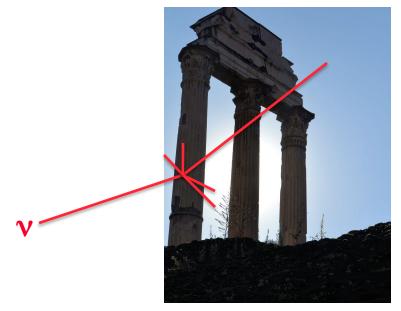
# Neutrino – Nucleus Scattering Physics with nuSTORM

## What can a dedicated nuSTORM neutrinonucleus scattering physics program deliver?

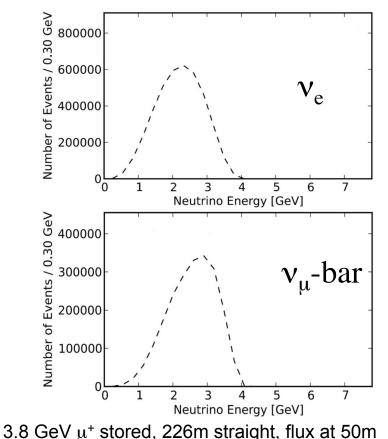


#### Jorge G. Morfín Fermilab

nuSTORM Workshop – Fermilab, November 2013

The nuSTORM Neutrino Beam: The Advantages  $\mu^+ \rightarrow \nu_{\mu} + \nu_e + e^+ \qquad \mu^- \rightarrow \nu_{\mu} + \nu_e + e^-$ Mitchell YU

- The vSTORM beam will provide a very well-known ( $\delta \phi(\mathbf{E}) \leq 1\%$ ) beam of v and  $\overline{v}$ . Intensity of  $v_{\mu}$  good not great for 10 ton detector.
- A high-intensity source of  $v_e$  events for experiments.



$\mu^{+}$		μ	
Channel	$N_{ m evts}$	Channel	$N_{ m evts}$
$\bar{ u}_{\mu}  { m NC}$	844,793	$\bar{\nu}_e  \mathrm{NC}$	709,576
$\nu_e~{\rm NC}$	1,387,698	$ u_{\mu} \; { m NC}$	$1,\!584,\!003$
$ar{ u}_{\mu}~{ m CC}$	$2,\!145,\!632$	$\bar{\nu}_e~\mathrm{CC}$	1,784,099
$\nu_e  { m CC}$	3,960,421	$ u_{\mu}  ext{ CC} $	$4,\!626,\!480$

event rates per 1E21 POT -100 tons at 50m

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# nuSTORM Event Rates

♦ A beam of 700 kW yields order  $6x10^{20}$  POT/year. The 1100 kW for LBNE could yield close to  $10^{21}$  POT/year (d LBNE proton bea **DON'T GET A PROTONS!** 

$\nu_e \ \mathrm{CC}$	3,960,421	$ u_{\mu}$
0		$\bar{\nu}_{\mu}$ $\bar{\nu}_{e}$
		č / / /

 It would be preferable to have a near detector of order 30-50 ton fiducial volume.

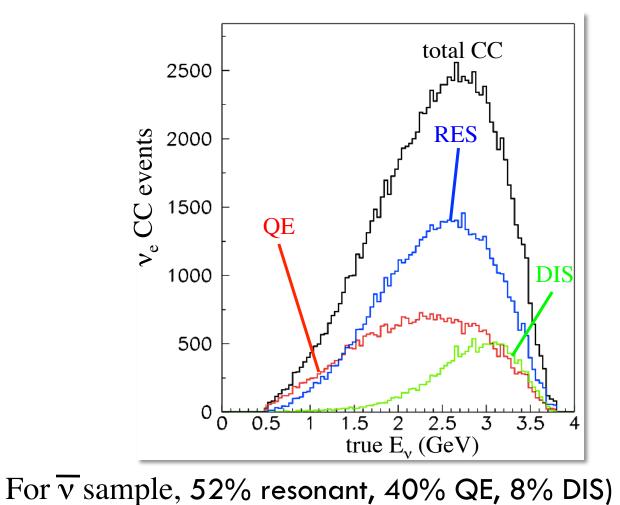
μ+			$\mu^-$	
Channel	$N_{ m evts}$	Channel	$N_{ m evts}$	
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1F21 POT at 50m

## v Produced Events in a nuSTORM Near Detector

Jorge G. Morfín - Fermilab

•  $\nu$  produced by 3.8 GeV  $\mu^+$  beam.





\* 56% resonant \* 32% QE \* 12% DIS

### Why is Neutrino Nucleus Scattering Important? What do we observe in our detectors?

• The events we observe in our detectors are convolutions of:  $Y_{c-like}(E) \alpha (E' \ge E) (Y (C_{c,d,e..}(E' \ge E))) (V_{c,d,e..} \rightarrow c) (E' \ge E)$ 

- φ(E) is the energy dependent neutrino flux that enters the detector. Currently, with traditional meson-decay-source neutrino beams, φ(E) ≈10% absolute and ≈ 7% energy bin-to-bin accuracy. Significant contribution to systematics.
- σ<sub>c,d,e.</sub>(E' ≥ E) is the measured or the Monte Carlo (model) energy dependent
   neutrino cross section off a nucleon within a nucleus.
- $\operatorname{Nuc}_{c,d,e.. \to c} (E' \ge E) \operatorname{Nuclear Effects}$ 
  - Nuclear Effects a migration matrix that mixes produced/observed channels and energy
  - In general the interaction of a neutrino with energy E' creating initial channel d,e...
     can appear in our detector as energy E and channel c.
  - Particularly **fierce bias** when using the **QE hypothesis** to calculate E and Q<sup>2</sup>!
- $Y_{c-like}(E)$  is the event energy and channel / topology of the event observed in the detector. Appears to be channel c but may not have been channel c at interaction.

# What do we observe in our detectors? Further implications for Oscillation Experiments

• The events we observe in our detectors are convolutions of:  $Y_{c-like}(E) \alpha \phi(E' \ge E) \otimes \sigma_{c,d,e..}(E' \ge E) \otimes Nuc_{c,d,e.. \rightarrow c}(E' \ge E)$ 

- Experimentally, the convolution of initial cross section and nuclear effects are combined into an effective cross section σ<sub>c</sub><sup>A</sup>(E) that depends on incoming neutrino energy spectrum and nuclear effects that populate the yield Y<sub>c</sub><sup>A</sup>(E).
- This implies, for example, effective σ<sub>π+</sub><sup>C</sup> (1 GeV) measured in the Booster beam will be different than the same effective σ<sub>π+</sub><sup>C</sup> (1 GeV) observed in the higher energy NuMI beam due to, for example, more feed down from multi-pi events. Can not simply plug in effective σ<sub>π+</sub><sup>A</sup> from experiments in a different beam.
- In a two-detector LBL oscillation experiment, neutrino flux entering the FD is different than the neutrino flux at the ND due to geometry and oscillations. The σ<sub>c</sub><sup>A</sup> (E) effective that should be applied to expectations (Monte Carlo) at FD is NOT the same as that which we would measure at the ND. The ND results give us an excellent starting point for calculating the difference.

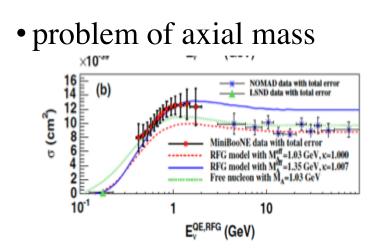
effective  $\sigma_c^A(E)$ 

How do we address this  $v_{\mu}$  scattering problem? What could a nuSTORM Scattering analysis add?

- Use the unique qualities of the nuSTORM beam meaning the fantastic knowledge of absolute and relative flux. And we can vary the energy distribution of this well-known beam.
- Combine with a high-resolution near detector with multiple nuclear targets to provide detailed studies of the final states including the vertex multiplicities and energy flow..
- nuSTORM, providing a beam with knowledge of the flux to  $\leq 1\%$ , to such a near detector would provide an outstanding neutrino-nucleus scattering experiment addressing both electroweak and nuclear physics questions. It would allow us to measure, for example,  $\sigma_{\pi^+}{}^A$  (E) for multiple A and various E.

# QE History Very important for nuSTORM

• problem of low Q<sup>2</sup>

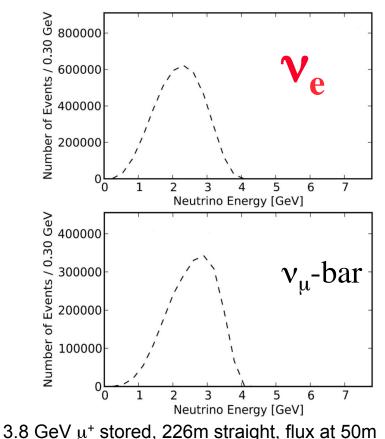


• problem of np-nh (more complex nuclear effects: SRC + MEC) • M<sub>A</sub> provides a convenient tool to describe exp. data in shape & normalization with Fermi Gas

Have they got the flux wrong? **nuSTORM could tell us?** Distinction between Fermi Gas and Spectral Functions? With accurate  $d\phi / dE$ maybe nuSTORM could help.

•However there is an alternative path involving a more sophisticated nuclear models. MEC implies extra tracks and energy at vertex, nuSTORM could help. **Time to retire** Jorge G.Morfin - Fern**impulse approximation with RFG!** 8 The nuSTORM Neutrino Beam  $\mu^+ \rightarrow \overline{\nu}_{\mu} + \nu_e + e^+ \qquad \mu^- \rightarrow \nu_{\mu} + \overline{\nu}_e + e^-$ 

- The vSTORM beam will provide a very well-known ( $\delta \phi(E) \le 1\%$ ) beam of v and  $\overline{v}$ .
- A high-intensity source of ν<sub>e</sub> events for experiments.

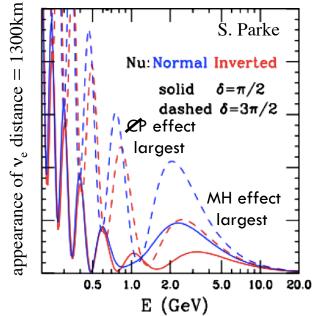


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event rates per 1E21 POT -100 tons at 50m

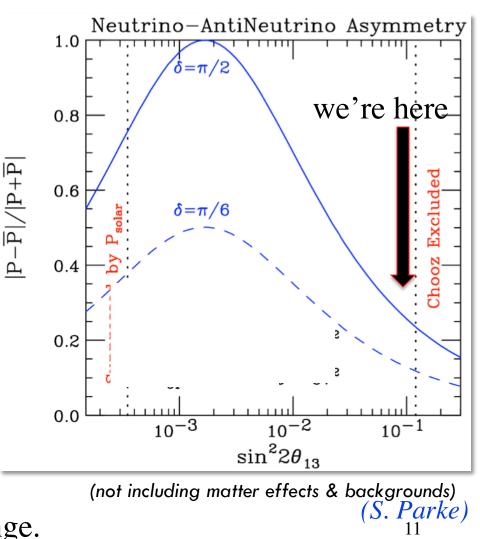
# Why are $v_e$ Cross Sections Important?

- $v_e A$  scattering results are interesting on their own.
- Recent determination of large  $\theta_{13}$  has opened up possibilities of
  - ▼ Determining v mass ordering.
  - **\checkmark** Searching for CP-violation in the  $\vee$  sector.
- To be sensitive to these effects, current/near-future long-baseline experiments will be looking for  $v_{\mu}$  to  $v_{e}$  and  $\overline{v}_{\mu}$  to  $\overline{v}_{e}$  oscillations over a range of energies.
- These will no longer be only "counting" experiments but rather will depend on observing distortions in the far detectors neutrino energy spectrum in **both neutrino** and anti-neutrino samples.



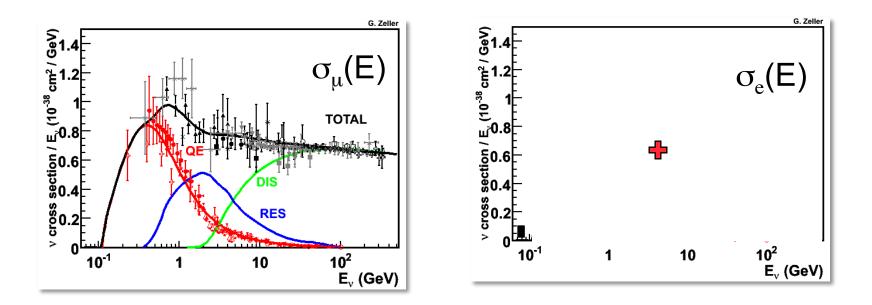
# Why are $v_e$ and $\overline{v}_e$ Cross Sections Important?

- Large  $\theta_{13}$  means we could have reasonable statistics.
- However, as the now-well-known plot at right suggests, the asymmetry between v and v will be small and the goal of constraining the range of δ will demand minimal systematic errors.
- ♦ One of these systematics will be our knowledge of v<sub>e</sub> and v<sub>e</sub> cross
   sections in the relevant energy range.



# How well do we know $v_e$ cross sections?

• WE DON' T! Need to measure the  $\sigma_{ve}(E)$  of multiple channels to fully predict a spectrum at a far detector for LBL experiments.



We infer them from σ<sub>νμ</sub>(E) results. The validity of this inference directly impacts the uncertainty of the measurements.

Jorge G. Morfín - Fermilab

# One (+ ONE) to add to the collection...of one

- Gargamelle experiment published with around 200 electron and 60 positron events.
- Error bars on the order of 30%.

TOTAL CROSS SECTIONS FOR  $\nu_e$  AND  $\overline{\nu}_e$  INTERACTIONS AND SEARCH FOR NEUTRINO OSCILLATIONS AND DECAY

Gargamelle Collaboration

J. BLIETSCHAU, H. DEDEN, F.J. HASERT, W. KRENZ, D. LANSKE, J. MORFIN, M. POHL, K. SCHULTZE, H. SCHUMACHER, H. WEERTS and L.C. WELCH *III. Physikalisches Institut der Technischen Hochschule, Aachen, Germany* 

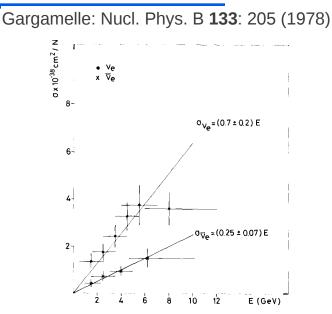


Fig. 2. Neutrino and antineutrino cross sections as a function of energy.

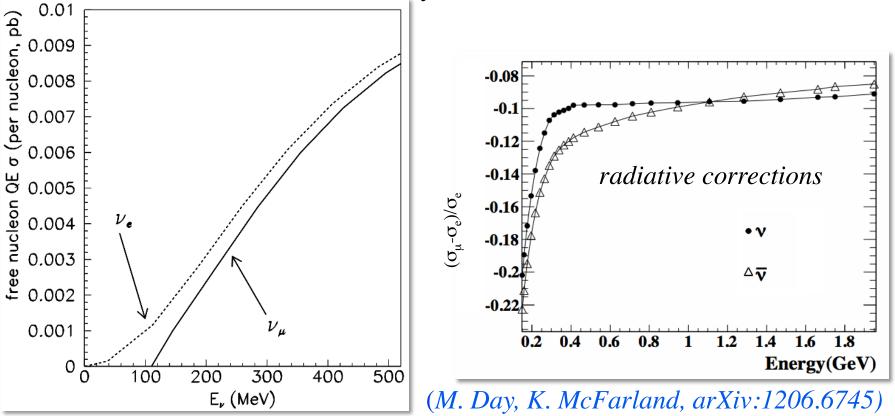
- MINERvA will have a sample of 65k  $v_e$  CC events; 2.5k  $v_e$  CCQElike produced events in LE beam. In the ME beam probably factor of 5 higher statistics. Will be systematics limited  $\rightarrow$  FLUX.
- Until then, we infer them from σ<sub>νμ</sub>(E) results. The validity of this inference directly impacts the uncertainty of measurements.

Jorge G. Morfin - Fermilab

#### What are the Differences $\sigma_{\nu\mu}(E)$ and $\sigma_{\nu e}(E)$ ? Quasi-elastic Scattering Day-McFarland study: Phys.Rev. D86 (2012) 053003

- QE scattering dominates at low energies (2<sup>nd</sup> oscillation maxima)
- Sources of possible differences and uncertainties obvious:
  - Kinematic limits from  $\mu$  / e mass difference.

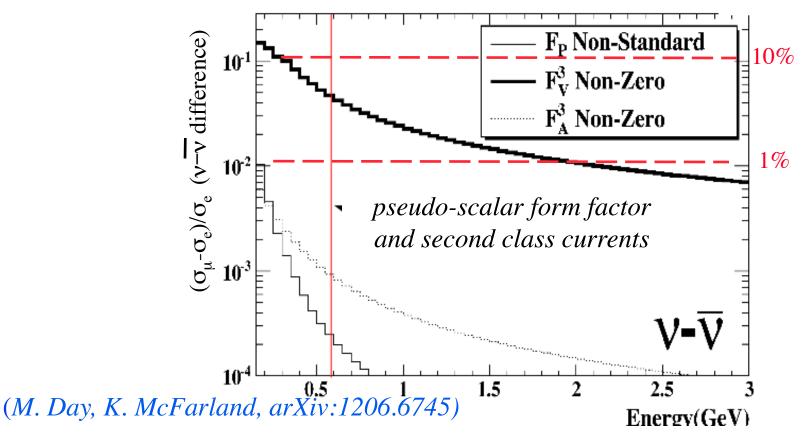
▼ Radiative Corrections. This may be an overestimate. Need full calculation.



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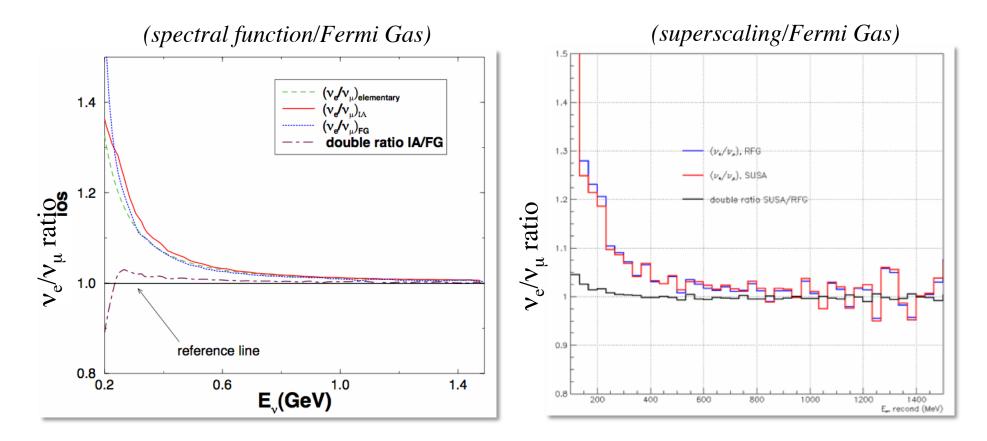
#### What are the Differences $\sigma_{\nu\mu}(E)$ and $\sigma_{\nu e}(E)$ ? Quasi-elastic Scattering Day-McFarland study: Phys.Rev. D86 (2012) 053003

- Sources of possible differences: form factor uncertainties entering through lepton mass alterations - much more subtle:
  - ▼ Form factor contributions both Axial and Pseudoscalar
  - ▼ Second class current contributions to vector and axial-vector form factors
- Possible contribution to CP uncertainties: effect on the FF could be different for v and  $\overline{v}$



#### What are the Differences? Mainly QE Scattering Due to Nuclear Effects

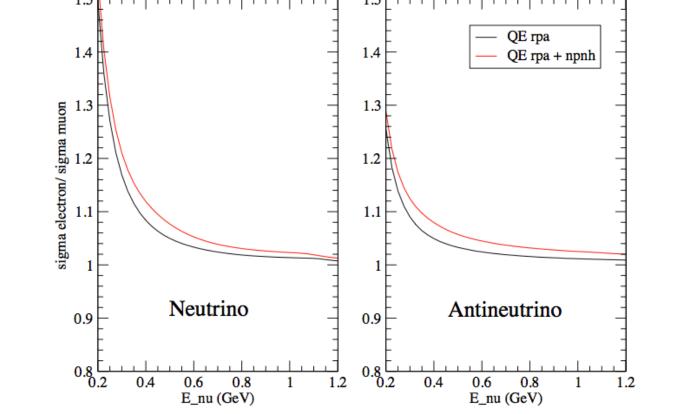
• For standard models,  $\leq 5\%$  differences on  $v_e/v_\mu$  ratio E < 200 MeV



S. Zeller: vSTORM Workshop

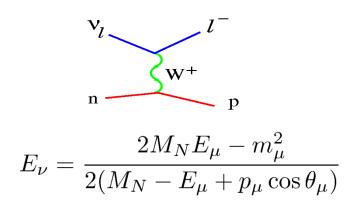
### What are the Differences? Mainly QE Scattering Meson-exchange Current Contributions – Marco Martini

- Hadronic part (nuclear response functions) is the same for  $v_e$  or  $v_\mu$  cross section.
- However, the lepton tensor changes  $\rightarrow$  the relative weight of the nuclear responses in the several channels may change.
- The double ratio suggests the effect on the  $v_e/v_\mu$  cross section ratio is  $\leq 5\%$  (S. Zeller)



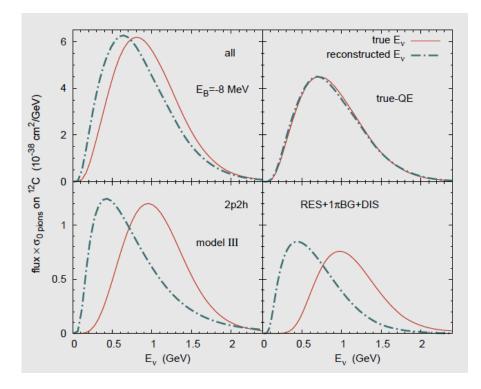
Nuclear Effects can Change the Energy Reconstruction for "QE" Events

In pure QE scattering on a nucleon at rest, the outgoing lepton can determine the neutrino energy:



#### However, not on nuclei.

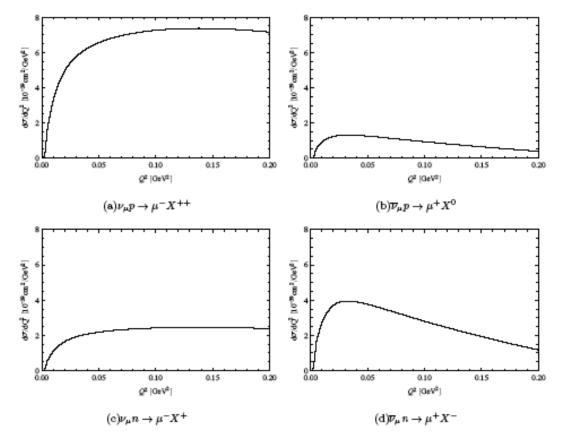
Reconstructed energy is shifted to lower values for all processes other than true QE off nucleon at rest



U. Mosel GiBUU

### What are the Differences? △ Production Paschos – Schalla: arXiv:1209.4219

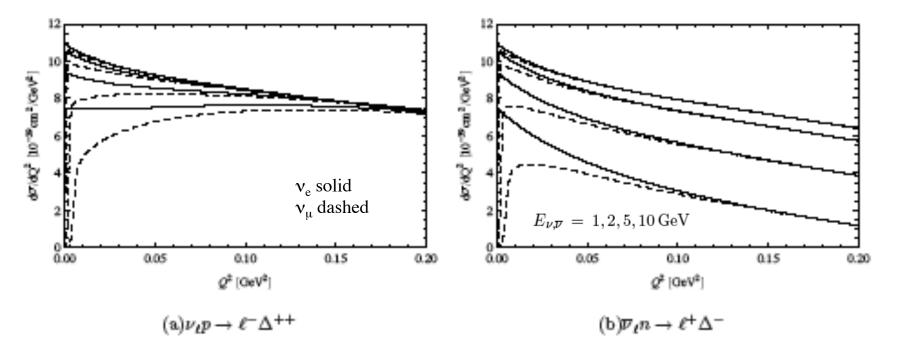
- Manny and his student have investigated  $v_{\mu}$  and  $\overline{v_{\mu}}$  differences in  $\Delta$  production in the low-Q ( $Q^2 \approx m_{\pi}^2$ ) region where PCAC dominates the axial contribution.
- At E = 1-2 GeV, V part and V/A interference same size  $\rightarrow$  cancel for  $\overline{v}$
- Use the Adler-Nussinov-Paschos model for nuclear corrections.



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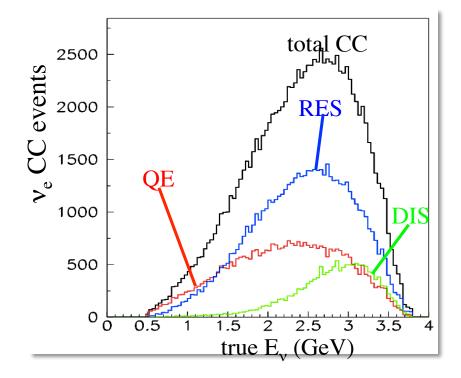
#### What are the Differences? Δ Production Paschos – Schalla: arXiv:1209.4219

 Paschos-Schalla predicts the following differences in cross sections where only the lepton mass term contributions are shown and any differences in form factors are not yet included.



# Can we Actually MEASURE these Differences in the 0.5 – 6 GeV region

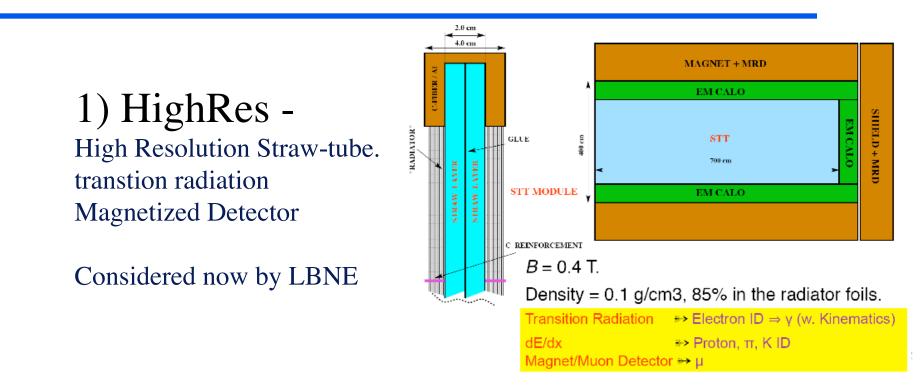
- Need to measure the σ<sub>e</sub>(E) of multiple channels to predict spectrum at the far detector.
  - Want an intense source of  $v_e$  events.
  - Would like to know the flux of  $v_e$  (and  $v_{\mu}$ , by the way) to order 1%.



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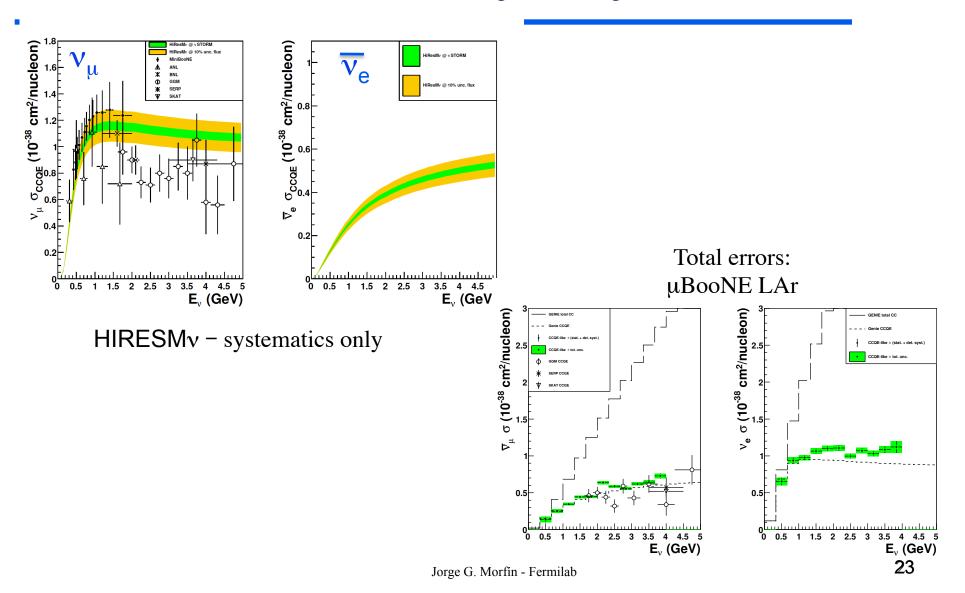
# nuSTORM Near Detector(s) Etam MESSOMO



2) A 1-2 ton fiducial liquid hydrogen/deuterium track sensitive target upstream of HiRes. This could be a "bubble chamber".

# Scattering Measurements with nuSTORM + Near Detector nuSTORM provides a well-known ( $\delta \phi(E) \approx 1\%$ ) beam of v and $\overline{v}$ .

Ed Santos – Imperial College



Conclusions: What does nuSTORM bring to Neutrino-nucleus Interaction Physics?

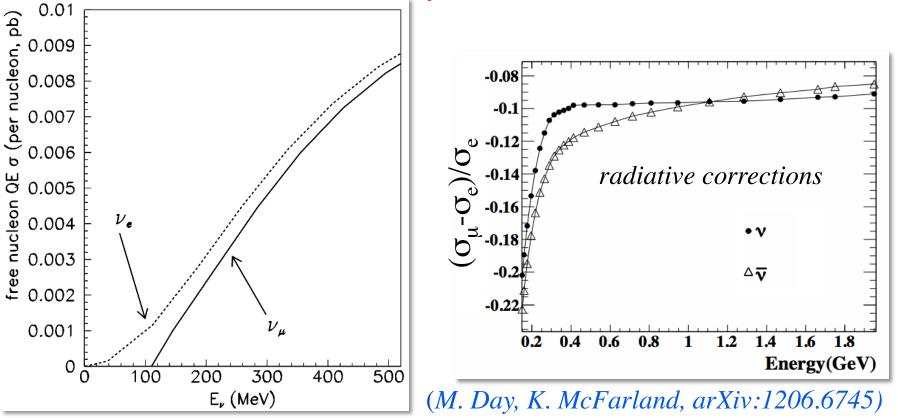
- Obvious benefit in measuring  $v_e$  events.
- Use vastly improved nuSTORM neutrino flux uncertainty to measure neutrino cross sections and nuclear effects!
- There are many physics topics important in their own right and essential for precision neutrino oscillation experiments that will be awaiting the results of a high-resolution detector in the accurate nuSTORM flux!
- However, this is not the nuSTORM experiment that was approved. Adding at least a precision near detector and perhaps a H/D target.
- This calls for a new collaboration using the **nuSTORM** facility. First meeting/workshop to establish this collaboration in November.

# BACKUP

#### What are the Differences $\sigma_{\nu\mu}(E)$ and $\sigma_{\nu e}(E)$ ? Quasi-elastic Scattering Day-McFarland study: Phys.Rev. D86 (2012) 053003

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- Sources of possible differences and uncertainties obvious:
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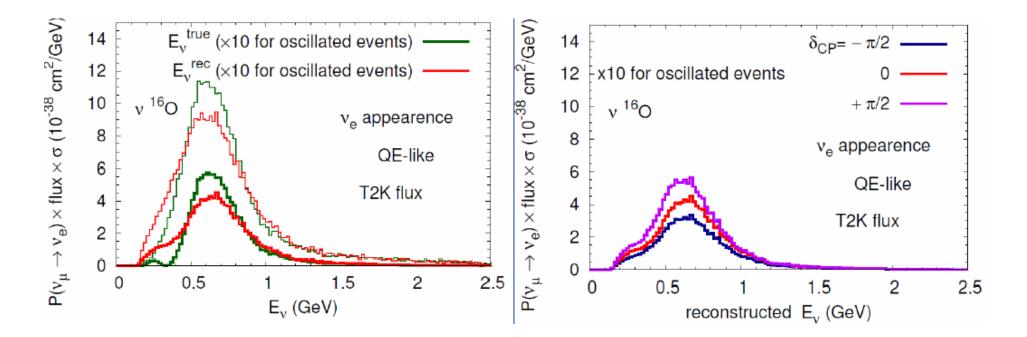




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# Nuclear Effects and Oscillation Measurements

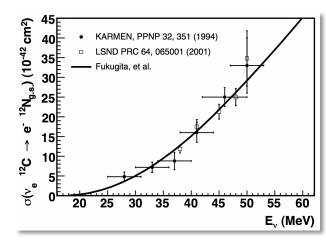
#### Ulrich Mosel using his Giessen Boltzmann-Uehling-Uhlenbeck (GiBUU) Transport Model looking at T2K



Jorge G. Morfin - Fermilab

How well do we know cross sections:  $v_e vs. v_{\mu}$ ? Existing  $v_e$  Cross Section Data

- What do we know about  $\sigma_{ve}(E)$ ? Mostly very low energy results.
  - Reactor neutrinos studying Inverse Beta Decay
  - ▼ Solar neutrino off deuterium (SNO)
  - Stopping  $\pi/\mu$  decay neutrinos off higher A targets
  - ▼ See Formaggio and Zeller **Rev. Mod. Phys. 84, 1307–1341 (2012).**
- One of few measurements of spectral shape of  $\sigma$  reflects the upper limit of most existing measurements,  $E \le 50$  MeV.





Jorge G. Morfín - Fermilab

 $v_e^{12}C \rightarrow e^{-12}N_{a.s}$ 

Addressing the lack of F<sub>2</sub> Neutrino Nuclear Effects Analyses

**Nuclear PDFs from neutrino deep inelastic scattering** 

#### nCTEQ

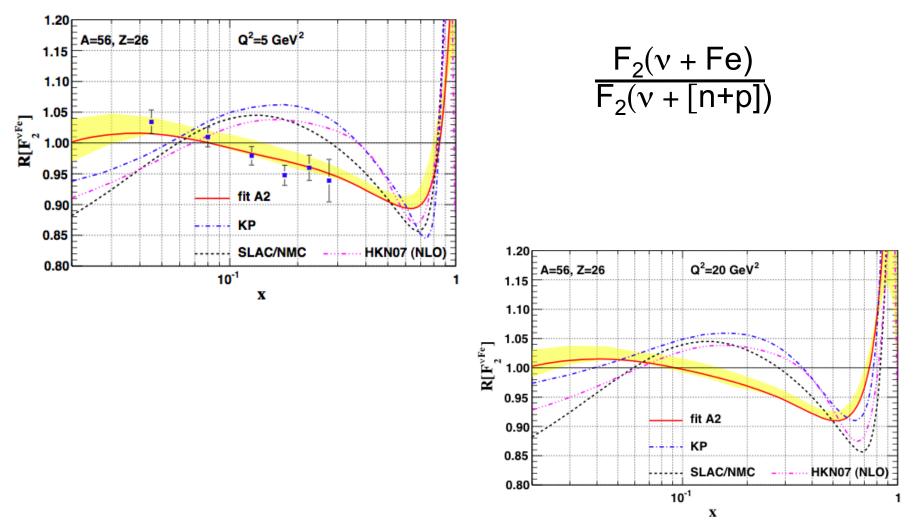
K. Kovarik (Karlsruhe) I. Schienbein (LPSC-Grenoble), J-Y. Yu (SMU), C. Keppel (Hampton/JeffersonLab) J.G.M. (Fermilab), F. Olness (SMU), J.F. Owens (Florida State U)

> Also analyses by: K. Eskola, V. Kolhinen and C. Salgado and D. de Florian, R. Sassot, P. Zurita and M. Stratmann

# Significant Implications for Oscillation Experiments

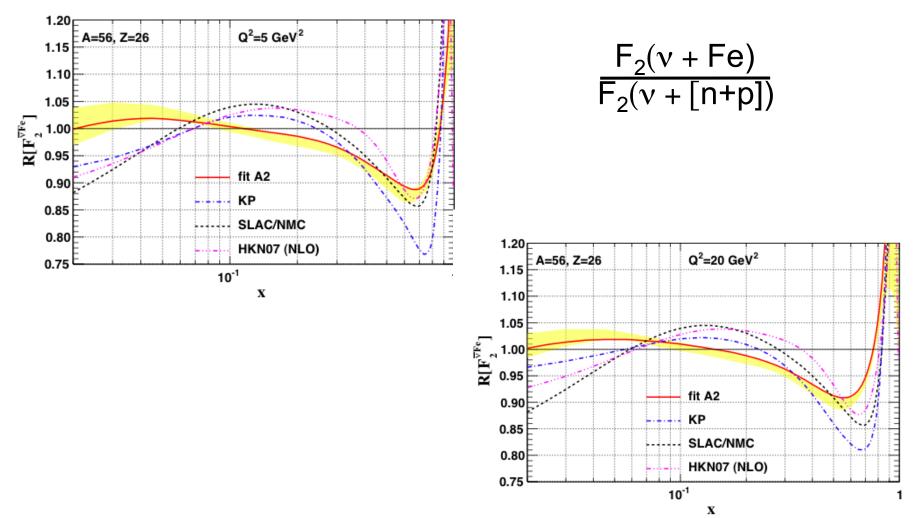
- Can not simply plug in effective  $\sigma_{\pi^+}^A$  from experiments in a significantly different beam.
- In a two-detector LBL oscillation experiment the neutrino flux entering the far detector is altered from the neutrino flux at the near detector due to geometry and oscillations.
- The  $\sigma_c^A(E)$  effective that should be applied to expectations (Monte Carlo) at the far detector is NOT the same as that which we would measure at the near detector. However, the near detector results give us an excellent starting point for calculating the difference.
- The convoluted  $\phi(E' \ge E)$  (X)  $\sigma(E)$  (X) Nuc(E' \ge E) systematics need to be correctly incorporated in determining the systematics of oscillation parameter measurements. Who is addressing this important consideration now?

### F<sub>2</sub> Structure Function Ratios: v-Iron



Jorge G. Morfín - Fermilab

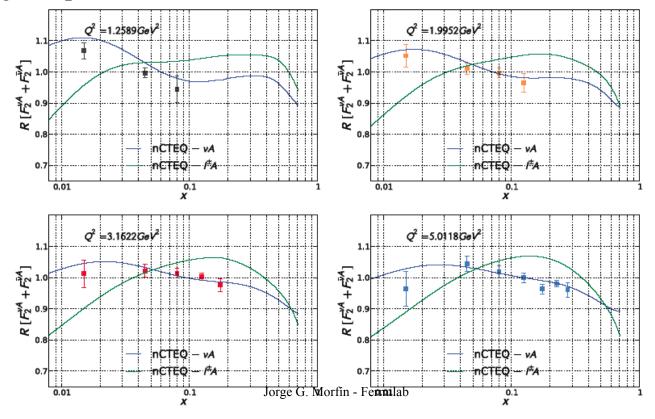
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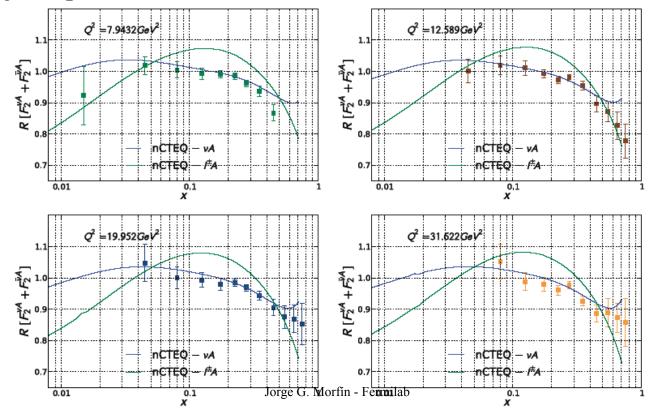
## A More-Detailed Look at Differences

- NLO QCD calculation of  $\frac{F_2^{\nu A} + F_2^{\bar{\nu} A}}{F_2^{\bar{\nu} A} + F_2^{\bar{\nu} A}}$  in the ACOT-VFN scheme
  - charge lepton fit undershoots low-x data & overshoots mid-x data
  - low-Q<sup>2</sup> and low-x data cause tension with the shadowing observed in charged lepton data



## A More-Detailed Look at Differences

- NLO QCD calculation of  $\frac{F_2^{\nu A} + F_2^{\bar{\nu} A}}{2}$  in the ACOT-VFN scheme
  - charge lepton fit undershoots low-x data & overshoots mid-x data
  - low-Q<sup>2</sup> and low-x data cause tension with the shadowing observed in charged lepton data



# What are these Nuclear Effects $Nuc_{c.d.e., \rightarrow c}$ (E' $\geq$ E) in Neutrino Nucleus Interactions? (Partial List)

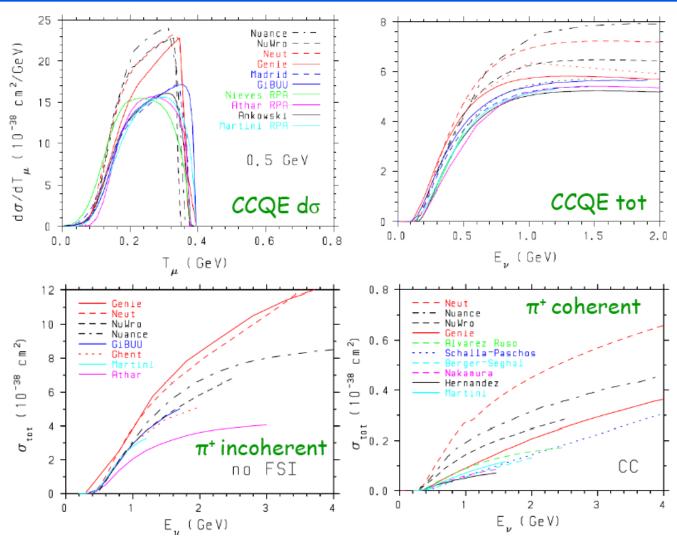
- Target nucleon in motion classical Fermi gas model or the superior spectral functions (Benhar et al.)
- Multi-nucleon initial states: Short-range correlations, meson exchange currents.
- Form factors, structure functions, resonance widths, parton distribution functions and, consequently, cross sections are modified within the nuclear environment. (Butkevich / Kulagin, Tsushima et al., Kovarik et al.)

(Produced topologies are modified by final-state interactions modifying topologies) ٠ and possibly reducing **detected** energy and **increasing** wrong-sign background. **v** Convolution of  $\delta\sigma(n\pi)(x)$  formation zone uncertainties(x)  $\pi$ -charge-exchange/ absorption probabilities and nuclear density uncertainties.

Systematics associated with each of these effects.

 Monte Carlos – like GENIE – try to include all these effects. **GENIE needs improvements!** GENIE group needs additional help from the community.

#### How well off are we with $v_{\mu}$ Cross sections: Range of Existing Model (MC) Predictions off C NuInt09 – Steve Dytman



Jorge G. Morfin - Fermilab

# **Example Model Uncertainties**

#### Cross Section Model Uncertainties

Uncertainty	1σ
M <sub>A</sub> (Elastic Scattering)	± 25%
Eta (Elastic scattering)	± 30%
MA (CCQE Scattering)	+25%
	-15%
CCQE Normalization	+20%
	-15%
CCQE Vector Form factor model	on/off
CC Resonance Normalization	± 20%
M <sub>A</sub> (Resonance Production)	$\pm 20\%$
M <sub>v</sub> (Resonance Production)	± 10%
1pl production from $vp / \overline{v}n$ non-	± 50%
resonant Interactions	
1pi production from $vn / \overline{v}p$ non-	± 50%
resonant interactions	. 50%
2pi production from vp / vn non- resonant Interactions	± 50%
2pi production from $vn/\overline{v}p$ non-	± 50%
resonant interactions	
Modfly Pauli blocking (CCQE) at low Q <sup>2</sup> (change PB momentum threshold)	± 30%

#### Intranuclear Rescattering Uncertainties

Uncertainty	1σ
Plon mean free path	± 20%
Nucleon mean free path	± 20%
Pion fates – absorption	± 30%
Pion fales – charge exchange	± 50%
Pion fates - Elastic	$\pm 10\%$
Pion fates - Inelastic	± 40%
Pion fates – pion production	± 20%
Nucleon fates – charge exchange	± 50%
Nucleon fates - Elastic	± 30%
Nucleon fates – Inelastic	± 40%
Nucleon fates – absorption	± 20%
Nucleon fates – plon production	± 20%
AGKY hadronization model – xr distribution	± 20%
Delta decay angular distribution	On/off
Resonance decay branching ratio to photon	± 50%

Hugh Gallagher

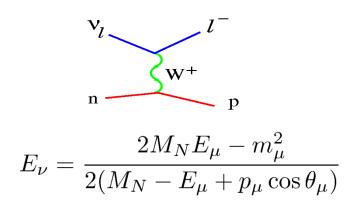
References: (1) www.genie-mc.org, (2) arXiv:0806.2119, (3) D. Bhattacharya, Ph. D Thesis (U. Pittsburgh) 2009.

# Have these experiments really measured M<sub>A</sub>?

- Just as we have noted, we are observing an effective  $\sigma_c^A(E)$  in our detectors...
  - $\checkmark$  What has been measured is a parameter  $M_a^{eff}$
  - ▼ It depends on the use of RFGM or Spectral Functions.
  - ▼ It depends on the nucleus used and...
  - ▼ It depends on the incoming flux.
  - ▼ It also depends on number of initial nucleons involved
- Need nuSTORM with its accurate flux and series of nuclear targets with high-resolution detector(s).
- Also need at least a good model for pion production which, through FSI, is the main background for QE.
- (QE) measurements calculating  $\underset{\text{Jorge G. Morfin Fermilab}}{\text{E and } Q^2}$  via the muon are in trouble!

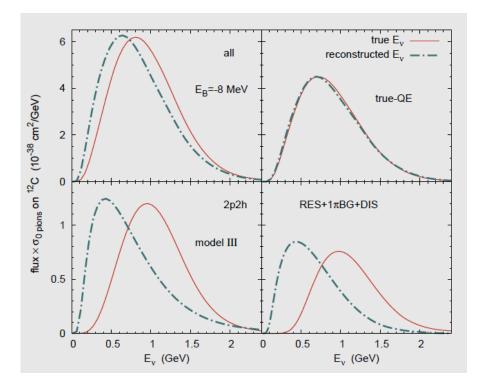
Nuclear Effects can Change the Energy Reconstruction for "QE" Events

In pure QE scattering on a nucleon at rest, the outgoing lepton can determine the neutrino energy:



#### However, not on nuclei.

Reconstructed energy is shifted to lower values for all processes other than true QE off nucleon at rest

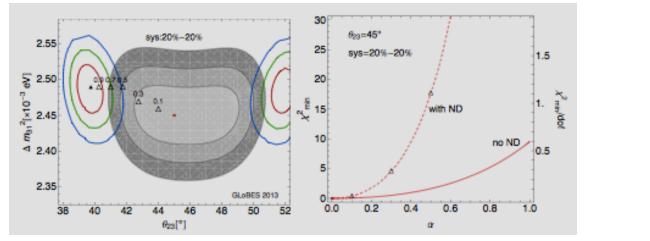


U. Mosel GiBUU

Jorge G. Morfín - Fermilab

# Detailed Study by P. Coloma and P. Huber arXiv 1307.1243

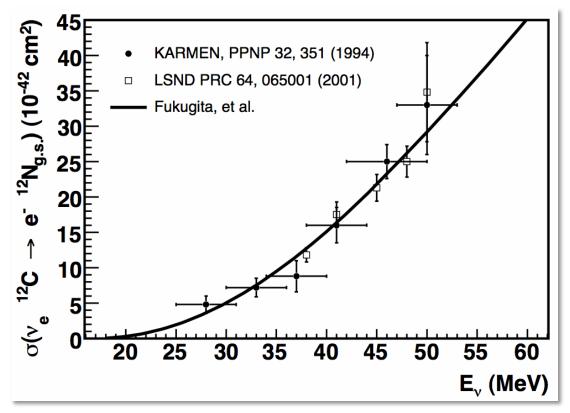
- Disappearance experiment using CC QE-like signal events. T2K 5 years; 850 QE
- QE-like includes pion absorption and scattering off nucleon pairs. 1300 QE-like
- $E_v$  is reconstructed from the observed muon which gives a lower  $E_v$  for non-QE.
- Give a quantitative estimate of this problem using:  $N_i^{\text{test}}(\alpha) = \alpha \times N_i^{QE} + (1 \alpha) \times N_i^{QE-like}$
- $\alpha = 1$  implies completely ignore nuclear effects while  $\alpha = 0$  implies you know/ model the nuclear effects completely.
- The importance of a near detector to help normalize the signal is obvious. However have not yet included different near and far incoming neutrino spectra.
- Even with ND,  $\alpha = 0.3 \rightarrow 1 \sigma$  bias in parameters! Need accurate nuclear model!



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# Example of Existing Data: Carbon $v_e^{12}C \rightarrow e^{-12}N_{g.s.}$

• One of few measurements of spectral shape of  $\sigma$  reflects the upper limit of most existing measurements,  $E \le 50$  MeV.



(Formaggio & Zeller, Rev. Mod. Phys. 2012)