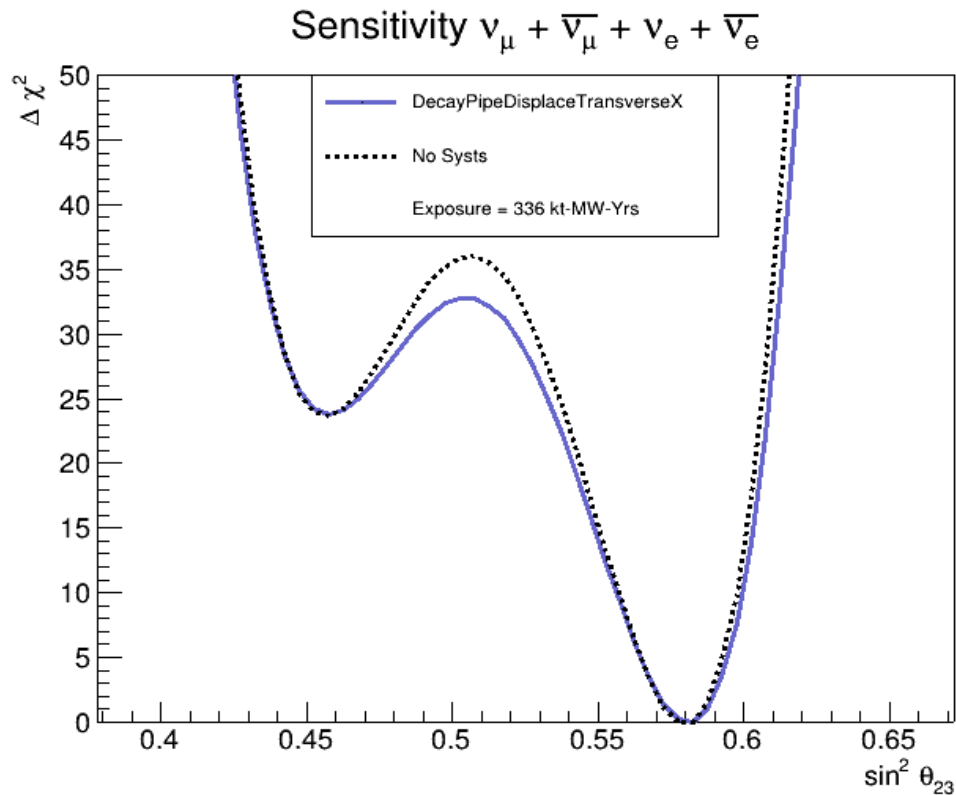
- fractional error a factor of  $\sim 40$  larger
- peak structure @  $\sim 2.6$  GeV

→ FD **unoscillated flux** is used as **normalization factor**

# Decay Pipe Displace Transverse X

SEMI

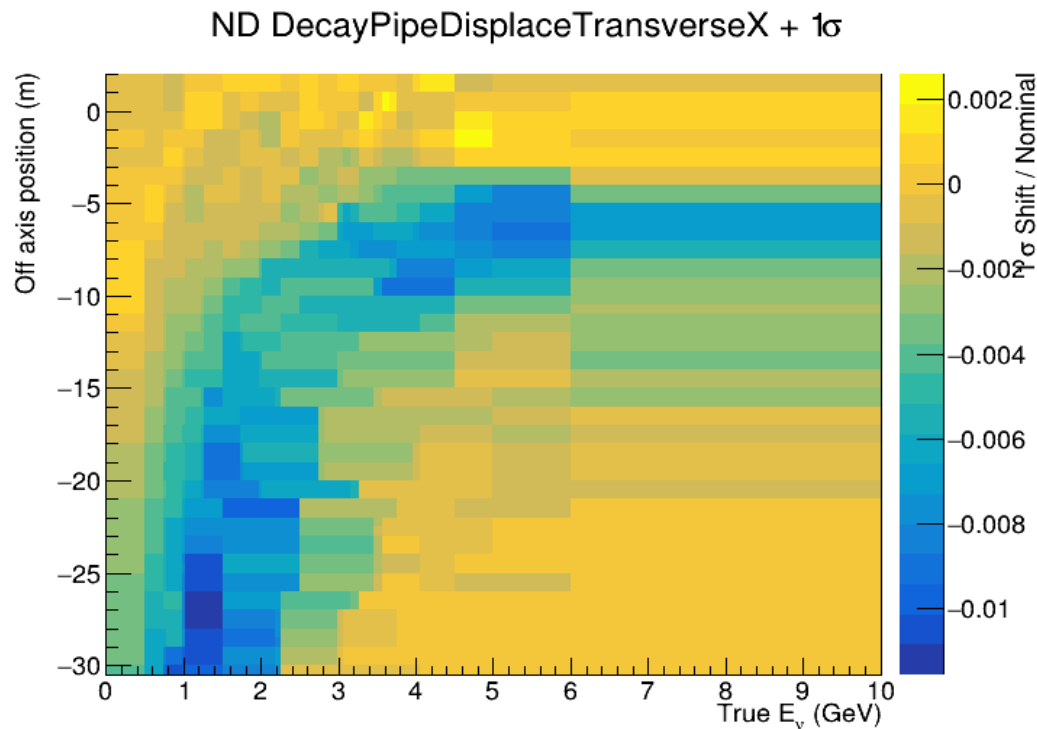
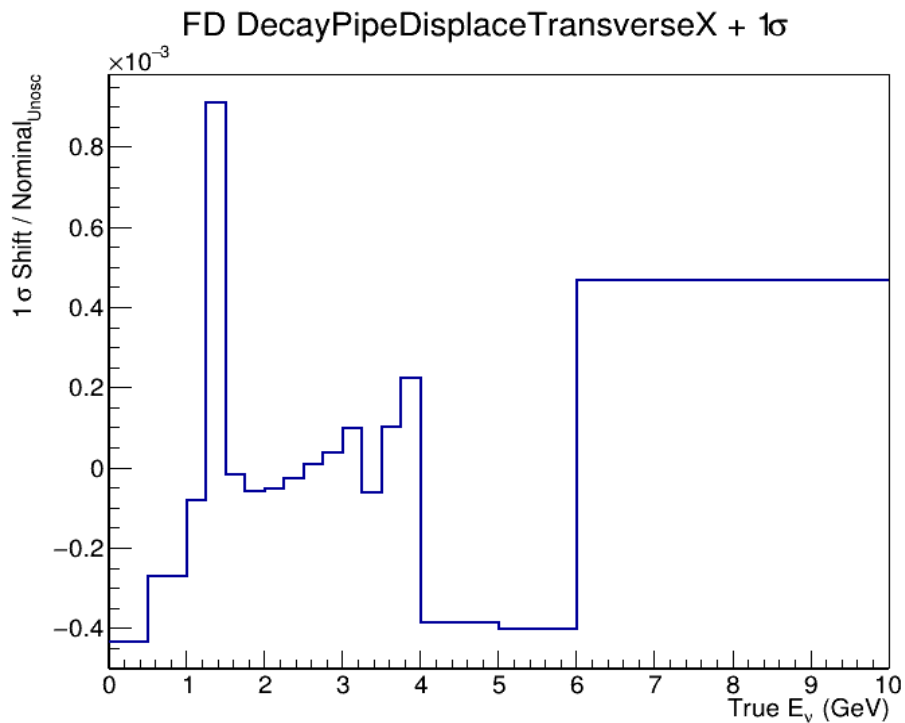
-  $1\sigma$  shift = 2.5 cm



# Decay Pipe Displace Transverse X

SEMI

-  $1\sigma$  shift = 2.5 cm



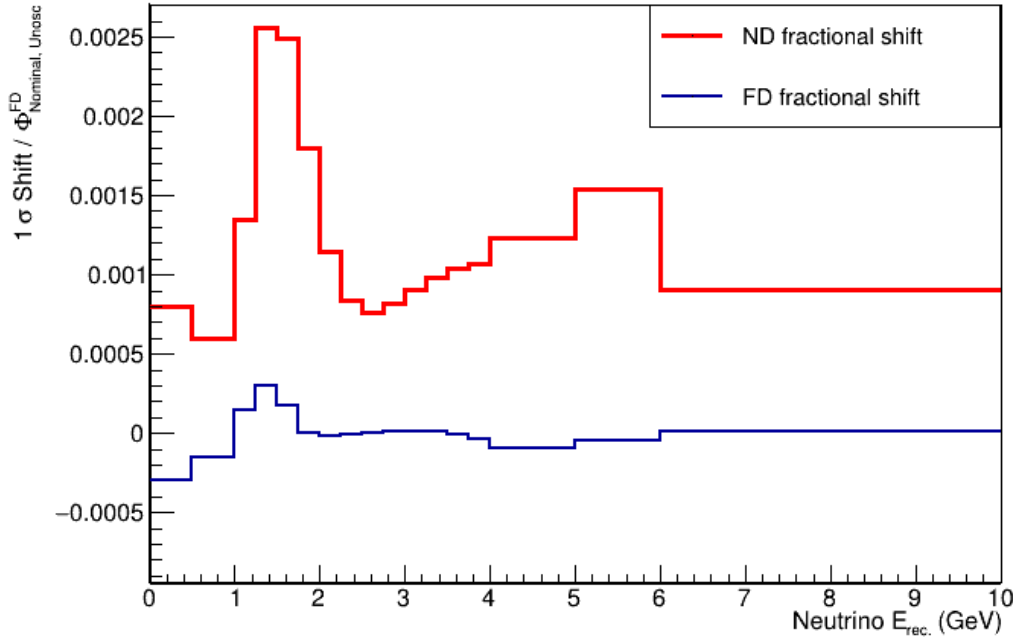


# Decay Pipe Displace Transverse X

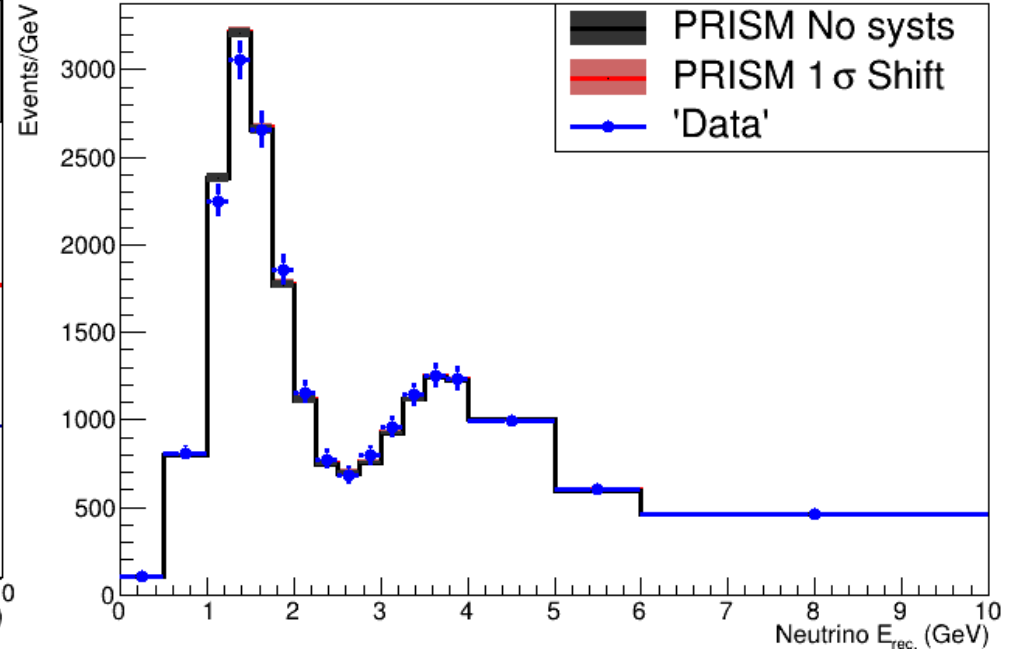
SEMI

-  $1\sigma$  shift = 2.5 cm

Fractional shift DecayPipeDisplaceTransverseX+  $1\sigma$



DecayPipeDisplaceTransverseX

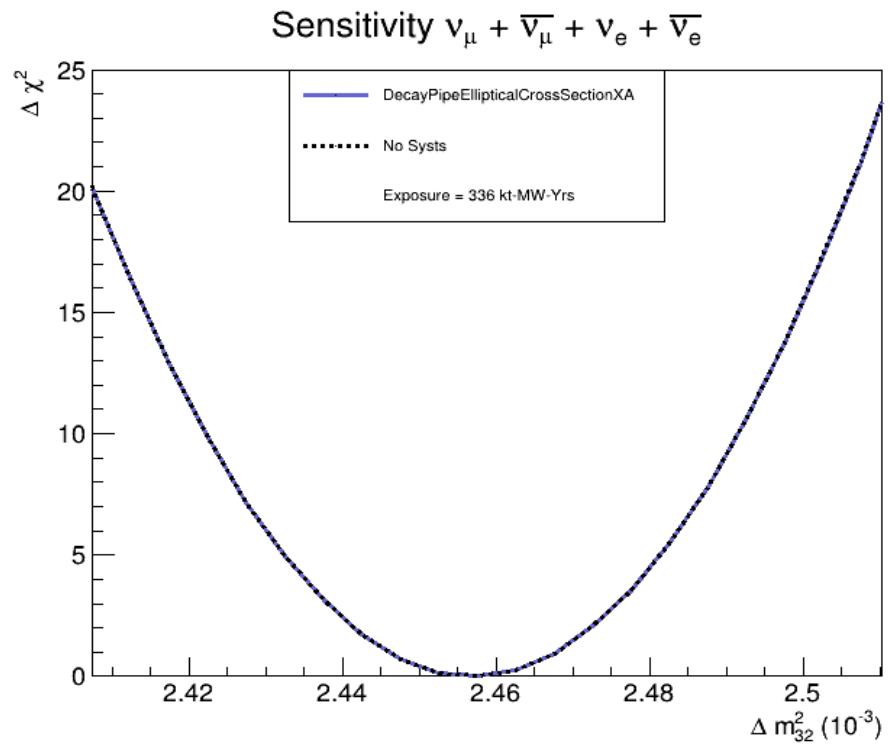
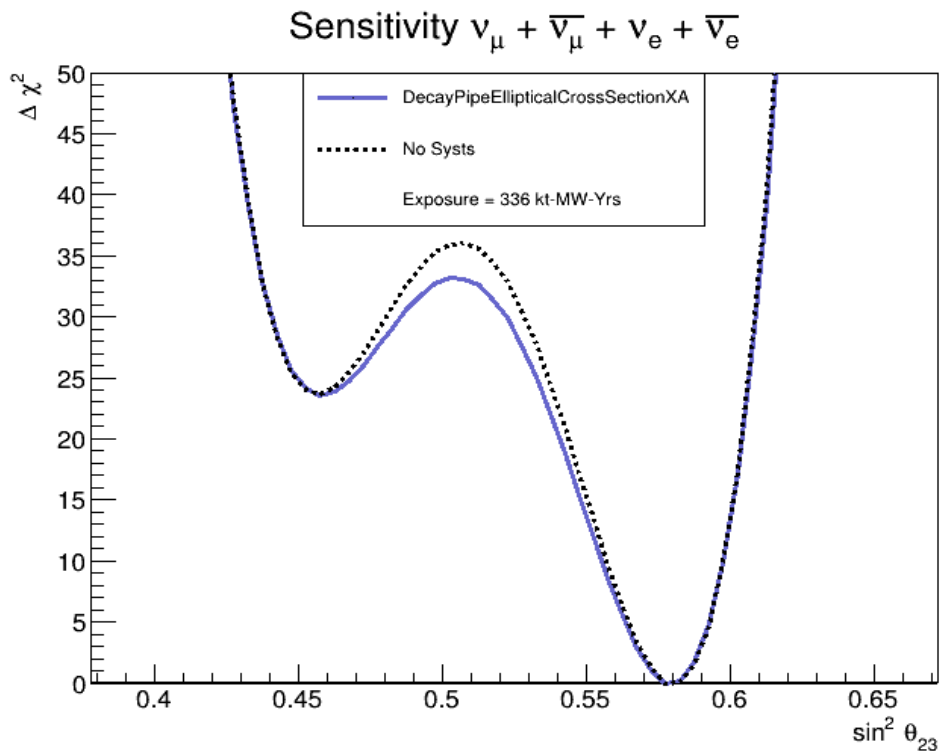


- Maximum difference between PRISM prediction (ND) and FD of  $\approx 0.25\%$  (larger than in the case of decay pipe radius  $\rightarrow$  stronger sensitivity reduction)

# Decay Pipe Elliptical Cross Section X A

SEMI

-  $1\sigma$  shift = 2.5 cm: ellipse with A (x-axis) varied while the other dimension fixed to nominal radius

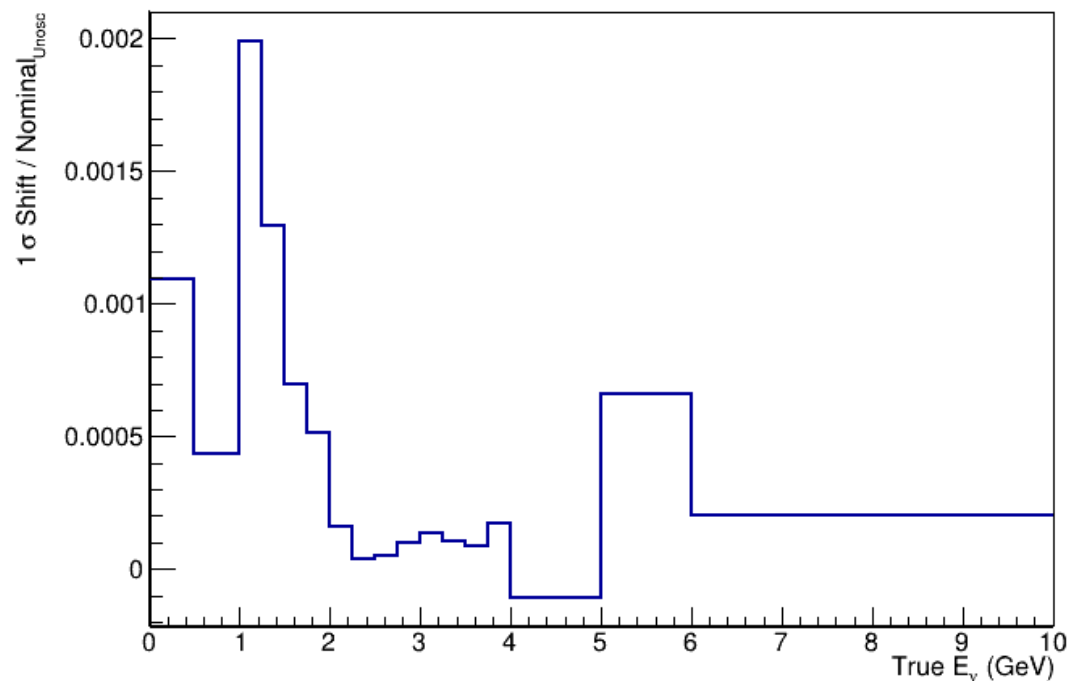


# Decay Pipe Elliptical Cross Section X A

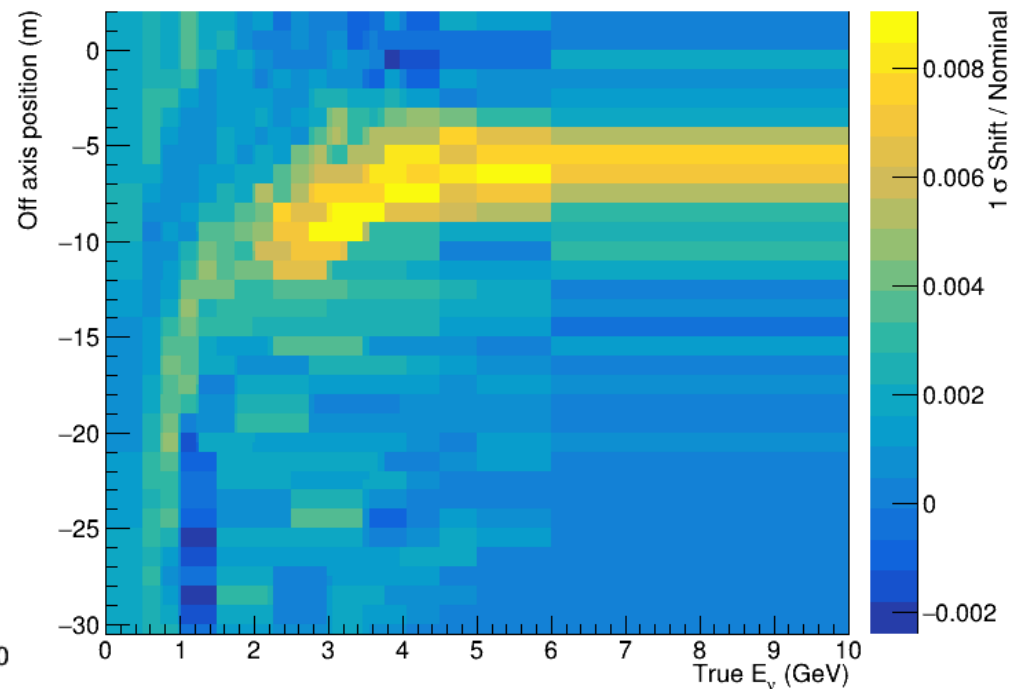
SEMI

-  $1\sigma$  shift = 2.5 cm: ellipse with A (x-axis) varied while the other dimension fixed to nominal radius

FD DecayPipeEllipticalCrossSectionXA +  $1\sigma$



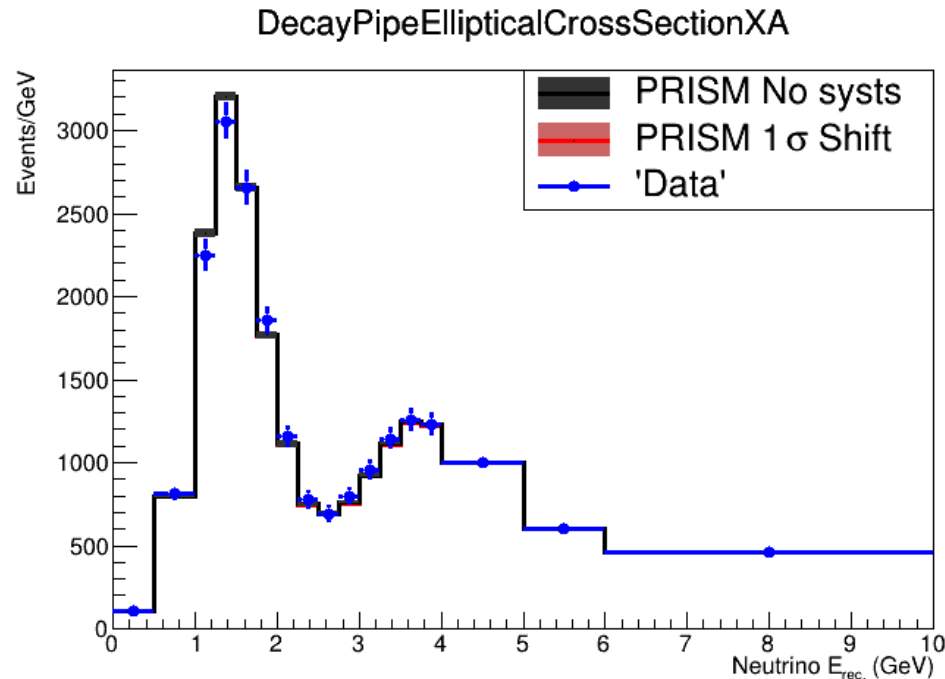
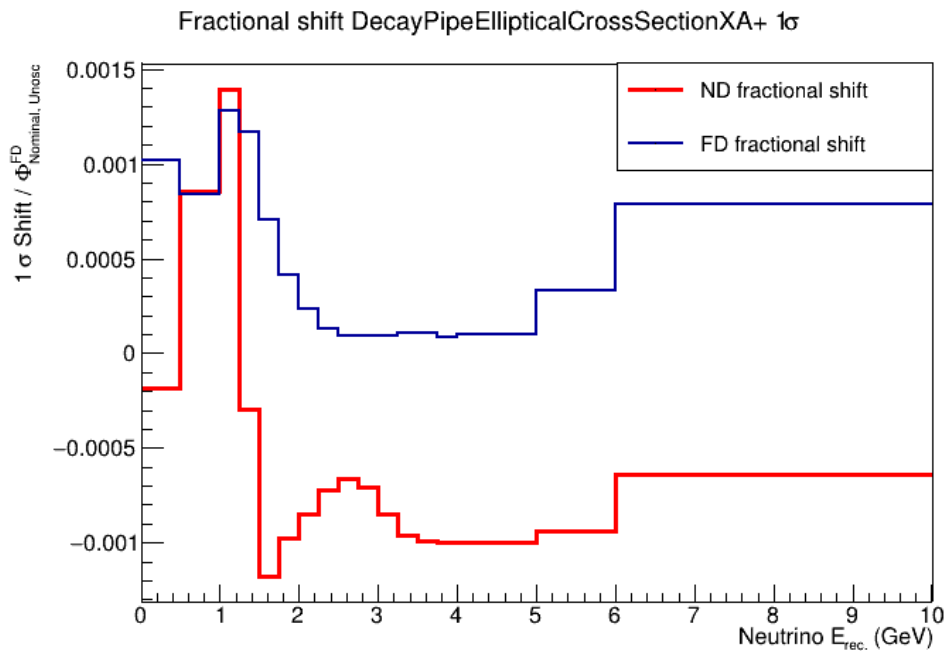
ND DecayPipeEllipticalCrossSectionXA +  $1\sigma$



# Decay Pipe Elliptical Cross Section X A

SEMI

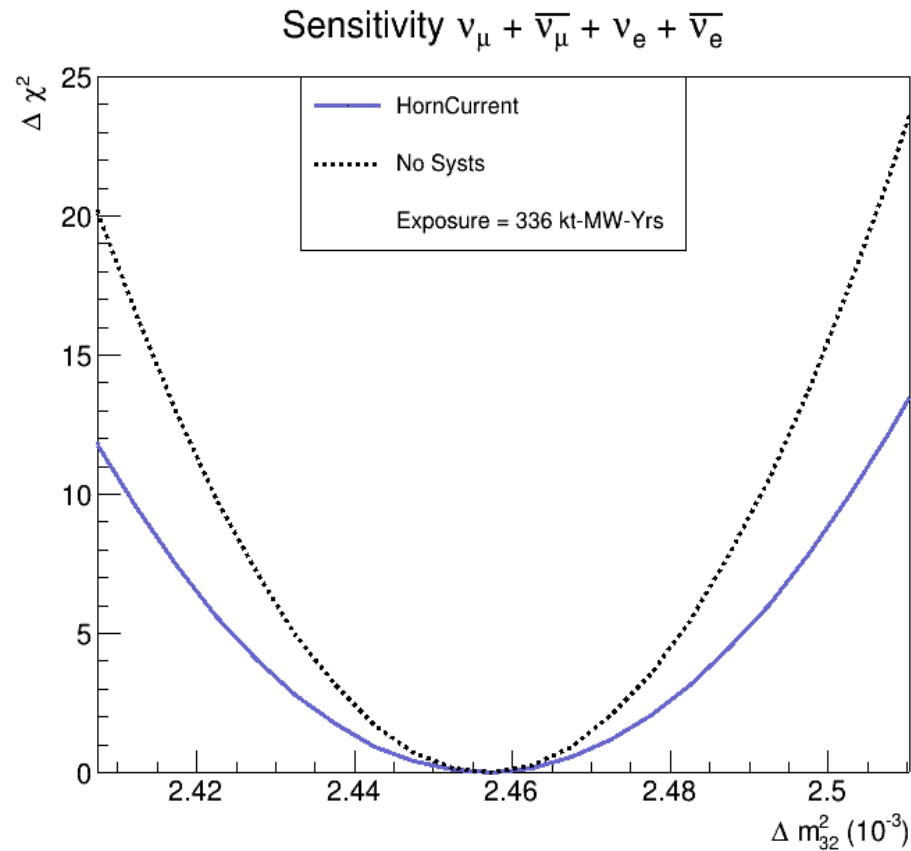
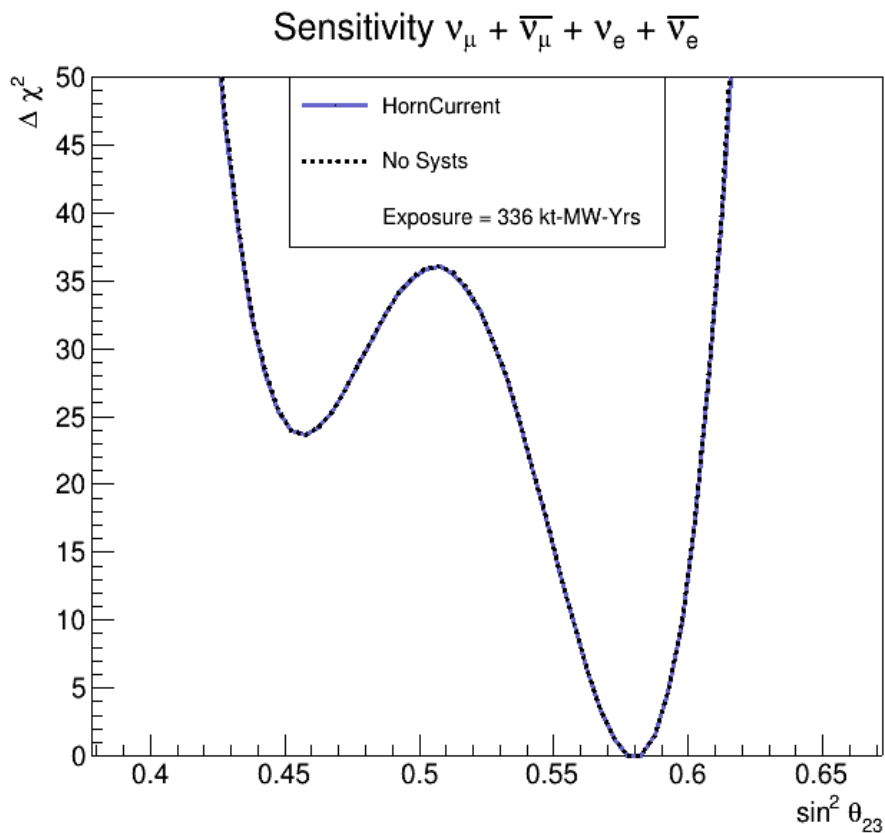
-  $1\sigma$  shift = 2.5 cm: ellipse with A (x-axis) varied while the other dimension fixed to nominal radius



# Horn Current

**IMPORTANT**

-  $1\sigma$  shift = 1% (3kA): simultaneous change to all 3 horns

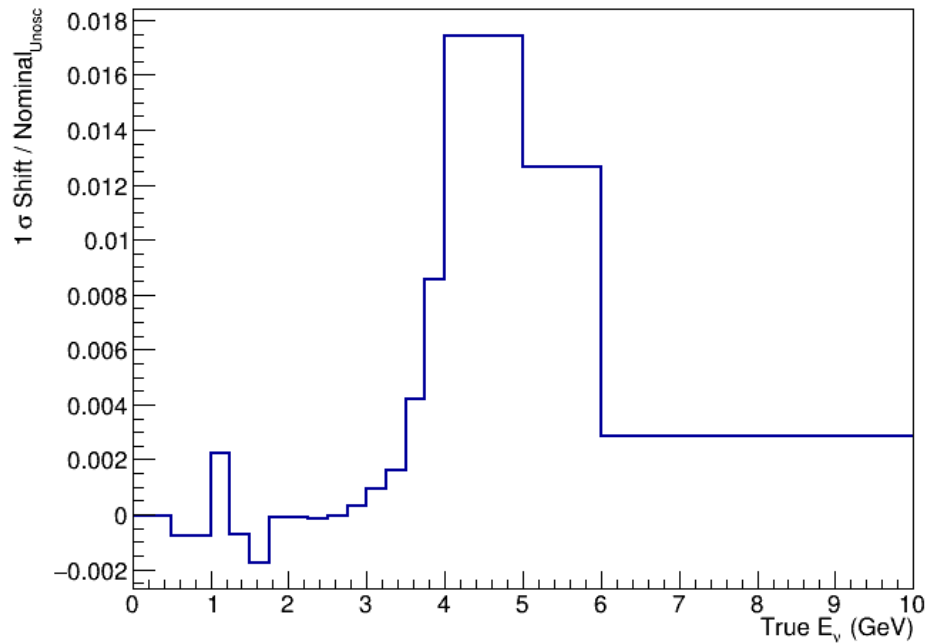


# Horn Current

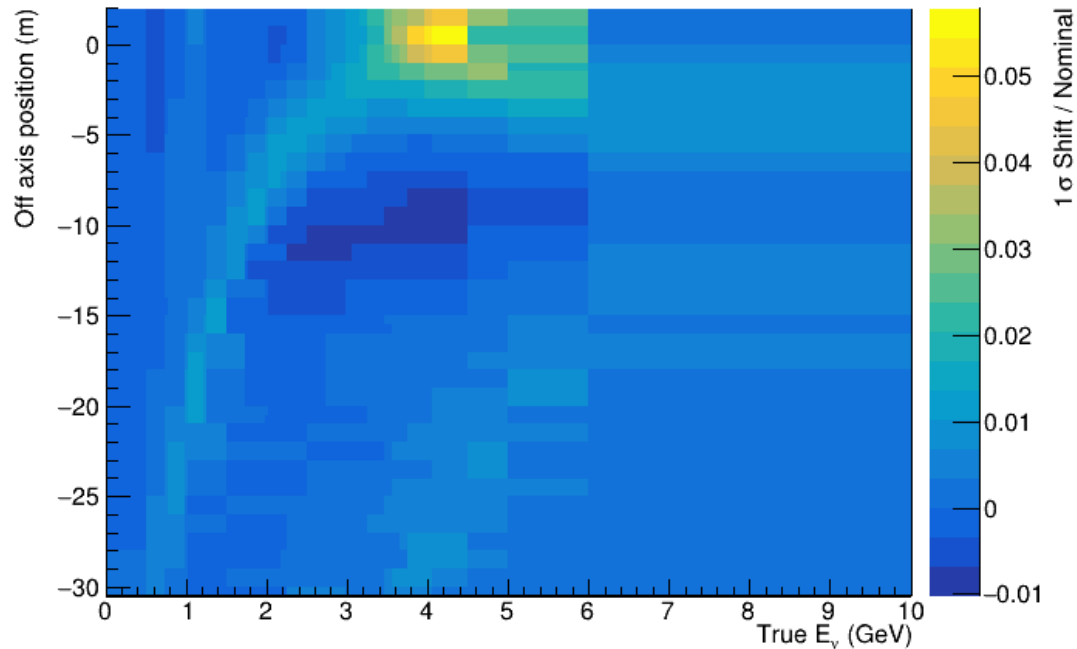
**IMPORTANT**

-  $1\sigma$  shift = 1% (3kA): simultaneous change to all 3 horns

FD HornCurrent +  $1\sigma$



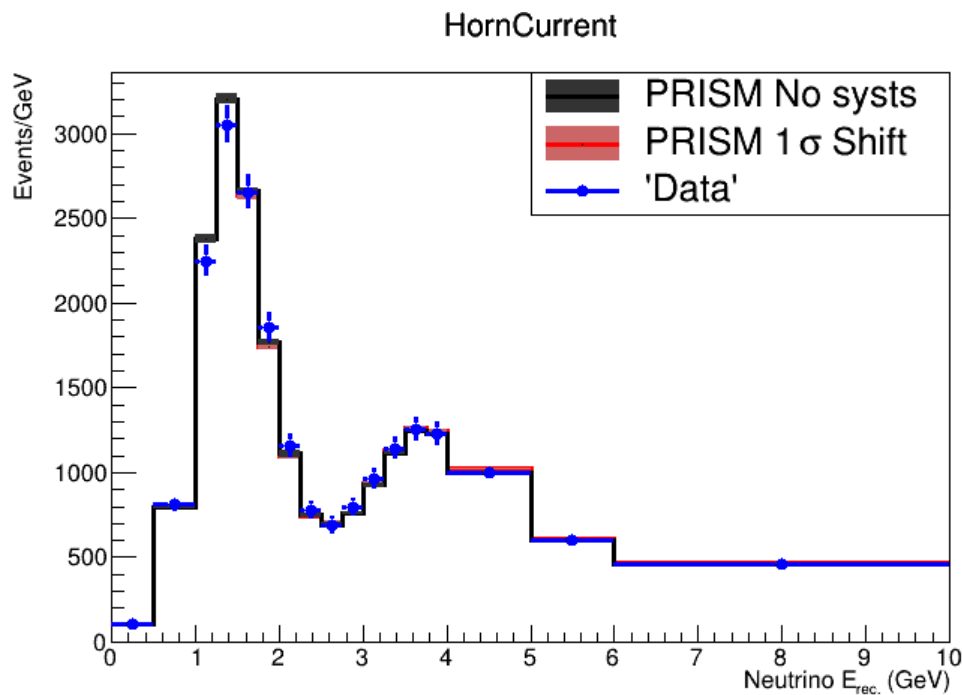
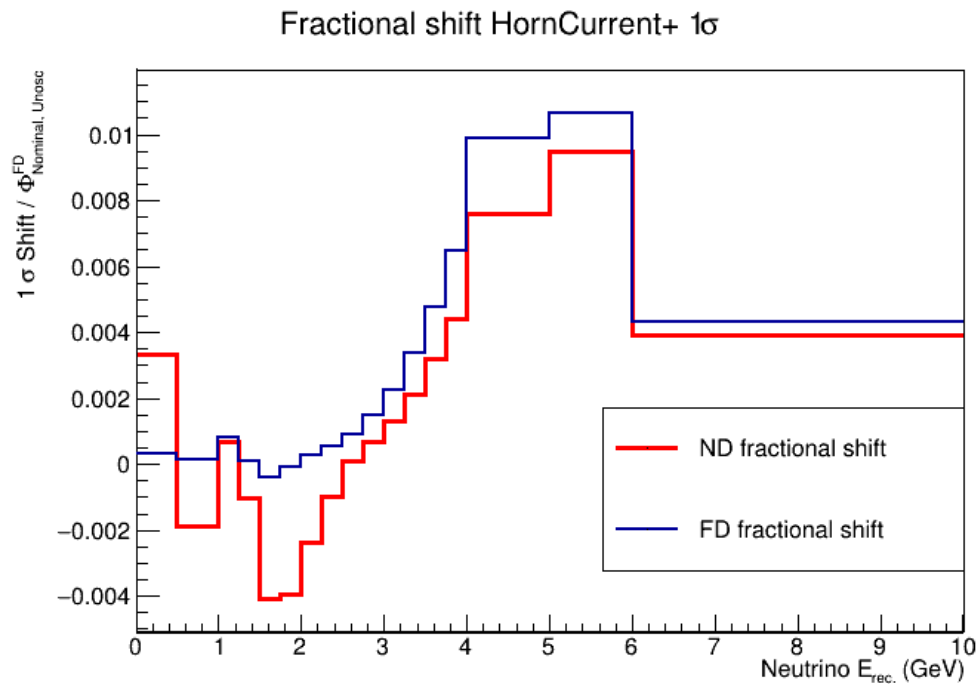
ND HornCurrent +  $1\sigma$



# Horn Current

**IMPORTANT**

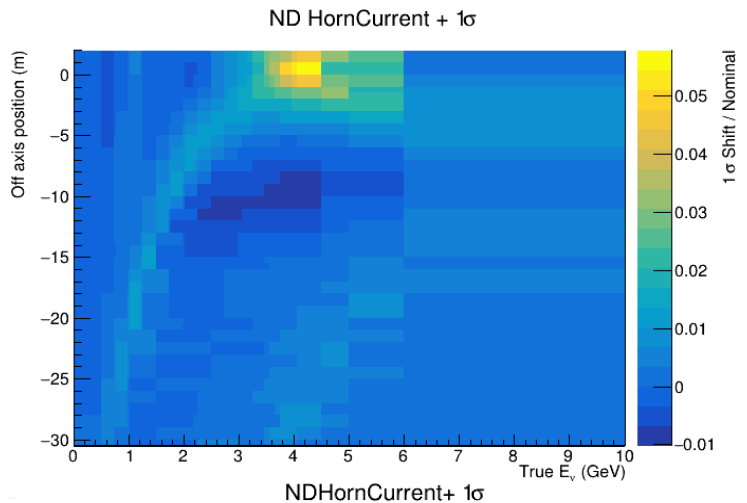
-  $1\sigma$  shift = 1% (3kA): simultaneous change to all 3 horns



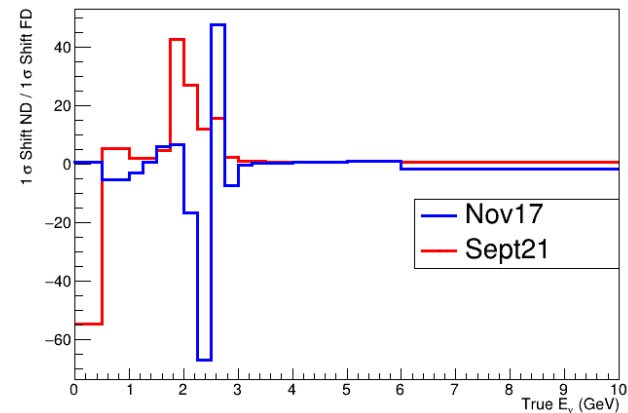
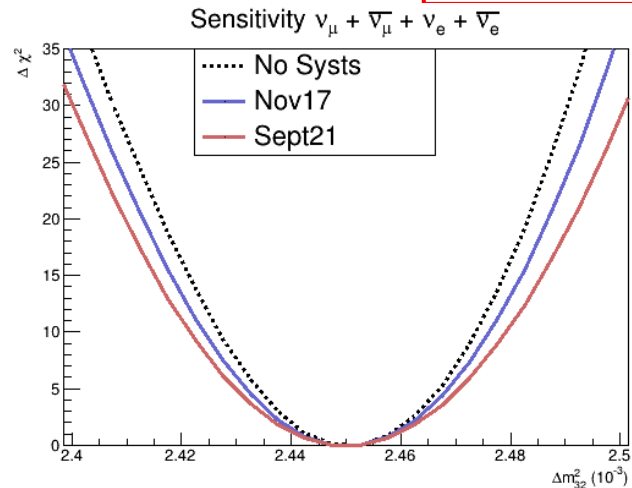
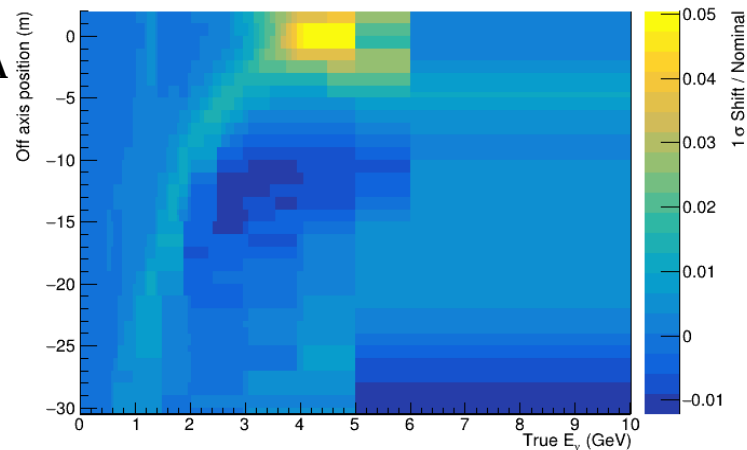
# Horn Current → Comparison to Nov17 systematics

**IMPORTANT**

**Sept21:**  
**1 $\sigma$  shift = 3kA**



**Nov17:**  
**1 $\sigma$  shift = 2.93kA**

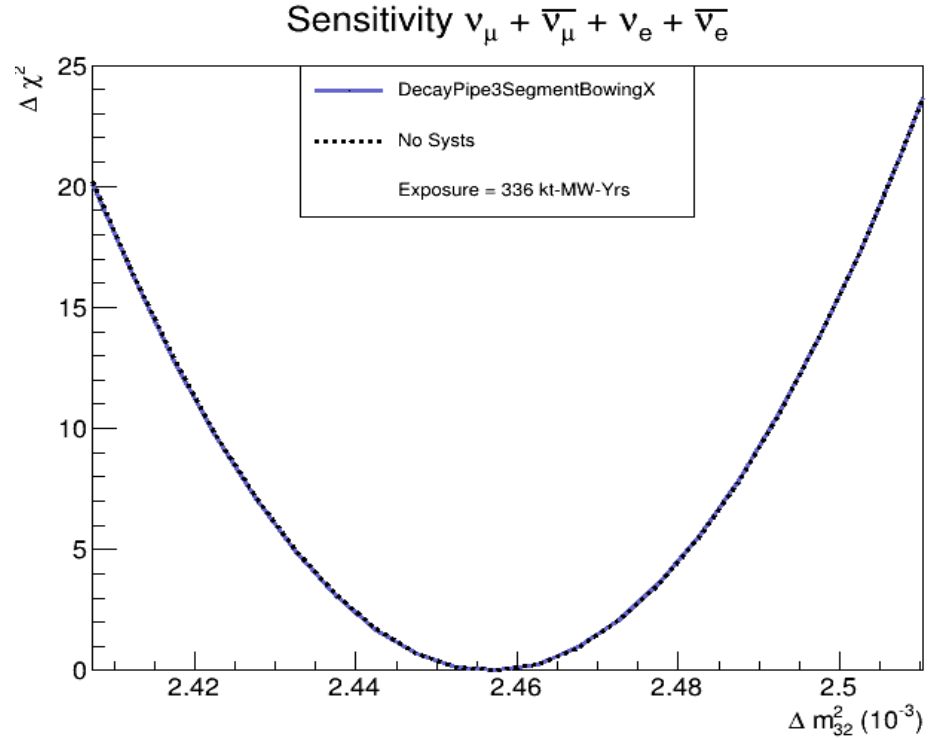
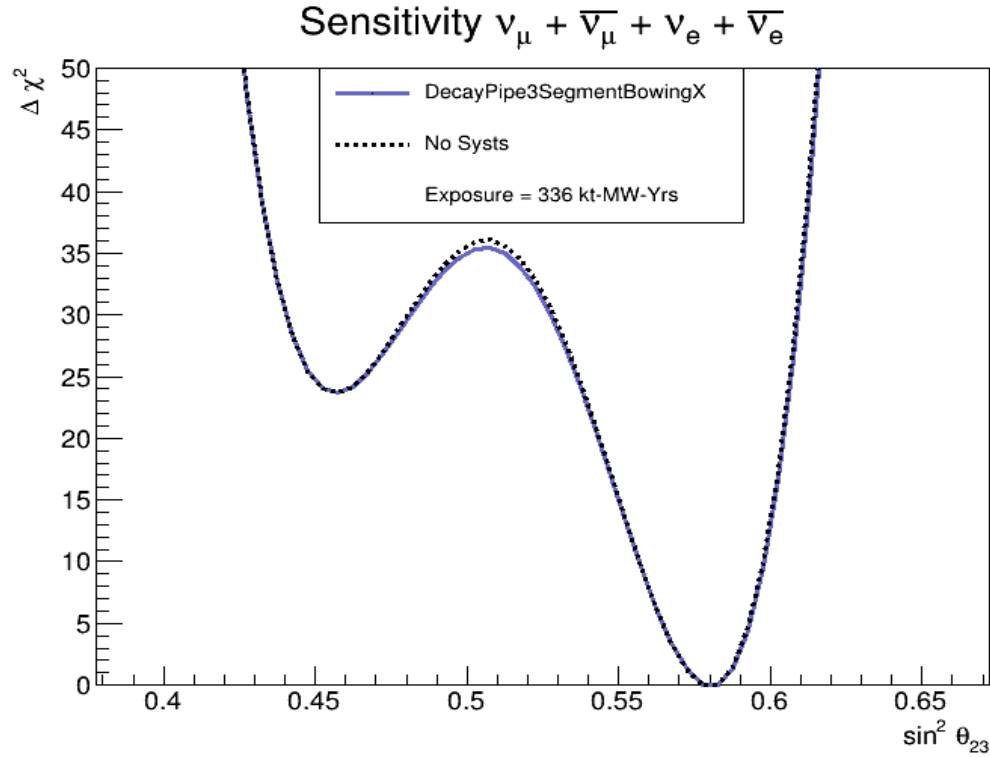




# Decay Pipe 3 Segment Bowing X

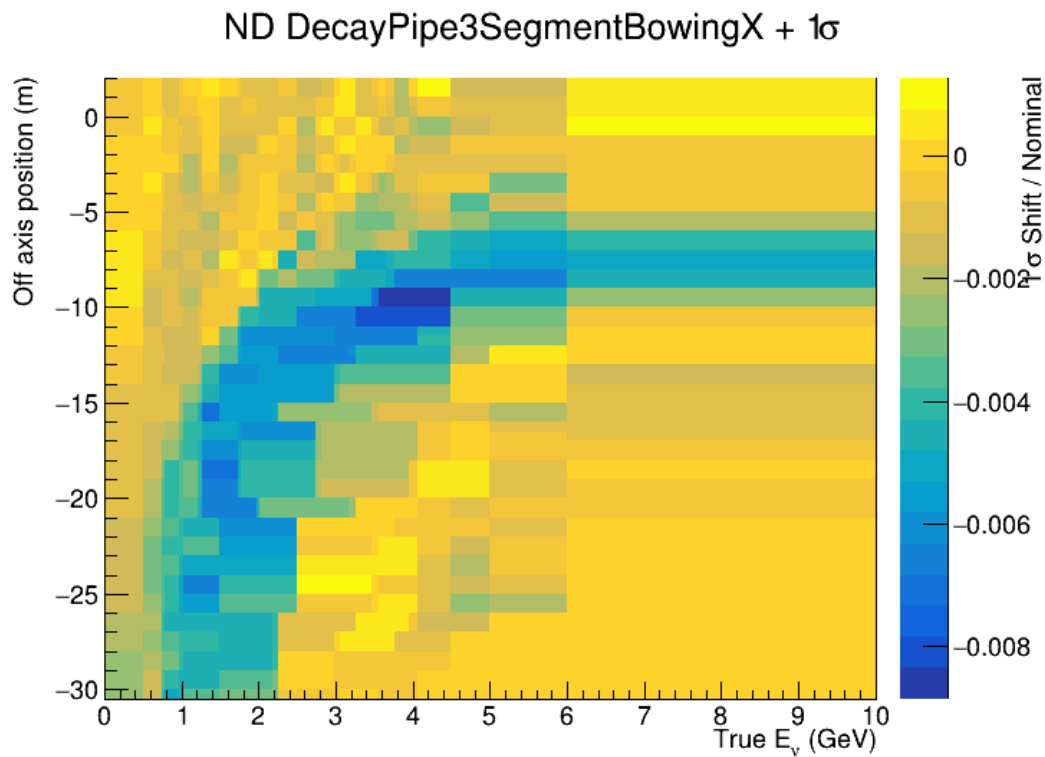
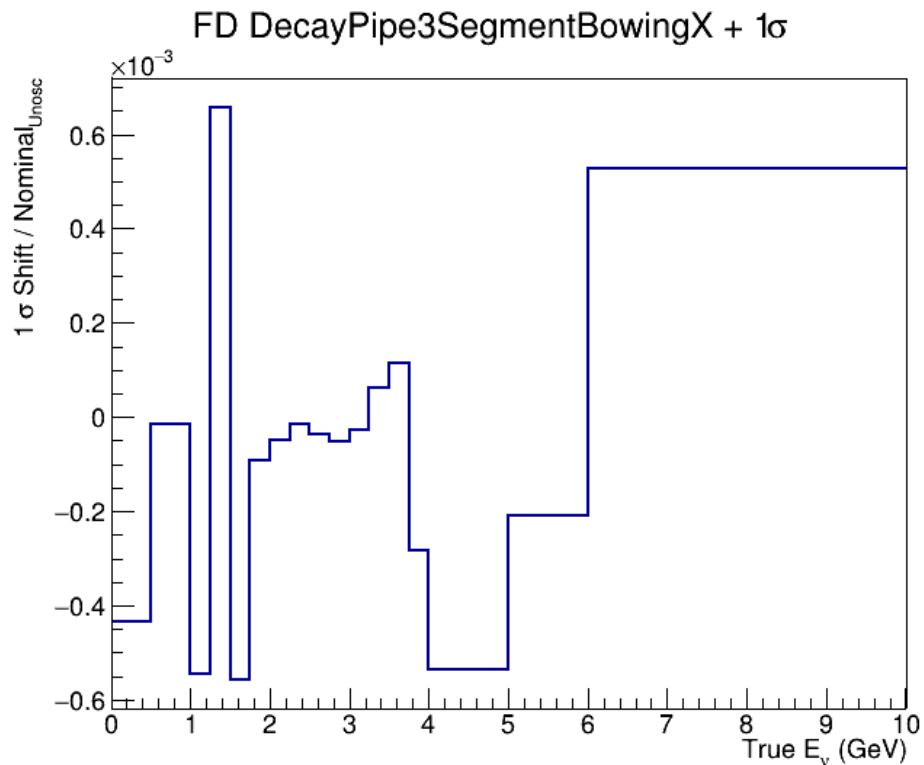
SEMI

-  $1\sigma$  shift = 2.5cm: decay pipe segmented into 3 equal pieces; the central piece is transverse shifted by tolerance



# Decay Pipe 3 Segment Bowing X

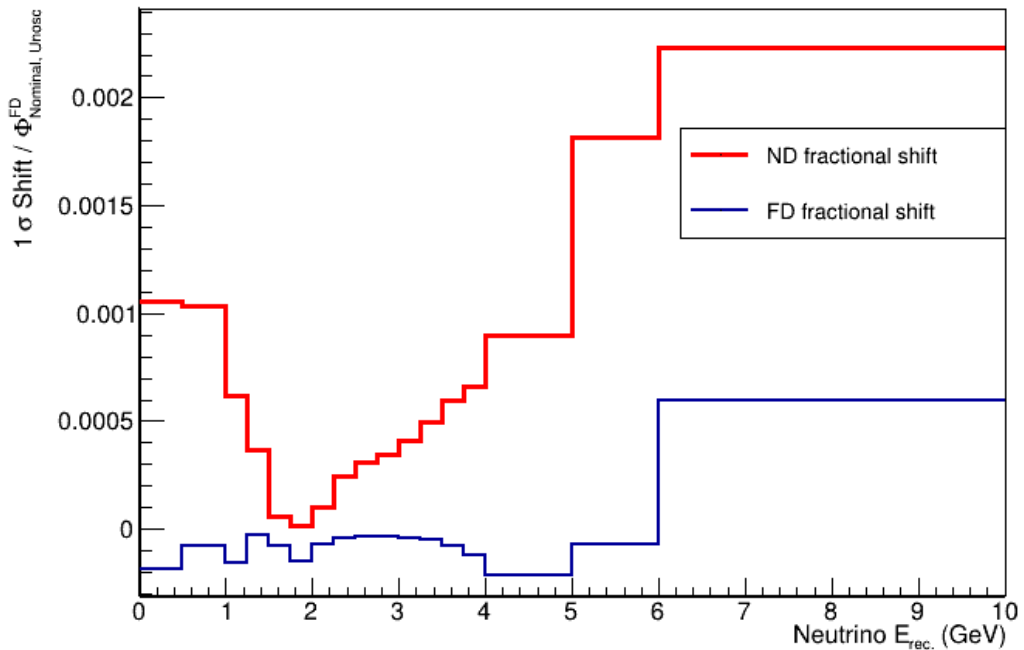
-  $1\sigma$  shift = 2.5cm: decay pipe segmented into 3 equal pieces; the central piece is transverse shifted by tolerance



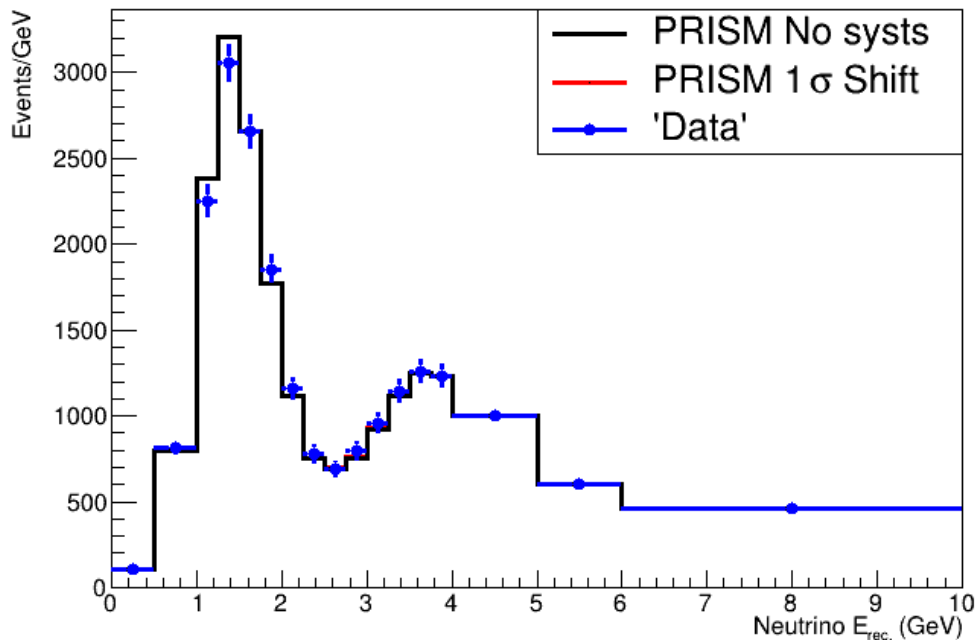
# Decay Pipe 3 Segment Bowing X

-  $1\sigma$  shift = 2.5cm: decay pipe segmented into 3 equal pieces; the central piece is transverse shifted by tolerance

Fractional shift DecayPipe3SegmentBowingX+  $1\sigma$



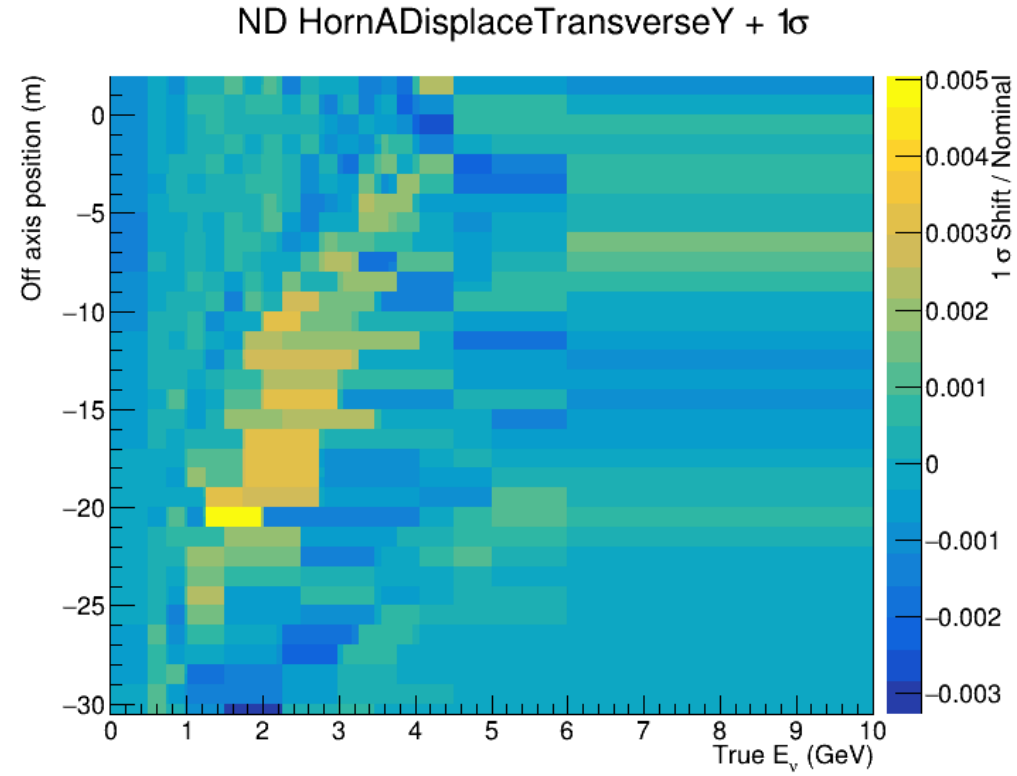
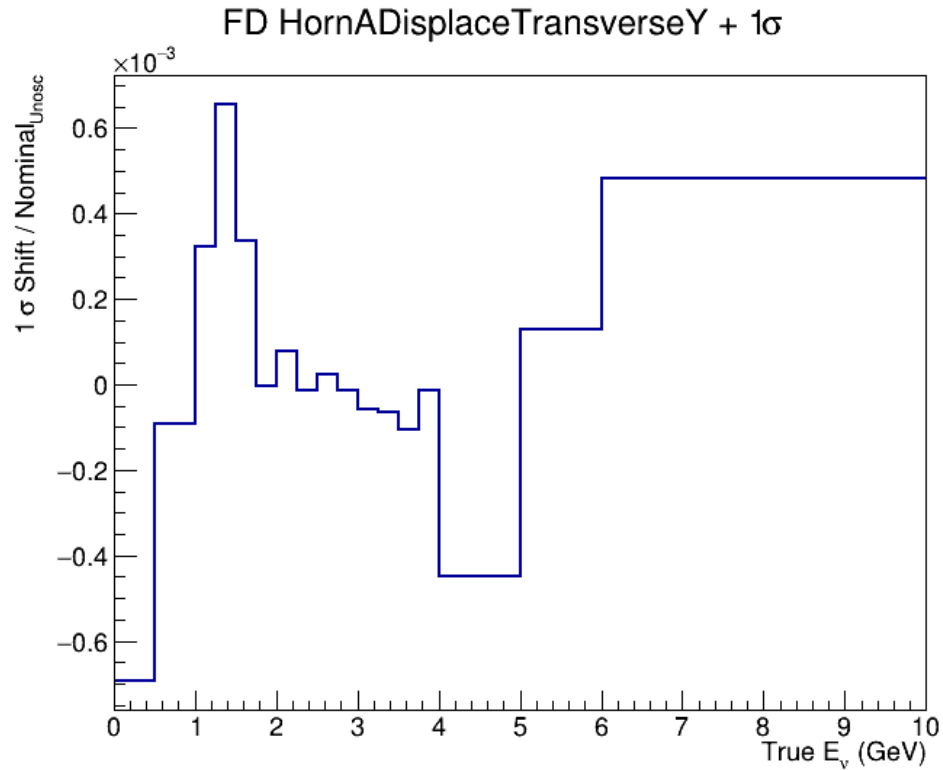
DecayPipe3SegmentBowingX



# Horn A Displace Transverse Y

NEGLIGIBLE

-  $1\sigma$  shift = 0.5 mm

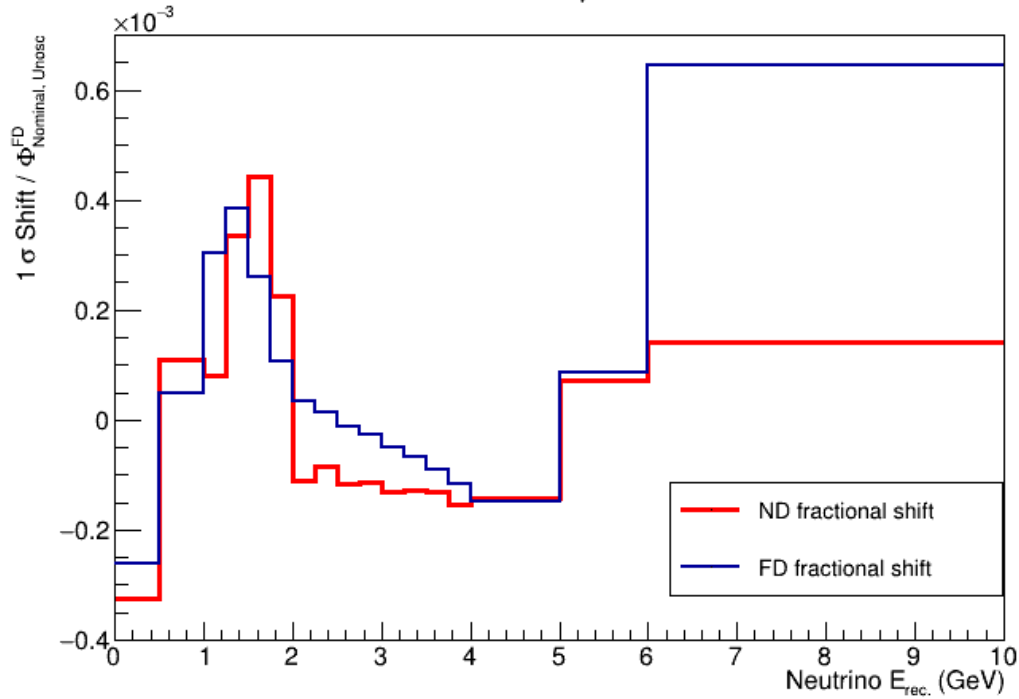


# Horn A Displace Transverse Y

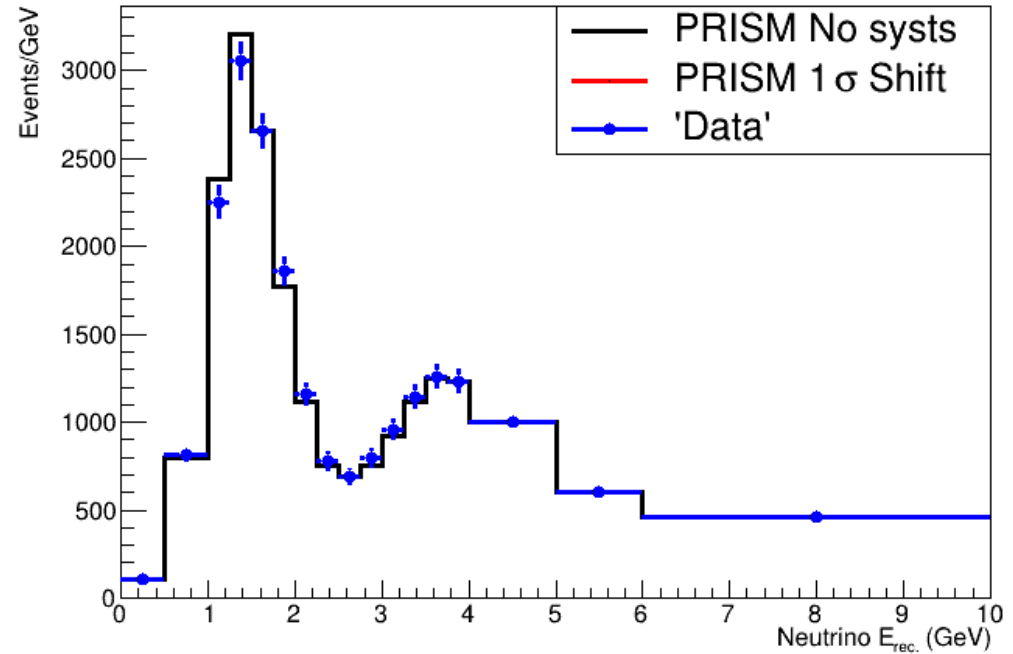
NEGLIGIBLE

-  $1\sigma$  shift = 0.5 mm

Fractional shift HornADisplaceTransverseY+  $1\sigma$

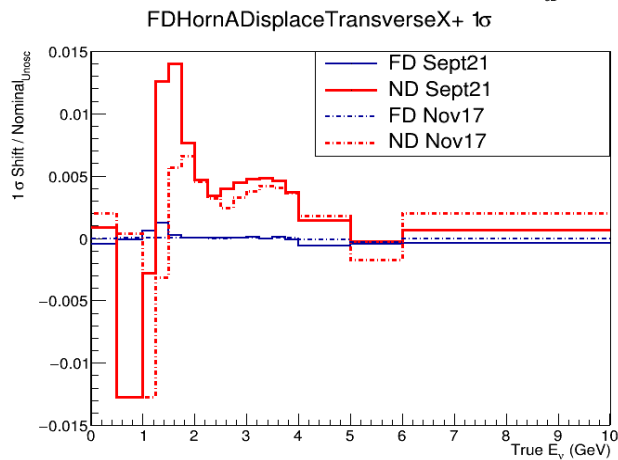
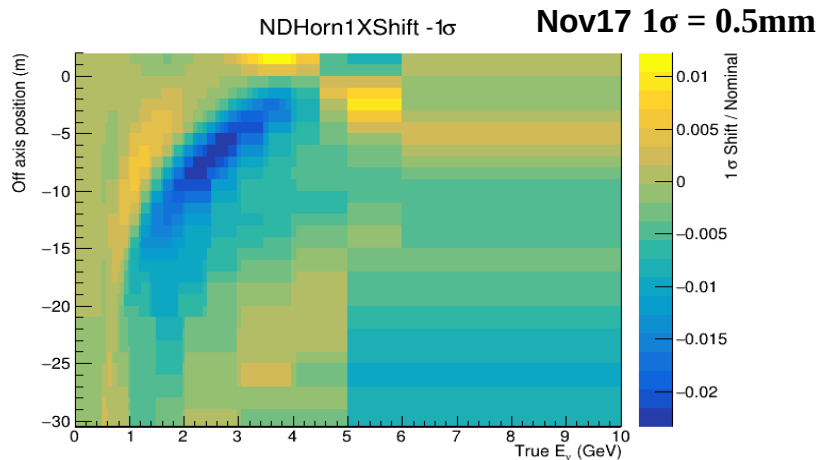
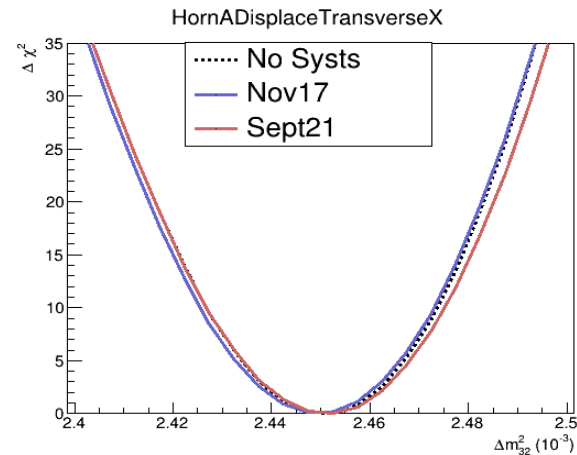
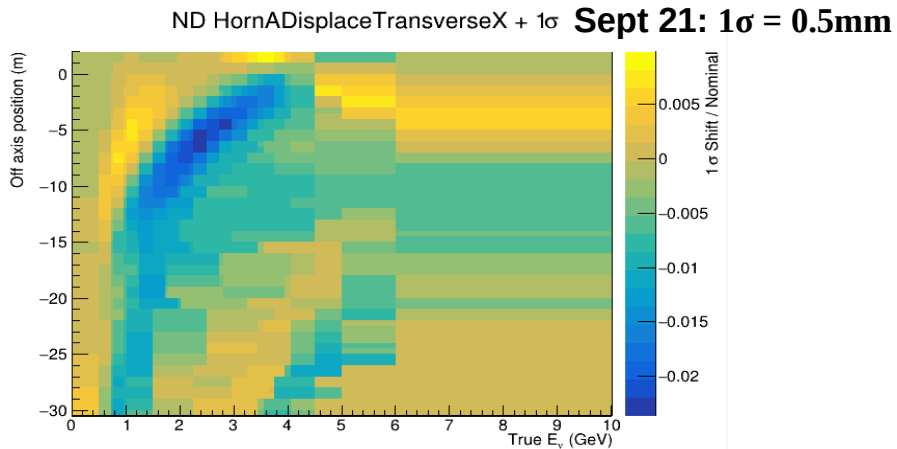


HornADisplaceTransverseY



# Horn A Displace Transverse X → comparison to Nov17 systs

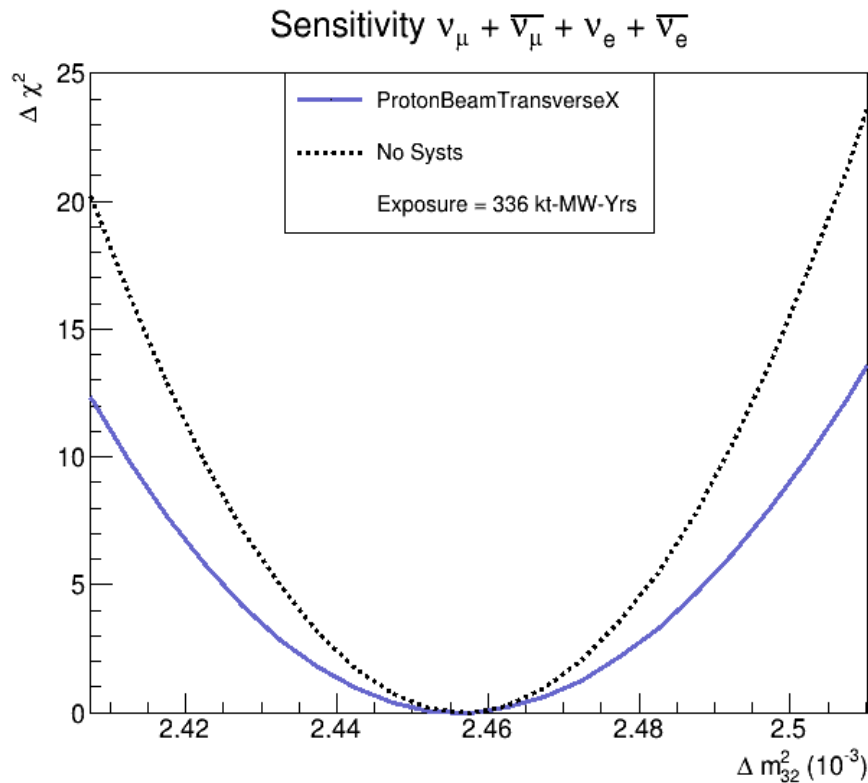
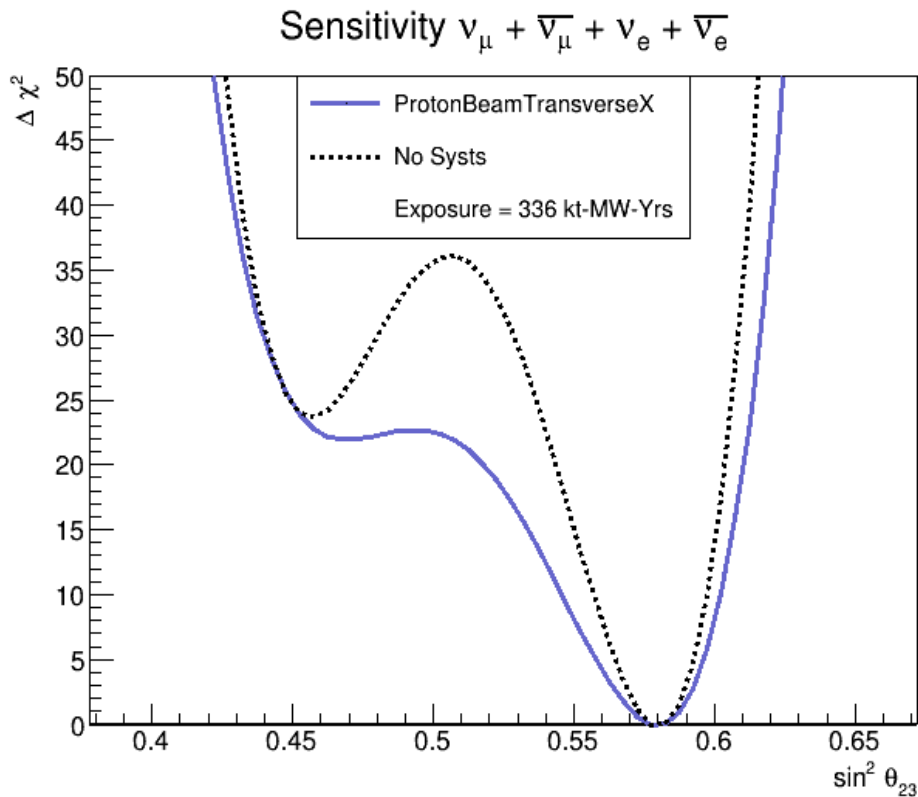
IMPORTANT



# Proton Beam Transverse X

**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm (updated from 4.5 mm in TDR)

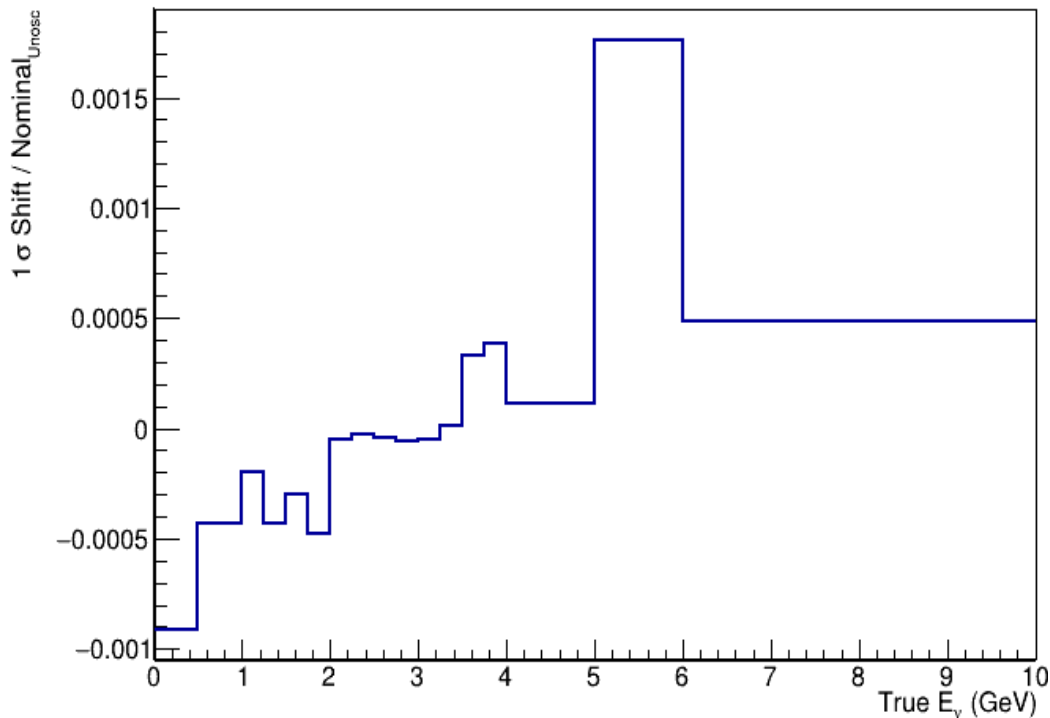


# Proton Beam Transverse X

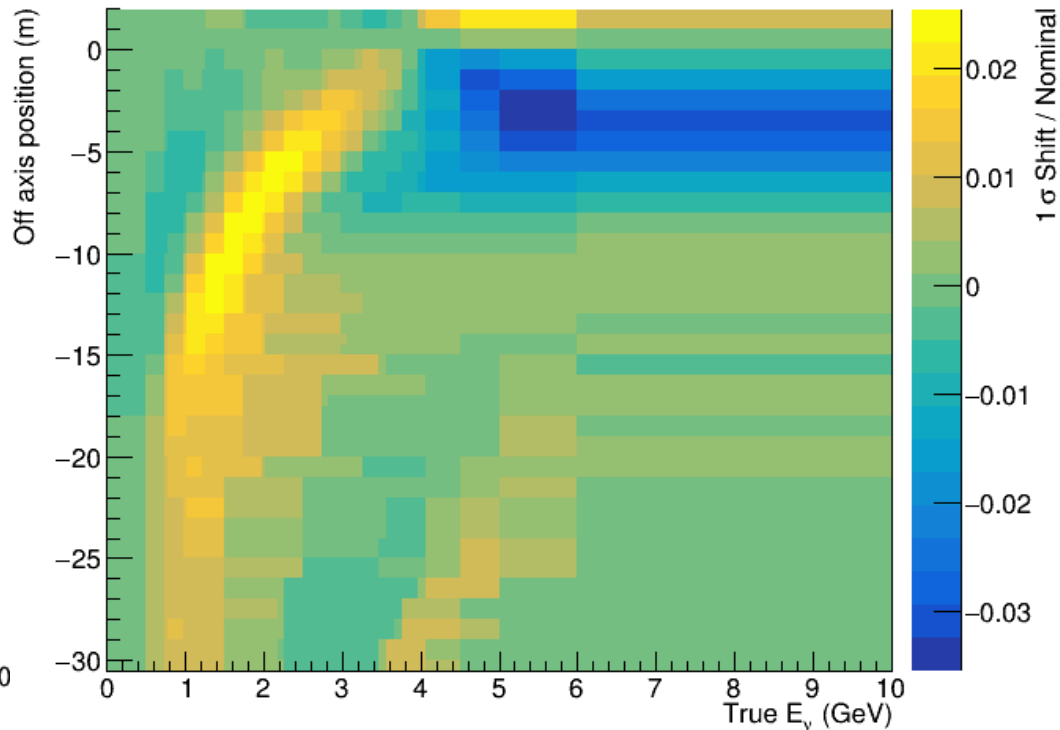
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm (updated from 4.5 mm in TDR)

FD ProtonBeamTransverseX +  $1\sigma$



ND ProtonBeamTransverseX +  $1\sigma$



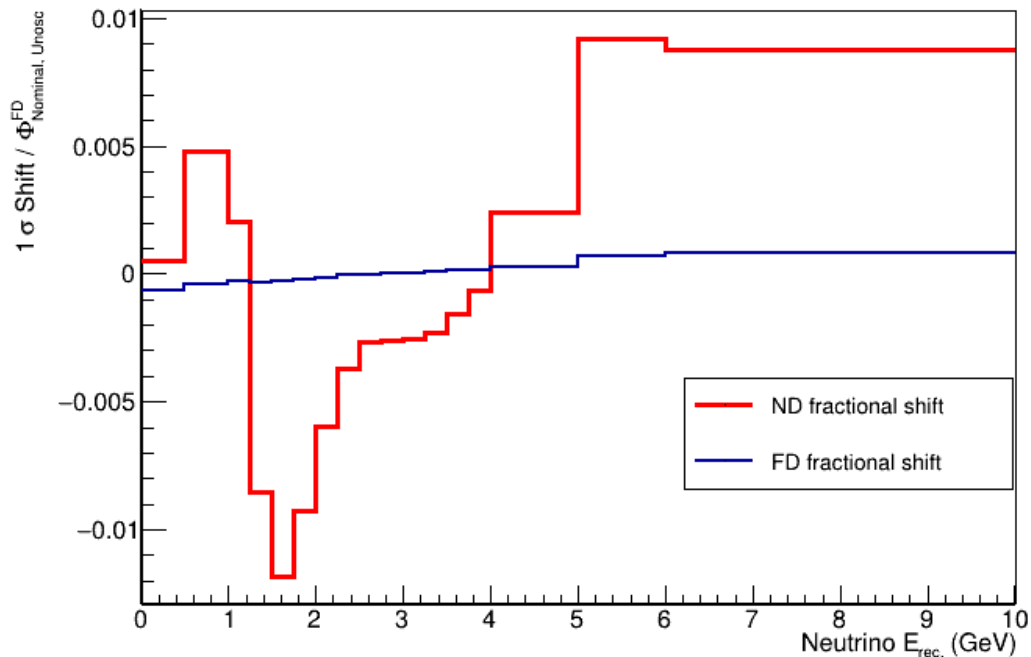


# Proton Beam Transverse X

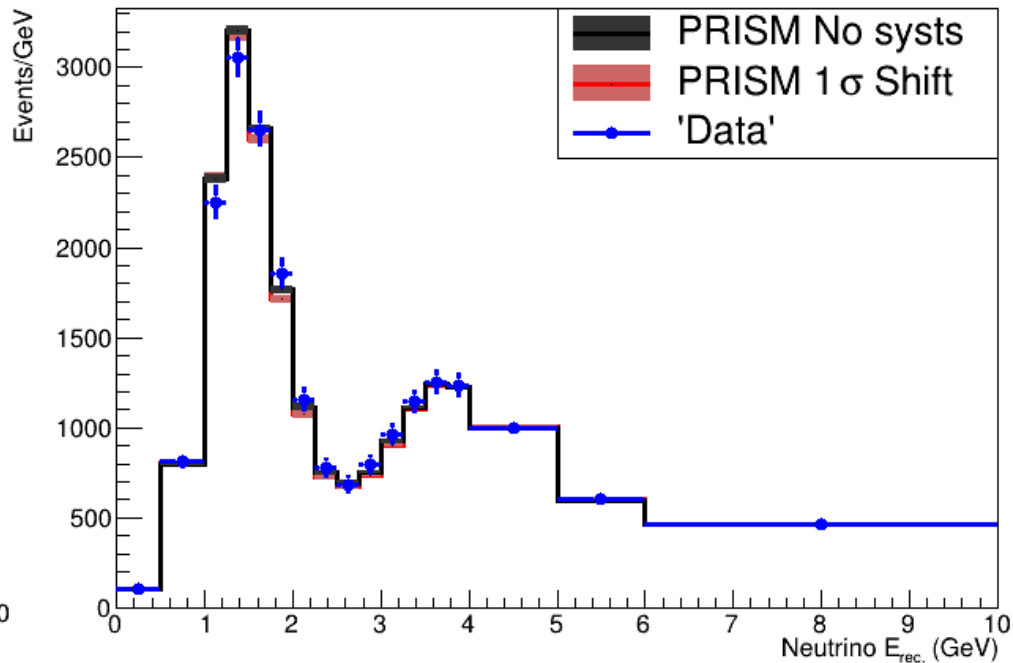
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm (updated from 4.5 mm in TDR)

Fractional shift ProtonBeamTransverseX+  $1\sigma$



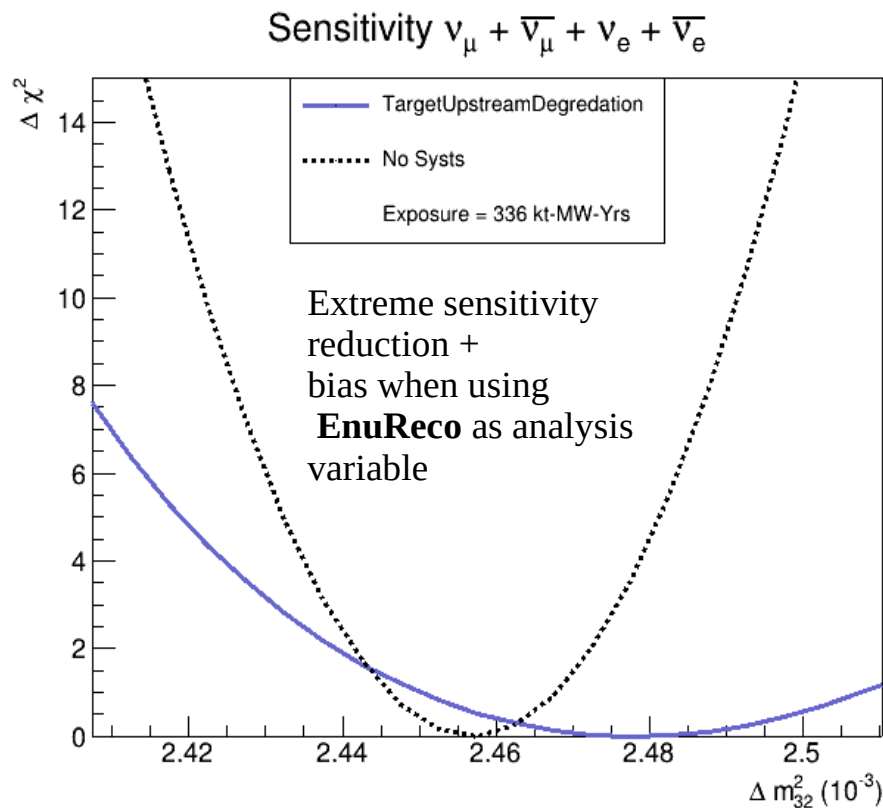
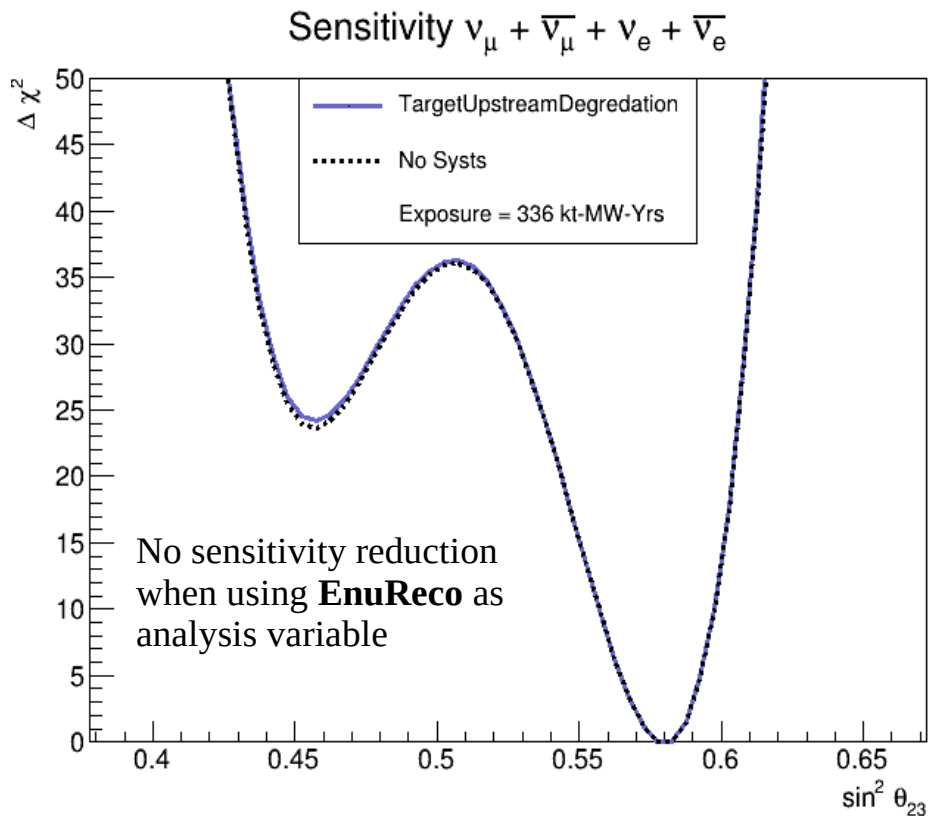
ProtonBeamTransverseX



# Target Upstream Degredation

**IMPORTANT**

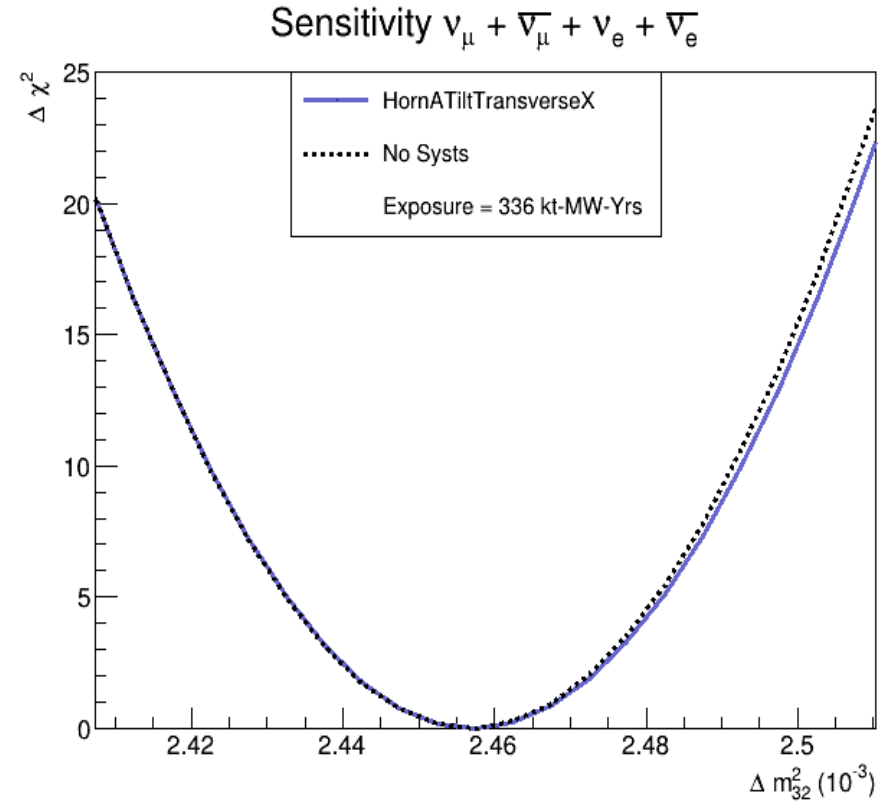
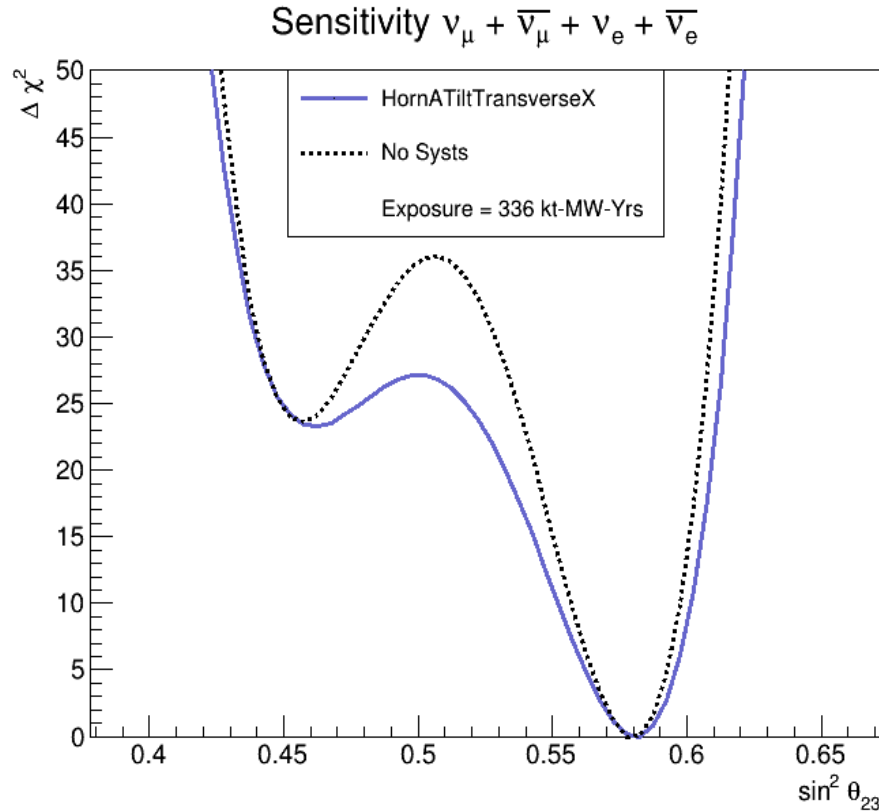
-  $1\sigma$  shift = 5 mm loss: assume complete loss of target on upstream end (a shorter target by  $dz$  shifted downstream by the loss  $dz$ )



# Horn A Tilt Transverse X

**IMPORTANT**

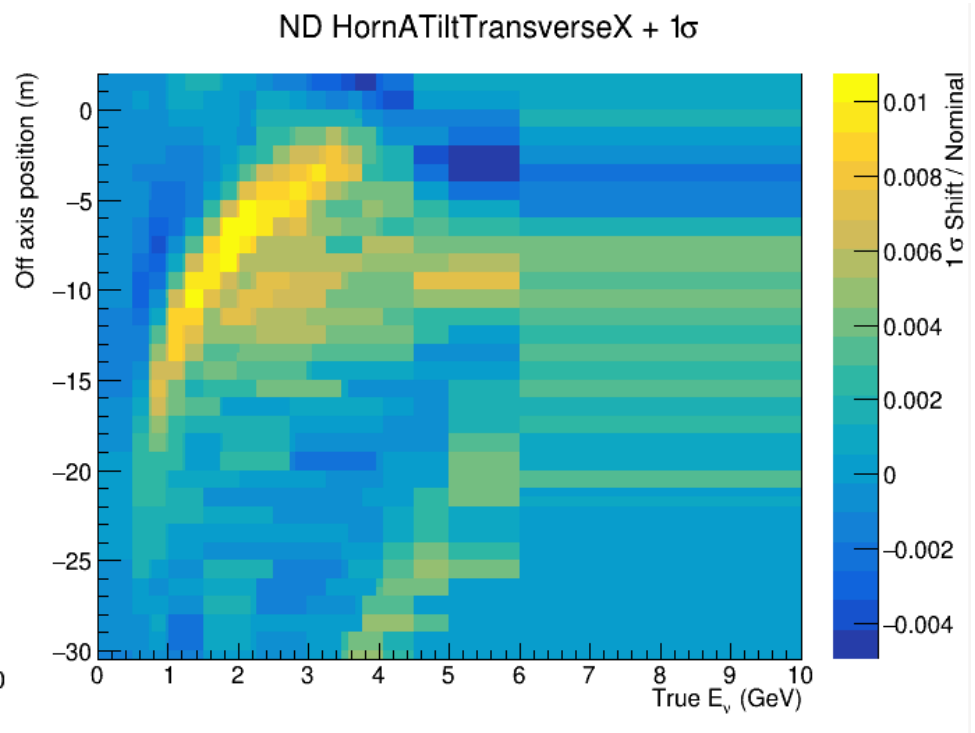
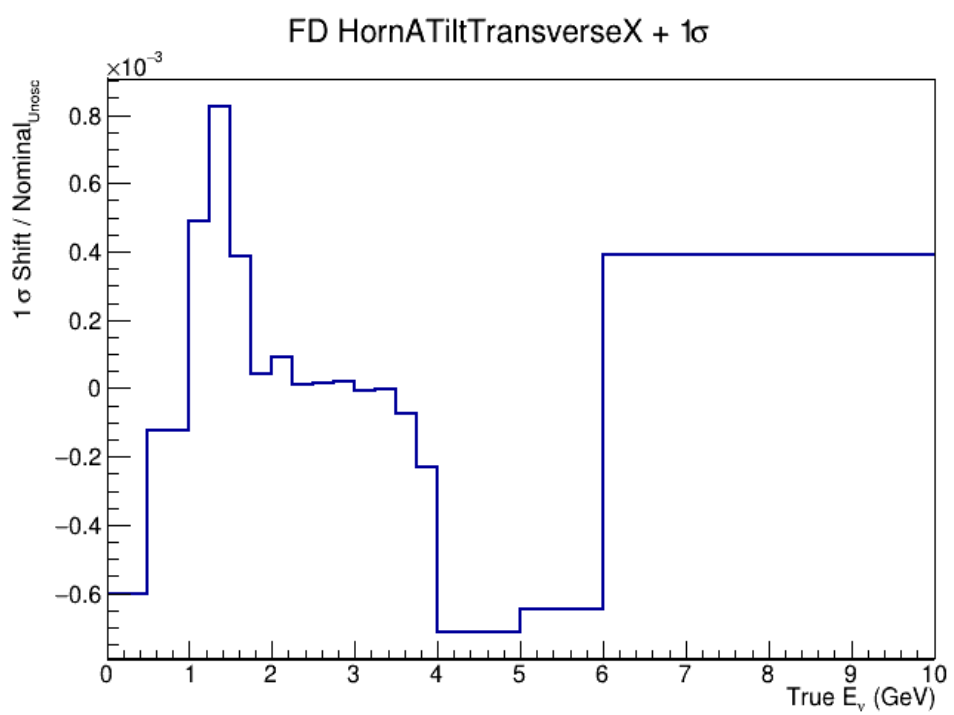
-  $1\sigma$  shift = 0.5 mm



# Horn A Tilt Transverse X

**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm

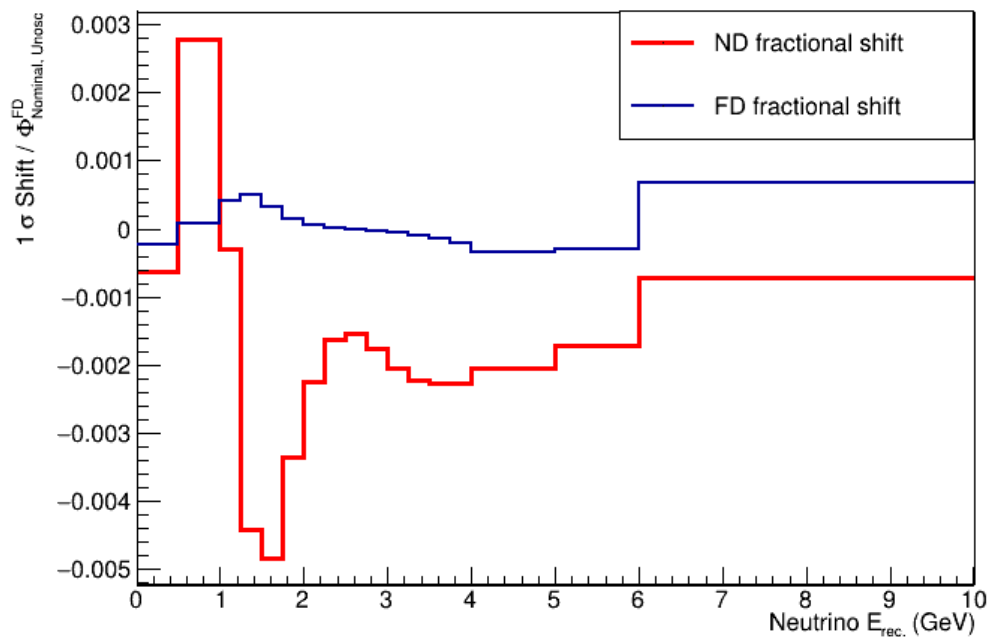


# Horn A Tilt Transverse X

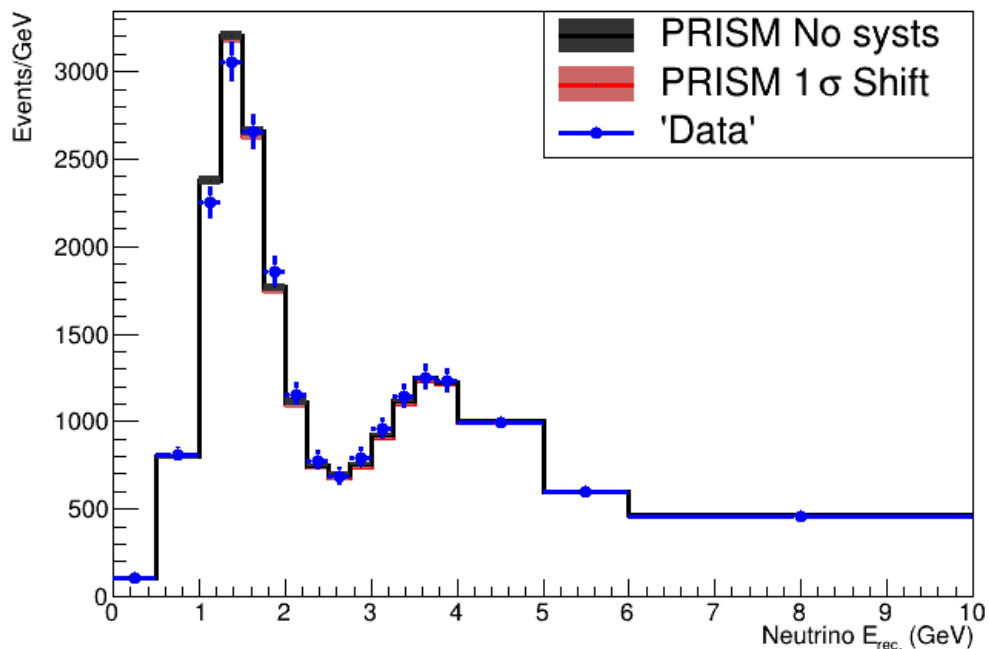
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm

Fractional shift HornATiltTransverseX+  $1\sigma$



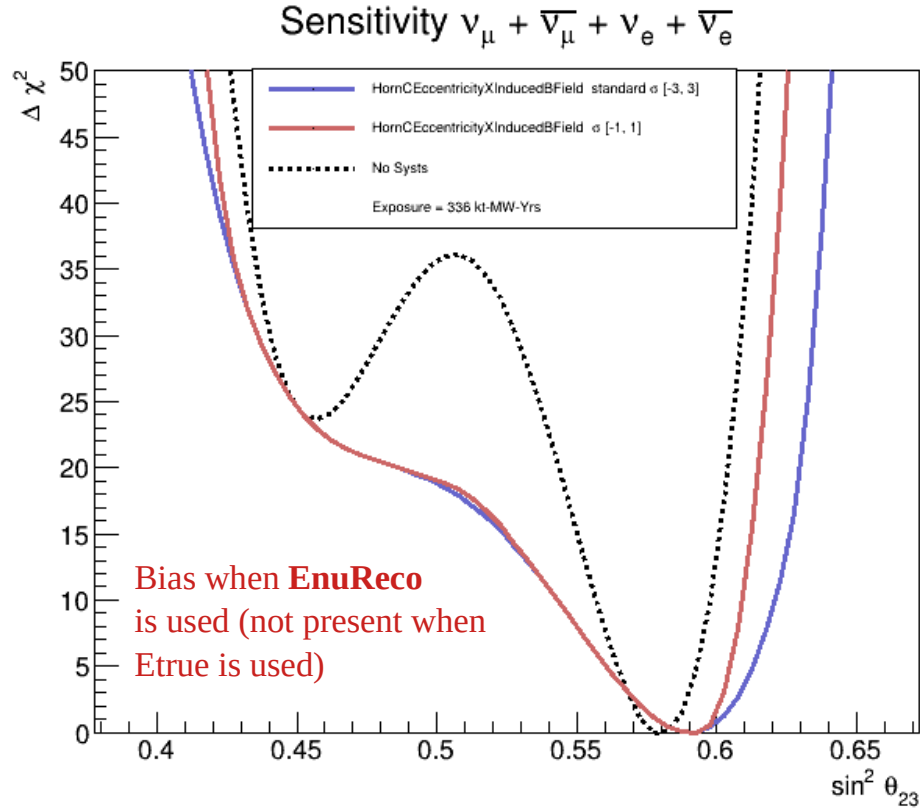
HornATiltTransverseX



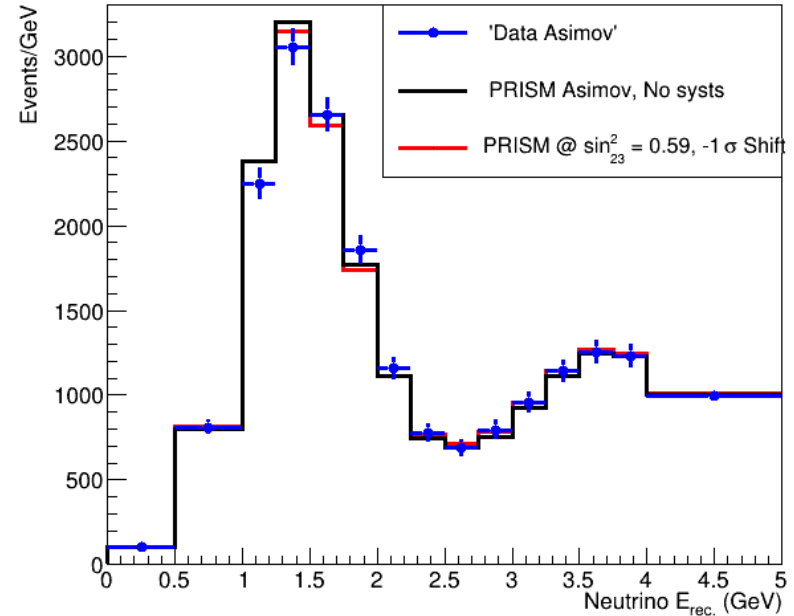
# Horn C Eccentricity X Induced Bfield

IMPORTANT

-  $1\sigma$  shift = 0.07 mm: NuMi Horn 2 tolerance assumed  
(off axis deformation of inner conductor)



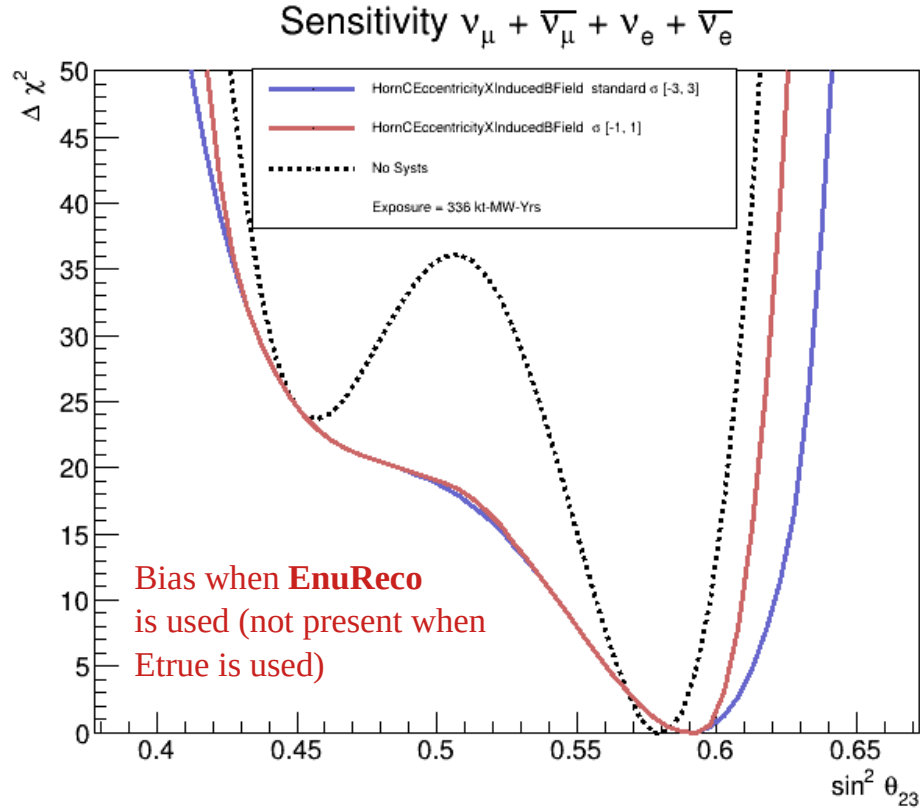
- PRISM prediction works well, but it is not a perfect match → mismatch comes from smearing + efficiency correction (perfect match for  $E_{true}$ )



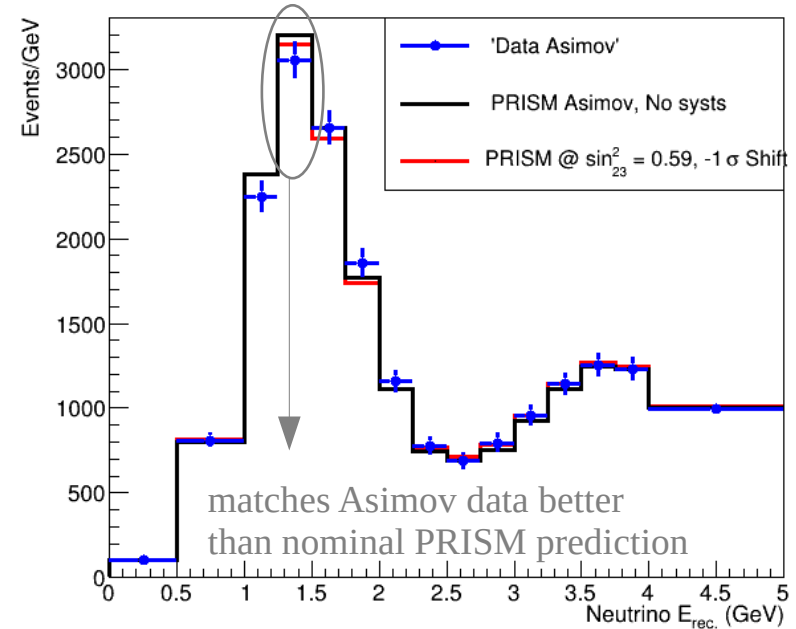
# Horn C Eccentricity X Induced Bfield

IMPORTANT

-  $1\sigma$  shift = 0.07 mm: NuMi Horn 2 tolerance assumed  
(off axis deformation of inner conductor)

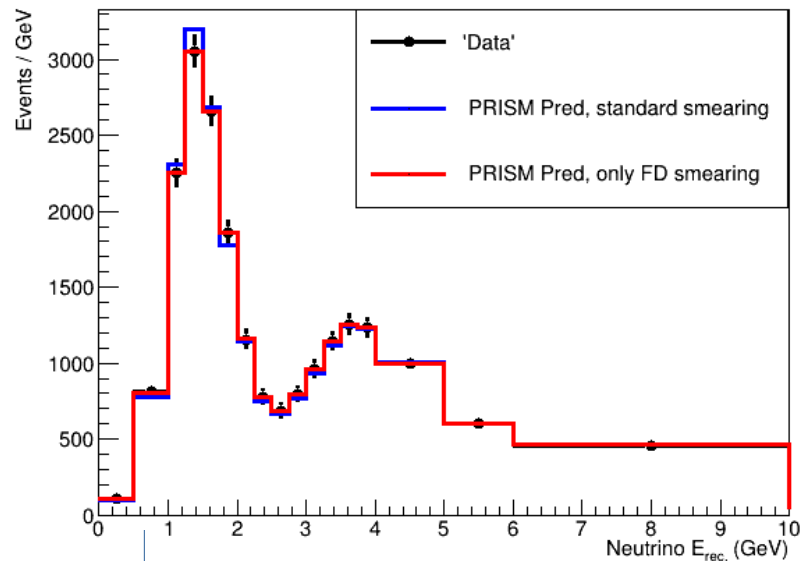


- PRISM prediction works well, but it is not a perfect match → mismatch comes from smearing + efficiency correction (perfect match for  $E_{true}$ )



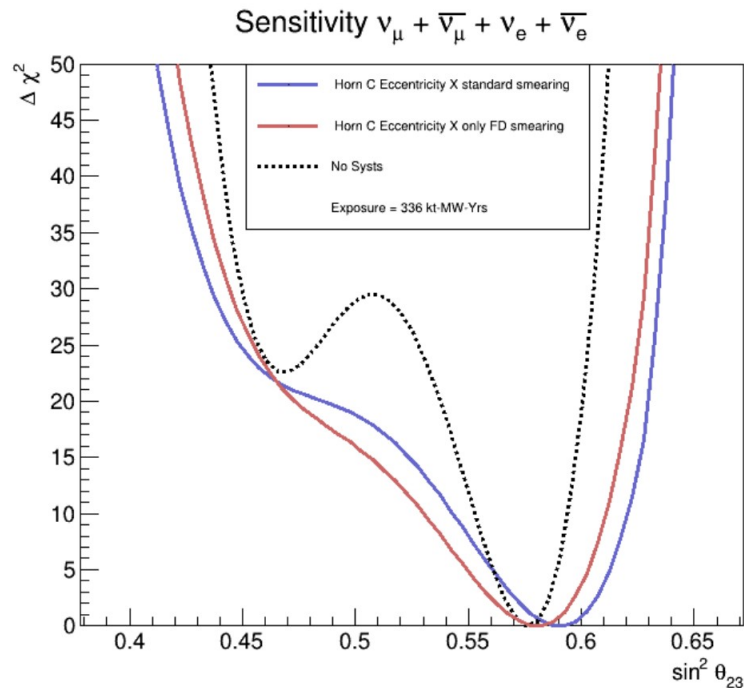
## Horn C Eccentricity X Induced Bfield – perfect PRISM match

- PRISM mismatch comes from smearing + efficiency correction (perfect match for  $E_{\text{true}}$ )  
→ disentangle FD + ND smearing: no ND smearing (work with  $E_{\text{true}}$  in ND)



mismatch comes from ND smearing + efficiency correction

No bias with  
→  
PRISM perfect match



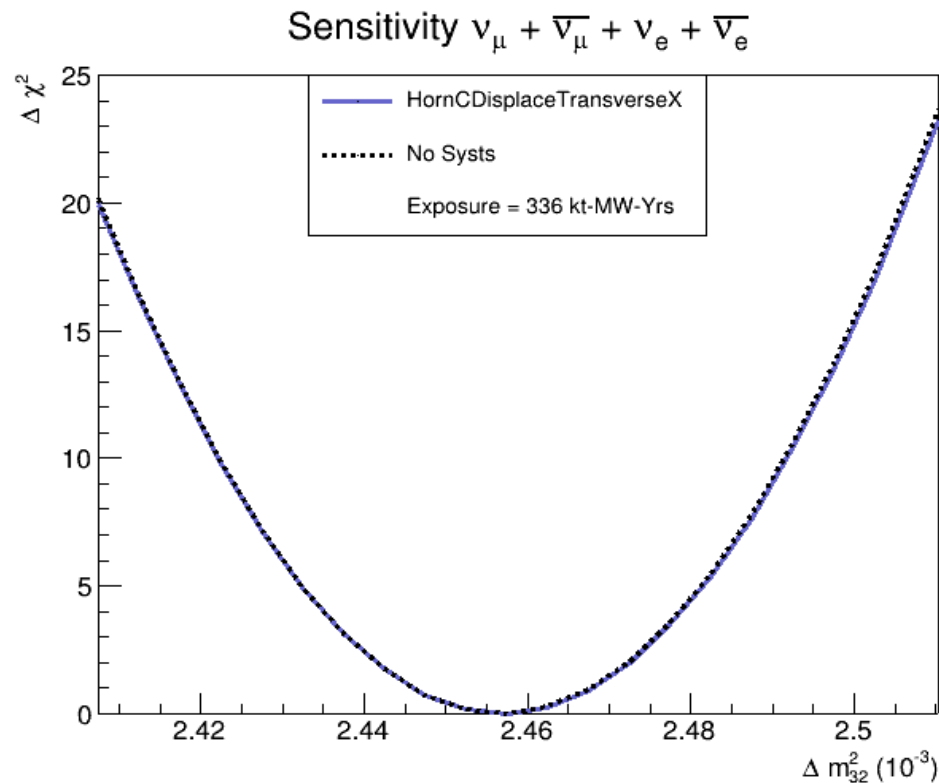
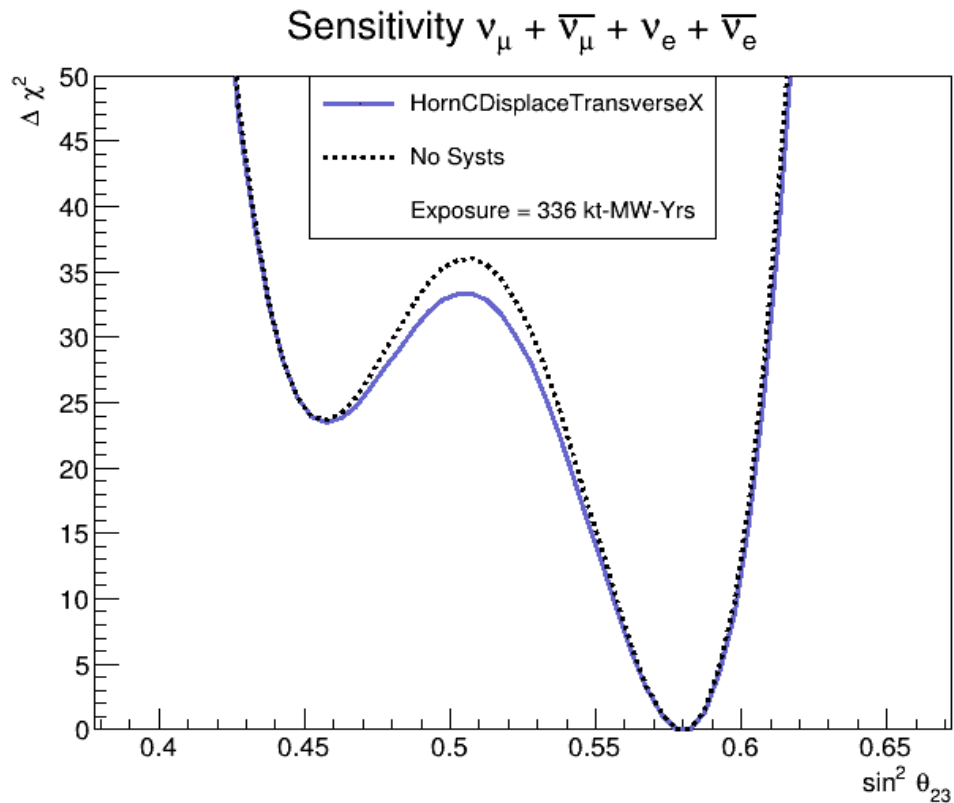
- There is no additional bias when PRISM prediction results in a perfect data match → sensitivity is still significantly reduced due to this focusing parameter**



# Horn C Displace Transverse X

**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm

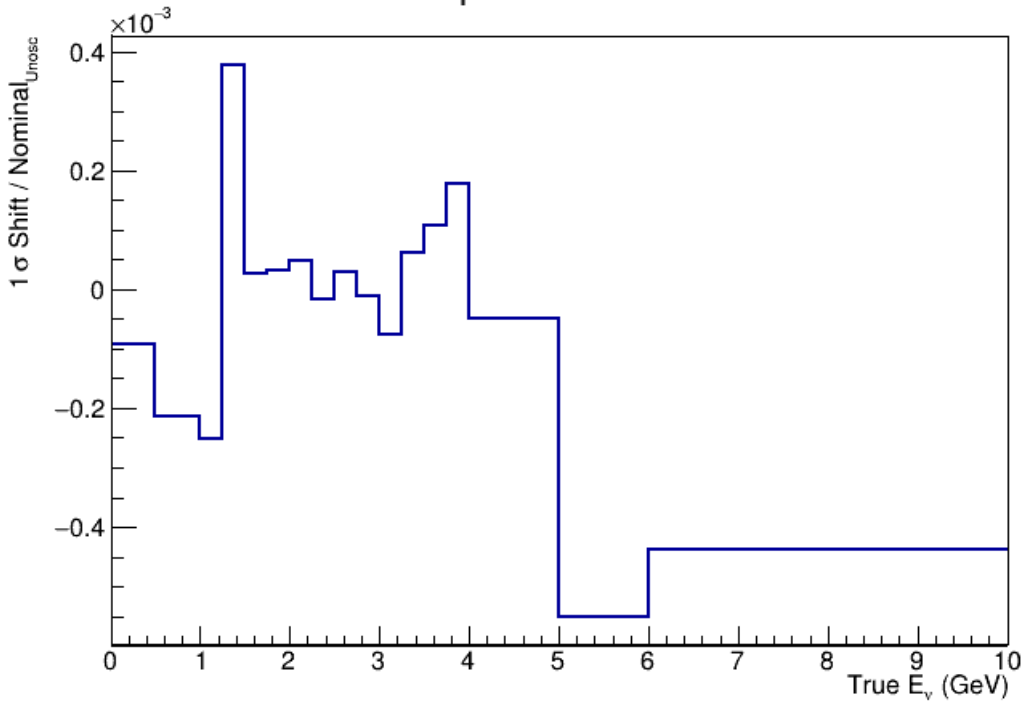


# Horn C Displace Transverse X

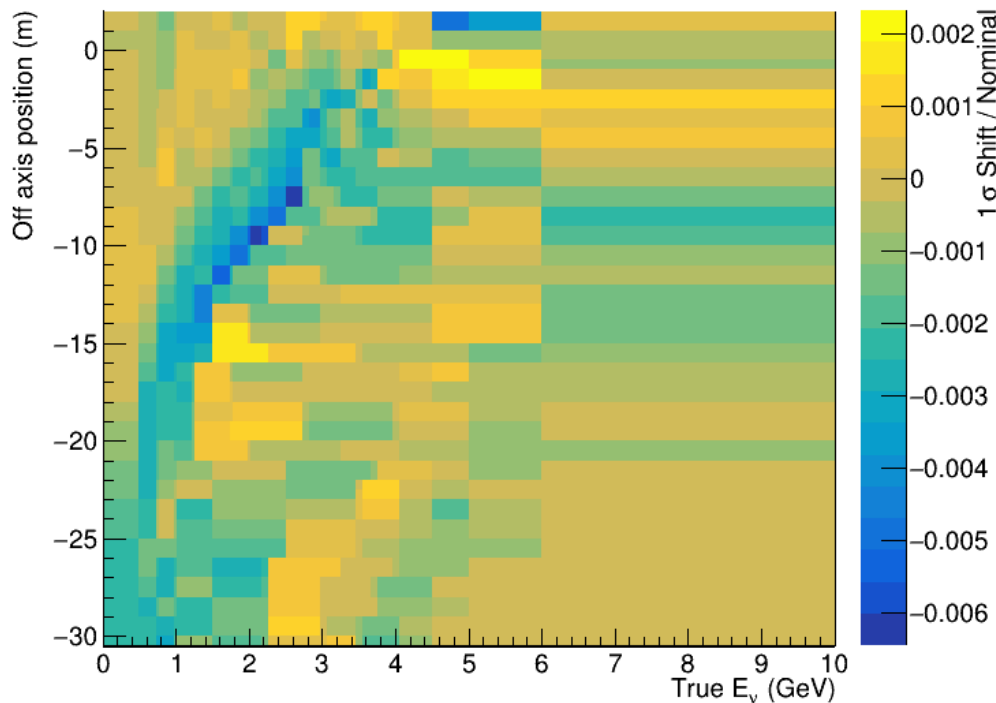
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm

FD HornCDisplaceTransverseX +  $1\sigma$



ND HornCDisplaceTransverseX +  $1\sigma$

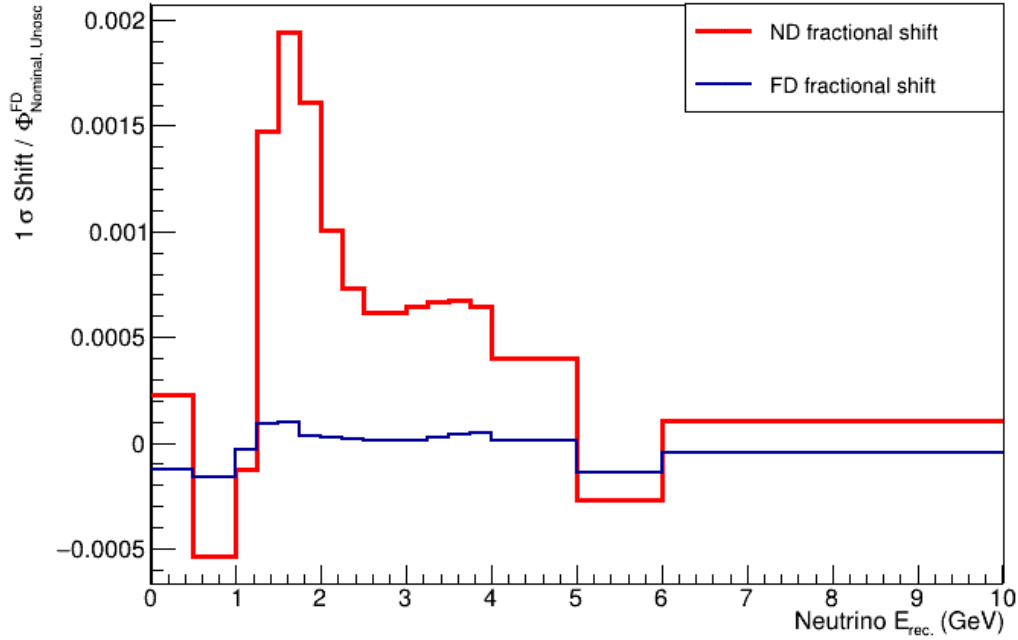


# Horn C Displace Transverse X

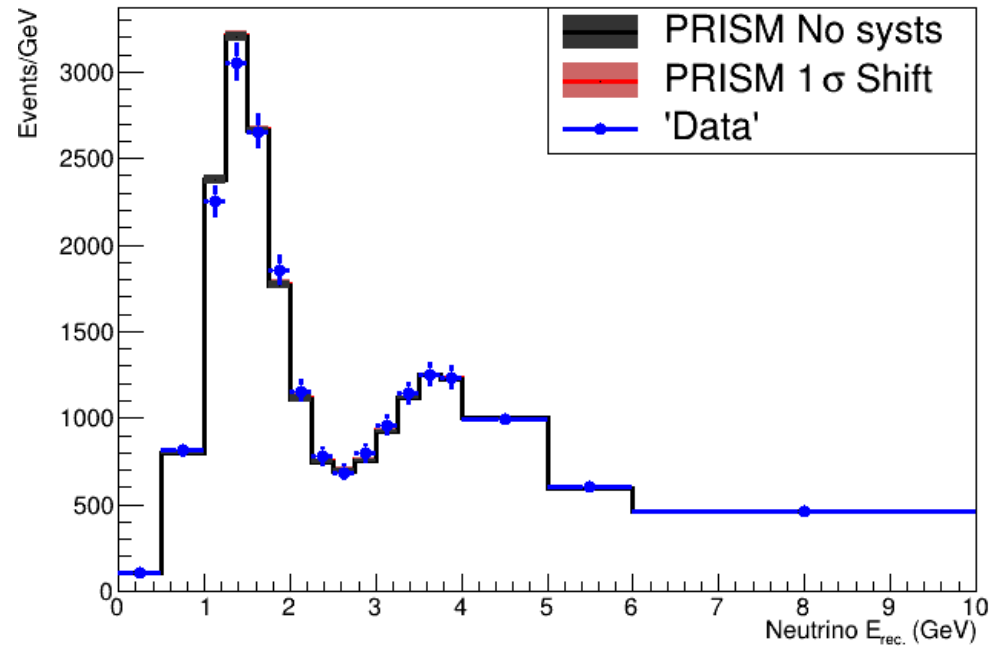
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm

Fractional shift HornCDisplaceTransverseX+  $1\sigma$



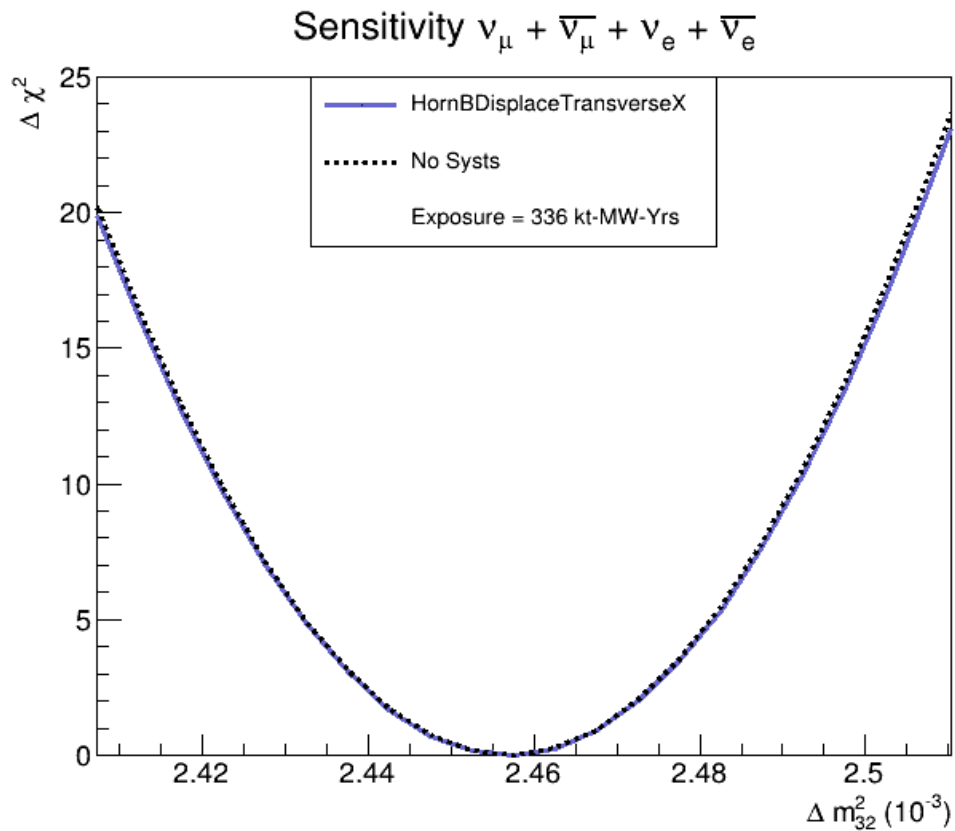
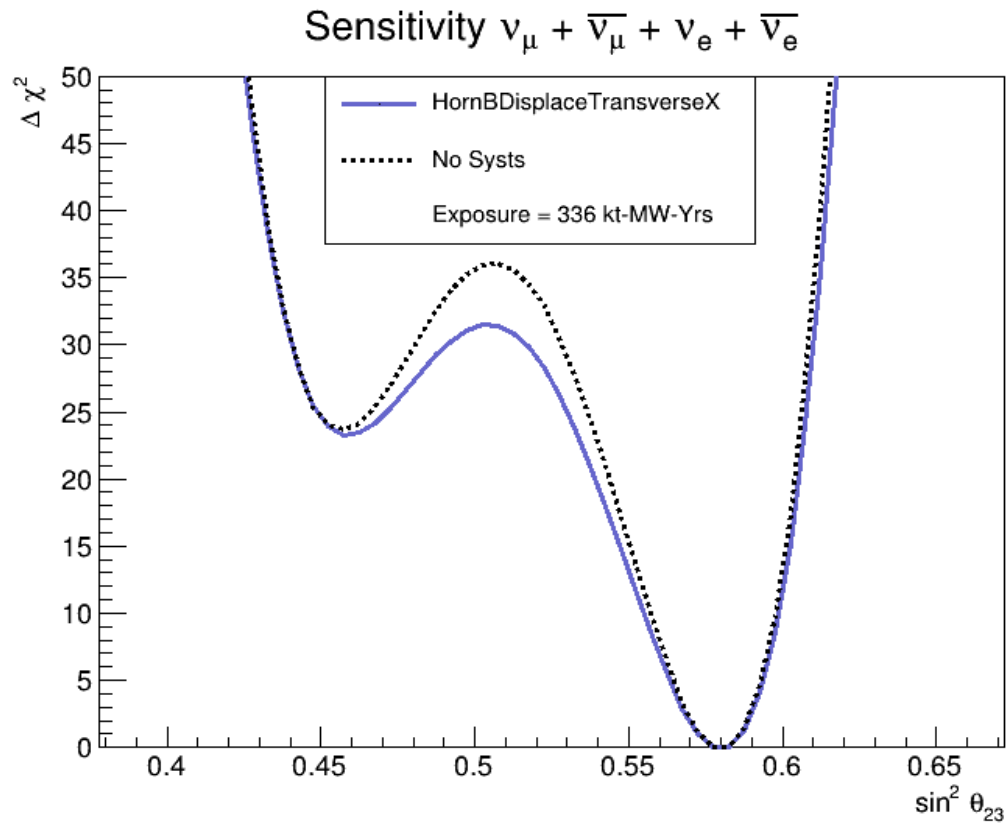
HornCDisplaceTransverseX



# Horn B Displace Transverse X

**IMPORTANT**

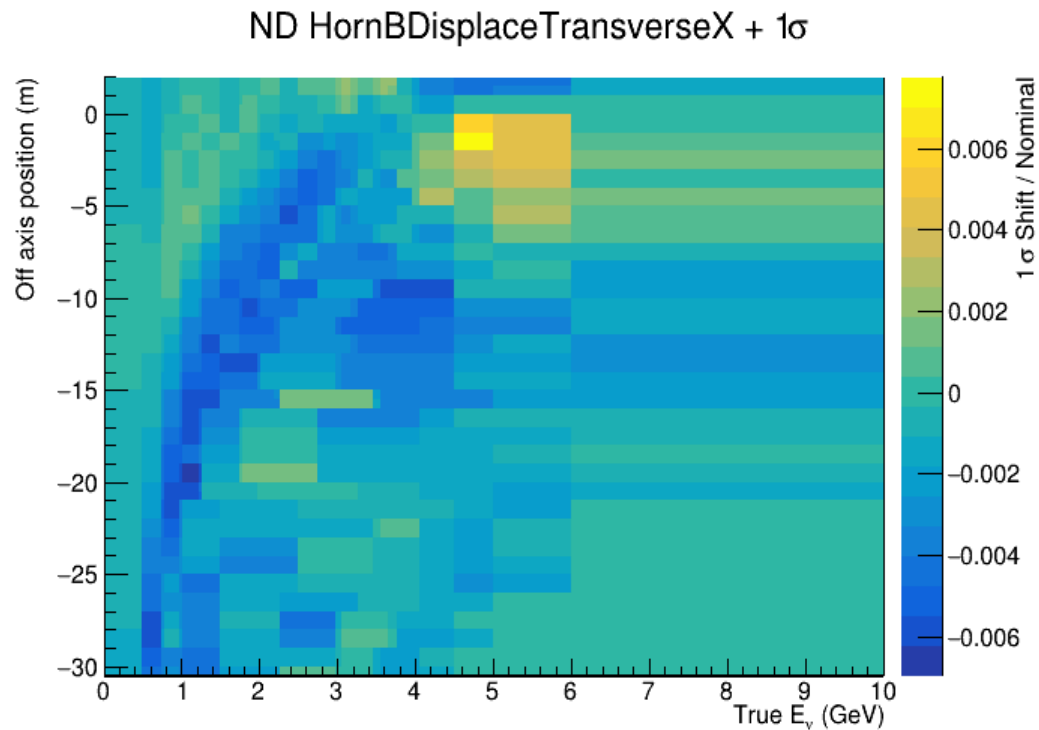
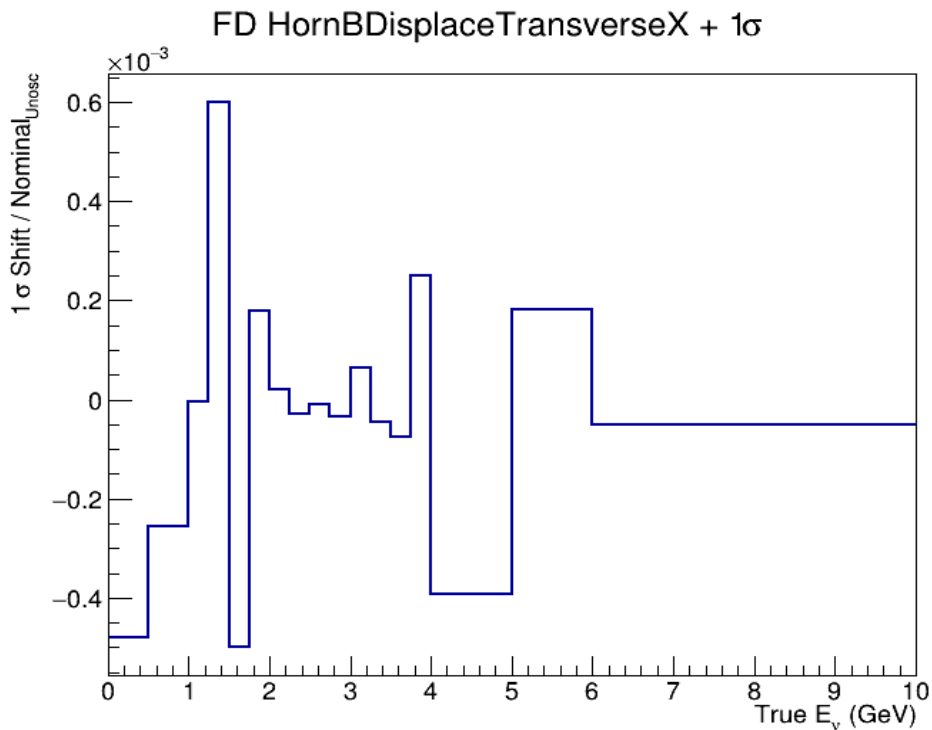
-  $1\sigma$  shift = 0.5 mm



# Horn B Displace Transverse X

**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm

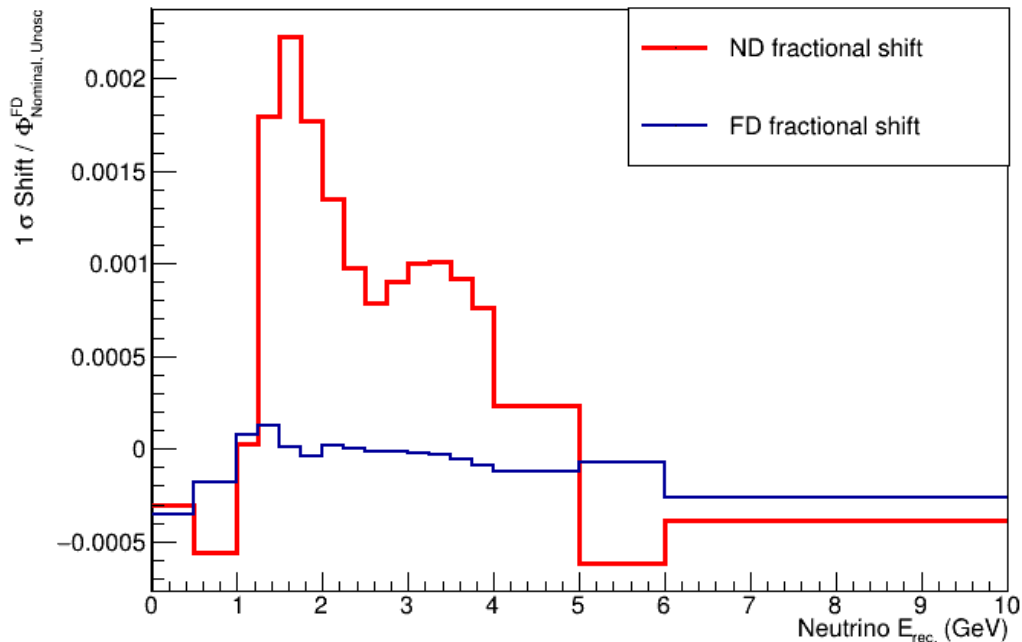


# Horn B Displace Transverse X

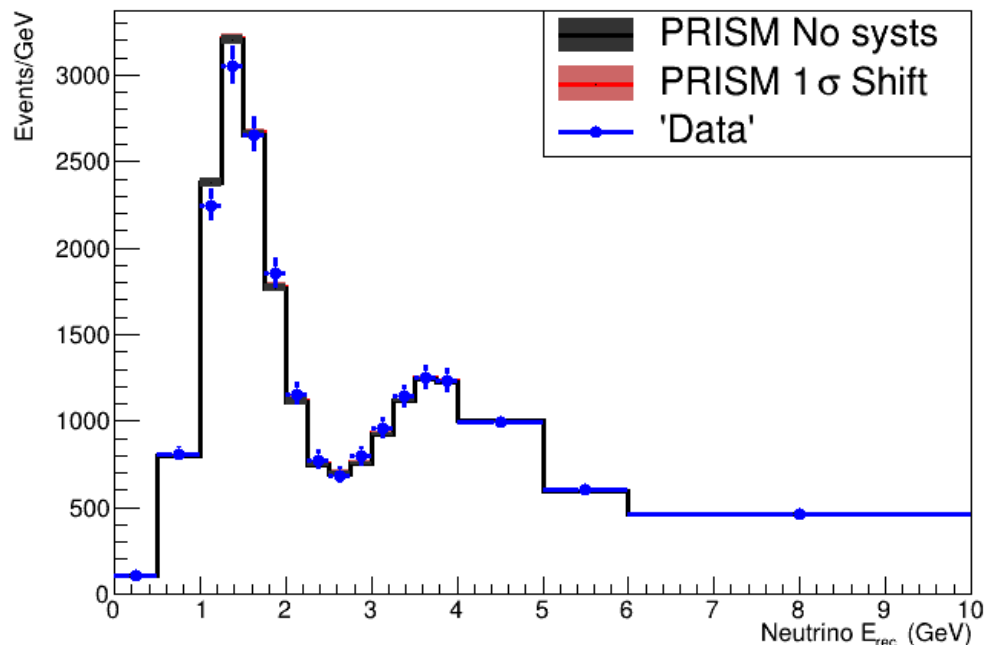
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm

Fractional shift HornBDisplaceTransverseX+  $1\sigma$



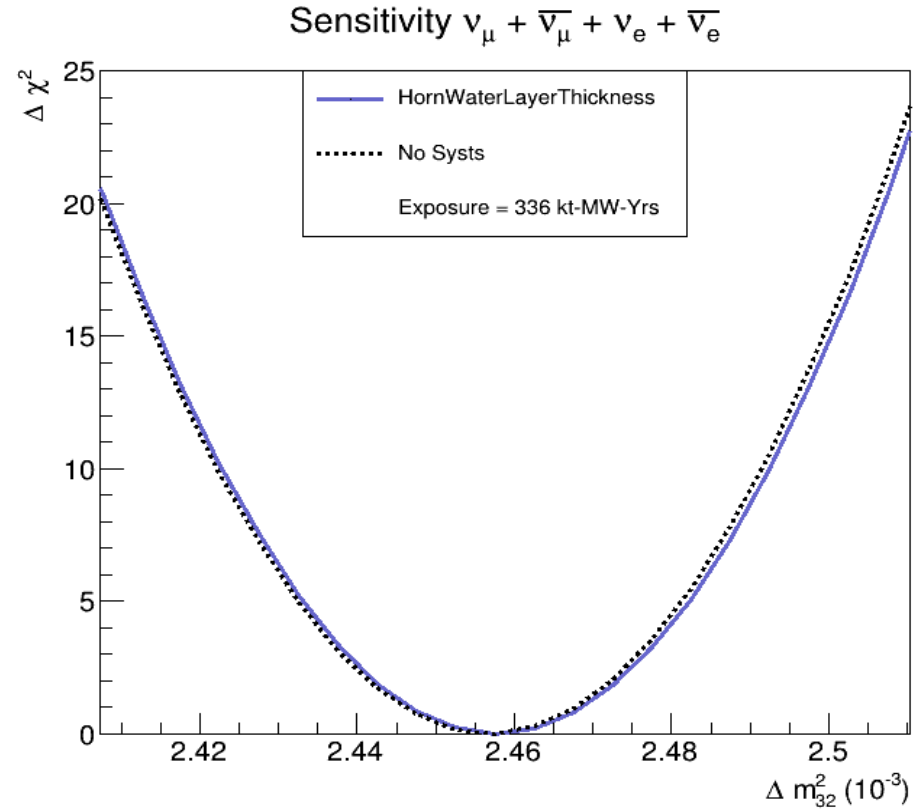
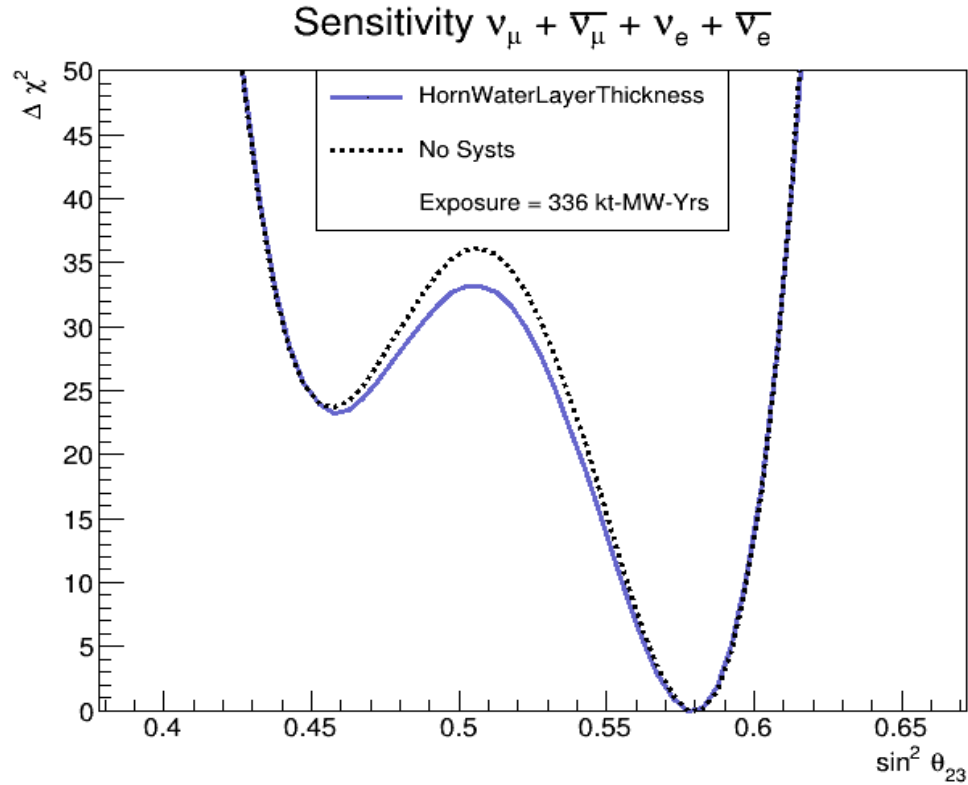
HornBDisplaceTransverseX



# Horn Water Layer Thickness

**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm: nominal = 1mm; simultaneous change to all 3 horns

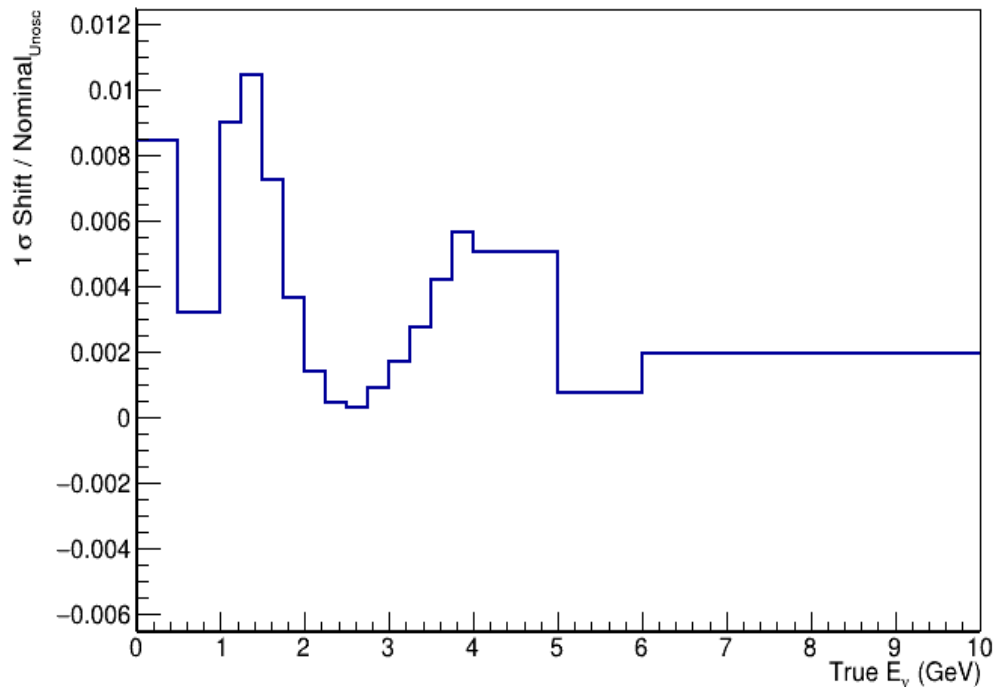


# Horn Water Layer Thickness

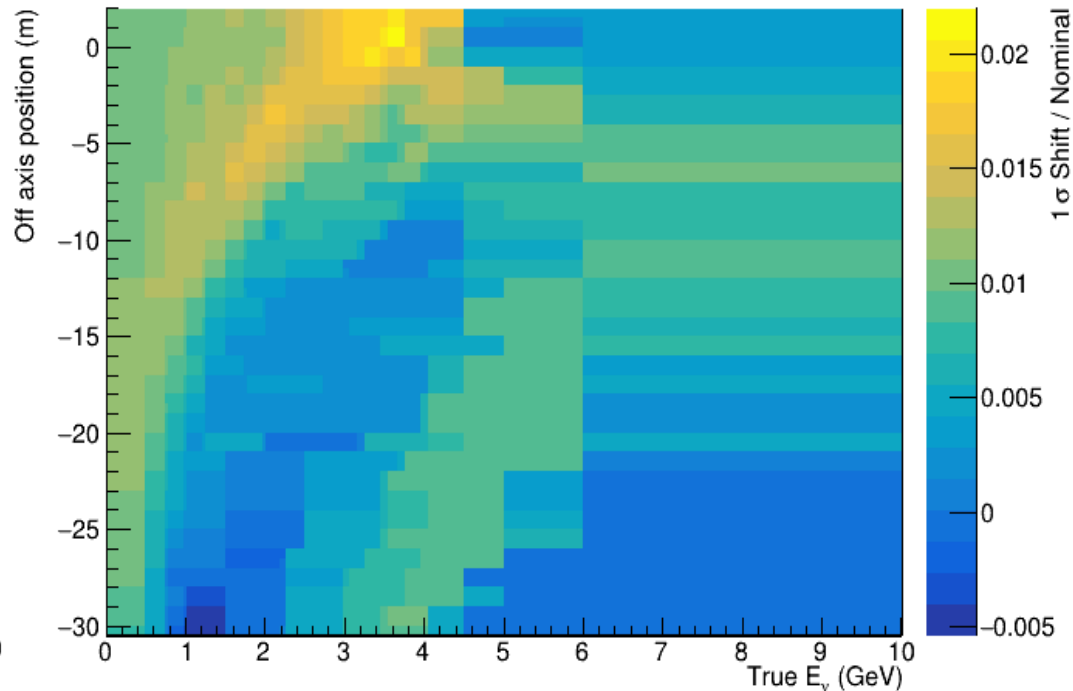
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm: nominal = 1mm; simultaneous change to all 3 horns

FD HornWaterLayerThickness +  $1\sigma$



ND HornWaterLayerThickness +  $1\sigma$



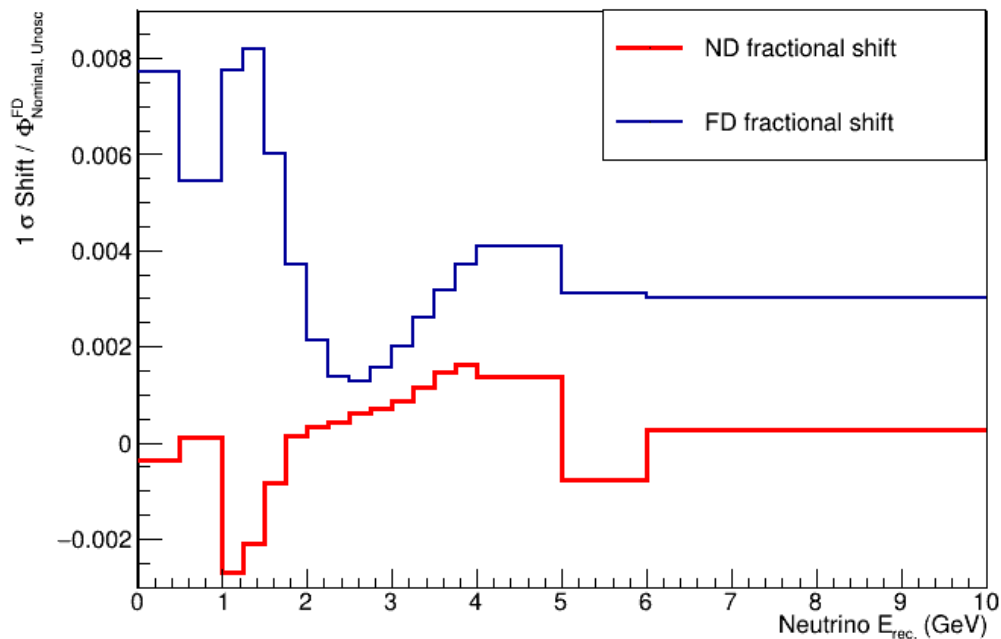


# Horn Water Layer Thickness

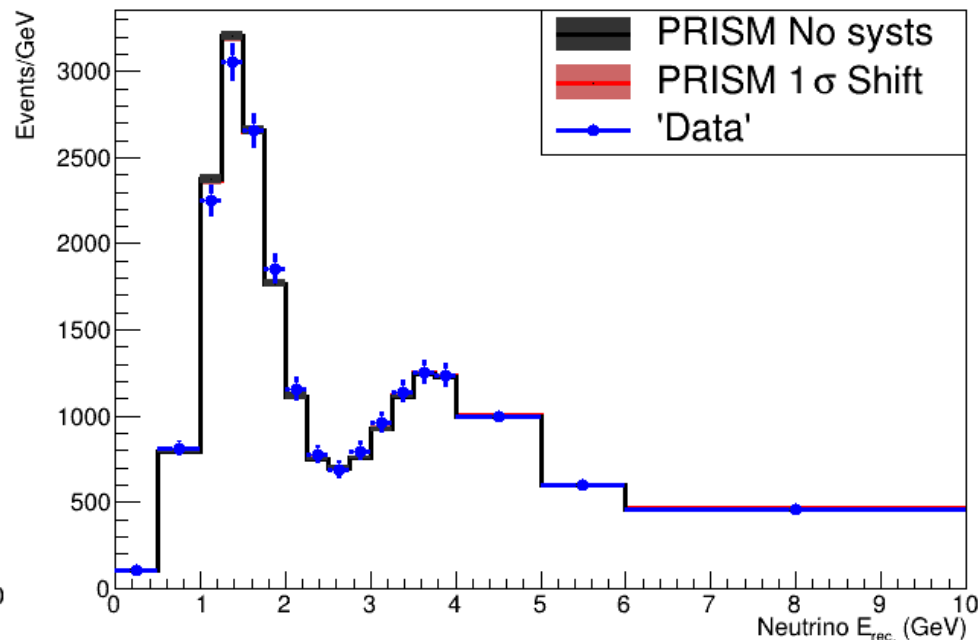
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm: nominal = 1mm; simultaneous change to all 3 horns

Fractional shift HornWaterLayerThickness+  $1\sigma$



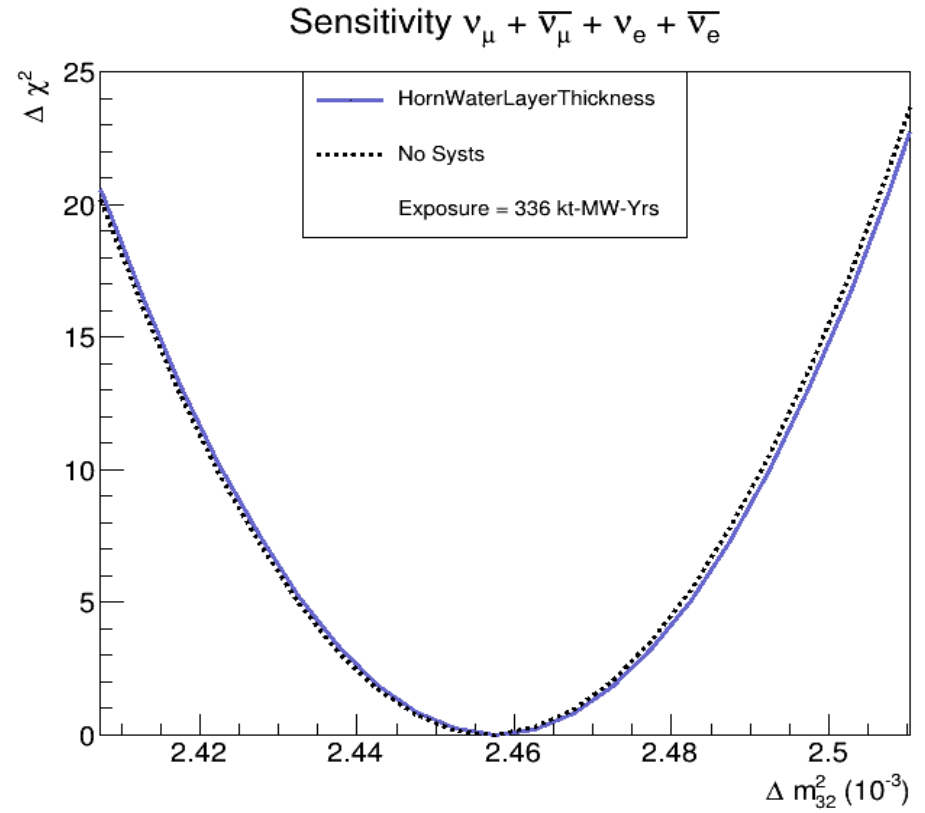
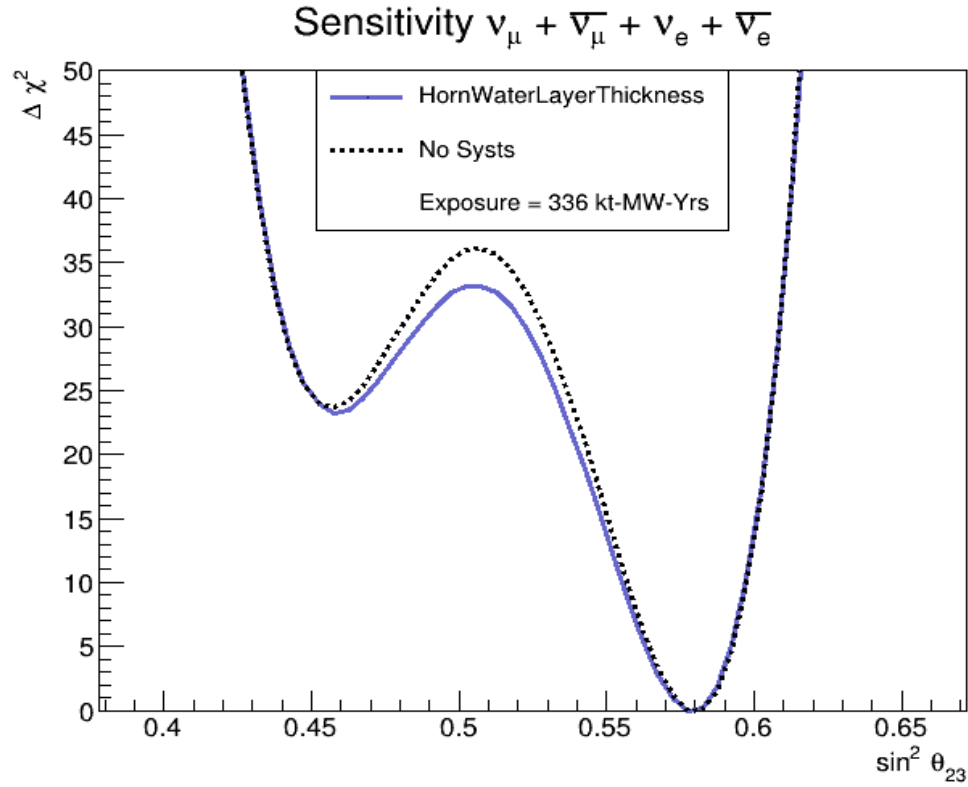
HornWaterLayerThickness



# Horn Water Layer Thickness

**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm: nominal = 1mm; simultaneous change to all 3 horns

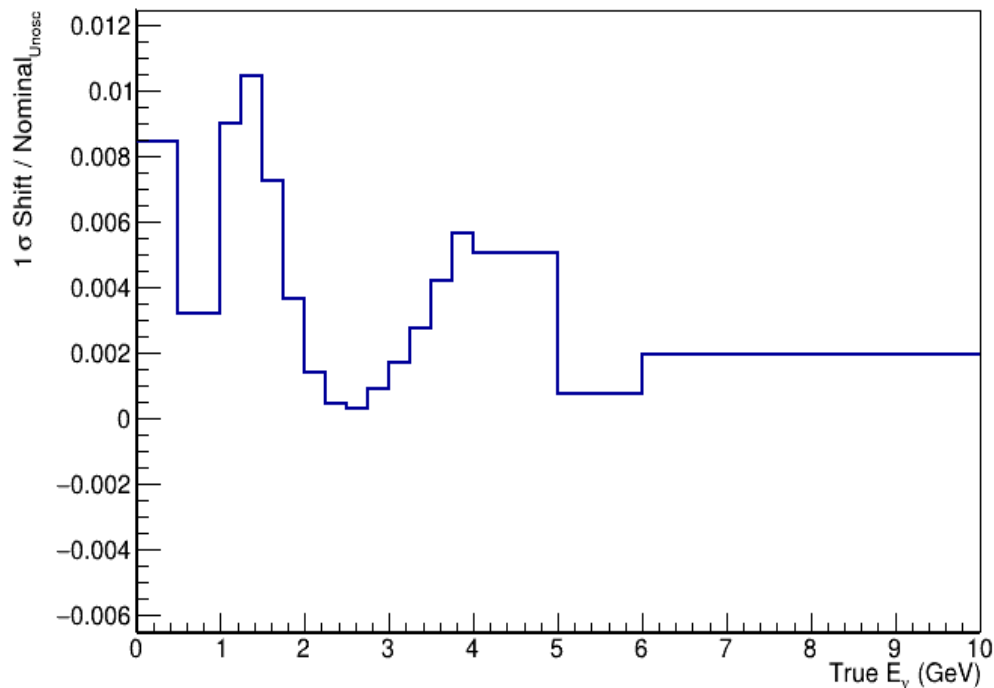


# Horn Water Layer Thickness

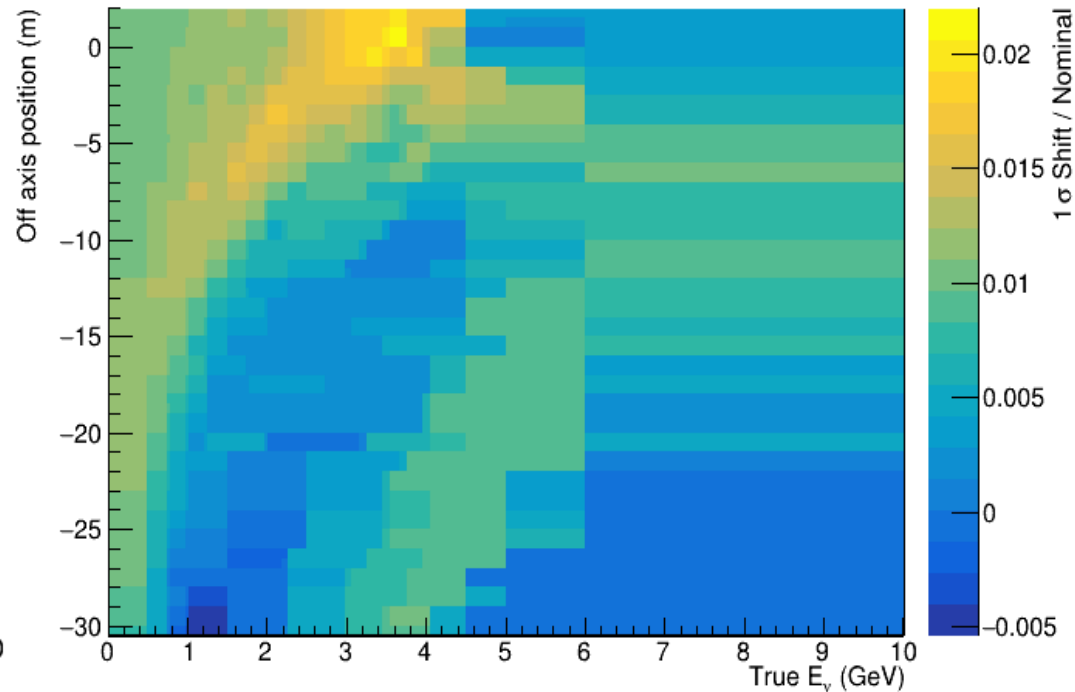
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm: nominal = 1mm; simultaneous change to all 3 horns

FD HornWaterLayerThickness +  $1\sigma$



ND HornWaterLayerThickness +  $1\sigma$

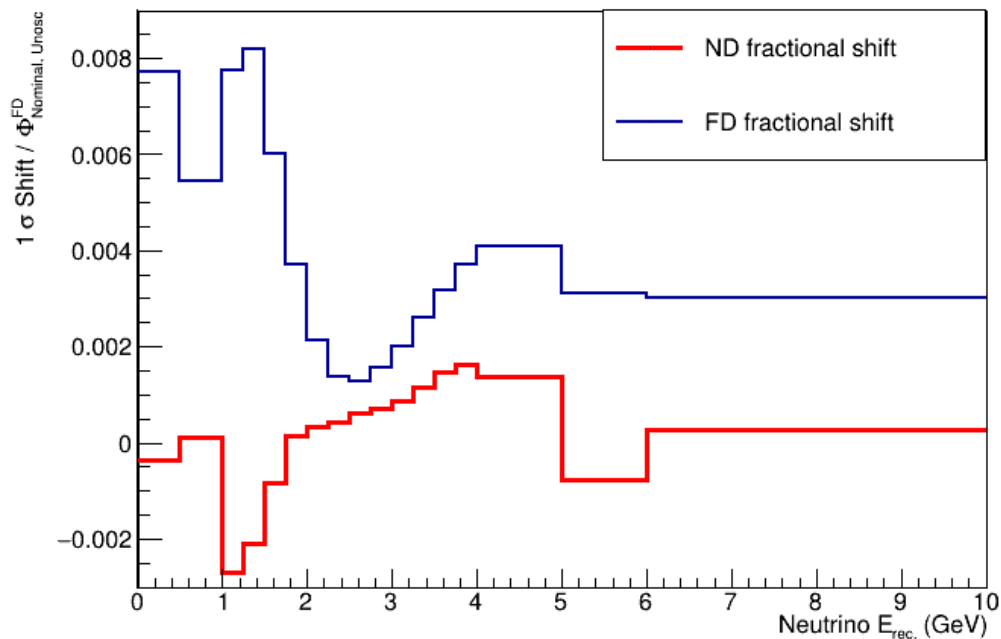


# Horn Water Layer Thickness

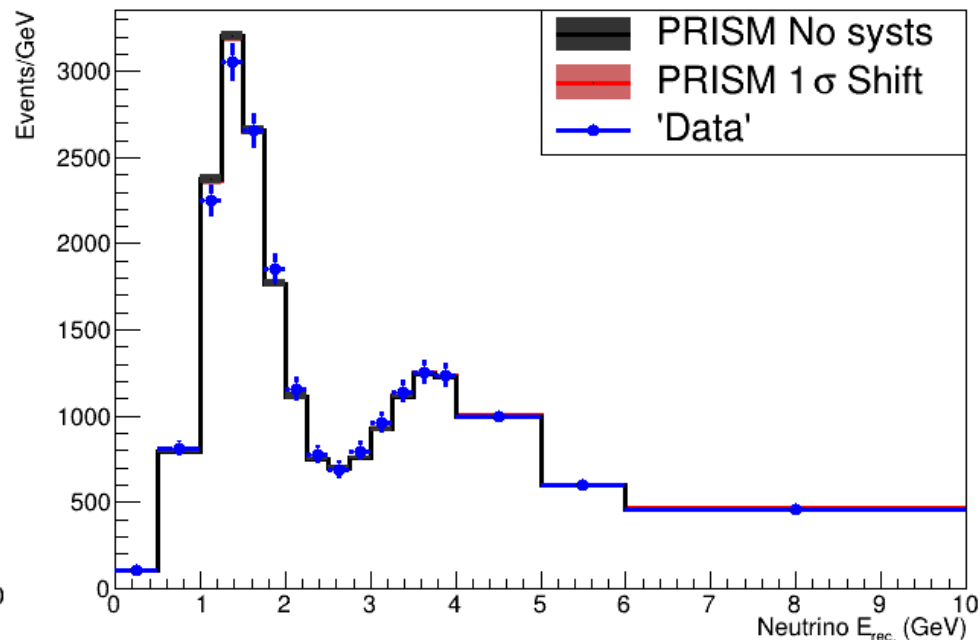
**IMPORTANT**

-  $1\sigma$  shift = 0.5 mm: nominal = 1mm; simultaneous change to all 3 horns

Fractional shift HornWaterLayerThickness+  $1\sigma$



HornWaterLayerThickness

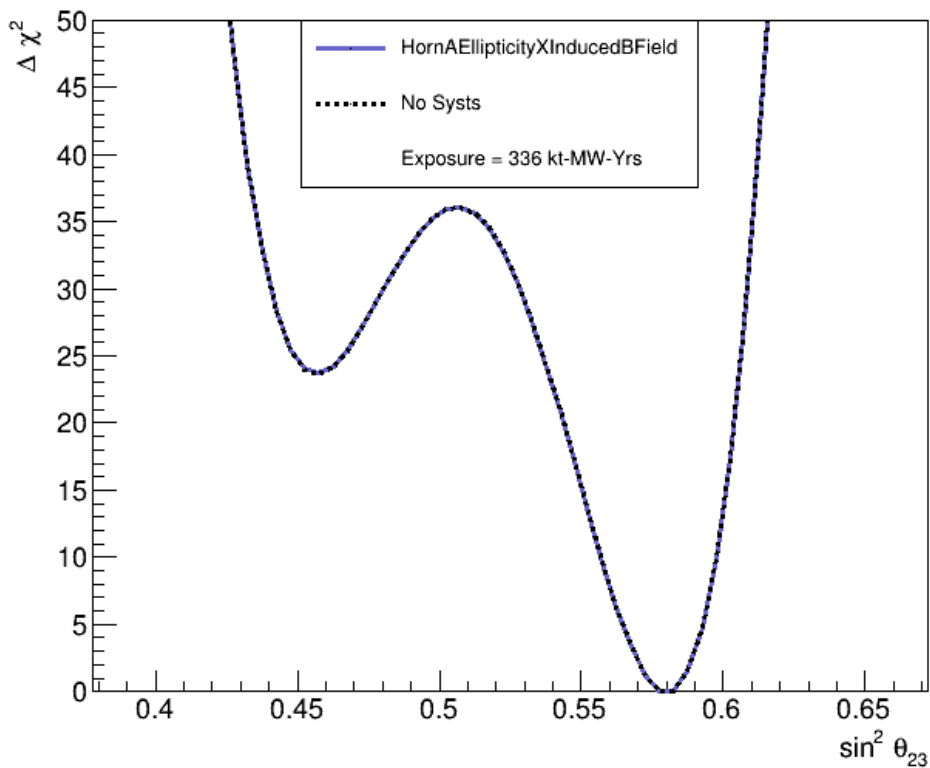


# Horn A Ellipticity X Induced Bfield

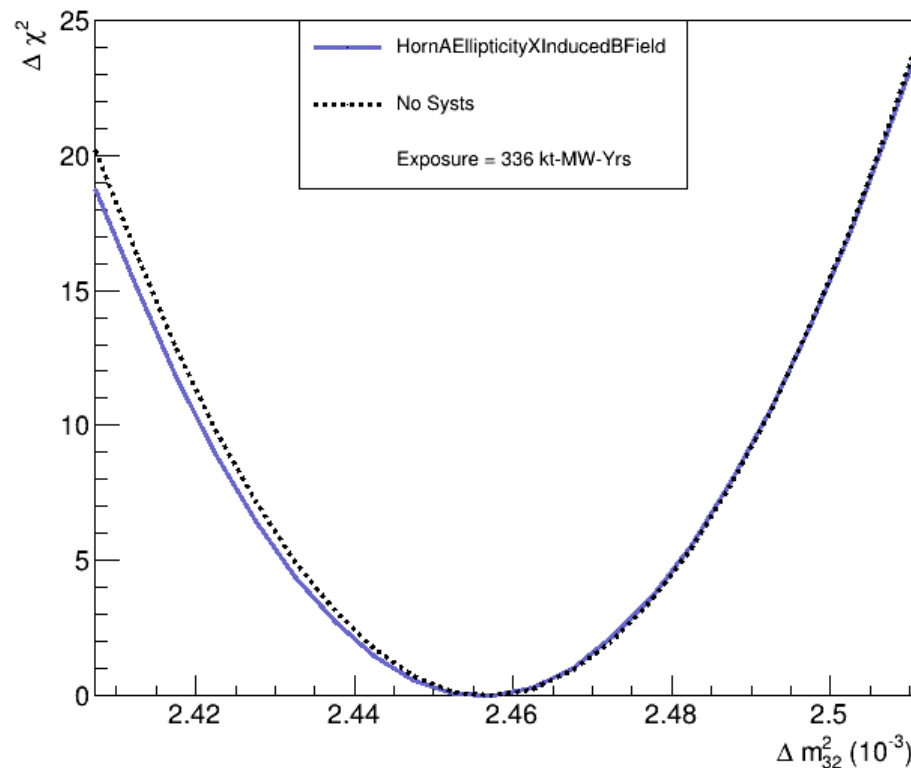
SEMI

-  $1\sigma$  shift = 0.120 mm: NuMi Horn 1 tolerance assumed  
(elliptical deformation of inner conductor)

Sensitivity  $\nu_\mu + \bar{\nu}_\mu + \nu_e + \bar{\nu}_e$



Sensitivity  $\nu_\mu + \bar{\nu}_\mu + \nu_e + \bar{\nu}_e$

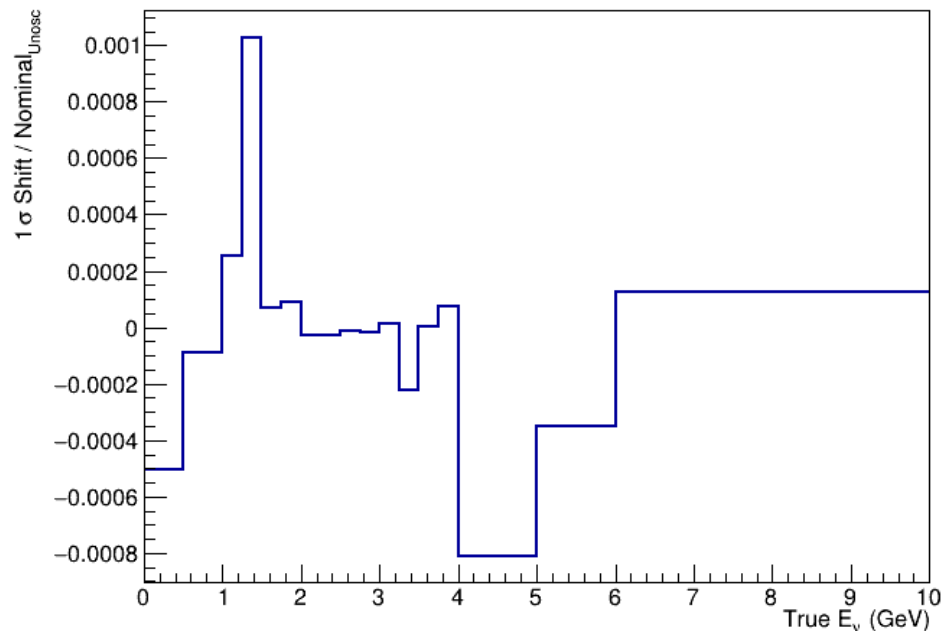


# Horn A Ellipticity X Induced Bfield

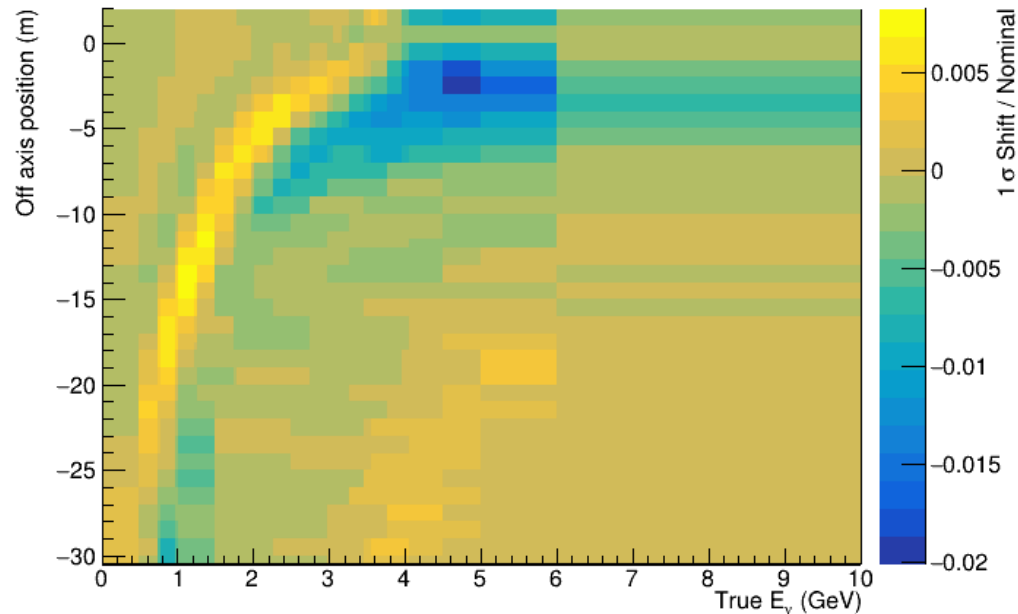
SEMI

-  $1\sigma$  shift = 0.120 mm: NuMi Horn 1 tolerance assumed (elliptical deformation of inner conductor)

FD HornAEllipticityXInducedBField +  $1\sigma$



ND HornAEllipticityXInducedBField +  $1\sigma$

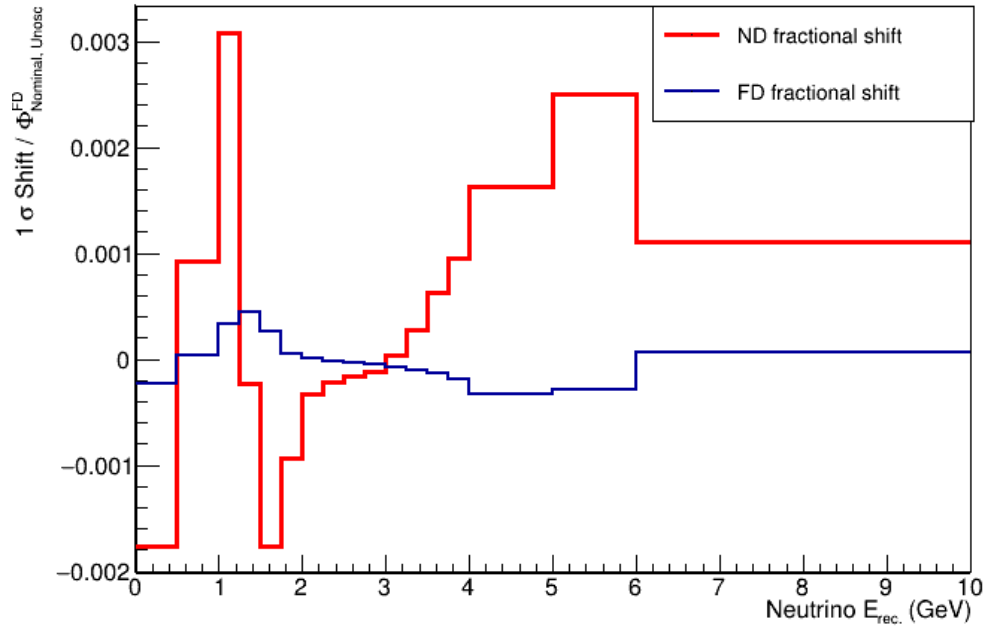


# Horn A Ellipticity X Induced Bfield

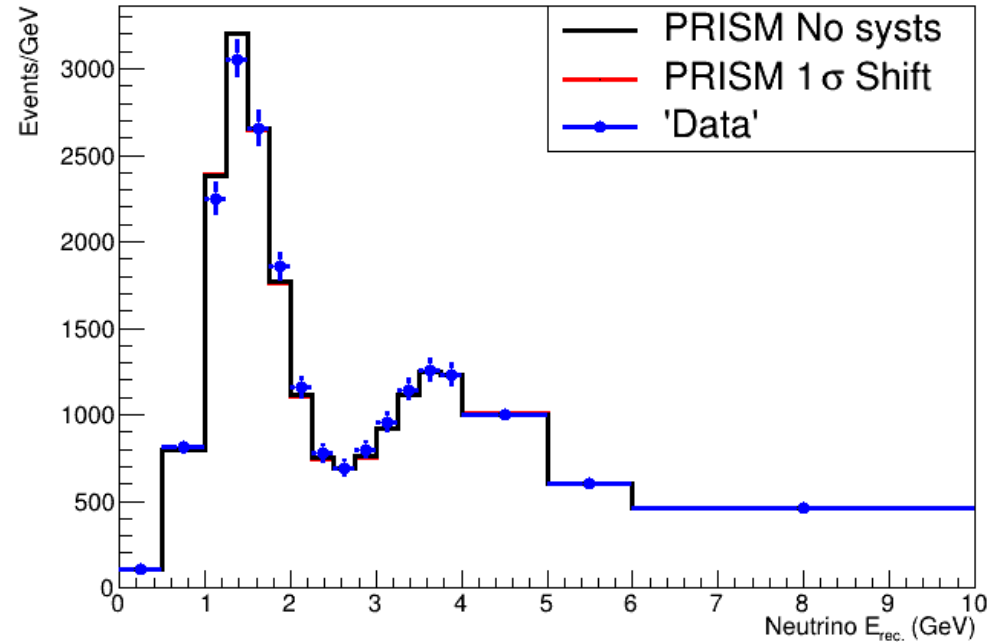
SEMI

-  $1\sigma$  shift = 0.120 mm: NuMi Horn 1 tolerance assumed (elliptical deformation of inner conductor)

Fractional shift HornAEllipticityXInducedBfield+  $1\sigma$



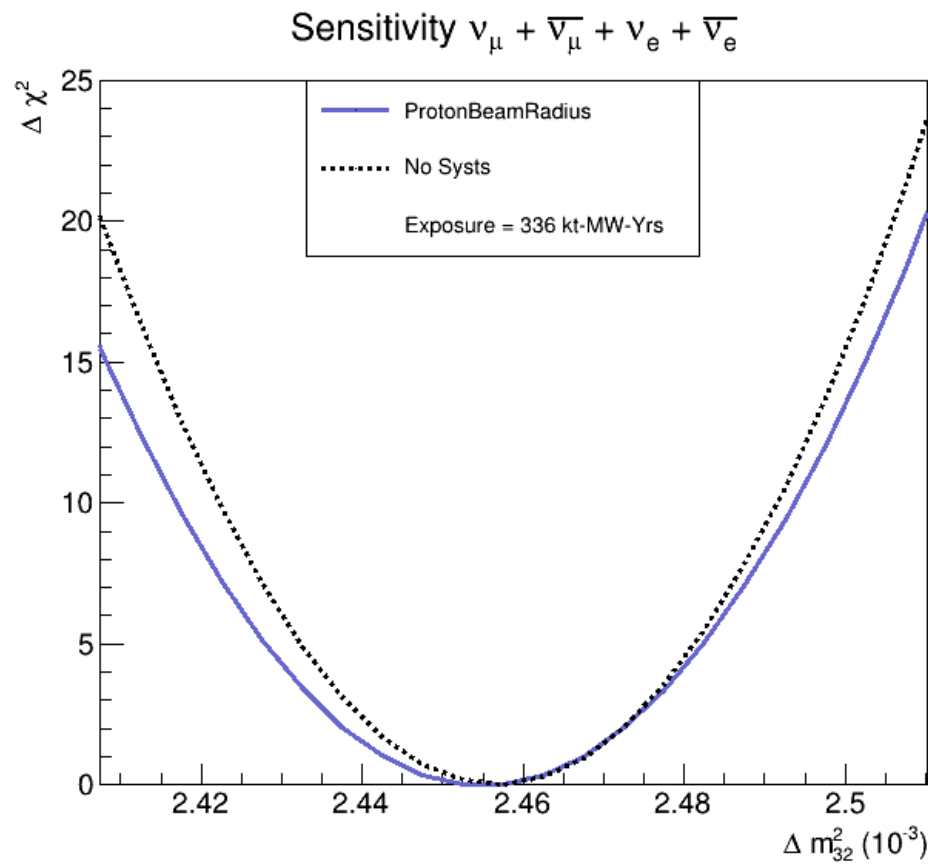
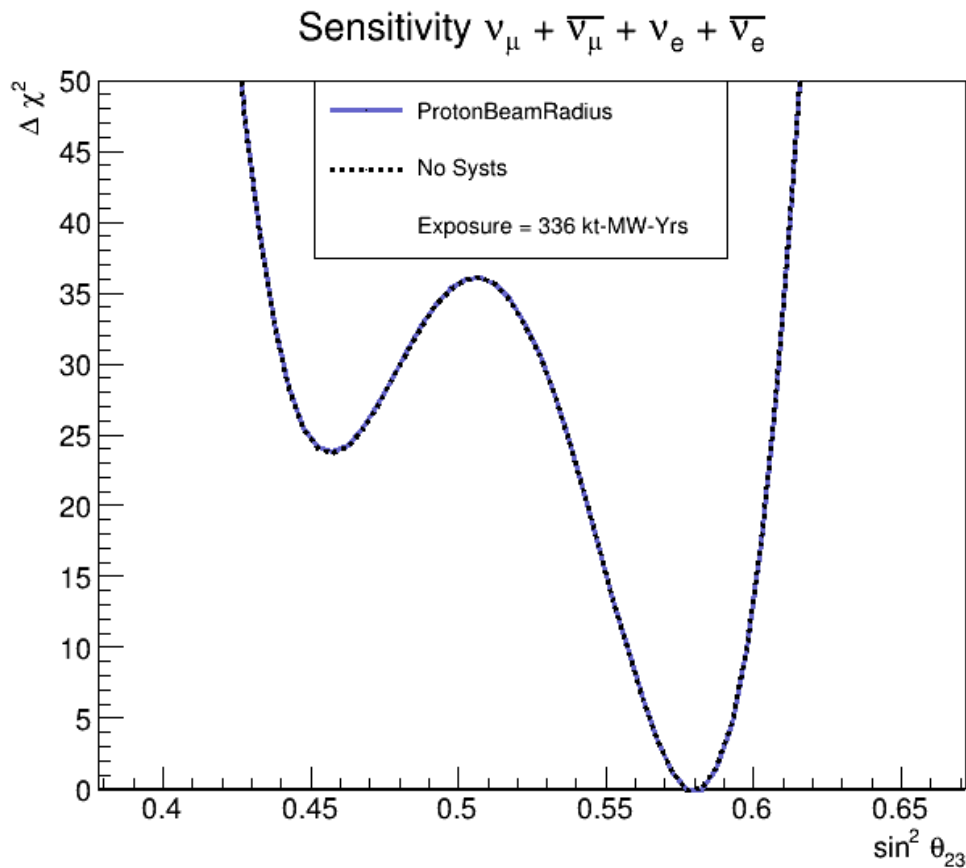
HornAEllipticityXInducedBField



# Proton Beam Radius

SEMI

-  $1\sigma$  shift = 10% (0.27 mm): updated from 1% in TDR



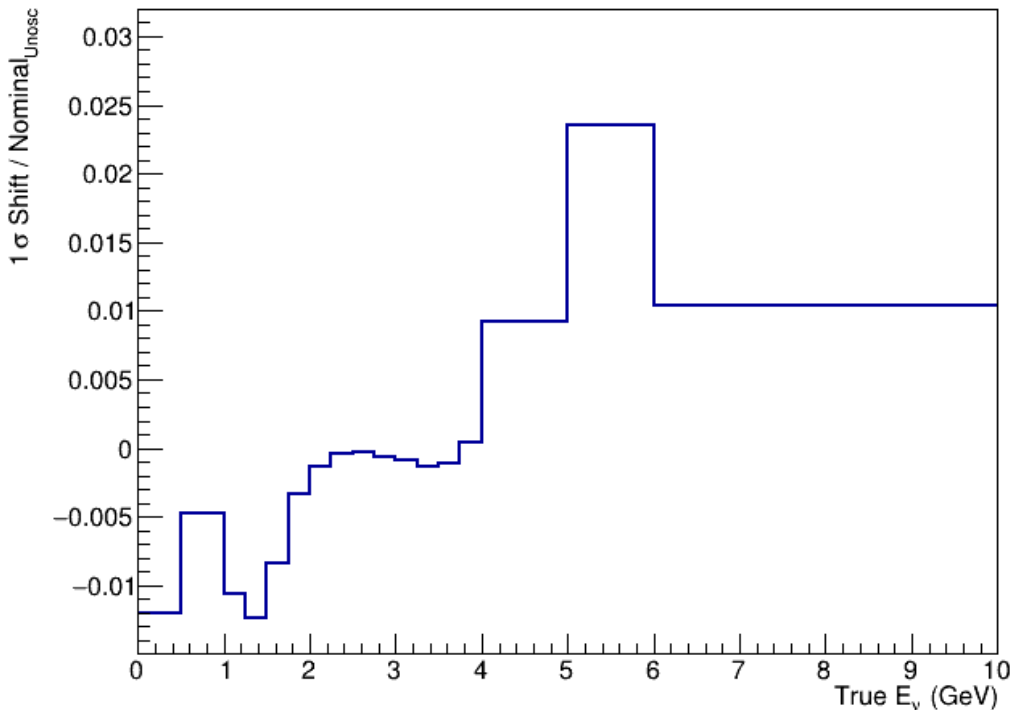


# Proton Beam Radius

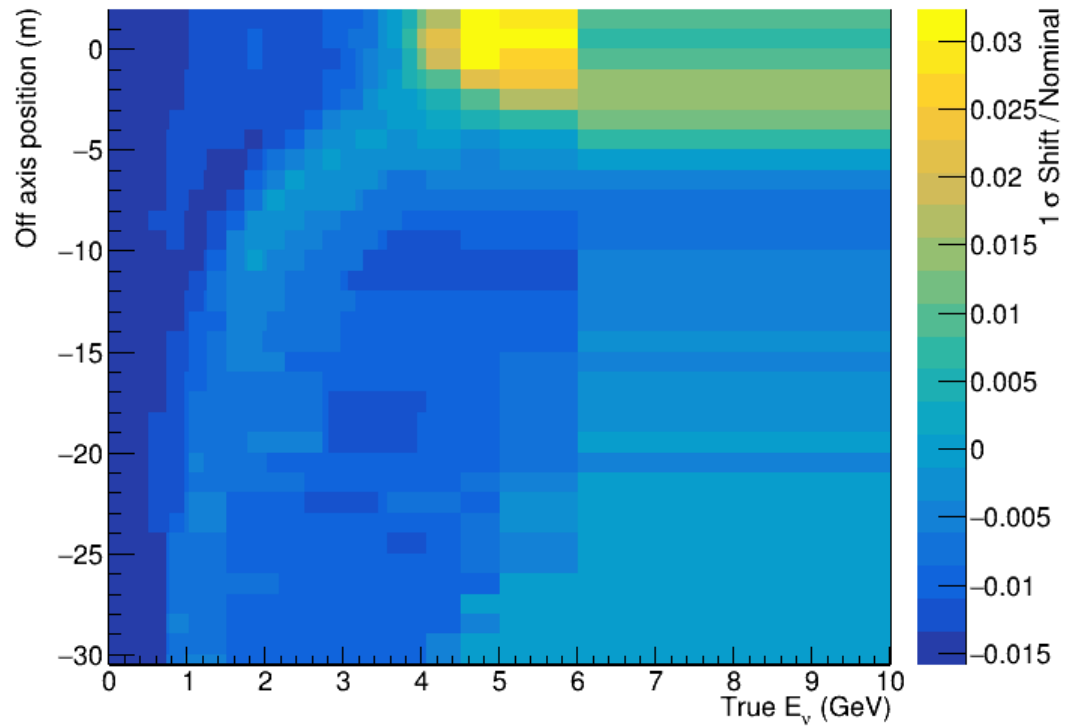
SEMI

-  $1\sigma$  shift = 10% (0.27 mm): updated from 1% in TDR

FD ProtonBeamRadius +  $1\sigma$



ND ProtonBeamRadius +  $1\sigma$

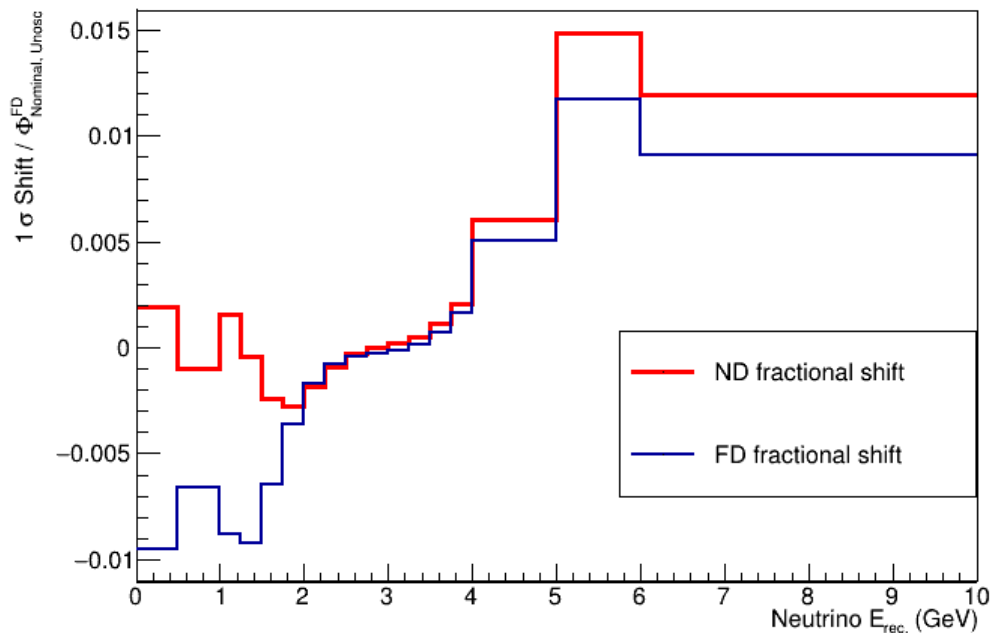


# Proton Beam Radius

SEMI

-  $1\sigma$  shift = 10% (0.27 mm): updated from 1% in TDR

Fractional shift ProtonBeamRadius+  $1\sigma$



ProtonBeamRadius

