



# ***Study of Top Pair Production Near Threshold***

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# Targets

The targets of ILC around  $E_{cm}$  350 GeV !!

Today's  
topic

- 
1. top mass  
→ In Pole,  $\overline{MS}$  & potential subtracted schemes
  2. top width
  3. top yukawa coupling
  4.  $\alpha_s$
  5. QCD wave function of top pair system

# Top Yukawa, Mass & Width from $t\bar{t}$ Cross Section

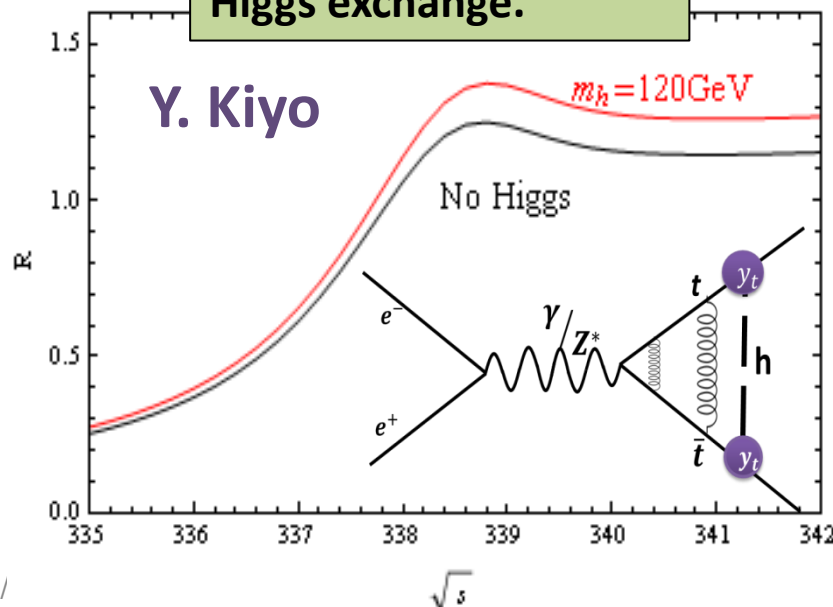
The total cross section of top pair production near threshold depends on following parameters. If we can measure the cross section precisely and fit it, fundamental parameters are determined !!

$$\sigma = f(\sqrt{s}, m_t, \Gamma_t, \alpha_s, m_h, y_t)$$

Especially, at near threshold we can define potential subtracted(PS) mass\*\* which is insensitive to long-distance physics.

\*\* [arXiv:hep-ph/9804241](https://arxiv.org/abs/hep-ph/9804241)

$\sigma$  enhancement due to Higgs exchange.



Contribution of Higgs exchange diagram to total cross section is about 9%.

So if we can measure total cross section precisely, we can extract **top Yukawa coupling** before going to  $E_{cm}=500\text{GeV}$ . (note. Current theoretical uncertainty in the cross section is about 4% and I hope this will be improved in coming 10 years)

# ***Condition of the Analysis***

# Simulation

Top mass (pole mass)

174 GeV

Ecm (using **threshold scan**)

340 - 350 GeV (every 1 GeV)

Polarization

$$\begin{aligned} (e^-, e^+) &= (-0.8, +0.3) \\ &\quad (+0.8, -0.3) \end{aligned}$$

Integrated luminosity

10 fb<sup>-1</sup> (each Ecm and polarization)

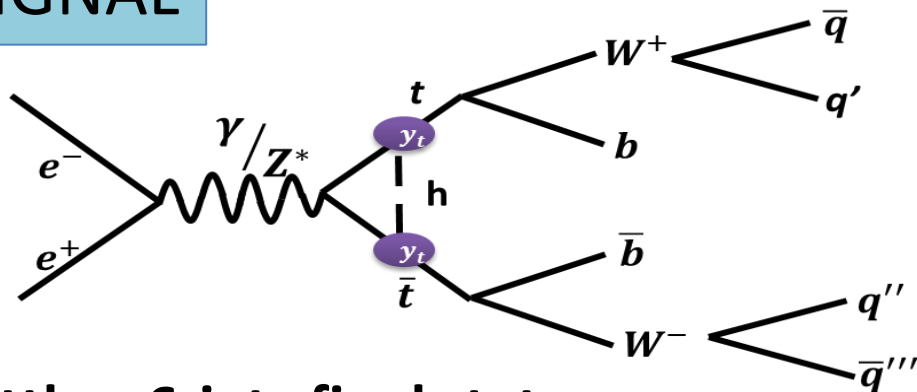
Top pair generator

Physsim  
(LO, On QCD enhancement,  
no higgs exchange, on ISR/beamstrahlung)

**Full simulation with the ILD detector is performed.**

# Signal and Background

## SIGNAL



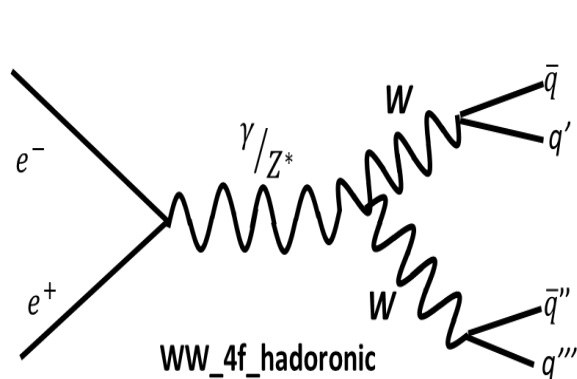
**ttbar 6-jets final state**

## Branching Ratio

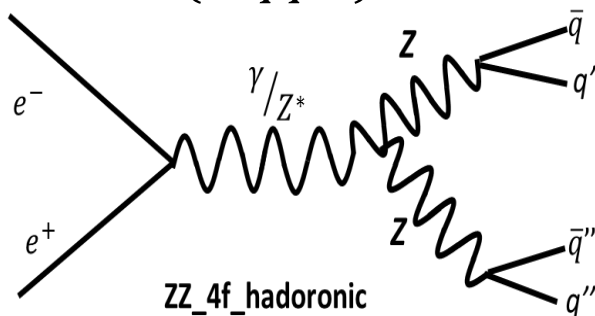
| Branching Ratio |     |
|-----------------|-----|
| 6-jets          | 45% |
| 4j1l1ν          | 44% |
| 2j2l2ν          | 11% |

## Main BG.

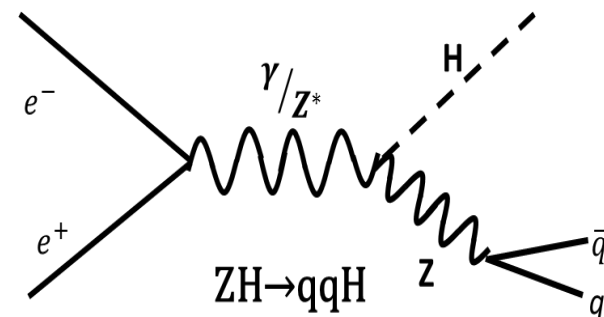
$ee \rightarrow WW (\rightarrow qq'q''q''')$   $q = (u, d, s, c, b)$   
 $\rightarrow ZZ (\rightarrow q\bar{q}q'\bar{q}')$   
 $\rightarrow ZH (\rightarrow qqH)$



WW\_4f\_hadronic



ZZ\_4f\_hadronic



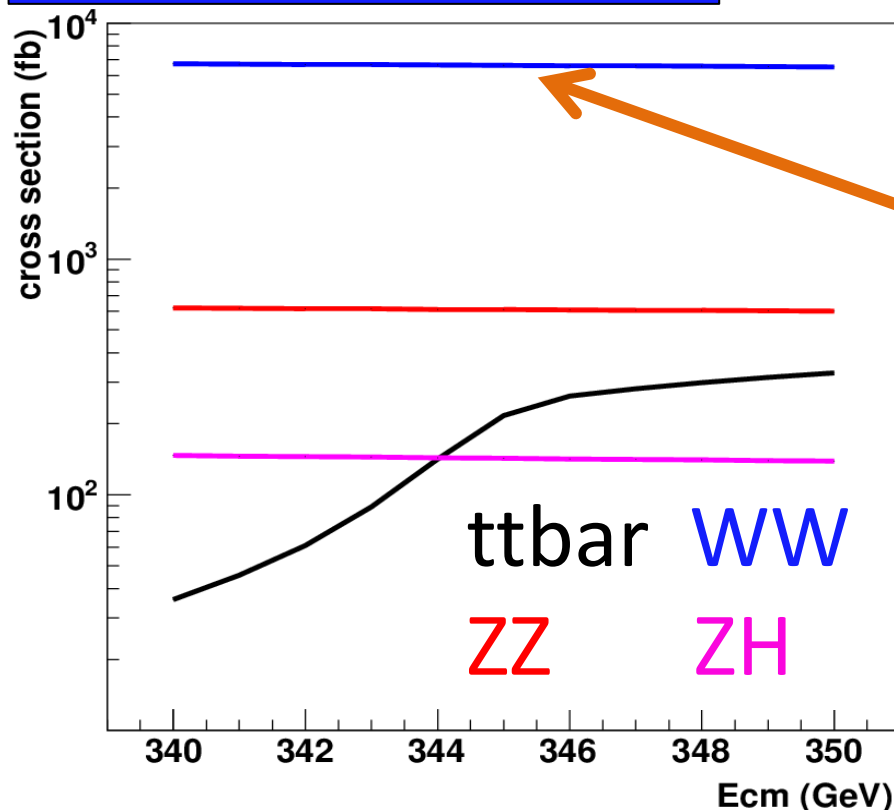
ZH→qqH

For future plan, we will add WWZ, ZZZ, tbW.

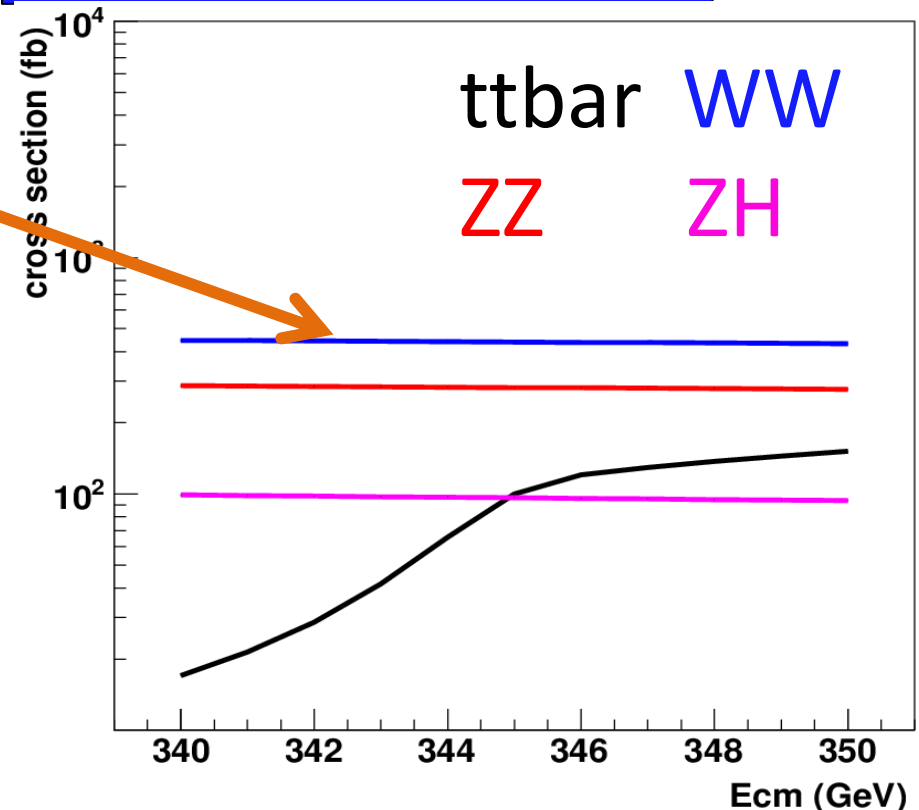
# Cross Section of $t\bar{t}$ and BG.

Since QCD theory is well-known at the threshold region, measuring the energy dependence of the cross section, we can determine the fundamental physics parameters. And since left-handed and right-handed top quarks have different SU(2) and U(1) charges, the cross section has difference between left- and right-handed polarizations.

Cross section ( $e^-, e^+$ ) = (-0.8, +0.3)



Cross section ( $e^-, e^+$ ) = (+0.8, -0.3)



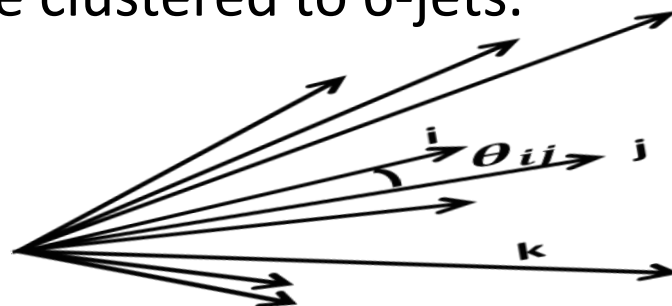
# ***Analysis***



# Reconstruction

- ① Using Durham algorithm, objects are clustered to 6-jets.

$$Y_{ij} = \frac{2E_i E_j (1 - \cos\theta_{ij})}{E_{vis}^2}$$



- ② b quark tagging  $\times 2$

Most b like jet and second most b like jet are selected.

- ③ Two Ws are reconstructed from remaining 4-jets.

- ④ top quarks are reconstructed by pairing W and b.

- ⑤ The best candidate of jet combination is selected by minimizing  $\chi^2$  from W and top mass.

$$\chi^2 = \frac{(M_{2j} - M_{W_1})^2}{\sigma_{W_1}} + \frac{(M_{2j} - M_{W_2})^2}{\sigma_{W_2}} + \frac{(M_{3j} - M_{t_1})^2}{\sigma_{t_1}} + \frac{(M_{3j} - M_{t_2})^2}{\sigma_{t_2}}$$

# Selections

Maximizing the significance of top pair to **6-jets final state**, these selections were applied.

First, for suppressing the large backgrounds, WW and ZZ, we tagged b quarks, and applied thrust cut.

And for suppressing 4-jets + 1-lepton, isolated lepton veto and visible energy cut are used.

Finally, we use Durham  $y$  values for 5 to 6 jets and 6 to 7 jets,  $y_{56}$  and  $y_{67}$ .

## Left handed

$b_{\text{tag}1} > 0.1, b_{\text{tag}2} > 0.1$

Thrust  $< 0.84$

# of isolated leptons = 0

Visible Energy  $> 310$  GeV

$y_{56} > 0.001, y_{67} > 0.0001$

## Right handed

$b_{\text{tag}1} > 0.07, b_{\text{tag}2} > 0.07$

Thrust  $< 0.83$

# of isolated leptons = 0

Visible Energy  $> 305$  GeV

$y_{56} > 0.001, y_{67} > 0.0001$

# Cut table @350GeV Left-Handed

$tt \rightarrow 6\text{jets}$  cut based analysis table at  
Center of Mass Energy 350(GeV).

Luminosity =  $10 \text{ fb}^{-1}$ , polarization **e(-80%)p(+30%)**

$$\text{Significance ; } S = \frac{\text{signal}}{\sqrt{\text{signal} + \text{background}}}$$

|                             | Signal | Background |         |       |      |      |          |
|-----------------------------|--------|------------|---------|-------|------|------|----------|
| Ecm=350(GeV)                | tt6j   | tt4j+1l    | tt2j+2l | WW    | ZZ   | ZH   | $S_{6j}$ |
| No cut                      | 3288   | 3167       | 763     | 65328 | 6008 | 1389 | 11.6     |
| btag $\times 2$             | 3136   | 3004       | 725     | 7567  | 2832 | 982  | 23.2     |
| Thrust<0.84                 | 3090   | 2882       | 645     | 867   | 917  | 815  | 32.2     |
| # of lepton = 0             | 3071   | 495        | 20      | 864   | 915  | 792  | 39.2     |
| Evis>310 GeV                | 3044   | 185        | 1       | 432   | 572  | 571  | 43.9     |
| y56 > 0.001<br>y67 > 0.0001 | 2880   | 127        | 0       | 134   | 126  | 142  | 49.3     |

Statistical error for cross section is  $1/49.3 = 2.0\%$

# Cut table @350GeV Right-Handed

$tt \rightarrow 6\text{jets}$  cut based analysis table at  
Center of Mass Energy **350(GeV)**.

Luminosity =  $10 \text{ fb}^{-1}$ , polarization **e(+80%)p(-30%)**

$$\text{Significance ; } S = \frac{\text{signal}}{\sqrt{\text{signal} + \text{background}}}$$

| Ecm=350(GeV)                | Signal | Background |         |      |      |     | $S_{6j}$ |
|-----------------------------|--------|------------|---------|------|------|-----|----------|
|                             | tt6j   | tt4j+1l    | tt2j+2l | WW   | ZZ   | ZH  |          |
| No cut                      | 1572   | 1515       | 365     | 4326 | 2773 | 937 | 14.7     |
| btag $\times 2$             | 1547   | 1483       | 356     | 1165 | 1585 | 720 | 18.7     |
| Thrust<0.83                 | 1512   | 1404       | 308     | 118  | 323  | 563 | 23.3     |
| # of lepton = 0             | 1503   | 241        | 9       | 118  | 322  | 543 | 28.7     |
| Evis>305 GeV                | 1496   | 105        | 0       | 59   | 185  | 409 | 31.5     |
| y56 > 0.001<br>y67 > 0.0001 | 1417   | 72         | 0       | 18   | 47   | 108 | 34.8     |

Statistical error for cross section is  $1/34.8 = 2.9\%$

# ***TOP YUKAWA***

# Statistical Error of Top Yukawa

Summing the events in **all the center of mass energy**, the statistical errors of the cross section and top yukawa coupling were estimated. Because of 9% enhancement by exchanging higgs boson, we can estimate the statistical error of top yukawa from following formula.

$$\frac{\delta y_t}{y_t} \sim \frac{109 \times \frac{1}{2} \times \frac{\delta \sigma}{\sigma}}{9}$$

**Top mass and width are fixed.**

| Statistical error | Left  | Right | Combined |
|-------------------|-------|-------|----------|
| Cross section     | 0.84% | 1.2%  |          |
| Top yukawa        | 5.0%  | 7.1%  | 4.2%     |

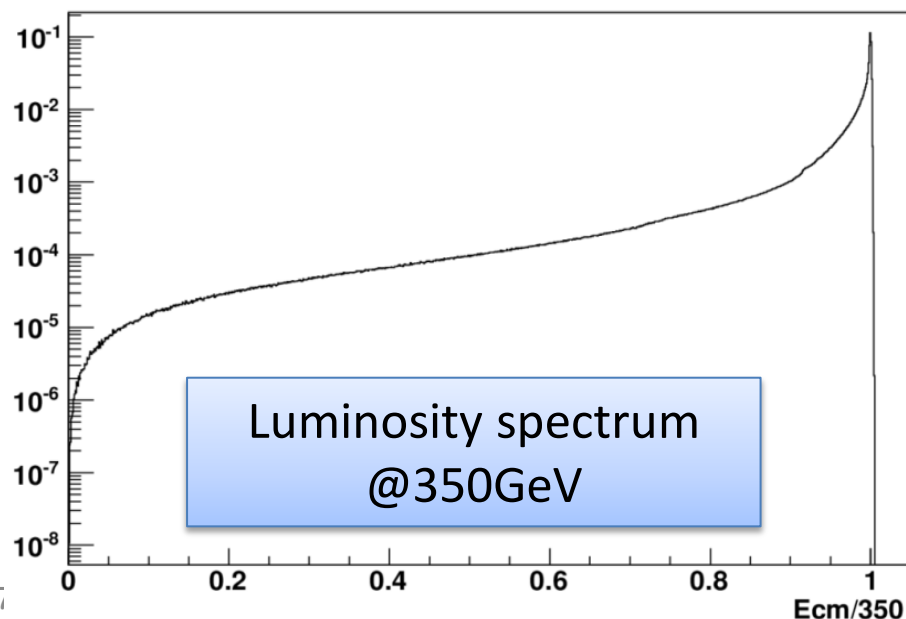
If we can combine 6-jets analysis with 4-jets one , the expected statistical error of top yukawa might be reduced to about **3 %**.

# ***Top Mass & Width***

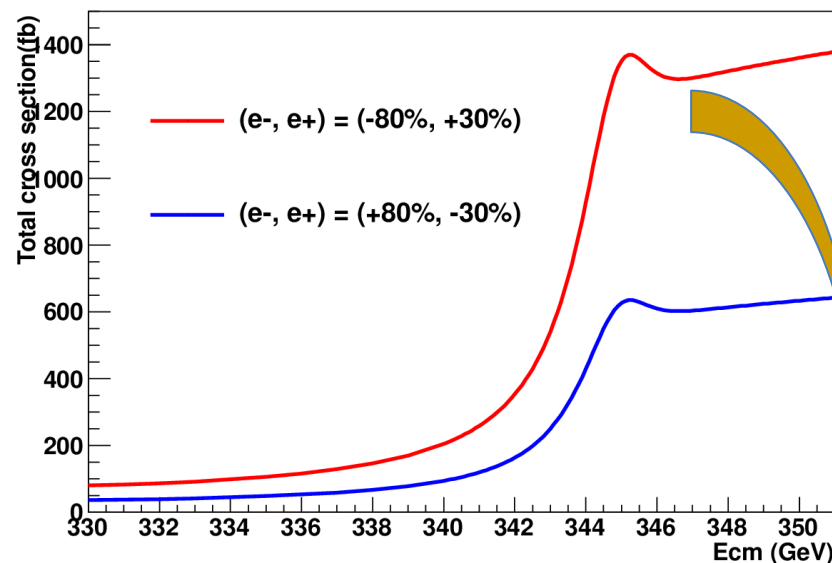
# Fitting the Cross Section

To take into account the beam energy spread, ISR, and beamstrahlung effects, theoretical cross section is **convoluted with luminosity spectrum**. This is done at each  $E_{cm}$ , top mass and width to make cross section tables.

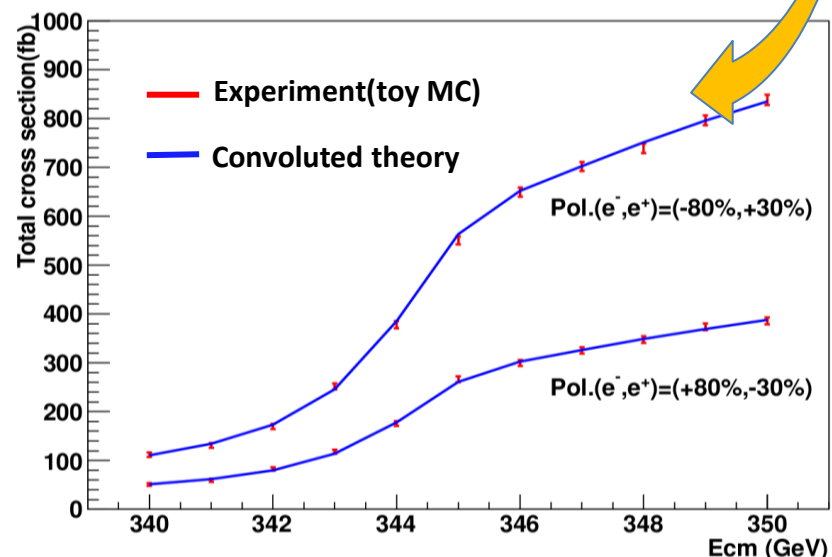
10000 toy MC experiments for 11  $E_{cm}$  points are generated and fitted with the function according to the tables by floating the mass and width ( $y_t$  is fixed).



Theoretical Cross Section

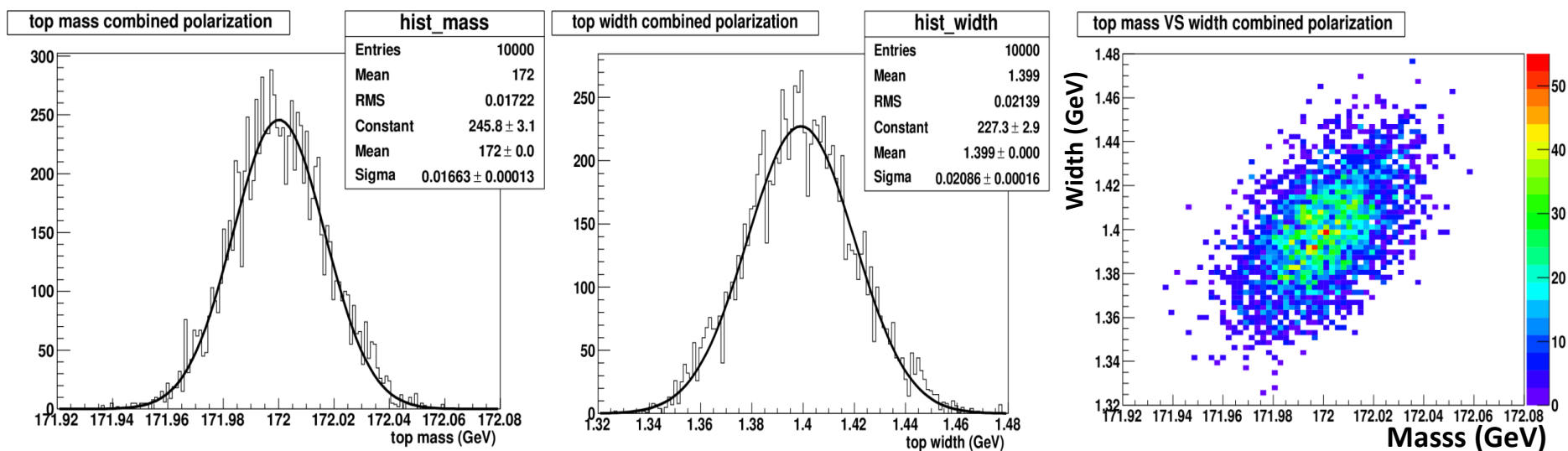


Total Cross Section of  $t\bar{t}$  near threshold





# Fit Result



PS Mass(GeV)

Width(GeV)

Left( $110\text{fb}^{-1}$ )

$172.000 \pm 0.021$

$1.400 \pm 0.025$

Right( $110\text{fb}^{-1}$ )

$172.000 \pm 0.030$

$1.399 \pm 0.037$

Left ( $110\text{fb}^{-1}$ ) + Right( $110\text{fb}^{-1}$ )

$172.000 \pm 0.017$

$1.399 \pm 0.021$

$\alpha_s(\text{Mz})$

PDG  $0.1184 \pm 0.0007$  (0.6%)

Future?  $0.1184 \pm 0.00012$  (0.1%)

$\overline{MS}$  mass(GeV)

$163.80 \pm 0.016(\text{stat}) \pm 0.054(\alpha_s) \pm \dots$

$163.80 \pm 0.016(\text{stat}) \pm 0.009(\alpha_s) \pm \dots$

From PS mass to  $\overline{MS}$  mass

$$\overline{MS}mass \sim M_{PS} - \frac{4}{3\pi} (M_{PS} - 20)\alpha_s + \dots$$

# SUMMARY & PLAN

## <SUMMARY>

- We have estimated the statistical error of top yukawa coupling and the accuracy of top mass and width using 6-jets final state for each polarization at ILC.
- The estimated statistical error of top yukawa coupling is 4.2%.
- The accuracy of  $\overline{MS}mass$  is 16MeV (stat) + 54 MeV( $\alpha_s$ )
  - If the systematic error in  $\alpha_s$  is reduced to 0.1%, the corresponding systematic becomes 54  $\rightarrow$  9 MeV.
- The accuracy of width is 21 MeV.

## <PLAN>

- Estimation of top yukawa coupling by fitting.
- 4-jets + 1-l study will be started which double the statistics.