Supermassive Black Holes of a Primordial Origin



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Based on [2308.00756]

Overview

- Motivations
- PBH Formation
- Spectral Distortions
- Departures from Gaussianity
- Non-Minimal Self-Interacting Curvaton
- Conclusions

Supermassive black holes (SMBHs)

- Massive: $M_{\rm SMBH} \ge 10^5 M_{\odot}$
- Ubiquitous:
 - Reside at the center of nearly all massive galaxies
 - Power quasars and other active galactic nuclei
- Poorly understood:
 - Origin and evolution remain active areas of research
 - New observations from JWST challenge the traditional paradigm of SMBH growth

early times, far away

• A surprising number of quasars have been observed in the high-z universe

Quasar/Galaxy	Redshift	Mass	Ref
GN-z11	10.6034 ± 0.0013	$1.6^{+1.6}_{-0.8}\times 10^6 M_{\odot}$	[2305.12492]
UHZ1	<i>≃</i> 10.1	$\simeq 4 \times 10^7 M_{\odot}$	[2308.03837]
J0313-1806	7.6423 ± 0.0013	$(1.6\pm0.4)\times10^9 M_{\odot}$	[2101.03179]
J1342+0928	7.5413 ± 0.0007	$7.8^{+3.3}_{-1.9} \times 10^8 M_{\odot}$	[1712.01860]

- Plus ~300 more at z > 6, including 9 at z > 7 [2212.06907]
- Only a small fraction of SMBHs are observable as quasars
 ⇒ actual number likely much larger!

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 - $M_{\rm BH} \sim 10^2 {\rm M}_{\odot} \rightarrow 10^{10} {\rm M}_{\odot} \Rightarrow \Delta t \sim 0.8 {\rm ~Gyr}$
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 - z = 6 7 corresponds to $\sim 0.7 0.9$ Gyr after the Big Bang
- SMBHs must have grown **continuously** at high rates throughout the first Gyr
 - Contrasts with **intermittent** accretion observed of SMBHs at lower *z*

Possible explanations:

- Super-Eddington accretion?
 - Pop III SMBH seeds are born in low density environments
 ⇒ prevents rapid initial growth
 - Super-Eddington periods are transient
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- Enhanced role of mergers?
 - Requires heavily clustered populations in the early universe
 - Can eject SMBHs out of material-rich galactic centers

- Also surprising: Growth rate has slowed dramatically since ~1 Gyr
- For the most massive SMBHs, the comoving mass density has remained approximately **constant** since $z \sim 5$



Estimates of quasar comoving mass density as a function of redshift; data from DR7 SDSS

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- For the most massive SMBHs, the comoving mass density has remained approximately **constant** since $z \sim 5$
- Possible explanations:
 - Galactic scale feedback effects?
 - Maximum mass after which accretion disks fragments?



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2) Why did their growth rate dramatically slow in the subsequent ~ 13 Gyr?



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Possibility: Primordial origin?

Many exciting implications of a primordial origin in light of recent observations!

- JWST high-redshift galaxy candidates
 - SMBHs could accelerate early galaxy formation
- Gravitational waves
 - Stochastic GW background in the nHz regime recently reported by NANOGrav and other PTAs
 - Leading astrophysical interpretation: SMBH binary mergers
 - Some aspects of fit are poor; better fit for primordial SMBHs?



- Previous works: **Primordial SMBH seeds**
 - Form much earlier than $z \sim 30 \Rightarrow$ timing problem allayed [1202.3848]
 - Light seeds $M_{\rm BH} \ge 10^2 M_{\odot}$ sufficient to seed present day SMBHs [1712.01311]
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- This work: SMBHs directly from inflation
 - Massive seeds $M_{\rm BH} \ge 10^5 M_{\odot}$
- Future data will help us to determine the nature of SMBH seeds
 - With JWST, can now observe smaller SMBHs in dimmer galaxies farther away
 - Opportunity to study how these early BHs and their host galaxies evolved together

- **Primordial black holes** (PBHs): \Rightarrow Form in the early universe from the collapse of large density perturbations $\delta \equiv \delta \rho / \bar{\rho}$ exceeding the collapse threshold $\delta > \delta_{th}$
- One source of overdensities:
 ⇒ Quantum fluctuations stretched to superhorizon scales during inflation
- PBH formation is a causal process; compare
 - Comoving length scale of perturbation mode, $\lambda = k^{-1}$
 - Comoving Hubble horizon, $R_H = (aH)^{-1}$

- $R_H = (aH)^{-1} \sim a^{(1+3w)/2}$
 - Inflation (w = -1): $R_H \sim a^{-1}$
 - Rad dom (w = 1/3): $R_H \sim a$
- Mode can be
 - Subhorizon: k > aH
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 - Superhorizon: k < aH
- Small scale modes (large k) exit later and re-enter earlier



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If $\delta > \delta_{th}$, entire horizon collapses upon re-entry \Rightarrow PBHs!





• Initial mass of PBH \simeq mass of cosmological horizon

$$M_{\rm PBH} = \left(5 \times 10^8 \, M_{\odot}\right) \left(\frac{\gamma}{0.2}\right) \left(\frac{92 \, \rm Mpc^{-1}}{k_{\rm PBH}}\right)^2 \left(\frac{g_{\star}(T)}{3.36}\right)^{1/2} \left(\frac{3.91}{g_{\star,s}(T)}\right)^{2/3}$$

- Initial abundance \Rightarrow mass fraction at formation, $\beta = \rho_{PBH} / \rho_{tot}$
- In the Press Schechter formalism:

$$\beta \simeq 2 \int_{\delta_{\rm th}}^{\infty} d\delta \, P[\delta]$$

• Usual assumption: Gaussian probability distribution function (pdf)

$$P_G[\delta] = \frac{1}{\sqrt{2\pi}\sigma_\delta} \exp\left(-\frac{\delta^2}{2\sigma_\delta^2}\right)$$

• Variance computed from **primordial power spectrum** $\mathcal{P}_{\delta}(k)$

$$\sigma_{\delta}^{2} = \int_{0}^{\infty} \frac{dk}{k} W^{2}(k,R) \mathcal{P}_{\delta}(k)$$

- Value for collapse threshold $\delta_{\rm th}$?
- Intuition: Perturbation will collapse if overdensity exceeds radiation pressure

$$\Rightarrow \delta_{\rm th} \simeq c_s^2 = 1/3$$

- Numerical simulations: $\delta_{th} \simeq 0.4 0.66$ [1309.4201]
- Precise value depends on overdensity profile
- PBH abundance is **extremely sensitive** to δ_{th}
- We take: $\delta_{\rm th} = 0.414$

$$\longleftarrow \beta \simeq \sqrt{\frac{2}{\pi}} \frac{\sigma_{\delta}}{\delta_{\rm th}} \exp\left(-\frac{\delta_{\rm th}^2}{2\sigma_{\delta}^2}\right)$$

- A non-vanishing abundance requires a large variance $\sigma_{\delta}^2 \sim \mathcal{P}_{\delta}(k)|_{\max}$ \Rightarrow need **significant enhancement** of power spectrum
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- For Gaussian pdf, need peak $\mathcal{P}_{\delta}(k)|_{\max} \sim \mathcal{O}(10^{-2})$
- Relatively **easy** to engineer amplified power
 - Single field: Inflection point, ultra-slow-roll plateau, localized features, etc.
 - Multifield: Scalar sector instabilities, non-canonical kinetic terms, non-minimal coupling to R, etc.
- More generically, any deviation from slow-roll \Rightarrow amplified $\mathcal{P}_{\delta}(k)$

- Shape of the inflaton potential determines
 - Shape of primordial power spectrum
 - Distribution of PBH masses and abundances





- Issue: SMBH form late!
 - $T \sim \text{MeV} \Rightarrow M_{\text{H}} \sim 1.7 \times 10^5 \text{M}_{\odot}$
 - $T \sim \text{keV} \Rightarrow M_{\text{H}} \sim 3 \times 10^{11} \text{M}_{\odot}$

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- Corresponding modes: 10 ${\rm Mpc^{-1}} \lesssim k_{\rm SMBH} \lesssim 10^4 \ {\rm Mpc^{-1}}$
 - Unconstrained by CMB anisotropy measurements
 - However, probed by CMB spectral distortions
- Enhanced power on these scales inevitably leads to spectral distortions of the CMB

- Spectral distortions = isotropic deviations from the CMB blackbody distribution
- μ-type distortions
 - $2 \times 10^5 < z < 2 \times 10^6$
 - Photon number changing processes become ineffective
 - Departure from chemical equilibrium \Rightarrow Bose-Einstein distribution with effective chemical potential μ
- y-type distortions
 - $z < 2 \times 10^5$
 - Compton scattering becomes ineffective
 - Complete departure from equilibrium distribution

- Quantify in terms of parameters μ , $y \sim \Delta \rho_{\gamma} / \bar{\rho}_{\gamma}$
- Constraints from COBE/FIRAS:

 $|\mu| \leq 9.0 \times 10^{-5}$, $|y| \leq 1.5 \times 10^{-5}$

• For sharply peaked $\mathcal{P}_{\zeta}(k)$

$$\mu \simeq 2.2 \ \sigma_{\zeta}^2 \left(\exp\left[-\left(\frac{1.5 \times 10^5 M_{\odot}}{M_{PBH}}\right)^{1/2} \right] - \exp\left[-\left(\frac{4.5 \times 10^9 M_{\odot}}{M_{PBH}}\right) \right] \right)$$
$$y \simeq 0.4 \ \sigma_{\zeta}^2 \exp\left[-\left(\frac{4.5 \times 10^9 M_{\odot}}{M_{PBH}}\right) \right]$$



Lognormal peaked power spectra with amplitude required for $\beta \simeq 10^{-20}$ overlaid against various constraints

- Fundamental tension
 - Compatibility with spectral distortions \Rightarrow Small $\sigma_{\zeta}^2 \sim \mathcal{P}_{\zeta}(k)|_{\max}$
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⇒ Want distribution with **heavy**, **non-Gaussian tail**

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- Recall: We compute PBH abundance by integrating over the tail of the distribution, δ > δ_{th}
 ⇒ Want distribution with heavy, non-Gaussian tail
- Incidentally, the Gaussian assumption is **generically false**

• To quantify required degree of non-Gaussianity, introduce

$$P_{\delta}^{(n)} = \frac{1}{2\sqrt{2}\Gamma(1+1/n)\sigma_0} \exp\left[-\left(\frac{|\delta|}{\sqrt{2}\sigma_0}\right)^n\right]$$

• Variance

$$\sigma_{\delta}^2(\sigma_0) = \int d\delta \,\delta^2 P_{\delta}^{(n)} = \frac{\Gamma(1+3/n)}{3\,\Gamma(1+1/n)}\,\sigma_0^2$$

- Cases
 - $n = 2 \Rightarrow$ Gaussian
 - $n = 1 \Rightarrow$ Exponential
 - $n < 1 \Rightarrow$ **Heavy**





saturating CMB spectral distortion constraints

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 - \Rightarrow Ultra-slow-roll regime \Rightarrow quantum diffusion
 - \Rightarrow Small scale features (bumps, dips)

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• Possibility: Non-minimal self-interacting curvaton model?

- Curvaton χ
 - Light $(m_{\chi}^2 \ll H)$ spectator field
 - Subdominant during inflation
 - Responsible for generating the dominant contribution ζ_{γ} to the curvature perturbation
- Curvature perturbation ζ_{χ}
 - Initially an **isocurvature** mode
 - Converted to **adiabatic** upon curvaton decay
- Non-Gaussianity arises due to inefficient conversion of isocurvature to adiabatic perturbations

- Curvaton cosmology
 - During inflation
 - Background value "frozen-in" at χ_*
 - Receives (Gaussian) perturbations $\delta \chi_* \simeq H_*/2\pi$
 - After inflation
 - Starts to oscillate about minimum when $H \simeq m_{\chi}$
 - Decays when $H \sim \Gamma_{\chi}$
- Non-linear mapping between ζ and $\zeta_{\chi} \Rightarrow$ non-Gaussian pdf
- Goal: Want to compute pdf for ζ

- *δN* formalism [astro-ph/0411220], [astro-ph/0504045]
 - Compute non-linear evolution of cosmological perturbations on super-horizon scales
 - Curvature perturbation = difference between perturbed vs unperturbed amount of expansion: $\zeta = N(\bar{\chi} + \delta \chi) N(\bar{\chi})$
- Curvaton curvature perturbation ζ_{χ} and total ζ related as [astro-ph/0607627]

$$e^{4\zeta} - \frac{4r}{3+r} \left(e^{3\zeta_{\chi}} \right) e^{\zeta} + \frac{3r-3}{3+r} = 0$$

• Solve for $\zeta = \ln X(\zeta_{\chi})$

$$r = \frac{3\Omega_{\chi}}{4 - \Omega_{\chi}} \Big|_{\text{decay}}$$

• Curvaton curvature perturbation ζ_{χ} related to field perturbation $\delta\chi$ as

$$e^{3\zeta_{\chi}} = \left(1 + \frac{\delta\chi}{\bar{\chi}}\right)^2$$

- Quadratic potential $\Rightarrow \delta \chi$ and $\bar{\chi}$ obey **same** e.o.m. on superhorizon scales $\Rightarrow \delta \chi / \bar{\chi} = \delta \chi_* / \bar{\chi}_* \equiv \delta_{\chi}$
- Result: Mapping between ζ and the **Gaussian reference variable** δ_{χ}
- Can now obtain pdf of ζ using conservation of probability

• By conservation of probability

$$P_{\zeta}[\zeta] = P_G[\delta_{\chi}^{+}(\zeta)] \left| \frac{d\delta_{\chi}^{+}}{d\zeta} \right| + P_G[\delta_{\chi}^{-}(\zeta)] \left| \frac{d\delta_{\chi}^{-}}{d\zeta} \right|$$

with

$$\delta_{\chi}^{\pm} = -1 \pm \sqrt{\frac{3+r}{4r}e^{3\zeta} + \frac{3r-3}{4r}e^{-\zeta}}$$

and

$$P_G[\delta_{\chi}] = \frac{1}{\sqrt{2\pi}\sigma_0} \exp\left(-\frac{\delta_{\chi}^2}{2\sigma_0^2}\right)$$



Probability distribution function for the curvature perturbation as a function of r

- Curvaton model yields ζ with non-Gaussian statistics
- Still need local amplification of $\mathcal{P}_{\zeta}(k)$
- Simple option: Non-minimal kinetic term [2112.12680]

$$\mathcal{L} = \frac{1}{2} (\partial \phi)^2 - V(\phi) + \frac{1}{2} f(\phi)^2 (\partial \chi)^2 - \frac{1}{2} m_{\chi}^2 \chi^2$$

• Choose $f(\phi)$ s.t. kinetic term is suppressed on scale $k_{\text{PBH}} \Rightarrow \text{peak}!$

$$\mathcal{P}_{\delta_{\chi}}(k) = \frac{k^3}{2\pi^2} \left| \frac{\delta \chi_k}{\chi} \right|^2 = \frac{1}{\chi(t_k)^2} \left(\frac{H(t_k)}{2\pi f(\phi_k)} \right)^2$$

• PBH mass fraction at formation

$$\beta = 2 \int_{\delta_{\chi,\text{th}}^{+}}^{\infty} d\delta_{\chi} P_{G}[\delta_{\chi}] + 2 \int_{-\infty}^{\delta_{\chi,\text{th}}^{-}} d\delta_{\chi} P_{G}[\delta_{\chi}]$$
$$= \operatorname{erfc}\left(\frac{\delta_{\chi,\text{th}}^{+}}{\sqrt{2}\sigma_{0}}\right) + \operatorname{erfc}\left(\frac{|\delta_{\chi,\text{th}}^{-}|}{\sqrt{2}\sigma_{0}}\right)$$

• Variance

$$\sigma_{\zeta}^{2} = \int d\delta_{\chi} \,\zeta^{2} \,P_{G}[\delta_{\chi}] - \left(\int d\delta_{\chi} \,\zeta \,P_{G}[\delta_{\chi}]\right)^{2}$$



Maximum PBH abundance β for variance σ_{δ}^2 saturating CMB spectral distortion constraints

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- One option: Curvaton self-interactions
- Quadratic potential
 - $\bar{\chi} \sim \delta \chi \Rightarrow \delta \chi / \bar{\chi} = \delta \chi_* / \bar{\chi}_* \equiv \delta_{\chi}$
 - No non-linear evolution for δ_{χ} between horizon exit and onset of oscillations
 - Exact relation $e^{3\zeta_{\chi}} = (1 + \delta_{\chi})^2$
- With self-interactions, mapping between ζ_{χ} and initial Gaussian perturbations $\delta \chi_*$ can be made even **more dramatically** non-linear!

- Curvaton cosmology
 - $t_* \leq t \leq t_{\text{int}} \qquad \Rightarrow \quad \bar{\chi} \simeq \bar{\chi}_*$
 - $t_{int} \leq t \leq t_{osc} \Rightarrow$ non-quadratic interaction regime
 - $t_{\rm osc} \leq t \leq t_{\rm dec} \Rightarrow$ quadratic field oscillations
- Gaussian reference variable $\delta \chi_*$
- Same mapping between ζ and ζ_{χ} : $\zeta = \ln X(\zeta_{\chi})$
- Need mapping between ζ_{χ} and $\delta \chi_*$: $\delta \chi_*^j = g_j(\zeta_{\chi})$
- By conservation of probability: $P_{\zeta} = \sum_{j} \left| \frac{g_{j}(\zeta)}{d\zeta} \right| P_{G}[g_{j}(\zeta)]$



Maximum PBH abundance β for variance σ_{δ}^2 saturating CMB spectral distortion constraints

Conclusions

- Inferred SMBH population in the high-redshift universe is surprising
- Possibility: Primordial origin?
- Issue: Required amplification of \mathcal{P}_{ζ} naively violates CMB spectral distortions
- Resolution: ζ with non-Gaussian, heavy-tailed probability distribution
- Physical realization: Non-minimal self-interacting curvaton model?
- Future directions:
 - Curvaton numerics, model building
 - Gravitational wave signal