

# Higgs Spin / Mixture Overview

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for

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# For the conclusion points

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(●) The spin of the 125 GeV boson will be constrained by the LHC. A limited parameter space of spin-two couplings may be left to be constrained by the data from the future facilities. Potential  $CP$  admixture in spin-zero  $H \rightarrow ZZ^*$  decay amplitude squared ( $f_{a3}$ ) will be measured by LHC to a few percent precision. The  $e^+e^-$  machines can measure this to a greater precision in the  $ee \rightarrow ZH$  mode.  $CP$  admixture in lepton couplings is not expected to suffer from loop suppression and can be studied in  $H \rightarrow \tau\tau$  decay and  $ttH$  production, leading to interesting measurements on both proton and lepton colliders. The photon and muon colliders are unique in their capability to probe  $CP$  violation directly with polarized beams.

- Next **important** milestone: have first draft report by **July 15**

# $CP$ Violation in the Higgs Sector

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- $CP$  mixture could arise for example in 2HDM neutral Higgs sector:

$$H = \cos \alpha_1 \cos \alpha_2 H_1 + \sin \alpha_1 \cos \alpha_2 H_2 + \sin \alpha_2 A$$

- ideally we want to measure  $\alpha_1$  and  $\alpha_2$
- but we measure decay/production amplitudes  
such as  $H \rightarrow VV$  or  $H \rightarrow f\bar{f}$
- additional model-dependent suppression (e.g. loop in  $A \rightarrow VV$ )  
e.g.  $\sin \alpha_2 \sim 0.1$ , if loop  $\times 0.03 \Rightarrow |A_{CP\text{-odd}}|^2 \sim 10^{-5} |A_{\text{even}}|^2$

- Therefore two parts in the report:

(I) experimental projection on  $CP$ -odd fraction (and spin)

in decay (production) amplitude

- basis for comparison of facility performance

(II) connect  $CP$ -odd fraction to theoretical models

- relate to models (e.g. 2HDM), baryogenesis, other meas. (EDM)

# Two main paths: spin and mixture

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- Two main paths to study “H(125)”

(1) test of exotic **spin**  $> 0$  assignments / hypothesis testing

LHC is excluding already  $\Rightarrow$  interest may be reducing  
nonetheless, identify **benchmark models** for comparison

(2) measure **mixture**: tensor structure of interactions (spin-0)  
equivalent **effective Lagrangian** or **scattering amplitude** approaches

(2a)  $ZZH$ ,  $WWH$  (SM  $a_1$ ),  $Z\gamma H$ ,  $\gamma\gamma H$ ,  $ggH$  (SM  $a_2$ ), or  $0^-$  ( $a_3$ )

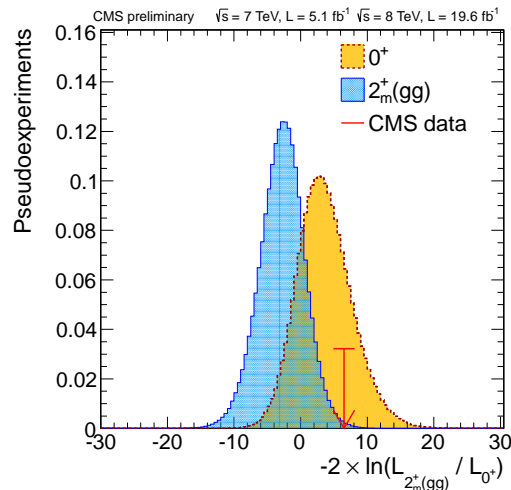
$$A_{VV} \propto a_1 m_V^2 \epsilon_1^* \epsilon_2^* + a_2 f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + a_3 f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}$$

$$(2b) \tau^+ \tau^- H, \mu^+ \mu^- H, b\bar{b}H, t\bar{t}H, .. \quad A_{f\bar{f}} \propto \frac{m_f}{v} \bar{u}_2 (\rho_1 + \rho_2 \gamma_5) v_1$$

$$(\text{field strength tensor } V^{\mu\nu} \Leftrightarrow f^{(i),\mu\nu} = \epsilon_i^\mu q_i^\nu - \epsilon_i^\nu q_i^\mu)$$

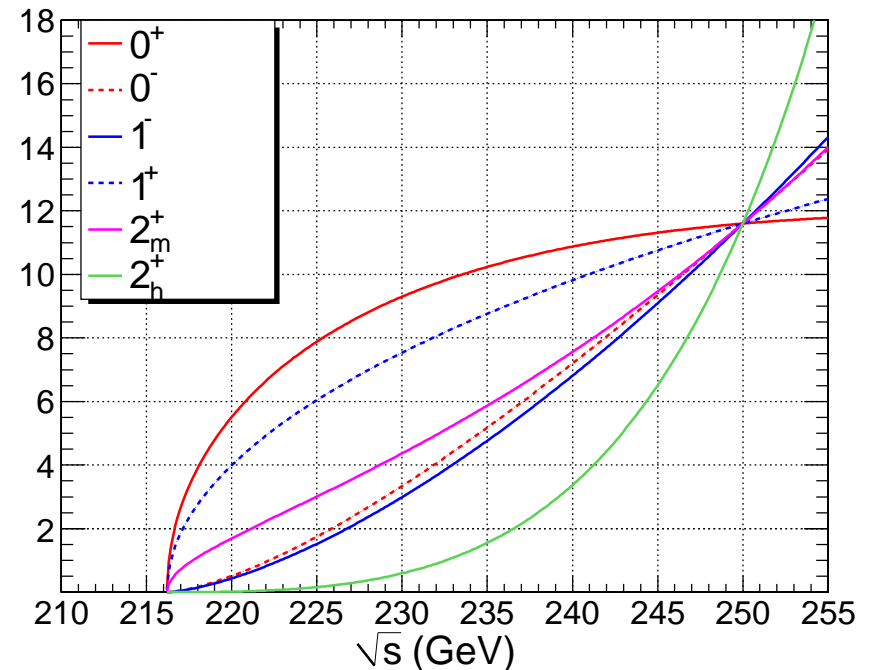
# Path 1: Spin $> 0$

- Several test models adopted by LHC for  $ZZH$ ,  $WWH$ ,  $\gamma\gamma H$ ,  $ggH$ 
  - may use min. coupling KK graviton as an example  $2_m^+$
- Possible measure tensor structure (less motivated than spin-0)



- LHC: MELA / BDT techniques, example:  
LHC expect  $2_m^+$  vs SM  $0^+$ :  $>2\sigma$   
scales to 300/fb LHC  $\sim 10\sigma$

- Measure at  $e^+e^- \rightarrow ZH$ 
  - energy scan ( $m_{Z^*}$  scan)
  - kinematics



# Path 2 (a): Mixture in $VVH$

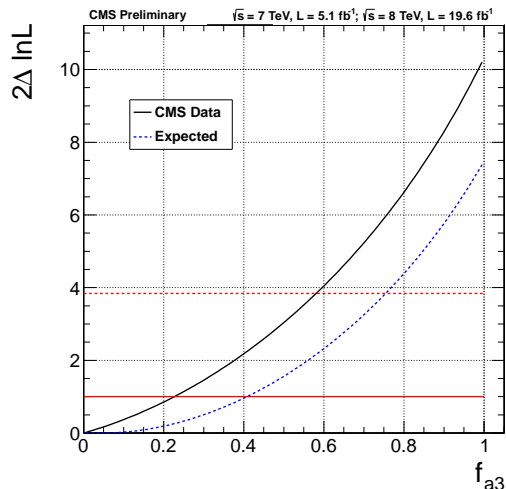
$ZZH$ ,  $WWH$  (SM  $a_1$ ),  $Z\gamma H$ ,  $\gamma\gamma H$ ,  $ggH$  (SM  $a_2$ ), or  $0^-$  ( $a_3$ )

$$A_{VV} \propto a_1 m_V^2 \epsilon_1^* \epsilon_2^* + a_2 f_{\mu\nu}^{*(1)} f^{*(2),\mu\nu} + a_3 f_{\mu\nu}^{*(1)} \tilde{f}^{*(2),\mu\nu}$$

When  $a_1$  dominates,  $f_{a3}$  is  $CP$ -violating fraction (here  $a_i = 1 \leftrightarrow \sigma_i$ ):

$$f_{CP} = f_{a3} = \frac{|a_3|^2 \sigma_4}{|a_1|^2 \sigma_1 + |a_2|^2 \sigma_2 + |a_3|^2 \sigma_4}; \quad \phi_{a3} = \arg\left(\frac{a_3}{a_1}\right)$$

$$f_{a2} = \frac{|a_2|^2 \sigma_2}{|a_1|^2 \sigma_1 + |a_2|^2 \sigma_2 + |a_3|^2 \sigma_4}; \quad \phi_{a2} = \arg\left(\frac{a_2}{a_1}\right)$$



- LHC: assuming SM

CMS expect (observe)  $f_{CP} = 0.00 \pm 0.40$  ( $\pm 0.23$ )

scales to 300/fb LHC  $f_{CP} = 0.00 \pm 0.08$  (?)

may include  $f_{a2}$ , phases in projections

## Path 2 (b): Mixture in $f\bar{f}H$

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- Mixture  $\tau^+\tau^-H, \mu^+\mu^-H, b\bar{b}H, t\bar{t}H$  harder to measure on  $e^+e^-$  &  $pp$ 
  - possible if polarization of fermion decay (production) is measured  
 $e^\pm$  beam polarization may help
  - feasibility in  $H \rightarrow \tau^+\tau^-$   
[arXiv:hep-ph/0307331](https://arxiv.org/abs/hep-ph/0307331):  $\Delta\theta \sim 6^\circ$  with 1000/fb at  $E_{e^+e^-} = 350$  GeV  
 $\Delta f_{CP}^\tau \sim 0.01$  (?) (more discussion today)
  - feasibility in  $e^+e^-(pp) \rightarrow t\bar{t}H$  (?)
- Similar parameterization:

$$A_{f\bar{f}} \propto \frac{m_f}{v} \bar{u}_2 (\rho_1 + \rho_2 \gamma_5) v_1 = \frac{m_f}{v} \bar{u}_2 \rho (\cos \theta + e^{i\phi_{\rho_2}} \sin \theta \gamma_5) v_1$$

$$f_{CP} = f_{\rho_2} = \frac{|\rho_2|^2 \sigma_2}{|\rho_1|^2 \sigma_1 + |\rho_2|^2 \sigma_2} \simeq \frac{|\rho_2|^2}{|\rho_1|^2 + |\rho_2|^2} = \sin^2 \theta$$

# Photon and Muon Colliders

- Polarized beams on  $\mu^+\mu^-$  and  $\gamma\gamma$  colliders with  $s$ -channel production
  - would allow to measure  $A_{++}$  vs  $A_{--}$  amplitudes  $\Rightarrow$   $CP$  fraction
  - need to quantify  $f_{CP}$  in  $\mu^+\mu^-H$  and  $\gamma\gamma H$   
(not “easily” possible on LHC and  $e^+e^-$ )

$\zeta_2$  is the degree of circular polarization

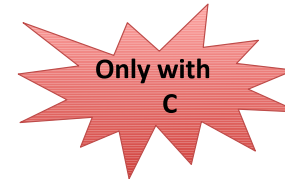
$(\zeta_3, \zeta_1)$  are the degrees of linear polarization

In  $s$ -channel production of Higgs:

$$|\overline{\mathcal{M}^{H_i}}|^2 = |\overline{\mathcal{M}^{H_i}}_0|^2 \left\{ [1 + \zeta_2 \bar{\zeta}_2] + \mathcal{A}_1 [\zeta_2 + \bar{\zeta}_2] + \mathcal{A}_2 [\zeta_1 \bar{\zeta}_3 + \zeta_3 \bar{\zeta}_1] - \mathcal{A}_3 [\zeta_1 \bar{\zeta}_1 - \zeta_3 \bar{\zeta}_3] \right\}$$

$\Rightarrow 0$  if CP is conserved

$\Rightarrow +1$  ( $-1$ ) for CP is conserved for  
A CP-Even (CP-Odd) Higgs



$\Rightarrow$  If  $\mathcal{A}_1 \neq 0$ ,  $\mathcal{A}_2 \neq 0$  and/or  $|\mathcal{A}_3| < 1$ , the Higgs  
is a mixture of CP-Even and CP-Odd states

$\Rightarrow$  Possible to search for CP violation in  
 $\tilde{Z} H \tilde{Z}$  fermions without having to measure their polarization

$\Rightarrow$  In  $b\bar{b}$ , a  $\leq 1\%$  asymmetry can be measure with 100 fb $^{-1}$   
that is, in 1/2 years

arXiv:0705.1089v2



# Spin and Mixture for Snowmass-2013

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- We already know many things, but need to focus on projections:
  - $VVH$  ( $V = W, Z$ ) on LHC covers  $H \rightarrow ZZ^*$
  - $e^+e^-$  expectations and fermion couplings need to quantify better
  - quantify  $\mu^+\mu^- \rightarrow H$  and  $\gamma\gamma \rightarrow H$  feasibility of  $CP$  measurements

$f_{CP}$	LHC 300/fb	LHC 3000/fb	$e^+e^-$ 250 GeV	$e^+e^-$ 500 GeV	$\mu^+\mu^-$ 125	$\gamma\gamma$ 125
spin-2 ...	$\sim 10\sigma$ ...	$\gg 10\sigma$ ...	$>10\sigma$ ...	$>10\sigma$ ...	? ...	? ...
$VVH$	$\pm 0.08$ (?)	$\pm 0.03$ (?)	0.0008 (?)	0.00005 (?)	?	?
$\tau\tau H$	?	?	$\sim 0.01$ (?)	$\sim 0.01$ (?)	?	?
$ttH$	?	?	–	?	–	–
$\mu\mu H$	–	–	–	–	?	–
$\gamma\gamma H$	–	(?)	–	–	–	?