

Taking the Muon for a Spin

Thomas Gadfort
Fermilab
47th FNAL Users Meeting

- Spin and the Muon Anomalous Magnetic Moment
- Measuring a_μ with Polarized Muons
- The BNL Result and Goals for Fermilab Muon g-2
- Last Summer and This Summer's Big Move

Spin and Its Observable Effects



● In the Standard Model (SM), the **muon** is a point-like spin $1/2$ particle.

● With spin comes a magnetic dipole moment (MDM) of strength:

$$\vec{\mu} = g \frac{q}{2m} \vec{s}$$

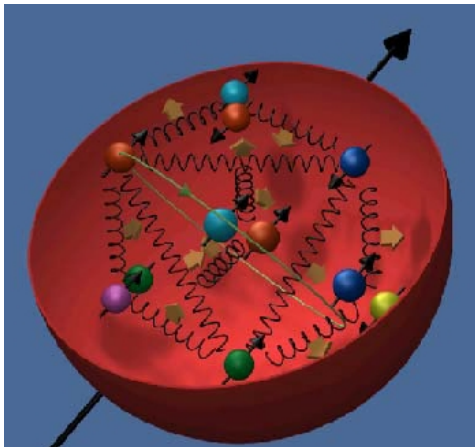


The Quantum Theory of the Electron.

By P. A. M. DIRAC, St. John's College, Cambridge.

● Dirac showed that **$g = 2$** for the electron as observed.

● The 1930's and 40's saw several breakthrough measurements of the g -factor that lead to a new understanding of particles and substructure.



$g_p \approx 5.6, g_n \approx -3.8$
 → nucleon substructure

Phys. Rev. 72 (1947)

Precision Measurement of the Ratio of the
 Atomic ' g Values' in the $^2P_{3/2}$ and
 $^2P_{1/2}$ States of Gallium*
 P. KUSCH AND H. M. FOLEY
 Columbia University, New York, New York
 November 3, 1947

$$g_e = 2.00229(8) \approx 2(1 + \alpha/2\pi)$$

→ QM corrections

Spin and Its Observable Effects



🌐 In the Standard Model (SM), the **muon** is a point-like spin $\frac{1}{2}$ particle.

🌐 With spin comes a magnetic dipole moment (MDM) of strength:

$$\vec{\mu} = g \frac{q}{2m} \vec{s}$$

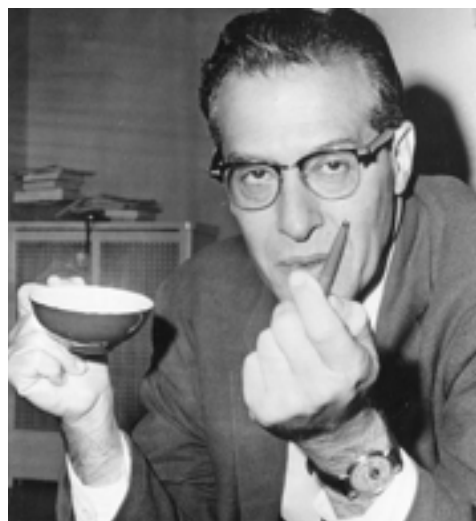


The Quantum Theory of the Electron.

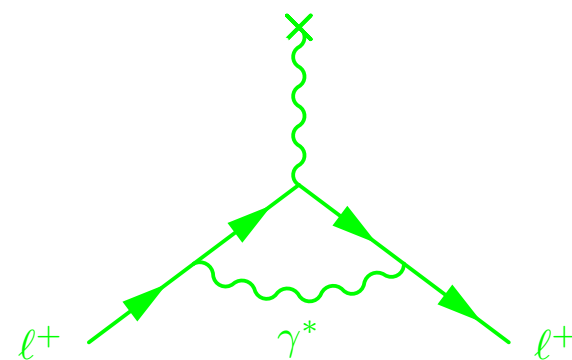
By P. A. M. DIRAC, St. John's College, Cambridge.

🌐 Dirac showed that **$g = 2$** for the electron as observed.

🌐 The 1930's and 40's saw several breakthrough measurements of the g -factor that lead to a new understanding of particles and substructure.



$$g_e = 2\left(1 + \frac{\alpha}{2\pi}\right) \approx 2.00232$$



Precision Measurement of the Ratio of the Atomic ' g Values' in the $^2P_{3/2}$ and $^2P_{1/2}$ States of Gallium*

P. KUSCH AND H. M. FOLEY
Columbia University, New York, New York
November 3, 1947

$$g_e = 2.00229(8) \approx 2\left(1 + \frac{\alpha}{2\pi}\right)$$

D. Hanneke, S. Fogwell, and G. Gabrielse
PRL 100, 120801 (2008)

$$g_e/2 = 1.001\,159\,652\,180\,73(28)$$

→ QM corrections

Understanding The Muon



- There is a rich history of muon g -factor measurements starting in the 1950's at Nevis.

$$g_\mu = 2(10\%)$$

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

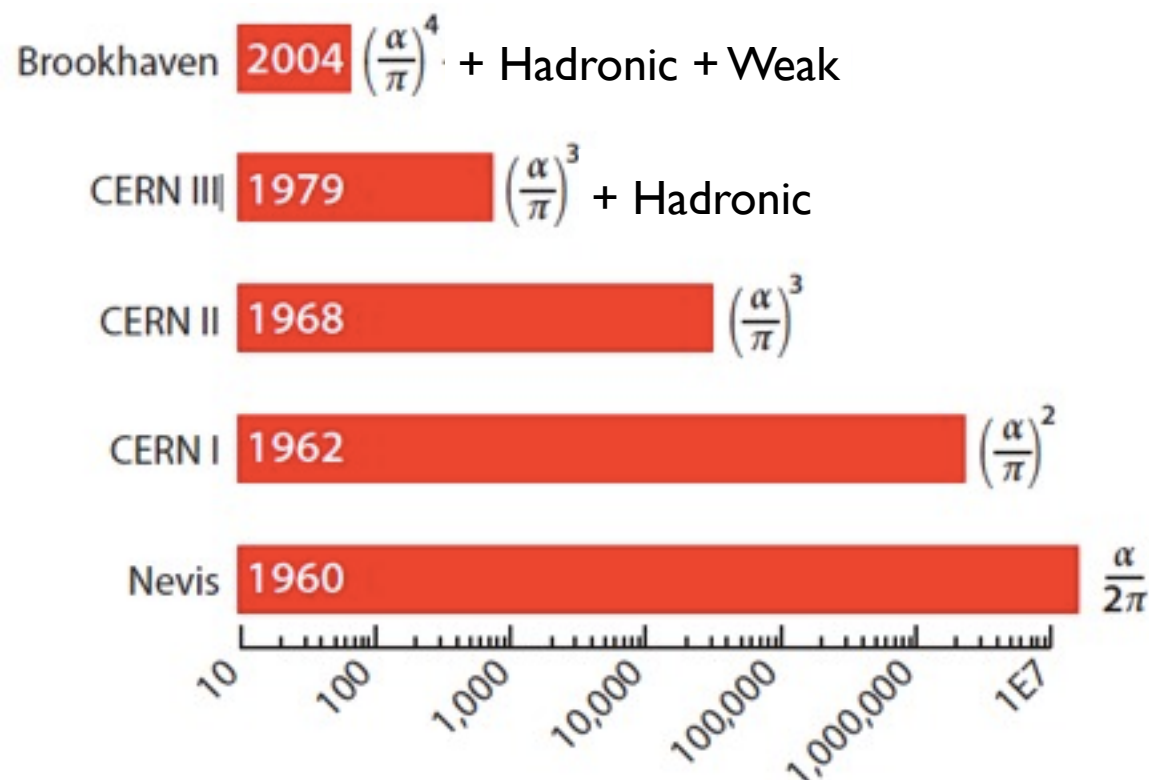
Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)

- Evidence that the muon is a fundamental particle.

- The past 50 years have seen dramatic improvements in precision and experimental techniques.



Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_\mu = 2(10\%)$$

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

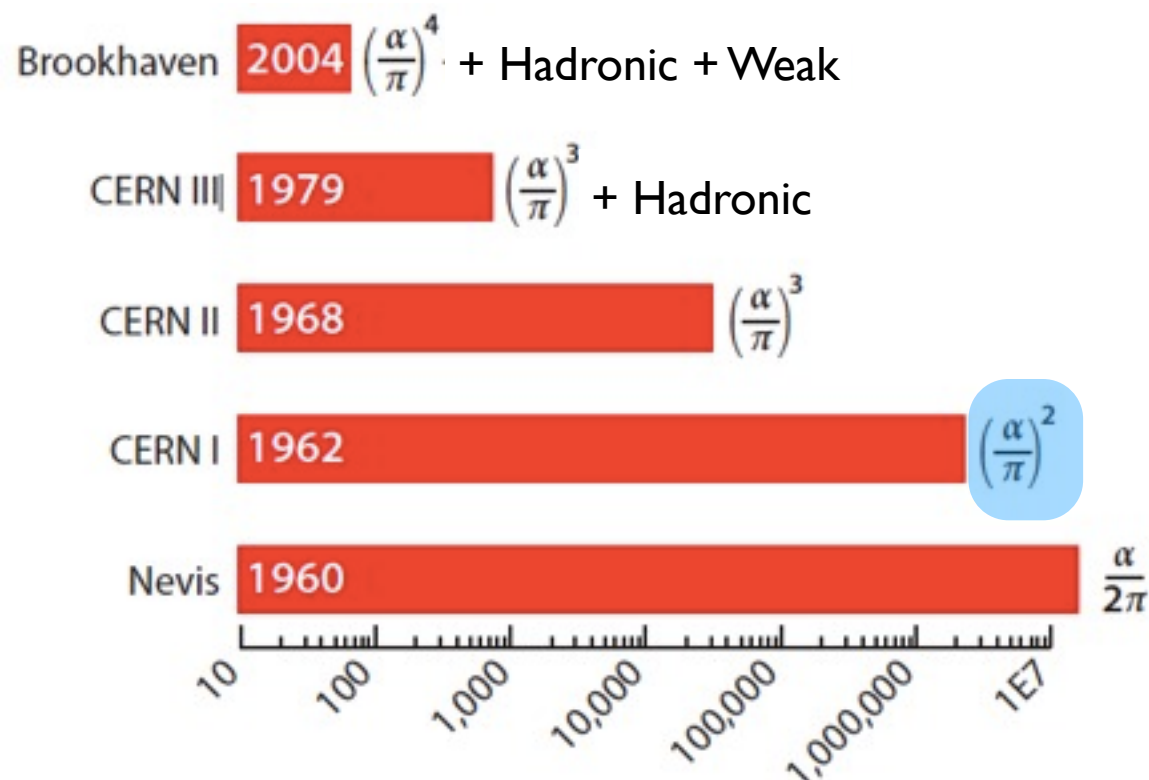
Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)

- Evidence that the muon is a fundamental particle.

- The past 50 years have seen dramatic improvements in precision and experimental techniques.



CERN I



Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

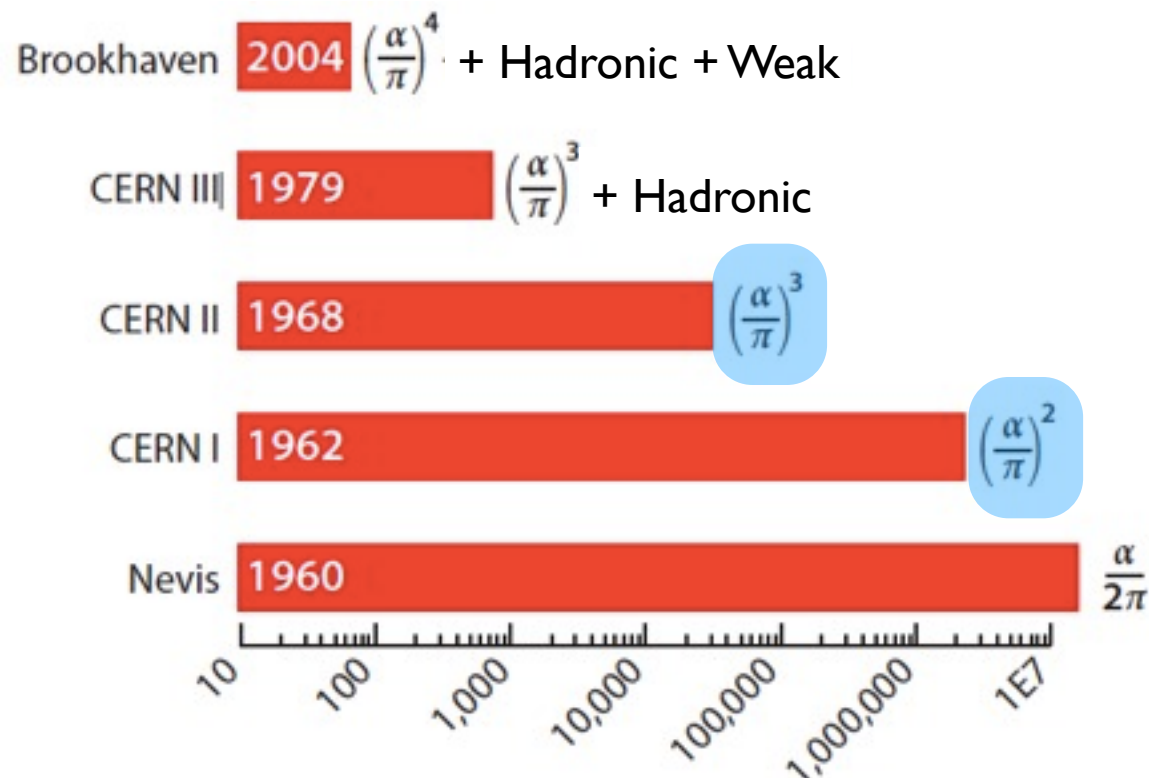
Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)

- Evidence that the muon is a fundamental particle.

- The past 50 years have seen dramatic improvements in precision and experimental techniques.



CERN I



CERN II



Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

- Evidence that the muon is a fundamental particle.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.

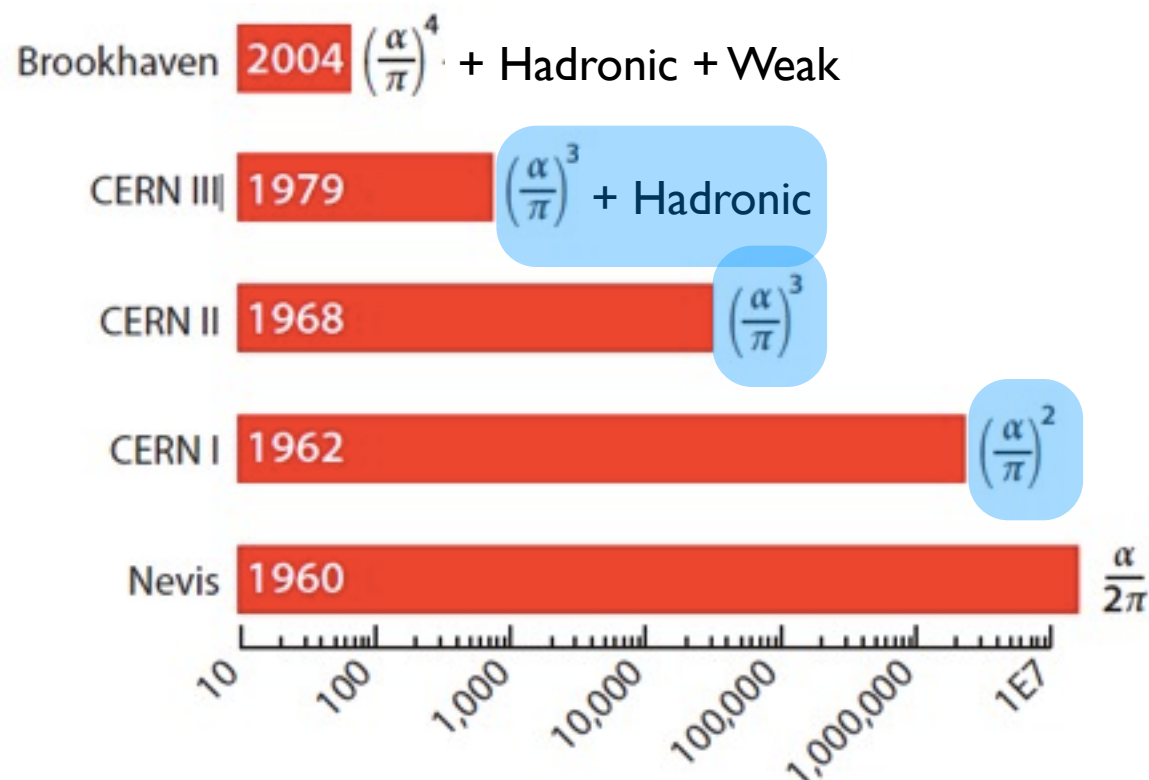
Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)



CERN I



CERN III



CERN II



Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

- Evidence that the muon is a fundamental particle.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.

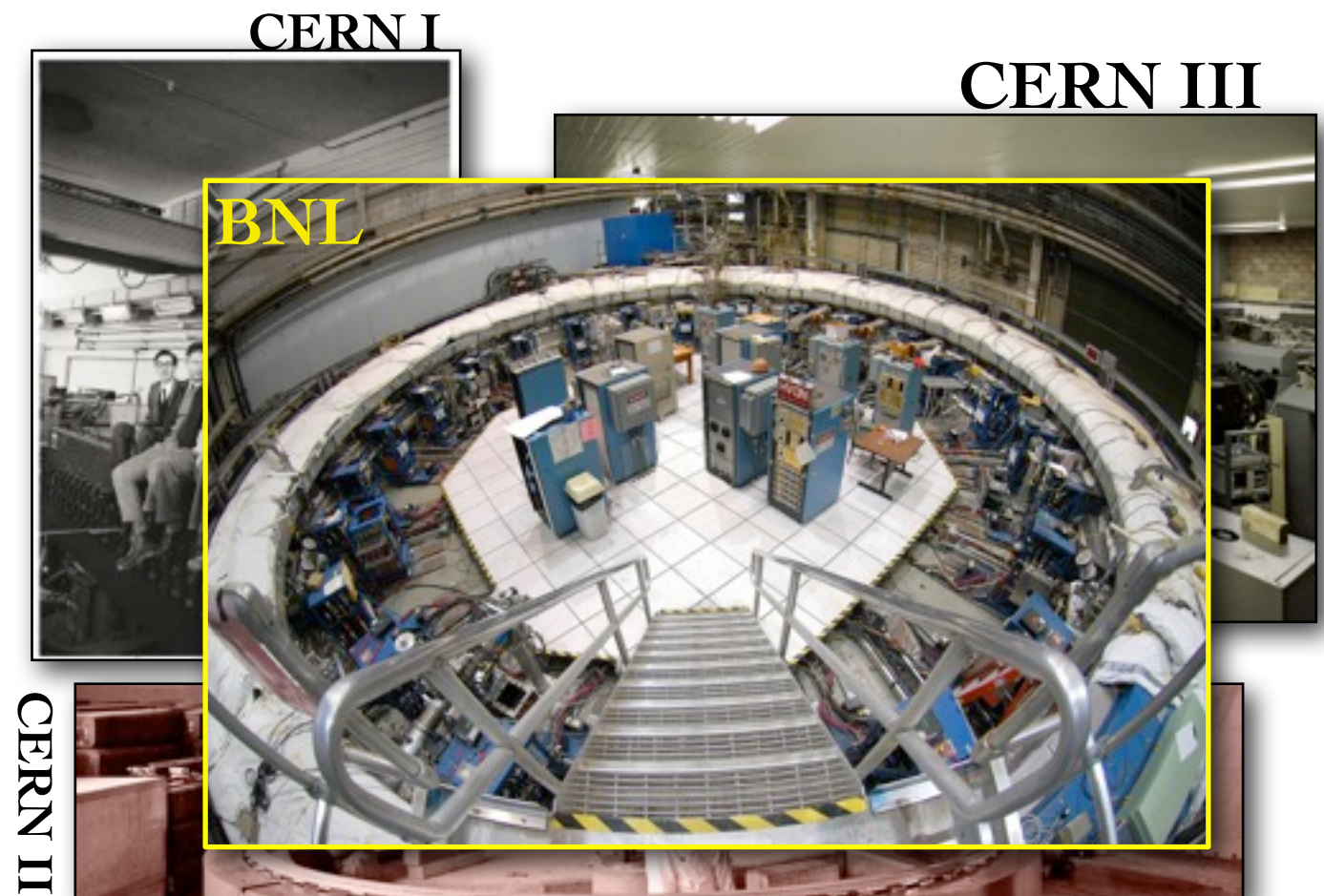
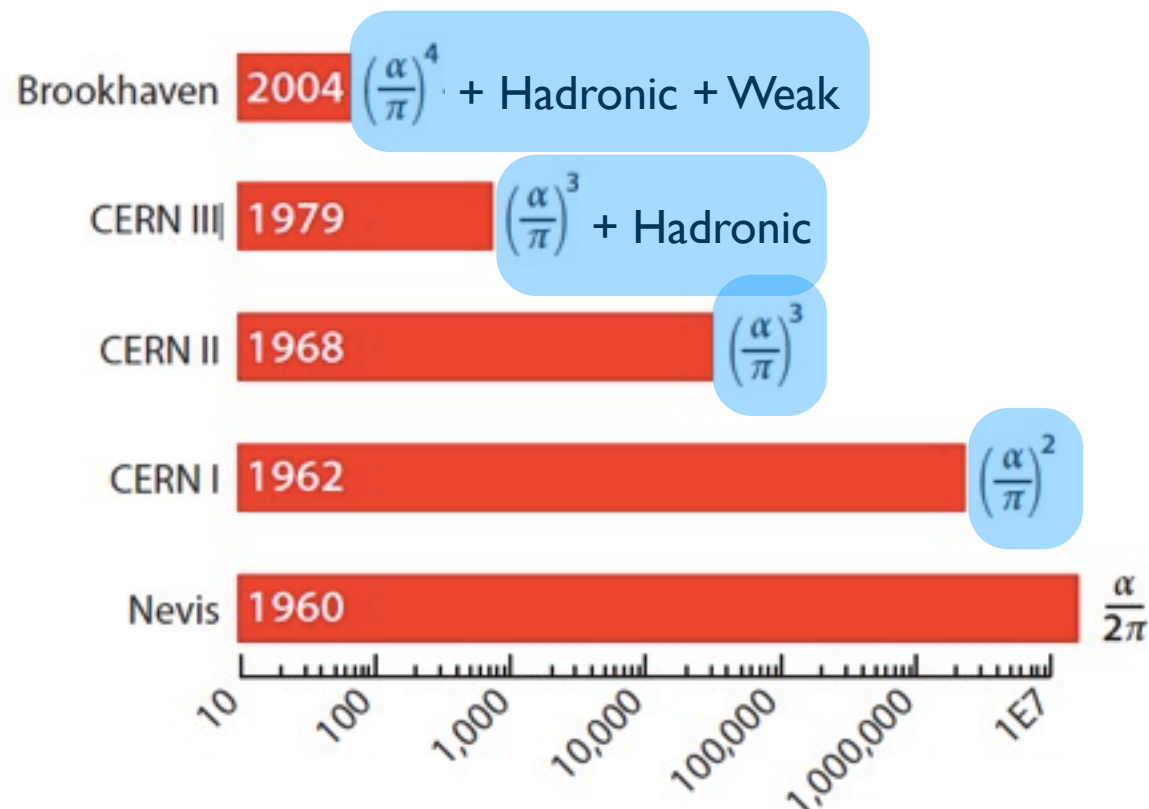
Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)



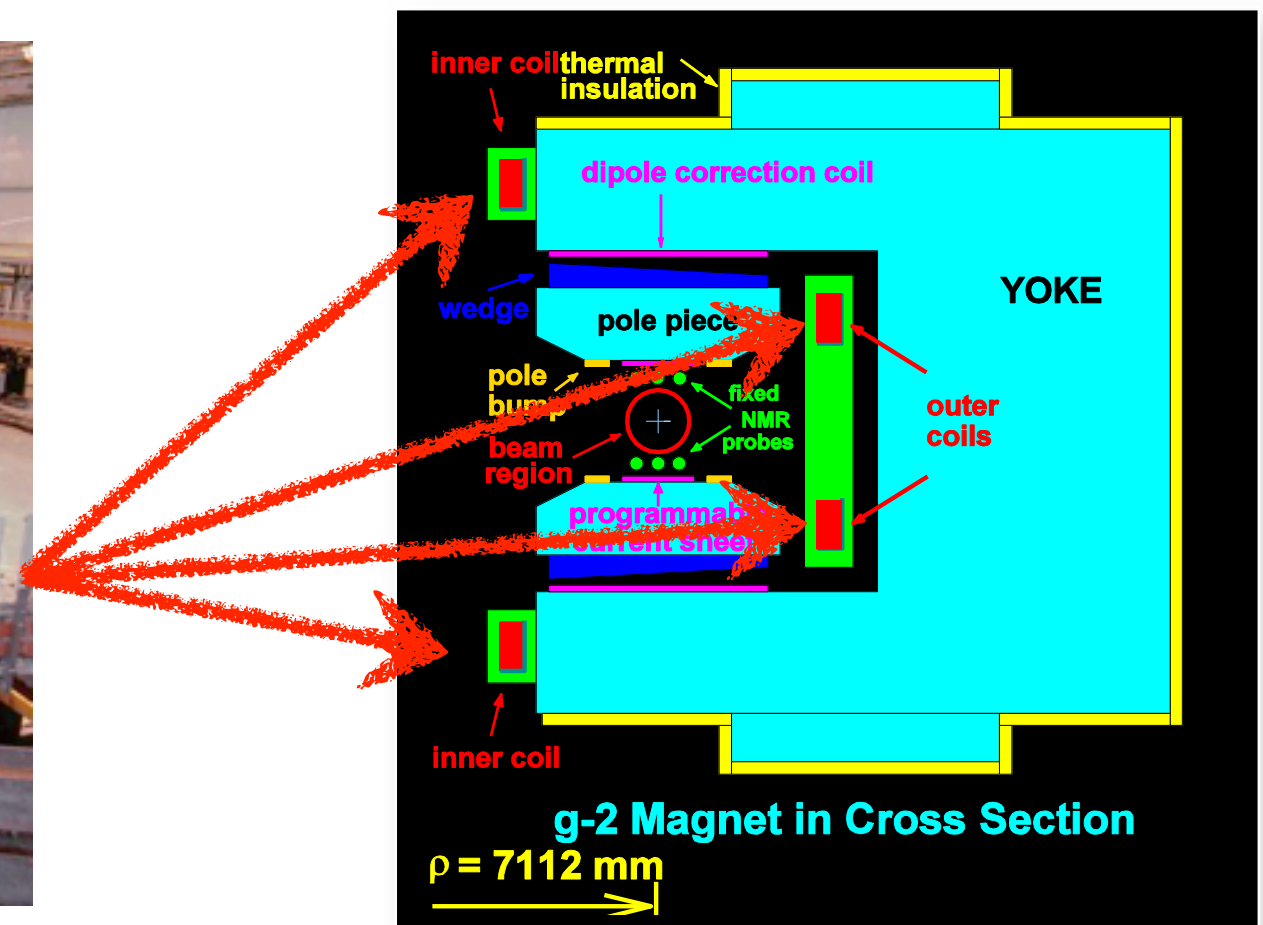
E821 Brookhaven Muon g-2



- Muon injection greatly improved statistics.
- Continuously wound superconducting (SC) main magnet coils + tunable shimming kit
→ Reduced multipole field terms.



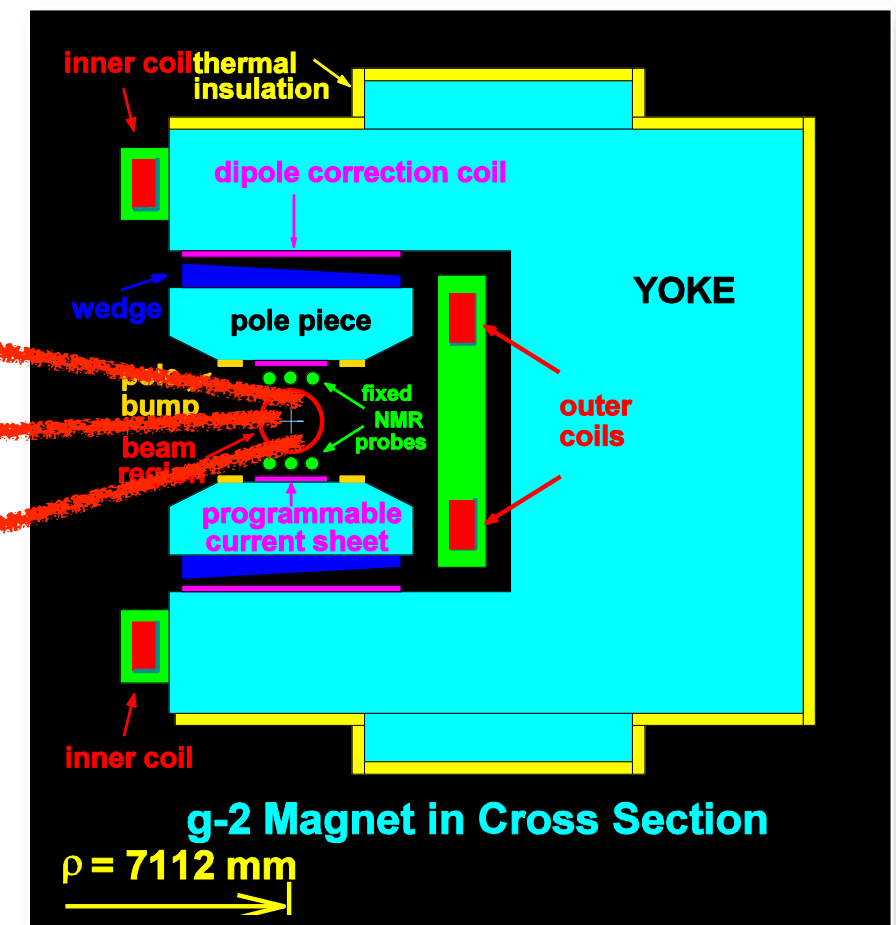
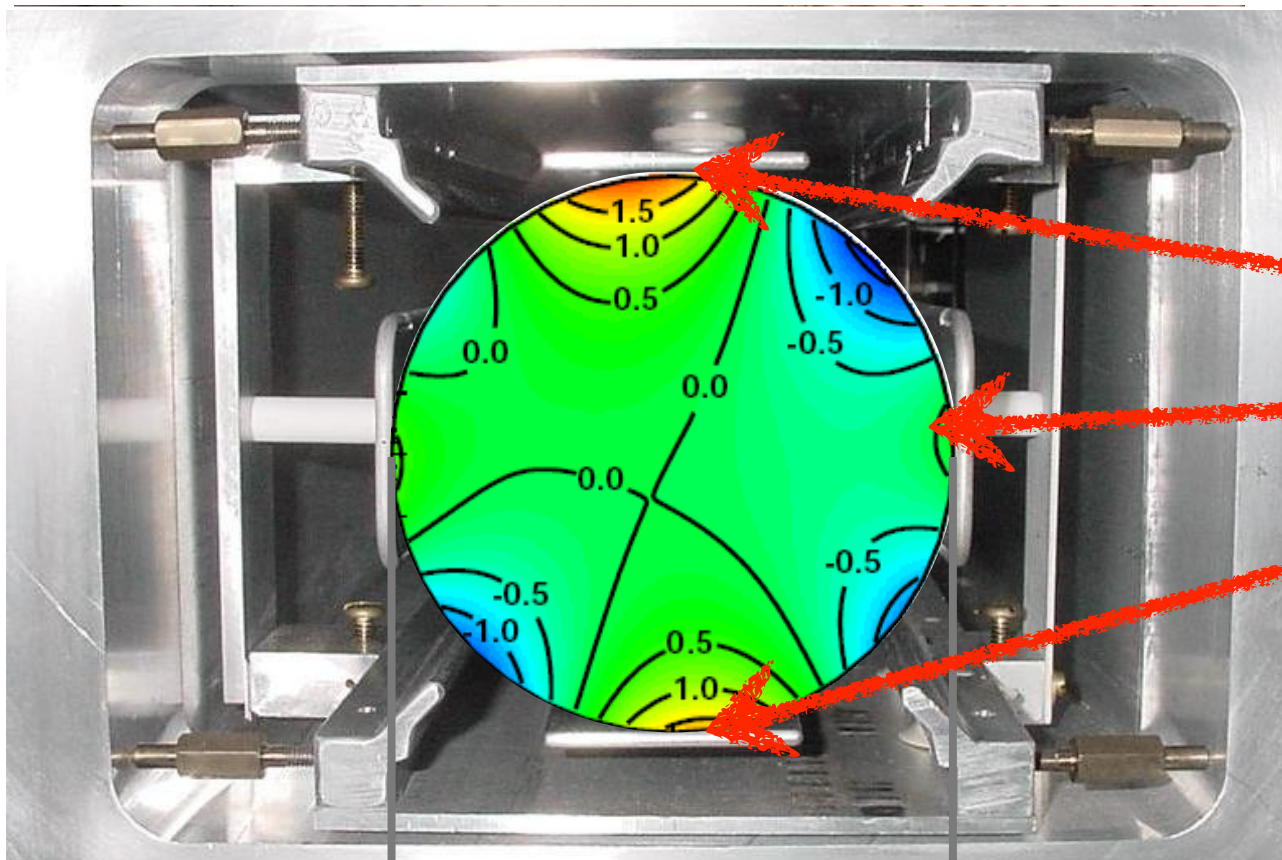
Superconducting coil winding



E821 Brookhaven Muon g-2



- Muon injection greatly improved statistics.
- Continuously wound superconducting (SC) main magnet coils + tunable shimming kit
→ Reduced multipole field terms.
- Dramatic improvement in field uniformity
Contours in [ppm]!



Storage Ring Measurement Technique (I)



In a dipole magnetic field:

Muon momentum revolution frequency, ω_C

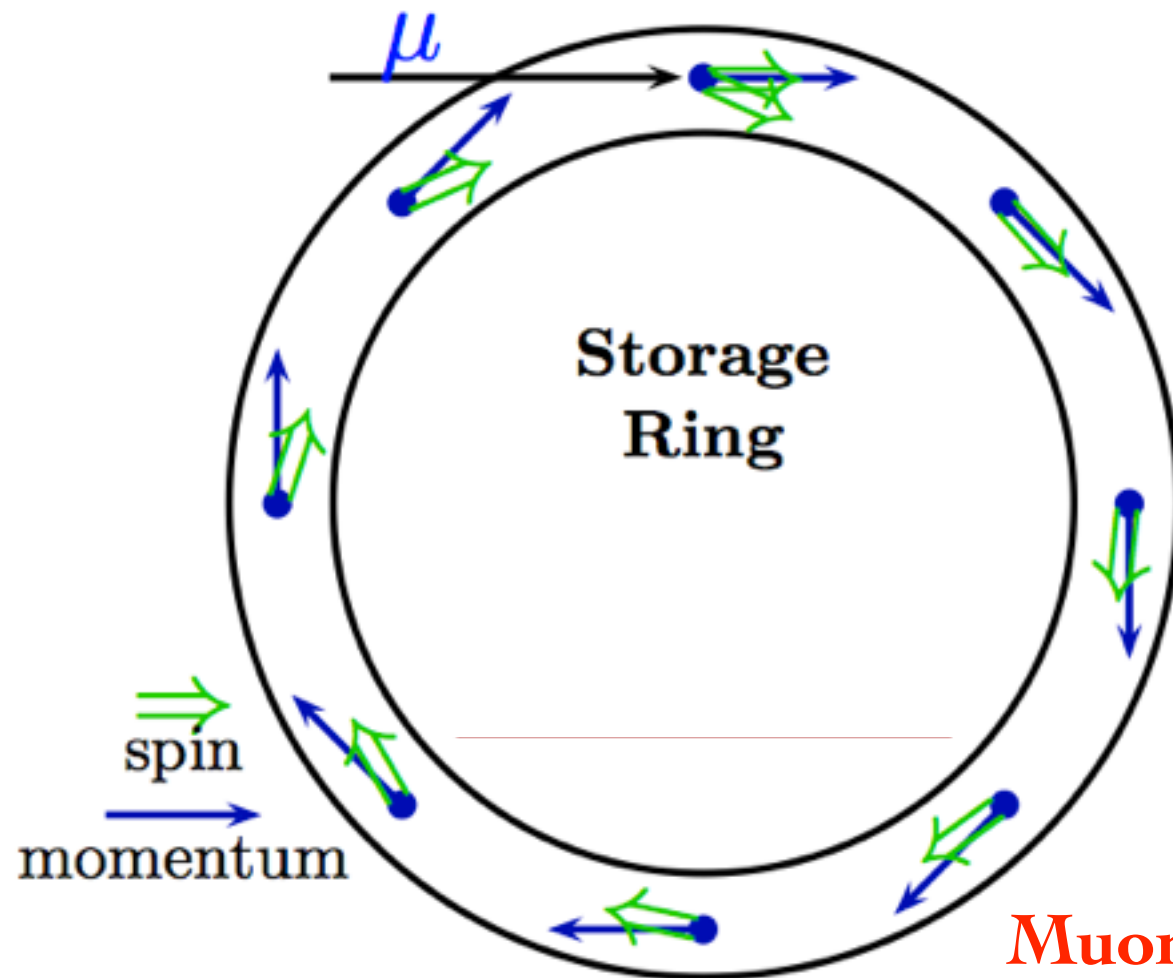
$$\omega_C = \frac{eB}{mc\gamma}$$

Muon spin revolution frequency, ω_S

$$\omega_S = \frac{geB}{2mc\gamma} + (1 - \gamma) \frac{eB}{mc\gamma}$$

Muon anomaly revolution frequency, ω_a

$$\omega_a \equiv \omega_S - \omega_C = \left(\frac{g - 2}{2} \right) \frac{eB}{mc} = a_\mu \frac{eB}{mc}$$

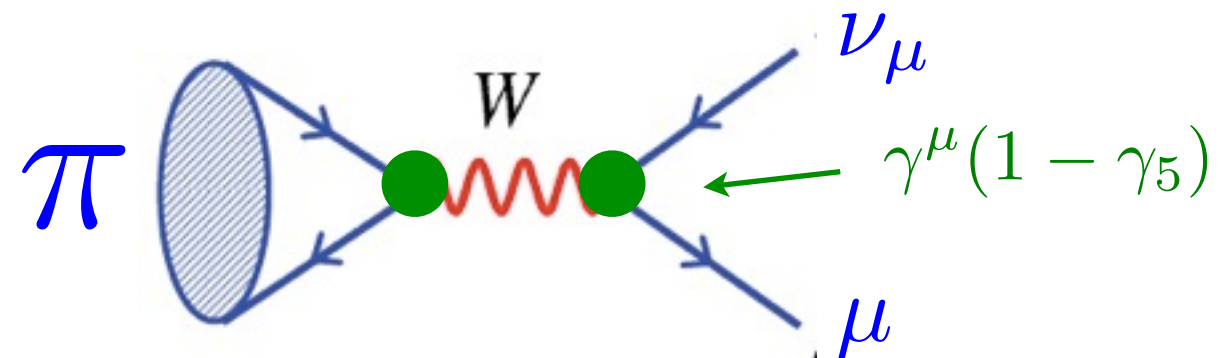


Storage Ring Measurement Technique (II)



Source of
Polarized Muons

Lucky break from parity violation

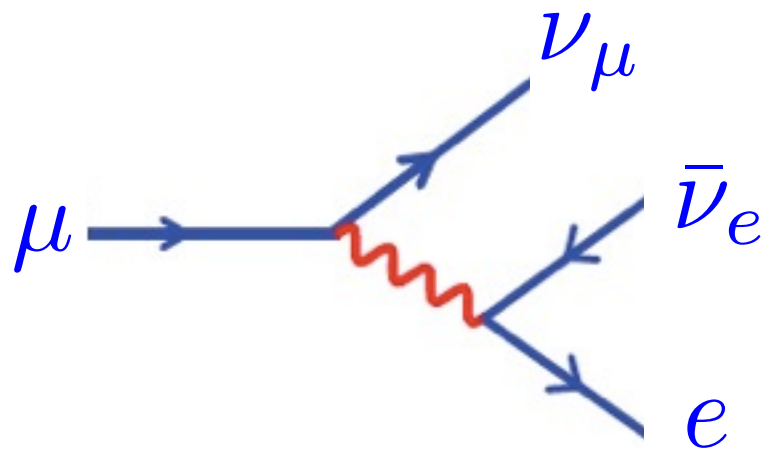


Measure Muon Spin

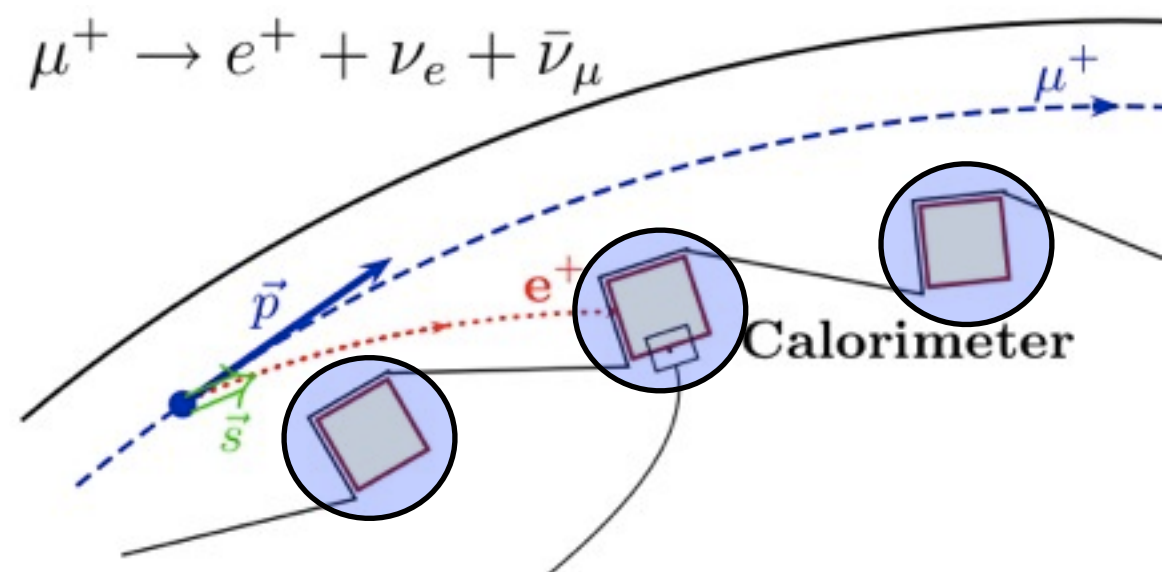


Measure Positron Energy

Weak decay correlates
muon spin and electron momentum



Highest energy positrons when spin
and momentum are aligned.

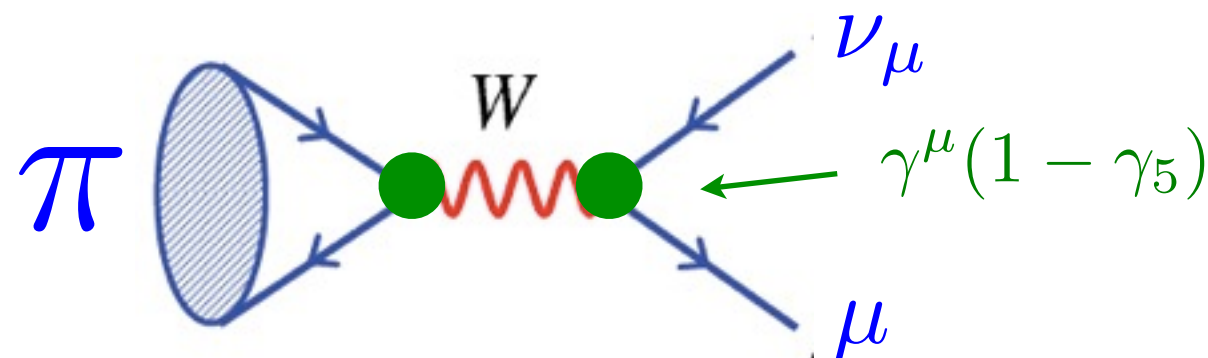


Storage Ring Measurement Technique (II)



Source of
Polarized Muons

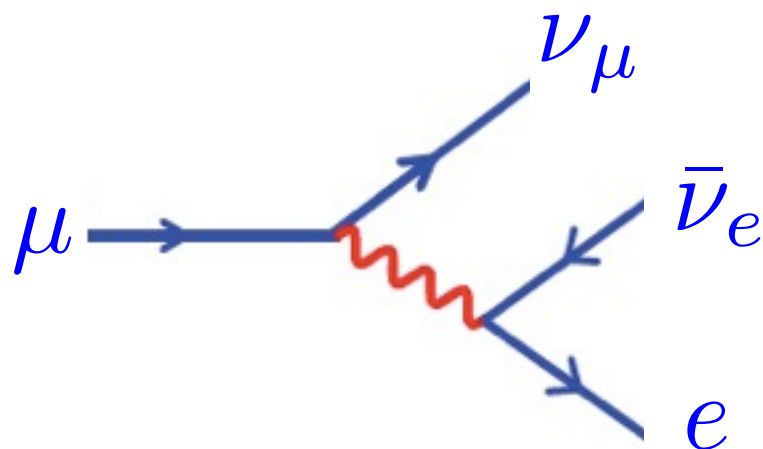
Lucky break from parity violation



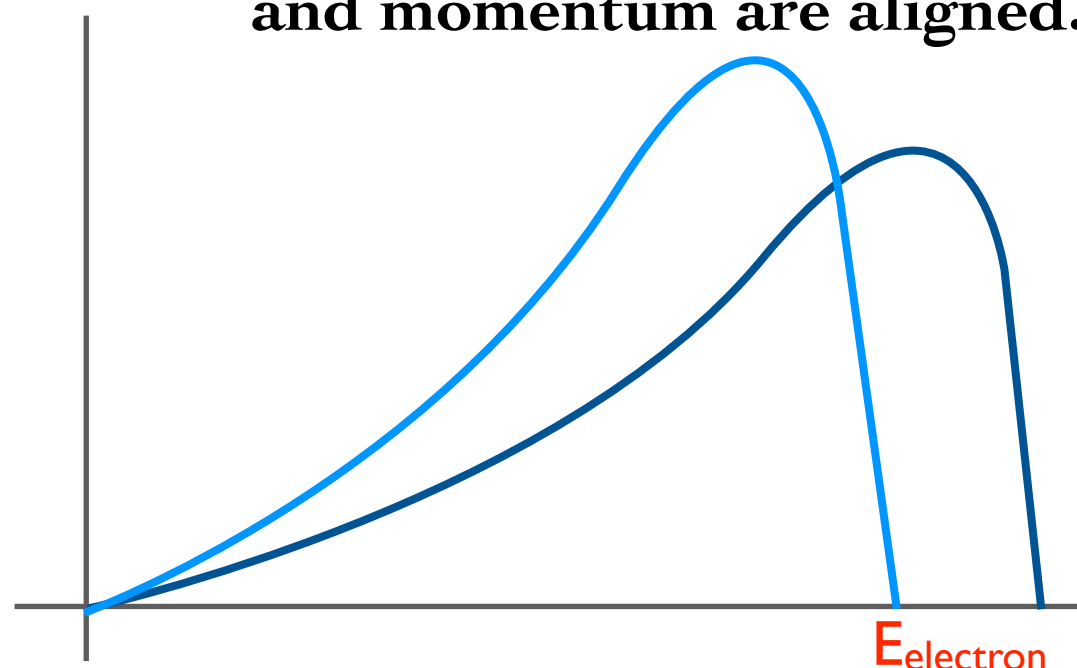
Measure Muon Spin

Measure Positron Energy

Weak decay correlates
muon spin and electron momentum



Highest energy positrons when spin
and momentum are aligned.

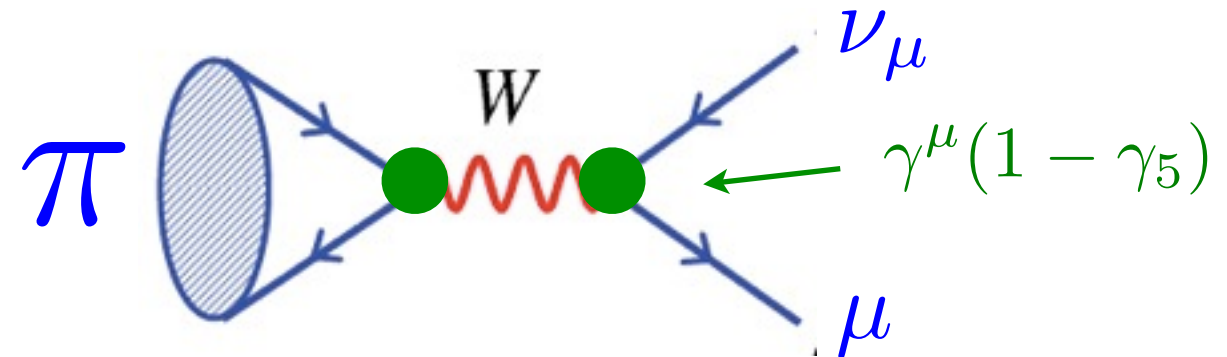


Storage Ring Measurement Technique (II)



Source of
Polarized Muons

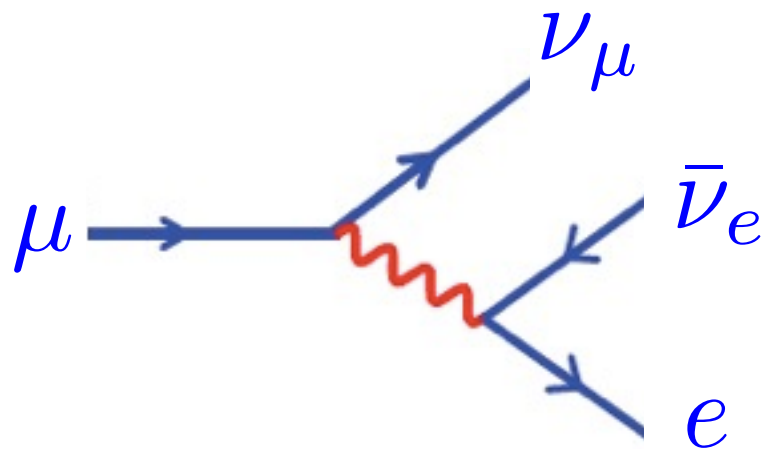
Lucky break from parity violation



Measure Muon Spin

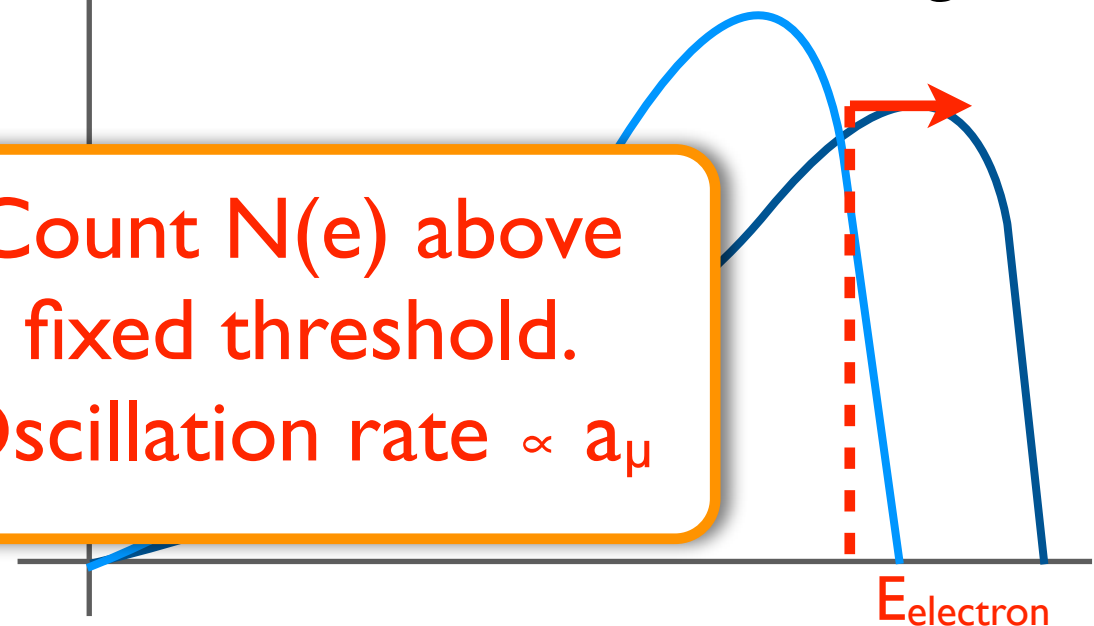
Measure Positron Energy

Weak decay correlates
muon spin and electron momentum



Highest energy positrons when spin
and momentum are aligned.

Count $N(e)$ above
fixed threshold.
Oscillation rate $\propto a_\mu$



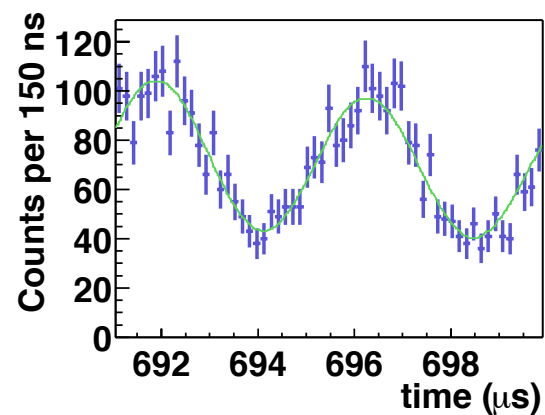
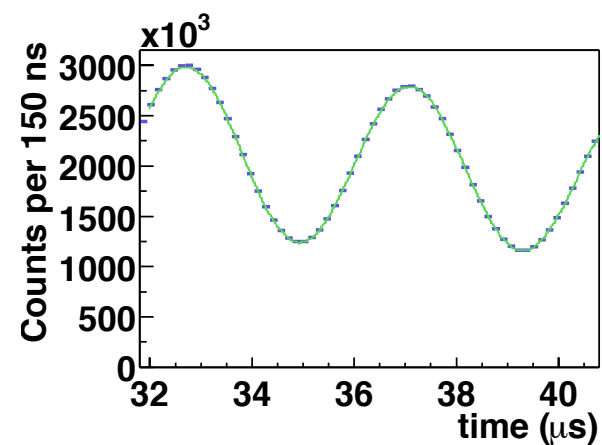
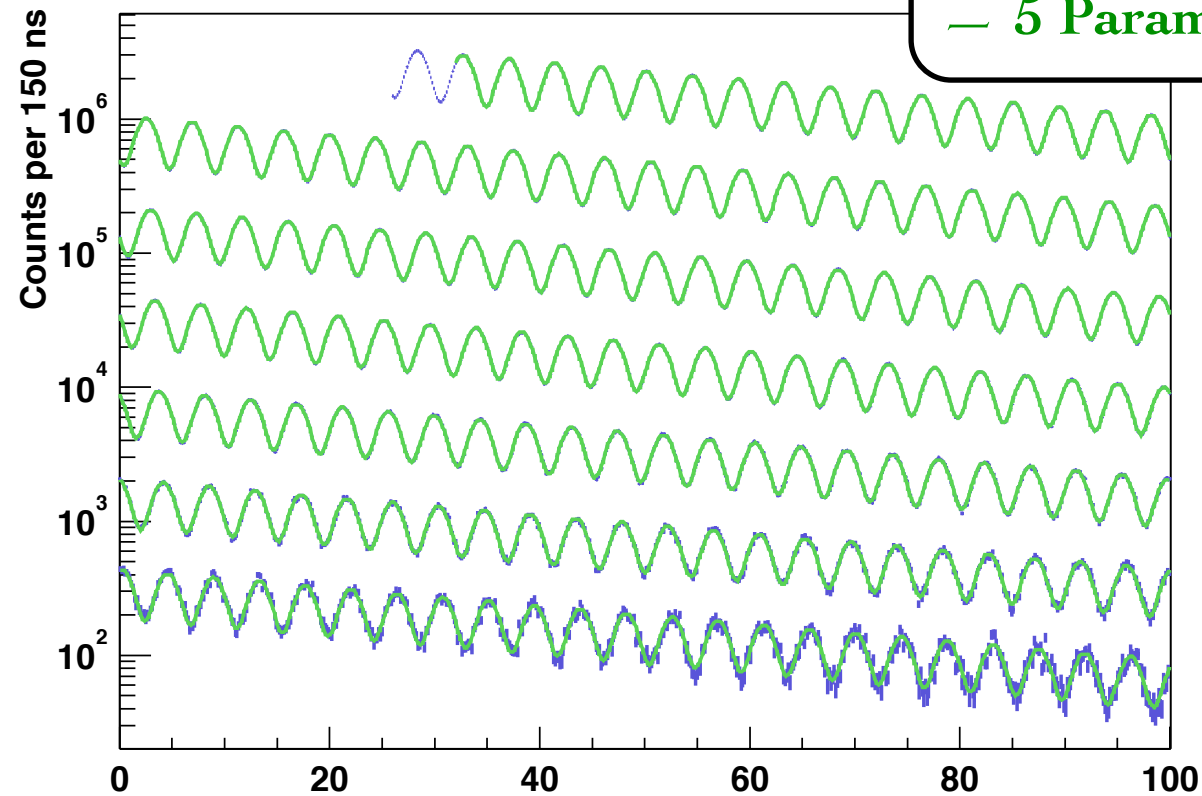
The Wiggle Plot, ω_a , ω_p , and a_μ



E821 data

• Data
— 5 Param Fit

$$N(t) = N_0 e^{-\frac{t}{\gamma\tau}} [1 + A \cos(\omega_a t + \phi)]$$



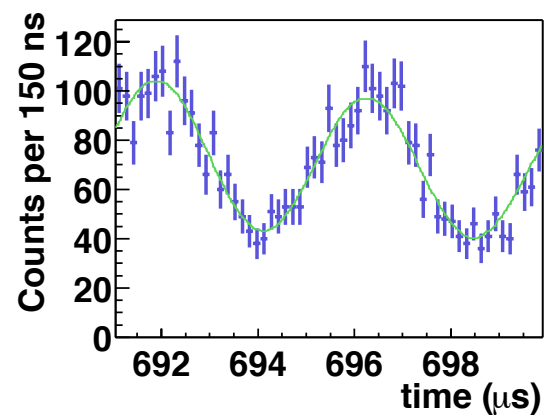
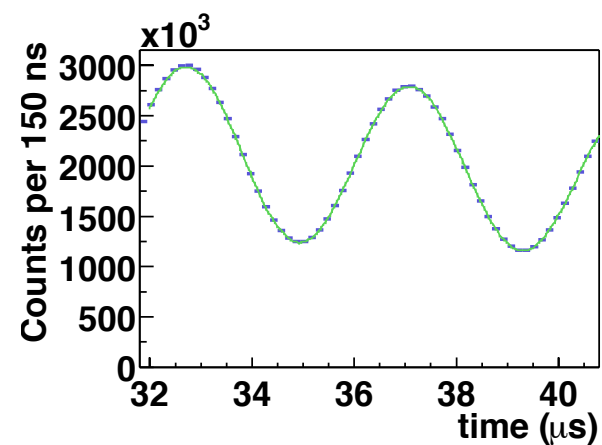
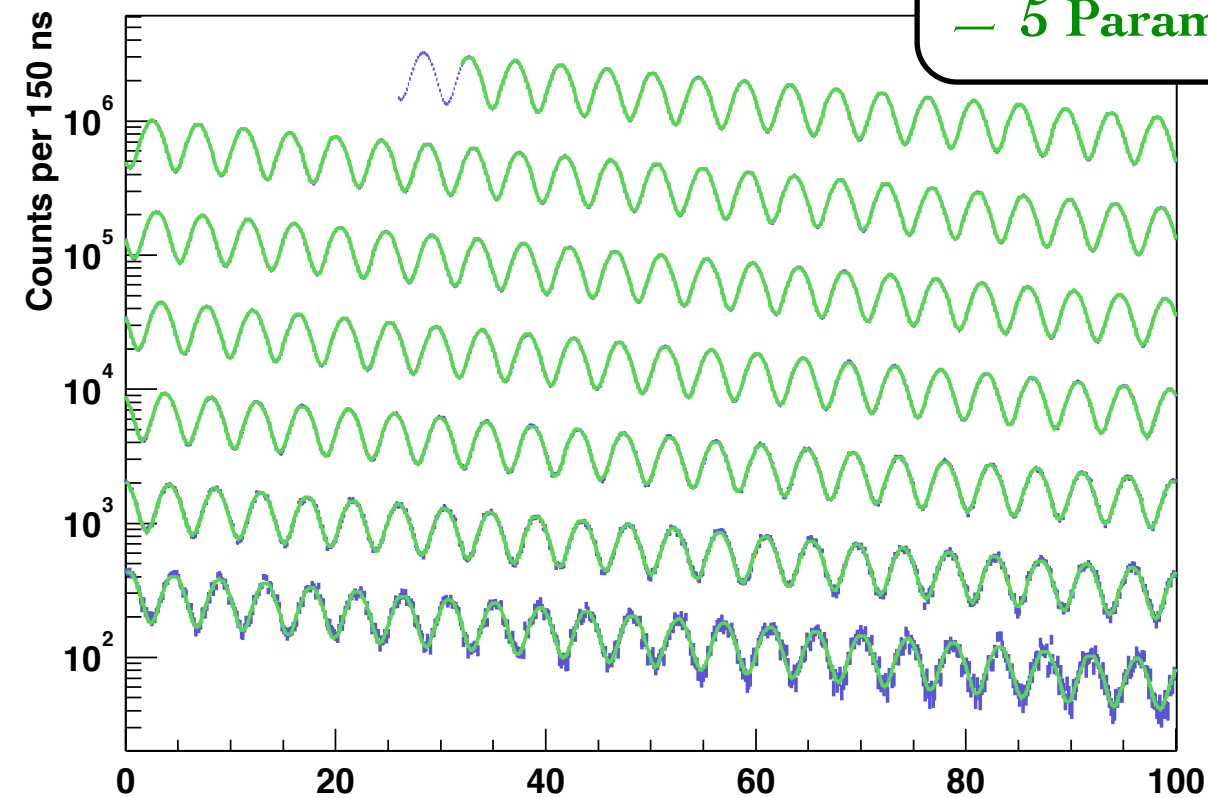
4 billion muon decays
($\approx 15\%$ yield > 1.8 GeV positrons)

The Wiggle Plot, ω_a , ω_p , and a_μ



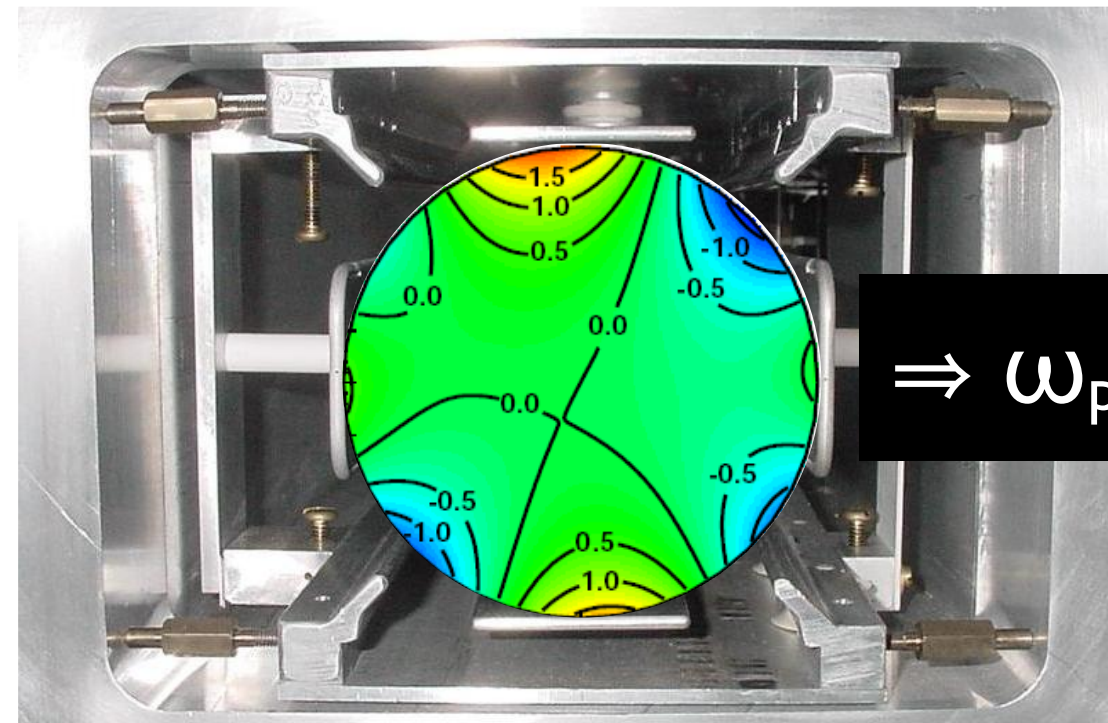
E821 data

• Data
— 5 Param Fit



$$N(t) = N_0 e^{-\frac{t}{\gamma\tau}} [1 + A \cos(\omega_a t + \phi)]$$

+



$\Rightarrow \omega_p (\langle B \rangle)$

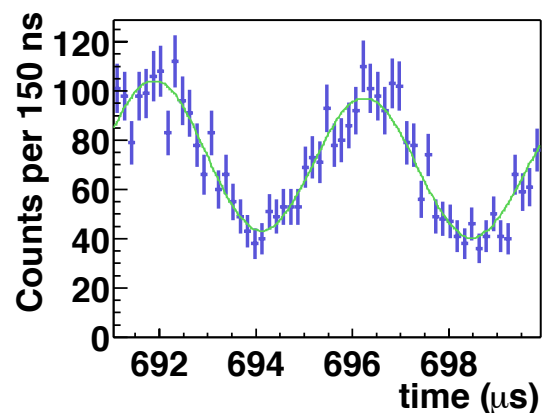
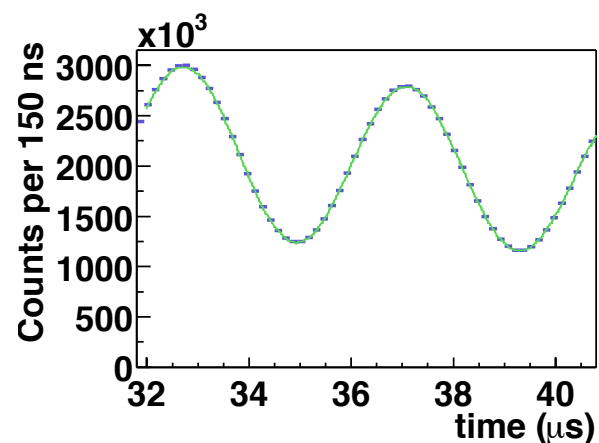
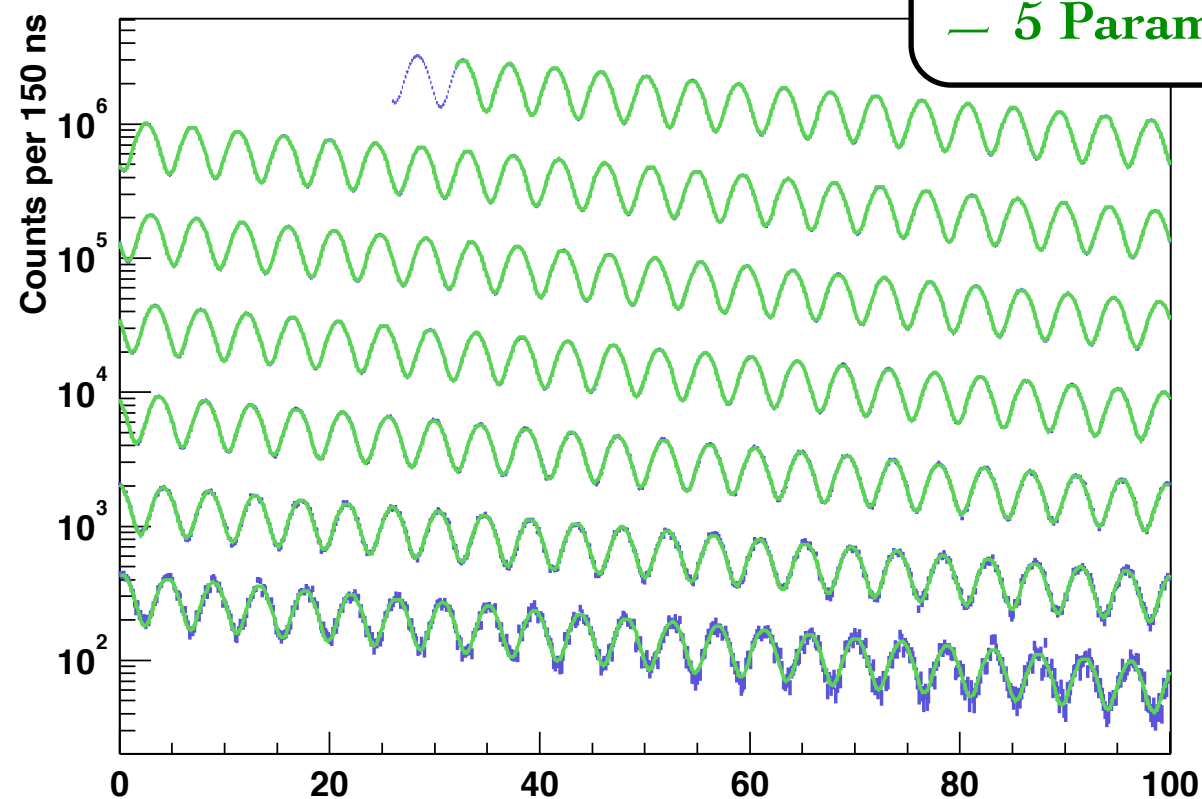
4 billion muon decays
($\approx 15\%$ yield > 1.8 GeV positrons)

The Wiggle Plot, ω_a , ω_p , and a_μ



E821 data

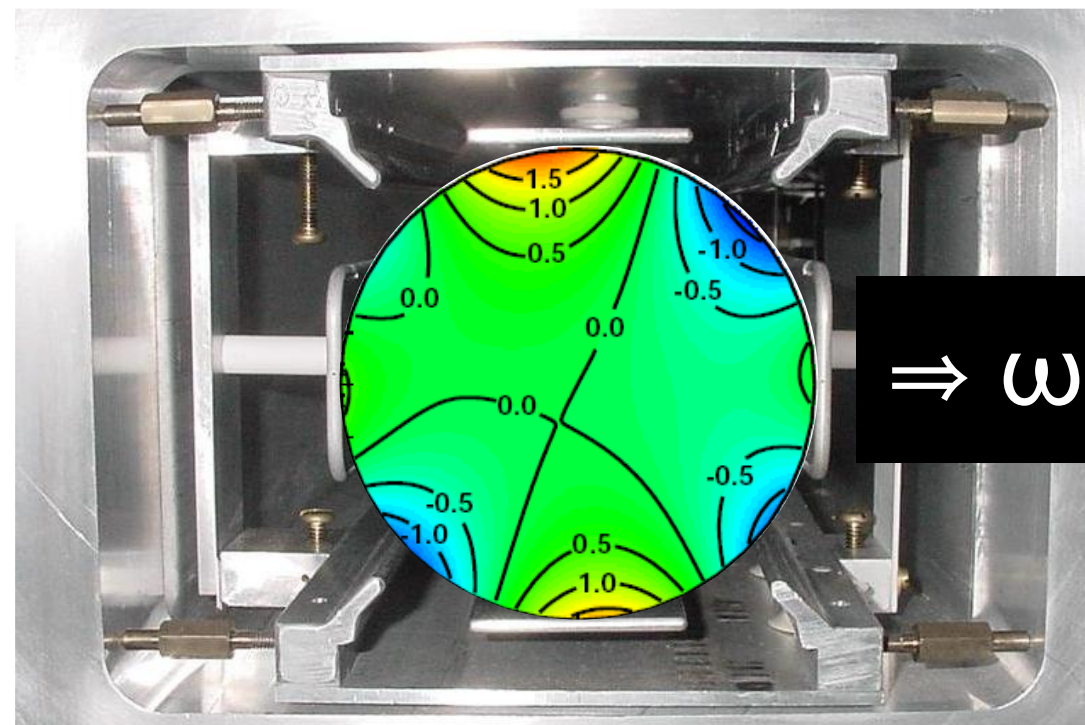
• Data
— 5 Param Fit



4 billion muon decays
($\approx 15\%$ yield > 1.8 GeV positrons)

$$N(t) = N_0 e^{-\frac{t}{\gamma\tau}} [1 + A \cos(\omega_a t + \phi)]$$

+



$\Rightarrow \omega_p (\langle B \rangle)$

Add prior knowledge...

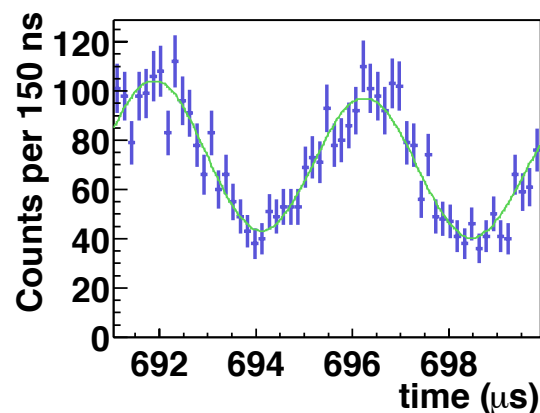
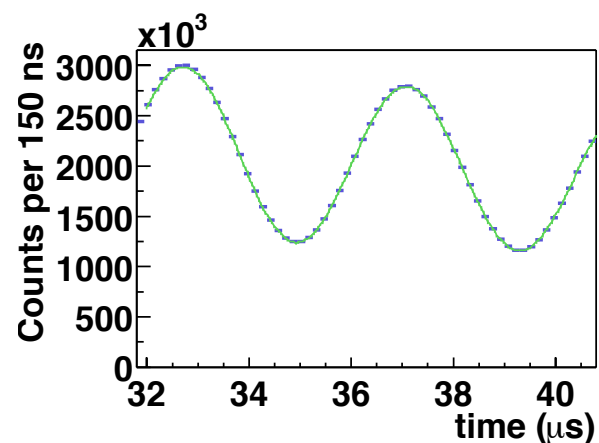
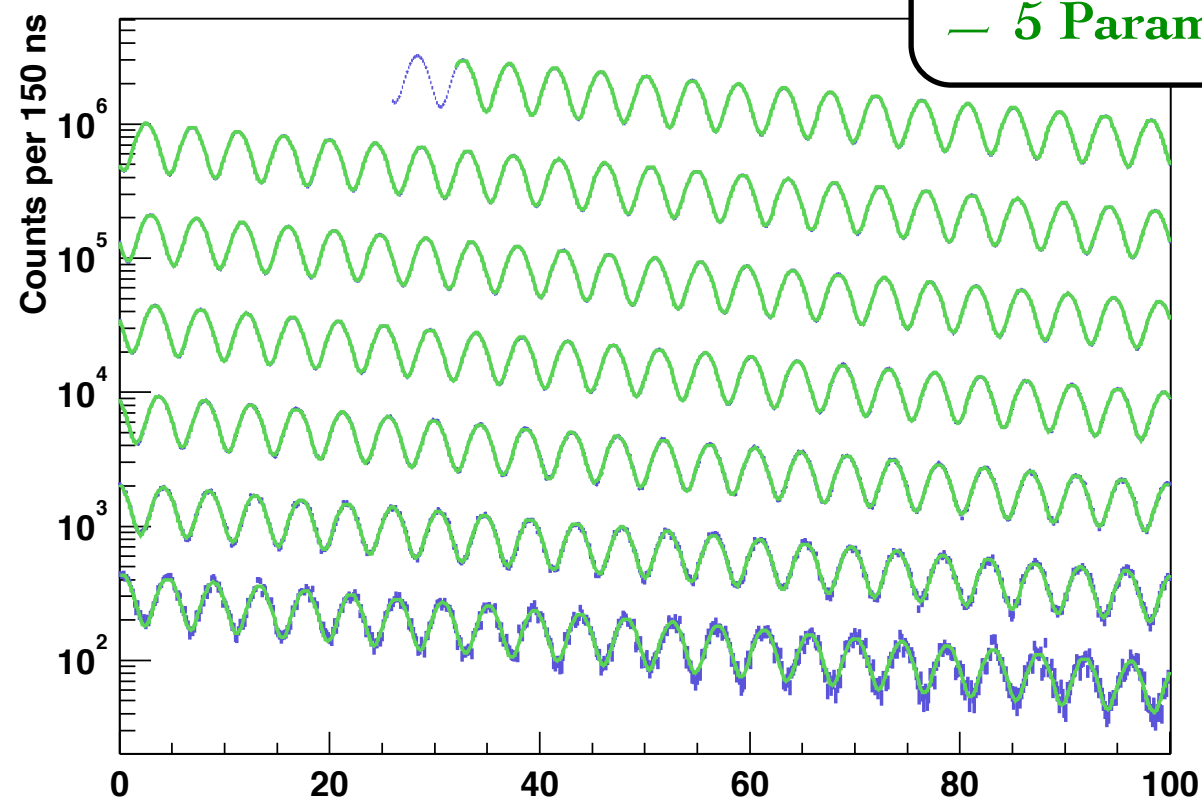
$$a_\mu = \frac{\omega_a / \omega'_p}{\mu_\mu / \mu_p - \omega_a / \omega'_p}$$

The Wiggle Plot, ω_a , ω_p , and a_μ



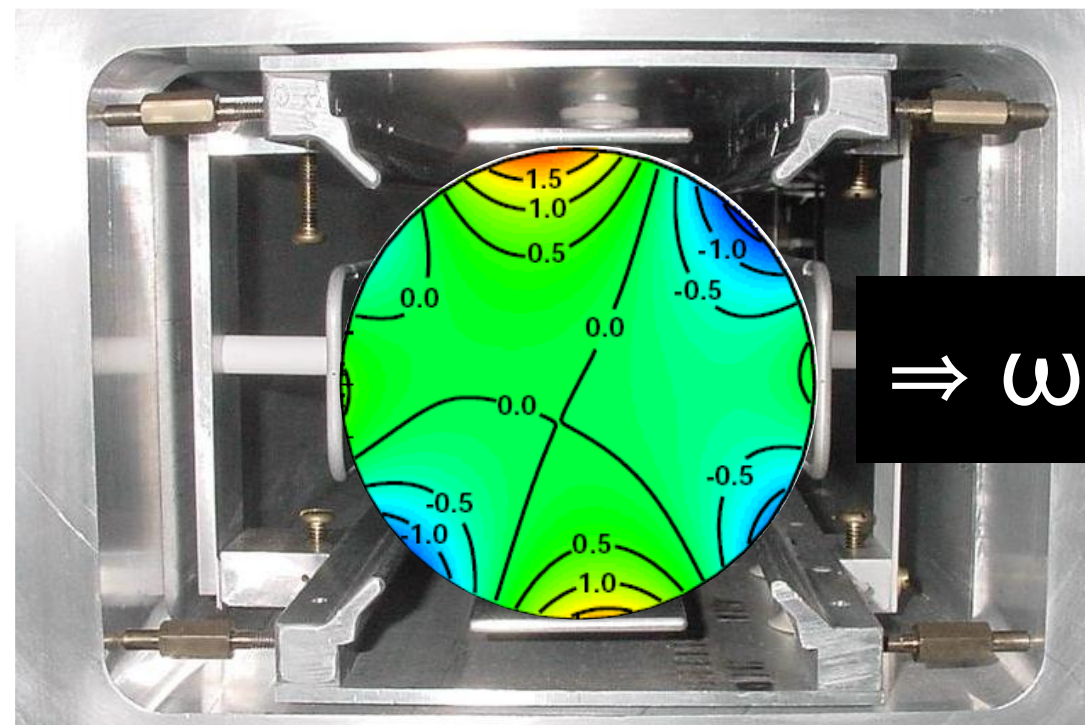
E821 data

• Data
— 5 Param Fit



$$N(t) = N_0 e^{-\frac{t}{\gamma\tau}} [1 + A \cos(\omega_a t + \phi)]$$

+



$\Rightarrow \omega_p (\langle B \rangle)$

$$a_\mu^{\text{E821}} = 0.00116592089(63)$$

$$a_\mu^{\text{SM}} = 0.00116591802(49)$$

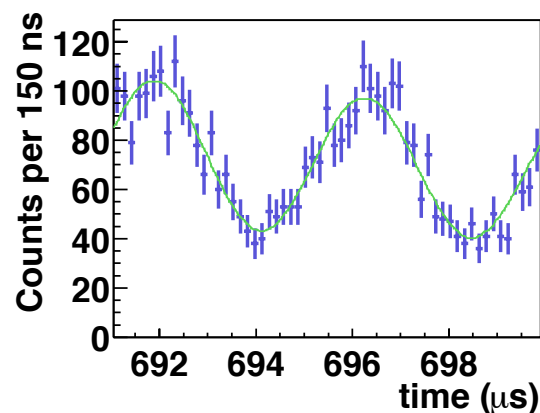
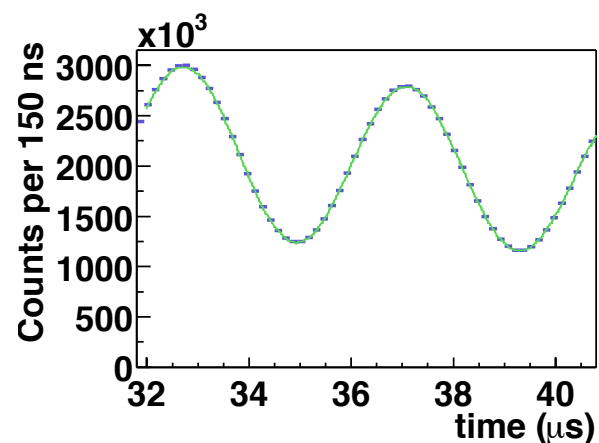
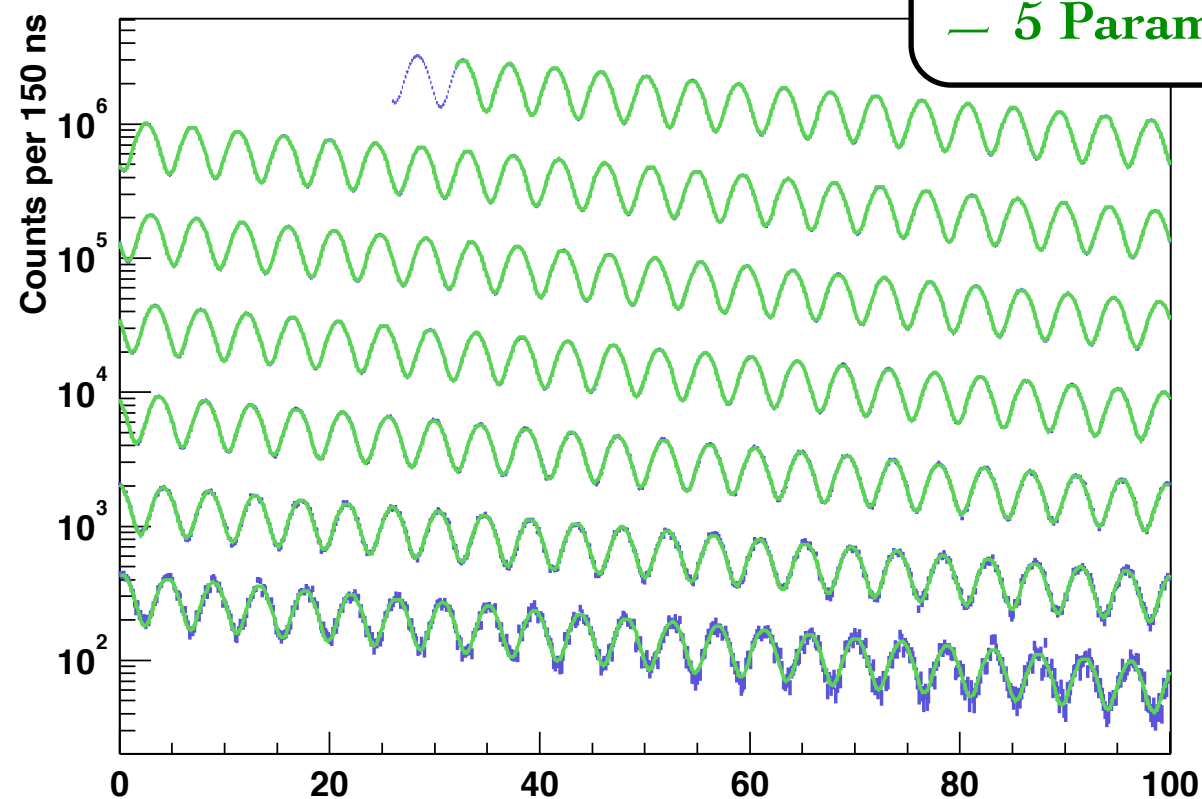
4 billion muon decays
($\approx 15\%$ yield > 1.8 GeV positrons)

The Wiggle Plot, ω_a , ω_p , and a_μ



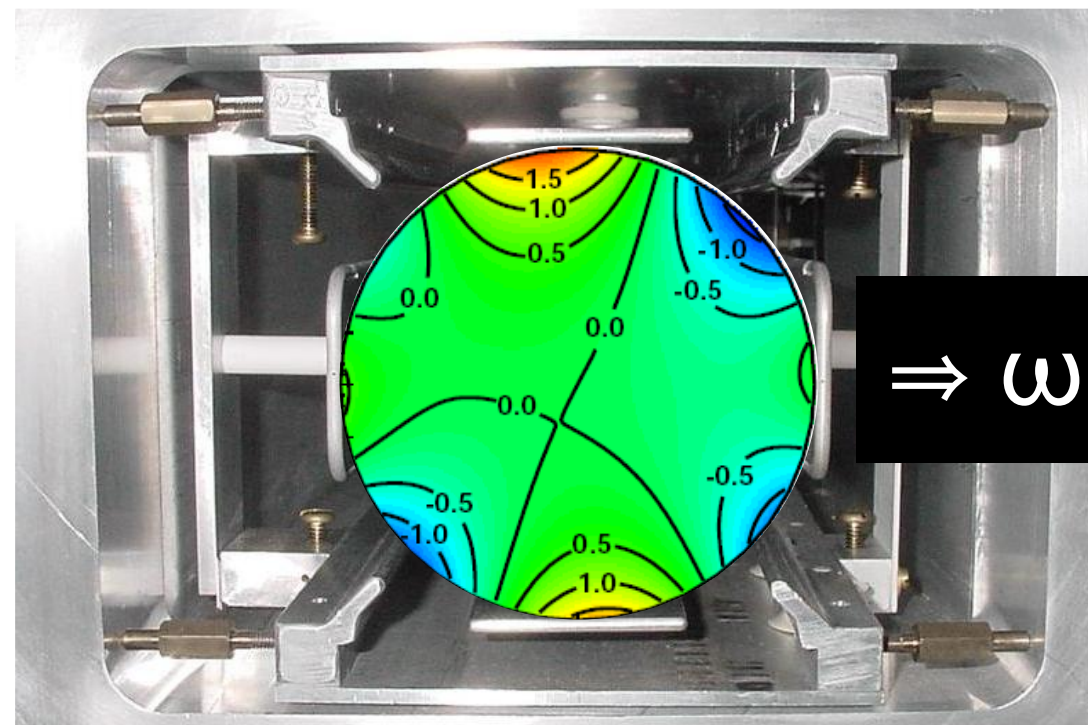
E821 data

• Data
— 5 Param Fit



$$N(t) = N_0 e^{-\frac{t}{\gamma\tau}} [1 + A \cos(\omega_a t + \phi)]$$

+



$\Rightarrow \omega_p (\langle B \rangle)$

$$a_\mu^{\text{E821}} - a_\mu^{\text{SM}} = 287 \pm 80$$

>3σ From SM Prediction!

4 billion muon decays
(≈15% yield >1.8 GeV positrons)

Explanations

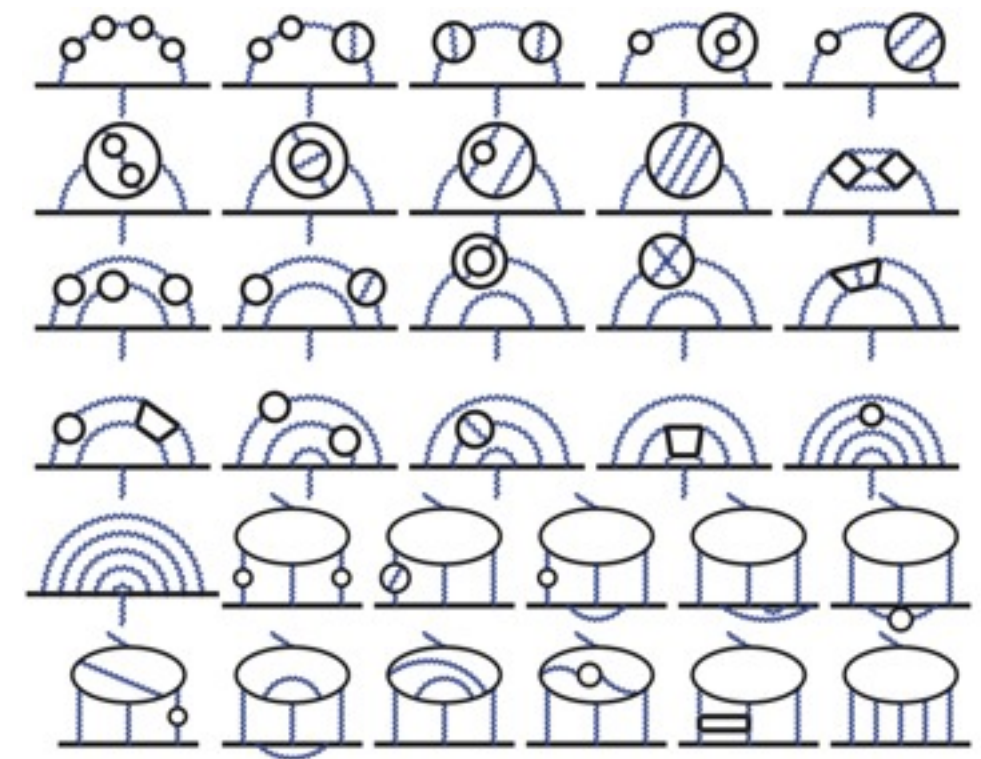


- Standard Model calculation is incomplete/wrong?

$$a_\mu = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{Had}}$$

Calculated out to 5 loops!

Contribution	a_μ Result $\times 10^{-11}$
QED	116 584 718.09 \pm 0.15
EW	153 \pm 1
HVP(LO)	6 949 \pm 43
HVP(NLO)	-98 \pm 1
LbL	105 \pm 26
SM	116 591 802 \pm 49
Exp-SM	287 \pm 80(3.3 σ)



T. Aoyama, M. Hayakawa, T. Kinoshita, M. Nio Phys. Rev. Lett. **109** 111807

Explanations

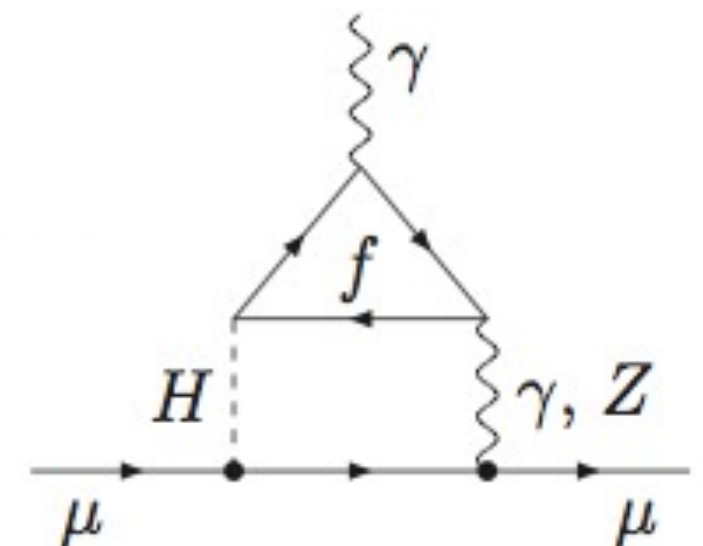
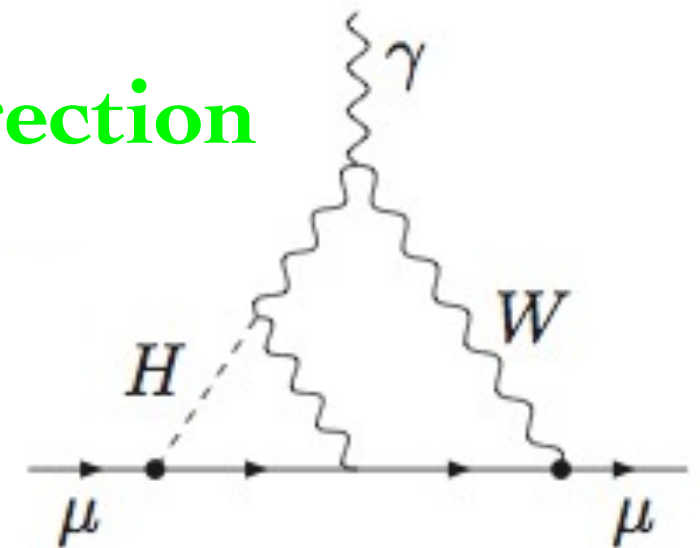


- Standard Model calculation is incomplete/wrong?

$$a_{\mu} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Had}}$$

2 loop calculation + known Higgs mass correction

Contribution	a_{μ} Result $\times 10^{-11}$
QED	116 584 718.09 \pm 0.15
EW	153 \pm 1
HVP(LO)	6 949 \pm 43
HVP(NLO)	-98 \pm 1
LbL	105 \pm 26
SM	116 591 802 \pm 49
Exp-SM	287 \pm 80(3.3 σ)



Explanations

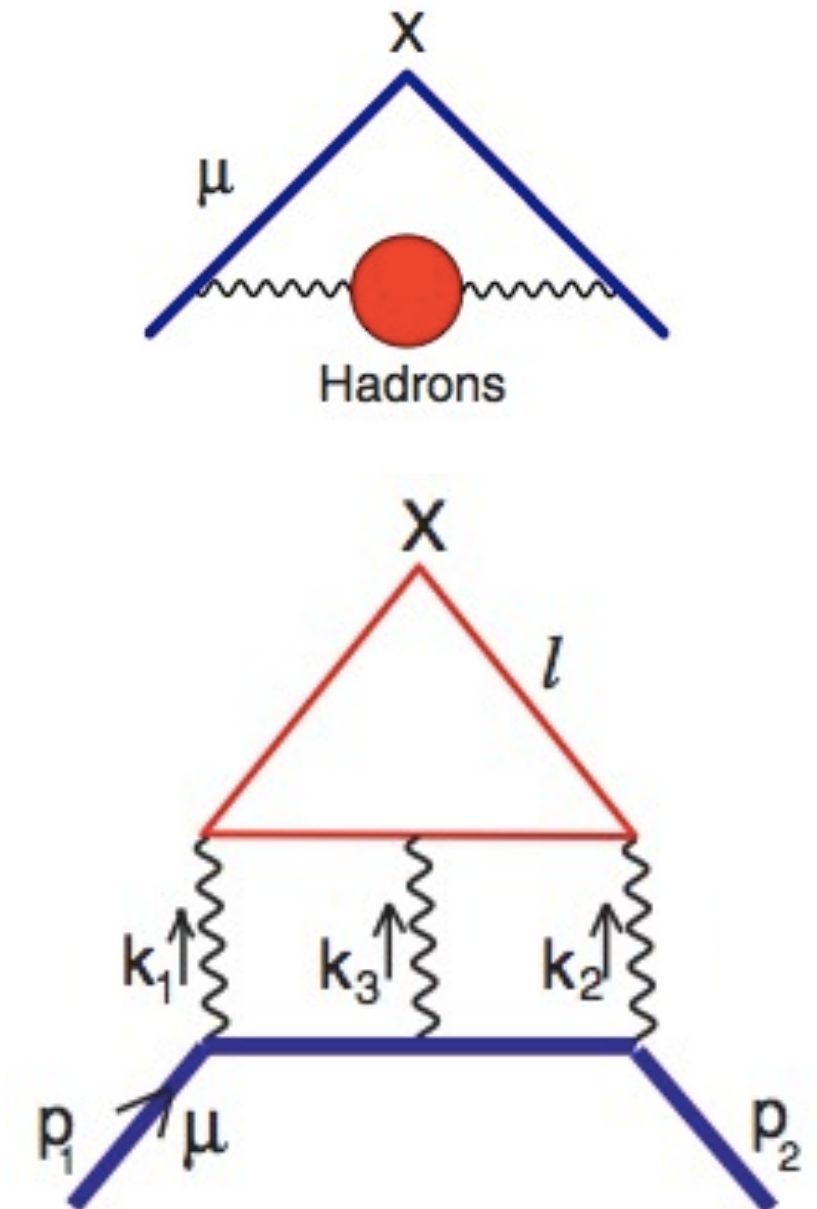


- Standard Model calculation is incomplete/wrong?

$$a_{\mu} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Had}}$$

Dominant source of uncertainty

Contribution	a_{μ} Result $\times 10^{-11}$
QED	116 584 718.09 \pm 0.15
EW	153 \pm 1
HVP(LO)	6 949 \pm 43
HVP(NLO)	-98 \pm 1
LbL	105 \pm 26
SM	116 591 802 \pm 49
Exp-SM	287 \pm 80 (3.3 σ)



Coming Soon: Constrain HVP with low energy $e^+e^- \rightarrow \pi^+\pi^-$ data,
LbL needs first principles LatticeQCD.

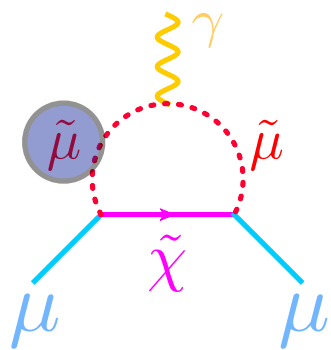
New Physics?



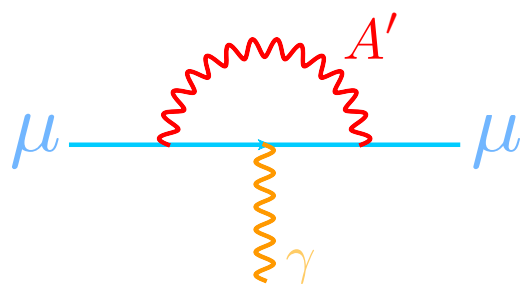
- Standard Model calculation is fine. We are just seeing new physics.

$$a_\mu = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{Had}} + \boxed{a_\mu^{\text{NP}}}$$

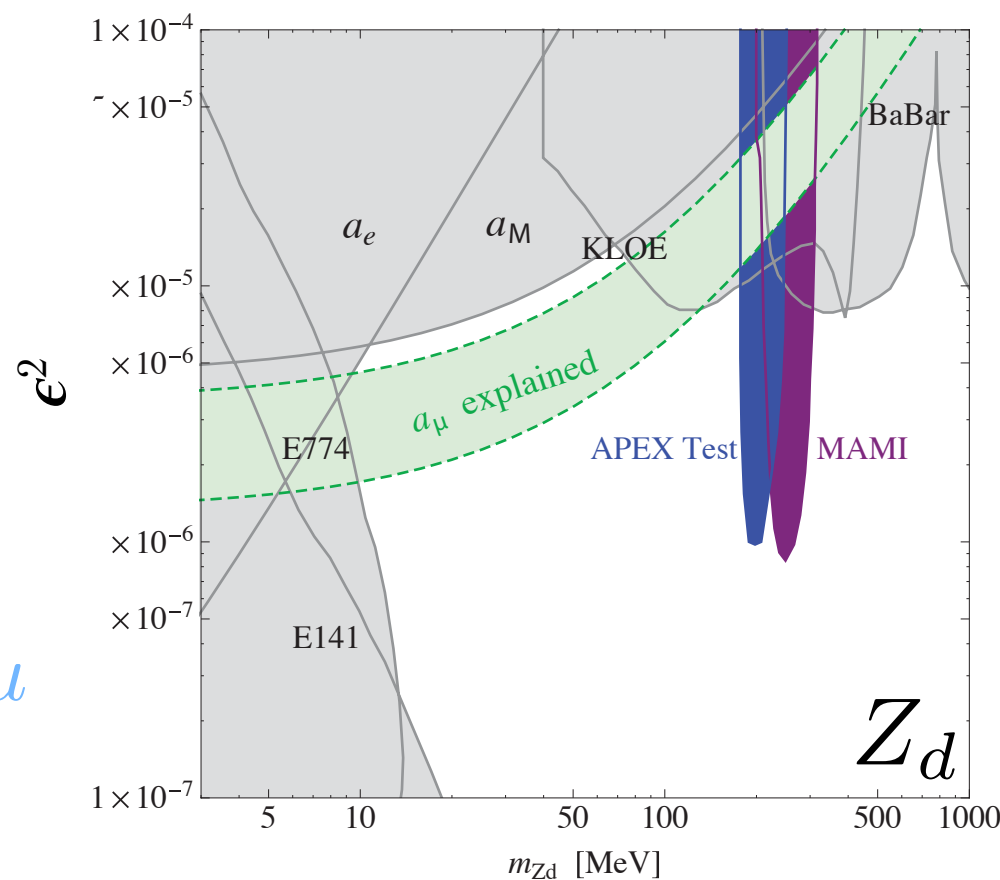
SUSY



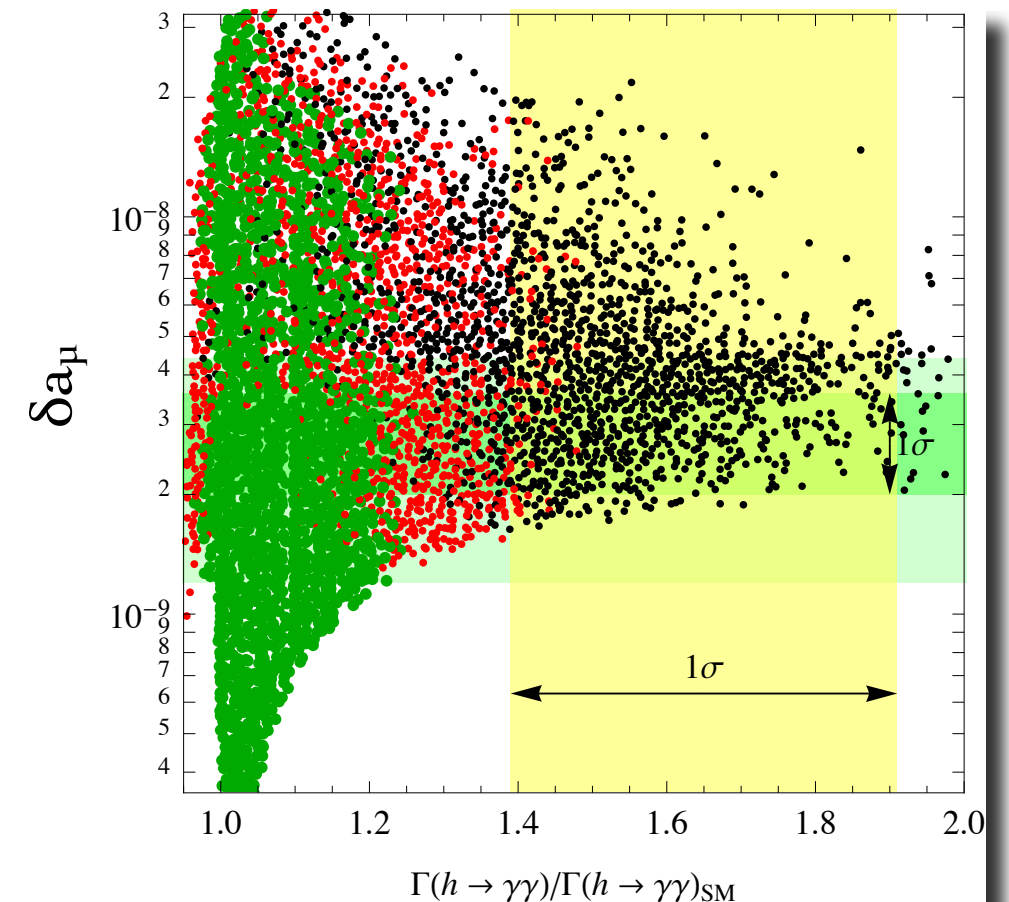
Dark Sector



Davoudiasl, Lee, Marciano '12



Giudice, Paradisi, Strumia '12



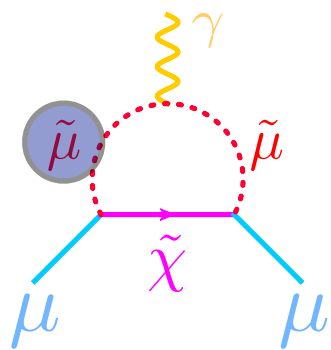
New Physics?



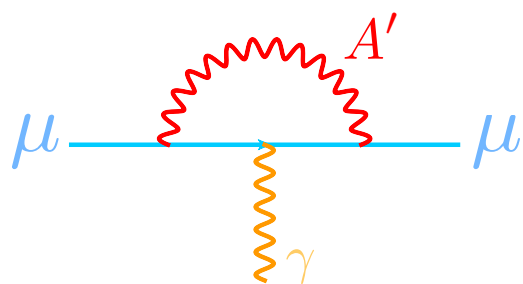
- Standard Model calculation is fine. We are just seeing new physics.

$$a_\mu = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{Had}} + \boxed{a_\mu^{\text{NP}}}$$

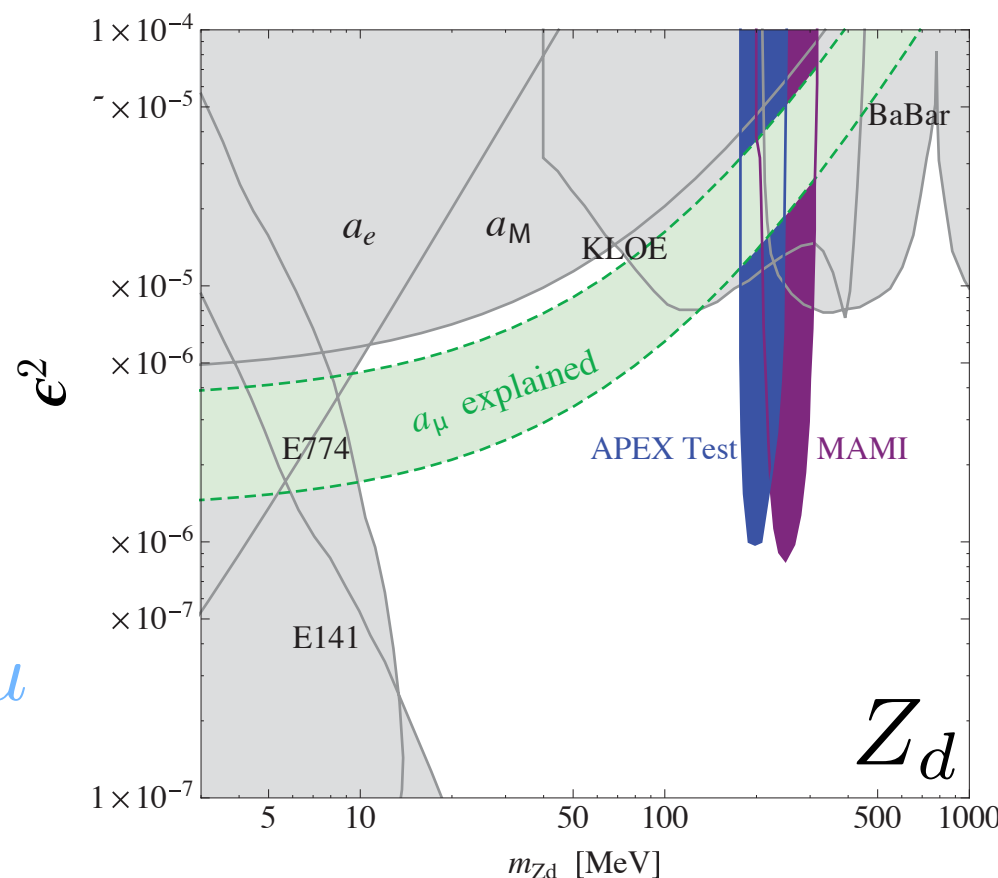
SUSY



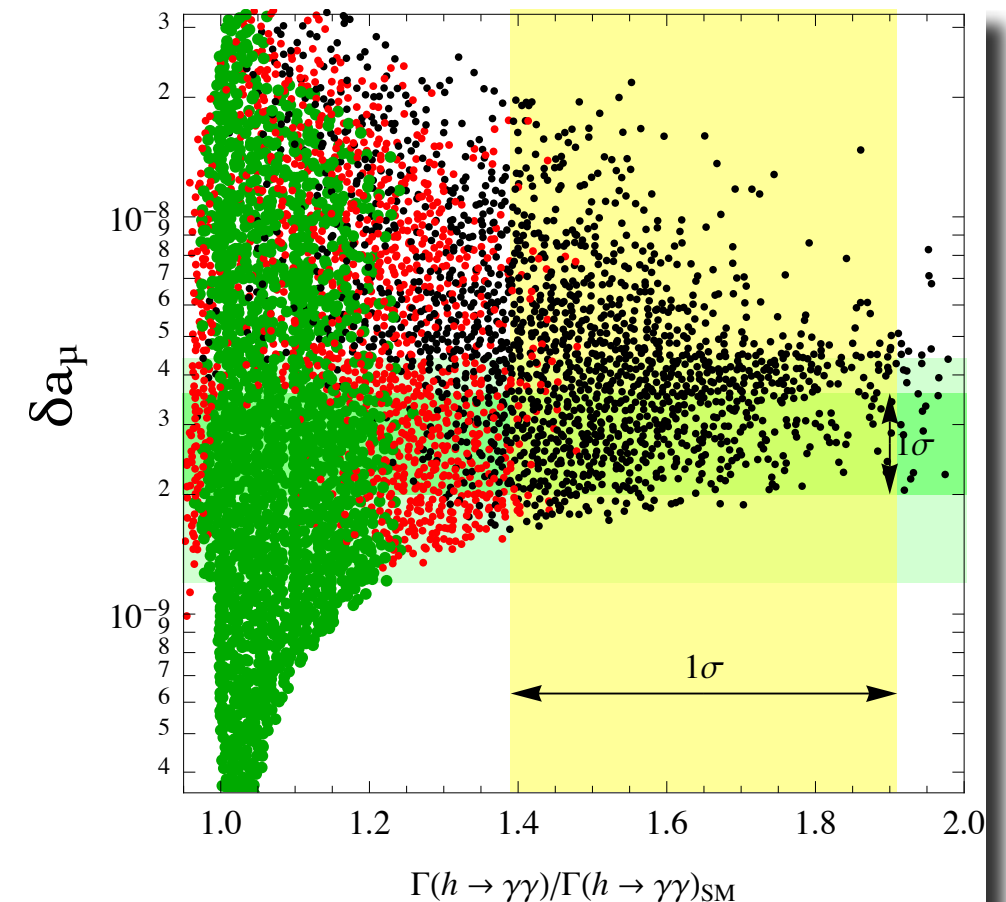
Dark Sector



Davoudiasl, Lee, Marciano '12



Giudice, Paradisi, Strumia '12



- A precise $g-2$ measurement is complimentary to Higgs measurements and a future LHC discovery.

The Fermilab Muon g-2 Experiment



Goal: Resolve E821 3σ measurement with $>5\sigma$ sensitivity

$$\sigma_{a_\mu} = 0.54 \rightarrow 0.14 \text{ ppm}$$

- Increased Statistics: Fermilab will provide us with $>20\times$ more muons.

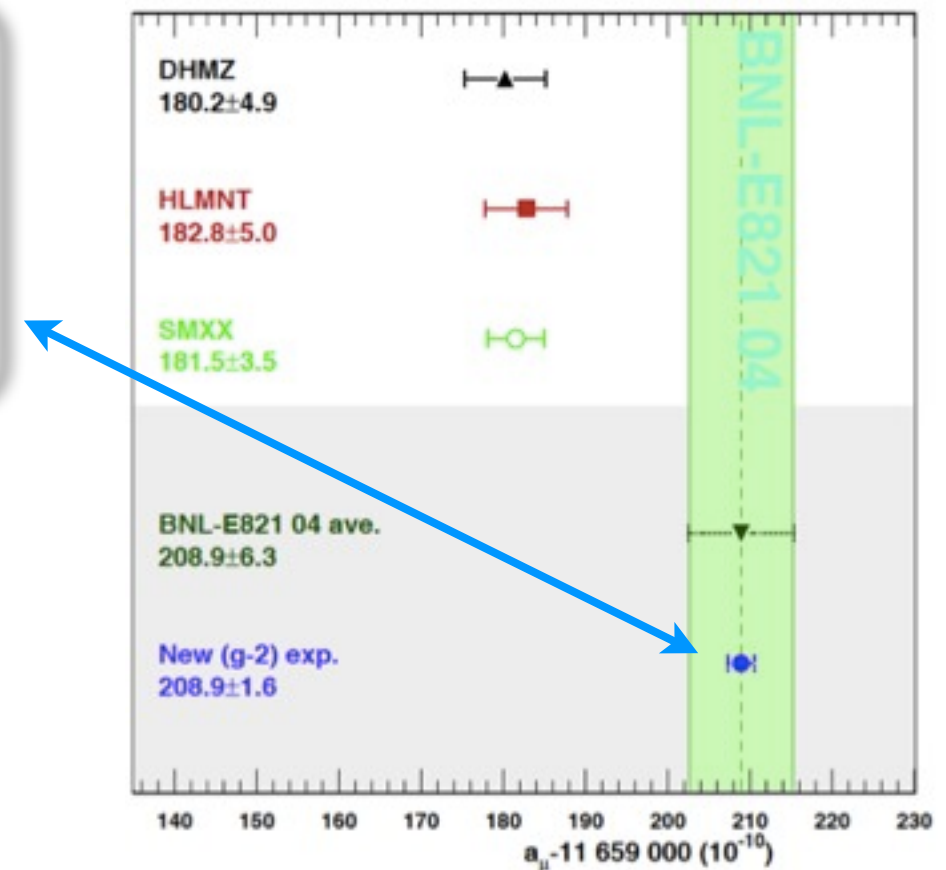
$$\sigma_{\text{stat}} = 0.4 \rightarrow 0.1 \text{ ppm}$$

- New segmented calorimeters, straw wire tracker, Fast muon kicker (and more).

$$\sigma_{\omega_a} = 0.18 \rightarrow 0.07 \text{ ppm}$$

- Long shimming period, magnet temperature stability, more in-situ calibrations (and more).

$$\sigma_{\langle B \rangle} = 0.17 \rightarrow 0.07 \text{ ppm}$$



The Fermilab Muon g-2 Experiment



Goal: Resolve E821 3σ measurement with $>5\sigma$ sensitivity

$$\sigma_{a_\mu} = 0.54 \rightarrow 0.14 \text{ ppm}$$

- Increased Statistics: Fermilab will provide us with **>20x** more muons.

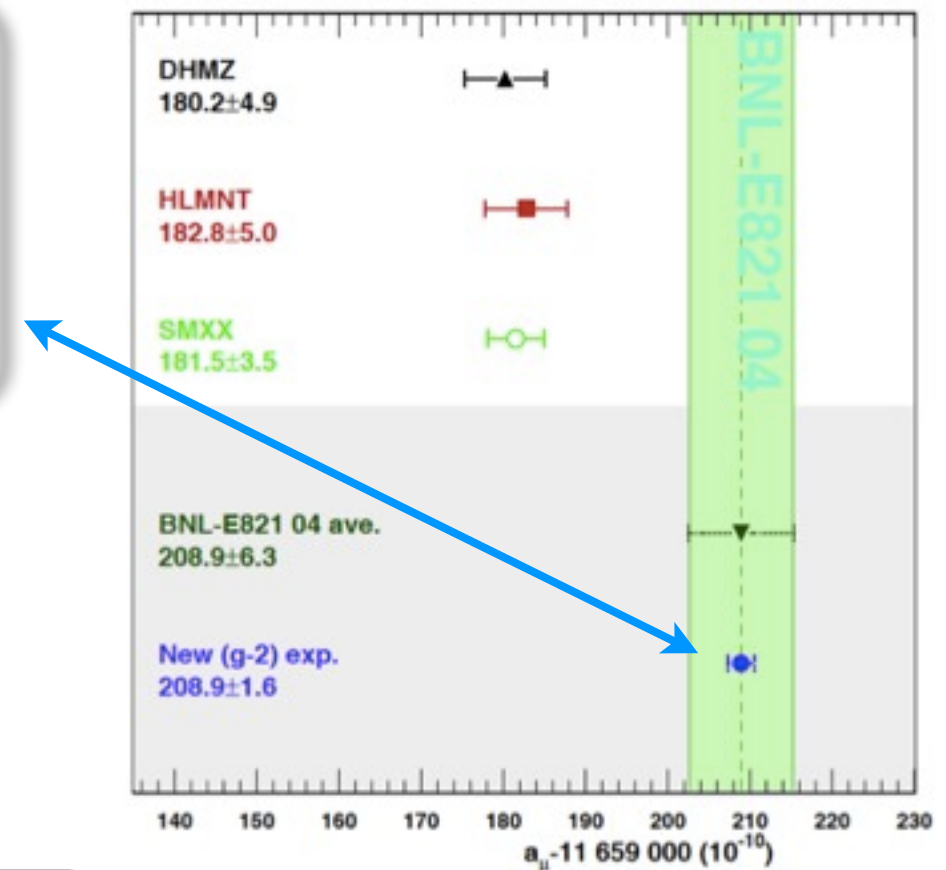
$$\sigma_{\text{stat}} = 0.4 \rightarrow 0.1 \text{ ppm}$$

- New segmented calorimeters, straw wire tracker, Fast muon kicker (and more).

$$\sigma_{\omega_a} = 0.18 \rightarrow 0.07 \text{ ppm}$$

- Long shimming period, magnet temperature stability, more in-situ calibrations (and more).

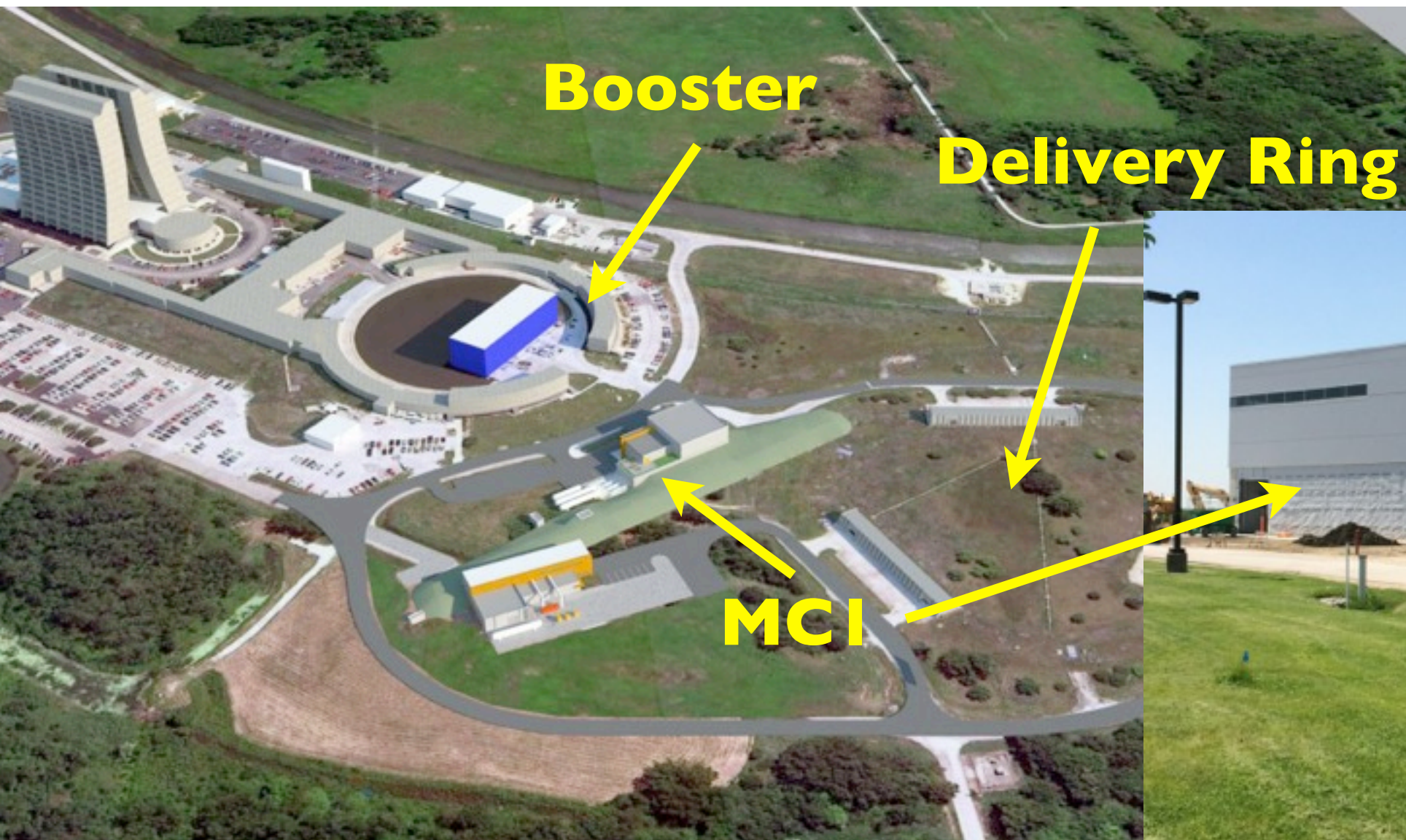
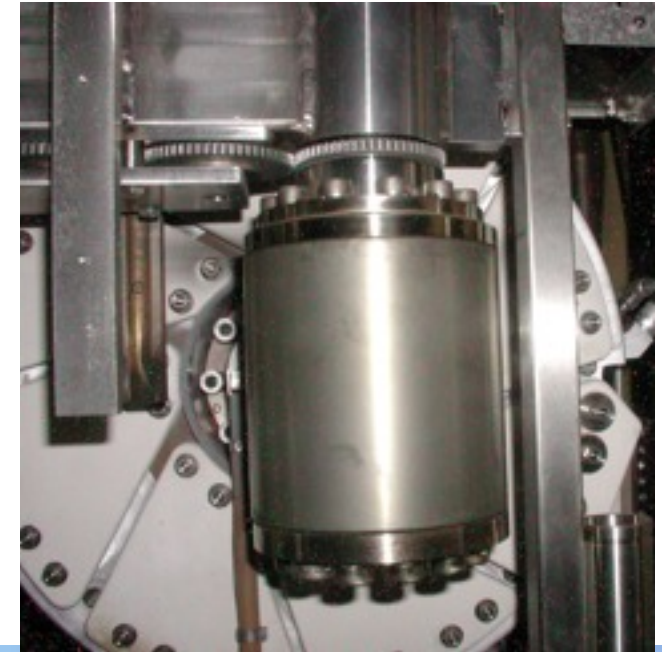
$$\sigma_{\langle B \rangle} = 0.17 \rightarrow 0.07 \text{ ppm}$$



Fermilab Muon Campus



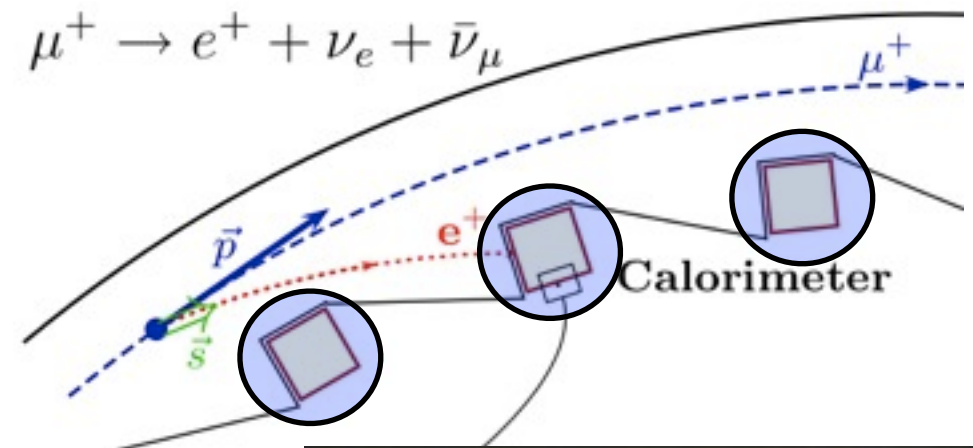
- Fermilab will produce pions using 8.9 GeV protons impacting the former antiproton production target
- Pions decay along long path \Rightarrow Pure muon beam. (E821 had large pion contamination).



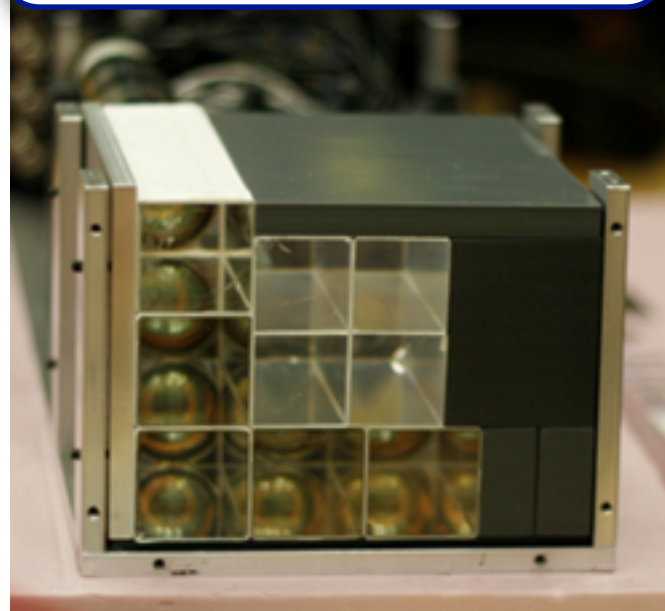
New Calorimetry



- Segmented Calorimeters and SiPMs
- We will use a 9x6 array of PbF₂ crystals with SiPM for light readout.
- Segmentation reduces pileup (two positrons in same time window).
Laser calibration system and lower energy thresholds

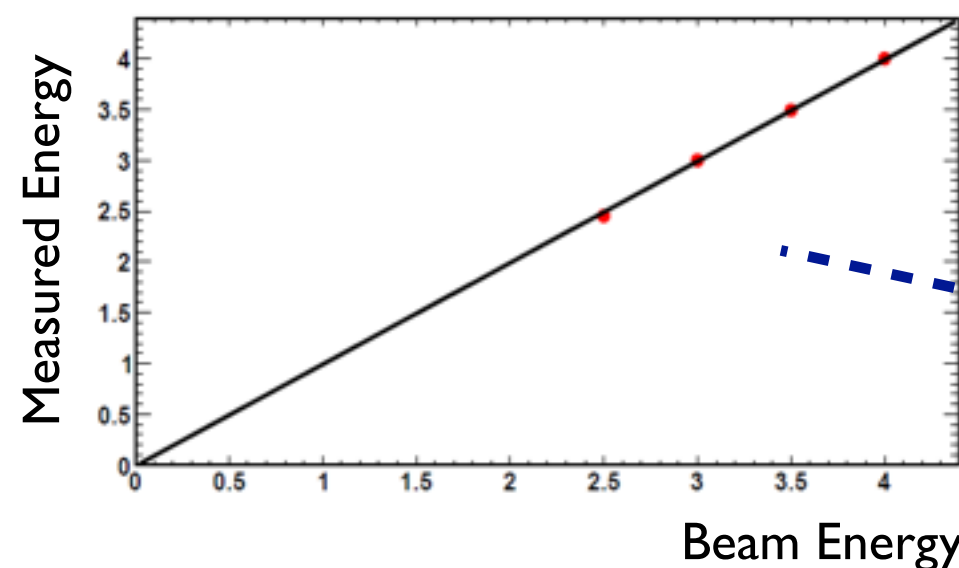
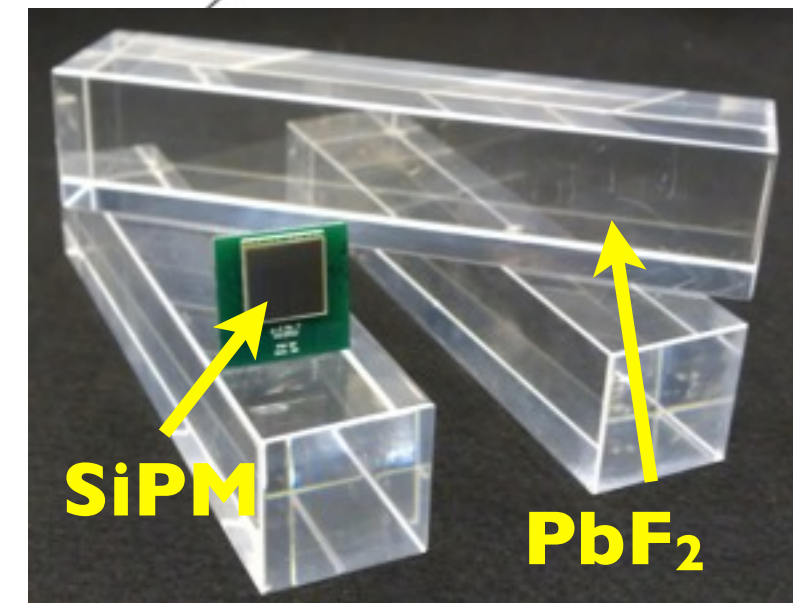


SLAC Test Beam,
Nov '13



$$\sigma_{\text{pileup}} = 80_{(\text{E821})} \rightarrow 40 \text{ ppb}$$

$$\sigma_{\text{gain}} = 120_{(\text{E821})} \rightarrow 20 \text{ ppb}$$



$$\frac{\sigma(E)}{E} = 2.8\%$$

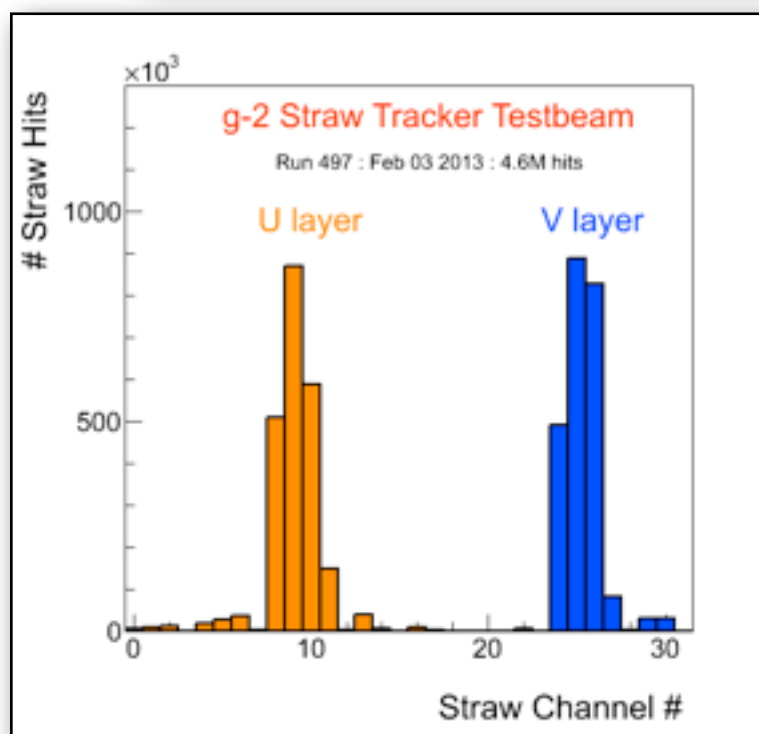
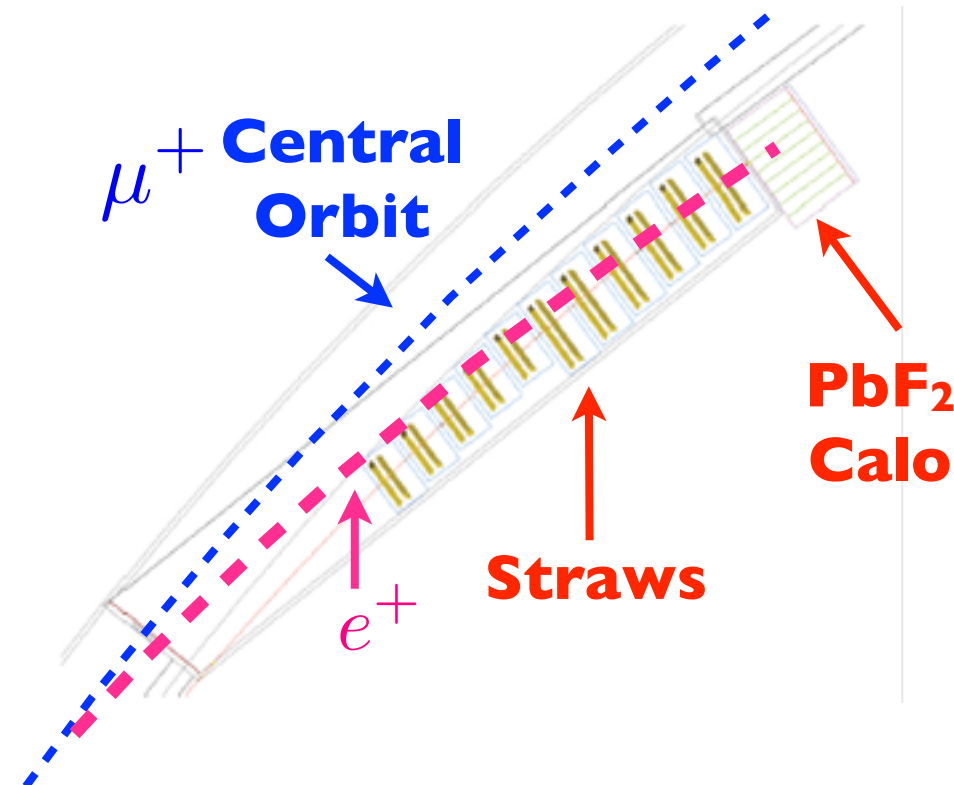
New Tracking Detectors



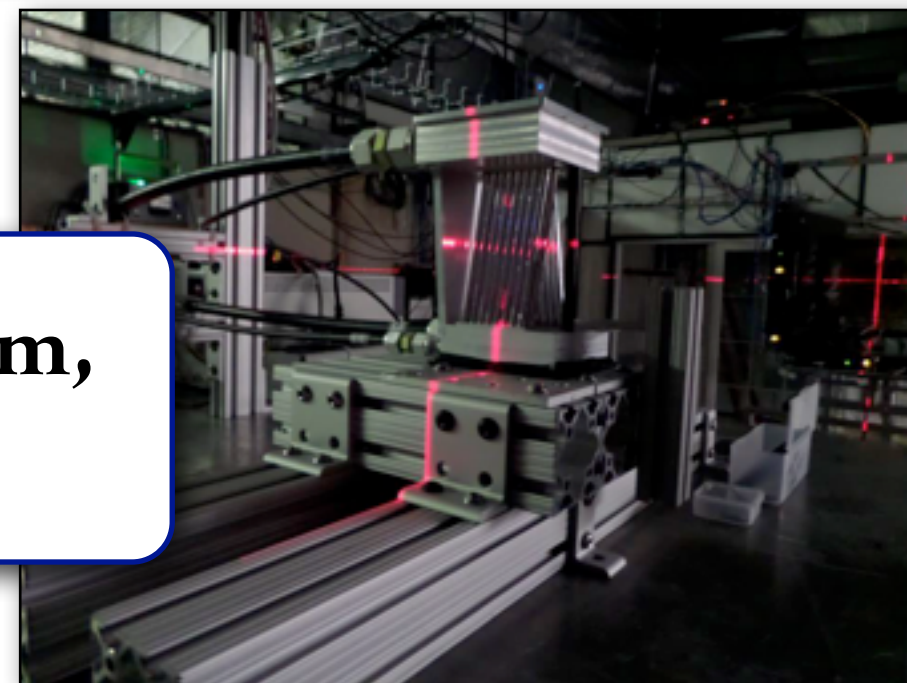
- Straw tracking detectors will measure muon decay vertex and momentum.
- Monitor beam profile fill-by-fill (required for $\langle B \rangle$ and ω_a measurements)
- Measure pile-up \leftrightarrow calorimeter hits

$$\sigma_{\langle B \rangle} = 30_{(E821)} \rightarrow 10 \text{ ppb}$$

$$\sigma_{\text{beam}} = 50_{(E821)} \rightarrow 30 \text{ ppb}$$



FNAL Test Beam,
Jan/Apr '14



The Big Move From Long Island ...



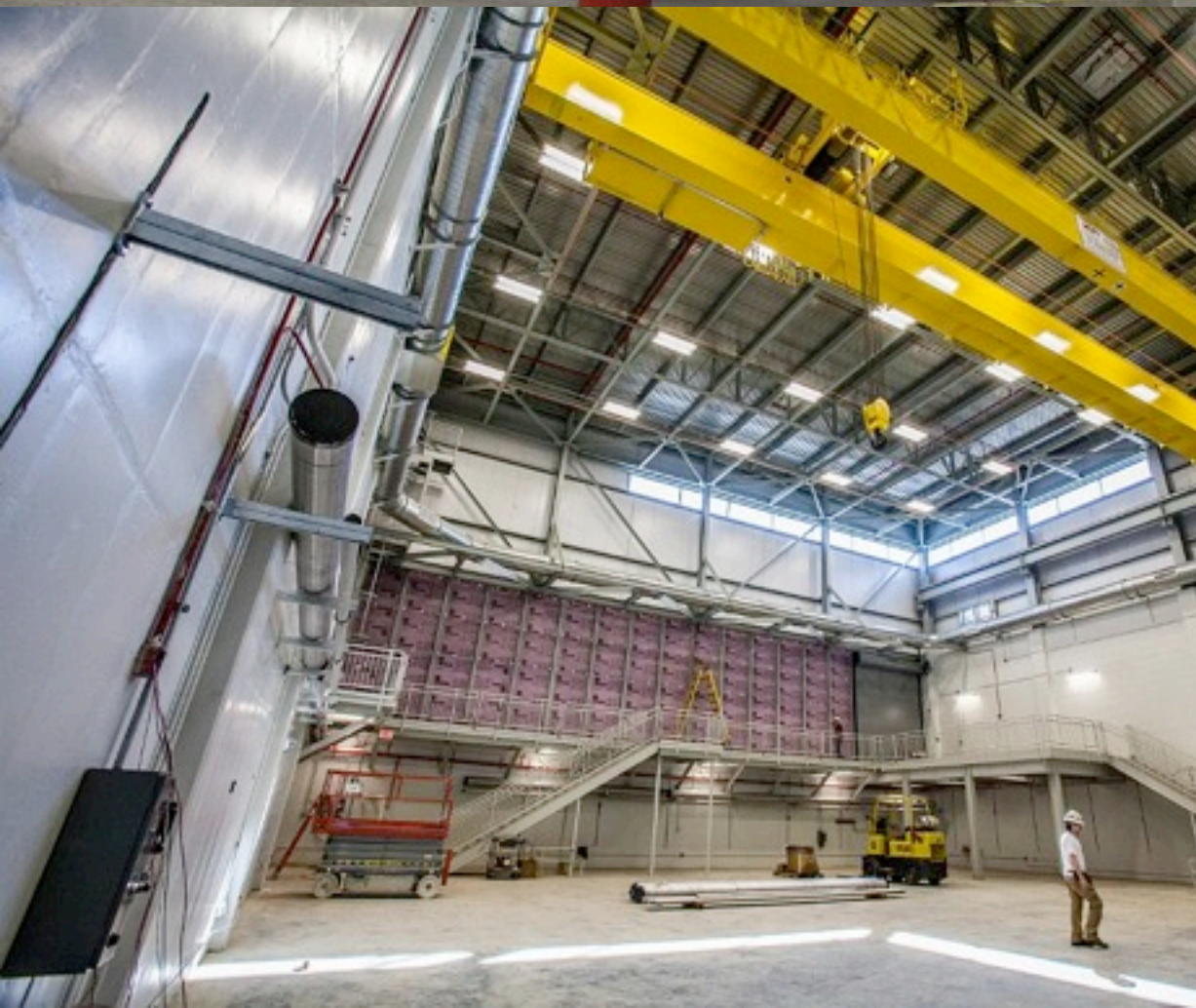
... To Fermilab



... To Its Final Resting Place in MC1



(from Brian Drendal)

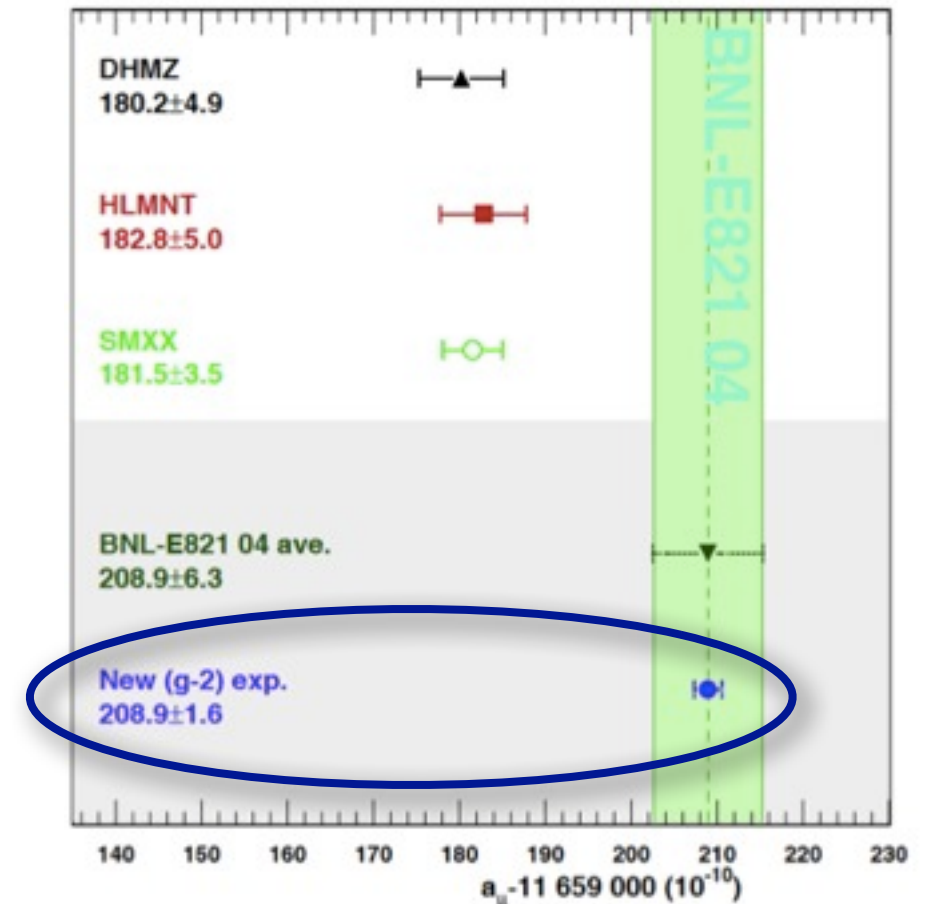


(from Lee Roberts)

Summary



- Fermilab muon g-2 will measure the muon anomalous magnet moment to sub-ppm level.
- $>5\sigma$ sensitivity to new physics!
- CD-1 approval. CD-2/3 review this July.
- Magnet shimming and detector commissioning in 2015/2016.
- Hopefully, stored muons in 2017.



“Magnetic Moment”
from Two Brothers
in Warrenville, IL



Luckily, we've
got plenty to
keep us busy



Back Ups

Fast Muon Kicker

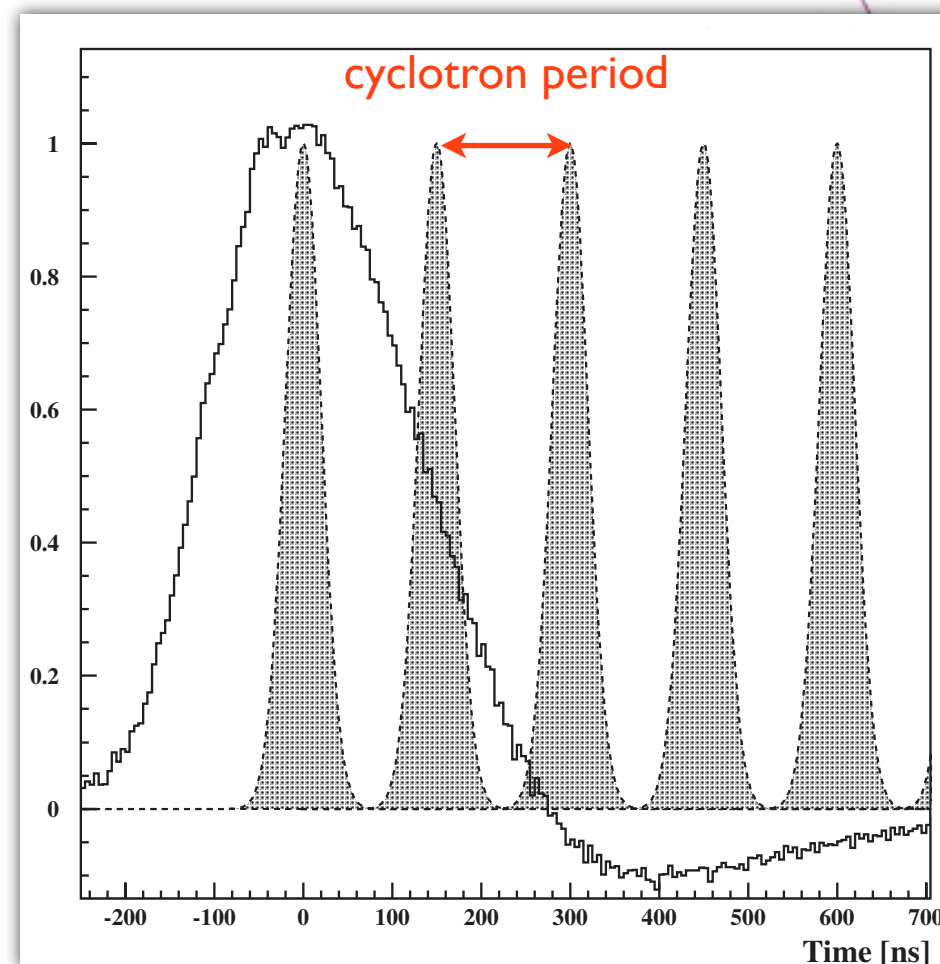
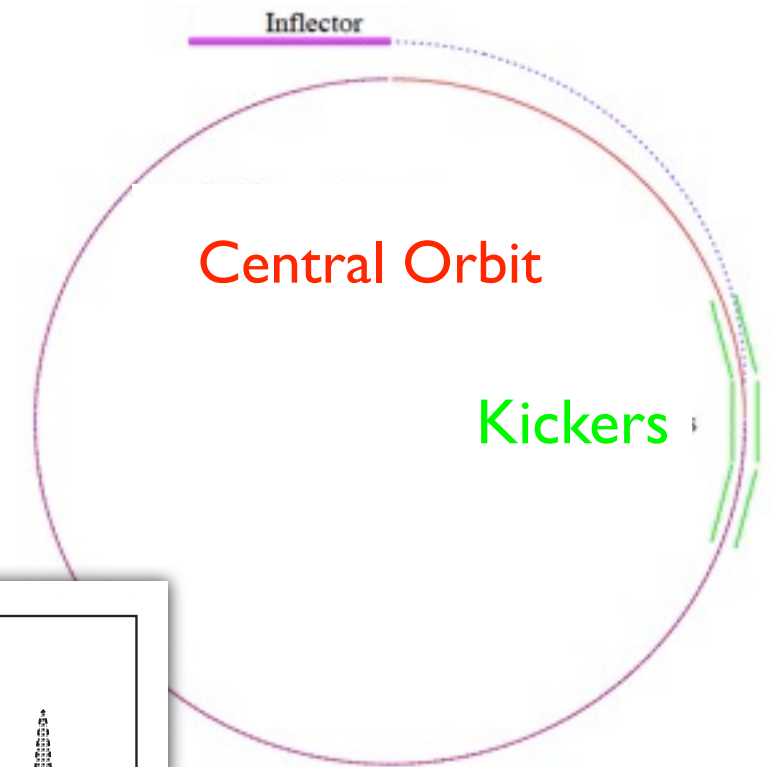


- Fast muon injection kicker
 - Produce a fast (**<150 ns**) ≈ 11 mrad kick. to place muons on central orbit.
 - Must turn OFF before 2nd orbit begins

Fast Muon Kicker



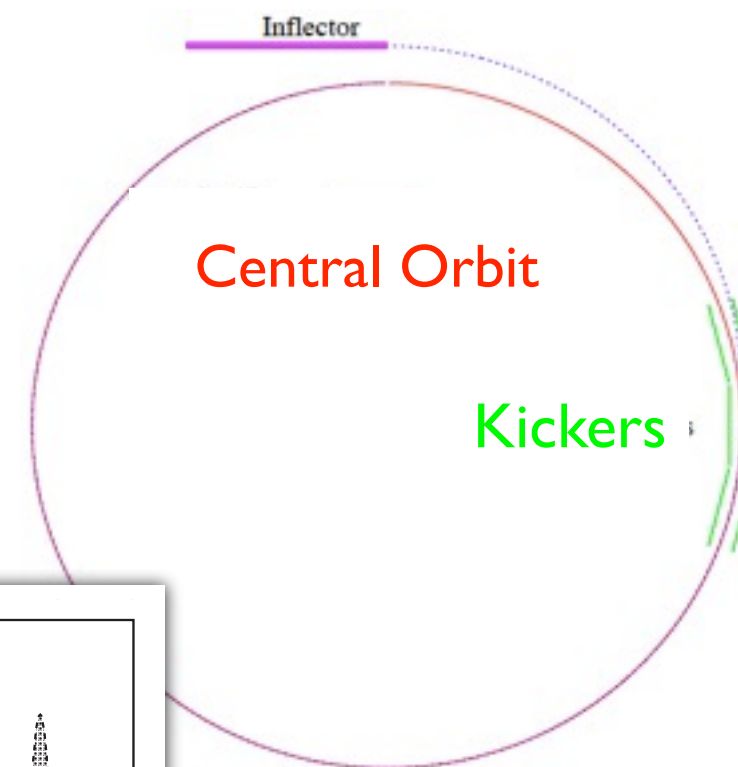
- Fast muon injection kicker
- Produce a fast (**<150 ns**) ≈ 11 mrad kick. to place muons on central orbit.
- Must turn OFF before 2nd orbit begins



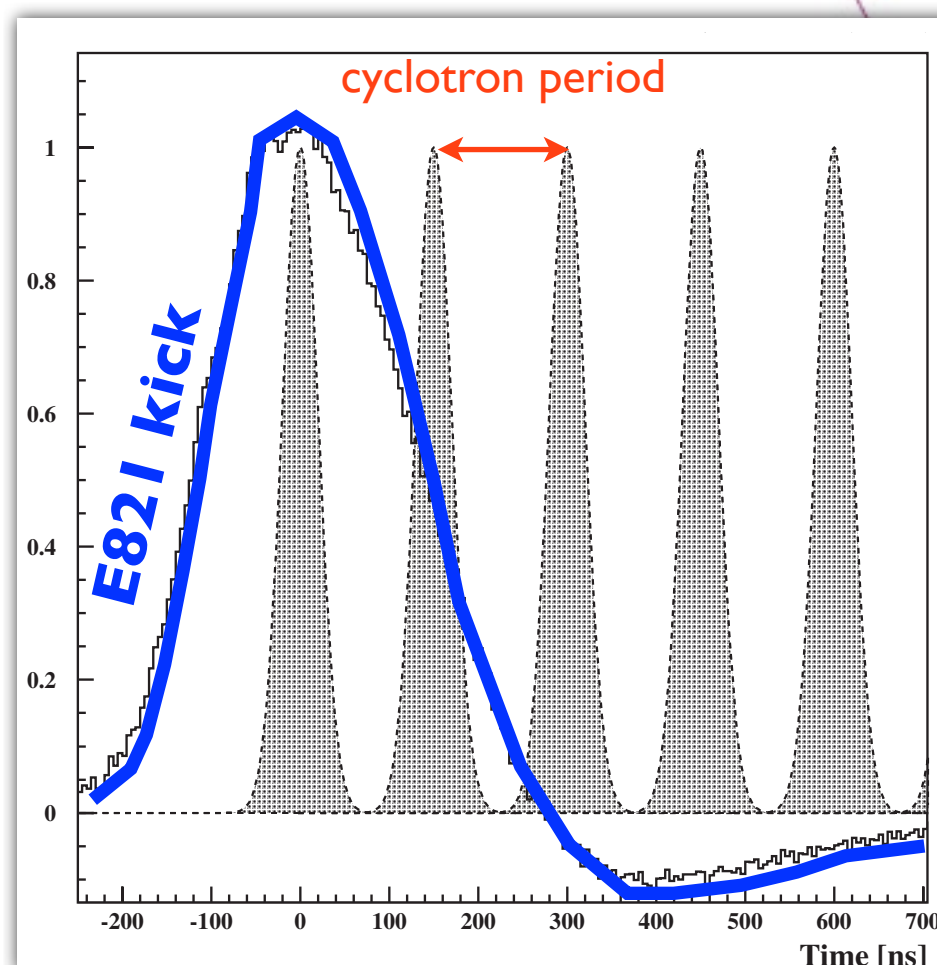
Fast Muon Kicker



- Fast muon injection kicker
- Produce a fast (**<150 ns**) ≈ 11 mrad kick to place muons on central orbit.
- Must turn OFF before 2nd orbit begins



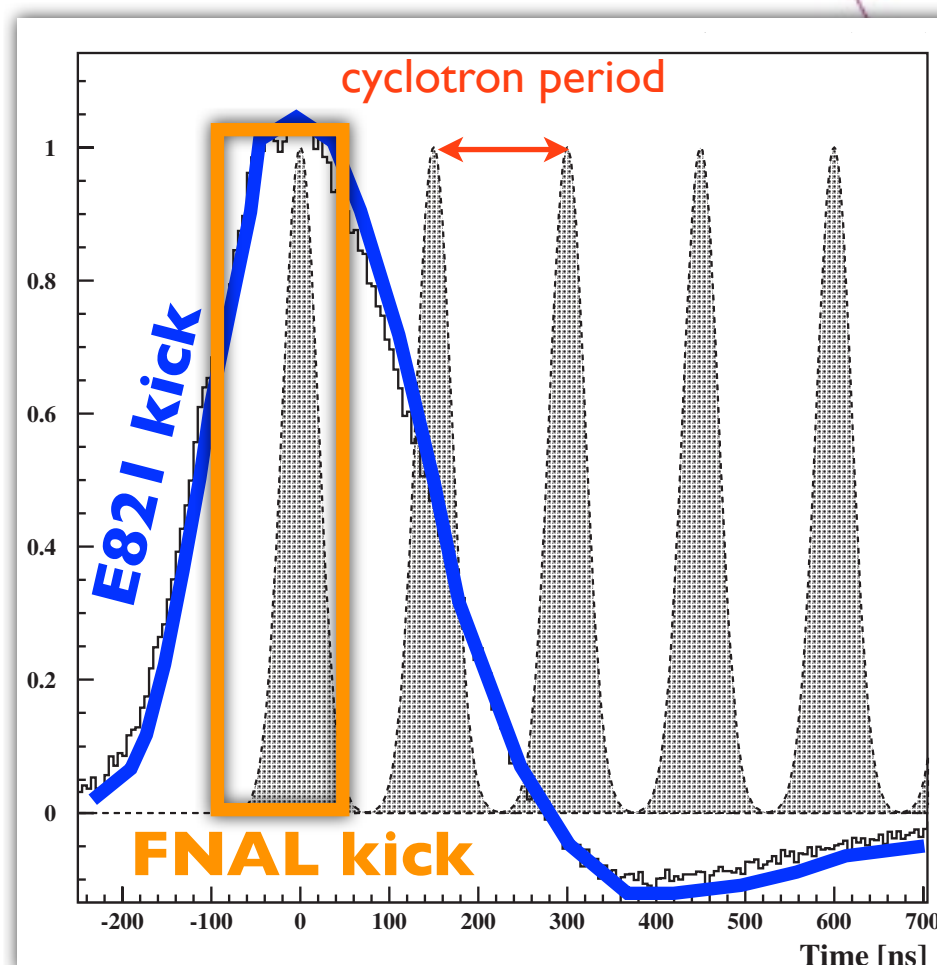
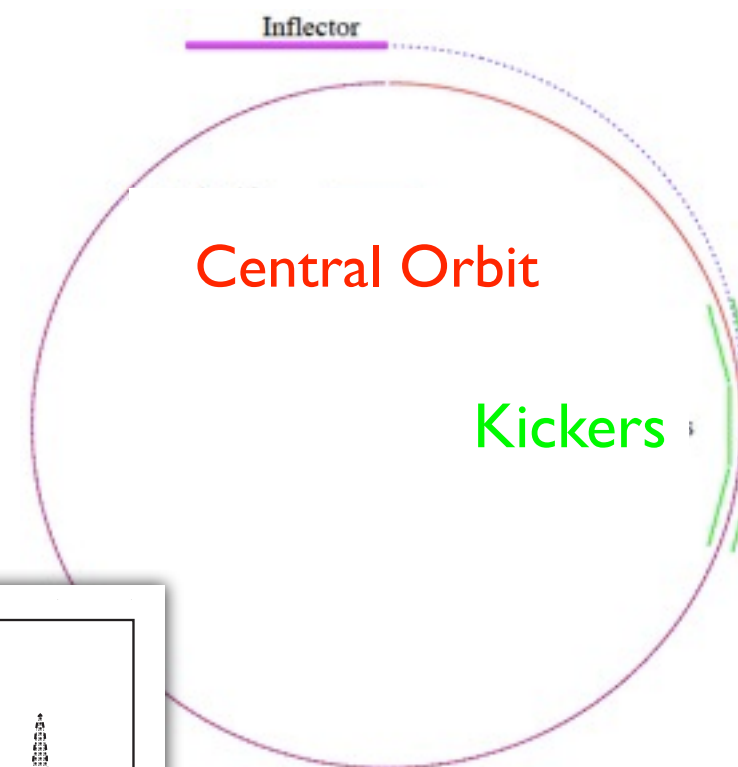
- E821** dramatically underkicked muons
→ lost muons and large betatron oscillations



Fast Muon Kicker



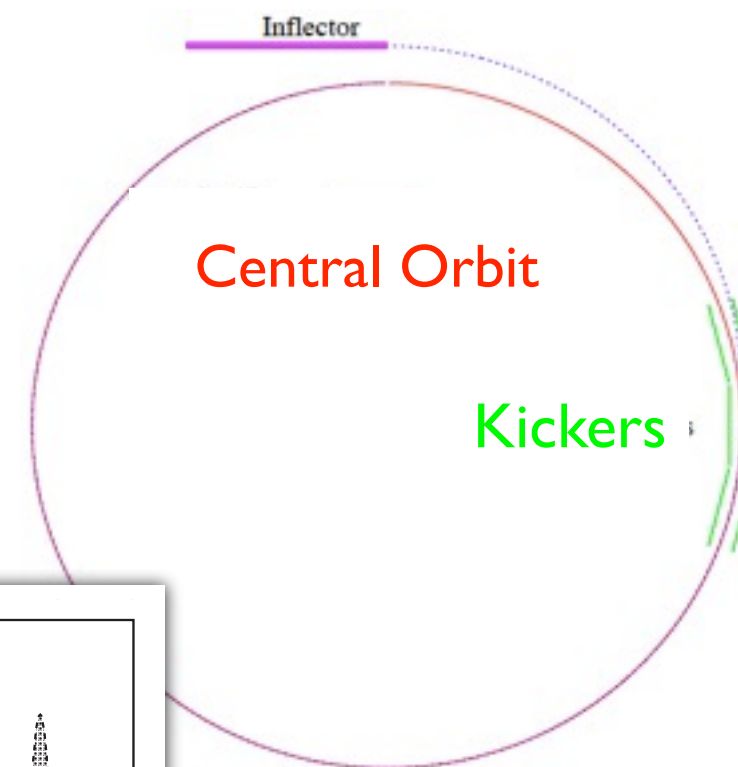
- Fast muon injection kicker
 - Produce a fast (**<150 ns**) ≈ 11 mrad kick. to place muons on central orbit.
 - Must turn OFF before 2nd orbit begins
 - E821** dramatically underkicked muons
 - lost muons and large betatron oscillations
 - FNAL** kicker uses a fast blumlien pulser



Fast Muon Kicker



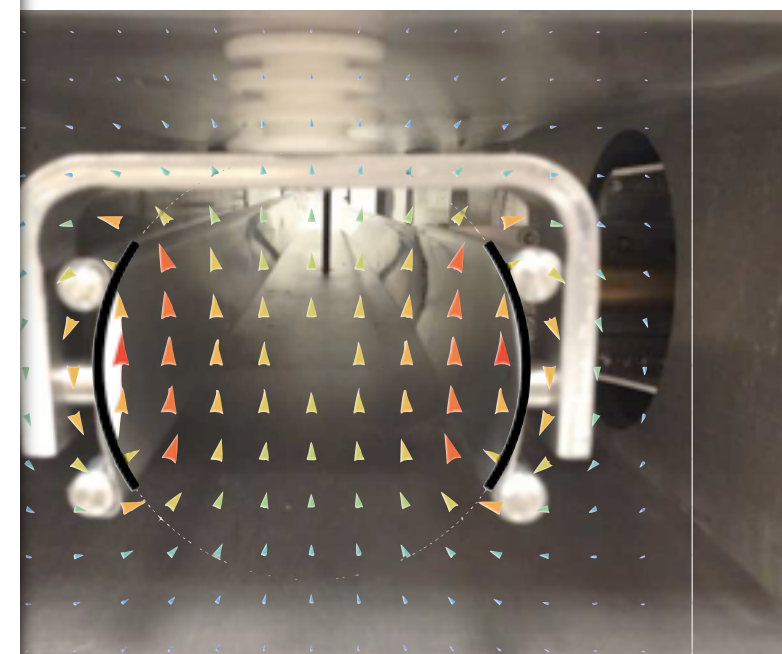
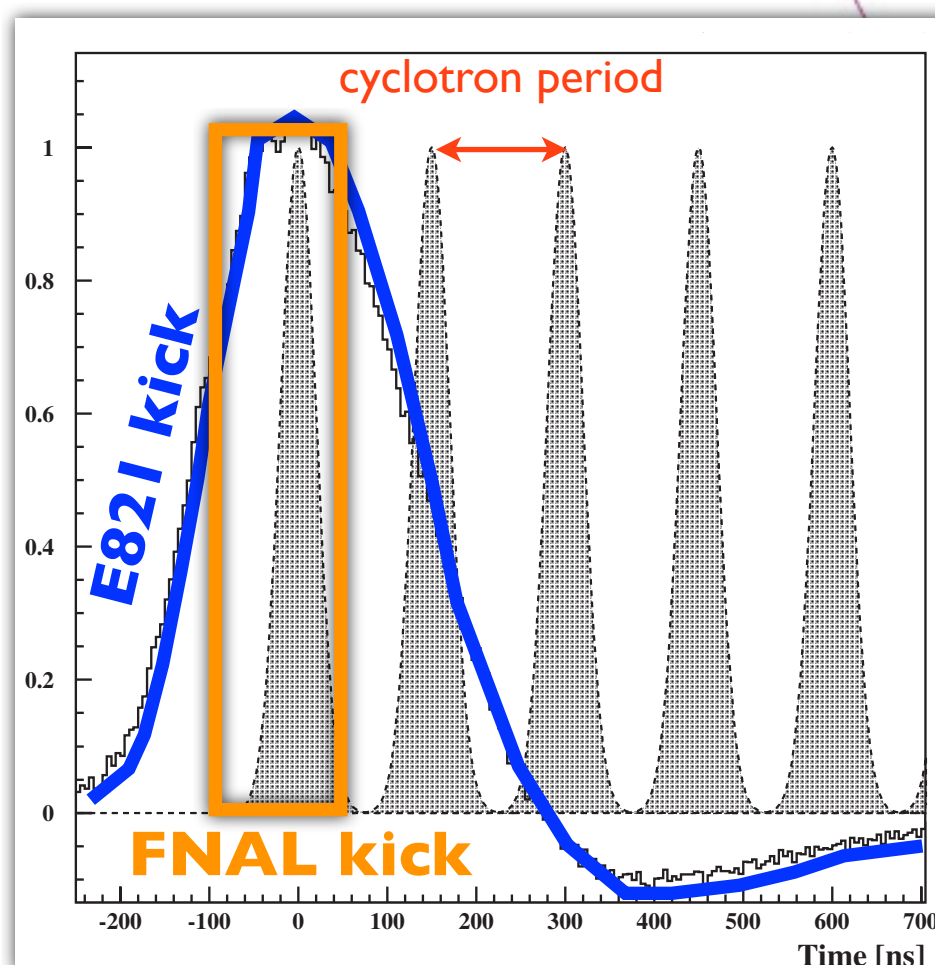
- Fast muon injection kicker
 - Produce a fast (**<150 ns**) ≈ 11 mrad kick. to place muons on central orbit.
 - Must turn OFF before 2nd orbit begins



- E821** dramatically underkicked muons
 - lost muons and large betatron oscillations

- FNAL** kicker uses a fast blumlien pulser

- Curved kicker plates allow for higher fields

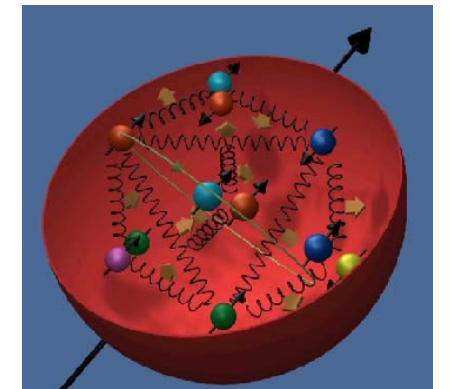


Field Goals



Category	E821 [ppb]	Main E989 Improvement Plans	Goal [ppb]
Absolute field calibration	50	Special 1.45 T calibration magnet with thermal enclosure; more calibration probes; better electronics	35
Trolley probe calibrations	90	3-axis motion of plunging probe; better position accuracy of probe active volumes; more frequent calib, better shimming	30
Trolley measurements of B_0	50	Reduced/measured rail irregularities; reduced position uncertainty by factor of 2 ; stabilized magnet field during measurements; smaller field gradients	30
Fixed probe interpolation	70	More frequent trolley runs; more fixed probes; better temperature stability of the magnet	30
Muon distribution	30	Move trolley probes to larger radii; improved field uniformity ; improved muon tracking	10
Time-dependent external magnetic fields	–	Direct measurement of external fields; simulations of impact; active feedback	5
Others †	100	Improved trolley power supply; reduced temperature effects on trolley; measure/reduce kicker field transients	30
Total syst. unc. on ω_p	170		70

g Does Not Equal 2



- The 1930's saw two unanticipated results for the g-factor of the proton ($g_p \approx 5.6$) and the neutron ($g_n \approx -3.8$).
- Strongly suggests nucleon substructure.
- In the late 1940's another breakthrough measurement was made at Columbia by Kusch and Foley.

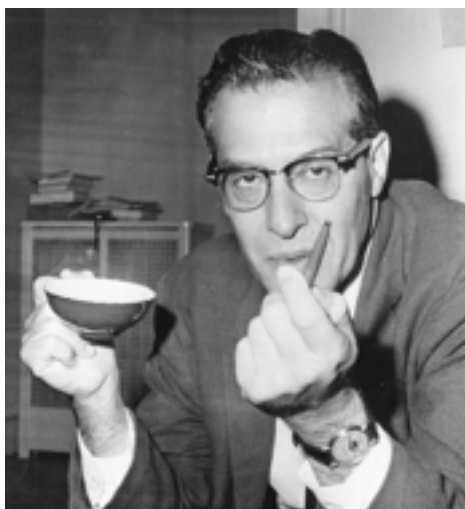
Phys. Rev. 72 (1947)

Precision Measurement of the Ratio of the Atomic 'g Values' in the $^2P_{3/2}$ and $^2P_{1/2}$ States of Gallium*
P. KUSCH AND H. M. FOLEY
Columbia University, New York, New York
November 3, 1947



$$g_e = 2.00229(8)$$

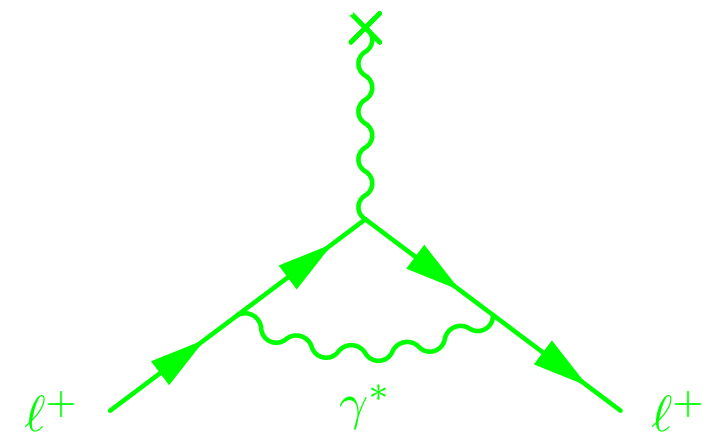
- Swinger showed this result to be consistent with QM + 1 loop correction.



$$g_e = 2\left(1 + \frac{\alpha}{2\pi}\right) \approx 2.00232$$

D. Hanneke, S. Fogwell, and G. Gabrielse
PRL 100, 120801 (2008)




$$g_e/2 = 1.001\,159\,652\,180\,73(28)$$

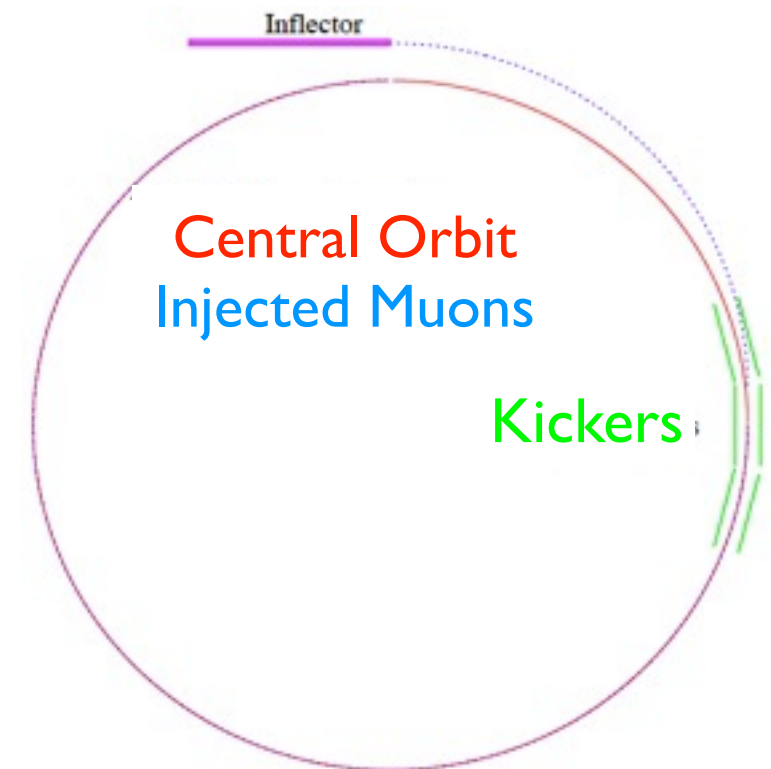


Improvements with E821






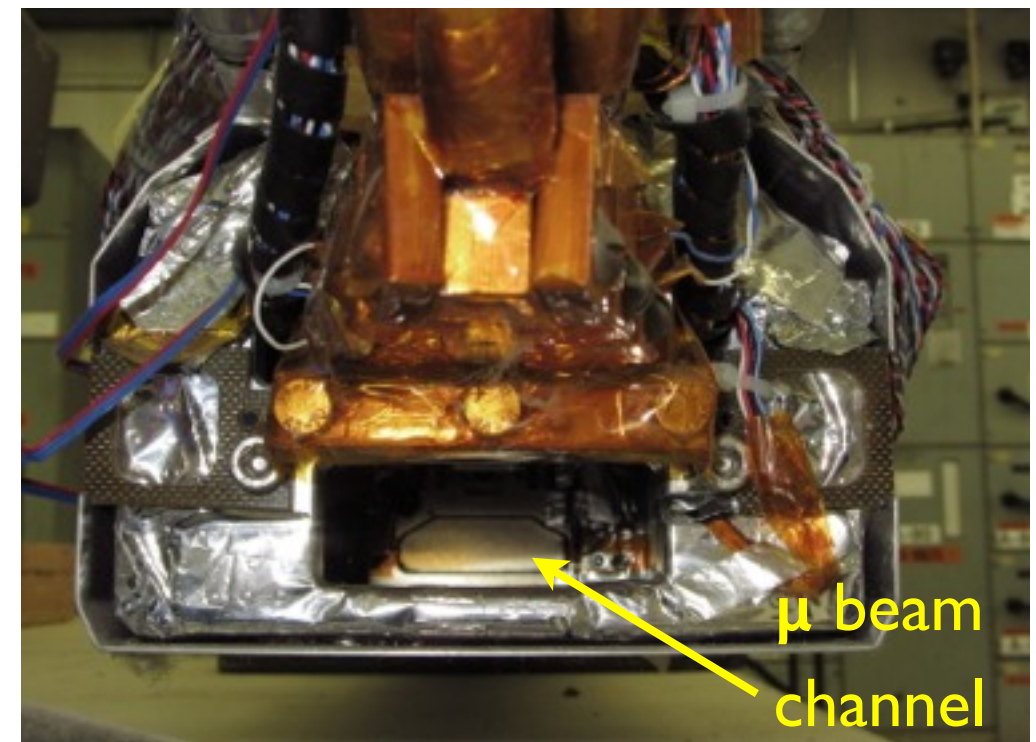
Muon Injection

-  Previous experiments inject pions into storage ring. Only fraction of pion decays create “storable” muons.
-  Direct muon injection also greatly reduces hadronic flash background on detectors.
-  Requires fast **kicker** to place muons onto stable orbit.



Superconducting Inflector Magnet

-  Novel double cosine theta septum magnet creates field free region for injected muons.
-  Avoids large gap in main magnet.
-  Key design feature: traps its own fringe field using a SC shield.



Spin and Its Observable Effects



- In the Standard Model (SM), the **muon** is a point-like particle with precisely measured properties.
- The muon is a spin $\frac{1}{2}$ particle and with spin comes a magnetic dipole moment (MDM).

$$\vec{\mu} = g \frac{q}{2m} \vec{s}$$

- Dirac explained in 1928 that **$g = 2$** for the electron.



- Dirac also postulated the existence of an electric dipole moment (EDM) of strength.

$$\vec{d} = \eta \frac{q}{2mc} \vec{s}$$

- The EDM of the electron, if present, is many orders of magnitude weaker than the MDM.

$$|d_e| < 8.7 \times 10^{-29} e \cdot cm$$

ACME Electron EDM ([arXiv:1310.7534](https://arxiv.org/abs/1310.7534))



The Quantum Theory of the Electron.

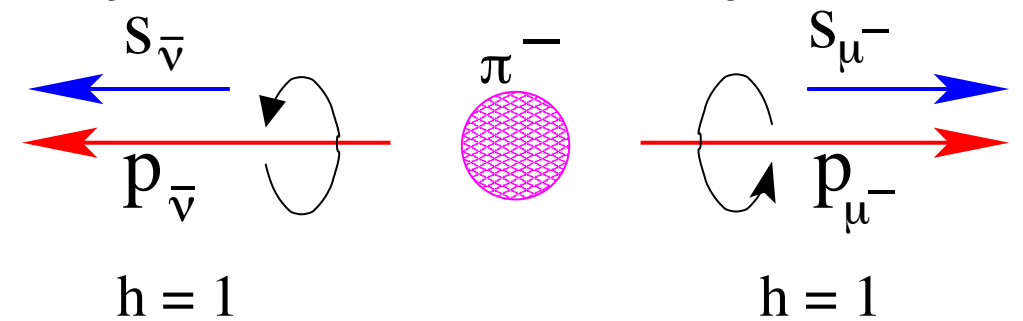
By P. A. M. DIRAC, St. John's College, Cambridge.

Measurement Technique



1. Source of Polarized Muons
(i.e., $\hat{s} \cdot \hat{p} \approx 1$)

Lucky break from parity violation



2. Magic Momentum Muons
(i.e., $\gamma = 29.3 \rightarrow p = 3.094 \text{ GeV/c}$)

Vertical focusing w/ E field adds new
term to oscillation frequency

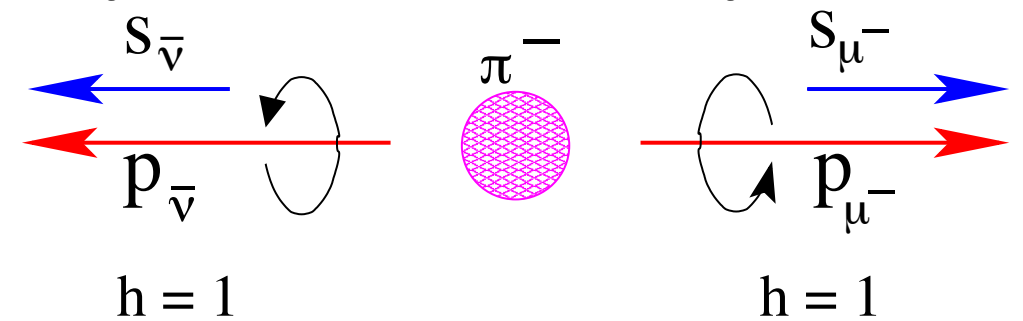
$$\vec{\omega}_a = -\frac{q}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

Measurement Technique



1. Source of Polarized Muons
(i.e., $\hat{s} \cdot \hat{p} \approx 1$)

Lucky break from parity violation



2. Magic Momentum Muons
(i.e., $\gamma = 29.3 \rightarrow p = 3.094 \text{ GeV/c}$)

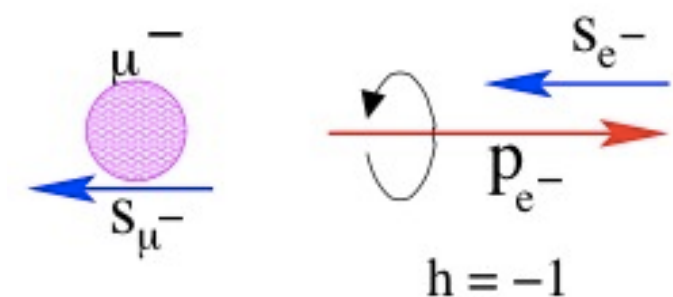
Vertical focusing w/ E field adds new term to oscillation frequency

$$\vec{\omega}_a = -\frac{q}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

The term $\left(a_\mu - \frac{1}{\gamma^2 - 1} \right)$ is highlighted in a red box, with an arrow pointing to it from the number 0.

3. Measure Electron Energy

Another lucky break from parity violation

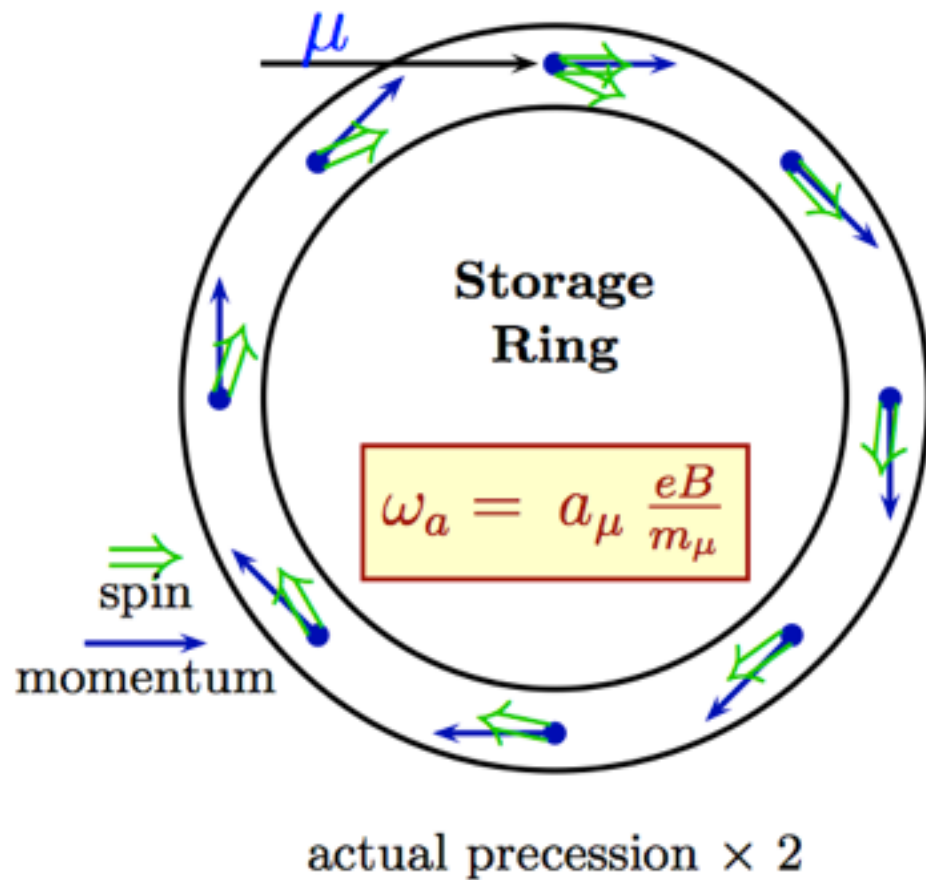


Electron spin follows muon spin

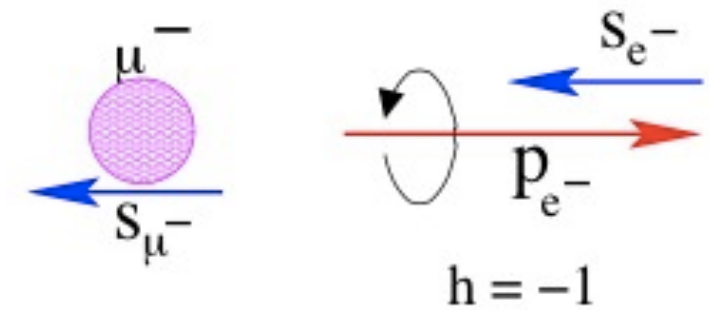
Measurement Technique



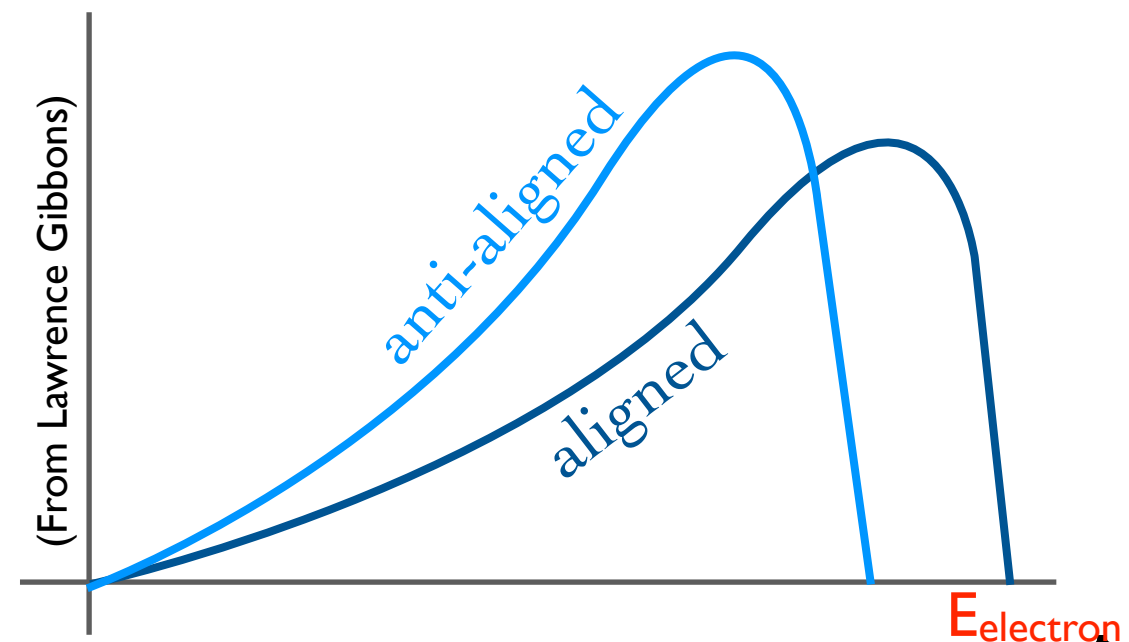
Spin precesses because $g_\mu \neq 2$



3. Measure Electron Energy



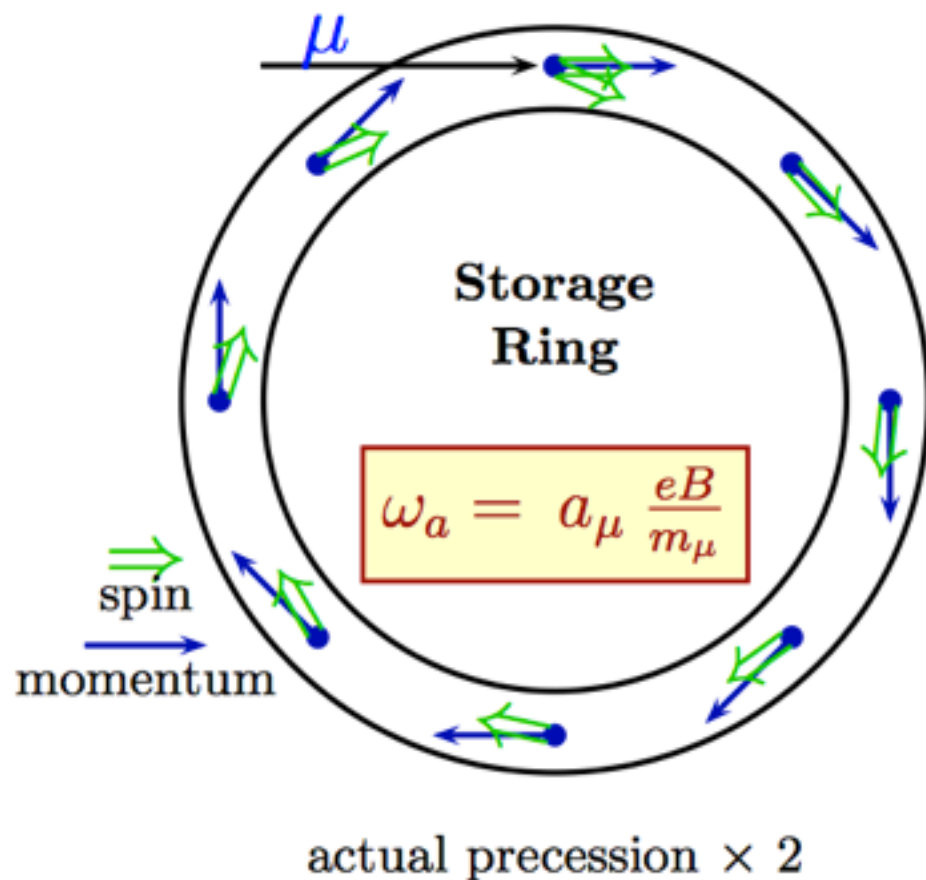
Harder electron spectrum when spin and momentum are aligned



Measurement Technique

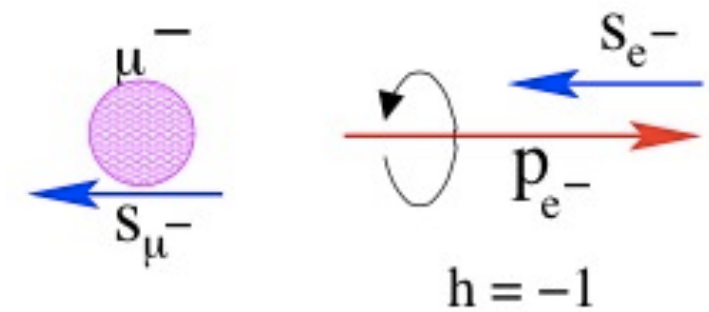


Spin precesses because $g_\mu \neq 2$

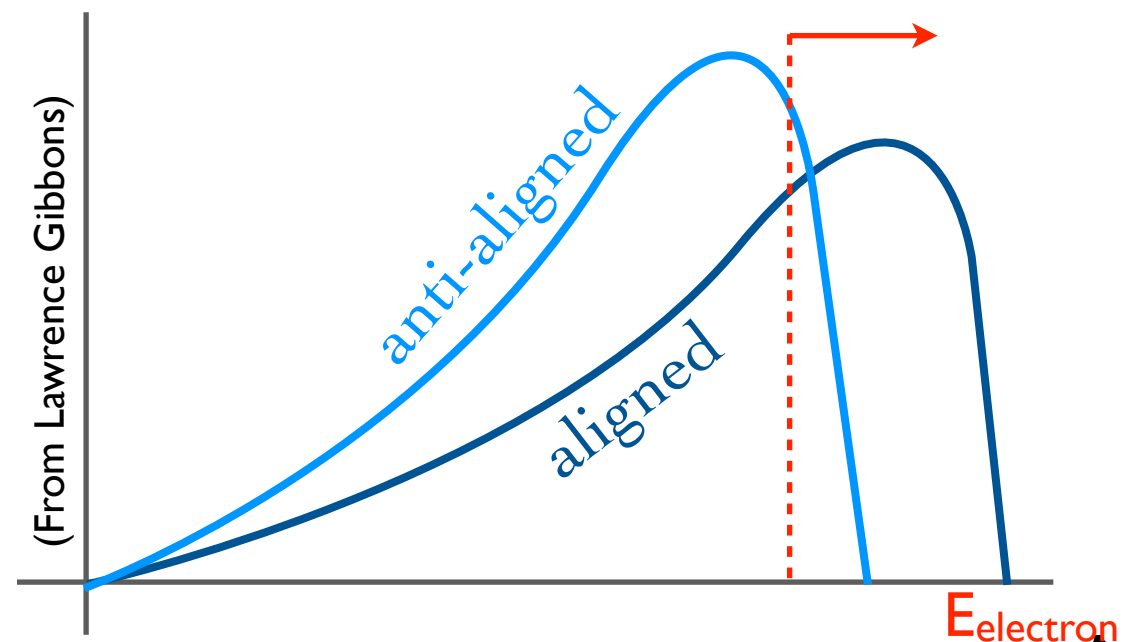


Count $N(e)$ above
fixed threshold.
Oscillation rate $\propto a_\mu$

3. Measure Electron Energy



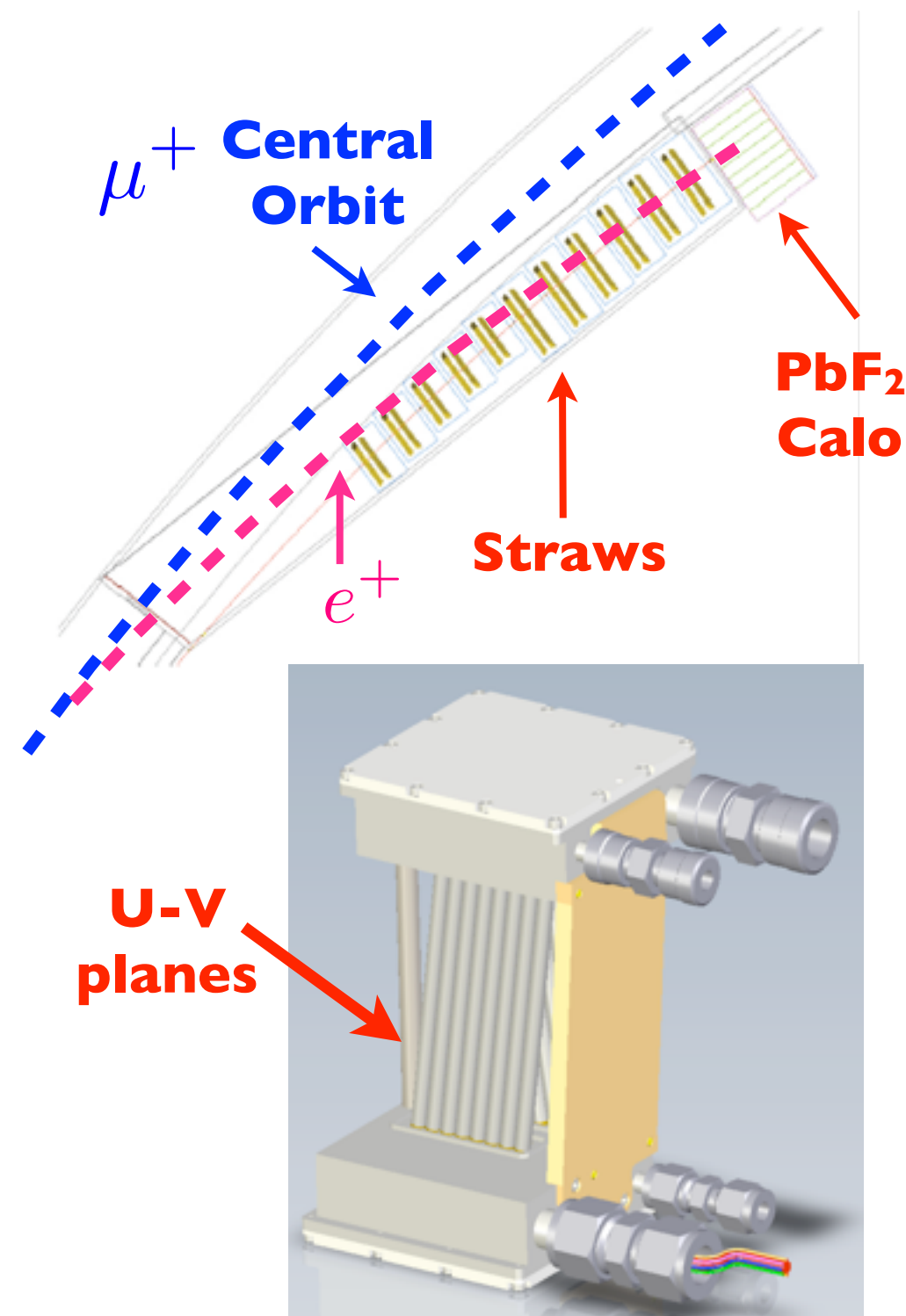
Harder electron spectrum when
spin and momentum are aligned



New Detector Elements



- Straw Tracking System
 - Two straw wire tracking chambers will record positrons before hitting the calorimeters.
- Allows non-destructive beam profile measurements
- Reconstruct muon decay vertex.
- Assist in pileup determination.

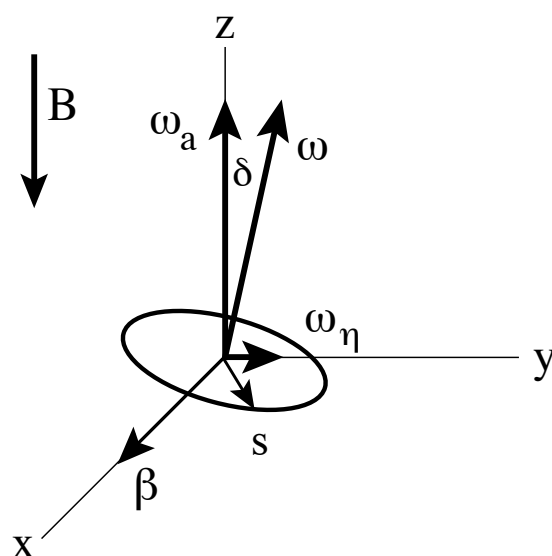


New Detector Elements

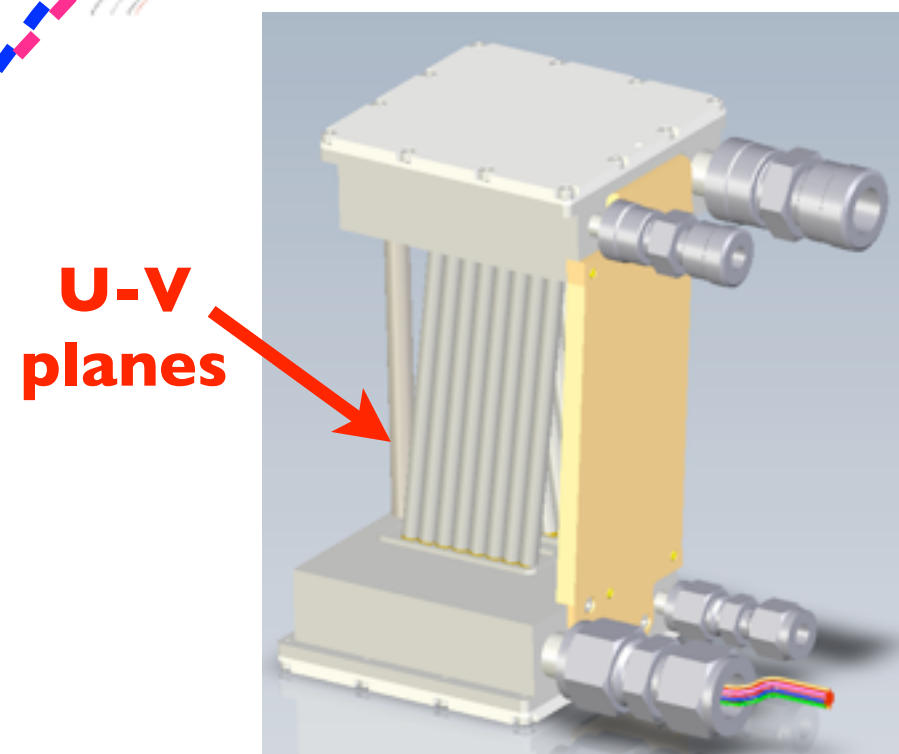
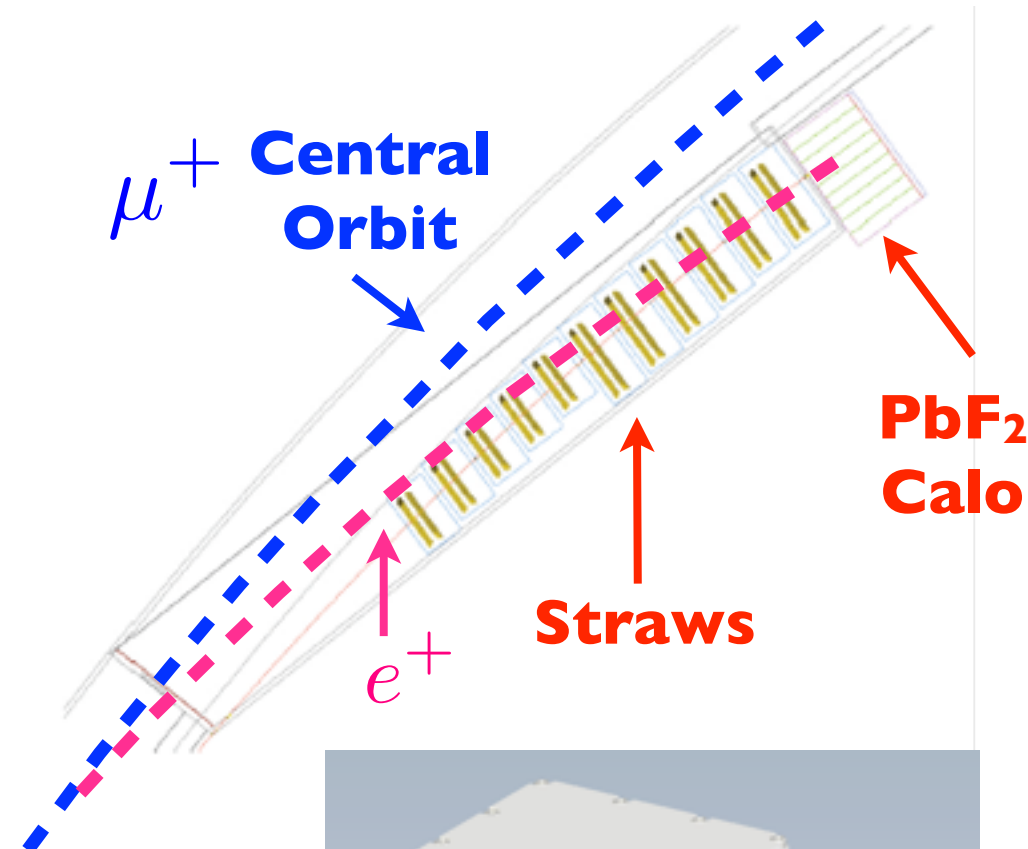


- Straw Tracking System
- Two straw wire tracking chambers will record positrons before hitting the calorimeters.
- Allows non-destructive beam profile measurements
- Reconstruct muon decay vertex.
- Assist in pileup determination.

- Allows Muon EDM Measurement



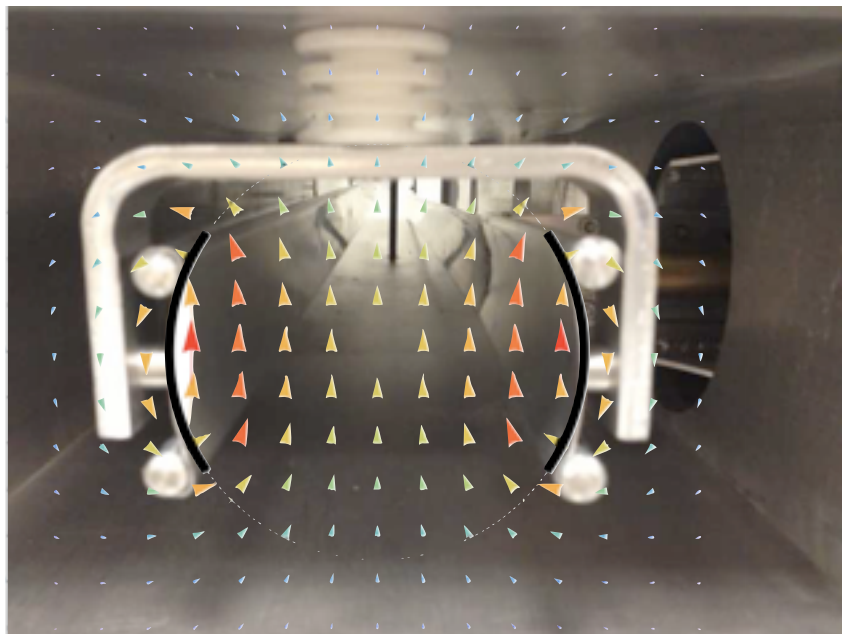
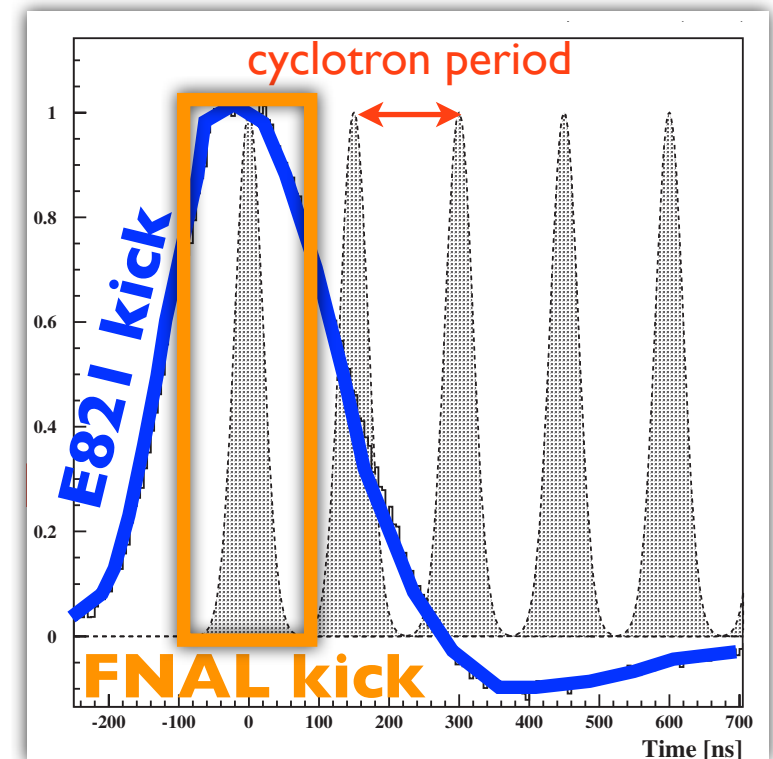
EDM tilts oscillation plane
 → Induces up-down asymmetry
 in positron spectrum



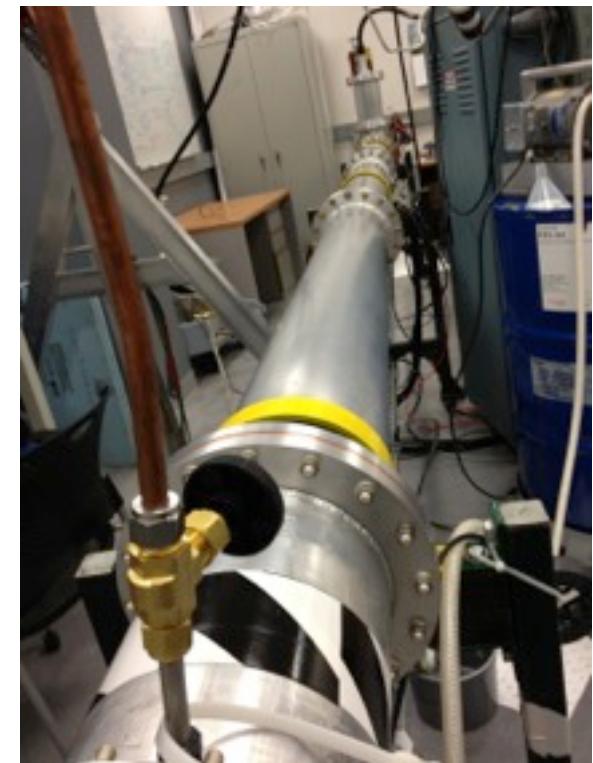
New Ring Elements



- New fast electrostatic kicker
 - Requirement: Produce a fast (**<150 ns**) ≈ 11 mrad kick. Otherwise, muon bunch will hit the inflector up return.
 - Requirement: Can not perturb precision field.
- **E821** design produced insufficient kick
 - Result: Lost muons and large betatron oscillations.



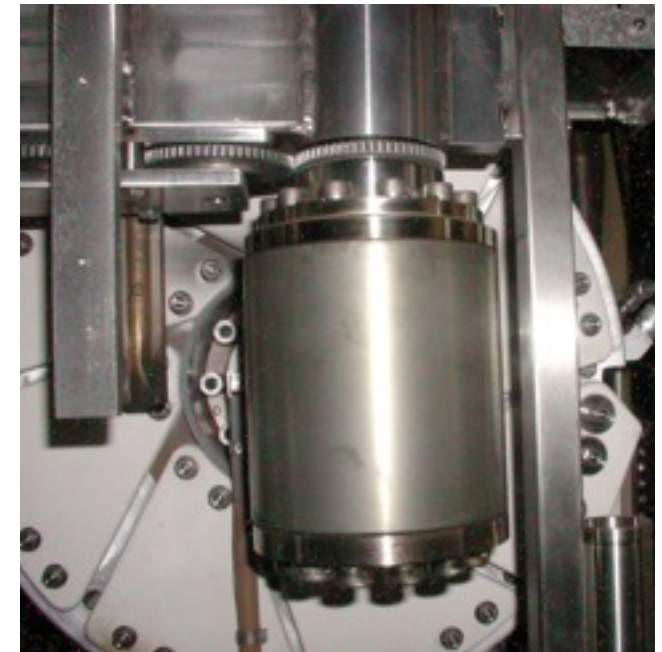
- **New design** creates a fast square pulse using 3 Blumleins.
- Curved kicker plates generate larger field / pulse.



Fermilab Muon Campus



- Fermilab will produce pions using 8.9 GeV protons impacting the former antiproton production target
- Yield is $\approx 10^{-5}$ π /POT within 2% of $P_{\text{magic}} = 3.094$ GeV.
- Pions travel through M2/M3 lines (900 m “decay pipe”) to delivery ring (DR) and accumulating muons ($\pi \rightarrow \mu$).
- Nearly pure muon beam in DR (big improvement over E821).



MI Line

Target

M2/3 Line

Delivery Ring

M5 Line

g-2 Hall

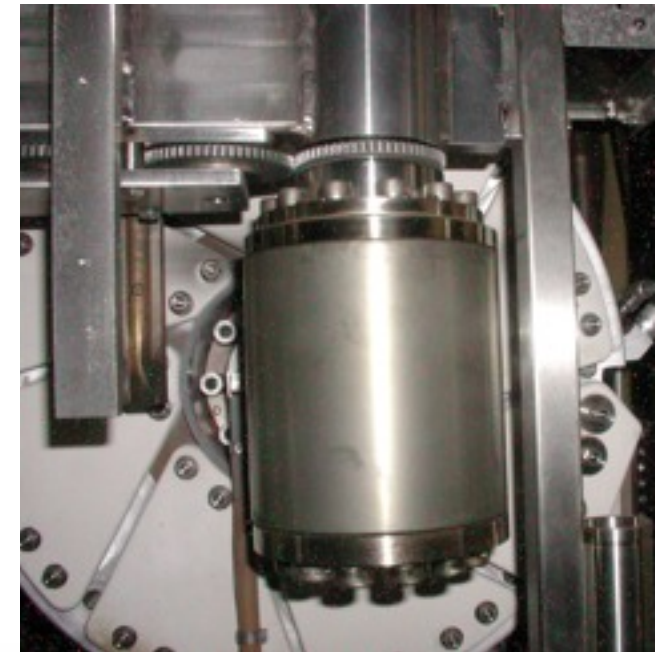


- After several turns in DR (to remove beam protons), muons are kicked into M5 beamline and into g-2 experimental hall.

Fermilab Muon Campus



- Fermilab will produce pions using 8.9 GeV protons impacting the former antiproton production target
- Yield is $\approx 10^{-5}$ π /POT within 2% of $P_{\text{magic}} = 3.094$ GeV.
- Pions travel through M2/M3 lines (900 m “decay pipe”) to delivery ring (DR) and accumulating muons ($\pi \rightarrow \mu$).
- Nearly pure muon beam in DR (big improvement over E821).



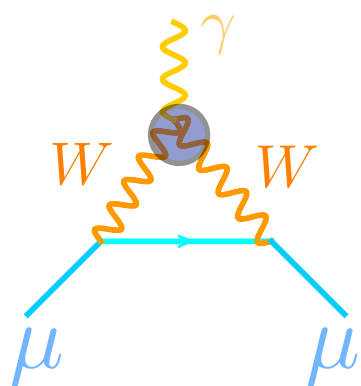
New Physics?



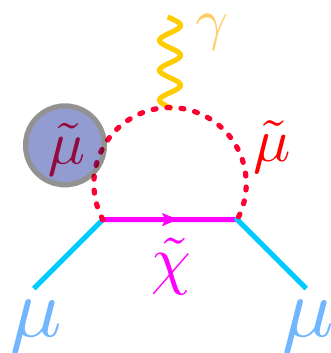
- Standard Model calculation is ok. We are just seeing new physics.

$$a_{\mu} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{Had}} + a_{\mu}^{\text{NP}}$$

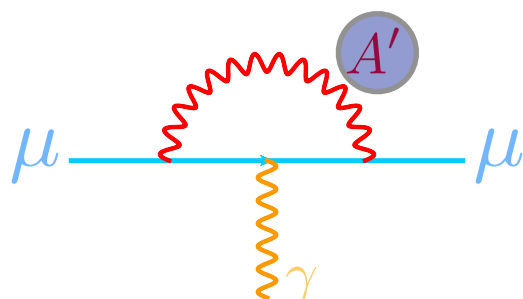
aTGC $WW\gamma$



SUSY



Dark Photons



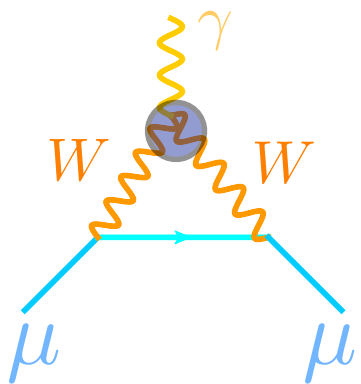
New Physics?



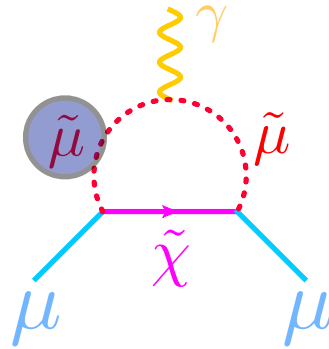
- Standard Model calculation is ok. We are just seeing new physics.

$$a_\mu = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{Had}} + \boxed{a_\mu^{\text{NP}}}$$

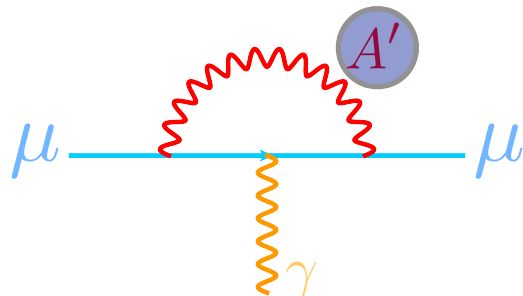
aTGC $WW\gamma$



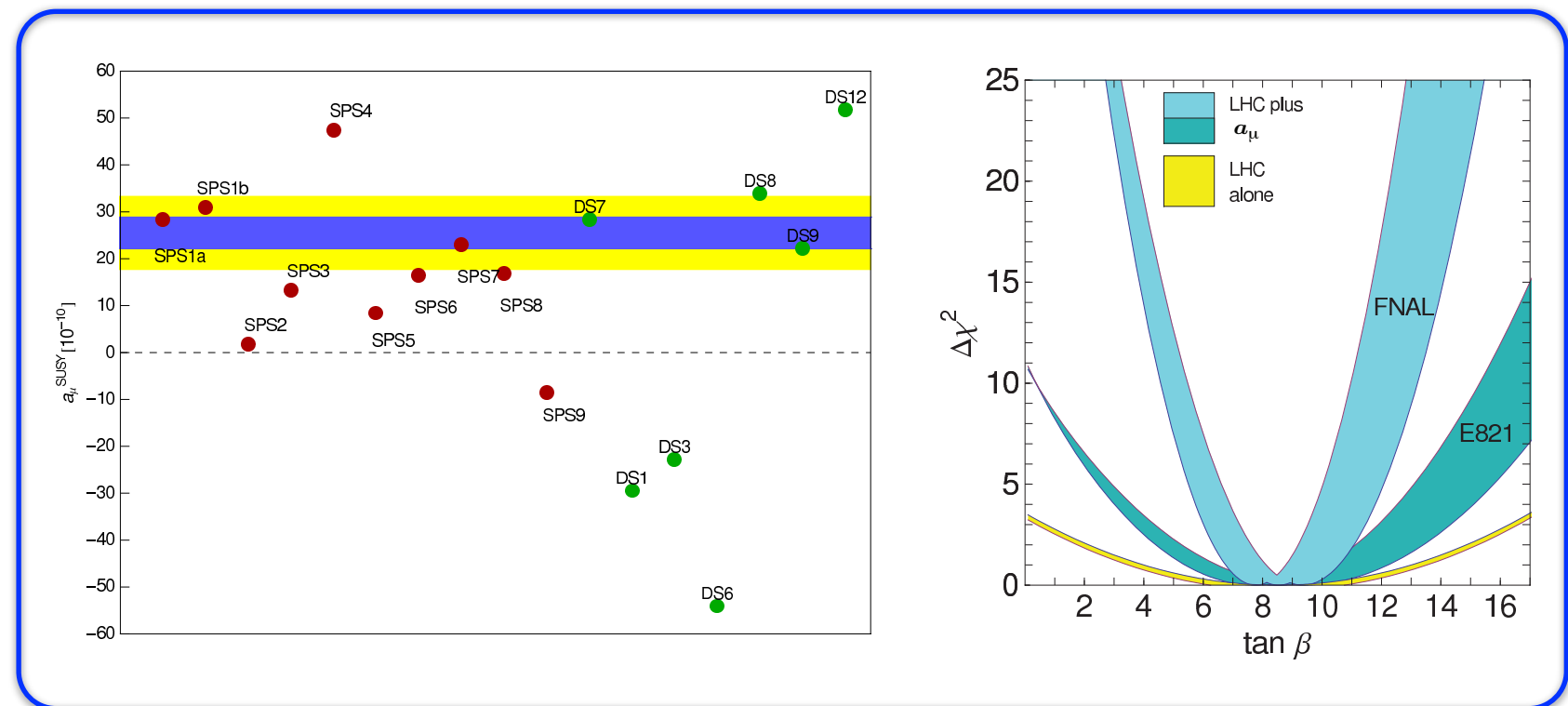
SUSY



Dark Photons



**g-2 can disentangle
allowed SUSY models**



- A precise g-2 measurement is very complimentary to a future LHC discovery.

Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

- Evidence that the muon is just a heavy electron.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.

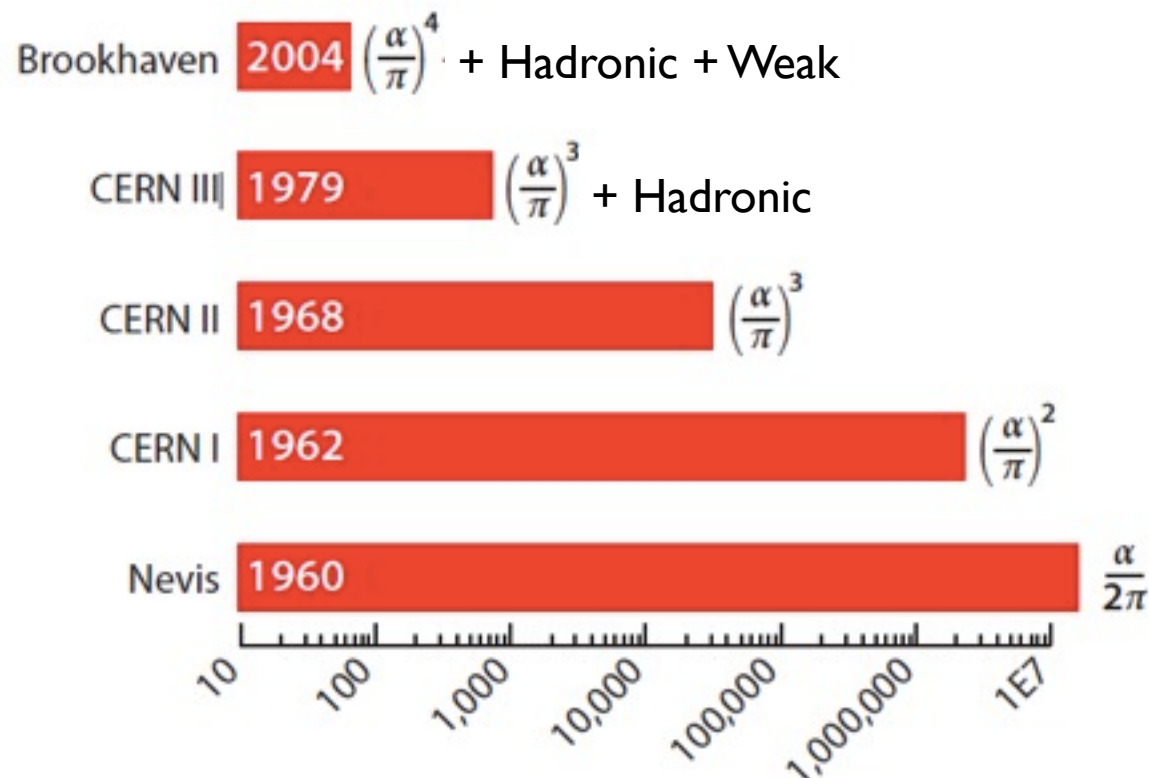
Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)



Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_\mu = 2(10\%)$$

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

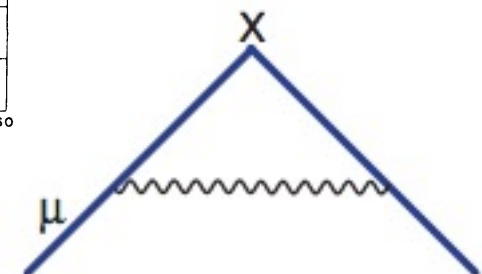
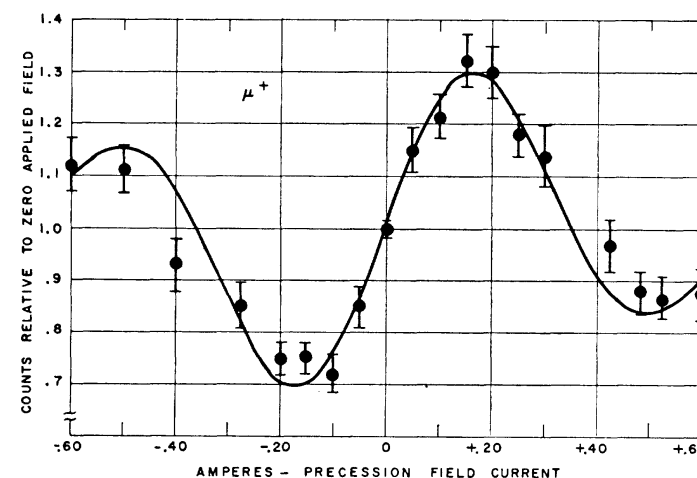
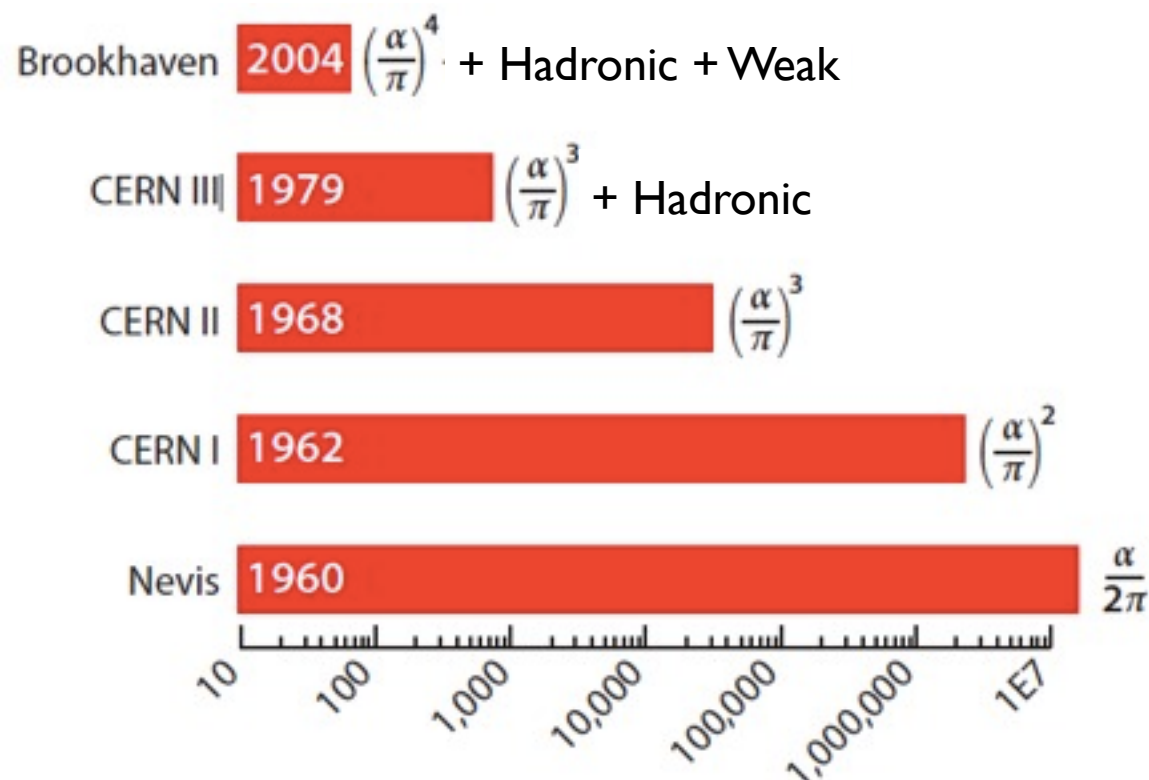
Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)

- Evidence that the muon is just a heavy electron.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.

Nevis



Muon spin rotation in magnetic field

Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

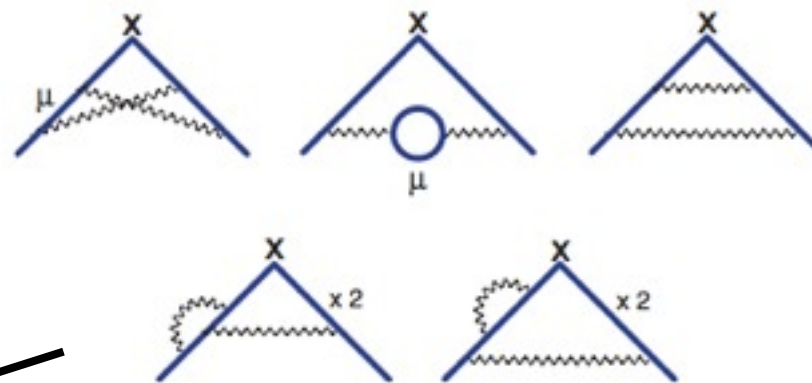
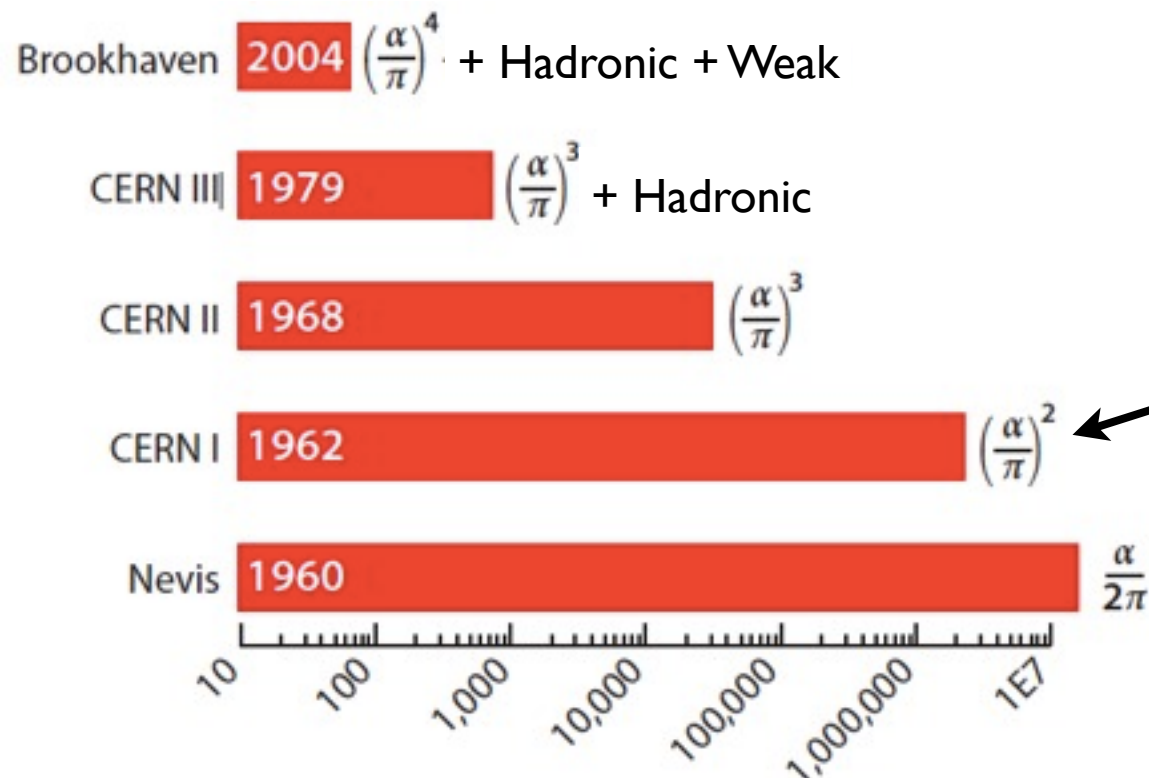
RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)

- Evidence that the muon is just a heavy electron.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.



Muon in circular orbits, spin precession relative to cyclotron frequency.

CERN I



Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

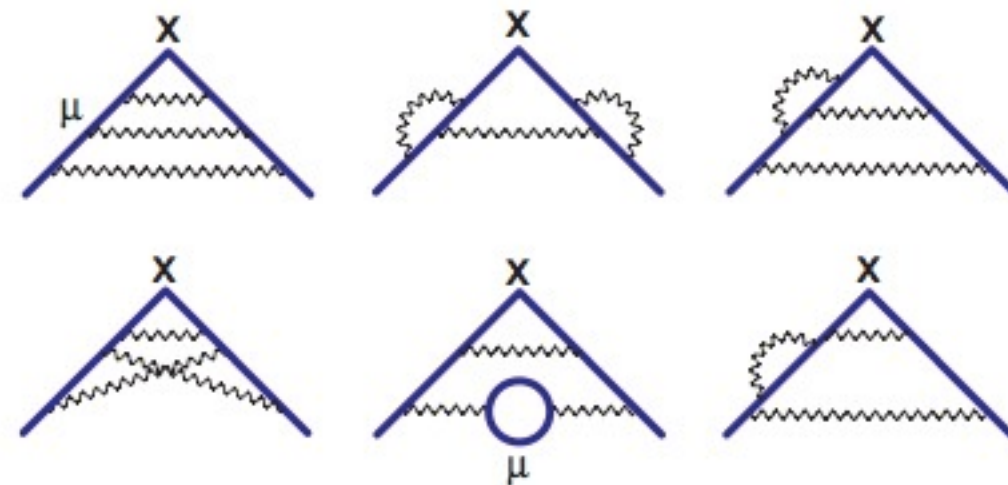
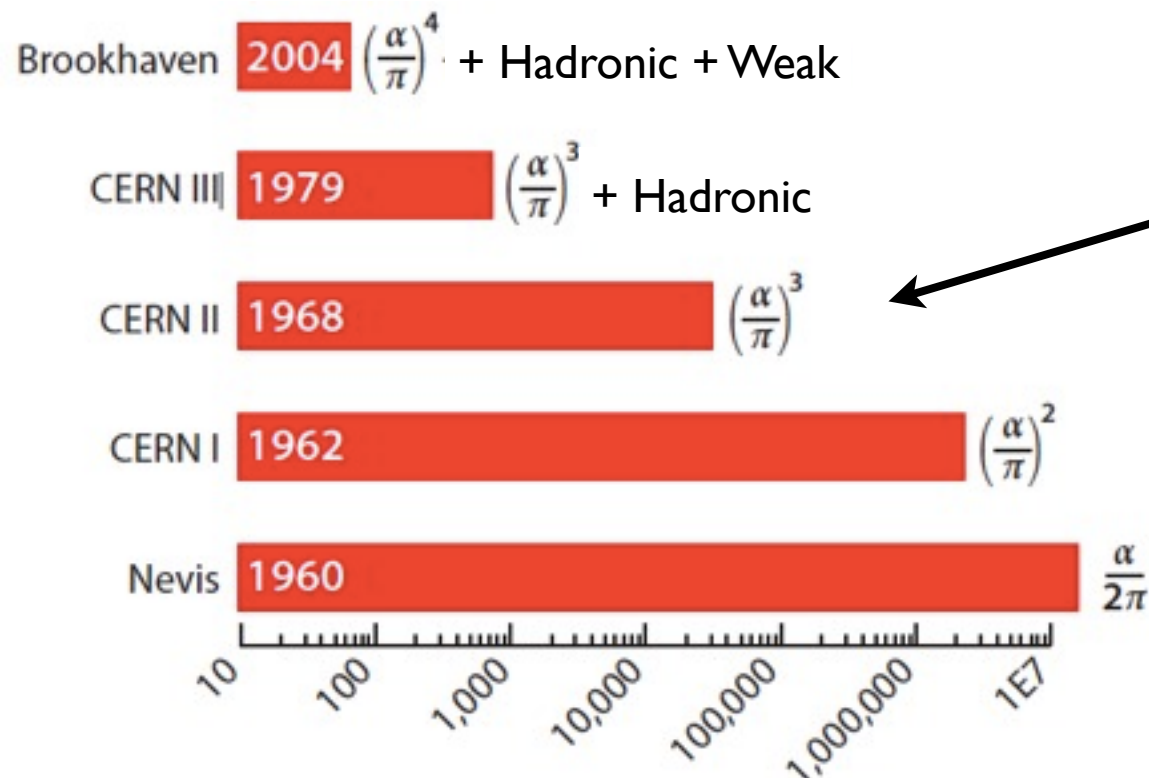
RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)

- Evidence that the muon is just a heavy electron.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.



Storage ring w/ vertical focusing + tying a_{μ} to hyperfine splitting in muonium



CERN II

Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

- Evidence that the muon is just a heavy electron.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.

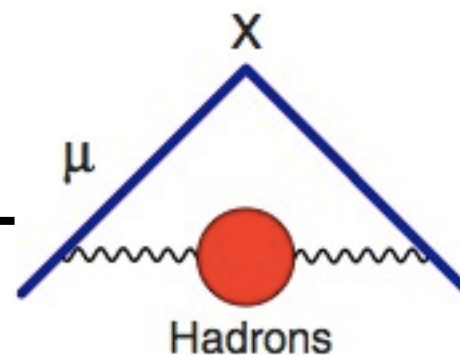
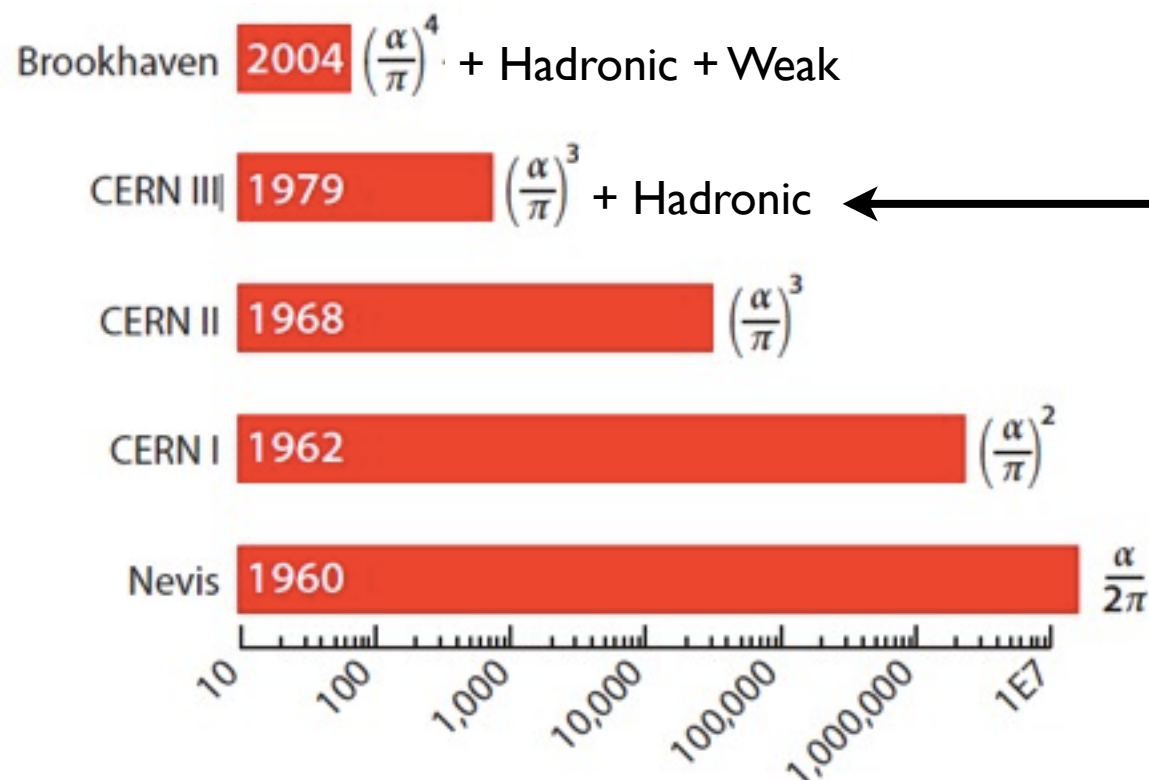
Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)



CERN III



Electrostatic focusing w/ “Magic momentum” muons w/ $\gamma = 29.3$

Understanding The Muon



- There is a rich history of muon g-factor measurements starting in the 1950's at Nevis.

$$g_{\mu} = 2(10\%)$$

Observations of the Failure of Conservation of Parity and Charge Conjugation in Meson Decays: the Magnetic Moment of the Free Muon*

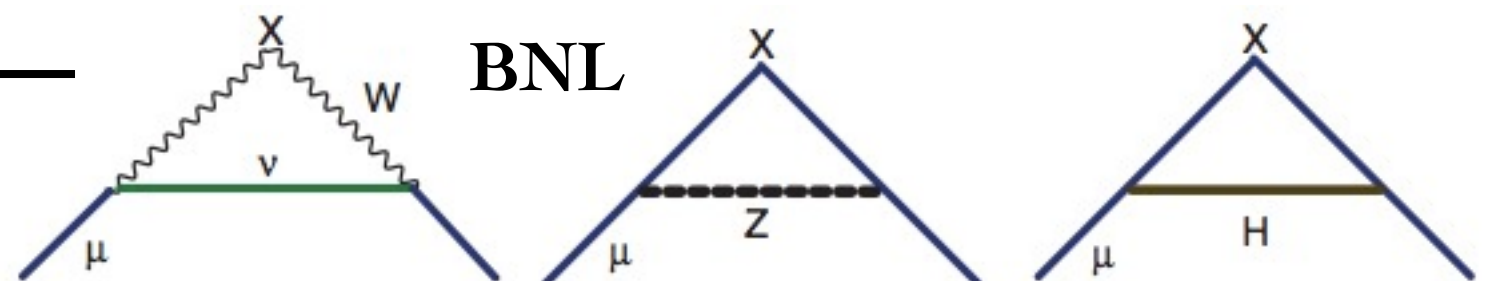
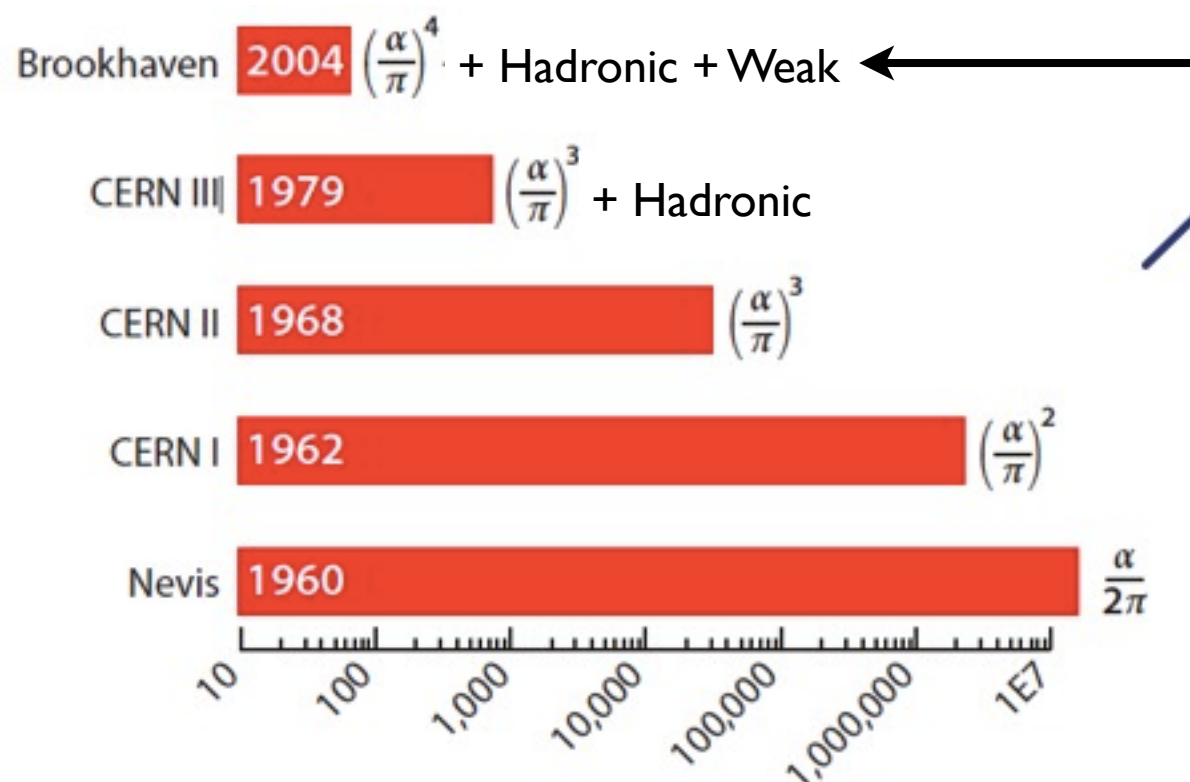
RICHARD L. GARWIN,† LEON M. LEDERMAN, AND MARCEL WEINRICH

Physics Department, Nevis Cyclotron Laboratories, Columbia University, Irvington-on-Hudson, New York, New York

(Received January 15, 1957)

Phys. Rev. 105, 1415–1417 (1957)

- Evidence that the muon is just a heavy electron.
- The past 50 years have seen dramatic improvements in precision and experimental techniques.

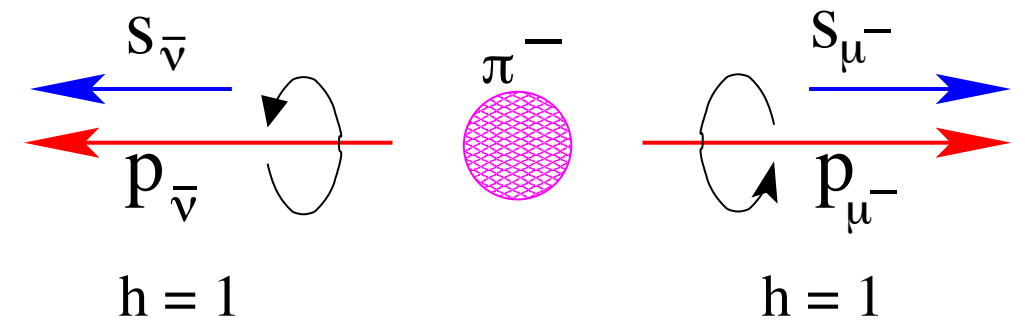


Measurement Technique



1. Source of Polarized Muons
(i.e., $\hat{s} \cdot \hat{p} \approx 1$)

Lucky break from parity violation

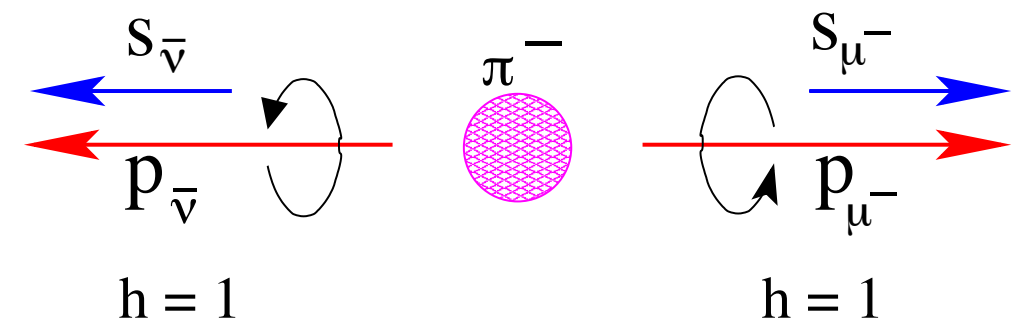


Measurement Technique



1. Source of Polarized Muons
(i.e., $\hat{s} \cdot \hat{p} \approx 1$)

Lucky break from parity violation



2. Vertical Focusing
(i.e., trapped muons)

Using quad E field adds new term to
oscillation frequency

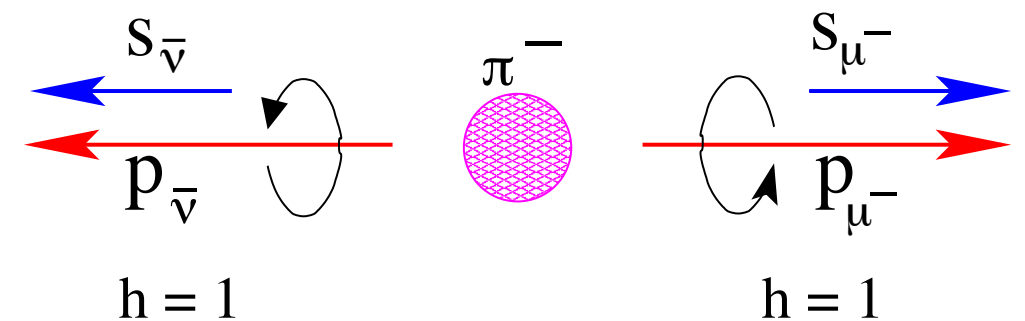
$$\vec{\omega}_a = -\frac{q}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

Measurement Technique



1. Source of Polarized Muons
(i.e., $\hat{s} \cdot \hat{p} \approx 1$)

Lucky break from parity violation



2. Vertical Focusing
(i.e., trapped muons)

Using quad E field adds new term to
oscillation frequency

$$\vec{\omega}_a = -\frac{q}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

If $\gamma = 29.3$ ($p_\mu = 3.09 \text{ GeV}/c$) \Rightarrow Cancels new term

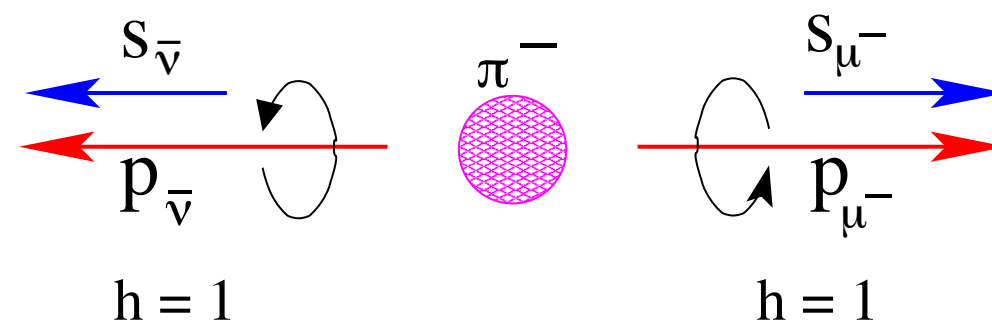
These are “Magic Momentum” muons

Measurement Technique



1. Source of Polarized Muons
(i.e., $\hat{s} \cdot \hat{p} \approx 1$)

Lucky break from parity violation



2. Vertical Focusing
(i.e., trapped muons)

3. Measure Muon Spin Precession

Using quad E field adds new term to oscillation frequency

$$\vec{\omega}_a = -\frac{q}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

If $\gamma = 29.3$ ($p_\mu = 3.09 \text{ GeV}/c$) \Rightarrow Cancels new term
These are “Magic Momentum” muons

Weak decay correlates muon spin and electron momentum

