OPTIMIZED SOLENOID BASED CAPTURE MECHANISM FOR A MUON COLLIDER/NEUTRINO FACTORY TARGET SYSTEM

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MAP COLLABORATION MEETING FERMILAB 2013
Muon Capture in Target & Front END

- Capture Solenoid Field Study:
  - Optimizing quantity: Muon (Pions) count – transverse capture
    - Target Solenoid peak field
    - Final end field
  - Optimizing quality: Muon (Pions) longitudinal phase space (transverse-longitudinal coupling) – transverse-longitudinal capture
    - Taper field profile

- Optimizing the time of flight of incident beam (Buncher-Rotator RF phase)
- Transverse focusing field in decay-channel-buncher-rotator
- Match to ionization cooling channel for every end field case 1.5 T → 3.5 T
- Performance of front end as a function of proton bunch length
- Realistic Coil Design & performance optimization
Target System Solenoid:
Capture $\mu^{\pm}$ of energies $\sim 100$-400 MeV from a 4-MW proton beam (E $\sim 8$ GeV).
TARGET SYSTEM CURRENT BASELINE DESIGN

- Production of $10^{14}$ μ/s from $10^{15}$ p/s (≈ 4 MW proton beam)
- Proton beam readily tilted with respect to magnetic axis.
- Shielding of the superconducting magnets from radiation is a major issue.
- Hg Target
- Proton Beam
  - E=8 GeV
- Solenoid Field
  - IDS120h → 20 T peak field at target position (Z=−37.5)
  - Aperture at Target R=7.5 cm - End aperture R = 30 cm
  - Fixed Field Z = 15 m → Bz=1.5 T

- Production: Muons within energy KE cut 40-180 MeV end of decay channel
  - $N_{μ+π+κ}/N_p$=0.3-0.4

5-T copper magnet insert; 10-T Nb3Sn coil + 5-T NbTi outsert. Desirable to eliminate the copper magnet (or replace by a 20-T HTS insert).
TAPERED TARGET SOLENOID OPTIMIZATION

Inverse-Cubic Taper

\[ B_z(0, z_i < z < z_f) = \frac{B_1}{[1 + a_1(z - z_i) + a_2(z - z_i)^2 + a_3(z - z_i)^3]^p} \]

\[ a_1 = \frac{B_1}{pB_1} \quad a_2 = 3\left(\frac{B_1}{B_2}\right)^{1/p} - 1 \quad a_3 = \frac{2a_1}{z_2 - z_1} \quad a_4 = \frac{2B_1}{(z_2 - z_1)^3} + \frac{a_1}{(z_2 - z_1)^2} \]

Off-axis field approximation

\[ B_r(r, z) = \sum_{n} (-1)^{n+1} \frac{a_0^{(2n+1)}(z)}{(n+1)(n)!} \left(\frac{r}{2}\right)^{2n+1} \]

\[ a_0^{(n)} = \frac{d^n a_0}{dz^n} = \frac{d^n B_z(0, z)}{dz^n} \]

Off-axis field approximation

\[ B_z(r, z) = \sum_{n} (-1)^n \frac{a_0^{(2n)}(z)(r^2)}{(n!)^2} \left(\frac{r}{2}\right)^{2n} \]

\[ a_0^{(n)} = \frac{d^n a_0}{dz^n} = \frac{d^n B_z(0, z)}{dz^n} \]

Graphs showing the magnetic field strength \( B_z \) as a function of \( z \) for different taper lengths: 5 m, 15 m, 25 m, and 35 m, with magnetic field strengths of 1.5 T, 2.5 T, and 3.5 T. The graphs are labeled with "Hisham Sayed - MAP meeting 2013."
MARS1510 Simulation:
Counting muons at 50 m with K.E. 80-140 MeV

L_taper [cm]

MARS SIMULATIONS & TRANSMISSION

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6/20/13
LONGITUDINAL PHASE SPACE DISTRIBUTIONS (SHORT VERSUS LONG TAPER)

End of taper

Long adiabatic taper 40 m

End of Decay

Short taper 4 m

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**Phase Space Distributions (Short versus Long Taper)**

T-Pz Correlations at end of decay channel

Long Solenoid taper:
- More particles
- More dispersed (misses the buncher acceptance windows)

Short Solenoid taper:
more condensed distributions that fits more particles within the buncher acceptance windows

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**Long Taper**

**Short Taper**
T-Pz phase space at end of decay channel

Long Taper 40 m

- More particles
- More dispersed (misses the buncher acceptance windows)

Short Taper 4 m

- Higher density t-pz distribution
- Fits more particles within the acceptance of buncher/rotator

Long Solenoid taper:

Short Solenoid taper:
PHASE SPACE - SHORT VERSUS LONG TAPER

T-Pz Correlations at end of decay channel of good particles

Green: Initial distribution of good particles which were bunched and cooled in 4D cooling channel.
Performance dependence on time of flight (RF phase)

- MARS1015 2012
- OLD
- OLD

Muons/protons at z = -200 cm

TOA vs. End n1 Ltaper=8 m B=20-1.5T

Muons+/protons at z = -75 cm

- Optimizing RF Phase

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Using baseline cooling section
(140 cooling cell)

Using longer cooling section
(200 Cooling cell)

High statistics tracking of Muons through the front end
Using longer cooling section (200 Cooling cell)

High statistics tracking of Muons through the front end
Muon yield versus end field

Bunch length=0 nsec

Bz(Target)=20 T

20% for every 1 T increase in constant field

Baseline

Constant Bz [T]

0.16
0.155
0.15
0.145
0.14
0.135
0.13
0.125
0.12
0.115

Muon yield versus Proton Bunch Length

Bz(Target)=15 T
Bz(Target)=20 T

~ 3% loss per 1 nsec increase in bunch length

Proton Bunch Length [nsec]

0
0.5
1
1.5
2
2.5
3

Muon yield versus end field & Bunch Length

Performance of FE as function of Constant solenoid filed in Decay Channel – Buncher – Rotator (matched to +/- 2.8 T ionization cooling channel)
New Short Target Capture Realistic Magnet (Weggel)

Muon Target Capture Magnet
Short Taper length = 7 m - B = 20-1.5 T

Muon Target Capture Magnet
Short Taper length = 5 m - B = 20-2.5 T
NEW SHORT TARGET CAPTURE MAGNET (WEGGEL)

Muon Target Short Taper Magnet taper length = 7 m - B=20-1.5 & 2.5 T

Target SC Magnets Field Map calculated from realistic coils

Engineering (V. Grave)
IDS120_20-1.5T7m2+5 Cryo 1
NEW DECAY CHANNEL REALISTIC MAGNET (WEGGEL)

- The pions produced in the target decay to muons in a Decay Channel (50 m)
- Three superconducting coils (5-m-long) $B_z(r=0) \sim 1.5$ or $2.5$ T solenoid field.
- Suppress stop bands in the momentum transmission.

Axial-field profile of two Decay-Channel modules

<table>
<thead>
<tr>
<th>Magnet</th>
<th>Length [m]</th>
<th>Inner R [m]</th>
<th>Outer R [m]</th>
<th>$J$ [A/mm$^2$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.19</td>
<td>0.6</td>
<td>0.68</td>
<td>47.18</td>
</tr>
<tr>
<td>2</td>
<td>3.8</td>
<td>0.6</td>
<td>0.63</td>
<td>40.00</td>
</tr>
<tr>
<td>3</td>
<td>0.19</td>
<td>0.6</td>
<td>0.68</td>
<td>47.18</td>
</tr>
</tbody>
</table>

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REALISTIC COIL BASED DECAY CHANNEL SOLENOID STOP BAND STUDY

Suppression of stop bands in the Decay Channel:
Tracking muons through decay channel 10 cells (50 m) optimize magnet design for best performance

Transmission:
- Constant 1.5 Solenoid Field: 67%
- IDS120L20to1.5T7m: 62%
- Modified IDS120L20to1.5T7m: 66%

IDS120L20to1.5T7m

Optimization

IDS120L20to1.5T7m

1.5 T constant solenoid field
Field generated from Coils

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6/21/13
CONCLUSION & SUMMARY

1- Target Solenoid parameters that affect the particle Capture & Transmission at target or after cooling
   
   Initial peak Field – Taper length – End Field

2- Impact:
   Short taper preserves the longitudinal phase-space → muons can be captured efficiently in the buncher-phase rotation sections and more muons at the end of cooling.
   The maximum yield requires taper length of 7-5 m for all cases (20-15T) (1.5-3.5T) for any bunch length.

3- Final constant end field increases the yield by 20% for every 1 T increase in the field beyond the 1.5 T baseline

4- Initial proton bunch length influence the muon/proton yield at the end of the cooling channel
   ~ 3% reduction per 1 nsec increase in bunch length.

5- Realistic Coil design.