# **String hadronization in PYTHIA8:** from $e^+e^-$ to pp and beyond

Javira Altmann - Monash University, visiting University of Oxford

- Confinement in High-Energy Collisions
- > String Junctions
- $\succ$  Strings from vacuum  $\rightarrow$  small systems  $\rightarrow$  heavy ion collisions

> String Hadronisation  $\rightarrow$  Modelling in PYTHIA (QCD Colour Reconnections)



# Confinement in high energy collisions

Consider "hard" processes with large momentum transfers  $Q^2 \gg \Lambda^2_{OCD}$ 

At wavelengths ~  $r_{proton} \sim 1/\Lambda_{QCD}$ 

Need a dynamical process to ensure partons (quarks and gluons) become confined within hadrons

i.e. non-perturbative parton → hadron map

> Example of  $pp \rightarrow t\bar{t}$  event From PYTHIA 8.3 guide arXiv:2201.11601



# Colour neutralisation

## **Require colour neutralisation:**

 $\succ$  The point of confinement is that partons are **coloured**  $\rightarrow$  a physical model needs two or more partons to create **colour neutral** objects

What does this **confinement field** look like?







# Colour neutralisation

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Lattice QCD "Cornell potential"  $V(r) = -\frac{a}{-} + \kappa r$  with  $\kappa \sim 1$  GeV/fm

shows us the potential energy of a colour singlet  $q\bar{q}$  at separation distance r







## **Lund String Model:**

Model the **confining field** between colour charges as a **string** 

Collapse the colour field into a **narrow flux tube** (relativistic 1+1 dimensional world) sheet) with uniform energy density

 $\kappa \sim 1 \text{ GeV/fm}$ 



### Example of a "dipole" string



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 $\kappa \sim 1 \text{ GeV/fm}$ 

### **Quarks / antiquarks**

(anti)triplet  $\rightarrow$  carry (anti)**colour** 

- $\rightarrow$  connected via a string to an anticolour charge
- → string endpoints

### Gluons

- Octet  $\rightarrow$  carry a **colour** and an **anticolour**
- $\rightarrow$  connected via a string to both a colour and an anticolour charge
- $\rightarrow$  transverse excitations on the string ("kinks")





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Signatures of gluon-kinks have been seen Factor ~ 2 more particles in gluon jets





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How does this map partons onto hadrons in high-energy collisions?





# Partons $\rightarrow$ Hadrons

## Hadronisation:

Partons move apart and stretch the string  $\rightarrow$  string breaks

These happen at **non-perturbative** scales, can'

Instead use the **Schwinger mechanism** 



**Schwinger**  $\rightarrow$  **Gaussian**  $p_{\perp}$  **spectrum** and heavy flavour suppression **Prob(u:d:s)**  $\approx$  **1 : 1 : 0.2** 

> Heavy quarks are only produced from hard processes → must be **string endpoints**

't use 
$$P_{g \to q\bar{q}}(z)$$

**Schwinger mechanism QED** 

Non-perturbative creation of  $e^+e^-$  pairs in a string electric field

Probability from tunnelling factor

$$\mathscr{P} \propto \exp\left(\frac{-m^2 - p_{\perp}^2}{\kappa/\pi}\right)$$

Gaussian suppression of high  $m_{\perp}$  =

Baryons formed from beam remnants or diquark-antidiquark pair creation















# Partons $\rightarrow$ Hadrons

## Hadronisation:

- **Schwinger**  $\rightarrow$  **Gaussian**  $p_{\perp}$  **spectrum** and heavy flavour suppression **Prob(u:d:s)**  $\approx$  **1 : 1 : 0.2**
- String breaks are **causally disconnected**
- $\rightarrow$  can fragment off hadrons from either end of the string
  - Probability distribution for the **fraction of quark**
  - **momenta**, z, the hadron will take is parametrised by the

**Lund Symmetric Fragmentation Function** 

$$f(z) \propto \frac{1}{z} (1-z)^a \exp\left(\frac{-b(m_h^2 + p_{\perp h}^2)}{z}\right)$$

Free tuneable parameters *a* and *b* 



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## Partons $\rightarrow$ Hadrons

## Hadronisation:

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→ can fragme Probability d What about colour? momenta, 2 Lund Symmetric rragmentation runction

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# Modelling Colour

## **Leading Colour limit:**

Starting point for Monte Carlo event generators  $N_C \rightarrow \infty$ 

 $\succ$  Each colour is unique  $\rightarrow$  only one way to make colour singlets

- > Only **dipole** strings
- > Used by PYTHIA in the default (Monash 2013) tune

## In $e^+e^-$ collisions :

> Corrections suppressed by  $1/N_C^2 \sim 10\%$ 

> Not much overlap in phase space



e.g. a dipole string configuration which make use of the **colour-anticolour** singlet state







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## In $e^+e^-$ collisions :

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> Not much overlap in phase space

But high-energy pp collisions involve very many coloured partons with significant phase space overlaps



e.g. a dipole string configuration which make use of the **colour-anticolour** singlet state

**QCD** Colour Reconnection (CR) model







Stochastically restores colour-space ambiguities according to **SU(3) algebra** 

> Allows for reconnections to **minimise string lengths** 

### **Colour - anticolour** singlet state









Stochastically restores colour-space ambiguities according to **SU(3) algebra** 

> Allows for reconnections to **minimise string lengths** 



- What about the **red-green-blue** colour singlet state?









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# Junction Rest Frame

## What is the junction rest frame?

If the momenta of the junction legs are at 120° angles  $\rightarrow$  the pull in each direction on the junction is equal  $\rightarrow$  junction is at rest









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### **Does a boost to the mercedes frame always exist?**

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# Junction Rest Frame

## What is the junction rest frame?

If the momenta of the junction legs are at 120° angles  $\rightarrow$  the pull in each direction on the junction is equal  $\rightarrow$  junction is at rest





\*no special consideration for these cases in current implementation









# Pearl-on-a-string

The junction gets "stuck" to the soft quark, which we call a pearl-on-a-string

> More likely to occur for junctions with heavy flavour endpoints





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> More likely to occur for junctions with heavy flavour endpoints

For a junction to make a **heavy baryon**, the junction leg with the heavy quark can't fragment (*i.e.* a "soft" junction leg) = pearl-on-a-string!







Use an "average" JRF

- Current procedure assumes the **average is the mercedes frame** > Uses energy weighted sum of momenta on each junction leg
- > Relies on convergence procedure that fails ~10% of cases

### New treatment:

- $\succ$  Considers pull on junction over time and average over junction motion
- > Includes pearl-on-a-string
- > Allow endpoint oscillations
- > No reliance on convergence

 $\succ$  Early time JRF defined by the first parton on each leg > Use smallest leg momentum as a measure of effective time for the JRF  $\gg$  When softest parton has lost its momentum, the next parton dominates the pull

# Updates to averaging







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Starting point for Monte Carlo is leading colour  $N_C \to \infty$  i.e. unique colour singlet configurations determined by colour tracing in hard processes

CR restores missing colour correlations from SU(3) assuming string "length" minimisation

Aims to stochastically restore these colour correlations using SU(3) algebra

- $3 \otimes \overline{3} = 8 \oplus 1$  (colour-anticolour)
- $3 \otimes 3 = 6 \oplus \overline{3}$  (colour-colour)

**Dipole-type reconnection: colour-anticolour** 



Recent brief review on CR arXiv:2405.19137

"string length" is not a spatial measure but measure of approx how many hadrons a string can make e.g. rapidity-type measure or invariant mass of the dipole









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Recent brief review on CR arXiv:2405.19137

# baryon-to-meson ratio increase, $\langle p_{\perp} \rangle$ increase with multiplicity, some flow-like effects





















After the string has had time after its initial creation to expand to its full transverse size, strings will start "shoving"



s = 7 TeV collision example e.g.  $\sqrt{}$ 

\*uses string radius of 0.2 fm for illustration purposes but in reality can be much larger

# Shoving





After the string has had time after its initial creation to expand to its full transverse size, strings will start "shoving"

**CR has already occurred** with string minimisation choosing singlet configurations

- $\rightarrow$  only octet states would likely be near one another
- → only **repulsion** left



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# Shoving

- After the string has had time after its initial creation to expand to its full transverse size, strings will start "shoving"

culable from the field 
$$E = N \exp(-\rho^2/2R^2)$$

- Energy per unit length of two strings overlapping  $\int d^2 \rho \frac{(E_1 + E_2)^2}{2}$
- Force between two strings transversely separated

$$\operatorname{en} f(d_{\perp}) = \frac{g\kappa d_{\perp}}{R^2} \exp\left(-\frac{d_{\perp}^2}{4R^2}\right)$$

p is the radius in cylindrical coordinates

R is the equilibrium radius

N is a normalization factor, determined by letting the energy in the field correspond to a **fraction g** of the total string tension.









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### **Force cale**

by  $d_{\parallel}$  is the

- > Use parallel dogbone frame
- $\succ$  Ordered in  $p_{\perp}$  in similar spirit to parton shower ordering

# Shoving

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### Monte Carlo implementation details

Requires space-time picture of strings











# Shoving in pp

After the string has had time after its initial creation to expand to its full transverse size, strings will start "shoving"

**CR has already occurred** with string minimisation choosing singlet configurations

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### First look at **toy case**

- $\gg$  Multiplicity generated by a single string well known (approx one hadron per unit of rapidity)
- centrality interval

Not perfect agreement however is only a toy model and uses same parameters as pp collision systems

### source of flow can be the same across collision systems!!!



 $\gg$  System of straight strings (no gluon kinks) that corresponds to the multiplicity of AA collisions in a given

Correlation between initial state  $\epsilon_2$  and final state  $v_2$  is linear in hydrodynamic deconfined QGP phase - similarly with shoving → hydrodynamic behaviour is not limited to deconfined systems







20 15



# Shoving in AA

### Full **Pb-Pb collision in Angantyr**

> Implementation issues

Many **soft gluons** → **short interaction time** for shoving mechanism as the mechanism does not consider the region formed from soft gluons  $\rightarrow$  insufficient level of shoving

> Trend is in the correct direction but insufficient, also lacks curved shape











### Use Schwinger mechanism to model tunnelling of quark-antiquark pairs created by string breaks



Strange production in the string picture









## Strange production in the string picture

### Use Schwinger mechanism to model tunnelling of quark-antiquark pairs created by string breaks

![](_page_41_Figure_4.jpeg)

## **Schwinger mechanism QED**

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Non-perturbative creation of  $e^+e^-$  pairs in a string electric field

Probability from tunnelling factor

$$\mathscr{P} \propto \exp\left(\frac{-m^2 - p_{\perp}^2}{\kappa/\pi}\right)$$

 $\kappa$  = string tension

![](_page_41_Picture_14.jpeg)

![](_page_41_Picture_15.jpeg)

![](_page_42_Figure_1.jpeg)

## Strange production in the string picture

Use **Schwinger mechanism** to model tunnelling of quark-antiquark pairs created by string breaks

![](_page_42_Figure_4.jpeg)

Schwinger  $\rightarrow$  Gaussian  $p_{\perp}$  spectrum and heavy flavour suppression **Prob(u:d:s)**  $\approx$  **1 : 1 : 0.2** 

# **Schwinger mechanism QED**

Non-perturbative creation of  $e^+e^-$  pairs in a string electric field

Probability from tunnelling factor

$$\mathscr{P} \propto \exp\left(\frac{-m^2 - p_{\perp}^2}{\kappa/\pi}\right)$$

 $\kappa = \text{string tension}$ 

### Heavy quarks (charm and bottom) are only produced from hard processes $\rightarrow$ must be string endpoints

![](_page_42_Picture_17.jpeg)

![](_page_42_Picture_18.jpeg)

## Rope hadronisation

arXiv:1412.6259

![](_page_43_Figure_4.jpeg)

![](_page_43_Picture_11.jpeg)

## Rope hadronisation

arXiv:1412.6259

 $\rightarrow$  not in conjunction with shoving

![](_page_44_Figure_6.jpeg)

![](_page_44_Picture_10.jpeg)

![](_page_44_Picture_11.jpeg)

![](_page_45_Figure_1.jpeg)

![](_page_45_Figure_3.jpeg)

![](_page_45_Figure_4.jpeg)

![](_page_45_Figure_5.jpeg)

![](_page_45_Picture_11.jpeg)

![](_page_46_Figure_1.jpeg)

![](_page_46_Figure_3.jpeg)

![](_page_46_Picture_9.jpeg)

![](_page_47_Figure_1.jpeg)

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![](_page_47_Picture_4.jpeg)

![](_page_47_Picture_5.jpeg)

![](_page_47_Picture_6.jpeg)

# Proton problem

### Popcorn mechanism for diquark production

### Diquark formation via successive colour fluctuations — popcorn mechanism

![](_page_48_Figure_3.jpeg)

![](_page_48_Figure_5.jpeg)

![](_page_48_Picture_7.jpeg)

# Proton problem

### Popcorn mechanism for diquark production

### Diquark formation via successive colour fluctuations — popcorn mechanism

![](_page_49_Figure_3.jpeg)

### What if there's a blue string nearby?

![](_page_49_Picture_5.jpeg)

blue  $q\bar{q}$  fluctuation breaks nearby blue string, preventing diquark formation

![](_page_49_Figure_8.jpeg)

![](_page_49_Picture_10.jpeg)

![](_page_49_Picture_11.jpeg)

# Results — ongoing

![](_page_50_Figure_1.jpeg)

### Cannot describe both baryon-to-meson ratios simultaneously

Taken from slide by Lorenzo Bernadinis: masters student currently undertaking tuning project with the model

![](_page_50_Picture_8.jpeg)

![](_page_50_Picture_9.jpeg)

![](_page_50_Picture_10.jpeg)

Evidence that collective effects can arise from non-QGP sources

- **CR** restores SU(3) colour correlations
- $\rightarrow$  baryons-to-meson ratio enhancement,  $\langle p_{\perp} \rangle$  increase with multiplicity, some flow-like Angantyr allows for *pA* and *AA* using strings instead of QGP

 $\rightarrow$  multiplicity distributions for AA

**Shoving** string interactions before hadronisation

### Ropes

 $\rightarrow$  strangeness enhancement

**Unmentioned:** jet quenching, hadron rescattering

Future studies: shoving considering regions formed by soft gluons, reexamination of results given updates to CR in Angantyr (previous modelling only included CR within each nucleon-nucleon collision, now CR is allowed between nucleon-nucleon collisions)

## Summary

 $\rightarrow$  near-sided ridge in pp, some  $v_2$  with full description hindered by implementation technicality issues

![](_page_51_Picture_14.jpeg)

![](_page_51_Picture_15.jpeg)

![](_page_52_Figure_1.jpeg)

![](_page_52_Figure_2.jpeg)

Clear observations of strangeness enhancement with respect to charged multiplicity [e.g. ALICE Nature Pays. 13, 535 (2017)]

# Vacuum $\rightarrow$ High multiplicities

### **Protons are composite**

- $\rightarrow$  lots of quarks and gluons inside
- → multiple parton-parton interactions
- $\rightarrow$  lots of colour charges

Strangeness enhancement with charged multiplicity suggests higher multiplicity string systems act different to the vacuum case

> Number of fundamental and antifundamental flux lines at central rapidity in *pp* collisions give us **effective** multiplet representation

Reach higher than simple quarkantiquark triplet string

![](_page_52_Picture_14.jpeg)

![](_page_52_Picture_18.jpeg)

## Popcorn Mechanism

arXiv:hep-ph/9606454

### Diquark formation via successive colour fluctuations

![](_page_53_Picture_4.jpeg)

![](_page_53_Figure_6.jpeg)

![](_page_53_Picture_7.jpeg)

![](_page_53_Picture_8.jpeg)

![](_page_53_Picture_13.jpeg)

## Popcorn Mechanism

arXiv:hep-ph/9606454

### Diquark formation via successive colour fluctuations

![](_page_54_Figure_4.jpeg)

blue  $q\bar{q}$  fluctuation on the string

![](_page_54_Figure_7.jpeg)

![](_page_54_Picture_8.jpeg)

![](_page_54_Picture_9.jpeg)

![](_page_54_Picture_14.jpeg)

## Popcorn Mechanism

arXiv:hep-ph/9606454

### Diquark formation via successive colour fluctuations

![](_page_55_Figure_4.jpeg)

![](_page_55_Figure_6.jpeg)

![](_page_55_Picture_7.jpeg)

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![](_page_55_Picture_13.jpeg)

## Popcorn Mechanism

arXiv:hep-ph/9606454

### Diquark formation via successive colour fluctuations

![](_page_56_Figure_4.jpeg)

### What if there's a blue string nearby?

![](_page_56_Picture_6.jpeg)

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![](_page_56_Picture_9.jpeg)

![](_page_56_Picture_14.jpeg)

## Popcorn Mechanism

arXiv:hep-ph/9606454

### Diquark formation via **successive colour fluctuations**

![](_page_57_Figure_4.jpeg)

### What if there's a blue string nearby?

![](_page_57_Figure_6.jpeg)

![](_page_57_Figure_8.jpeg)

Only basic model implemented thus far, further improvements on the modelling still happening!

![](_page_57_Picture_11.jpeg)

![](_page_57_Picture_12.jpeg)

![](_page_57_Picture_17.jpeg)

![](_page_58_Figure_4.jpeg)

![](_page_58_Figure_6.jpeg)

![](_page_58_Picture_9.jpeg)

![](_page_58_Picture_15.jpeg)

# Vacuum $\rightarrow$ Small Systems $\rightarrow$ Heavy Ion

String model has well described  $e^+e^-$  systems (i.e. cases with not many strings), and we've explored high multiplicity small systems, but what about heavy ion systems?

> Do we still have strings? Do we have QGP? Is it a mix of both, or is there a smooth transition between the strings and QGP?

Angantyr uses PYTHIA as its base to do pA and AA collisions, using only strings (**no QGP** formation)

Collective effects of strings can describe features that are typically described as signature of QGP

- $\succ$  Near-sided ridge  $\rightarrow$  string shoving
- $\gg v_2 \rightarrow \text{string repulsion}?$
- Strangeness enhancement → ropes/close-packing

How far can we push the string model?

![](_page_59_Picture_12.jpeg)

![](_page_59_Picture_16.jpeg)

# Thank you for listening!

![](_page_60_Picture_3.jpeg)