Baryon Number Violation

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Baryon Number postulated as a symmetry of Nature to stabilize matter
  Weyl (1929), Stueckelberg (1939), Wigner (1949)

Unlike electric charge, which guarantees stability of electron, $B$ is not a “fundamental” symmetry

Weak interactions violate $B$ non-perturbatively
  ‘t Hooft (1977)

Quantum gravity suspected to violate all global symmetries such as $B$

Baryon number violation essential for creation of matter asymmetry of the Universe
  Sakharov (1967)

Most extensions of Standard Model, notably Grand Unified Theories lead to baryon number violation
Gauge coupling unification

From S. Raby, PDG Review
SO(10) Grand Unification

Unifies all members of a family into a single 16-plet

<table>
<thead>
<tr>
<th>$u_R$: ${---+++}$</th>
<th>$d_R$: ${---+++}$</th>
<th>$u^C_R$: ${++--++}$</th>
<th>$d^C_R$: ${+-+-+-}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$u_B$: ${+---++}$</td>
<td>$d_B$: ${+---++}$</td>
<td>$u^C_B$: ${+-+++-}$</td>
<td>$d^C_B$: ${+-+-+-}$</td>
</tr>
<tr>
<td>$v$: ${----++}$</td>
<td>$e$: ${----++}$</td>
<td>$v^C$: ${++++++}$</td>
<td>$e^C$: ${++++++}$</td>
</tr>
</tbody>
</table>

Predicts right-handed neutrino and thus neutrino masses

Frist 3 spins refer to color, last 2 are weak spins

$$Y = \frac{1}{3} \Sigma(C') - \frac{1}{2} \Sigma(W)$$

Eg: $Y(e^C) = \frac{1}{3}(3) - \frac{1}{2}(-2) = 2$

Such an elegant arrangement very strongly suggestive of GUTs
Grand Unified Theories: Motivations

- Electric charge quantization
  - $Q_p = -Q_e$ to better than 1 part in $10^{21}$
- Miraculous cancellation of anomalies
- Quantum numbers of quarks and leptons
- Existence of $\nu_R$ and thus neutrino mass via seesaw
- Unification of gauge couplings with low energy SUSY
- $b - \tau$ unification
- Baryon asymmetry of the universe via leptogenesis

Pati, Salam (1973)
Georgi, Glashow (1974)
Minimal SO(10) Model

\[ \mathcal{L}_{\text{Yukawa}} = Y_{10} 16 \ 16 \ 10_H + Y_{126} 16 \ 16 \ 1\overline{2}6_H \]

Two Yukawa matrices determine all fermion masses and mixings, including the neutrinos

\[
\begin{align*}
M_u &= \kappa_u Y_{10} + \kappa'_u Y_{126} \\
M_d &= \kappa_d Y_{10} + \kappa'_d Y_{126} \\
M_{\nu}^D &= \kappa_u Y_{10} - 3\kappa'_u Y_{126} \\
M_l &= \kappa_d Y_{10} - 3\kappa'_d Y_{126} \\
M_{\nu R} &= \langle \Delta_R \rangle Y_{126} \\
M_{\nu L} &= \langle \Delta_L \rangle Y_{126}
\end{align*}
\]

Model has only 11 real parameters plus 7 phases

Babu, Mohapatra (1993)  
Fukuyama, Okada (2002)  
Babu, Macesanu (2005)  
Bertolini, Malinsky, Schwetz (2006)  
Dutta, Mimura, Mohapatra (2007)  
Bajc, Dorsner, Nemevsek (2009)
Specific Example: Type I Seesaw

Input at the GUT scale:

\[
\begin{align*}
  m_u &= 0.0006745 & m_c &= 0.3308 & m_t &= 97.335 \\
  m_d &= 0.0009726 & m_s &= 0.02167 & m_b &= 1.1475 \\
  m_e &= 0.000344 & m_\mu &= 0.0726 & m_\tau &= 1.350 \text{ GeV} \\
  s_{12} &= 0.2248 & s_{23} &= 0.03278 & s_{13} &= 0.00216 \\
  \delta_{CKM} &= 1.193
\end{align*}
\]

Output for neutrinos:

\[
\begin{align*}
  \sin^2 \theta_{12} &\approx 0.27, & \sin^2 2\theta_{23} &\approx 0.90, & \sin^2 2\theta_{13} &\approx 0.08 \\
  m_i &= \{0.0021e^{0.11i}, 0.0098e^{-3.08i}, 0.048\} \text{ eV} \\
  \Delta m^2_{23}/\Delta m^2_{12} &\approx 24
\end{align*}
\]

K.S. Babu and C. Macesanu (2005)
Theta(13) in Minimal SO(10)

\[ \sin^2 2\theta_{13} \text{ and CP violating phase } \delta_N \]

K.S. Babu and C. Macesanu (2005)

\[ \sin^2 2\theta_{13} = 0.089 \pm 0.010 \pm 0.005 \]

Daya Bay (2012)
Unlike $SU(5)$, $SO(10)$ allows an intermediate symmetry

$$SO(10) \rightarrow SU(4)_c \times SU(2)_L \times SU(2)_R \times P$$

Pati-Salam symmetry

Unification of gauge couplings consistent with data

Intermediate scale may be identified as Peccei-Quinn scale to solve strong CP problem

Proton decays via exchange of $SO(10)$ gauge bosons

Lifetime within reach of currently envisioned experiments

Unification and Proton Decay in non-SUSY SO(10)

Mohapatra, Parida (1993)
Deshpande, Keith, Pal (1995)
Lee, Mohapatra, Parida, Rani (1995)
Bertolini, Luzio, Malinsky (2012)
Altarelli, Meloni (2013)
Babu, Khan (2013)

Rich literature:
Intermediate symmetry: $SO(10) \rightarrow SU(4)_c \times SU(2)_L \times SU(2)_R \times P$

Babu, Khan (2013)
Nucleon decay in non-SUSY SO(10)

$SO(10)$ breaks to an intermediate Pati–Salam symmetry $SU(2)_L \times SU(2)_R \times SU(4)_c \times P$

Proton decays to $e^+\pi^0$ via GUT scale $X, Y$ gauge boson exchange

\[
\Gamma^{-1}(p \to e^+\pi^0) \approx (8.2 \times 10^{34} \text{ yr}) \\
\times \left( \frac{\alpha_H}{0.0122 \text{ GeV}^3} \right)^{-2} \left( \frac{\alpha_G}{1/34.7} \right)^{-2} \left( \frac{A_R}{3.35} \right)^{-2} \left( \frac{M_X}{10^{16} \text{ GeV}} \right)^4
\]

Threshold corrections play important role
Threshold corrections: All Higgs fields assumed to be in the range \((1/20 - 2)\) of gauge boson mass

Proton lifetime cannot exceed \(5 \times 10^{35}\) yrs in this model

Babu, Khan (2013)
Nucleon decay in SUSY GUTs

Gauge boson exchange

\[ \Gamma^{-1}(p \rightarrow e^+ \pi^0) = (2.0 \times 10^{35} \text{ yr}) \]

\[ \times \left( \frac{\alpha_H}{0.01 \text{ GeV}^3} \right)^{-2} \left( \frac{\alpha_G}{1/25} \right)^{-2} \left( \frac{A_R}{2.5} \right)^{-2} \left( \frac{M_X}{10^{16} \text{ GeV}} \right)^4 \]

\[ (-2\alpha_3^{-1} - 3\alpha_2^{-1} + 3\alpha_Y^{-1})(M_Z) = \frac{1}{2\pi} \left\{ 36 \ln \left( \frac{M_X}{M_Z} \left( \frac{M_{\Sigma}}{M_X} \right)^{1/3} \right) + 8 \ln \left( \frac{M_{\text{SUSY}}}{M_Z} \right) \right\} \]

\( M_{\Sigma} \): Heavy color octet mass, uncertain: Threshold effect

Hisano, Murayama, Yanagida (1993)
\[
\Gamma_{d=5}^{-1}(p \to \bar{\nu}K^+) \simeq 1.2 \times 10^{31} \text{ yrs} \times \left( \frac{0.012 \text{ GeV}^3}{\beta_H} \right)^2 \left( \frac{7}{A_S^\alpha} \right)^2 \left( \frac{1.25}{R_L} \right)^2 \\
\times \left( \frac{M_T}{2 \times 10^{16} \text{ GeV}} \right)^2 \left( \frac{m_{\tilde{q}}}{1.5 \text{ TeV}} \right)^4 \left( \frac{190 \text{ GeV}}{M_{\tilde{W}}} \right)^2,
\]

Minimal SUSY $SU(5)$

Sakai, Yanagida (1982)
Weinberg (1982)

Murayama, Pierce (2002)
Proton Lifetime in a Realistic SUSY SU(5)

\[
\begin{array}{|c|c|}
\hline
\Gamma_{d=5}^{-1}(p \rightarrow \bar{\nu} K^+) & 4 \cdot 10^{33} \text{ yrs.} \\
\Gamma_{d=5}^{-1}(n \rightarrow \bar{\nu} K^0) & 2 \cdot 10^{33} \text{ yrs.} \\
\Gamma_{d=5}^{-1}(p \rightarrow \mu^+ K^0) & 1.0 \cdot 10^{34} \text{ yrs.} \\
\Gamma_{d=5}^{-1}(p \rightarrow \mu^+ \pi^0) & 1.8 \cdot 10^{34} \text{ yrs.} \\
\Gamma_{d=5}^{-1}(p \rightarrow \bar{\nu} \pi^+) & 7.3 \cdot 10^{33} \text{ yrs.} \\
\Gamma_{d=5}^{-1}(n \rightarrow \bar{\nu} \pi^0) & 1.5 \cdot 10^{34} \text{ yrs.} \\
\hline
\end{array}
\]

5 + \bar{5} fermions at GUT scale corrects wrong mass relations

\[ m_d^0 = m_e^0 \text{ and } m_s^0 = m_{\mu}^0 \]

SUSY spectrum \( \leq 3 \text{ TeV} \) assumed

Nucleon lifetime cannot exceed \( 2 \times 10^{34} \) yrs

Babu, Bajc, Tavartkiladze (2012)
- Continue Super-K exposure
- Improve analysis
- Search in new channels
- Next generation experiments
  - Detector R&D
  - Experiment proposals

### Near Future

### Next Future

<table>
<thead>
<tr>
<th>Technique</th>
<th>Examples</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water Cherenkov</td>
<td>22.5 kton Super-K</td>
<td>Best for $e^+\pi^0$</td>
</tr>
<tr>
<td></td>
<td>560 kton Hyper-Kamiokande</td>
<td>Good for all modes</td>
</tr>
<tr>
<td>Liquid Argon</td>
<td>34 kton LBNE LAr TPC</td>
<td>Best for $K^+\nu$</td>
</tr>
<tr>
<td></td>
<td>20 kton LBNO 2-phase TPC</td>
<td>Good for many other modes</td>
</tr>
<tr>
<td>Scintillator</td>
<td>50 kton LENA</td>
<td>Specific to $K^+\nu$</td>
</tr>
<tr>
<td></td>
<td>Next gen. reactor (DB2) ?</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Water-based LSc ?</td>
<td></td>
</tr>
</tbody>
</table>

Kearns, Asilomar 2013
Proton Decay Search Territory

\[ p \rightarrow e^+ \pi^0 \]

\[ p \rightarrow K^+ \nu \]

Lifetime Sensitivity (90% CL)

- **Hyper-K**: \( \tau/B = 5e34 \)
  - 17 evts
  - 1 BG
- **LAr-34**: \( \tau/B = 1e34 \)
  - 9 evts
  - 0.3 BG

Starting time? Guess 1 decade from now. Adjust starting time as you wish.

- 0.5 Mt yr exposure by Super-K before next generation experiments
Unification of couplings in SUSY SO(10)

Small Higgs representations used for symmetry breaking \((16, \overline{16}, 45, 10)\)
Threshold corrections calculable and small
Higgs doublet mass obtained without fine-tuning
Fairly sharp predictions for proton lifetime possible

Babu, Pati, Tavartkiladze (2010)
Correlation for spectrum with $\tan\beta = 7$ and $r=1/1200$.

(i): $\alpha_3 = 0.1177$.
(ii): $\alpha_3 = 0.1184$.
(iii): $\alpha_3 = 0.1191$. 

Correlation between $d = 5$ and $d = 6$ proton decay.
Proton Lifetime Predictions

\[ \Gamma_{d=5}^{-1}(p \rightarrow \bar{\nu}K^+) \simeq 3.6 \cdot 10^{33} \text{ yrs} \times \left( \frac{0.012 \text{ GeV}^3}{\beta_H} \right)^2 \left( \frac{6.9}{\bar{A}_S^\alpha} \right)^2 \left( \frac{1.25}{R_L} \right)^2 \]

\times \left( \frac{M_{\text{eff}}}{3.4 \times 10^{19} \text{ GeV}} \right)^2 \left( \frac{500 \text{ GeV}}{M_W} \right)^2

\[ \Gamma_{d=6}^{-1}(p \rightarrow e^+\pi^0) \simeq 1.0 \times 10^{34} \text{ yrs} \left( \frac{0.012 \text{GeV}^3}{\alpha_H} \right)^2 \left( \frac{2.78}{A_R} \right)^2 \left( \frac{5.12}{f(p)} \right) \left( \frac{1/20}{\alpha_G(M_X)} \right)^2 \left( \frac{M_X}{6.24 \times 10^{15} \text{GeV}} \right)^4 \]

Imposing the correlation equation we obtain the predictions:

\[ \Gamma_{d=6}^{-1}(p \rightarrow e^+\pi^0) \lesssim 10^{35} \text{ yrs} \]

\[ \Gamma^{-1}(p \rightarrow \bar{\nu}K^+) \leq 7 \times 10^{34} \text{ yrs}. \]

Both modes should be within reach of experiments!
Proton lifetime expectations

\[ p \rightarrow e^+ \pi^0 \]
\[ p \rightarrow \bar{\nu} K^+ \]

\( \tau/B \) (years)
Neutron-Antineutron Oscillations

$n - \bar{n}$ oscillations violate baryon number by 2 units


Analogous to $K^0 - \bar{K}^0$ mixing

$$M_B = \begin{pmatrix} m_n - \bar{\mu}_n \cdot \bar{B} - i\lambda/2 & \delta m \\ \delta m & m_n + \bar{\mu}_n \cdot \bar{B} - i\lambda/2 \end{pmatrix}$$

$$P(n \rightarrow \bar{n}, t) \simeq [\delta m t]^2$$

Probes new physics scale of order $10^5 - 10^6$ GeV

Pati-Salam unification predicts transition time $\tau_{n-\bar{n}} \sim 10^{10}$ sec.

Mechanism of $n - \bar{n}$ oscillation can explain baryon asymmetry
Conceptual Horizontal NNbarX Search in Project X at Fermilab

with elliptical focusing reflector

Typical initial baseline parameters:

Cold LD$_2$ source from 1MW spallation target
Luminous source area, dia 30 cm
Annihilation target, dia 200 cm
Reflector starts at 1.5 m
Reflector ends at 40 m
Reflector semi-minor axis 2.0 m
Distance to target 200 m
Super-mirror m=6
Vacuum < $10^{-5}$ Pa
Residual magnetic field < 1 nT

MC Simulated sensitivity $Nt^2$: 110 “ILL units” x years

Sensitivity and parameters are subject of optimization by Monte-Carlo including overall cost

N-nbar effect can be suppressed by weak magnetic field.
Summary and Conclusions

- There is strong circumstantial evidence for grand unification
- Proton decay is the missing link
- Proton decay discovery will be transformative to the field
- SUSY and non-SUSY modes should be searched for, along with various unconventional modes
- Large underground detectors absolutely essential
- Free neutron oscillations well motivated and probes a different sector of $B$ violation and should be pursued
Neutrino Theory

Patrick Huber

Center for Neutrino Physics at Virginia Tech

Snowmass at the Mississippi
July 26 – August 6, 2013, Minneapolis
Status quo

A common framework for all the neutrino data is oscillation of three active neutrinos

- $\Delta m_{21}^2 \sim 8 \cdot 10^{-5} \text{ eV}^2$ and $\theta_{12} \sim 1/2$
- $\Delta m_{31}^2 \sim 2 \cdot 10^{-3} \text{ eV}^2$ and $\theta_{23} \sim \pi/4$
- $\theta_{13} \sim 0.16$

This implies a lower bound on the mass of the heaviest neutrino

$$\sqrt{2 \cdot 10^{-3} \text{ eV}^2} \sim 0.04 \text{ eV}$$

but we currently do not know which neutrino is the heaviest.
Mixing matrices

Quarks

\[ |U_{CKM}| = \begin{pmatrix} 1 & 0.2 & 0.005 \\ 0.2 & 1 & 0.04 \\ 0.005 & 0.04 & 1 \end{pmatrix} \]

Neutrinos

\[ |U_\nu| = \begin{pmatrix} 0.8 & 0.5 & 0.15 \\ 0.4 & 0.6 & 0.7 \\ 0.4 & 0.6 & 0.7 \end{pmatrix} \]
Fermion masses

Scale

Ordering – mass hierarchy

\[ \Delta m^2_{\text{atm}} \]

\[ \Delta m^2_{\text{sun}} \]

\[ \Delta m^2_{31} > 0 \]

\[ \Delta m^2_{31} < 0 \]
Low energy observables

The most sensitive low energy observables are

- Which one is the heaviest neutrino? $-0\nu\beta\beta$, $\beta$-decay endpoint, Oscillation
- Absolute $m_\nu$ – $\beta$-decay endpoint, Cosmology
- Majorana vs Dirac mass – $0\nu\beta\beta$
- Is $\theta_{23}$ maximal? – Oscillation
- Is there leptonic CP violation? – Oscillation
- Are there only 3 light neutrinos? – Oscillation
$\theta_{13}$ is large!

Many results from reactor and beam experiments

Some single results exceed $5\sigma$ significance

All results agree well

NB – 2 years ago we had only $2\sigma$ indications.
Model selection

... a large fraction has been excluded!

Antusch, 2012

Figure shows only a small subset of the existing models ...!

based on figure from Albright, Mu-Chun Chen ('06)
Neutrinos are massive – so what?

Neutrinos in the Standard Model (SM) are strictly massless, therefore the discovery of neutrino oscillation, which implies non-zero neutrino masses requires the addition of new degrees of freedom.
We always knew they are . . .

The SM, likely, is an effective field theory, i.e. at some high scale $\Lambda$ new degrees of freedom will appear

$$\mathcal{L}_{SM} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \ldots$$

The first operators sensitive to new physics have dimension 5. It turns out there is only one dimension 5 operator

$$\mathcal{L}_5 = \frac{1}{\Lambda} (LH)(LH) \rightarrow \frac{1}{\Lambda} (L\langle H \rangle)(L\langle H \rangle) = m_\nu \nu \nu$$

Thus studying neutrino masses is, in principle, the most sensitive probe for new physics at high scales

Weinberg
Effective theories

The problem in effective theories is, that there are \emph{a priori} unknown pre-factors for each operator

\[ \mathcal{L}_{SM} + \frac{\#}{\Lambda} \mathcal{L}_5 + \frac{\#}{\Lambda^2} \mathcal{L}_6 + \ldots \]

Typically, one has \( \# = \mathcal{O}(1) \), but there may be reasons for this being wrong

- lepton number may be conserved \( \rightarrow \) no Majorana mass term
- lepton number may be approximately conserved \( \rightarrow \) small pre-factor for \( \mathcal{L}_5 \)

Therefore, we do not know the scale of new physics responsible for neutrino masses – anywhere from keV to the Planck scale is possible.
Neutrino masses are different

The crucial difference between neutrinos and other fermions is the possibility of a Majorana mass term

\[-\frac{1}{2}m_L(\bar{\psi}_L\psi^C_R + \bar{\psi}_R\psi^C_L) - \frac{1}{2}m_R(\bar{\psi}_R\psi^C_L + \bar{\psi}_L\psi^C_R)\]

on top of the usual Dirac mass term

\[m_D(\bar{\psi}_L\psi_R + \bar{\psi}_R\psi_L)\]

This allows for things like the seesaw mechanism (many versions) and implies that the neutrino flavor sector probes very different physics than the quark sector.
Neutrino mass determination

Finding the scale $\Lambda$ of neutrino mass generation rests crucially on knowing

- Dirac vs Majorana mass
- Absolute size of mass

All direct experimental techniques for mass determination rely on $\nu_e$, which is mostly made up of $m_1$ and $m_2$. Thus, the effective mass in both kinematic searches and $0\nu\beta\beta$ has a lower bound only if $m_1, m_2 > m_3$, which we call the inverted mass hierarchy.
What did we learn from that?

Our expectations where to find BSM physics are driven by models – but we should not confuse the number of models with the likelihood for discovery.

- CKM describes all flavor effects
- SM baryogenesis difficult
- New Physics at a TeV
  - does not exist or
  - has a special flavor structure

and a vast number of parameter and model space excluded.

Neutrinos are very different from quarks, therefore precision measurements will yield very different answers, relating to physics at scales inaccessible by any collider.
Non-standard interactions

NSI are the workhorse for BSM physics in the neutrino sector. They can be parameterized by terms like this

\[ \mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_f \epsilon_{\alpha\beta}^{fp} (\bar{\nu}_\alpha \gamma^\rho \nu_\beta) (\bar{f} \gamma_\rho P f), \]

where \( f \) can be any fermion and \( P \) is the projection onto right and left-handed components. Wolfenstein, 1978

At higher energy, this contact term has to be replaced with a propagating exchange particle. This scale typically is closely related to scale of neutrino mass generation and sizable effects occur if the scale \( \ll m_{\text{GUT}} \).
Impact on three flavors

Three flavor analysis are not safe from these effects!

Especially, global fits for the phase and mass hierarchy need to be aware of NSI.

Friedland, 2012
CP violation

There are only very few parameters in the $\nu$SM which can violate CP

- CKM phase – measured to be $\gamma \simeq 70^\circ$
- $\theta$ of the QCD vacuum – measured to be $< 10^{-10}$
- Dirac phase of neutrino mixing
- Possibly: 2 Majorana phases of neutrinos

At the same time we know that the CKM phase is not responsible for the Baryon Asymmetry of the Universe...
Flavor models

Simplest un-model – anarchy Murayama, Naba, DeGouvea

\[ dU = ds_{12}^2 dc_{13}^4 ds_{23}^2 d\delta_{CP} d\chi_1 d\chi_2 \]

predicts flat distribution in \( \delta_{CP} \)

Simplest model – Tri-bimaximal mixing Harrison, Perkins, Scott

\[
\begin{pmatrix}
\sqrt{\frac{1}{3}} & \frac{1}{\sqrt{3}} & 0 \\
\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \\
\frac{1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}}
\end{pmatrix}
\]

to still fit data, obviously corrections are needed – predictivity?
Sum rules

\[ \theta_{12} = 35^\circ + \theta_{13} \cos \delta \]
\[ \theta_{12} = 32^\circ + \theta_{13} \cos \delta \]
\[ \theta_{23} = 45^\circ + \sqrt{2} \theta_{13} \cos \delta \]
\[ \theta_{23} = 45^\circ - 1/\sqrt{2} \theta_{13} \cos \delta \]
\[ \theta_{12} = 45^\circ + \theta_{13} \cos \delta \]

Antusch, King

3 \sigma resolution of 15° distance requires 5° error. NB – smaller error on \( \theta_{12} \) requires dedicated experiment like JUNO

current best fit values and errors for \( \theta_{12}, \theta_{13} \) and \( \theta_{23} \) taken from Fogli et al. 2012

P. Huber – VT-CNP – p. 18
Is $5^\circ$ feasible?

![Graph showing the fraction of $\delta$ vs $\Delta \delta$ for various projects at 1$\sigma$ confidence level with $\theta_{23}=40^\circ$](image-url)
LSND and MiniBooNE

\[ P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \approx 0.003 \]
Reactor and Gallium anomalies

<table>
<thead>
<tr>
<th>k source</th>
<th>GALLEX</th>
<th>SAGE</th>
</tr>
</thead>
<tbody>
<tr>
<td>$^{51}\text{Cr}$</td>
<td>G1</td>
<td>S1</td>
</tr>
<tr>
<td>$R_B^k$</td>
<td>0.953 ± 0.11</td>
<td>0.812 ± 0.10</td>
</tr>
<tr>
<td>$R_H^k$</td>
<td>0.84 ± 0.13</td>
<td>0.71 ± 0.12</td>
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<tr>
<td>source height [m]</td>
<td>2.7</td>
<td>2.38</td>
</tr>
</tbody>
</table>
Finding a sterile neutrino

All pieces of evidence have in common that they are less than $5 \sigma$ effects and they may be all due to the extraordinary difficulty of performing neutrino experiments, if not:

- N sterile neutrinos are the simplest explanation
- Tension with null results in disappearance remains

Due to their special nature as SM gauge singlets sterile neutrinos are strong candidates for being a portal to a hidden sector – significant experimental activity.
Summary

• Neutrino oscillation is solid evidence for new physics
• Current data allows $\mathcal{O}(1)$ corrections to three flavor framework
• Precision measurements have the best potential to uncover even “newer” physics
• Sterile neutrinos?

Neutrinos have provided us with many surprises and neutrinos are still largely unexplored!
A Discovery Program of Neutrino Experiments

Karsten M. Heeger
Snowmass on the Mississippi, July 31, 2012

This is not a comprehensive summary. Highlights of opportunities!
Neutrino sources provide many opportunities
Tools of Discovery - Neutrino Detectors

detectors must match requirements of ν sources, leads to a broad field with a variety of detectors and techniques
The First Anomaly

CI-Ar Solar Neutrino Experiment at Homestake

“deficit” of solar neutrinos

experiment only sensitive to $\nu_e$

1970 - 1994
Discoveries of Neutrino Oscillation

1968 Ray Davis detects 1/3 of expected solar neutrinos. (Nobel prize in 2002)

1998 SuperK reports evidence for oscillation of atmospheric neutrinos.

2001/2002 SNO finds evidence for solar $\nu_e$ flavor change.

2003 KamLAND discovers disappearance of reactor $\bar{\nu}_e$

2012 Daya Bay, Double Chooz, RENO measure $\theta_{13}$

2013 T2K sees $\nu_e$ appearance
Neutrino Oscillation Implies Neutrino Mass

mass eigenstates ≠ flavor eigenstates

\[ |\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle \]

flavor composition of neutrinos changes as they propagate

Observables in oscillation experiments

energy E and baseline L
oscillation frequency \( \Delta m^2 \)
oscillation amplitude \( \theta \)

Parameterized in a mixing matrix

\[ |\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle \]

\[ P_{i \rightarrow j} = \sin^2 2\theta \sin^2 \left( 1.27 \Delta m^2 \frac{L}{E} \right) \]

\[ U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \]
Neutrino Oscillation Measurements

Lots of Experimental Data

• atmospheric $\nu_\mu$ and $\bar{\nu}_\mu$ disappear most likely to $\nu_\tau$ (SK, MINOS)
• accelerator $\nu_\mu$ and $\bar{\nu}_\mu$ disappear at $L\sim 250, 700$ km (K2K, T2K, MINOS)
• accelerator $\nu_\mu$ appear as $\nu_e$ at $L\sim 250, 700$ km (T2K, MINOS)
• solar $\nu_e$ convert to $\nu_\mu/\nu_\tau$ (Cl, Ga, SK, SNO, Borexino)
• reactor $\bar{\nu}_e$ disappear at $L\sim 200$ km (KamLAND)
• reactor $\nu_e$ disappear at $L\sim 1$ km (DC, Daya Bay RENO)

Experiments have demonstrated oscillation L/E pattern

matter effects can be probed in long-baseline experiments or extreme environments
Neutrino Mixing is Different

Mixing Angles

\[
U = \begin{pmatrix}
U_{e1} & U_{e2} & U_{e3} \\
U_{\mu1} & U_{\mu2} & U_{\mu3} \\
U_{\tau1} & U_{\tau2} & U_{\tau3}
\end{pmatrix} = \begin{pmatrix} 0.8 & 0.5 & U_{e3} \\
0.4 & 0.6 & 0.7 \\
0.4 & 0.6 & 0.7
\end{pmatrix}
\]

\[U_{\text{MNSP}} \text{ Matrix}
\]

Maki, Nakagawa, Sakata, Pontecorvo

\[
= \begin{pmatrix} 1 & 0 & 0 \\
0 & \cos \theta_{23} & \sin \theta_{23} \\
0 & -\sin \theta_{23} & \cos \theta_{23}
\end{pmatrix} \times \begin{pmatrix}
cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\
0 & 1 & 0 \\
-e^{i\delta_{CP}} \sin \theta_{13} & 0 & \cos \theta_{13}
\end{pmatrix} \times \begin{pmatrix}
\cos \theta_{12} & \sin \theta_{12} & 0 \\
-\sin \theta_{12} & \cos \theta_{12} & 0 \\
0 & 0 & 1
\end{pmatrix} \times \begin{pmatrix} 1 & 0 & 0 \\
0 & e^{i\alpha/2} & 0 \\
0 & 0 & e^{i\alpha/2+i\beta}
\end{pmatrix}
\]

atmospheric

reactor, accelerator

solar, reactor

\[0\nu\beta\beta\]

Quarks

Leptons

\[\begin{pmatrix}
\end{pmatrix}
\]

\[\begin{pmatrix}
\end{pmatrix}\]
Neutrino Oscillation Measurements

Experiments provide complementary data

- **Solar Experiments**
  - Dominant: $\theta_{12}$
  - Important: $\Delta m_{21}^2$, $\theta_{13}$

- **Reactor LBL (KamLAND)**
  - Dominant: $\theta_{13}$

- **Reactor MBL (Daya-Bay, Reno, D-Chooz)**
  - Dominant: $\theta_{23}$
  - Important: $\Delta m_{atm}^2$, $\theta_{13}$, $\delta_{cp}$

- **Atmospheric Experiments**
  - Dominant: $\theta_{23}$

- **Accelerator LBL $\nu_\mu$ Disapp (Minos)**
  - Dominant: $\Delta m_{atm}^2$
  - Important: $\theta_{13}$, $\theta_{23}$

- **Accelerator LBL $\nu_e$ App (Minos, T2K)**
  - Dominant: $\delta_{cp}$
  - Important: $\theta_{13}$, $\theta_{23}$

Gonzalez-Garcia et al, ICHEP2012

Complete suite of measurements can over-constrain the 3-ν framework

\[
U = \begin{pmatrix}
U_{e1} & U_{e2} & U_{e3} \\
U_{\mu1} & U_{\mu2} & U_{\mu3} \\
U_{\tau1} & U_{\tau2} & U_{\tau3}
\end{pmatrix}
\]
From Anomalies to Precision Oscillation Physics

1960-1990

oscillation searches

precision measurements

solar neutrino problem

1990-2000

>2000

http://hitoshi.berkeley.edu/neutrino
Recent Anomalies

Anomalies in 3-v interpretation of global oscillation data

LSND \((\bar{\nu}_e \text{ appearance})\)
MiniBoone \((\bar{\nu}_e, \nu_e \text{ appearance})\)
Ga anomaly \((\nu_e \text{ appearance})\)
Reactor anomaly \((\bar{\nu}_e \text{ disappearance})\)

new oscillation signal requires \(\Delta m^2 \sim O(1 \text{eV}^2)\) and \(\sin^2 2\theta > 10^{-3}\)

New physics or experimental artifacts?

Planning experiments with reactors, radioactive sources, and accelerators to confirm/refute short-baseline anomalies
Neutrinos - Open Questions

- Neutrino have mass, but why are they so light?
- What is the absolute mass scale?
- Do neutrinos have Majorana mass?
- Normal or inverted mass ordering?
- Is $\theta_{23}$ maximal?
- CP violation?
- Are there more than 3 $\nu$?
Precision Oscillation Measurements

Studying neutrino flavor change as a function of distance and energy

accelerator-based program over short and long baselines

measuring appearance and disappearance

LBNE 34kt, 5 yrs, ν
Precision Oscillation Measurements

A staged program of experiments for the next decade

LBNE

NOvA

MINOS+

MicroBoone

Minerva

d Detectors at various scales
Precision Oscillation Measurements

A phased development of accelerator capabilities

[Diagram of accelerator development with various facilities and distances indicated]
Precision Oscillation Measurements

Searching for CP violation

Determining the mass hierarchy

alternative approaches to mass hierarchy:
reactor experiments at ~50km baseline;
atmospheric neutrinos

exposure of order of Mt.MW.yr, very long baseline (> 1000 km) and tight control of systematics (< 2% on signal) is needed to reach CKM level precision
Oscillation Physics with Atmospheric Neutrinos

Atmospheric neutrinos observable in a large underground detectors are sensitive to all currently unknown oscillation parameters.

Large underground detectors enable other physics, e.g. proton decay searches.

Multi-purpose detectors when placed in beam.
Importance of Mass Hierarchy

What is the flavor content of the lightest neutrino mass state?

Knowing the mass hierarchy will help us understand the nature of neutrino mass from neutrinoless double beta-decay ($0\nu\beta\beta$).

\[ \Gamma_{0\nu} = G_{0\nu} |M_{0\nu}|^2 \left( m_{\beta\beta} \right)^2 \]

$0\nu\beta\beta$ depends on effective neutrino mass
Majorana or Dirac Neutrino Masses?

Neutrinoless double beta decay is the only feasible experimental approach to establish Majorana mass of neutrinos.

Observation of $0
\nu\beta\beta$ would imply:
- lepton number non-conservation
- Majorana nature of neutrinos

$0\nu\beta\beta$ allow us to determine:
- effective neutrino mass

Several technologies feasible. Ready to explore the inverted hierarchy region.

Majorana neutrino mass = beyond SM physics
Absolute Neutrino Mass

Precision measurements of beta decay to determine absolute neutrino mass

\[ \frac{dN}{dT} = \frac{G_F \cos \theta_C}{2\pi^3} |M_{\text{nuc}}|^2 F(Z, T)(T + m)(T^2 + 2mT)^{1/2}(T_0 - T) \sum_i |U_{ei}|^2 [(T_0 - T)^2 - m_i^2]^{1/2} \]

For \( m_1 \approx 100 \text{ meV} \) and no sterile neutrinos, the beta spectrum simplifies to an “effective mass”

\[ m_\beta = \left[ \sum_i |U_{ei}|^2 m_i^2 \right]^{1/2} \]

Smallness of neutrino mass may be related to GUT- or Planck-scale physics.
Synergies and Applications - Examples

Cyclotrons for neutrino physics (and industrial applications)

Neutrino detectors for reactor monitoring and non-proliferation

remote discovery of undeclared nuclear reactors with large detectors at km scale

reactor antineutrino studies at short baselines
Summary

• Recent discoveries have shown that neutrinos mix and have mass. Evidence for new physics.

• A staged program of neutrino oscillation experiments is underway to make precision measurements of oscillation parameters, test 3-flavor paradigm, and understand neutrino interactions.

• Historic anomalies have turned into discoveries of solar and atmospheric neutrino oscillations. Neutrinos may continue to surprise us!

• The nature of neutrino mass is not yet understood and may hold the clue to physics beyond the Standard Model.

• Synergies with instrumentation and technology developments; connections with other frontiers.

*This is not a comprehensive summary. Apologies for any omissions.*

*Thanks to many colleagues for input, figures, and comments.*
Tough Questions for Neutrinos & GUTs

• Several have been answered in the course of the three intro talks: (IF1, IF2, IF17...)
  – What are we testing by pushing proton decay limits?
  – What do we learn from measuring neutrino mixing parameters, and how well do we need to know them?
• We have selected several other Colloquium Questions (or sub-questions—sometimes rephrased for conciseness, or modified) to be addressed in micro-talks by the panelists.
• Will take ~2 questions from the floor per panelist
• After going through all questions, will open floor for general discussion
The Questions

- IF15: Should searches from proton decay be continued in absence of a signal? (Ed Kearns)
- IF10/13: What do CP $\delta$ measurements tell us about leptogenesis? (Boris Kayser)
- IF7: Is there an experimental floor to the search for neutrinoless double beta decay? (Josh Klein)
- IF5: How important is breadth of program? (Bonnie Fleming)
- IF7: What is the relative importance of testing the 3-flavor paradigm and exploring anomalies? (Steve Brice)
- IF11/12: What are the priorities and reach of LBNE? (Jon Urheim)
- G1: What are the interfaces with the CF? (Scott Dodelson)
- IF8: What should be the strategy beyond the next decade? (Ken Long)
Theoretical motivation is still profound:
  - BAU, quark-lepton charges, GUTs, running coupling constants
  - Many predictive models— not fine-tuned (mostly)

Experiment is achievable:
  - Hyper-Kamiokande is a straightforward scale up
  - We have a plan, and a growing community, for a massive LArTPC (e.g. LBNE)
  - Can be done as part of a multipurpose underground experiment

Benchmarks:
\[ e^+\pi^0 \] – nearly model independent prediction of gauge unification
\[ \nu K^+ \] – leading suspect if SUSY plays a role
Many other modes, but these are the benchmarks (experimentally and theoretically)

Experimental goal: exceed previous generation by order of magnitude (15-20 years)
\[ e^+\pi^0 \] – few \( \times 10^{35} \) years, \( \nu K^+ \) – many\( \times 10^{34} \) years
Reaching these levels does not “rule out” GUT proton decay, but is in the right territory for discovery and if none is seen, further confounds a wide range of models.
The Connection Between Leptogenesis and the CP-Violating Phase $\delta_{CP}$

The key ingredients of baryogenesis via leptogenesis are:
1. CP violation in the leptonic sector
2. Nonconservation of lepton number $L$.

The first would be established by finding that the leptonic CP-violating phase $\delta_{CP}$ is nonzero, and the second by observing neutrinoless double beta decay.

Leptogenesis is a very natural consequence of the See-Saw picture of why neutrinos are so light.

Owing to the See-Saw relation between high- and low-mass physics, generically, neutrino CP violation and leptogenesis imply each other.
IF7. Is there an experimental floor to the search for neutrinoless double beta decay?

Short answer: Sure, depends on how much time and money you’re willing to spend.

Where we are now

Under construction

“tonne-scale”

With enough work:
• Radioactive backgrounds can be reduced through purification and tagging
• Even solar neutrinos can be removed through tracking or tagging
• But you can never get around $2\nu$ background:

There may be a tradeoff between achievable mass and achievable resolution.

A. Mastbaum, S. Seibert
IF5. How important is breadth of program for the next-generation neutrino oscillation experiments? If important, how can this be achieved?

*Breadth in program = Breadth and depth in physics discovery*

What is breadth?
- Complementary techniques to address the physics
  - Different detector technologies (eg: LAr and WCh)
  - Different baselines, different beams
- A variety of physics to address with the same experiments
  - Underground adds proton decay, astrophysical and atmospheric neutrinos, ...
  - Near detector physics for oscillations and cross sections

What does breadth give you?
- Comprehensive approach to understanding neutrinos
- Broad program beyond neutrinos
- Enables:
  - Large and small experiments (Range cost and timescale)
  - Program with many Ph.D results!
IF6. What is the relative importance of testing the 3-flavor neutrino paradigm and exploring anomalies?

1. We are charting new territory in neutrino physics and must search all regions available to us
   - Measure 3 flavor mixing parameters
   - Check the validity of the 3 flavor paradigm
   - Be constantly alert for surprises
   - Follow up decisively on anomalies

2. If you pick a fertile region you may make unintended discoveries, but we must devote resources in proportion to the *a priori* likelihood and significance of discovery

3. We have to be able to respond to surprises and reprioritize accordingly
**IF 12:** In the current configuration for Phase-I of LBNE (assuming no new international support), what 5-sigma discoveries are possible?

1) LBNE Phase-I will constitute a decisive step for the U.S. particle physics program.
   - Fully realized, LBNE (34kt, underground) is a bold experiment aiming to address a broad array of key questions in particle physics, including leptonic CPV, neutrino MH, tests of 3-flavor mixing picture, searches for proton decay, studies of supernova neutrinos, and precision neutrino interaction measurements, exploiting the cost-effectiveness, scalability, and exquisite capabilities of the LArTPC technology. Its design is mature and costs are well understood.
   - **The first phase will be the enabler for this program.**

2) Strong support from international partnerships is emerging,
   - examples: India (near detector), UK (STFC), Italy (INFN – Icarus), Europe/LBNO, Brazil

3) We can discover the mass hierarchy
   - Significance $> 5\sigma$, LBNE alone, if $\delta_{CP}$ has the right sign
     $> 5\sigma$, everywhere with LBNE+ NOvA/T2K

4) CP Phase Resolution & Establishing CPV
   - Extended reach in phase-I $\rightarrow \delta_{CP}$ to 15-30$^\circ$.
   - $3\sigma$ to just under $5\sigma$ for CPV significance for favorable $\delta_{CP}$

**IF 11:** If additional resources can be found to restore some of the LBNE scope, what is the highest scientific priority: moving underground, or improving beam and/or detectors?

- Already have heard comments on:
  - Importance of the breadth of the program
  - Discovery potential in non-beam physics (e.g., proton decay, supernova & atm. ν’s)
  - Example: expect ~900 ν_e events in 10kt LArTPC from SN explosion at 10 kpc.

- Moving underground provides infrastructure for further detector expansion at the right baseline & depth for full LBNE program

- Strong consensus within LBNE collaboration to go underground as highest priority given additional resources from new domestic/international partners.

- Potential European partners agree w/ collaboration’s goal, namely that LBNE FD should be **underground** and larger **in the first phase.**

- Geotechnical studies are now being carried out for the underground site, in anticipation of this.
G1. How do we exploit science opportunities at the interfaces between the Frontiers?

Complementarity:
- Oscillation experiments sensitive to mass differences → we live along either blue or green line
- Cosmology experiments sensitive to sum of the masses → where are we on the line
- Long baseline determination → which line we live on
- Anomalies on either or both frontiers could point to a sterile sector
Neutrino strategy beyond the next decade?

- Neutrino strategy must include search for 0ν2β and search for sterile neutrinos;
  - Comments below confined to strategy for oscillations

- Beyond the next decade; > 2023:
  - i.e. the LBNE (T2HK) era
    - The mass hierarchy will be “on the way to being determined”
    - First scan of CP-violation underway
    - Sterile-neutrino searches underway
      - Changes development of field if discovered!

- The Neutrino Factory is capable of performing “at the quark level”:
  - Best discovery reach, best precision
  - Need to:
    - Demonstrate that a muon-accelerator-based facility can serve neutrino science;
    - Prove ionization cooling technique

- So, oscillation strategy must encompass:
  - Full exploitation of LBNE (and T2HK):
    - Includes programme by which systematic errors are reduced
  - Incremental development of muon-accelerator-based facilities for neutrino science:
    - nuSTORM:
      - Exquisite sensitivity to sterile neutrinos
      - Detailed and precise study of νₑ-N scattering required to allow LBNE (T2HK) programme to fulfill its potential
      - Test-bed for next increment
    - Demonstration of ionization cooling (MICE)
  - Active review of potential of alternative techniques (cyclotrons, CERN, ESS, etc.) and new results (e.g. sterile neutrino searches, long-baseline νₑ-appearance measurements)
Backups
Constraints on neutrino parameters degrade when NSI allowed

Constraints on neutrino parameters degrade when Dark Energy freedom allowed