

# Bounding Higgs Width Through Interferometry

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*work with:*

*Lance Dixon - 1305.3854*

*Lance Dixon and Stefan H*öche - ongoing

*Ye Li*

*Snowmass Energy Frontier Workshop*

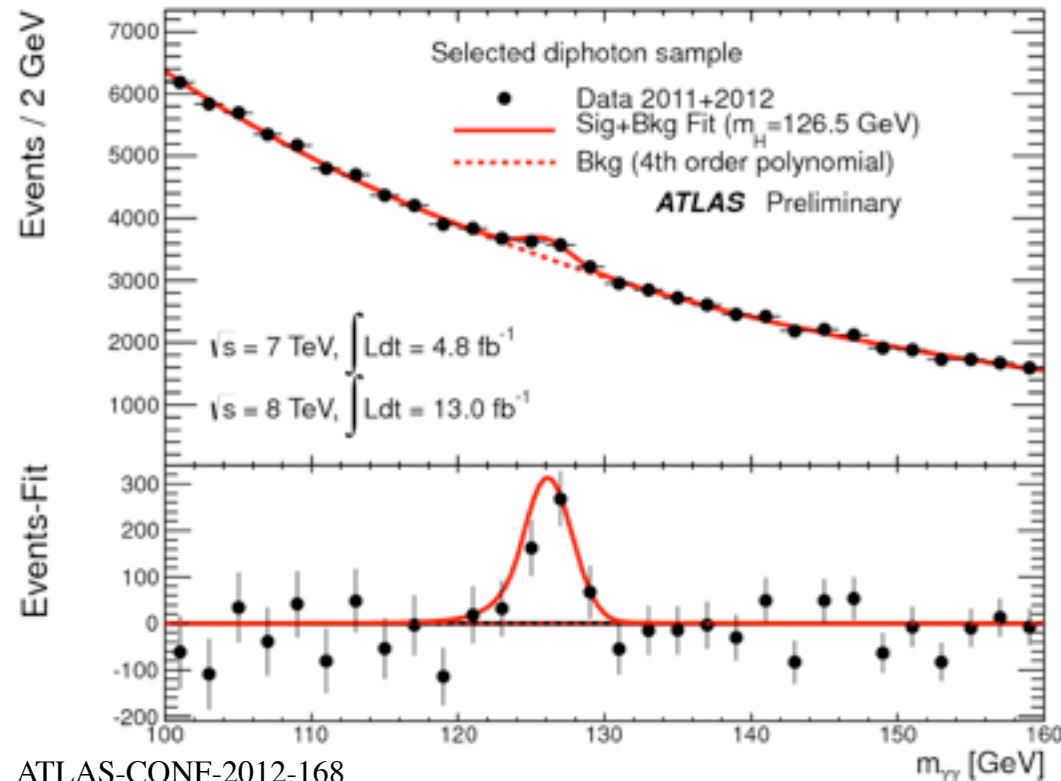
*University of Washington, Seattle*

*June 30, 2013*



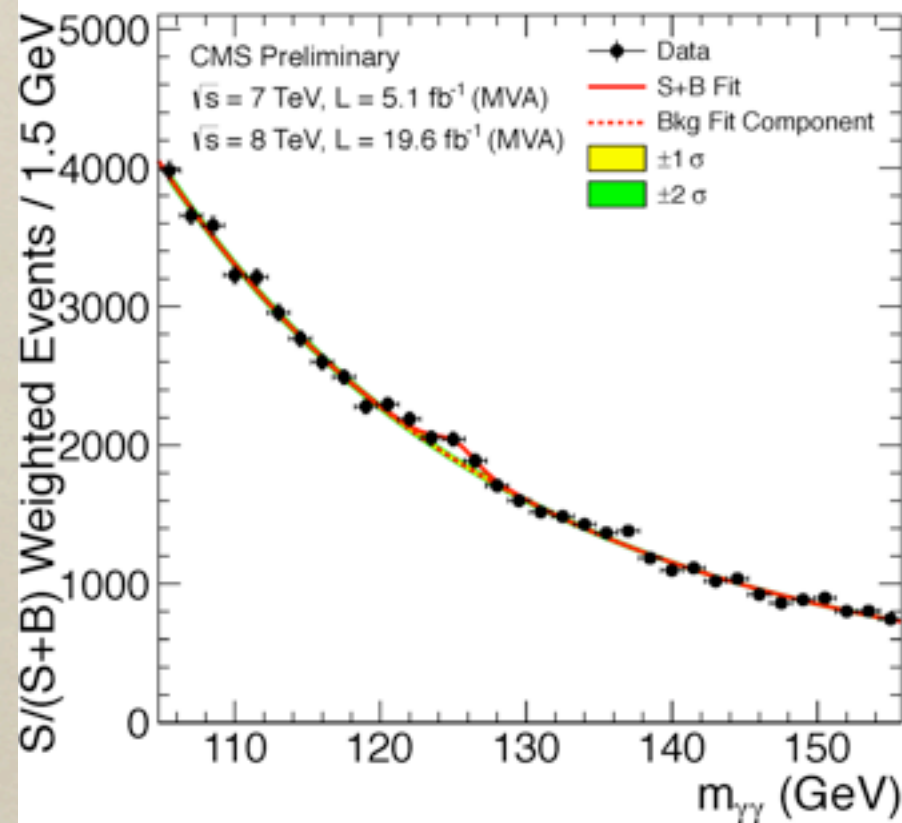


# Higgs Boson Discovered!



ATLAS-CONF-2012-168

CMS-PAS-HIG-13-001



- *Biggest discovery in years*
- *Great achievement of SM*
- *How much can we learn about Higgs from LHC?*



# Outline

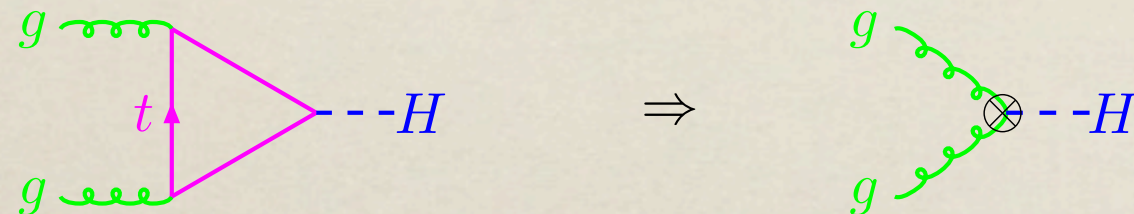
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- *Interference in  $gg \rightarrow H \rightarrow \gamma\gamma$*
- *Real part interference: mass shift*
- *NLO corrections to interference*
- *Bounding  $\Gamma_H$  using mass shift*
- *Non-SM Higgs: CP mixed state*
- *Non-SM Higgs: spin-2 scenario*
- *Conclusion*



# Higgs Production

- Dominated by gluon fusion through a top quark loop



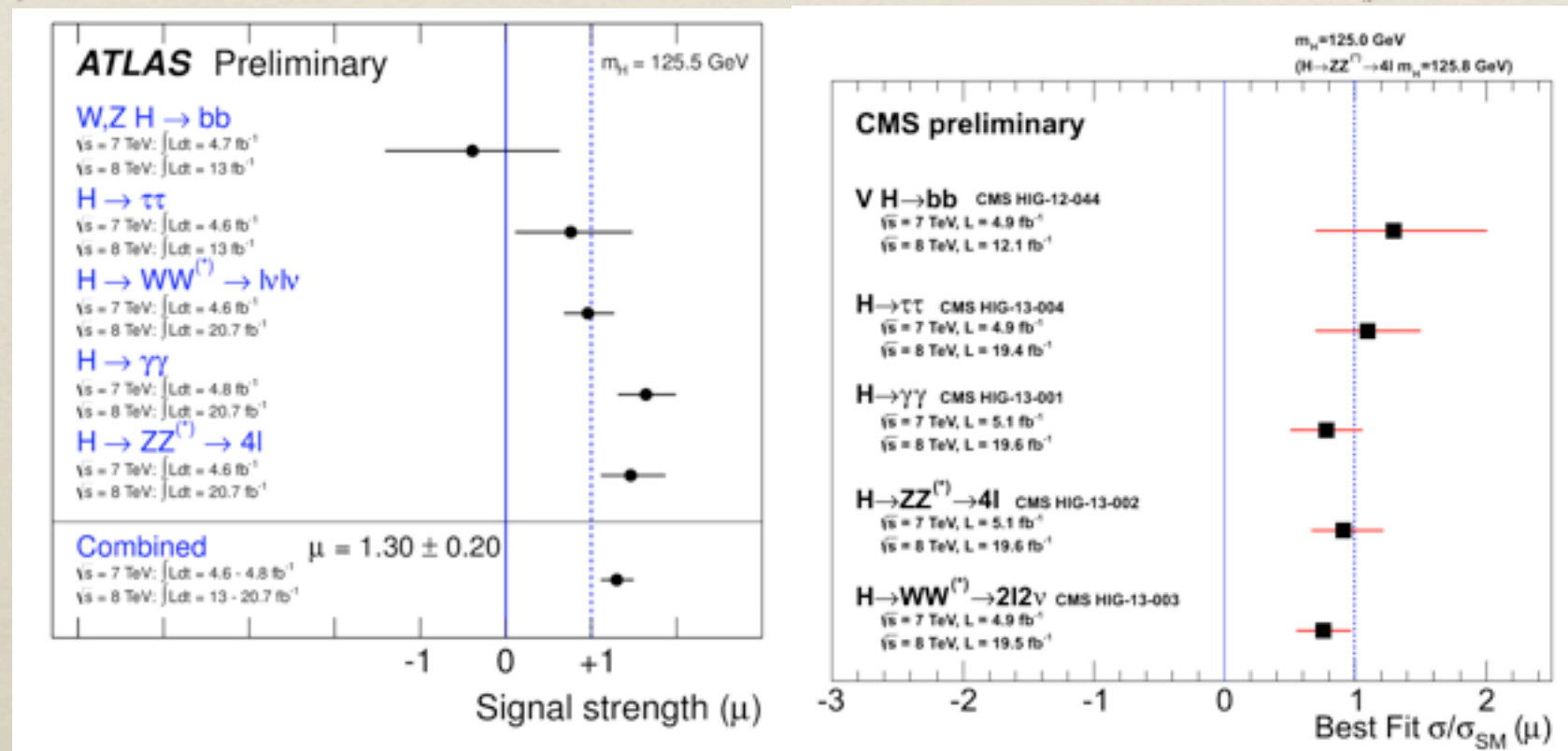
- To make higher order correction feasible, approximate top quark loop by effective  $ggH$  vertex
- Similarly, photon couples to Higgs through top quark and  $W$  boson loop, can also be approximated by effective  $\gamma\gamma H$  vertex

SM :  $b_{g,\gamma} = \frac{2}{3}, \frac{47}{9}$  at LO in heavy top/W limit

$$\mathcal{L} = - \left[ \frac{\alpha_s}{8\pi} \underbrace{c_g}_{\text{new physics correction}} b_g G_{a,\mu\nu} G_a^{\mu\nu} + \frac{\alpha}{8\pi} \underbrace{c_\gamma}_{\text{new physics correction}} b_\gamma F_{\mu\nu} F^{\mu\nu} \right] \frac{h}{v}$$



# Higgs Decay



- For  $m_H \sim 125 \text{ GeV}$ , Higgs resonance is weak
- Diphoton decay
  - excellent experimental photon energy resolution  $\Rightarrow \gamma\gamma$  signal visible even though  $\text{Br}(H \rightarrow \gamma\gamma) \sim 0.0023$
  - fully reconstructed invariant mass
- large SM background
- data in reasonable agreement with SM prediction
- Additional invisible/ undetectable decay channels could increase Higgs total width and reduce  $\gamma\gamma$  BR



# Full Diphoton Amplitude

- *Gluon pair to diphoton full amplitude*

$$\mathcal{A}_{gg \rightarrow \gamma\gamma} = -\frac{\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H}}{M_{\gamma\gamma}^2 - m_H^2 + im_H \Gamma_H} + \mathcal{A}_{\text{cont}}$$

$$\begin{aligned} \mathcal{A}_{gg \rightarrow H} &\propto c_g \\ \mathcal{A}_{\gamma\gamma \rightarrow H} &\propto c_\gamma \end{aligned}$$

- *Higgs signal appears as resonance in diphoton invariant mass  $M_{\gamma\gamma}$  spectrum*

$$S \sim |\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H}|^2$$

- *Signal strength in narrow width approximation*

$$\sigma^{\text{sig}} = \int dM_{\gamma\gamma} \frac{S}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2} \sim \frac{c_g^2 c_\gamma^2}{\Gamma_H} \rightarrow \text{Always appears as a combo!}$$

- *In SM, all Higgs properties dictated by  $m_H$ , how well can we test them at LHC?*

- *Need to decouple width from couplings in LHC*



# Interference

$$\left[ \begin{array}{c} g \\ t, b \\ g \end{array} \right] \rightarrow H \rightarrow \left[ \begin{array}{c} \gamma \\ W, t \\ b, c, \tau \\ \gamma \end{array} \right] + \dots$$

$$\times \left[ \begin{array}{c} \gamma \\ b, c, \dots \\ \gamma \end{array} \right] + \left[ \begin{array}{c} \gamma \\ u, c, d, s, b \\ \gamma \end{array} \right] + \dots$$

L.Dixon, M.Siu, hep-ph/0302233

- *The interference contribution*

$$-2m_H\Gamma_H \frac{\text{Im}(\mathcal{A}_{gg\rightarrow H}\mathcal{A}_{\gamma\gamma\rightarrow H}\mathcal{A}_{\text{cont}}^*)}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2\Gamma_H^2} - 2(M_{\gamma\gamma}^2 - m_H^2) \frac{\text{Re}(\mathcal{A}_{gg\rightarrow H}\mathcal{A}_{\gamma\gamma\rightarrow H}\mathcal{A}_{\text{cont}}^*)}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2\Gamma_H^2}$$

- *Integrated cross section of interference term has **different** dependence on total width: suppressed by small Higgs width w.r.t pure signal*

$$\sigma^{\text{int}} = \int dM_{\gamma\gamma} \frac{(M_{\gamma\gamma}^2 - m_H^2)R + m_H\Gamma_H I}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2\Gamma_H^2} \sim c_g c_\gamma$$

$$R \sim \text{Re}(\mathcal{A}_{gg\rightarrow H}\mathcal{A}_{\gamma\gamma\rightarrow H}\mathcal{A}_{\text{cont}}^*)$$

$$I \sim \text{Im}(\mathcal{A}_{gg\rightarrow H}\mathcal{A}_{\gamma\gamma\rightarrow H}\mathcal{A}_{\text{cont}}^*)$$



# Interference

- *Interference has two pieces*

$$R \sim \text{Re}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$$
$$I \sim \text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$$

$$\sigma^{\text{int}} = \int dM_{\gamma\gamma} \frac{(M_{\gamma\gamma}^2 - m_H^2)R + m_H \Gamma_H I}{(M_{\gamma\gamma}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2} \sim c_g c_\gamma$$

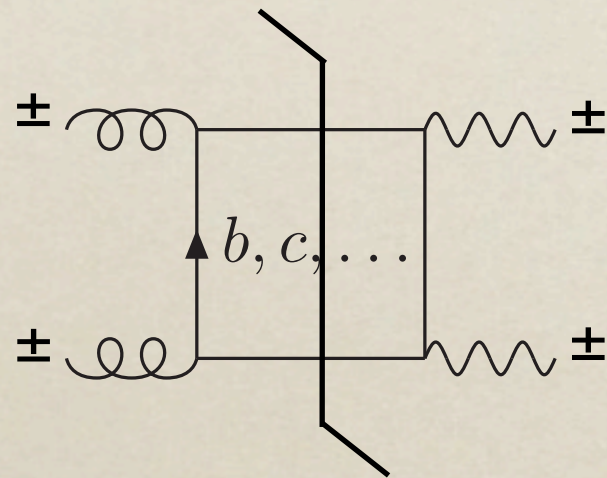
D.Dicus, S.Willenbrock, Phys.Rev.D37,1801

- *Real part of Breit-Wigner: asymmetric around Higgs peak, negligible contribution to integrated cross section given that R doesn't vary too quickly*
- *Imaginary part of Breit-Wigner: constructive or destructive depending on the relative phase between signal and background*



# Imaginary part of Interference

$$\mathcal{A}^{\text{tree}}(g^\pm g^\pm \rightarrow q\bar{q}) = \mathcal{A}^{\text{tree}}(q\bar{q} \rightarrow \gamma^\pm \gamma^\pm) = 0 \text{ for } m_q = 0$$



$$I \sim \text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{\gamma\gamma \rightarrow H} \mathcal{A}_{\text{cont}}^*)$$

- *The full  $ggH$  and  $\gamma\gamma H$  amplitudes are dominantly real for  $m_H < 2m_t, 2m_W$  as top and  $W$  contribute most to the effective couplings; small imaginary part from light quark loops is suppressed by Yukawa couplings*
- *Need imaginary part from SM background for the relative phase*
- *SM continuum contribution starts at 1-loop*
  - *vanishing imaginary part in massless quark limit at LO*
- *2-loop imaginary part leads to 1-2% destructive interference*
- *Too small an effect to see ...*

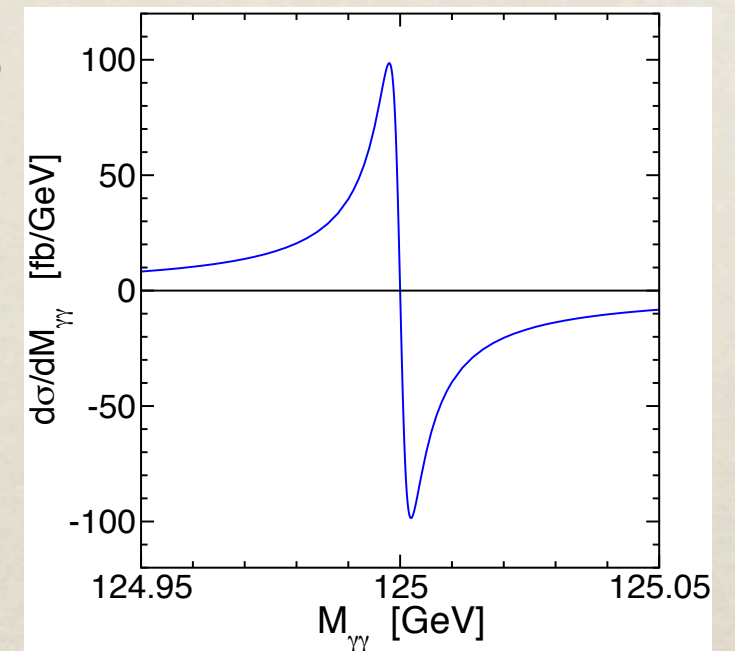
*Theoretical uncertainty on signal ~15%*



# LO Mass Shift

*Interference only (LO)*

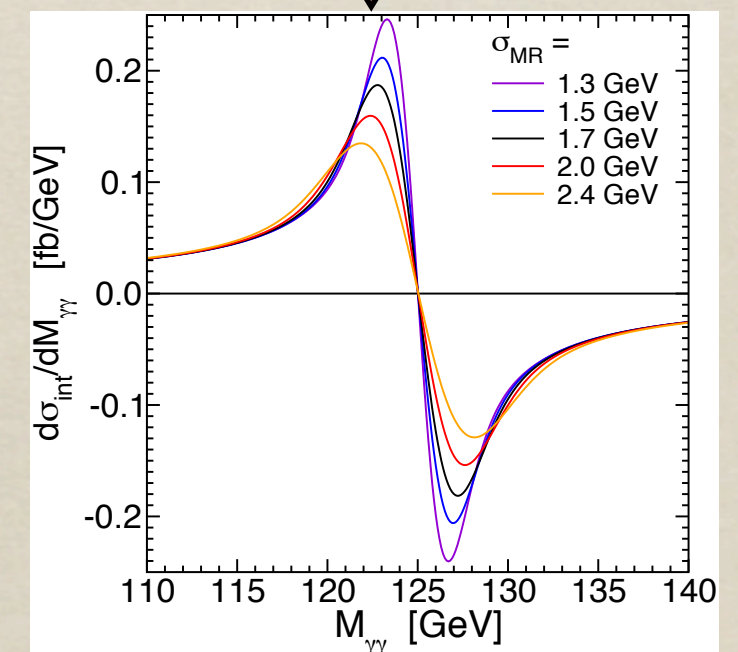
- *Real-part interference*
  - *non-vanishing at 1-loop with massless quarks*
  - *odd around Higgs mass  $\Rightarrow$  Higgs mass peak shift*
  - *generically, asymmetric shape peaks/dips at  $m_H \pm \Gamma_H/2 \Rightarrow$  mass shift  $\sim \Gamma_H$*



S.Martin, hep-ph/1208.1533

- *Different story when including effect of finite detector resolution*

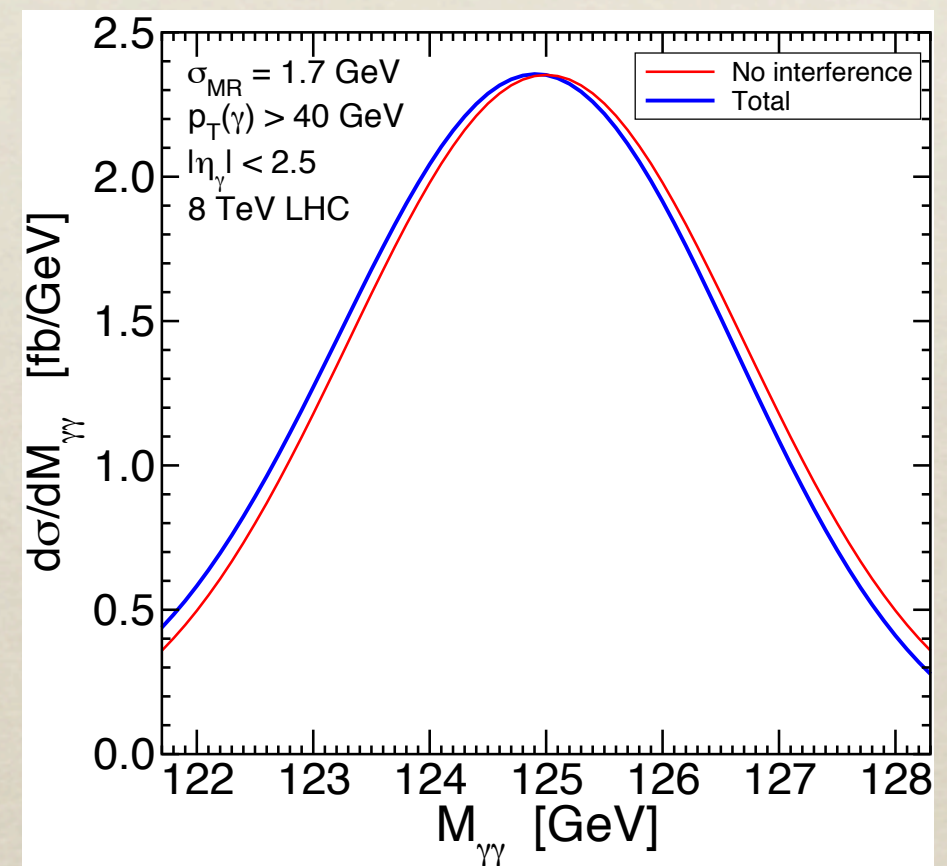
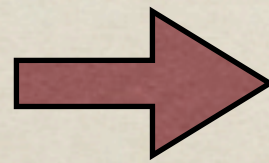
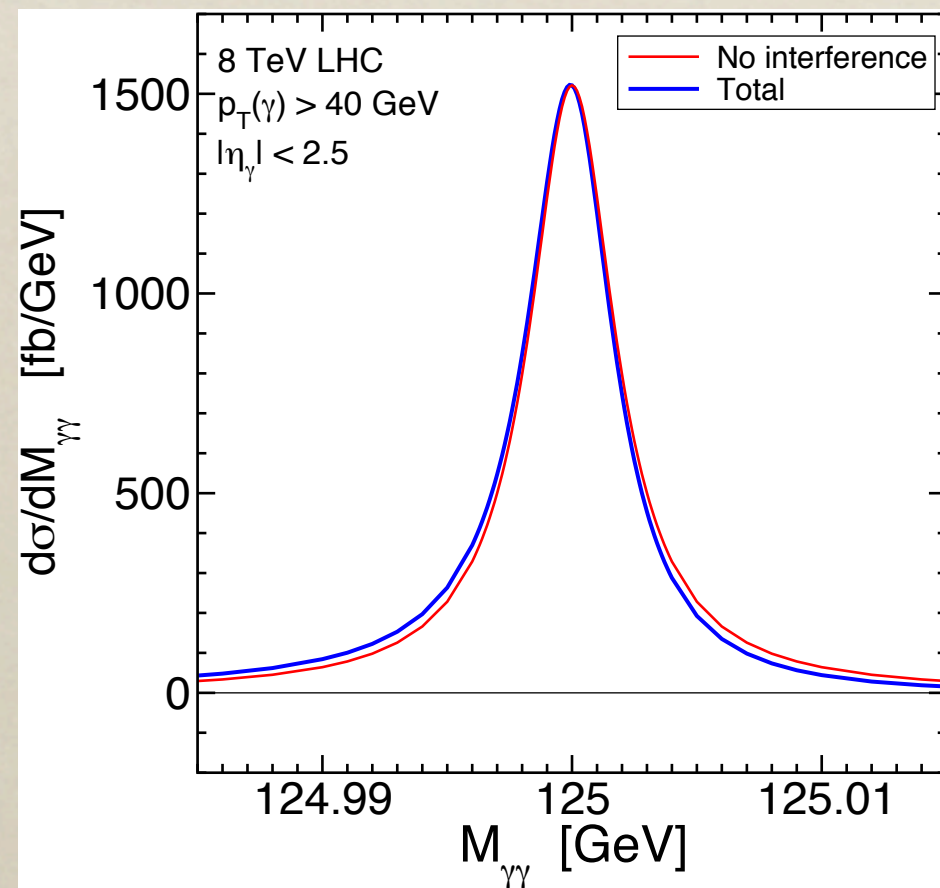
- *considerable contribution from Breit-Wigner tails*
- *potentially visible shift of Higgs mass peak  $\sim 100$  MeV*





# LO Mass Shift

S.Martin, hep-ph/1303.3342

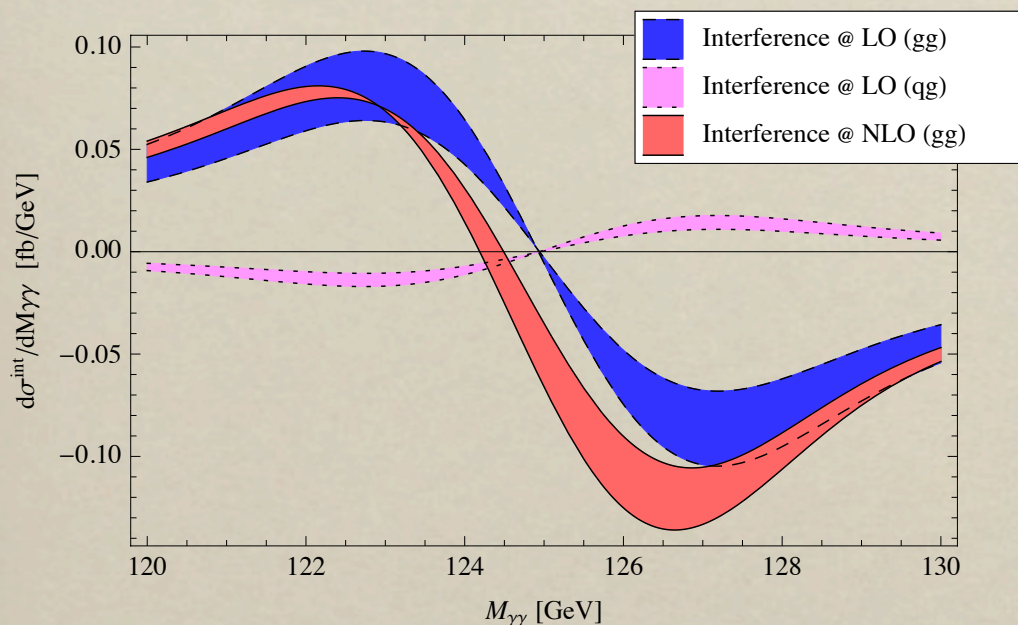
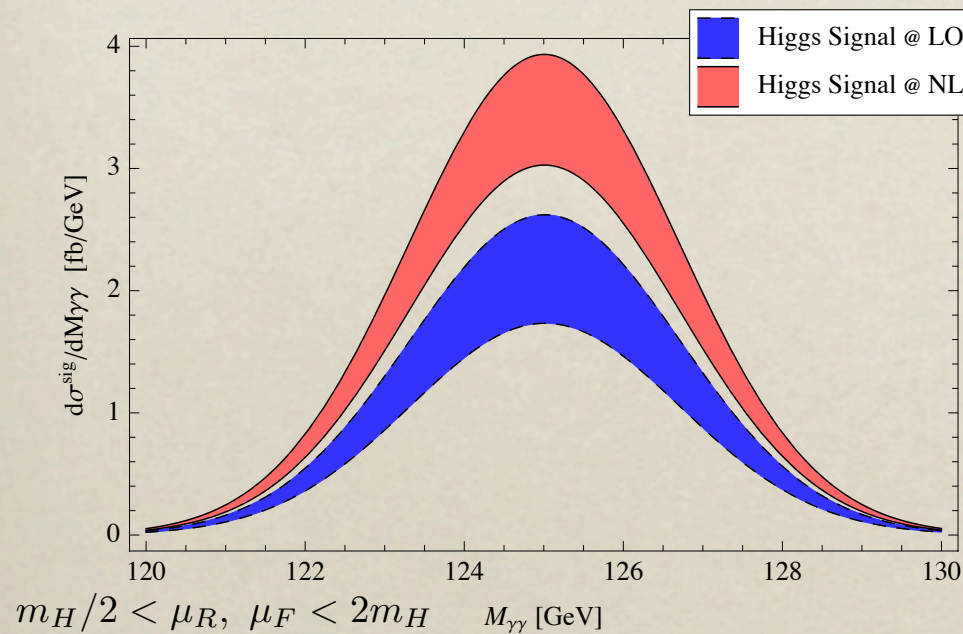




# NLO QCD Correction

LHC @ 8 TeV

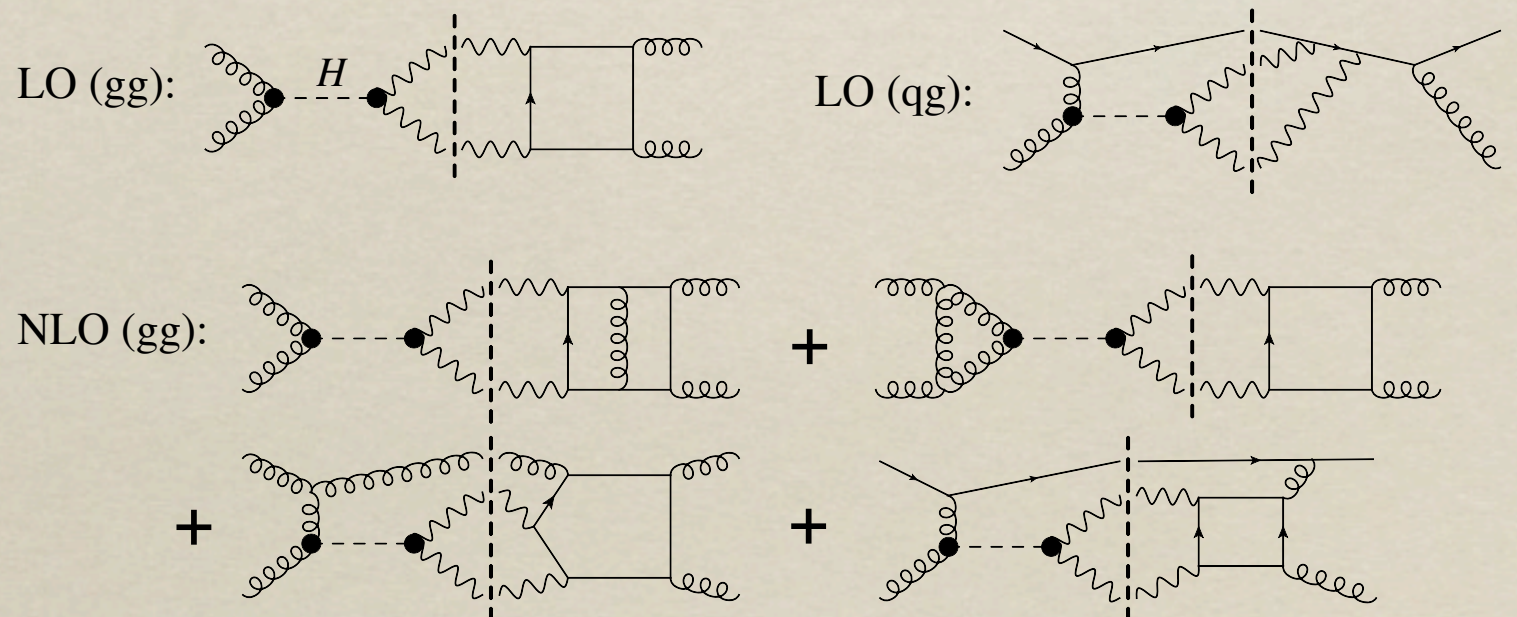
$\sigma_{MR} = 1.7 \text{ GeV}$



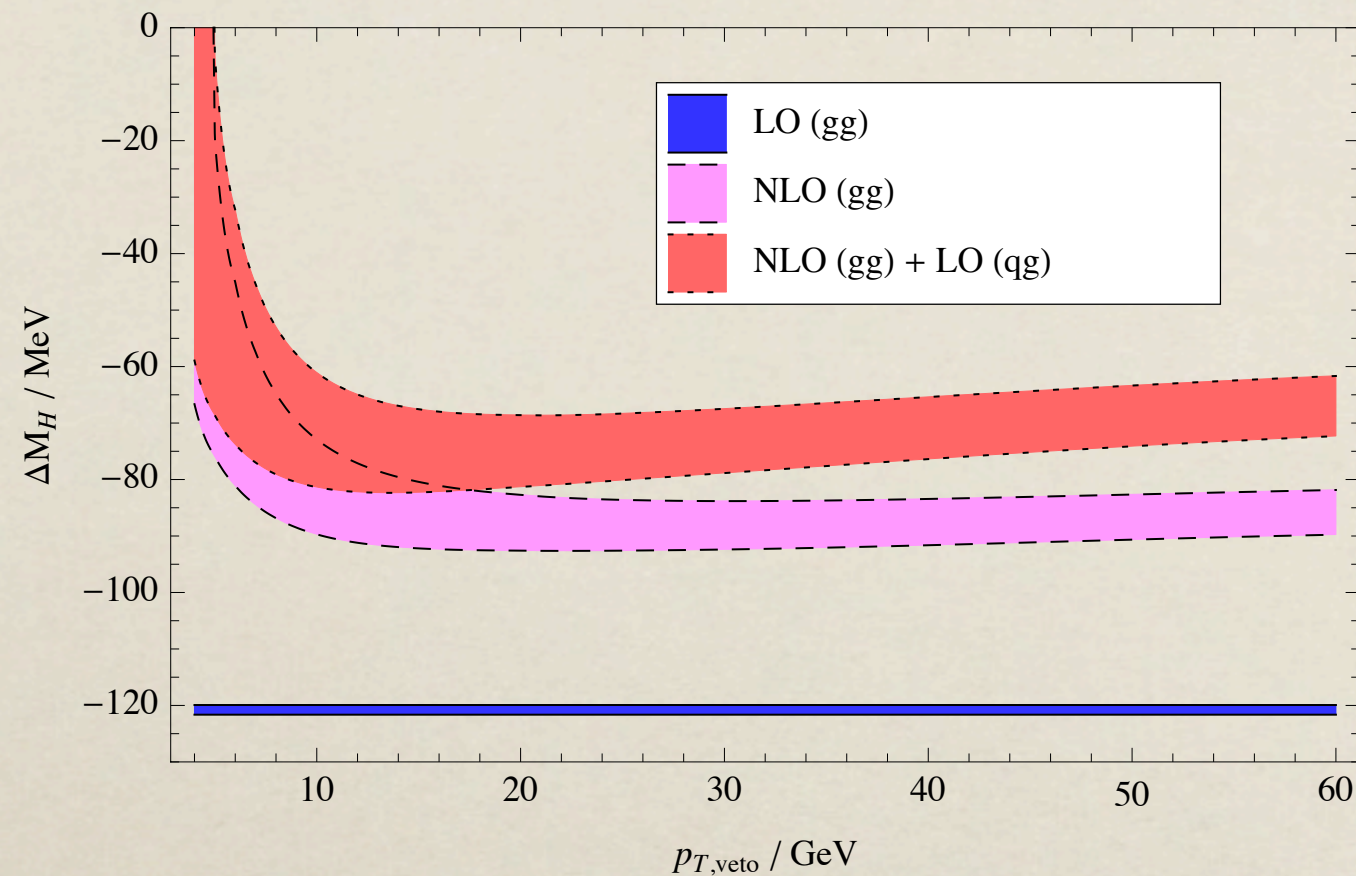
$p_{T,\gamma}^{\text{hard/soft}} > 40/30 \text{ GeV}, |\eta_\gamma| < 2.5$   
 Isolation:  $\Delta R_{\gamma j} < 0.4, p_{T,j} > 3 \text{ GeV}$   
 Veto jet :  $p_{T,j} > 20 \text{ GeV}, \eta_j < 3$

Known large  $K$  factor of Higgs production and SM background in QCD at NLO

- more uncertainty when  $p_T$  veto is involved
- Interplay between real and imaginary part of the interference leads to  $K$  factor depending on  $M_{\gamma\gamma}$ 
  - imaginary part interference starts at 2-loop and is small
  - real part interference receives a relative constant  $K$  factor ( $\sim 2$  for inclusive case) between that of pure signal ( $\sim 2.5$ ) and background ( $\sim 1.5$ )







- *smaller background K factor  $\Rightarrow$  reduced mass shift*
- *with radiation, the extra contribution from the interference with tree level diagram in quark gluon channel,  $LO(qg)$ , partly cancels with interference of gluon gluon channel,  $(N)LO(gg) \Rightarrow$  further reduces mass shift*
- *mostly insensitive to  $p_T$  veto choice because of large contribution from virtual correction*

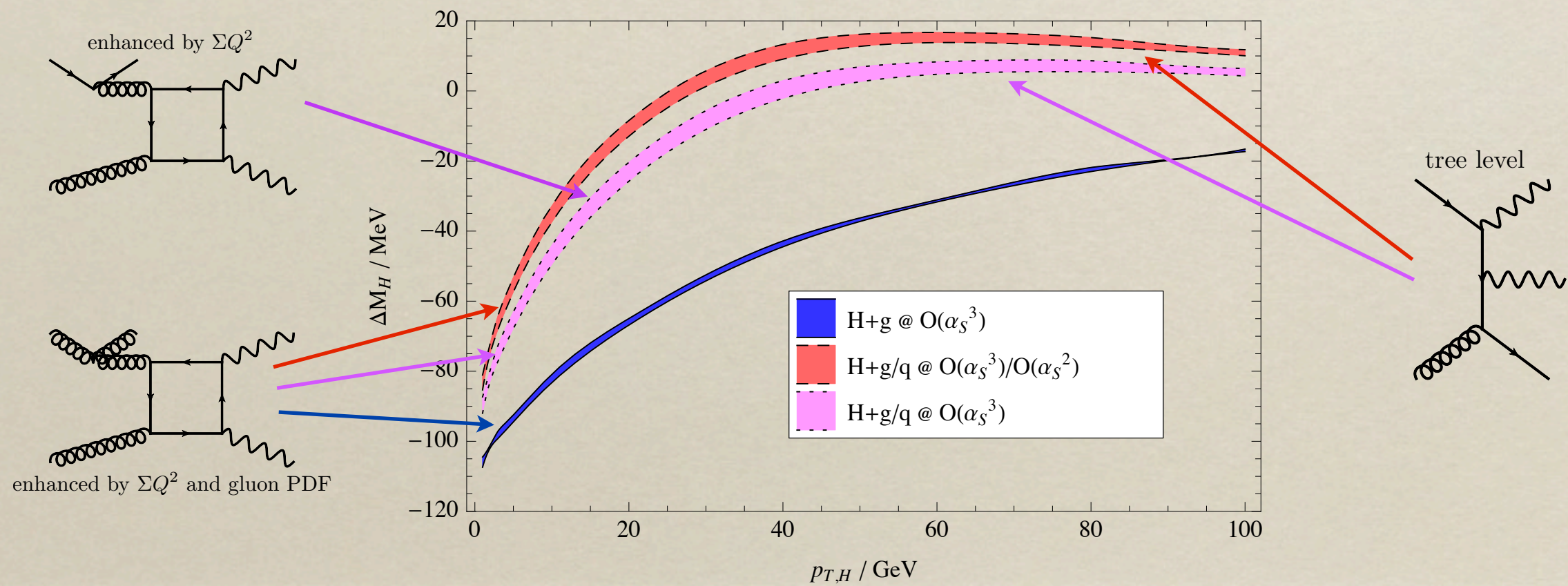


# Probing Mass Shift

- *Need a reference channel to measure the shift:*
  - *ZZ\* channel where interference near Higgs resonance is negligible*
  - *do it within  $\gamma\gamma$  channel alone?*
- *Cancellation between  $qg$  and  $gg$  channels results in strong dependence on Higgs  $p_T$*
- *Potentially observable with high luminosity data: better choice because experimental systematic uncertainty may cancel to some extent*

N.Kauer, G.Passarino, hep-ph/1206.4803

S.Martin, hep-ph/1303.3342





# Bounding Higgs Width

- *Mass shift sensitive to Higgs width due to modified couplings*

- *must keep constant signal yields to be consistent with current experimental observation*

$$c_{g\gamma} = c_g c_\gamma \rightarrow \frac{c_{g\gamma}^2 S(m_H)}{\Gamma_H} + c_{g\gamma} I(m_H) = \frac{S(m_H)}{\Gamma_H^{SM}} + I(m_H)$$

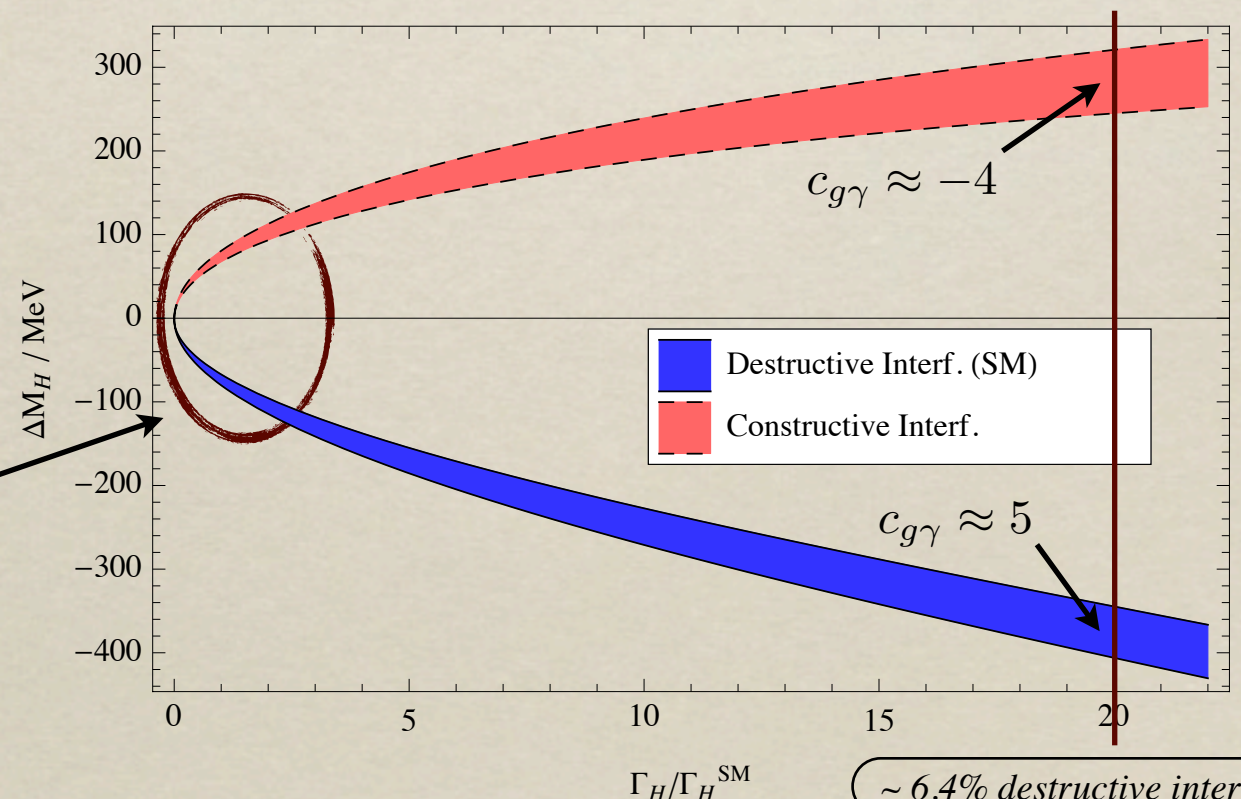
- *simple solution if vanishing destructive (constructive) interference*

$$|c_{g\gamma}| = \sqrt{\Gamma_H / \Gamma_H^{SM}}$$

- *In case NP flips the sign of Higgs amplitude  $\Rightarrow$  Constructive Interference*

- *Constrain/determine Higgs width!*

*~ 8% constructive interference*





# Recap

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- *The interference of Higgs signal and SM continuum background survives at NLO, allowing the width to be measured separately from couplings experimentally*
- *Part of interference proportional to real part of BW propagator yields potentially observable mass shift with finite detector resolution*
- *Strong dependence of mass shift on finite Higgs  $p_T$  provides way of detecting without reference to  $ZZ^*$*
- *Increasing Higgs width leads to considerably larger mass shift and enhanced constructive/destructive interference*



# Other Scenarios

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- *The discussion so far applies to any CP-even spin-0 particles that couples to photons and gluons similar to SM Higgs*
- *Could the observed “Higgs” be in a mixed state of CP, or even a spin-2 particle?*
  - *Interference could modify angular distribution of diphoton final states*
  - *Possible large constructive/destructive interference to signal strength*



# Higgs in Mixed CP State

- *New CP-odd couplings in the effective Lagrangian*

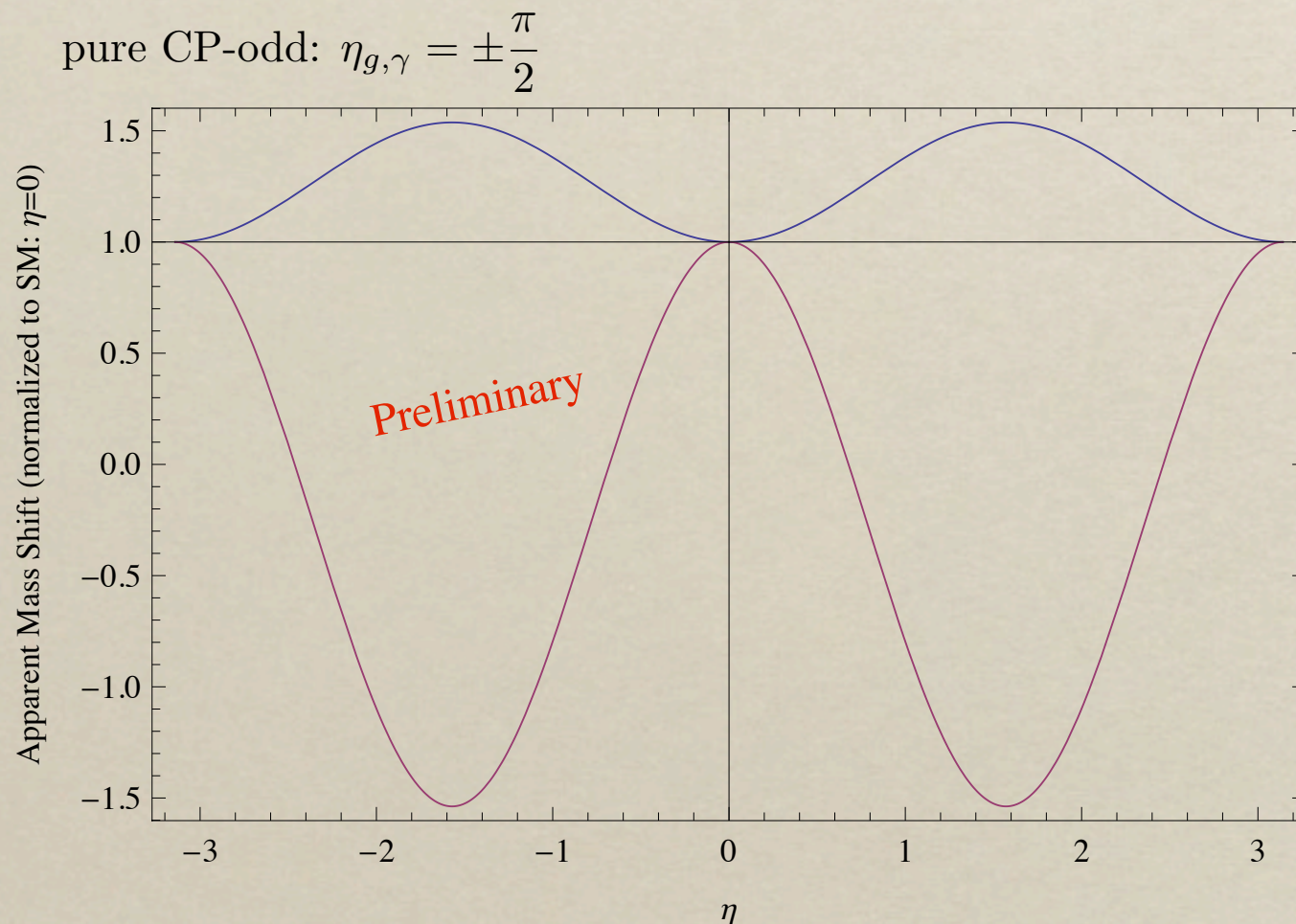
$$\mathcal{L} = - \left[ \frac{\alpha_s}{8\pi} (c_g b_g G_{a,\mu\nu} G_a^{\mu\nu} + s_g d_g G_{a,\mu\nu} \tilde{G}_a^{\mu\nu}) + \frac{\alpha}{8\pi} (c_\gamma b_\gamma F_{\mu\nu} F^{\mu\nu} + s_\gamma d_\gamma F_{\mu\nu} \tilde{F}^{\mu\nu}) \right] \frac{h}{v}$$

- *In SM,  $c_{g/\gamma}=1$  is reserved for adjusting couplings for Higgs in mixed CP state;  $b_{g/\gamma}$  is given via matching from full theory;  $s_{g/\gamma}d_{g/\gamma}=0$  when Higgs is a CP-even scalar*
- *$s_{g/\gamma}$  is reserved for the same purpose as  $c_{g/\gamma}$*
- *Define  $d_{g/\gamma}$  so that when we turn off original CP-even coupling ( $c_{g/\gamma}b_{g/\gamma}=0$ ) and set  $s_{g/\gamma}=1$ , the total cross section of SM Higgs signal is reproduced  $\Rightarrow d_{g/\gamma} = b_{g/\gamma}$  at LO*



# Higgs in CP Mixed State

- To keep constant signal yield, it's not hard to find the solution:  $c_{g/\gamma}^2 + s_{g/\gamma}^2 = 1$ , naturally parametrized as  $c_{g/\gamma}, s_{g/\gamma} = \cos(\eta_{g/\gamma}), \sin(\eta_{g/\gamma})$ 
  - If we treat the two CP phases  $(\eta_g, \eta_\gamma)$  independently, the interference could change signs, resulting in positive mass shift
  - The mass shift is roughly 1.5 times stronger in pure CP-odd case compared to CP-even case at LO, though CP-odd case strongly disfavored experimentally



- NLO effect is hard to tell (depending on the full theory giving rise to the CP-odd couplings) but is expected to increase signal and interference both as in the SM case

$$\begin{aligned} \text{--- } \eta &= \eta_g = \eta_\gamma \\ \text{--- } \eta &= \eta_g = -\eta_\gamma \end{aligned}$$

$$\mathcal{A}(g^\pm g^\pm H) = (c_g \pm i s_g) \mathcal{A}^{\text{SM}}(g^\pm g^\pm H)$$

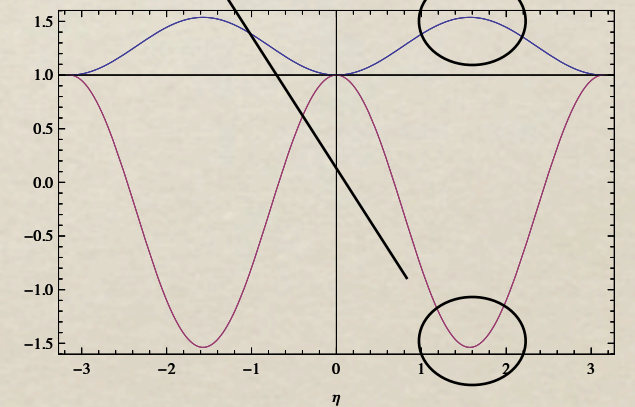
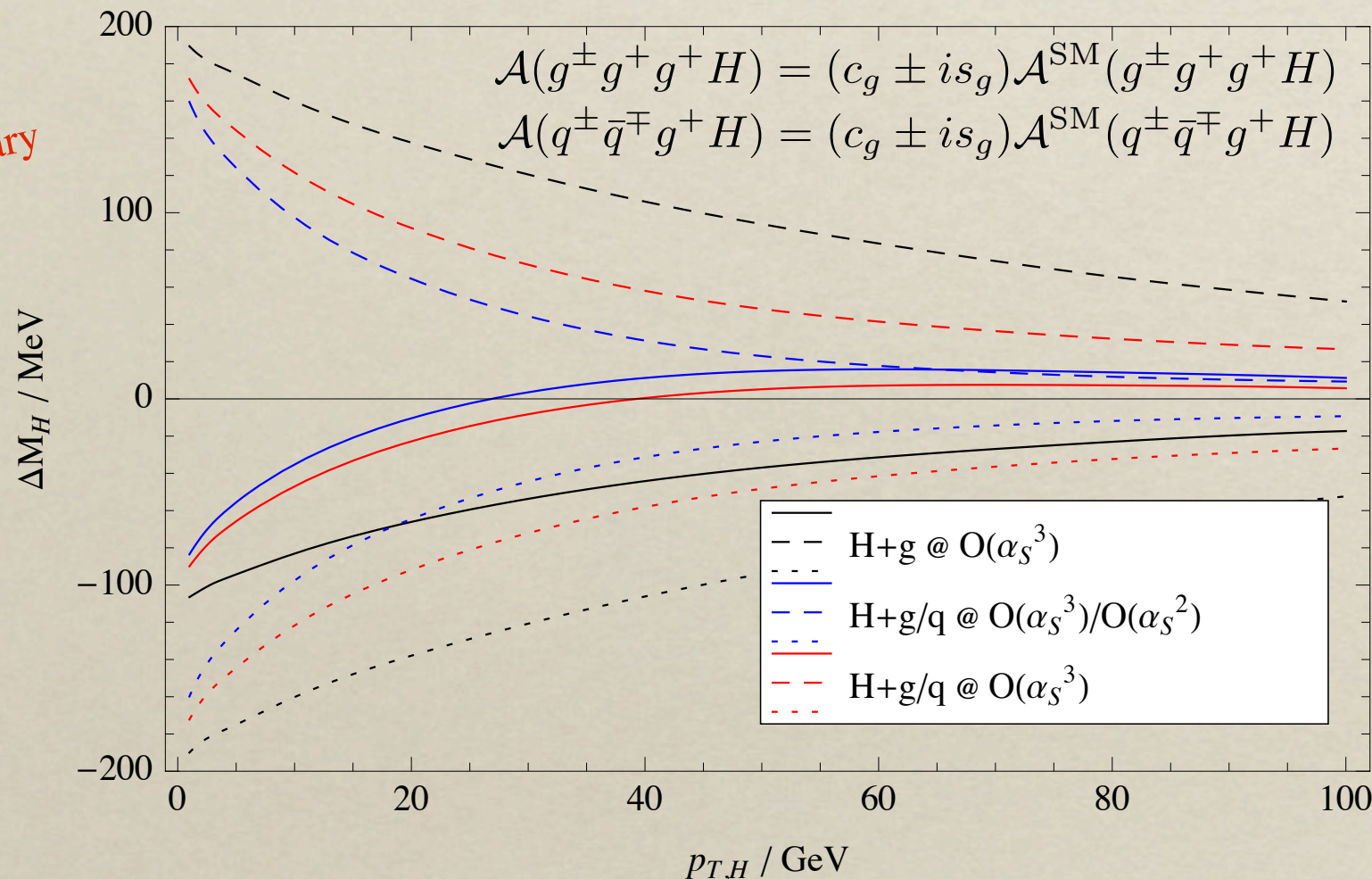
$$\mathcal{A}(\gamma^\pm \gamma^\pm H) = (c_\gamma \pm i s_\gamma) \mathcal{A}^{\text{SM}}(\gamma^\pm \gamma^\pm H)$$



# Higgs with Finite pT

- The mass shift dependence of finite pT as CP phases vary has similar behavior to the zero pT case
  - solid line is for SM; dotted line is for  $c_{g/\gamma}=0, s_g=s_\gamma=1$ ; dashed line is for  $c_{g/\gamma}=0, s_g=-s_\gamma=1$
  - mass shift no longer crosses 0 in pure CP-odd case

Preliminary



tree level  
analysis  
only



# Higgs with Spin-2

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- *The interference btw signal and background occurs with different helicity configurations (compared to spin-0 case)*
  - *Gluon and photon pairs have opposite helicity due to spin conservation*
  - *Thus non-vanishing imaginary part of SM background amplitude in massless quark limit at LO*
- *Graviton-like: photon and gluon couples to spin-2 particle via stress energy tensor*
  - *Dictates couplings to photon and gluon with the same sign*
  - *Also discuss couplings with different signs here for completeness*
  - *Direct coupling of  $H$  to quarks not included as it's small for graviton-like case*



# Signal vs. Interference

$$\overline{|\mathcal{A}|^2} = \left[ \frac{G_{g\gamma}^2}{256} f_0(c) + \pi \xi M \Gamma f_i(c) \right] \frac{1}{(\hat{s} - M^2)^2 + M^2 \Gamma^2} + \xi f_r(c) \frac{\hat{s} - M^2}{(\hat{s} - M^2)^2 + M^2 \Gamma^2}, \quad c = \cos \theta$$

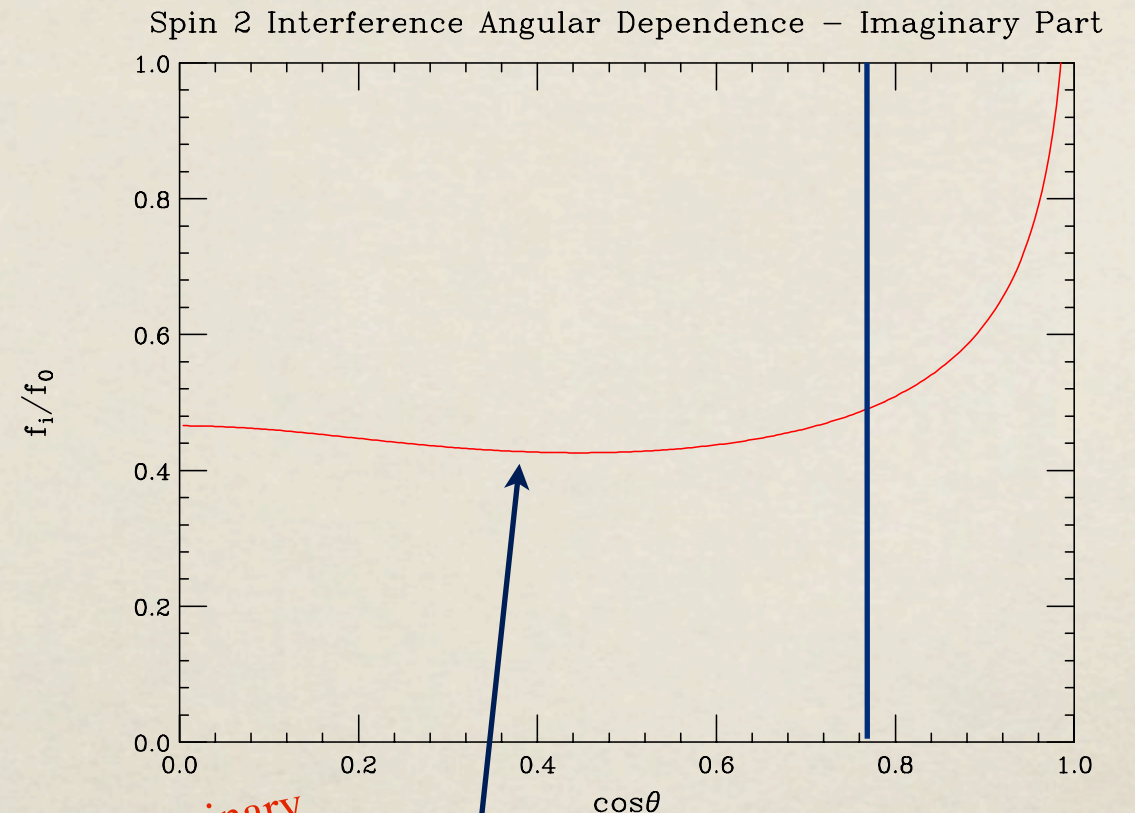
$$\xi = \frac{11}{72} G_{g\gamma} \alpha \alpha_s$$

- Normalize the spin-2 coupling so that signal yield is the same as the SM Higgs
- Need non-zero photon  $p_T$  cut for finite interference contribution in spin-2 case
- Choose  $p_{T\text{cut}} = 40 \text{ GeV}$  to solve for  $G_{g\gamma}$  by equating the yields for spin-0 and spin-2
- Moderate  $p_T$  cut (40 GeV) limits photon to central region where interference and signal has relatively similar angular dependence

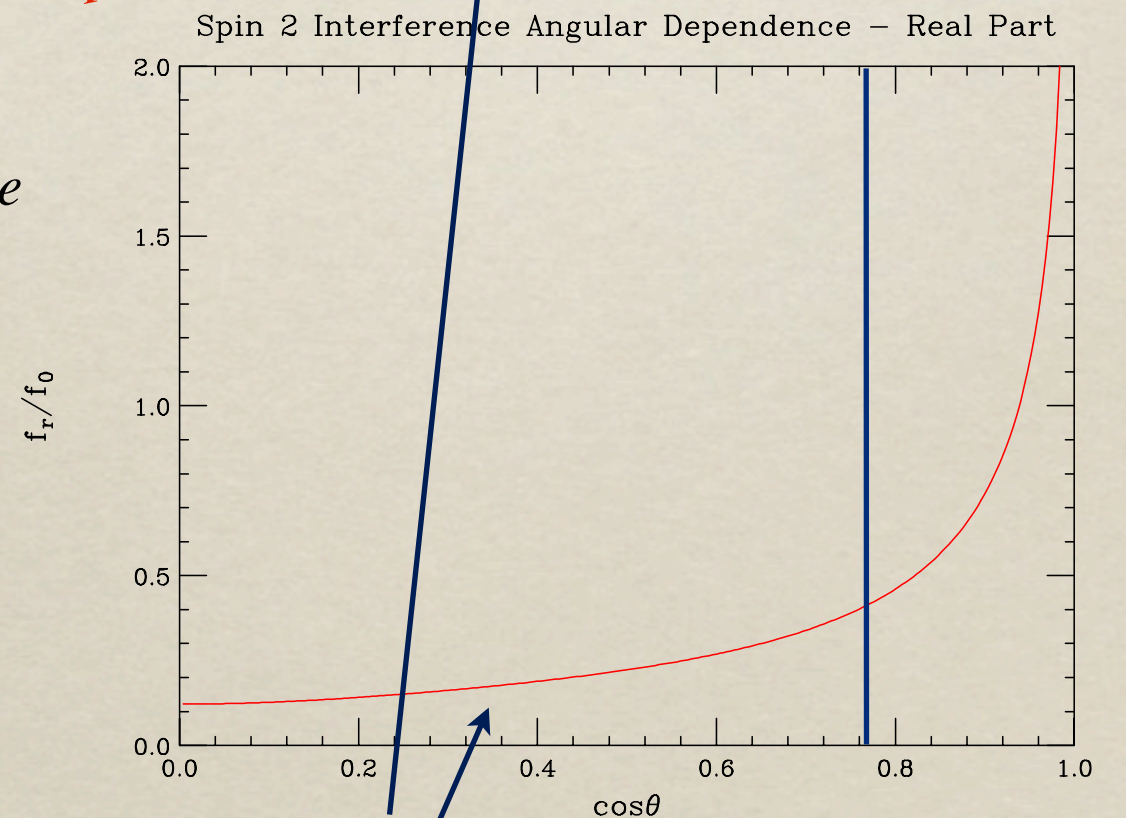
$$\cos \theta_{\max} = \sqrt{1 - 2(p_T^{\text{cut}}/M_{\gamma\gamma})^2} \xrightarrow{p_T^{\text{cut}}=40\text{GeV}} 0.77$$

- signal-only angular distribution analysis largely unaffected by interference contribution

$G_{g\gamma} > 0$  for heavy graviton



Preliminary



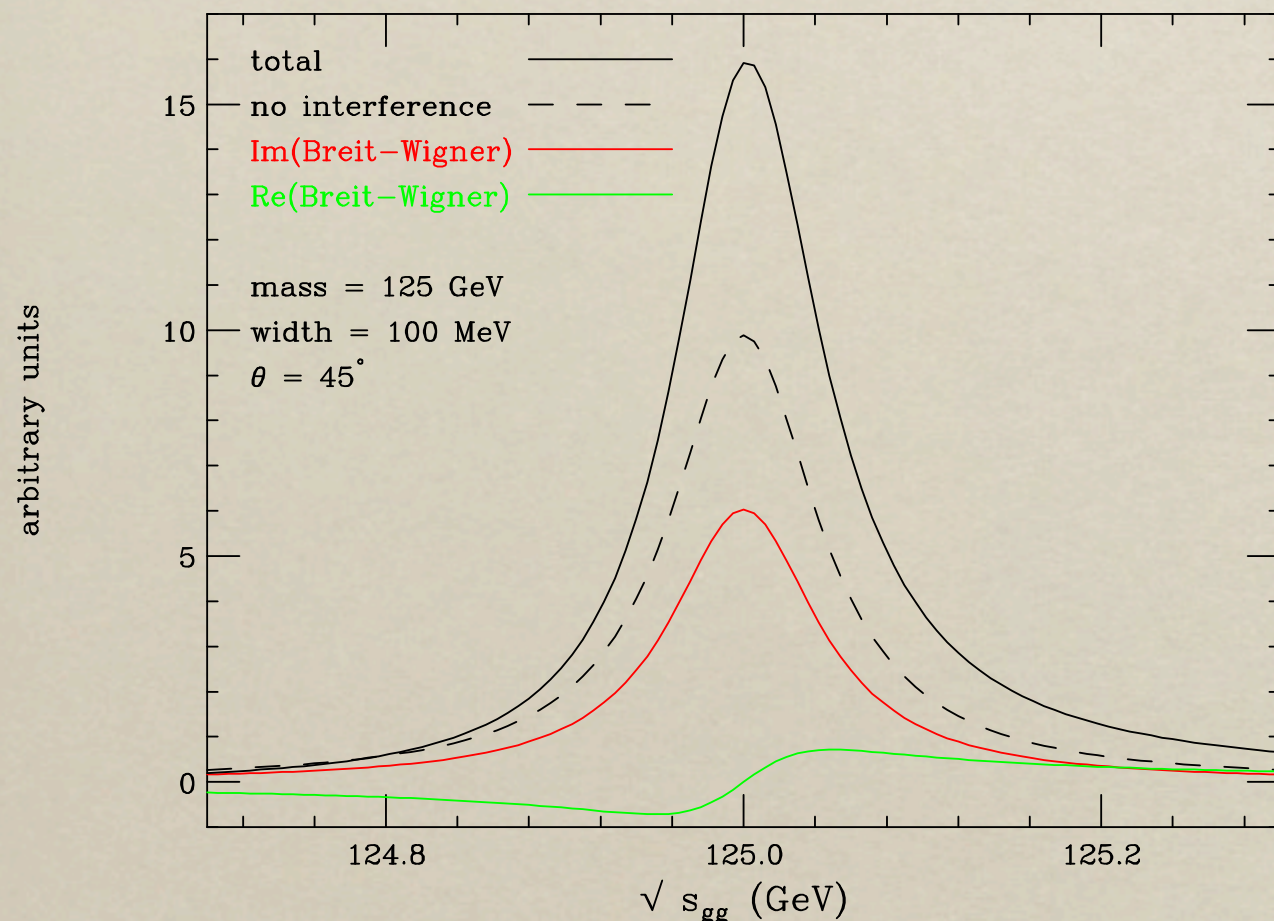
almost flat profile for small scattering angle



# Interference on Signal Yields (Spin-2)

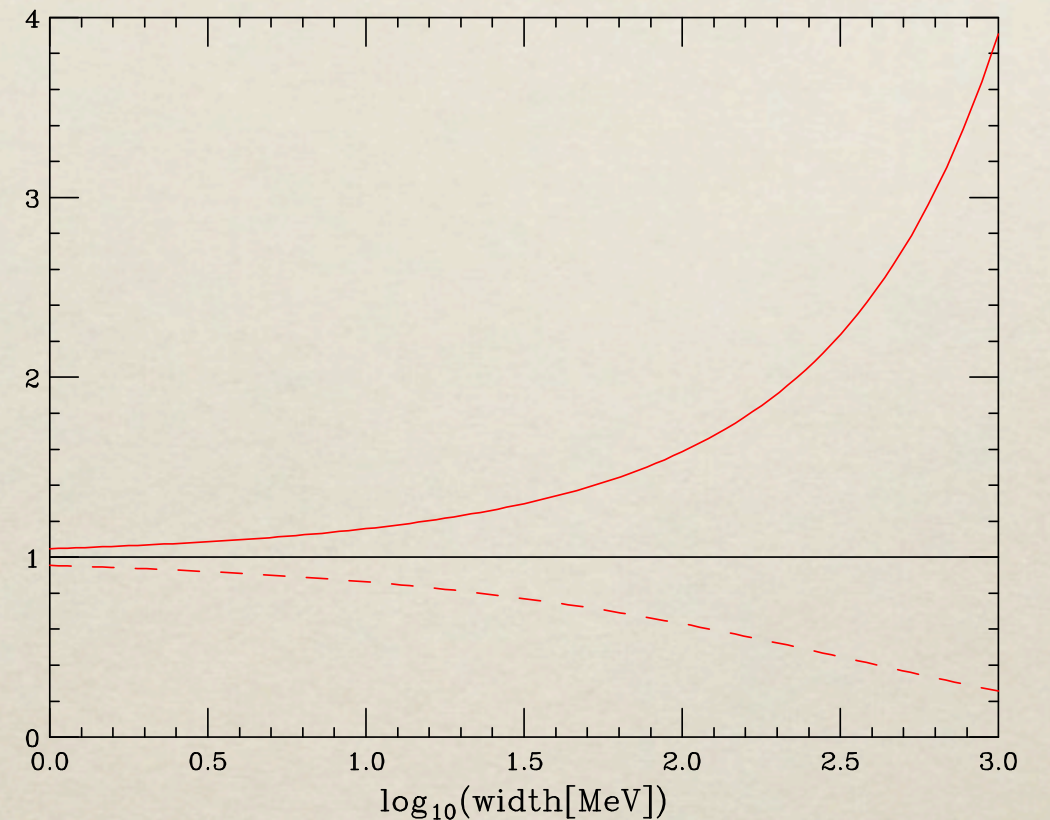
- Strong constructive/destructive interference at large width because imaginary part interference starts at LO

$gg \rightarrow G \rightarrow \gamma\gamma$  Lineshape



$R(p_T^\gamma > 40 \text{ GeV})$

Interference Correction to Event Rate



- for  $\Gamma = 100 \text{ MeV}$  :  $O(1)$  correction to signal yields ( $\sim 50\%$ )
- Affect the coupling measurement in spin-2 interpretation



# Future Work

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- *Continue study of interference with jets: important due to strong dependence on finite  $p_T$  in Higgs case*
  - *Calculation implemented in Sherpa for further angular correlation analysis*
  - *Higher order correction with resummation helpful for future precision studies*
- *What role interference plays in Higgs production via vector boson fusion?*
  - *most likely small but needs to be examined*



# Conclusion

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- *The interference in Higgs diphoton decay channel provides additional degree of freedom to constrain/measure Higgs width*
- *Interference can also be used to probe other properties of Higgs: spin, CP ...*



Backup slides

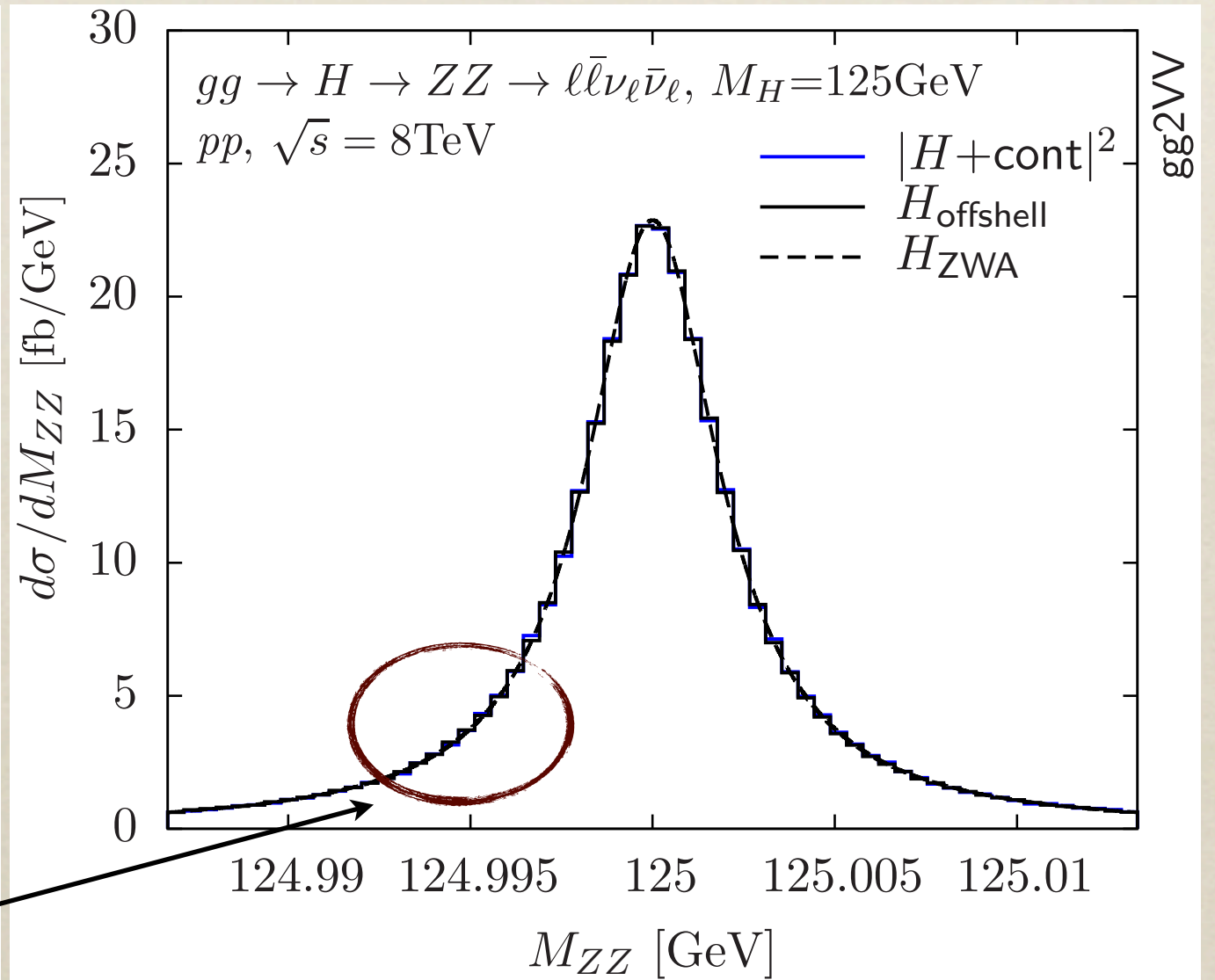
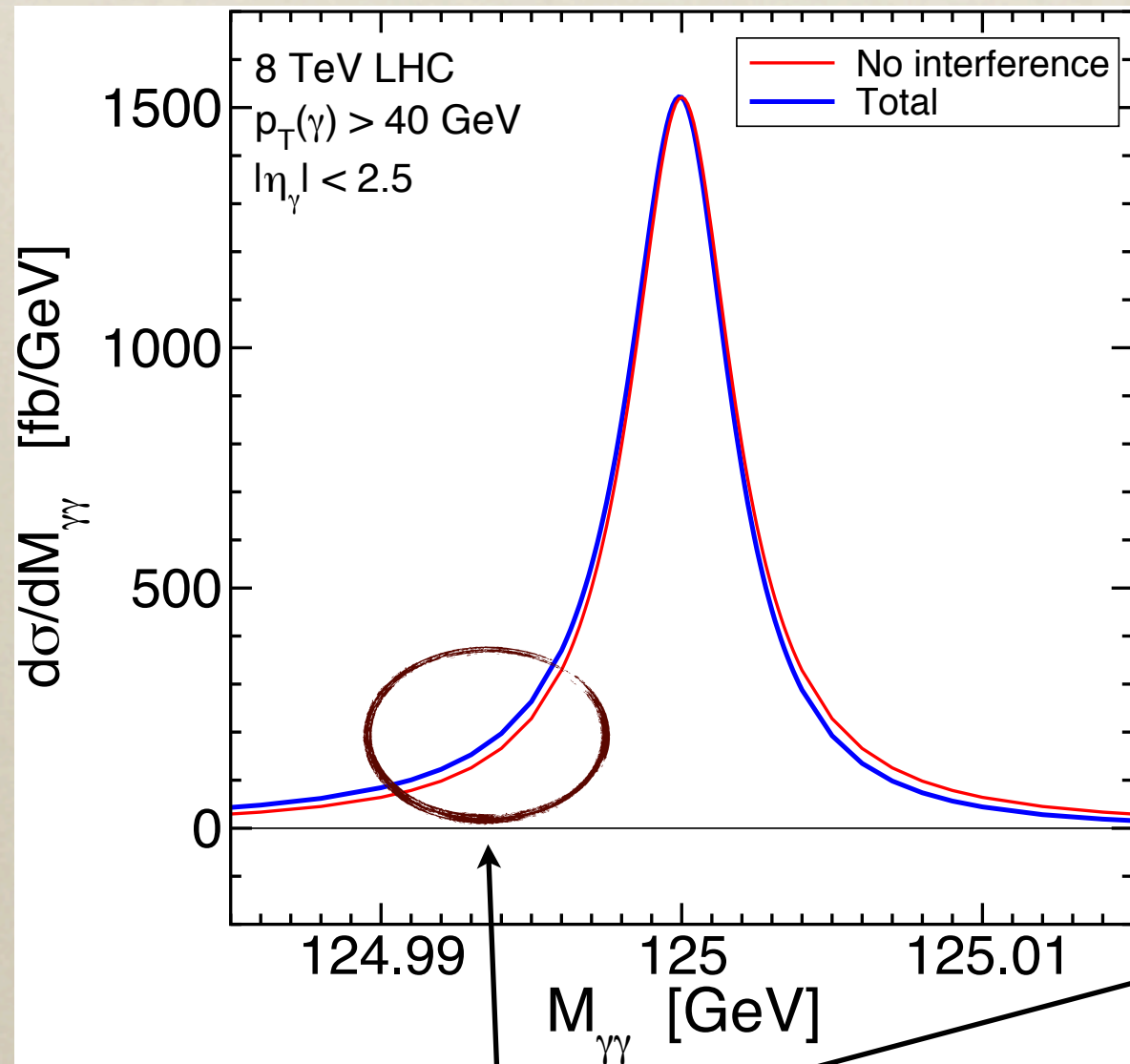




# Interference in ZZ and $\gamma\gamma$

S.Martin, hep-ph/1303.3342

N.Kauer, G.Passarino, hep-ph/1206.4803



*interference  
 in ZZ is very  
 small*

*The mass measurement can be approximated by a least square fit of the mass peak, which can be shown via likelihood analysis by assuming a relatively constant and well-modeled background in the mass range of consideration*