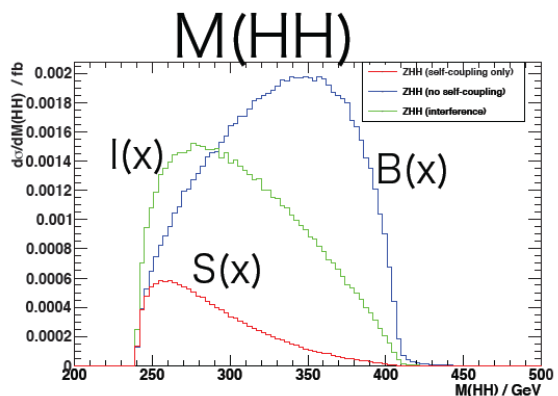


# Example of recent improvement in ILC Higgs self coupling analysis

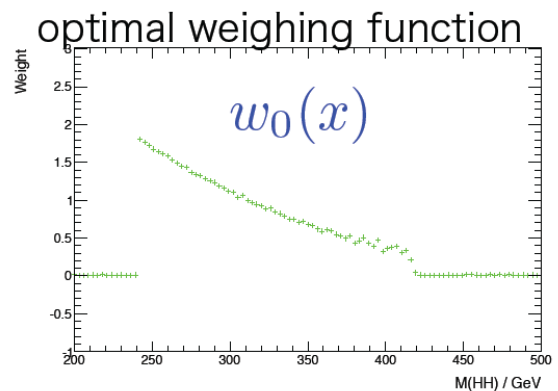
## Weighting Method to Enhance the Sensitivity to $\lambda$



$$\frac{d\sigma}{dx} = \underbrace{B(x)}_{\text{irreducible}} + \underbrace{\lambda I(x)}_{\text{interference}} + \underbrace{\lambda^2 S(x)}_{\text{self-coupling}}$$

**Observable:** weighted cross-section

$$\sigma_w = \int \frac{d\sigma}{dx} w(x) dx$$



**Equation for the optimal  $w(x)$**  (variational principle):

$$\sigma(x)w_0(x) \int (I(x) + 2S(x))w_0(x)dx = (I(x) + 2S(x)) \int \sigma(x)w_0^2(x)dx$$

**General solution:**

$$w_0(x) = c \cdot \frac{I(x) + 2S(x)}{\sigma(x)}$$

**c:** arbitrary normalization factor

$$e^+e^- \rightarrow ZHH \quad @ \sqrt{s} = 500 \text{ GeV} \quad \frac{\delta\lambda}{\lambda} = 1.8 \frac{\delta\sigma}{\sigma} \Rightarrow 1.66 \frac{\delta\sigma}{\sigma}$$

$$e^+e^- \rightarrow \nu\bar{\nu}HH \quad @ \sqrt{s} = 1000 \text{ GeV} \quad \frac{\delta\lambda}{\lambda} = 0.85 \frac{\delta\sigma}{\sigma} \Rightarrow 0.76 \frac{\delta\sigma}{\sigma}$$

# ILC Higgs Self Coupling Summary

Scenario A:  $HH \rightarrow bbbb$ , full simulation done

Scenario B: add  $HH \rightarrow bbWW^*$ , full simulation ongoing

Scenario C: additional Higgs decay modes; color-singlet clustering

$$\frac{\delta\lambda}{\lambda}$$

HHH	500 GeV			500 GeV + 1 TeV		
	Scenario	A	B	C	A	B
Canonical	104%	83%	66%	26%	21%	17%
LumiUP	58%	46%	37%	16%	13%	10%