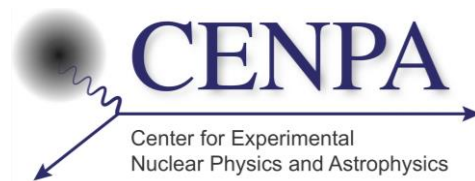




# Beam Dynamics Challenges in the Muon $g - 2$ Experiment

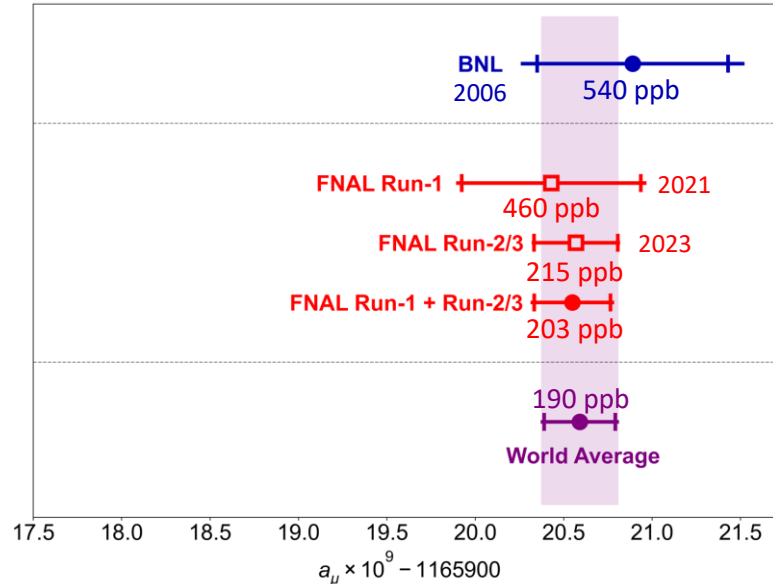
Brynn MacCoy, University of Washington

July 11, 2024



# Muon g-2 measurements reached unprecedented precision in 2023

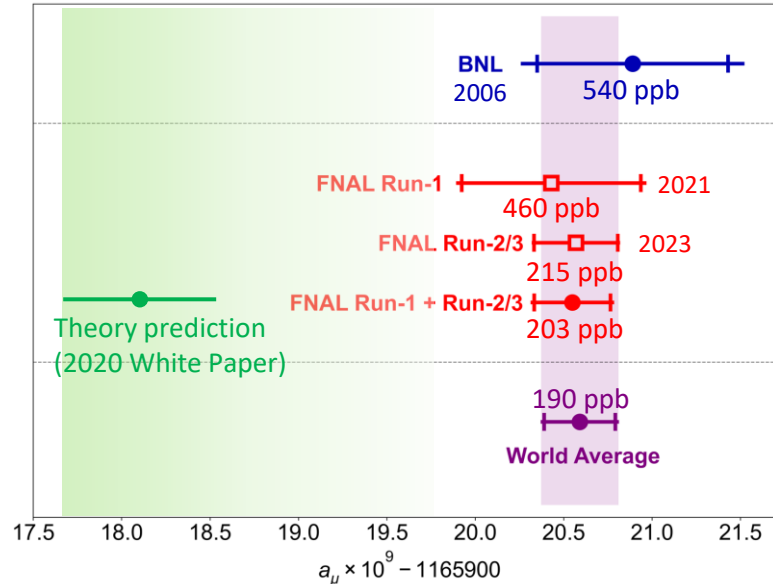
Measured values of the muon anomalous magnetic moment  $a_\mu$



- Latest Fermilab Muon g-2 measurement confirmed previous measurements with highest precision yet

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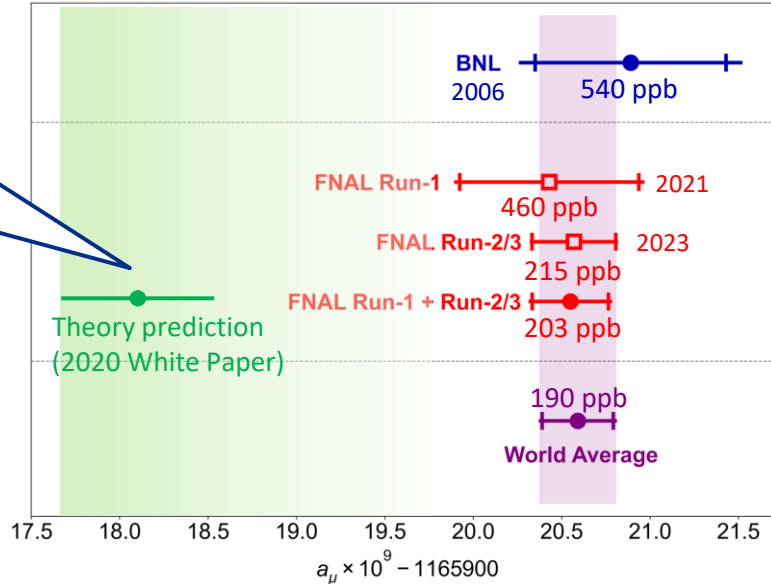


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Awaiting next theory update – will likely decrease current tension

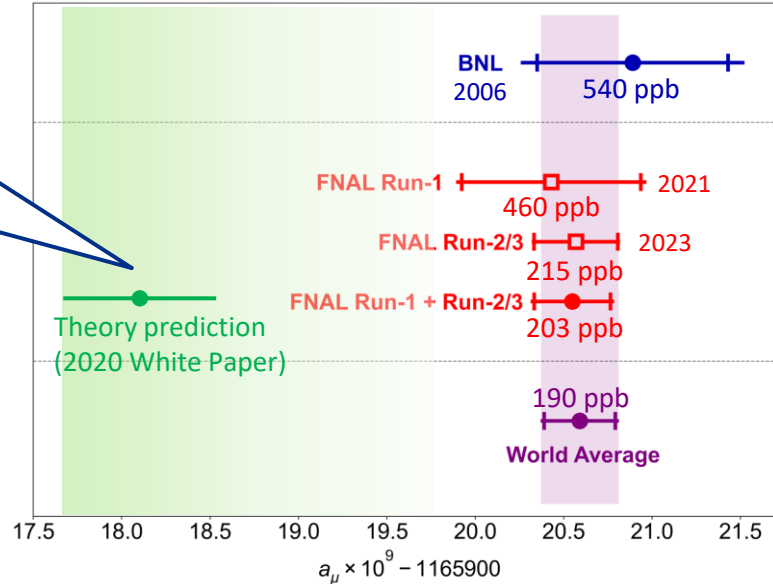


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- Latest Fermilab Muon g-2 measurement confirmed previous measurements with highest precision yet
- Strengthened standing discrepancy in experiment vs. Standard Model theory
- More motivation than ever to deliver highest-precision measurement

# Magnetic moment is affected by virtual particles

magnetic  
moment

spin

$$\vec{\mu} = g \frac{q}{2m} \vec{S}$$

gyromagnetic ratio

# Magnetic moment is affected by virtual particles

magnetic  
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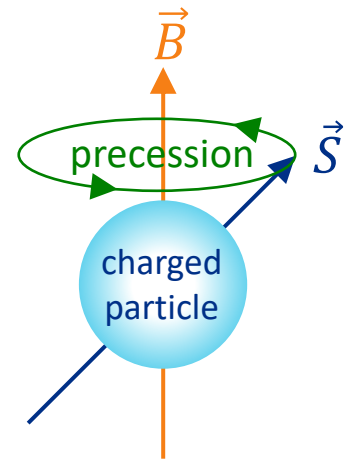
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Spins precess in  
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$$\omega = g \frac{q}{2m} B$$



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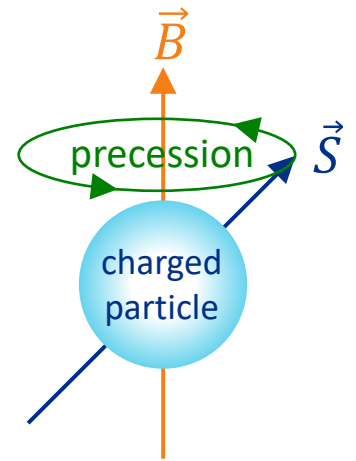
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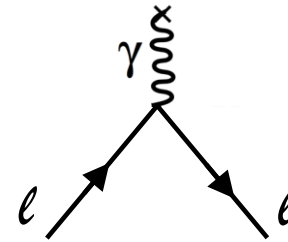
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- Dirac equation for spin  $\frac{1}{2}$  particles  $g = 2$





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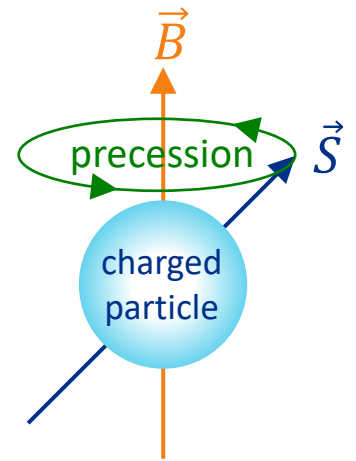
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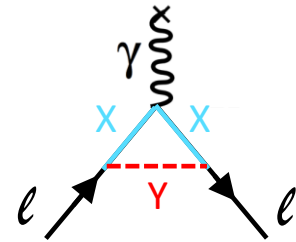


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- Loop corrections  $\rightarrow$

anomalous magnetic moment

$$g = 2(1 + a)$$



Virtual  
particles  $X, Y$

# Magnetic moment is affected by virtual particles

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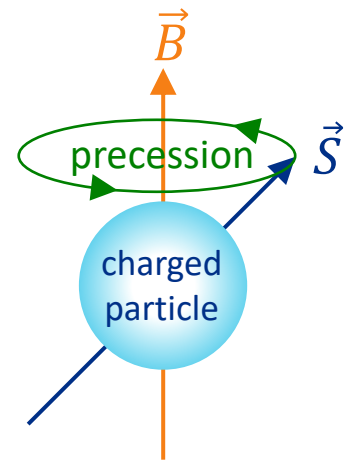
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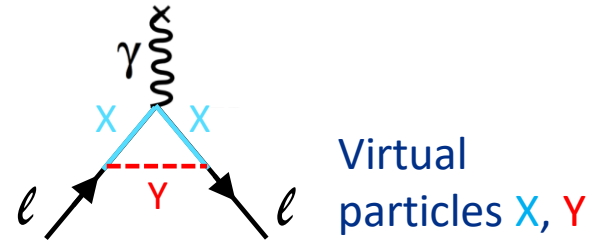
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- Predict with Standard Model:  
QED (dominant), EW, QCD contributions

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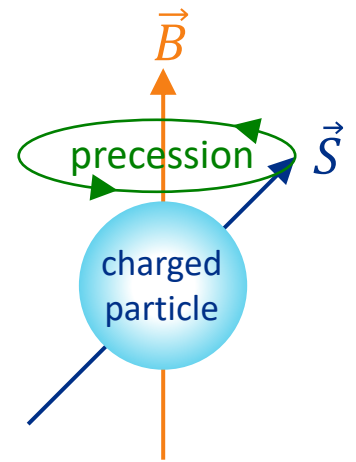
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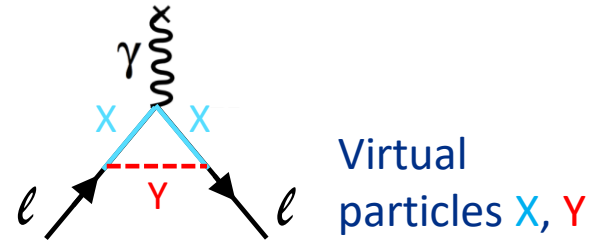
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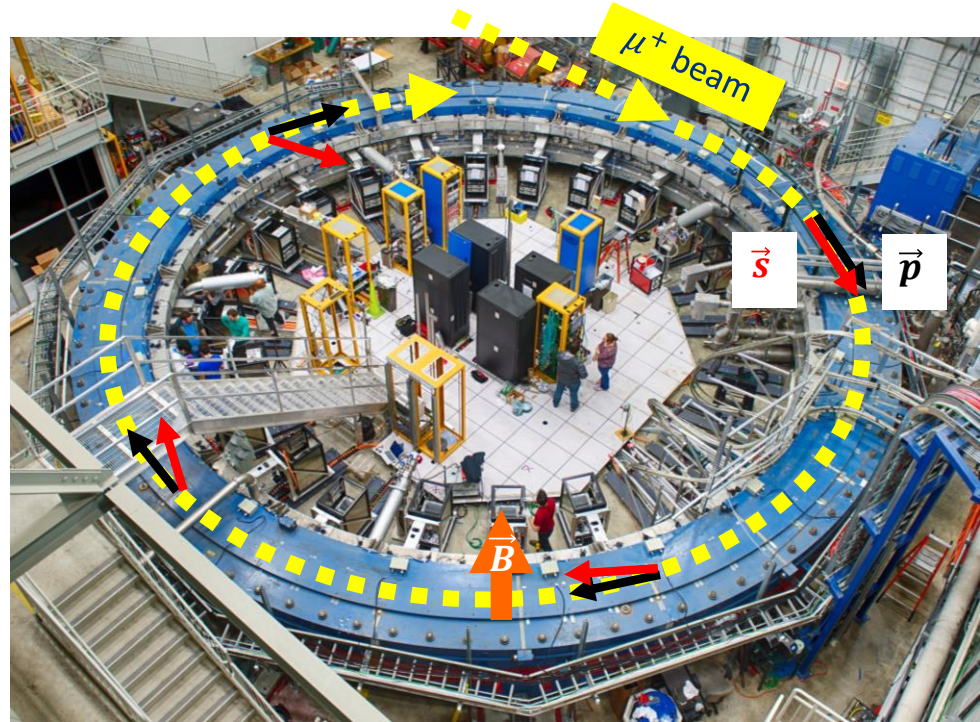
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- Predict with Standard Model:  
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- Discrepancy with experiment suggests new physics

# Measuring $a_\mu$ at Fermilab Muon g-2

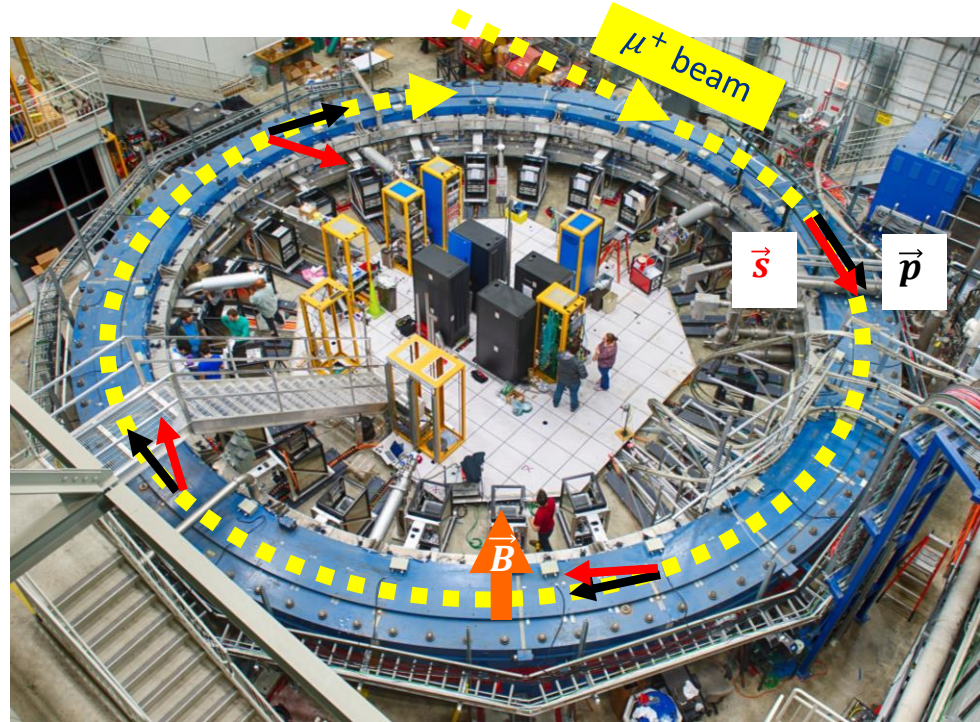
- Goal: Measure  $a_\mu$  to 140 ppb (4× more precise than BNL, on par with theory precision target)
- Details in On Kim's g-2 report today
- Inject polarized muons ( $\mu^+$ ) into magnetic storage ring



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$$\vec{\omega}_a = \vec{\omega}_s - \vec{\omega}_c = -a_\mu \frac{e}{m} \vec{B}$$



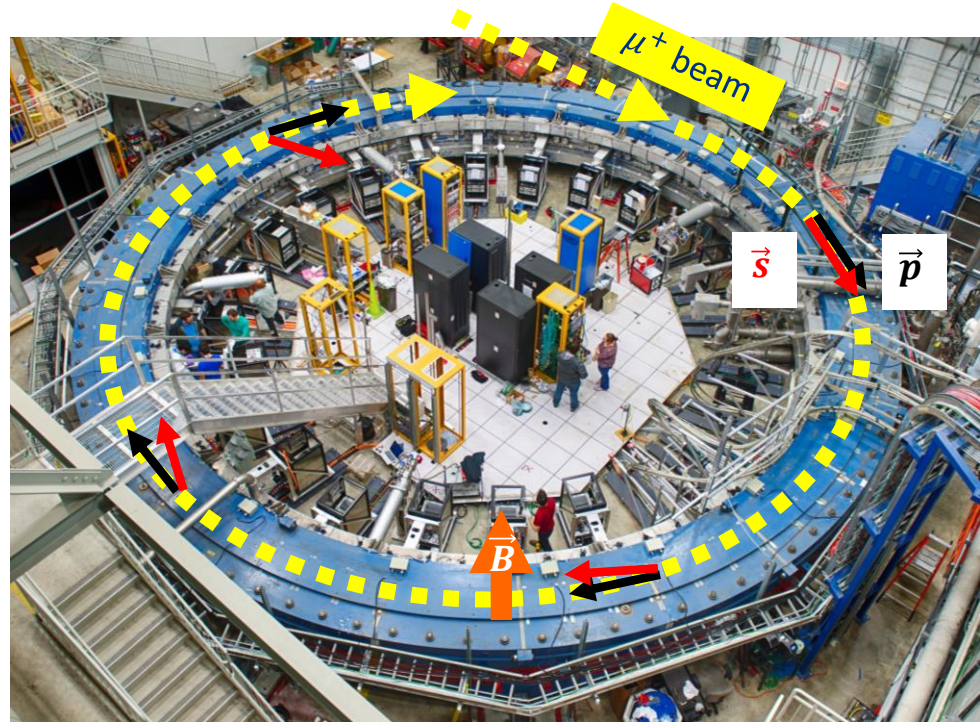


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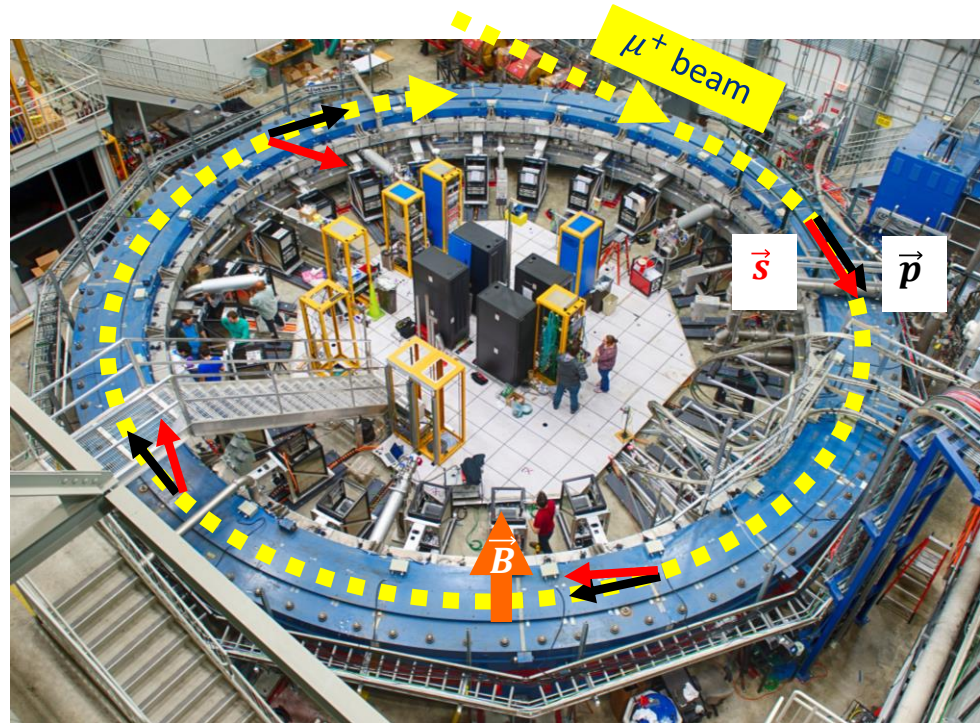
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Measure with  
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Measure with  
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# Measuring $a_\mu$ at Fermilab Muon g-2

- $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$
- 24 calorimeters measure  $e^+$  energy and arrival time



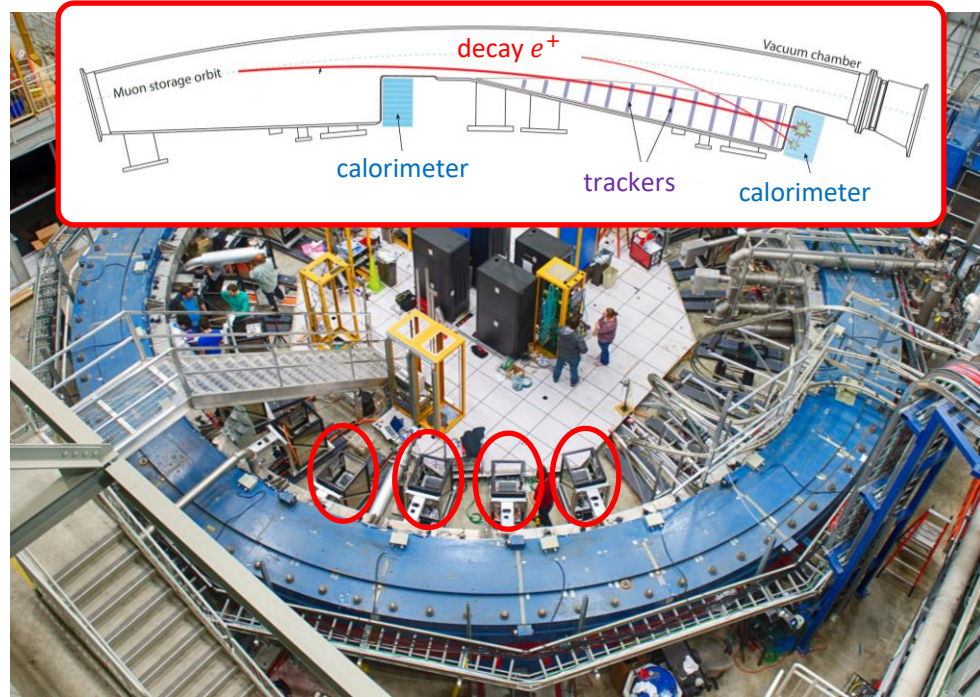
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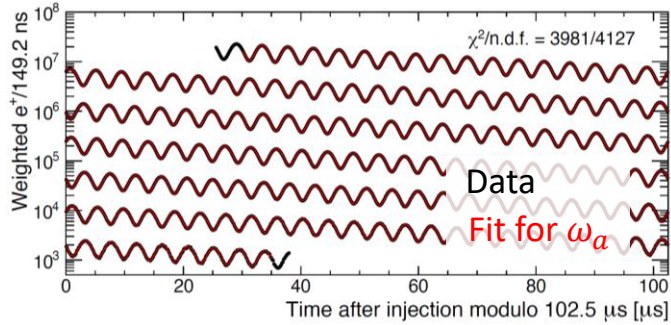
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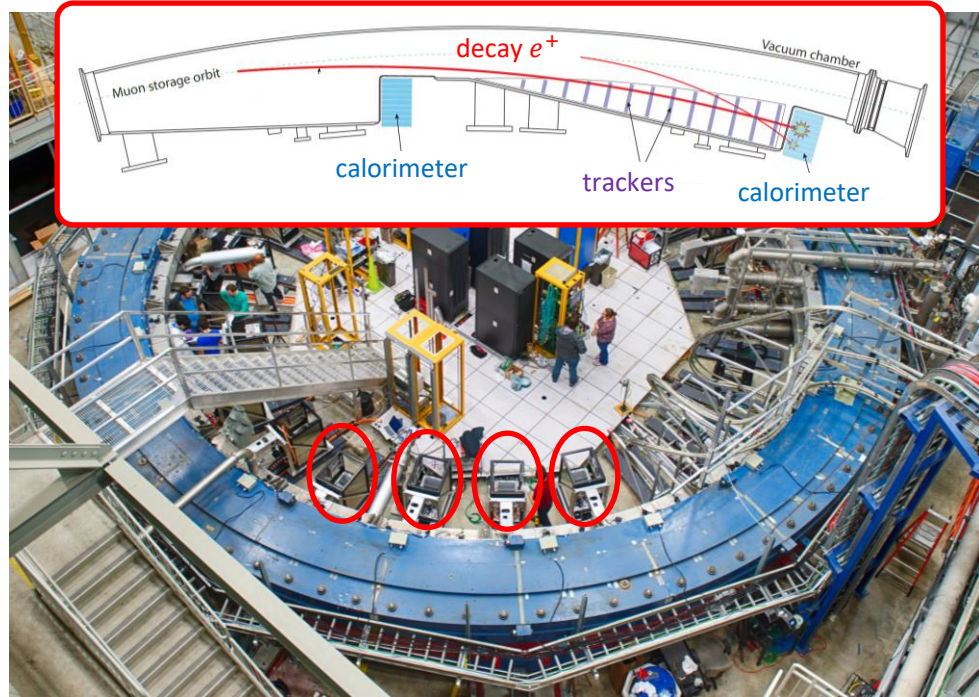
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$e^+$  above E threshold vs time modulated by  $\omega_a$

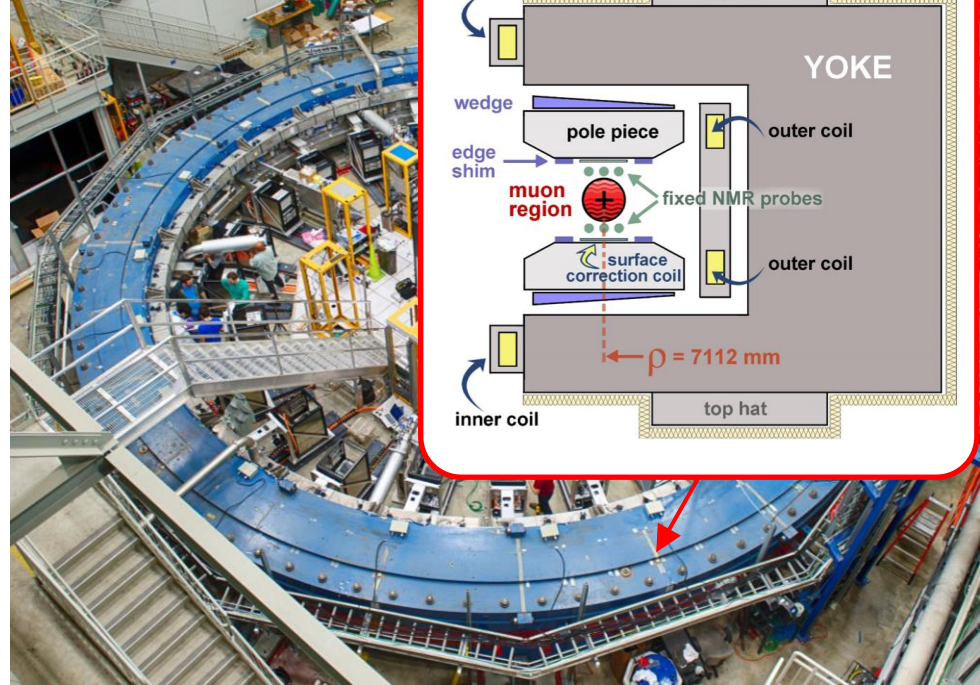


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# Measuring $a_\mu$ at Fermilab Muon g-2



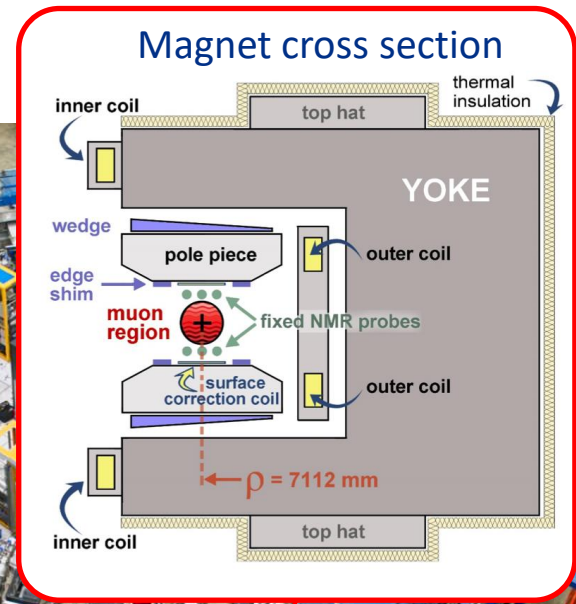
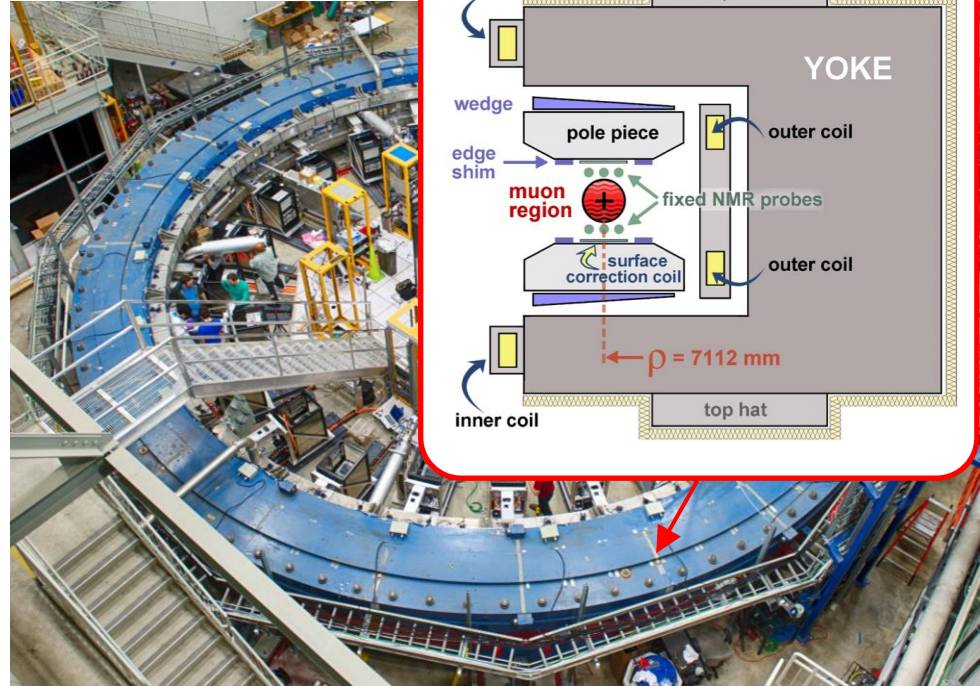
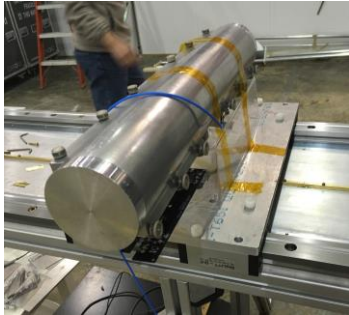
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# Measuring $a_\mu$ at Fermilab Muon g-2

- Trolley maps field every few days

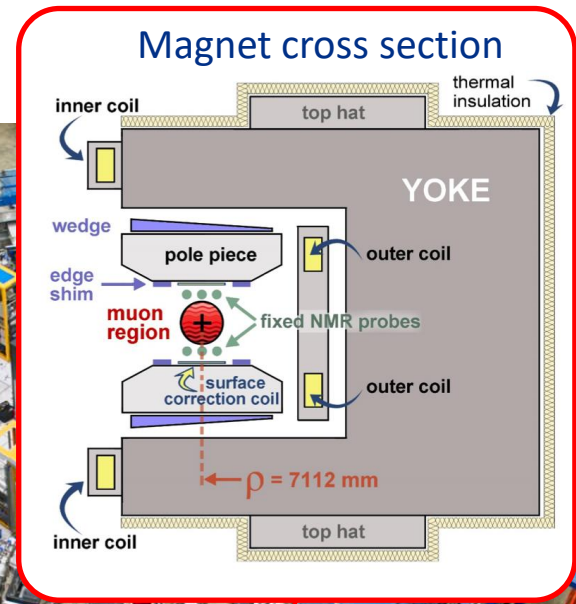
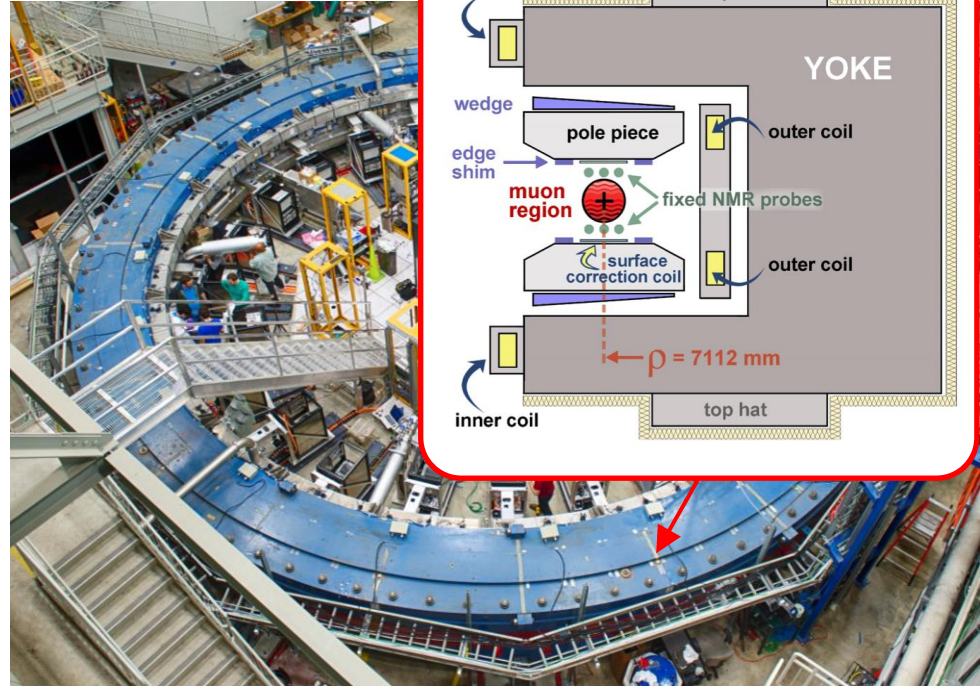
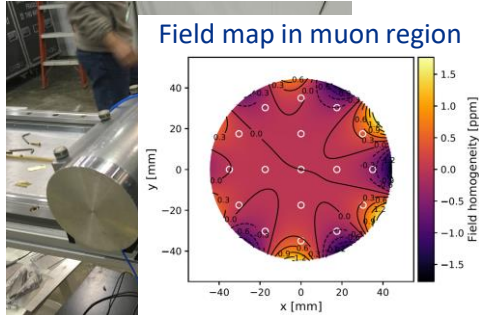


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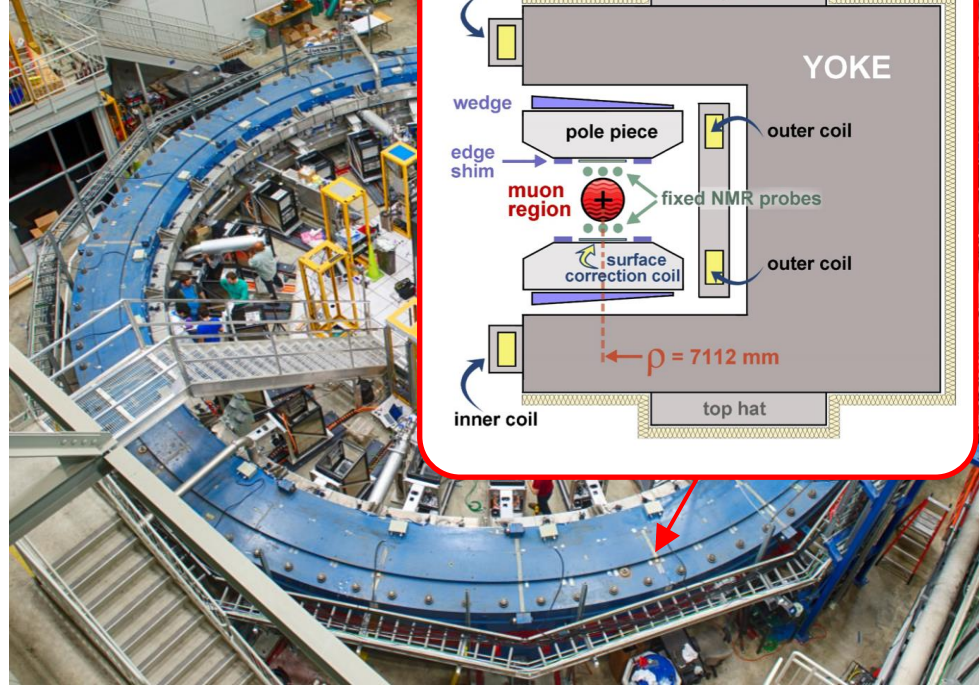
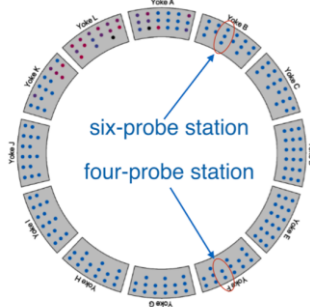
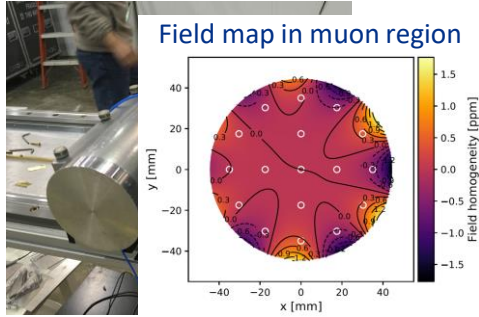


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# Measuring $a_\mu$ at Fermilab Muon g-2

- Trolley maps field every few days
- Fixed probes monitor field drift



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Measure with  
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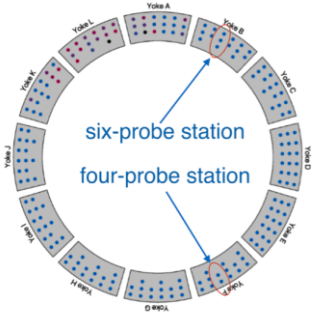
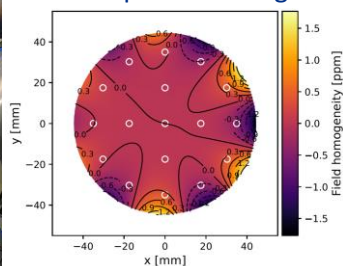


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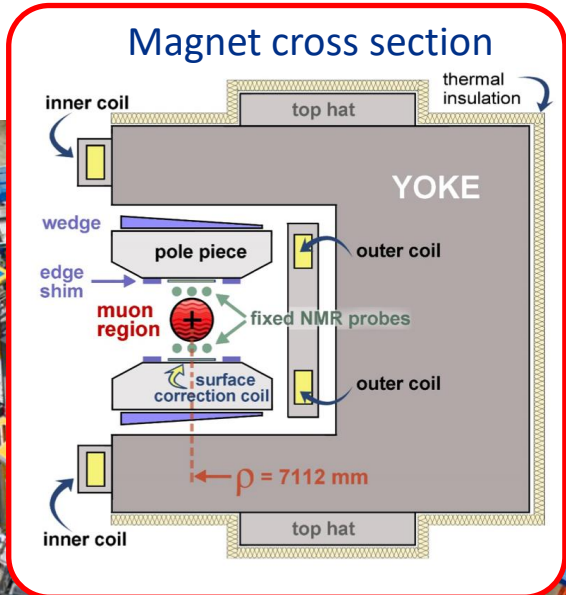
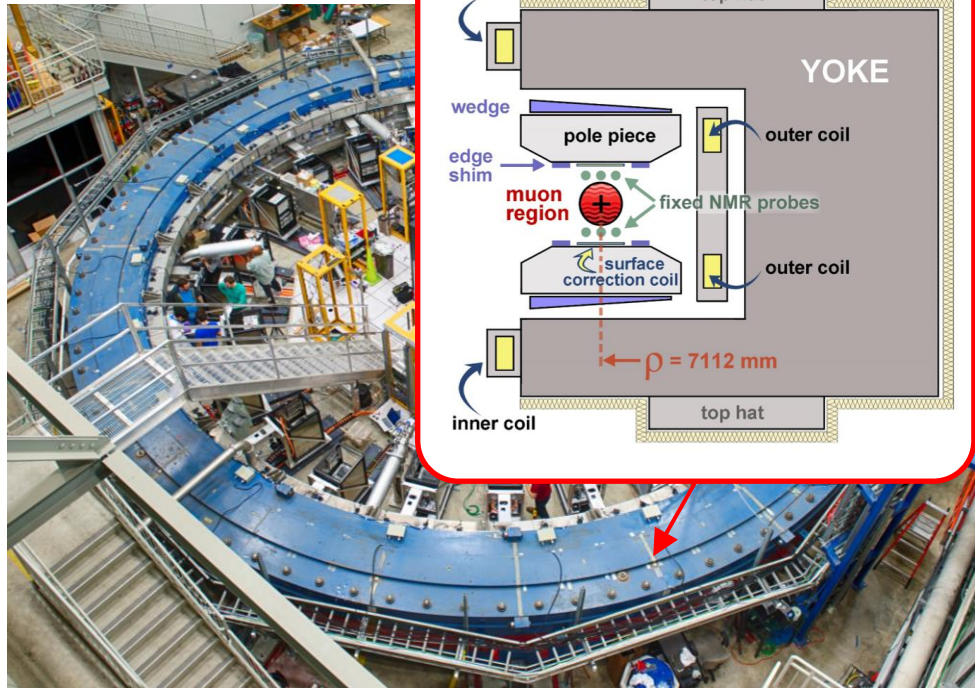
Field map in muon region



Field in ring during  $\omega_a$  measurements

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Measure with  
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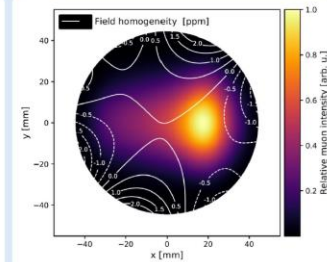
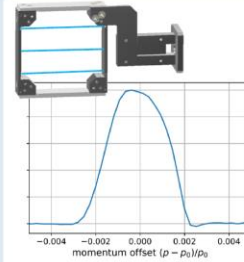
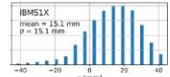
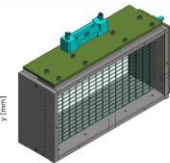
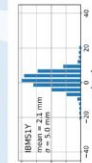
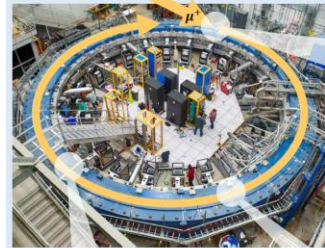


# Measuring $a_\mu$ at Fermilab Muon g-2

- Beam dynamics (motion of the muons) affects both observables
- My thesis focused on several beam dynamics effects critical for precision goal

$$\vec{\omega}_a = \vec{\omega}_s - \vec{\omega}_c = -a_\mu \frac{e}{m} \vec{B}$$

## Beam Dynamics Challenges in the Muon g-2 Experiment

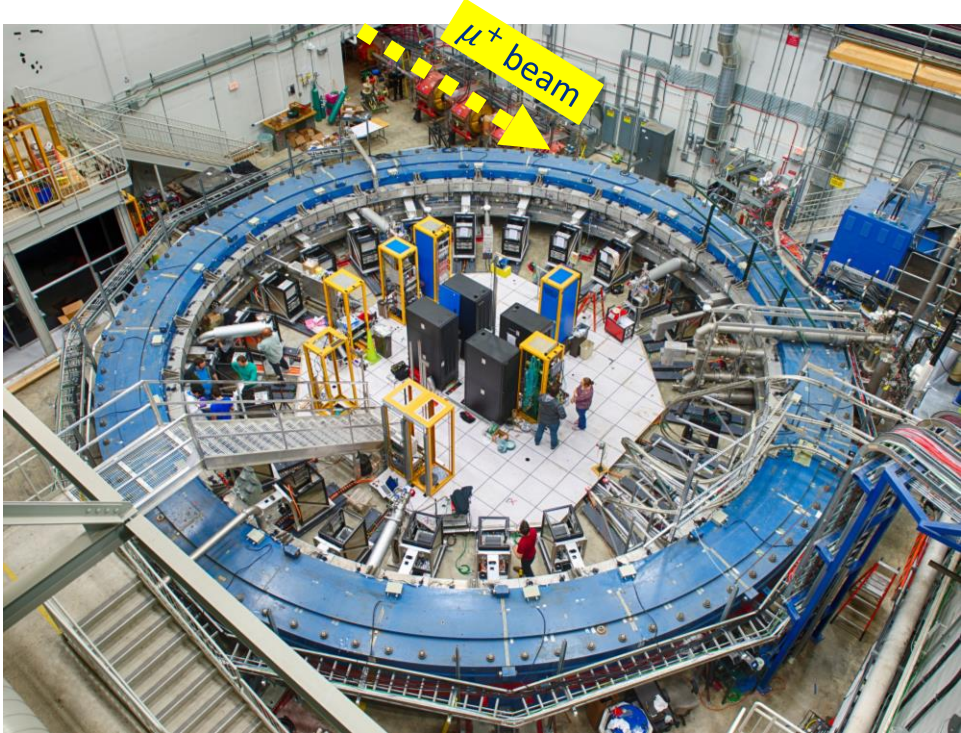


Brynn MacCoy

A dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy  
University of Washington | June 2023

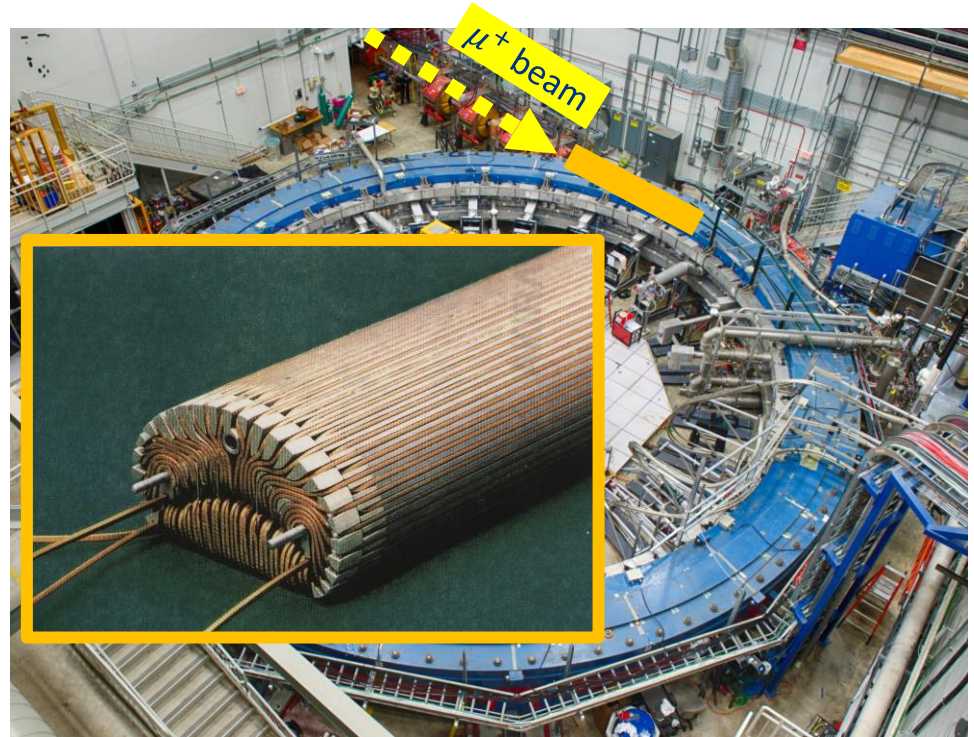


# Injecting and storing muons in the ring



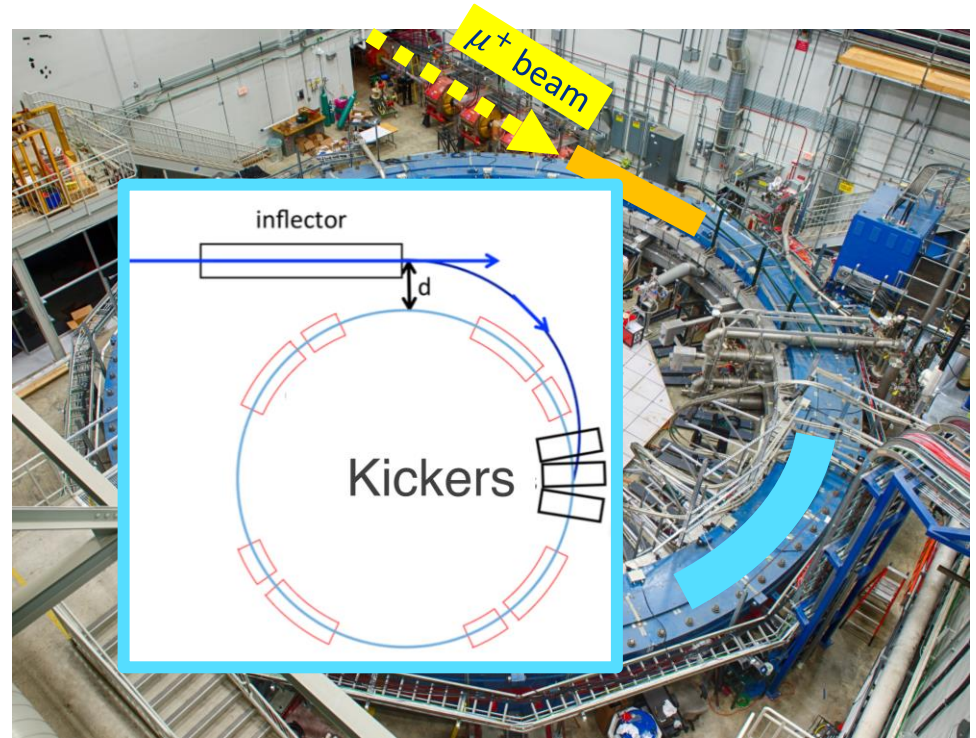
# Injecting and storing muons in the ring

- **Inflector magnet** cancels field along injection path



# Injecting and storing muons in the ring

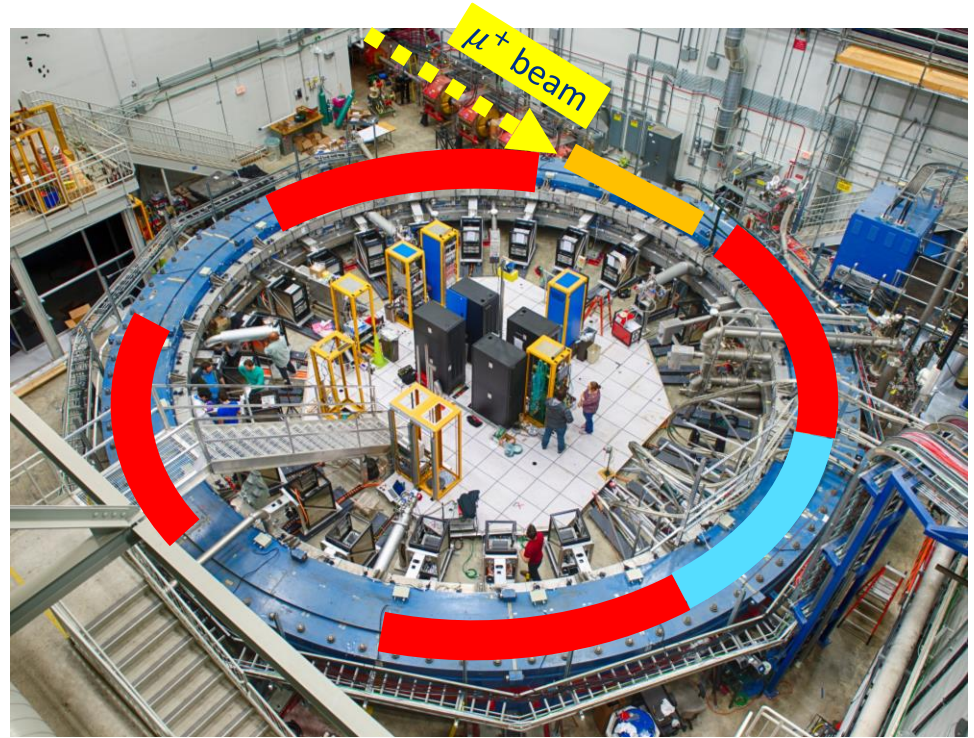
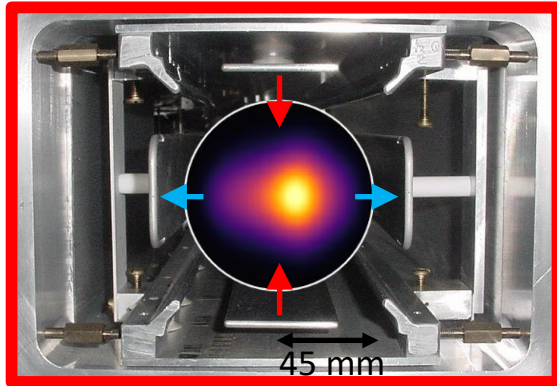
- **Inflector magnet** cancels field along injection path
- Pulsed **kicker magnets** shift beam to nominal orbit





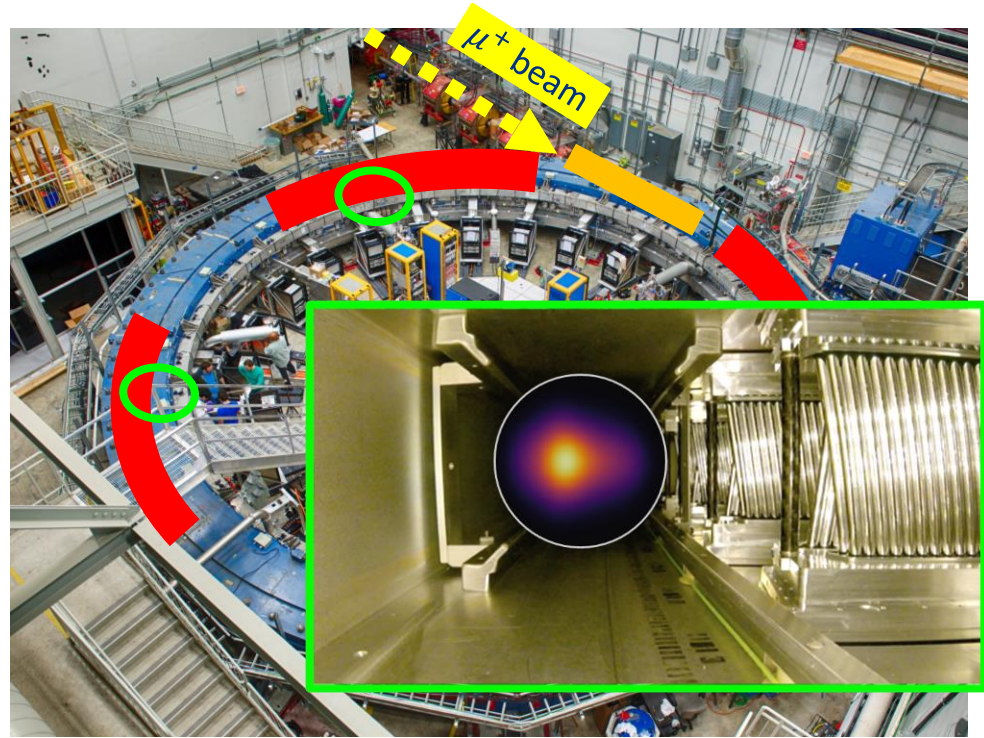
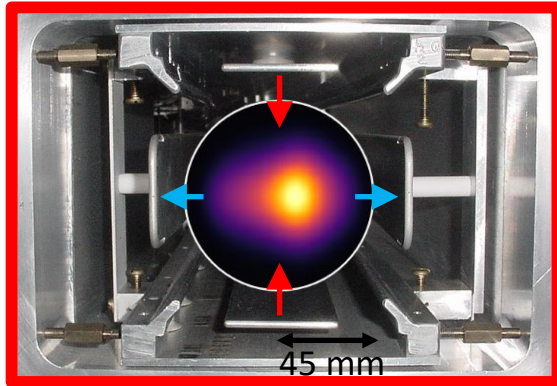
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- **Inflector magnet** cancels field along injection path
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- **Electric quadrupoles** contain beam vertically



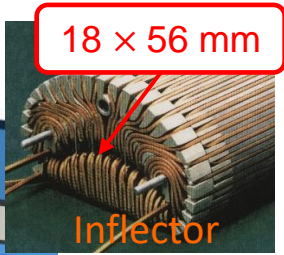
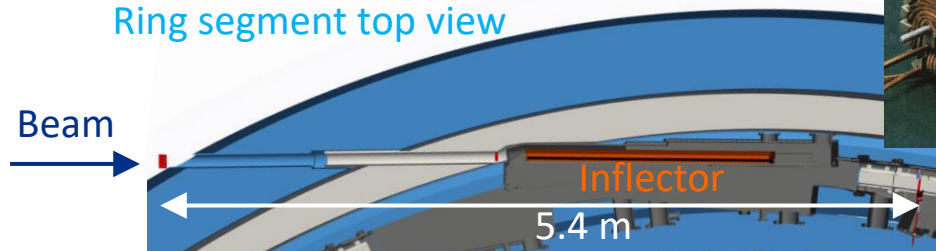
# Injecting and storing muons in the ring

- **Inflector magnet** cancels field along injection path
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- **Straw trackers** reconstruct muon distribution



# Characterizing beam during challenging injection

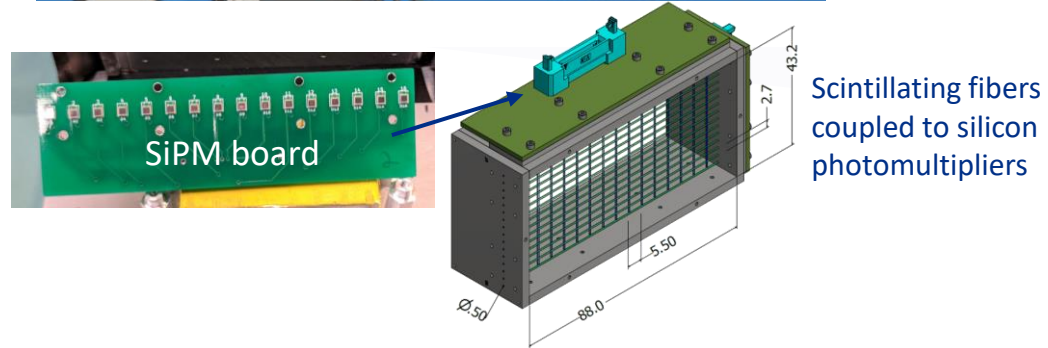
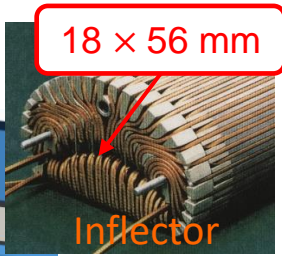
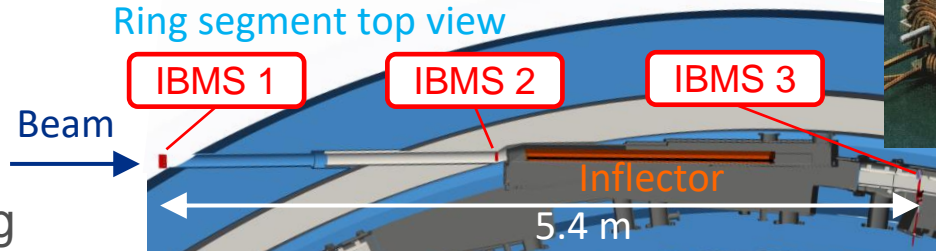
- Challenges: fringe fields, no steering elements





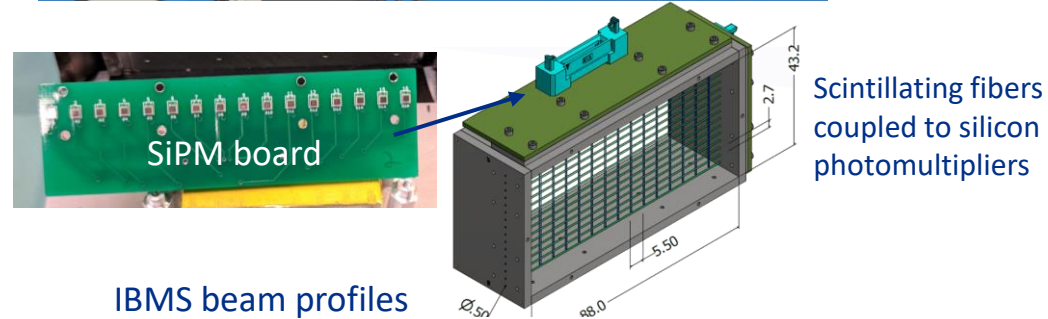
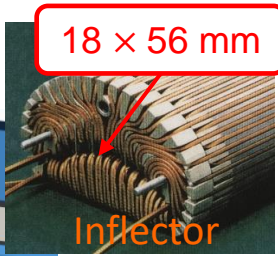
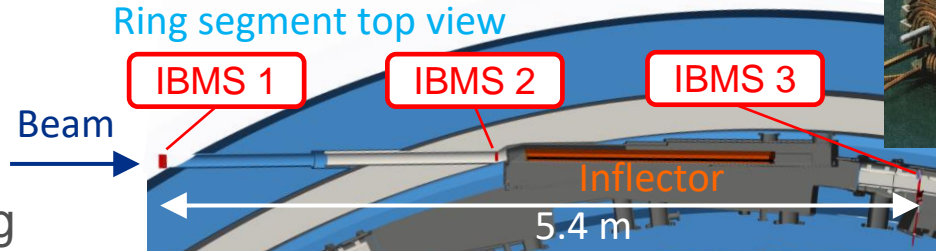
# Characterizing beam during challenging injection

- Challenges: fringe fields, no steering elements
- Built Inflector Beam Monitoring System (IBMS) detectors to monitor injected beam

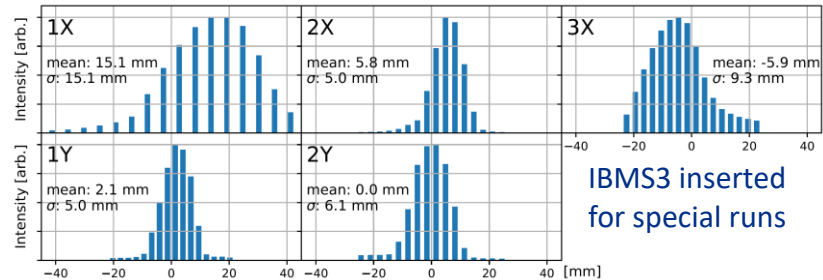


# Characterizing beam during challenging injection

- Challenges: fringe fields, no steering elements
- Built Inflector Beam Monitoring System (IBMS) detectors to monitor injected beam
- IBMS assisted with beam tuning and injection modeling
- Collaboration with AD members
- Critical for muon storage efficiency, systematics



IBMS beam profiles



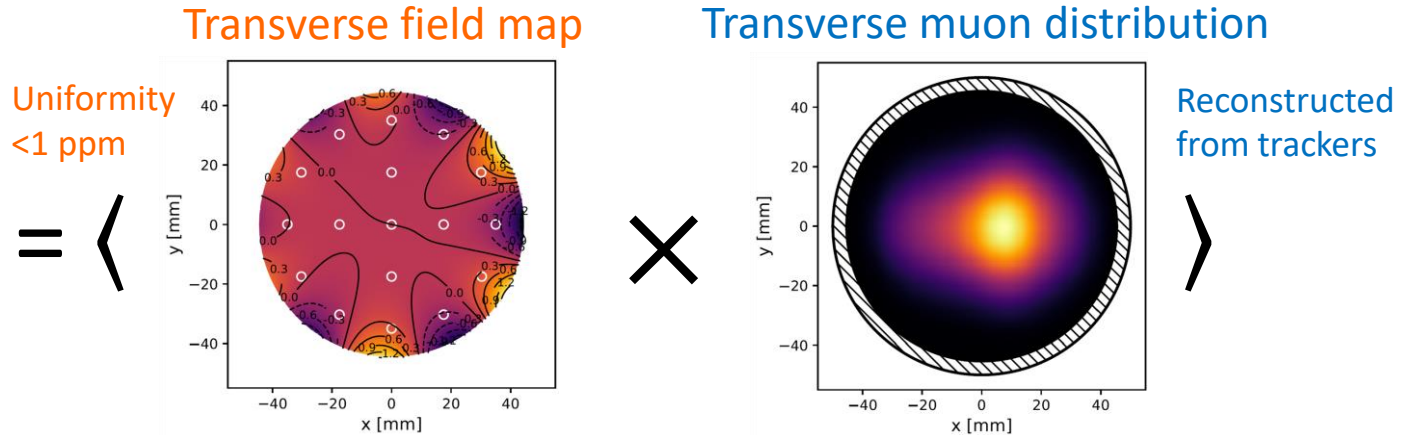


# Average magnetic field experienced by muons

- Inputs: **Field maps** and **beam profiles** around the ring
- Weight field in azimuth slices, then average around ring

$$\omega_a = -a_\mu \frac{e}{m} \tilde{B}$$

$$\tilde{B} = \langle B(\vec{r}) \times M(\vec{r}) \rangle$$



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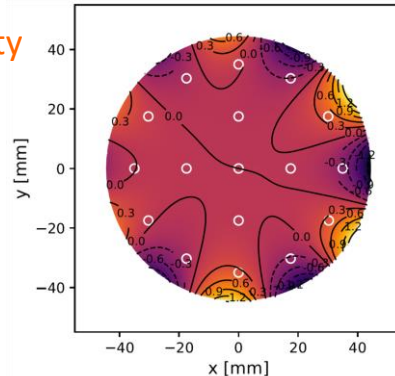
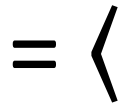
Field



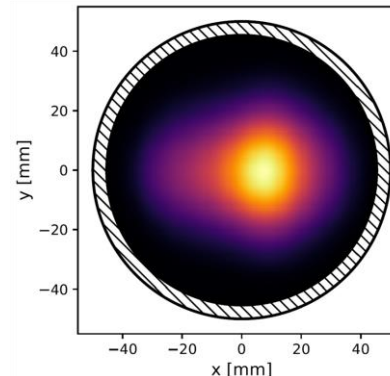
Beam dynamics

Transverse field map

Uniformity  
<1 ppm



Transverse muon distribution



Reconstructed  
from trackers



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- Weight field in azimuth slices, then average around ring

$$\tilde{B} = \langle B(\vec{r}) \times M(\vec{r}) \rangle$$

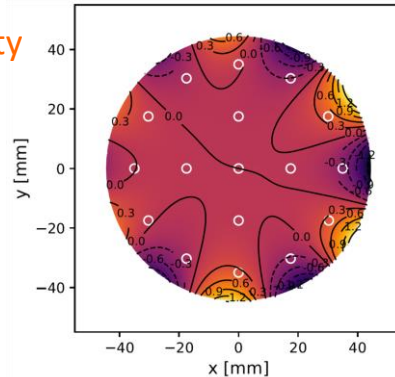
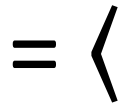
Field



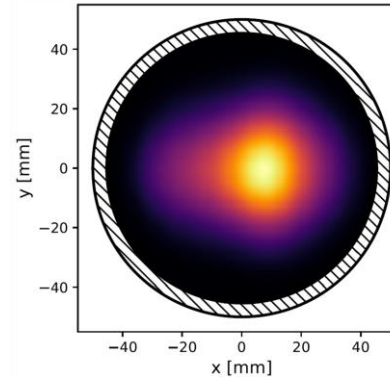
Beam dynamics

Transverse field map

Uniformity  
<1 ppm



Transverse muon distribution



Reconstructed  
from trackers



- Led analysis for 2021 and 2023 results
- Proper muon distribution weighting prevents a bias of up to **~50 ppb** with excellent uncertainty **~10 ppb**

# Correcting for electric field

- Original: Ideal motion in vertical B field

$$\vec{\omega}_a = -a_\mu \frac{e}{m} \vec{B}$$

# Correcting for electric field

- Original: Ideal motion in vertical B field

$$\vec{\omega}_a = -a_\mu \frac{e}{m} \vec{B}$$

- Electric quadrupole field  
→ motional B field

$$-\frac{e}{m} \left[ - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$$

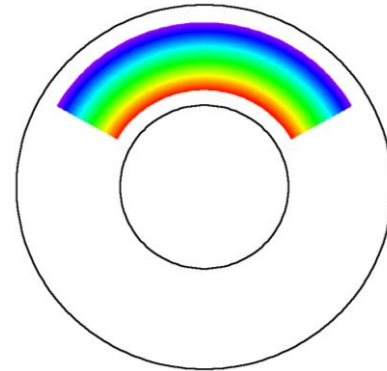
- Cancel with nominal momentum 3.094 GeV
- Nonzero due to momentum spread (~0.1%) → correction to  $\omega_a$

# Correcting for electric field

- Original: Ideal motion in vertical B field
- Electric quadrupole field → motional B field

$$\vec{\omega}_a = -a_\mu \frac{e}{m} \vec{B} - \frac{e}{m} \left[ - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$$

Higher momentum muons orbit at larger radius → lower cyclotron frequency

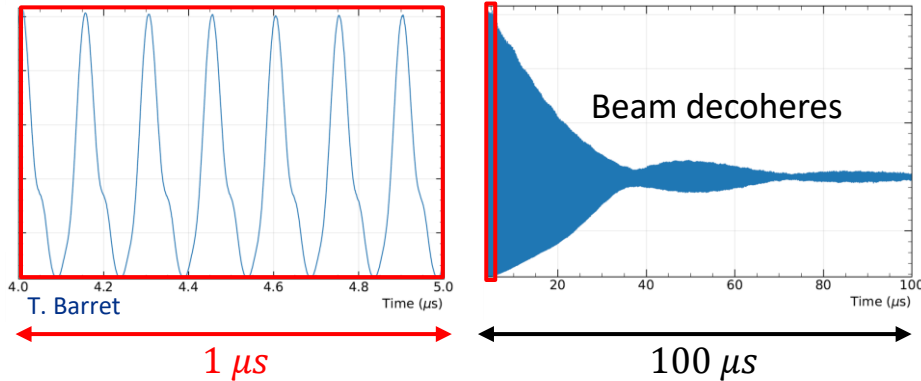


# Correcting for electric field

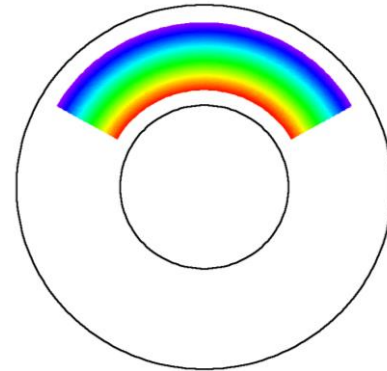
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Circulating beam intensity seen by calos



Higher momentum muons orbit at larger radius → lower cyclotron frequency



# Correcting for electric field

- Original: Ideal motion in vertical B field
- Electric quadrupole field → motional B field

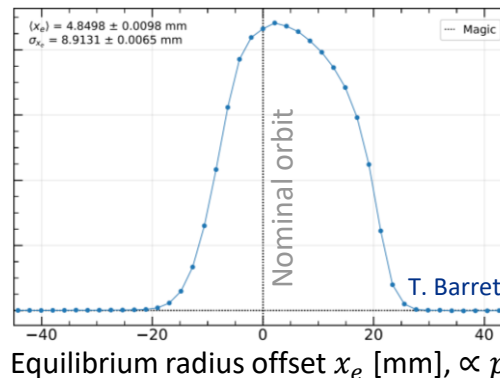
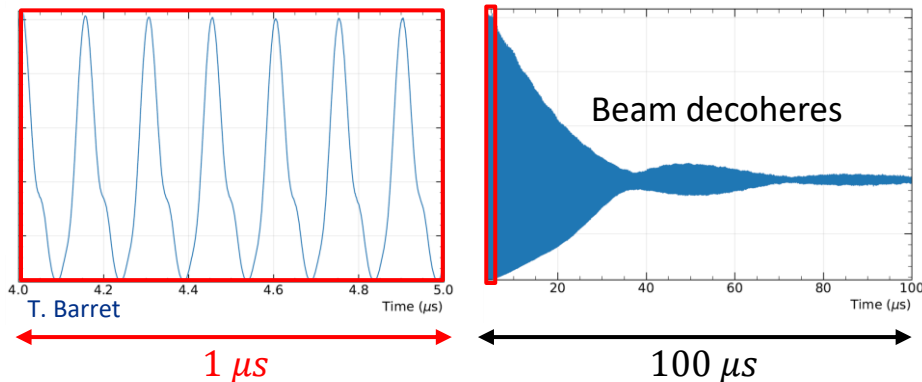
$$\vec{\omega}_a = -a_\mu \frac{e}{m} \vec{B}$$

$$-\frac{e}{m} \left[ - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$$

Circulating beam intensity seen by calos



Reconstruct momentum from frequency analysis





# Correcting for electric field

- Original: Ideal motion in vertical B field
- Electric quadrupole field → motional B field

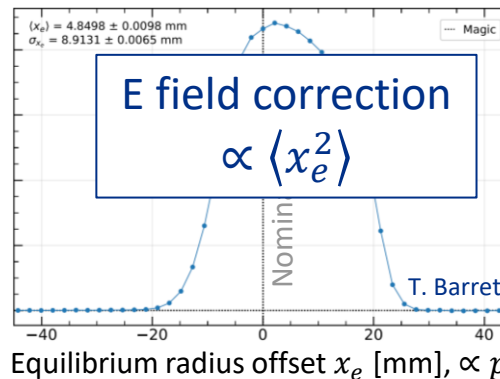
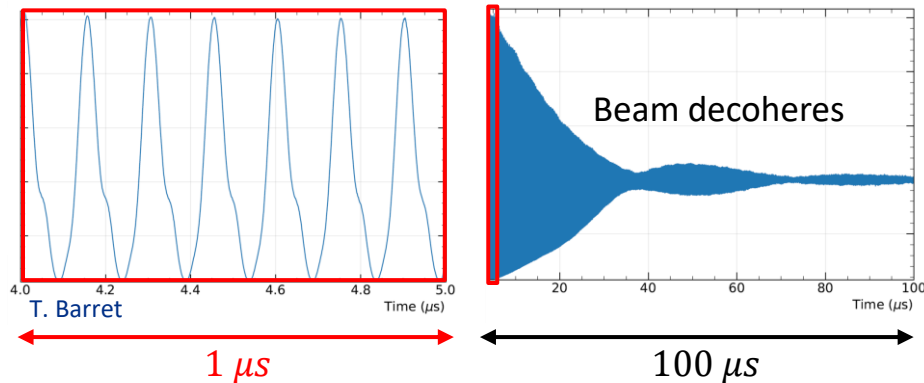
$$\vec{\omega}_a = -a_\mu \frac{e}{m} \vec{B}$$

$$-\frac{e}{m} \left[ - \left( a_\mu - \frac{1}{\gamma^2 - 1} \right) \vec{\beta} \times \vec{E} \right]$$

Circulating beam intensity seen by calos

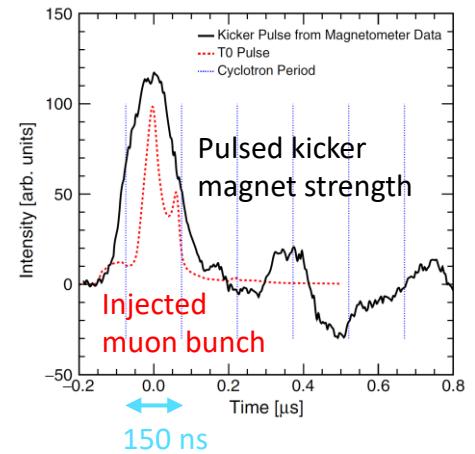


Reconstruct momentum from frequency analysis



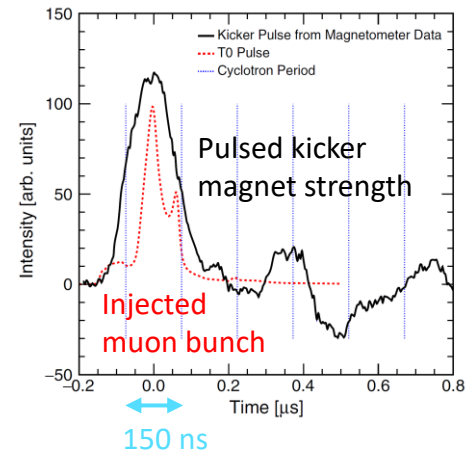
# Lingering uncertainty on E field correction

- Injection kicker strength varies over muon injection time → stored momentum is time-dependent; distorts reconstruction

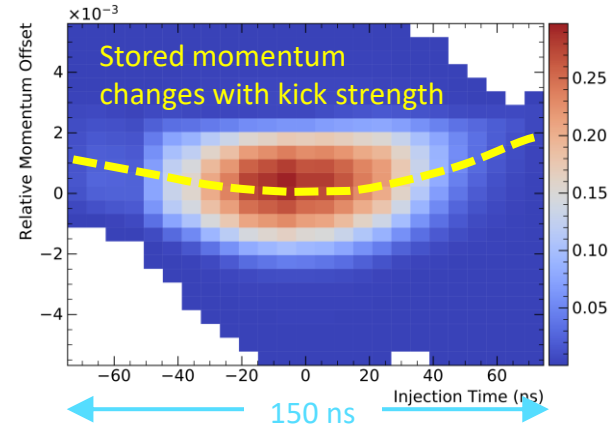


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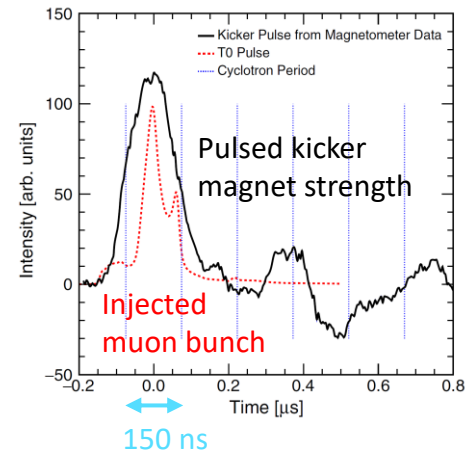


## Injection time vs. momentum correlation

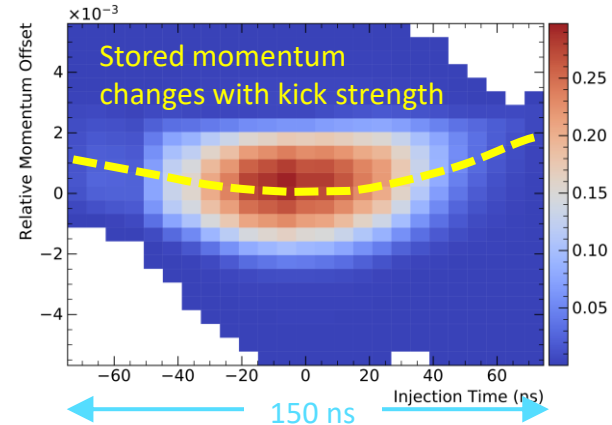


# Lingering uncertainty on E field correction

- Injection kicker strength varies over muon injection time → stored momentum is time-dependent; distorts reconstruction
- Still a significant uncertainty in 2023 result (32 ppb out of 70 ppb total systematic)

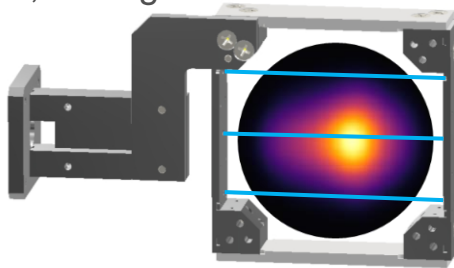


## Injection time vs. momentum correlation



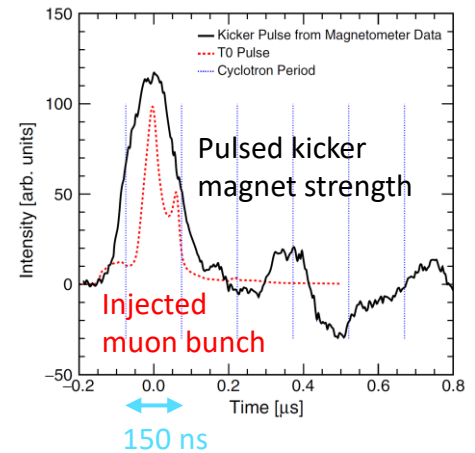
# Lingering uncertainty on E field correction

- Injection kicker strength varies over muon injection time → stored momentum is time-dependent; distorts reconstruction
- Still a significant uncertainty in 2023 result (32 ppb out of 70 ppb total systematic)
- Special measurements with new detector in final run to map the correlation
  - Ongoing analysis is helping deepen our understanding of subtle effects, aiming to reduce the uncertainty

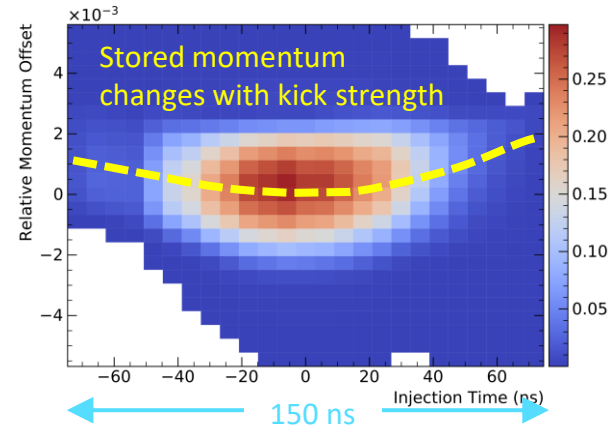


Scintillating fibers coupled to SiPMs

- Directly sample circulating beam → measure momentum
- Collaborated in development led by C. Claessens



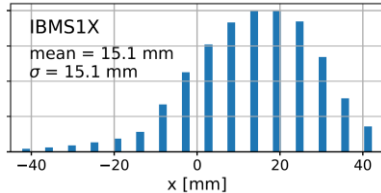
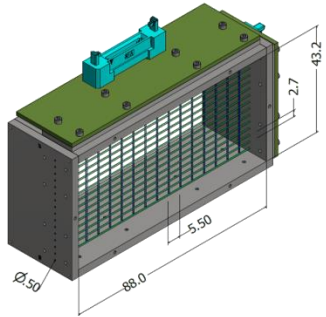
## Injection time vs. momentum correlation



# Conclusions

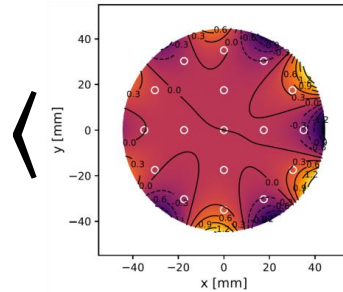
- Characterizing effects from beam dynamics is critical for reaching Muon g-2 precision target of 140 ppb
- My thesis focused on key beam dynamics challenges necessary to achieve this result

Detectors to assist with beam injection

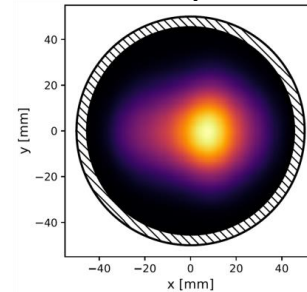


Muon-weighted magnetic field

Field map

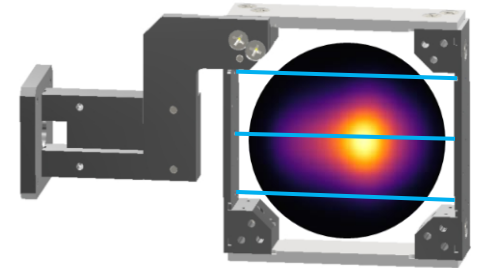


Beam profile



×

Direct measurement of beam momentum to reduce uncertainty





# Thanks to Muon g-2 members and the URA!



Muon g-2 Collaboration meeting at University of Liverpool, July 2023